

Cosmological constraints on neutrino masses

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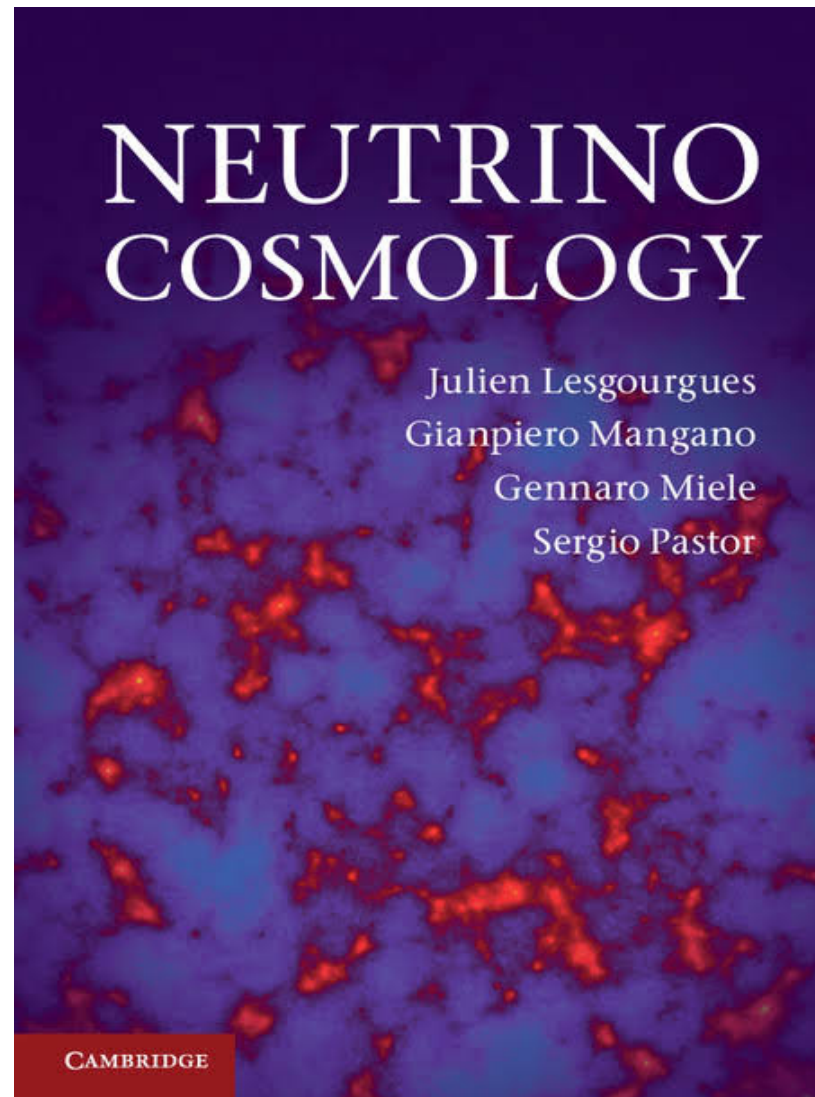
Plan of Talk

- Neutrinos in cosmology
- Planck 2015 results
- Tensions in the standard model
 - combining with large scale structure probes
- Future probes

Plan of Talk

- Neutrinos in cosmology
- Planck 2015 results
 - safe limit from CMB alone
- Tensions in the standard model
 - combining with large scale structure probes
 - complicated story
- Future probes
 - very bright future

Neutrino Cosmology : a good reference



Standard Cosmological Model

GEOMETRY & GRAVITY

$$ds^2 = dt^2 - a^2(dr^2 + r^2 d\Omega^2)$$

$$\left(\frac{\dot{a}}{a}\right)^2 = H^2 = \frac{8\pi G}{3}\rho$$

$$\dot{\rho} = -3H(\rho + P)$$

INITIAL PERTURBATIONS

$$P_i(k) = A_S \left(\frac{k}{k_p}\right)^{n_S}$$

ASSUMED SCALAR
CURVATURE PERTS

MATTER CONTENT

$$\rho = \rho_r + \rho_b + \rho_c + \rho_d$$

$$P = \frac{1}{3}\rho_r - \rho_d$$

RAD → ρ_r
 COSMOLOGICAL CONSTANT → ρ_d
 BARYONS → ρ_b
 COLD DM → ρ_c

7 PARAMETERS

H_0 HUBBLE'S CONSTANT

ρ_r, ρ_b, ρ_c MATTER DENSITIES
TODAY

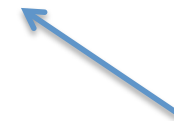
A_S, n_S INITIAL
PERTURBATIONS

τ OPTICAL DEPTH

Power spectrum norm : σ_8

- R.M.S. density contrast in $R=8h^{-1}\text{Mpc}$

$$\sigma_R^2 = 4\pi \int \frac{dk}{k} k^3 P(k) [W(kR)]^2$$



Filter function for a
sphere of radius R

- Value ~ 1 – in fact approx 0.8
- Related to A_s
 - plus other cosmological parameters relating large and small scales

Active neutrinos : textbook stuff

- Decoupling

$$T_{\text{dec}} \approx 1 \text{ MeV}$$

- Fermi-Dirac Temperature

$$T_\nu = \left(\frac{4}{11}\right)^{1/3} T_{\text{CMB}} = 1.945 \text{ K} = 1.676 \times 10^{-4} \text{ eV}/k_{\text{B}}$$

- Number Density for each flavour

$$n_\nu = n_{\bar{\nu}} \approx 56 \text{ cm}^{-3}$$

- Contribution to the energy density budget

$$\Omega_\nu h^2 = \frac{\sum m_\nu}{94.1 \text{ eV}}$$

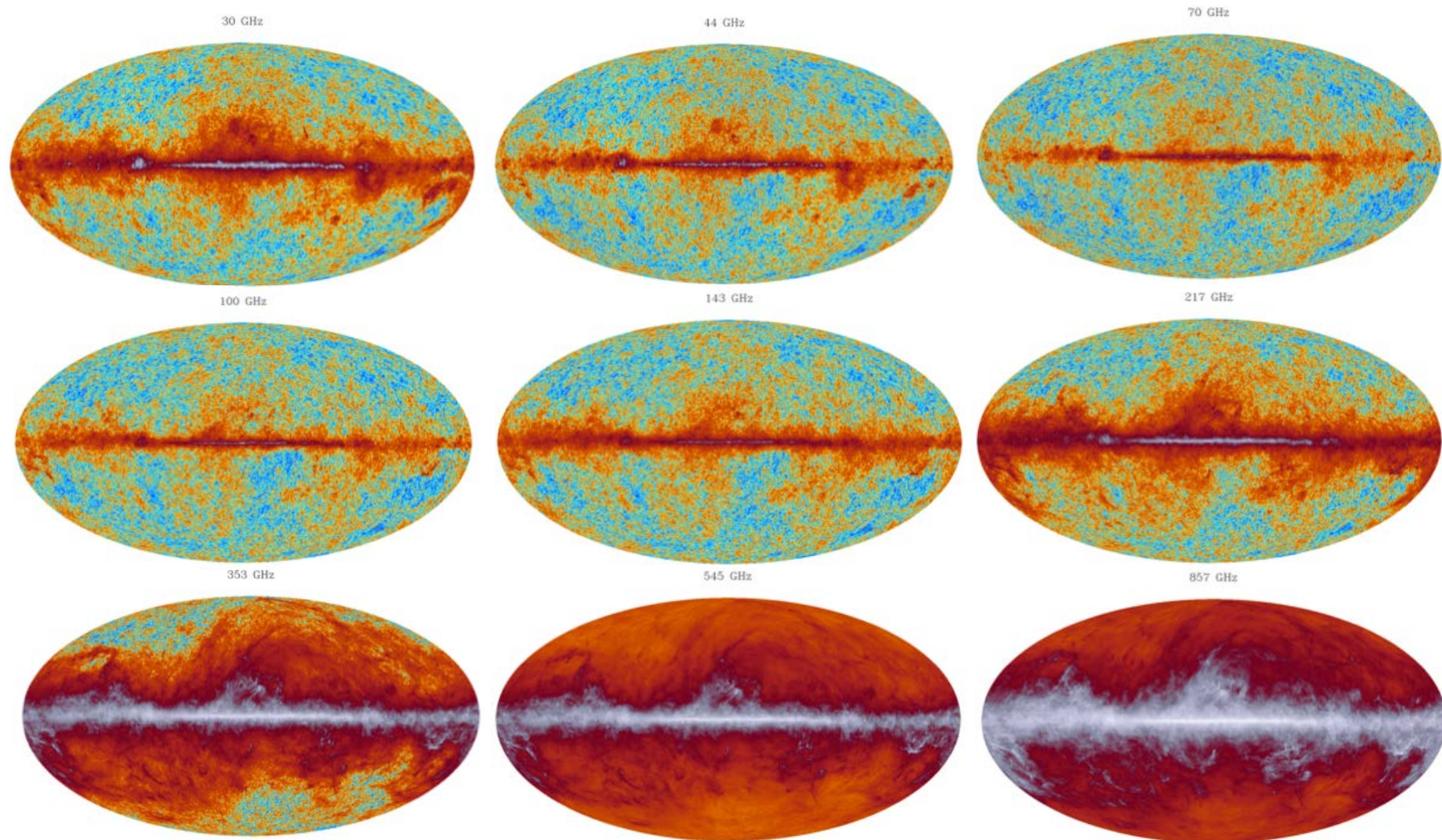
Impact on cosmological observables

- One parameter : $\sum m_\nu$ Sensitivity to individual masses is limited
- Contribution to the energy density
 - Changes the time of equal-matter radiation
- Evolution of perturbations
 - Neutrinos are “hot” and therefore free stream
 - They do not fall into potential wells until they become non-relativistic

