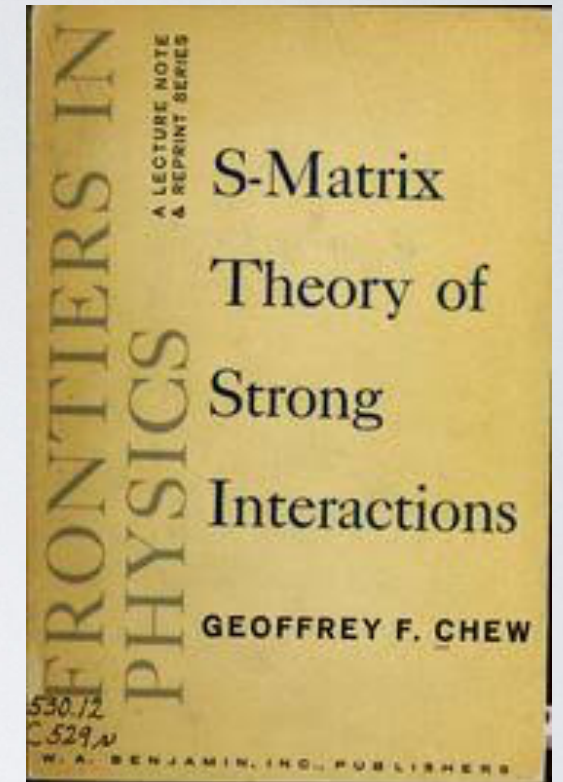
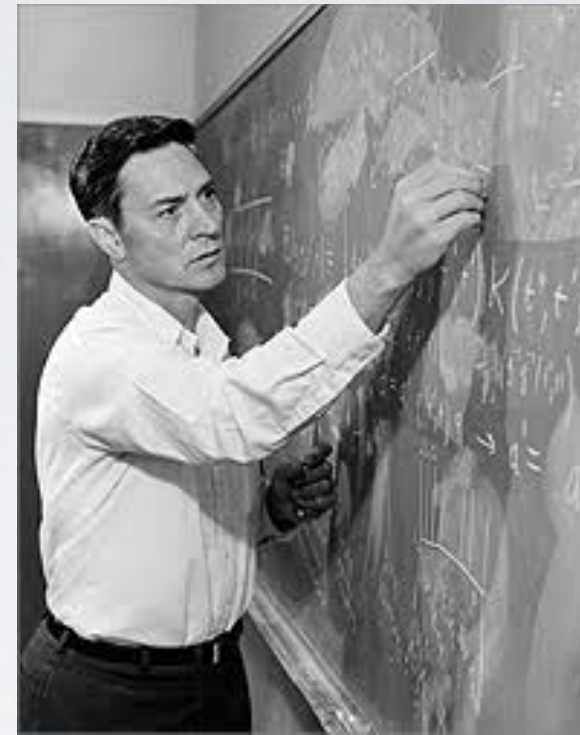
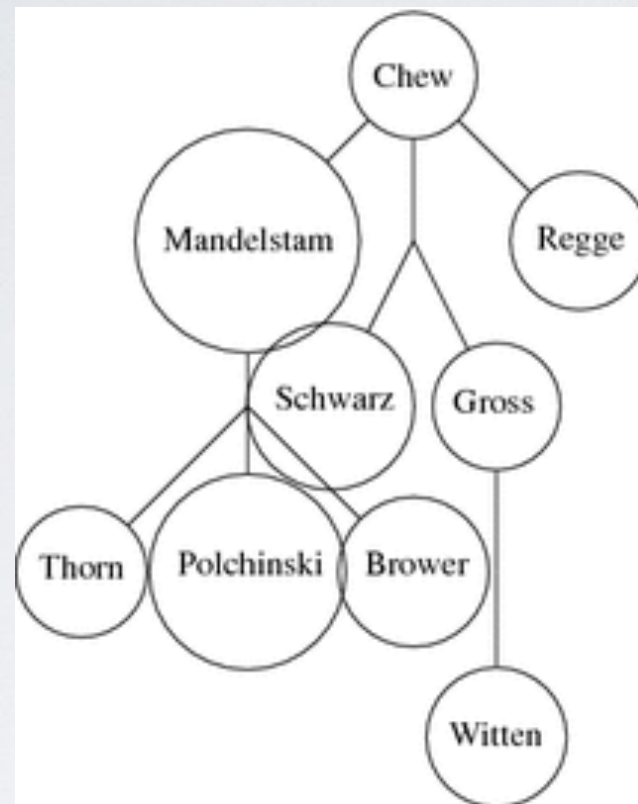


