

# The $\epsilon'_K/\epsilon_K$ tension and supersymmetric interpretation

**Teppei Kitahara**

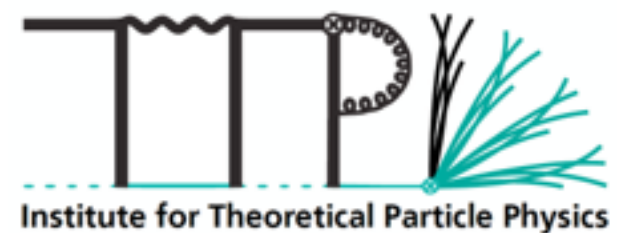
Karlsruhe Institute of Technology (KIT), TTP

in collaboration with **Ulrich Nierste,**  
**Paul Tremper, Andreas Crivellin,**  
and **Giancarlo D'Ambrosio**

Phys.Rev.Lett.117, 091802 (2016) [arXiv:1604.07400],  
JHEP 1612, 078 (2016) [arXiv:1607.06727],  
Phys.Lett.B771, 37-44 (2017) [arXiv:1612.08839],  
and arXiv:1703.05786

XIIth Meeting on B Physics. Tensions in Flavour measurements:  
a path toward Physics beyond the Standard Model

Napoli, Italy, May 23, 2017



# $K \rightarrow \pi\pi$ system

- Precise measurements for Kaon decay into two pions have discovered the **two type of CP violations**: indirect CPV  $\epsilon_K$  & direct CPV  $\epsilon'_K$ :

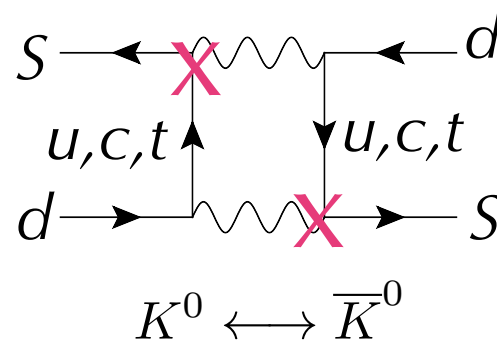
$$\mathcal{A}(K_L \rightarrow \pi^+\pi^-) \propto \epsilon_K + \epsilon'_K \quad \text{with } \epsilon_K = \mathcal{O}(10^{-3}) \neq 0 \quad [\text{Christenson, Cronin, Fitch, Turlay, '64 with Nobel prize}]$$

$$\mathcal{A}(K_L \rightarrow \pi^0\pi^0) \propto \epsilon_K - 2\epsilon'_K \quad \epsilon'_K = \mathcal{O}(10^{-6}) \neq 0 \quad [\text{NA48/CERN and KTeV/FNAL '99}]$$

$\Delta S=2$

Indirect CP violation  
Kaon oscillation  
W box

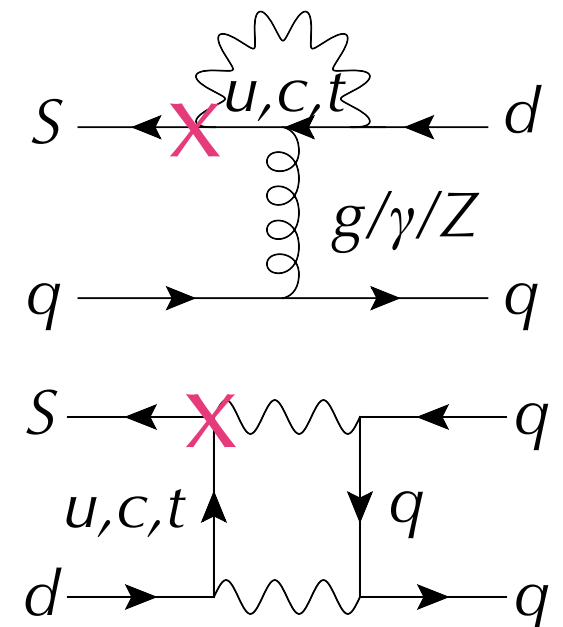
$$\epsilon_K \propto \text{Im}[(\text{CKM})^2]$$



$\Delta S=1$

Direct CP violation  
W-box and penguin

$$\epsilon'_K \propto \text{Im}[\text{CKM}]$$

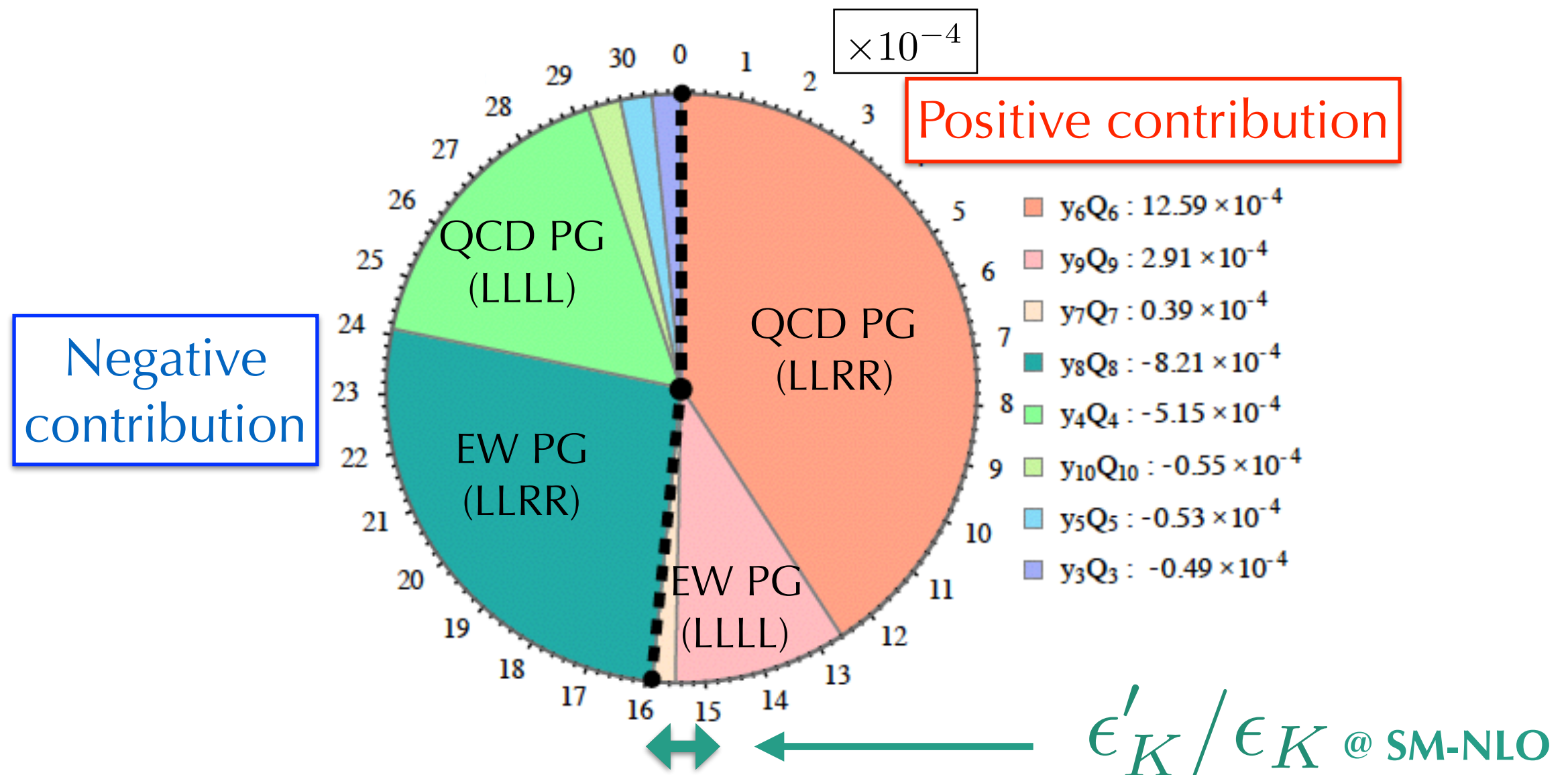


- The **strong suppression** of  $\epsilon'_K$  comes from the smallness of the isospin-3/2 amplitude ( $\Delta I = 1/2$  rule) and an accidental cancellation of the SM contribution

# Accidental cancellation

[TK, Nierste, Tremper, JHEP '16]

Composition of  $\epsilon'_K/\epsilon_K$  with respect to the operator basis



# $\epsilon'_K/\epsilon_K$ discrepancy

- A determination of all hadronic matrix elements for  $\epsilon'_K/\epsilon_K$  by **RBC-UKQCD group** has been obtained **with controlled errors (first lattice result)**, so that one becomes able to estimate  $\epsilon'_K/\epsilon_K$  without using the effective theories, e.g. chiPT, dual QCD model, NJL model, ... [RBC-UKQCD, PRL '15]

- SM expectation value at NLO [TK, Nierste, Tremper, JHEP '16]

$$\left(\frac{\epsilon'_K}{\epsilon_K}\right)_{\text{SM-NLO}} = (1.06 \pm 4.66_{\text{Lattice}} \pm 1.91_{\text{NNLO}} \pm 0.59_{\text{IV}} \pm 0.23_{m_t}) \times 10^{-4}$$

