

Three-body model study of unbound nucleus ^{26}O

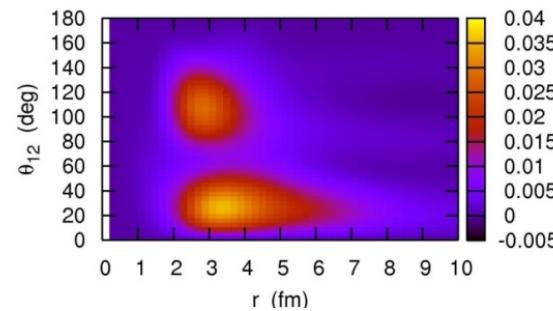
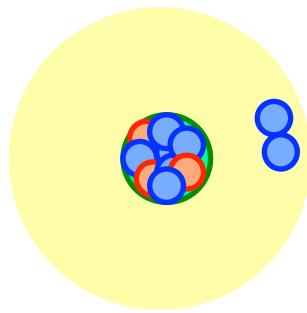
--- NN2015 ---

June 22-26, 2105 Catania, Italy

Hiroyuki Sagawa (RIKEN/U. of Aizu)

and

Koichi Hagino(Tohoku University)



- 1. di-neutron correlation and three-body model approach*
- 2. Nuclei beyond drip line and $2n$ -decay*
- 3. Summary and future perspectives*

Exotic structure close to drip lines

- Halo, Giant halo/skin structure
- shell evolution
- di-neutron and di-proton correlations
- Shape evolution, shape coexistence
- Anti-halo effect

Exotic Nuclei Far from the Stability Line

K. Hagino¹, I. Tanihata^{2,3} and H. Sagawa⁴

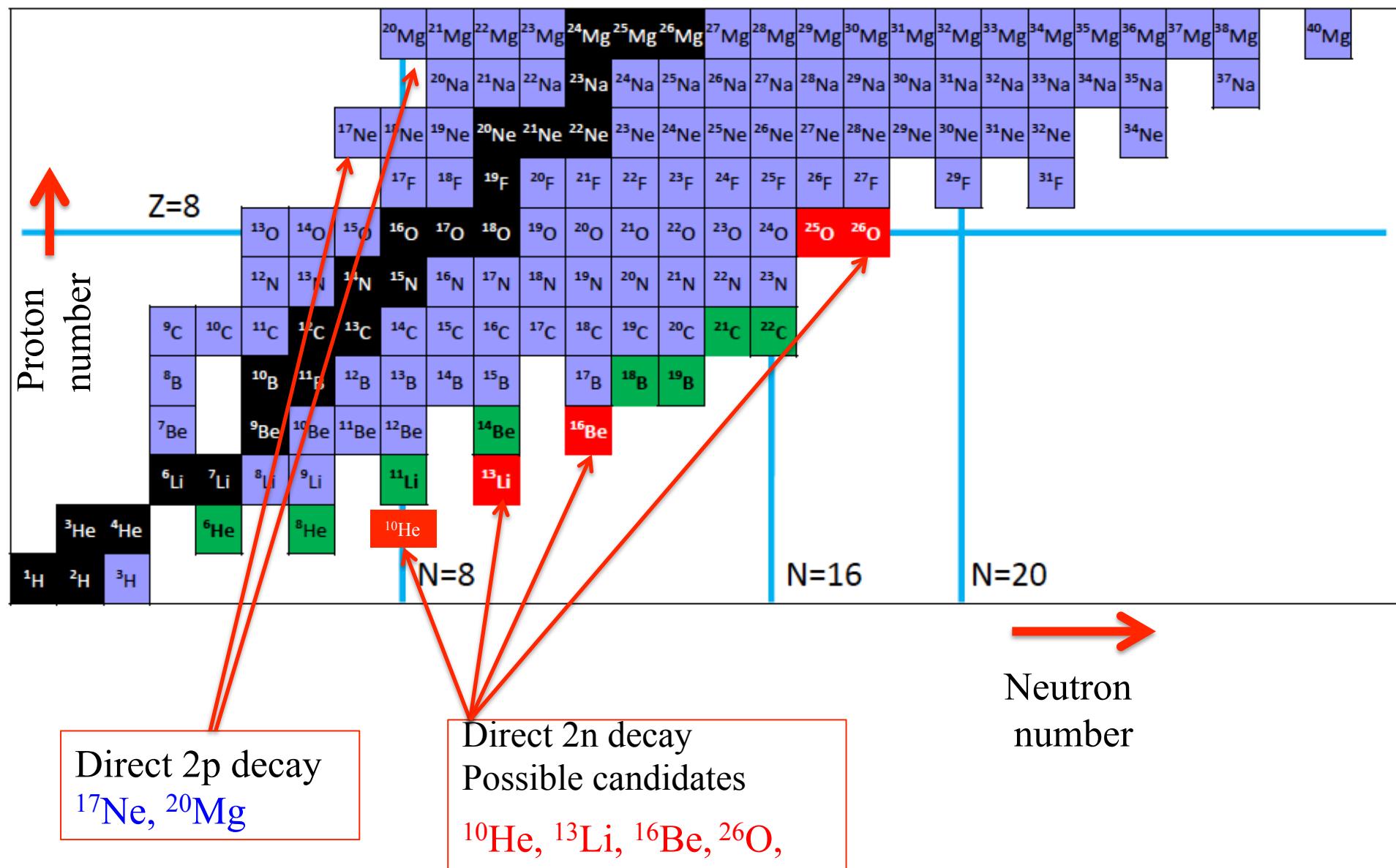
"100 years of subatomic physics"
(Edited by E.M. Henley and S. D. Ellis)
pp. 231-273 (World Scientific, 2013)

How to probe these exotic structures ?

