

# Hard Diffraction: from HERA to LHC

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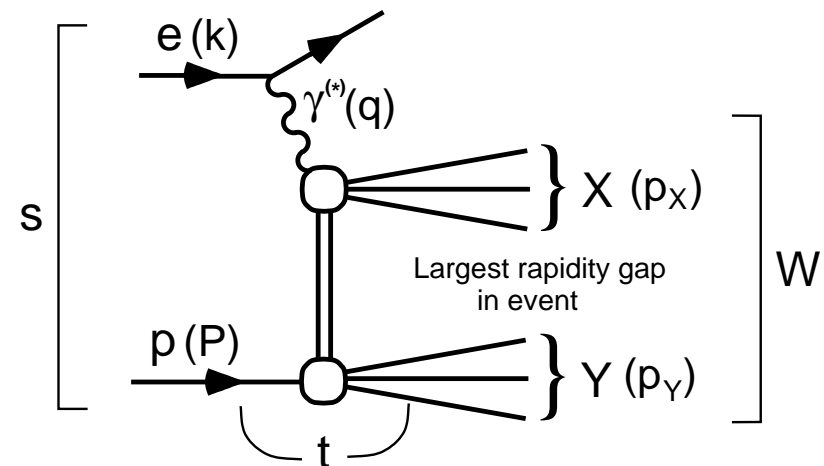
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## Outline

- Hard diffraction in DIS
- Theoretical framework: factorisation and evolution
- Factorisation tests at HERA
- Preliminary diffractive PDFs from combined HERA proton-tagged data
- Hard diffraction at hadron colliders

## Hard diffraction in DIS

- **Experiment**
  - (hard) diffraction rebirth at HERA
  - $e(k) + p(P) \rightarrow e(k') + p(P') + X$
- **kinematics**
  - Target fragmentation region
  - $|t| \leq 1 \text{ GeV}^2$
  - $x_{\mathbb{P}} \simeq 1 - E_{P'}/E_P < 0.1$
- **diffractive selection:**
  - large rapidity gap
  - $M_X$ -method
  - proton tagging
- **Key features**
  - Leading twist:  $\mathcal{O}(Q^{-4})$  (as iDIS)
  - scaling violations  $\rightarrow$  parton dynamics



## Theory setup in DDIS

- Hard-scattering factorisation:

$$F_k^{D(3)}(\beta, Q^2, x_{\mathcal{I}}) = \sum_i \int_{\beta}^1 \frac{d\xi}{\xi} M_i(\beta, \mu_F^2; x_{\mathcal{I}}) C_{ki}\left(\frac{\beta}{\xi}, \frac{Q^2}{\mu_F^2}, \alpha_s(\mu_R^2)\right) + \mathcal{O}\left(\frac{1}{Q^2}\right)$$

Grazzini, Trentadue, Veneziano'98, Collins '98

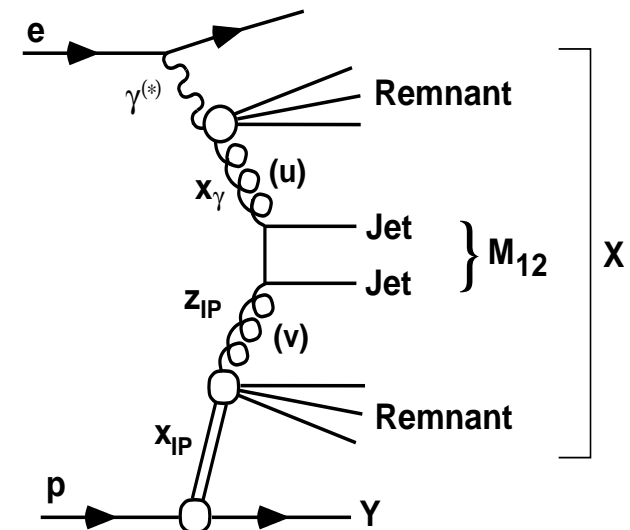
- $C_{ki}$  ( $k = 2, L$ ) calculable as a power expansion  $\alpha_s$ , same as in iDIS
- Diffractive parton distributions:  $M_i(\beta, \mu_F^2, x_{\mathcal{I}})$
- Partonic structure of the colourless exchange
- DPDFs obey DGLAP evolution equations

$$Q^2 \frac{\partial M_i(\beta, Q^2, x_{\mathcal{I}})}{\partial Q^2} = \frac{\alpha_s(Q^2)}{2\pi} \int_{\beta}^1 \frac{du}{u} P_{ji}(u) M_j\left(\frac{\beta}{u}, Q^2, x_{\mathcal{I}}\right)$$

- Phenomenological analyses of DPDFs via pQCD fits of DDIS data

## Factorisation in hard diffraction: overview

- Diffractive PDFs have been used to test hard-scattering factorisation in
  - dijet in DIS
  - dijet in PHP ( $Q^2 \simeq 0$ ,  $E_T \sim 5, 6$  GeV)
  - dijet or  $W^\pm$  in  $p\bar{p}$  collisions
  
- Results:
  - dijet in DIS:  $\text{data/NLO} \simeq 1$
  - dijet in PHP: debated  
 H1 reports violation:  $\text{data/NLO} \simeq 0.5$   
 ZEUS consistent with no violation:  $\text{data/NLO} \simeq 1$
  - $pp$  : Striking breakdown confirmed at Tevatron:  $\text{data/NLO} \simeq 0.1$
  
- NB: Factorisation predicted to fail in Resolved PHP and hadronic collisions



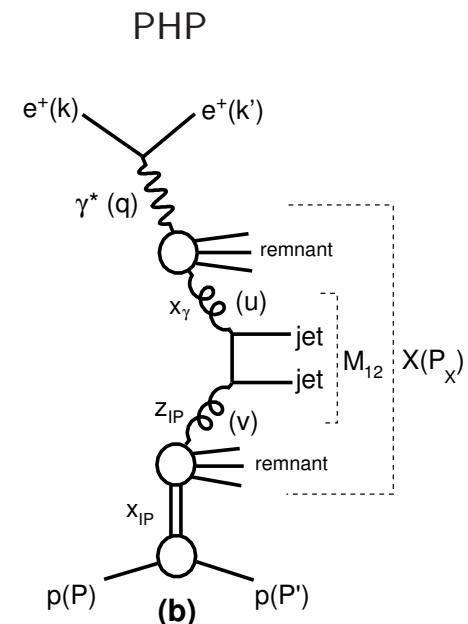
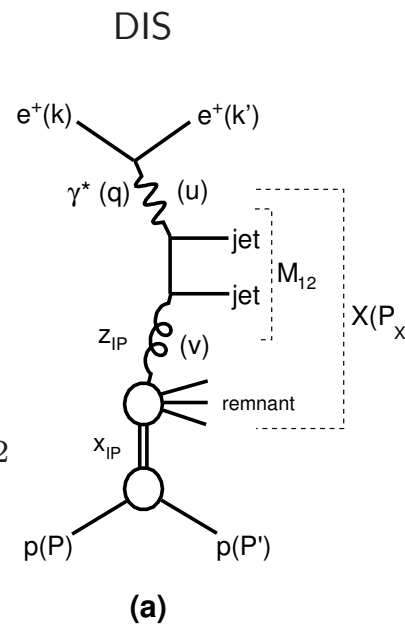
## Most recent factorisation tests at HERA