THE NO-GHOST THEOREM & BACK TO THE FUTURE

50 Years of the Veneziano Model:
From Dual Models to Strings, M-theory and Beyond

Rich Brower, Boston University:
Galileo Galilei Institute (GGI), May 11, 2018

The 60s Berkeley Bootstrap Scene



REMARKS

1. *Zero Width Bootstrap (aka leading $1/N$)*
2. *The No Ghost Theorem**
3. *Maldacena's "Counter Revolution"*
 - *Graviton/Pomeron & Wide Angle ?*
 - *Truncating SUSY: Glueballs & NS string?*

(*) See Brower's & Goddard's chapter in ***The Birth of String Theory*** for more details and the crucial collaborations with Charles Thorn

HADRONIC BOOTSTRAP

$$\sum_k \begin{array}{c} \phi_1 \quad \phi_4 \\ \diagdown \quad \diagup \\ f_{12k} \text{---} \phi_k \text{---} f_{34k} \\ \diagup \quad \diagdown \\ \phi_2 \quad \phi_3 \end{array} = \sum_k \begin{array}{c} \phi_1 \quad \phi_4 \\ \diagdown \quad \diagup \\ f_{14k} \text{---} \phi_k \text{---} f_{23k} \\ \diagup \quad \diagdown \\ \phi_2 \quad \phi_3 \end{array}$$



* **Kinematic Constraints on Infinitely Rising Regge Trajectories**

Brower & Harte: received 13 June 1967 (WRONG!)

Dynamics based on rising Regge trajectories*

Mandelstam: received 5 Sept 1967 (Amazing)

$$\alpha_\rho(t) = \alpha' t + 0.5$$

$$A(s, t) = \sum_{k,l} \frac{g_{kl}^2 P_l(\cos\theta)}{s - m_{k,l}^2} \rightarrow \beta_0 \Gamma(1 - \alpha_\rho(t)) (-\alpha' s)^{\alpha_\rho(t)}$$

**Construction of a crossing symmetric,
Reggeon behaved amplitude for
linearly rising trajectories (Wow!)**

Veneziano: ricevuto 29 Luglio 1968

$$A(s, t) = \beta_0 \frac{\Gamma(1 - \alpha_\rho(t)) \Gamma(1 - \alpha_\rho(s))}{\Gamma(2 - \alpha_\rho(t) - \alpha_\rho(s))}$$

GHOST BUSTING

- The Problem of Ghosts: Minkowski metric $g^{00} = -1$

The on-shell covariant oscillator basis,

$$[a_n^\mu, a_m^{\dagger\nu}] = g^{\mu\nu} \delta_{n,m}$$

$$|\{N_{i,\mu}\}, p\rangle = [(a_1^{\mu_1\dagger})^{N_{1,\mu}} (a_2^{\mu_2\dagger})^{N_{2,\mu}} \dots] |0, p\rangle ,$$

$$[L_n, L_m] = (n - m)L_{n+m} + \frac{D - 2}{12} n(n^2 - 1) \delta_{n,-m} ,$$



Virasoro

Joe Weis

$$(L_0 - 1)|\text{Phys}\rangle = L_n|\text{Phys}\rangle = 0 \quad \text{for } n > 0 ,$$

$$|\text{Spurious}\rangle = [(L_1^\dagger)^{n_1} (L_2^\dagger)^{n_2} (L_3^\dagger)^{n_3} \dots] |\text{Phys}\rangle$$

Brower/Thorn “Verma Module”?

