



JOHANNES GUTENBERG  
UNIVERSITÄT MAINZ



THE LOW-ENERGY FRONTIER  
OF THE STANDARD MODEL



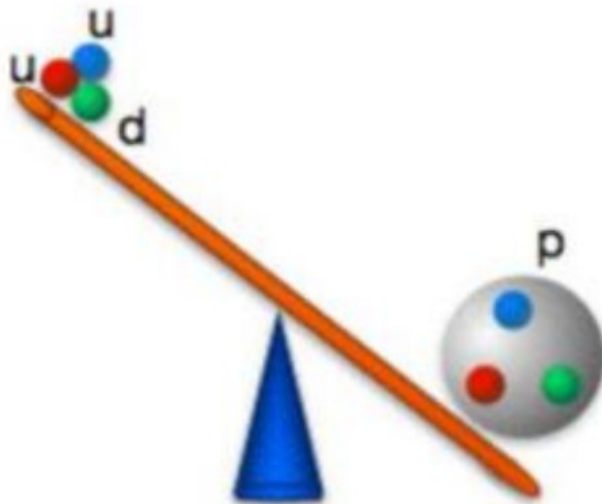
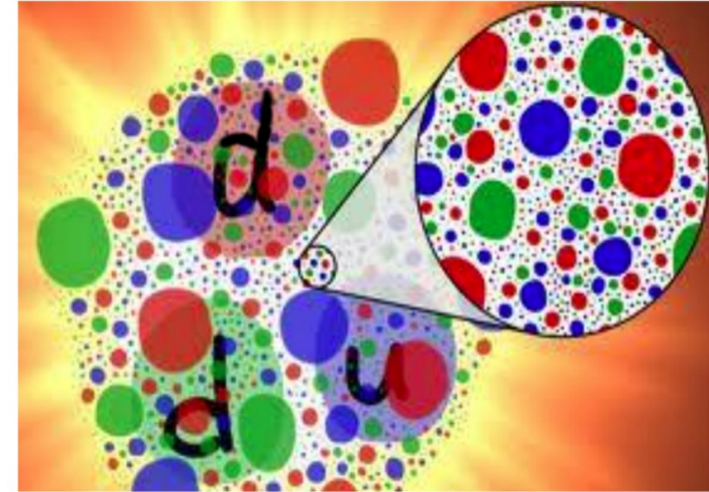
# Measurement of hadron form factors at **BESIII**

June 26, 2018 |

Christoph Florian Redmer  
for the BESIII Collaboration

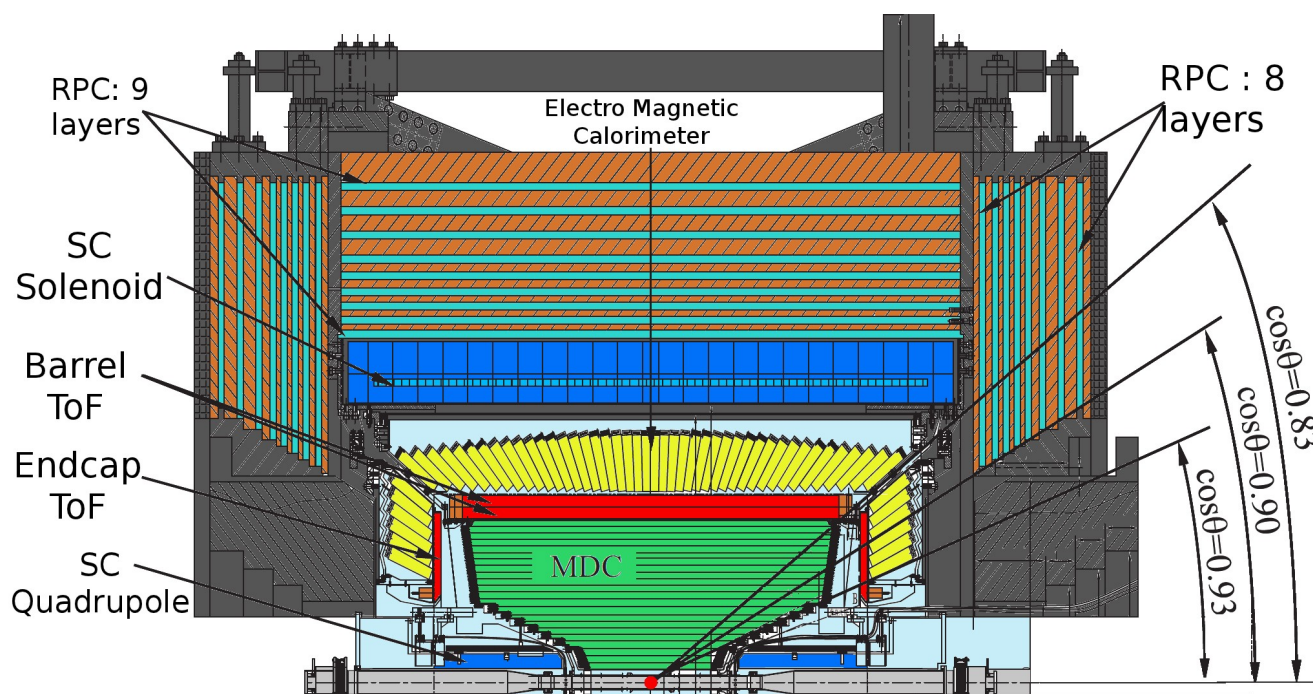
QCD@Work - International Workshop on QCD Theory and Experiment  
Matera, 2018

- Hadrons not point-like
  - Internal structure
- Sum of valence quark masses not hadron mass
  - Internal dynamics



Form factors as parametrization of structure and internal dynamics of hadrons

NIM A614 (2010) 345



### Muon Chambers

- 8 – 9 layers of RPC
- $p > 400 \text{ MeV}/c$
- $\delta R\Phi = 1.4 \sim 1.7 \text{ cm}$

### Superconducting Magnet

- 1 T magnetic field

### EM Calorimeter (EMC)

- 6240 CsI(Tl) crystals
- $\sigma(E)/E = 2.5\%$
- $\sigma_{z,\phi}(E) = 0.5 - 0.7 \text{ cm}$

### Time-of-flight system (TOF)

- $\sigma(t) = 90\text{ps}$  (barrel)
- $\sigma(t) = 110\text{ps}$  (endcap)

### Drift Chamber (MDC)

- $\sigma(p)/p = 0.5\%$
- $\sigma_{dE/dx} = 6.0\%$



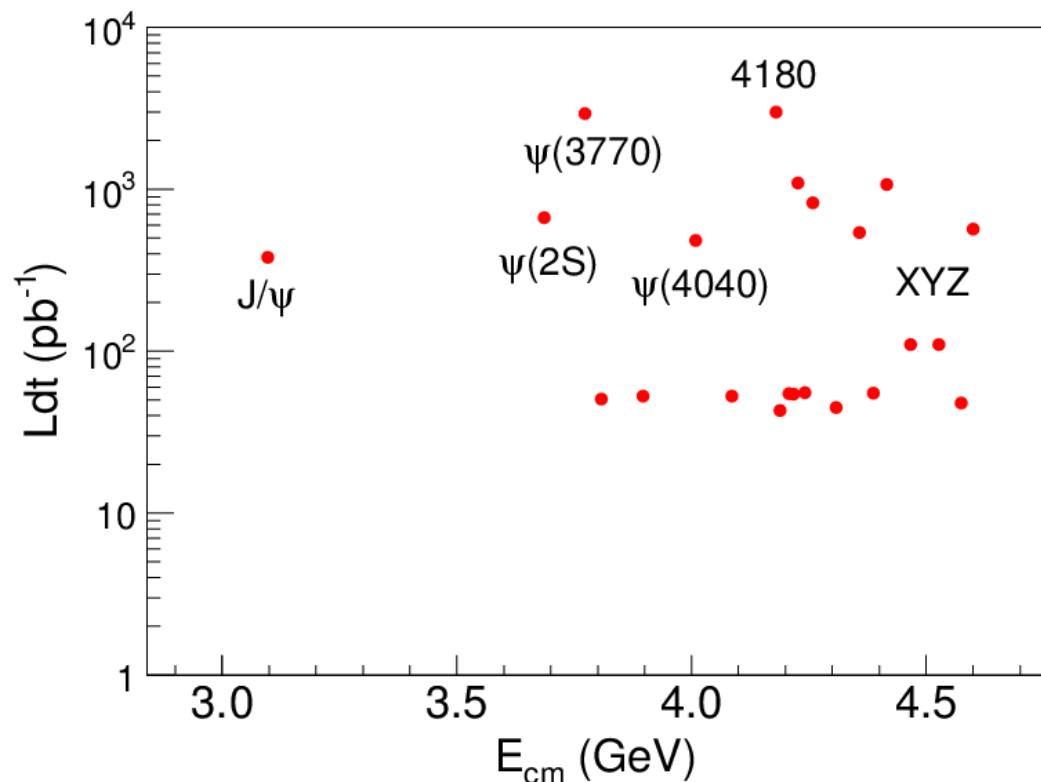
Operated at BEPCII collider in Beijing

- $2.0 \leq \sqrt{s}$  [GeV]  $\leq 4.6$
- Design luminosity achieved

$$\mathcal{L} = 1.0 \times 10^{33} \text{cm}^{-2} \text{s}^{-1} \text{ at } \psi(3770)$$

