



# Standard model extensions for PV electron scattering, $g-2$ , EDM: *Overview*

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# Outline

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- **Parity violation in electron scattering atoms and ions**
- **Electric Dipole Moments**

# The *SM* and Beyond

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  - discovery of weak neutral currents
  - *PVeDIS (consistent with  $\nu$  scattering) SLAC-E-122 (1978)*
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  - $P\nu eDIS$  (consistent with  $\nu$  scattering) *SLAC-E-122 (1978)*
  - discovery of W and Z bosons
- SM as spontaneously broken, renormalizable QFT established — **before Higgs discovery** — through
  - high precision Z factories *LEP* & *SLC* (also *Tevatron*)

# Status

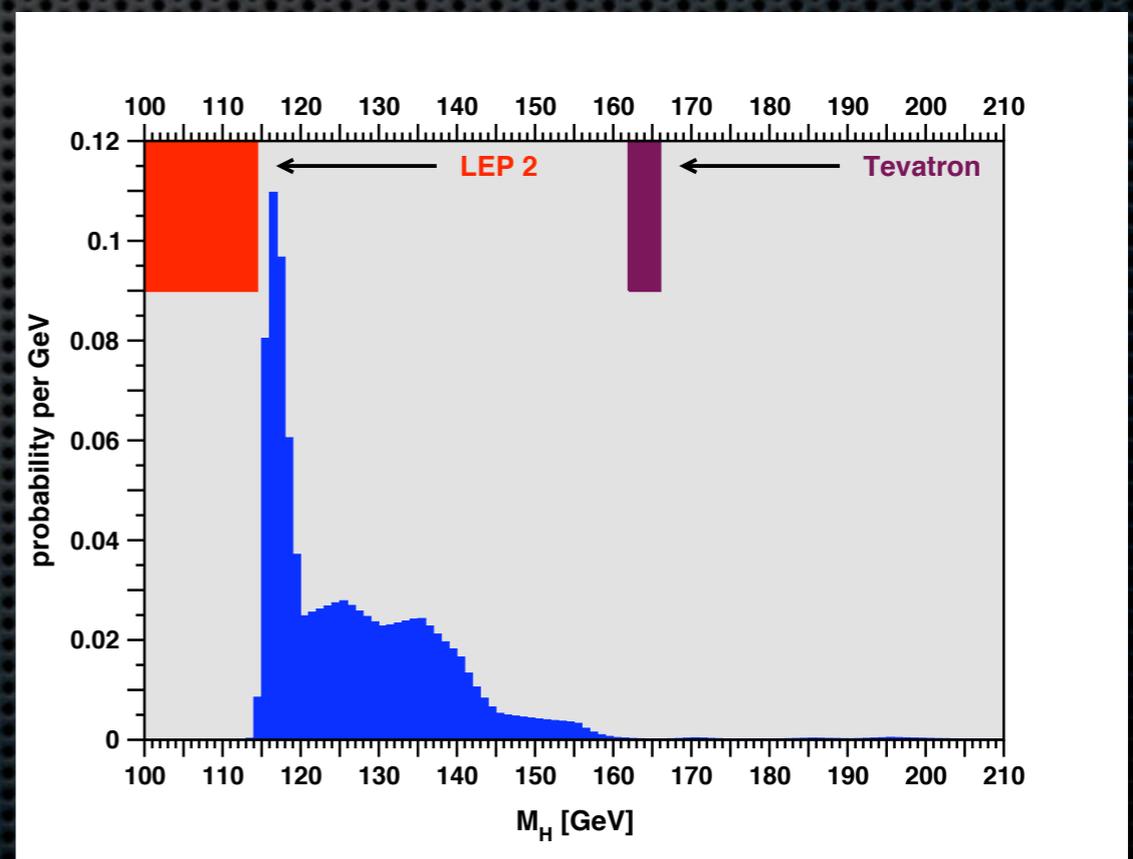
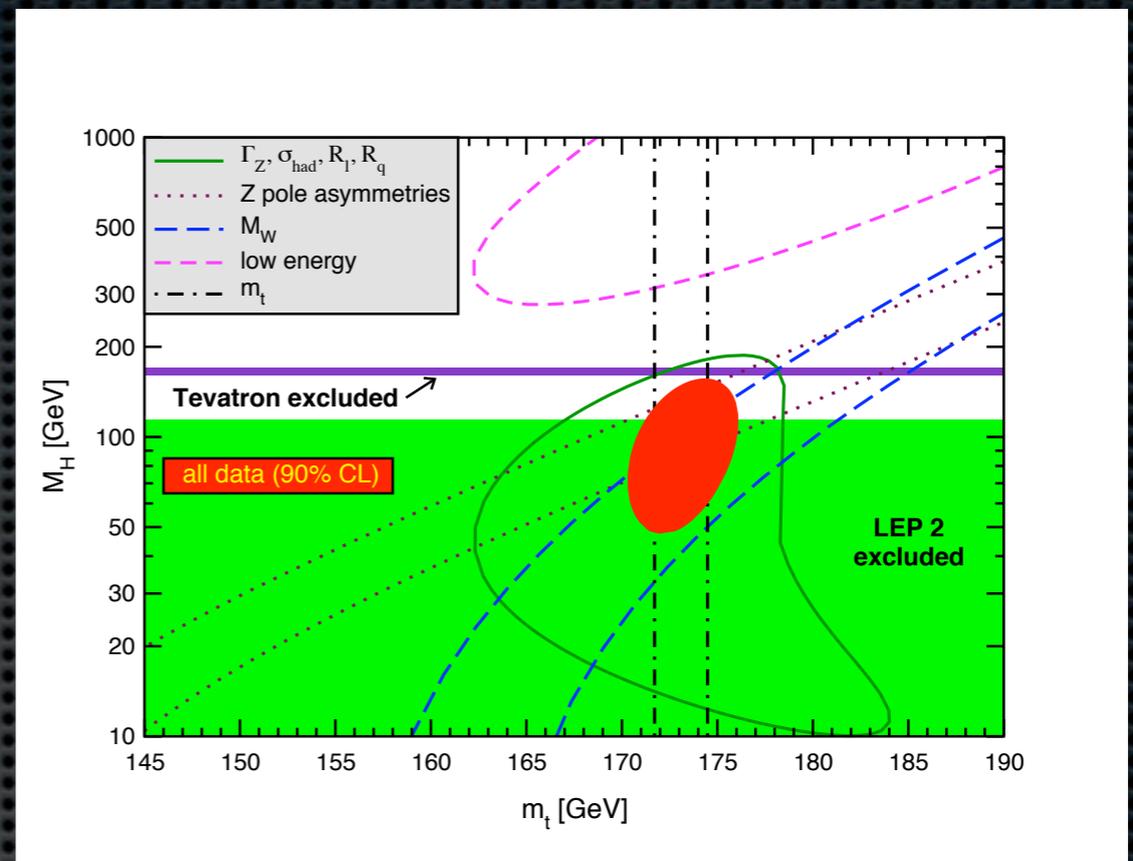
- closing in on the Higgs

👉 *talk by Daniele del Re*

consistent (sadly) with  
precision constraints

- small deviations occur,  
but nothing conclusive

- $m_\nu$  just dimension 5  
HH $\bar{L}$ -operator?



