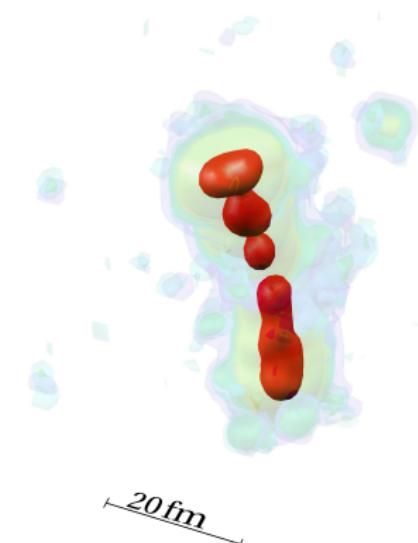


Dynamical description of heavy-ion collisions at Fermi energies

P. Napolitani (*IPN Orsay*), M. Colonna (*INFN-LNS*)

$^{130}\text{Xe} + ^{130}\text{Xe}$ 32 AMeV
 $b=7\text{ fm}$ $t=420\text{ fm/c}$

- Modelling fragment formation
- Fast and slow processes
- Focus on spinodal fragmentation
- Focus on neck fragmentation
- Focus on distillation
- *Putting all together*



Reaching Fermi energies : extensions and reductions

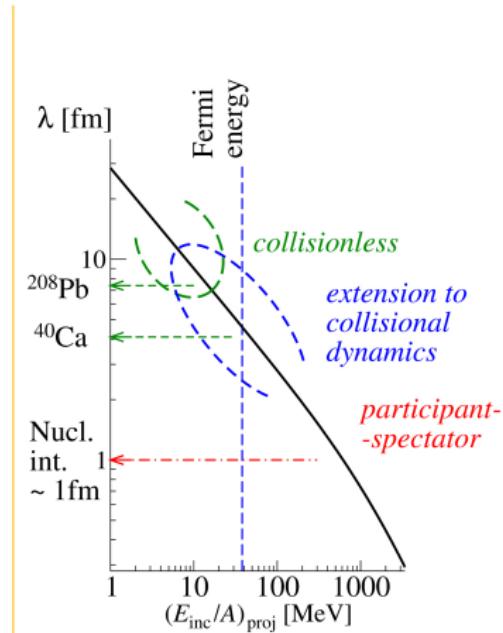
When moving to Fermi E , phase space allows for N-N collisions
(not Pauli blocked)



Extension to collisional dynamics

- All features of collisionless dynamics + ...
- dissipation → stopping and flow
- phase-sp. isoscalar/isovector fluctuations

Predominant feature of Fermi E is fragment formation and exit channel variety
⇒ Reduction of ρ -functional representation
(coherent states, no E -level scheme)



BLOB approach

- BLE for a fermionic system :

$$\dot{f} = \partial_t f - \{H[f], f\} = \bar{I}[f] + \delta I[f]$$

- BLOB : Fluctuations from N-N correlations in full phase space

At a given time t , in $(\mathbf{r}_a, \mathbf{p}_a)$, for elastic coll. :

$$\dot{f}_a(\mathbf{r}_a, \mathbf{p}_a) = g \int \frac{d\mathbf{p}_b}{h^3} \int d\Omega W(\mathbf{AB} \leftrightarrow \mathbf{CD}) F(\mathbf{AB} \rightarrow \mathbf{CD})$$

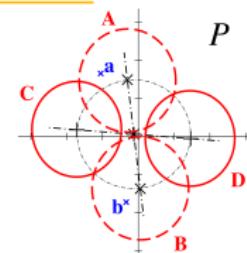
(P.Napolitani, M.Colonna, PLB726(2013)382)

$$\text{trans. rate} : W(\mathbf{AB} \leftrightarrow \mathbf{CD}) = \left\langle |v_a - v_b| \frac{d\sigma}{d\Omega} \right\rangle_{\mathbf{AB} \rightarrow \mathbf{CD}} = \left\langle W(ab \leftrightarrow cd) \right\rangle_{\mathbf{AB} \rightarrow \mathbf{CD}}$$

$$\text{occupancy} : F(\mathbf{AB} \rightarrow \mathbf{CD}) = \bar{f}_A \bar{f}_B f_C f_D - f_A f_B \bar{f}_C \bar{f}_D = \left\langle F(ab \rightarrow cd) \right\rangle_{\mathbf{AB} \rightarrow \mathbf{CD}}$$

occupancy variance : fluctuations amplitude determined by the variance $= f(1 - f)$ in a phase space cell h^3 at equilibrium.