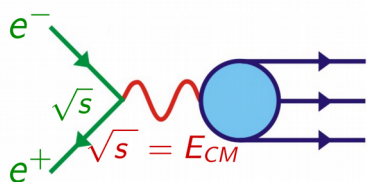
Large data sets for

- Charmonium spectroscopy
- Charm physics
- Light hadrons
- $\tau$ -mass and R-scan

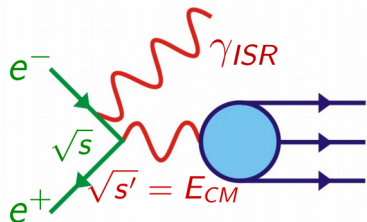


- Exclusive Cross Sections

- Direct scan

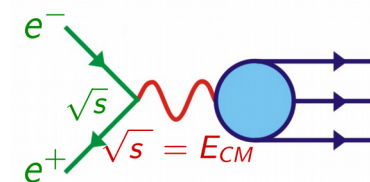


- Initial State Radiation



- Inclusive Cross Sections

- Direct scan

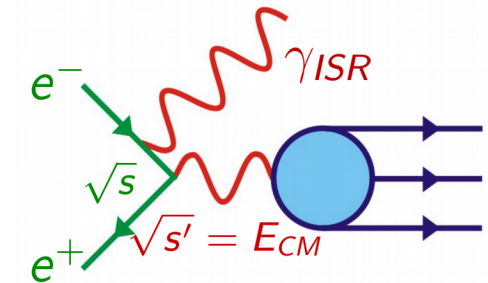


- Reduces effective CMS energy

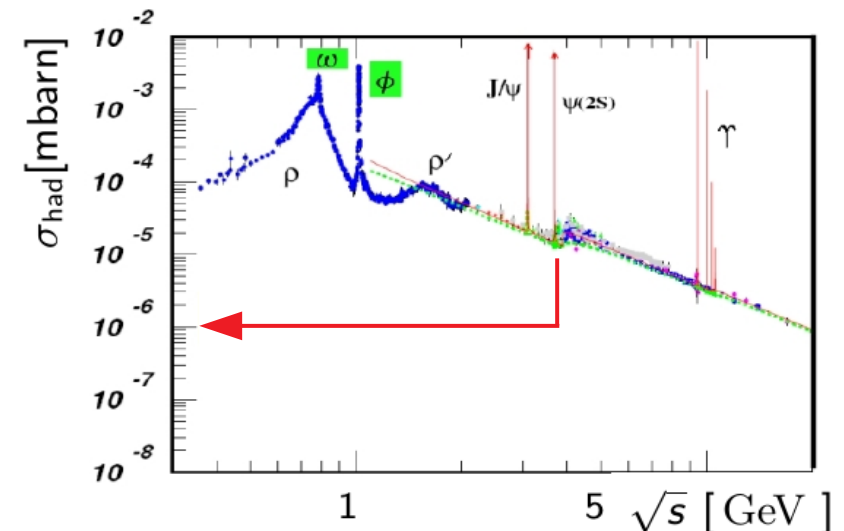
$$\sqrt{s'} = \sqrt{s - 2\sqrt{s}E_\gamma}$$

- Radiator function relates to non-radiative process

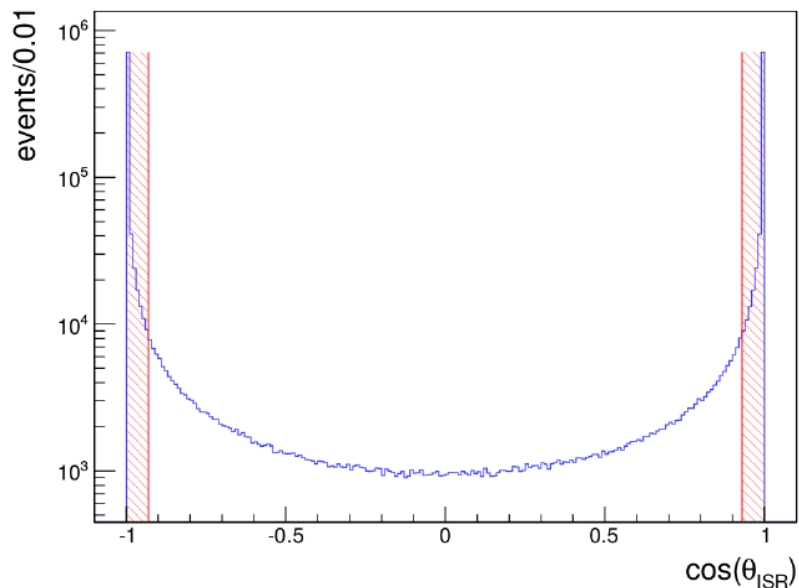
$$\frac{d\sigma_{\text{had}+\gamma}}{dm_\gamma} = \frac{2m_{\text{had}}}{s} W(s, E_\gamma, \theta_\gamma)_{\text{had}}$$



- Emission of ISR suppressed by  $\frac{\alpha}{\pi}$
- Large integrated luminosity needed for precision studies
  - $> 10 \text{ fb}^{-1}$  at BESIII with  $3.77 \leq \sqrt{s}[\text{GeV}] \leq 4.6$

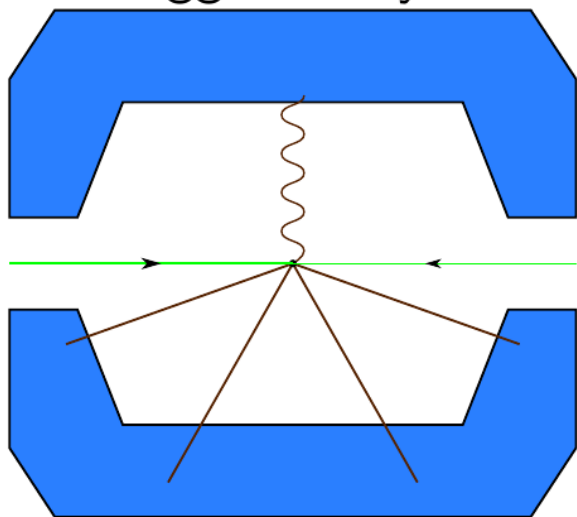


polar angle distribution of ISR photons (MC)

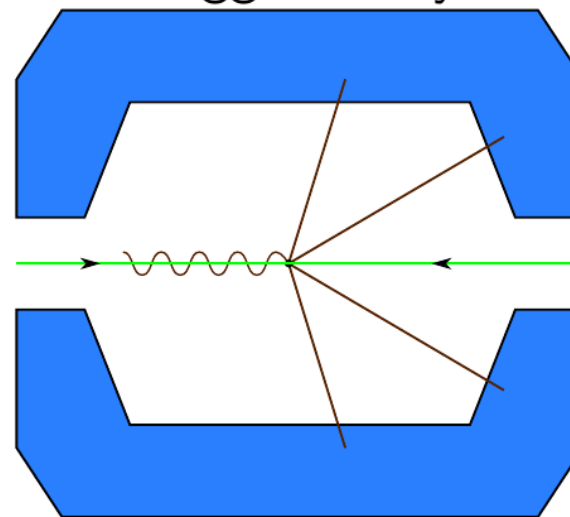


- Detect hadronic system
- ISR photon detected
  - Acceptance from  $\pi^+\pi^-$  threshold
  - Large background contamination at high  $\sqrt{s'}$
- ISR photon undetected
  - High statistics
  - Acceptance for  $\sqrt{s'} > 1$  GeV
  - Small background contamination

Tagged analysis



Untagged analysis



# JG|U Anomalous Magnetic Moment of $\mu$

Muon anomaly:  $a_\mu = \frac{g_\mu - 2}{2}$

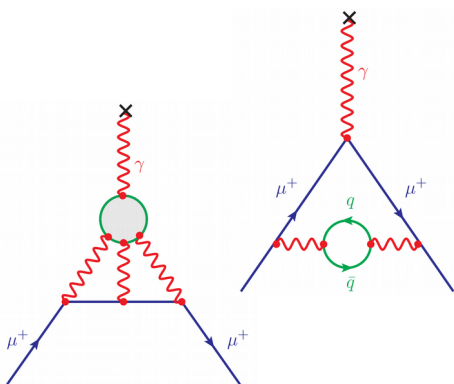
$a_\mu$	in units of $10^{-10}$	
Standard Model	$11659182.3 \pm 4.3$	Davier et al. EPJC 77 (2017) 827
Direct Measurement	$11659209.1 \pm 6.3$	BNL-E821, PRD 73 (2006) 072003
Difference	$26.8 \pm 7.6$	

More than three standard deviations !  
**Indication of New Physics?**

Theory uncertainty completely dominated by hadronic contributions!

