



# Quantitative X-Ray Phase-Contrast Microtomography from a Compact Laser Driven Betatron Source

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2. Ludwig-Maximilians-Universität München, Am Coulombwall 1, 85748 Garching, Germany

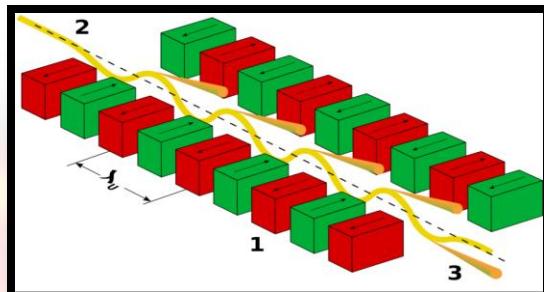
3. Technische Universität München, James Franck-Straße 1, 85748 Garching, Germany

EAAC 2015, La Biodola, Isola d'Elba

J. Wenz et al., Nature Comm. DOI:10.1038/ncomms8568 (2015)

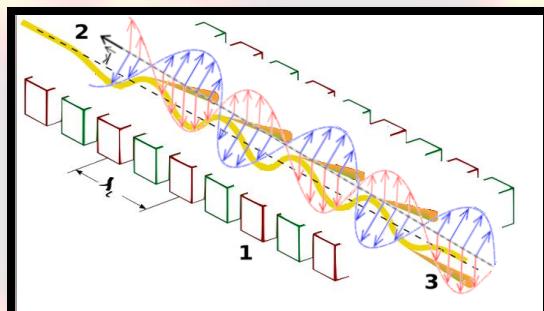


# Sources of X-Ray Radiation from LWFA electrons

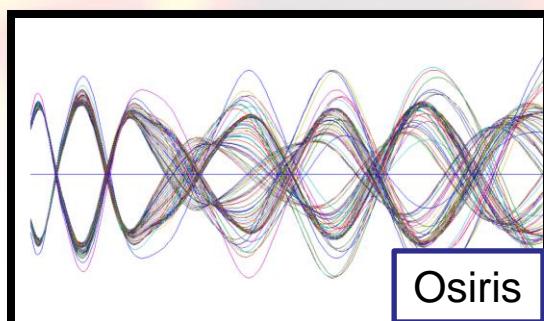


Based on electron oscillation due to

External magnetic field → Undulator radiation



External laser field → Thomson scattering



Internal EM fields → Betatron radiation



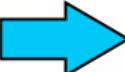
# Betatron Radiation

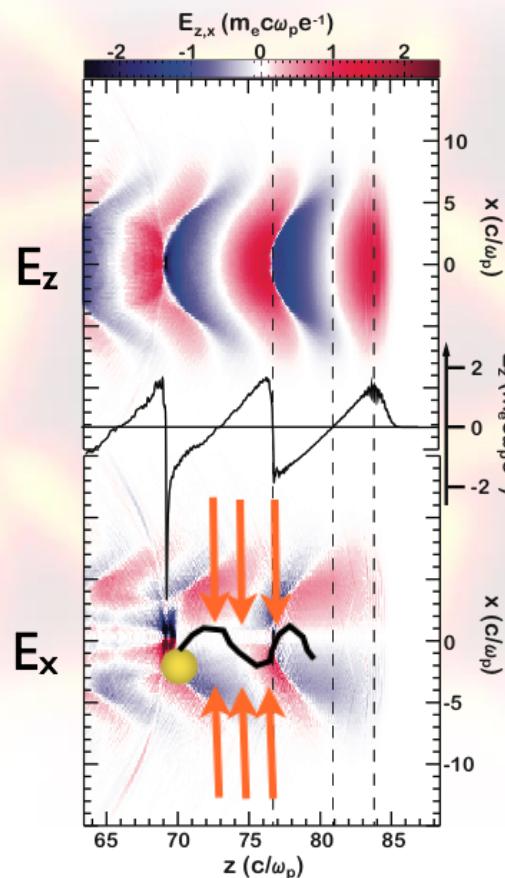
## Electric Fields in the Plasma Wave

strong transverse focusing fields

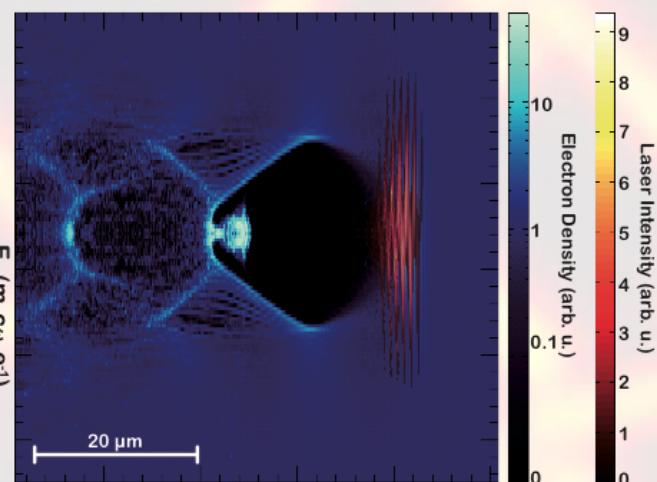
- + small source size
- increased divergence

BUT

Betatron Oscillation  X-ray radiation

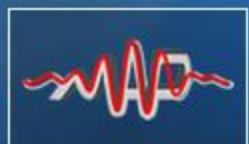


$$\lambda_\beta \approx \sqrt{2\gamma}\lambda_p \approx 300 \text{ } \mu\text{m}$$

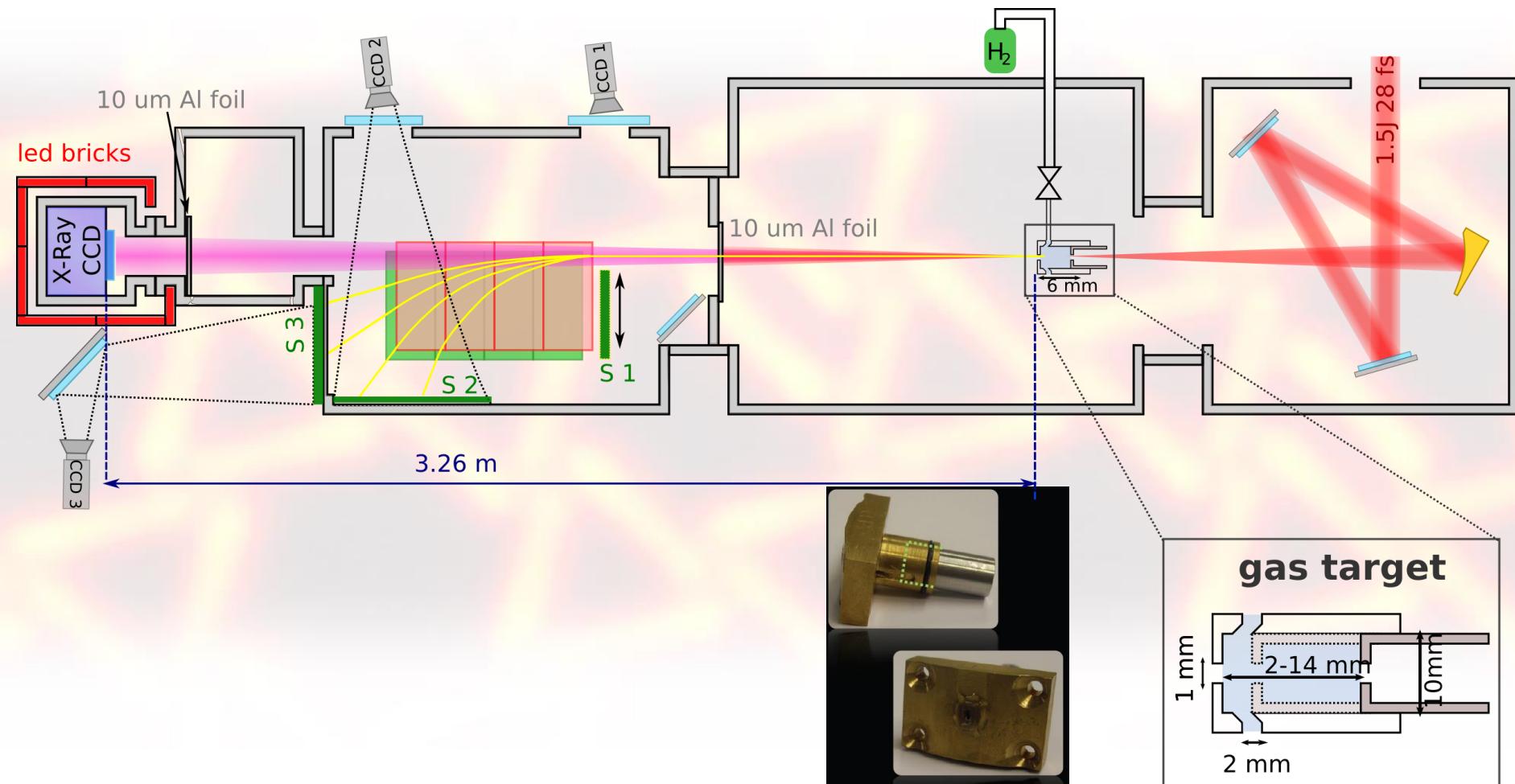


$$K_\beta = \gamma r_\beta k_\beta$$

$$\lambda = \frac{\lambda_\beta}{n2\gamma^2} \left( 1 + \frac{K^2}{2} + \gamma^2 \theta^2 \right)$$



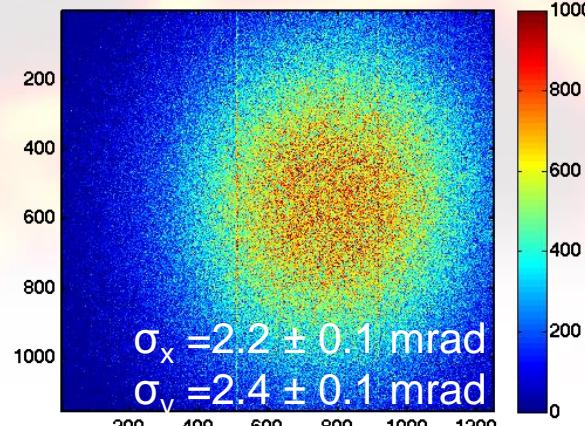
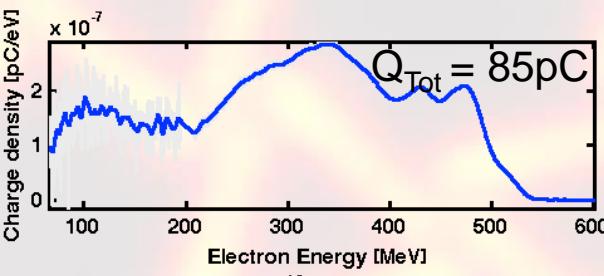
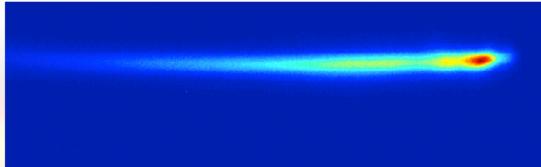
# Experimental Setup