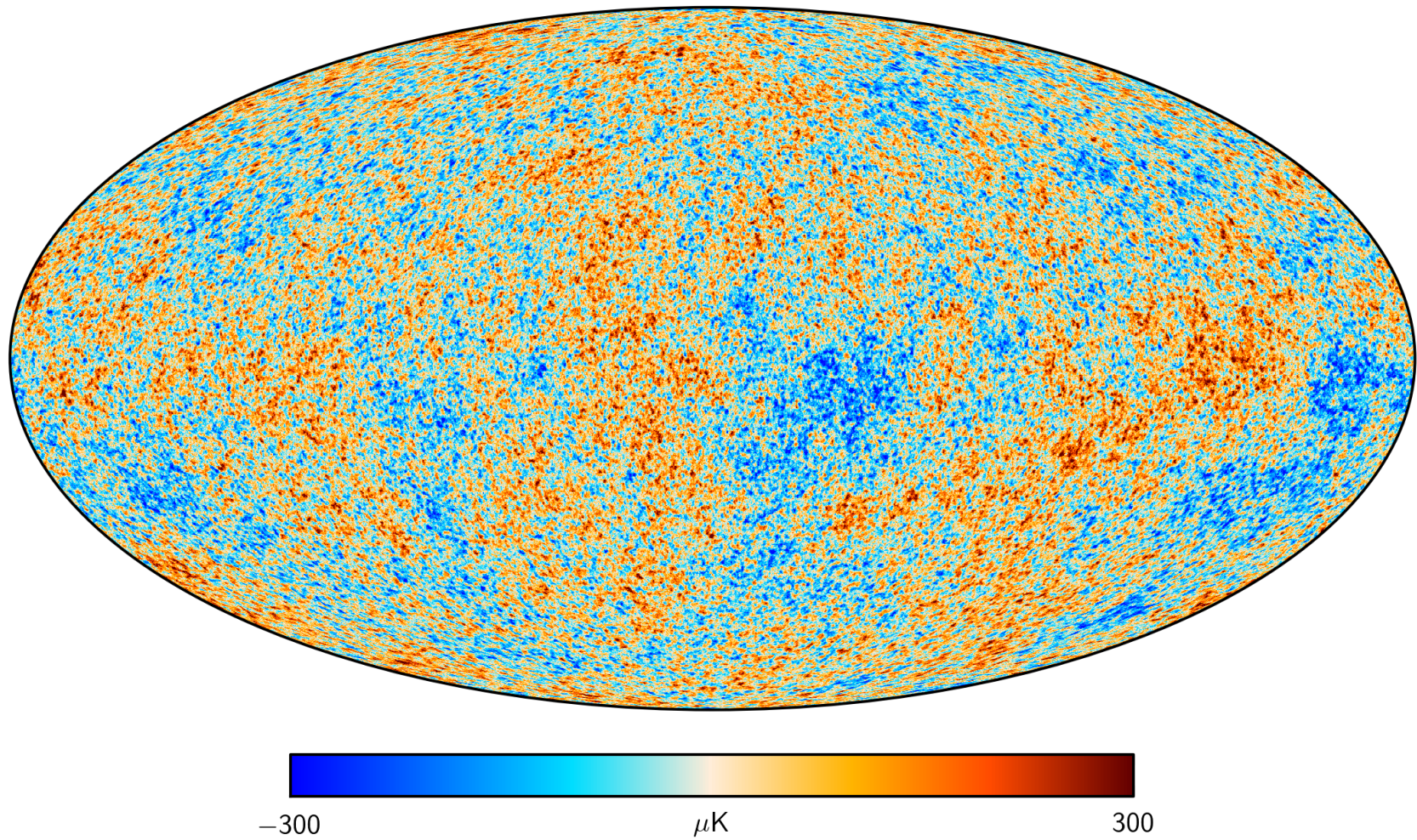
Sterile Neutrinos

- Effects governed by two parameters
 - N_{eff} and m_ν
- $N_{\text{eff}} > 3$ - effective number of neutrinos
 - not necessarily an integer: partial thermalization
 - governs contribution to energy density
- M_ν
 - impacts perturbations via rel v non-rel
- Specific models link the two parameters

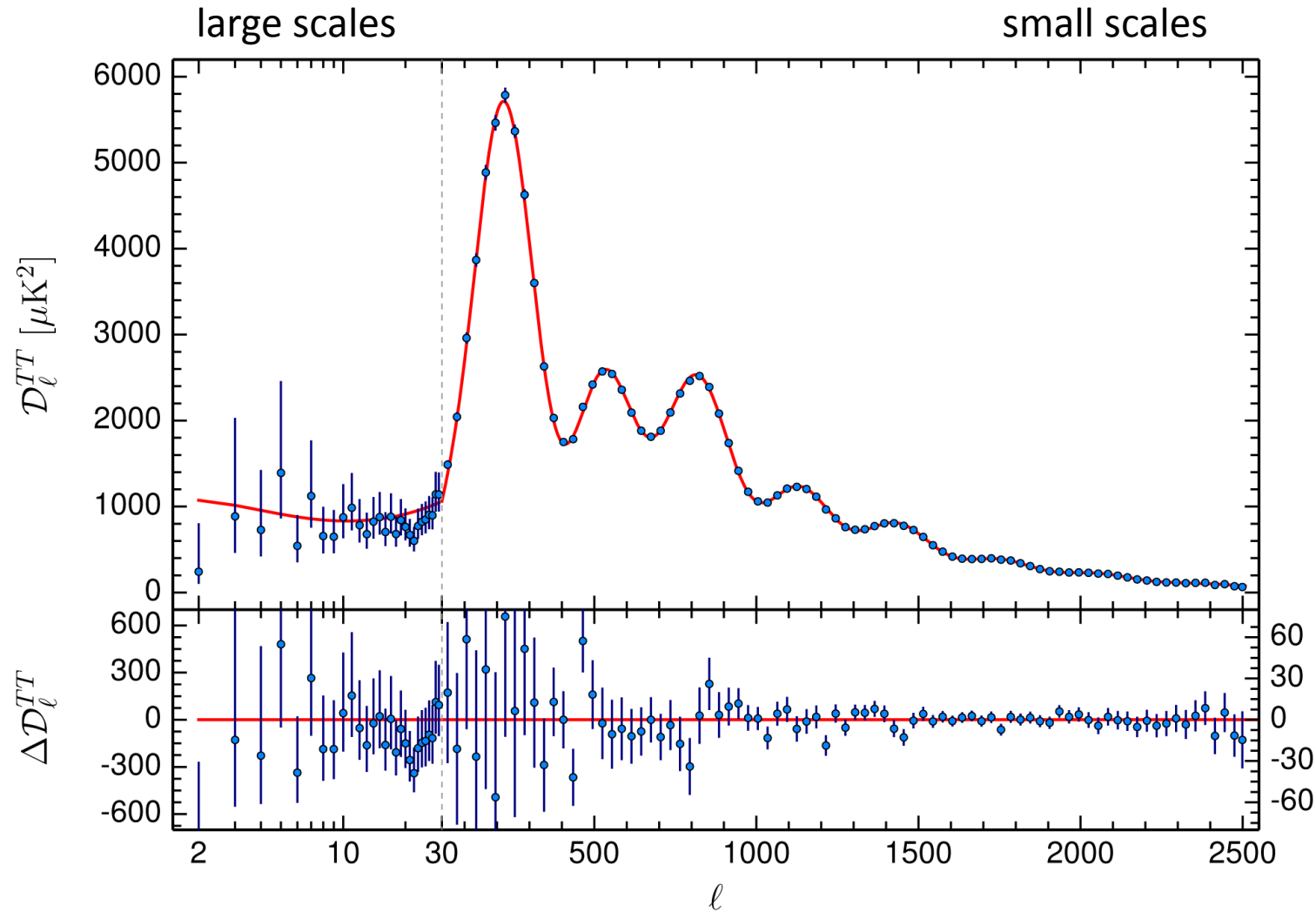
Observables : CMB



Observables : CMB



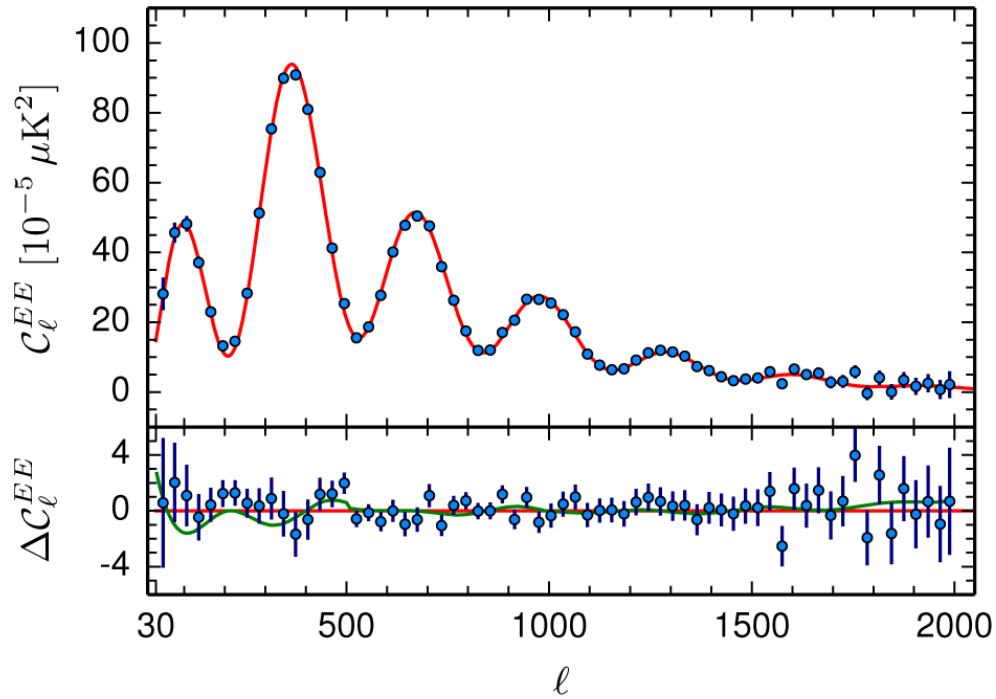
Observables : CMB



Temperature power spectrum

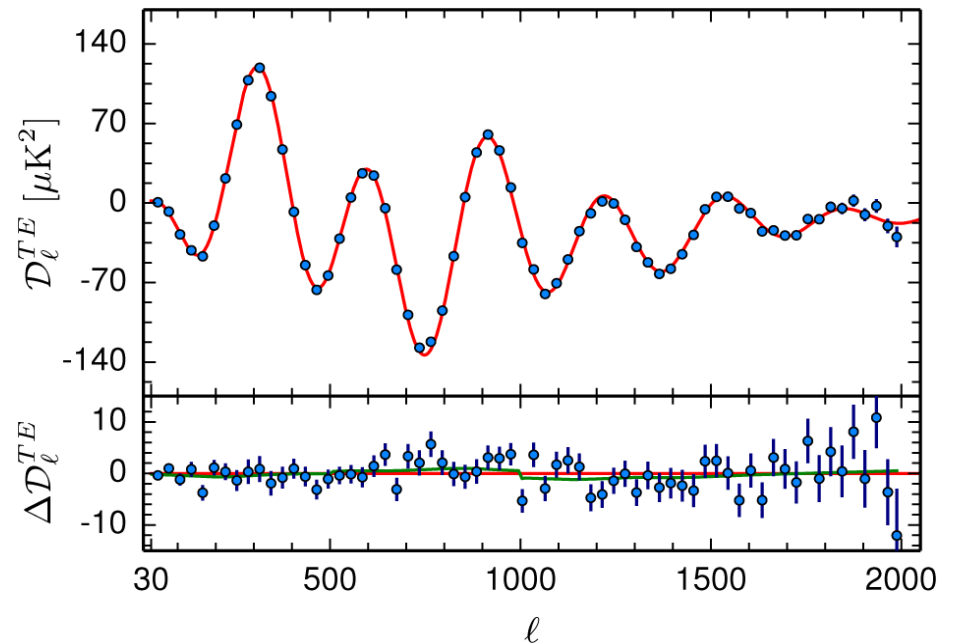
– where the most reliable constraints come from