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- arbitrariness of gauge group, multiplets & parameters, but tantalizing hints at unification structure ( $E_6$  & subgroups) and gauge coupling unification (in MSSM)
- overriding goal: finding principles underlying the SM

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1	H=1							
2	Li=7	Be=9,4	B=11	C=12	N=14	O=16	F=19	
3	Na=23	Mg=24	Al=27,3	Si=28	P=31	S=32	Cl=35,5	
4	K=39	Ca=40	—=44	Ti=48	V=51	Cr=52	Mn=55	Fe=56, Co=59, Ni=59, Cu=63.
5	(Cu=63)	Zn=65	—=68	—=72	As=75	So=78	Br=80	
6	Rb=86	Sr=87	?Yt=88	Zr=90	Nb=94	Mo=96	—=100	Ru=104, Rh=104, Pd=106, Ag=108.
7	(Ag=108)	Cd=112	In=113	Sn=118	Sb=122	Te=125	J=127	
8	Cs=133	Ba=137	?Di=138	?Ce=140	—	—	—	
9	(—)	—	—	—	—	—	—	
10	—	—	?Er=178	?La=180	Ta=182	W=184	—	Os=195, Ir=197, Pt=198, Au=199.
11	(Au=199)	Hg=200	Tl=204	Pb=207	Bi=208	—	—	
12	—	—	—	Th=231	—	U=240	—	

*Mendeleev (1871)*

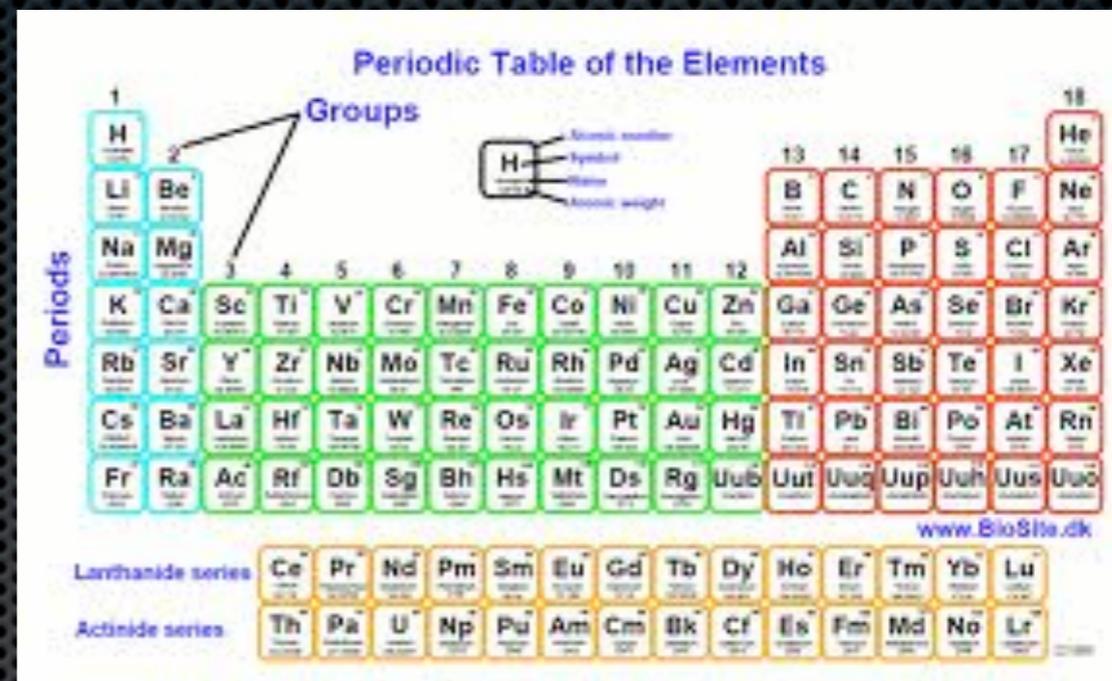
**Periodic Table of the Elements**

The image shows a modern periodic table with the following features:

- Groups:** Labeled 1 through 18 at the top.
- Periods:** Labeled 1 through 7 on the left side.
- Legend:** A box for Hydrogen (H) shows its symbol, atomic number (1), name, and atomic weight.
- Color Coding:** Groups 1-2 are blue, groups 3-10 are green, groups 11-12 are yellow, and groups 13-18 are red.
- Lanthanide series:** A row of elements from Ce to Lu below group 2.
- Actinide series:** A row of elements from Th to Lr below the lanthanide series.
- Source:** www.BioSite.dk

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$V_\mu$ $s=1/2$	$\mu^-$ $s=1/2$	$\mu^+$ $s=1/2$	$c$ $s=1/2$	$c$ $s=1/2$	$c$ $s=1/2$	$\bar{c}$ $s=1/2$	$\bar{c}$ $s=1/2$	$\bar{c}$ $s=1/2$	$s$ $s=1/2$	$s$ $s=1/2$	$s$ $s=1/2$	$\bar{s}$ $s=1/2$	$\bar{s}$ $s=1/2$	$\bar{s}$ $s=1/2$
$V_e$ $s=1/2$	$e^-$ $s=1/2$	$e^+$ $s=1/2$	$u$ $s=1/2$	$u$ $s=1/2$	$u$ $s=1/2$	$\bar{u}$ $s=1/2$	$\bar{u}$ $s=1/2$	$\bar{u}$ $s=1/2$	$d$ $s=1/2$	$d$ $s=1/2$	$d$ $s=1/2$	$\bar{d}$ $s=1/2$	$\bar{d}$ $s=1/2$	$\bar{d}$ $s=1/2$
$H$ $s=0$	$H^\pm$ $s=0$	$Z$ $s=1$	$W^-$ $s=1$	$W^+$ $s=1$	$g$ $s=1$	$g$ $s=1$	$g$ $s=1$	$g$ $s=1$	$g$ $s=1$	$g$ $s=1$	$g$ $s=1$	$g$ $s=1$	$Y$ $s=1$	$G$ $s=2$

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  - $\Lambda_{\text{new}} \approx 3.4 \text{ TeV}$  (E158)
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- EM dipole moments:  $L = \frac{1}{2} [D \bar{\psi} \sigma_{\mu\nu} P_R \psi + \text{H.c.}] F^{\mu\nu}$ 
  - $\Re D = e a / (2 m) \Rightarrow \Lambda_{\text{new}} \approx m_\mu / \sqrt{\Delta a_\mu} = 3.8 \text{ TeV}$  (MDM)
  - $\Im D = d \Rightarrow \Lambda_{\text{new}} \approx \sqrt{(e m_e / 2 \Delta d_e)} = 83 \text{ TeV}$  (EDM)
  - $\mu \rightarrow e$  conversion:  $\Lambda_{\text{new}} \approx 130 \text{ TeV}$  (transition moment)