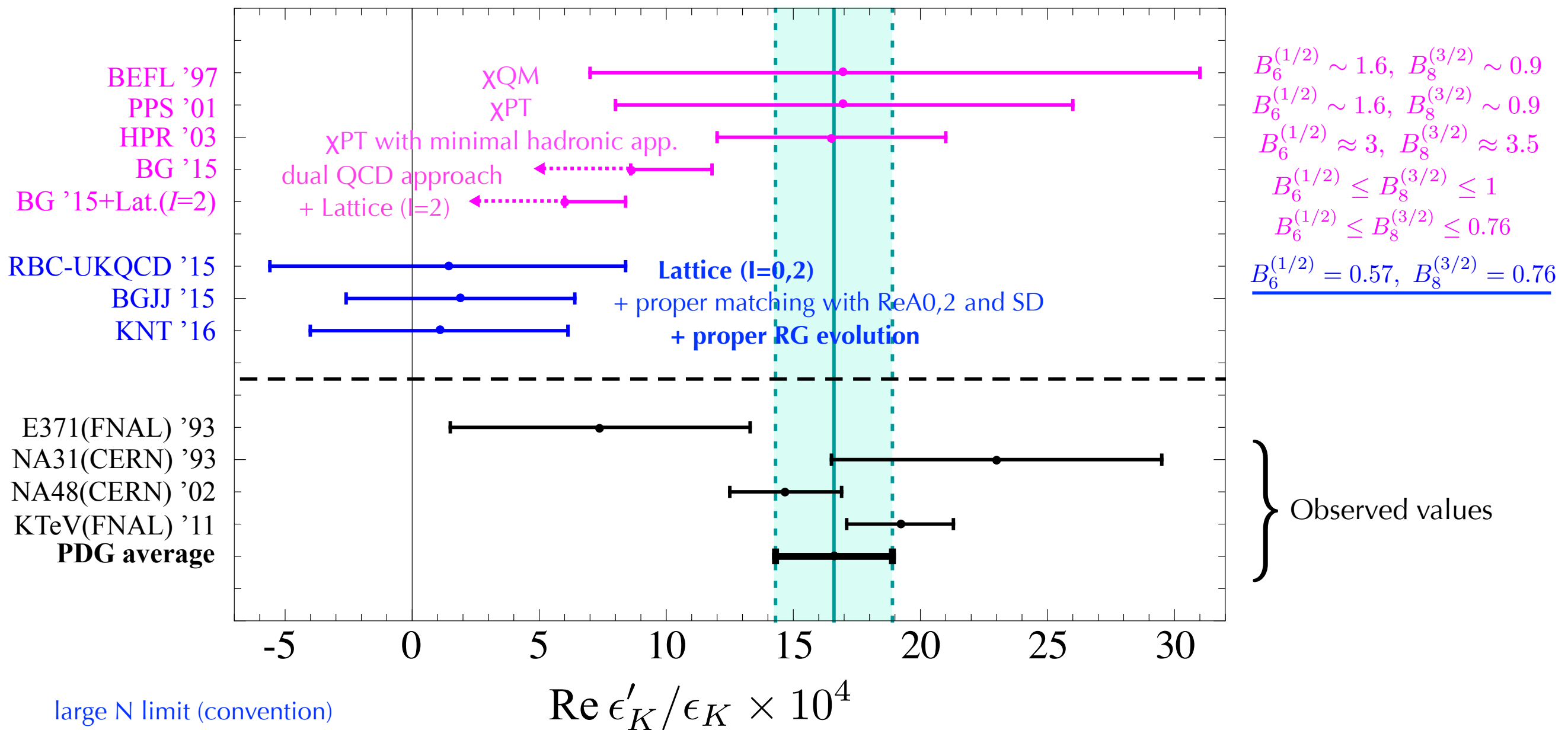
Our prediction uses the methodology of [Buras et al. \(JHEP 1511 \(2015\) 202\)](#) (taking  $\text{Re}A_{0,2}$  from data) and a **new formula** for the NLO RG evolution

- World average of experimental results  $\text{Re} \left(\frac{\epsilon'_K}{\epsilon_K}\right)_{\text{exp}} = (16.6 \pm 2.3) \times 10^{-4}$  [NA62, KTeV, PDG]

- **Discrepancy with a significance of  $2.8\sigma$**

[Buras et al. \(JHEP 1511 \(2015\) 202\)](#) obtained  $2.9\sigma$  discrepancy

# Current situation of $\epsilon'_K / \epsilon_K \propto \text{Im}A_0 - \left( \frac{\text{Re}A_0}{\text{Re}A_2} \right) \text{Im}A_2$



large N limit (convention)

$$B_6^{(1/2)} = B_8^{(3/2)} = 1$$

dual QCD prediction

$$B_6^{(1/2)} \leq B_8^{(3/2)} < 1, B_8^{(3/2)} = 0.8$$

$$\left( \frac{\text{Re}A_0}{\text{Re}A_2} \right)$$

Exp.  
 $22.45 \pm 0.05$

$\chi$ PT  
 $\sim 14$

dual QCD  
 $16.0 \pm 1.5$

Lattice (I=0,2)  
 $31.0 \pm 11.1$

The epsilon'/epsilon tension and supersymmetric interpretation

Teppei Kitahara: Karlsruhe Institute of Technology (KIT), XIIth Meeting on B Physics, 23 May, 2017, Napoli, Italy

$\epsilon_K$  and  $\epsilon'_K$

in the supersymmetric model

# Preliminary for NP part

- The SM prediction of  $\epsilon'_K/\epsilon_K$  is **2.8 sigma below** the experimental values, which give strong motivation for searching for NP contributions
- $\epsilon'_K/\epsilon_K$  is highly sensitive to CP violation of NP

SM    loop suppression  $\times$  GIM suppression  $\times$  accidental cancelation  
VS.

NP    (loop suppression)  $\times$  (large coupling)  $\times$  NP scale suppression

- Some models can explain this discrepancy, e.g. Littlest Higgs model, 331 model, generic  $Z'$  models, modified Z-coupling model, RH coupling of quarks to W, and **supersymmetric (SUSY) models**

[Buras,Fazio,Girrbach '14, Buras,Buttazzo,Knegjens '15, Buras '15, Buras, Fazio '15, '16, Goertz,Kamenik,Katz,Nardecchia '15, Blanke,Buras,Recksiegel '16, Cirigliano,Dekens, Vries, Mereghetti '16, TK,Nierste,Tremper '16, Tanimoto, Yamamoto '16, Endo,Mishima,Ueda,Yamamoto '16]



# Main Constraint: $\epsilon_K$ ( $\Delta S=2$ , ID-CPV)

- Although  $\epsilon'_K/\epsilon_K$  ( $\Delta S=1$ , D-CPV) is sensitive to NP, once  $\epsilon_K$  ( $\Delta S=2$ , ID-CPV) constraint is taken into account, NP effects in  $\Delta S=1$  is highly suppressed

If the NP CPV contribution comes with the  $\Delta S = 1$  parameter  $\delta$  and is mediated by heavy particles of mass  $M$ , one finds

$$\epsilon_K^{\text{NP}} \propto \frac{\text{Im}(\delta^2)}{M^2} \quad \epsilon_K'^{\text{NP}} \propto \frac{\text{Im}\delta}{M^2}$$

➔

$$\frac{\epsilon_K'^{\text{NP}}}{\epsilon_K'^{\text{SM}}} \leq \frac{\frac{\epsilon_K'^{\text{NP}}}{\epsilon_K^{\text{NP}}}}{\frac{\epsilon_K'^{\text{SM}}}{\epsilon_K^{\text{SM}}}} = \mathcal{O}\left(\frac{\text{Re}\tau}{\text{Re}\delta}\right)$$

$\uparrow$   
 $\epsilon_K^{\text{NP}} \leq \epsilon_K^{\text{SM}}$ : ID-CPV constraint

$$\tau = -\frac{V_{td}V_{ts}^*}{V_{ud}V_{us}^*} \sim (1.5 - i0.6) \cdot 10^{-3}$$

when loop factor  $1/(4\pi)$  is the same as the SM

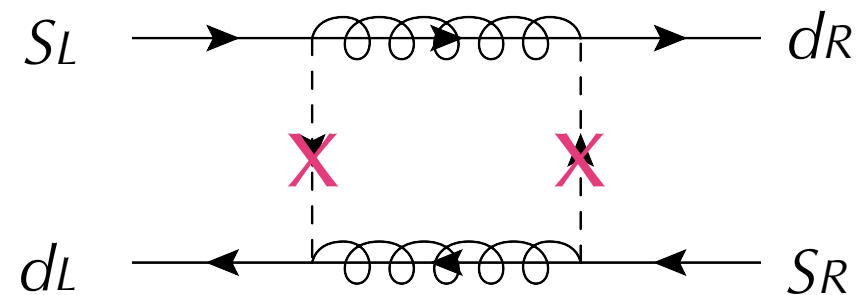
- With  $M > 1$  TeV, NP effects can only be basically relevant for  $|\delta| \gg |\tau|$ , so that this equation seemingly forbids detectable NP contributions to  $\epsilon'_K/\epsilon_K$