- Focus on the latest H1 results : DESY-14-242

1. Event phase space:  
 PHP :  $Q^2 < 2 \text{ GeV}^2$   
 DIS :  $4 \text{ GeV}^2 < Q^2 < 80 \text{ GeV}^2$
2. diffractive phase space:  
 $0.010 < x_{\mathbb{P}} < 0.024$
3. jet phase space:  
 $E_T^{*\text{jet}1(2)} > 5.5(4.0) \text{ GeV}$

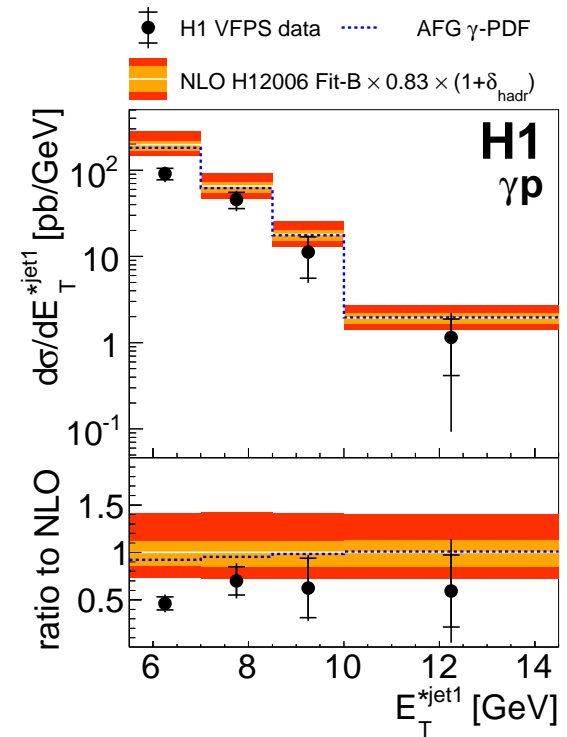
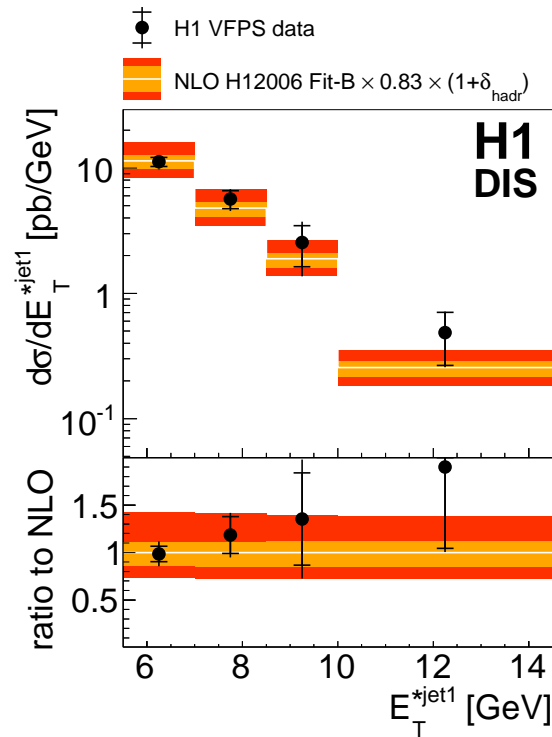
- Theory

1. NLO accuracy
2. scale set to  $\mu_R^2 = \mu_F^2 = \langle E_T^{*\text{jet}} \rangle^2 + Q^2$
3. Theo uncertainty:  $\mu \rightarrow 0.5\mu, 2.0\mu$
4. DPDFs from previous H1 '06 analysis



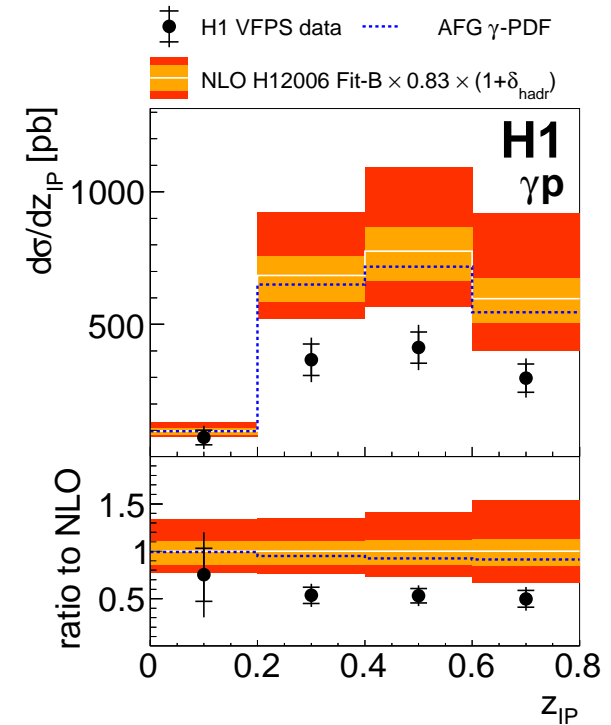
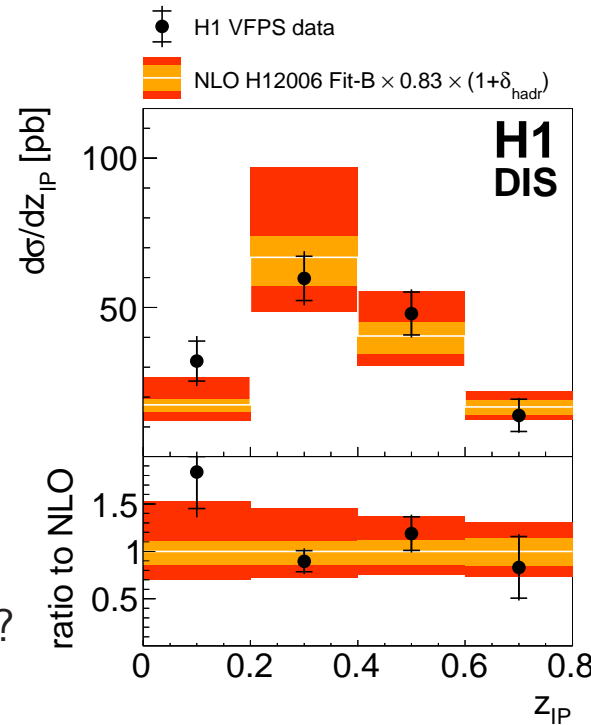
## Results: $E_T^{*jet1}$ distribution