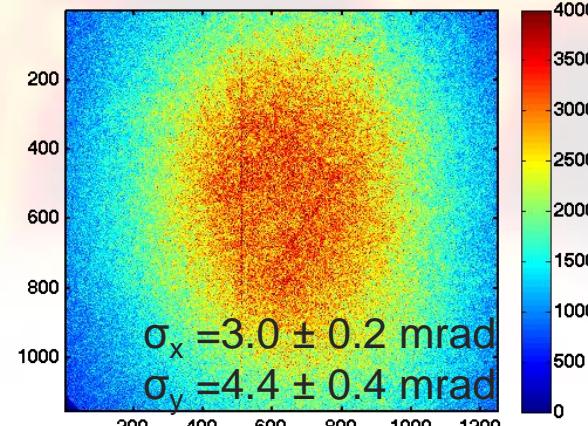
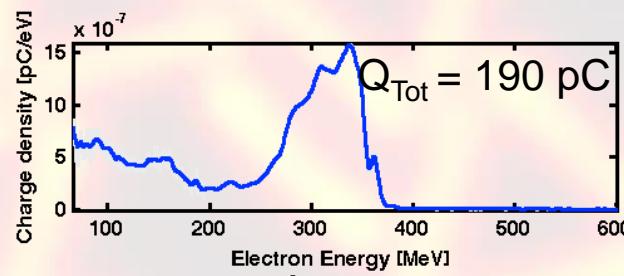
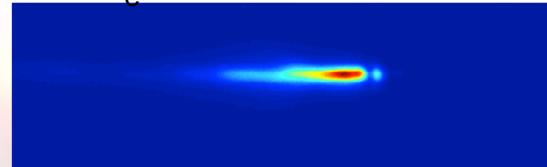


# Betatron Beam Profile

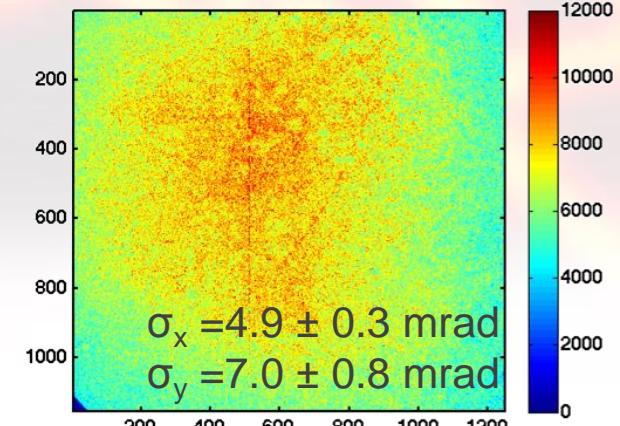
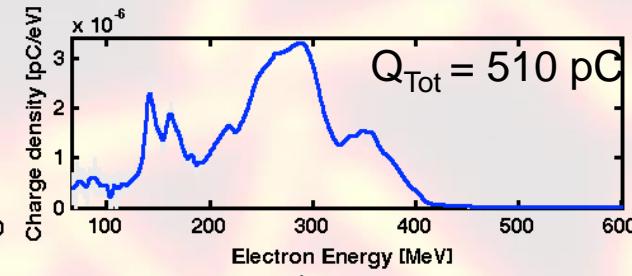
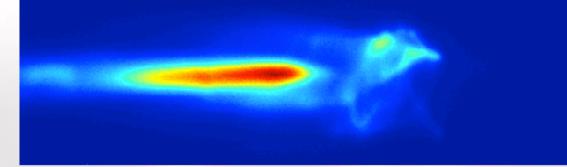
$$n_e = 7.4 \times 10^{18} \text{ e/cm}^3$$

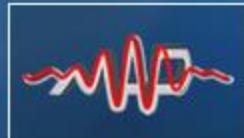


$$n_e = 9.4 \times 10^{18} \text{ e/cm}^3$$

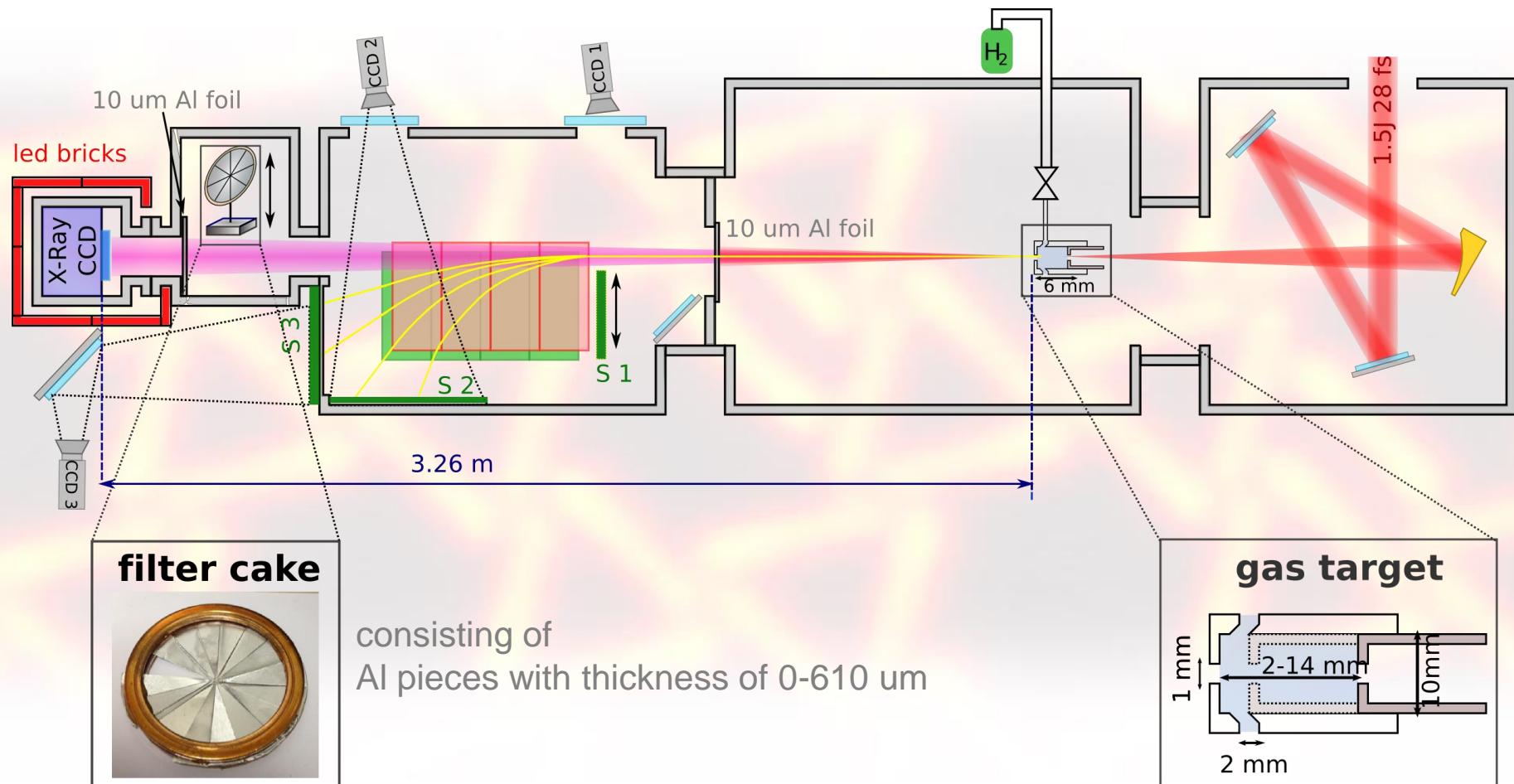


$$n_e = 1.1 \times 10^{19} \text{ e/cm}^3$$





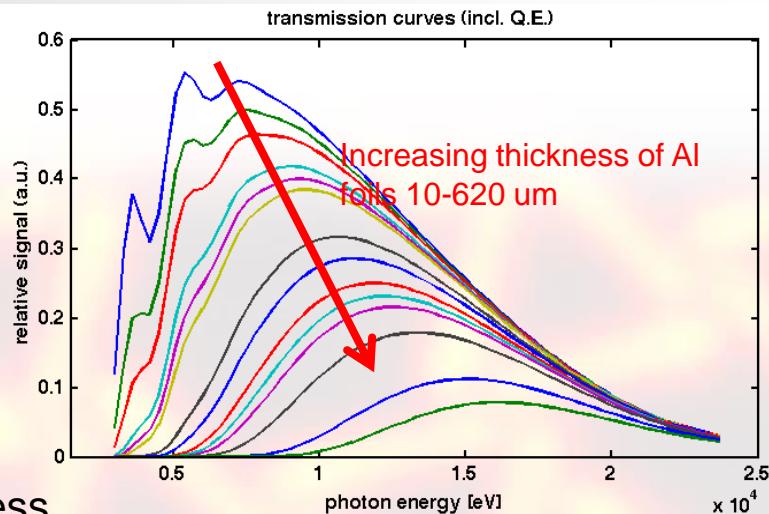
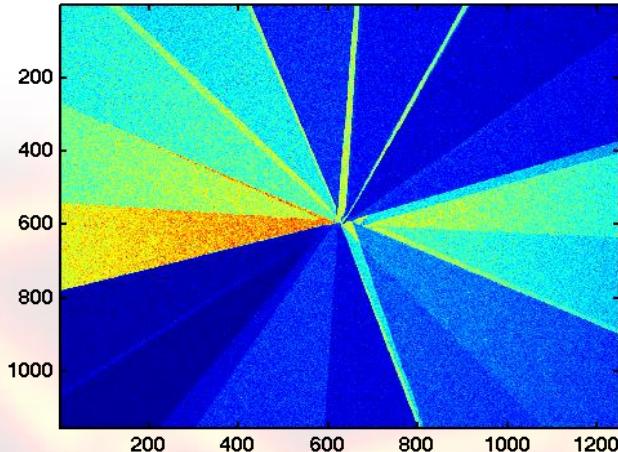
# Single-Shot Characterization of the Betatron Spectrum



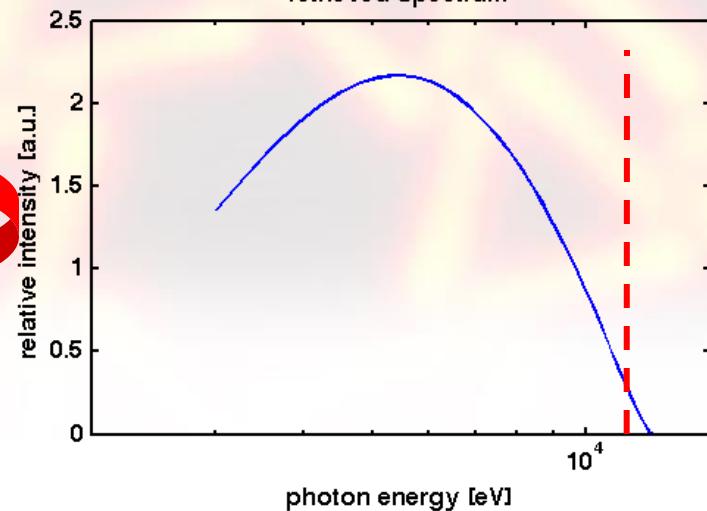
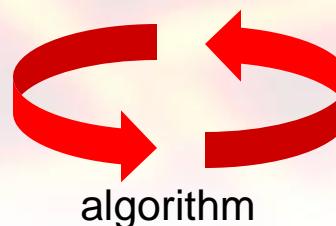
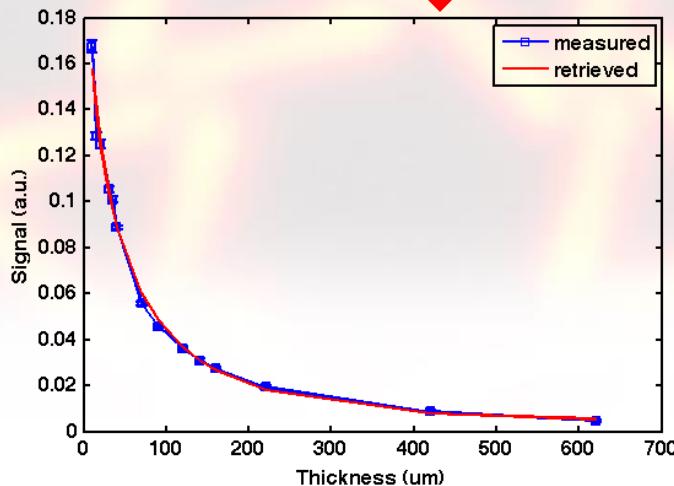


