

# Measurements of $\phi_1/\beta$

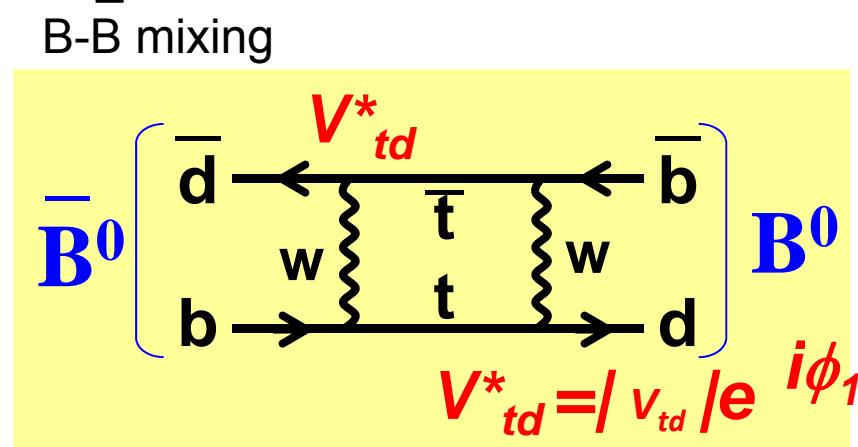
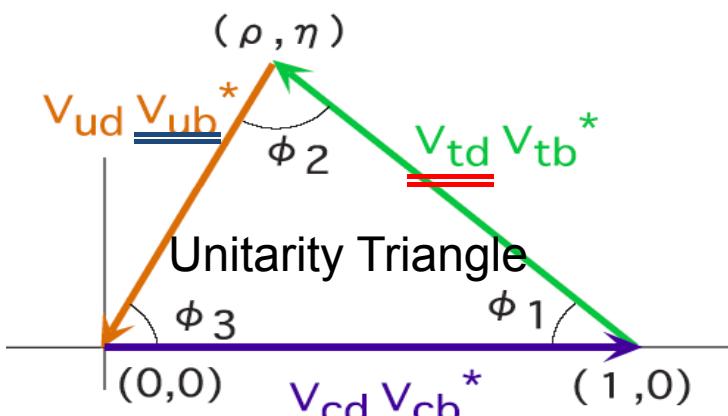
K. Sumisawa (KEK)

Flavor Physics and CP Violation 2010,  
May 25, 2010, Torino, Italy,

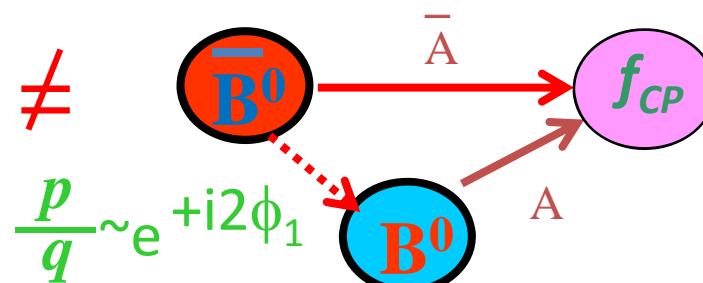
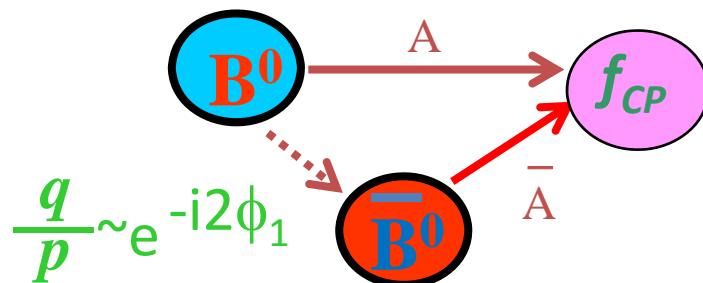
# Time-dependent CP Violation in $B^0$ decays

KM ansatz: CPV is due to a complex phase in the quark mixing matrix

$$V_{n=3} = \begin{pmatrix} V_{ud} & V_{us} & \underline{\overline{V_{ub}}} \\ V_{cd} & V_{cs} & \underline{\overline{V_{cb}}} \\ \underline{\overline{V_{td}}} & V_{ts} & V_{tb} \end{pmatrix} \simeq \begin{pmatrix} 1 - \lambda^2/2 & \lambda & \underline{\overline{\frac{A\lambda^3(\rho - i\eta)}{A\lambda^2}}} \\ -\lambda & 1 - \lambda^2/2 & \underline{\overline{-A\lambda^2}} \\ \underline{\overline{A\lambda^3(1 - \rho - i\eta)}} & -A\lambda^2 & 1 \end{pmatrix}$$



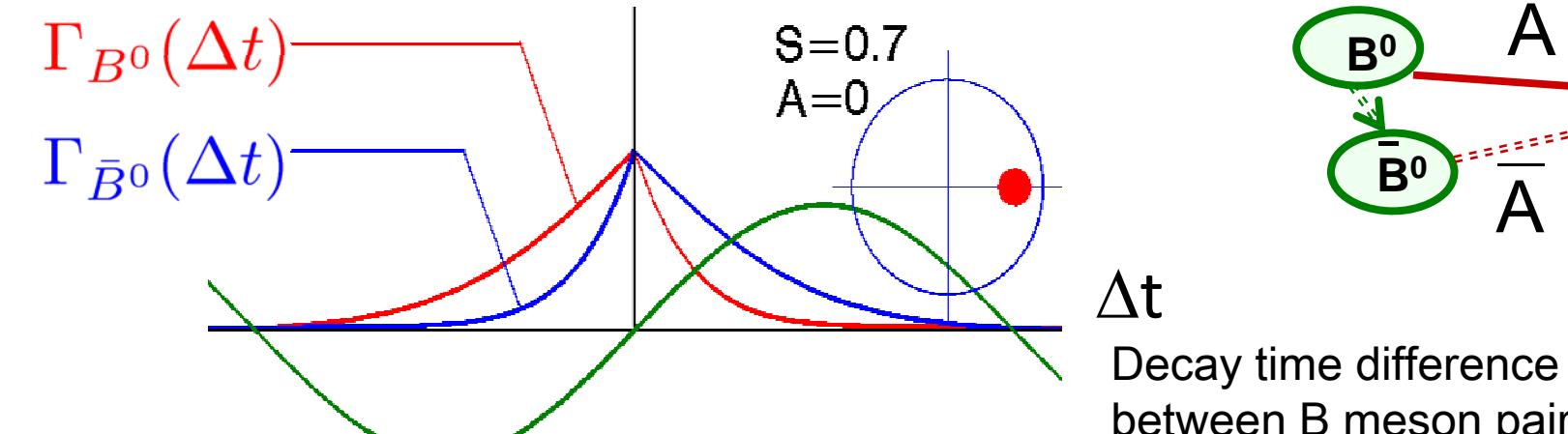
mixing induced CP violation



$\beta = \phi_1$
$\alpha = \phi_2$
$\gamma = \phi_3$

# Time-dependent CP Violation in $B^0$ decays

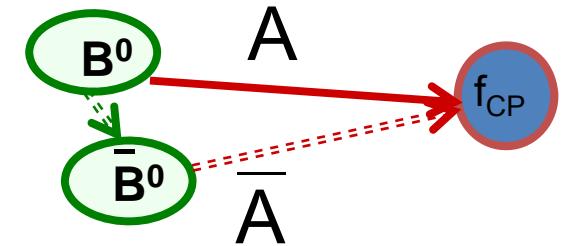
We can measure CPV (asym.) as a function of proper time diff ( $\Delta t$ ).



$$\begin{aligned} &\equiv \frac{\Gamma_{\bar{B}^0}(\Delta t) - \Gamma_{B^0}(\Delta t)}{\Gamma_{\bar{B}^0}(\Delta t) + \Gamma_{B^0}(\Delta t)} \\ &= S \sin \Delta m \Delta t + A \cos \Delta m \Delta t \end{aligned}$$

Mixing-induced CPV

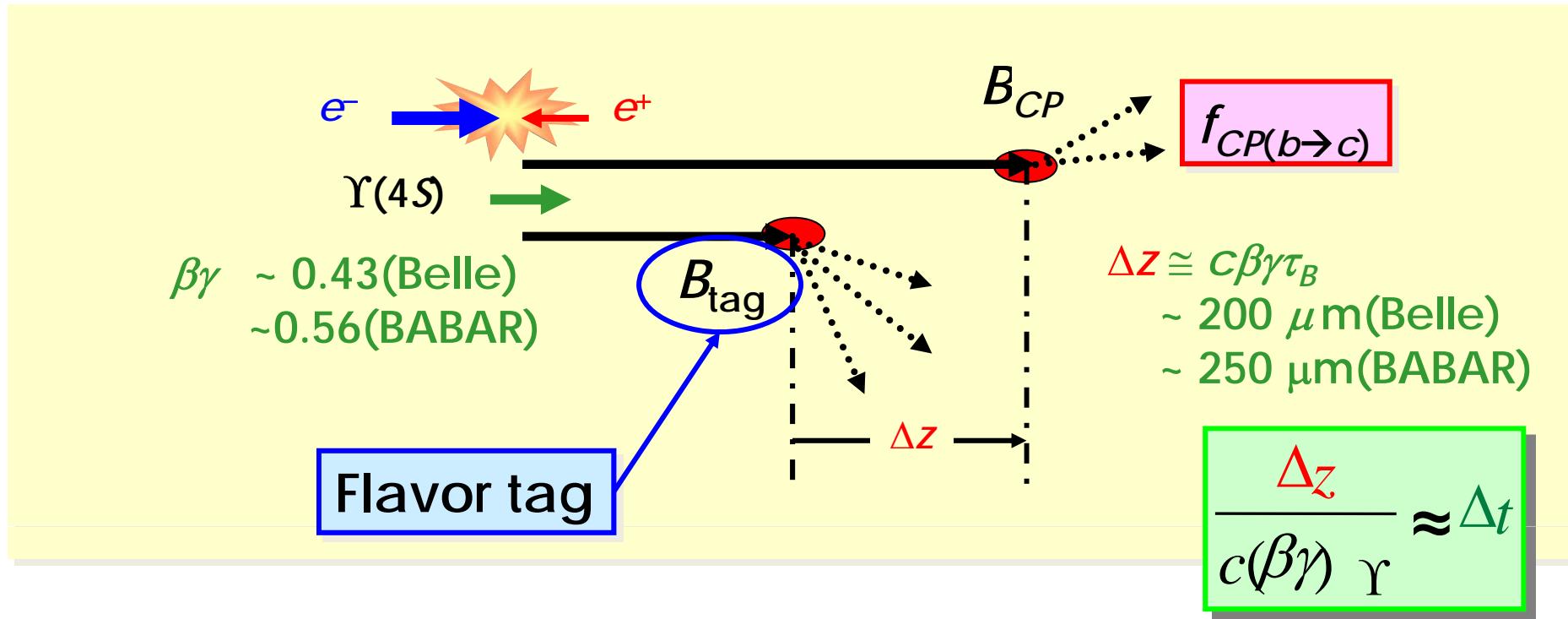
Direct CPV



e.g. for  $B^0 \rightarrow J/\psi K_s$   
 $S = -\xi_{CP} \sin 2\phi_1 = +\sin 2\phi_1$   
 $A \sim 0 \quad (A = -C)$   
 $(\xi_{CP} : \text{CP eigenvalue } \pm 1)$

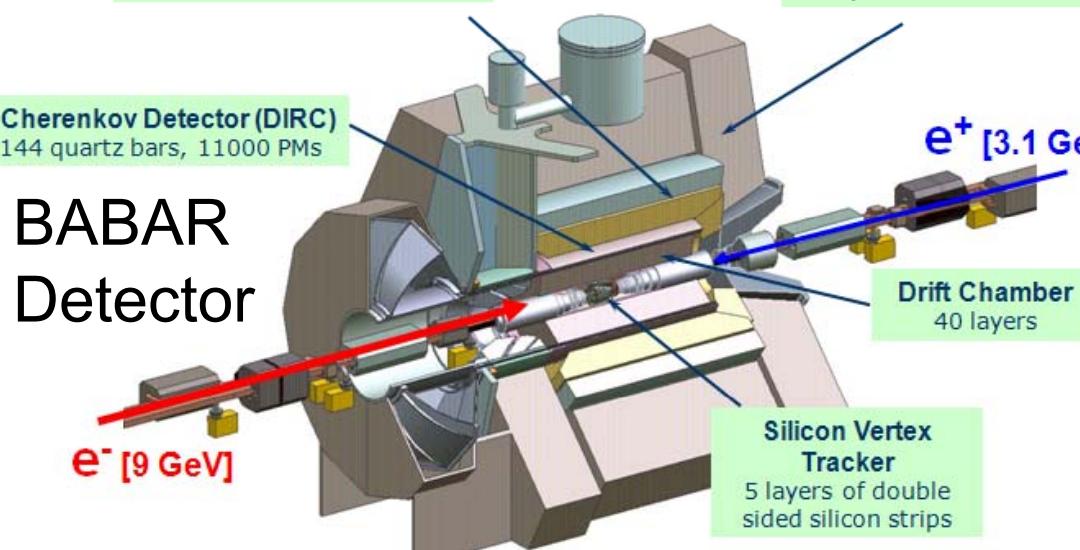
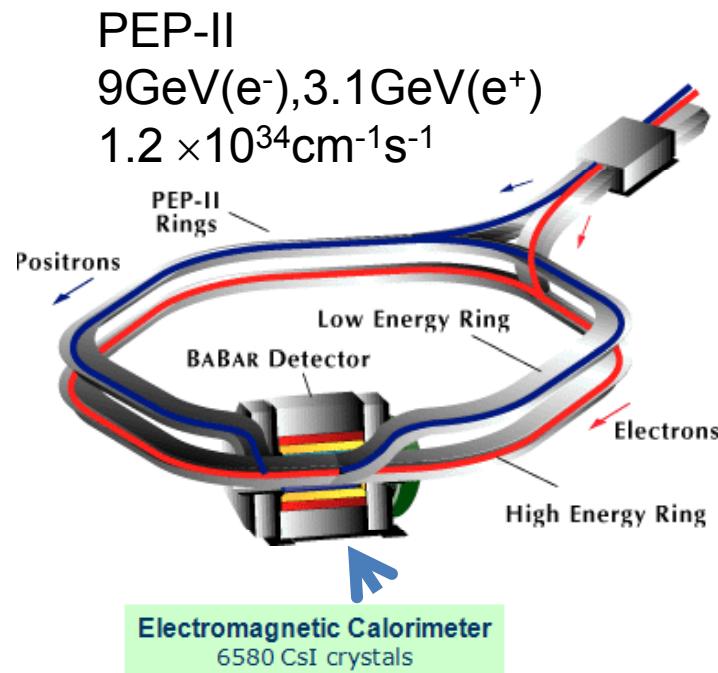
$$S = \frac{2 \operatorname{Im}(q/p \bar{A} A^*)}{|\bar{A}|^2 + |A|^2}, \quad A = \frac{|\bar{A}|^2 - |A|^2}{|\bar{A}|^2 + |A|^2}$$