➔ **There is a loophole in the SUSY model (next slide)**



# Main Constraint: $\epsilon_K$ ( $\Delta S=2$ , ID-CPV) cont.

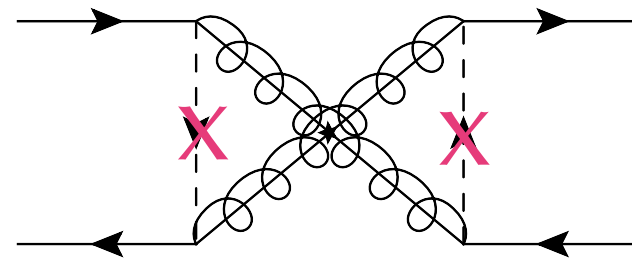
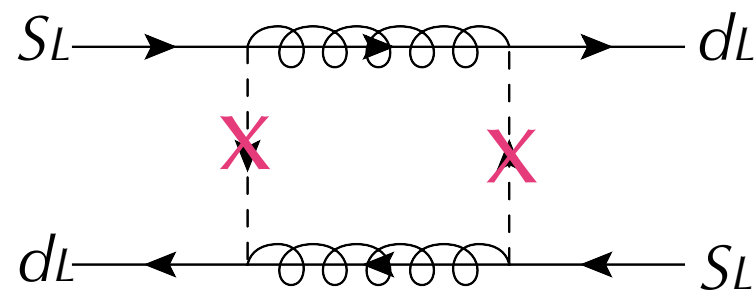
- The leading contribution is given by  $\overline{d}_L s_L \overline{d}_R s_R$



$$\propto \left( \frac{m_K}{m_s + m_d} \right)^2$$

this contribution is suppressed  
when  $\Delta_{\bar{D},12} \simeq 0$

- The next contribution is given by  $\overline{d}_L s_L \overline{d}_L s_L$



Crossed diagram gives  
**relatively negative**  
contributions

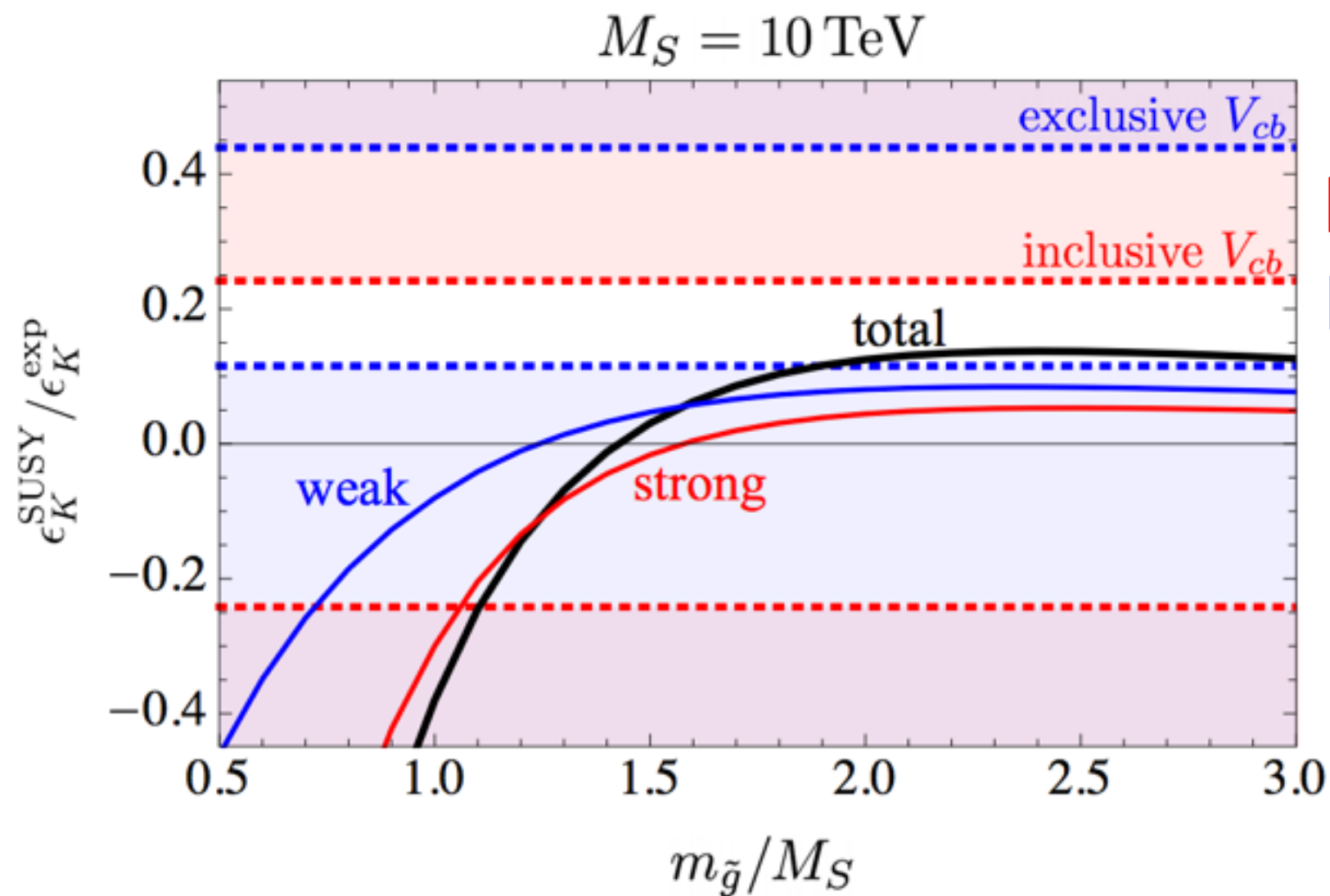
$m_{\tilde{g}} \simeq 1.5 m_{\tilde{q}}$  : these contributions almost cancel out

[Crivellin, Davidkov '10]

$m_{\tilde{g}} \gtrsim 1.5 m_{\tilde{q}}$  : suppressed by heavy gluino mass

# Constraint from $\epsilon_K$

[TK, Nierste, Tremper, PRL '16]



values in our plot

$$|V_{cb}|_{\text{inc.}} = 42.21(78) \times 10^{-3}$$

$$|V_{cb}|_{\text{exc.}} = 39.04(74) \times 10^{-3}$$

value from Silvestrini's slide

$$|V_{cb}|_{\text{UTfit predictions2017}} = 42.1(6) \times 10^{-3}$$

- Actually, there are several expected values of  $\epsilon_K$  depending on the input CKM parameters

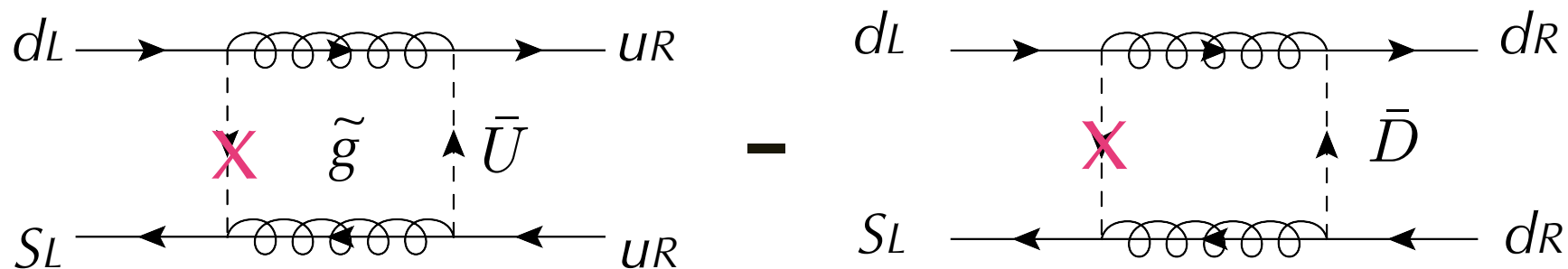
$|V_{cb}|_{\text{incl.}}$ , measured in inclusive  $b \rightarrow c\ell\nu$  decays.....  $\epsilon_K$  is consistent with exp. value

$|V_{cb}|_{\text{incl.}}$ , measured in exclusive  $B \rightarrow D(*)\ell\nu$  decays.....  $\epsilon_K$  is  $3\sigma$  below the exp. value

# Gluino contribution to $\epsilon'_K/\epsilon_K$

[Kagan, Neubert, PRL '99, Grossman, Kagan, Neubert, JHEP '99]

- The main contribution to  $\epsilon'_K/\epsilon_K$  comes from gluino box loop
- In spite of QCD correction, gluino box diagrams **can** break isospin symmetry through mass difference between right-handed up and down squark masses, and they can contribute **ImA<sub>2</sub>**, which is enhanced by small **ReA<sub>2,exp</sub>** value



$m_{\bar{U}} \neq m_{\bar{D}}$   $\xrightarrow{\text{RGE}}$  EW penguin operators are generated at the low energy scale  
 with HMEs  $\longrightarrow$  contribute to **ImA<sub>2</sub>**

$$\frac{\epsilon'_K}{\epsilon_K} = \frac{1}{\sqrt{2}|\epsilon_K|_{\text{exp}}} \frac{\omega_{\text{exp}}}{(\text{Re}A_0)_{\text{exp}}} \left( -\text{Im}A_0 + \frac{1}{\omega_{\text{exp}}} \text{Im}A_2 \right) \quad \text{where} \quad \frac{1}{\omega} \equiv \frac{\text{Re}A_0}{\text{Re}A_2} = 22.46 \text{ (exp.)}$$

# SUSY contributions to $\epsilon'_K/\epsilon_K$

[TK, Nierste, Tremper, PRL, '16]

- We take universal SUSY mass ( $M_S$ ) without gaugino masses ( $M_3$ ) and right-handed up-type squark mass ( $m_{\bar{U}}$ )