⇒ Wave packets should contain $N_{\text{test}} = \text{num. of test particles}$ contained in the system / A



Chronology

Set of BLOB calculations

- soft EOS
($k_{\text{inf}} = 200 \text{ MeV}$)
- linear asy-EOS
(Guarnera,Colonna,Chomaz PLB373 (1996) 297)

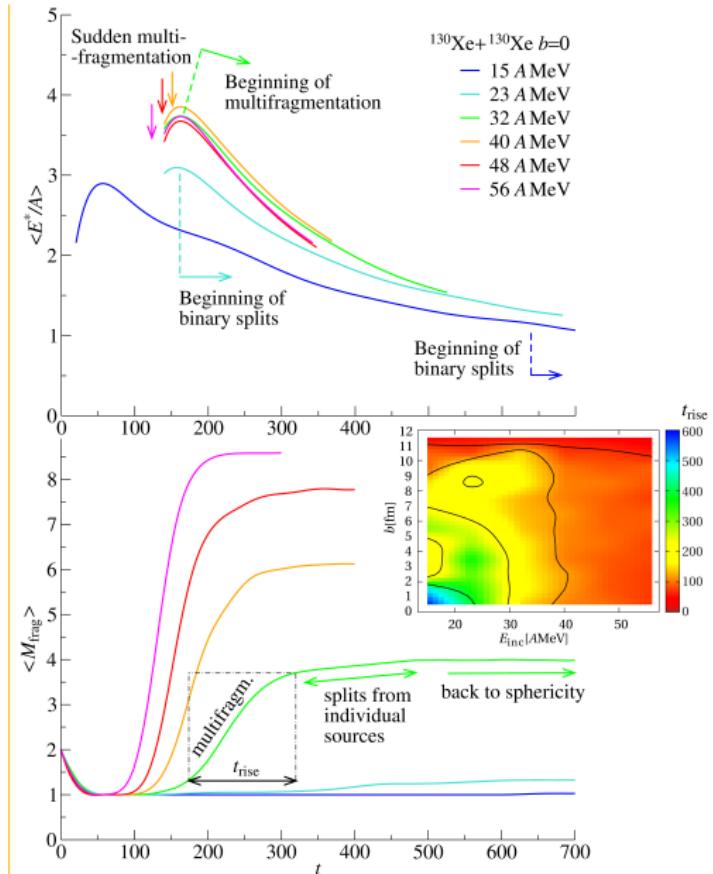
- W with in-medium

σ_{NN}

(Danielewicz Acta Phys.Pol.B33 (2002) 45)

- Dynamics till saturation of fragm. multiplicity
(\neq F.O. !)

System : $^{130}\text{Xe} + ^{130}\text{Xe}$
(recalling widely investigated Sn-to-Xe region
see reviews in EPJA 50 (2014))