PHYSICAL STATE ALGEBRA

How do we find the Physical subspace?

$$\vec{A}_n = \frac{1}{2\pi i} \oint \frac{dz}{z} \vec{P} e^{inX_-} \equiv \langle \vec{P} e^{inX_-} \rangle \quad (\text{DDF}) \text{ Del Giudice, Di Vecchia and Fubini}$$

These beautiful Physical operators

$$[A_m^i, A_n^j] = m\delta^{ij}\delta_{m.-n} \quad , \quad [L_m, \vec{A}_n] = 0$$

$$|\text{Phys}, \{n_i\}, p\rangle = [(\vec{A}_1^\dagger)^{n_1} (\vec{A}_2^\dagger)^{n_2} \cdots] |0, p\rangle .$$

D-2 Transverse tensor products

Problem: DDF gives a D-2 dim physical space but Virasoro kills 1-dim space

For $D > 26$ there are Ghost states!

At $D = 26$ like the “photon” with D-2 transverse “polarizations” and 2 null states.

Very elegant solution of Goldstone, Goddard, Rebbi and Thorn (GGRT) using light-cone gauge quantization. Restoring LI only for 24 transverse modes

$$^\dagger P^\mu(z) = z\partial_z X^\mu(z)$$

SEARCH FOR LONGITUDINAL

Need Physical Longitudinal modes:

$$A_n^{(-)} = \langle P_- e^{inX_-} \rangle = 0 \quad \text{and} \quad A_n^{(+)} = \langle : P_+ e^{inX_-} : \rangle + \frac{n^2}{2} \langle P_- \log(P_-) e^{inX_-} \rangle$$

$$[A_m^{(+)}, A_n^{(+)}] = (m - n) A_{m+n}^{(+)} + m^3 \delta_{m,-n} \quad , \quad [L_m, A_n^{(+)}] = 0$$

$$[A_m^{(+)}, A_n^i] = -n A_{m+n}^i$$

Off-Shell Derivation $k^\mu = n \hat{e}_+^\mu + (k^2/2n) \hat{e}_-^\mu \quad \text{and} \quad e^\mu(k) = n \hat{e}_+^\mu - (k^2/2n) \hat{e}_-^\mu$

Expand $\langle : (\epsilon P)^{1-k^2/2} e^{ikX} : \rangle \quad \text{as} \quad k^2 \rightarrow 0$

$$\implies n \langle P_- e^{inX_-} \rangle + k^2 \langle : [-P_+/2n - (n/2) P_- \ln(P_-) + n P_- i X_+ / 2n] e^{inX_-} : \rangle$$

$$\implies -(k^2/n) [\langle : P_+ e^{inX_-} : \rangle + \frac{n^2}{2} \langle P_- \ln(P_-) e^{inX_-} \rangle] \quad \text{after integration by parts}$$