- $E_T^{*jet1}$ :  
leading jet  
transverse energy
- distribution controlled  
by ME :  $E_T^{-4}$
- large NLO corrections
- Theo hp:  
 $E_T$ -dependence  
of the suppression?
- Desiderata :  
same analysis  
at higher  $E_T$  with good statistics



## Results: $z_{IP}$ distribution

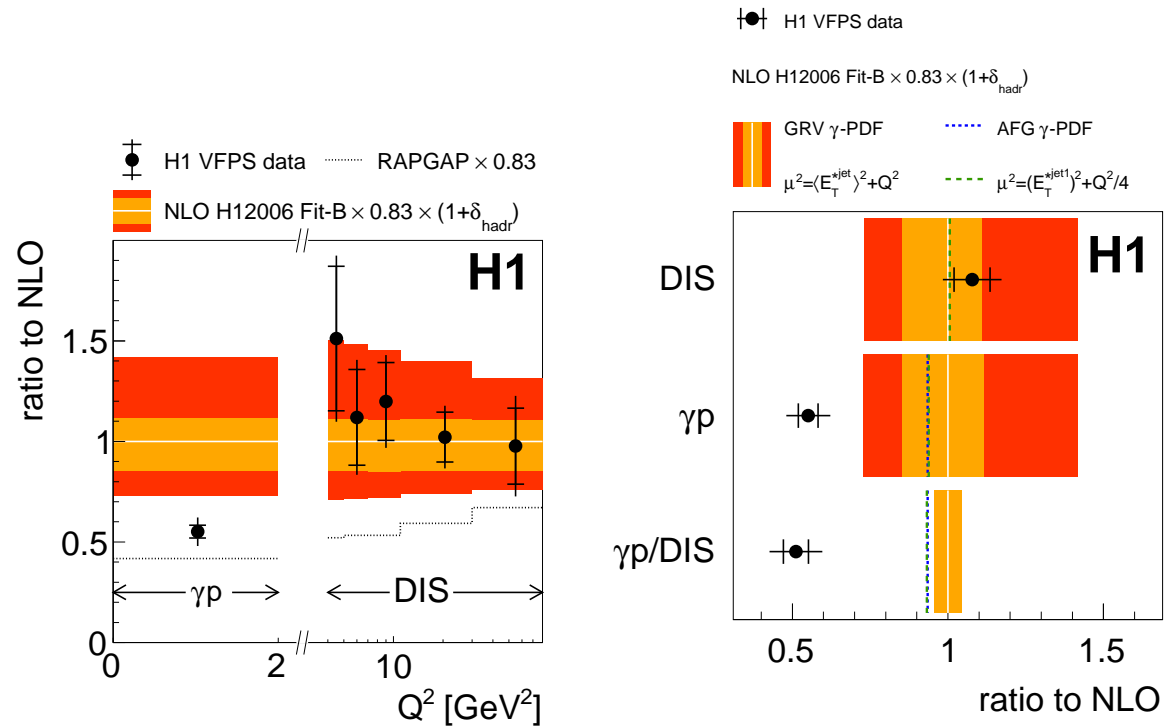
- $z_{IP}$  fractional momentum of the interacting parton
- determined by jets kinematics
- sensitive to DPDFs
- large NLO corrections
- shape ok
- "just" renorm DPDFs?





## Results: ratios

- Ratio: get rid of large NLO corrections (or soft resummation?)
- H1 confirms an overall suppression factor  $\sim 0.5$
- Critical variable:  $Q^2$  not  $E_T$
- factorisation broken for on-shell hadrons
- factorisation OK for pointlike probes virtual photon



## Advances in DPDFs determination

- Knowledge on DPDFs can be further refined
  - Global fit? LRG+FPS+jets+charm diffractive data from both HERA collaboration
  - Latest fits:
    - \* H1 2006 (iDIS)
    - \* H1 2007 (iDIS+jets)
    - \* ZEUS 2010 (iDIS+jets)
  - gluon DPDF poorly constrained in DDIS: use diffractive dijet
- In this talk: [alternative strategy](#)
  - QCD analysis of combined proton tagged DDIS data from H1 and ZEUS (EPJ '12)
  - cross-calibration: improved precision of the cross section measurements
  - $2.5 < Q^2 < 200 \text{ GeV}^2$
  - $0.00035 < x_P < 0.09$
  - $0.09 < |t| < 0.55 \text{ GeV}^2$

## Fitting strategy

### Important remark:

- hard-scattering factorisation holds at fixed values of  $x_{\mathcal{P}}$  and  $t$
- dependence on  $x_{\mathcal{P}}$  and  $t$  fully contained in DPDFs
- these conditional parton distributions are uniquely fixed by the kinematics of the outgoing proton:  
they are, at least in principle, different for different values of  $x_{\mathcal{P}}$  and  $t$ .

### In practice:

- perform a series of QCD fits at fixed values of  $x_{\mathcal{P}}$  with a common initial condition controlled by a set of parameters  $\{p_i\}$ .
- infer the approximate dependence of parameters  $\{p_i\}$  on  $x_{\mathcal{P}}$
- construct a generalised initial condition in the  $(\beta, x_{\mathcal{P}})$ -space to be used in a  $x_{\mathcal{P}}$ -combined QCD fit.