Observables : CMB

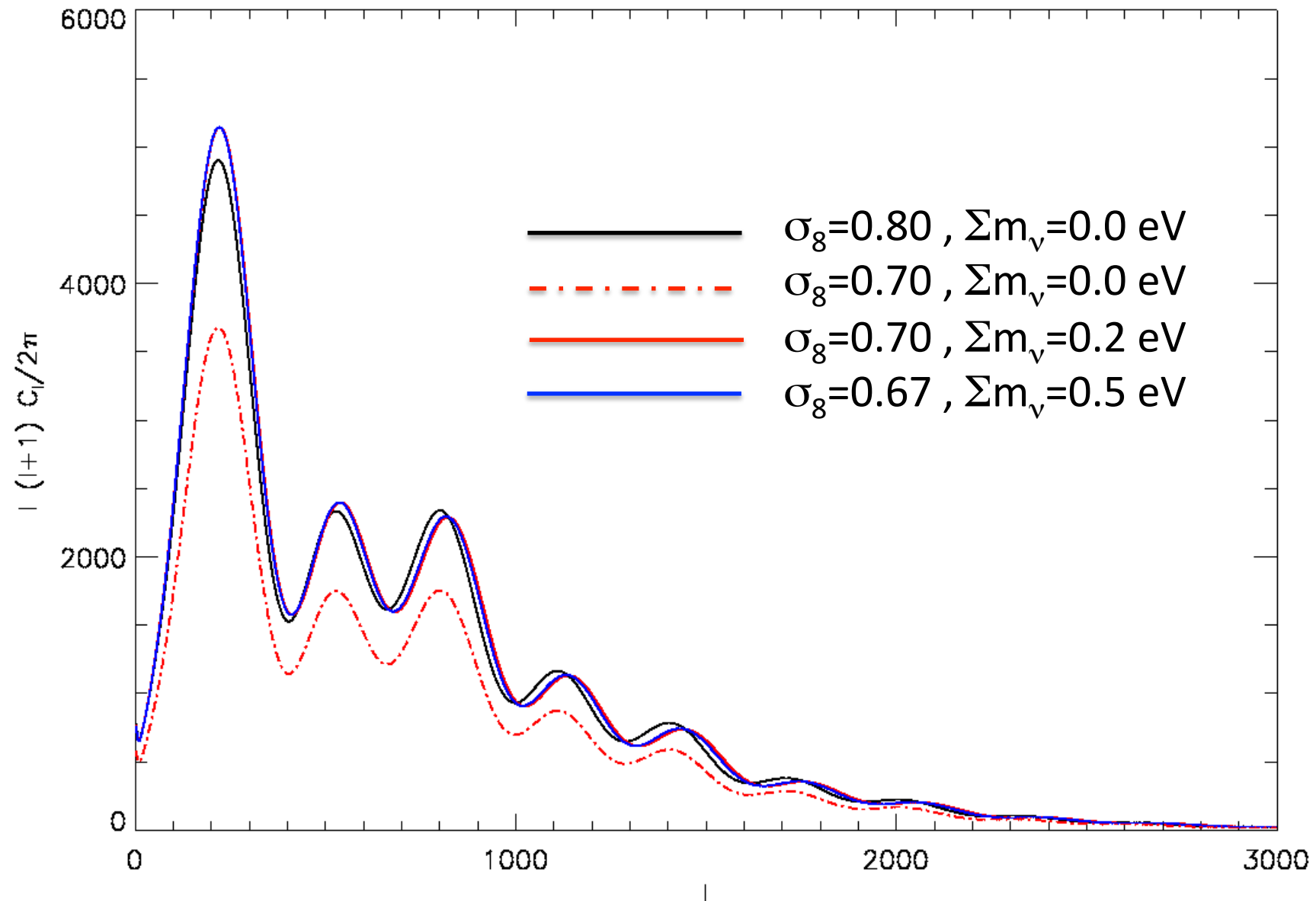


E-mode polarization
power spectrum

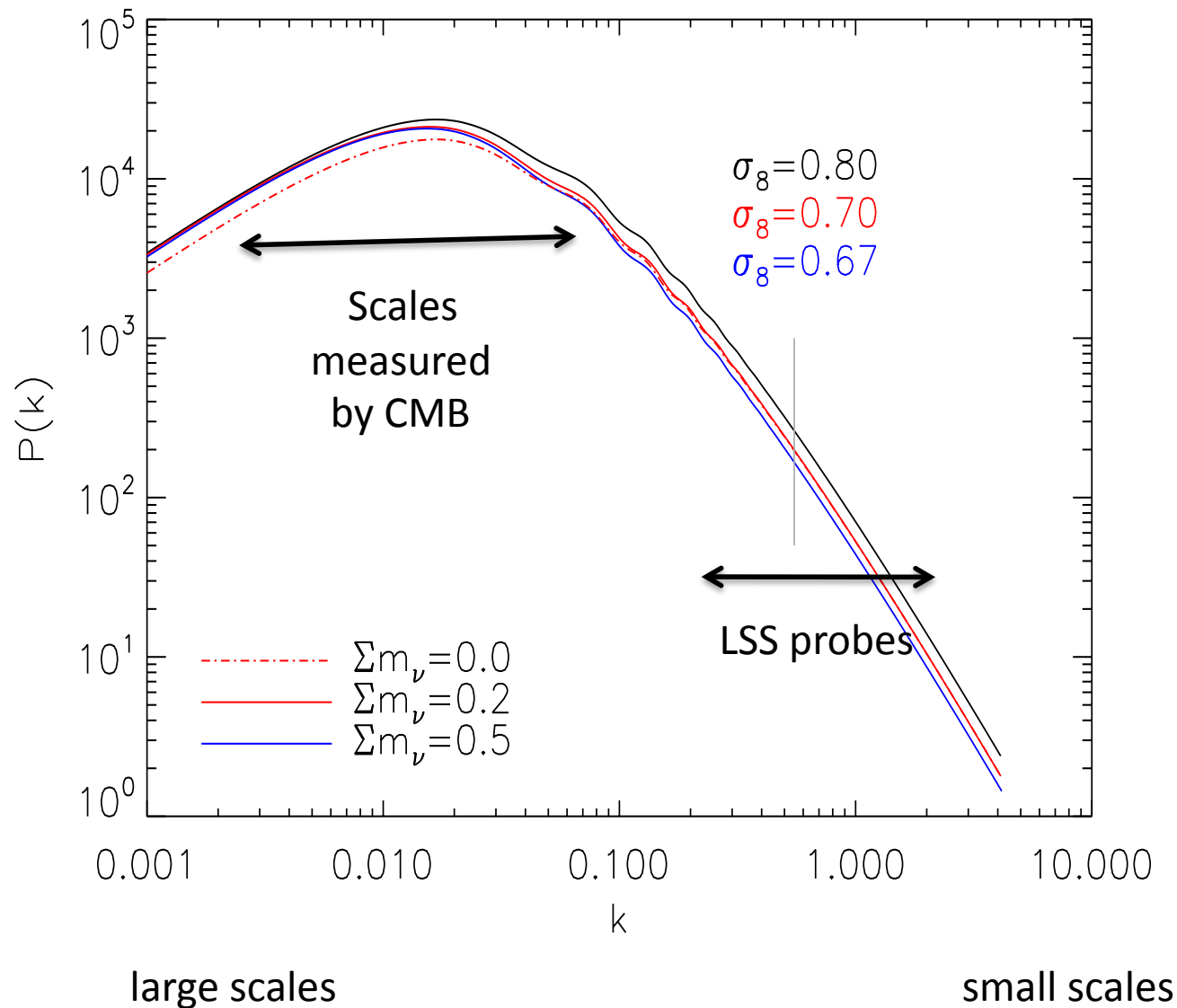
Temperature-polarization
cross power spectrum



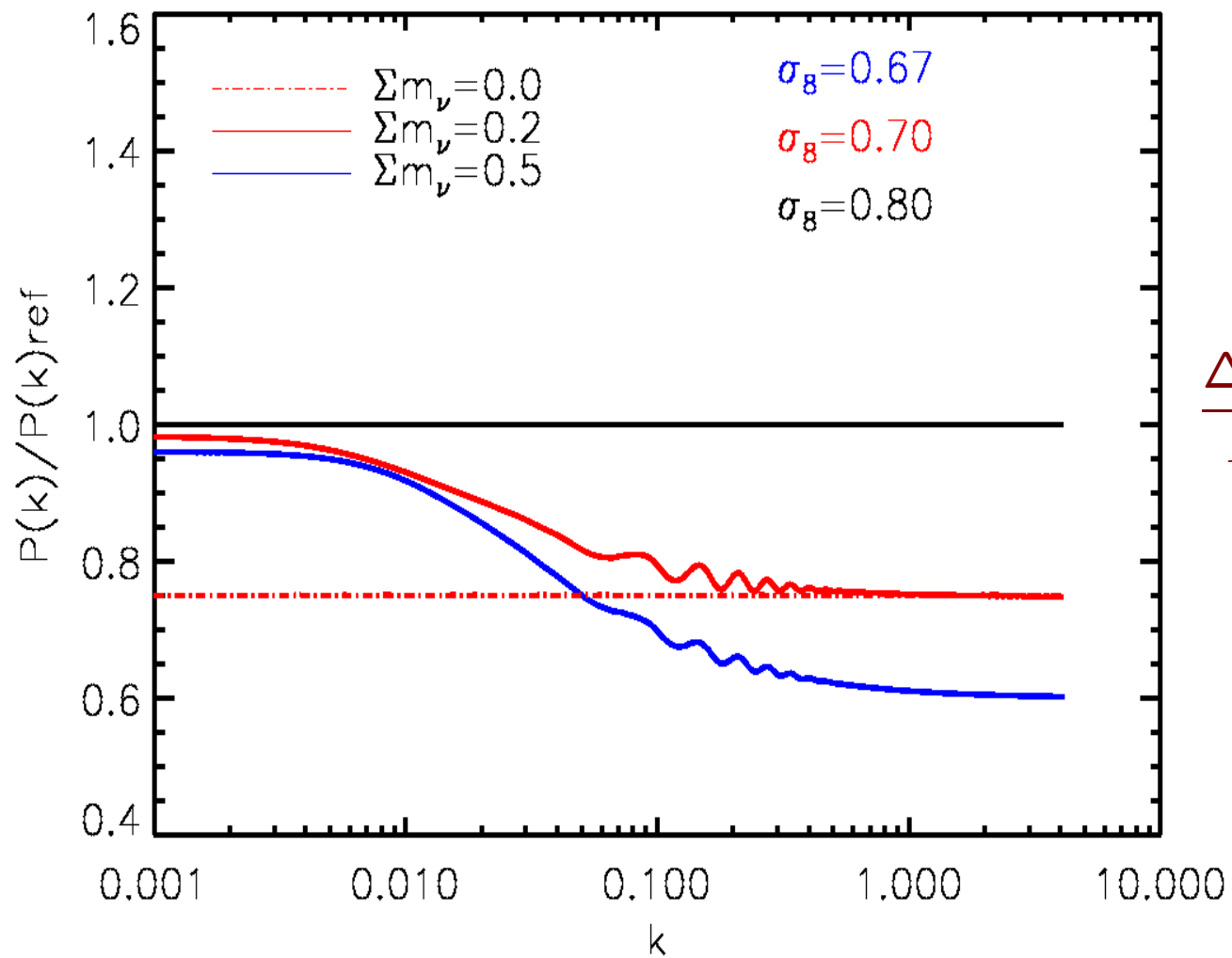
Sensitivity of CMB to neutrinos



Observables : matter power spectrum



Impact of massive neutrinos



$$\frac{\Delta P}{P} \approx -8 \frac{\Omega_\nu}{\Omega_m} \text{ for } k > k_{\text{FS}}$$

Probing the matter power spectrum

- Galaxy redshift surveys
- Lensing effects
 - CMB temperature anisotropies lensing
 - Cosmic shear (weak lensing of galaxy shapes)
 - CMB polarization lensing
- Cluster counts
 - Using the SZ effect, X-ray or optical
- Redshift space distortions
- ...