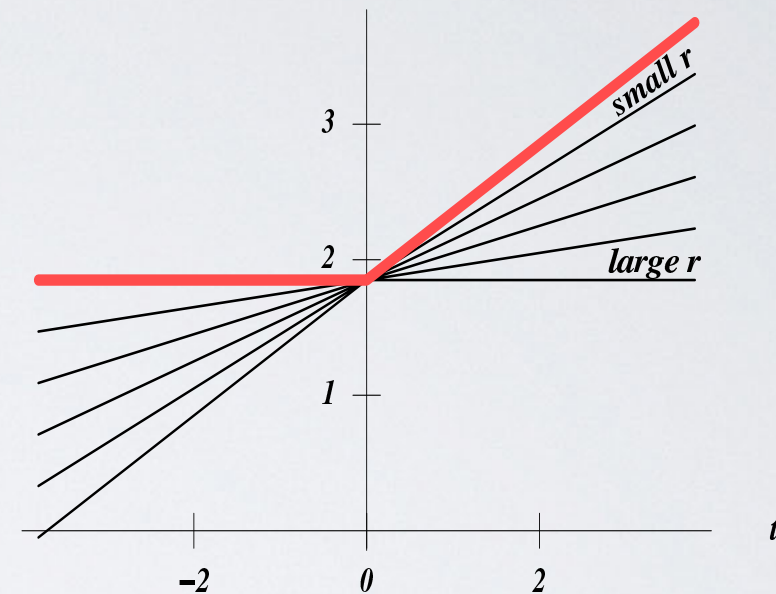
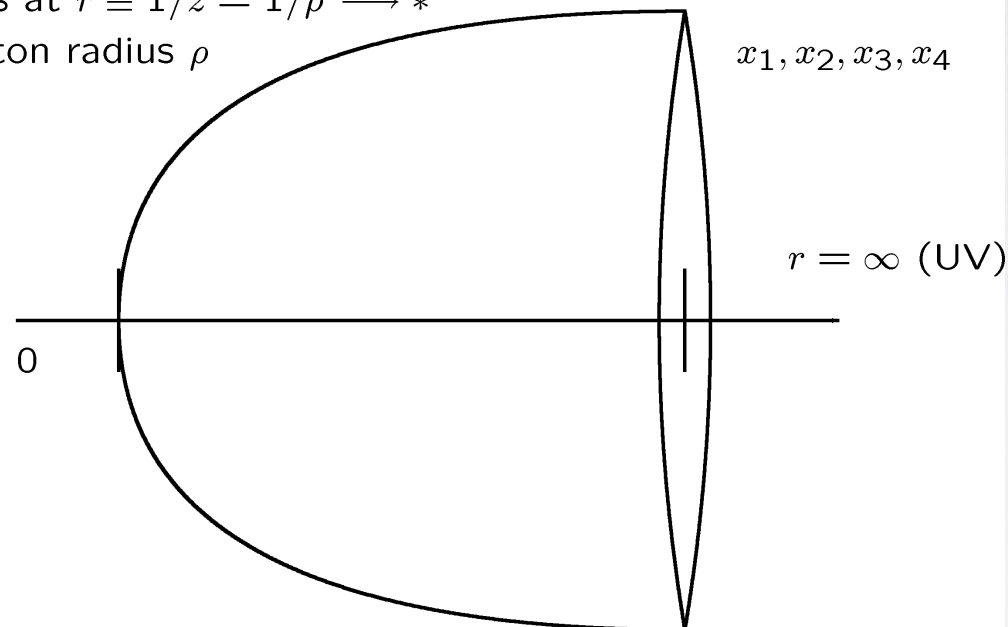
ADS GRAVITON/POMERON