# Principle of Measurement in B-factories

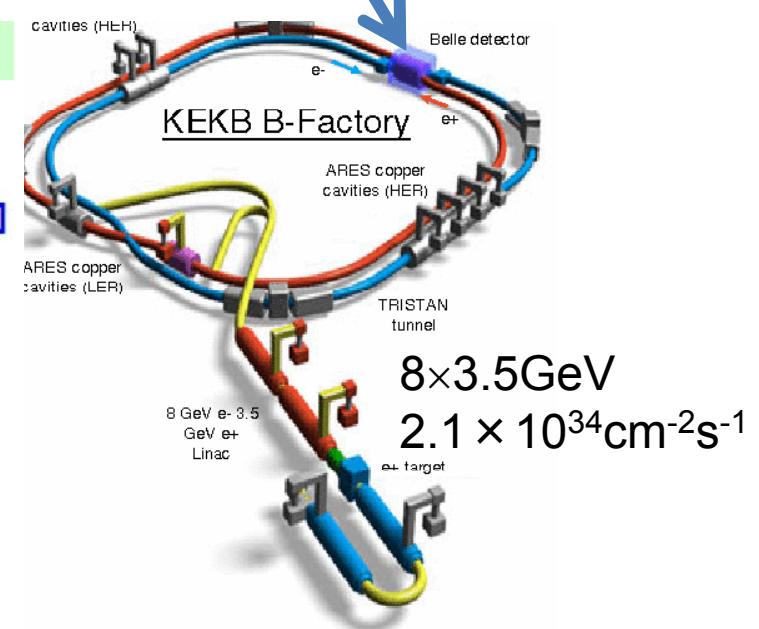
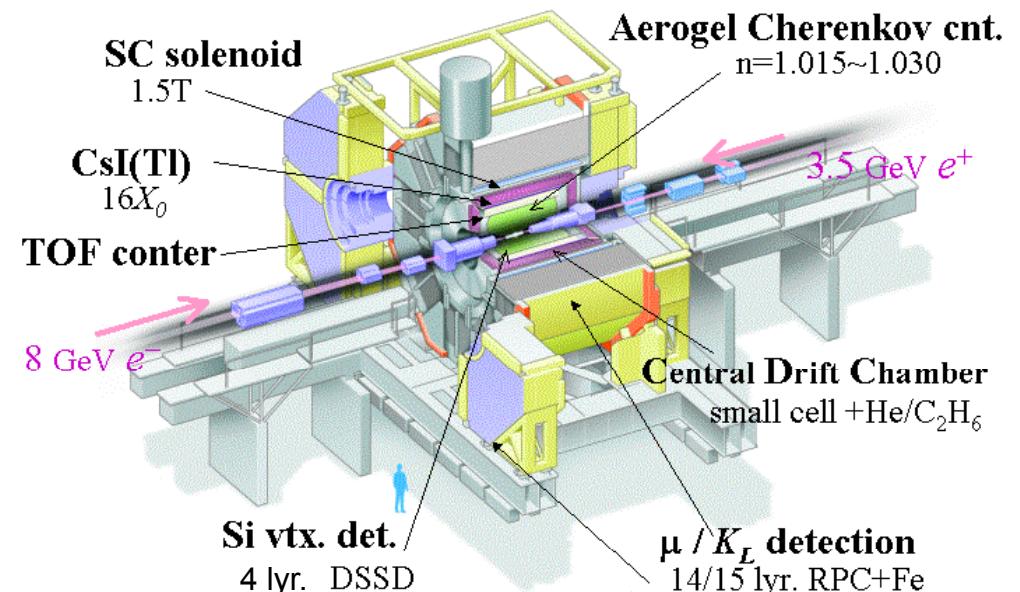


- Reconstruct  $B \rightarrow f_{CP(b \rightarrow c)}$  decays
- Measure proper-time difference:  $\Delta t$
- Determine flavor of  $B_{tag}$
- Evaluate  $CP$  asymmetry from  $\Delta t$  and flavor of  $B_{tag}$

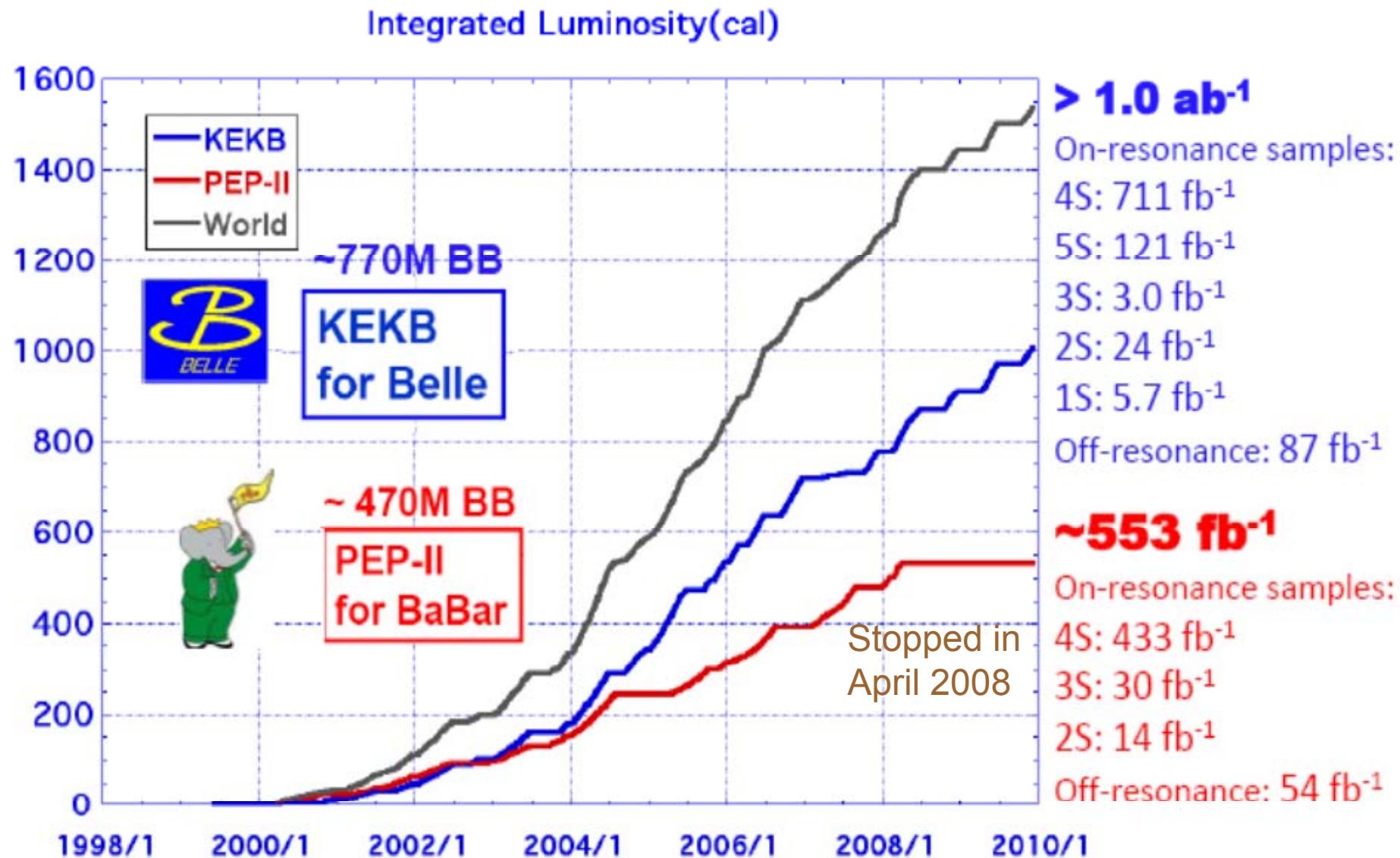
# 2 B-factories



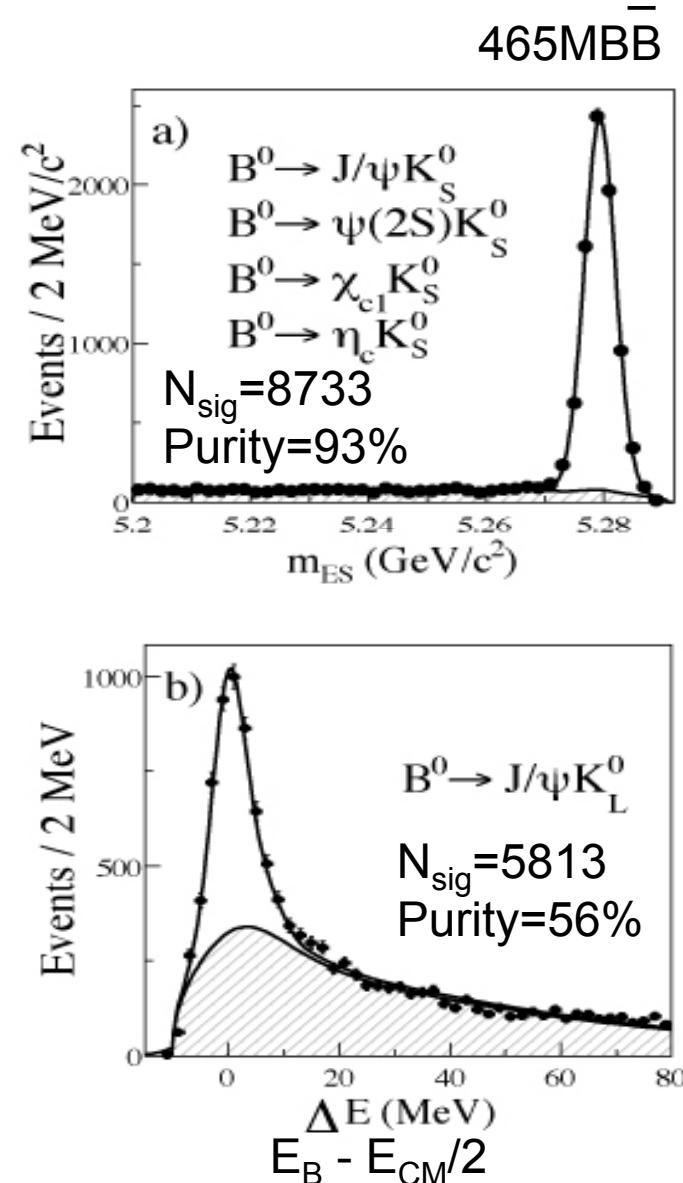
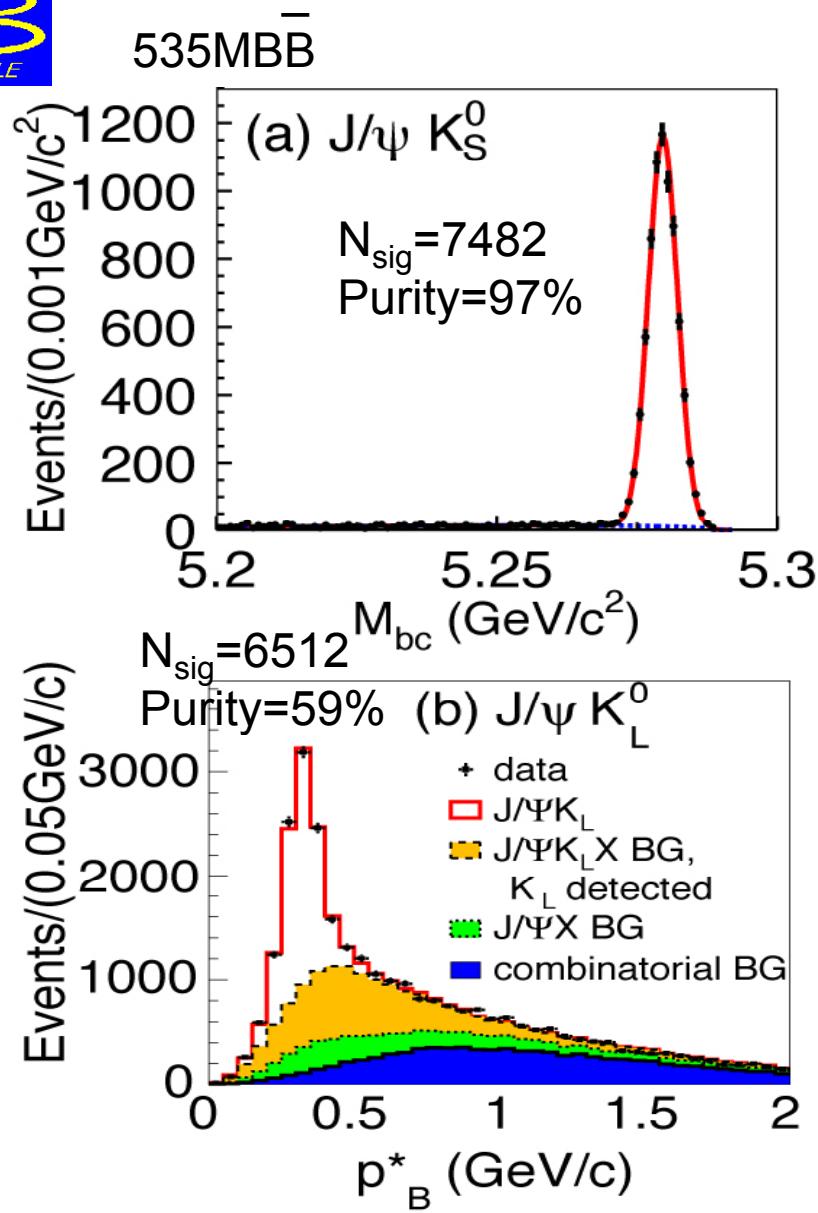
# Belle Detector