Illustrative example:  
supersymmetric extensions

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- **theory:** unique extension of Poincaré group
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  - elegant solution to hierarchy problem (makes sense also in combination with other ideas like **LEDs**)
- **observation:** gauge coupling unification (one-loop)
  - solid prediction for a light Higgs ( **$M_H \approx 150 \text{ GeV}$** )
  - natural radiative EW symmetry breaking for large  $m_t$
  - dark matter candidate

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- little hierarchy problem (fine tuning)

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- **SUSY** may itself be merely one ingredient to stabilize other types of possible TeV scale physics (like **LEDs**)

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- $\Delta a_{\mu}(\tau) - \Delta a_{\mu}(e^{+} e^{-}) = (0.91 \pm 0.50) \times 10^{-9}$  (**1.8  $\sigma$** )  
*Davier, Höcker, Malaescu, Zhang (2010)*

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- $\Delta a_{\mu}(\gamma \times \gamma) = (1.05 \pm 0.26) \times 10^{-9}$  (included above)  
*Prades, de Rafael, Vainshtein (2009)*
- $\Delta a_{\mu}(\gamma \times \gamma) < 1.59 \times 10^{-9}$  (95% CL) *JE, Toledo (2006)*

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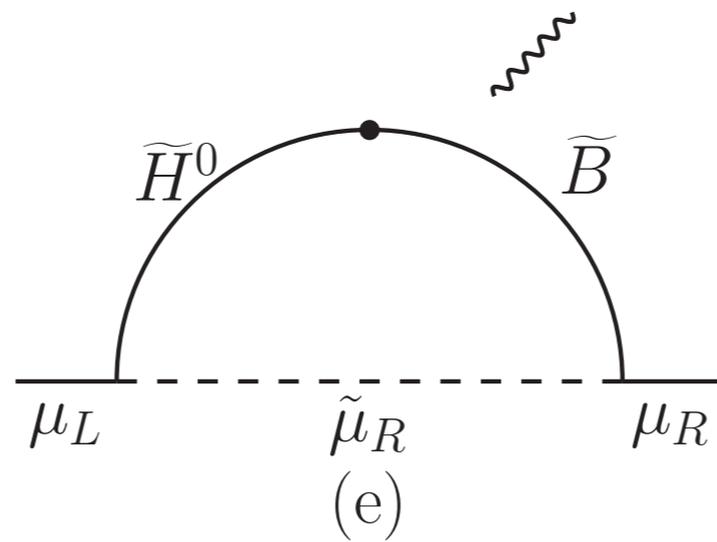
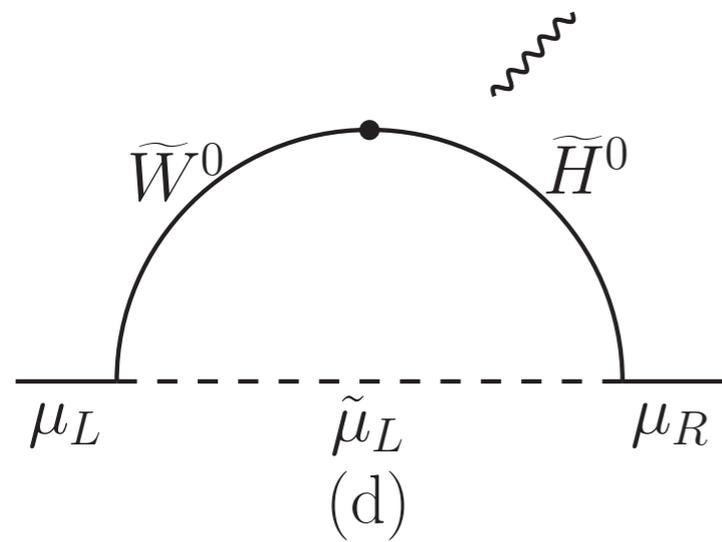
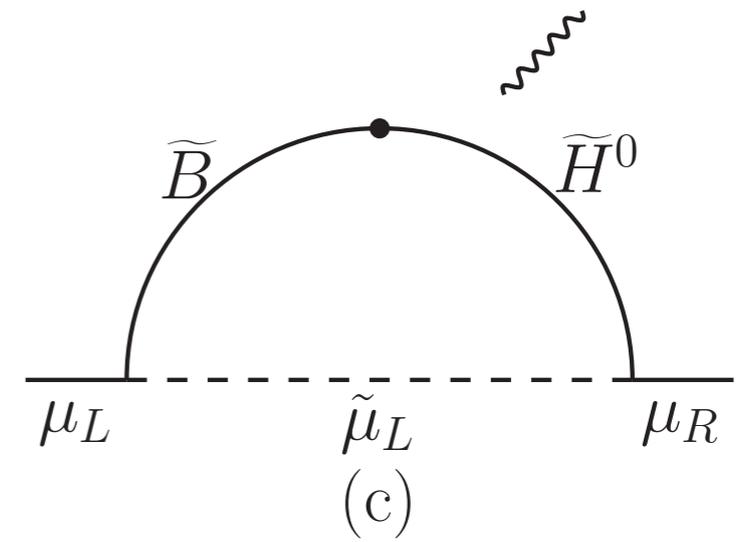
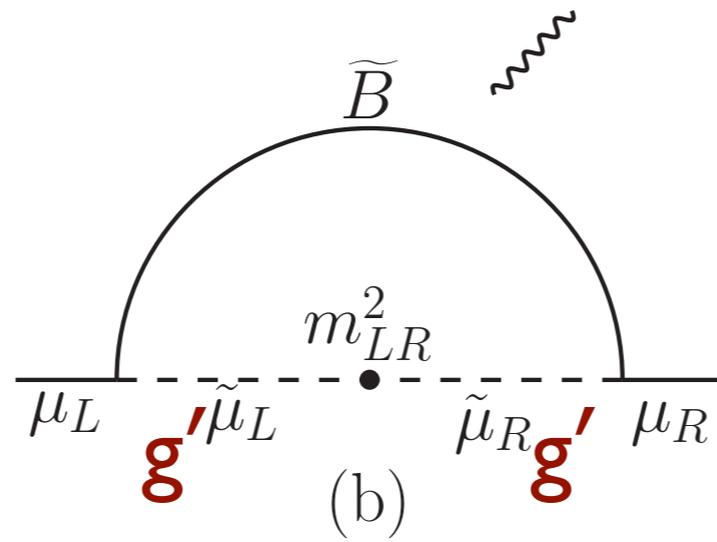
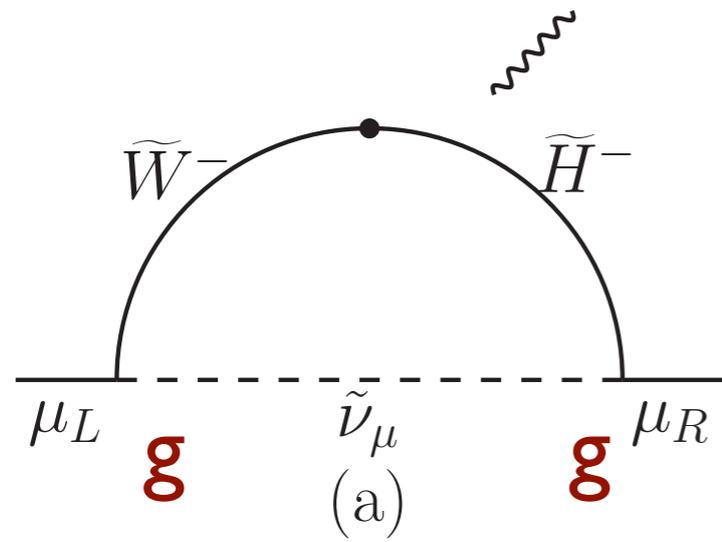
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can be pushed below  $3 \times 10^{-10}$  then  $5 \sigma$  discovery would be established (if central value does not change)

