

# FPCP 2010

## Measurements of $\phi_2$

Jeremy Dalseno

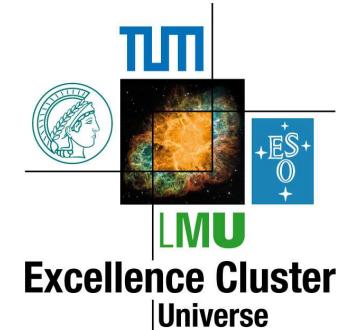


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Excellence Cluster Universe

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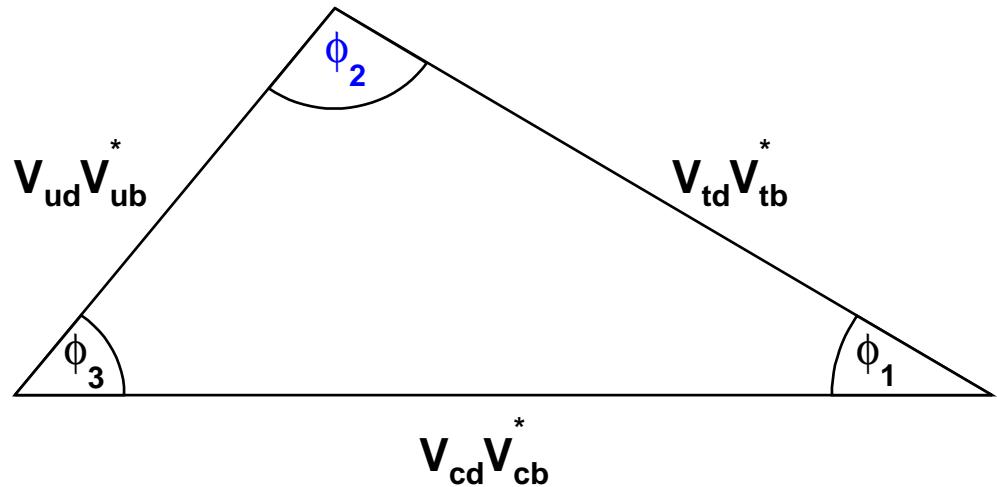
25 Maggio 2010



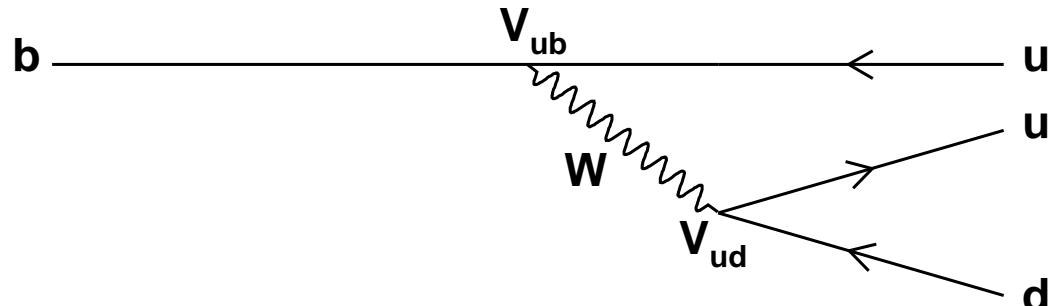
# Outline

1.  $B^0 \rightarrow \pi^+ \pi^-$
2.  $B^0 \rightarrow (\rho\pi)^0$
3.  $B \rightarrow \rho\rho$
4.  $B^0 \rightarrow a_1(1260)^\pm \pi^\mp$

From CKM matrix unitarity,

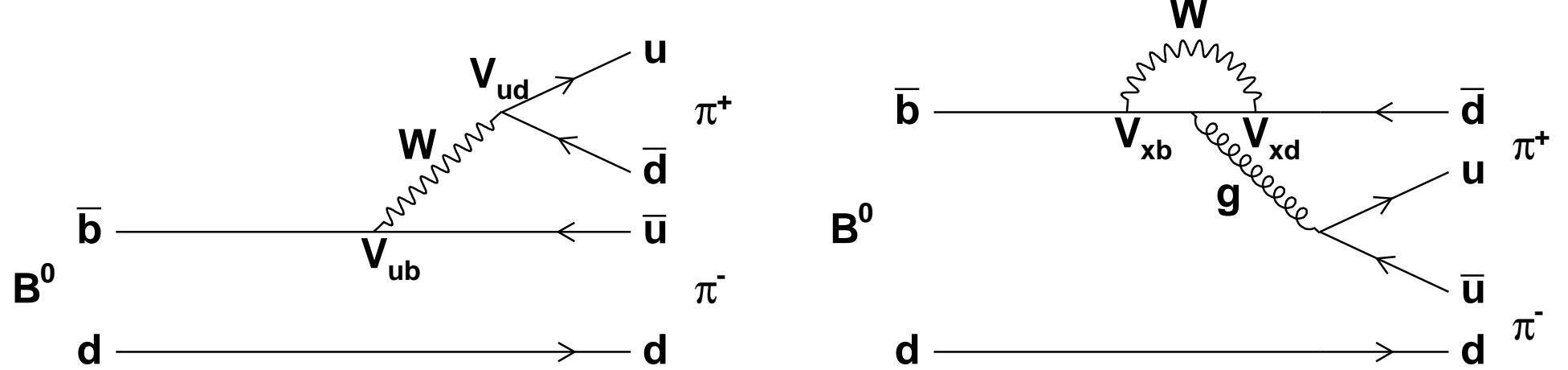


Tree-level  $b \rightarrow u\bar{u}d$  transitions sensitive to  $\phi_2$



$$B^0 \rightarrow \pi^+ \pi^-$$

Both tree and penguin amplitudes may contribute to the final state



Tree and penguin amplitudes have different strong and weak phases

Direct  $CP$  violation,  $\mathcal{A}_{CP} \neq 0$ , possible

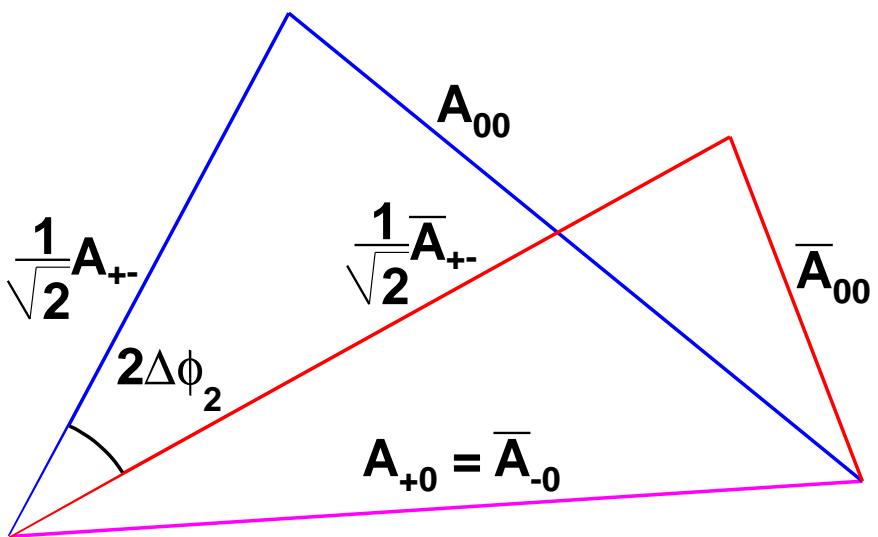
Measure an effective  $\phi_2$

$$\mathcal{S}_{CP} = \sqrt{1 - \mathcal{A}_{CP}^2} \sin(2\phi_2 - 2\Delta\phi_2) = \sqrt{1 - \mathcal{A}_{CP}^2} \sin 2\phi_2^{\text{eff}}$$

$$B^0 \rightarrow \pi^+ \pi^-$$

Can recover  $\phi_2$  with an SU(2) isospin analysis

M. Gronau and D. London, PRL 65, 3381 (1990)



$$A_{+0} = \frac{1}{\sqrt{2}} A_{+-} + A_{00}$$

$$\bar{A}_{-0} = \frac{1}{\sqrt{2}} \bar{A}_{+-} + \bar{A}_{00}$$

$A_{ij}$ : Amplitude of  $B \rightarrow \pi^i \pi^j$

$B^+ \rightarrow \pi^+ \pi^0$  is a pure tree mode

Neglecting electroweak penguins,  $A_{+0} = \bar{A}_{-0}$

4-fold ambiguity in  $2\Delta\phi_2$

Fully determined from 6 physical observables

$$\mathcal{B}(B^0 \rightarrow \pi^+ \pi^-), \mathcal{B}(B^0 \rightarrow \pi^0 \pi^0), \mathcal{B}(B^+ \rightarrow \pi^+ \pi^0)$$

$$\mathcal{A}_{CP}(\pi^+ \pi^-), \mathcal{S}_{CP}(\pi^+ \pi^-), \mathcal{A}_{CP}(\pi^0 \pi^0)$$