Sidky et al, J. Appl. Phys. 97, 124701 (2005)

# Spectrum Reconstruction

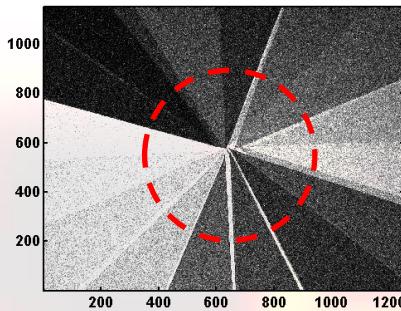


Different filter thickness  
Different CCD counts

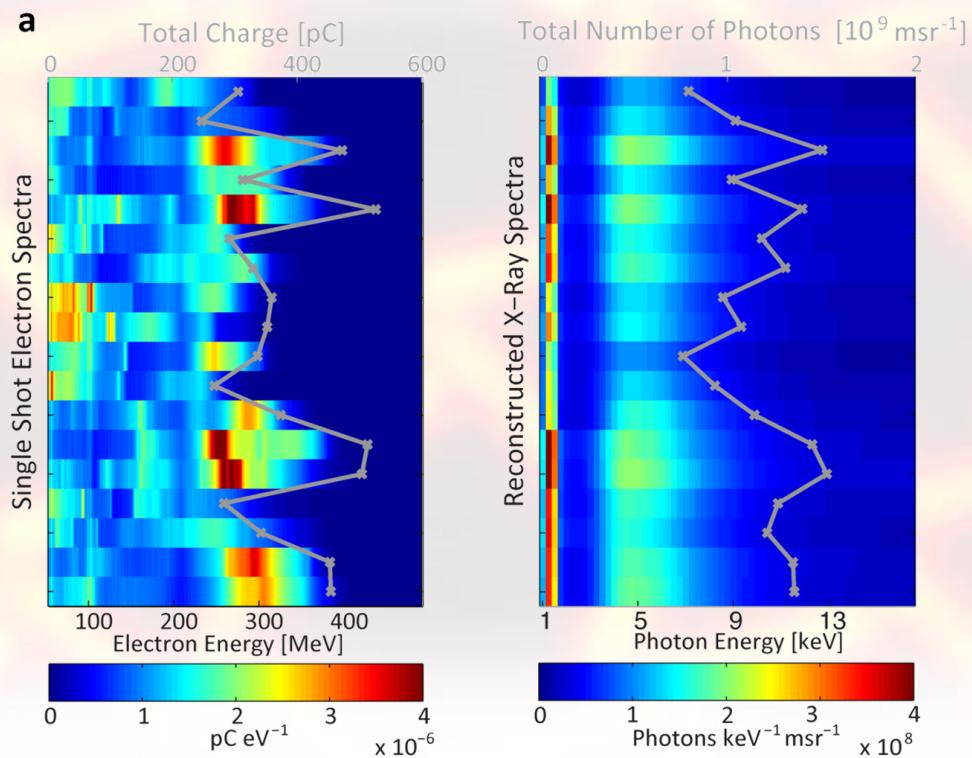
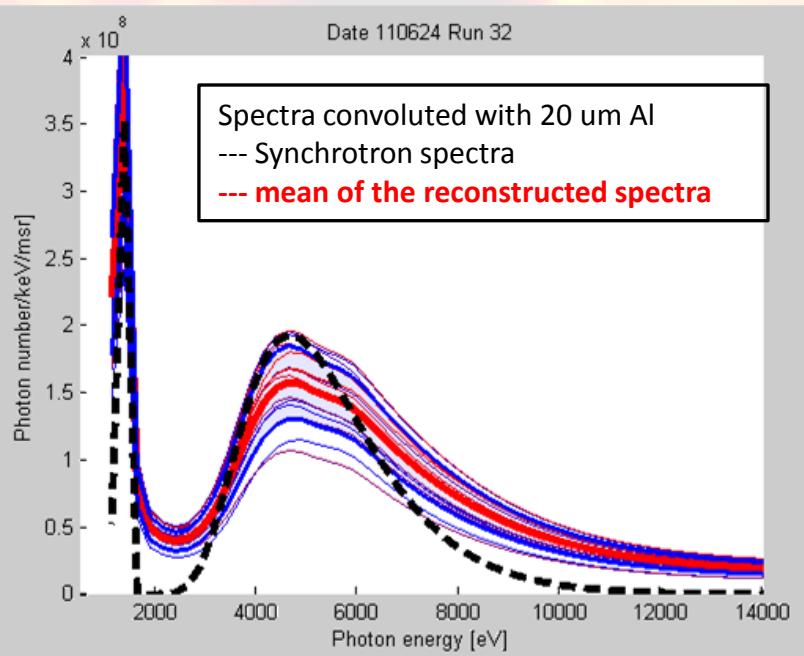


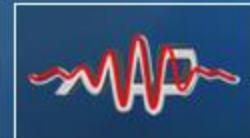


# Reconstructed Betatron Spectrum

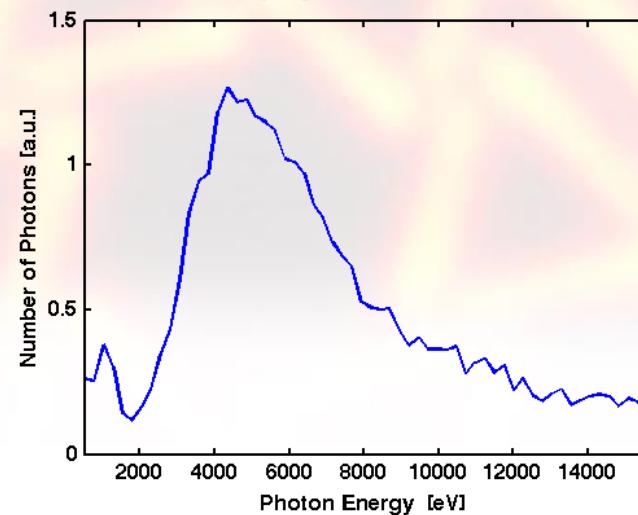
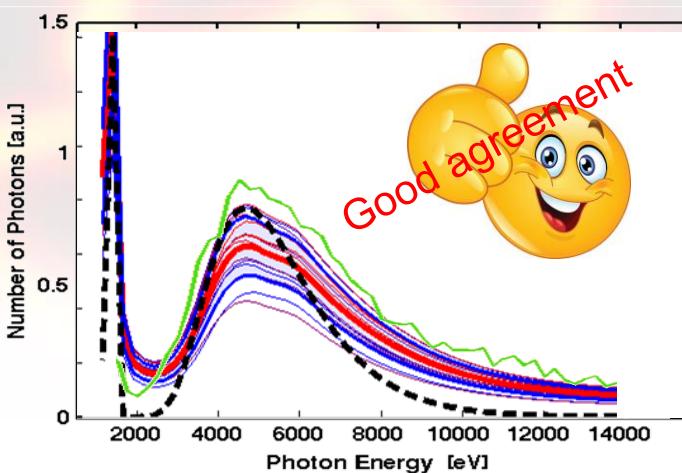
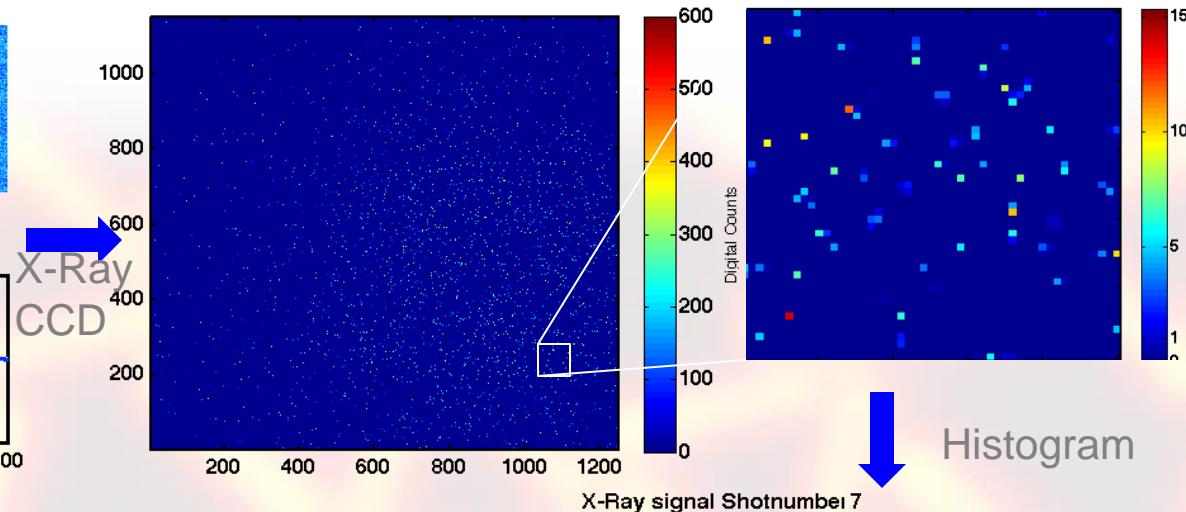
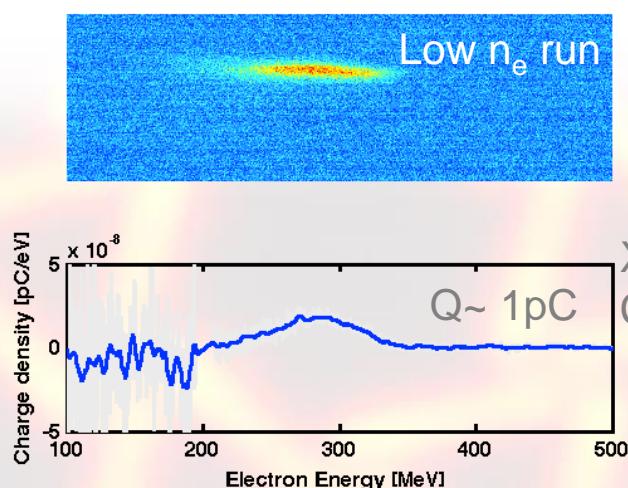