Nuclear reactions

- Coulomb breakup reactions
- Nuclear breakup reactions
- Nucleon transfer reactions
- Direct two-nucleon decays
- Sequential two-nucleon decays
- n-n correlation measurements
- Charge exchange reactions

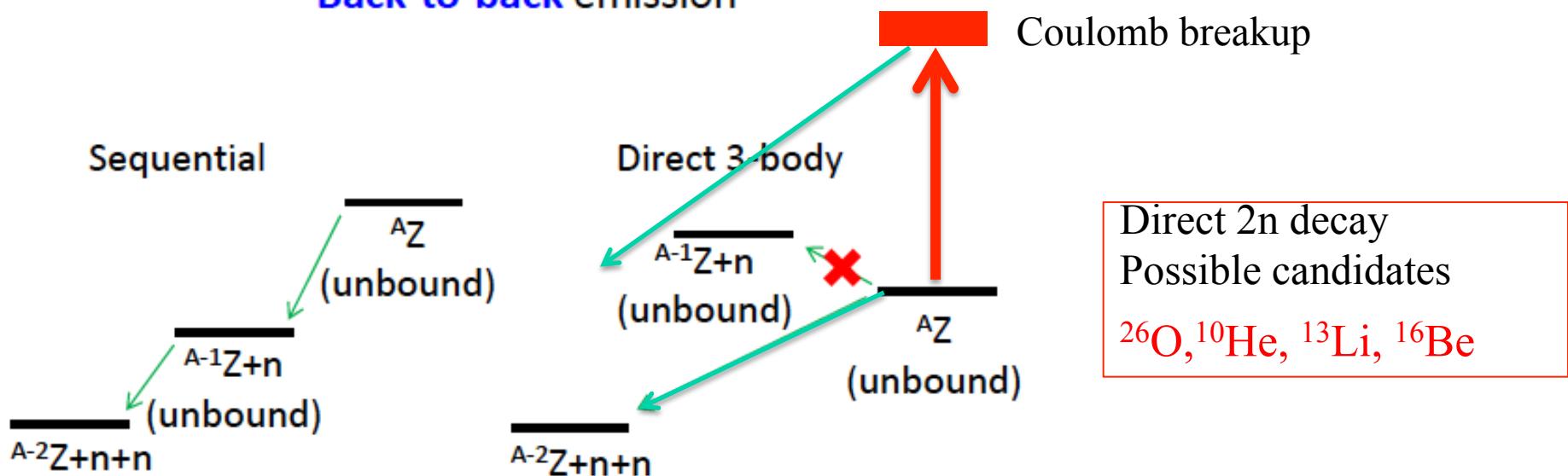
Next generation RI beam facilities : e.g., RIBF (RIKEN, Japan)



Nuclei beyond drip lines

----- direct two neutron decays -----

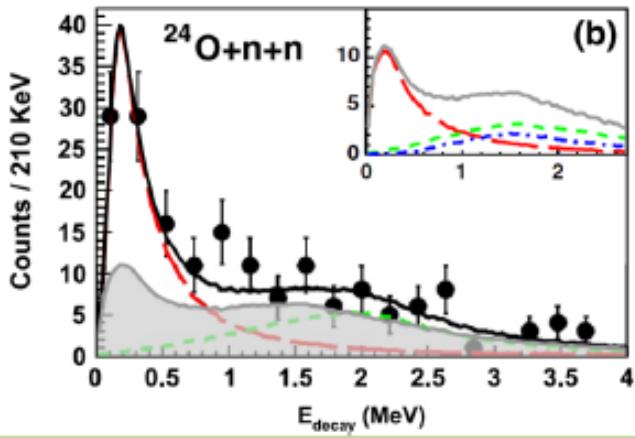
- Decay of 3-body unbound system
 - **Sequential** decay via core + n resonance
 - Direct 3-body decay
 - **Democratic** decay (phase space decay)
 - **Di-neutron** emission
 - **Back-to-back** emission





2n radioactivity of ^{26}O ?

E. Lunderberg et al.PRL108, 142503 (2012)

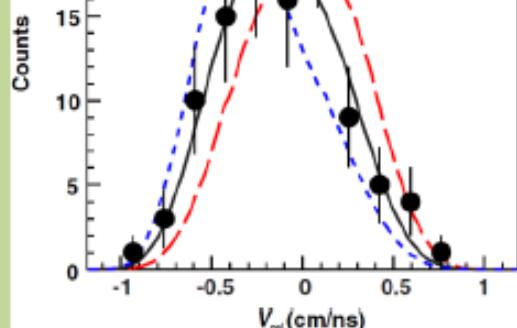


$E_r < 200\text{keV}$

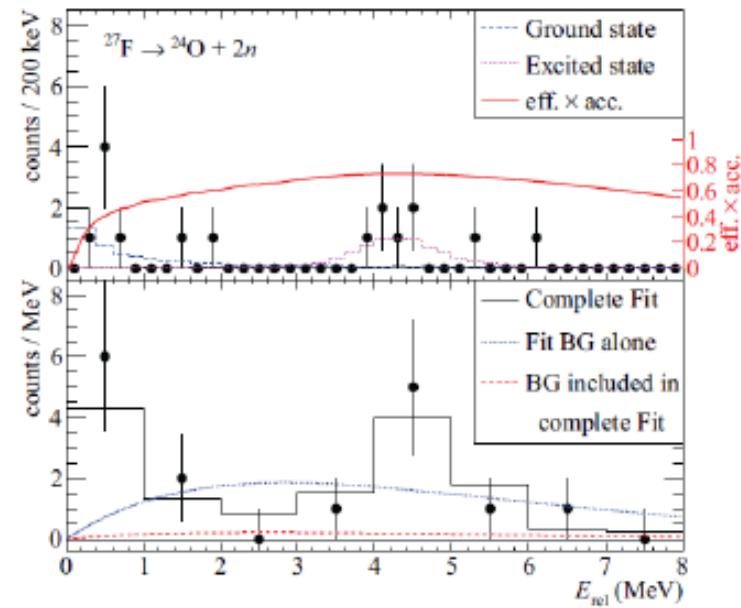
2-neutron decay (MoNA@MSU)

Z. Kohley et al,PRL110,152501 (2013)

(a) $T_{1/2} = 4.5^{+1.1}_{-1.5}\text{ ps}$
(3ps systematic error)
→ 2n radioactivity?