( $\gamma \times \gamma$  already there but hardest to defend)

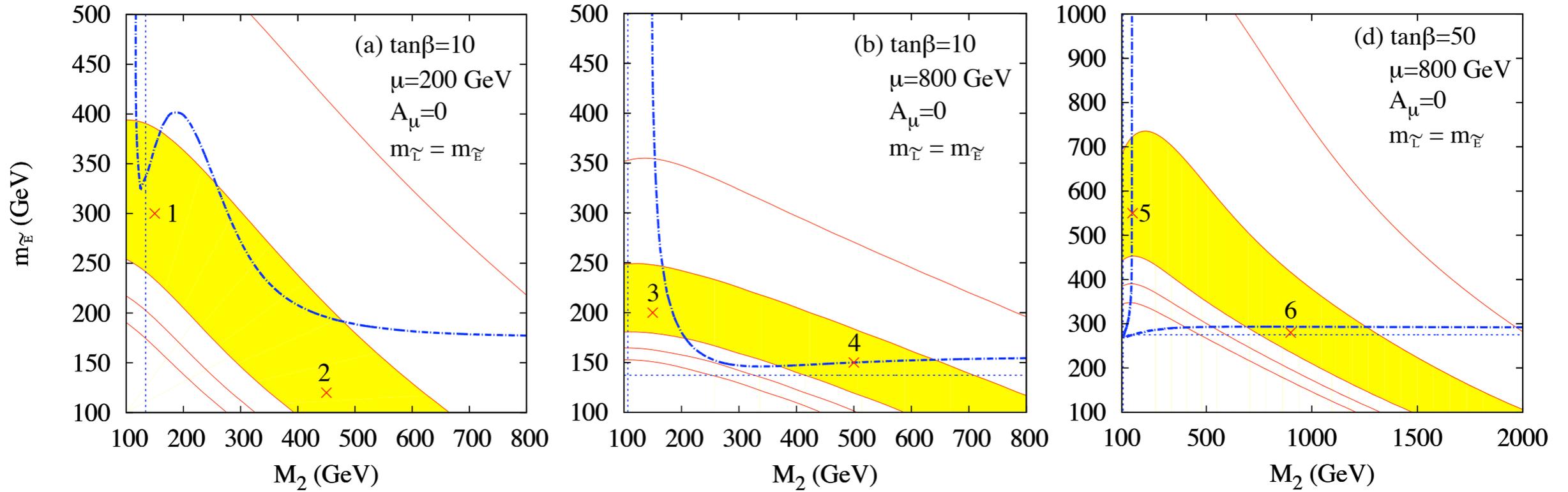
# $g_{\mu-2}$ in the MSSM



$$\propto g^2 / 8\pi \tan\beta$$

$$(m_\mu / M_{\text{SUSY}})^2$$

*Cho, Hagiwara,  
Matsumoto, Nomura (2011)*



No.	$\tan \beta$	$\mu$	$M_2$	$m_{\tilde{E}}$	(a)	(b)	(c)	(d)	(e)	(a)-(e)	total	pull
1	10	200	150	300	29.6	1.1	0.7	-2.9	-1.3	27.2	25.0	-0.1
2	10	200	450	120	27.5	8.8	3.3	-7.1	-6.7	25.9	25.9	0.0
3	10	800	150	200	14.3	16.2	0.6	-2.7	-1.3	27.1	27.1	0.1
4	10	800	500	150	6.9	21.3	1.0	-2.5	-2.1	24.7	24.3	-0.2
5	50	800	150	550	26.9	2.4	0.5	-2.6	-1.0	26.3	26.0	0.0
6	50	800	900	280	18.0	18.0	2.5	-5.9	-5.1	27.7	27.6	0.2

$(\delta a_\mu \times 10^{-10})$

*Cho, Hagiwara, Matsumoto, Nomura (2011)*

# Practical example: gauge extensions

$Z'$  bosons

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- discrimination: angular distribution can indicate spin
- diagnostics: charges can hint at underlying principles

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  - the  $U(1)'$  forbids dimension 4 proton decay *JE (2000)*