Date 110624 Run 32



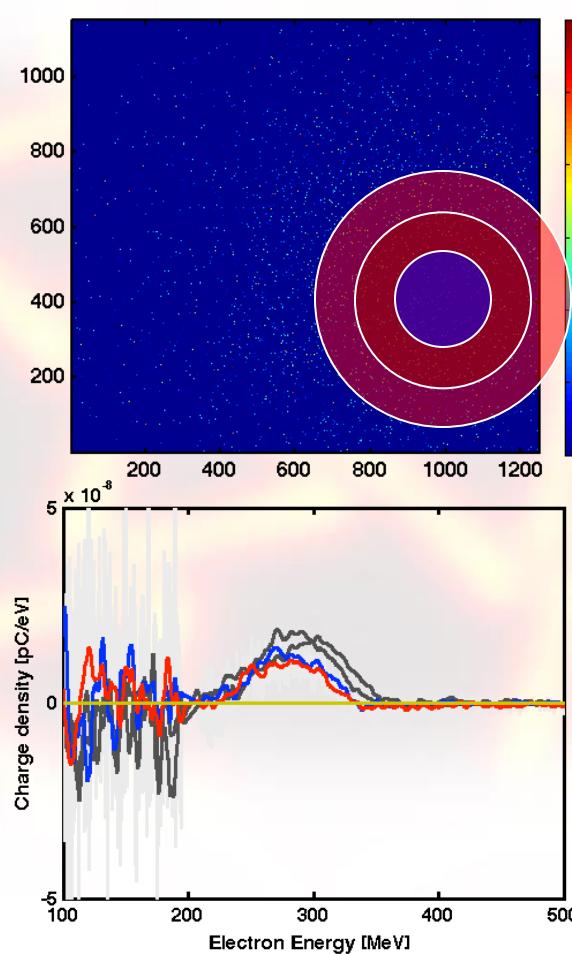


# Single Pixel Counting–Method with low charge bunches



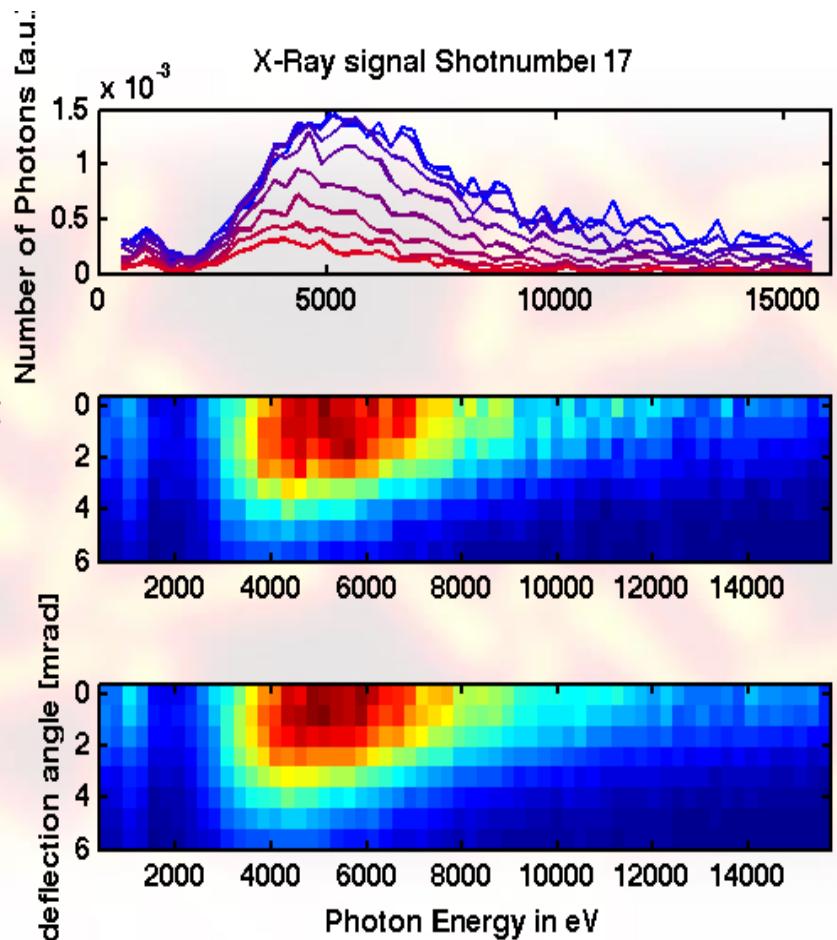


# Angular resolved Photon Energies



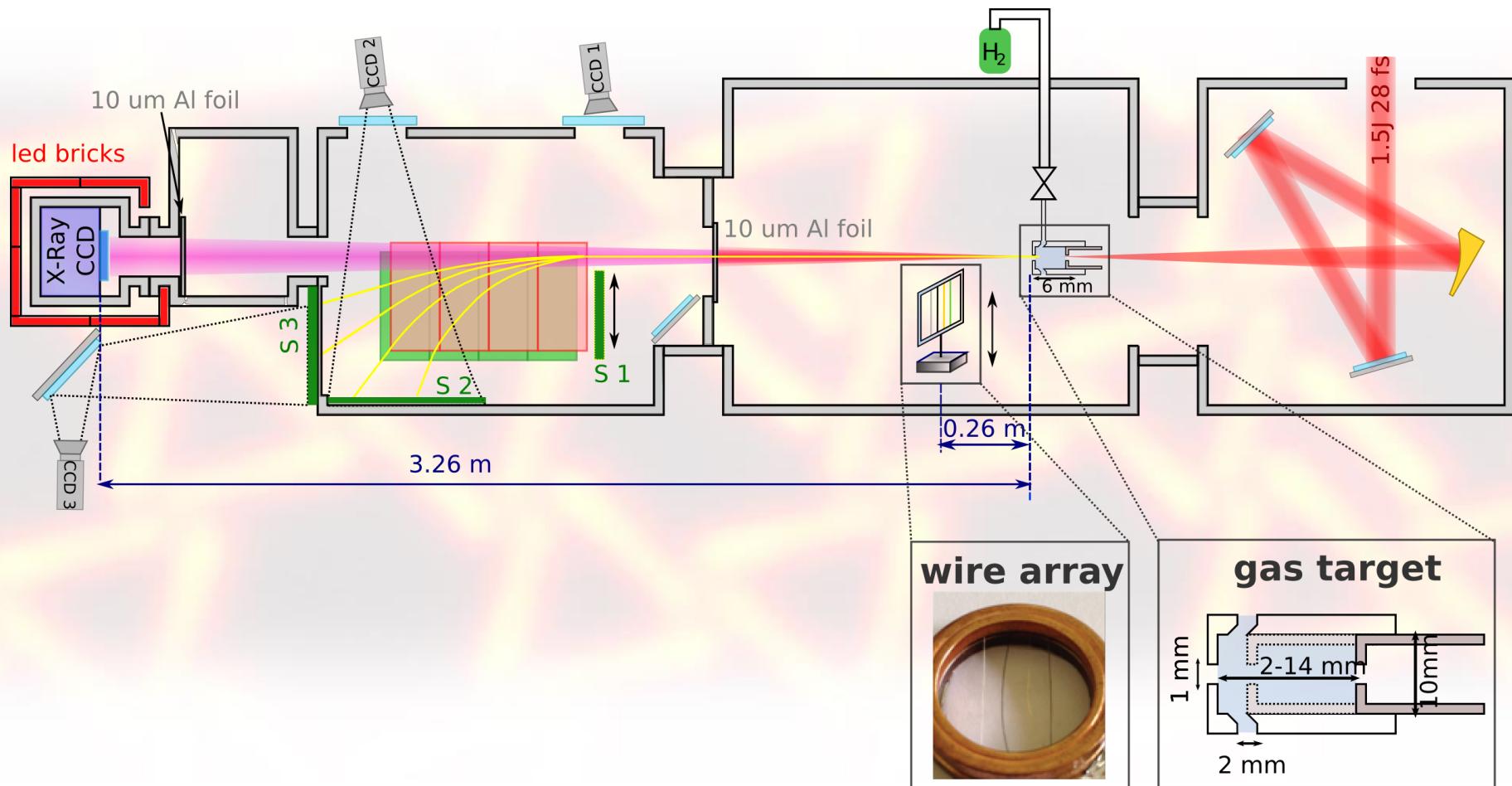
Single shot

Average



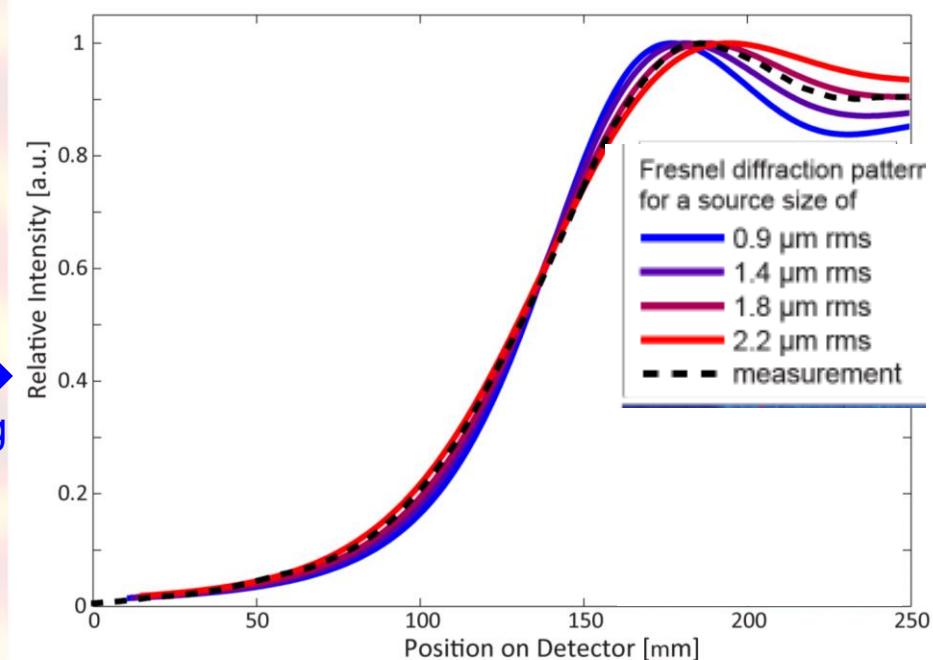
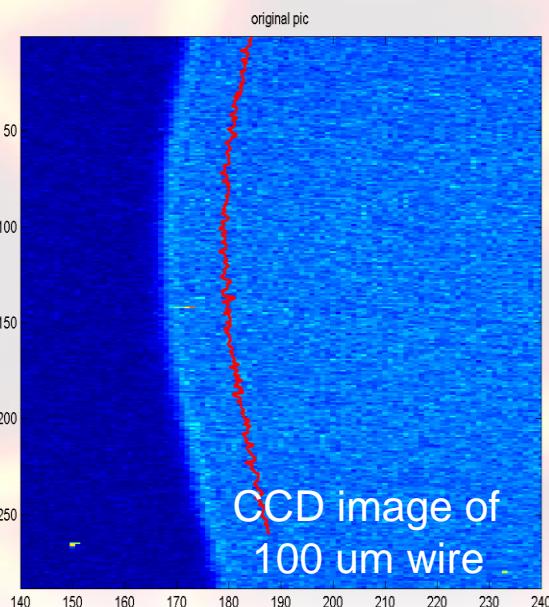