# Success of the B-factories

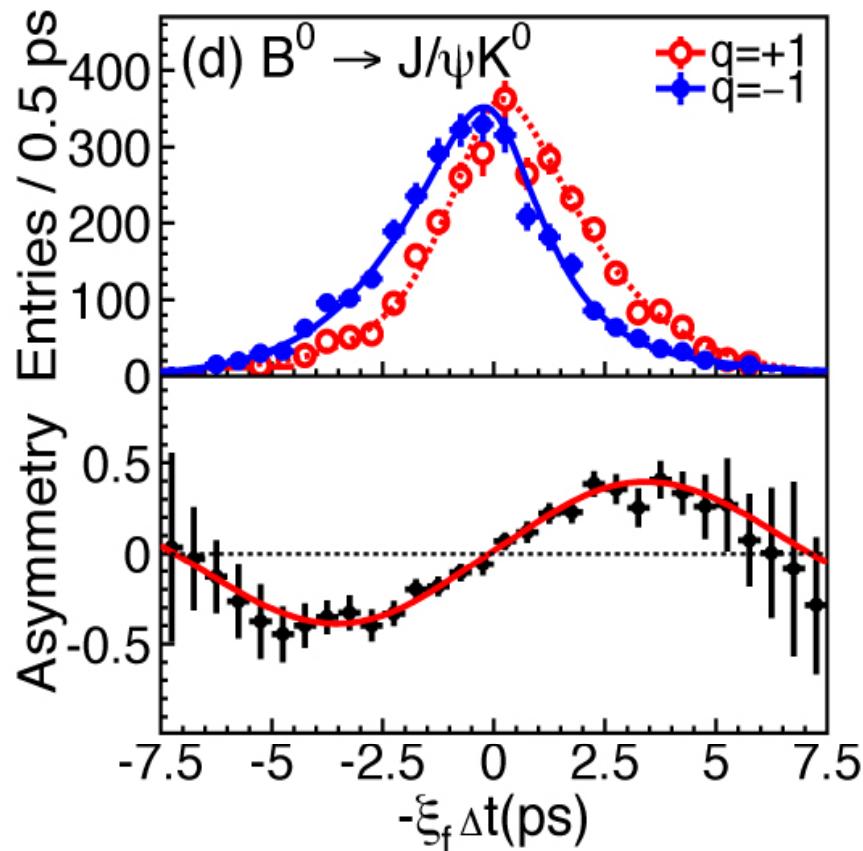


# $\sin 2\phi_1$ with charmonium $K^0$ modes

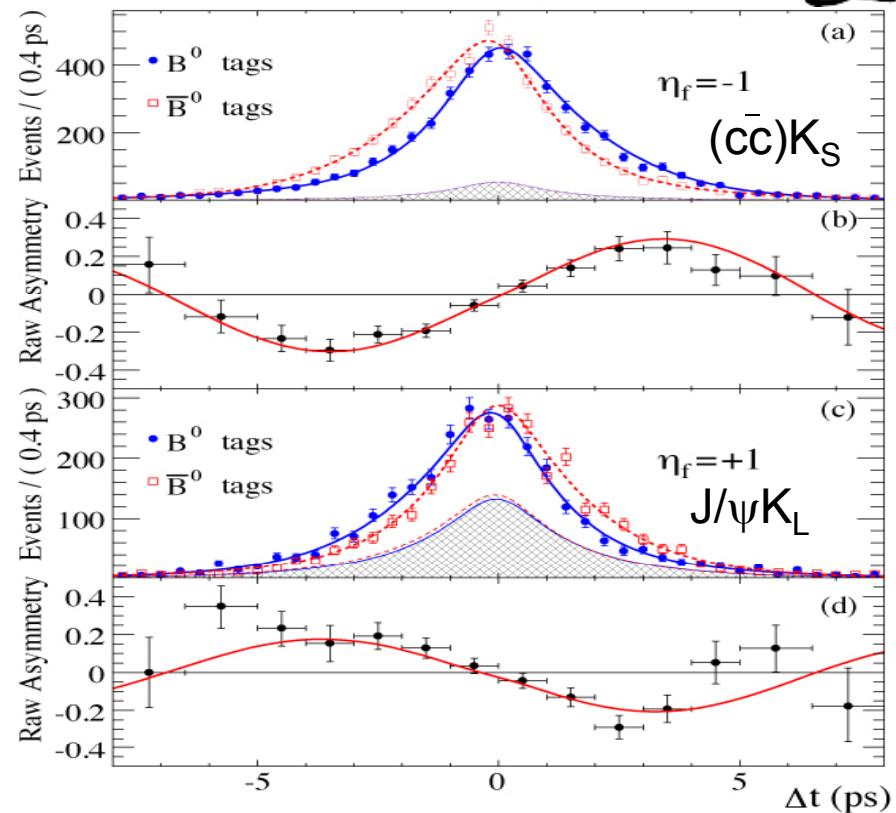




# $\sin 2\phi_1$ with charmonium $K^0$ modes



PRL98,031802(2007)

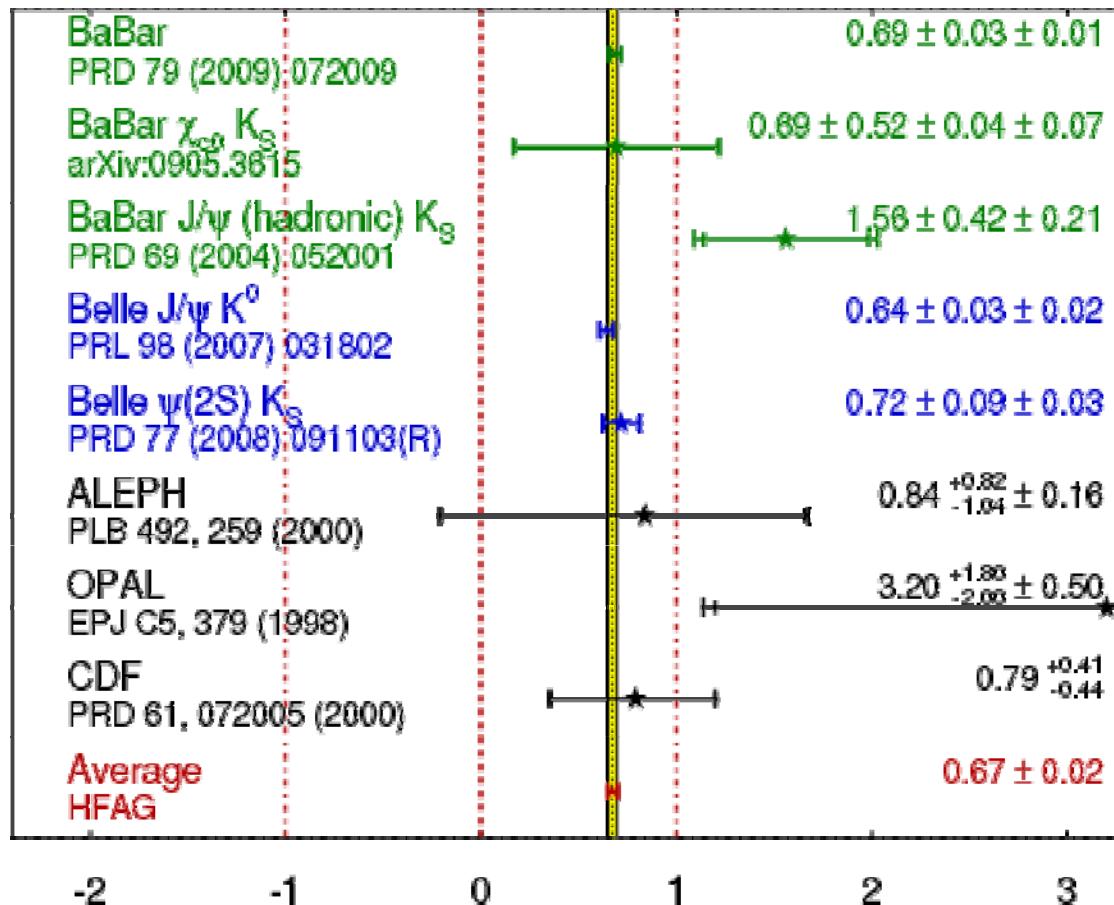


$$\begin{aligned}\sin 2\phi_1 &= 0.687 \pm 0.028 \pm 0.012 \\ A_f &= -0.024 \pm 0.020 \pm 0.016\end{aligned}$$

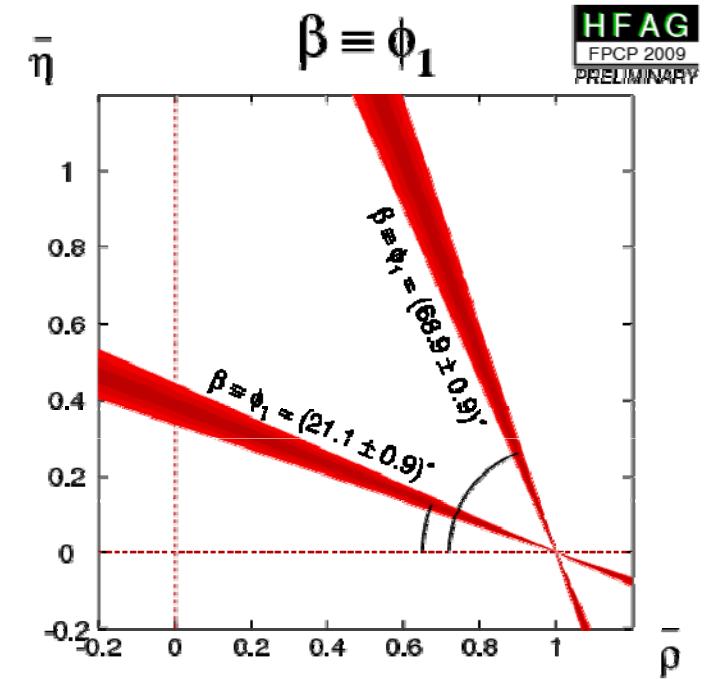
PRD79,072009(2009)

# $\sin 2\phi_1 \rightarrow \phi_1$

$\sin(2\beta) \equiv \sin(2\phi_1)$  **HFAG**  
FPCP 2009  
PRELIMINARY



agreement between two experiments



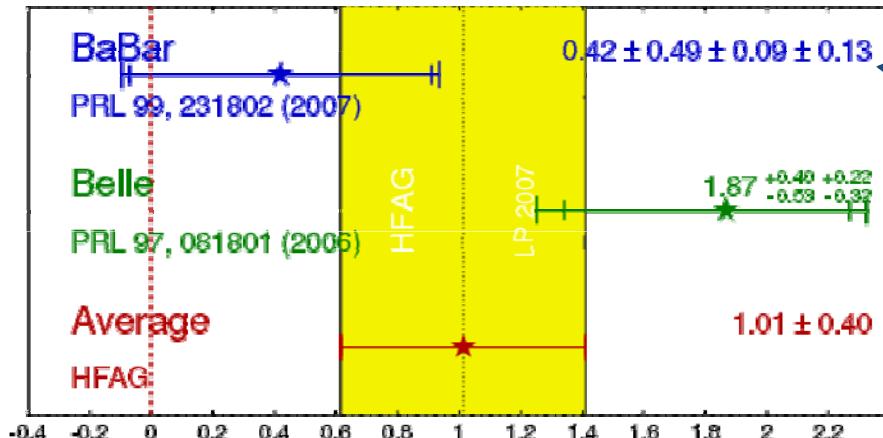
error in  $\phi_1 < 1^\circ$   
but ambiguities exist.

$$\bar{B^0} \rightarrow D[K_S \pi^+ \pi^-] h^0 \text{ (} h^0 = \pi^0, \omega, \eta \text{)}$$

Time dependent Dalitz analysis gives  $\sin 2\phi_1$  and  $\cos 2\phi_1$

$$S \propto \text{Im}(\exp(-2i\phi_1) \bar{A} A^*) = \text{Re}(\bar{A} A^*) \sin(2\phi_1) - \text{Im}(\bar{A} A^*) \cos(2\phi_1)$$

$D^{(*)} h^0 \cos(2\beta) \equiv \cos(2\phi_1)$  HFAG LP 2007 PRELIMINARY



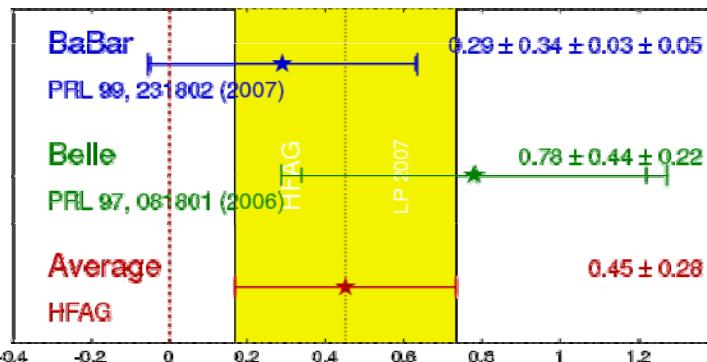
describe Dalitz variables.

$\cos 2\phi_1 > 0$  at 86% C.L.

$\cos 2\phi_1 > 0$  at 98.3% C.L.

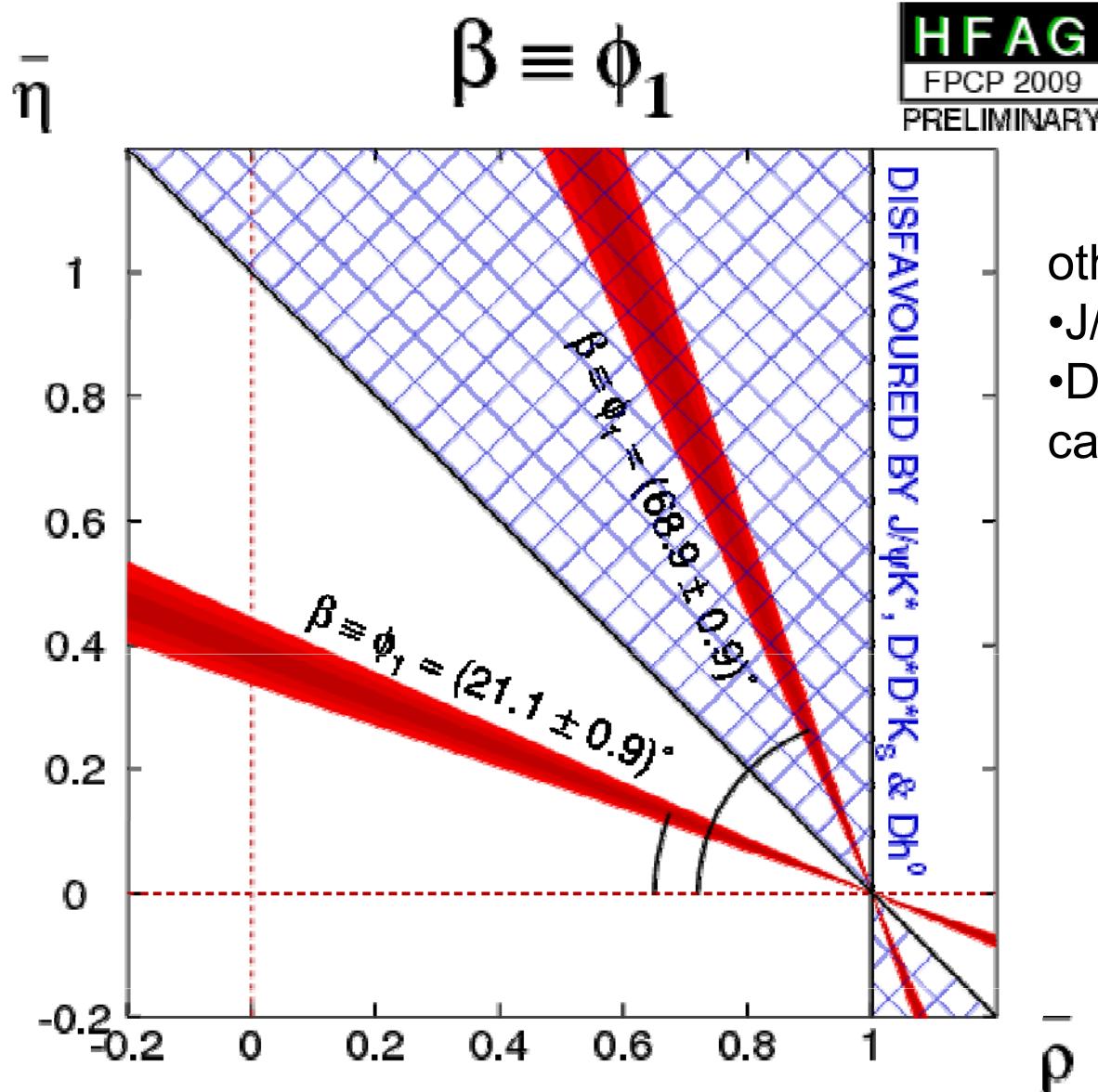
smaller  $\phi_1$  ( $< 45^\circ$ ) solution is favored.

