

Low temperature electroweak phase transition with hidden scale invariance

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ARC Centre of Excellence for
Particle Physics at the Terascale

S. Arunasalam, A. Kobakhidze, CL, S. Liang, A. Zhou, PLB 776 (2018) 48-53

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This talk: a study of the **electroweak phase transition** in an extension of the Standard Model with **classical scale invariance**.

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 - Standard Model Higgs potential at UV scale Λ

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- spontaneously broken scale invariance manifests through **dilaton field** χ

$$\begin{aligned}\Lambda &\rightarrow \Lambda \frac{\chi}{f_\chi} \equiv \alpha\chi \\ v_{ew}^2(\Lambda) &\rightarrow \frac{v_{ew}^2(\alpha\chi)}{f_\chi^2} \chi^2 \equiv \frac{\xi(\alpha\chi)}{2} \chi^2 \\ V_0(\Lambda) &\rightarrow \frac{V_0(\alpha\chi)}{f_\chi^4} \chi^4 \equiv \frac{\rho(\alpha\chi)}{4} \chi^4\end{aligned}$$

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We get an effective scale invariant potential:

$$V(\Phi^\dagger\Phi, \chi) = \lambda(\alpha\chi) \left[\Phi^\dagger\Phi - \frac{\xi(\alpha\chi)}{2} \chi^2 \right]^2 + \frac{\rho(\alpha\chi)}{4} \chi^4$$

Hierarchy and light dilaton

- Scale invariance is broken by quantum effects:

$$\lambda^{(i)}(\alpha\chi) = \lambda^{(i)}(\mu) + \beta_{\lambda^{(i)}}(\mu) \ln(\alpha\chi/\mu) + \beta'_{\lambda^{(i)}}(\mu) \ln^2(\alpha\chi/\mu) + \dots$$

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$$\left. \frac{\partial V}{\partial \chi} \right|_{\Phi=v_{ew}, \chi=v_\chi} = 0, \quad \left. \frac{\partial V}{\partial \Phi} \right|_{\Phi=v_{ew}, \chi=v_\chi} = 0, \quad V(v_{ew}, v_\chi) = 0$$

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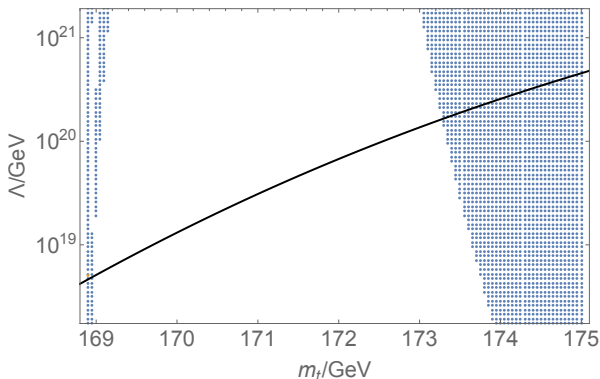
- Prediction of a **light dilaton**: $m_\chi^2 \simeq \frac{\beta'_\rho(v_\chi)}{4\xi(v_\chi)} v_{ew}^2 \quad \frac{m_\chi}{m_h} \sim \sqrt{\xi}$

