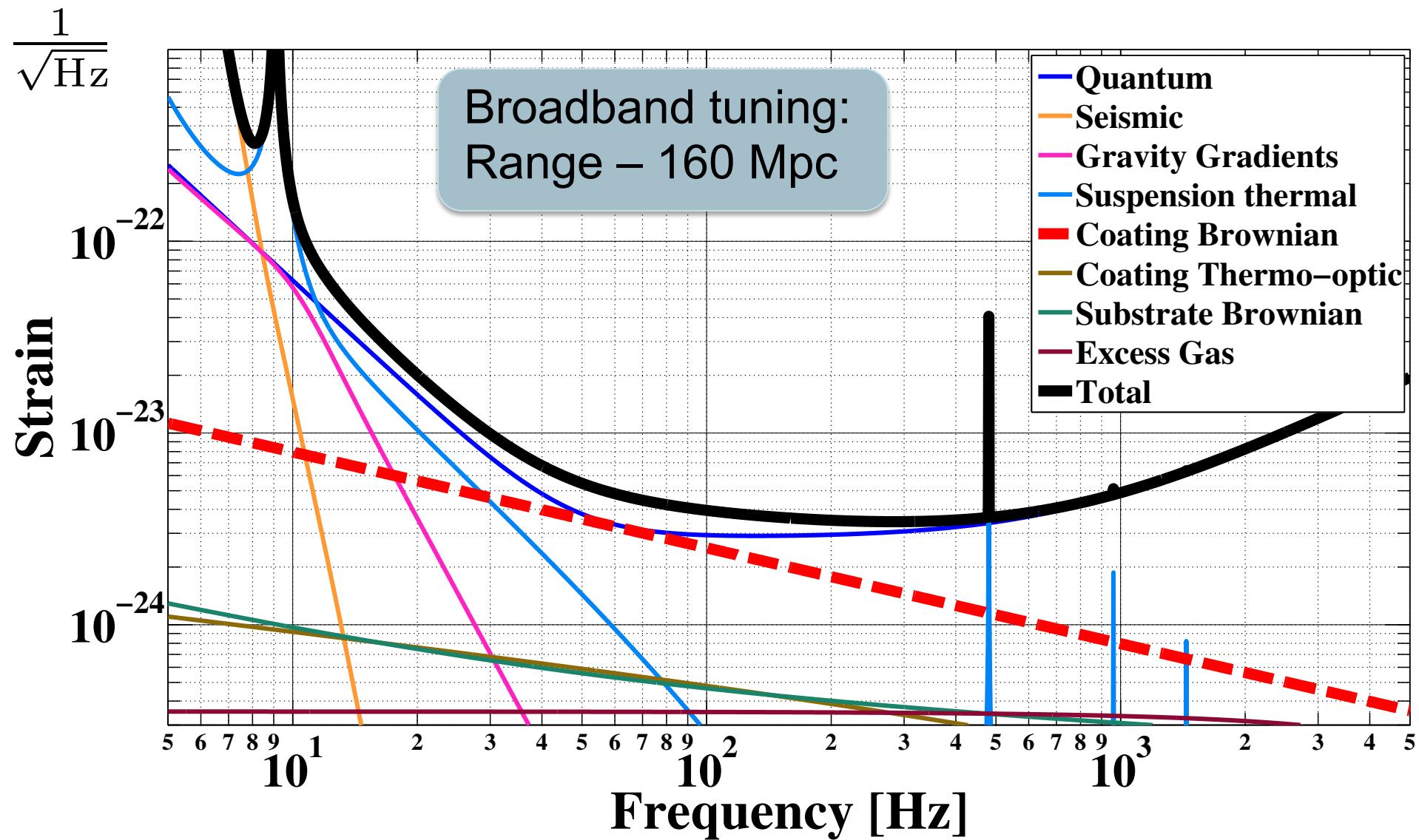
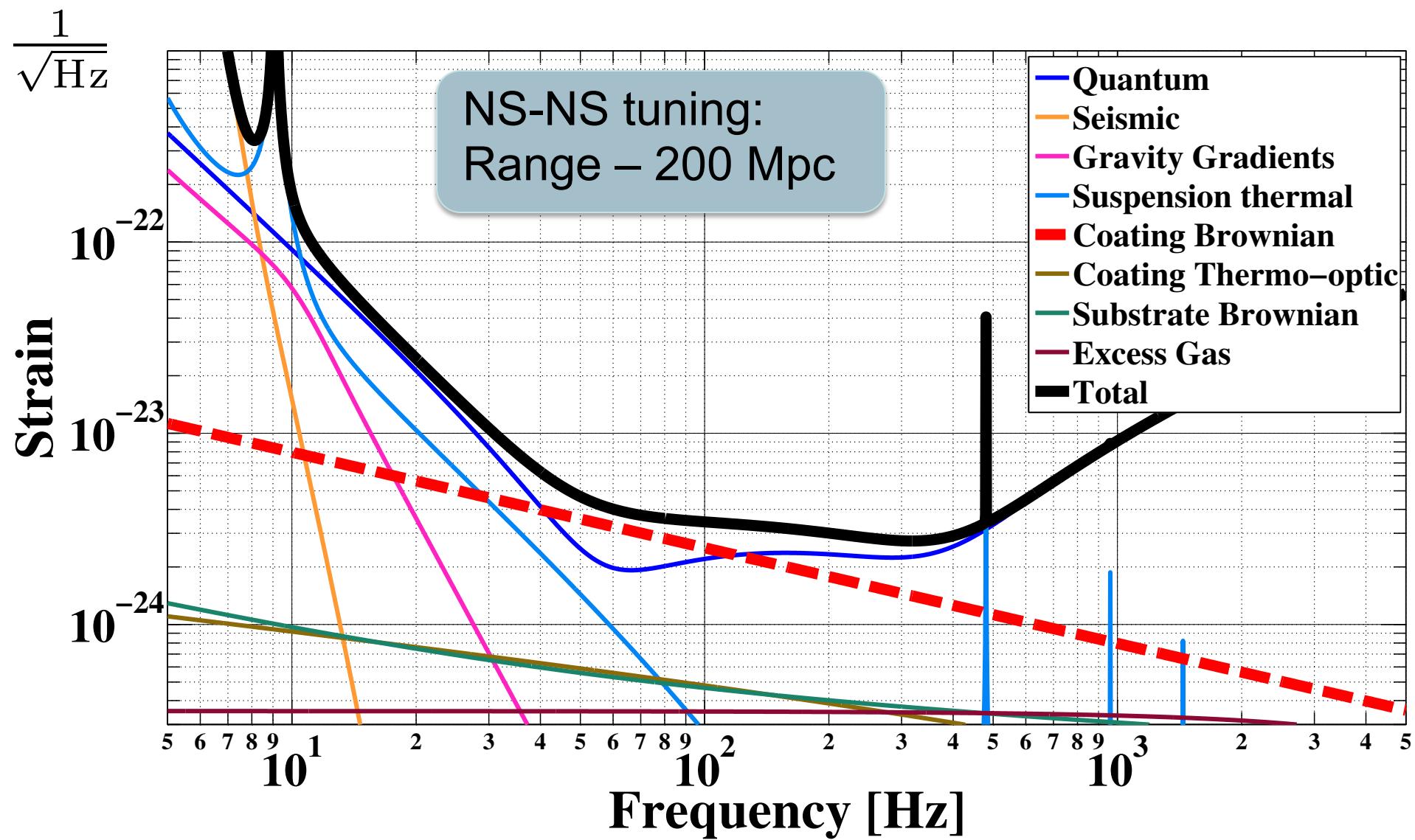




In short

- Due to mirror surface roughness, adopting LG_{33} beams in the near future will be extremely challenging

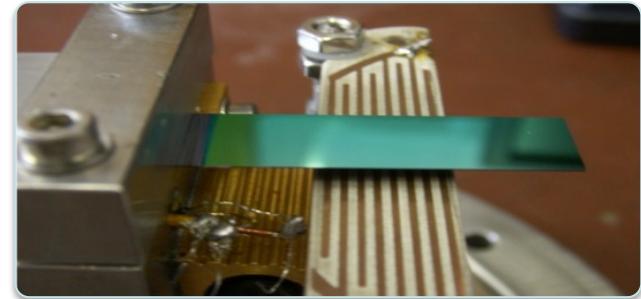




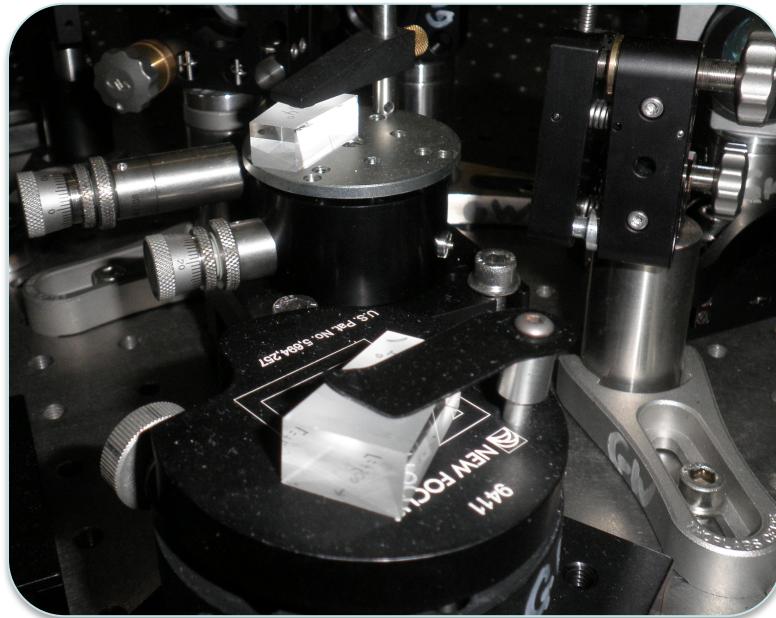


Methods of reducing thermal noise

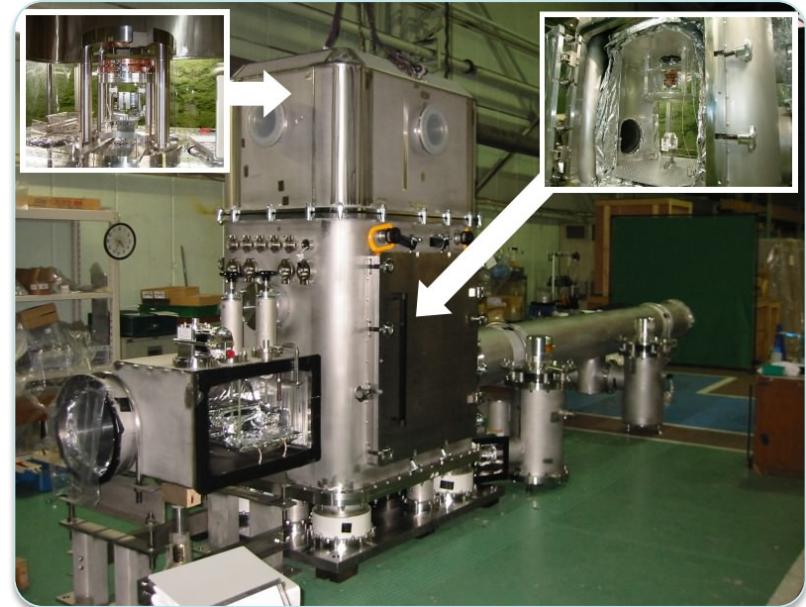
- Materials
- Cooling
- BEAM SHAPE



M. Abernathy, IGR, U. of Glasgow



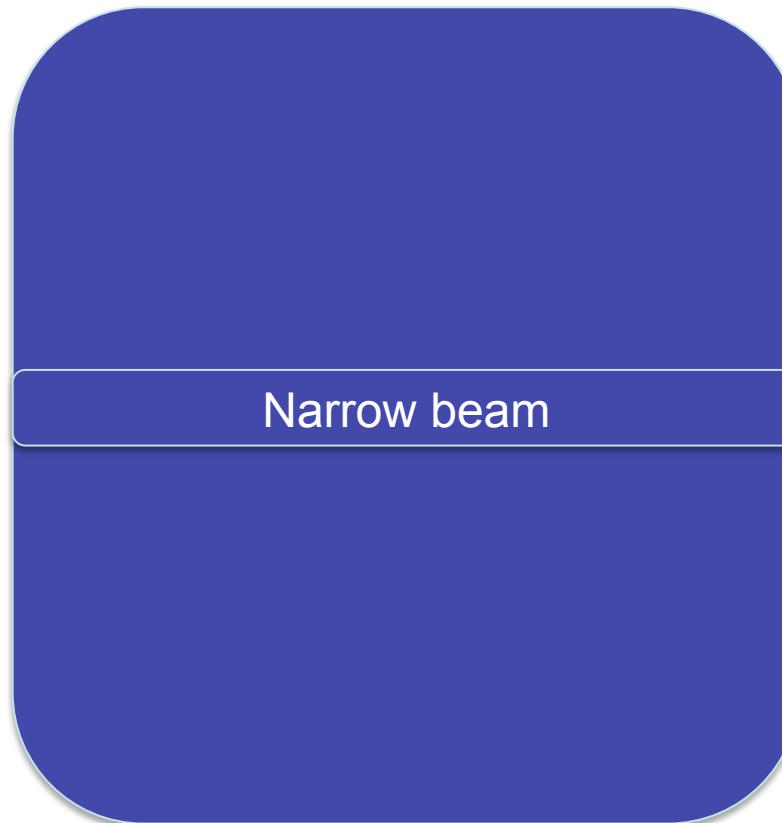
Undergraduate coating-free mirror project, ANU