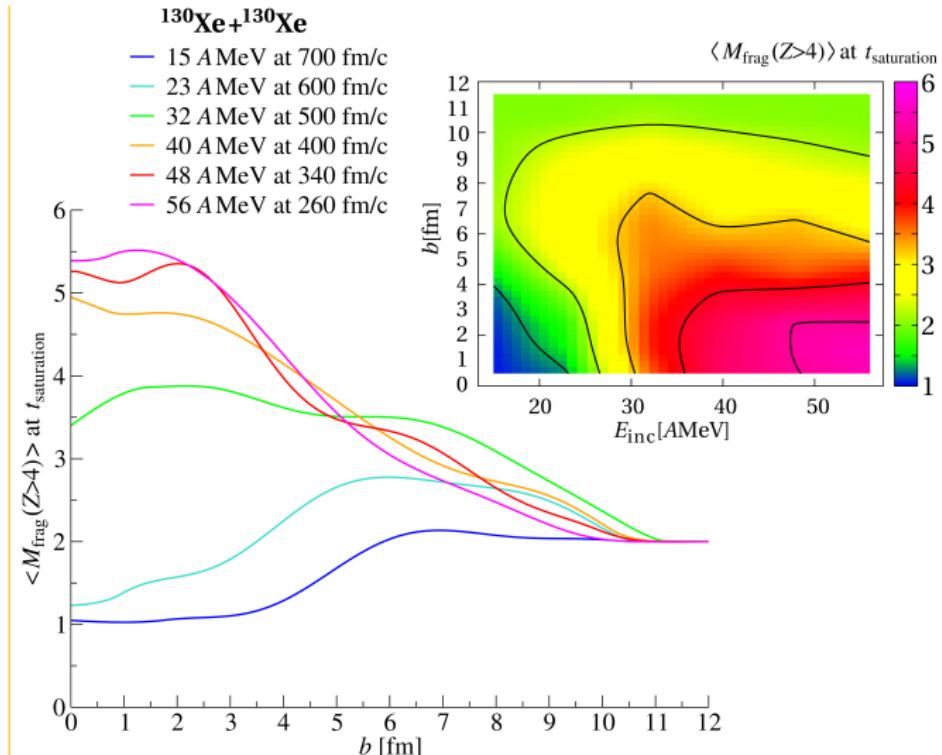


Multiplicity survey

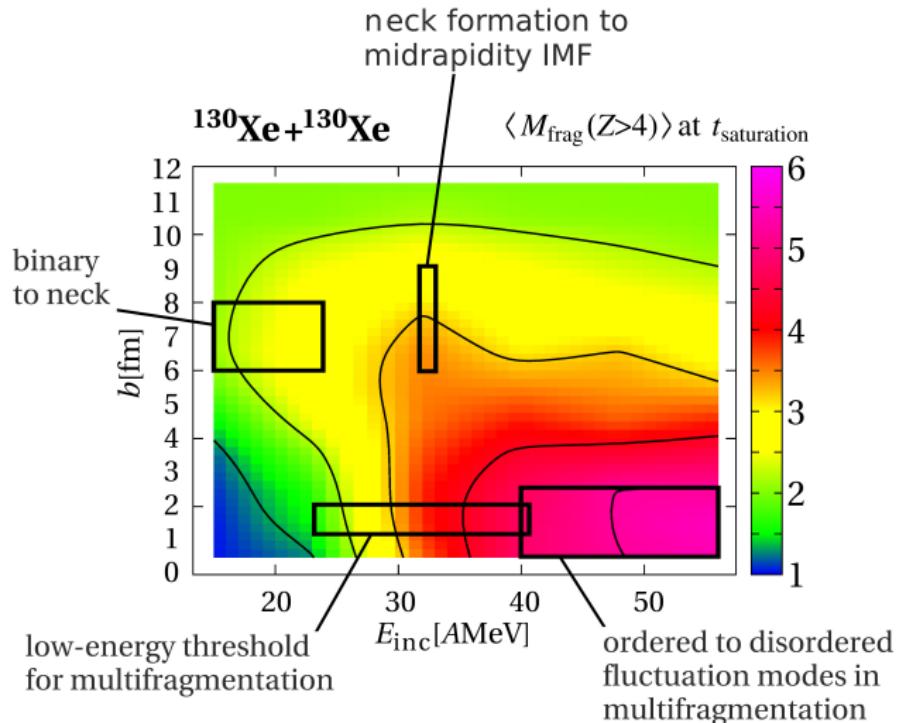
along b - E_{inc} landscape,

- Large variation of reaction times
- Large variation of fragment multiplicity (for $Z > 4$) (mostly around 30 A MeV)

⇒ several transitions of mechanisms ?