New experiments at Fermilab and J-PARC aim at fourfold improvement of accuracy

Hadronic Vacuum Polarization



HVP (LO):  $(693.1 \pm 3.4) 10^{-10}$  EPJC 77 (2017) 827

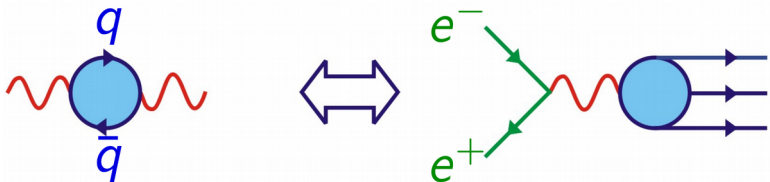
HLBL :  $(10.5 \pm 2.6) 10^{-10}$  Adv. Ser. Direct. High Energy Phys. 20, 303 (2009)

**Use input from experiments!**



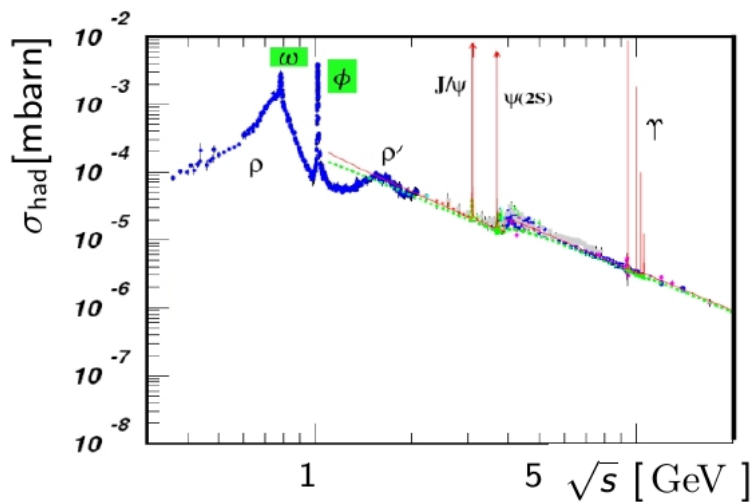
# Hadronic Vacuum Polarization

Related to hadronic cross sections by optical theorem

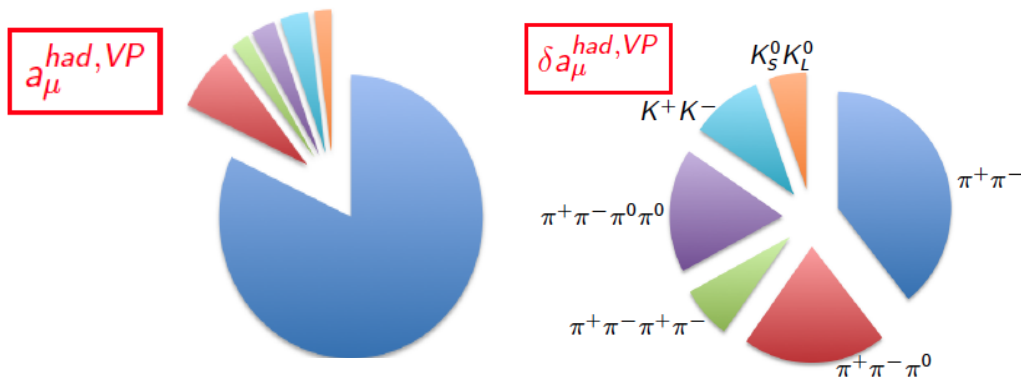


Dispersion integral :

$$a_{\mu}^{hVP,LO} = \frac{1}{4\pi^3} \int_{4m_{\pi}^2}^{\infty} K(s) \sigma(e^+e^- \rightarrow \text{hadr}) ds$$

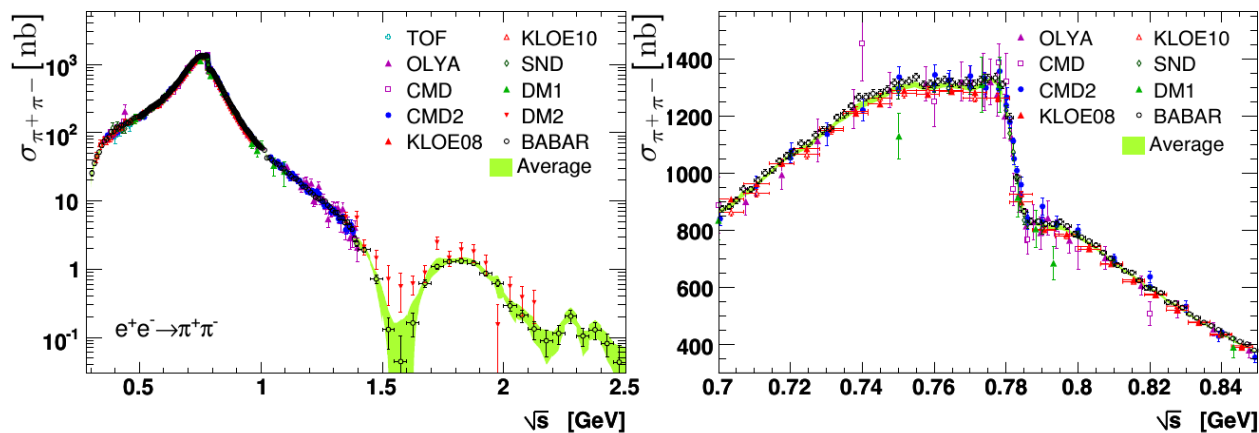


$$\left. \begin{aligned} K(s) &\sim \frac{1}{s} \\ \sigma(e^+e^- \rightarrow \text{hadr}) &\sim \frac{1}{s} \end{aligned} \right\} \text{Low energy contributions dominate !}$$





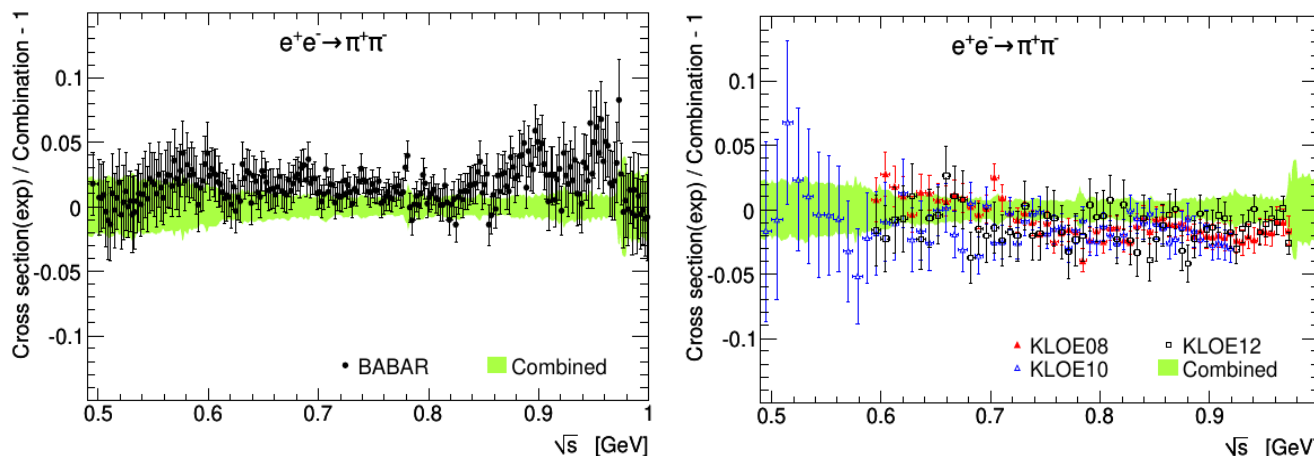
Accounts for 75% of  $a_\mu^{hVP}$   $\longrightarrow$  Good knowledge important !



Systematic uncertainties:

0.5%	BaBar	} Limited by statistics
0.8%	KLOE	
0.8%	CMD	
1.5%	SND	

KLOE and BaBar measurements dominate world average



systematic differences  $\longrightarrow$

large uncertainty for  $a_\mu^{hVP}$

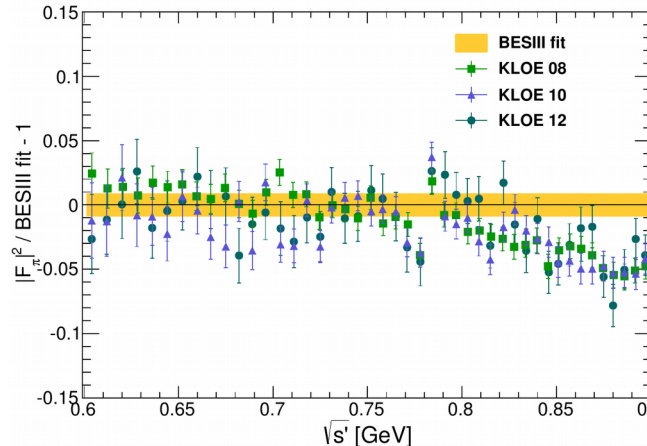
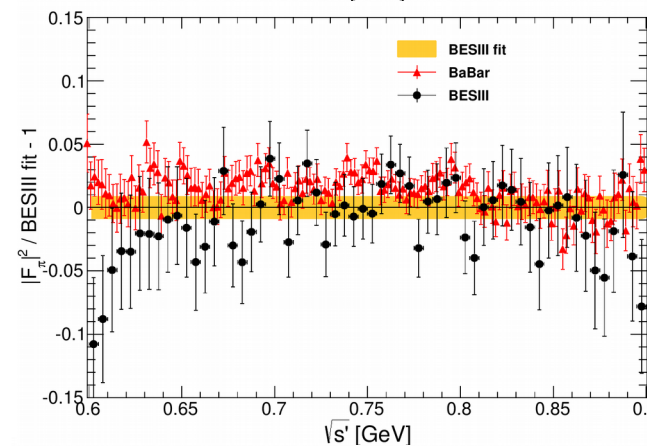
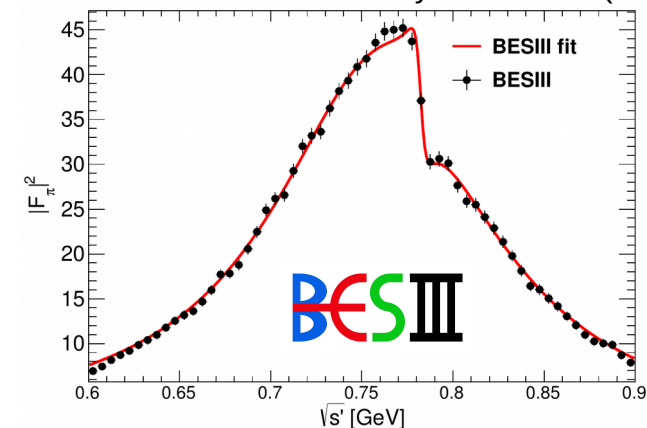
$$e^+e^- \rightarrow \pi^+\pi^-$$

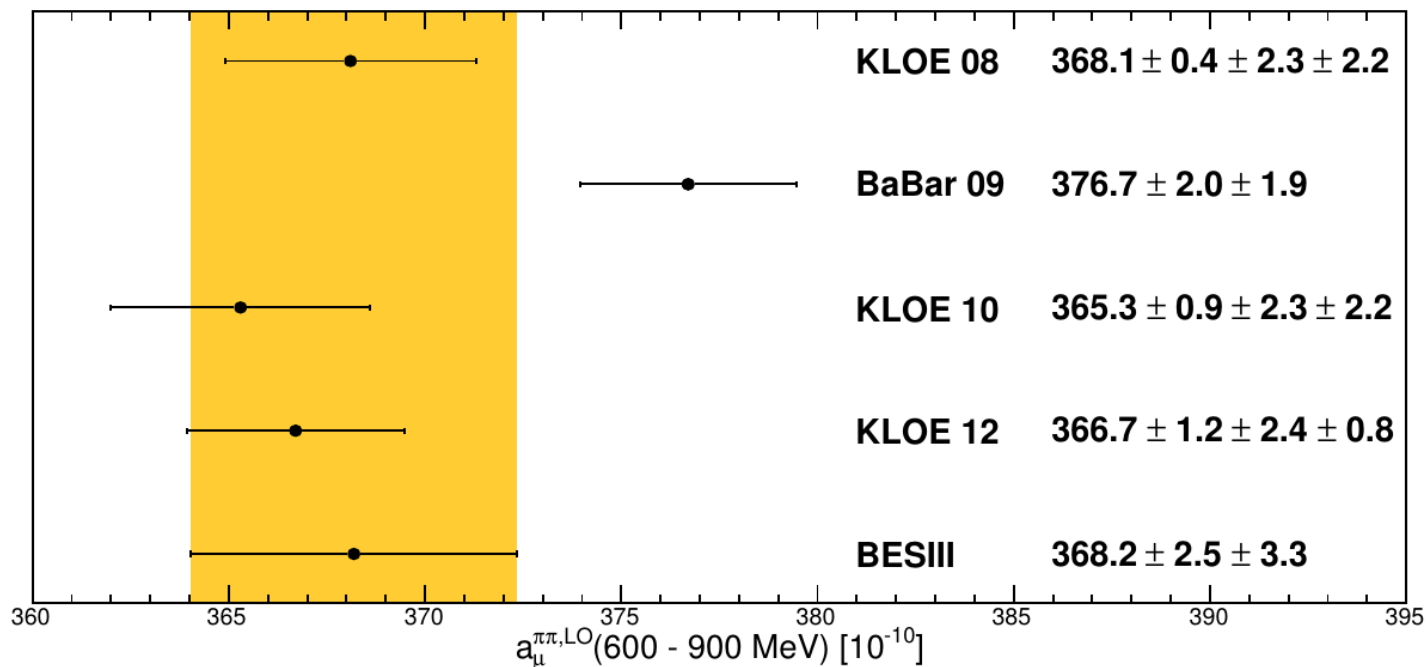
- Tagged ISR technique
- $\mu - \pi$  separation with Artificial Neural Network
- careful evaluation of systematics
  - Total uncertainty of 0.9% achieved
  - Dominated by
    - Luminosity (0.5%)
    - Radiator function (0.5%)
- evaluation for  $0.6 \leq m_{\pi\pi} \leq 0.9$ 
  - 70% of total  $2\pi$  contribution
  - 50% of  $a_\mu^{hVP}$  contribution

Comparison to previous measurements:

Systematic shift in pion form factor

- below  $\rho/\omega$  interference w.r.t. BaBar
- above  $\rho/\omega$  interference w.r.t. KLOE



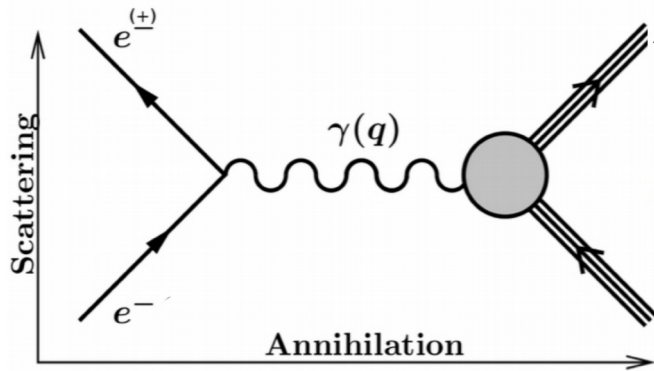


Ablikim et al., Phys.Lett.B753 (2016) 629

- Precision competitive to measurements by BaBar and KLOE
- Good agreement with all KLOE results
- BESIII result confirms  $a_\mu^{\text{theo, SM}} - a_\mu^{\text{exp}} > 3\sigma$
- Reevaluations of  $a_\mu^{\text{hVP}}$  including BESIII result improve accuracy by 20%

EPJ C77 (2017), 820

## BESIII: Time-like EM form factors (EMFF)



- Hadronic vector currents  $\rightarrow (2s+1)$  EMFF
- 2 EMFF for baryons
  - Pauli and Dirac FF

$$\Gamma^\mu = \gamma^\mu F_1(q^2) \frac{i\sigma^{\mu\nu} q_\nu}{2M_B} F_2(q^2)$$

- Sachs parametrization:  $G_E(q^2) = F_1(q^2) + \frac{q^2}{4M_B} F_2(q^2)$        $G_M(q^2) = F_1(q^2) + F_2(q^2)$

- Differential cross section:  $\frac{d\sigma_{BB}^{\text{Born}}}{d\Omega} = \frac{\alpha^2 \beta^2 C}{4q^2} \left[ (1 + \cos^2 \theta_B^{\text{CM}}) |G_M(q^2)|^2 + \frac{1}{\tau} |G_E(q^2)|^2 \sin^2 \theta_B^{\text{CM}} \right]$

- Total cross section:  $\sigma_{BB}^{\text{Born}} = \frac{4\pi\alpha^2\beta^2C}{3q^2} \left[ |G_M(q^2)|^2 + \frac{1}{2\tau} |G_E(q^2)|^2 \right]$