Recovering the Standard Model at $\mu = v_{ew}$

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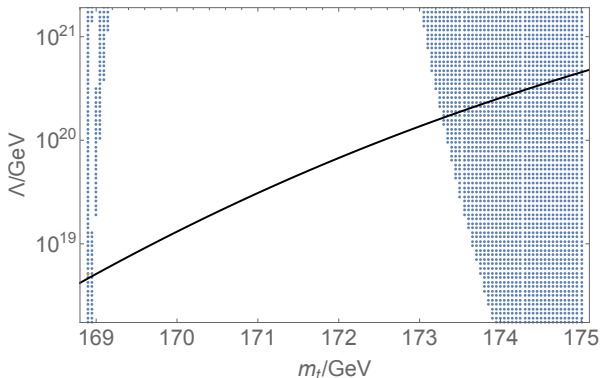
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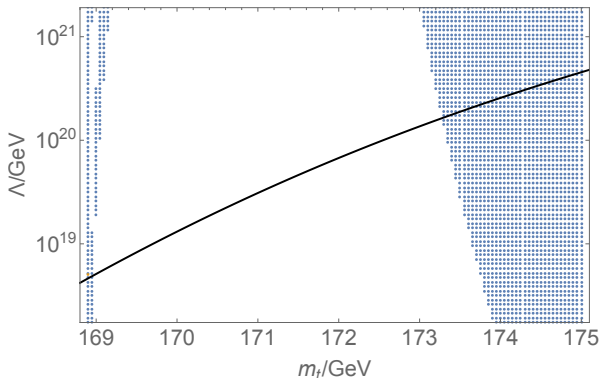
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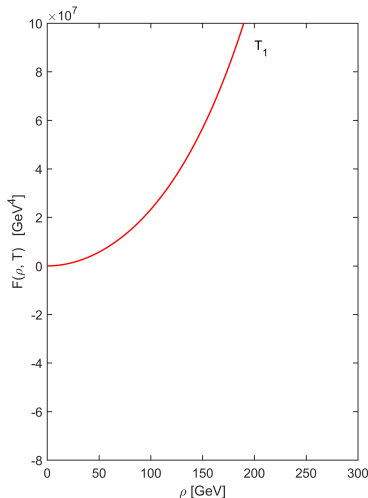
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Hot Big Bang scenario:

- early Universe \sim hot plasma (high T)
- scalar field(s) behaviour dictated by their free energy density $\mathcal{F}(\rho, T)$
- dynamics depend on the underlying particle physics model

2nd-order transition / crossover:

- smooth dynamics
- no particular signatures



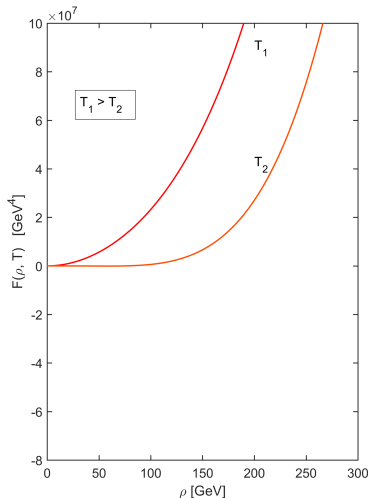
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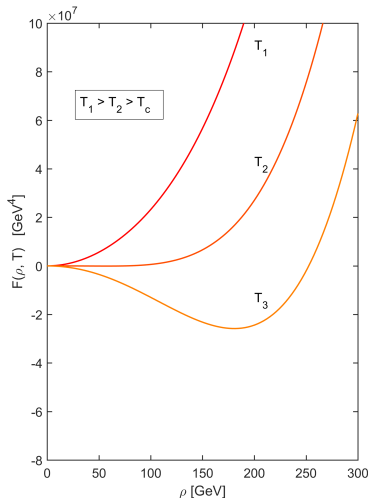
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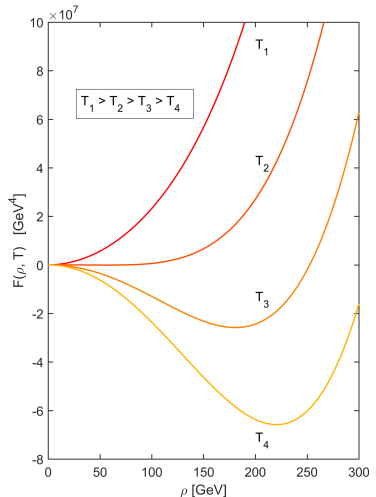
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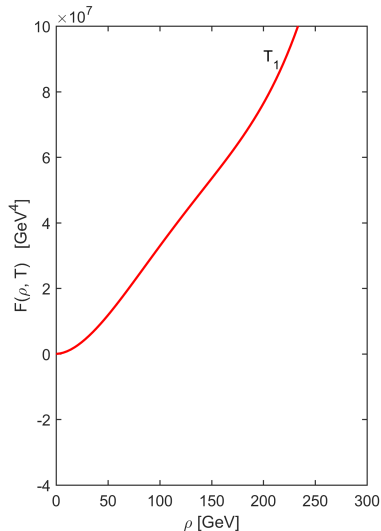
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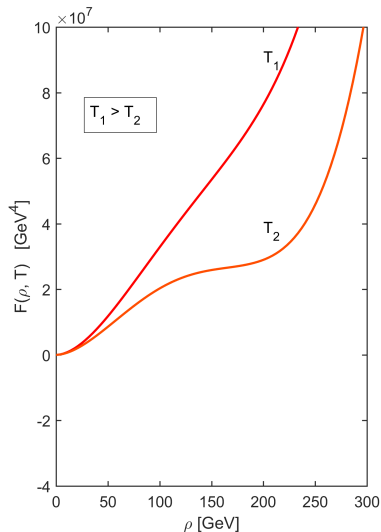
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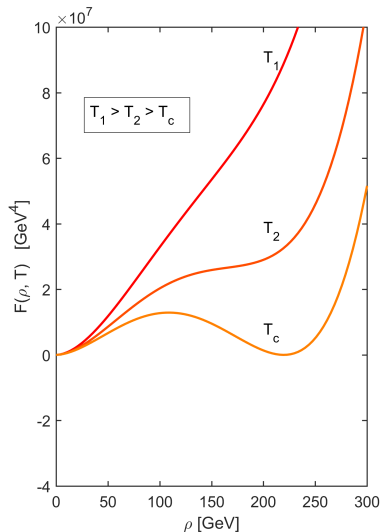
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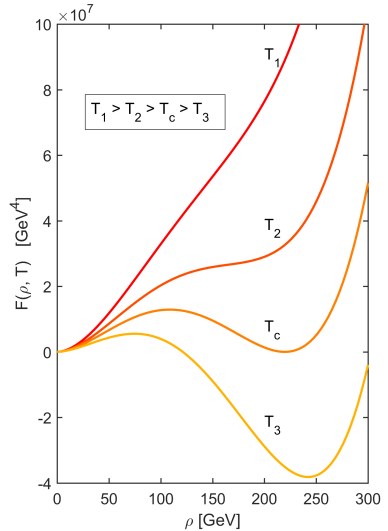
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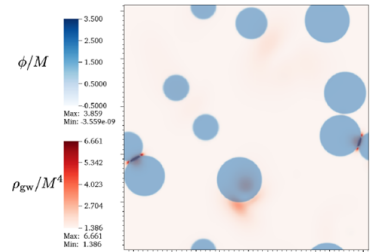
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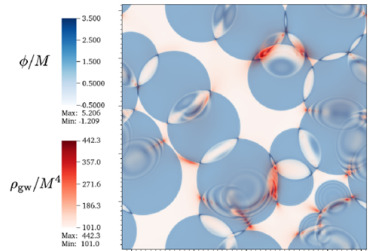
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(a) $t/R_* = 0.35$

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(b) $t/R_* = 0.66$

[D. Cutting, M. Hindmarsh, D. Weir, arXiv:1802.05712]

Electroweak and QCD phase transitions

In the Standard Model, both electroweak and QCD PTs are crossover

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- vacua are almost degenerate ⇒ no EWPT until $T \ll T_{EW}$

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See also: [E. Witten Nucl.Pys.B177 (1981) 477] [W. Buchmuller, D. Wyler, PLB 249 (1990) 281] [S. Iso et al., PRL 119 (2017) 141301] [B. von Harling, G. Servant, JHEP 1801 (2018) 159]