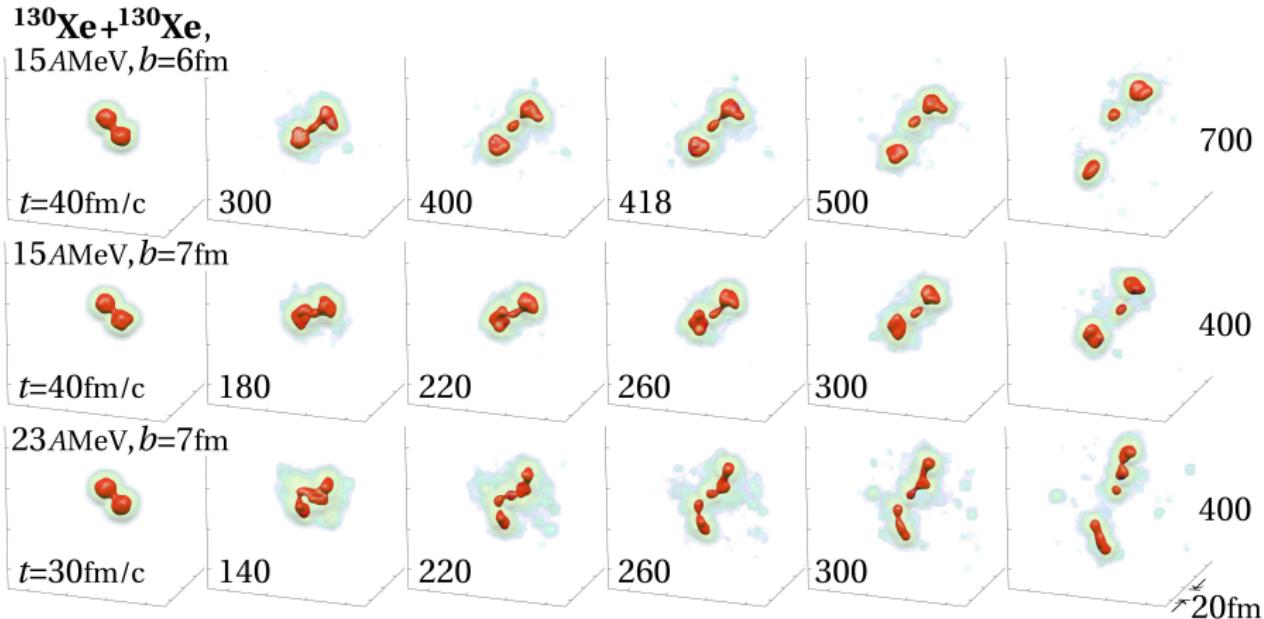
Exploring Fermiland



Exp : Kohley, Yennello EPJA 50 (2014) 31 ; DeFilippo, Pagano EPJA 50 (2014) 32 ; Ademard et al., EPJA 50 (2014) 33...

Theo : B.-A.Li C.M.Ko W.Bauer, Int.J.Mod.Phys. E7 (1998) 147 ; Baran et al., Phys.Rep. 410 (2005) 335 ; EPJA 50 (2014)...

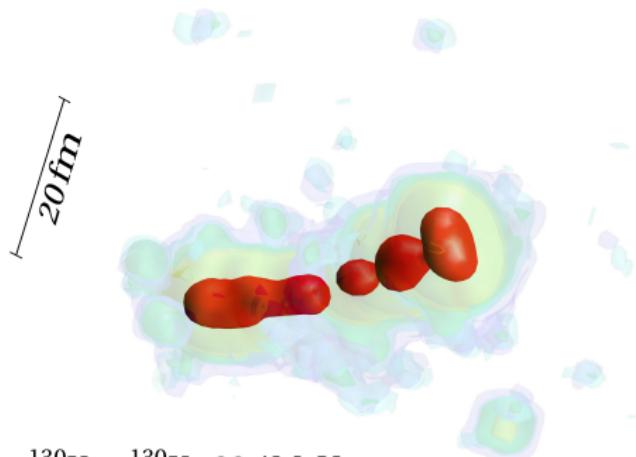
Neck fragmentation



Exp : G.Casini et al., PRL 71, 2567 (1993) ; F.Bocage et al. NPA676 (2000) 391 ; E.DeFilippo et al. PRC71 (2005) 044602...

Isoscalar / isovector neck features

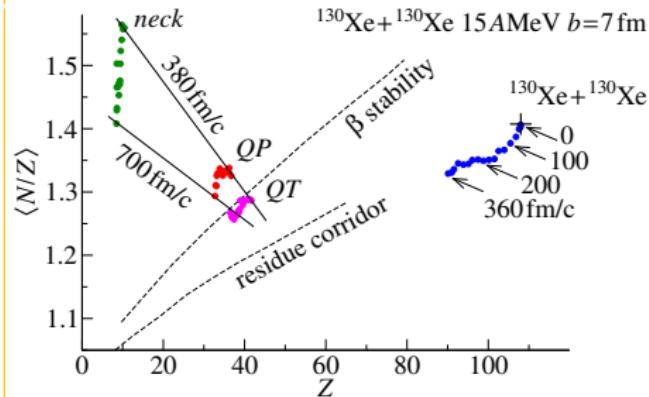
Isoscalar) : hierarchy of sizes in neck fragmentation :