## Fixed $x_{\mathcal{P}}$ fits

### pQCD settings

- Evolution and convolution with QCDNUM17 Botje '11
- ZM VFNS scheme to NLO
- $m_c = 1.4$  GeV,  $m_b = 4.5$  GeV,  $\alpha_s(M_Z^2) = 0.118$ ,  $Q_0^2 = 1$  GeV<sup>2</sup>
- $\mu_F^2 = \mu_R^2 = Q^2$

Momentum distributions at  $Q_0^2$ :

$$\begin{aligned}\beta M_{\Sigma}(\beta, Q_0^2) &= A_q \beta^{B_q} (1 - \beta)^{C_q}, \\ \beta M_g(\beta, Q_0^2) &= A_g \beta^{B_g} (1 - \beta)^{C_g}\end{aligned}$$

- $M_{\Sigma}$ : flavour symmetric singlet distribution
- minimisation performed with MINUIT, stat  $\oplus$  syst errors

## Fixed $x_{\mathbb{P}}$ fits : Results

- No  $Q^2$  or  $y$  cuts imposed.  $M_X > 2$  GeV
- gluon constrained only by scaling violations:  
eigenvalue analysis suggests :  $C_g = 0$  and  $B_g = 0$
- initial condition contains 4 free parameters in each  $x_{\mathbb{P}}$ -bin
- mild dependence of  $\chi^2$  on  $Q_0^2$

$x_{\mathbb{P}}$	$\chi^2$	Fitted points
0.90E-03	3.52	8
0.25E-02	10.03	14
0.85E-02	15.95	23
0.16E-01	24.36	26
0.25E-01	26.96	25
0.35E-01	20.79	24
0.50E-01	28.48	27
0.75E-01	13.51	26
0.90E-01	6.36	10
Sum	149.9	183

## Generalised initial conditions

- Let depend the coefficients  $A_q, B_q, C_q$  and  $A_g$  on  $x_{\mathcal{P}}$
- functional  $x_{\mathcal{P}}$ -dependence:

$$A_q(x_{\mathcal{P}}) = A_{q0} x_{\mathcal{P}}^{A_{q,1}}$$

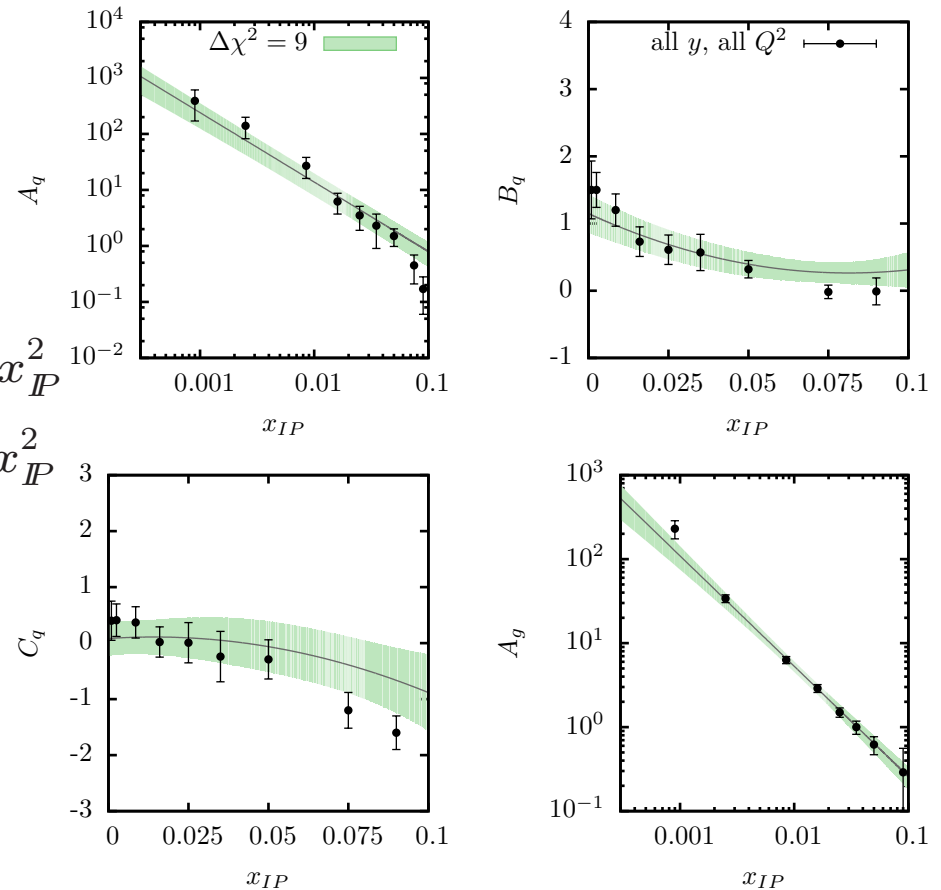
$$B_q(x_{\mathcal{P}}) = B_{q0} + B_{q1} x_{\mathcal{P}} + B_{q,2} x_{\mathcal{P}}^2$$

$$C_q(x_{\mathcal{P}}) = C_{q0} + C_{q1} x_{\mathcal{P}} + C_{q,2} x_{\mathcal{P}}^2$$

$$A_g(x_{\mathcal{P}}) = A_{g0} x_{\mathcal{P}}^{A_{g,1}}$$

- 10 free pars

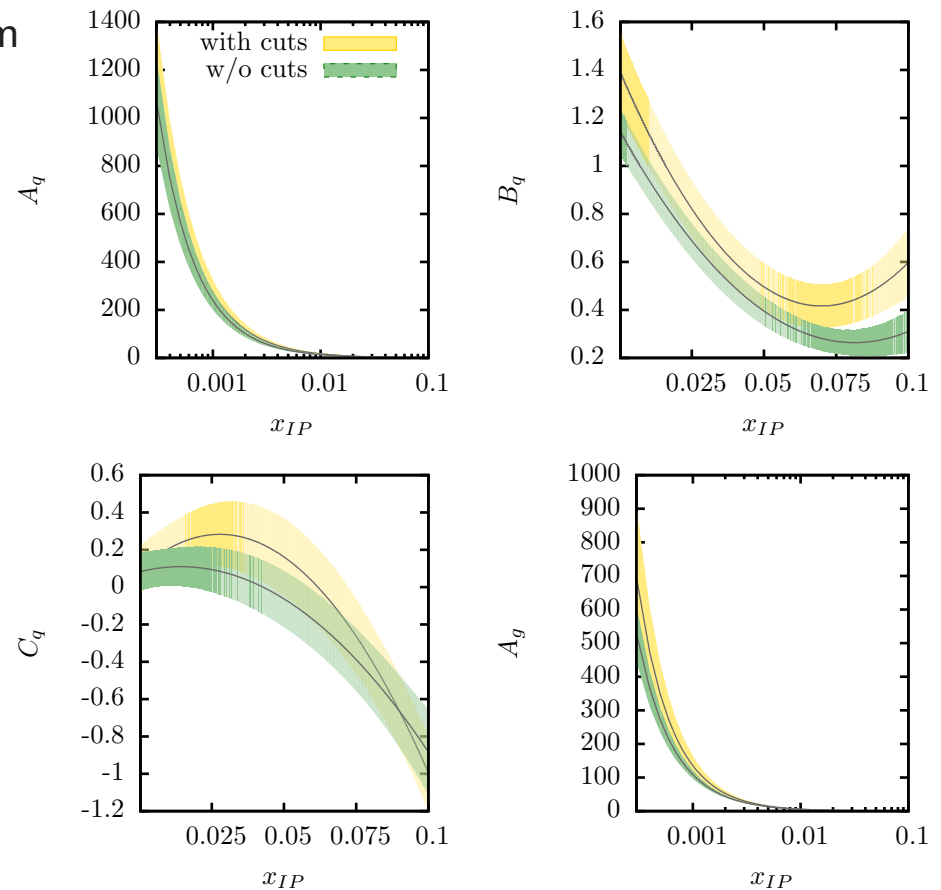
Pars vs  $x_{\mathcal{P}}$  with error band