C. Caesar et al.PRC88, 034313 (2013)



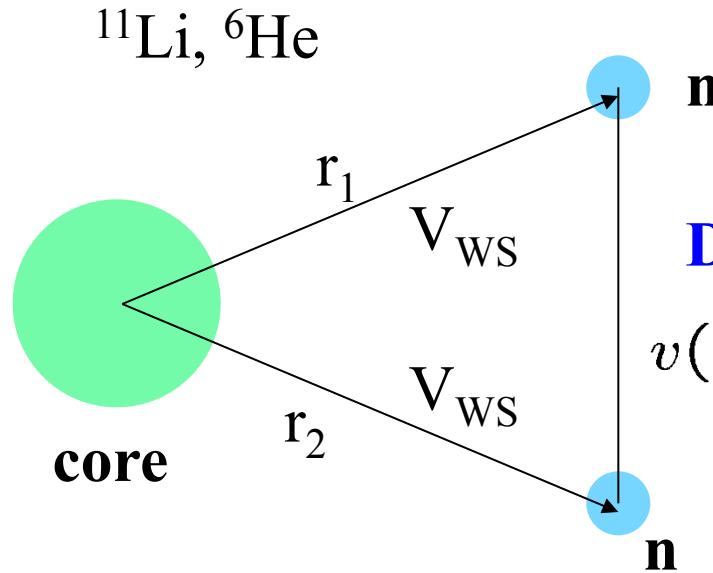
$E_r < 120\text{keV}$ (95% CL)
 $\tau < 5.7\text{ns}$
Excite state at 4.2MeV?

R3B-LAND at GSI

Large uncertainty of experimental study

- Only upper limit is given for the ground state energy
- Large systematic error in the lifetime measurement

Di-neutron correlations and three-body model



G.F. Bertsch and H. Esbensen,

Ann. of Phys. 209 ('91) 327

H. Esbensen, G.F. Bertsch, K. Hencken,

Phys. Rev. C 56 ('99) 3054

K. Hagino and H. S., *PRC* 72 ('05) 044321

H. S. and K. Hagino, *EPJA review* (2015)

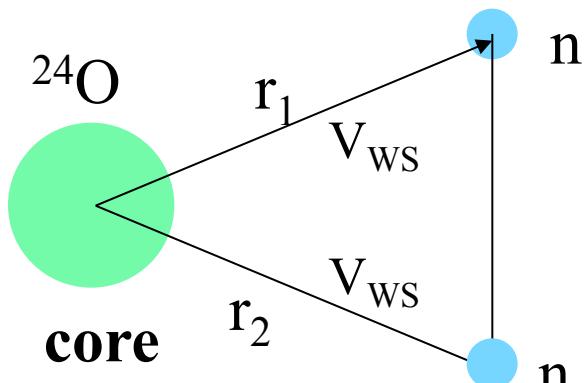
Density-dependent delta-force

$$v(r_1, r_2) = v_0(1 + \alpha\rho(r)) \times \delta(r_1 - r_2)$$

$$H = \frac{\mathbf{p}_1^2}{2m} + \frac{\mathbf{p}_2^2}{2m} + V_{nC}(r_1) + V_{nC}(r_2) + V_{nn} + \frac{(p_1 + p_2)^2}{2A_c m}$$

All parameters are determined empirically to fit the s.p. energies of neighboring nuclei and n-n scattering lengths.

Decay energy spectrum



➤ $^{24}\text{O} + \text{n}$ potential

Woods-Saxon potential to reproduce

$$e_{2s1/2} = -4.09(13) \text{ MeV},$$

$$e_{1d3/2} = +770^{+20}_{-10} \text{ keV},$$

$$\Gamma_{1d3/2} = 172(30) \text{ keV}$$

➤ nn interaction

density-dep. contact interaction

$$E(^{27}\text{F}) = -2.69 \text{ MeV}$$

$$\begin{aligned} \frac{dP_I}{dE} &= \sum_k |\langle \Psi_k^{(I)} | \Phi_{\text{ref}}^{(I)} \rangle|^2 \delta(E - E_k) = -\frac{1}{\pi} \Im \sum_k \langle \Phi_i^{(I)} | \Psi_k^{(I)} \rangle \frac{1}{E_k - E - i\eta} \langle \Psi_k^{(I)} | \Phi_i^{(I)} \rangle \\ &= -\frac{1}{\pi} \Im \langle \Phi_{\text{ref}}^{(I)} | G^{(I)}(E) | \Phi_{\text{ref}}^{(I)} \rangle, \end{aligned}$$

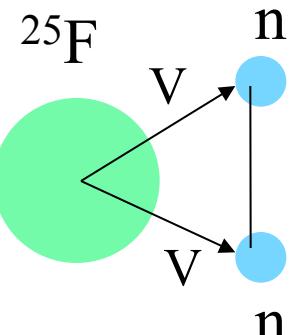
$$G^{(I)}(E) = G_0^{(I)}(E) - G_0^{(I)}(E)v(1 + G_0^{(I)}(E)v)^{-1}G_0^{(I)}(E)$$

$$G_0^{(I)}(E) = \sum_{1,2} \frac{|(j_1 j_2)^{(I)}\rangle \langle (j_1 j_2)^{(I)}|}{\varepsilon_1 + \varepsilon_2 - E - i\eta} \quad \xleftarrow{\text{continuum effects}}$$

