

20 April, 2015



# Beta decay as an absolute calibration probe for spin-isospin responses

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# Today's concern

- GT strength and Spin dipole(SD) strength by charge-exchange reaction
- Extract  $B(GT)$  and  $B(SD)$
- For that, needs calibration on reaction probe by  $\beta$  decay data.

# $\beta$ -decay & Nuclear Reaction

- $\beta$ -decay transition rate =  $\frac{1}{t_{1/2}} = f \frac{\lambda^2}{D} B(J^\pi)$

$B(J^\pi)$  : reduced transition strength  $\propto |M|^2$

- Provide **absolute** value
- △  $Q_\beta$  window

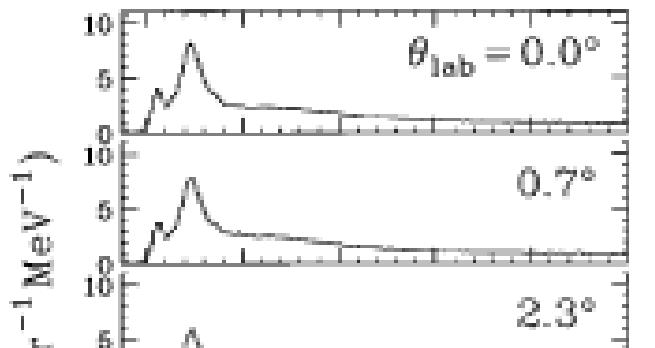
- Charge-exchange reaction cross-section  
=  $K(E, A) * B(J^\pi)$

- △ Needs calibration
- No  $Q_\beta$  window

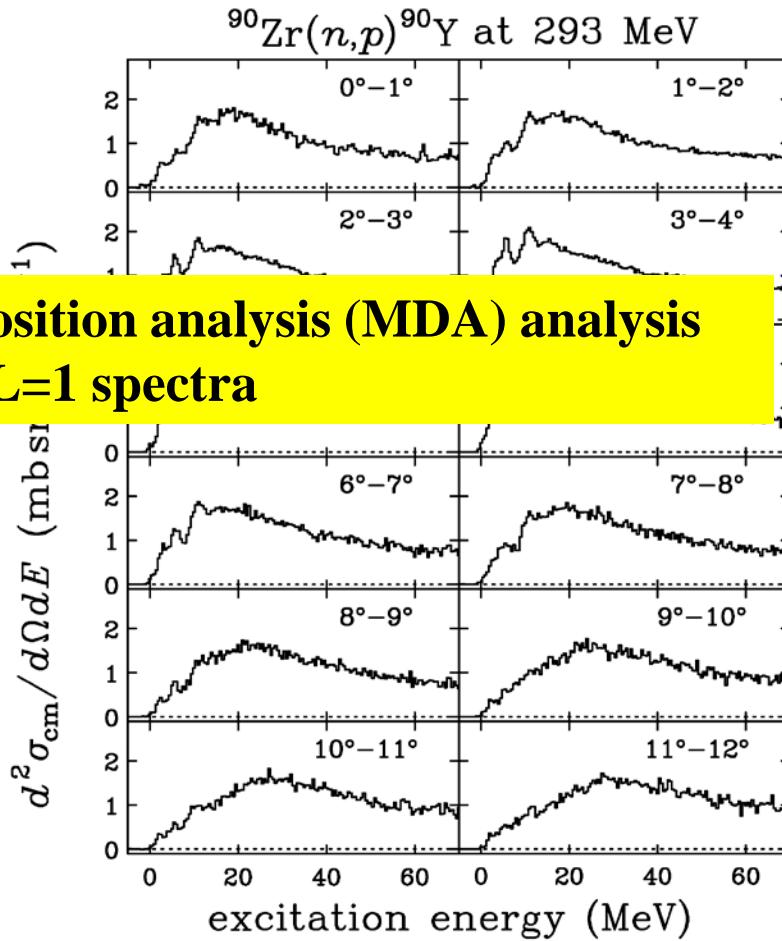
Reaction cross section can be **calibrated** by  $B(J^\pi)$  of  $\beta$  decay.

# $^{90}\text{Zr}(p,n)/(\bar{n},p)$ measurements

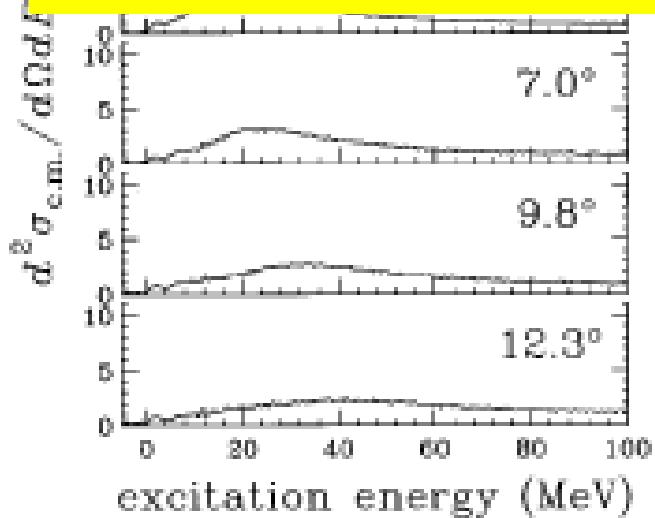
$^{90}\text{Zr}(p,n)^{90}\text{Nb}$  at 295 MeV



$^{90}\text{Zr}(n,p)^{90}\text{Y}$  at 293 MeV



Apply the multipole decomposition analysis (MDA) analysis  
 $\rightarrow \Delta L=0$  and  $\Delta L=1$  spectra



# Gamow-Teller (Op: $t_{+/-}\sigma$ ) strength $B(GT)$

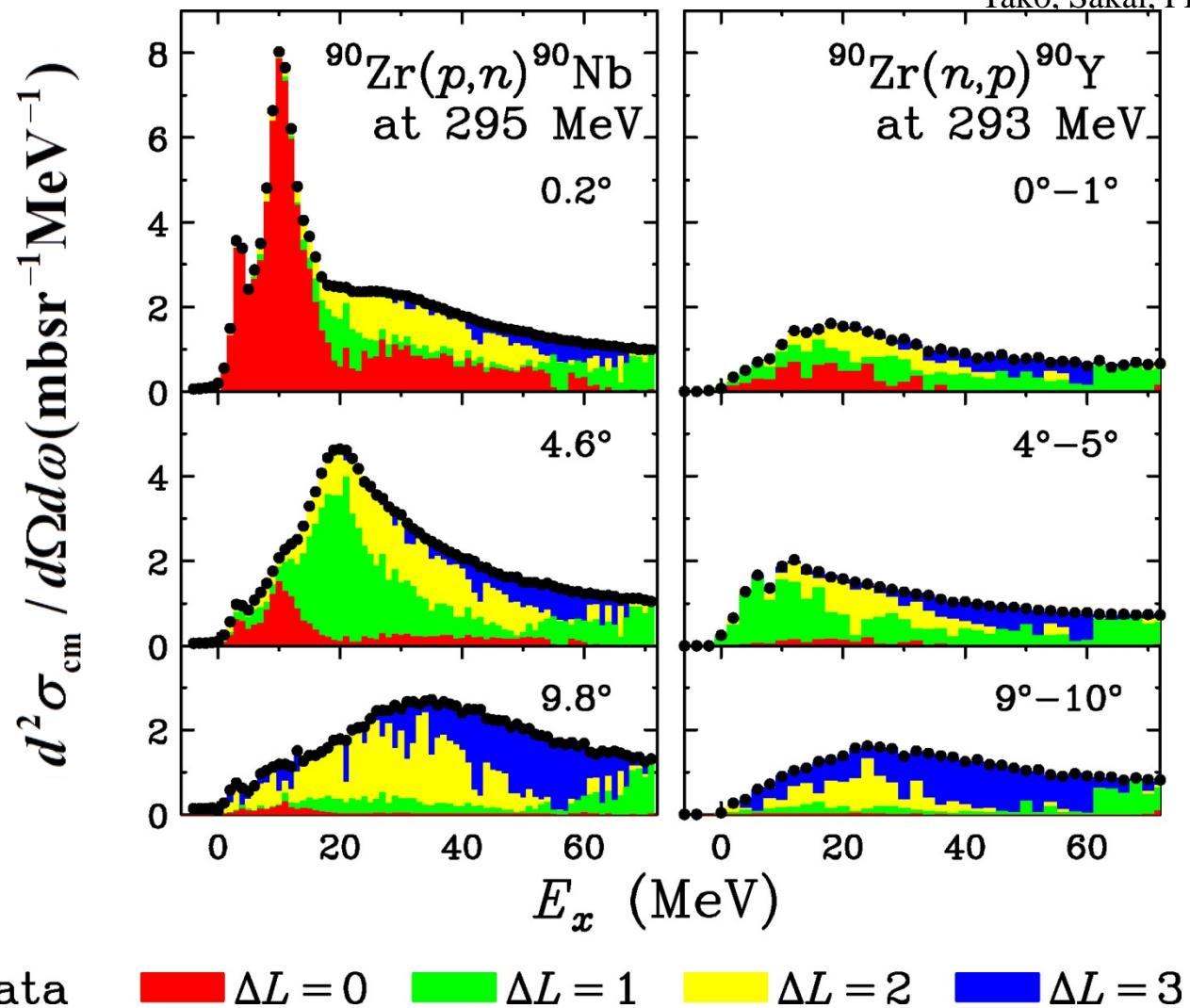
**Model independent spin sum rule (Ikeda sum rule)**