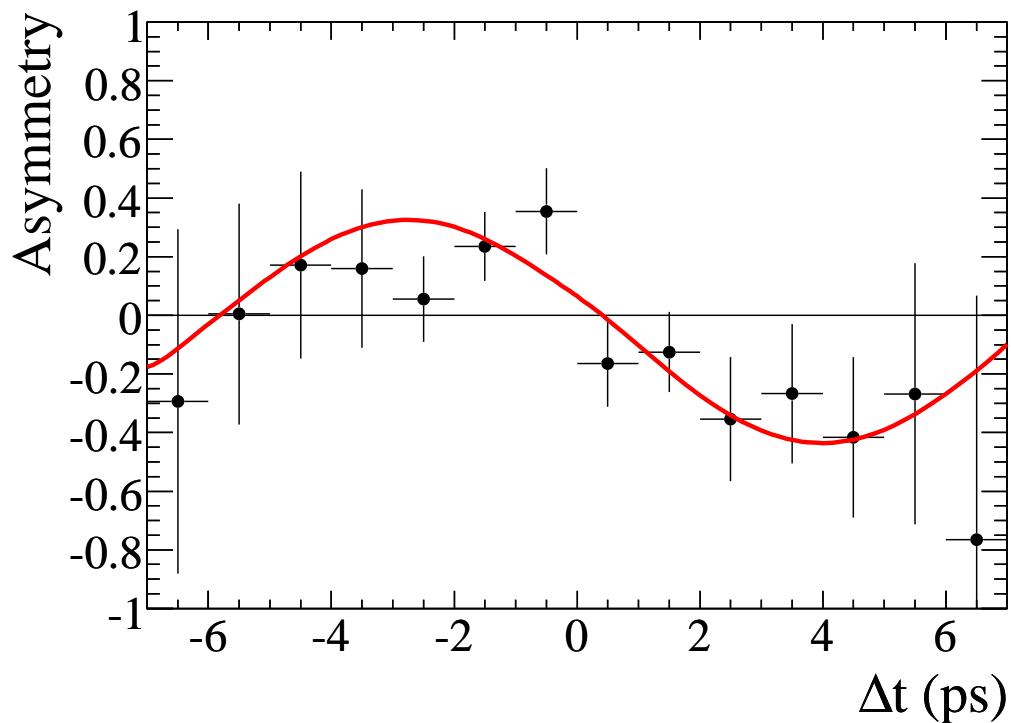
# $B^0 \rightarrow \pi^+ \pi^-$

BaBar

arXiv:0807.4226 (2008)

467 million  $B^0 \bar{B}^0$  pairs

$$A(\Delta t) \equiv (N_{B^0} - N_{\bar{B}^0}) / (N_{B^0} + N_{\bar{B}^0})$$



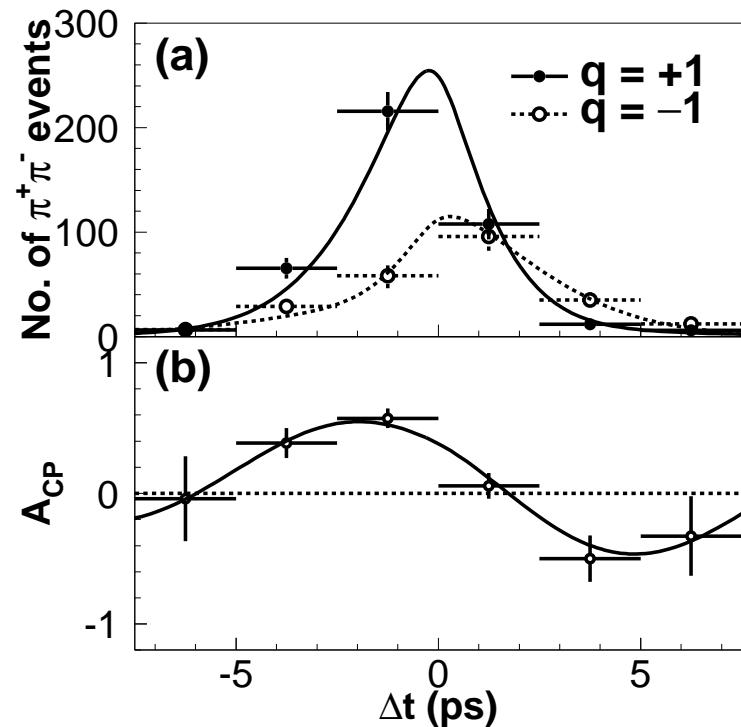
Clear mixing-induced asymmetry

Belle

PRL 98, 211801 (2007)

535 million  $B^0 \bar{B}^0$  pairs

$\Delta t$  distribution and asymmetry



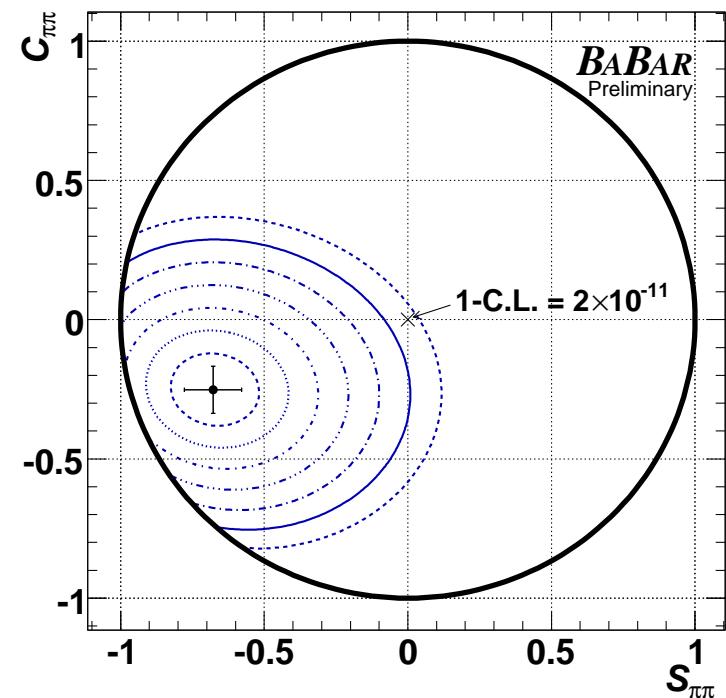
Height difference shows direct  $CP$  asymmetry

# $B^0 \rightarrow \pi^+ \pi^-$

BaBar

$$\mathcal{A}_{CP} = +0.25 \pm 0.08 \pm 0.02 \text{ (3.0}\sigma\text{)}$$

$$\mathcal{S}_{CP} = -0.68 \pm 0.10 \pm 0.03 \text{ (6.3}\sigma\text{)}$$



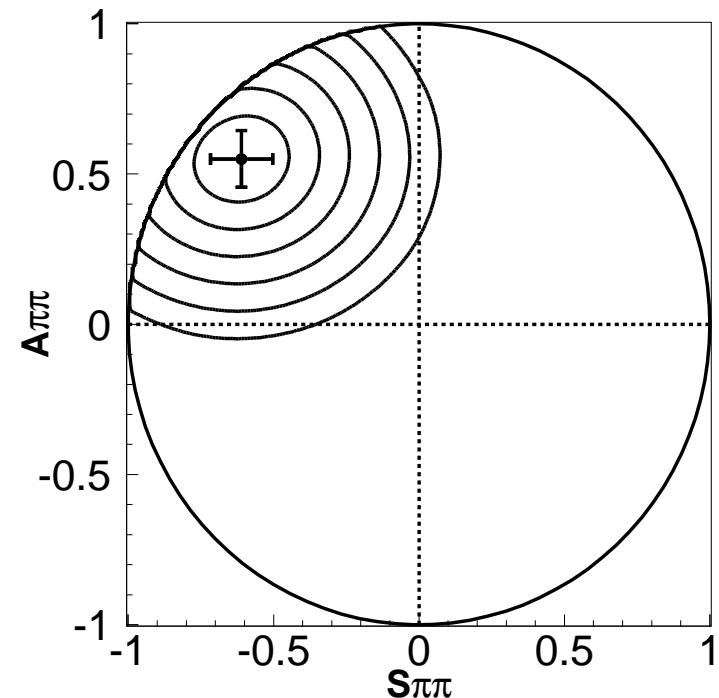
$$\mathcal{C}_{CP} = -\mathcal{A}_{CP}$$

Both experiments have observed  $CP$  violation

Belle

$$\mathcal{A}_{CP} = +0.55 \pm 0.08 \pm 0.05 \text{ (5.5}\sigma\text{)}$$

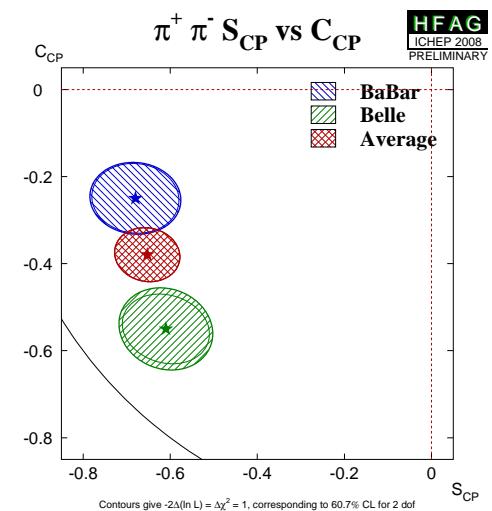
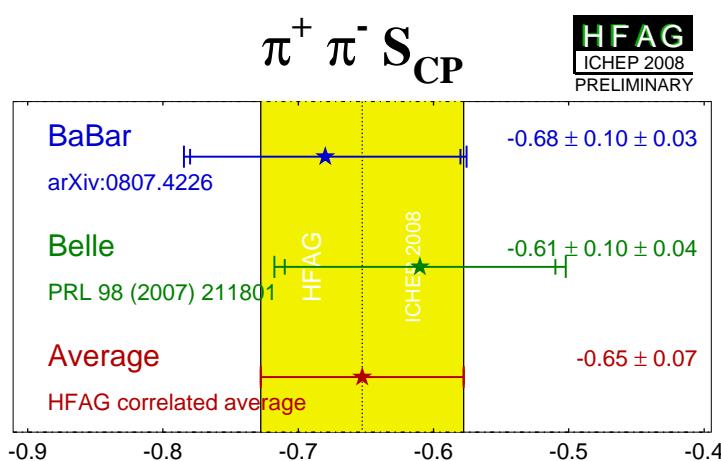
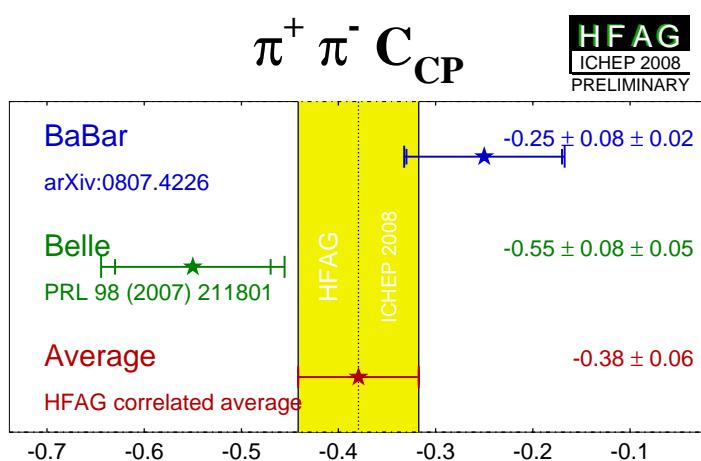
$$\mathcal{S}_{CP} = -0.61 \pm 0.10 \pm 0.04 \text{ (5.3}\sigma\text{)}$$