$D^{(*)} h^0 \sin(2\beta) \equiv \sin(2\phi_1)$  HFAG LP 2007 PRELIMINARY



consistent with  $b \rightarrow c\bar{c}s \sin 2\phi_1$

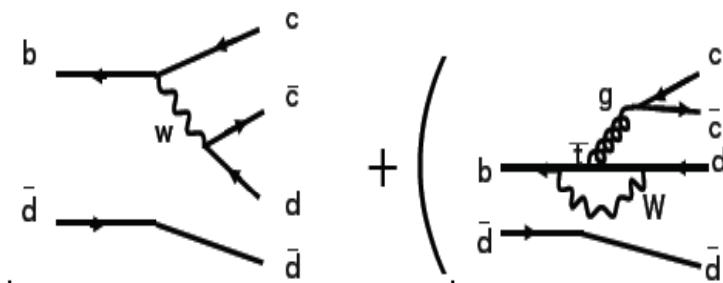
# constraint for $\phi_1/\beta$



# $b \rightarrow ccd$

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

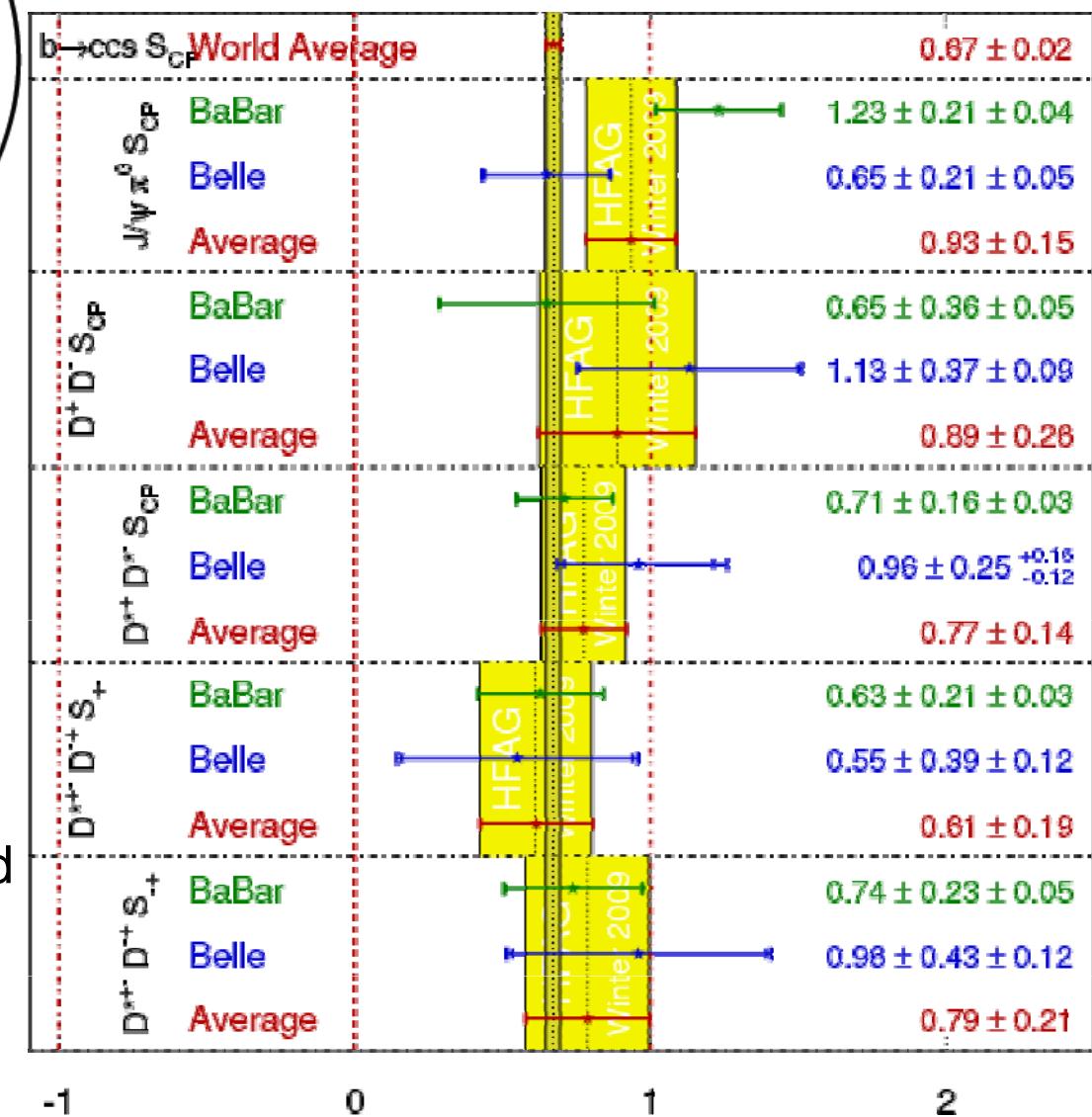
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tree + (penguin)

$J/\psi \pi^0$  :  
constrain penguin contribution  
in Golden mode( $J/\psi K^0$ )  
without model dependence.

$D^{(*)+} D^{(*)-}$  :  
penguin contribution is expected  
to be small.



$b \rightarrow ccd$

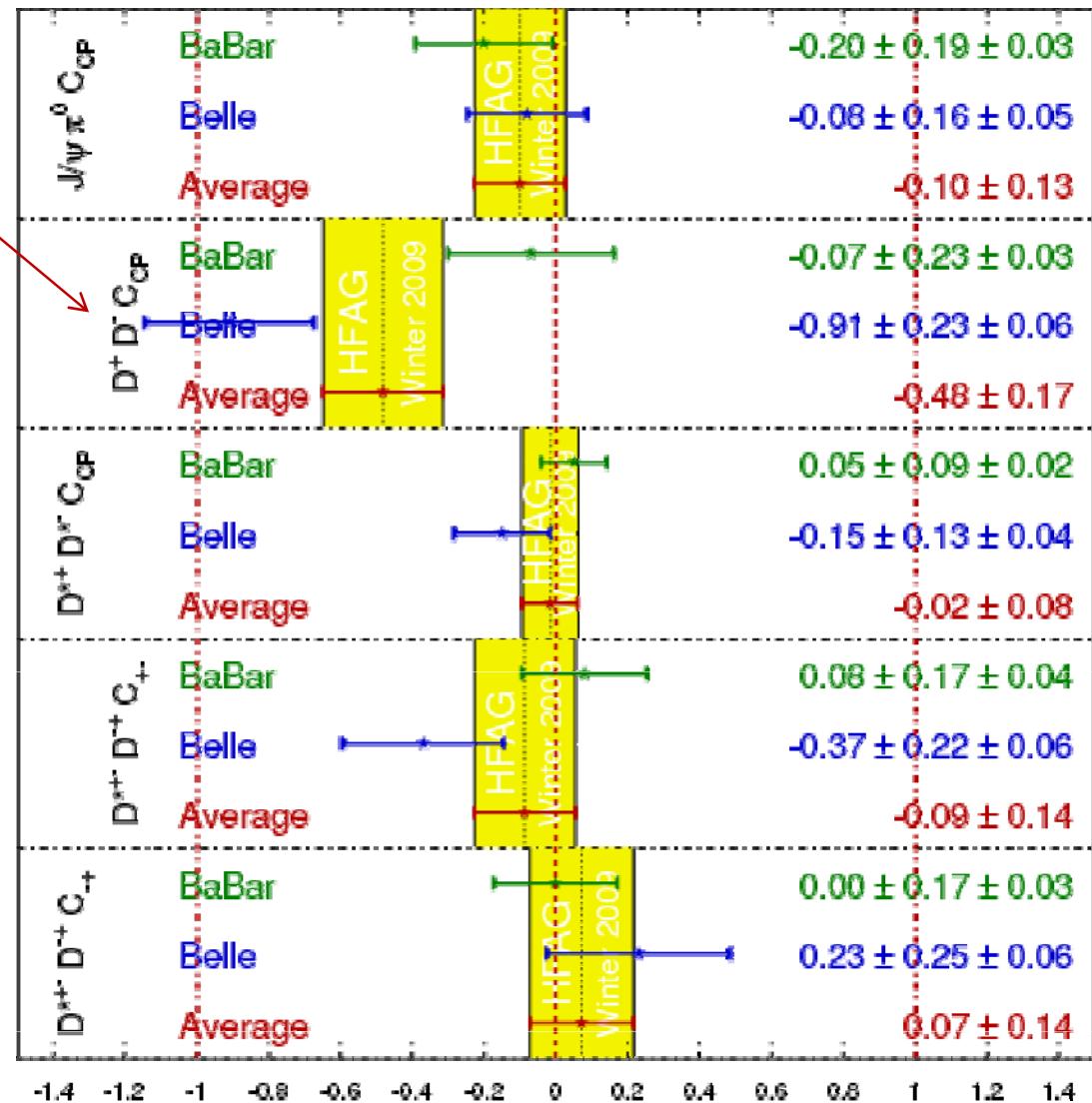
$$C_f = -A_f$$

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Winter 2009  
PRELIMINARY

Belle  
 $A = -C = 0.91 \pm 0.23 \pm 0.06$   
( $3.2\sigma$  significance  $A \neq 0$ )

$J/\psi \pi^0$  :  
constrain penguin contribution  
in Golden mode( $J/\psi K^0$ )  
without model dependence.

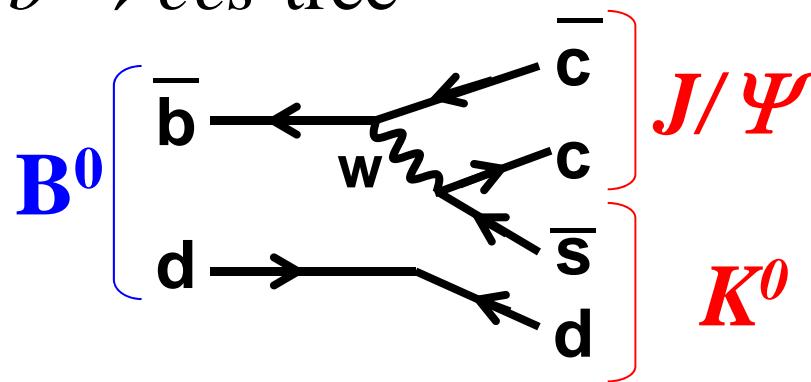
$D^{(*)+} D^{(*)-}$  :  
penguin contribution is expected  
to be small.



# $b \rightarrow sq\bar{q}$ TCPV

Time-Dependent  $CP$  asymmetry in  $B^0$  decays

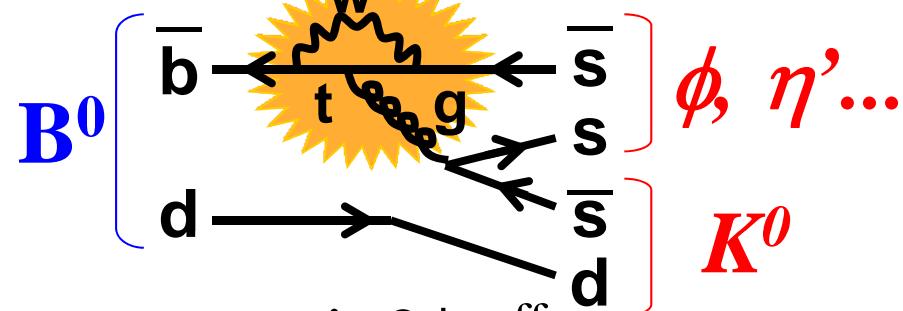
$b \rightarrow c\bar{c}s$  tree



$$S = \sin 2\phi_1$$

$$\mathcal{A} \sim 0$$

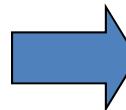
$b \rightarrow s\bar{q}\bar{q}$  penguin



$$S = \sin 2\phi_1^{\text{eff}}$$

$$\mathcal{A} \sim 0$$

Extra CPV phase from New Physics

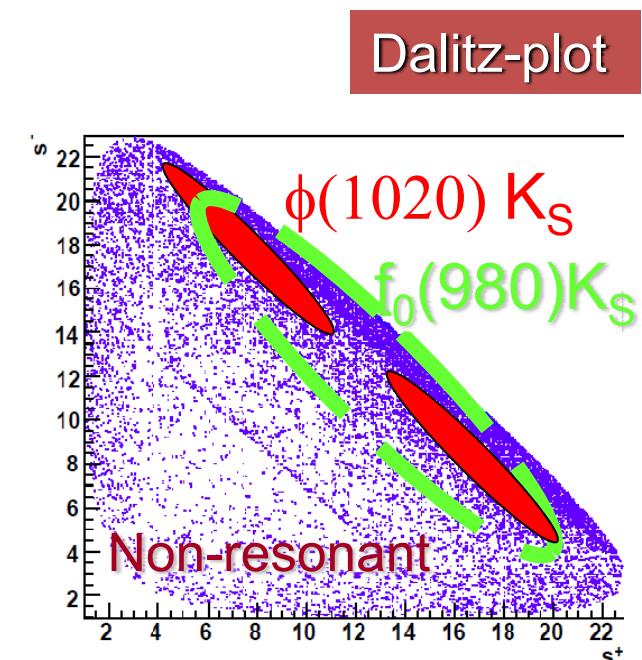
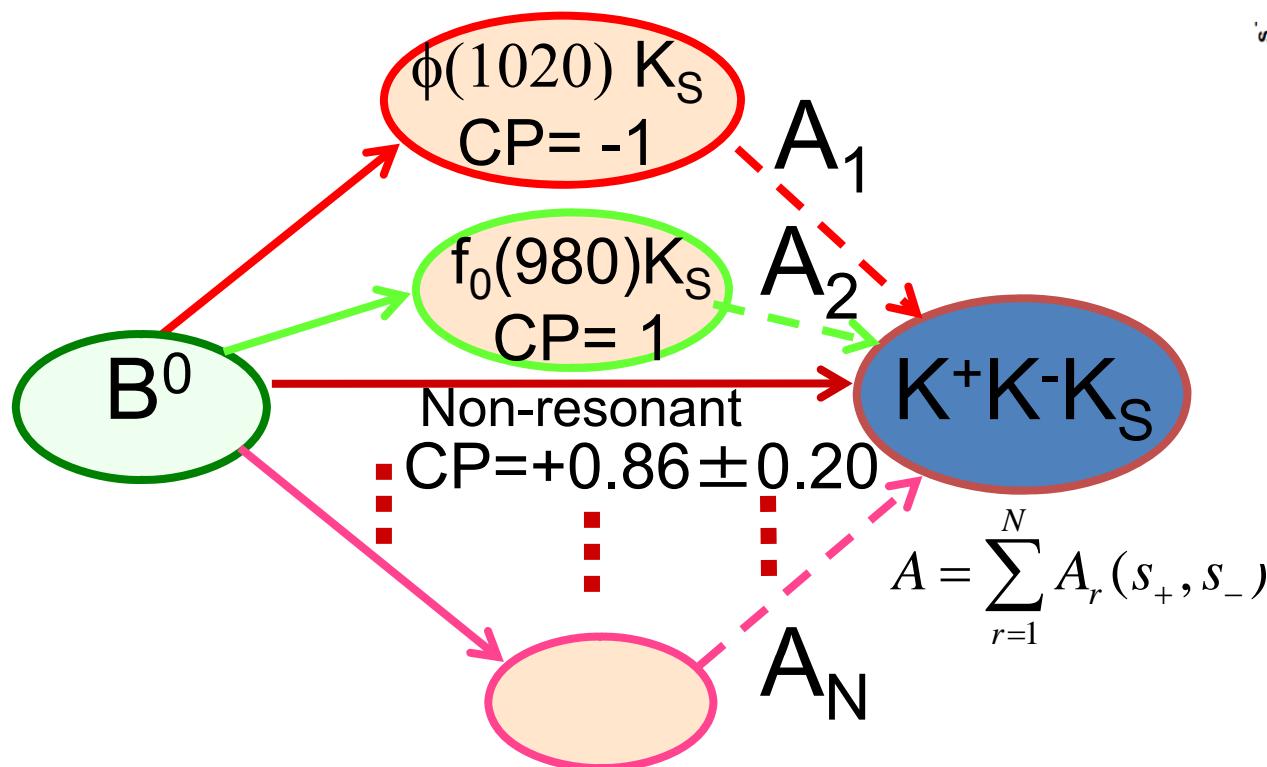


$$\Delta \sin 2\phi_1 = \sin 2\phi_1^{\text{eff}} - \sin 2\phi_1 \neq 0$$

Many two-body and quasi-two body analyses have been done. Since  $\phi \rightarrow K^+K^-$ ,  $f_0 \rightarrow K^+K^-$  and non-resonant contributions overlap invariant mass(as do  $\rho^0 \rightarrow \pi^+\pi^-$  and  $f_0 \rightarrow \pi^+\pi^-$ ), recently time-dependent Dalitz analyses have been performed in three-body decays such as  $B^0 \rightarrow (K^+K^-)K_S$  and  $B^0 \rightarrow (\pi^+\pi^-)K_S$ .