$$\begin{aligned} S_{\beta^-} - S_{\beta^+} &= \frac{1}{2J_i + 1} \sum_f \left| \left\langle f \left\| \sum_{i=1}^A t_-(i) \sigma_i \right\| i \right\rangle \right|^2 - \frac{1}{2J_i + 1} \sum_f \left| \left\langle f \left\| \sum_{i=1}^A t_+(i) \sigma_i \right\| i \right\rangle \right|^2 \\ &= \sum B(GT-) - \sum B(GT+) \\ &= 3(N - Z) \end{aligned}$$

If nucleus can be described in terms of  
nucleon degrees of freedom

# Decomposed results

Yako, Sakai, PLB615(2005)193

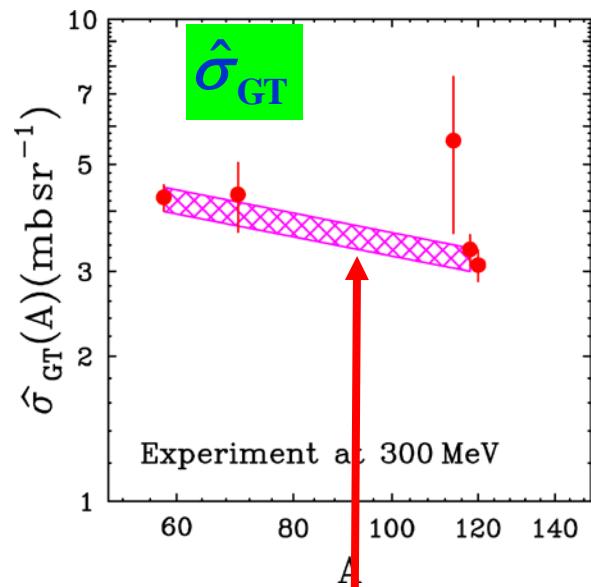


$$\left. \frac{d\sigma(0^\circ)}{d\Omega} \right|_{\Delta L=0} \Rightarrow \mathbf{B(GT)}$$

# Proportionality assumption to extract $B(\text{GT})$

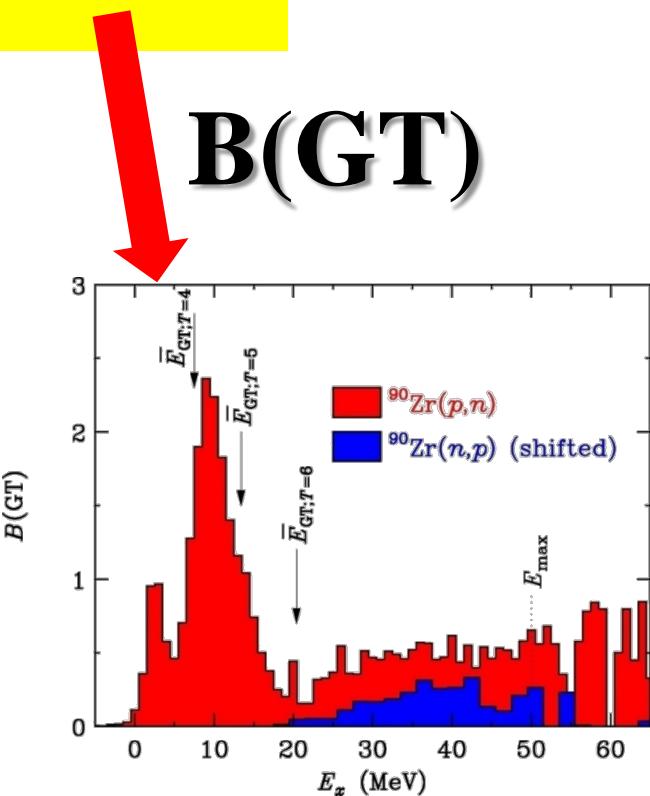
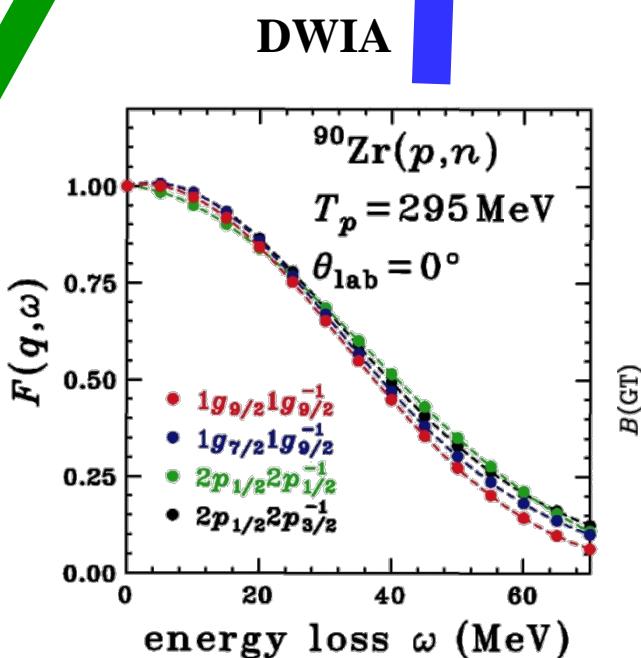
$$\left. \frac{d\sigma(0^\circ)}{d\Omega} \right|_{\Delta L=0} = \hat{\sigma}_{\text{GT}}(E_p, A) \cdot F_{\text{GT}}(q, \omega) \cdot B(\text{GT})$$

Unit cross section



M. Sasano et al., PRC 79, 23602 ('09)

$$\hat{\sigma}_{\text{GT}}(^{90}\text{Zr}) = 3.6 \pm 0.2 \text{ (mb/sr)}$$

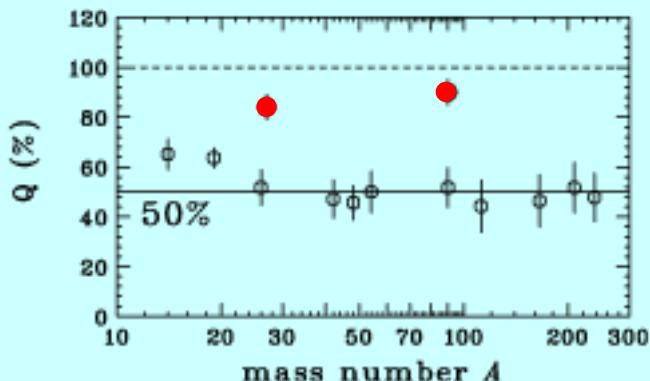


$$S_{\beta^-} - S_{\beta^+} = 27.6$$

For  $0 \leq \omega \leq 50$  MeV

# Quenching factor ( $^{90}\text{Zr}$ )

$$Q = 0.92 \pm 0.07$$



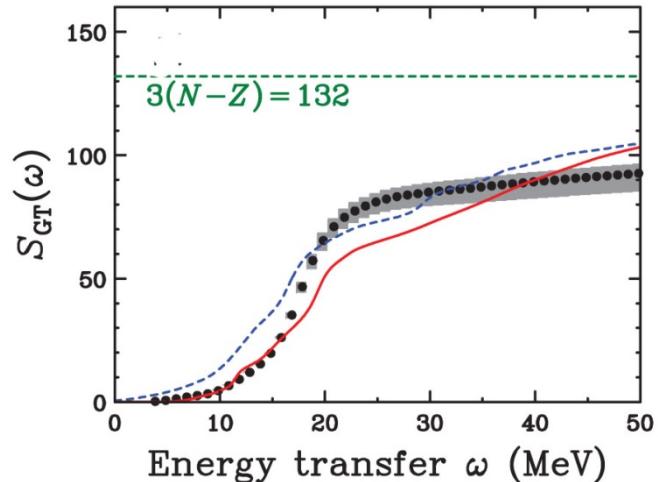
Wakasa et al., PRC 55, 2909 (1997)

Strength spread into 2p2h coupled states  
Small  $\Delta h^{-1}$  contribution

Quenching problem solved !