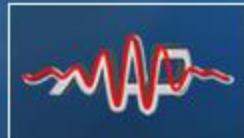
# Characterization of the Source Size



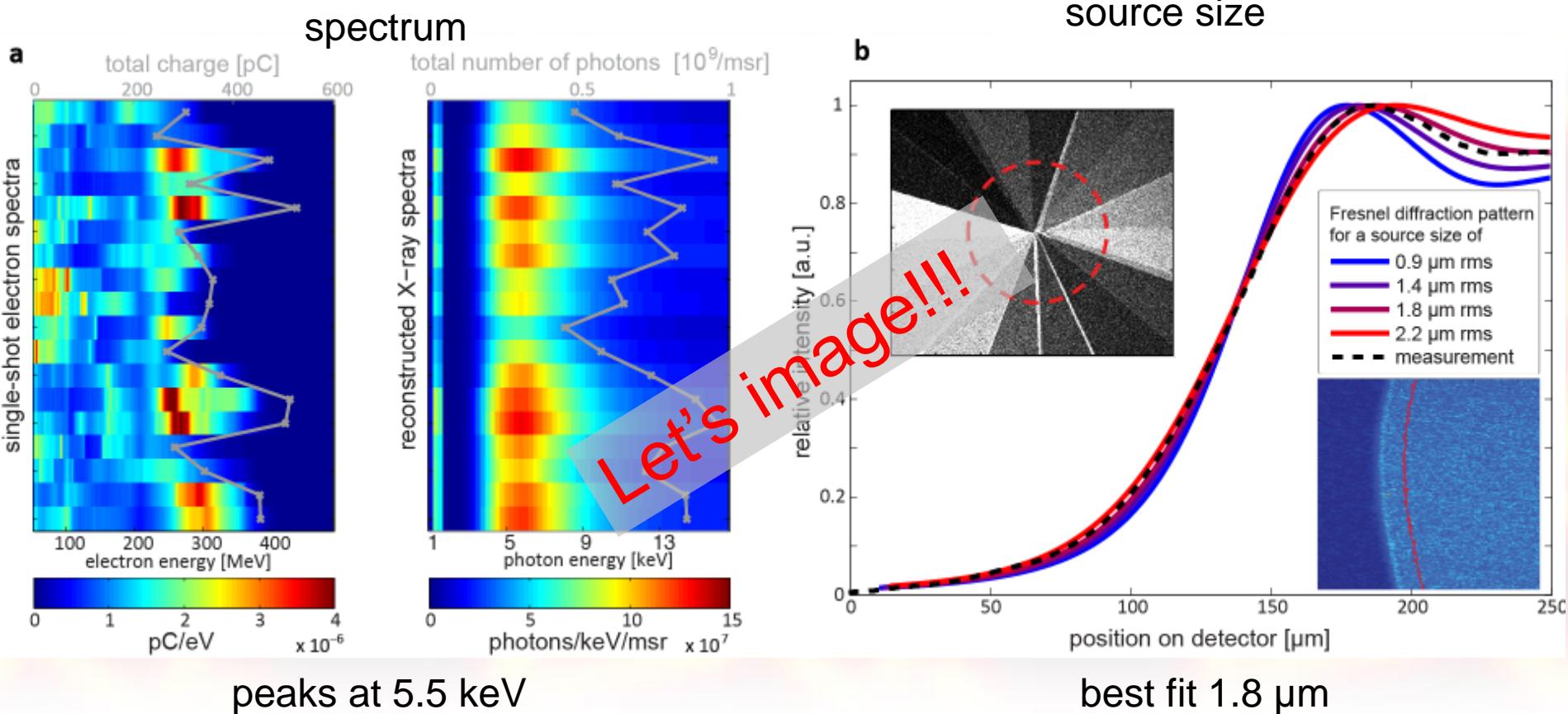


# Source size reconstruction





# Betatron radiation source characteristics



peak brilliance:  $2 \times 10^{22} \text{ ph s}^{-1} \text{ mm}^{-2} \text{ mrad}^{-2}/0.1\% \text{ BW}$  (assuming pulse length of 10 fs)

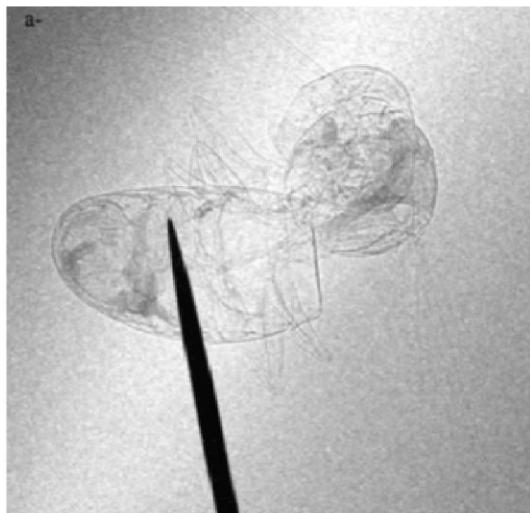


# Previous work

First X rays betatron !  
contrast images

S. Fourmaux *et al.*,!  
Opt. Lett. **36**, 13 (2011)

S. Kneip *et al.*, Appl. Phys. !  
Lett. **99**, 093701 (2011)



Courtesy of K. Krushelnick

V. Malka *et al.*, Nature Physics **4** (2008)!  
E. Esarey *et al.*, Rev. Mod. Phys. **81**, 1229 (2009)  
S. Corde *et al.*, Rev. of Modern Physics **85**, 1 (2013)



# Propagation-based Phase-Contrast Imaging

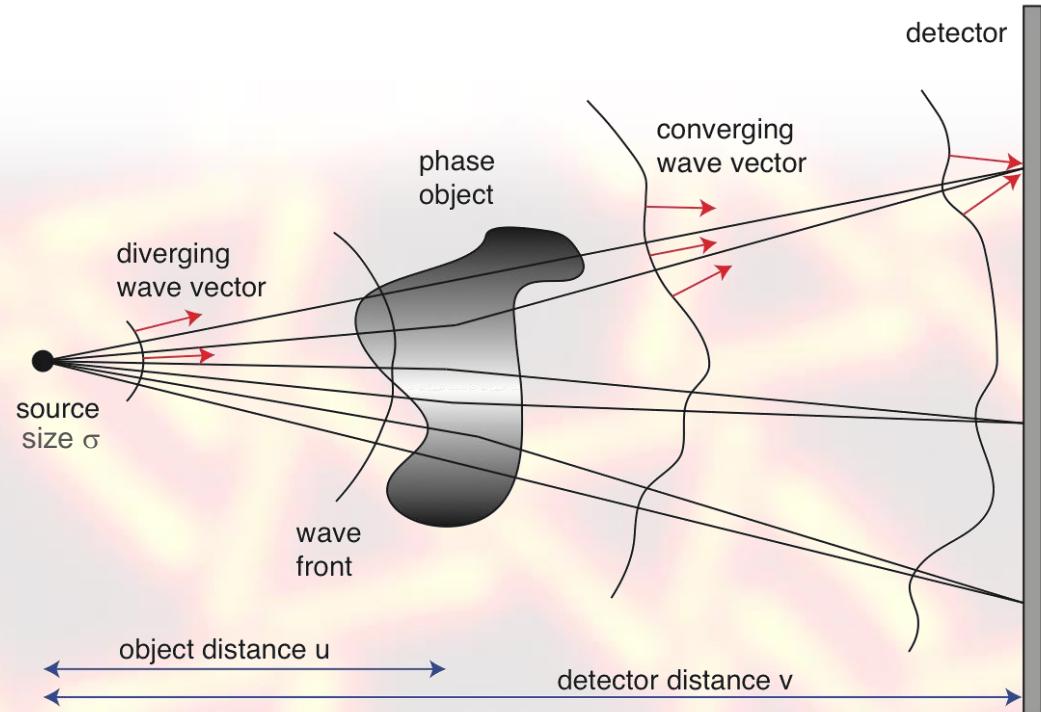
Requirements:

- sufficient degree of spatial coherence  
transverse coherence length  $l_t$

$$l_t = \lambda v / \sigma > \sqrt{\lambda D} / (2\sqrt{2}) \approx O(1-10 \mu\text{m})$$

$$D = d(v - u) / (d + u)$$

- a high resolution detector

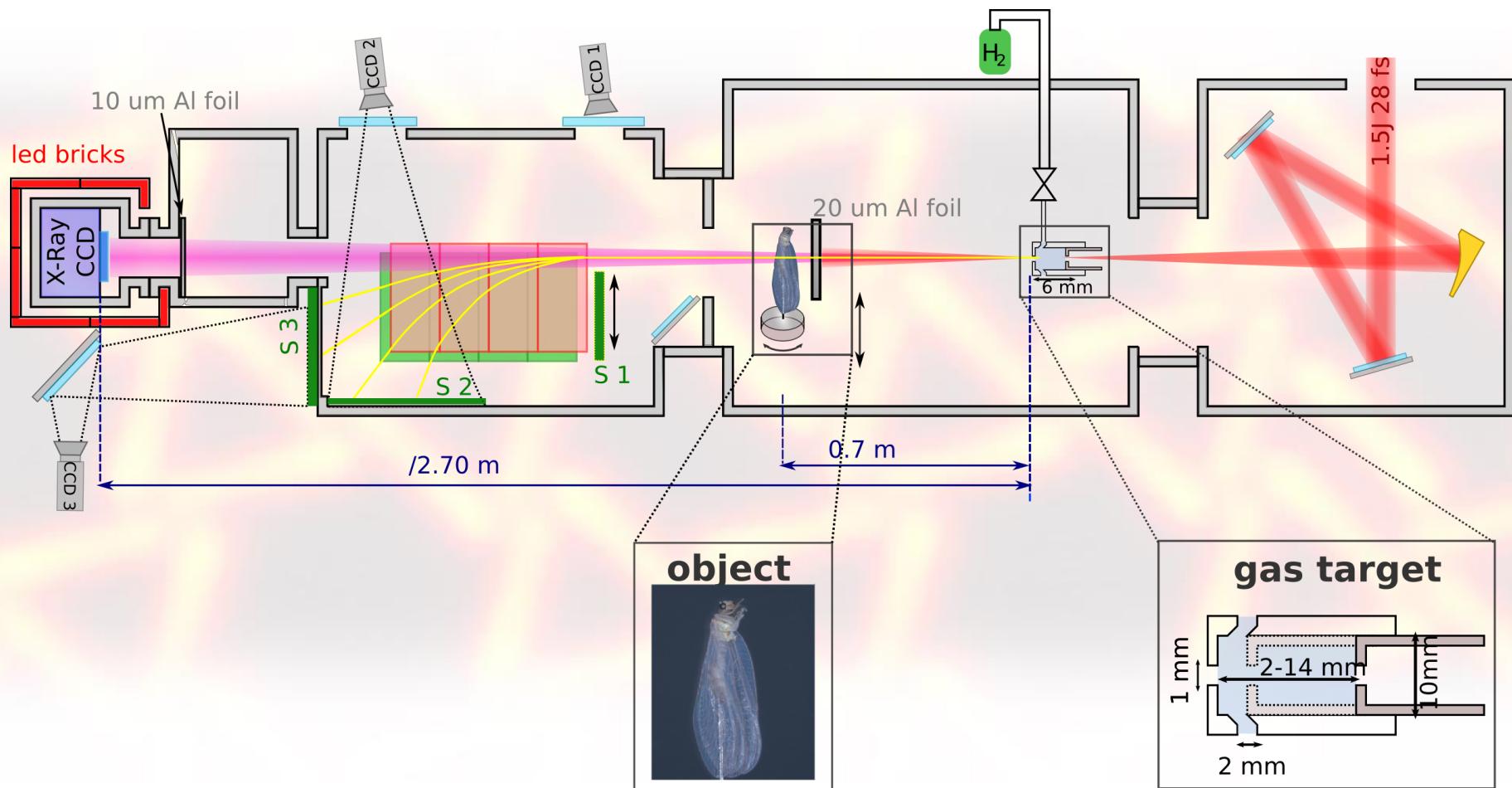


The intensity distribution on the detector is a result of wavefront distortions introduced by phase object. The Transport of Intensity Equation relates sample thickness to measured intensity distribution:

$$T(\vec{r}) = -\frac{1}{\mu_{poly}} \times \ln \left( IFT \left\{ \frac{\frac{FT(I(v/u \cdot \vec{r}))}{I_0}}{1 + \frac{(v-u)\delta_{poly}}{v/u \mu_{poly}} |\vec{k}|^2} \right\} \right)$$