$^{130}\text{Xe} + ^{130}\text{Xe}$ 32 AMeV
 $b=7\text{ fm}$ $t=420\text{ fm/c}$

Colin et al. PRC67 (2003) 064603

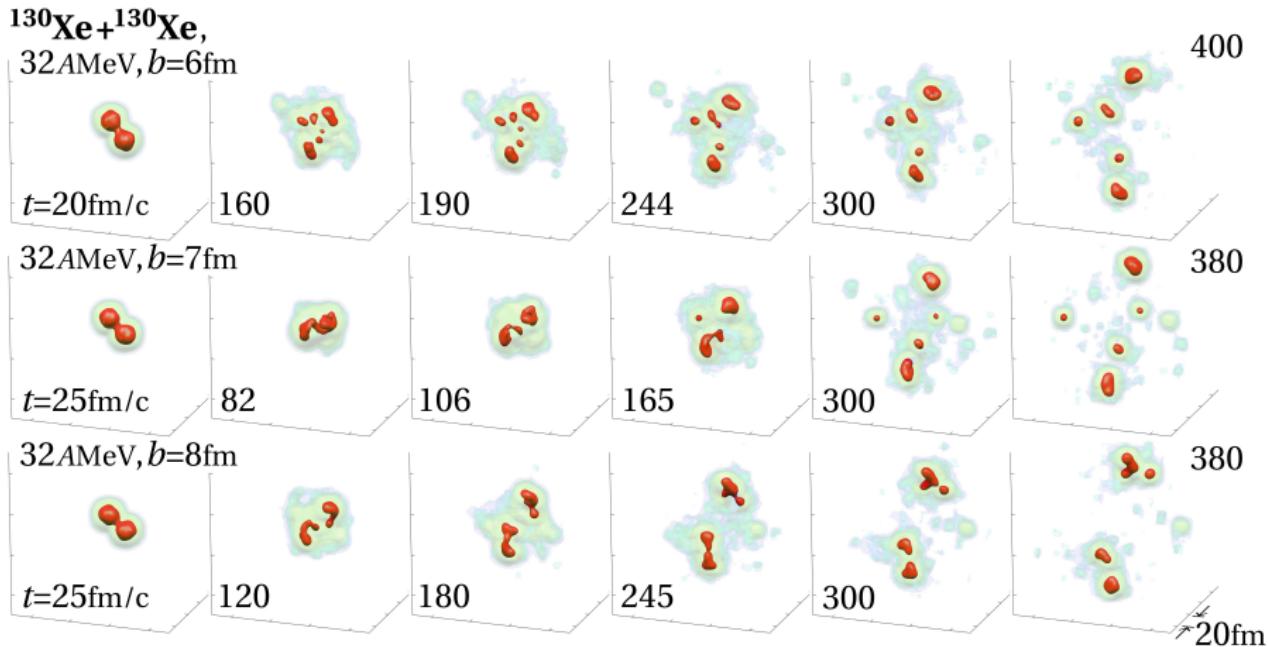
Isovector) : Isospin migration towards the neck :



(reduced effect if the neck joins back to QP/QT)

Lionti,Baran,Colonna,DiToro, PLB625 (2005) 33...

Midrapidity

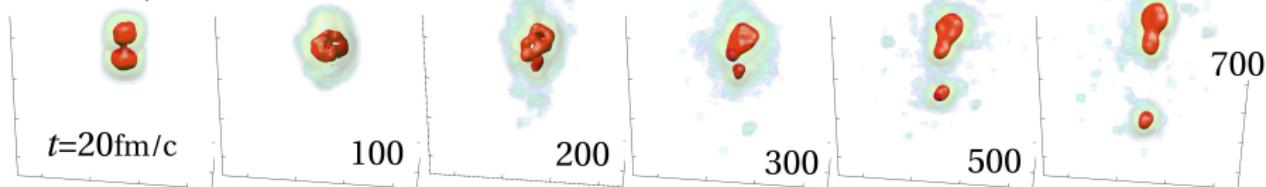


- more than one neck IMF, eventually very forward emitted

Baran,Colonna,DiToro,Zus PRC85 (2012) 054611 ; Rizzo,Colonna,Baran,DiToro PRC90 (2014) 054618...

spinodal multifragmentation & re-aggregation

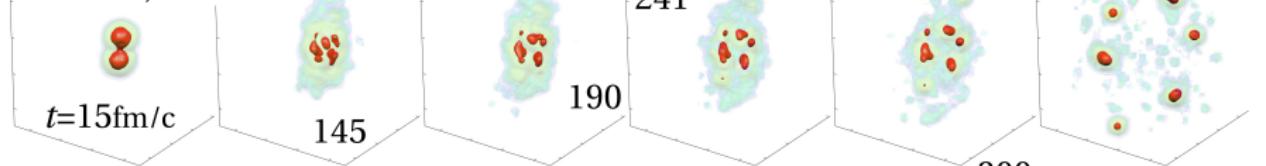
$^{130}\text{Xe} + ^{130}\text{Xe}$,
23AMeV, $b=1\text{fm}$



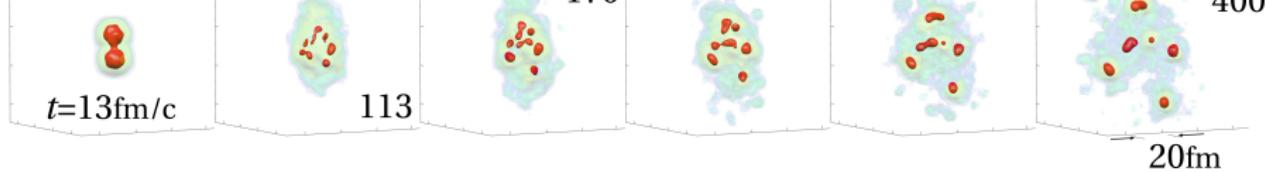
32AMeV, $b=1\text{fm}$



32AMeV, $b=1\text{fm}$



40AMeV, $b=1\text{fm}$



20fm

10

spinodal multifragmentation & re-aggregation

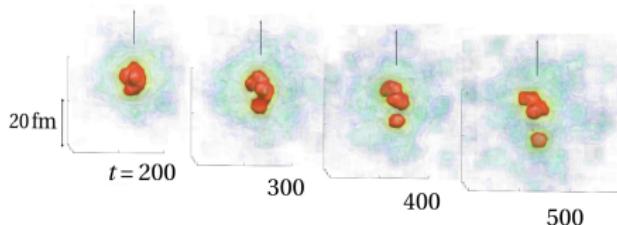
- Spinodal regime : wavelength of the leading isoscalar mode λ is reflected in fragm. sizes → IMF of similar $A_{\text{frag}} \approx \rho(\lambda')^3$ (\approx region O, Ne)