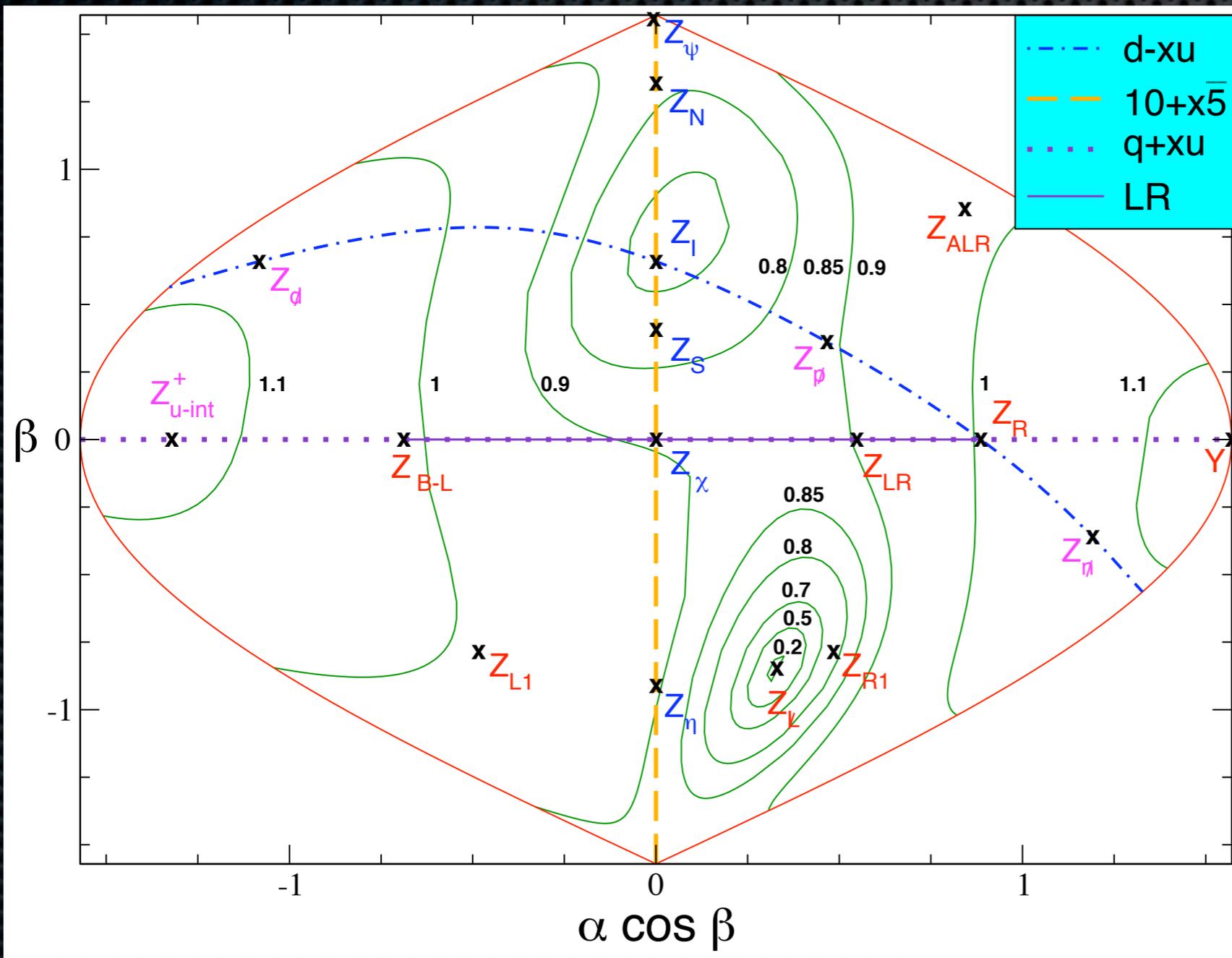
# $Z'$ bosons from $E_6$

- $E_6 \rightarrow SO(10) \times U(1)_\psi \rightarrow SU(5) \times U(1)_X \times U(1)_\psi$
- $Z' = \cos\alpha \cos\beta Z_X + \sin\alpha \cos\beta Z_Y + \sin\beta Z_\psi$   
 $\sim C_1 Z_R + \sqrt{3} (C_2 Z_{R1} + C_3 Z_{L1})$
- kinetic mixing:  $\alpha \neq 0 \sim F^{\mu\nu} F'_{\mu\nu}$
- trinification:  $E_6 \rightarrow SU(3)^3 \rightarrow$   
 $SU(3)_C \times SU(2)_L \times U(1)_{L1} \times SU(2)_R \times U(1)_{R1}$
- classification in progress *JE, Rojas (2011)*

# $Z'$ charges in $E_6$ models

l	$\nu$	$-2C_2$	$-C_3$	$\bar{\nu}$	$-C_1$	$+C_2$	$+2C_3$
	$e^-$			$e^+$	$+C_1$	$+C_2$	$+2C_3$
q	u	$+C_3$	$\bar{u}$	$-C_1$	$-C_2$		
	d		$\bar{d}$	$+C_1$	$-C_2$		
L	N	$-C_1$	$+C_2$	$-C_3$	D		$-2C_3$
	$E^-$				$\bar{D}$	$+2C_2$	
$\bar{L}$	$E^+$	$+C_1$	$+C_2$	$-C_3$	S	$-2C_2$	$+2C_3$
	$\bar{N}$						