$CP$  violation observed in individual parameters

$$B^0 \rightarrow \pi^+ \pi^-$$

World average



$$\mathcal{C}_{CP} = -\mathcal{A}_{CP}$$

$1.9\sigma$  difference between BaBar and Belle measurements

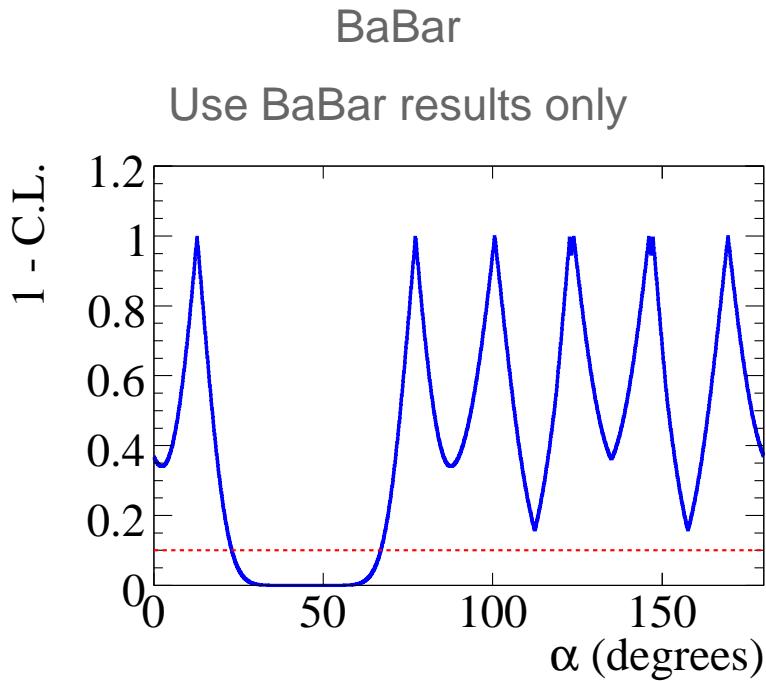
Both experiments demonstrate that more than a tree amplitude is present

$$B^0 \rightarrow \pi^+ \pi^-$$

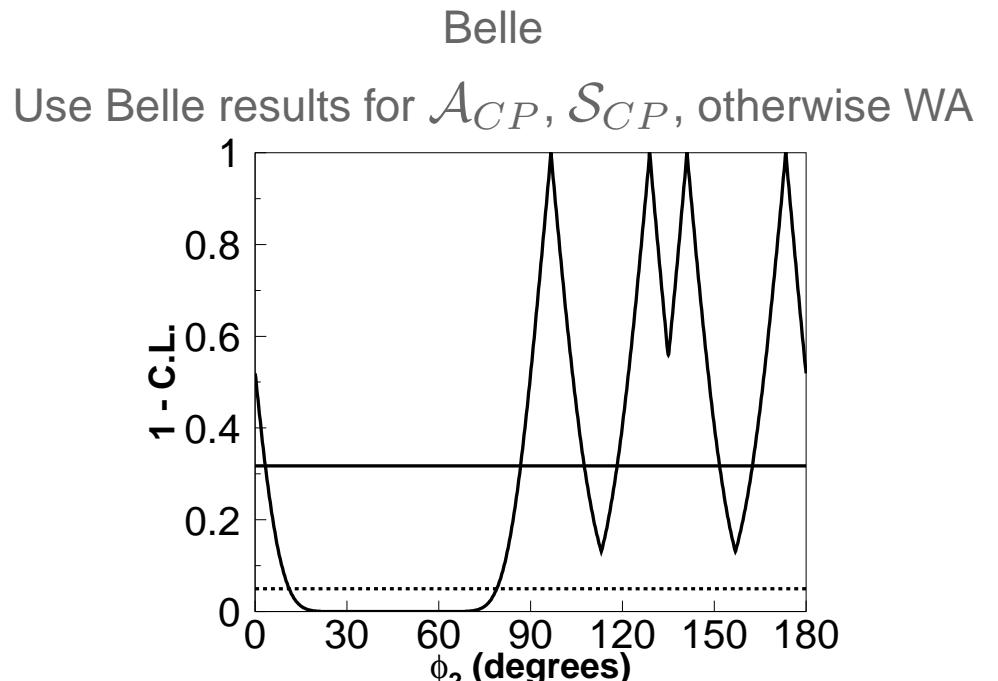
Perform isospin analysis

Scan  $\phi_2$  and construct  $\chi^2$  for the five amplitudes ( $A_{+0}, A_{+-}, A_{00}, \bar{A}_{+-}, \bar{A}_{00}$ )

Convert to CL



Two-fold ambiguity of  $\phi_2^{\text{eff}}$  in  $\mathcal{S}_{CP}$  included  
 $[23^\circ, 67^\circ]$  excluded at 90% CL



Only SM expectation of  $\phi_2^{\text{eff}}$  in  $\mathcal{S}_{CP}$  included  
 $[11^\circ, 79^\circ]$  excluded at 95% CL

$$B^0 \rightarrow (\rho\pi)^0$$

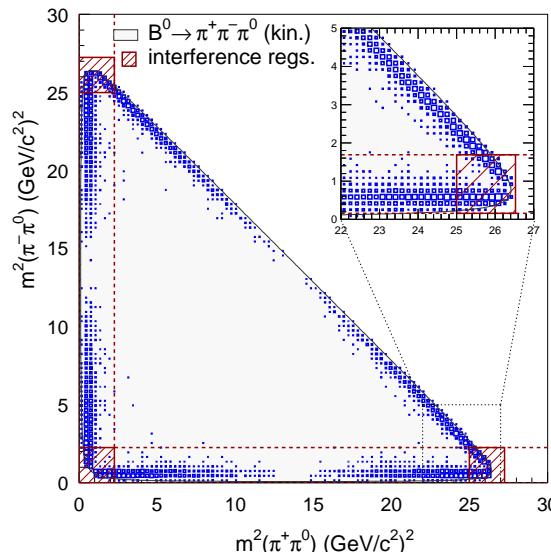
Not a  $CP$  eigenstate, need to consider the 4 flavour-charge configurations

Corresponding isospin analysis has 12 unknowns compared to 6 for  $CP$  eigenstates

However, can constrain  $\phi_2$  without ambiguity explicitly in the analysis

A. Snyder and H. Quinn, PRD **48** 2139 (1993)

Include variation of the strong phases of the interfering  $\rho$  resonances in the Dalitz Plot



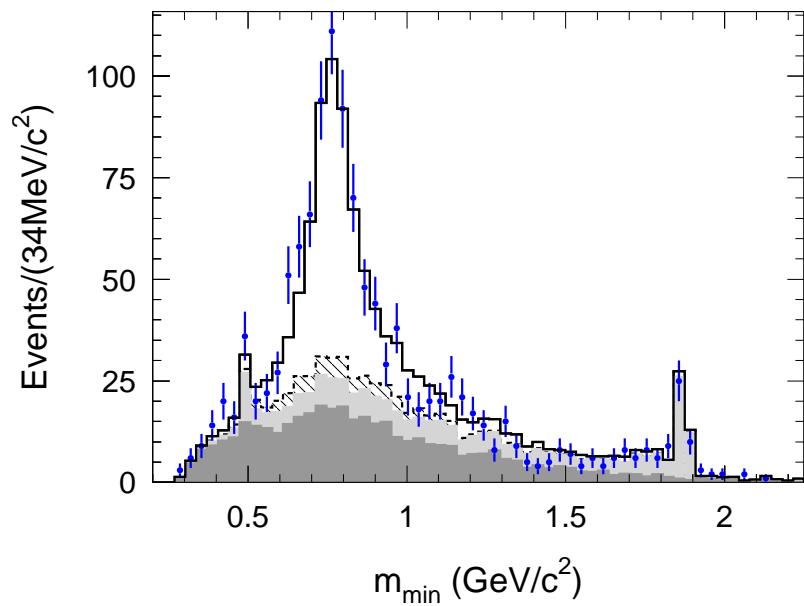
# $B^0 \rightarrow (\rho\pi)^0$

BaBar

PRD **76** 012004 (2007)