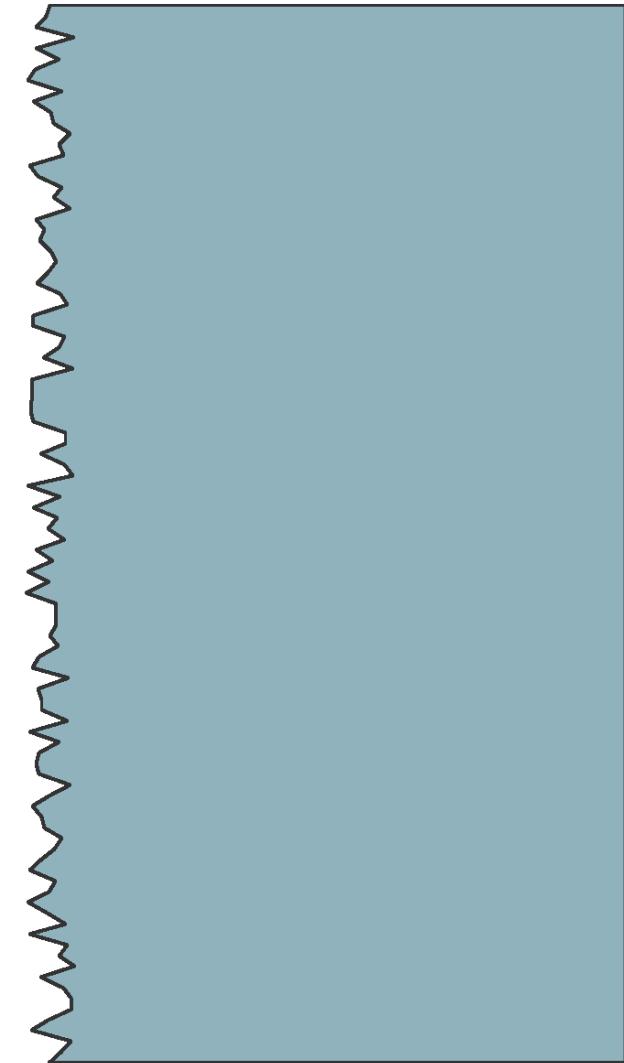
<http://www.icrr.u-tokyo.ac.jp/gr/lcgt/lcgt2010e.html>



Bigger is better

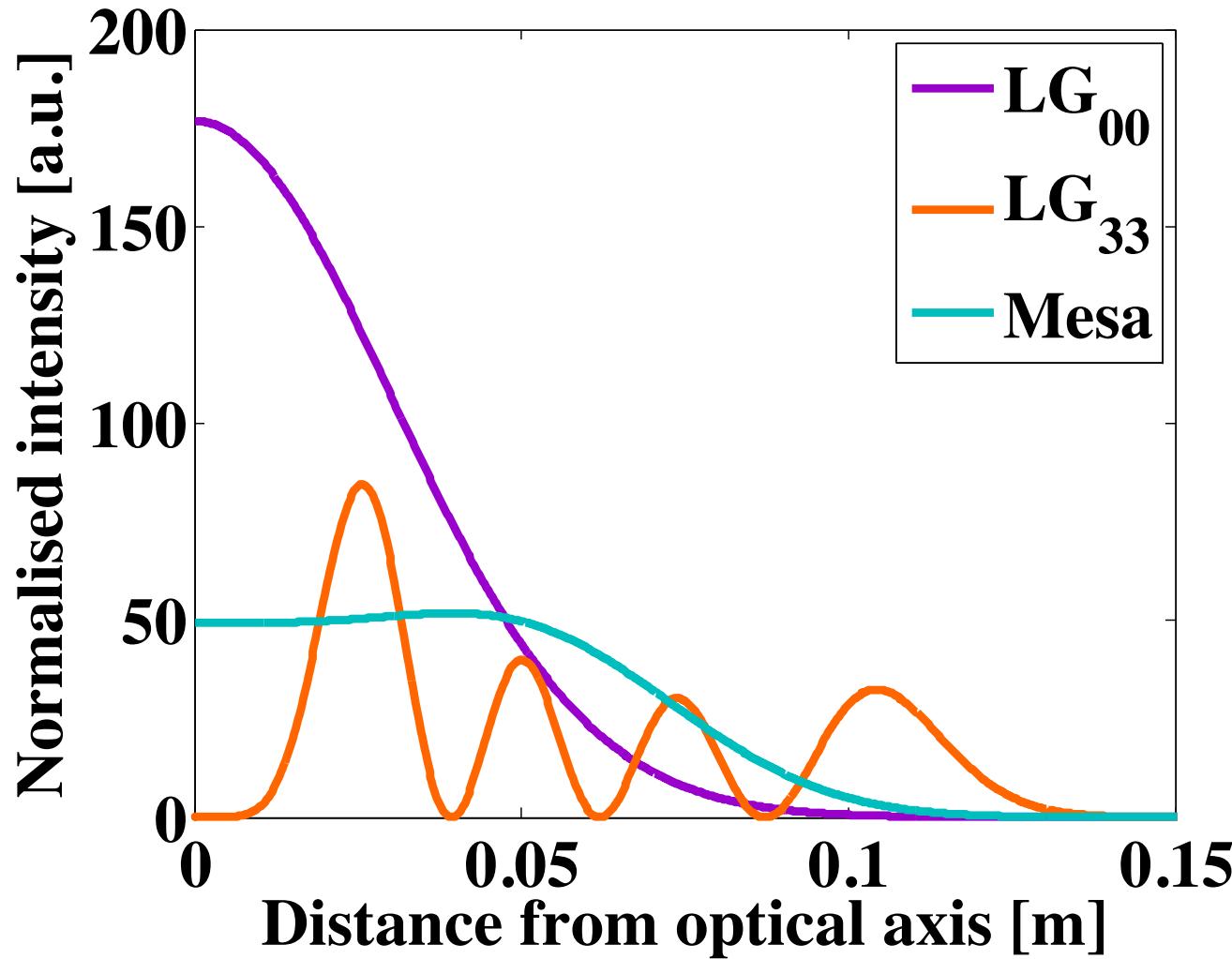


$$S_{CB} \propto \frac{1}{\omega^2}$$



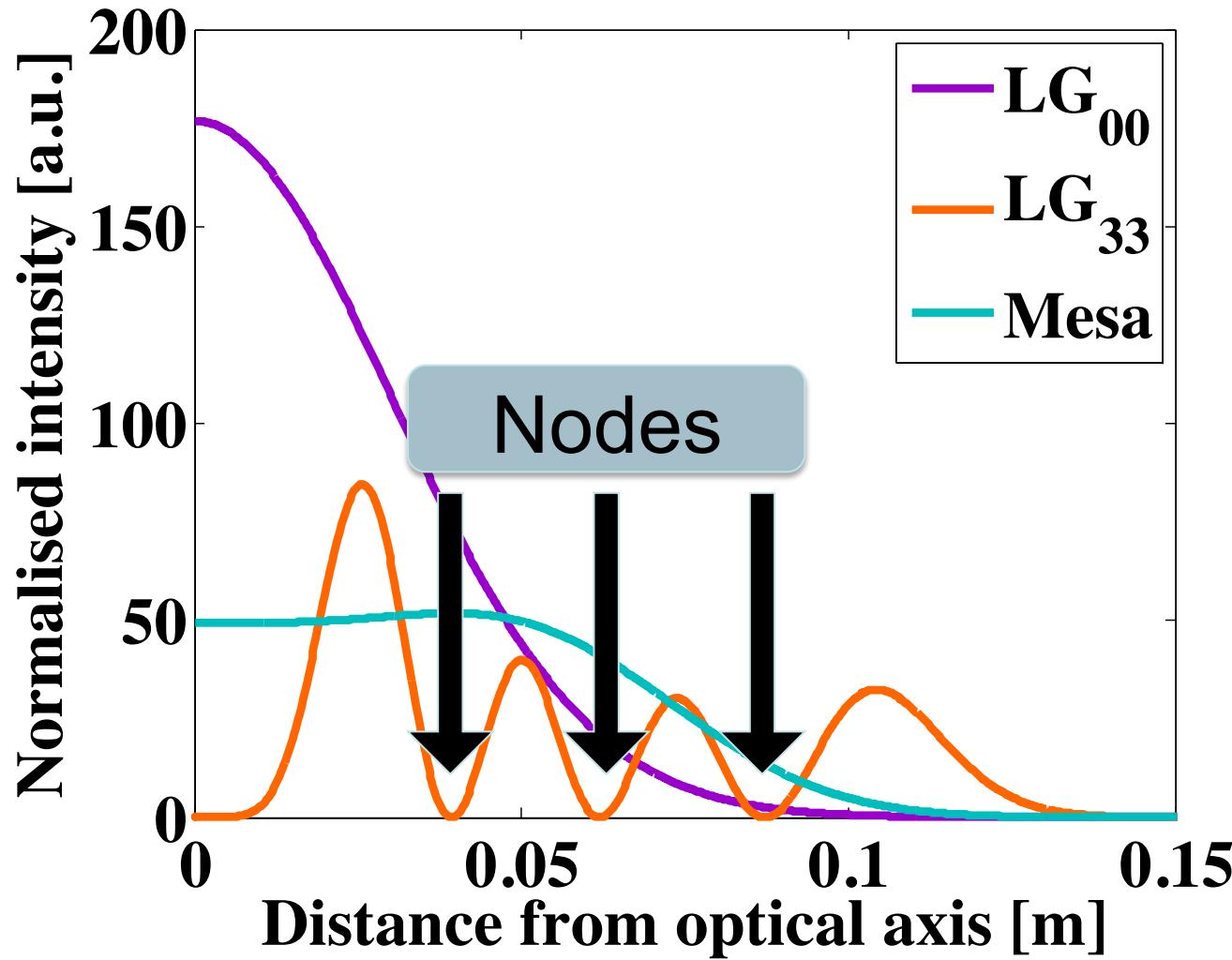
Pierro et al., Phys. Rev. D 76, 122003 (2007)

New beam shapes for GW III – LG_{33}



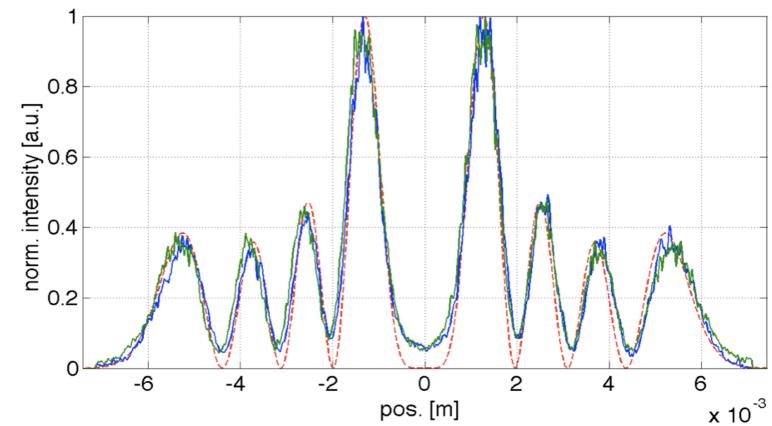
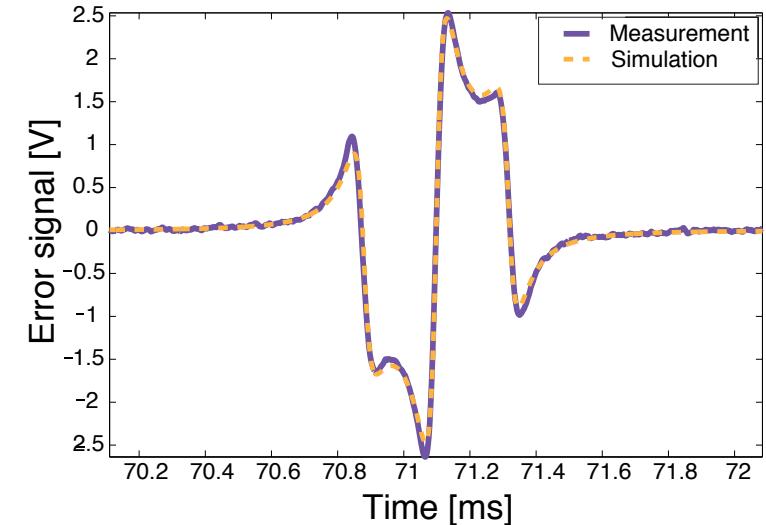
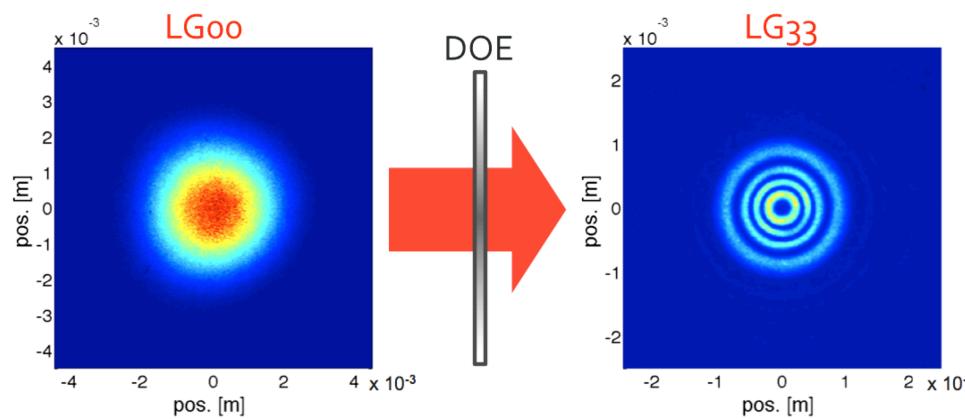
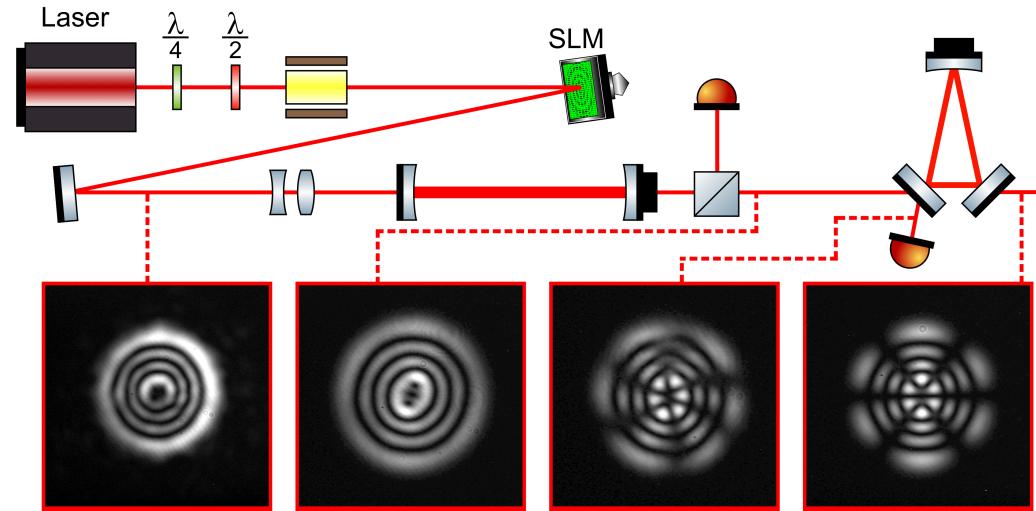
Mours et al., Class. Quantum Grav. 23, 5777–5784 (2006)