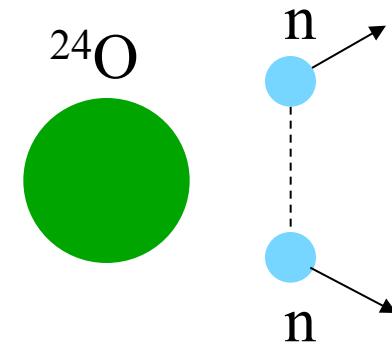
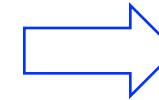
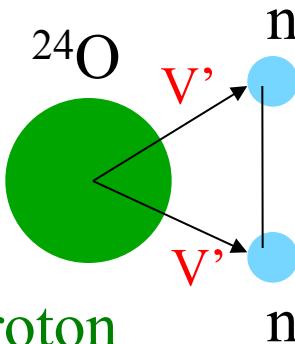
3-body model analysis for ^{26}O decay

K.Hagino and H. S.,
PRC89 ('14) 014331

cf. Expt. : ^{27}F (82 MeV/u) + $^9\text{Be} \rightarrow ^{26}\text{O} \rightarrow ^{24}\text{O} + \text{n} + \text{n}$



sudden
removal of proton



g.s. of ^{27}F (bound)

$$\Psi_{nn} \otimes |^{25}\text{F}\rangle$$

$$\Psi_{nn} \otimes |^{24}\text{O}\rangle$$

spontaneous decay

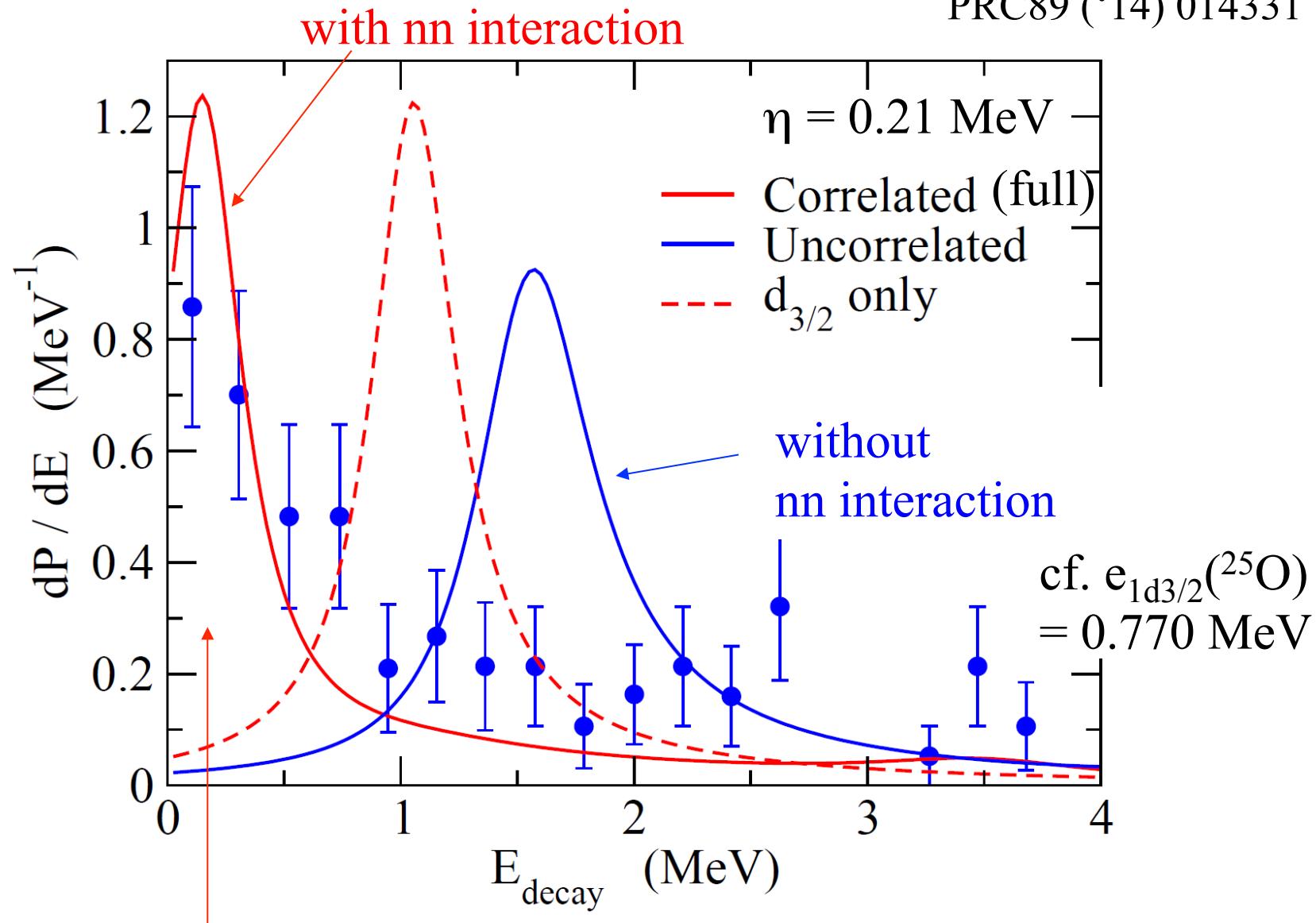
the same config. (non-eigenstate of $^{24}\text{O} + \text{n} + \text{n}$)