375 million  $B^0\bar{B}^0$  pairs

Mass projections



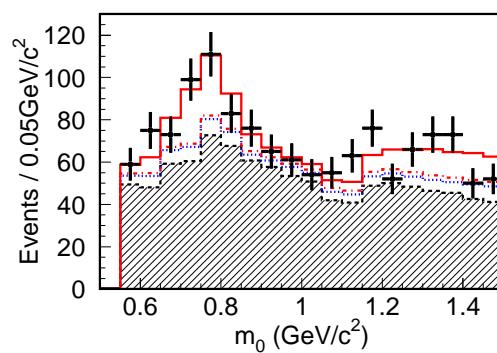
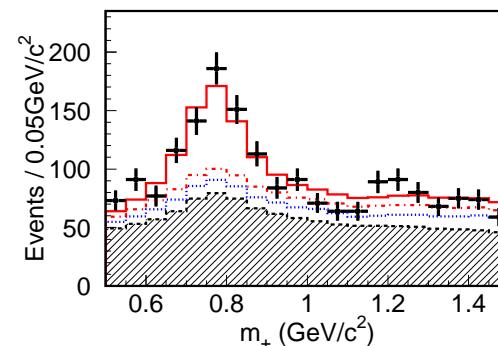
Plot minimum of  $m_+, m_-, m_0$

Belle

PRL **98** 221602 (2007)

449 million  $B^0\bar{B}^0$  pairs

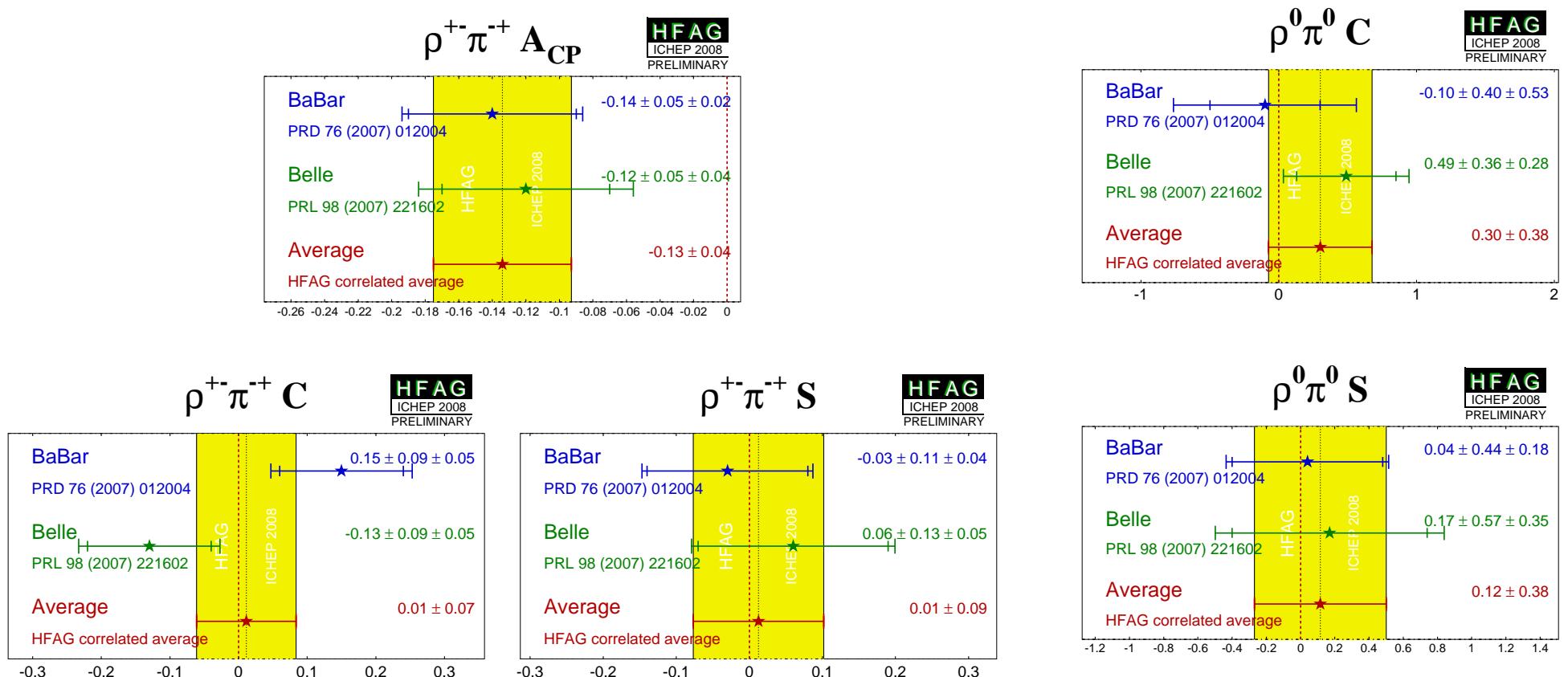
Mass projections



$$B^0 \rightarrow (\rho\pi)^0$$

For  $B^0 \rightarrow \rho^\pm \pi^\mp$

$\mathcal{A}_{CP}$  is time and flavour-integrated  $CP$  asymmetry



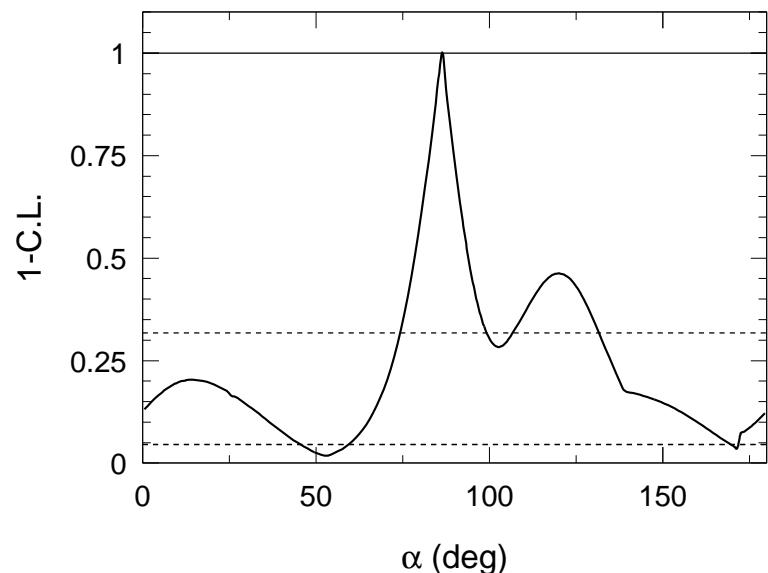
Good agreement between experiments

$$B^0 \rightarrow (\rho\pi)^0$$

Perform  $\phi_2$  scan

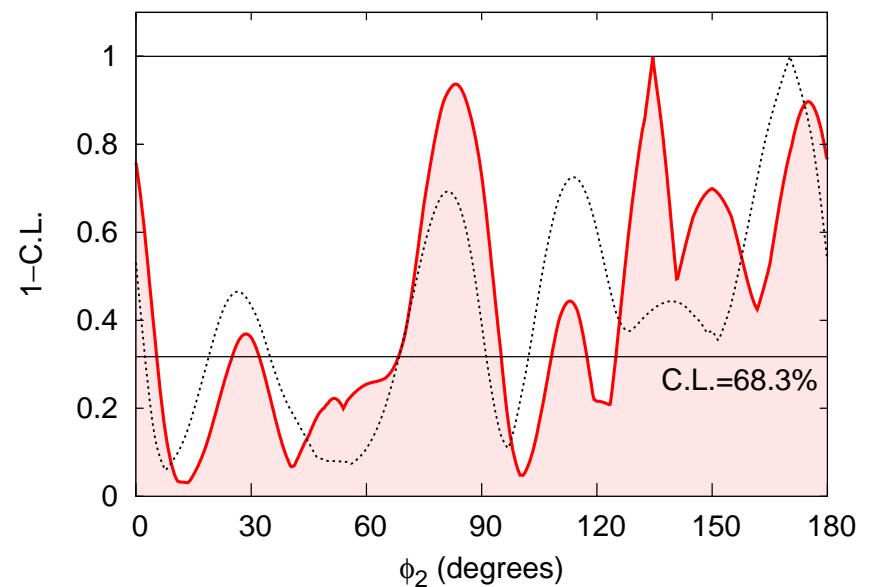
BaBar

Use  $B^0 \rightarrow (\rho\pi)^0$  results only



Belle

Also include  $\mathcal{B}$  and  $\mathcal{A}_{CP}$  of  $B^+ \rightarrow \rho^+\pi^0, \rho^0\pi^+$