However . . .

$^{208}\text{Pb}(p,n)$  at 300 MeV



Wakasa et al., PRC 85, 064606 (2012)

$Q \sim 72\%$  !

# Spin Dipole strength $B(GT)$

$$\hat{O}_{SD\pm} = \sum_{im\mu} t_{\pm}^i \sigma_m^i r_i Y_1^{\mu}(\hat{r}_i)$$

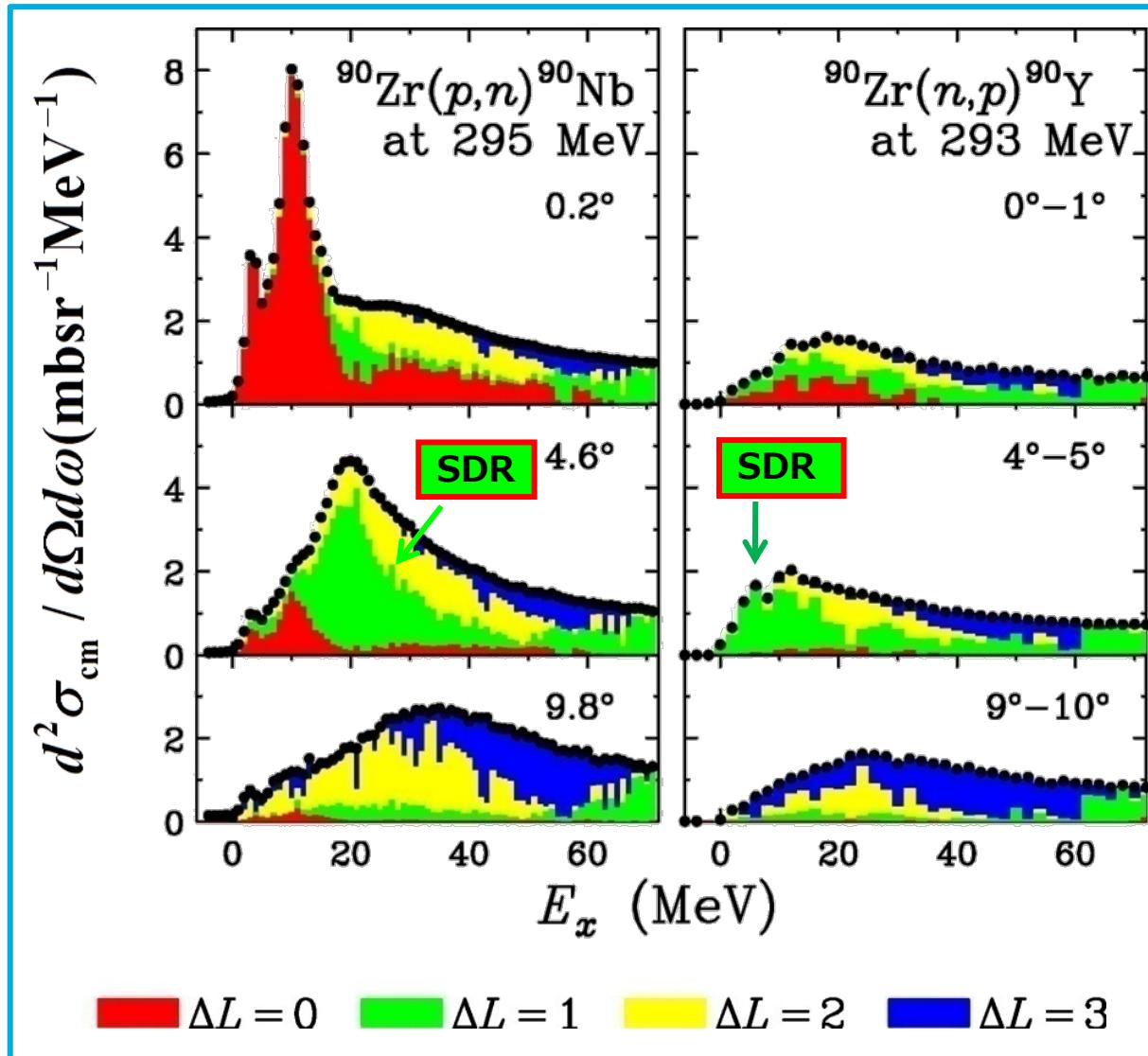
Model independent spin sum rule

$$S_{-}(SD) - S_{+}(SD) = \frac{9}{4\pi} \left( N \langle \mathbf{r}^2 \rangle_n - Z \langle \mathbf{r}^2 \rangle_p \right)$$

(p,n)      (n,p)      extract      e scatt.

$$\delta_{np} = \sqrt{\langle \mathbf{r}^2 \rangle_n} - \sqrt{\langle \mathbf{r}^2 \rangle_p}$$

# Spin dipole strength



# Extraction of B(SD)

## ● Proportionality relation (**assumption !**)

$$\sigma_{\Delta L=1,\pm}(q,\omega) = \hat{\sigma}_{SD\pm}(q,\omega) \cdot B(SD\pm)$$

Characterized by  $\Delta S=1$ ,  $\Delta L=1$ ,  $\Delta J=0,1,2$

$0+ \rightarrow 0-$  first forbidden

$0+ \rightarrow 1-$  first forbidden

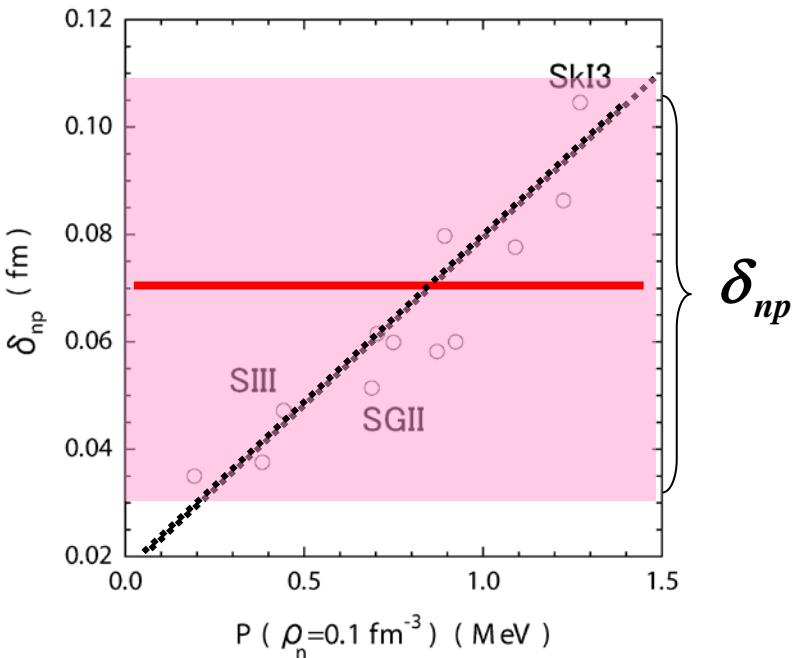
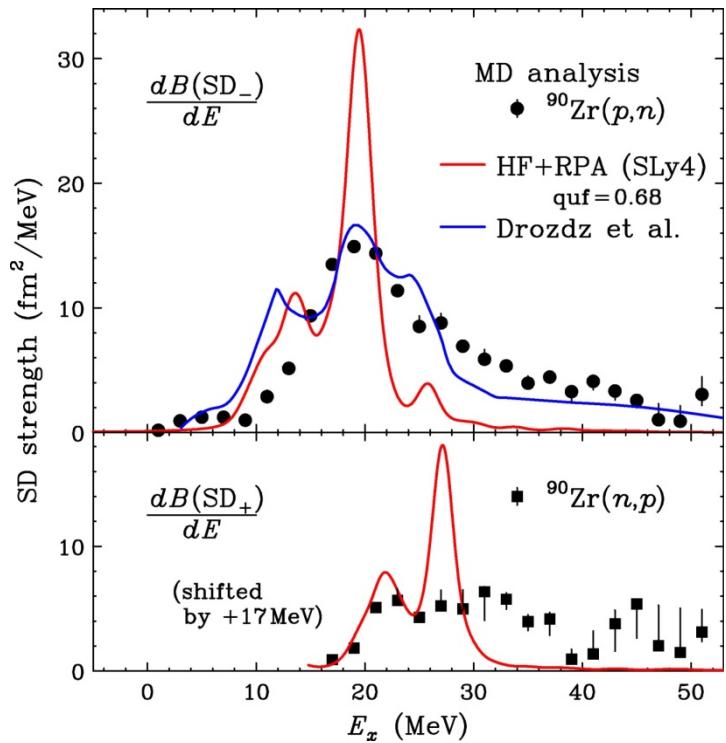
$0+ \rightarrow 2-$  unique first forbidden