New beam shapes for GW III – LG_{33}



Mours et al., Class. Quantum Grav. 23, 5777–5784 (2006)

Experimental work



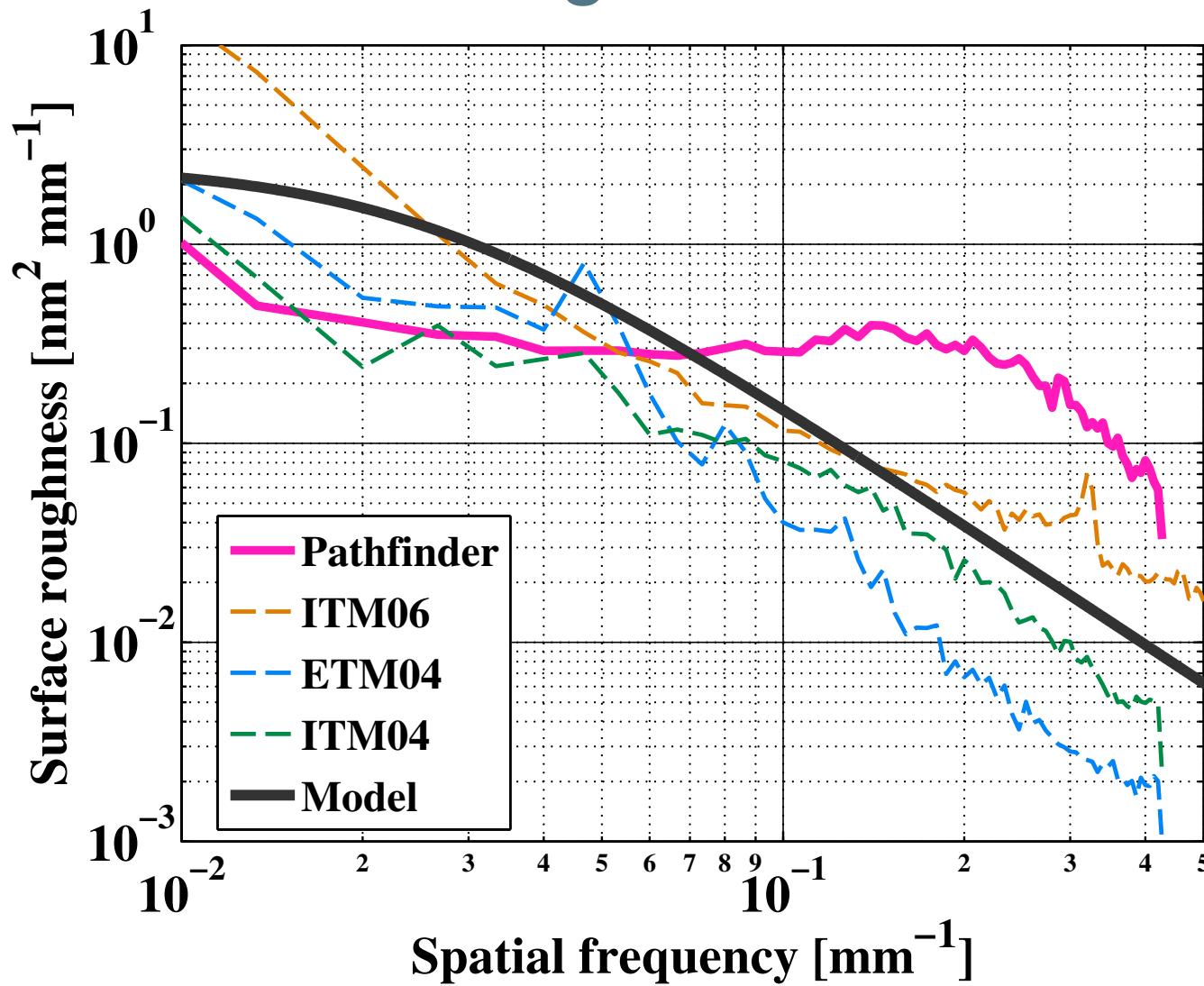
Fulda et al., Phys. Rev. D 82, 012002 (2010)
 Granata et al., Phys. Rev. Lett. 105, 231102 (2010)



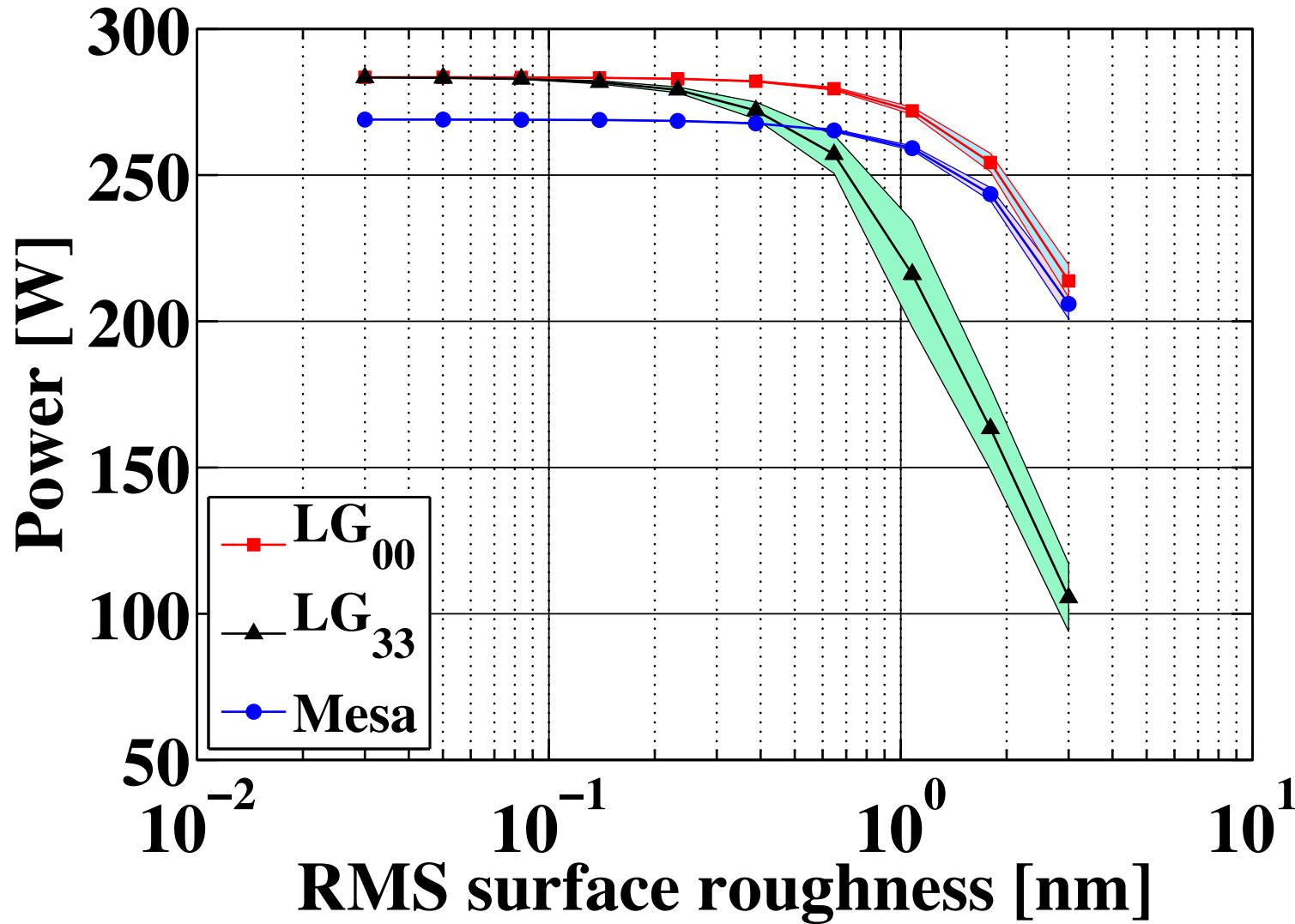
FFT simulations of LG₃₃

- Evaluate performance in real IFO
- SIS tool (H. Yamamoto)
- Simulate single 2nd generation style arm cavity
 - ROCs chosen to give diffraction loss equal to that of LG₀₀
- Assume input is pure LG₃₃