## Fit result and stability

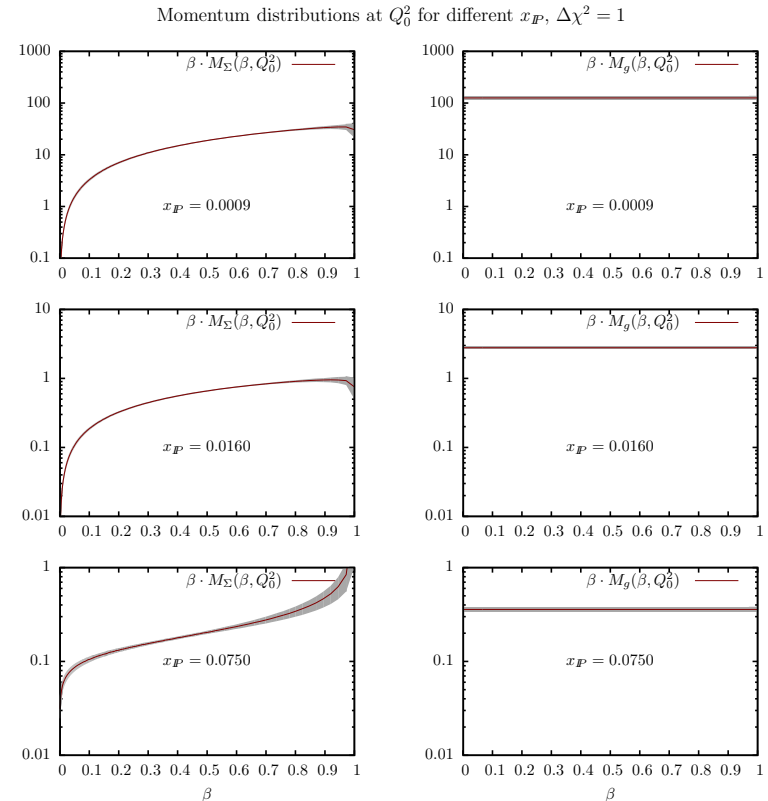
- $\chi^2 = 193$  for 192-10 degree of freedom
- stability of the fit checked against variation of the cuts:
- $y < 0.5, Q^2 > 8 \text{ GeV}^2$
- No cuts : default
- No dependence on  $Q_{\min}^2$  (unlike H1 and ZEUS fits based on LRG data)
- some tension at large  $y$  ( $y > 0.5$ )
- combination price:  $\sim 40 \chi^2$  units: need improvements

Pars vs  $x_P$  with  $1\sigma$  error band



## DPDFs at $Q_0^2$ at different $x_{\mathcal{P}}$

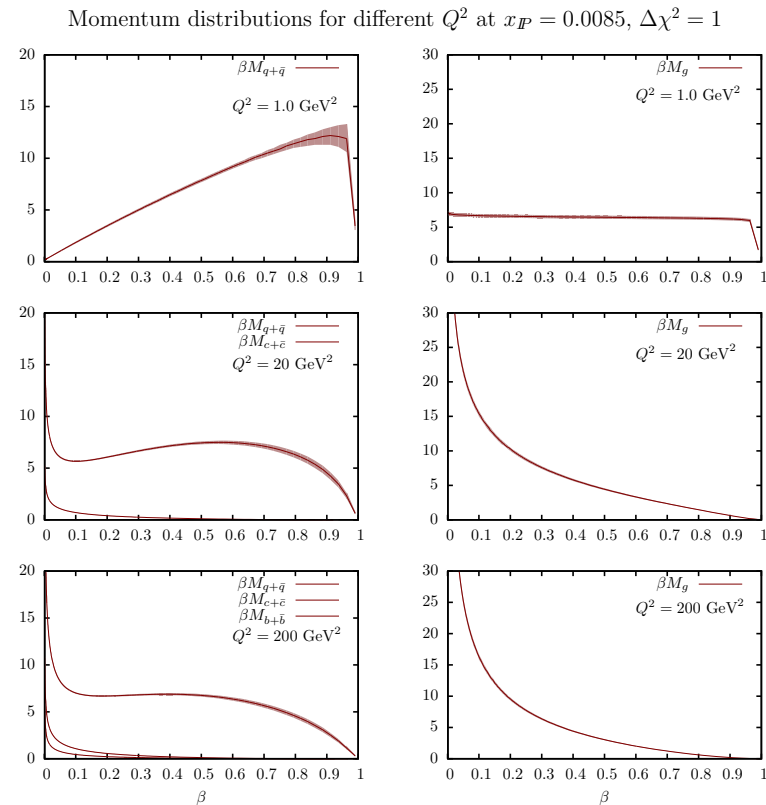
- initial condition at  $Q_0^2 = 1 \text{ GeV}^2$
- Light red band :  $\Delta\chi^2 = 1$
- Slight shape deformation vs  $x_{\mathcal{P}}$  at large  $\beta$