$$\phi_2 = (87^{+45}_{-13})^\circ$$

for entire  $\phi_2$  range

Difficult to pin down  $\phi_2$  with  $B^0 \rightarrow (\rho\pi)^0$

Dotted line: Use  $B^0 \rightarrow (\rho\pi)^0$  results only

$68^\circ < \phi_2 < 95^\circ$  at 68.3% CL

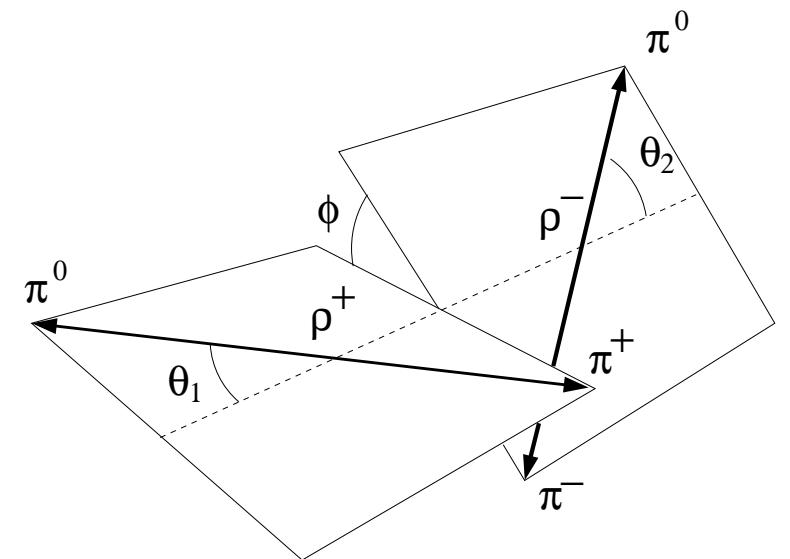
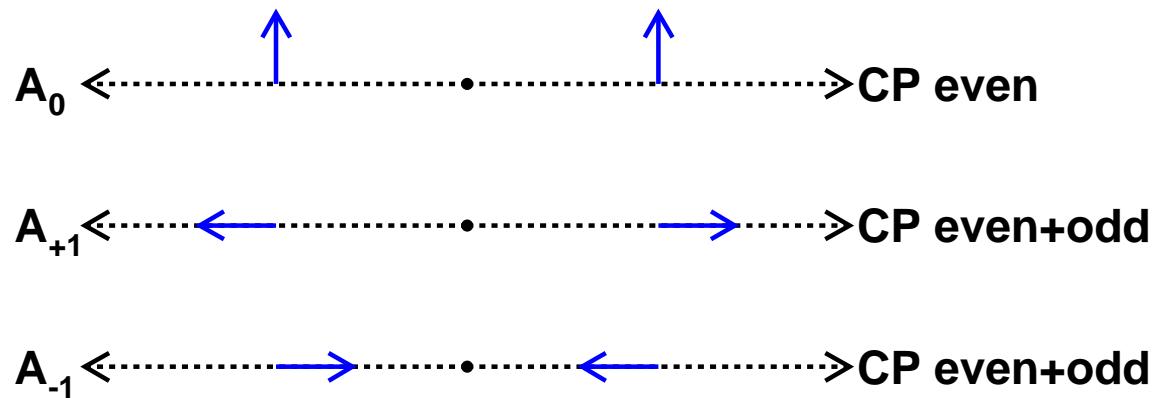
for solution consistent with SM

$$B^0 \rightarrow \rho^+ \rho^-$$

$$S \rightarrow VV$$

Final state contains 1 longitudinal and 2 transverse amplitudes

In helicity basis,



Integrating over  $\phi$ , angular decay rate

$$\frac{d^2 N}{d \cos \theta_1 d \cos \theta_1} \propto 4f_L \cos^2 \theta_1 \cos^2 \theta_2 + (1 - f_L) \sin^2 \theta_1 \sin^2 \theta_2, \quad f_L \equiv \frac{|A_0|^2}{|A_0|^2 + |A_{+1}|^2 + |A_{-1}|^2}$$

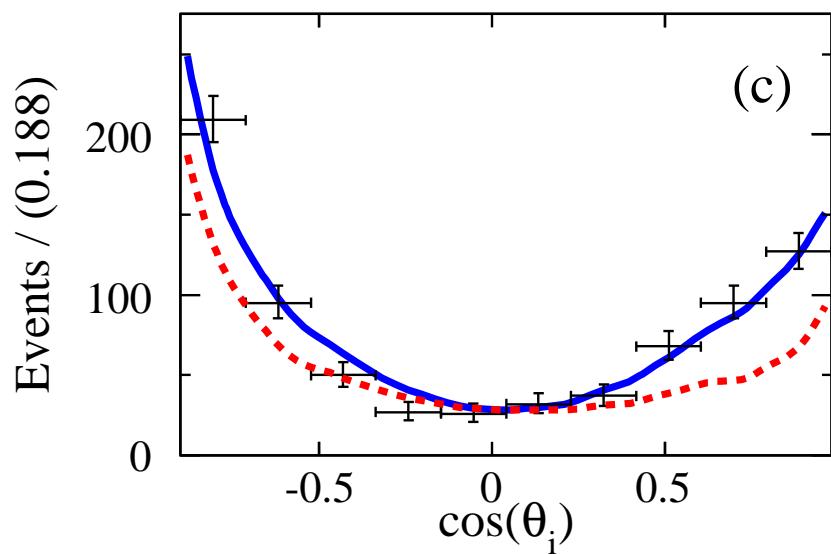
$$B^0 \rightarrow \rho^+ \rho^-$$

BaBar

PRD **76** 052007 (2007)

384 million  $B^0 \bar{B}^0$  pairs

Helicity

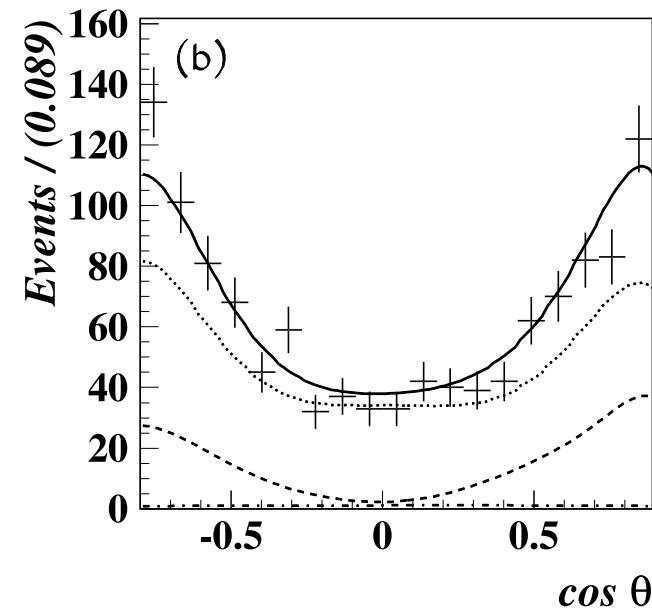


Belle

PRL **96** 171801 (2006)

275 million  $B^0 \bar{B}^0$  pairs

Helicity



$$\mathcal{B}(B^0 \rightarrow \rho^+ \rho^-) = (25.5 \pm 2.1^{+3.6}_{-3.9}) \times 10^{-6} \quad \mathcal{B}(B^0 \rightarrow \rho^+ \rho^-) = (22.8 \pm 3.8^{+2.3}_{-2.6}) \times 10^{-6}$$

$$f_L = 0.992 \pm 0.024 \text{ (stat)} {}^{+0.026}_{-0.013} \text{ (syst)} \quad f_L = 0.941^{+0.034}_{-0.040} \text{ (stat)} \pm 0.030 \text{ (syst)}$$

Longitudinal polarisation dominates

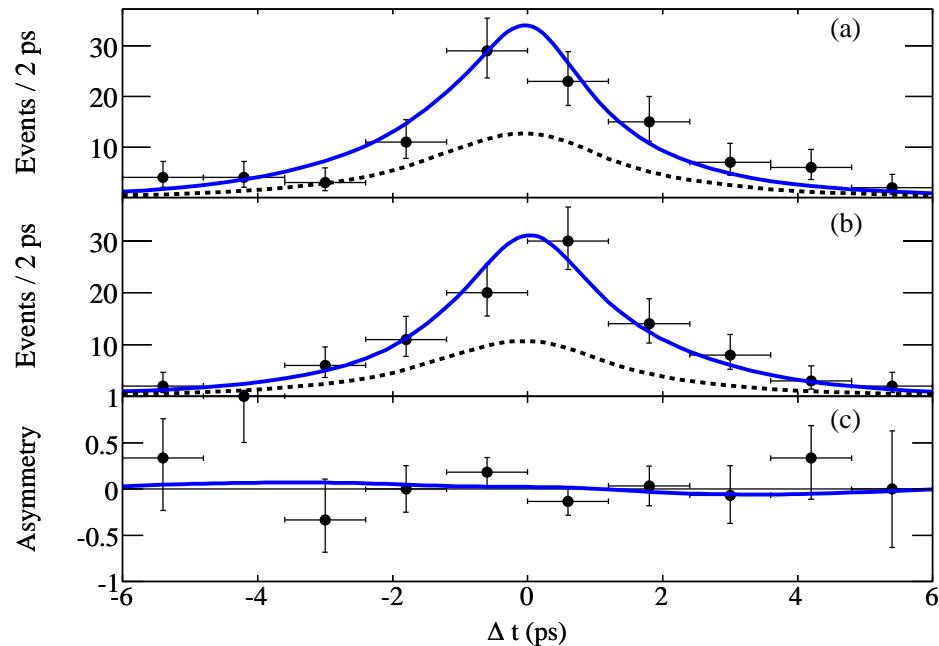
$$B^0 \rightarrow \rho^+ \rho^-$$

BaBar

PRD 76 052007 (2007)