Probing the matter power spectrum

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Large scale structure probes

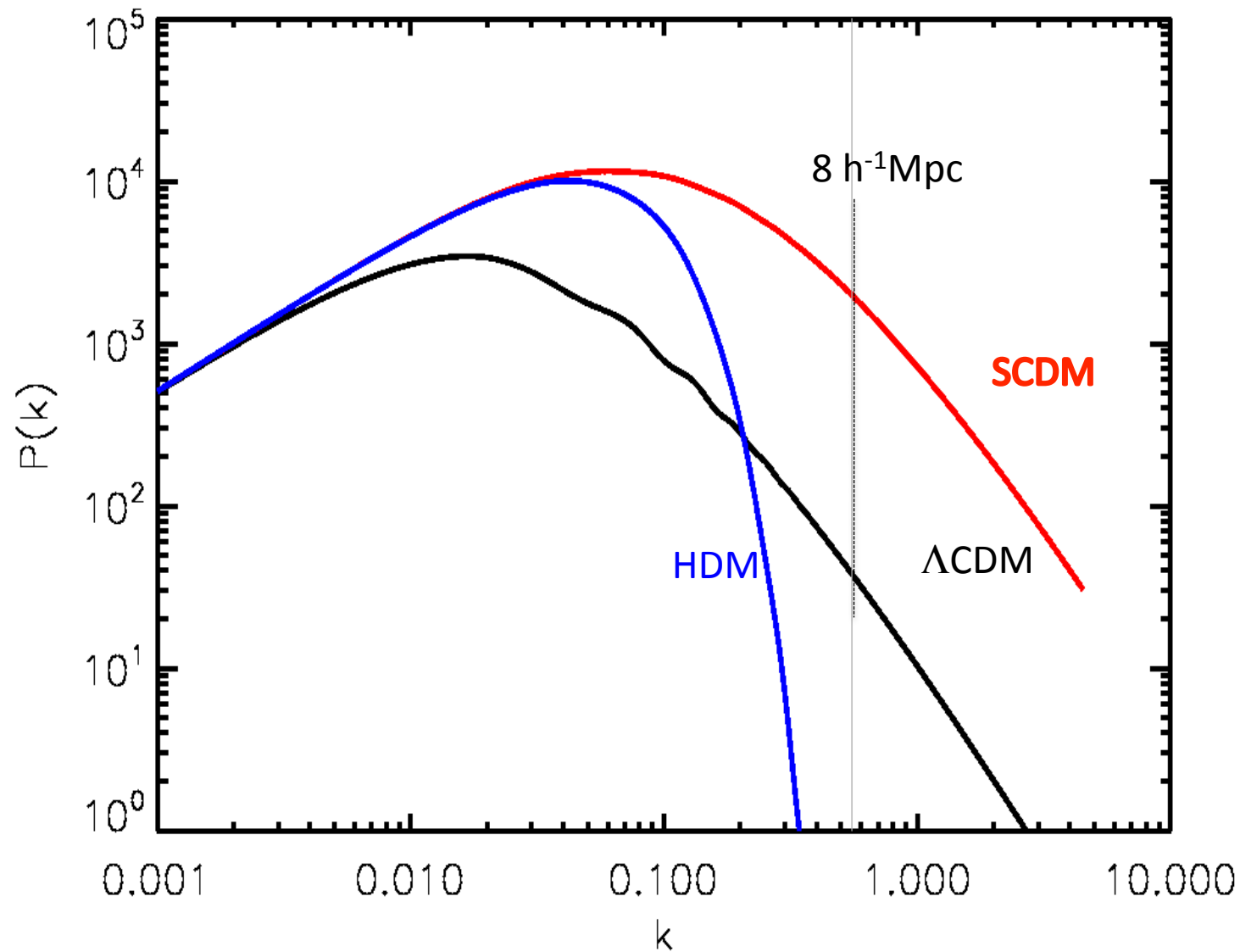
Typically constrain :

$$s_8 = \sigma_8 \left(\frac{\Omega_m}{0.30} \right)^{0.5}$$

Amplitude of perturbations

Amount of matter
in the Universe

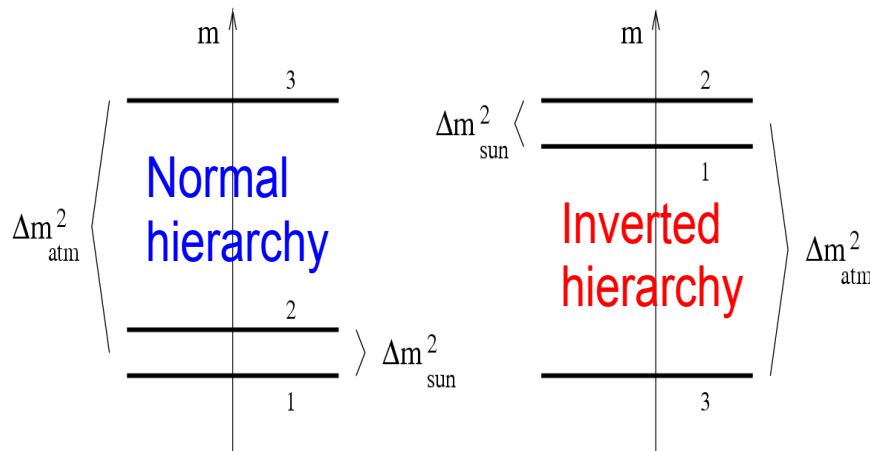
Ruling out of pure HDM & pure CDM



Limit on the sum of neutrino masses

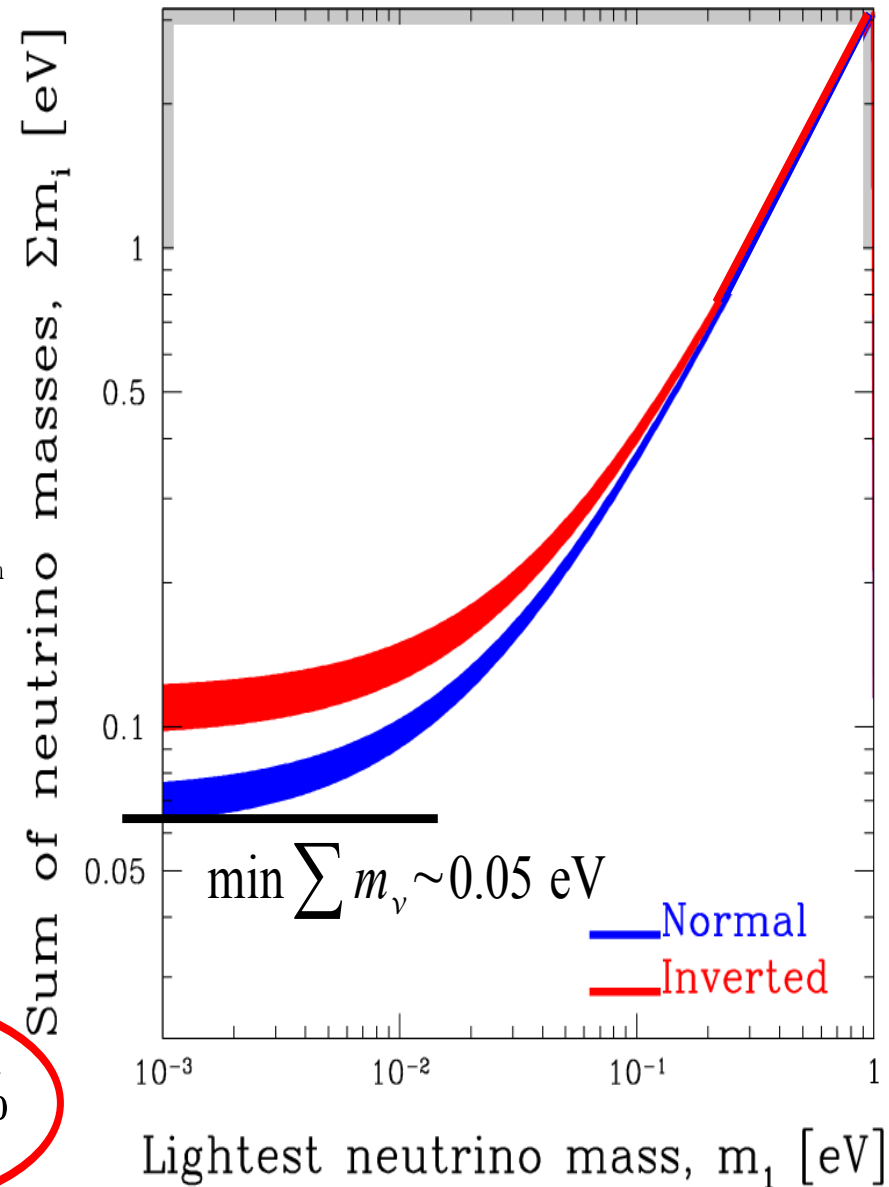
- Neutrino oscillations:

$$\Delta m_{\text{atm}}^2 \sim 10^{-3} \text{ eV}^2 \quad \Delta m_{\text{sun}}^2 \sim 10^{-5} \text{ eV}^2$$