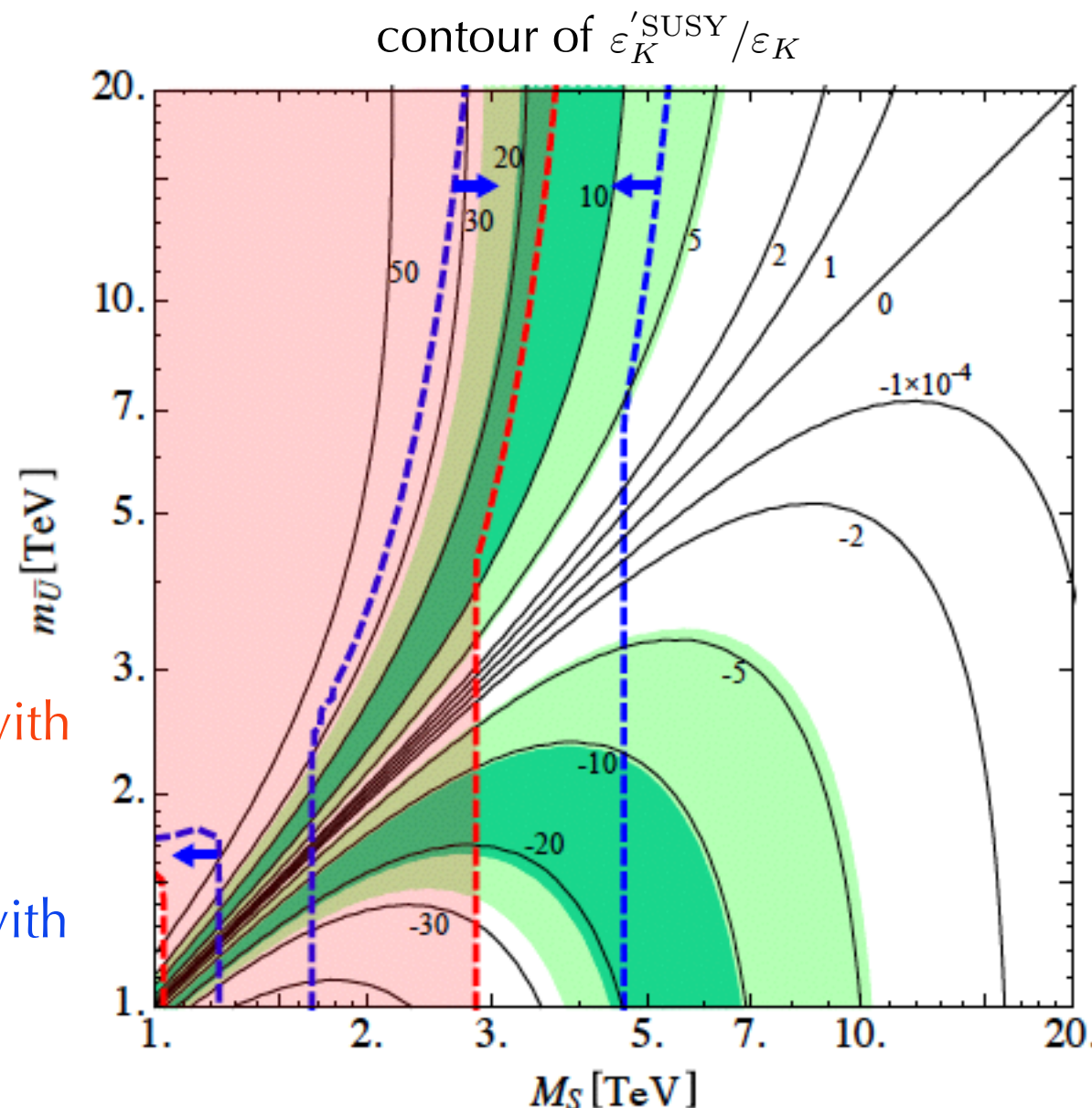
$\epsilon'_K/\epsilon_K$  discrepancy can be solved at

1 $\sigma$

2 $\sigma$

excluded by  $\epsilon_K$  with inclusive  $|V_{cb}|$

preferred by  $\epsilon_K$  with exclusive  $|V_{cb}|$



$$M_3 = 1.5M_S$$

for suppressed  $\epsilon_K$

$$m_{Q,ij}^2 = \Delta_{Q,ij} M_S^2$$

$$\Delta_{Q,12,13,23} = 0.1 \exp(-i\pi/4)$$

maximum CPV phase for  $\epsilon_K$

when  $i\pi/4 \rightarrow i\pi/2$

amplifies  $\epsilon'_K/\epsilon_K$

suppresses  $\epsilon_K$

$\epsilon_K$ ,  $\epsilon'_K$ , and  $\mathcal{B}(K \rightarrow \pi \nu \bar{\nu})$   
in the supersymmetric model

# Other rare kaon decay

- **CP violation + FCNC decays of kaon**  $K \rightarrow \pi\pi$ ,  $K \rightarrow \pi\nu\bar{\nu}$ ,  $K \rightarrow \pi\ell\bar{\ell}$  are **extremely sensitive to NP** and can probe virtual effects of particles with masses far above the reach of LHC
- They are correlated to each other

$\epsilon'_K$  discrepancy  $\longrightarrow$  deviations of the other rare kaon decay  
( $K_L \rightarrow \pi\pi$ )

$K \rightarrow \pi\nu\bar{\nu}$  **Good** The experiments are on-going!

NA62 experiment at CERN  $K^+ \rightarrow \pi^+\nu\bar{\nu}$ , target : **10% precision compared with SM** (2018)

KOTO experiment at J-PARC  $K_L \rightarrow \pi^0\nu\bar{\nu}$ , target : **100%** (step1), **10%** (step2)

$K_L \rightarrow \pi^0\ell^+\ell^-$  : CPV, the theoretical uncertainty can be reduced by **precise measurement of  $K_S \rightarrow \pi^0\ell^+\ell^-$**   $\longrightarrow$  **LHCb**

direct detection of  $K_L \rightarrow \pi^0\ell^+\ell^-$  is also important

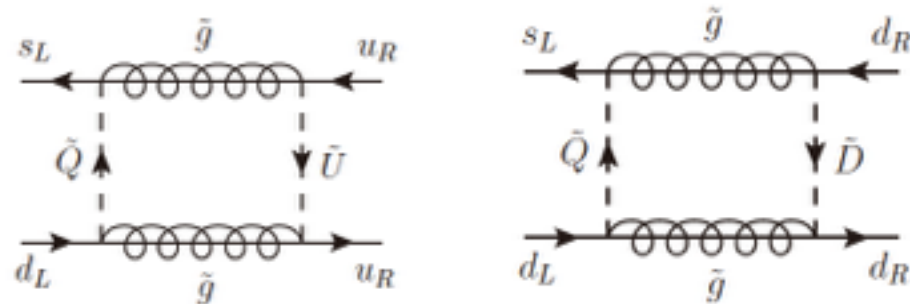


# Overview in our SUSY scenario

- In the supersymmetric model (MSSM), the following parameter region is interesting for  $\epsilon'_K$  discrepancy:

$$M_3 \gtrsim 1.5M_S, \quad m_{Q,12}^2 \neq 0, \quad \text{and} \quad m_{\bar{U}}/m_{\bar{D}} \neq 1$$

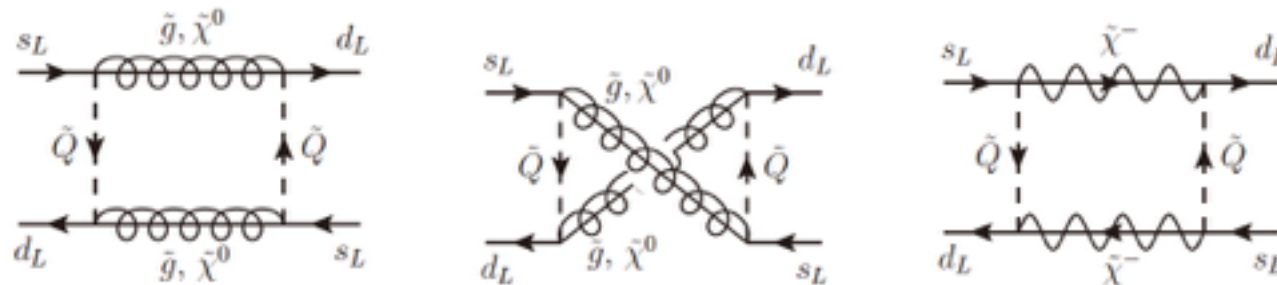
$\Delta S=1$



can explain  $\epsilon'_K$  discrepancy

[TK, Nierste, Tremper, '16]

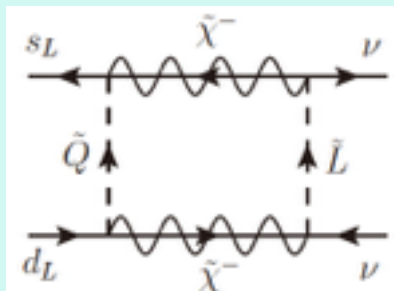
$\Delta S=2$



can **suppress**  $\Delta S=2$  process

[Crivellin, Davidkov, '10]

$\Delta S=1$



can contribute to  $K \rightarrow \pi \nu \bar{\nu}$  correlating with above two physics