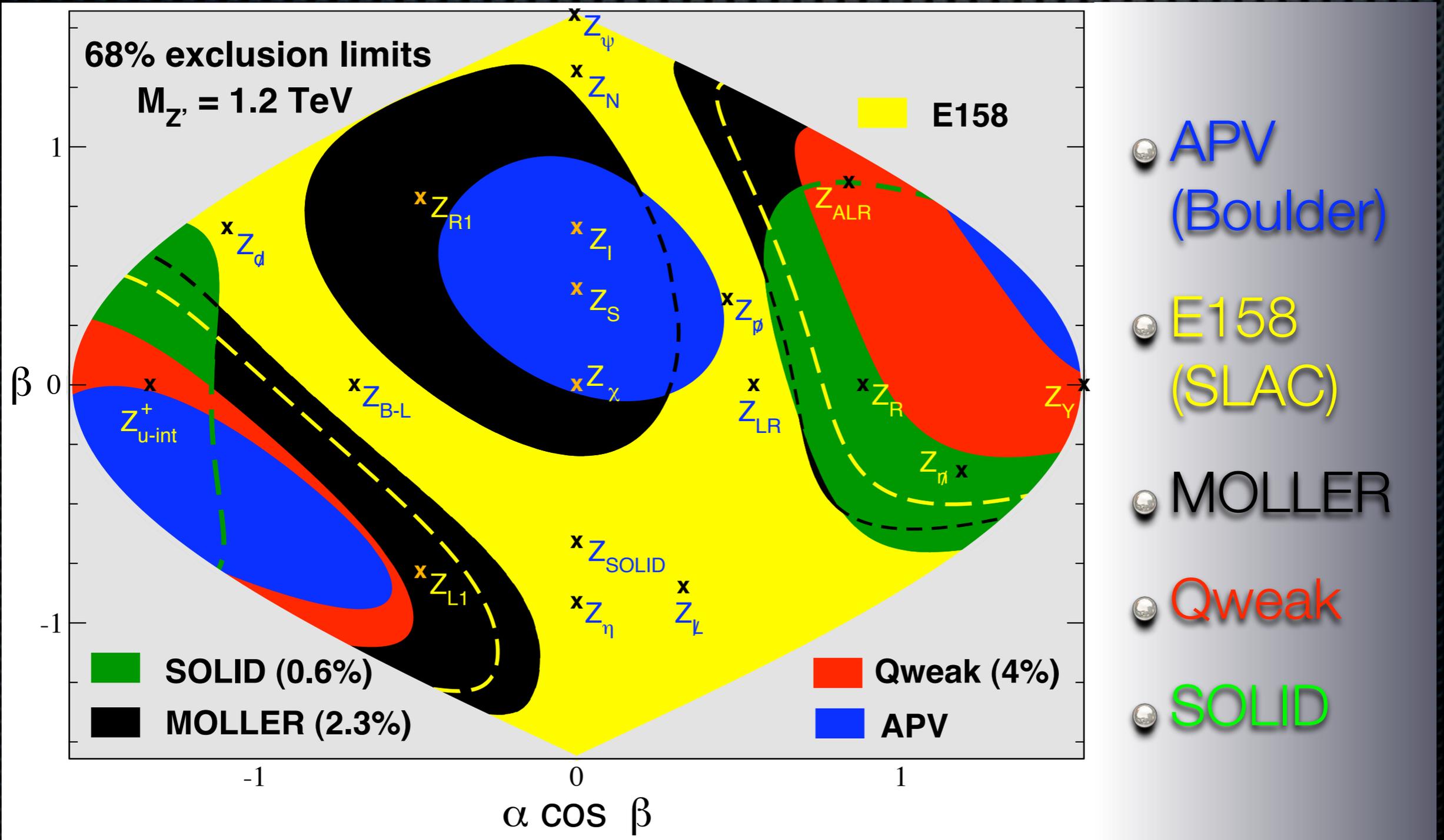
# $E_6$ inspired models



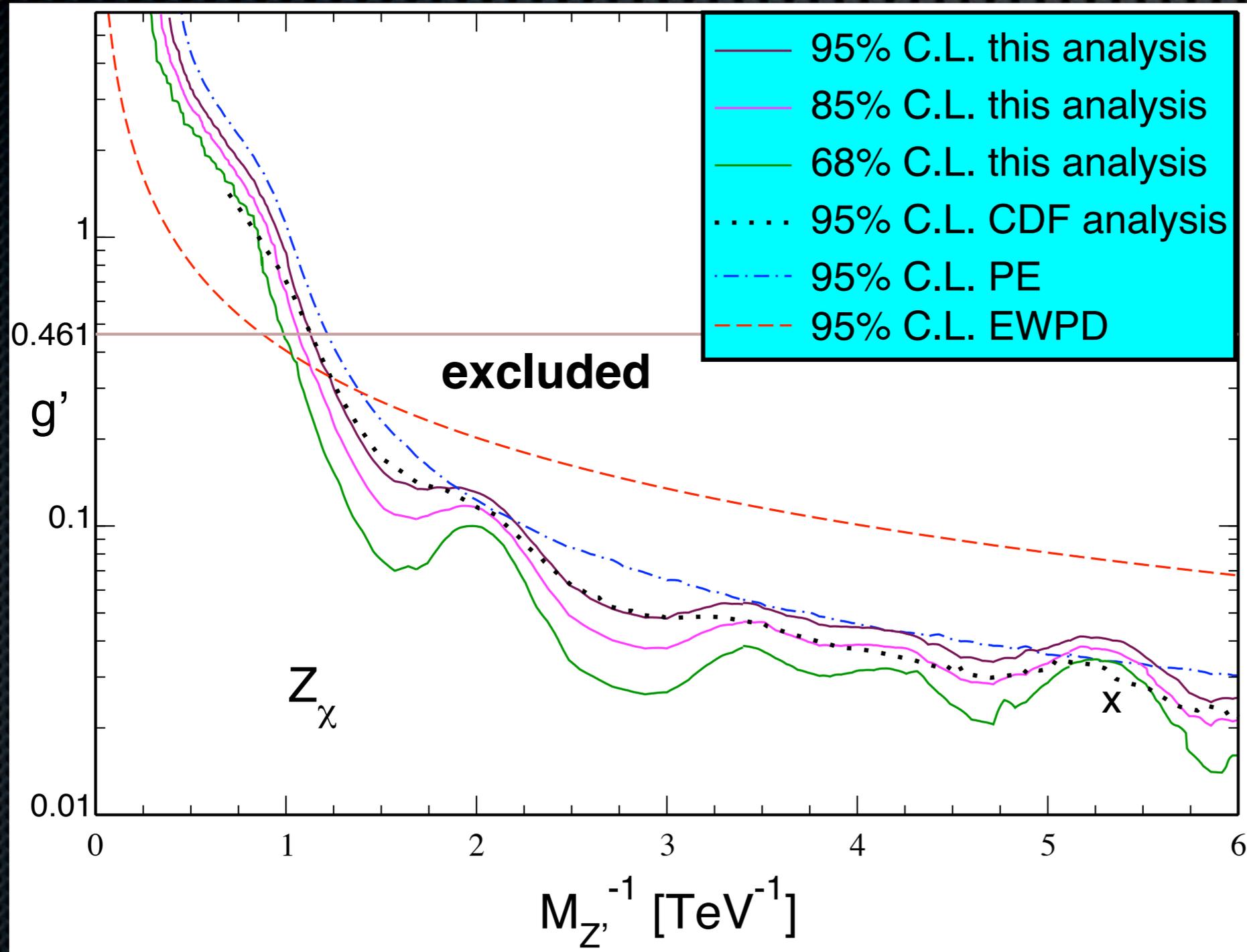
- horizontal line:  
SO(10)  
(including  
left-right)  
models
- vertical line:  
no kinetic  
mixing
- blue line:  
 $U(1)_{d-xu}$