## ● Unit cross section $\hat{\sigma}_{SD\pm}(q,\omega)$

$\Rightarrow$  Estimated with **DWIA calculation at  $4.5^\circ$**

$$\sigma_{\Delta L=1,\pm}(4.5^\circ, \omega) = \hat{\sigma}_{SD\pm}(4.5^\circ, \omega) \cdot B(SD\pm)$$

# Spin dipole strength and sum rule value



$$S_- - S_+ = 148 \pm 13 \text{ fm}^2$$

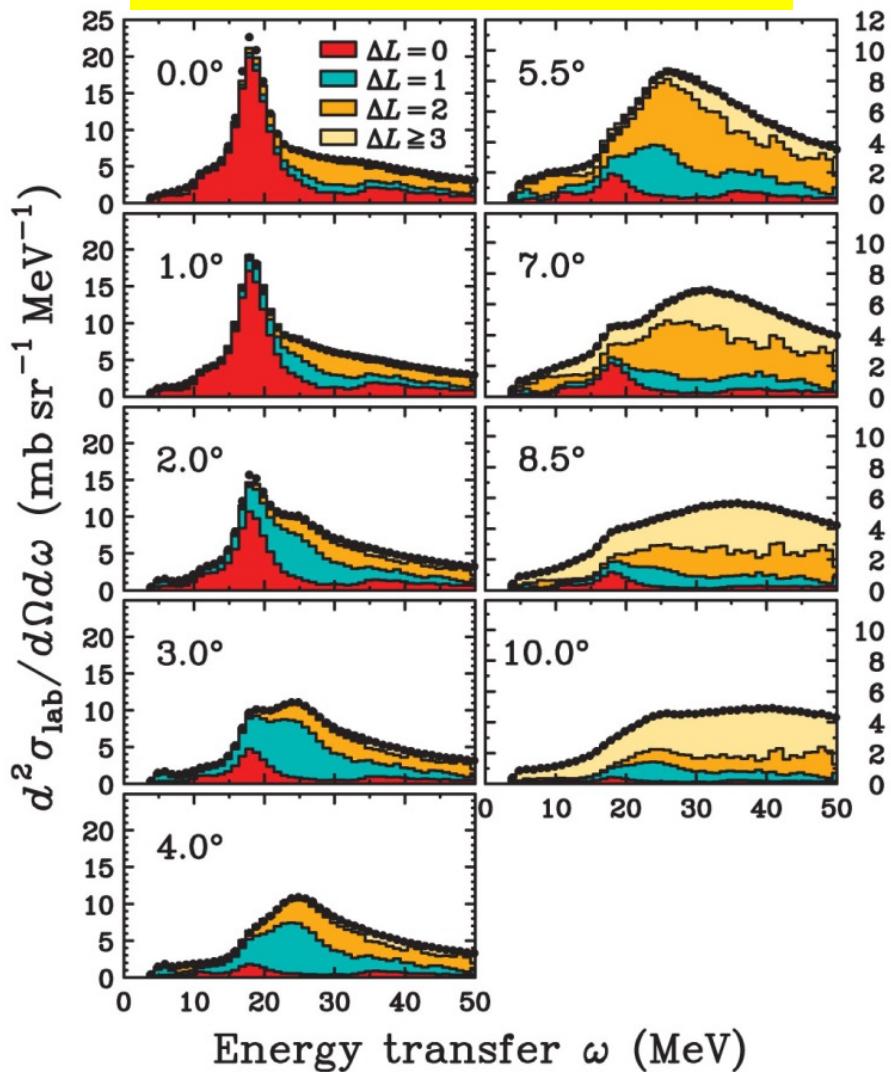
$$\sqrt{\langle r^2 \rangle_p} = 4.19 \text{ fm}$$

$$\left. \begin{aligned} \sqrt{\langle r^2 \rangle_n} &= 4.26 \pm 0.04 \text{ fm} \\ \delta_{np} &= 0.07 \pm 0.04 \text{ fm} \end{aligned} \right\}$$

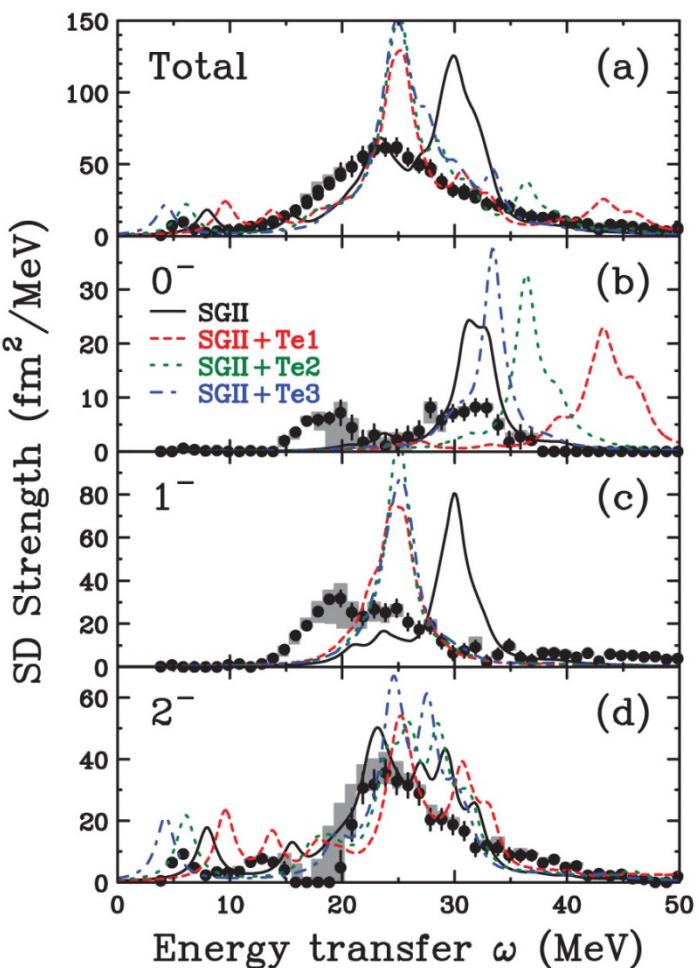
# Spin dipole strength in $^{208}\text{Pb}$ by Wakasa (Kyushu U)

Wakasa et al., 85(2012)064606

Excellent experiment !



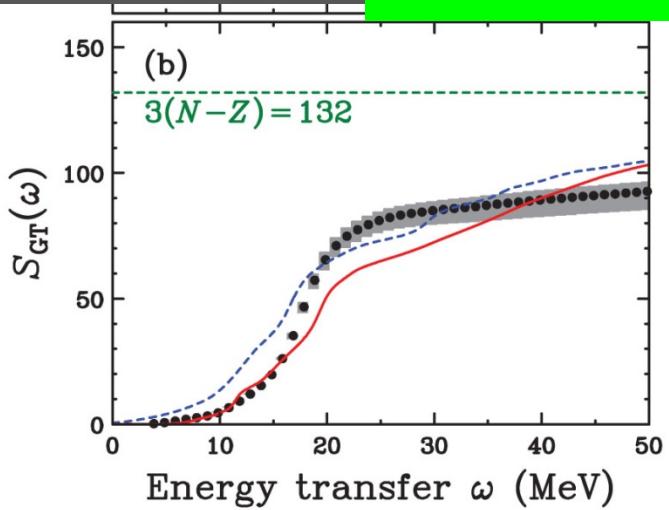
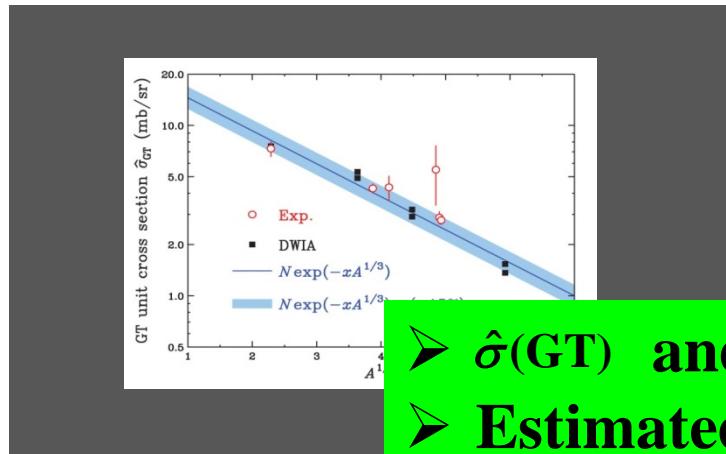
SD decomposed !