Minimum amount of
neutrino dark matter

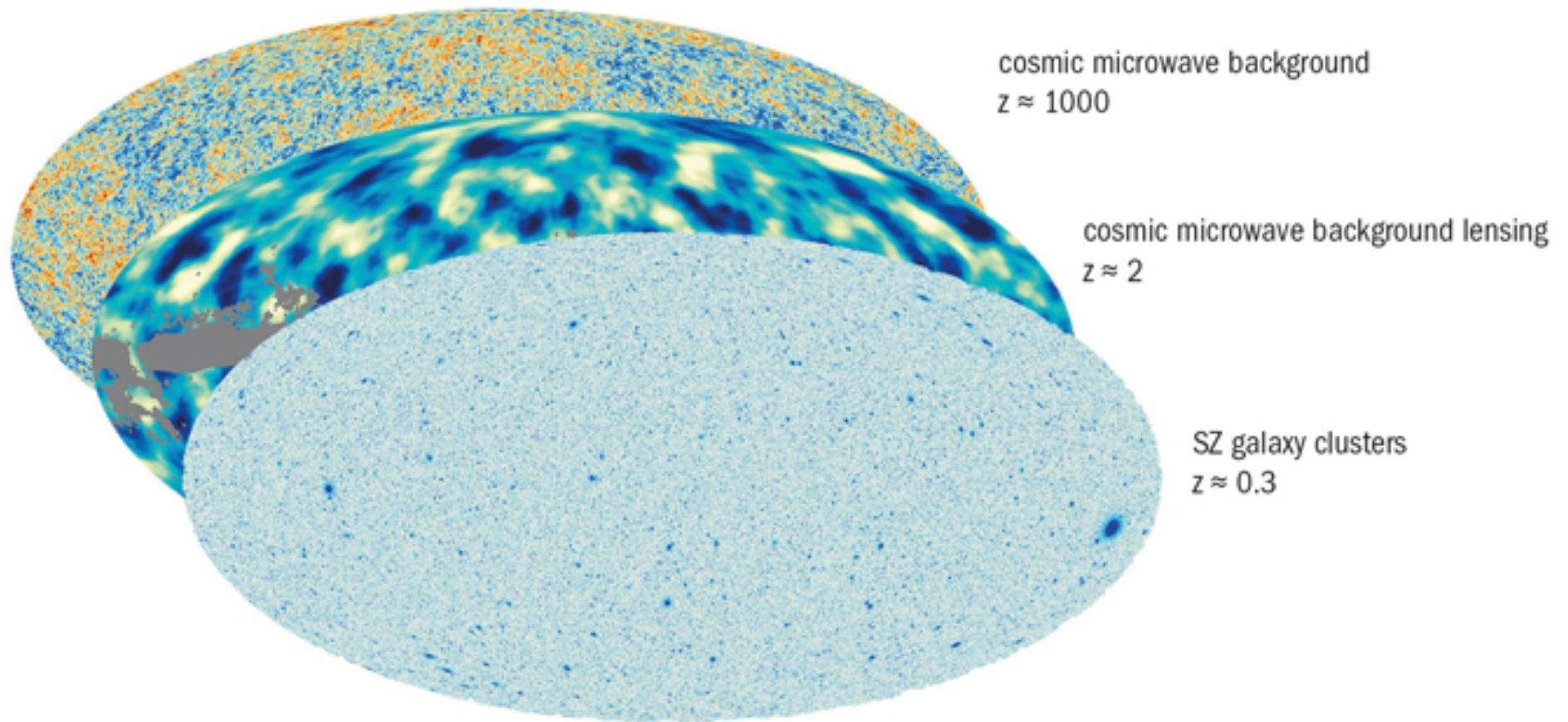
$$\min \sum m_\nu \sim 0.05 \text{ eV} \rightarrow \min \Omega_\nu \sim 0.1 \%$$



!!! Health Warning !!!

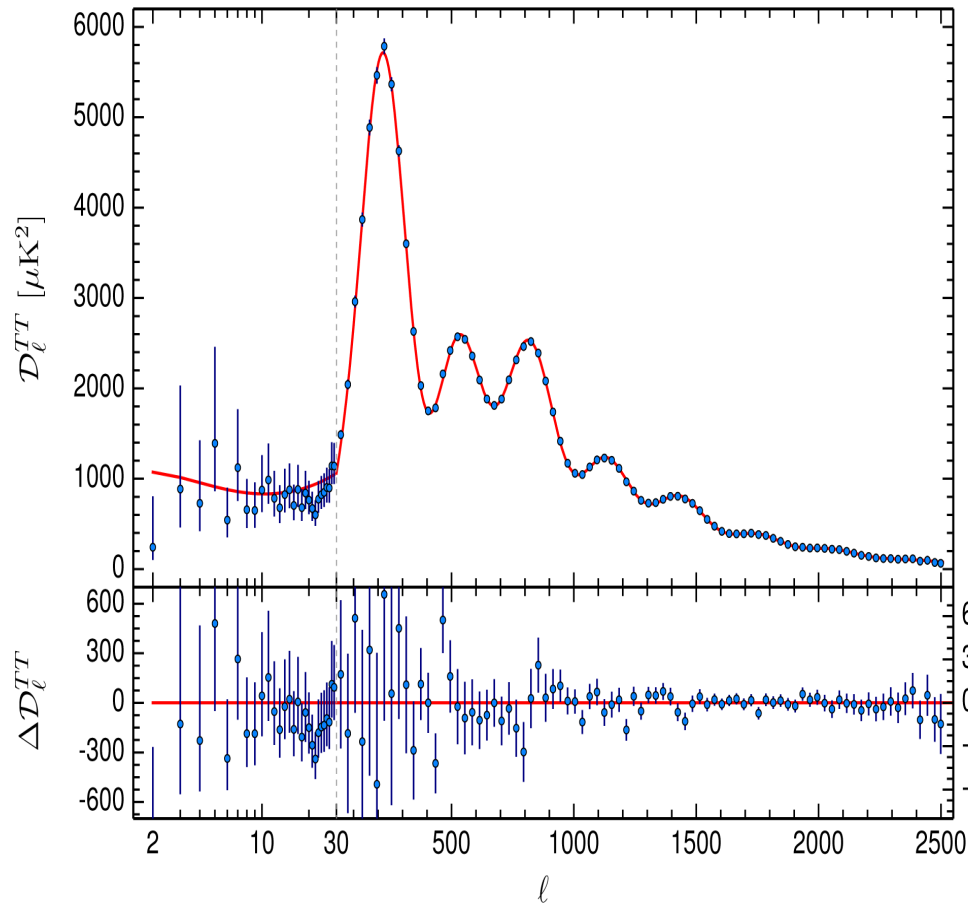
- All cosmological limits on neutrino masses are model dependent
- Standard cosmological limits on all other parameters are sensitive to neutrino history
- At the moment $\sum m_\nu = 0.06 \text{ eV}$ is used with 2 equal masses and 1 zero mass
- Probes of LSS are less mature at the moment

Planck 2015 results

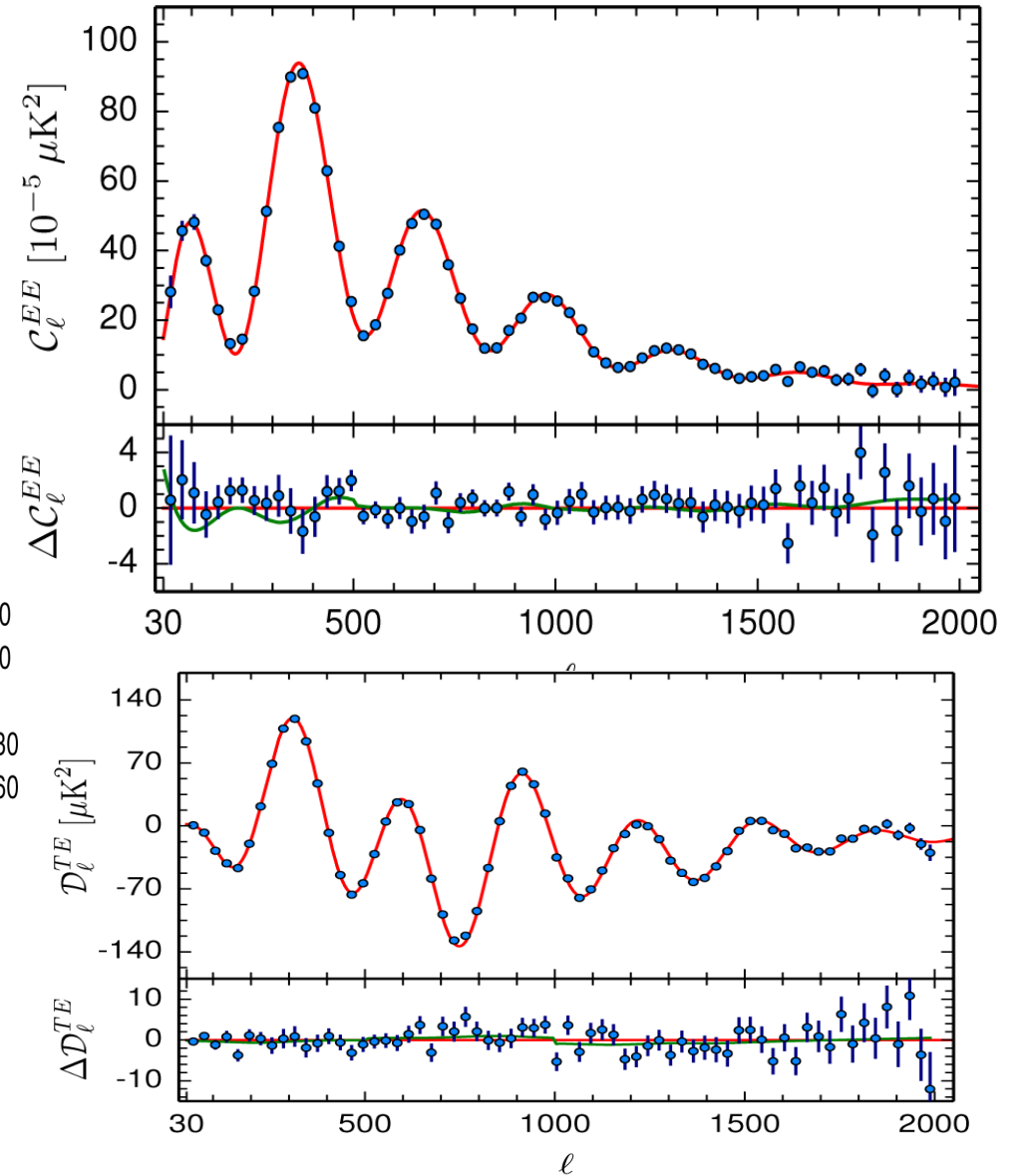


Three separate probes of cosmology !