# Parity violation in electron scattering atoms and ions

# E<sub>6</sub> models & parity violation

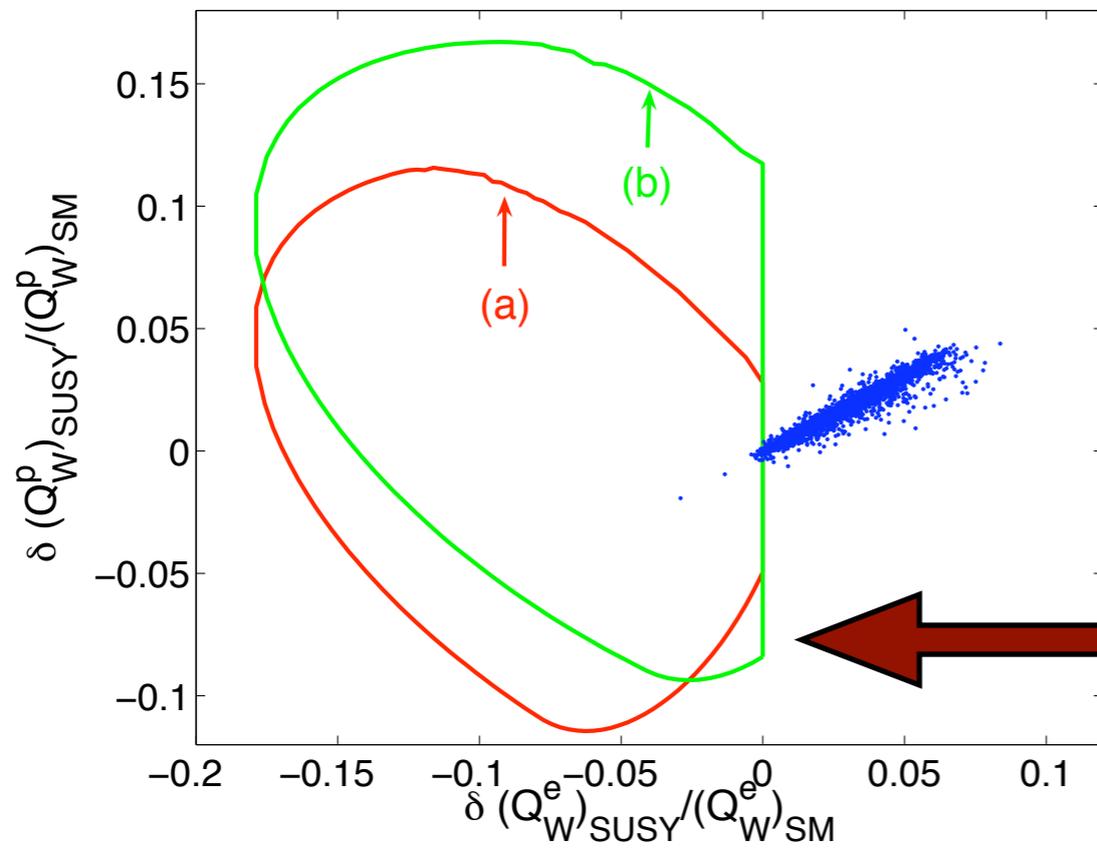


# Comparative analysis of the $Z_\chi$



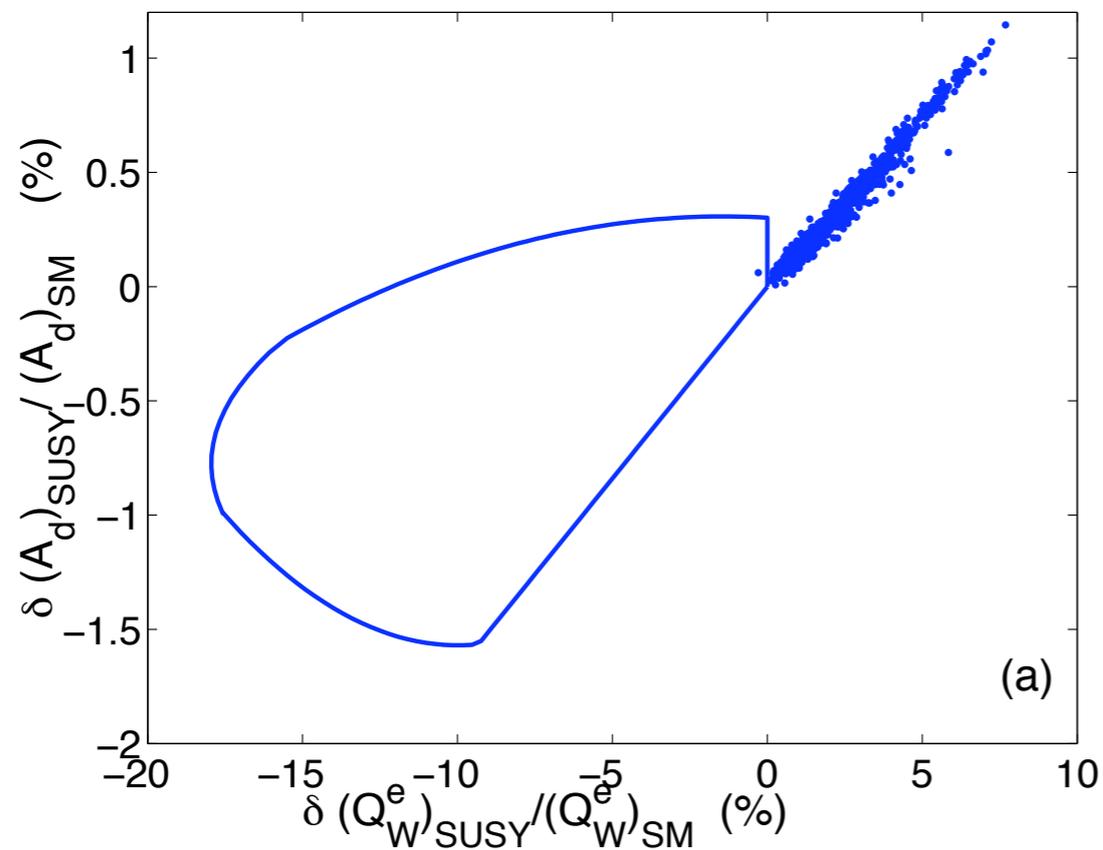
electroweak  
precision  
data  
complement  
di-lepton  
channel  
analyses

# $e^-$ scattering and SUSY

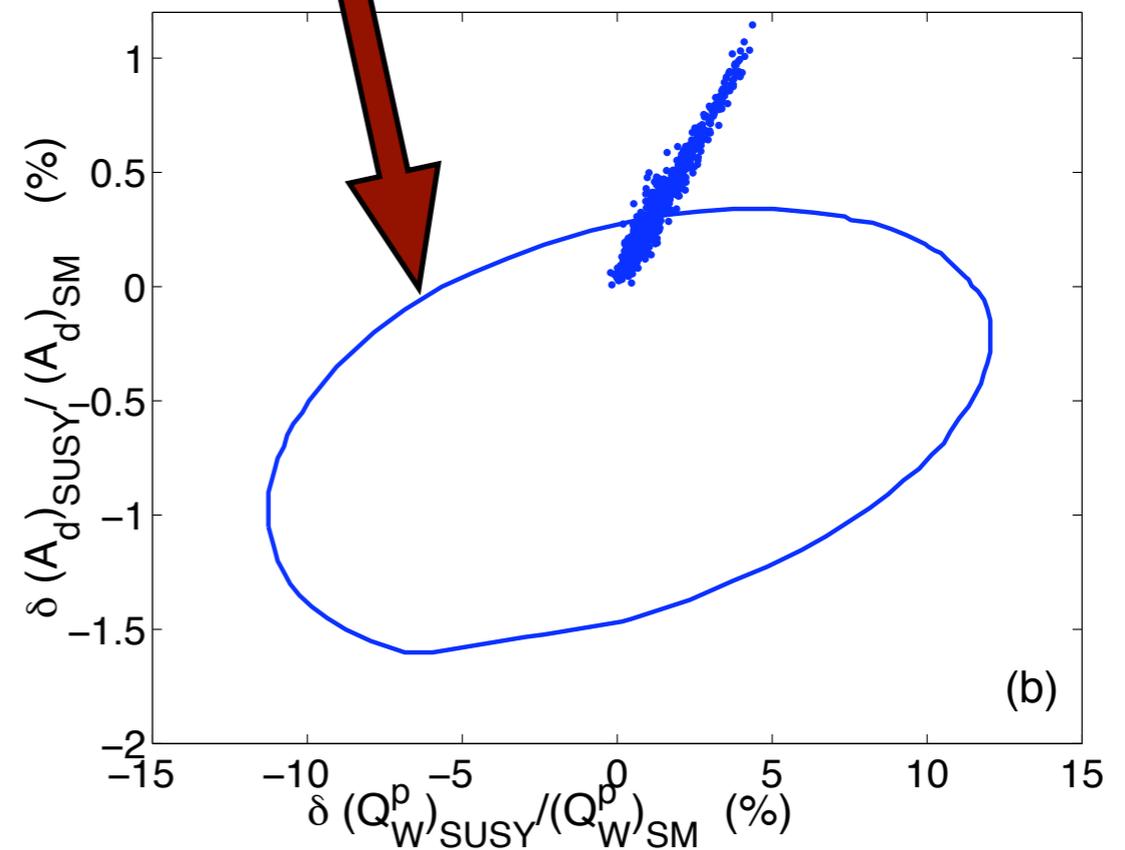


~~RP~~

*Ramsey-Musolf,  
Su (2006)*



(a)