Mirror surface roughness

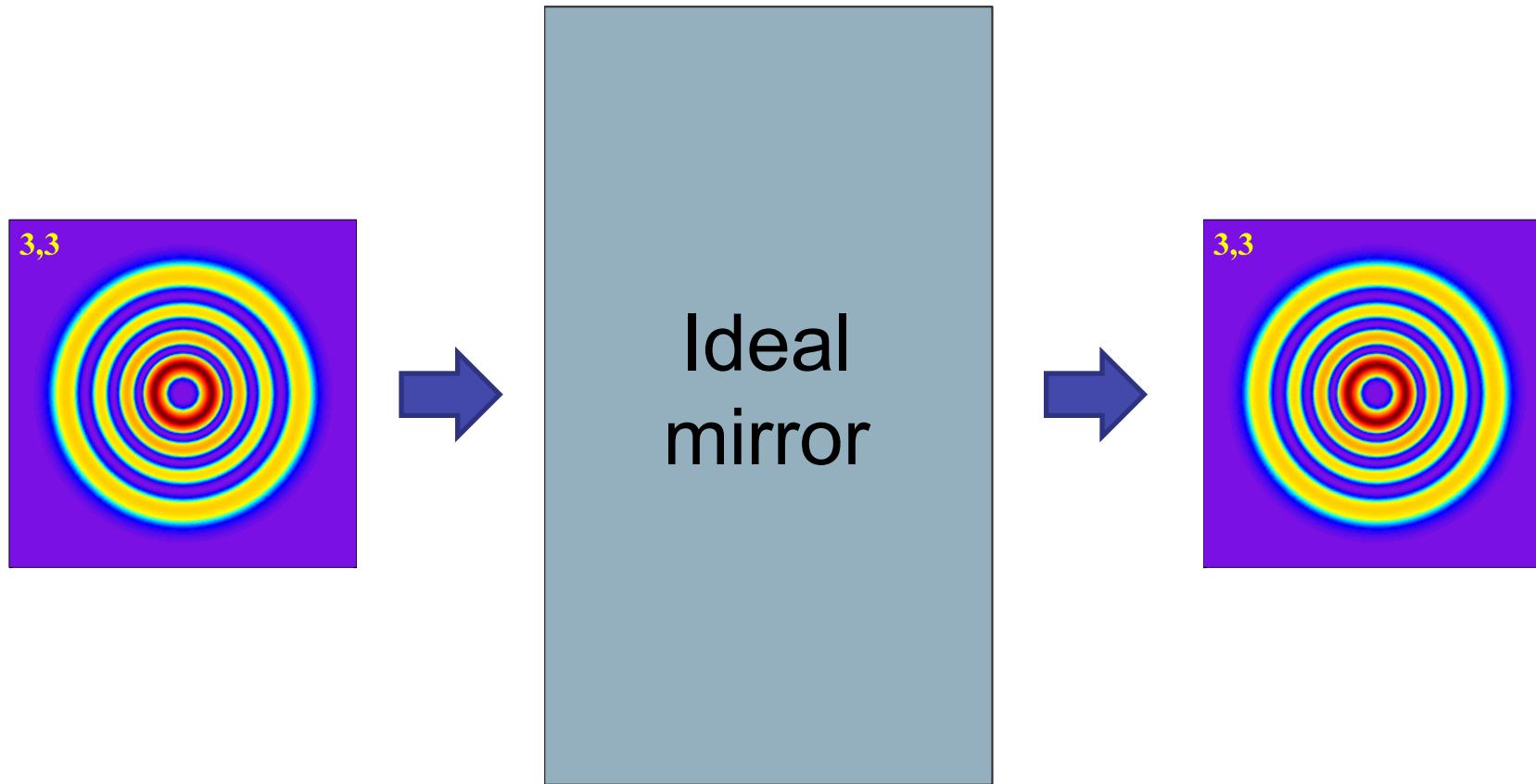


Circulating power



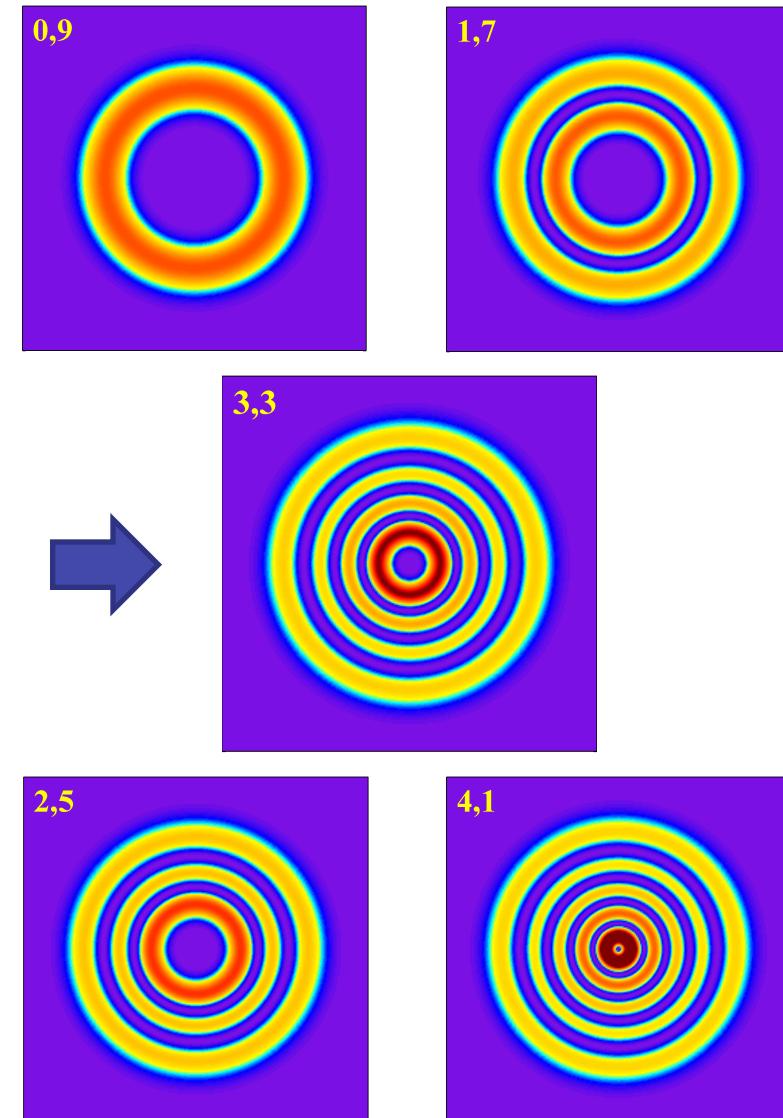
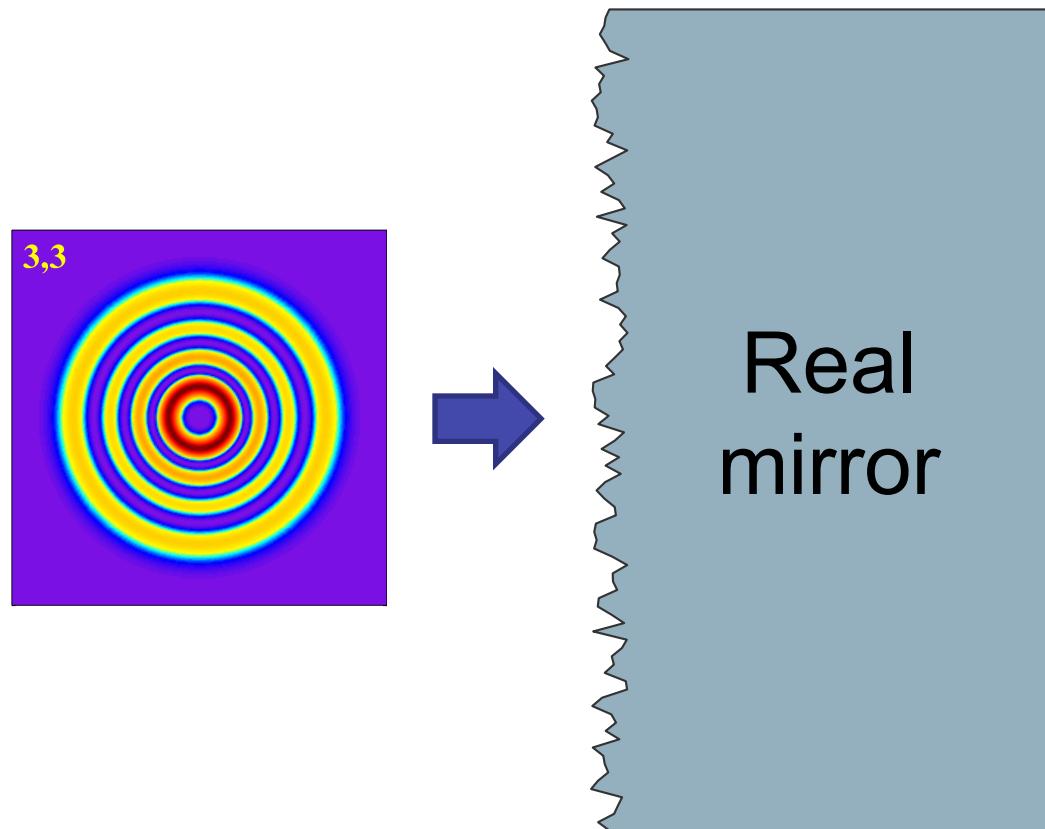


Explanation



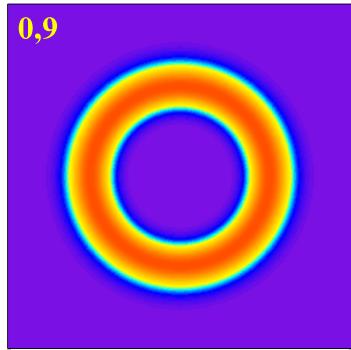


Explanation

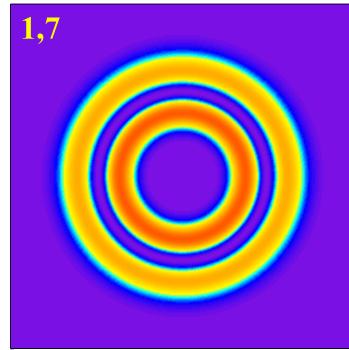




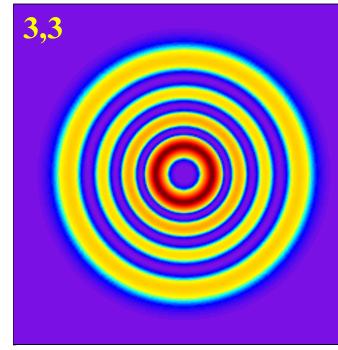
Modal contamination



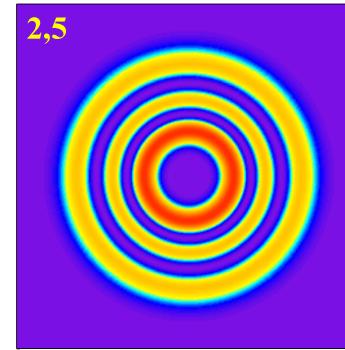
$0,\pm 9$: 0.3 %



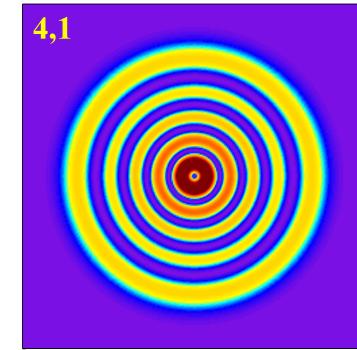
$1,\pm 7$: 0.2 %



$3,-3$: 0.7 %

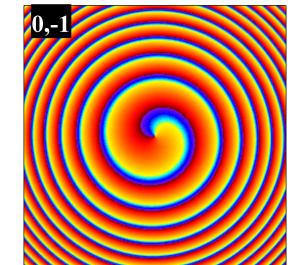
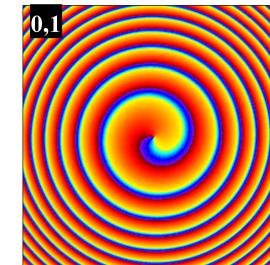