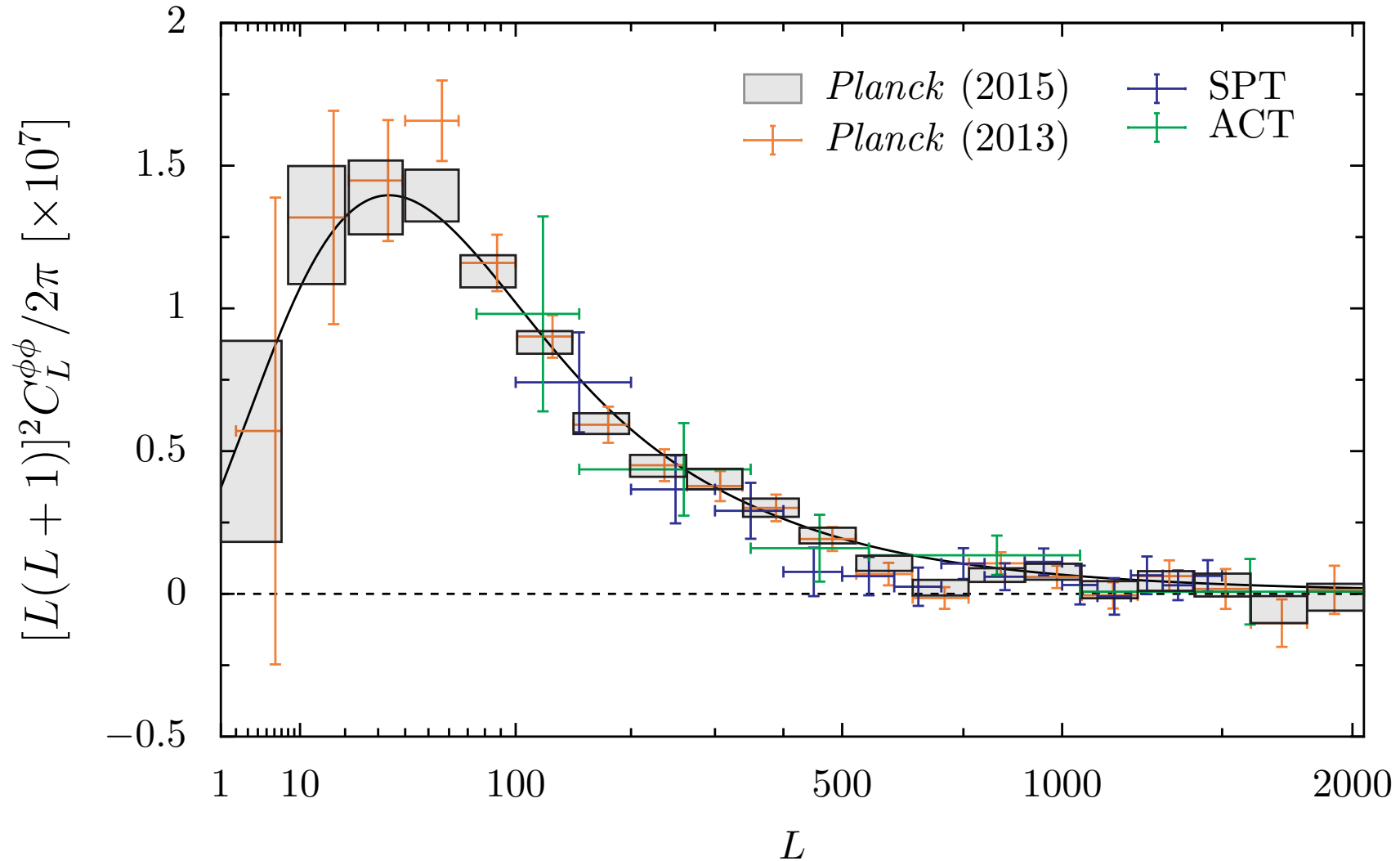
Primary CMB measurements



+ low P : large scale polarization



CMB lensing power spectrum



Constraints on base Λ CDM

Fitted parameters	$100\Omega_b h^2$	$=$	2.225 ± 0.016	
	$\Omega_c h^2$	$=$	0.1198 ± 0.015	
	$100\theta_{MC}$	$=$	1.04077 ± 0.00052	
	τ	$=$	0.079 ± 0.017	
	$\log(10^{10} A_S)$	$=$	3.094 ± 0.034	NB paper now Cited > 4000 times
	n_S	$=$	0.9645 ± 0.0049	
Derived parameters	Ω_m	$=$	0.3156 ± 0.0091	
	σ_8	$=$	0.831 ± 0.013	
	$10^9 A_S e^{-2\tau}$	$=$	1.882 ± 0.012	

Planck TT, TE, EE + low P (ie just CMB) : 68% confidence

Extensions to Λ CDM

$$\Omega_k = -0.04 \pm 0.04$$

$$\sum m_\nu / \text{eV} < 0.492$$

$$N_{\text{eff}} = 2.99 \pm 0.40$$

$$Y_p = 0.25 \pm 0.03$$

$$dn_S/d(\log k) = -0.006 \pm 0.014$$

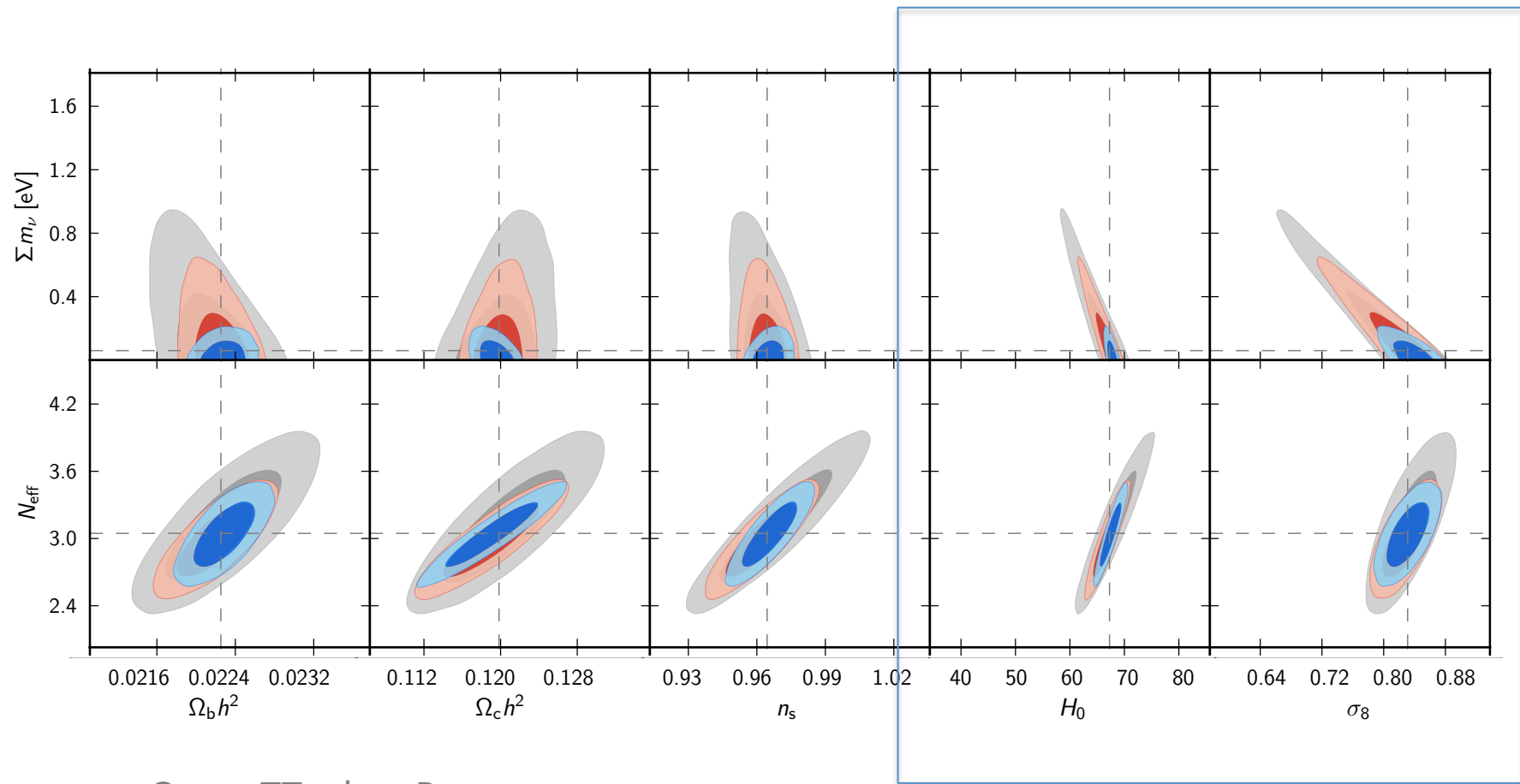
$$r_{0.002} < 0.0987$$

$$w = -1.5 \pm 0.5$$

Our
interest
here !