(b)

# Weak Charges & New Physics

$$Q_W^p = 0.0716$$

$$\text{---} \bigcirc \text{---} \pm 0.0029$$

Experiment

SUSY Loops

$E_6$   $Z'$

RPV SUSY

Leptoquarks

SM

*JE, Ramsey-Musolf (2003)*

$$Q_W^e = -0.0449$$

$$\text{---} \bigcirc \text{---} \pm 0.0051$$

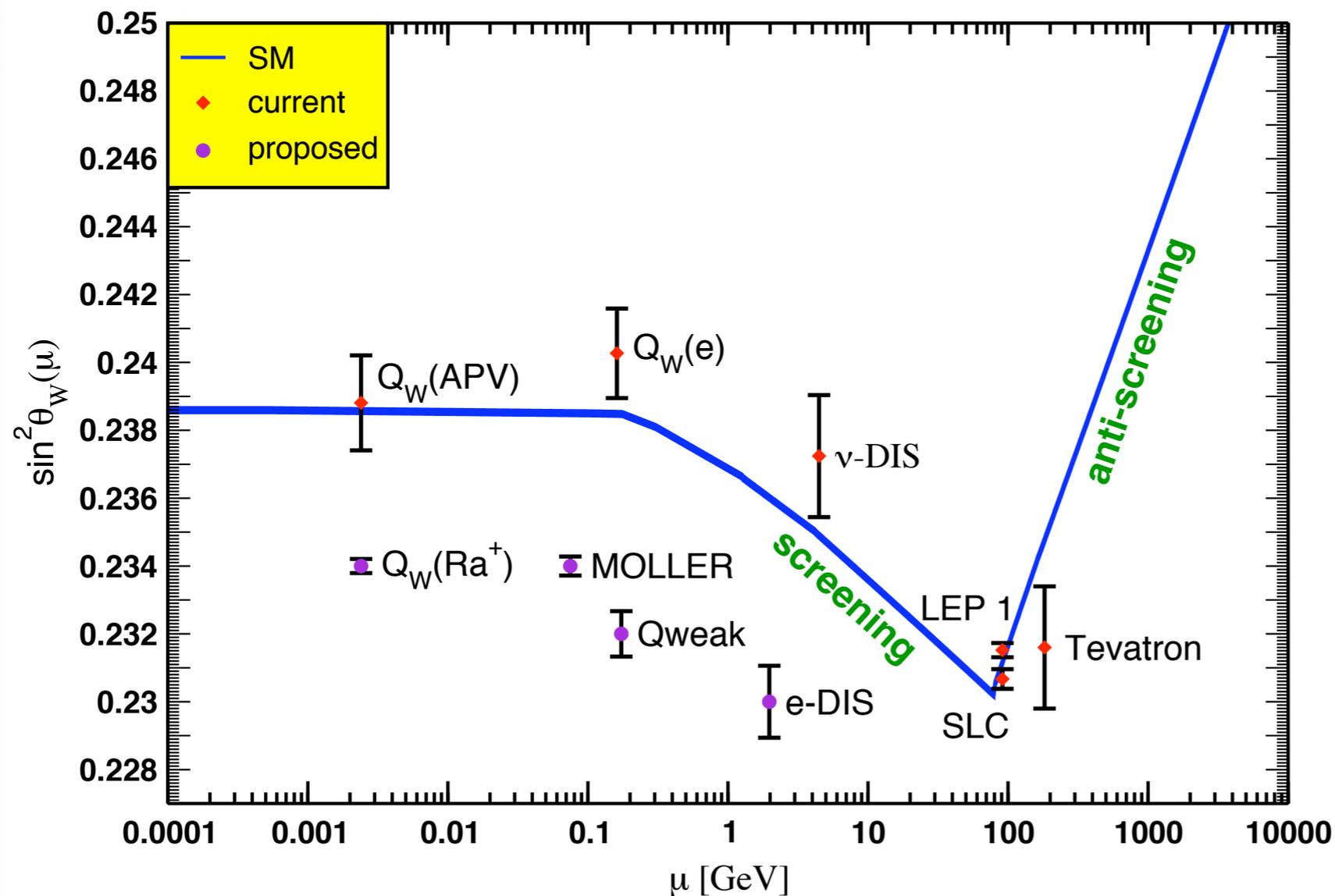
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# Running weak mixing angle



uncertainty  
in prediction  
is small  
except  
possibly in  
the hadronic  
transition  
region *JE,*  
*Ramsey-Musolf*  
*(2005)*

# Electric Dipole Moments

# EDMs and CP violation

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- SM:  $|d_n| \approx 10^{-19} \text{ e fm}$  *McKellar, Choudhury, He, Pakvasa (1987)*



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- analogous logs enter chromo-electric *de Vries, Timmermans, Mereghetti, van Kolck (2010)* and gravitational dipole moments

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- $\bar{\theta} \lesssim 10^{-10}$

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- consider simple toy model

*Grojean, Servant, Wells (2004); Huber, Pospelov, Ritz (2005)*

$$L = (H^\dagger H)^3 / \Lambda^2 + Z_t (H^\dagger H) \bar{Q}_3 H t$$

$\Rightarrow \eta_B \sim 10^{-10}$  if  $\Lambda_{CP} \sim 400 \dots 800 \text{ GeV}$ , while next generation of EDM experiments will probe  $\Lambda_{CP} \sim 3 \text{ TeV}$ !

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- SUSY thresholds:  $\Lambda \gtrsim 10^5 \text{ TeV}$  *Pospelov, Ritz, Santoso (2005)*

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- scenario 2: nothing or little beyond the Higgs at LHC
  - use ultra-high precision  $Møller$ ,  $APV$  &  $EDM$  efforts to see if new physics is pushed up by merely a little hierarchy – such as in little and littlest Higgs theories  
*Arkani-Hamed, Cohen, Georgi (2001);*  
*Arkani-Hamed, Cohen, Katz, Nelson (2002)*

# Summary and outlook

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- scenario 2+: beyond that, need SM rare and forbidden processes from CP (**EDMs**) and flavor sectors
  - 👉 *talk by Toshio Numao* to study PeV region
- these observables have fantastic reach
- but single number measurements (no cross checks)
- on the other hand, no “look elsewhere effect”
- **nEDM** by itself — while a breakthrough in its own right ( **$\theta_{\text{QCD}}$** ) — not enough to establish new physics