Theo : Chomaz,Colonna,Randrup Phys.Rep. 389 (2004) 263

Exp : B.Borderie et al. PRL 86 (2001) 3252 ; G.Tabacaru EPJA 18 (2003) 103

- Low-energy multifragmentation threshold : recombining of fragments → loss of size asymmetry and reduction of multiplicity
→ similar effect in relativistic proton-induced spallation :

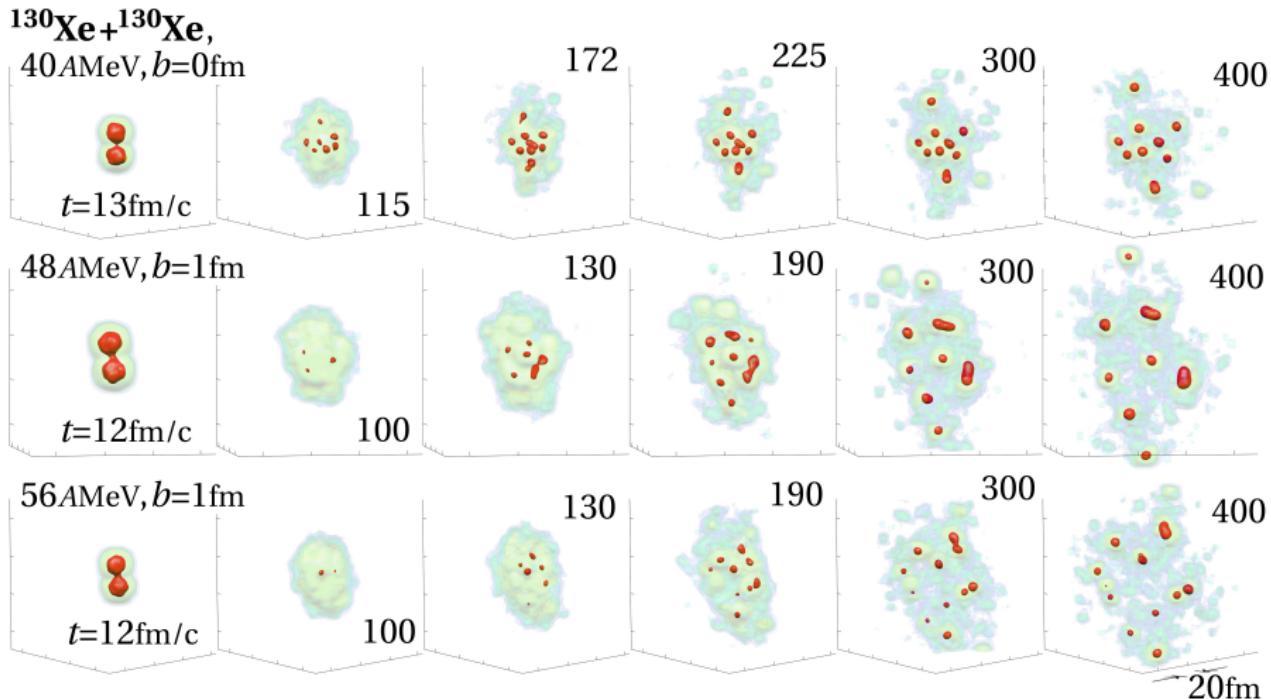
$^{136}\text{Xe} + p$ 1 AGeV



Napolitani Colonna PRC 92 (2015) 034607

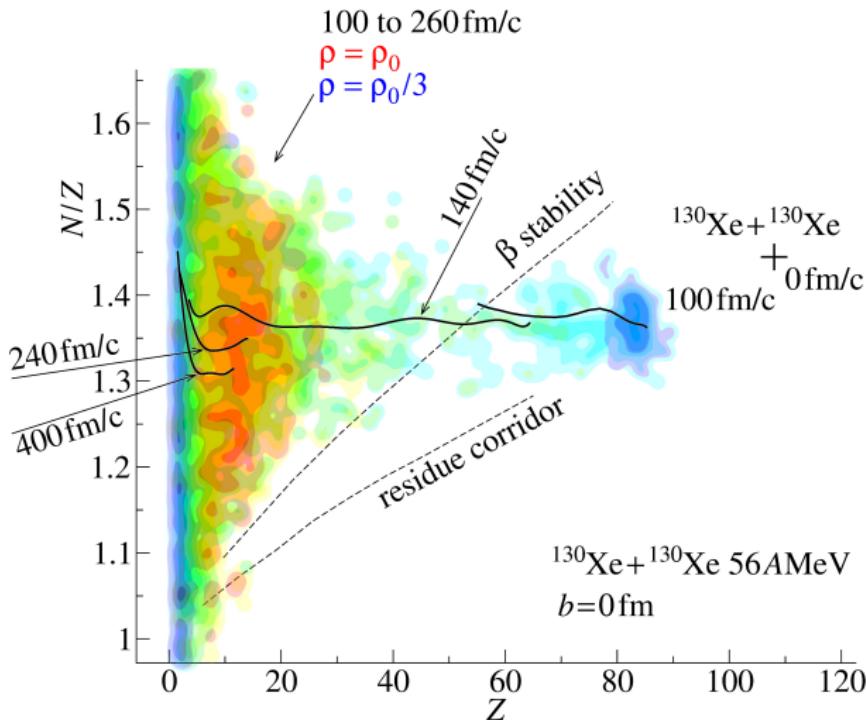