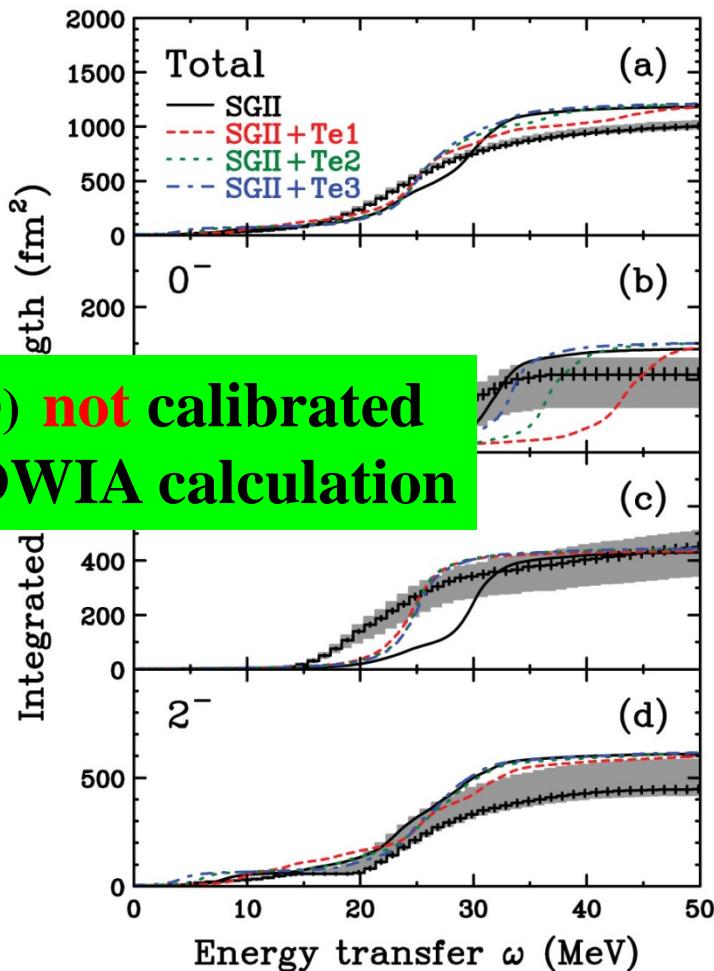
# Spin dipole strength in $^{208}\text{Pb}$ by Wakasa (Kyushu U)

Wakasa et al., 85(2012)064606

GT quenched by 30% !



0- and 2- quenched by 30% !



- $\hat{\sigma}(\text{GT})$  and  $\hat{\sigma}(\text{SD})$  **not calibrated**
- Estimated by DWIA calculation

# Probe calibration by $\beta$ -decay $B(GT/SD)$ values

- Rely on proportional relation

$$\left. \frac{d\sigma(\theta)}{d\Omega} \right|_{\Delta L=0} = \hat{\sigma}_{GT}(E_p, A) \cdot F_{GT}(q, \omega) \cdot B(GT)$$

$$\left. \frac{d\sigma(\theta)}{d\Omega} \right|_{\Delta L=1} = \hat{\sigma}_{SD}(E_p, A) \cdot F_{SD}(q, \omega) \cdot B(SD)$$

- Unit cross section should be calibrated using known  $B(GT/SD)$  by  $\beta$  decay !

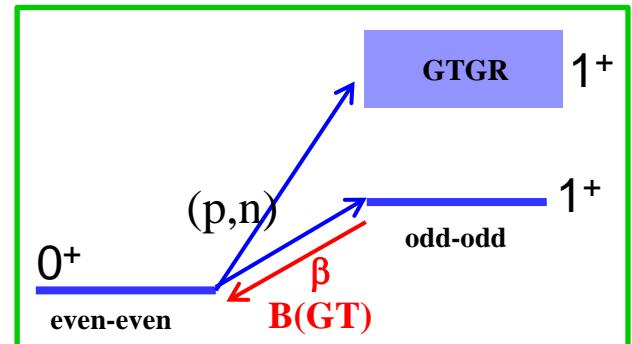
- Calibration is **NOT** available

➤  $\hat{\sigma}_{GT}$  for  $A > 130$

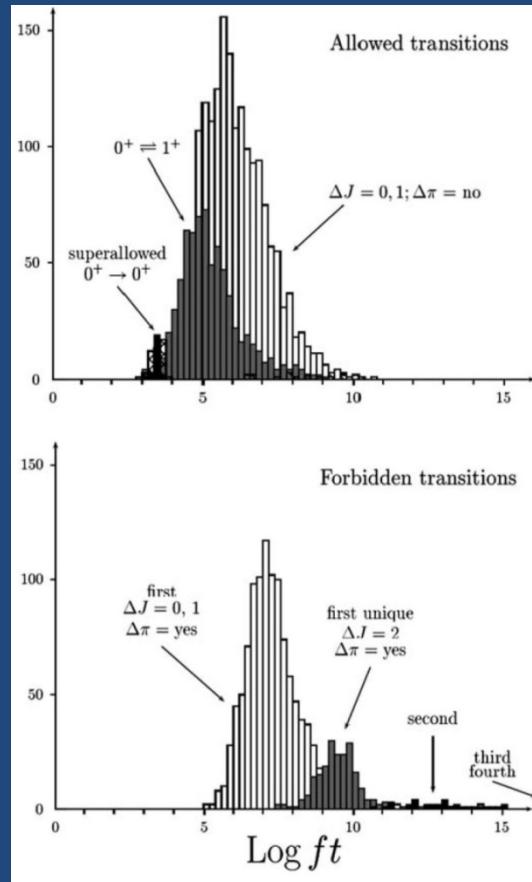
➤  $\hat{\sigma}_{SD}$  for  $A > 1$  (**nothing**)

- Why no calibration ?

➤ No good candidate with stable target



# $\beta$ -decay matrix elements for GT state

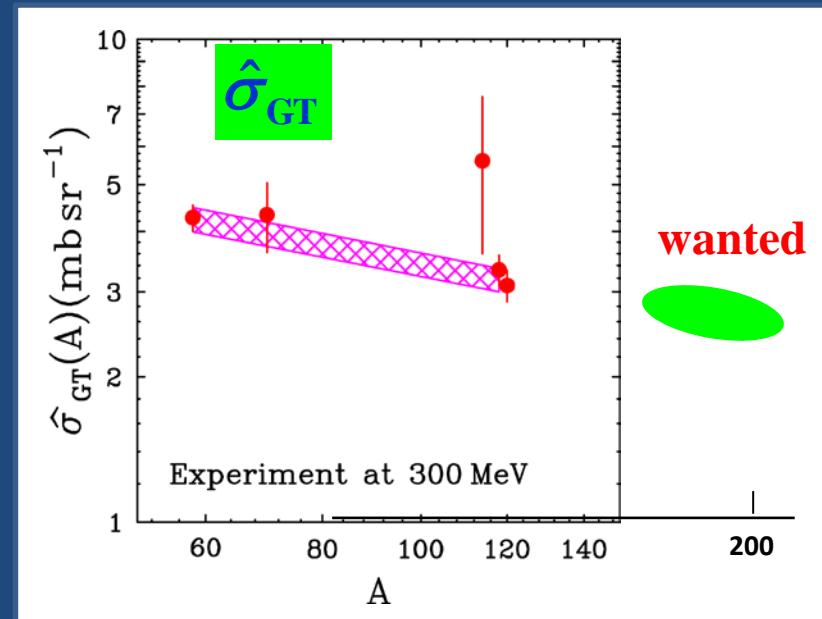


## ◆ GT moment

Bohr-Mottelson

$$\mathcal{M}(j_A, \kappa = 0, \lambda = 1, \mu) = \frac{g_A}{(4\pi)^{1/2}} \sum_k t_-(k) \sigma_\mu(k) \quad (3D-42)$$

- Operator is similar to reaction probe
- need unit  $\sigma(GT)$  for  $A \sim 200$



# Feasibility of $\sigma(GT)$ calibration for $A>160$

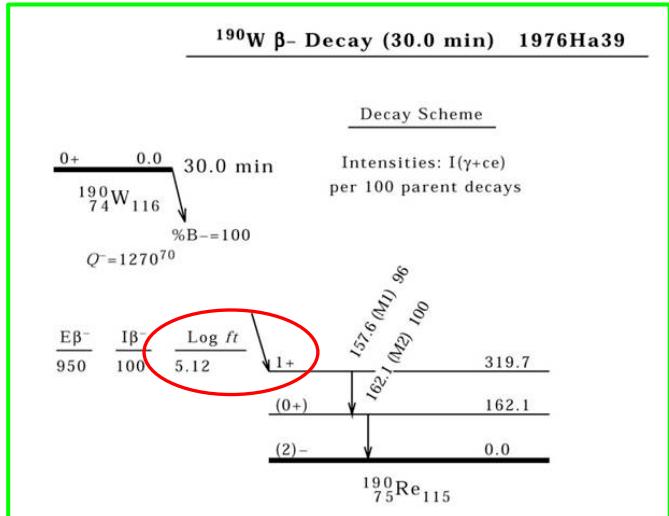
- Possible case ?  $^{190}\text{W}(\text{p},\text{n})$

- $\log ft = 5.12 \Rightarrow B(\text{GT})=0.03$
- Isolated : ?
- Why No F-trans. to 162 keV ?
- Isomer involvement ?
- Unstable beam exp.