FSI → Di-neutron correlations

$$G^{(I)}(E) = G_0^{(I)}(E) - G_0^{(I)}(E)v(1 + G_0^{(I)}(E)v)^{-1}G_0^{(I)}(E)$$

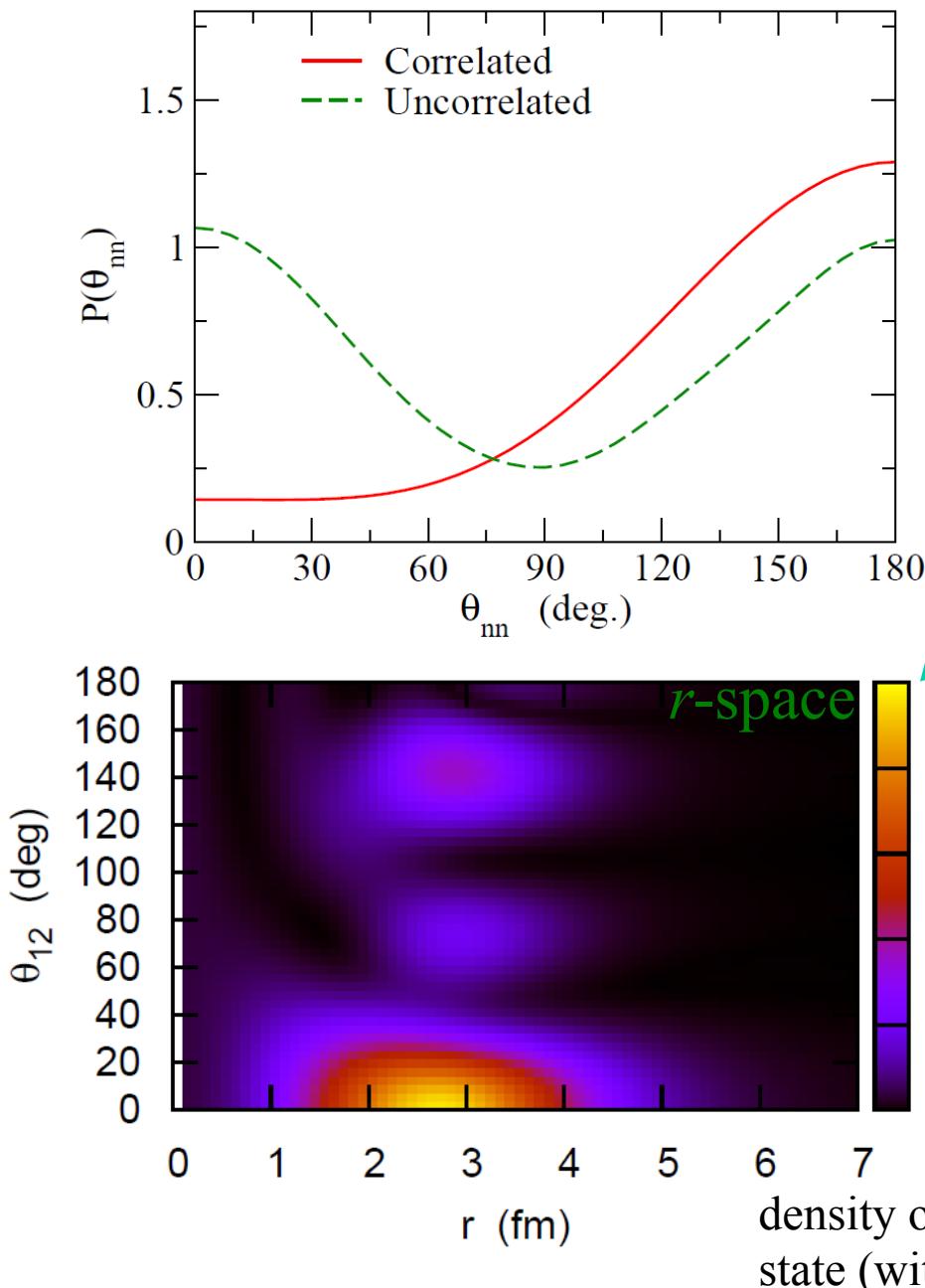
i) Decay energy spectrum for ^{26}O decay