384 million  $B^0 \bar{B}^0$  pairs

$\Delta t$  distribution and asymmetry



$$\mathcal{A}_{CP} = -0.01 \pm 0.15 \pm 0.06$$

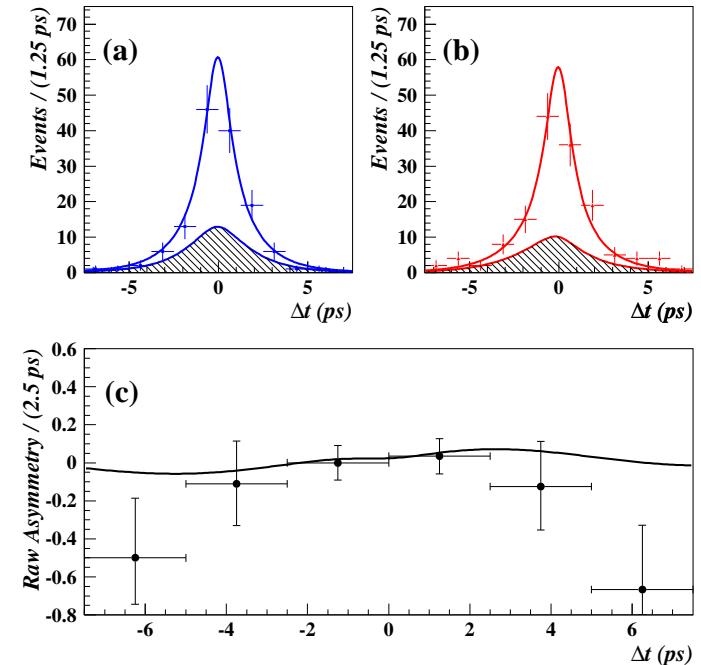
$$\mathcal{S}_{CP} = -0.17 \pm 0.20^{+0.05}_{-0.06}$$

Belle

PRD 76 011104 (2007)

Update to 535 million  $B^0 \bar{B}^0$  pairs

$\Delta t$  distribution and asymmetry

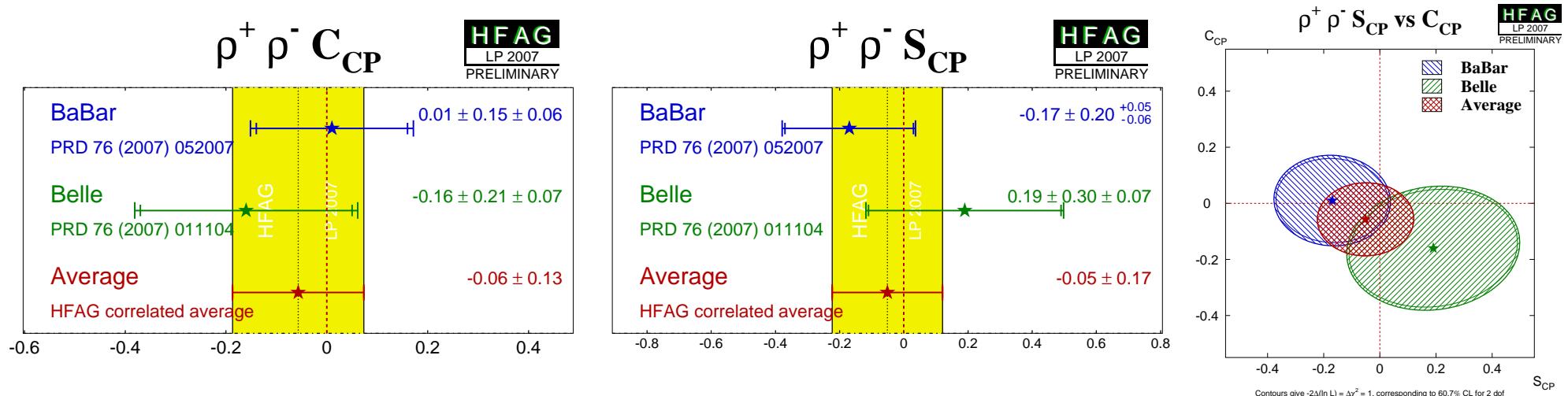


$$\mathcal{A}_{CP} = +0.16 \pm 0.21 \pm 0.07$$

$$\mathcal{S}_{CP} = +0.19 \pm 0.30 \pm 0.07$$

$$B^0 \rightarrow \rho^+ \rho^-$$

World average



$$\mathcal{C}_{CP} = -\mathcal{A}_{CP}$$

Good agreements between experiments

$\mathcal{A}_{CP} \approx 0$ , small penguin contribution

$$B^0 \rightarrow \rho^0 \rho^0$$

Time-dependent measurement provides additional information to isospin analysis

BaBar

PRD **78** 071104(R) (2008)

465 million  $B^0 \bar{B}^0$  pairs

$$\mathcal{B}(B^0 \rightarrow \rho^0 \rho^0) =$$

$$(0.92 \pm 0.32 \pm 0.14) \times 10^{-6}$$

$3.1\sigma$  evidence

$$f_L = 0.75^{+0.11}_{-0.14} \text{ (stat)} \pm 0.04 \text{ (syst)}$$

$$\mathcal{A}_{CP} = -0.2 \pm 0.8 \pm 0.3$$

$$\mathcal{S}_{CP} = +0.3 \pm 0.7 \pm 0.2$$

Difficult to isolate  $\rho^0 \rho^0$  in presence of other 4-body signals,  $a_1 \pi$ ,  $\rho \pi \pi$ ,  $4\pi$ ,  $f_0 \rho^0$ ,  $f_0 f_0$ ,  $f_0 \pi \pi$

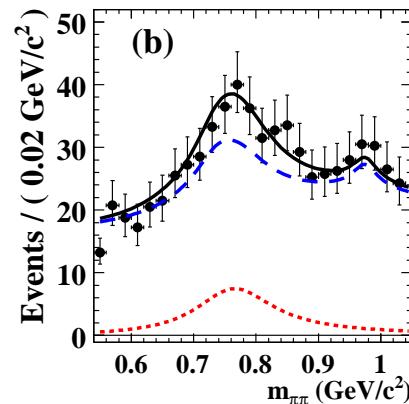
Belle

PRD **78** 111102(R) (2008)

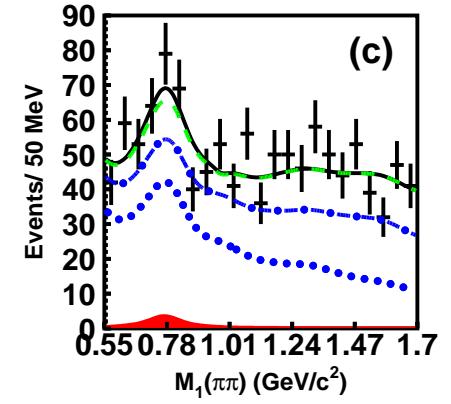
657 million  $B^0 \bar{B}^0$  pairs

$$\mathcal{B}(B^0 \rightarrow \rho^0 \rho^0) < 1.0 \times 10^{-6} \text{ at 90% CL}$$

BaBar



Belle



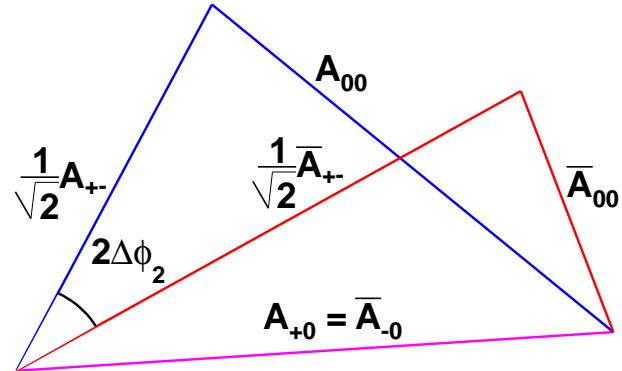
# $B^+ \rightarrow \rho^+ \rho^0$

Recent results from BaBar

PRL 102 141802 (2009)

$$\mathcal{B}(B^+ \rightarrow \rho^+ \rho^0) = (23.7 \pm 1.4 \pm 1.4) \times 10^{-6}$$

Precise measurement of isospin triangle base

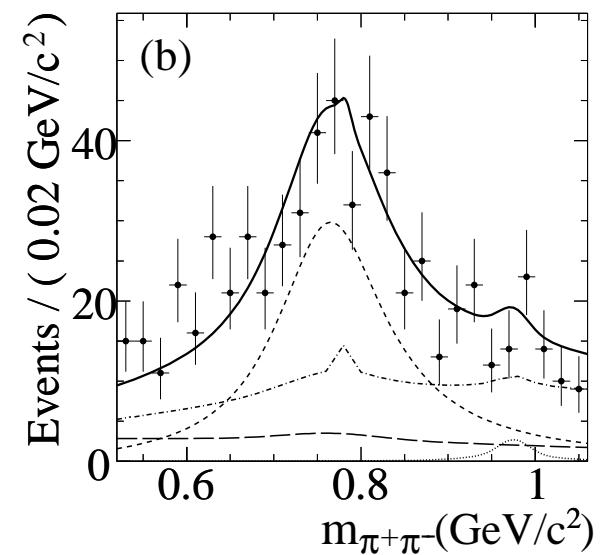
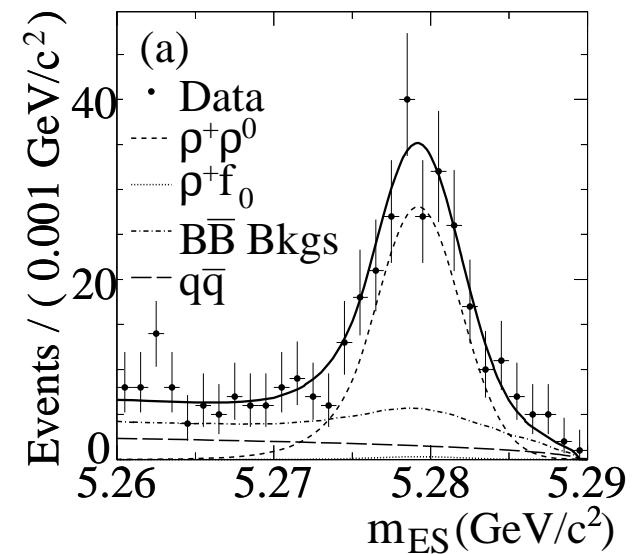


$$f_L = 0.950 \pm 0.015 \pm 0.006$$

Dominantly longitudinally polarised

$$\mathcal{A}_{CP} = 0.054 \pm 0.055 \pm 0.010$$

No evidence for electroweak penguins



# $B^0 \rightarrow \rho\rho$

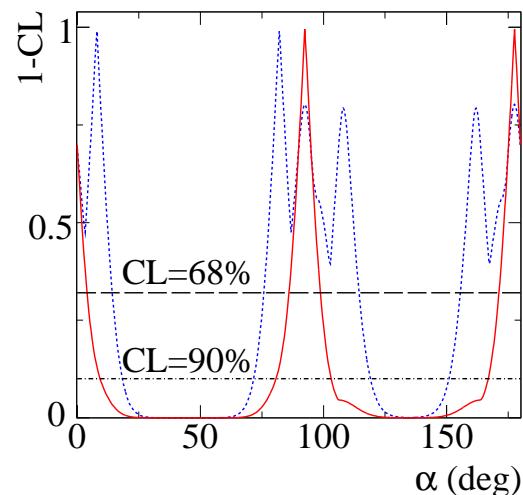
Branching fraction of  $B^+ \rightarrow \rho^+\rho^0$  large compared to  $B^0 \rightarrow \rho^0\rho^0$