- High-energy multifragmentation threshold : no more ordered modes → loss of size asymmetry

"disordered" multifragmentation



Isospin distillation at low-density

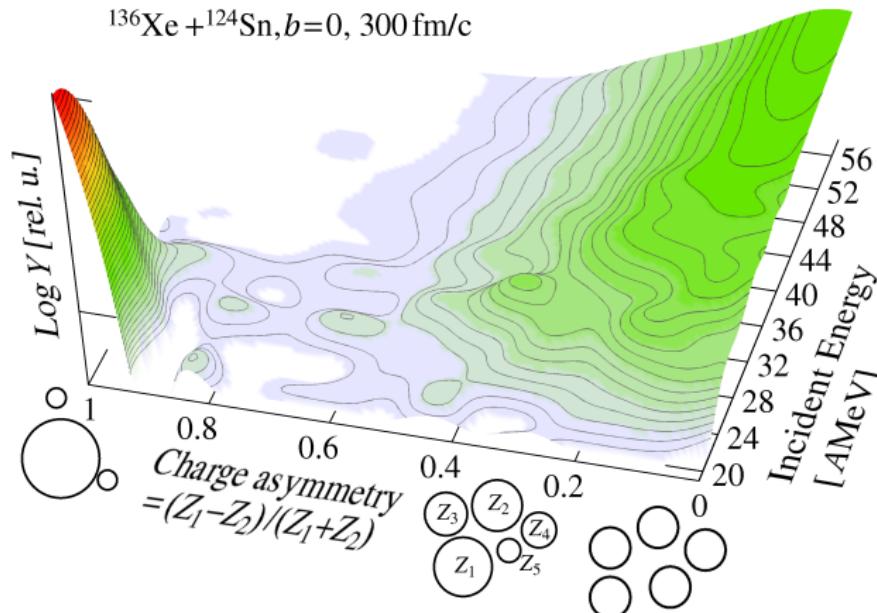
- *distillation :*
more n in the most volatile phase



(Muller, Serot, PRC 52 (1995) 2072 ;
B.-A.Li, C.M.Ko, NPA 618 (1997) 498 ;
Ducoin et al. NPA 781 (2007) 407 ;
Colonna et al. PRC 78 (2008) 064618 ;
Colonna, PRL 110 (2013) 042701...)