$$\alpha'_{eff}(r) = \alpha' R^2 / r^2$$

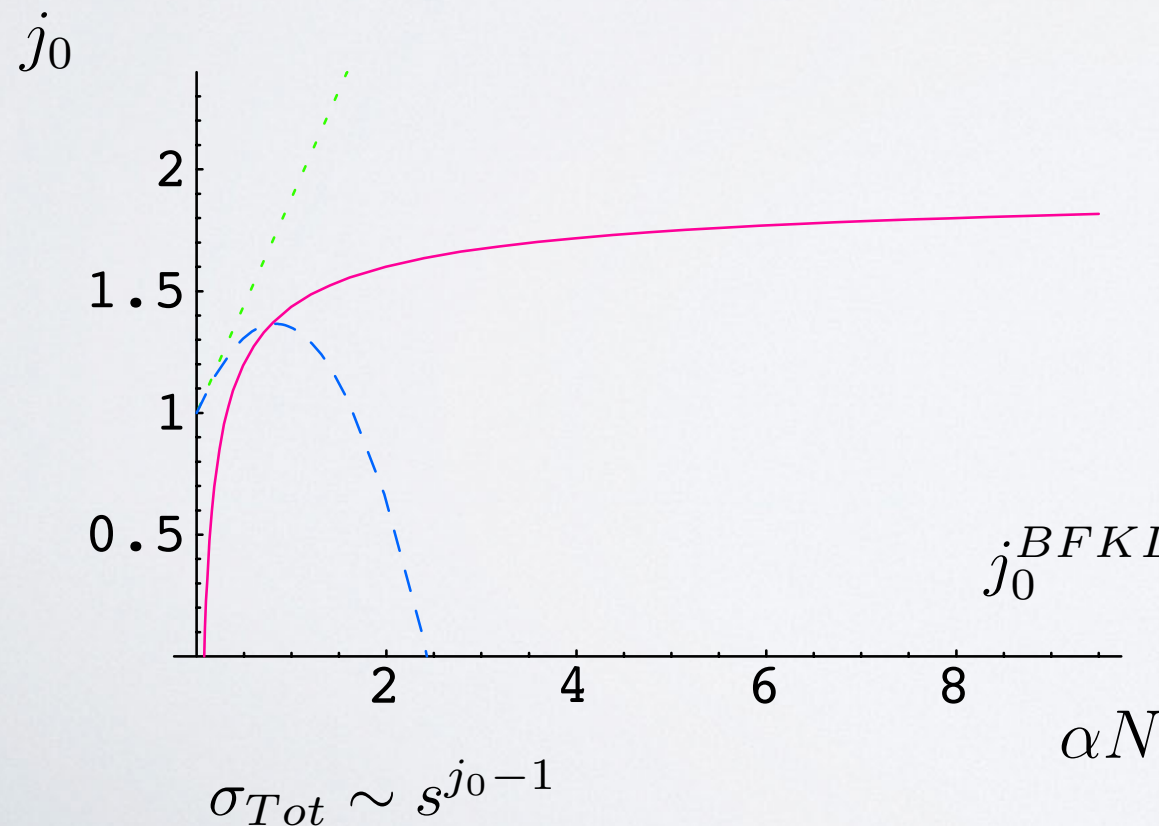
Wide angle has naive conformal scaling

pt defects at $r \equiv 1/z = 1/\rho \rightarrow *$

$\Leftrightarrow$ Instanton radius ρ



ultra Local Approximation



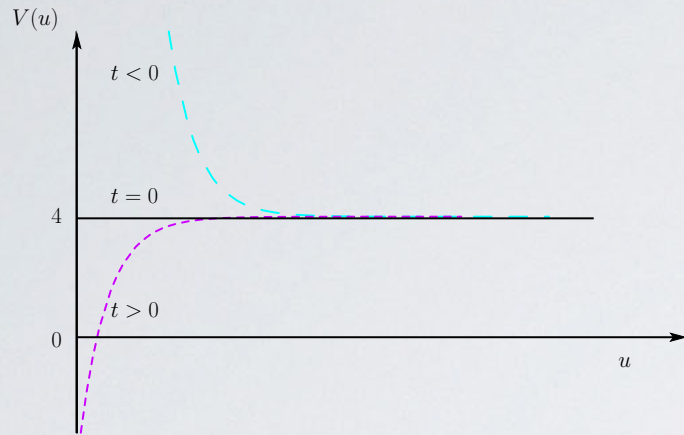
$$j_0^{AdS} = 2 - 2/\sqrt{\lambda} + O(1/\lambda)$$

$$j_0^{BFKL} = 1 + 4 \ln 2 \frac{\lambda}{\pi^2} \left(1 - 7.58 \frac{\lambda}{16\pi^2} \right)$$