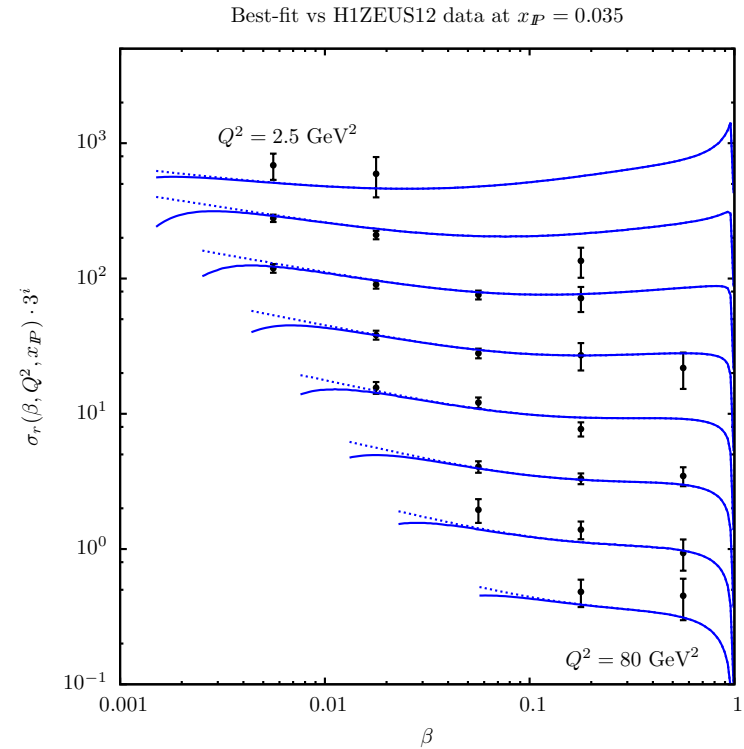
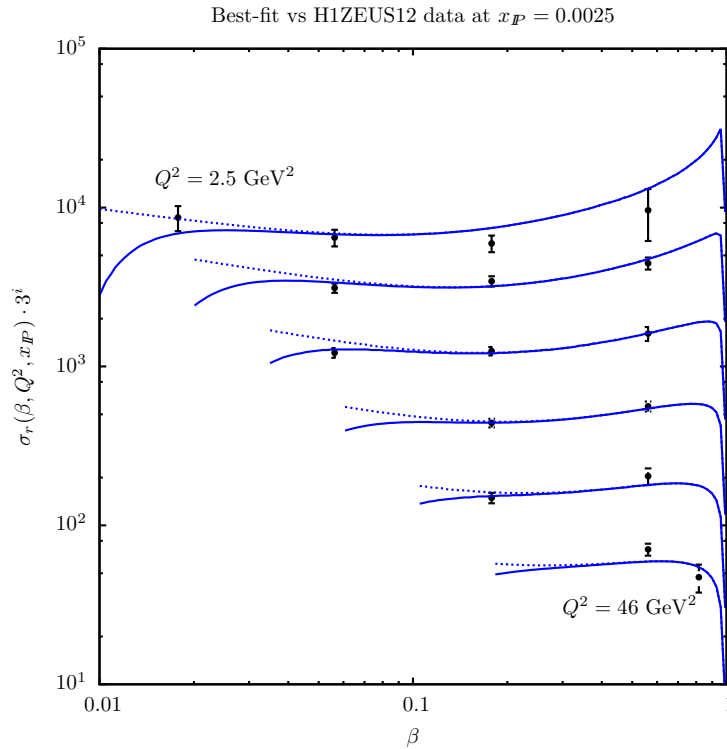


## DPDFs evolution

- Singlet and gluon momentum distributions at  $x_{\mathbb{P}} = 0.0085$
- Light red band: propagation experimental uncertainties with  $\Delta\chi^2 = 1$  (eigenvector method)
- Singlet: valence-like at low  $Q^2$
- Gluon: fast rise with raising  $Q^2$  at low  $\beta$
- Error shrinkage at high  $Q^2$ : effect of pQCD evolution

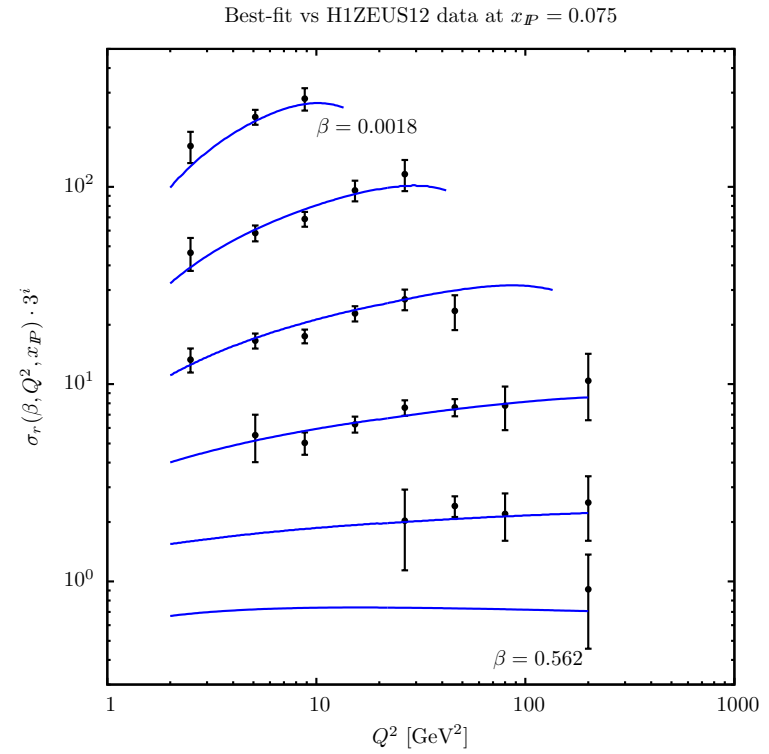
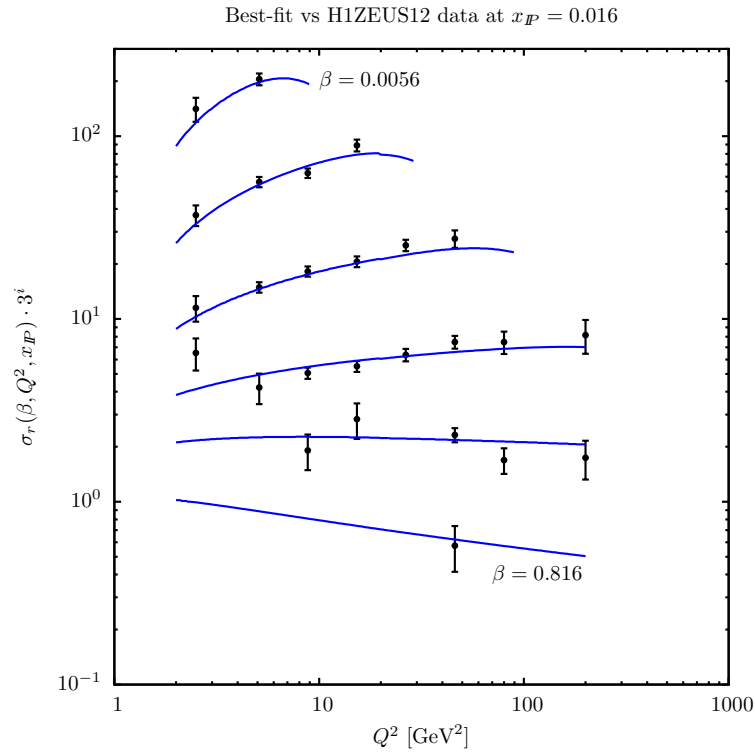