Nearly flat isospin triangles  $\Rightarrow$  4 solutions of  $\Delta\phi_2$  nearly degenerate

BaBar

PRL 102 141802 (2009)

Use BaBar results only

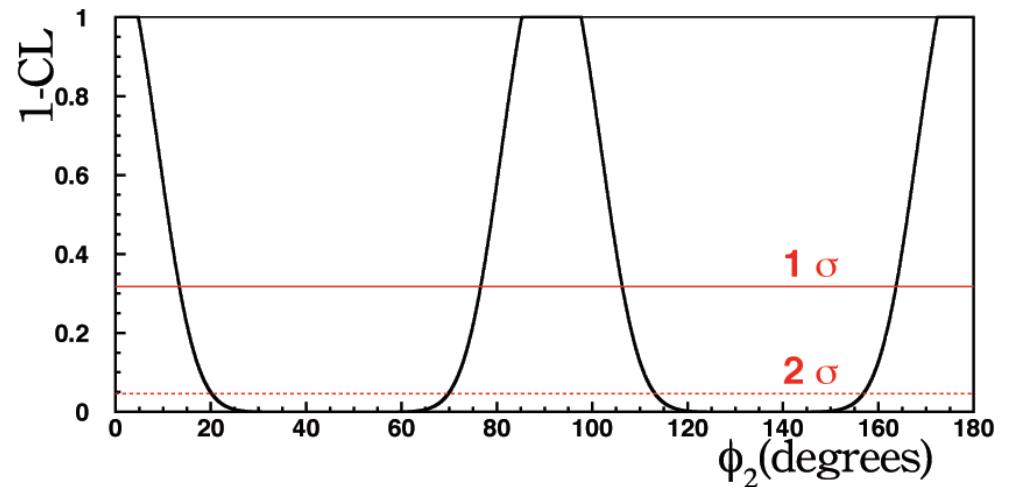


Blue: Before  $\mathcal{B}(B^+ \rightarrow \rho^+\rho^0)$  increase  
 $\phi_2 = (92.4^{+6.0}_{-6.5})^\circ$

$B \rightarrow \rho\rho$  the best environment for constraining  $\phi_2$  because of relatively small penguins

Belle

Use Belle results for  $\mathcal{B}(\rho^0\rho^0)$ , otherwise WA  
Before BaBar's  $B^+ \rightarrow \rho^+\rho^0$  update



Plateau due to no constraint on  $\mathcal{A}_{CP}(\rho^0\rho^0)$   
 $\phi_2 = (91.7 \pm 14.9)^\circ$

$$B^0 \rightarrow a_1(1260)^\pm \pi^\mp$$

Not a  $CP$  eigenstate, need to consider the 4 flavour-charge configurations

$$\mathcal{P}_{a_1\pi}(\Delta t, q, c) = (1 + c\mathcal{A}_{CP}) \frac{e^{-|\Delta t|/\tau_{B^0}}}{8\tau_{B^0}} \left\{ 1 + q \times \left[ (\mathcal{S}_{CP} + c\Delta\mathcal{S}) \sin \Delta m_d \Delta t - (\mathcal{C}_{CP} + c\Delta\mathcal{C}) \cos \Delta m_d \Delta t \right] \right\}$$

$q = \pm 1$ : flavour tag,  $c = \pm 1$ :  $a_1$  charge

Only  $\mathcal{A}_{CP}$ ,  $\mathcal{C}_{CP}$  and  $\mathcal{S}_{CP}$  sensitive to  $CP$  violation

BaBar: 384 million  $B^0\bar{B}^0$  pairs

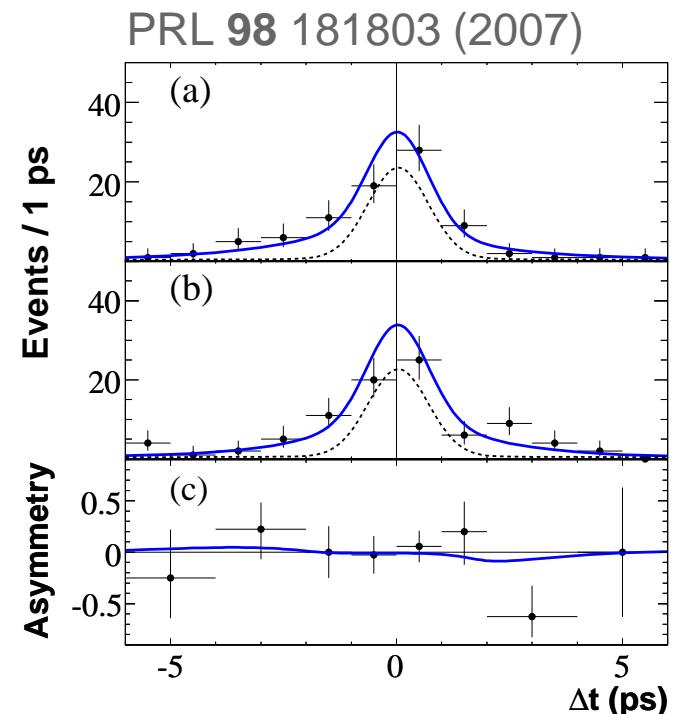
$$\mathcal{A}_{CP} = -0.07 \pm 0.07 \text{ (stat)} \pm 0.02 \text{ (syst)}$$

$$\mathcal{C}_{CP} = -0.10 \pm 0.15 \text{ (stat)} \pm 0.09 \text{ (syst)}$$

$$\mathcal{S}_{CP} = +0.37 \pm 0.21 \text{ (stat)} \pm 0.07 \text{ (syst)}$$

$$\Delta\mathcal{C} = +0.26 \pm 0.15 \text{ (stat)} \pm 0.07 \text{ (syst)}$$

$$\Delta\mathcal{S} = -0.14 \pm 0.21 \text{ (stat)} \pm 0.06 \text{ (syst)}$$



# $B \rightarrow K_1 A \pi$

4-fold ambiguity for  $\phi_2^{\text{eff}}$

$$\phi_2^{\text{eff}} = \frac{1}{4} \left[ \arcsin\left(\frac{\mathcal{S}_{CP} + \Delta\mathcal{S}}{\sqrt{1 - (\mathcal{C}_{CP} + \Delta\mathcal{C})^2}}\right) + \arcsin\left(\frac{\mathcal{S}_{CP} - \Delta\mathcal{S}}{\sqrt{1 - (\mathcal{C}_{CP} - \Delta\mathcal{C})^2}}\right) \right]$$

Can measure  $|\Delta\phi_2|$  using  $SU(3)$  symmetry involving  $B^0 \rightarrow a_1 K$ ,  $B \rightarrow K_1 A \pi$  decays

M. Gronau and J. Zupan, PRD 73 057502 (2006)

New result from BaBar, 454 million  $B^0 \bar{B}^0$  pairs

Amplitude analysis of WA3 data taken by ACCMOR collaboration

Needed to determine  $K\pi\pi$  model

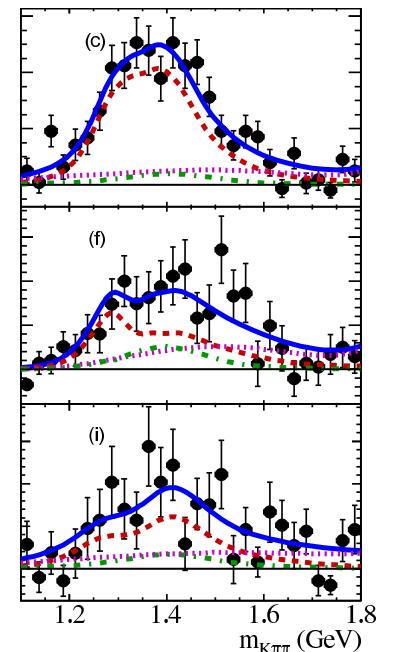
First measurement!

$$\mathcal{B}(B^0 \rightarrow K_1(1270)^+ \pi^- + K_1(1400)^+ \pi^-) = 3.1_{-0.7}^{+0.8} \times 10^{-5} \quad (7.5\sigma)$$

$$\mathcal{B}(B^+ \rightarrow K_1(1270)^0 \pi^+ + K_1(1400)^0 \pi^+) = 2.9_{-1.7}^{+2.9} \times 10^{-5} \quad (3.2\sigma)$$

Relative contributions also determined

PRD 81 052009 (2010)