*Cf. Sasano*

$^{118}\text{Sn}$ ,  $^{120}\text{Sn}$  :  $B(\text{GT})=0.34$

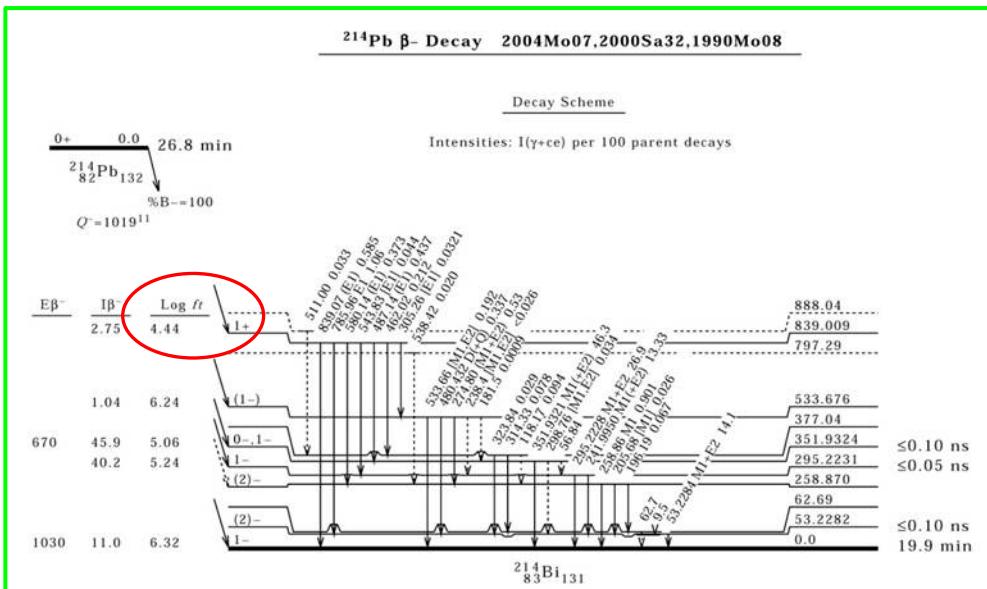
Too small !



- Possible case ?  $^{214}\text{Pb}(\text{p},\text{n})$

- $\log ft = 4.44 \Rightarrow B(\text{GT})=0.14$   
⇒ effective  $B(\text{GT}) \sim 0.07$
- Isolated : many states around
- Isomer involvement ?
- Unstable beam exp.

Still too small !



Need isolated GT decay with  $B(\text{GT})>0.5$  for  $A\sim 200$ .

# $\beta$ -decay matrix elements of SD states

◆ SD moment

Bohr-Mottelson

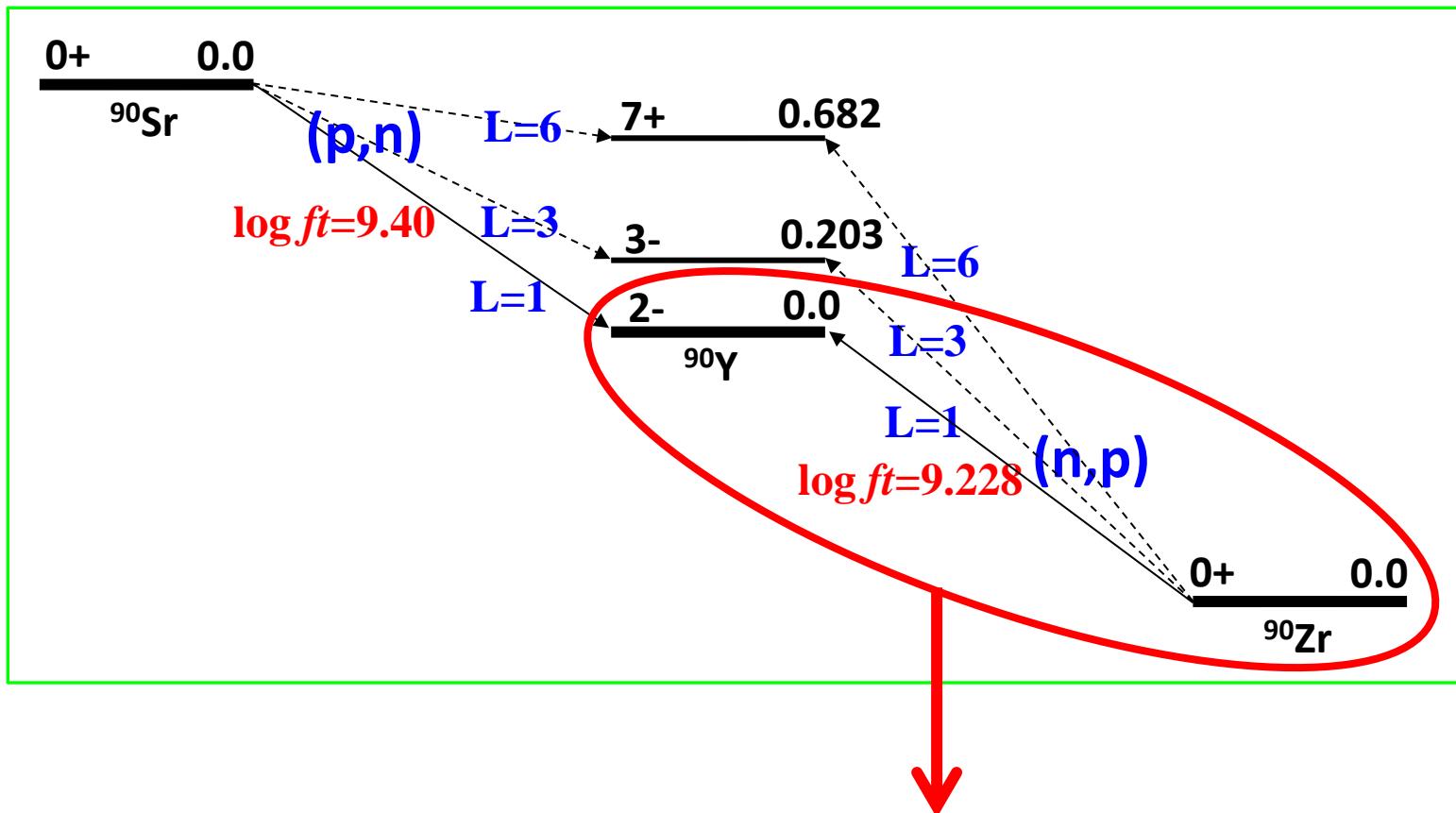
$$\left. \begin{aligned}
 \mathcal{M}(\rho_A, \lambda=0) &= (4\pi)^{-1/2} \frac{g_A}{c} \sum_k t_-(k) (\sigma(k) \cdot \mathbf{v}_k) \\
 \mathcal{M}(j_A, \kappa=1, \lambda=0) &= g_A \sum_k t_-(k) r_k (Y_1(\hat{\mathbf{r}}_k) \sigma(k))_0 \\
 \mathcal{M}(\rho_V, \lambda=1, \mu) &= g_V \sum_k t_-(k) r_k Y_{1\mu}(\hat{\mathbf{r}}_k) \\
 \mathcal{M}(j_V, \kappa=0, \lambda=1, \mu) &= (4\pi)^{-1/2} \frac{g_V}{c} \sum_k t_-(k) (v_k)_{1\mu} \\
 \mathcal{M}(j_A, \kappa=1, \lambda=1, \mu) &= g_A \sum_k t_-(k) r_k (Y_1(\hat{\mathbf{r}}_k) \sigma(k))_{1\mu} \\
 \mathcal{M}(j_A, \kappa=1, \lambda=2, \mu) &= g_A \sum_k t_-(k) r_k (Y_1(\hat{\mathbf{r}}_k) \sigma(k))_{2\mu}
 \end{aligned} \right\} \begin{aligned}
 \lambda\pi &= 0 - \\
 & \\
 & \\
 & \\
 & \\
 \lambda\pi &= 1 - \\
 & \\
 & \\
 & \\
 & \\
 \lambda\pi &= 2 - \quad \text{Unique FF !}
 \end{aligned} \quad (3D-43)$$