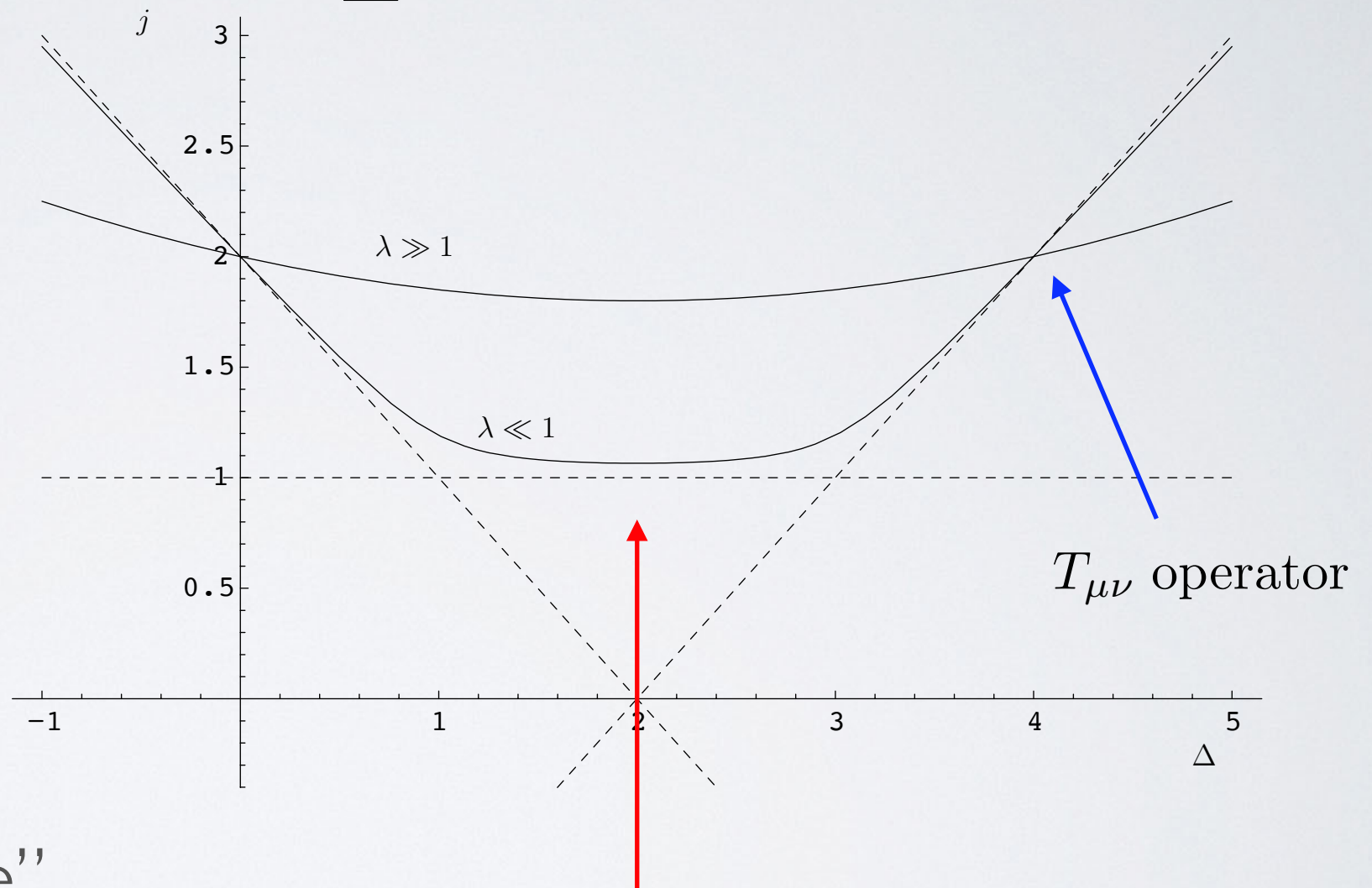
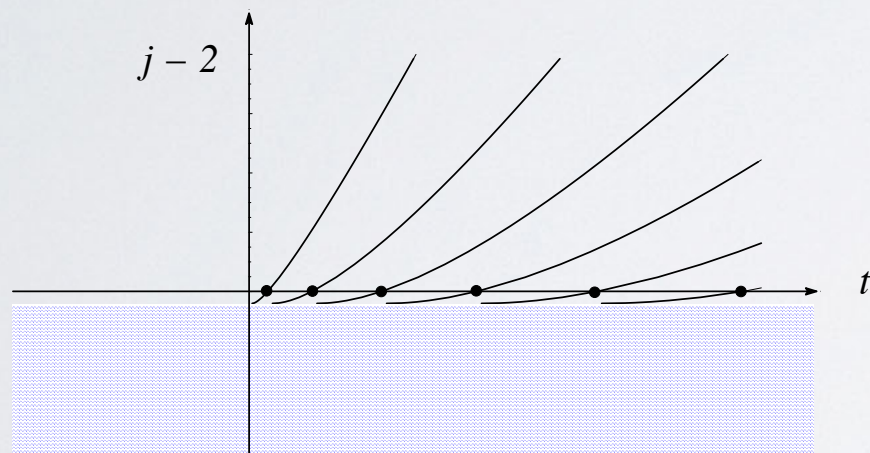
$$\lambda = g_{YM}^2 N$$

ADS POMERON VERTEX*

$$V^{Pomeron} = [\epsilon^\mu(k) \epsilon^\nu(k) P_\mu \bar{P}_\nu]^{1-k^2/4} : e^{ik^\mu (X_\mu + \bar{X}_\mu)} :$$