# Interferences in $B$ decays with $K^+K^-K_S$ final state

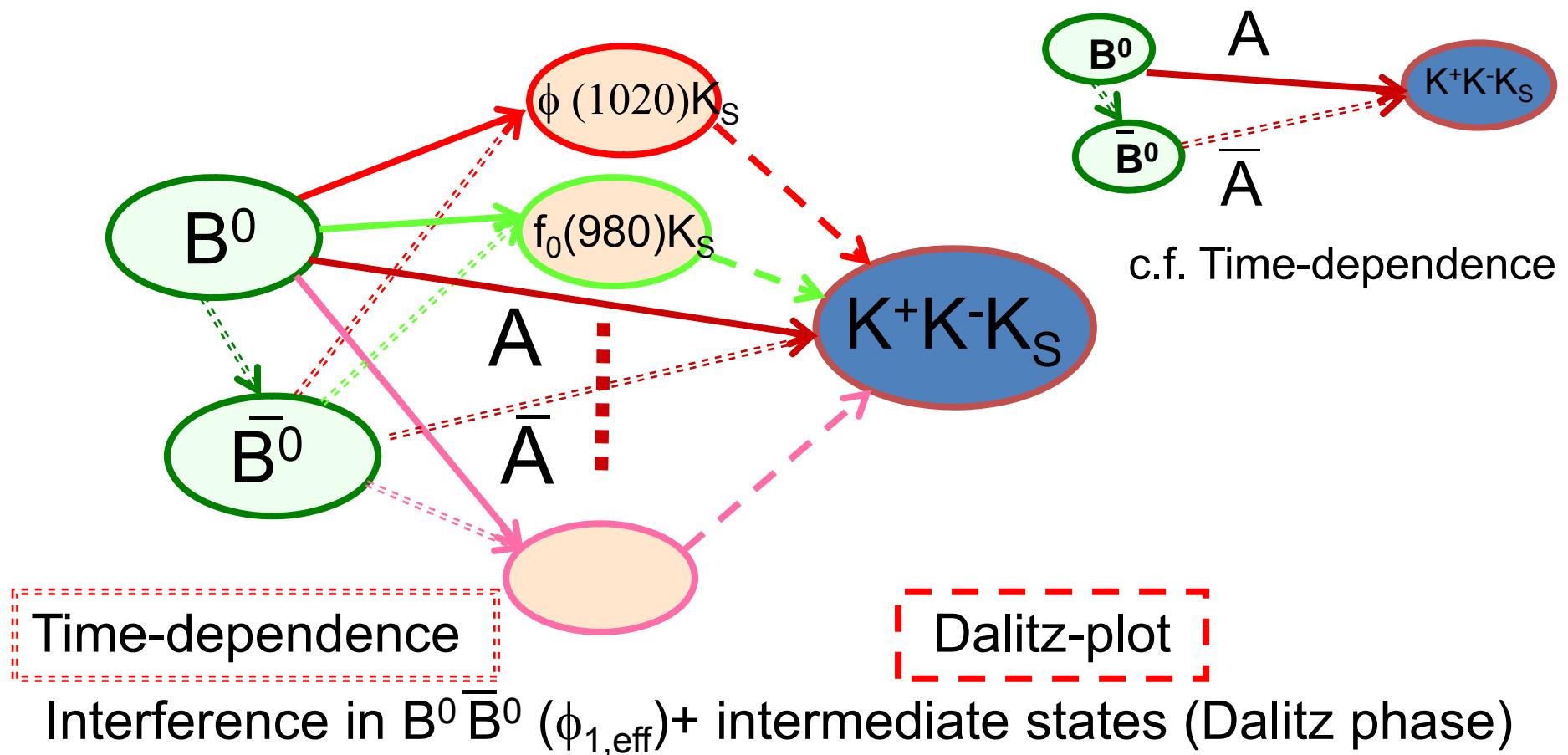
- Dalitz-plot  
⇒ distinguish the intermediate states considering interferences
- Opposite CP eigenvalue from  $\phi K_S$   
⇒ State-by-state CP measurement



$$s_+ = M^2(K^+ K_S)$$

$$s_- = M^2(K^- K_S)$$

# Time-dependence of Dalitz plot in $B^0 \rightarrow K^+ K^- K_S$



CP asymmetry ( $\phi_{1,\text{eff}}$ ,  $A_{\text{CP}}$ ) of  $B \rightarrow \phi(1020) K_S$   
using Time-dependent Dalitz plot analysis in  $B \rightarrow K^+ K^- K_S$



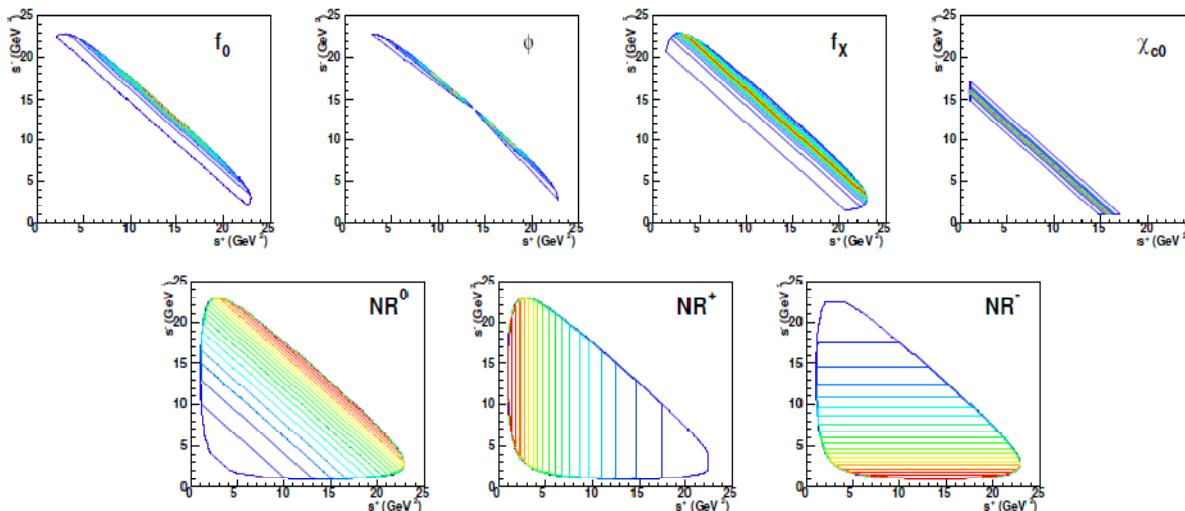
# updated Belle result ( $B^0 \rightarrow K^+ K^- K_S$ )

Decay amplitude

Belle 657MBB to be submitted to PRD.

resonance	Form factor	Spin	CP eigenvalue
$f_0(980)$	Flatté	0	1
$\phi(1020)$	RBW	1	-1
$f_x(1500)$	RBW	0	1
$\chi_{c0}$	RBW	0	1
$(K_S K^-) K^+$	$\exp(-\alpha s_-)$	0	1
$(K_S K^+) K^-$	$\exp(-\alpha s_+)$	0	1
$(K^+ K^-) K_S$	$\exp(-\alpha s_0)$	0	1

RBW:  
Relativistic  
Breit Wigner



19 free parameters  
•12: isobar model  
•6: CPV parameters.  
•1:  $\alpha$  for NR



# Multiple solution

4 preferable solutions

Decay mode fractions

Parameter	Solution 1	Solution 2	Solution 3	Solution 4
$f_{f_0 K_S^0}$	$26.0 \pm 7.4$	$54.0 \pm 9.6$	$26.4 \pm 7.8$	$68.1 \pm 12.3$
$f_{\phi K_S^0}$	$14.2 \pm 1.2$	$14.5 \pm 1.2$	$14.2 \pm 1.2$	$14.4 \pm 1.2$
$f_{f_X K_S^0}$	$5.10 \pm 1.39$	$5.89 \pm 1.86$	$39.6 \pm 2.6$	$59.0 \pm 3.0$
$f_{\chi_{c0} K_S^0}$	$3.73 \pm 0.74$	$3.71 \pm 0.73$	$3.68 \pm 0.73$	$4.15 \pm 0.79$
$f_{(K^+ K^-)_{\text{NR}} K_S^0}$	$138.4 \pm 44.8$	$175.0 \pm 52.6$	$157.4 \pm 29.5$	$48.1 \pm 11.7$
$f_{(K_S^0 K^+)_{\text{NR}} K^-}$	$1.65 \pm 4.17$	$21.0 \pm 17.3$	$4.63 \pm 6.76$	$7.87 \pm 4.78$
$f_{(K_S^0 K^-)_{\text{NR}} K^+}$	$26.0 \pm 12.9$	$78.0 \pm 36.2$	$38.6 \pm 18.1$	$6.27 \pm 3.81$
$F_{\text{tot}}$	$215.2 \pm 47.5$	$352.0 \pm 66.8$	$284.5 \pm 36.3$	$207.9 \pm 18.4$

External information from  $B^0 \rightarrow \pi^+ \pi^- K_S$

•  $f_0(980)$

- $\text{B.F.}(f_0(980) \rightarrow \pi^+ \pi^-)/\text{B.F.}(f_0(980) \rightarrow K^+ K^-)$  and compare with PDG
- solutions with low  $f_0(980) K_S$  fraction preferred

•  $f_x(1500)$

- If  $f_x(1500) = f_0(1500)$  for both decays
- $\text{B.F.}(f_0(1500) \rightarrow \pi^+ \pi^-)/\text{B.F.}(f_0(1500) \rightarrow K^+ K^-)$  and compare with PDG
- solutions with low  $f_x(1500) K_S$  fraction preferred

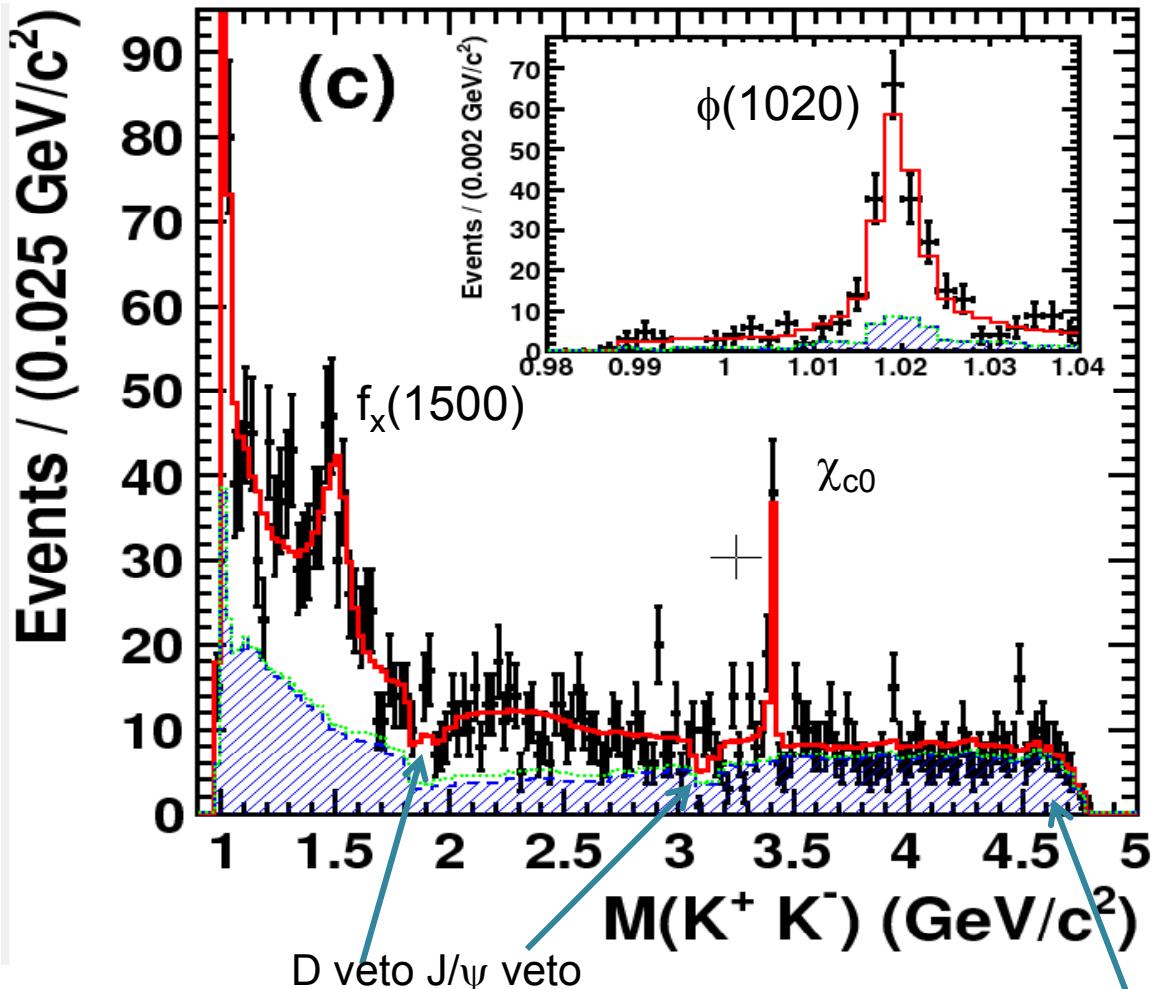


Solution 1  
preferred.