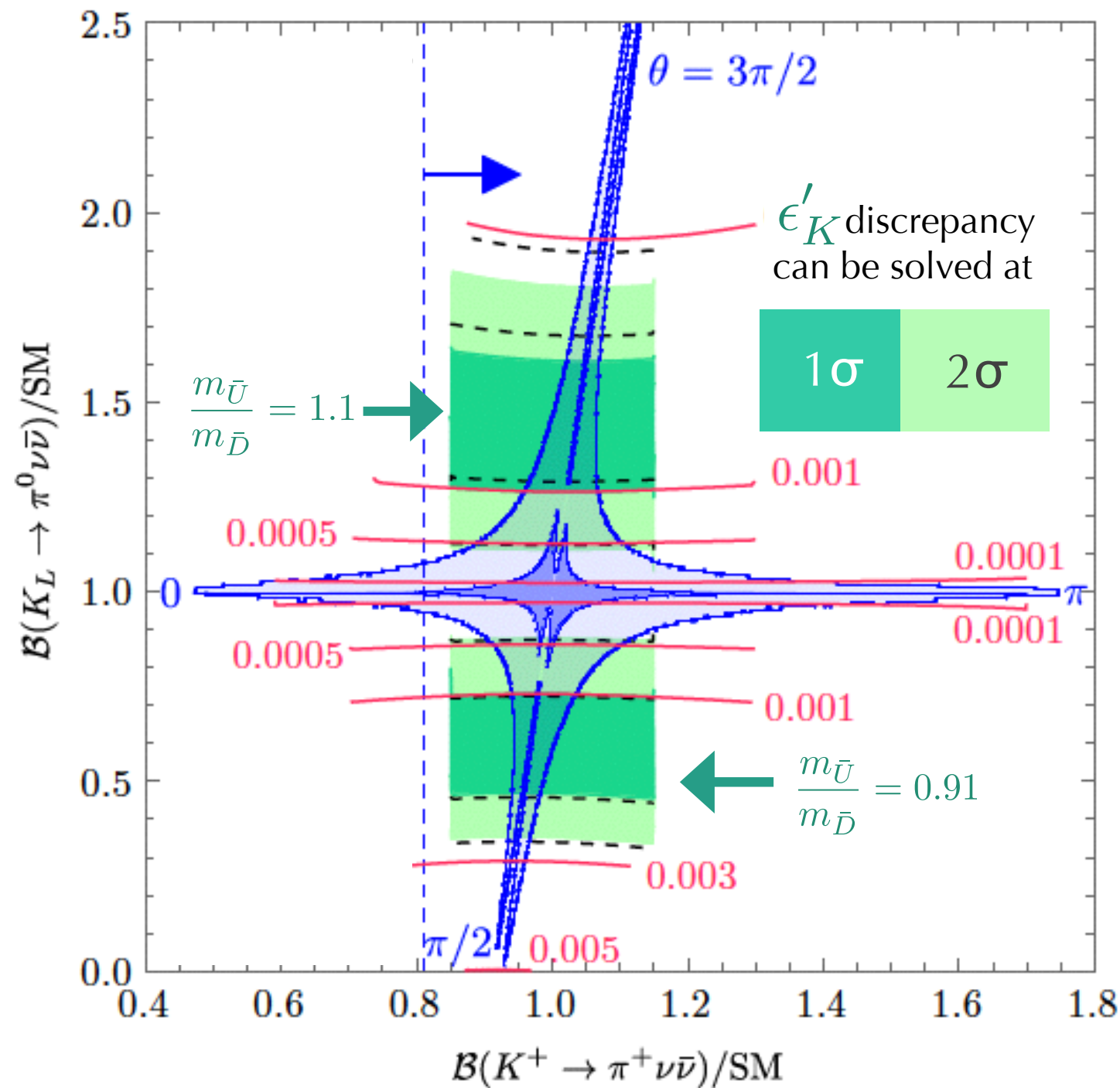
[Crivellin, D'Ambrosio, TK, Nierste, '17]



# $B(K \rightarrow \pi \nu \nu)$

[Crivellin, D'Ambrosio, TK, Nierste, '17]

$$m_{\tilde{q}_1} = 1.5 \text{ TeV}, m_L = 300 \text{ GeV}$$



more than 10% mass shift of the gluino mass from  $M_3 \simeq 1.45 M_S$  is possible in light of the constraint from  $\epsilon_K$

1-10 % mass shift of the gluino mass is possible

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})/\text{SM} \lesssim 2 \quad (1.2)$$

$$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})/\text{SM} \lesssim 1.4 \quad (1.1)$$

for a fine-tuning at the 1(10)% level

$m_{\tilde{U}}/m_{\tilde{D}}$  determines a position of the green band

Positive  $\epsilon'_K$  predicts a strict correlation

$$\text{sgn} [\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) - \mathcal{B}^{\text{SM}}(K_L \rightarrow \pi^0 \nu \bar{\nu})] = \text{sgn} [m_{\tilde{U}} - m_{\tilde{D}}]$$

$$\text{sgn} [m_{\tilde{U}} - m_{\tilde{D}}] \xrightarrow{\epsilon'_K} \arg [m_{Q12}^2]$$

$$\text{sgn} [\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) - \mathcal{B}^{\text{SM}}(K_L \rightarrow \pi^0 \nu \bar{\nu})]$$

$\epsilon_K$ ,  $\epsilon'_K$ , and  $\mathcal{B}(K \rightarrow \pi \nu \bar{\nu})$   
in modified  $Z$ -coupling scenario  
(SUSY/non-SUSY)

# Modified Z-coupling scenario

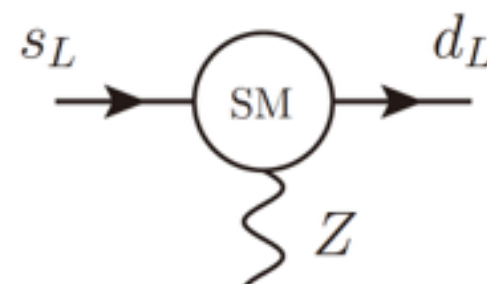
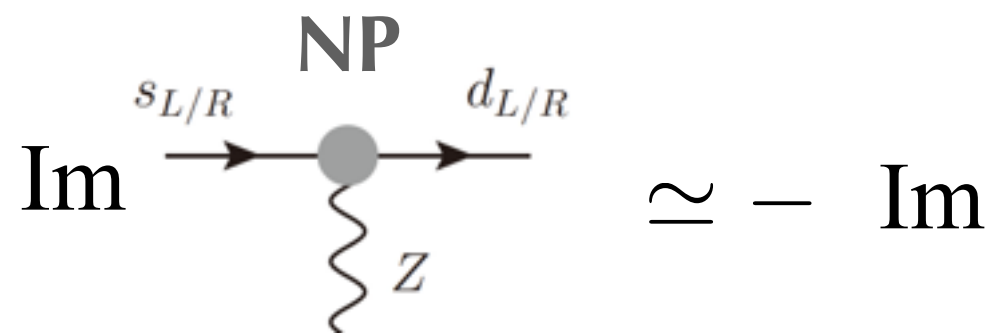
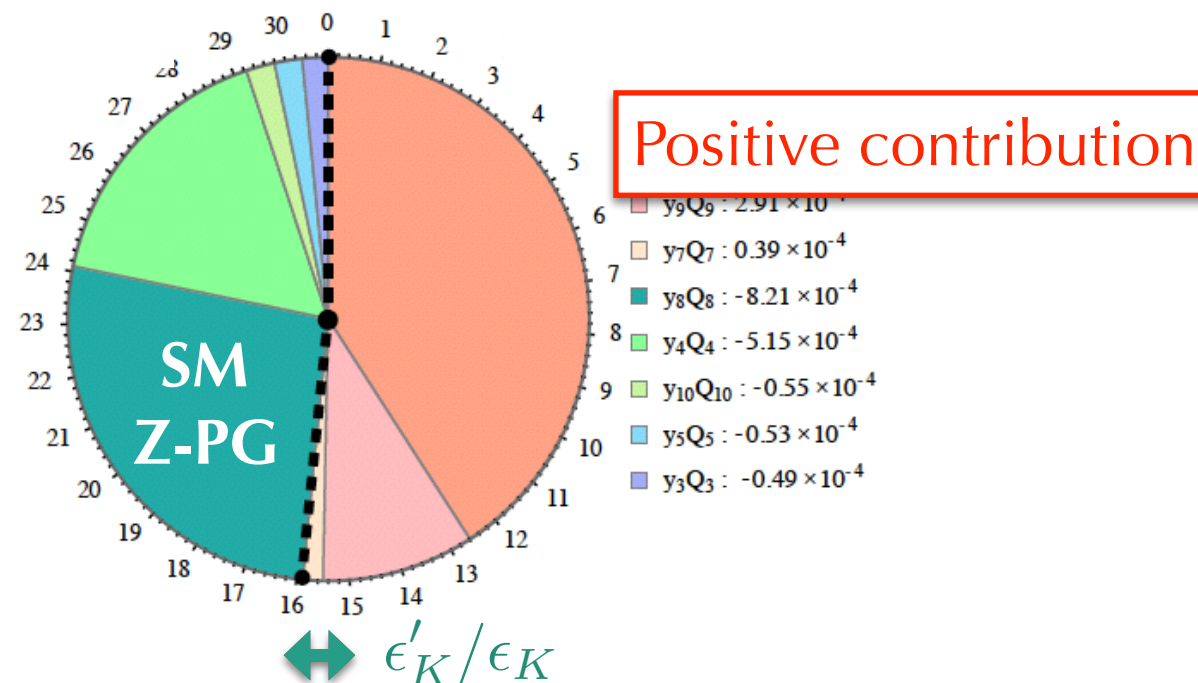
[Buras, De Fazio, Girschbach, '13, '14]  
 [Buras, Buttazzo, Kneijens, '15]  
 [Buras, '16]  
 [Endo, TK, Mishima, Yamamoto, '16]  
 [Bobeth, Buras, Celis, Jung, '17]