K.Hagino and H. S.,
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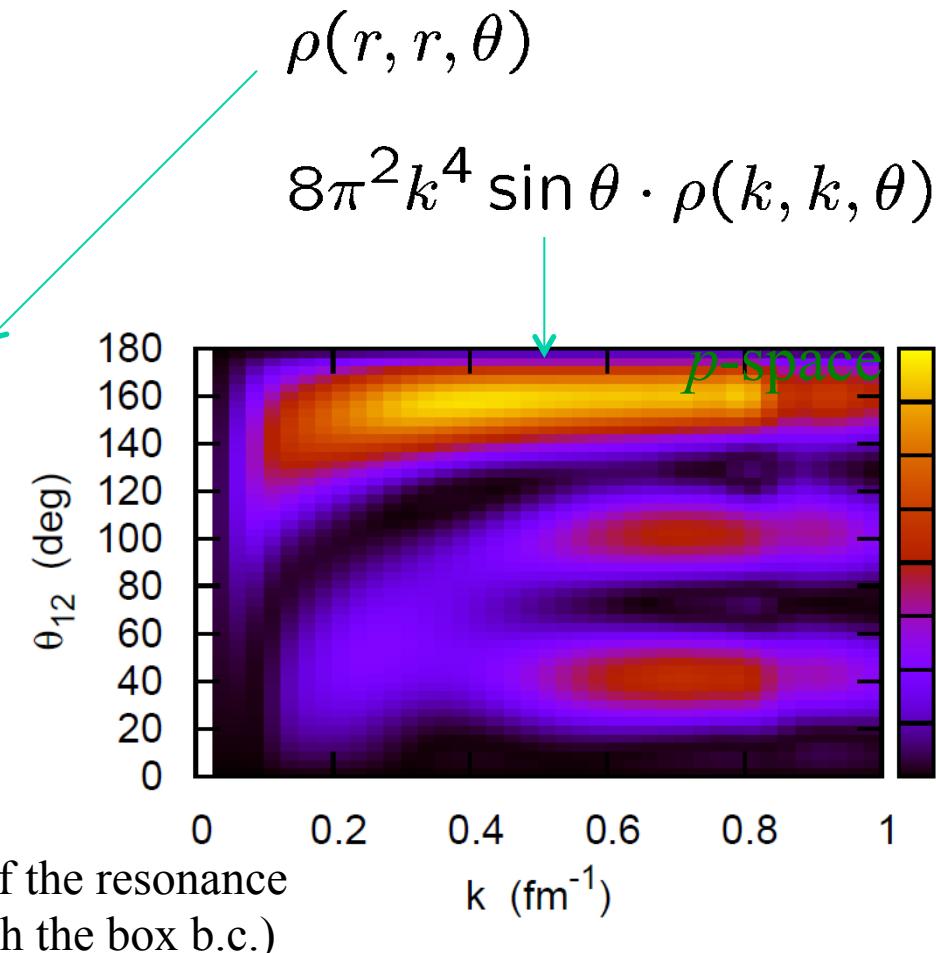
very narrow three-body resonance state ($\Gamma_{\text{exp}} \sim 10^{-10} \text{ MeV}$)
 $E_{\text{peak}} = 0.14 \text{ MeV}$ with this setup for the Hamiltonian

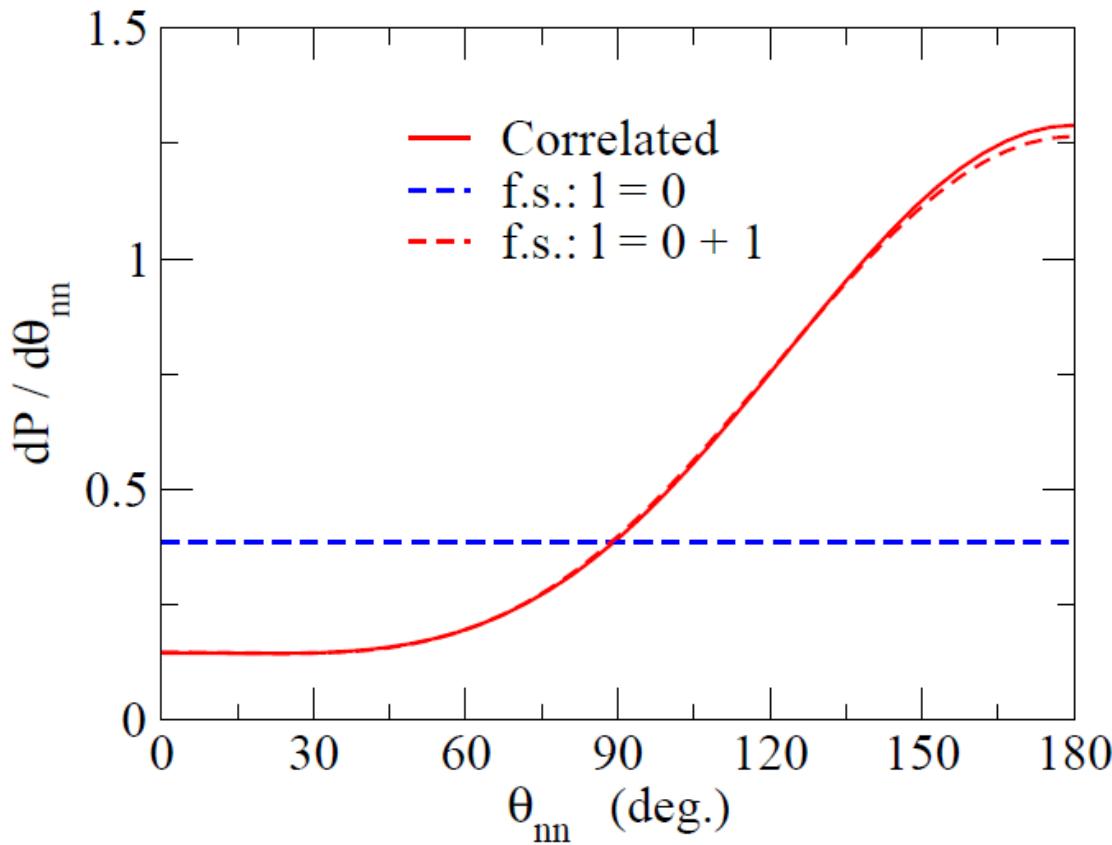
ii) distribution of opening angle for two-emitted neutrons