Operators are NOT necessarily similar to reaction probe operator  $t_{\pm} \sigma r Y_1$

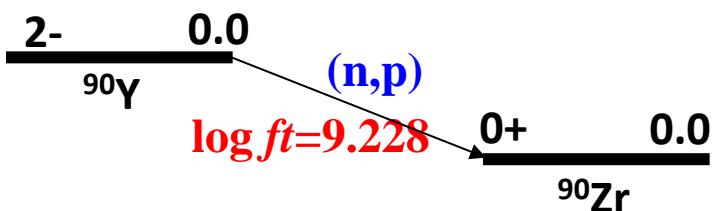
# Calibration of 2- SD at A=90

$$\mathcal{M}(j_A, \kappa = 1, \lambda = 2, \mu) = g_A \sum_k t_-(k) r_k (Y_1(\hat{r}_k) \sigma(k))_{2\mu} \quad \boxed{[\sigma \times r]^2}$$

Similar to reaction probe  $t_- \sigma r Y_1$



# Extraction of unit cross section for 2-



$$B(\text{SD}2-) \uparrow = 5 \frac{9}{4\pi} \frac{D}{ft} \left( \frac{g_v}{g_A} \right)^2 C^2$$

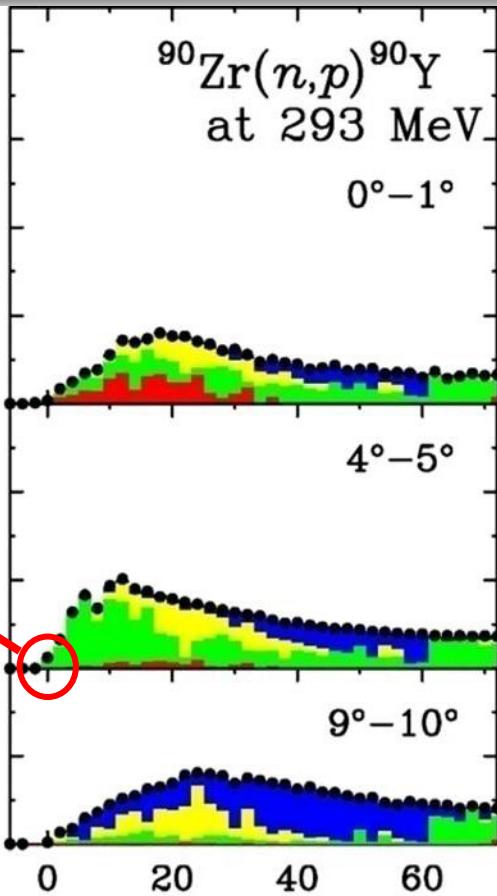
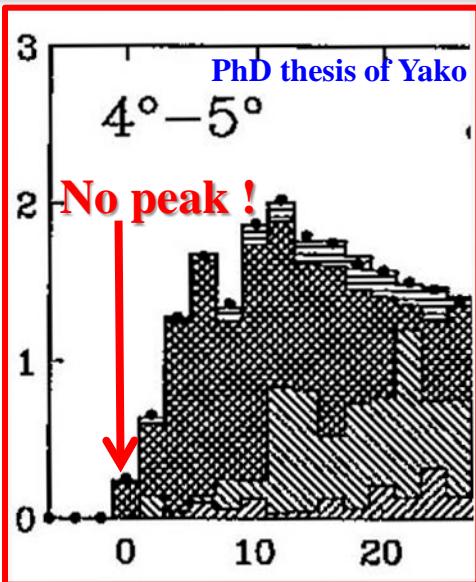
$$D=6143 \text{ s}, \quad C=386 \text{ fm}$$

$$\Rightarrow B(\text{SD}2-) \uparrow = 0.74 \text{ fm}^2$$

$$\sigma(\text{exp}) = \hat{\sigma}(\text{SD}2-) \cdot B(\text{SD}2-)$$

$$0.25 \left( \frac{\text{mb}}{\text{sr}} \right) = \hat{\sigma}(\text{SD}2-) \cdot 0.74 \text{ fm}^2$$

$$\Rightarrow \hat{\sigma}(\text{SD}2-) = 0.34 \left( \frac{\text{mb/sr}}{\text{fm}^2} \right)$$



DWIA estimation by Yako

Reasonable

$$\hat{\sigma}(\text{SD}2-) = 0.29 \left( \frac{\text{mb/sr}}{\text{fm}^2} \right)$$

# Most favorable case unit- $\sigma_{SD}(2^-)$

3- 0.11 (258 s) Isomer

0- 0.0 (158 s)

<sup>90</sup>Rb

**log ft=7.19 fastest !**

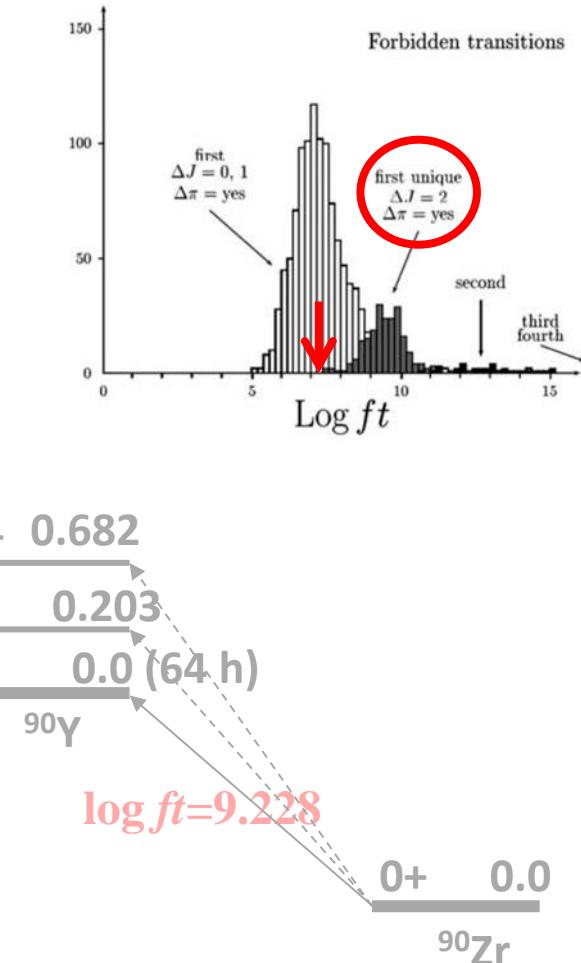
4+ 1.656

**log ft=7.35**  
 $0^- \rightarrow 0^+$

2+ 0.832  
<sup>90</sup>Sr

0+ 0.0 (29 y)

**log ft=9.40**



- Possible case ? <sup>90</sup>Rb(p,n)

- $\log ft = 7.19 \Rightarrow B(SD2-) = 26 \text{ fm}^2$

- Moderately isolated

- Unstable beam exp.

- Isomer involvement : Yes

7+ 0.682

3- 0.203

2- 0.0 (64 h)

**log ft=9.228**

0+ 0.0

<sup>90</sup>Zr

$$\sigma(\text{exp}) = \hat{\sigma}(\text{SD2-}) \times B(\text{SD2-}) = 0.34 \times 26 = 8.8 \left( \frac{\text{mb}}{\text{sr}} \right)$$

**Maybe measurable ?**

# Calibration of 0- and 1- SD

Not necessarily similar to reaction probe  $t_\pi \sigma r Y_1$

0-

$$\mathcal{M}(\rho_A, \lambda = 0) = (4\pi)^{-1/2} \frac{g_A}{c} \sum_k t_-(k)(\sigma(k) \cdot \mathbf{v}_k)$$

$\left. \begin{array}{l} \text{hadronic weak current} \\ \text{timelike comp. } \gamma_5 \end{array} \right\} \lambda\pi = 0 -$

$$\mathcal{M}(j_A, \kappa = 1, \lambda = 0) = g_A \sum_k t_-(k) r_k (Y_1(\hat{\mathbf{r}}_k) \sigma(k))_0$$

$[\sigma \times \mathbf{r}]^0$

- Two terms tend to cancel.