# $B \rightarrow K_{1A} \pi$

Solve system of inequalities,

$$\cos 2(\phi_{2, \text{eff}}^\pm - \phi_2) \geq \frac{1 - 2R_\pm^0}{\sqrt{1 - \mathcal{A}_{CP}^{\pm 2}}}$$

$$\cos 2(\phi_{2, \text{eff}}^\pm - \phi_2) \geq \frac{1 - 2R_\pm^+}{\sqrt{1 - \mathcal{A}_{CP}^{\pm 2}}}$$

$$R_+^0 \equiv \frac{\bar{\lambda}^2 f_{a_1}^2 \bar{\Gamma}(K_{1A}^+ \pi^-)}{f_{K_{1A}}^2 \bar{\Gamma}(a_1^+ \pi^-)}, \quad R_-^0 \equiv \frac{\bar{\lambda}^2 f_\pi^2 \bar{\Gamma}(a_1^- K^+)}{f_K^2 \bar{\Gamma}(a_1^- \pi^+)}$$

$$R_+^+ \equiv \frac{\bar{\lambda}^2 f_{a_1}^2 \bar{\Gamma}(K_{1A}^0 \pi^+)}{f_{K_{1A}}^2 \bar{\Gamma}(a_1^+ \pi^-)}, \quad R_-^+ \equiv \frac{\bar{\lambda}^2 f_\pi^2 \bar{\Gamma}(a_1^+ K^0)}{f_K^2 \bar{\Gamma}(a_1^- \pi^+)}$$

$$\lambda^2 = |V_{us}|/|V_{ud}| = |V_{cd}|/|V_{cs}|$$

$\bar{\Gamma}$ : averaged decay rates,  $f_i$ : decay constants

Calculate bound on  $|\Delta\phi_2| \equiv |\phi_2^{\text{eff}} - \phi_2|$  from

$$|\phi_2^{\text{eff}} - \phi_2| \leq (|\phi_{2, \text{eff}}^+ - \phi_2| + |\phi_{2, \text{eff}}^- - \phi_2|)/2$$

$|\Delta\phi_2| < 11^\circ(13^\circ)$  at 68% (90%) CL

Solution nearest SM expectation,  $\phi_2^{\text{eff}} = (79 \pm 7 \pm 11)^\circ$

# Summary

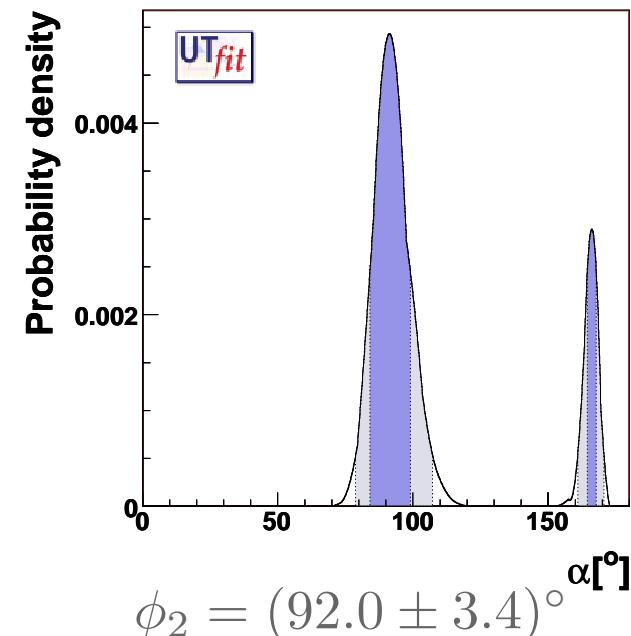
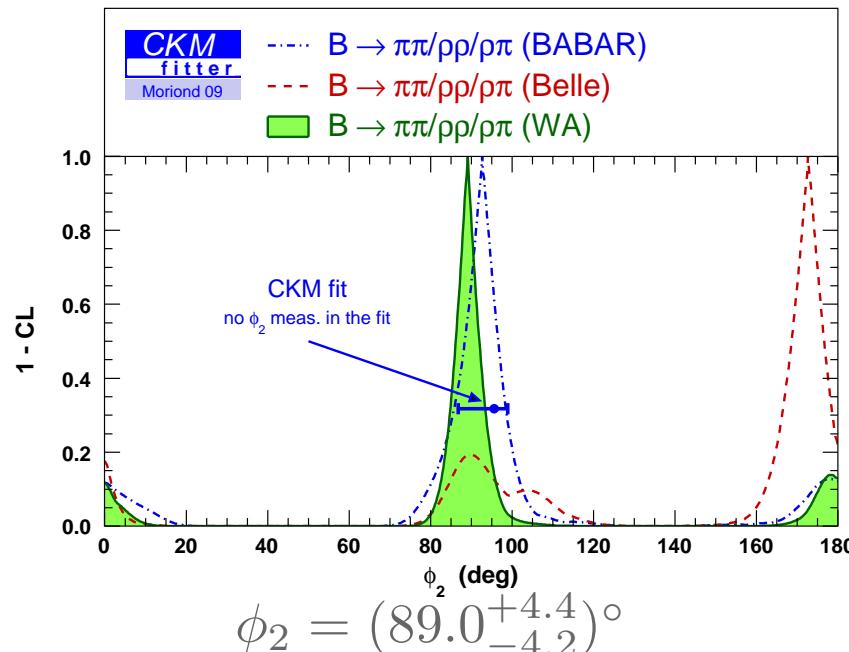
Many measurements of  $\phi_2$  performed by the  $B$  factories

Recent results from BaBar on  $B^+ \rightarrow \rho^+ \rho^0$  and  $B \rightarrow K_{1A} \pi$

$B \rightarrow \rho\rho$  gives tightest constraint on  $\phi_2$

Both experiments have final data sets taken at  $\Upsilon(4S)$  resonance

Many final results still anticipated



# Backup

$$B^0 \rightarrow (\rho\pi)^0$$

Time and amplitude differential decay rate,

$$\frac{d^3\Gamma}{d\Delta t ds_+ ds_-} \propto e^{-|\Delta t|/\tau_{B^0}} \left\{ (|A_{3\pi}|^2 + |\bar{A}_{3\pi}|^2) - q(|A_{3\pi}|^2 - |\bar{A}_{3\pi}|^2) \cos \Delta m_d \Delta t + 2q \Im \left[ \frac{q}{p} A_{3\pi}^* \bar{A}_{3\pi} \right] \sin \Delta m_d \Delta t \right\}$$

$$|A_{3\pi}|^2 \pm |\bar{A}_{3\pi}|^2 = \sum_{\kappa \in \{+, -, 0\}} |f_\kappa|^2 U_\kappa^\pm + \sum_{\kappa < \sigma \in \{+, -, 0\}} 2(\Re[f_\kappa f_\sigma^*] U_{\kappa\sigma}^{\pm, \Re} - \Im[f_\kappa f_\sigma^*] U_{\kappa\sigma}^{\pm, \Im})$$

$$\Im \left[ \frac{q}{p} A_{3\pi}^* \bar{A}_{3\pi} \right] = \sum_{\kappa \in \{+, -, 0\}} |f_\kappa|^2 I_\kappa + \sum_{\kappa < \sigma \in \{+, -, 0\}} (\Re[f_\kappa f_\sigma^*] I_{\kappa\sigma}^{\Im} + \Im[f_\kappa f_\sigma^*] I_{\kappa\sigma}^{\Re})$$

27 coefficients  $U, I$  determined from a fit to data

$f$ : Form factors and line shapes

$$B^0 \rightarrow (\rho\pi)^0$$

Convert to Quasi-two-body parameters

For  $B^0 \rightarrow \rho^\pm \pi^\mp$

$$U_\kappa^\pm = |A_\kappa|^2 \pm |\bar{A}_\kappa|^2$$

$$U_{\kappa\sigma}^{\pm,\Re} = \Re[A_\kappa A_\sigma^* \pm \bar{A}_\kappa \bar{A}_\sigma^*]$$

$$U_{\kappa\sigma}^{\pm,\Im} = \Im[A_\kappa A_\sigma^* \pm \bar{A}_\kappa \bar{A}_\sigma^*]$$

$$I_\kappa = \Im[\bar{A}_\kappa A_\kappa^*]$$

$$I_{\kappa\sigma}^{\Re} = \Re[\bar{A}_\kappa A_\sigma^* - \bar{A}_\sigma A_\kappa^*]$$

$$I_{\kappa\sigma}^{\Im} = \Im[\bar{A}_\kappa A_\sigma^* + \bar{A}_\sigma A_\kappa^*]$$

$$e^{+2i\phi_2} = \frac{\bar{A}_+ + \bar{A}_- + 2\bar{A}_0}{A_+ + A_- + 2A_0}$$

$$\mathcal{A}_{CP} = \frac{U_+^+ - U_-^+}{U_+^+ + U_-^+}$$

$$\mathcal{C}_{CP} = \frac{1}{2} \left( \frac{U_+^-}{U_+^+} + \frac{U_-^-}{U_-^+} \right), \quad \mathcal{S}_{CP} = \frac{I_+}{U_+^+} + \frac{I_-}{U_-^+}$$

$$\Delta\mathcal{C} = \frac{1}{2} \left( \frac{U_+^-}{U_+^+} - \frac{U_-^-}{U_-^+} \right), \quad \Delta\mathcal{S} = \frac{I_+}{U_+^+} - \frac{I_-}{U_-^+}$$

For  $B^0 \rightarrow \rho^0 \pi^0$

$$\mathcal{A}_{CP} = -\frac{U_0^-}{U_0^+}, \quad \mathcal{S}_{CP} = \frac{2I_0}{U_0^+}$$