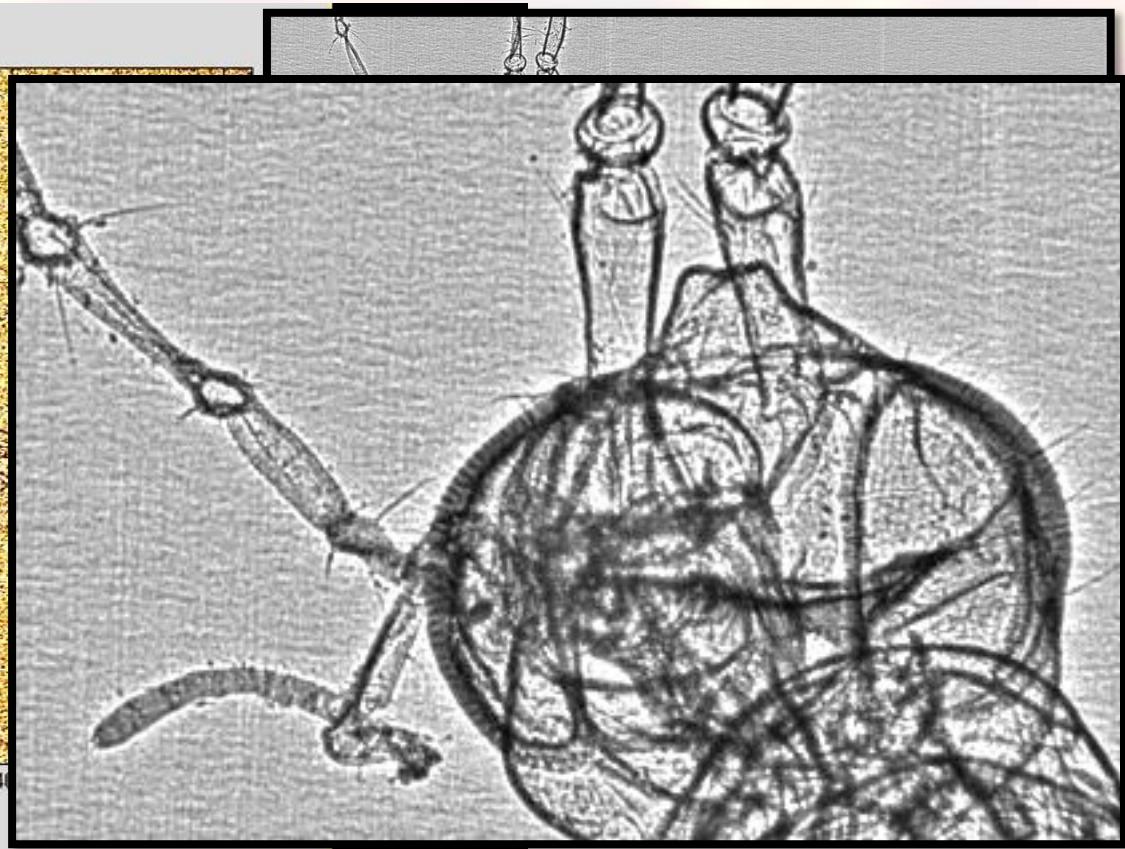
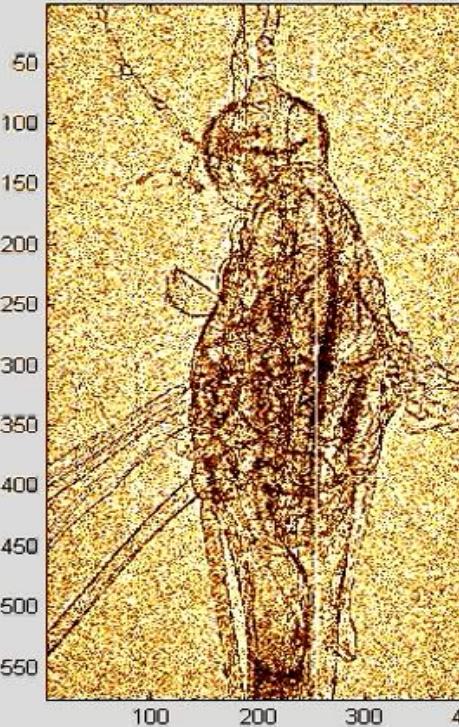
# Experimental Setup- Phase Contrast Imaging

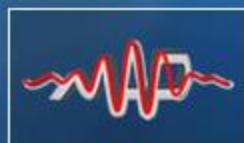




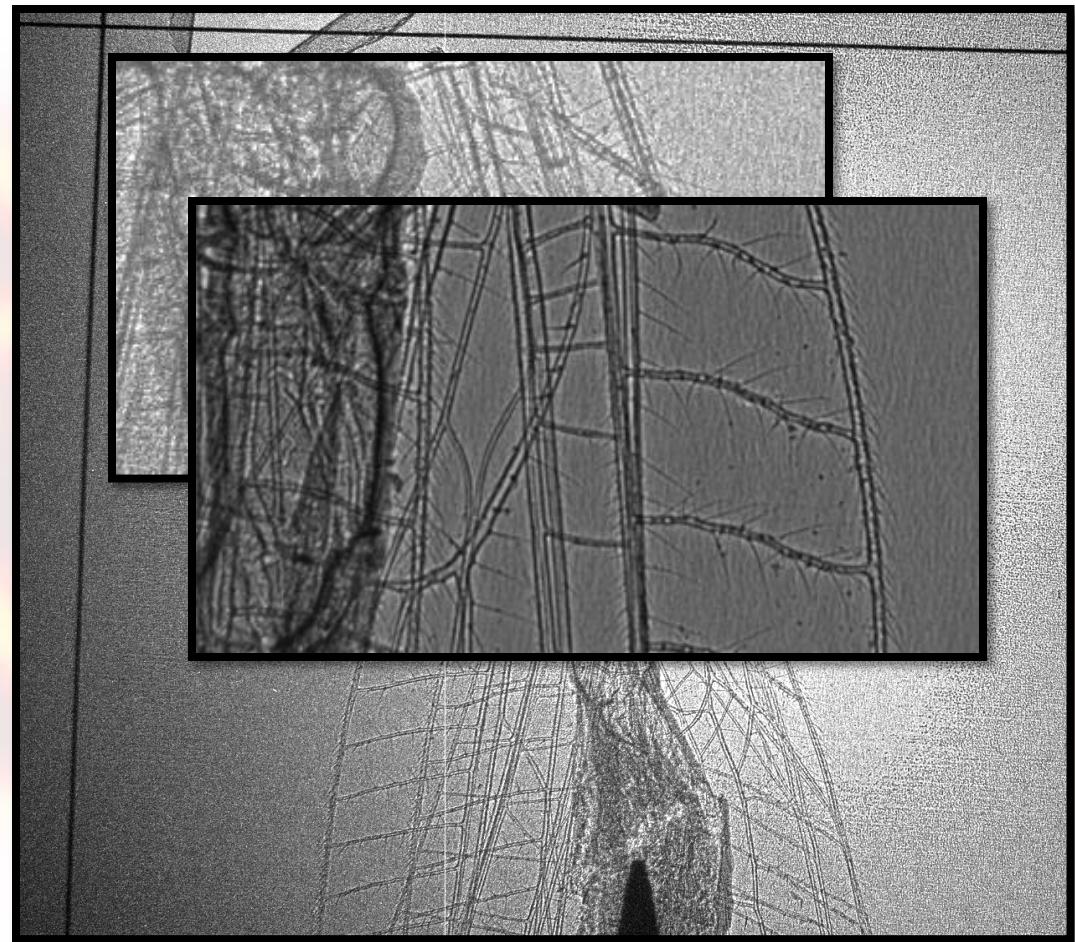
# Going beyond the resolution of your detector

Adding and sub-sampling the 100 shots:





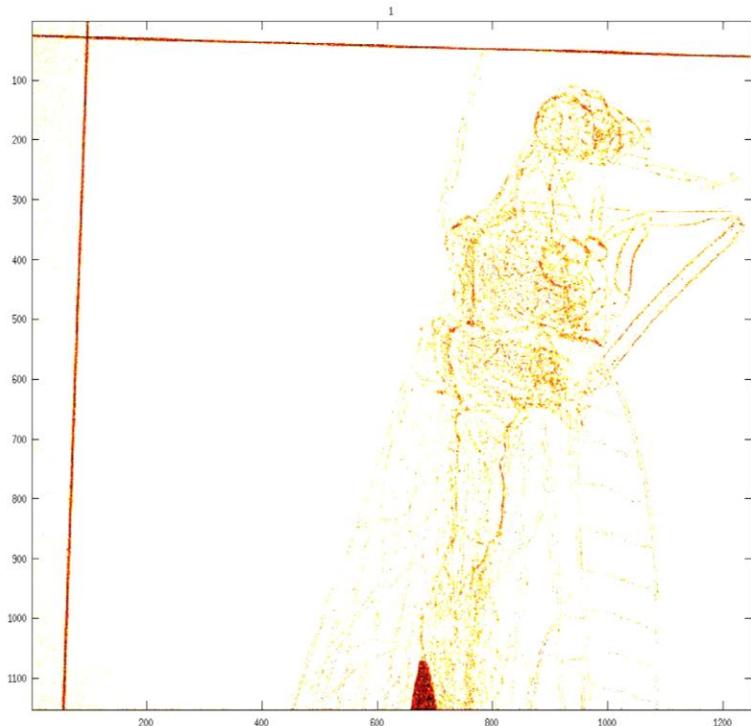
# Single shot imaging





# Phase contrast tomography of biological sample

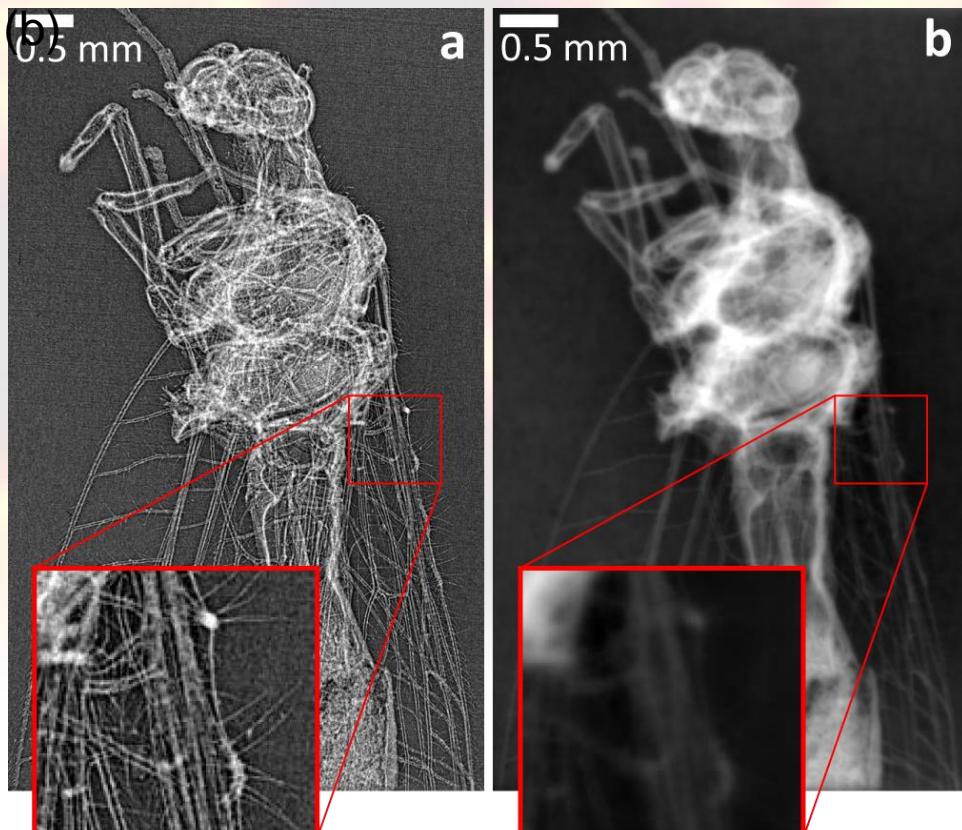
data analysis by the group of F. Pfeiffer