## Best fit vs $\beta$ at different $Q^2$



$$\sigma_r^{D(3)}(\beta, Q^2, x_{\mathbb{P}}) = F_2^{D(3)}(\beta, Q^2, x_{\mathbb{P}}) - \frac{y^2}{1+(1-y)^2} F_L^{D(3)}(\beta, Q^2, x_{\mathbb{P}})$$

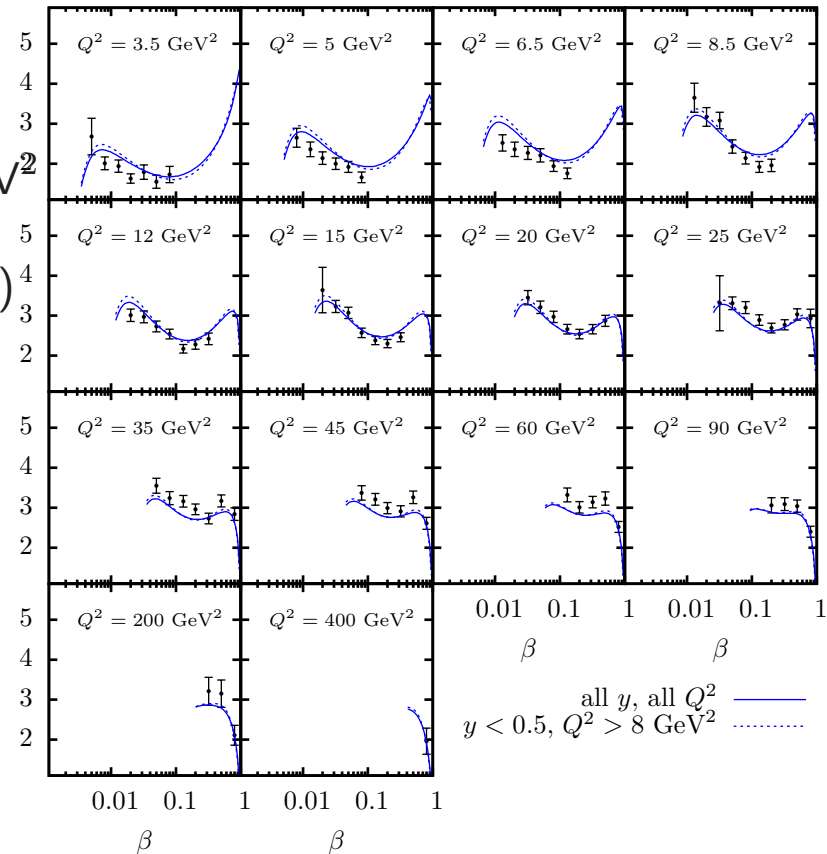
## Best fit vs $Q^2$ at different $\beta$



## Comparison with H1 LRG12 data at $x_P = 0.01$

- LRG:  $M_Y < 1.6 \text{ GeV}$ ,  $|t| < 1 \text{ GeV}^2$
- FPS:  $M_Y = m_p$ ,  $0.09 < |t| < 0.55 \text{ GeV}^2$
- Expected a constant rescaling factor ( $\simeq 2$ )
- BUT: rescaling does depend on  $Q^2$
- same results for a fit with additional  $y < 0.5$  and  $Q^2 > 8 \text{ GeV}^2$  cuts
- Open problem

Best-fit vs H1 LRG12 data at  $x_P = 0.01$



## Test: $\beta$ - $x_{\mathcal{I}P}$ factorised ansatz

- Accomodate all  $x_{\mathcal{I}P}$ -dependence in a common flux factor for gluon and singlet

$$\mathcal{F}(x_{\mathcal{I}P}) = x_{\mathcal{I}P}^{f_0} \cdot (1 - x_{\mathcal{I}P})^{f_1}$$

so that

$$\Sigma(\beta, Q_0^2, x_{\mathcal{I}P}) = \mathcal{F}(x_{\mathcal{I}P}) s_0 \beta^{s_1} (1 - \beta)^{s_2}$$

$$g(\beta, Q_0^2, x_{\mathcal{I}P}) = \mathcal{F}(x_{\mathcal{I}P}) g_0 \beta^{g_1} (1 - \beta)^{g_2}$$

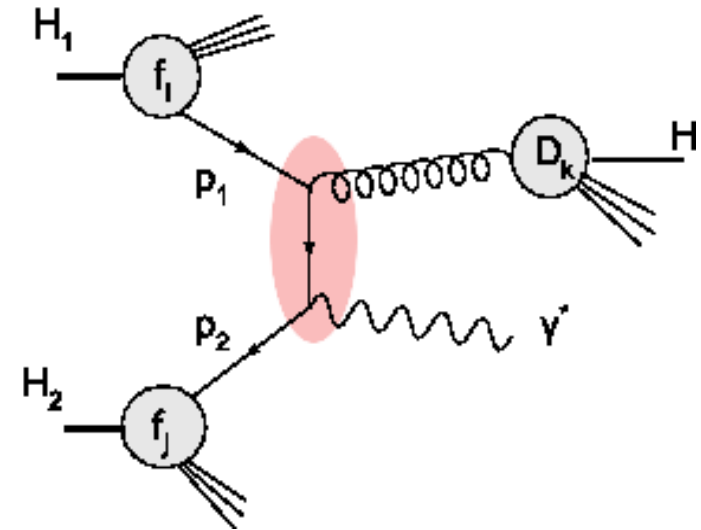
- ◇ 8 free parameters fit, additional  $\beta$  and  $x_{\mathcal{I}P}$  dependence
- Same pQCD settings and error treatment
- The fit returns  $\chi^2 = 207$  (vs 193) for 192-8 degrees of freedom
- This implies an increase  $\Delta\chi^2 = +14$
- Indication for a modulation in the  $\beta$ -shape of DPDFs depending on  $x_{\mathcal{I}P}$
- NB: with additional shaping, the factorised ansatz could still give a competitive fit

## Near future plan

- Fit still preliminar but hopefully publicly available soon
- test of internal consistency with HERA LRG data
- input for predictions of hard diffraction at hadron collider

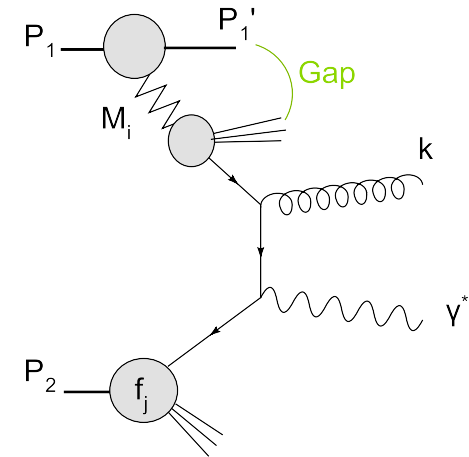
## On hard-scattering factorisation

- Hard-scattering factorisation is at the basis of discovery and precision physics (especially) at hadron colliders.
  - Consider  $H_1 + H_2 \rightarrow H + \gamma^* + X$
  - Assume hard scattering factorisation:  
 $d\sigma \propto f_{H_1} \otimes f_{H_2} \otimes D_H \otimes d\hat{\sigma}$
  - **No factorisation theorem** for generic QCD and/or BSM processes **but** we found it works well phenomenologically
  - Factorisation proven only for inclusive Drell-Yan (where it is easier to show that soft exchanges are power suppressed when one sums over final states).
  - Use semi-inclusive DY to test factorisation: it will depend on the phase space region in which  $H$  is detected
- Factorisation failure **opens** a window on NP (soft) physics:  
 NP physics is in **the way** it **fails**..