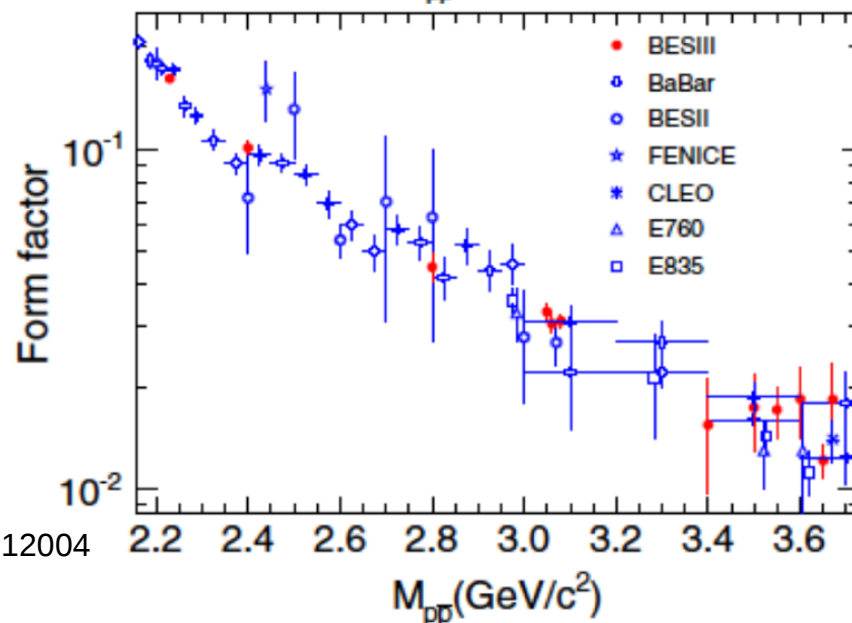
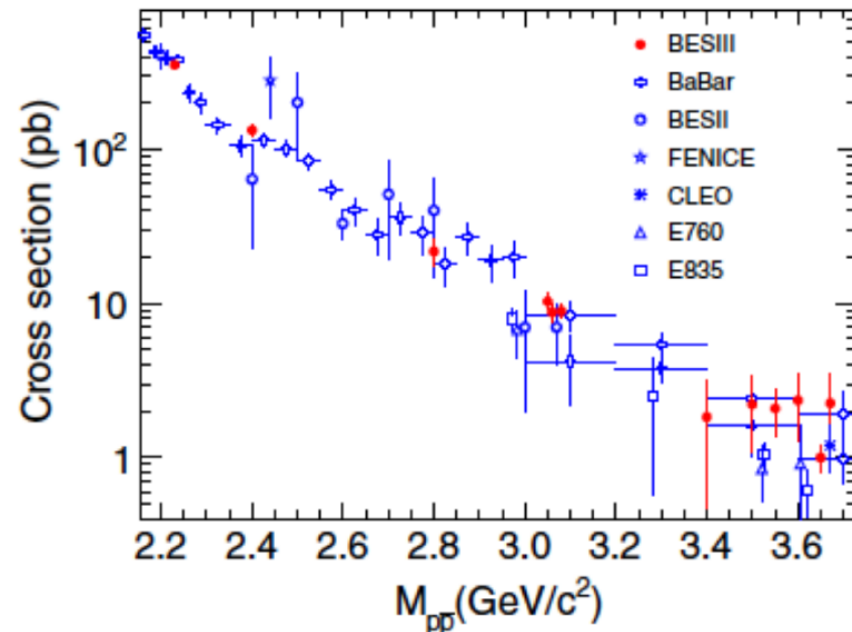
- Effective EMFF:  $|G_{\text{eff}}(q^2)| = \sqrt{\frac{\sigma_{BB}^{\text{Born}}}{\left(1 + \frac{1}{2\tau}\right) \frac{4\pi\alpha^2\beta^2C}{3q^2}}}$ , assuming  $|G_M(q^2)| = |G_E(q^2)|$

- 'pilot scan' analyzed
  - 157 pb<sup>-1</sup> at 12 scan points 2232.4 ≤ √s[MeV] ≤ 3671.0
- Two tracks, PID by dE/dx and TOF
- Kinematic constraints to reduce background

$$\sigma^{\text{Born}} = \frac{N_{\text{obs}} - N_{\text{bkg}}}{\mathcal{L}\epsilon(1 + \delta)}$$

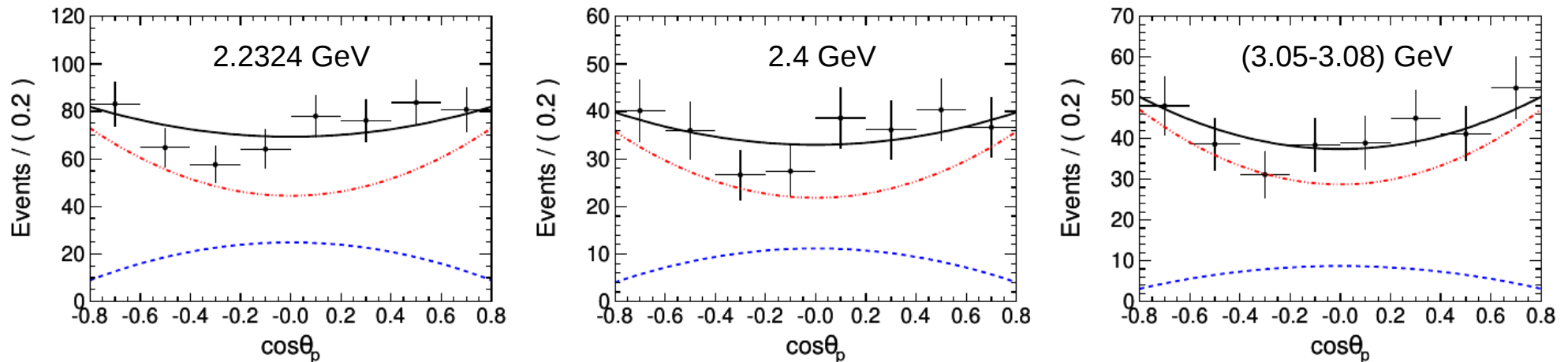
luminosity →  $\mathcal{L}$       efficiency →  $\epsilon$       rad. corrections →  $\delta$

- Cross section and effective EMFF
  - Good agreement with previous measurements
  - Overall improvement of uncertainties by ~ 30%



Phys.Rev. D91 (2015) 112004

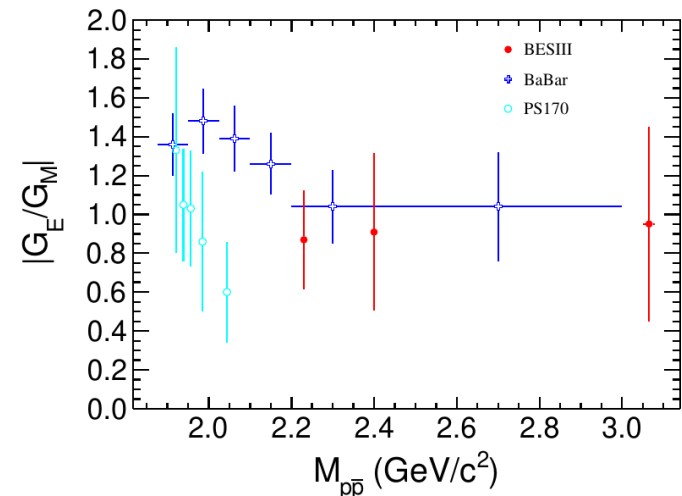
Extraction of EMFF ratio  $R = |G_E|/|G_M|$  at scan points with largest statistics



Phys.Rev. D91 (2015) 112004

$\sqrt{s}$ (MeV)	$ G_E/G_M $	$ G_M  (\times 10^{-2})$
<i>Fit on <math>\cos\theta_p</math></i>		
2232.4	$0.87 \pm 0.24 \pm 0.05$	$18.42 \pm 5.09 \pm 0.98$
2400.0	$0.91 \pm 0.38 \pm 0.12$	$11.30 \pm 4.73 \pm 1.53$
(3050.0, 3080.0)	$0.95 \pm 0.45 \pm 0.21$	$3.61 \pm 1.71 \pm 0.82$
<i>method of moments</i>		
2232.4	$0.83 \pm 0.24$	$18.60 \pm 5.38$
2400.0	$0.85 \pm 0.37$	$11.52 \pm 5.01$
(3050.0, 3080.0)	$0.88 \pm 0.46$	$3.34 \pm 1.72$

- EMFF ratio consistent with 1
- Agreement with BaBar measurement
- BESIII result statistics limited
  - New high statistics scan data under evaluation



- 7.4 fb<sup>-1</sup> at  $3.773 \leq \sqrt{s}[\text{GeV}] \leq 4.6$  analyzed
- Both ISR analysis schemes exploited!

### Tagged [large angle(LA)]

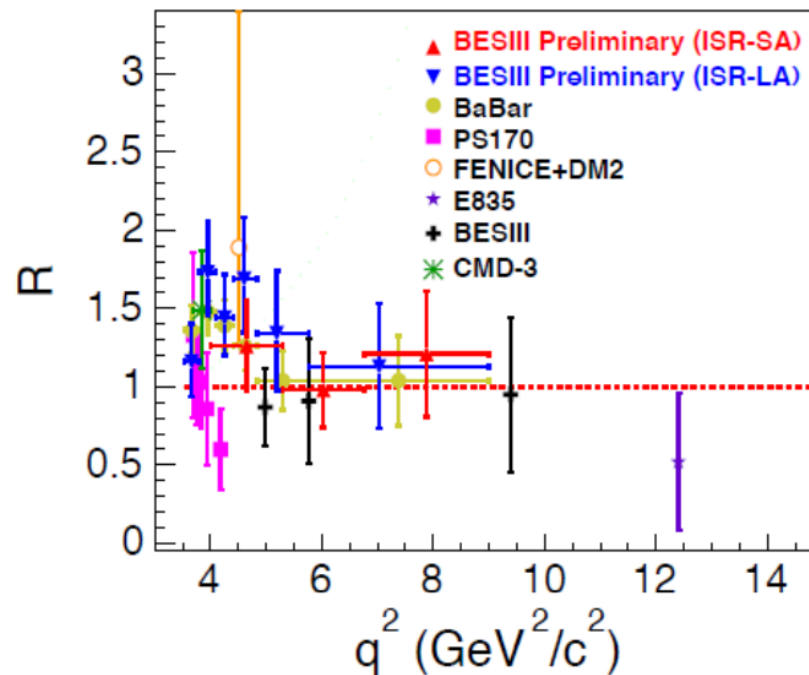
- Two tracks, one cluster
- 4C kinematic fit
- 5C veto fit with additional  $\gamma$