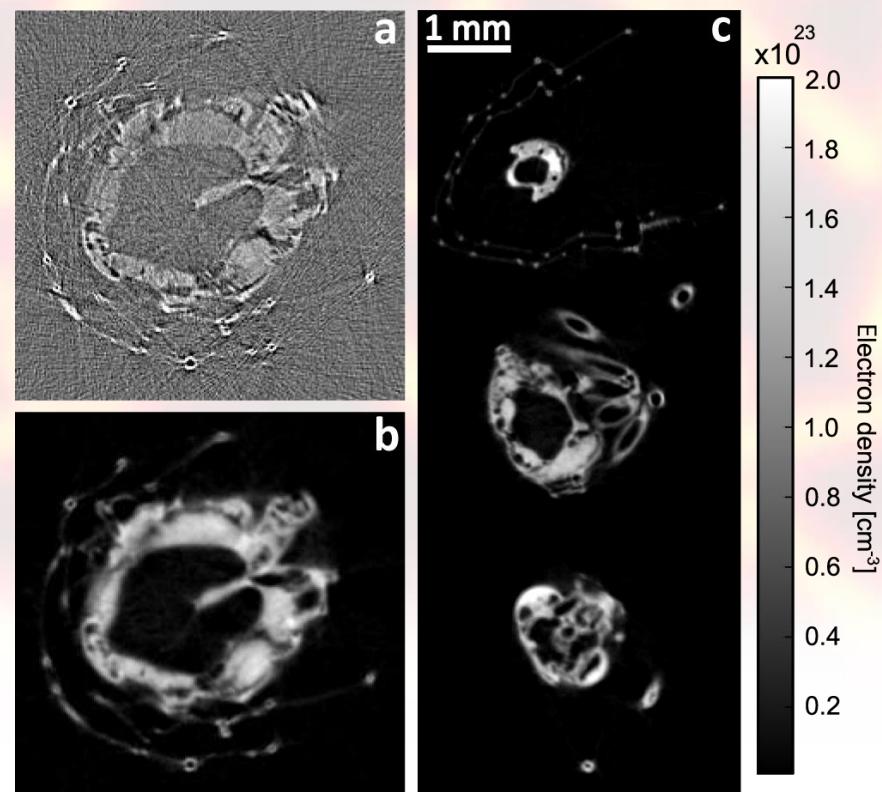


# Quantitative Phase Map and Reconstruction

The transport-of intensity-equation (TIE) relates the edge-enhanced image at the detector (a) to the phase map of the insect

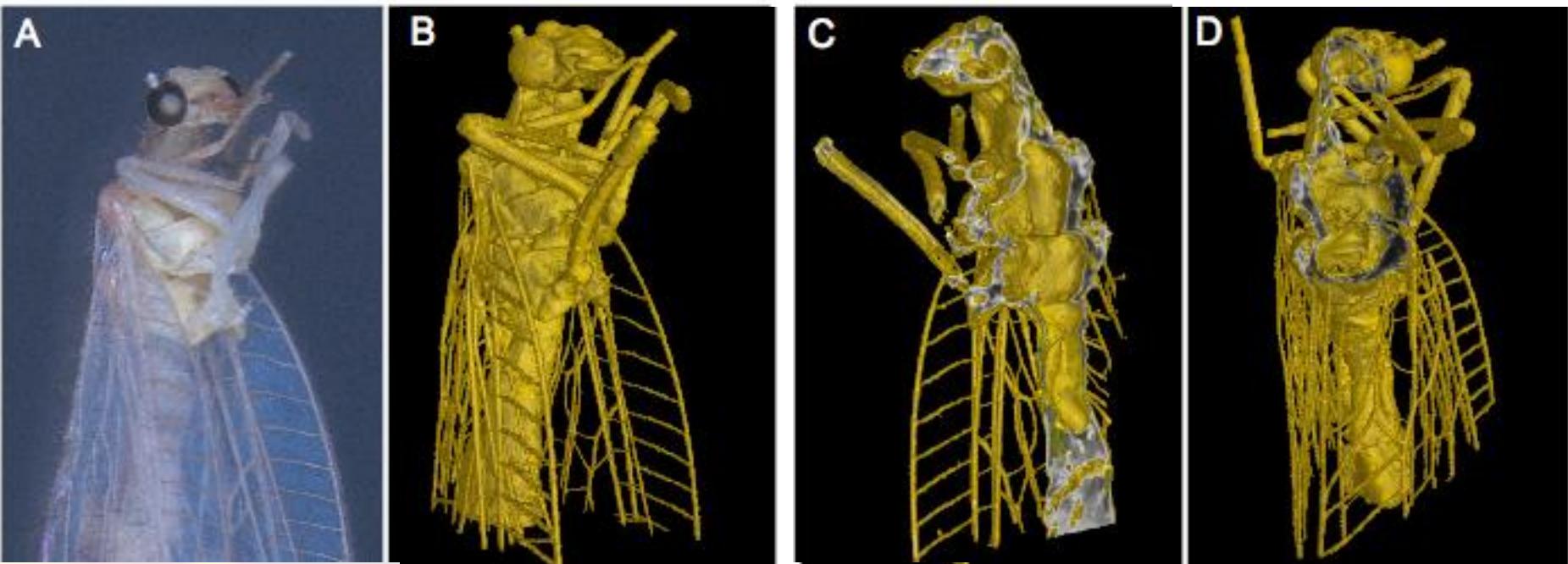


tomographic reconstruction of 2-D projections yields cuts through sample (edge enhancement (a) and phase images (b,c))





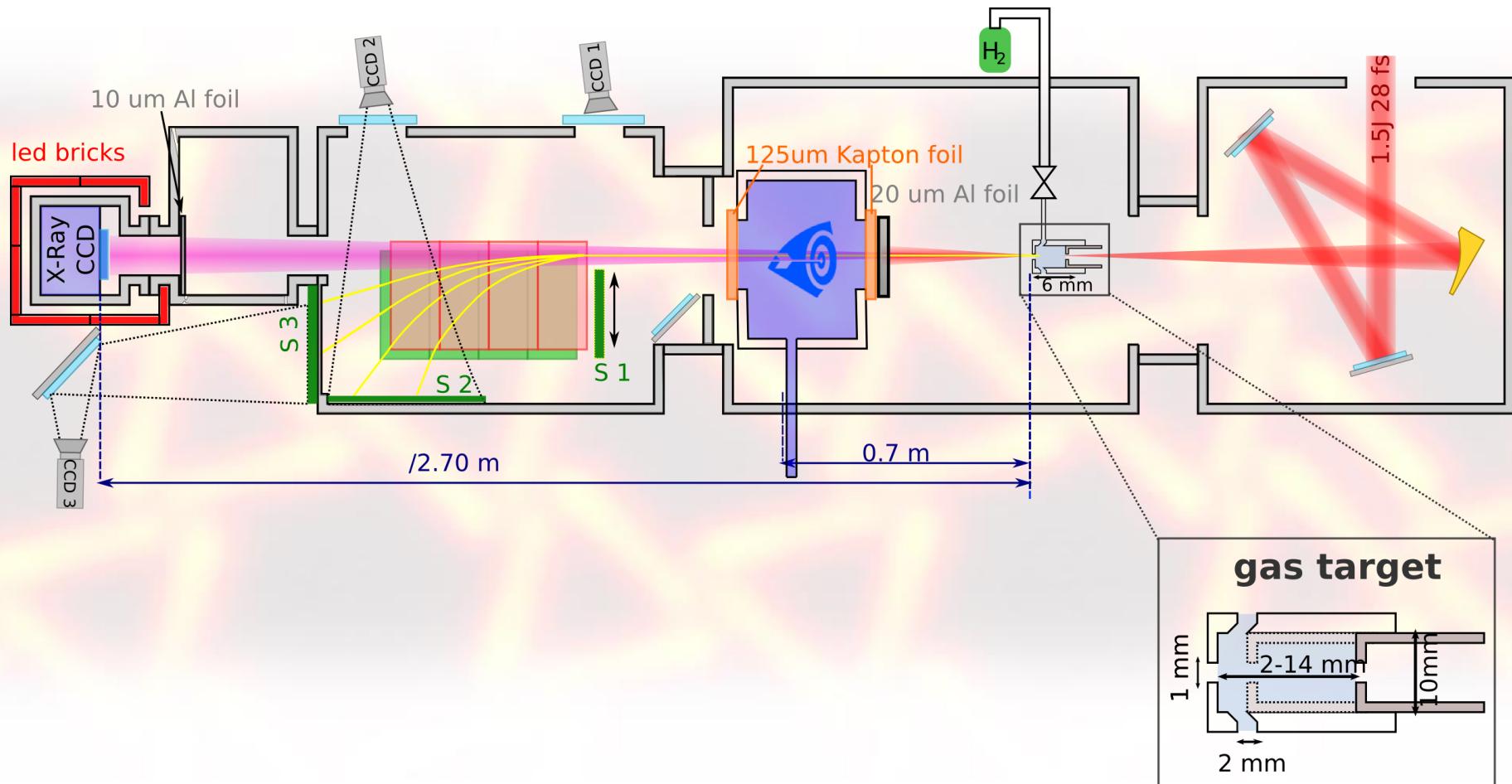
## 3D rendering of the fly



From background (void) of the reconstructed sample one can estimate a conservative limit for our measurement sensitivity of the electron density **sensitivity of  $0.1 \times 10^{23} \text{ cm}^{-3}$**