K.Hagino and H. S.,
PRC89 ('14) 014331

**Heisenberg uncertainty principle
between r and p**



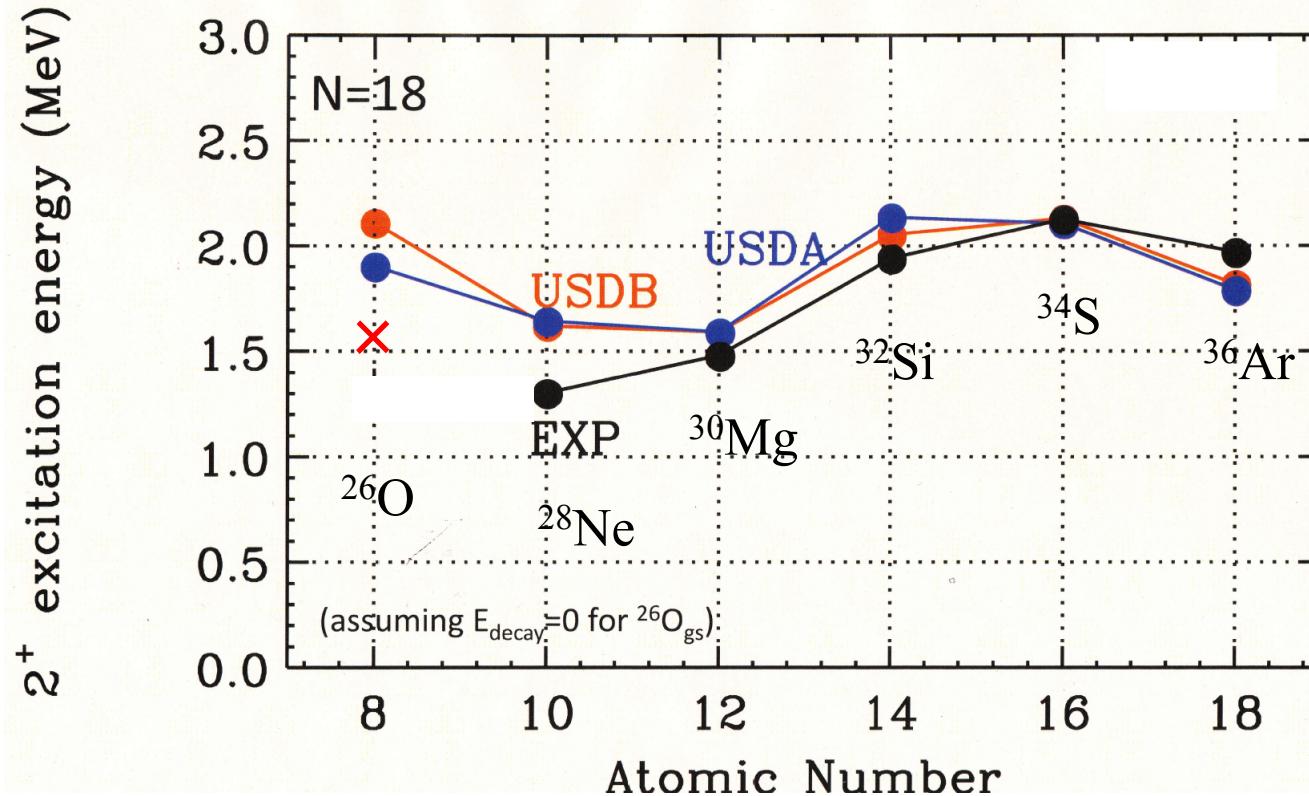


main contributions: s - and p -waves in three-body wave function
(no or low centrifugal barrier)

*higher l components: largely suppressed due to the centrifugal pot.
($E_{\text{decay}} \sim 0.14 \text{ MeV}$, $e_1 \sim e_2 \sim 0.07 \text{ MeV}$)

Excited 2^+ state in ^{26}O

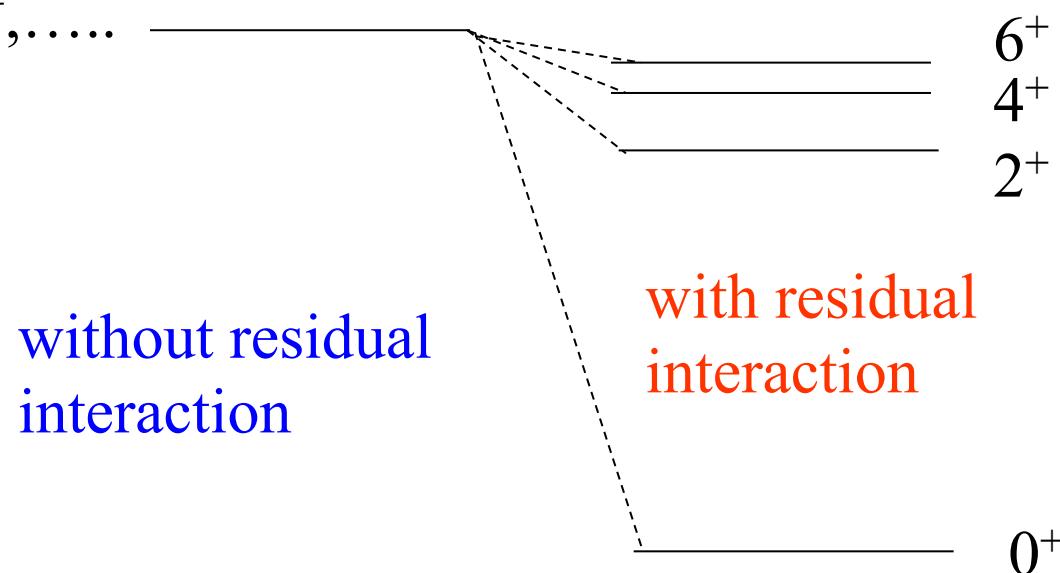
✖ Ab initio shell model with three-body interaction



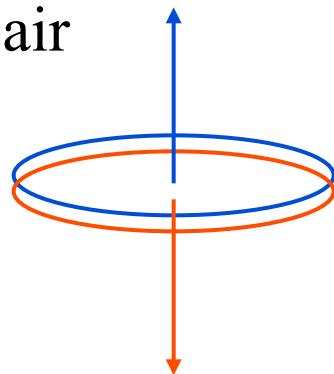
Energy spectrum of contact interaction

$$v(\mathbf{r}_1, \mathbf{r}_2) = \delta(\mathbf{r}_1 - \mathbf{r}_2) \left\{ v_0 + \frac{v_\rho}{1 + \exp[(r_1 - R_\rho)/a_\rho]} \right\},$$