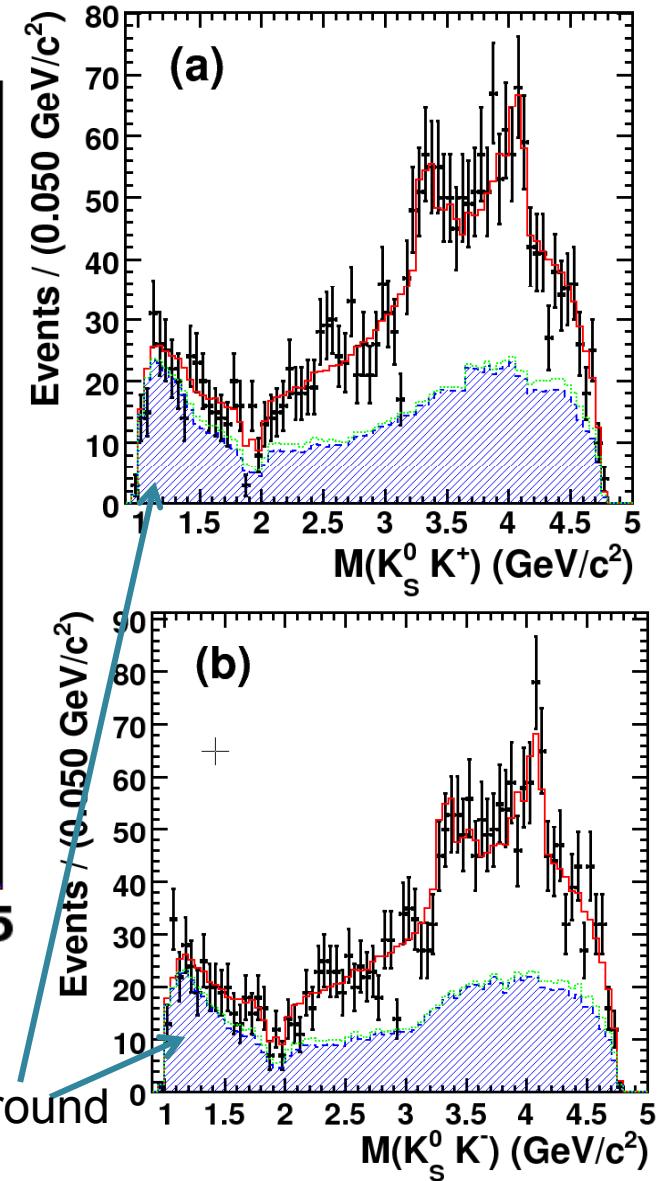


# fit result (Dalitz plot)

Solution 1



background

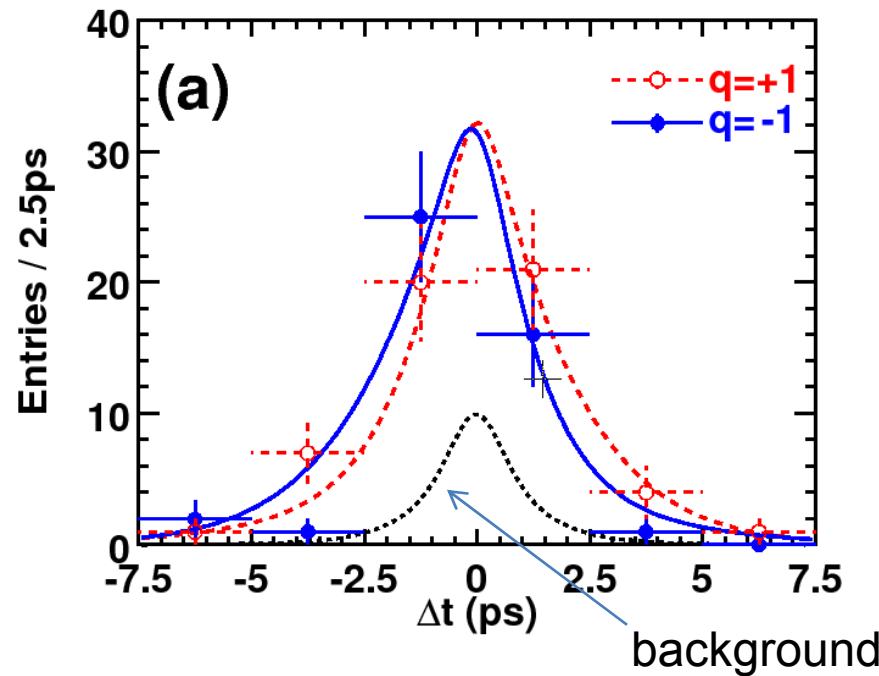




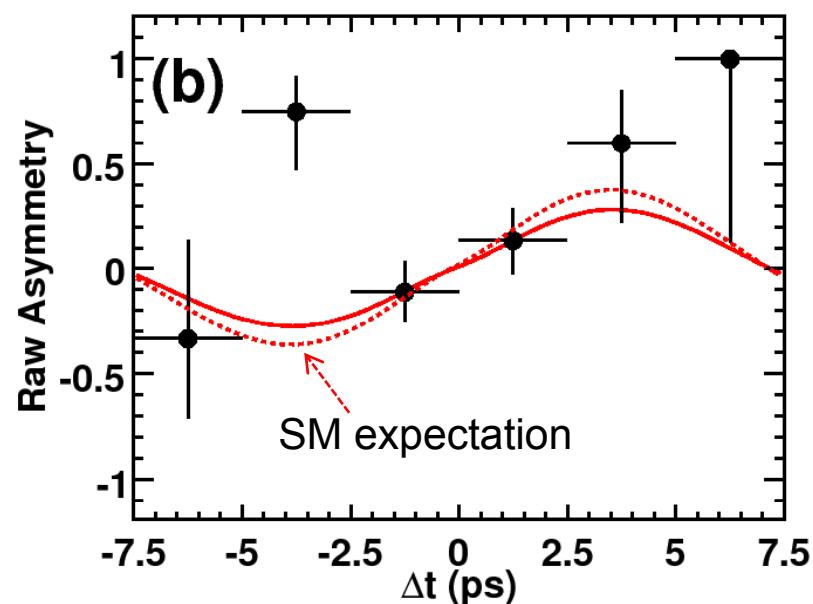
# fit result ( $\Delta t$ plot)

## Solution 1

proper time distribution and raw asymmetry plot in  $\phi$  mass region



Belle 657MBB to be submitted to PRD.

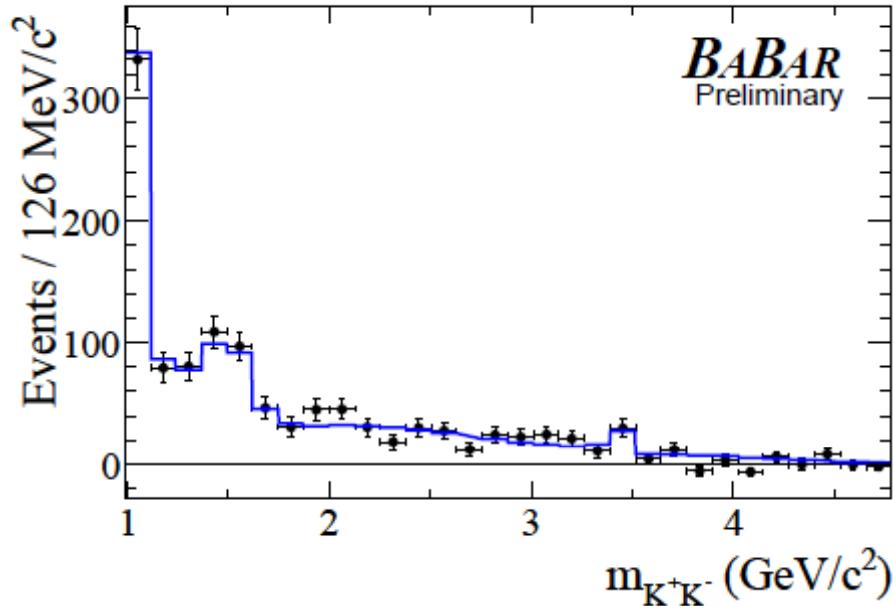


	Solution 1	Solution 2	Solution 3	Solution 4
$\mathcal{A}_{CP}(f_0 K_S^0)$	$-0.30 \pm 0.29 \pm 0.11 \pm 0.09$	$-0.20 \pm 0.15 \pm 0.08 \pm 0.05$	$+0.02 \pm 0.21 \pm 0.09 \pm 0.09$	$-0.18 \pm 0.14 \pm 0.08 \pm 0.06$
$\phi_1^{\text{eff}}(f_0 K_S^0)$	$(31.3 \pm 9.0 \pm 3.4 \pm 4.0)^\circ$	$(26.1 \pm 7.0 \pm 2.4 \pm 2.5)^\circ$	$(25.6 \pm 7.6 \pm 2.9 \pm 0.8)^\circ$	$(26.3 \pm 5.7 \pm 2.4 \pm 5.8)^\circ$
$\mathcal{A}_{CP}(\phi K_S^0)$	$+0.04 \pm 0.20 \pm 0.10 \pm 0.02$	$+0.08 \pm 0.18 \pm 0.10 \pm 0.03$	$-0.01 \pm 0.20 \pm 0.11 \pm 0.02$	$+0.21 \pm 0.18 \pm 0.11 \pm 0.05$
$\phi_1^{\text{eff}}(\phi K_S^0)$	$(32.2 \pm 9.0 \pm 2.6 \pm 1.4)^\circ$	$(26.2 \pm 8.8 \pm 2.7 \pm 1.2)^\circ$	$(27.3 \pm 8.6 \pm 2.8 \pm 1.3)^\circ$	$(24.3 \pm 8.0 \pm 2.9 \pm 5.2)^\circ$

the third error: Dalitz plot model uncertainty



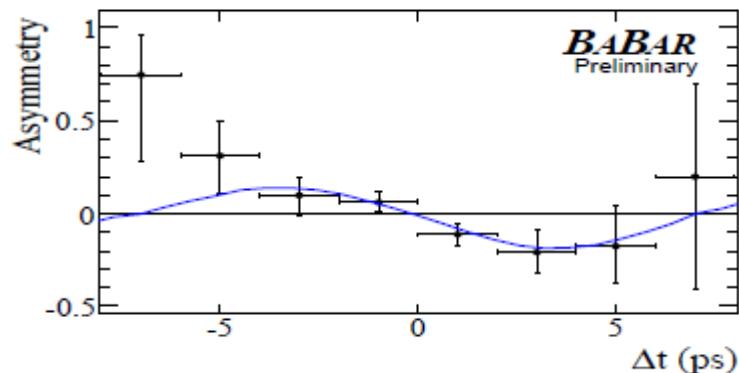
# BABAR $K^+K^-K_S$ result



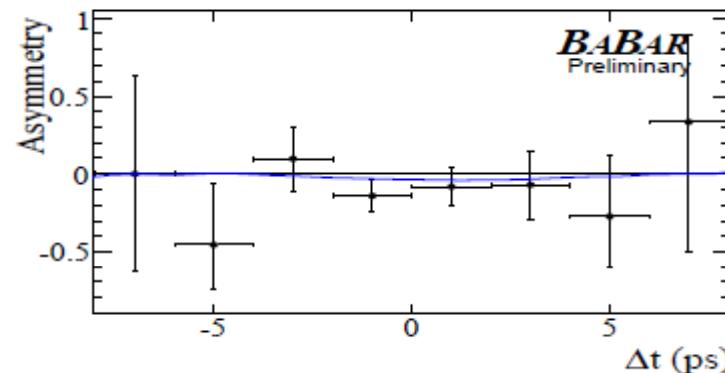
BABAR 465MBB arXiv:0808.0700

Name	Solution (1)
1 $A_{CP}(\phi K_S^0)$	$0.14 \pm 0.19 \pm 0.02$
2 $\beta_{eff}(\phi K_S^0)$	$(7.7 \pm 7.7 \pm 0.9)^\circ$
3 $A_{CP}(f_0 K_S^0)$	$0.01 \pm 0.26 \pm 0.07$
4 $\beta_{eff}(f_0 K_S^0)$	$(8.5 \pm 7.5 \pm 1.8)^\circ$

whole region



low mass region



# average in $B \rightarrow \phi K_S$ , $B \rightarrow f_0(980) K_S$

$K^+ K^- K_S \beta(\phi K_S)$

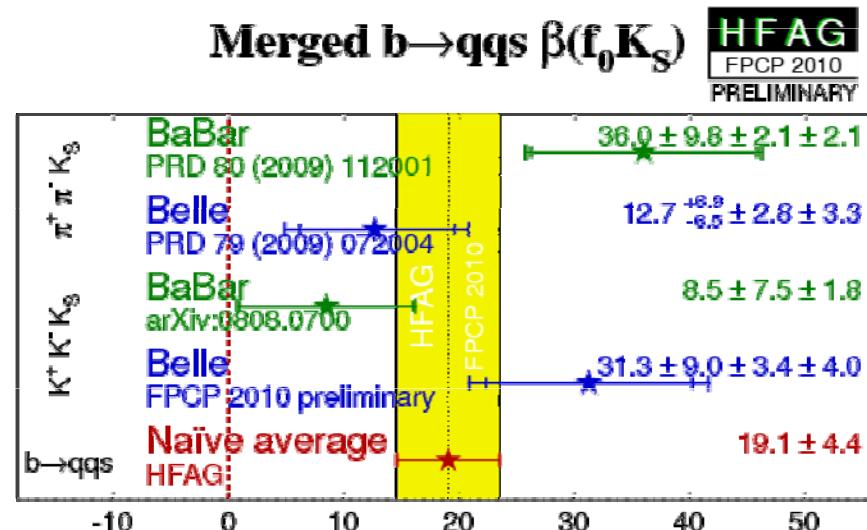
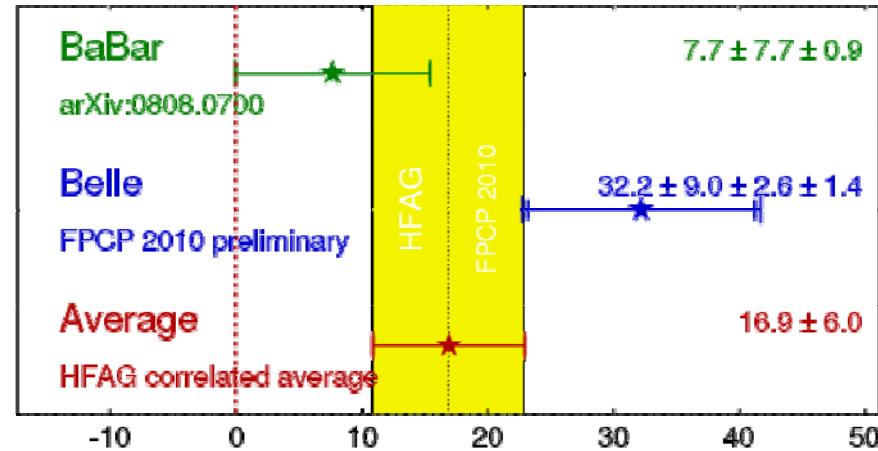
**HFAG**  
FPCP 2010  
PRELIMINARY



	Solution 1
$A_{CP}(f_0 K_S^0)$	$-0.30 \pm 0.29 \pm 0.11 \pm 0.09$
$\phi_1^{\text{eff}}(f_0 K_S^0)$	$(31.3 \pm 9.0 \pm 3.4 \pm 4.0)^\circ$
$A_{CP}(\phi K_S^0)$	$+0.04 \pm 0.20 \pm 0.10 \pm 0.02$
$\phi_1^{\text{eff}}(\phi K_S^0)$	$(32.2 \pm 9.0 \pm 2.6 \pm 1.4)^\circ$