Δ plane meromorphy



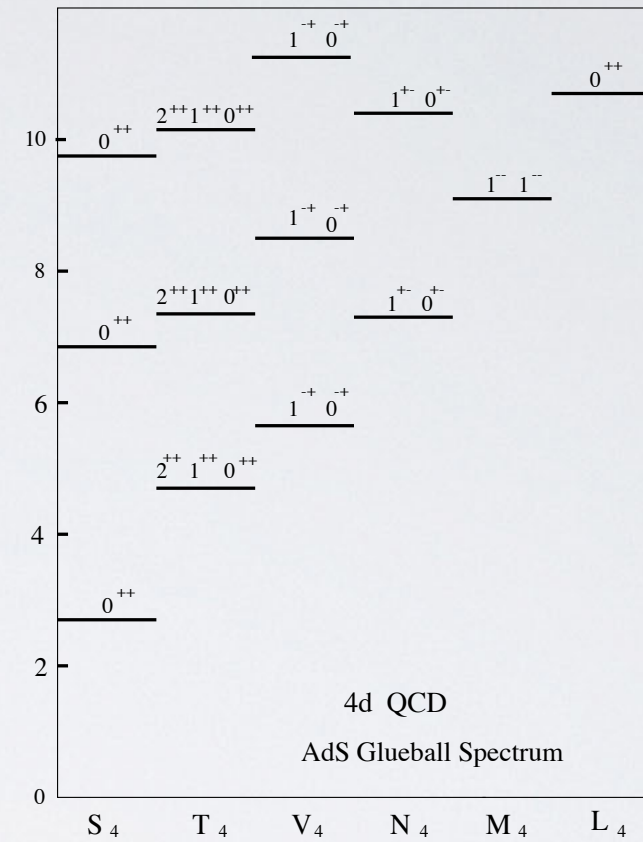
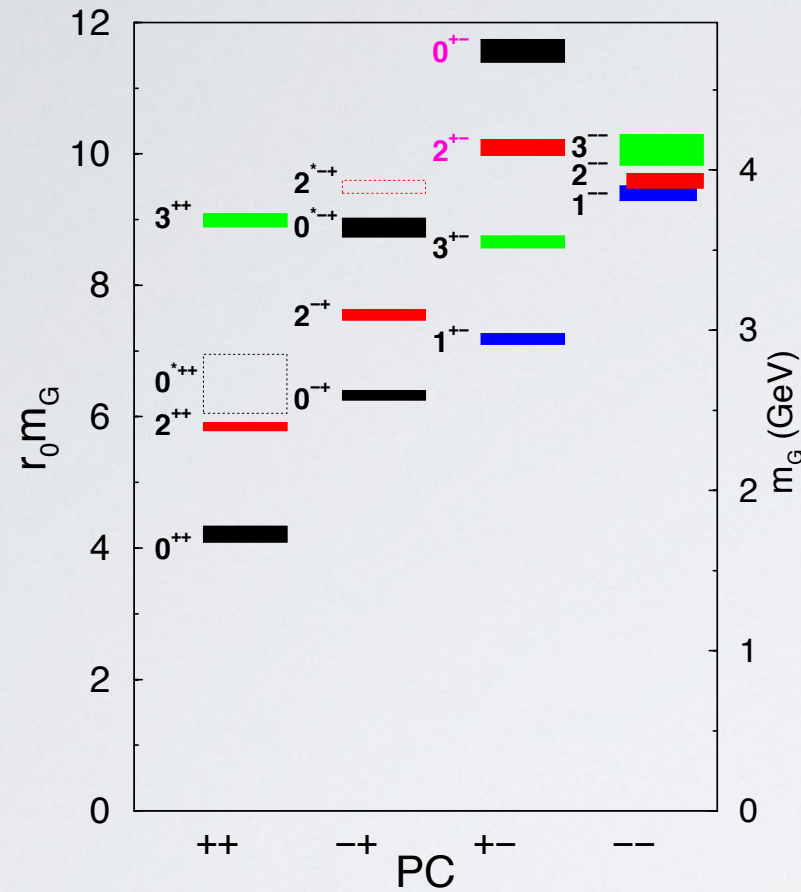
AdS/CFT “Regge”

pole Δ - plan but a cut in the **J**-plane

$$j_0 = \text{Min}[\Delta(\lambda)]$$

*The Pomeron and Gauge/String Duality, Brower, Polchinski, Strassler, Tan received 2006