# Reentrance setup for water containing samples

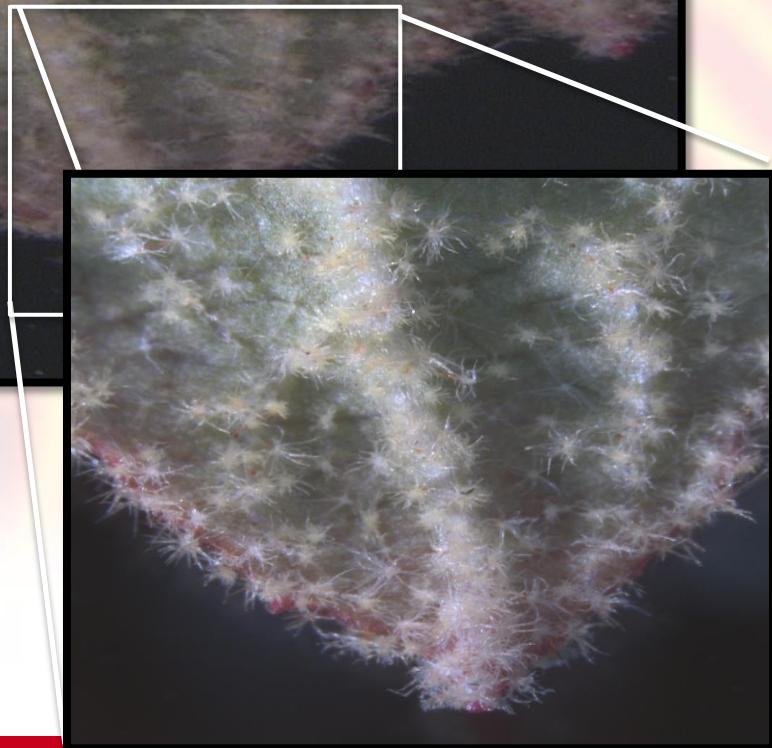




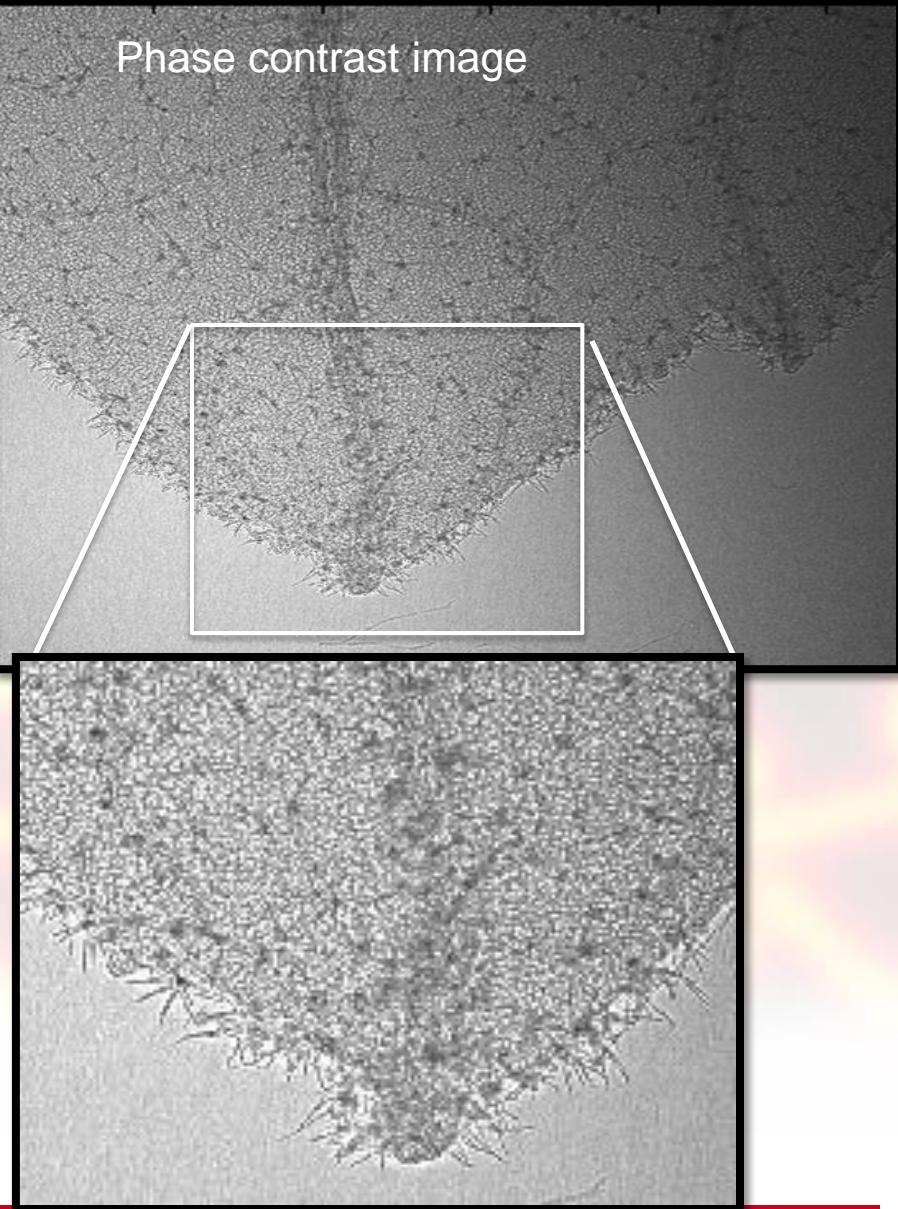
# Water containing samples

microscope image

1 mm

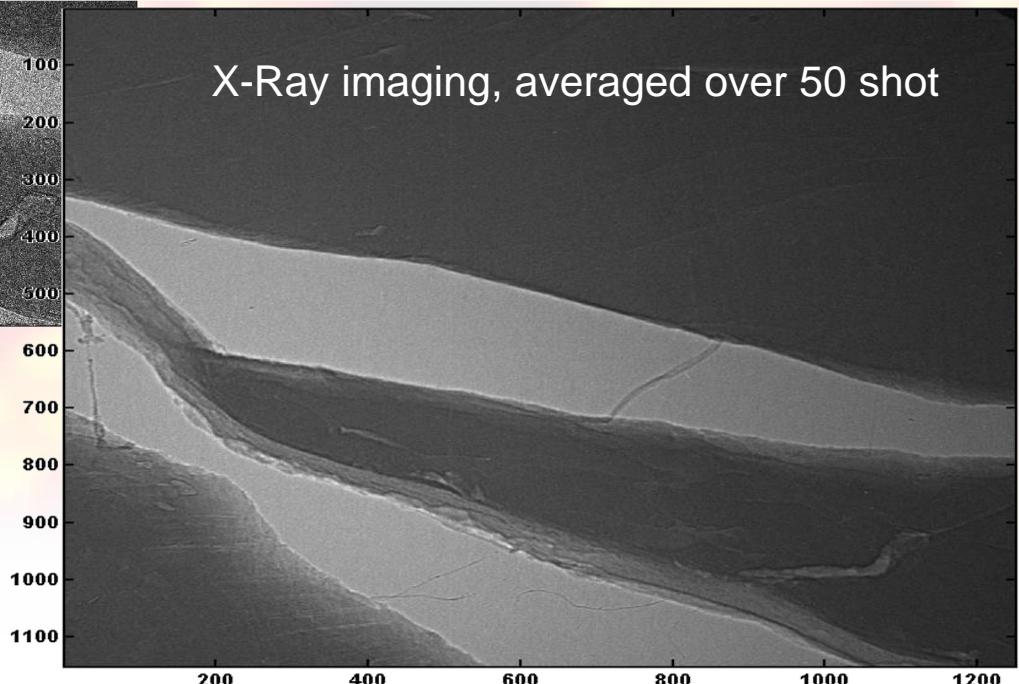
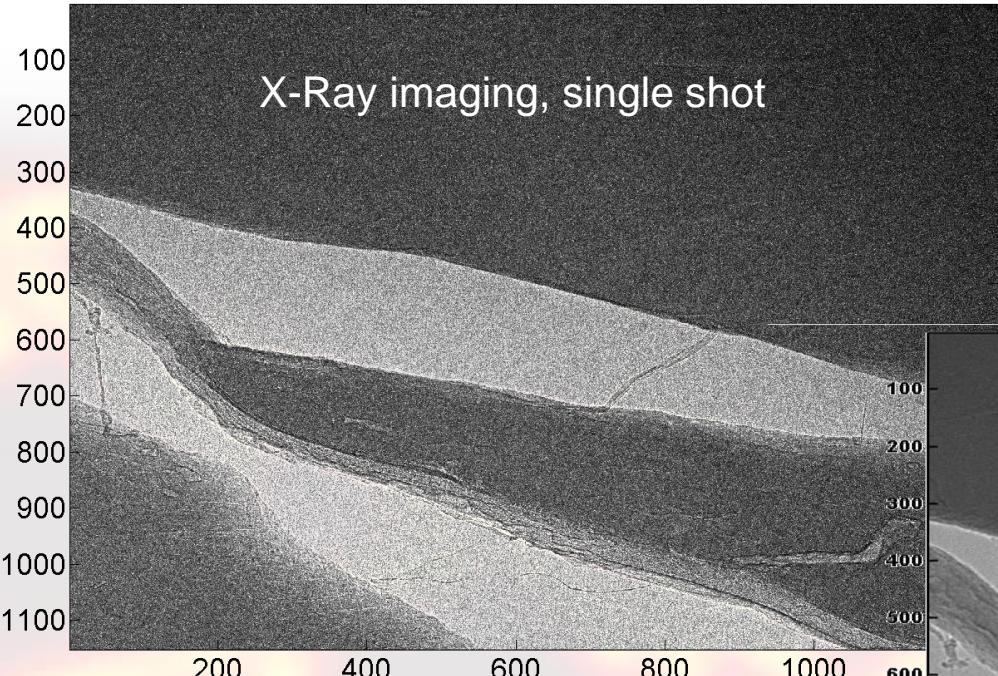


Phase contrast image





# Hamon iberico





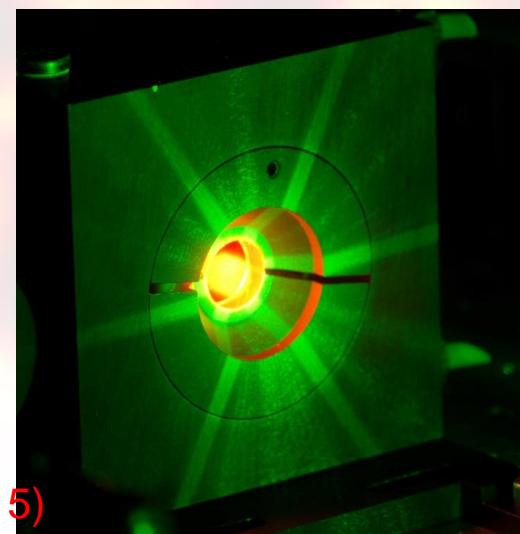
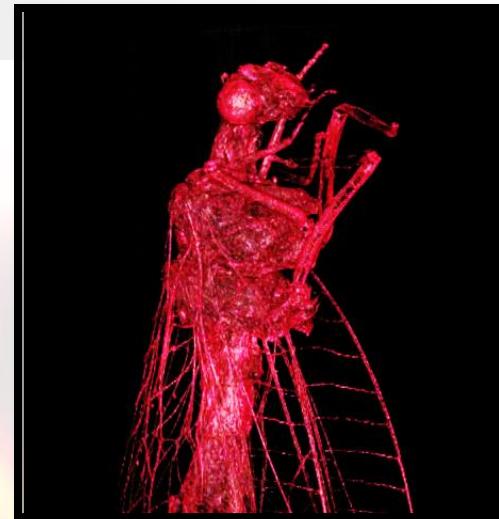
# Summary

LWFA electrons are able to provide highly brilliant X-Ray sources enabling phase contrast tomography

Intrinsic properties of LWFA Betatron source:

Compact, high spatial coherence, low spectral fluctuation  
well suited for multi-exposure scans, fs duration

Source and spectral characterization enables reconstruction  
of absolute electron densities  
complete tomography scan (1500 laser shots)



## Thank you very much for your attention!!!

J. Wenz et al., Nature Comm. DOI:10.1038/ncomms8568 (2015)