Name	Solution (1)
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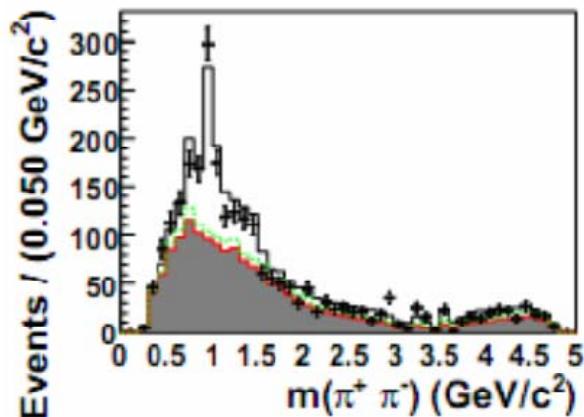


Consistent with the Standard Model prediction at current sensitivity

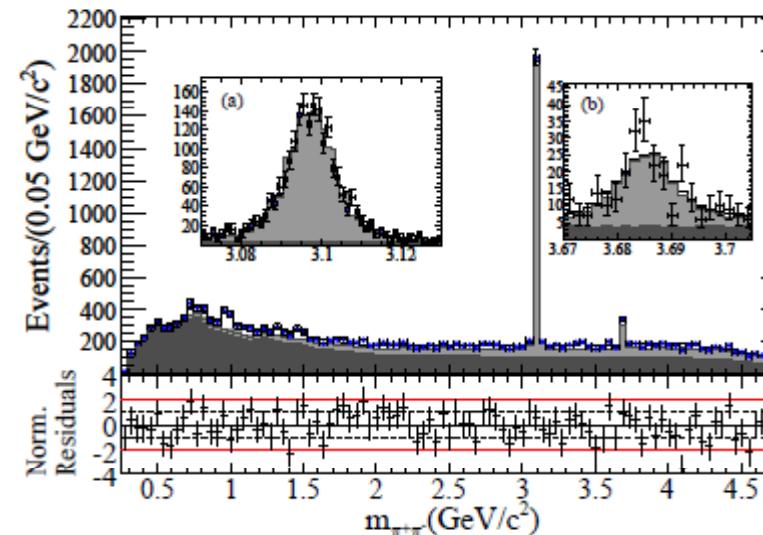
$$\phi_{1(b \rightarrow c\bar{c})} = (21.0 \pm 0.9)^\circ$$

# result using $\pi^+\pi^-K_S$

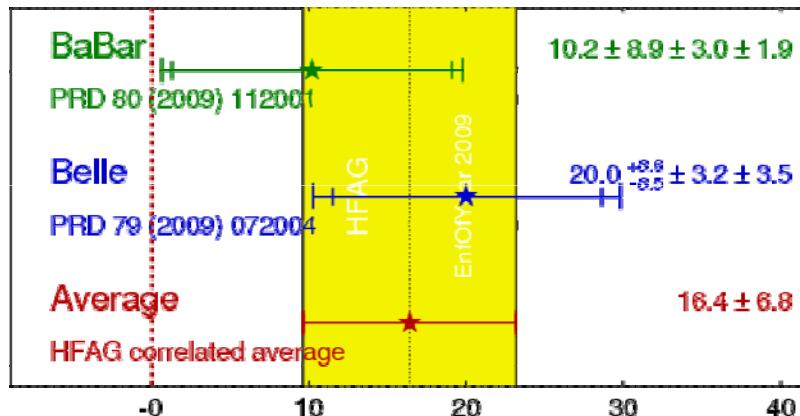
Belle 657MBB PRD79(2009) 072004



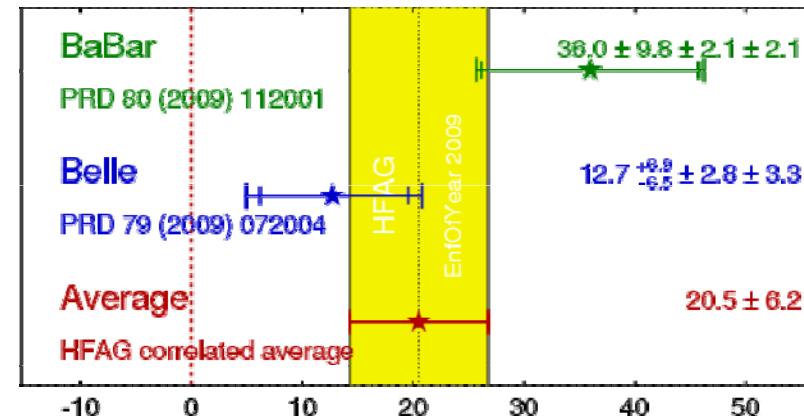
BABAR 383MBB PRD80(2009) 112001



$\pi^+\pi^-K_S \beta(\rho K_S)$  HFAG EnfOfYear 2009 PRELIMINARY



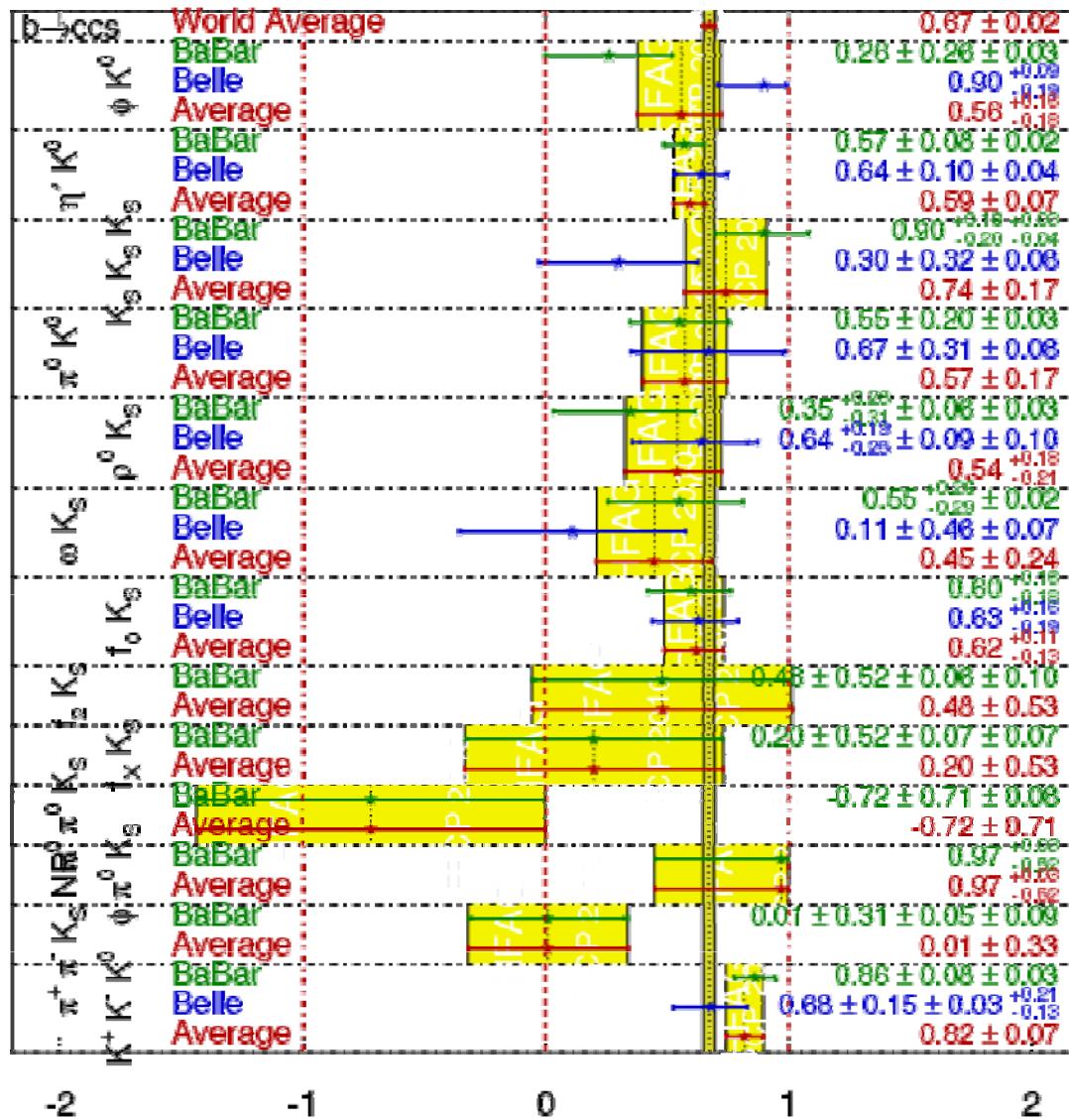
$\pi^+\pi^-K_S \beta(f_0 K_S)$  HFAG EnfOfYear 2009 PRELIMINARY



# Compilation of effective $\sin 2\phi_1$

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

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Still precision is statistically dominated.



To obtain sensitivity in effective  $\sin 2\phi_1$  of  $O(10^{-2})$ , we need  $O(10ab^{-1})$  of integrated luminosity.

# Summary

- $\phi_1/\beta = (21.1 \pm 0.9)^\circ$  in B-factories
  - $\sin 2\phi_1$  from  $b \rightarrow c\bar{c}s$  modes.
  - resolve the quadratic ambiguity by measuring  $\cos 2\phi_1$  with Dalitz analysis, etc.
- penguin modes are good probes of new physics.  
We need more data.
- Belle is now updating its result with the full data sample.
  - $J/\psi K^0$ 
    - full data:  $535M \rightarrow 771MBB$  (factor 1.44)
    - improved tracking software: 20% gain for  $J/\psi Ks$
    - yield : factor 1.61
  - $\psi(2S)Ks, \chi_{c1}Ks, \eta_cKs$ , and combined analysis  
last update with  $150MB\bar{B}$  ( $657MB\bar{B}$  for  $\psi(2S)Ks$ )
  - (statistical error for  $\sin 2\phi_1$ )  $\sim 0.02$
  - etc..

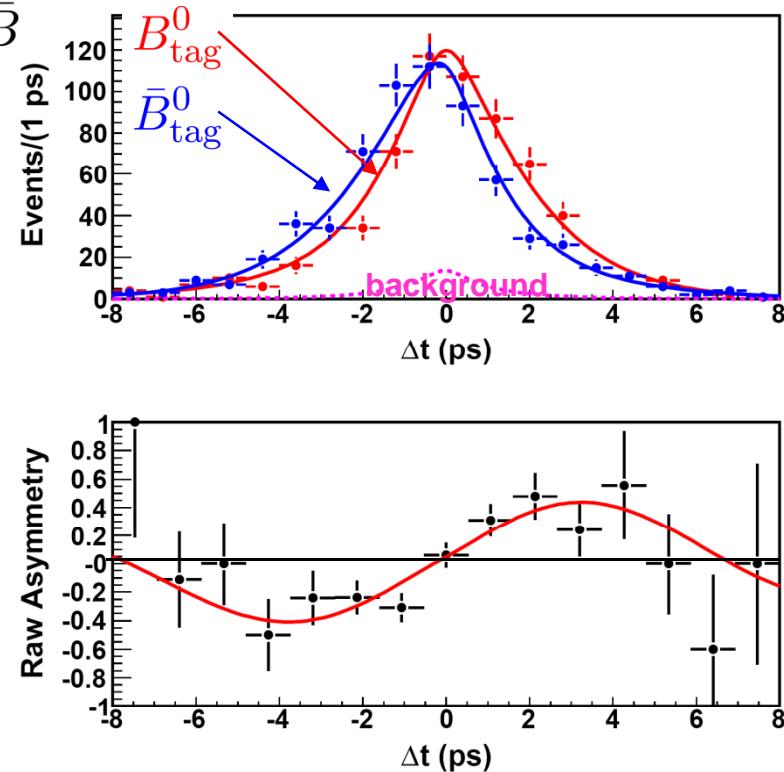
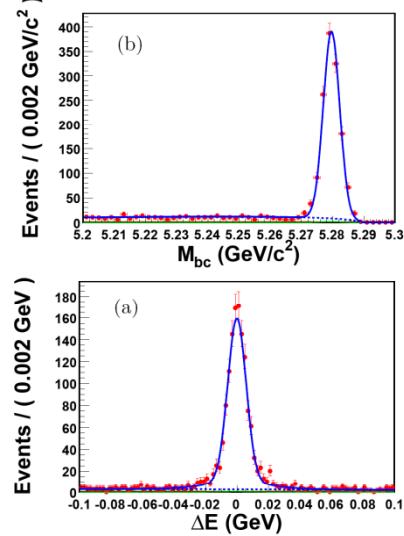
# backup

$b \rightarrow c\bar{c}s$  $B^0 \rightarrow \psi(2S)K_S$ 

arXiv:0708.2604v2[hep-ex] 4 Feb 2008



$657 \times 10^6 B\bar{B}$   
 $1284 \pm 37$  signal events  
 $92 \pm 1\%$  purity



$$\mathcal{S}_{\psi(2S)K_S^0} = 0.72 \pm 0.09(\text{stat}) \pm 0.03(\text{syst})$$

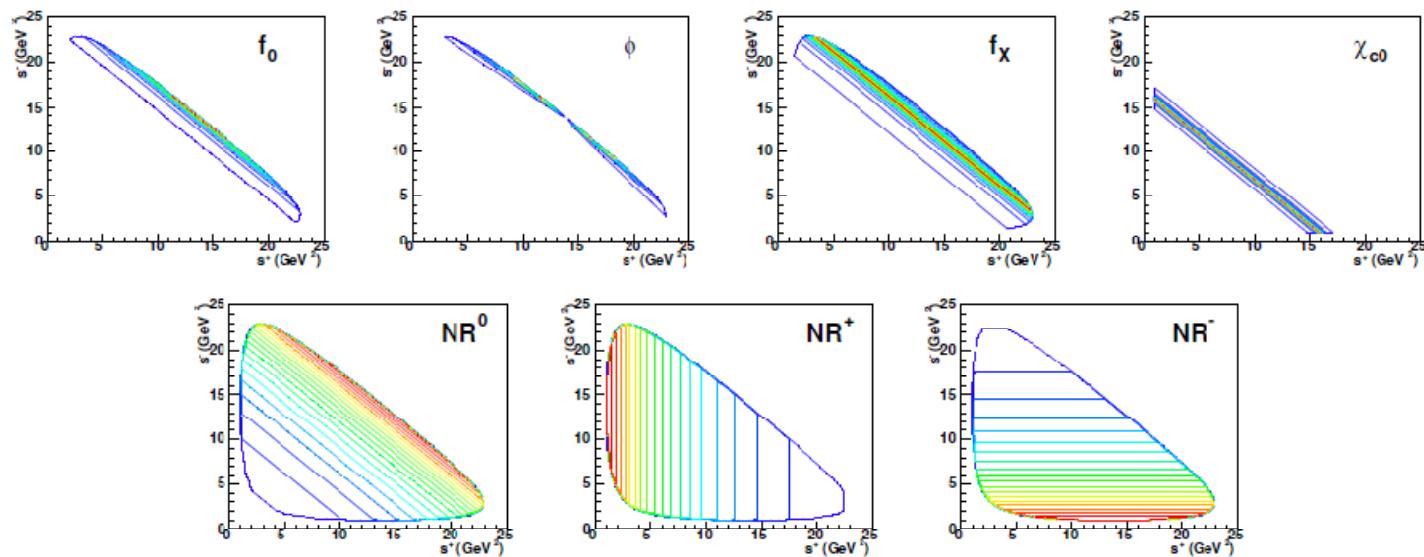
$$\mathcal{A}_{\psi(2S)K_S^0} = 0.04 \pm 0.07(\text{stat}) \pm 0.05(\text{syst})$$