### Determination of EMFF ratio:

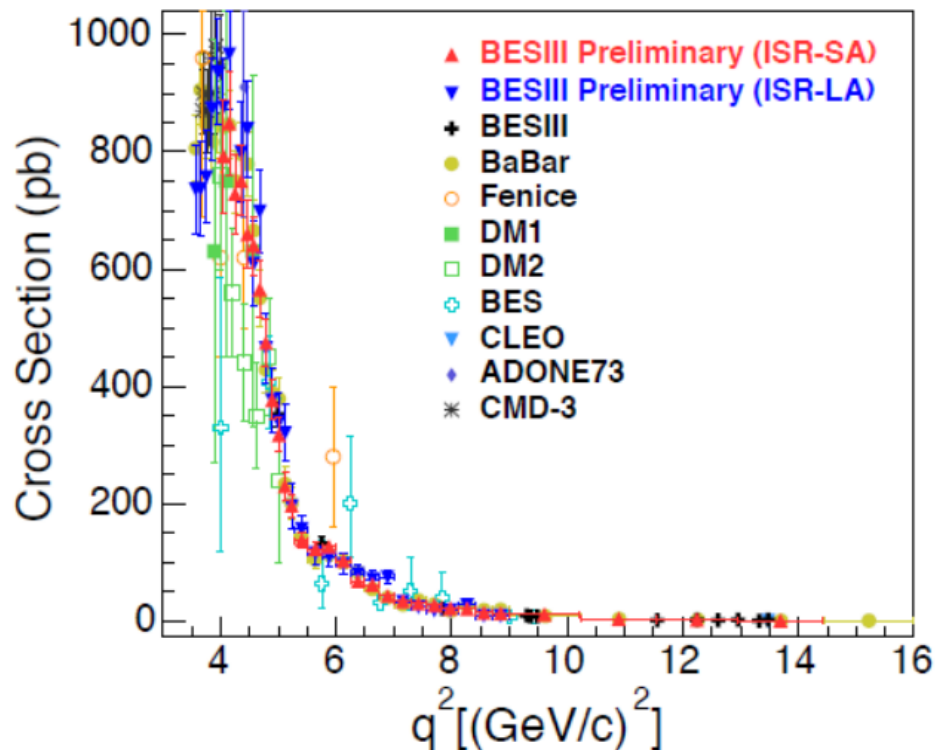
- Tagged: 6 bins in  $1.877 \leq \sqrt{s}[\text{GeV}] \leq 3.0$
- Untagged: 3 bins in  $2.0 \leq \sqrt{s}[\text{GeV}] \leq 3.0$
- Competitive accuracy
- Agreement with BaBar and BESIII scan

### Untagged [small angle (SA)]

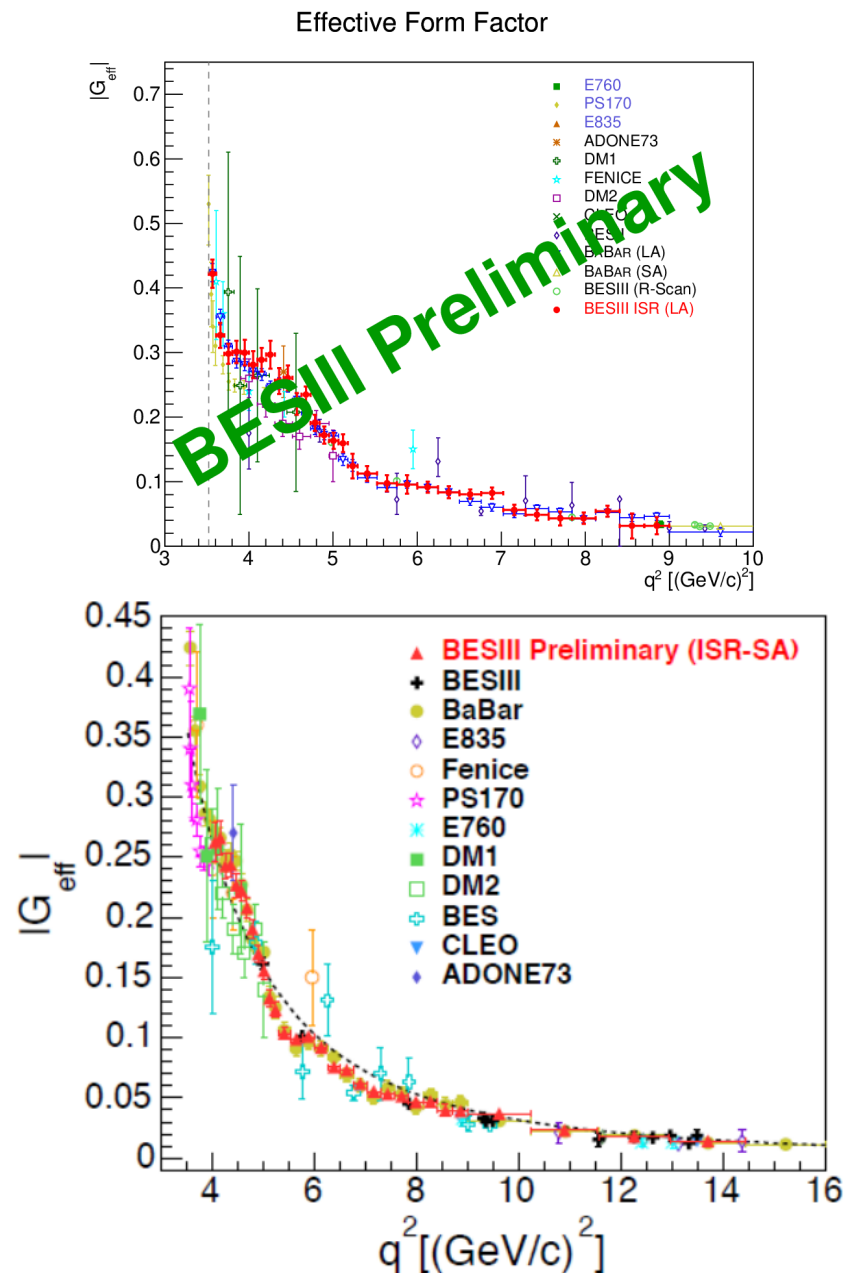
- Two tracks, PID by dE/dx and TOF
- Small polar angle of missing momentum
- Missing mass squared







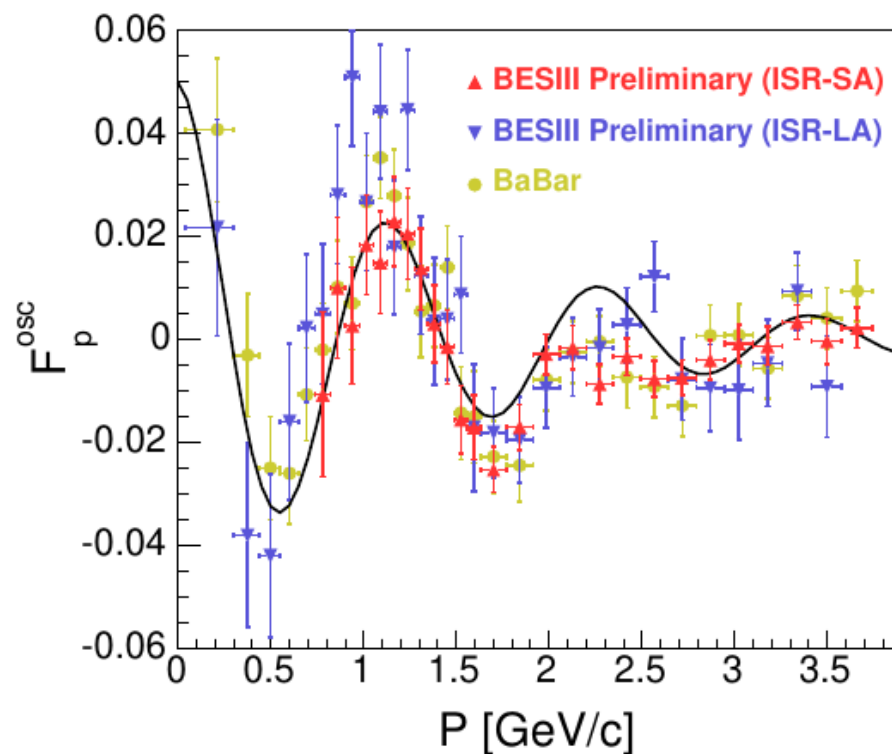
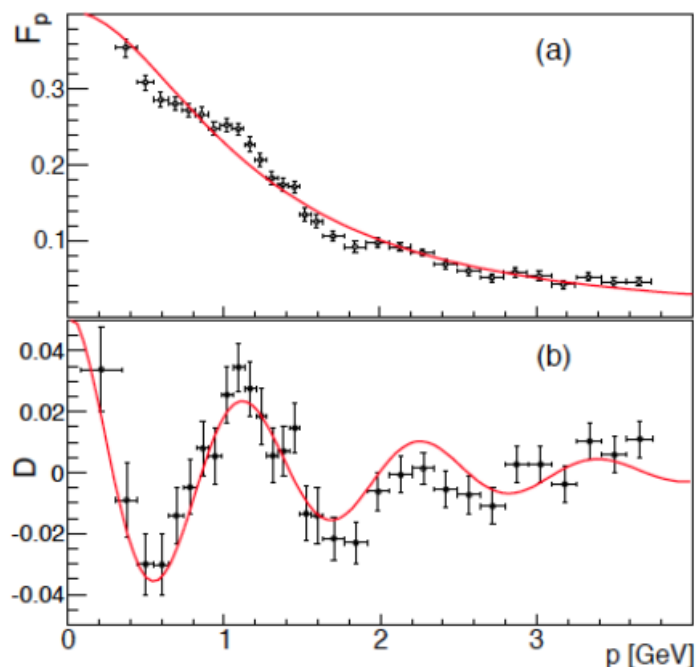
- Measurement of cross section and effective EMFF
  - Tagged: 31 bins in  $1.877 \leq \sqrt{s}[\text{GeV}] \leq 3.0$
  - Untagged: 30 bins in  $2.0 \leq \sqrt{s}[\text{GeV}] \leq 3.8$
- Consistent with previous measurements
- Untagged ISR competitive in statistics with BaBar