$2,\pm 5$: 0.1 %



$4,\pm 1$: 0.2 %

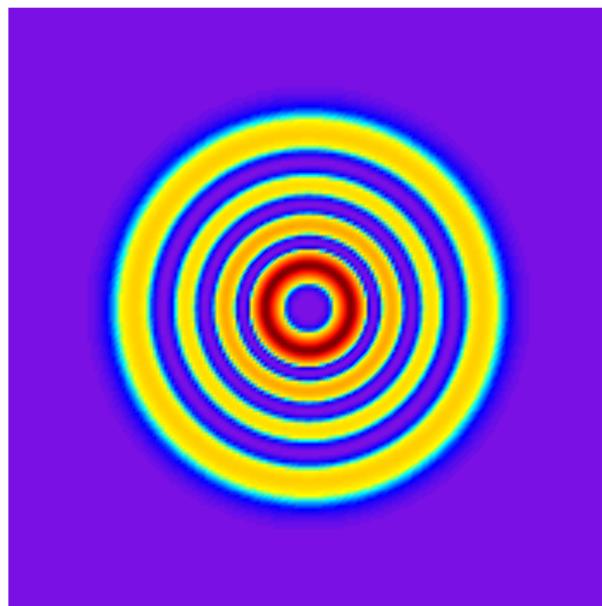
Total contamination: 1.5 %



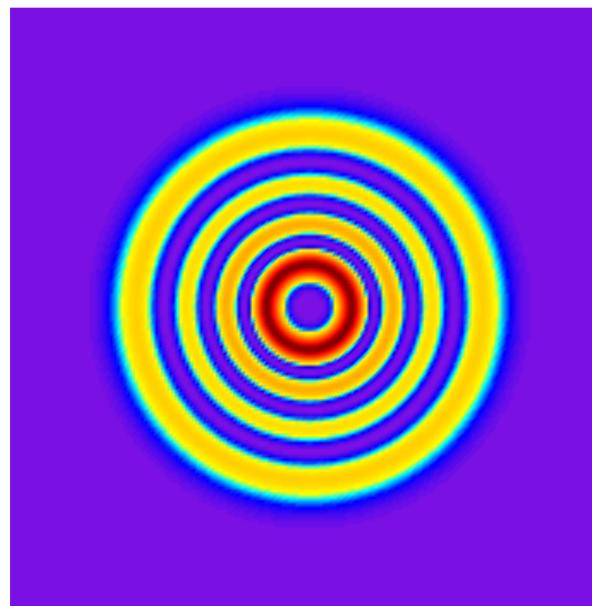
\pm modes have opposite helicity



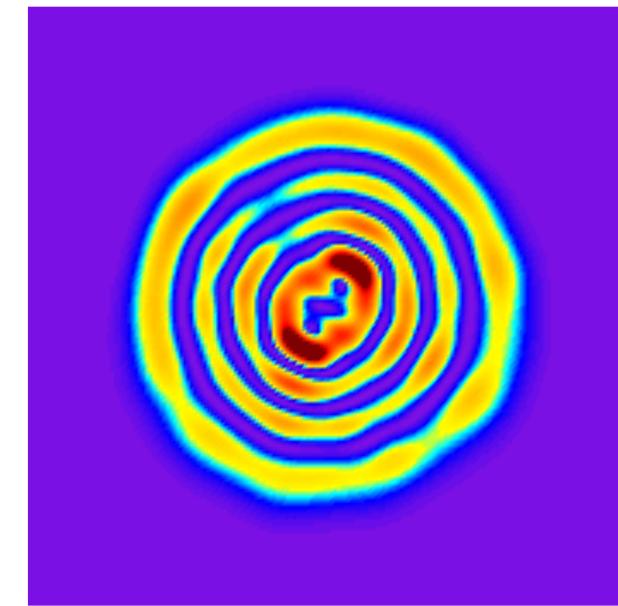
Output modes – LG_{33}



Input



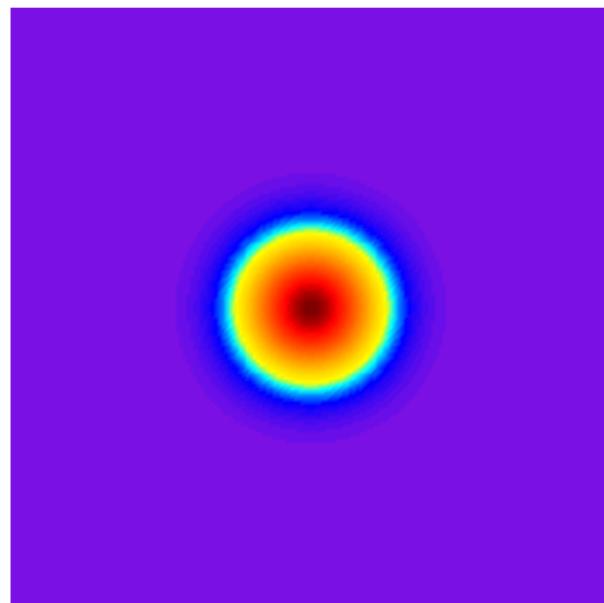
Reflected with
ideal mirrors



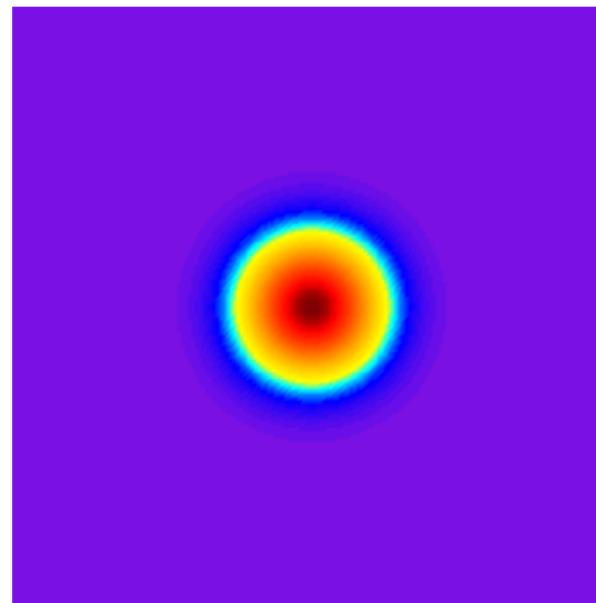
Reflected with
real mirrors



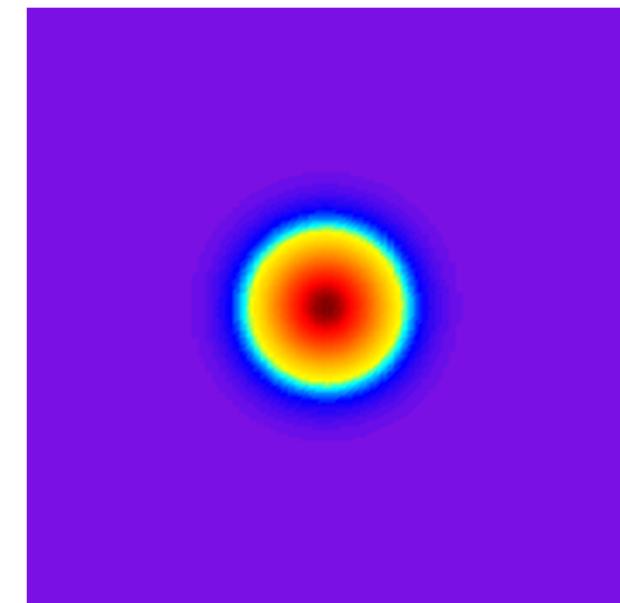
Output modes – LG_{00}



Input



Reflected with
ideal mirrors



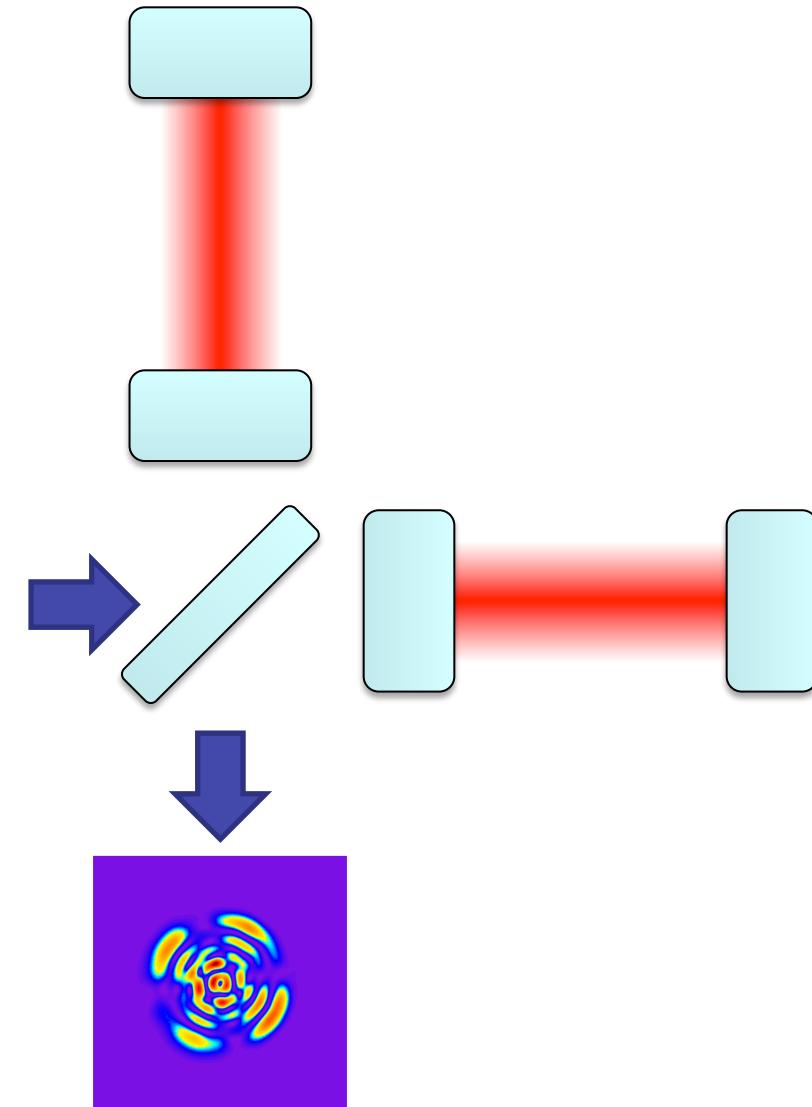
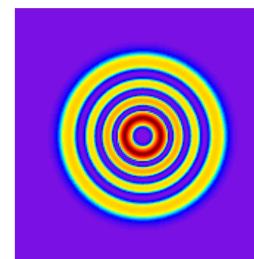
Reflected with
real mirrors



Contrast defect - I

- Combine discrete arm cavity simulations to create IFOs

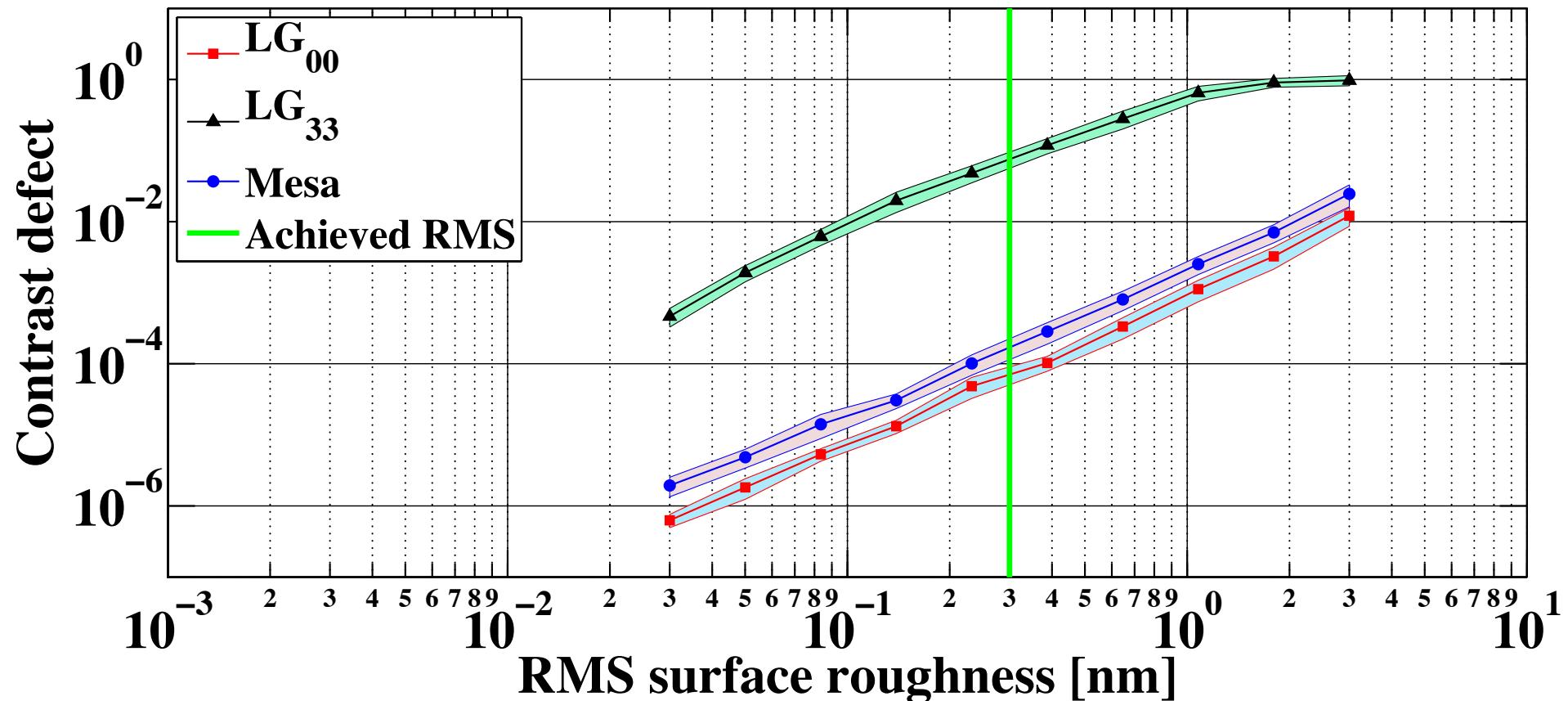
$$\binom{n}{2}$$



- Estimate contrast defect

$$C = \frac{P_{AS}}{P_X + P_Y}$$

Contrast defect - II





Mitigation – better polishing/ tuning

- Polishing needs to be around 10 times better to match Gaussian
 - State of the art not quite good enough
- Frequency tuning
 - Mirror imperfections break degeneracy
 - HOMs have discrete resonance frequencies
 - Tune f_{input} to optimise