VESTIGIAL SUSY ? : I GLUEBALLS



States from 11-d G_{MN}				States from 11-d A_{MNL}		
$G_{\mu\nu}$	$G_{\mu,11}$	$G_{11,11}$	m_0 (Eq.)	$A_{\mu\nu,11}$	$A_{\mu\nu\rho}$	m_0 (Eq.)
G_{ij} 2^{++}	C_i $1^{++}_{(-)}$	ϕ 0^{++}	4.7007 (T_4)	B_{ij} 1^{+-}	C_{123} $0^{+-}_{(-)}$	7.3059 (N_4)
$G_{i\tau}$ $1^{+-}_{(-)}$	C_τ 0^{-+}		5.6555 (V_4)	$B_{i\tau}$ $1^{--}_{(-)}$	$C_{ij\tau}$ 1^{--}	9.1129 (M_4)
$G_{\tau\tau}$ 0^{++}			2.7034 (S_4)	G_α^α State 0^{++}		10.7239 (L_4)

Table 1: IIA Classification for QCD_4 . Subscripts to J^{PC} designate $P_\tau = -1$.

Ramond-Ramond 2-form $C_{\mu\nu}$, NS NS 2-form field $B_{\mu\nu}$.

Glueball Spectrum for QCD for AdS Supergravity Dual,

IS NEVEU-SCHWARZ SUPER STRING

A N EFFECTIVE STRING THEORY (EST*) FOR QCD?

Factorizable Dual Model Of Pions,

Neveu and J. H. Schwarz, Nucl. Phys. B 31, 86 (1971)

Phenomenological six-pion amplitude,

R. Brower and G. Chu, Phys. Rev. D 7, 56 (1973). Phys. Rev. D 7, 56 (1973).

For $p_i^\mu \rightarrow 0$ has soft pion Adler zeros

$$A_{\pi^+\pi^-\rightarrow\pi^+\pi^-}(s,t) = g_0^2 \frac{\Gamma[1 - \alpha_\rho((t))]\Gamma[1 - \alpha_\rho(s)]}{\Gamma[1 - \alpha_\rho((t) - \alpha_\rho((s))]} \\ \sim g_0^2(s+t) \sim 0$$

*

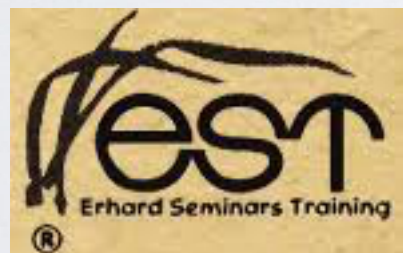


TABLE I. Meson spectrum. The experimental masses and widths are in square brackets, and are taken from the Review of Particle Properties.^a

Name	$I^G(J^P)$	Mass M (MeV)	Partial width Γ (MeV)	Mode
π	$1^-(0^-)$	137 ^b [137]		
σ	$0^+(0^+)$	760 [~ 800]	756[$\gg 100$]	2π
ρ	$1^+(1^-)$	760 [765]	145 ^b [145]	2π
ω	$0^-(1^-)$	784 ^b [784]	6[9]	3π
π'	$1^-(0^-)$	1060[NE] ^c	1100[NE]	3π
H	$0^-(1^+)$	1060[990]	180[?]	3π
A_1	$1^-(1^+)$	1060[1070]	154	$\rho\pi$
			2	$\sigma\pi$
			165[100–200]	3π ^d
σ'	$0^+(0^+)$	1300 ^e	–17 ^e	2π
ρ'	$1^+(1^-)$	1300[NE]	145[NE]	2π
f	$0^+(2^+)$	1300[1269]	124[125]	2π
			[12] ^f	4π
A_2	$1^+(2^+)$	1315[1310]	7.5[75]	$\rho\pi$
π_A	$1^-(2^-)$	1500[1640]	[108] ^f	3π
g	$1^+(3^-)$	1670[1680]	48[64]	2π
			[80] ^f	4π

QUESTIONS?