1^{st} o. phase trans. in central collisions

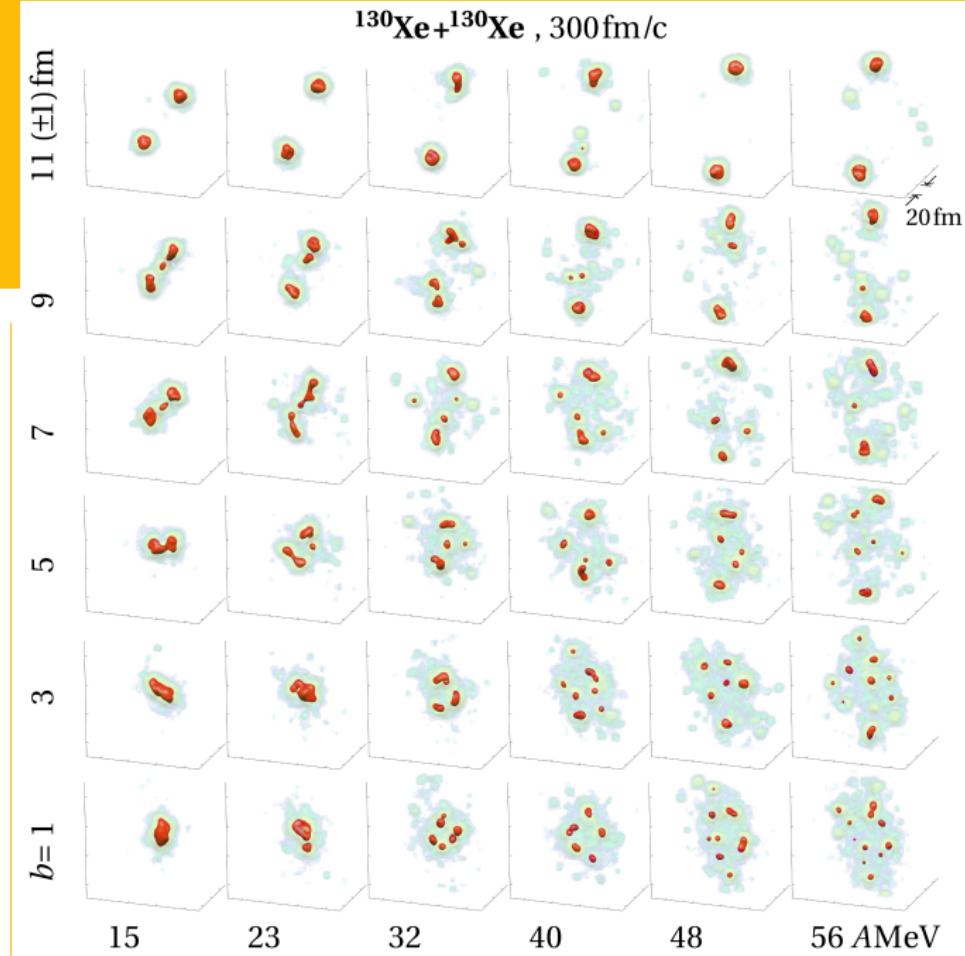
Same macroscopic initial conditions $\rightarrow E$ fluctuations
 \rightarrow oscillation between two energetically favoured configurations.
Studied in a similar system for $b = 0$ ([P.N.,M.Colonna PLB726\(2013\)382](#)) :



$\rightarrow 1^{st}$ o. phase trans. features found as a result of fragm. dynamics
(recolling bimodality : [E.Bonnet et al. PRL103 \(2009\) 072701](#) ; [M.Pichon et al. NPA779 \(2006\) 267](#))

Map of dynamical processes at Fermi E

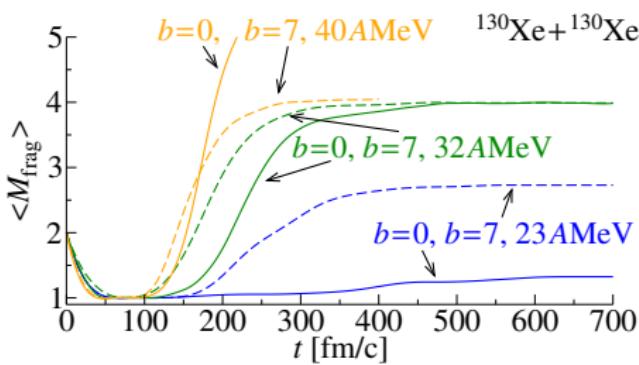
Examples of most probable mechanisms leading to IMFs at 300 fm/c where fragments are present



Conclusions

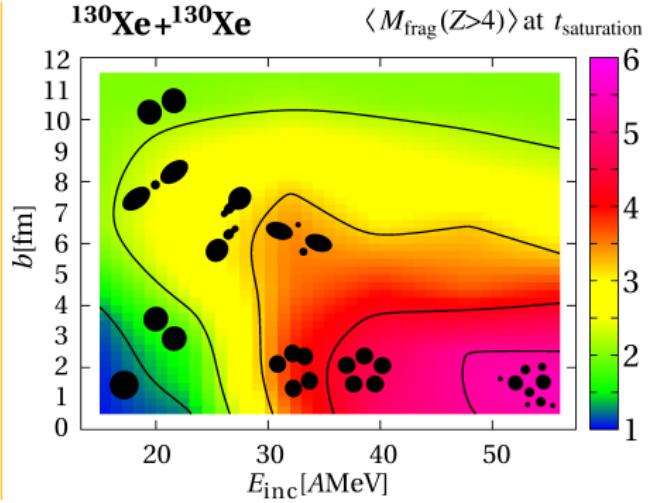
- From a full survey of the dynamical process (including the **out-of-equilibrium** stage, and even allowing for some model dependence) we can expect for intermediate-size nuclear systems :

1) Processes over different time intervals :



2) Variety of exit channels

→ Fermi- E “bestiary” :



- The clustering process should complete the above picture.