- NP contributions to  $sdZ$  coupling which has the same magnitude as the SM Z-penguin can explain  $\epsilon'_K$  discrepancy

$$\epsilon'_K/\epsilon_K \times 10^{-4}$$

Negative contribution

SM Z-penguin gives the biggest negative contribution



$\epsilon'_K$  can be solved

O(1) contribution to  $\mathcal{B}(K \rightarrow \pi \nu \bar{\nu})$

Note: (SM) is suppressed by the GIM mechanism, so that it is a numerically small coupling

# Modified Z-coupling scenario cont.

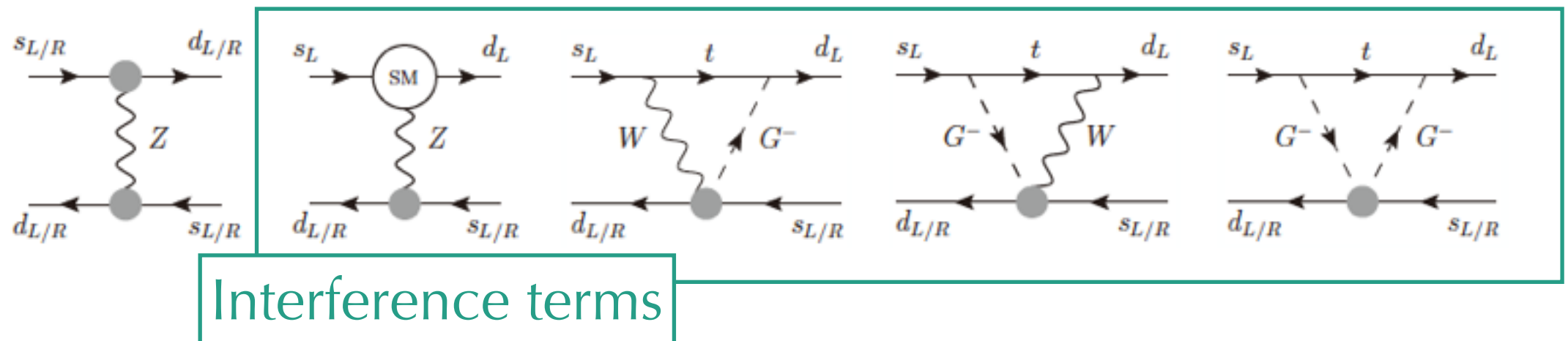
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[Buras, '16]  
[Endo, TK, Mishima, Yamamoto, '16]  
[Bobeth, Buras, Celis, Jung, '17]

- SM + dim-6 eff. operators

$$\begin{aligned}\mathcal{L} &= \mathcal{L}_{\text{SM}} + \frac{c_L}{\Lambda^2} i(H^\dagger \overleftrightarrow{D}_\mu H)(\bar{Q}_L \gamma^\mu Q'_L) + \frac{c_R}{\Lambda^2} i(H^\dagger \overleftrightarrow{D}_\mu H)(\bar{d}_R \gamma^\mu d'_R), \\ &= \mathcal{L}_{\text{SM}} - \frac{\sqrt{2}vM_Z}{\Lambda^2} (c_L \bar{s} \gamma^\mu Z_\mu P_L d + c_R \bar{s} \gamma^\mu Z_\mu P_R d) + \dots\end{aligned}$$

→ modified Z-couplings (FCNC) emerge

- Constraint comes from  $\Delta S=2$  process :  $\epsilon_K$  ( Assumption: NP  $\Delta S=2$  (sd)<sup>2</sup> operator is suppressed )

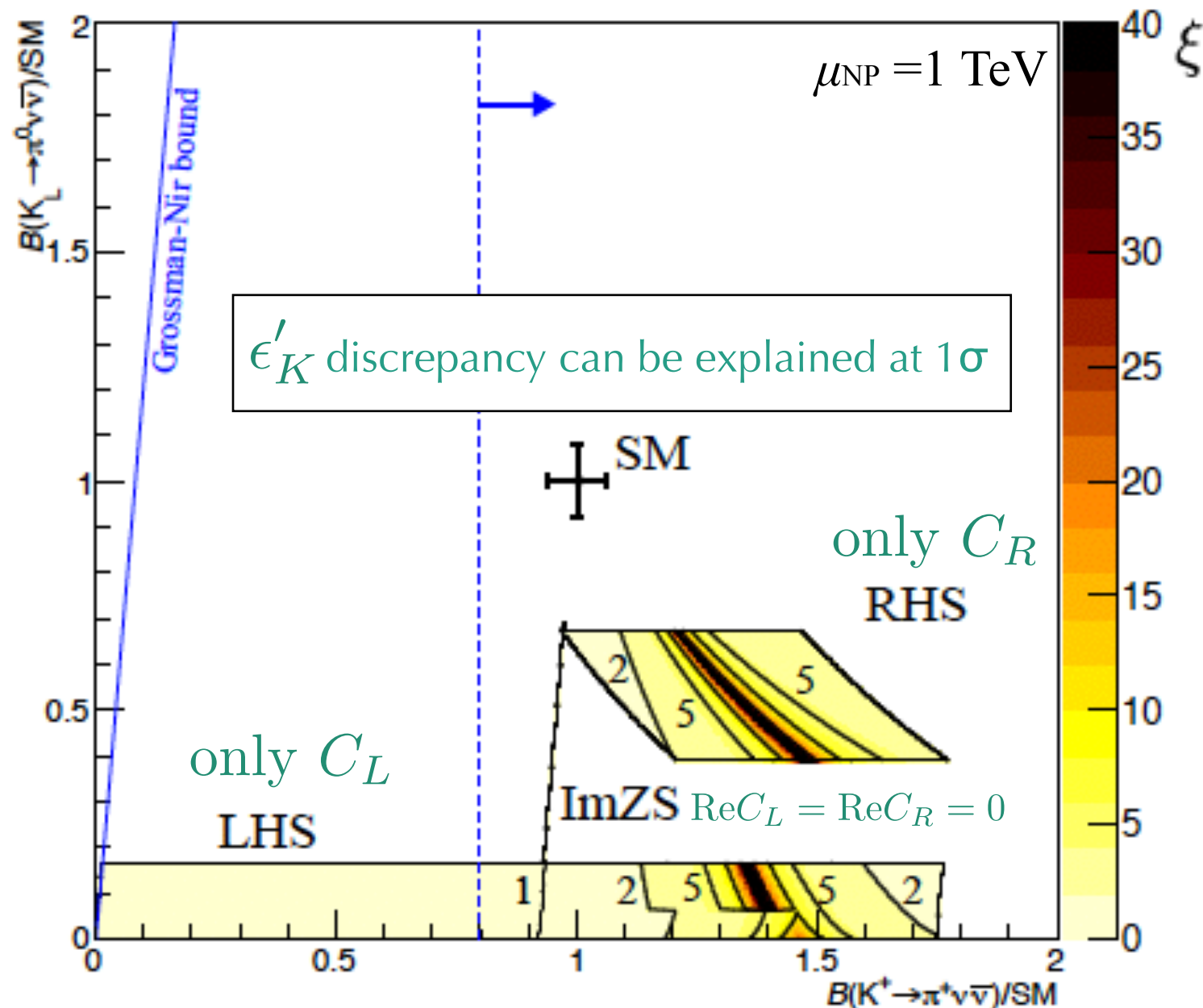


we included these contributions: **Novel point**

# $B(K \rightarrow \pi \nu \bar{\nu})$

## Result of simplified case

constraint comes from  $\epsilon_K$ ,  $\Delta M_K$ ,  $\mathcal{B}(K_L \rightarrow \mu^+ \mu^-)$



[Endo, TK, Mishima, Yamamoto, '16]

- The interference contributions are crucial, especially in right-handed scenario (RHS)
- $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})$  is smaller than the SM prediction
- .....
- $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})$  can be enhanced by **overshooting**  $\epsilon'_K$  from  $C_R$  + **destructive**  $\epsilon'_K$  from  $C_L$  case
- parameter tuning is required
- UV complete model would be implausible in light of the assumption
- : NP  $\Delta S=2$  (sd)<sup>2</sup> is negligible

# Summary

- RBC-UKQCD lattice group and the SM calculations of  $\epsilon'_K/\epsilon_K$  have revealed that the SM expected value deviates significantly from exp. data ( $2.8\sigma$ )
- In the SUSY, gluino box diagram with mass splitting of the right-handed squarks can contribute to  $\epsilon'_K/\epsilon_K$  significantly
  - Heavy gluino ( $M_3 > 1.5M_S$ ) can relax the constraint from  $\epsilon_K$
  - $\mathcal{B}(K \rightarrow \pi\nu\bar{\nu})$  data will test our scenario.  $\mathcal{B}(K_L \rightarrow \pi^0\nu\bar{\nu})$  can determine whether the right-handed up or down squark is the heavier one
- The modified Z-coupling scenario can also explain  $\epsilon'_K/\epsilon_K$  discrepancy with  $O(1)$  contribution to  $\mathcal{B}(K \rightarrow \pi\nu\bar{\nu})$ 
  - NA62 experiment  $\mathcal{B}(K^+ \rightarrow \pi^+\nu\bar{\nu})$  with **10% precision** (2018) could probe whether modified Z-coupling scenario is realized or not
  - KOTO experiment  $\mathcal{B}(K_L \rightarrow \pi^0\nu\bar{\nu})$  with **10% precision** can probe both SUSY and modified-Z coupling scenarios