Thermal Higgs-dilaton potential + quark condensates

- Thermal contributions to the Higgs-dilaton potential \Rightarrow barrier along the flat direction:

$$V_T(h, \chi(h)) \approx AT^4 + \frac{1}{48} \left[4\lambda(\Lambda) + 6y_t^2(\Lambda) + \frac{9}{2}g^2(\Lambda) + \frac{3}{2}g'^2(\Lambda) \right] h^2 T^2 + \dots$$

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$$\langle \bar{q}q \rangle_T = \langle \bar{q}q \rangle \left[1 - (N^2 - 1) \frac{T^2}{12Nf_\pi^2} - \frac{1}{2}(N^2 - 1) \left(\frac{T^2}{12Nf_\pi^2} \right)^2 + \dots \right]$$

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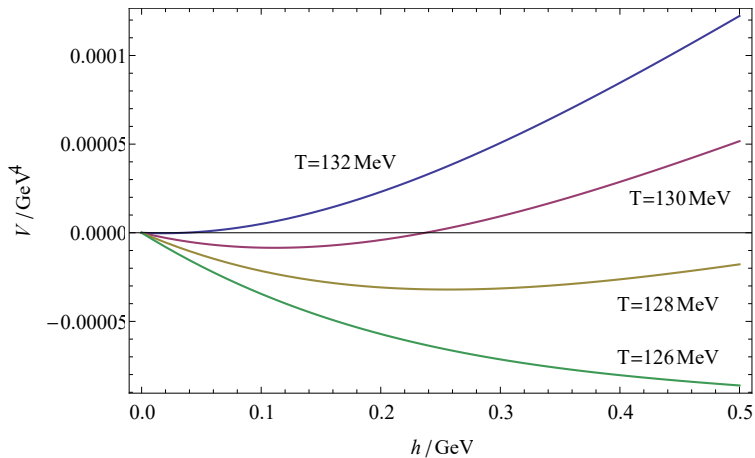
- This linear term **dominates over the barrier** for small enough T

Results and dynamics of the transitions

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- More refined analysis currently under investigation:
 - effective field theory for the Higgs, dilaton and pions
 - $U(6) \times U(6)$ linear sigma model for the pions

$$\mathcal{L} = \text{Tr} \left(\partial_\mu \varphi^\dagger \partial^\mu \varphi - m^2 \varphi^\dagger \varphi \right) - \lambda_1 \left[\text{Tr} \left(\varphi^\dagger \varphi \right) \right]^2 - \lambda_2 \text{Tr} \left(\varphi^\dagger \varphi \right)^2 + \mathcal{L}(\varphi, \phi, \chi)$$

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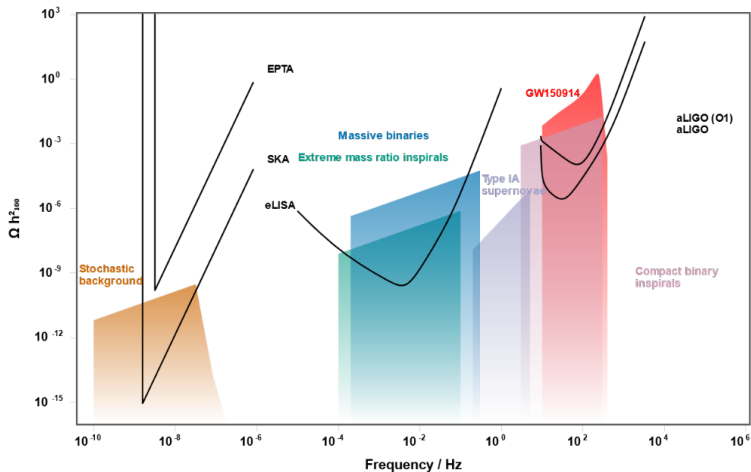
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- precise spectrum and amplitude of the background currently under computation

Gravitational Waves



[From rhcole.com/apps/GWplotter/]

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- Low energy effective formulation with a **dilaton field**
- Interesting predictions:
 - small dilaton mass: $m_\chi \approx 10^{-8}$ eV
 - **low temperature QCD-induced** electroweak transition
 - GW signal in the range of **Pulsar Timing Arrays**