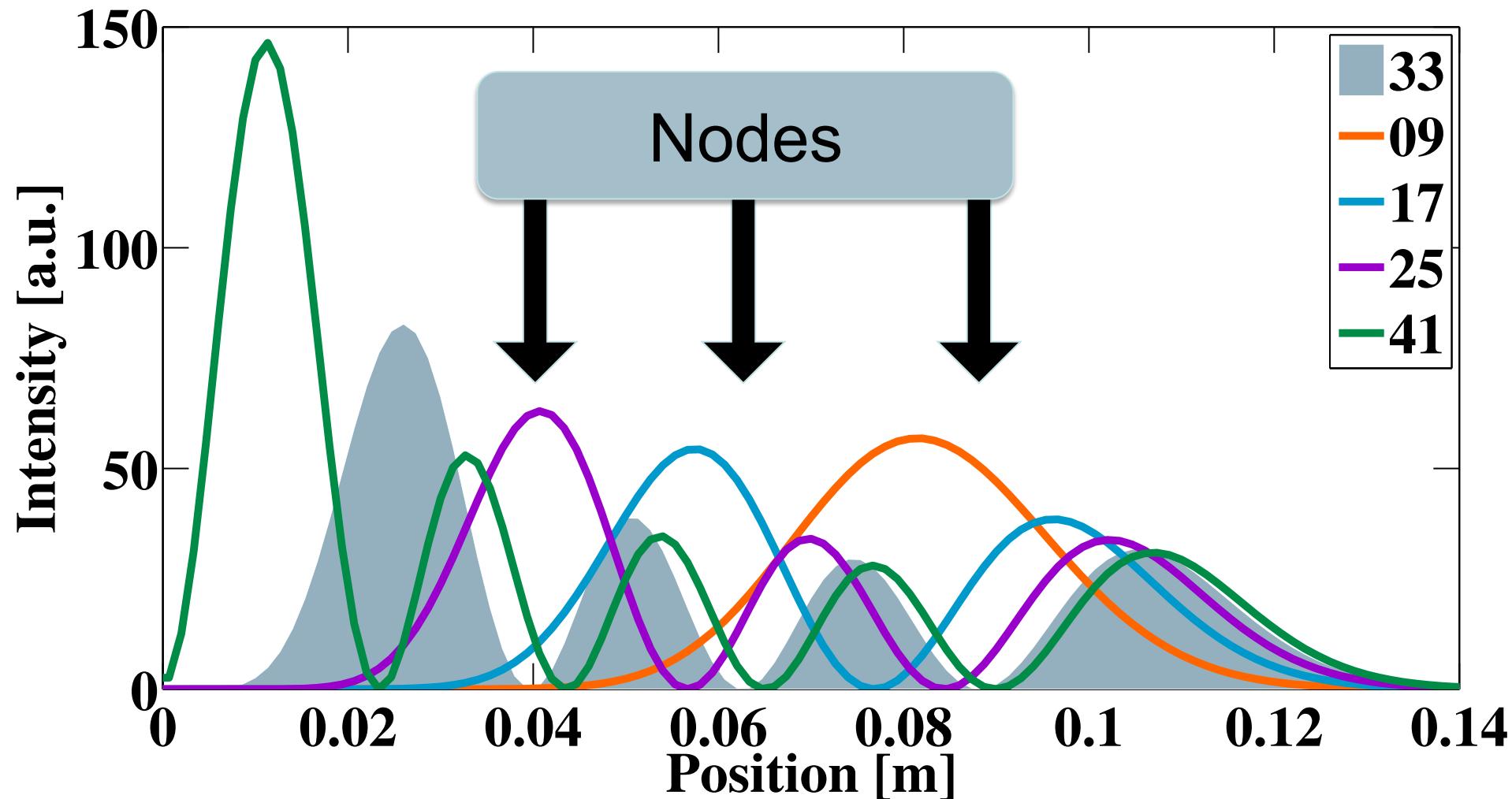


Mitigation - rings



R. Glauber and W. Rueckner (Harvard Natural Sciences Lecture Demonstrations, Photo by Laura Wulf)

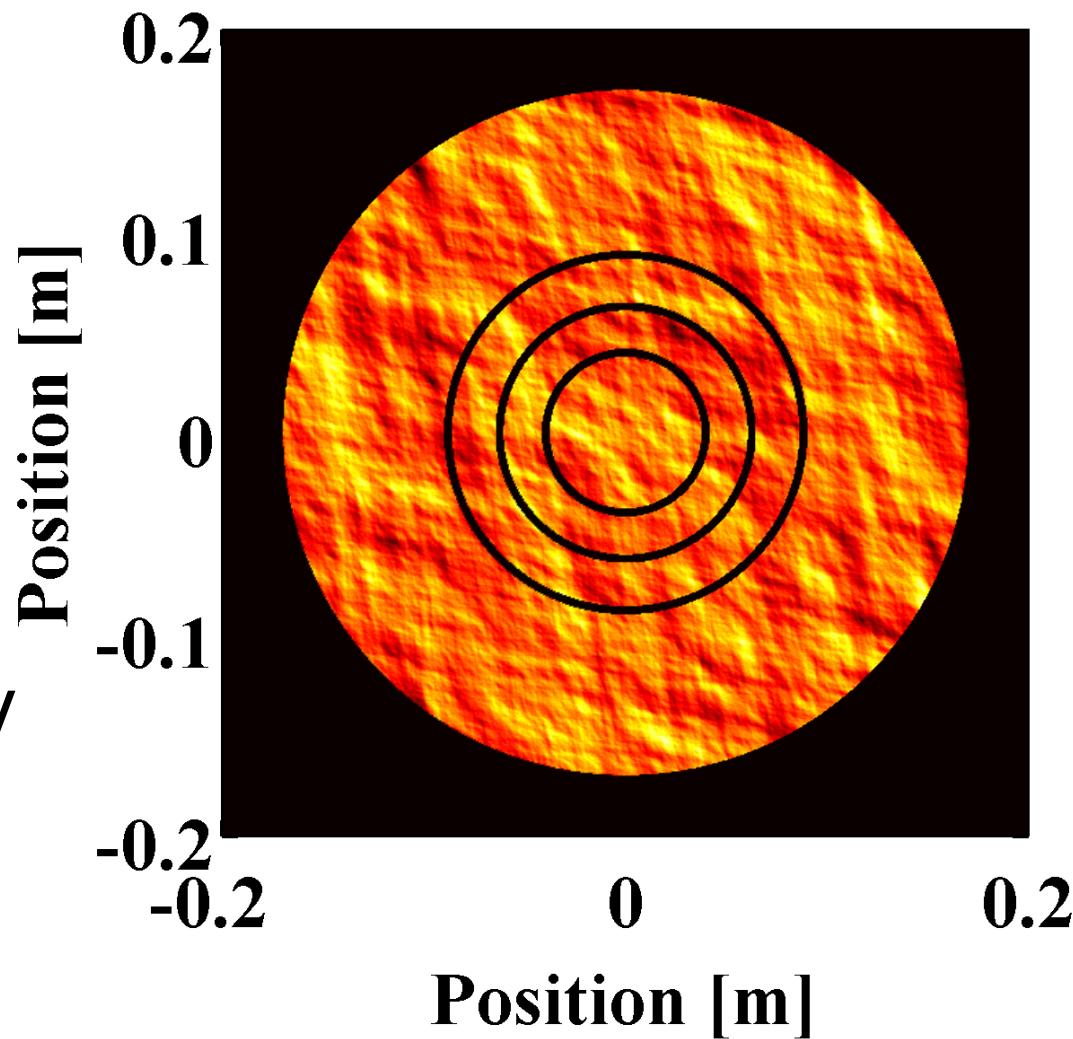
Degenerate modes



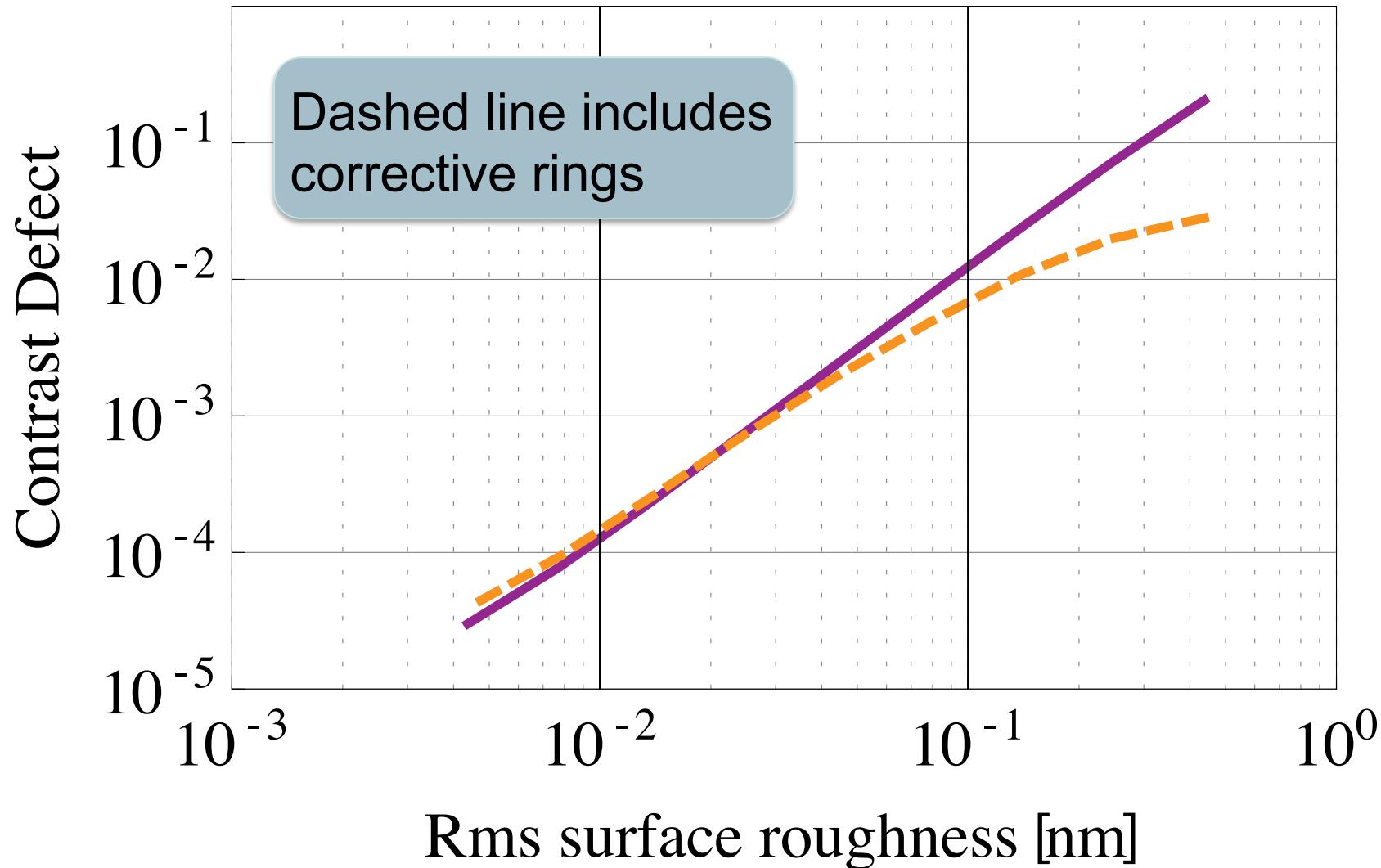


Mitigation - rings

- Modify mirror at nodes of LG_{33} to 'damp' other modes
- Add material or reduce reflectivity

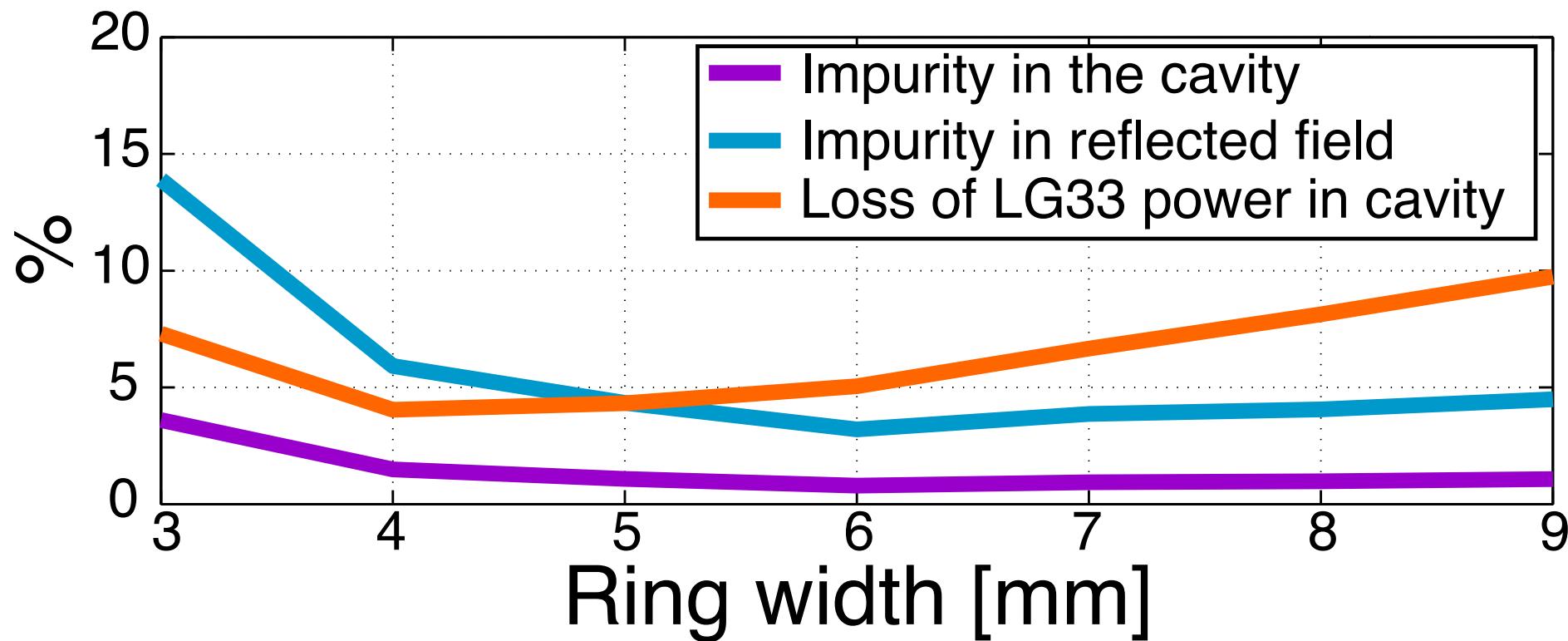


Mitigation – Rings (Hong)



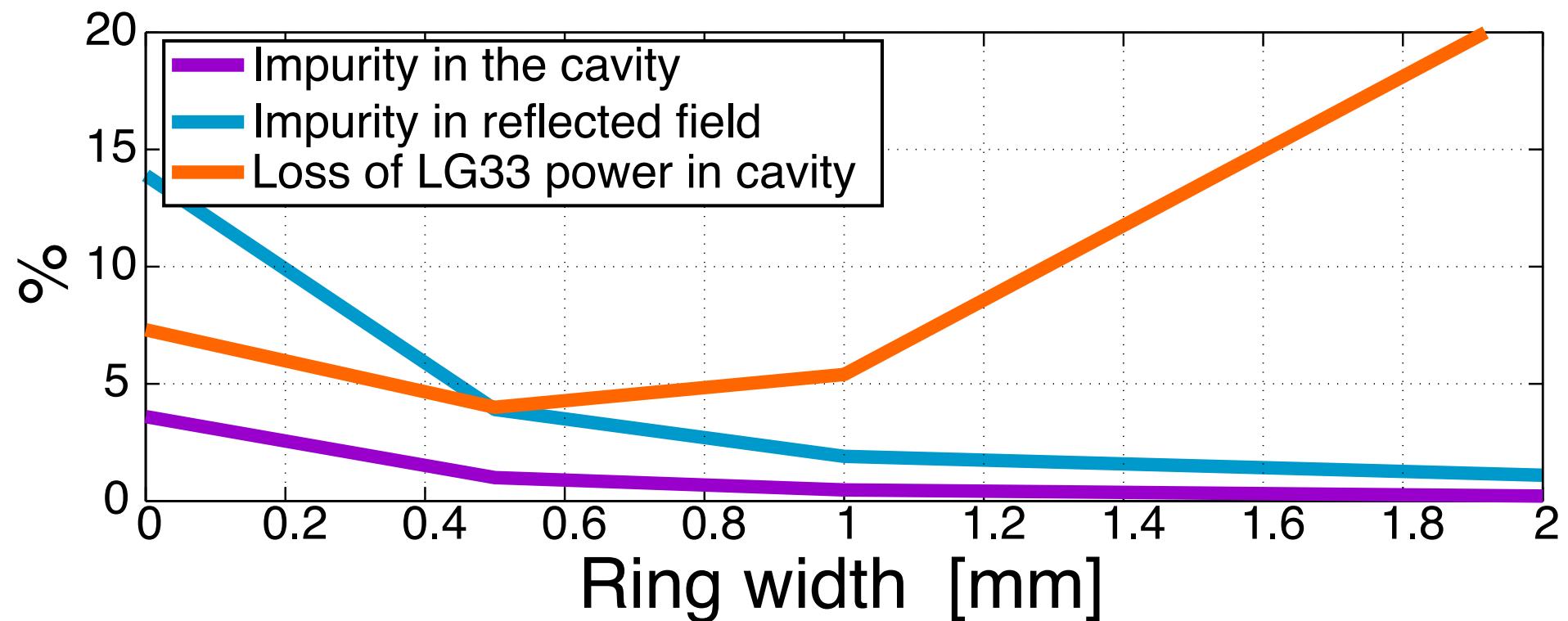


Mitigation – Rings (Yamamoto)