# BACKUP

made by  
Philipp Frings





# Numerical results

- Wilson coefficients @  $\mu = 1.3$  GeV  $C_i(\mu) \equiv z_i(\mu) - \frac{V_{ts}^* V_{td}}{V_{us}^* V_{ud}} y_i(\mu)$  new results

| $i$              | $z_i(\mu)$ | $y_i(\mu)$ | $\mathcal{O}(1)$ | $\mathcal{O}(\alpha_{EM}/\alpha_s)$ | $\mathcal{O}(\alpha_s)$ | $\mathcal{O}(\alpha_{EM})$ | $\mathcal{O}(\alpha_{EM}^2/\alpha_s^2)$ |
|------------------|------------|------------|------------------|-------------------------------------|-------------------------|----------------------------|---|
| 1                | -0.3903    | 0          | 0                | 0                                   | 0                       | 0                          | 0                                       |
| 2                | 1.200      | 0          | 0                | 0                                   | 0                       | 0                          | 0                                       |
| 3                | 0.0044     | 0.0275     | 0.0254           | 0.0001                              | 0.0007                  | 0.0012                     | 0                                       |
| 4                | -0.0131    | -0.0566    | -0.0485          | -0.0002                             | -0.0069                 | -0.0009                    | 0                                       |
| 5                | 0.0039     | 0.0068     | 0.0124           | 0.0001                              | -0.0059                 | 0.0001                     | 0                                       |
| 6                | -0.0128    | -0.0847    | -0.0736          | -0.0003                             | -0.0099                 | -0.0008                    | 0                                       |
| $7/\alpha_{EM}$  | 0.0040     | -0.0321    | 0                | -0.1116                             | 0                       | 0.0760                     | 0.0035                                  |
| $8/\alpha_{EM}$  | 0.0019     | 0.1148     | 0                | -0.0227                             | 0                       | 0.1366                     | 0.0009                                  |
| $9/\alpha_{EM}$  | 0.0051     | -1.3815    | 0                | -0.1267                             | 0                       | -1.2581                    | 0.0034                                  |
| $10/\alpha_{EM}$ | -0.0013    | 0.4883     | 0                | 0.0217                              | 0                       | 0.4672                     | -0.0006                                 |

- Hadronic matrix elements @  $\mu = 1.3$  GeV

| $i$ | $\langle Q_i(\mu) \rangle_0^{\text{MS-NDR}} (\text{GeV})^3$ | $i$ | $\langle Q_i(\mu) \rangle_2^{\text{MS-NDR}} (\text{GeV})^3$ |
|-----|---|-----|---|
| 1   | $-0.144 \pm 0.046$  | 1   | $0.01006 \pm 0.00002$                                       |
| 2   | $0.105 \pm 0.015$   | 2   | $0.01006 \pm 0.00002$                                       |
| 3   | $-0.040 \pm 0.068$  | 3   | —   |
| 4   | $0.210 \pm 0.069$   | 4   | —   |
| 5   | $-0.179 \pm 0.068$  | 5   | —   |
| 6   | $-0.338 \pm 0.121$  | 6   | —   |
| 7   | $0.154 \pm 0.065$   | 7   | $0.127 \pm 0.012$   |
| 8   | $1.540 \pm 0.372$   | 8   | $0.852 \pm 0.052$   |
| 9   | $-0.197 \pm 0.070$  | 9   | $0.01509 \pm 0.00003$                                       |
| 10  | $0.053 \pm 0.038$   | 10  | $0.01509 \pm 0.00003$                                       |

RBC-UKQCD lattice simulation  
calculated them at  $\mu=1.5\text{GeV}(I=0)$   
and  $\mu=3.0\text{GeV}(I=2)$  with 2+1F

We exploit CP-conserving  
data (with  $z_i$ ) to reduce hadronic  
uncertainties

[TK, Nierste, Tremper, JHEP '16]

# Overview of effective models

- Chiral perturbation theory

- Effective theory of the QCD Goldstone bosons:  $\Phi = \begin{pmatrix} \sqrt{\frac{1}{2}}\pi^0 + \sqrt{\frac{1}{6}}\eta & \pi^+ & K^+ \\ \pi^- & -\sqrt{\frac{1}{2}}\pi^0 + \sqrt{\frac{1}{6}}\eta & K^0 \\ K^- & \bar{K}^0 & -\sqrt{\frac{2}{3}}\eta \end{pmatrix}$

$$\mathcal{L} = -\frac{G_F}{\sqrt{2}} V_{ud} V_{us}^* \left( g_8 f^4 \text{tr}(\lambda L_\mu L^\mu) + g_{27} f^4 \left( L_{\mu 23} L_{11}^\mu + \frac{2}{3} L_{\mu 21} L_{13}^\mu \right) + \mathcal{O}(g_E W) \right)$$

with  $L_\mu = -iU^\dagger D_\mu U$   $U = \exp\left(i\frac{\sqrt{2}\Phi}{f}\right)$

- dual QCD method [\[Bardeen, Buras, Gerard, '87, '14\]](#)

- Effective theory of the truncated pseudo-scalar and vector mesons:

$$\mathcal{L} = \frac{f^2}{4} \text{tr}(\partial_\mu U \partial^\mu U^\dagger) - \frac{1}{4} \text{tr}(V_{\mu\nu} V^{\mu\nu}) - \frac{f^2}{2} \text{tr}(\partial_\mu \xi^\dagger \xi + \partial_\mu \xi \xi^\dagger - 2igV_\mu)^2 \quad \text{with} \quad U = \xi \xi$$

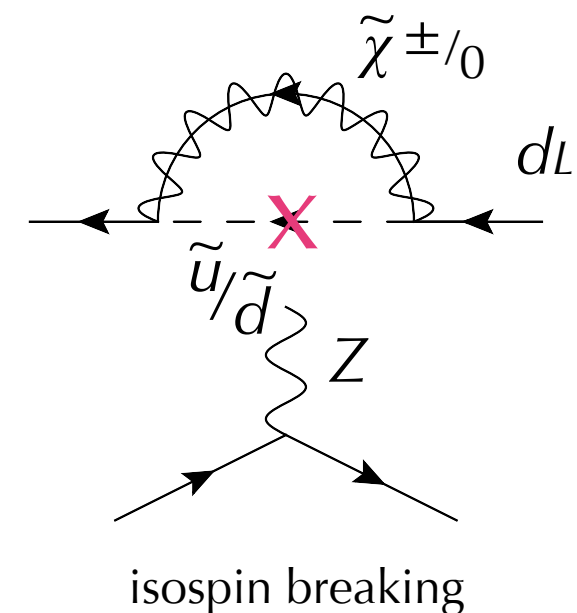
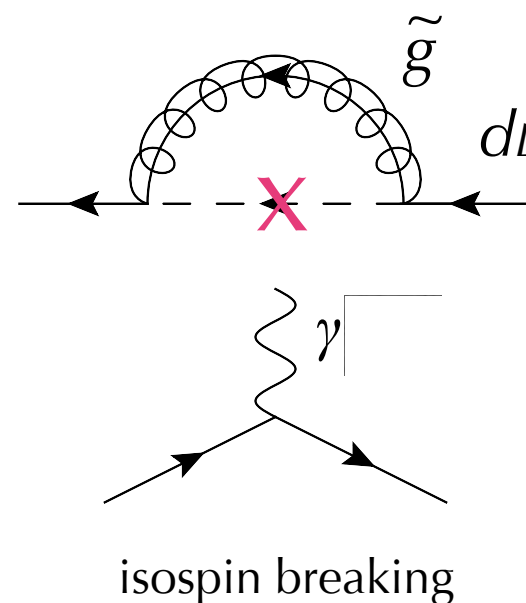
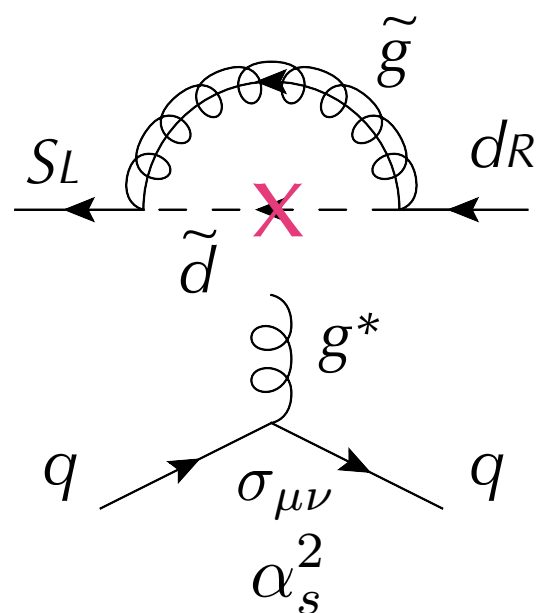
- Chiral quark model

- Mean-field approximation of the full extended NJL model

$$\mathcal{L} = \mathcal{L}_{QCD} - M (\bar{q}_R U q_L + \bar{q}_L U^\dagger q_R)$$