From Planck Collaboration (2016) : arXiv: 1502.01589v3 published in A&A

Degeneracies with standard parameters



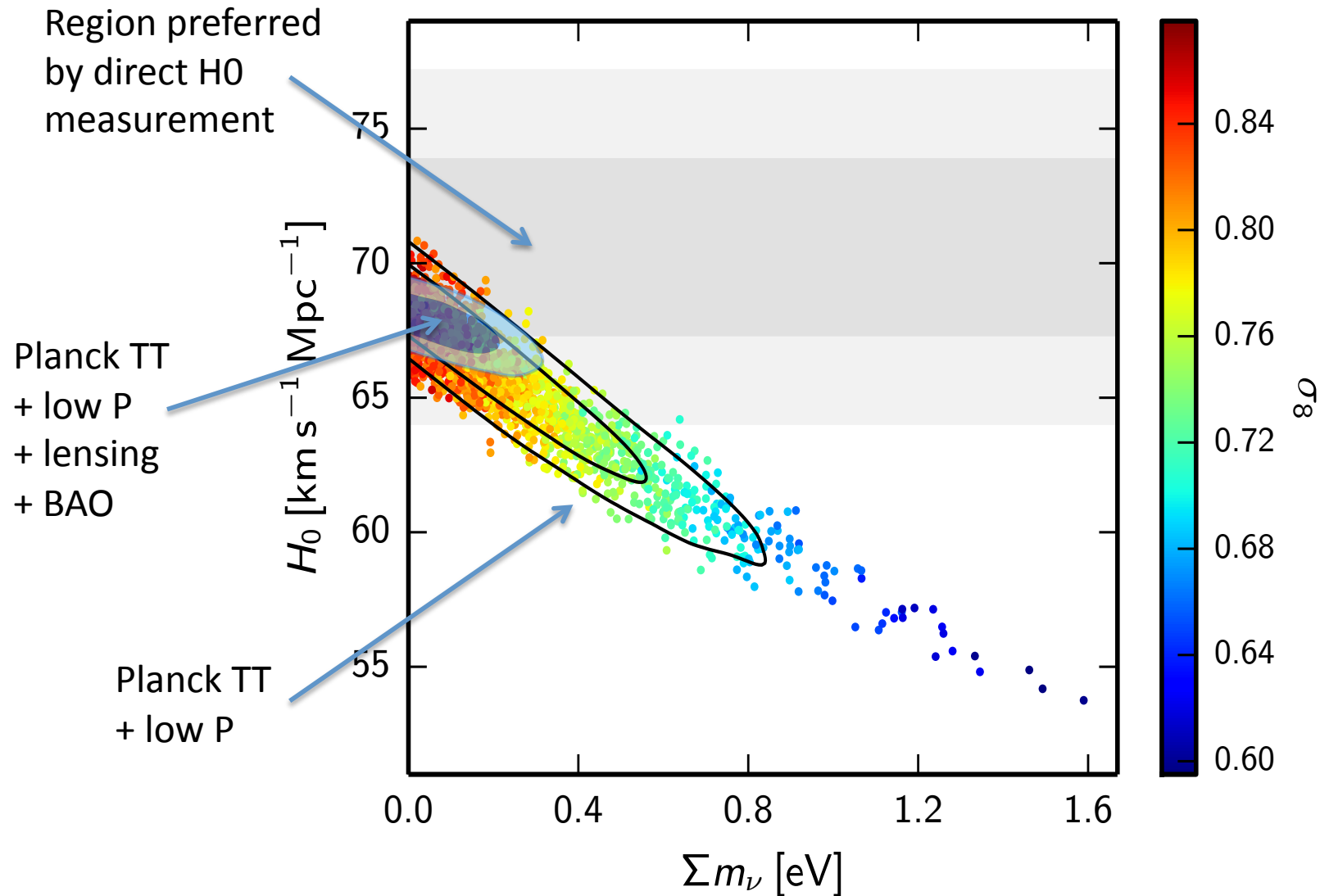
Grey : TT + low P

Red : TT, EE, TE + low P

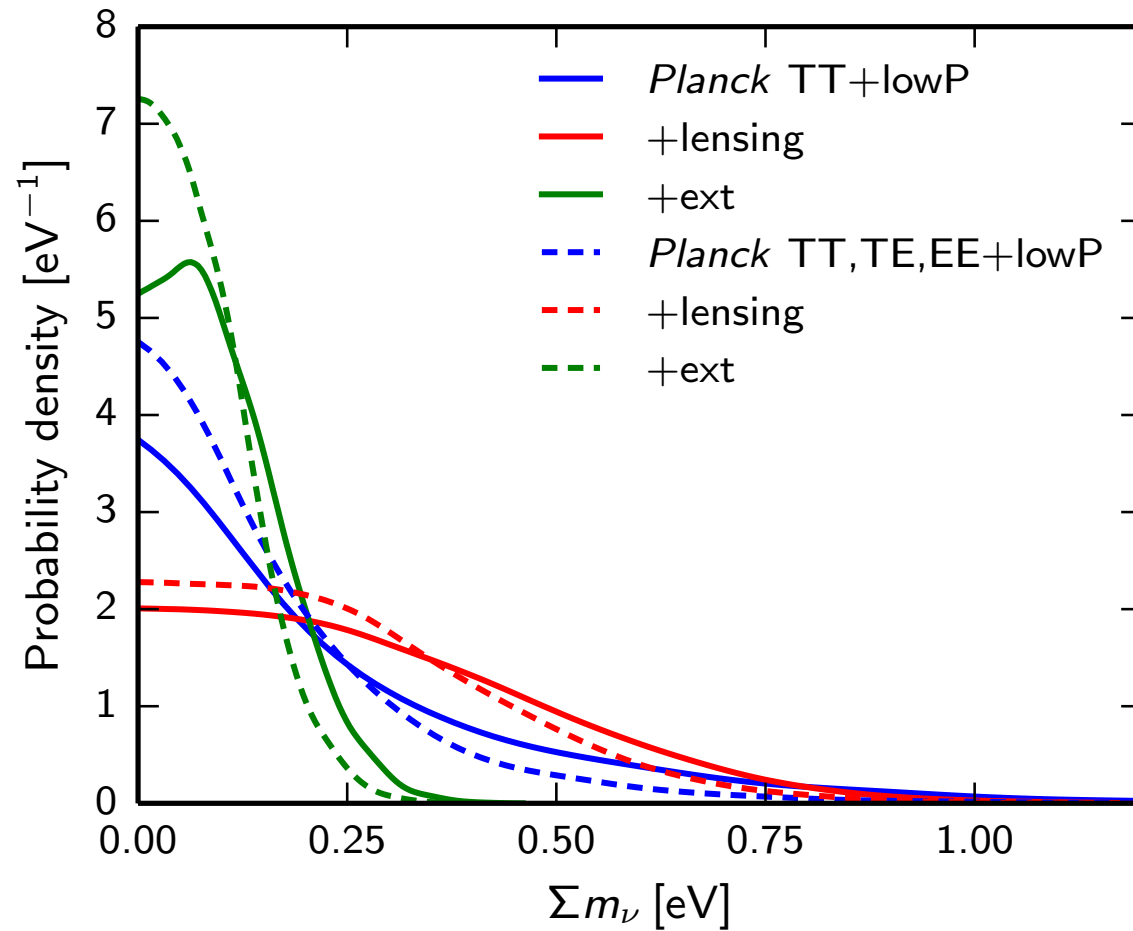
Blue : TT, EE, TE, low P + BAO

Key degeneracies

Neutrinos v H_0 and σ_8



Limits on active neutrinos



$\text{ext} = \{\text{BAO, JLA, } H_0\}$

Limits on active neutrinos

$$\text{TT, TE, EE} \quad \sum m_\nu < 0.492 \text{ eV}$$

$$\text{TT, TE, EE + Planck lensing} < 0.589 \text{ eV}$$

Safe
bound



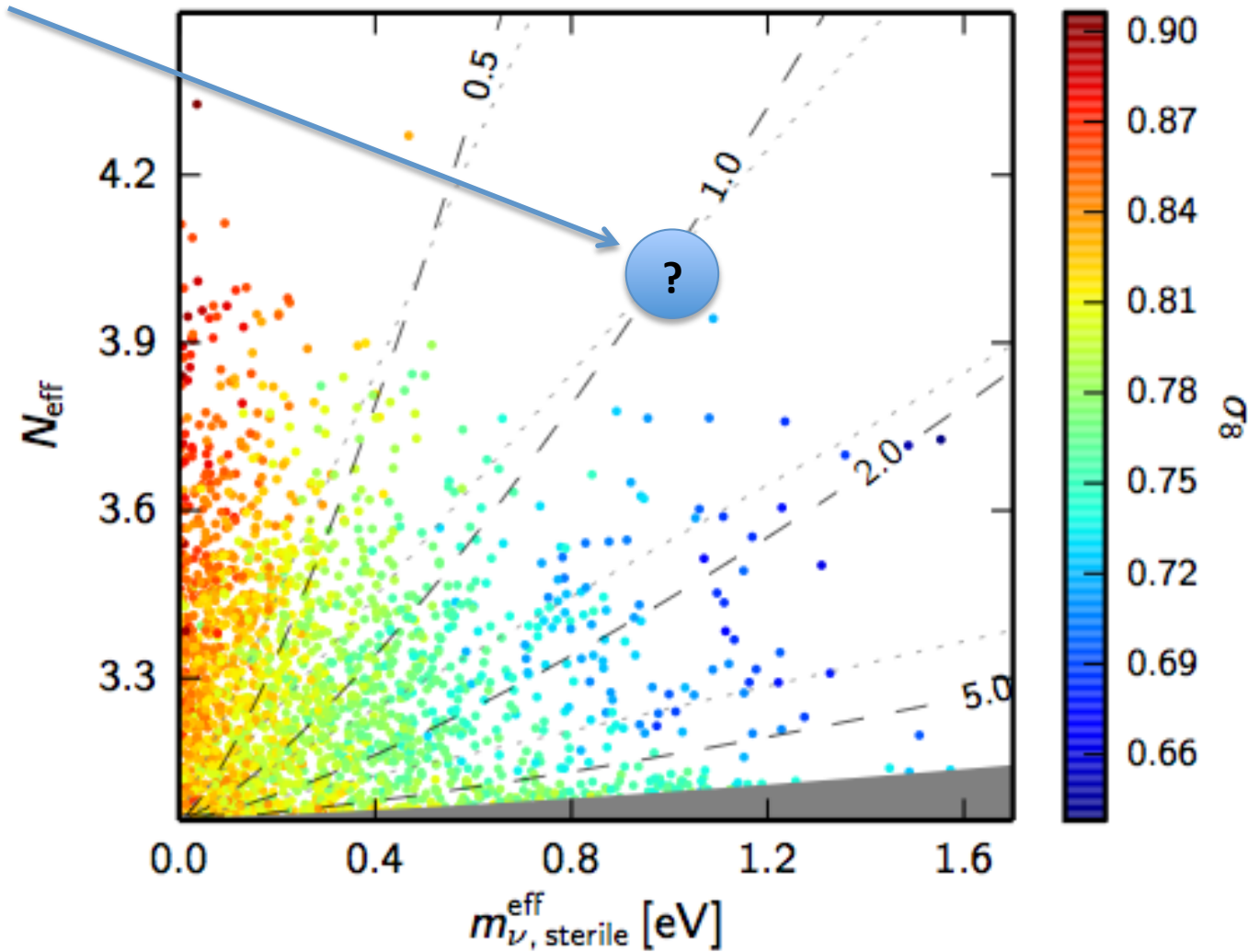
$$\text{TT, TE, EE + lensing + ext} < 0.194 \text{ eV}$$

ext = {BAO, JLA, H_0 }

(95 % upper limits)

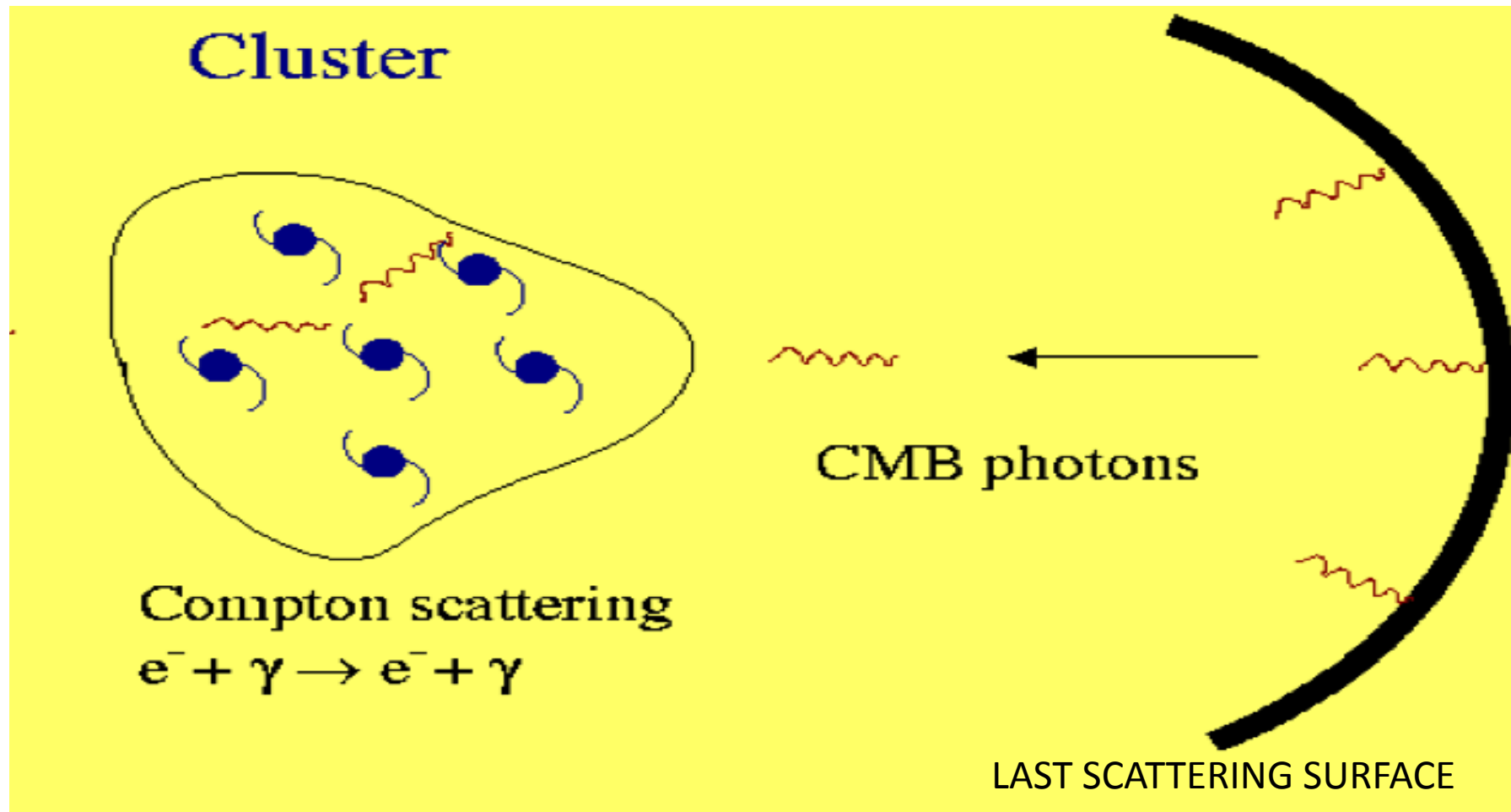
Sterile Neutrinos

Possible
solution to
reactor
anomalies



$$N_{\text{eff}} < 3.7 \quad m_{\nu, \text{sterile}}^{\text{eff}} < 0.52 \text{ eV}$$