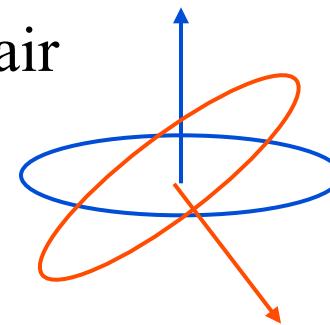
[jj]^(I) = 0⁺, 2⁺, 4⁺, 6⁺,



$I=0$ pair



$I \neq 0$ pair



Three-body model calculation of the 2^+ state in ^{26}O

K. Hagino^{1,2} and H. Sagawa^{3,4}

$$E(0^+) = 5.0 \text{ keV}$$

$$E(2^+) = 1.338 \text{ MeV}$$

^{25}O resonance of d3/2 state $e(\text{d}3/2) = 0.77 \text{ MeV}$

2^+ with a simple configuration $(\text{d}3/2)^2$:
 $E_x = 1.54 \text{ MeV}$ (unperturbed)

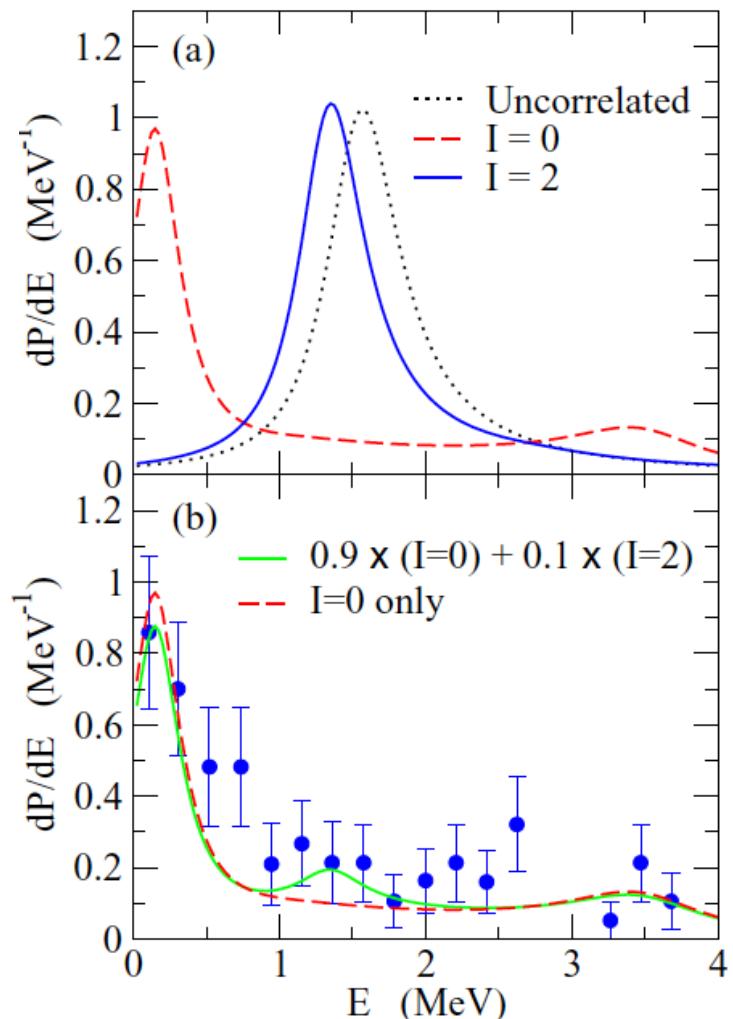


FIG. 1. (Color online) (Top) The decay energy spectrum for the two-neutron emission decay of ^{26}O . The dashed and the solid lines are for the 0^+ and 2^+ states, respectively. The dotted line shows the uncorrelated spectrum obtained by ignoring the interaction between the valence neutrons. (Bottom) The decay energy spectrum obtained by superposing the $I = 0$ and $I = 2$ components. The dashed line is the same as the one in the top panel, that is, the decay energy spectrum for the pure $I = 0$ configuration. The experimental data, normalized to the unit area, are taken from Ref. [5].

	^{25}O ($3/2^+$)	^{26}O (2^+)
Experiment	$+ 770^{+20}_{-10}$ keV	~ 1.3 MeV
USDA	1301 keV	1.9 MeV
USDB	1303 keV	2.1 MeV
sdpf-m	2.15MeV	2.6 MeV
chiral NN+3N	742 keV	1.6 MeV
continuum SM (Volya-Zelevinsky)	1002 keV	1.8 MeV
3-body model (Hagino-Sagawa)	770 keV (input)	1.35 MeV

Summary

Di-neutron correlation : spatial localization of two neutrons

- ✓ Theroy: large model space (**parity mixing**)
- ✓ scattering to **the continuum states**
 - enhancement of pairing on the surface

how to probe it?

- Direct two-neutron emission decay (^{26}O , ^{14}Be)
 - ✓ decay energy spectrum
 - ✓ Final state interaction=di-neutron correlations
 - ✓ opening angle of two emitted neutrons (back-to-back)

^{26}O

ground state: very small width ($\Gamma \sim 10^{-10}\text{MeV}$)
very small resonance energy ($E_x < 140\text{keV}$)

2^+ : The three-body model with a contact pairing interaction gives $E_x = 1.3\text{MeV}$. ab initio and USD shell model calculations give higher energy than $E_x > 1.6\text{MeV}$.