# Sub leading contributions

- Gluino chromomagnetic penguin operator can give subleading contribution, but there is no reliable results for hadronic matrix element  
[Buras,Colangelo,Ishidori,Romanino,Silvestrini, '00 ]
- Gluino photon-penguin breaks isospin sym. explicitly, but is suppressed by  $\alpha/\alpha_s$   
[Langacker,Sathiapalan, '84,Grossman,Worah, '97,Abel,Cottingham,Whittingham, '98]
- Z-penguin contribution needs to break the EW sym. like  $\mathcal{L}_{\text{eff}} = \frac{\lambda_{ij}}{M^2} |H|^2 \bar{d}_i \not{D} d_j$ ,  
Hence, chargino Z-penguin contribution is always larger than gluino Z-penguin  
[Colangelo,Ishidori, '98@ $K \rightarrow \pi \nu \nu$  ]



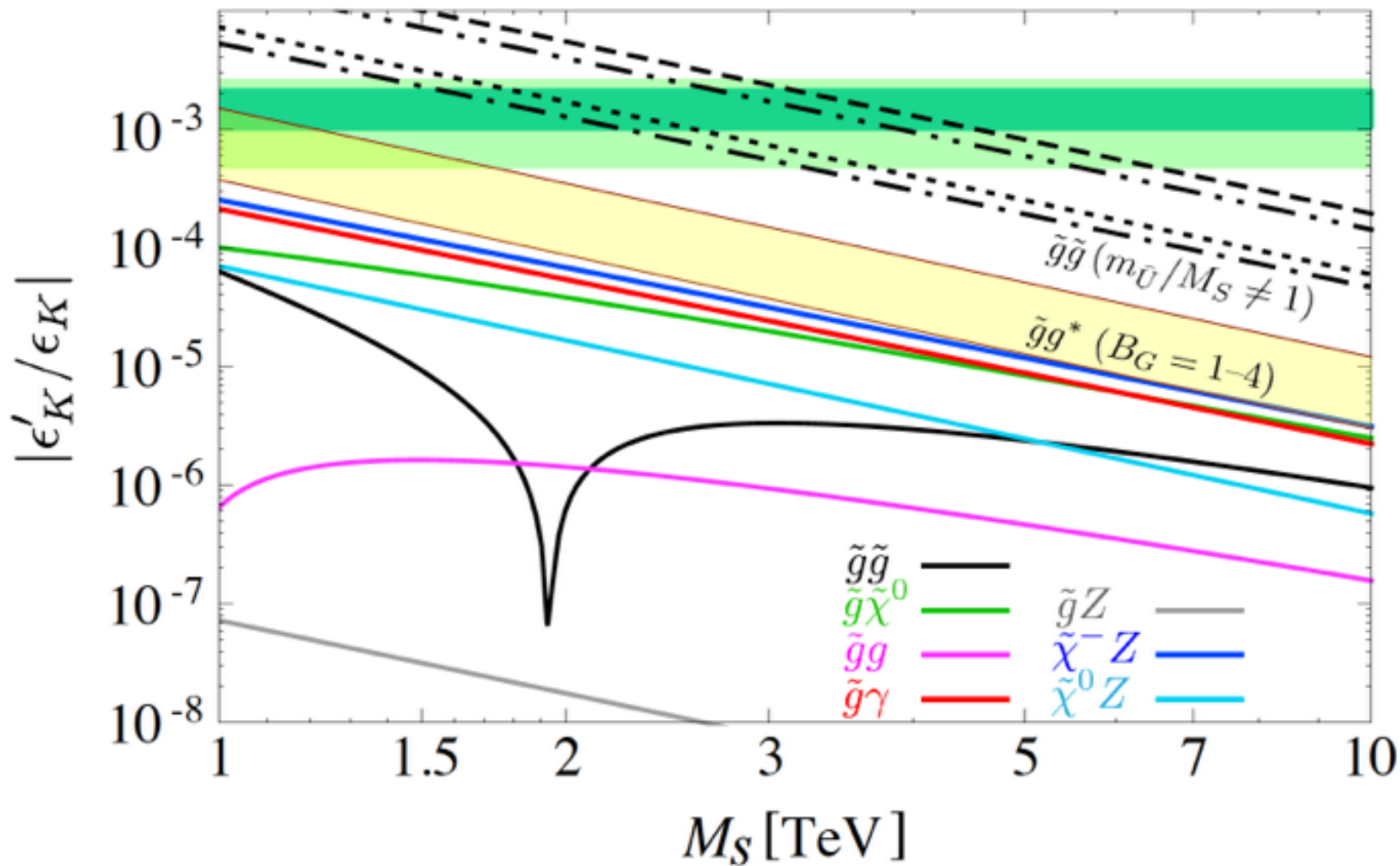
# SUSY contributions to $\epsilon'_K/\epsilon_K$

$\epsilon'_K/\epsilon_K$  discrepancy  
can be solved at

1σ

 $2\sigma$ 

[TK, Nierste, Tremper, PRL, '16]



$$M_3 = 1.5M_S$$

for suppressed  $\epsilon_K$

$$m_{Q,ij}^2 = \Delta_{Q,ij} M_S^2$$

$$\Delta_{Q,12,13,23} = 0.1 \exp(-i\pi/4)$$

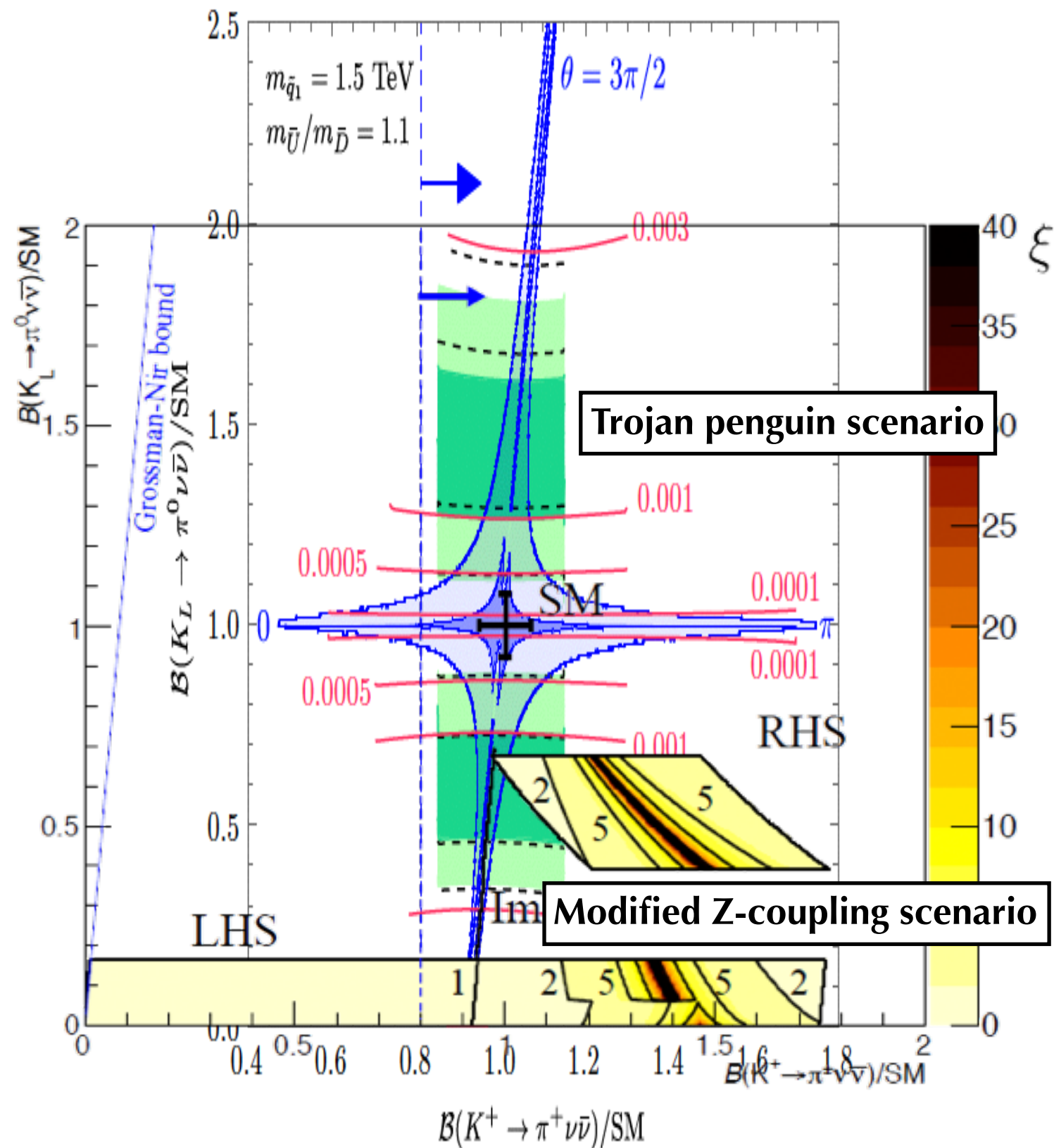
maximum CPV phase  
for  $\epsilon_K$

when  $i\pi/4 \rightarrow i\pi/2$

amplifies  $\epsilon'_K / \epsilon_K$

suppresses  $\epsilon_K$





- NA62 experiment  $\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$  with **10% precision** (2018) could probe whether modified Z-coupling scenario is realized or not
- KOTO experiment  $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})$  with **10% precision** can probe both Trojan penguin and modified-Z coupling scenario