Combined  
 $b \rightarrow c\bar{c}s$   
result:

$\sin 2\phi_1$	$= 0.650 \pm 0.029(\text{stat}) \pm 0.018(\text{syst})$	
$\sin 2\phi_1$	$= 0.714 \pm 0.032(\text{stat}) \pm 0.018(\text{syst})$	

# Resonances considered in the KsKK signal model

Resonances	Fixed parameters (GeV)	Form Factor, $R_i(s_+, s_-)$	$L$
$f_0$	$M = 0.965 \pm 0.010$ $g_\pi = 0.165 \pm 0.018$ $g_K = (4.21 \pm 0.09)g_\pi$	Flatté	0
$\phi$	$M = 1.019455 \pm 0.020$ $\Gamma = 0.00426 \pm 0.00004$	RBW	1
$f_X$	$M = 1.524 \pm 0.014$ $\Gamma = 0.136 \pm 0.023$	RBW	0
$\chi_{c0}$	$M = 3.41475 \pm 0.00035$ $\Gamma = 0.0104 \pm 0.0007$	RBW	0
$(K^+K^-)_{\text{NR}}$		$e^{-\alpha s^0}$	
$(K_S^0K^+)_{\text{NR}}$		$e^{-\alpha s^+}$	
$(K_S^0K^-)_{\text{NR}}$		$e^{-\alpha s^-}$	



# Signal PDF

$$P(\Delta t, q; s_+, s_-) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \left[ (|A|^2 + |\bar{A}|^2) - q (|A|^2 - |\bar{A}|^2) \cos \Delta m_d \Delta t + 2 q \text{Im}(\bar{A} A^*) \sin \Delta m_d \Delta t \right]$$

[ Dalitz-plot ] × [ Time-dependence ]

Decay amplitude

$$B^0: A = \sum_{r=1}^7 a_r (1 + c_r) e^{i(b_r + d_r)} \cdot f_r(s_+, s_-)$$

$$\bar{B}^0: \bar{A} = \sum_{r=1}^7 a_r (1 - c_r) e^{i(b_r - d_r)} \cdot f_r(s_+, s_-)$$

⇒ 19 fit parameters

$\phi_1^{eff}$

1. Dalitz amplitude and phases

2. CP-violating amplitude and phases

( $\phi_{Ks}$ ,  $f_0 Ks$ , others)

3. Kinematics (Dalitz plot)

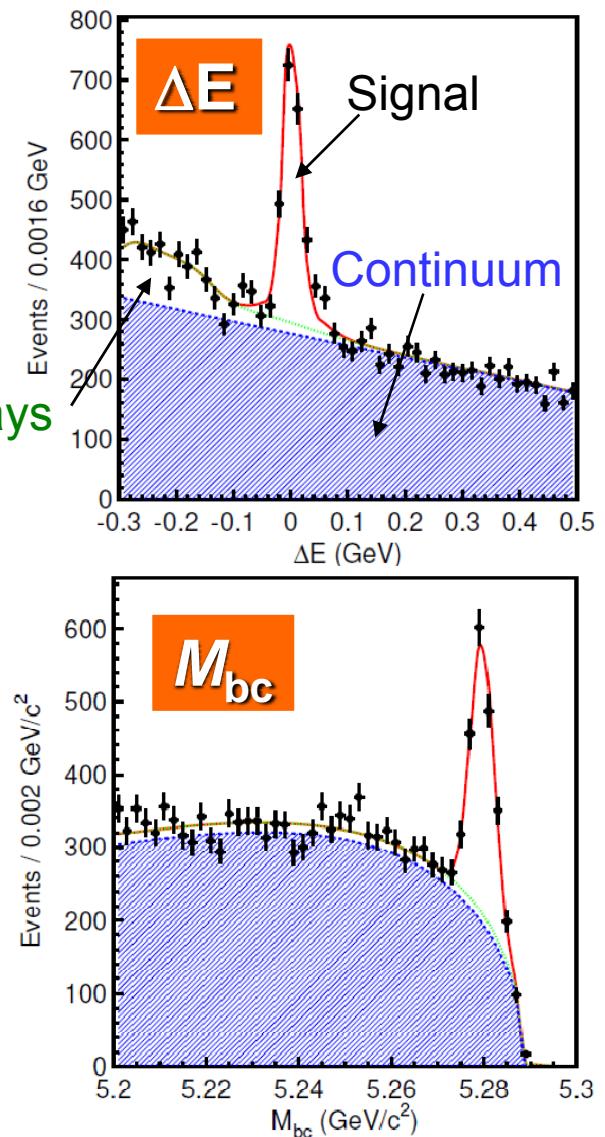
$\alpha$  for NR

$f_r(s_+, s_-)$

# Reconstructed $B^0 \rightarrow K_s K^+ K^-$ candidates

- Event selection
  - $B^0 \rightarrow K_s K^+ K^-$  reconstruction
    - $K_s$  selection
    - $K^\pm$  selection by PID ( $K/\pi$ )
  - Continuum suppression
  - Efficiency:  $\sim 16\%$
- Unbinned ML fit to  $\Delta E$  and  $M_{bc}$  distributions
  - $B^0 \rightarrow K_s K^+ K^-$   $1176 \pm 51$  evts. Purity  $\sim 50\%$
  - Background
    - Continuum  $\sim 47\%$
    - Other  $B$  decays  $\sim 3\%$
- Event-by-event signal probability  $f_{sig}(\Delta E, M_{bc})$  for CP measurement
- Time-dependent Dalitz plot fit to the selected  $B^0 \rightarrow K_s K^+ K^-$  candidates.

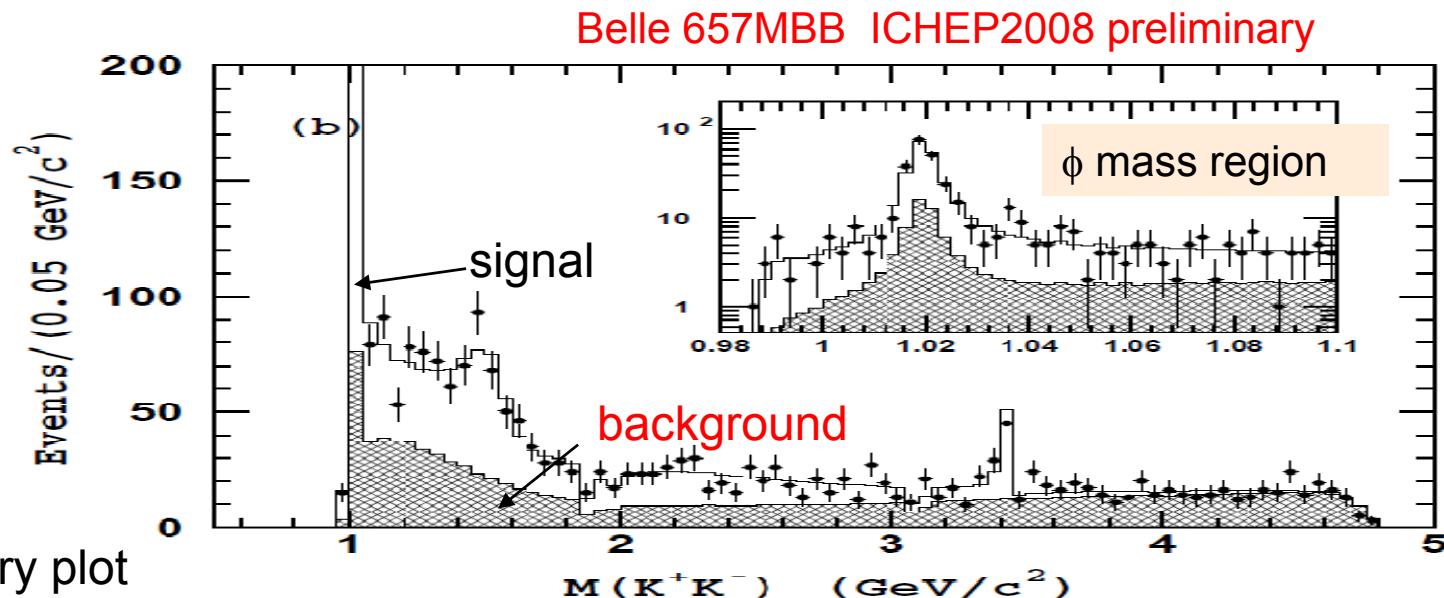
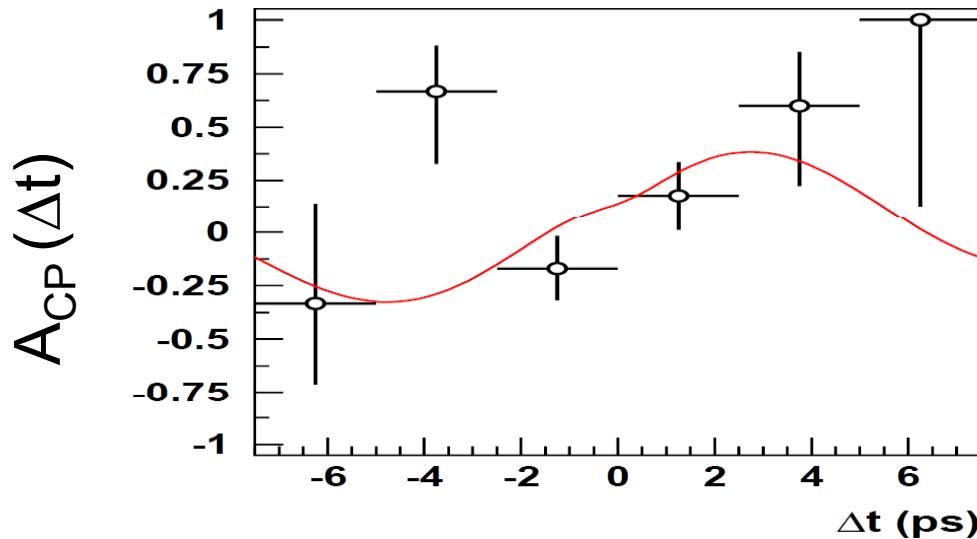
Other  $B$  decays



# plots for $K^+K^-K_S$



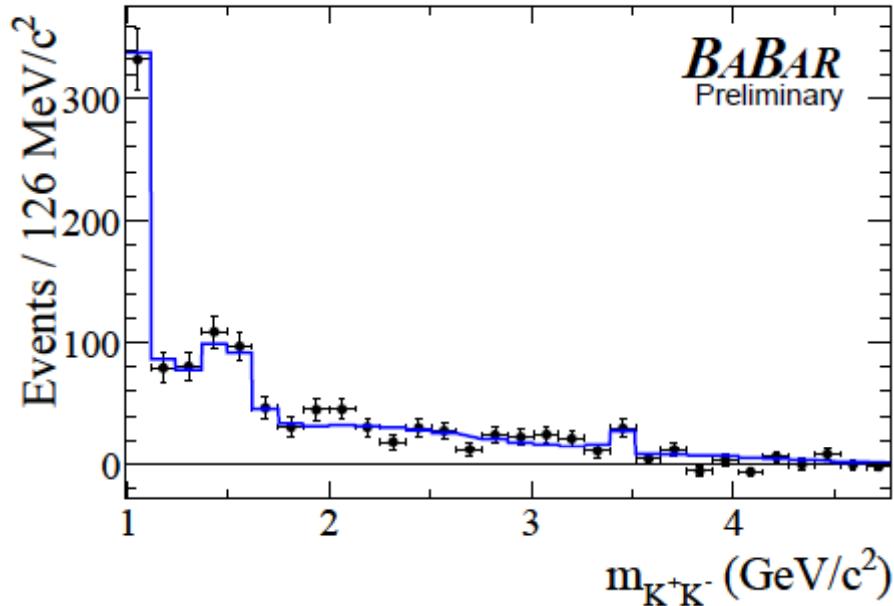
raw asymmetry plot  
in  $\phi$  mass region



Solution	$CP$ Parameter	Fit Result
1	$\phi_1^{\text{eff}}(f_0(980)K_S^0)$	$(28.2^{+9.8}_{-9.9})^\circ$
	$\phi_1^{\text{eff}}(\phi(1020)K_S^0)$	$(21.2^{+9.8}_{-10.4})^\circ$
2	$\phi_1^{\text{eff}}(f_0(980)K_S^0)$	$(64.1^{+7.6}_{-8.0})^\circ$
	$\phi_1^{\text{eff}}(\phi(1020)K_S^0)$	$(62.1^{+8.3}_{-8.8})^\circ$
3	$\phi_1^{\text{eff}}(f_0(980)K_S^0)$	$(61.5^{+6.5}_{-6.5})^\circ$
	$\phi_1^{\text{eff}}(\phi(1020)K_S^0)$	$(65.1^{+8.7}_{-8.7})^\circ$
4	$\phi_1^{\text{eff}}(f_0(980)K_S^0)$	$(36.9^{+10.9}_{-9.6})^\circ$
	$\phi_1^{\text{eff}}(\phi(1020)K_S^0)$	$(44.9^{+13.2}_{-13.6})^\circ$



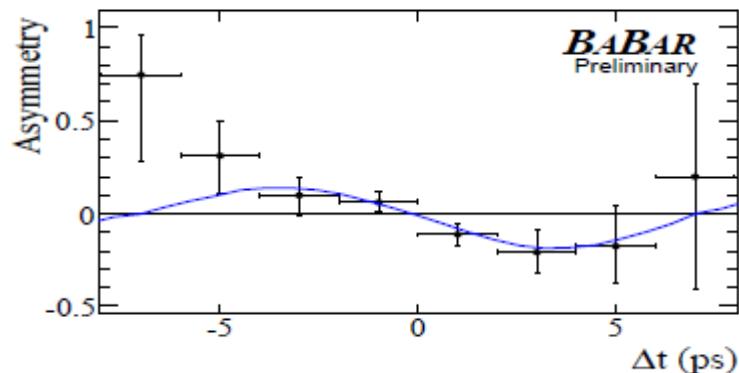
# BABAR $K^+K^-K_S$ result



BABAR 465MBB arXiv:0808.0700

Name	Solution (1)	Solution (2)
1 $A_{CP}(\phi K_S^0)$	$0.14 \pm 0.19 \pm 0.02$	$0.13 \pm 0.18$
2 $\beta_{eff}(\phi K_S^0)$	$(7.7 \pm 7.7 \pm 0.9)^\circ$	$(8.7 \pm 8.7)^\circ$
3 $A_{CP}(f_0 K_S^0)$	$0.01 \pm 0.26 \pm 0.07$	$-0.49 \pm 0.25$
4 $\beta_{eff}(f_0 K_S^0)$	$(8.5 \pm 7.5 \pm 1.8)^\circ$	$(197 \pm 11)^\circ$

whole region



low mass region