Effective EMFF as a function of three-momentum of the relative motion of the protons

- Damped oscillation pattern in  $F^{\text{osc}} = |G_{\text{eff}}| - F^0$ 
  - $F^0$  : regular behavior of  $|G_{\text{eff}}|$  over long range of  $M_{p\bar{p}}$

A. Bianconi, E. Tomasi-Gustafsson  
 Phys.Rev.Lett. 114 (2015) 232301  
 Phys.Rev. C93 (2016) 035201



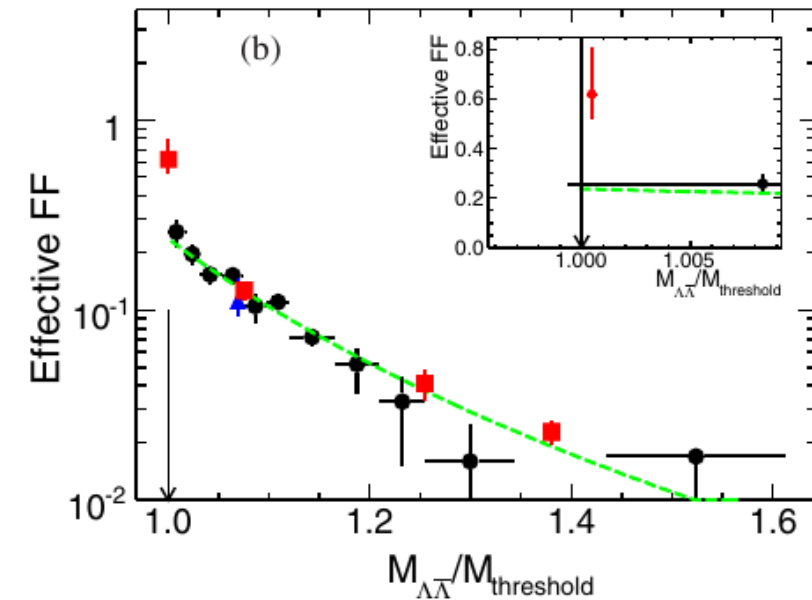
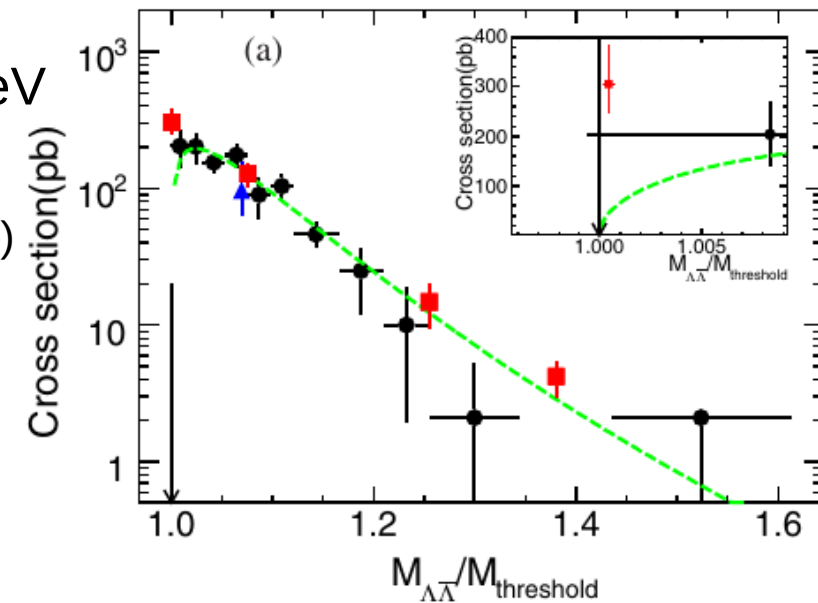
- Observed in BaBar results of  $|G_{\text{eff}}|$
- Confirmed by BESIII result

$$e^+e^- \rightarrow \Lambda\bar{\Lambda}$$

- Four scan points: 2232.4, 2400, 2800, 3080 MeV
- 1 MeV above threshold:  $\Lambda \rightarrow p\pi, \Lambda \rightarrow \bar{n}\pi^0$ 
  - Indirect reconstruction (nucleons stopped in beam pipe)
- Other:  $\Lambda \rightarrow p\pi^-, \bar{\Lambda} \rightarrow \bar{p}\pi^+$
- Cross section and effective EMFF determined
- Unexpected enhancement at threshold!

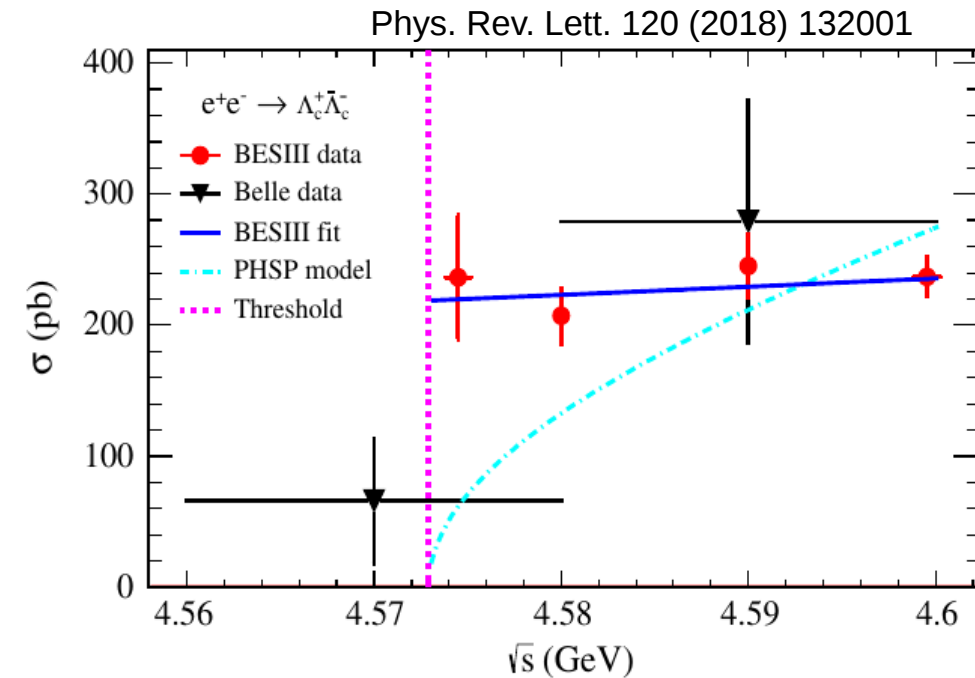
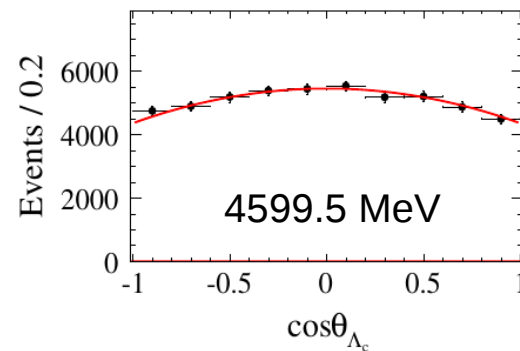
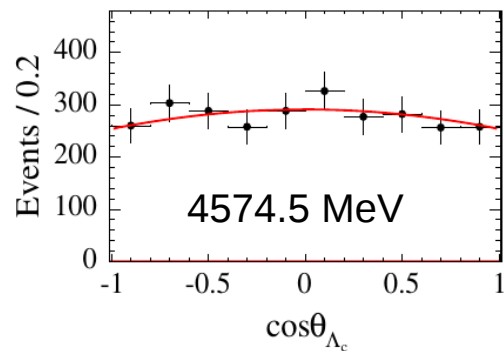
$\sqrt{s}$ (GeV)	$\mathcal{L}_{\text{int}}$ (pb $^{-1}$ )	$N_{\text{obs}}$	$\epsilon(1+\delta)$ (%)	$\sigma^B$ (pb)	$ G $ ( $\times 10^{-2}$ )
2.2324 <sub>1</sub>	2.63	43 $\pm$ 7	12.9	312 $\pm$ 51 $^{+72}_{-45}$	
2.2324 <sub>2</sub>	2.63	22 $\pm$ 6	8.25	288 $\pm$ 96 $^{+64}_{-36}$	
2.2324 <sub>c</sub>				305 $\pm$ 45 $^{+66}_{-36}$	61.9 $\pm$ 4.6 $^{+18.1}_{-9.0}$
2.400	3.42	45 $\pm$ 7	25.3	128 $\pm$ 19 $\pm$ 18	12.7 $\pm$ 0.9 $\pm$ 0.9
2.800	3.75	8 $\pm$ 3	36.1	14.8 $\pm$ 5.2 $\pm$ 1.9	4.10 $\pm$ 0.72 $\pm$ 0.26
3.080	30.73	13 $\pm$ 4	24.5	4.2 $\pm$ 1.2 $\pm$ 0.5	2.29 $\pm$ 0.33 $\pm$ 0.14