Mitigation – R=0 Rings (Yamamoto)

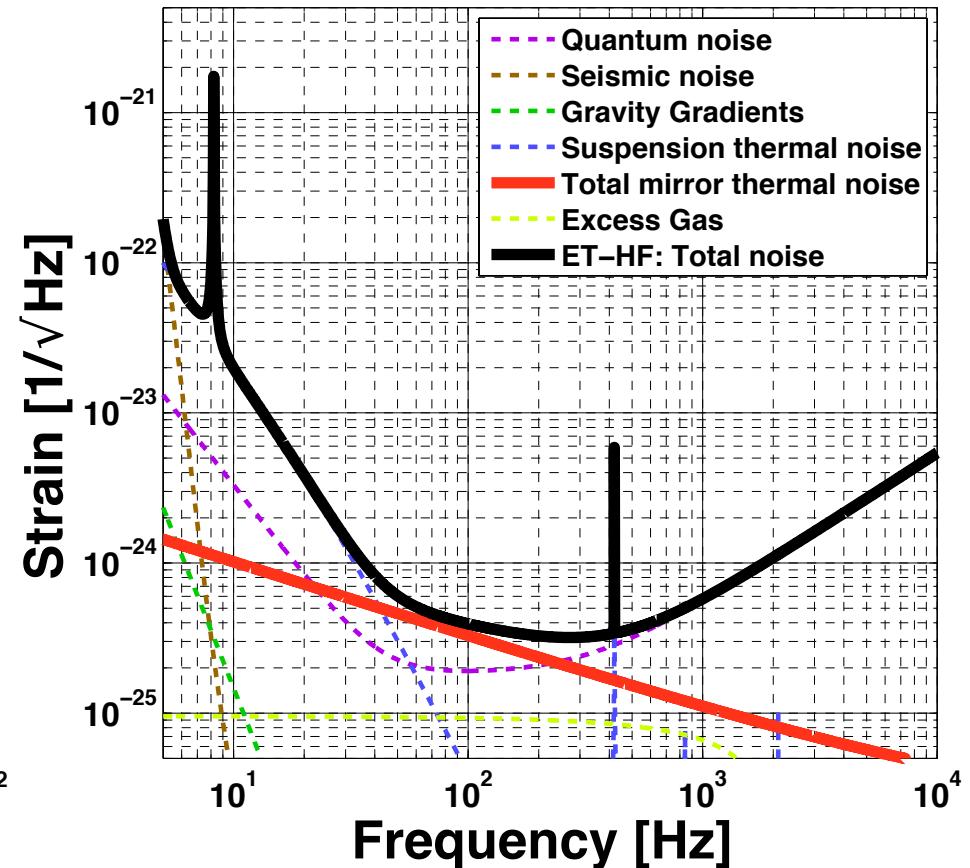
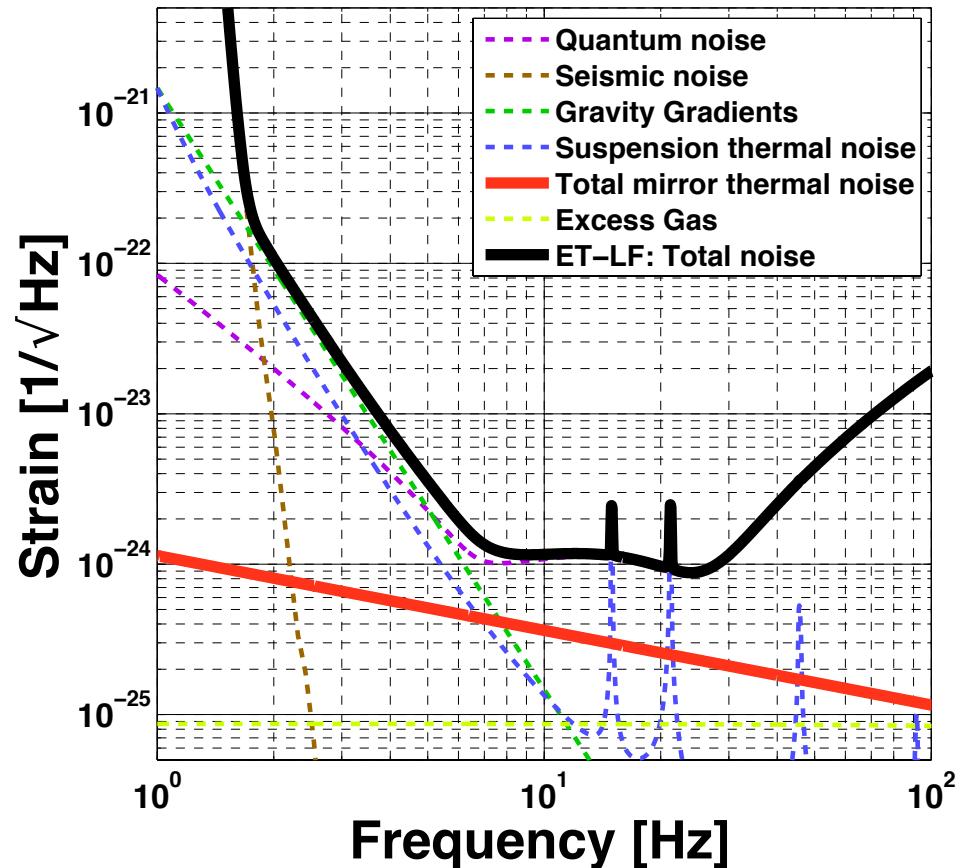




In short

- Due to mirror surface roughness, adopting LG_{33} beams in the near future will be extremely challenging

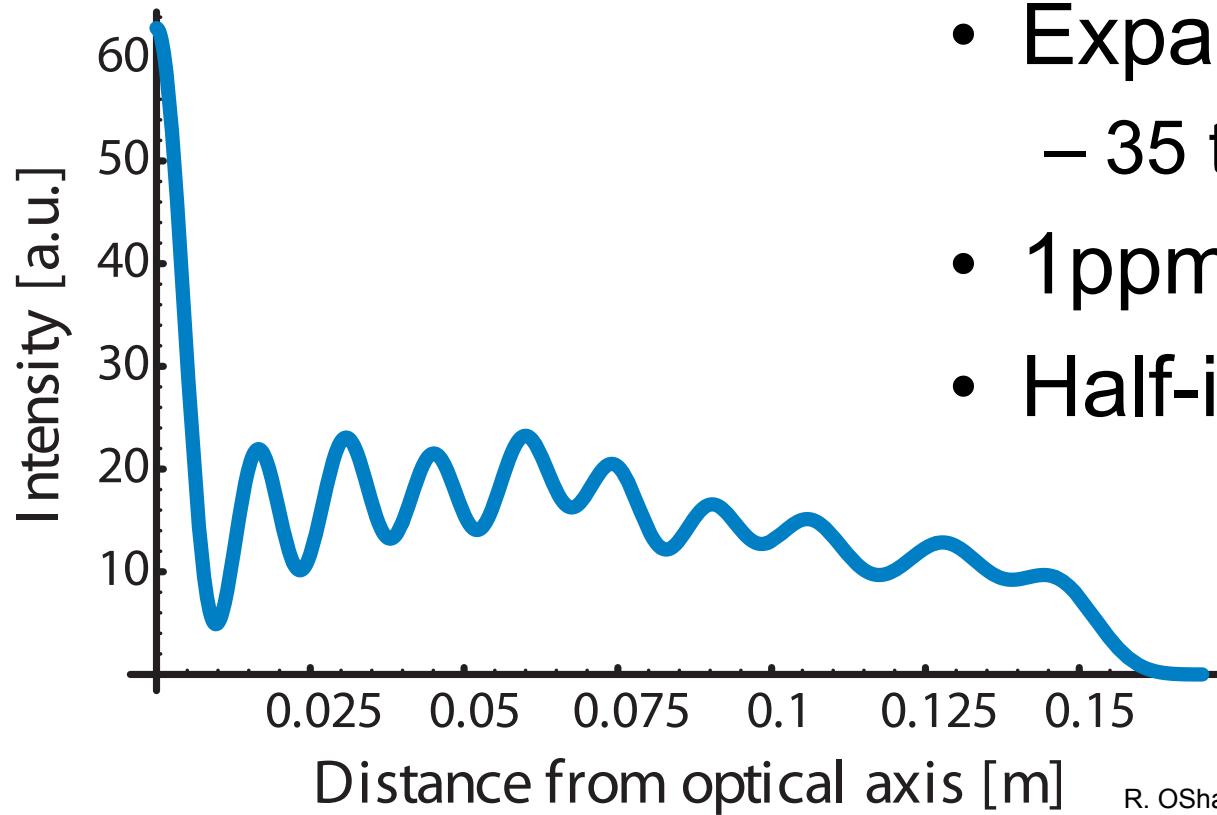
Designing the 'ultimate' beam



Hild et al., Class. Quantum Grav. 28, 094013 (2011)

Designing the ‘ultimate’ beam

- Lovelace scaling law
- Expansion in LG basis
 - 35 terms
- 1ppm per bounce
- Half-infinite mass

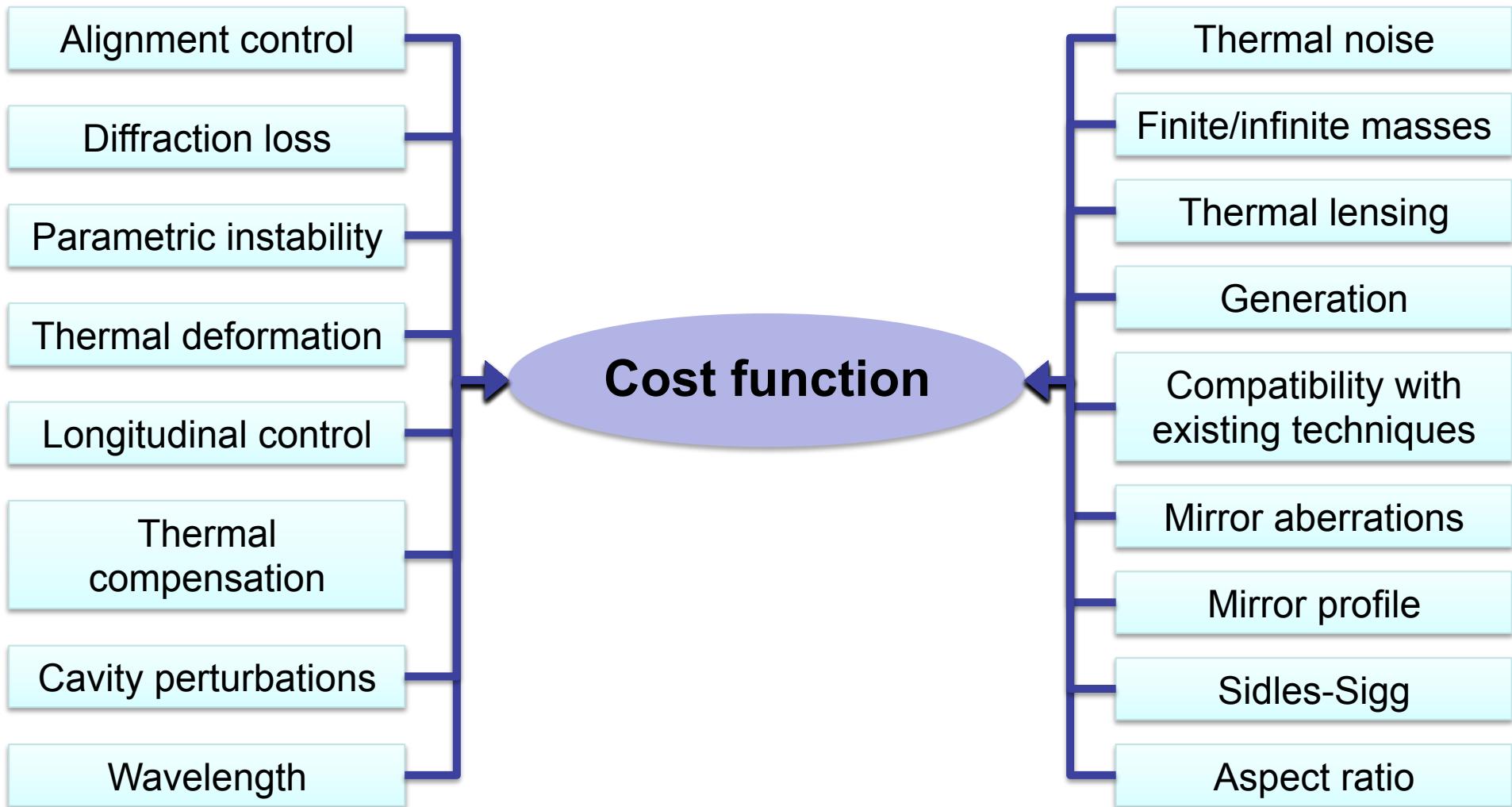


G. Lovelace, Class. Quant. Gravity 24, 4491 (2007).

R. O’Shaughnessy, S. Srigirin, S. Vyatchanin, arXiv:gr-qc/0409050.



Optimisation parameters/constraints





Requirements

- Experience required to define weighting/veto/constraints
 - What can polishers/TCS/control systems do?
 - What are critical parameters?
- Modular code with compatible input/output
 - Analytical/modal/FFT
- Clever optimisation – avoid local minima