## Hard Diffraction at LHC

- Numerous analyses on soft and hard diffraction are ongoing at LHC by all Collaborations.
- Method :
  - LRG with main detectors
  - forward proton tagger
- ▶ Strategy: Assume hard scattering factorization : use HERA DPDFs to predict (single) diffractive cross sections for
  - $W^\pm, Z$  (clean, rare)
  - dijet (abundant, busy)
  - $\gamma$ -jet
  - ...
- more processes, more knowledge





## Drell-Yan : motivations

Drell-Yan process :  $P_1 + P_2 \rightarrow \gamma^* + X$

Drell, Yan 1970

- Factorization of the process at "soft" level

Lindsay, Ross, Sachrajda, 1983

Collins, Soper, Sterman 1984

Bodwin, 1985

1. **Perturbative trigger**: the invariant mass  $Q^2$  of the lepton pair can be **accurately reconstructed**;
2. The process is **free** of final state QCD corrections;
3. Higher order corrections known for  $d\sigma/dQ^2$ ,  $d\sigma/dy dQ^2$  and  $d\sigma/dq_\perp^2 dQ^2$

⊕ soft gluon resummations.

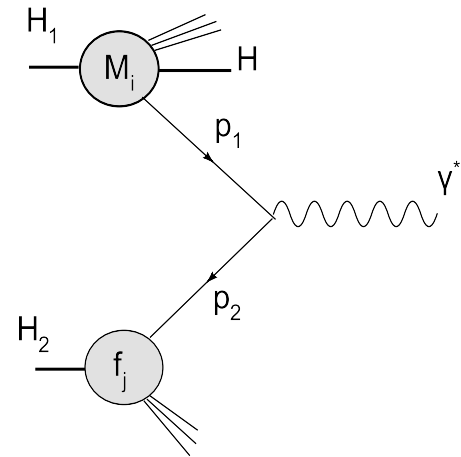


Prototype process for factorisation studies in hadronic collisions.

## Prototype process: diffractive DY

- consider:  $H_1 + H_2 \rightarrow H_1 + \gamma^* + X$
- ▶ Let us **assume factorisation**:

$$x_{\mathbb{P}} \frac{d\sigma^{DDY}}{dQ^2 dY dx_{\mathbb{P}}} = \sigma_0 \sum_q e_q^2 M_{q/\mathbb{P}}^D \left( \frac{\sqrt{\tau} e^Y}{x_{\mathbb{P}}}, Q^2, x_{\mathbb{P}} \right) f_{\bar{q}/P_2}(\sqrt{\tau} e^{-Y}, Q^2)$$



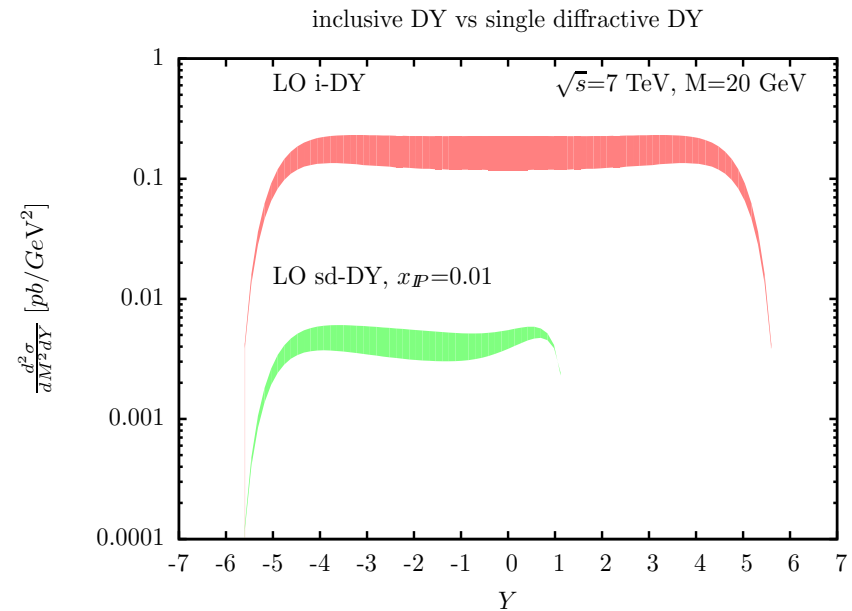
- **Dependencies** of the cross section:
  - DY mass: factorisation breaking vs  $Q^2$  (not only around  $M_Z$ )
  - $x_{\mathbb{P}}$ : possible different physics at different  $x_{\mathbb{P}}$
  - DY rapidity: test the shape of HERA DPDFs vs measurements
  - If possible, avoid extrapolation from HERA ranges:  $0.001 < \beta < 1$ ,  $0.001 < x_{\mathbb{P}} < 0.1$

## Open questions

- Can we correct the factorisation formula by a factor  $S$ ?  

$$d\sigma \propto f^D \otimes f \otimes d\hat{\sigma} \otimes S(..)$$
- which are the dependences of  $S$ ?
- do we see the same partonic structure observed at HERA?
- can be the cross section factorised at all?
- Compare Single and Double Diffraction  

$$d\sigma \propto f^D \otimes f^D \otimes d\hat{\sigma} \otimes S'(..)$$
- what are the relations between  $S$  and  $S'$ ?
- What if one measures forward neutron instead of protons?



## Hard diffraction : present and future

- **Impressive knowledge** on hard diffraction accumulated by HERA and Tevatron
- This knowledge is **quantitative** and **predictive** (dPDFs etc.)
  - New fit ready soon
- **discovery-like** program at hadron collider:
  - how factorisation is broken
  - to which extent the pomeron is universal?
  - if not, can we define modified DPDFs in hard diffraction in hadronic collisions?
  - Can we recover approximate predictivity?
- Single diffractive DY good candidate process for such studies