1-

$$\mathcal{M}(\rho_V, \lambda = 1, \mu) = g_V \sum_k t_-(k) r_k Y_{1\mu}(\hat{\mathbf{r}}_k)$$

Non-spinflip !

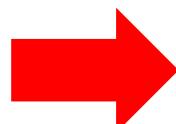
$$\mathcal{M}(j_V, \kappa = 0, \lambda = 1, \mu) = (4\pi)^{-1/2} \frac{g_V}{c} \sum_k t_-(k) (v_k)_{1\mu}$$

hadronic weak current  $\alpha$

$$\mathcal{M}(j_A, \kappa = 1, \lambda = 1, \mu) = g_A \sum_k t_-(k) r_k (Y_1(\hat{\mathbf{r}}_k) \sigma(k))_{1\mu}$$

$[\sigma \times \mathbf{r}]^1$

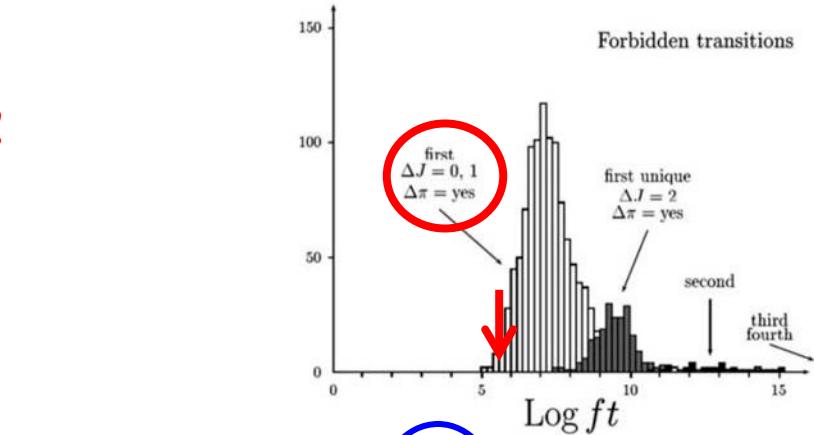
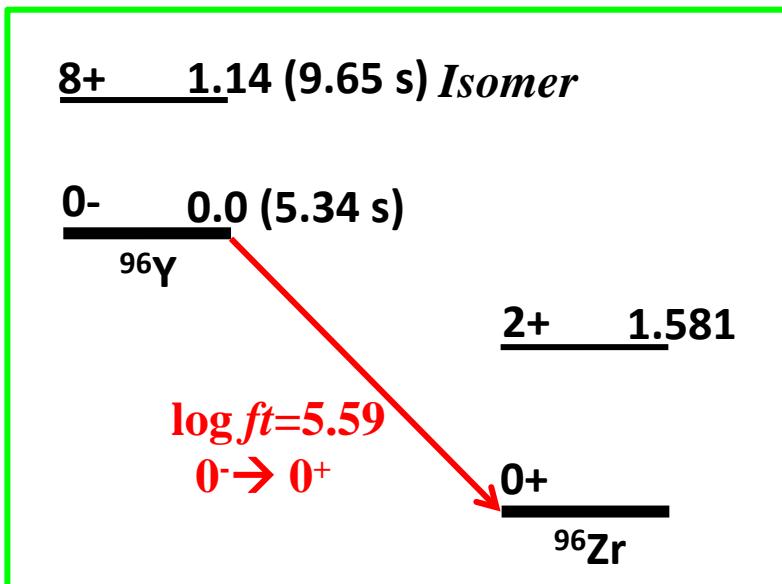
- Involves non-spinflip.



Probably  $B(0^-/1^-)$  of  $\beta$  decay is unable to use as a probe calibration purpose.

# Candidate of 0- SD calibration

- Possible case ?  $^{96}\text{Y}(\text{p},\text{n})$ 
  - $\log ft = 5.59 \Rightarrow B(\text{SD}0^-) = 1,125 \text{ fm}^2$  !
  - Isolated
  - Unstable beam exp.
  - Isomer involvement : Yes



$$O(0^-) = g_A \left[ \frac{\vec{\sigma} \cdot \vec{p}}{M_N} + \xi i \vec{\sigma} \cdot \vec{r} \right] t_-$$

~ 2 enhancement due to MEC

(p,n)

- Assume:  $B(\text{SD}0^-; \text{SF}) = 0.1 \times B(\text{SD}0^-)$

$$\sigma(\text{exp}) = \hat{\sigma}(\text{SD}2^-) \times B(\text{SD}0^-; \text{SF}) \approx 10 \left( \frac{\text{mb}}{\text{sr}} \right)$$

- Feasible with RI beam exp.
- Proportionality ???

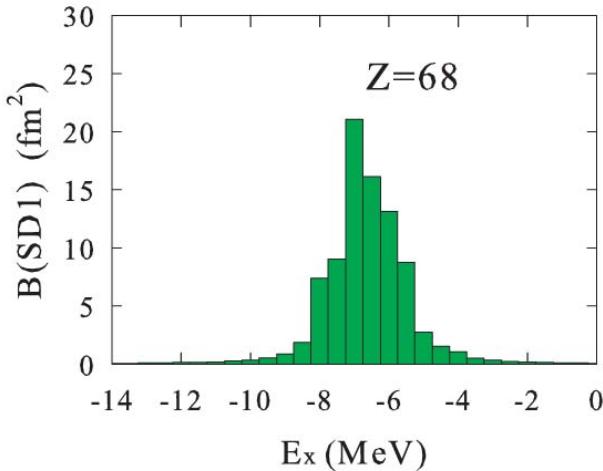
# Difficulty of 1<sup>-</sup> SD calibration

## ● Shell model estimate of 1<sup>-</sup> SD

PHYSICAL REVIEW C **85**, 015802 (2012)

$\beta$  decays of isotones with neutron magic number of  $N = 126$  and  $r$ -process nucleosynthesis

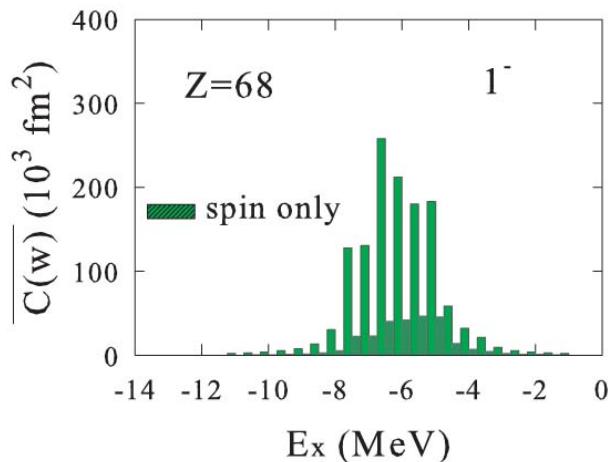
Toshio Suzuki,<sup>1,2,3</sup> Takashi Yoshida,<sup>4</sup> Toshitaka Kajino,<sup>3,4</sup> and Takaharu Otsuka<sup>5,6</sup>



$$B(SD\lambda) = \frac{1}{2J_i + 1} |\langle f || r [Y^{(1)} \times \vec{\sigma}]^\lambda t_- || i \rangle|^2 \quad (7)$$

$$O(1^-) = \left[ g_V \frac{\vec{p}}{M_N} - \xi (g_A \vec{\sigma} \times \vec{r} - i g_V \vec{r}) \right] t_-,$$

(p,n)



- Strong non-spinflip strength
- log  $ft$  is large
- Small branching ratio

⇒ Probably non-realistic to use  $\beta^- B(1^-)$  for calibration

# Summary

## 1. GT and SD : important spin-isospin responses

- (p,n) reaction could provide B(GT) and B(SD)

## 2. (p,n) reaction must be calibrated by $\beta$ B(GT/SD)

- No B(GT) for  $A > 160$
- Nothing for B(SD)

## 3. RI beam is now available → open new possibilities

### 4. GT:

- $B(GT) > 0.5$  is needed for  $A > 160$

### 5. SD: with 0- or 1-

- $B(2-) : {}^{90}\text{Rb}(p,n)$  may be feasible with  $\log ft = 7.19$
- $B(1-) : \text{Maybe essential difficulty with non-spinflip}$
- $B(0-) : {}^{96}\text{Y}(p,n)$  may be with  $\log ft = 5.59$  but  $\gamma_5$  term ?

### 6. SPES project

- $B(GT)/B(SD)$  are always precious for structure study
- $\beta$  decay measurement ?