Thoughts

- Difficult problem – start small
- How much improvement is available?
- Other ideas
 - unstable cavities
 - delay lines
 - coating-free cavities



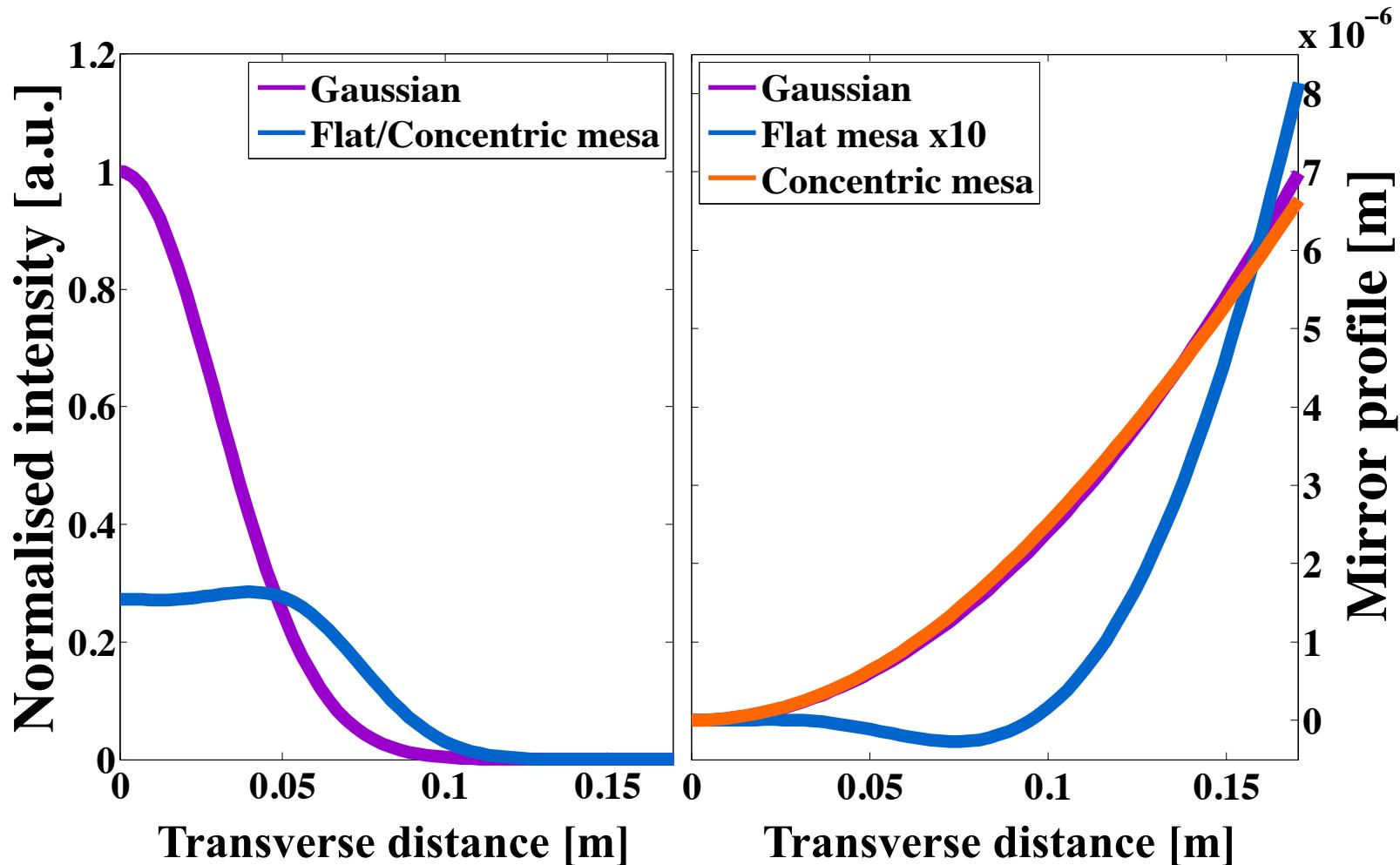
Summary

- Higher order LG beams appear to be hampered by mirror surface aberrations
- Efforts are ongoing to solve this problem
- Coating thermal noise will remain a significant problem in future detectors
- In the meantime we should think about methods of devising the optimal beam



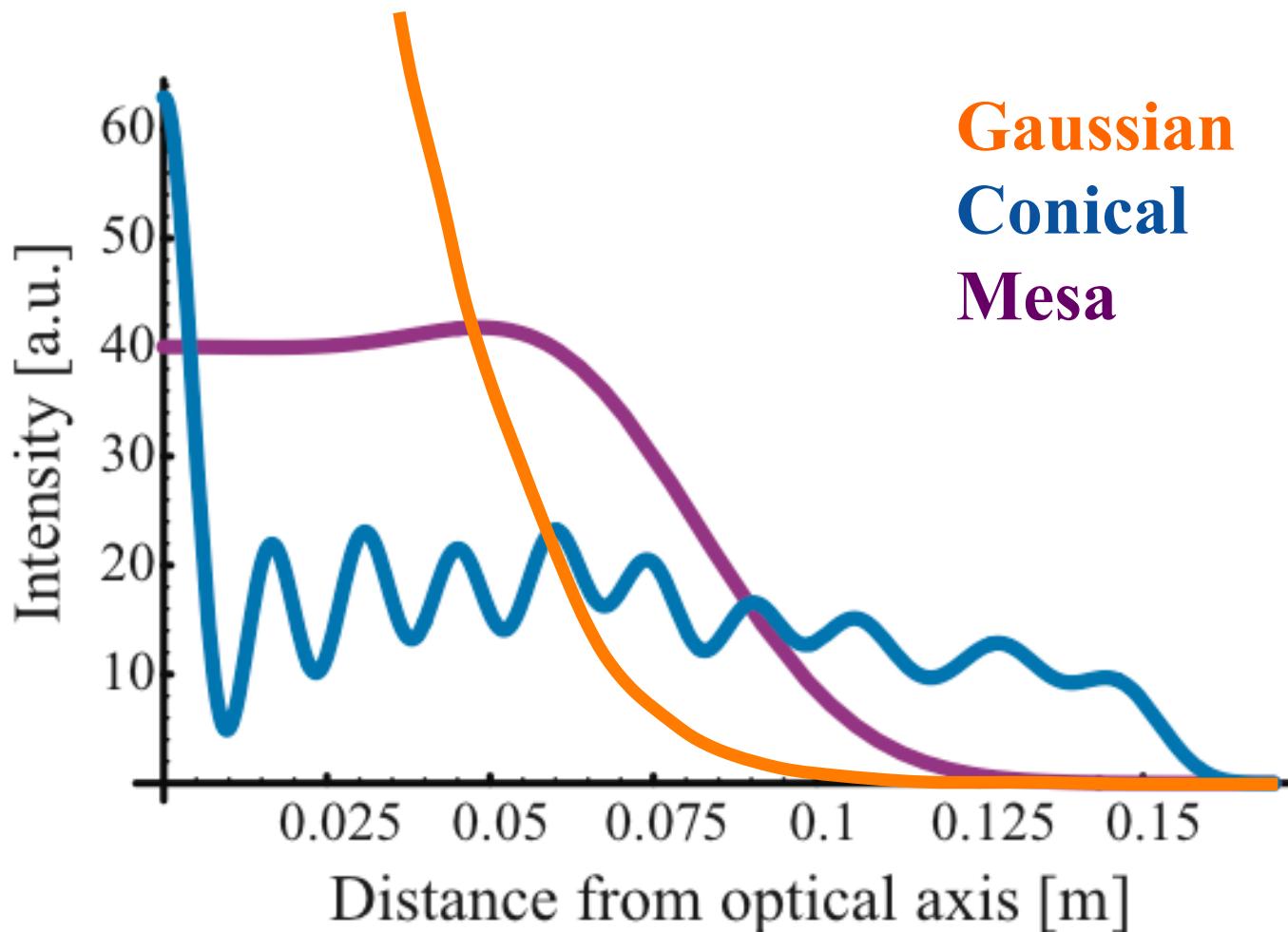
Contact details

New beam shapes for GW I - Mesa



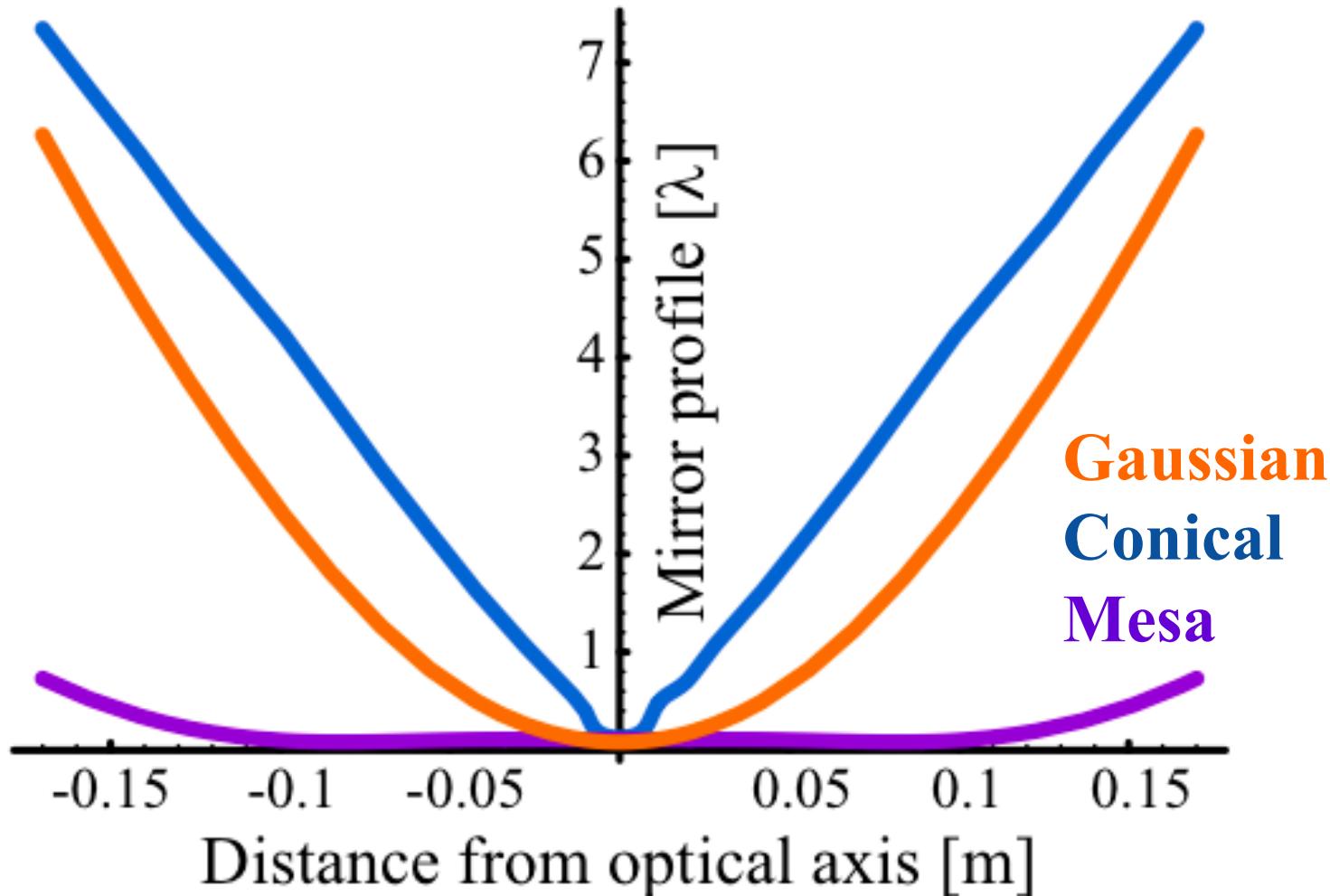
Bondarescu et al., Phys. Rev. D 74, 082003 (2006)

New beam shapes for GW II - Conical



Bondarescu et al., Phys. Rev. D 78, 082002 (2008)

New beam shapes for GW II - Conical



Bondarescu et al., Phys. Rev. D 78, 082002 (2008)



New beam shapes for GW - comparison

	Mesa	Conical	LG ₃₃
Thermal noise	✓ ✓	✓ ✓ ✓	✓ ✓
Creation/coupling	✓ ✓	✗	✓
Perturbations	✗	✗ ✗ ✗	✓
Control	✓	?	✓ ✓
Thermal effects	✓ ✓	?	✓ ✓ ✓
Mirror shape	✗	✗ ✗	✓ ✓ ✓ ✓ ✓ ✓ ✓