Phys. Rev. D97 (2018) 032013



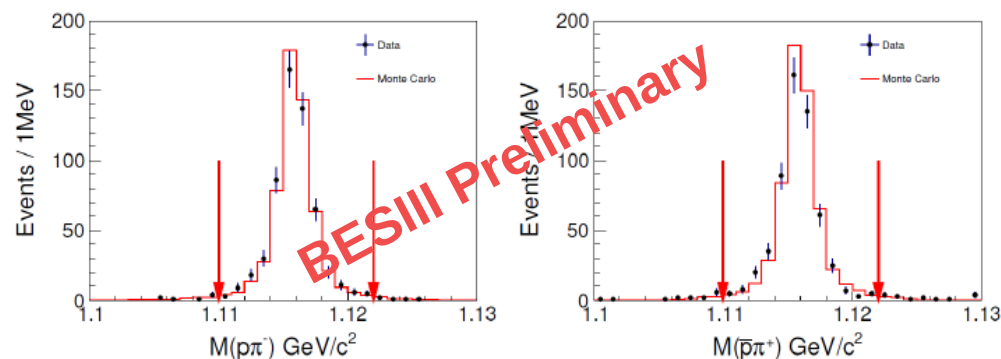
$$e^+e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^-$$

- Four scan points: 4574.5 , 4580.0, 4590.0, 4599.5 MeV
- 10 Cabbibo-favored decay modes (+c.c.)
- Cross section as weighted average
- Plateau at threshold observed
- Tension with Belle result
- EMFF ratio extracted for the first time!



$\sqrt{s}$ (MeV)	$\alpha_{\Lambda_c}$	$ G_E/G_M $
4574.5	$-0.13 \pm 0.12 \pm 0.08$	$1.14 \pm 0.14 \pm 0.07$
4599.5	$-0.20 \pm 0.04 \pm 0.02$	$1.23 \pm 0.05 \pm 0.03$

- Weak decay of  $\Lambda$  self analyzing: Access to phase information!
- High statistics sample at 2.396 GeV
- $e^+e^- \rightarrow \Lambda\bar{\Lambda}$ 
  - Four charged tracks, PID by momentum
  - Mass windows to select  $\Lambda$
- $\sigma^{Born} = 119.0 \pm 5.3_{stat} \pm 7.3_{syst}$
- $|G_{eff}| = 0.123 \pm 0.003_{stat} \pm 0.004_{syst}$ 
  - Compatible with previous measurements by BaBar and BESIII
- Relative phase from fit to decay distributions



$$\begin{aligned} \mathcal{W}(\xi) = & \mathcal{T}_0(\xi) + \eta \mathcal{T}_5(\xi) \\ & - \alpha_\Lambda^2 \left( \mathcal{T}_1(\xi) + \sqrt{1 - \eta^2} \cos(\Delta\Phi) \mathcal{T}_2(\xi) + \eta \mathcal{T}_6(\xi) \right) \\ & + \alpha_\Lambda \sqrt{1 - \eta^2} \sin(\Delta\Phi) (\mathcal{T}_3(\xi) - \mathcal{T}_4(\xi)). \end{aligned}$$

$$\mathcal{T}_0(\xi) = 1$$

$$\mathcal{T}_1(\xi) = \sin^2 \theta \sin \theta_1 \sin \theta_2 \cos \phi_1 \cos \phi_2 + \cos^2 \theta \cos \theta_1 \cos \theta_2$$

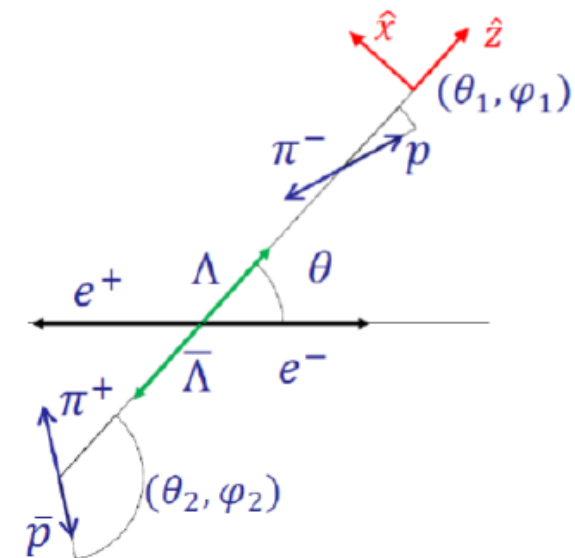
$$\mathcal{T}_2(\xi) = \sin \theta \cos \theta (\sin \theta_1 \cos \theta_2 \cos \phi_1 + \cos \theta_1 \sin \theta_2 \cos \phi_2)$$

$$\mathcal{T}_3(\xi) = \sin \theta \cos \theta \sin \theta_1 \sin \phi_1$$

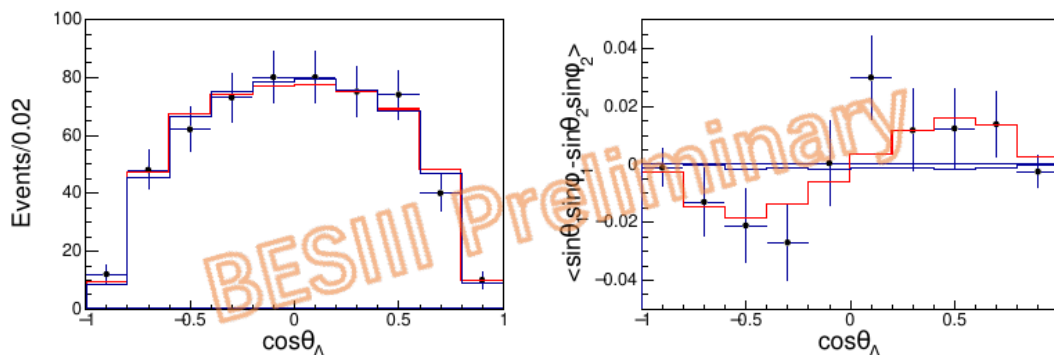
$$\mathcal{T}_4(\xi) = \sin \theta \cos \theta \sin \theta_2 \sin \phi_2$$

$$\mathcal{T}_5(\xi) = \cos^2 \theta$$

$$\mathcal{T}_6(\xi) = \cos \theta_1 \cos \theta_2 - \sin^2 \theta \sin \theta_1 \sin \theta_2 \sin \phi_1 \sin \phi_2$$



Unbinned maximum log likelihood fit with relative phase  $\Delta\Phi$  and  $\eta = \frac{\tau - R^2}{\tau + R^2}$  as free parameters



$$R = 0.94 \pm 0.16_{\text{stat}} \pm 0.03_{\text{syst}} \pm 0.02_{\alpha_\Lambda}$$

$$|\Delta\Phi| = 42^\circ \pm 16^\circ_{\text{stat}} \pm 8^\circ_{\text{syst}} \pm 6^\circ_{\alpha_\Lambda}$$

First measurement!

- Form factors contain valuable information on hadron structure
- BESIII perfect laboratory to study hadron FF's
  - Scan, tagged, and untagged ISR
- Mesons
  - Important input to calculations of  $a_\mu^{hVP}$
  - Precision measurement of  $e^+e^- \rightarrow \pi^+\pi^-$
  - Higher multiplicities ( $\pi^+\pi^-\pi^0, \pi^+\pi^-\pi^0\pi^0, \dots$ ) in internal review
- Baryons
  - First measurements of  $p, \Lambda, \Lambda_c$ 
    - Intriguing enhancements at threshold
    - Oscillating behavior of  $p$  effective FF
  - High statistics scan data available
    - First measurement of relative phase of EMFF in  $\Lambda$
    - Measurements of nucleon ( $p$  and  $n$ !) form factors in internal review
  - Prospects for  $\Lambda_c$ : Potential energy upgrade of the accelerator

Phys. Lett. B753 (2016) 629

Phys. Rev. D91 (2015) 112004

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