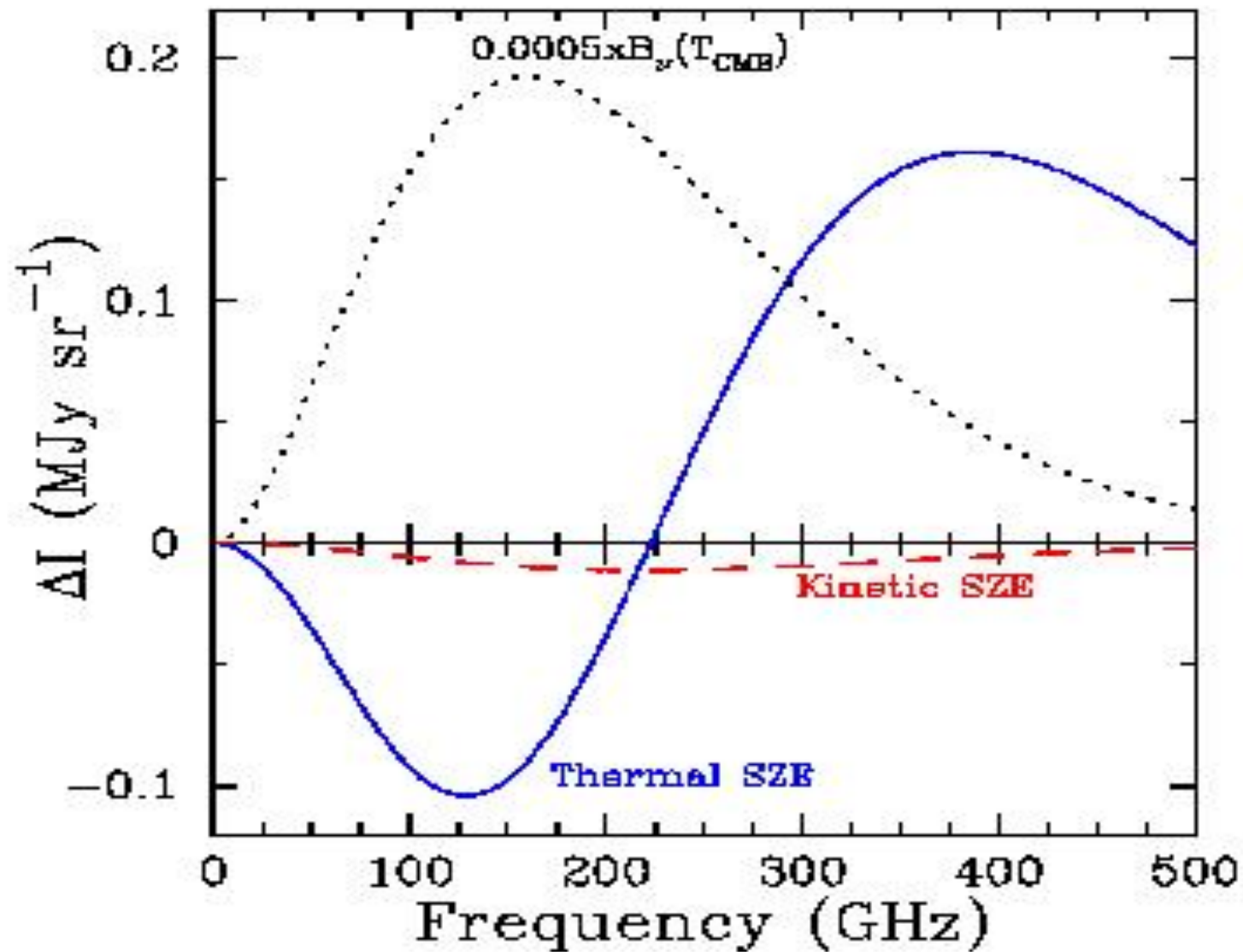
Sunyaev-Zeldovich Effect



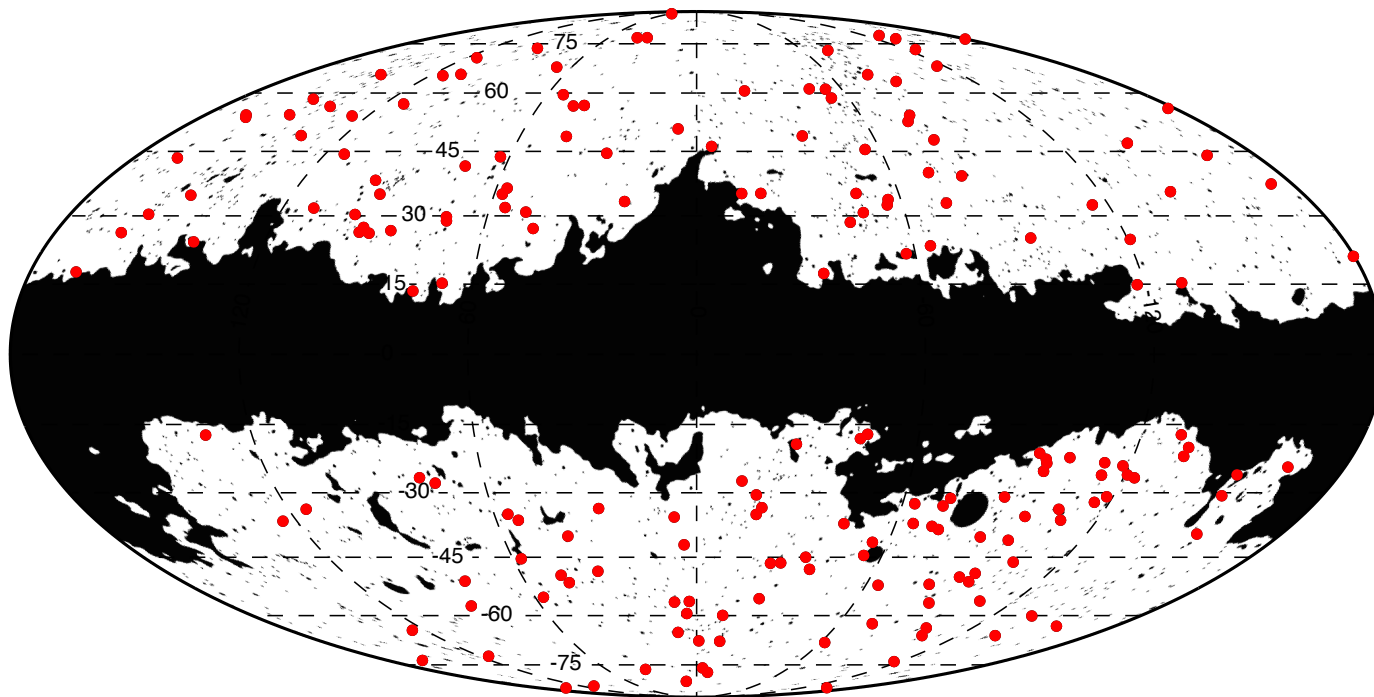
$$\frac{\Delta T}{T} \propto \sigma_T \int n_e T_e dl$$

= integrated gas pressure
along the line of sight

Spectral Signature



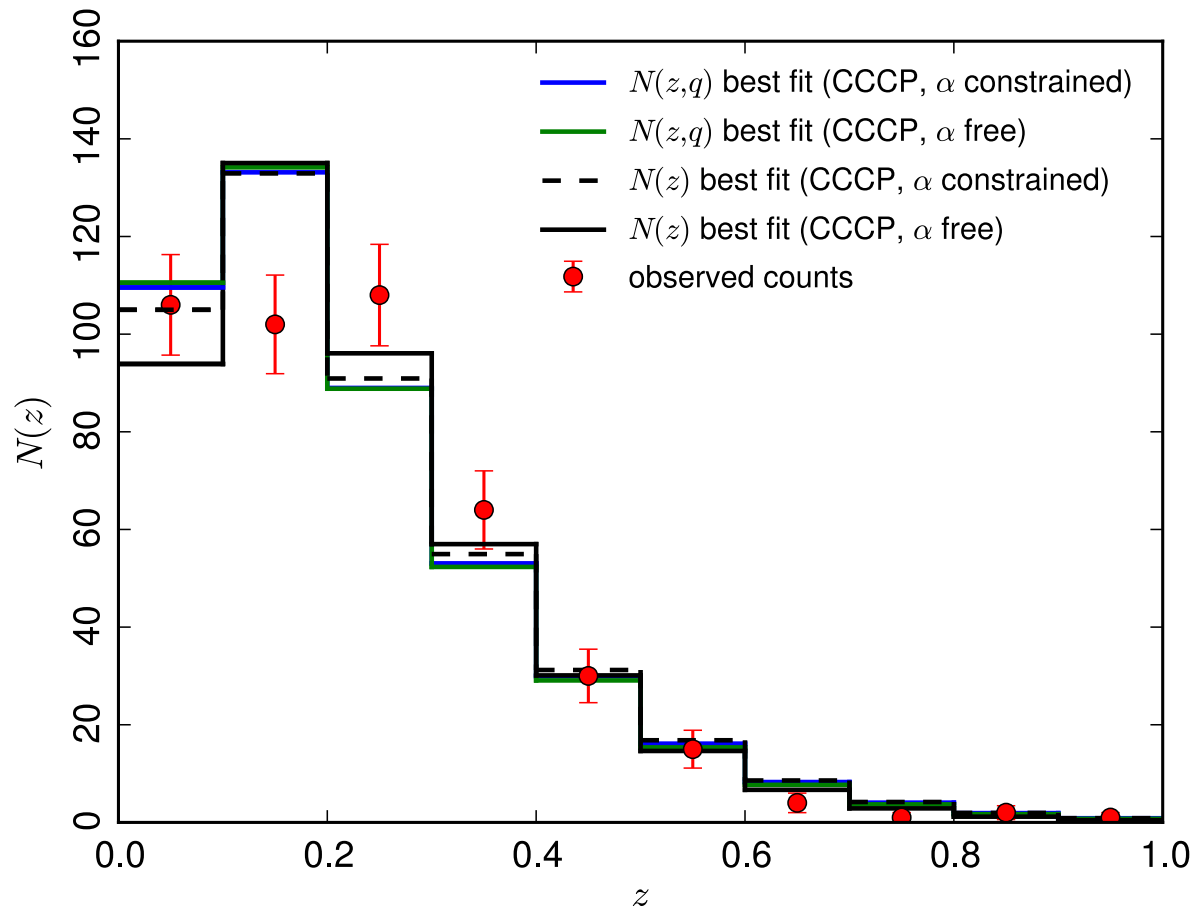
SZ cluster survey



Planck 2013 : 189 clusters with $S/N > 7$

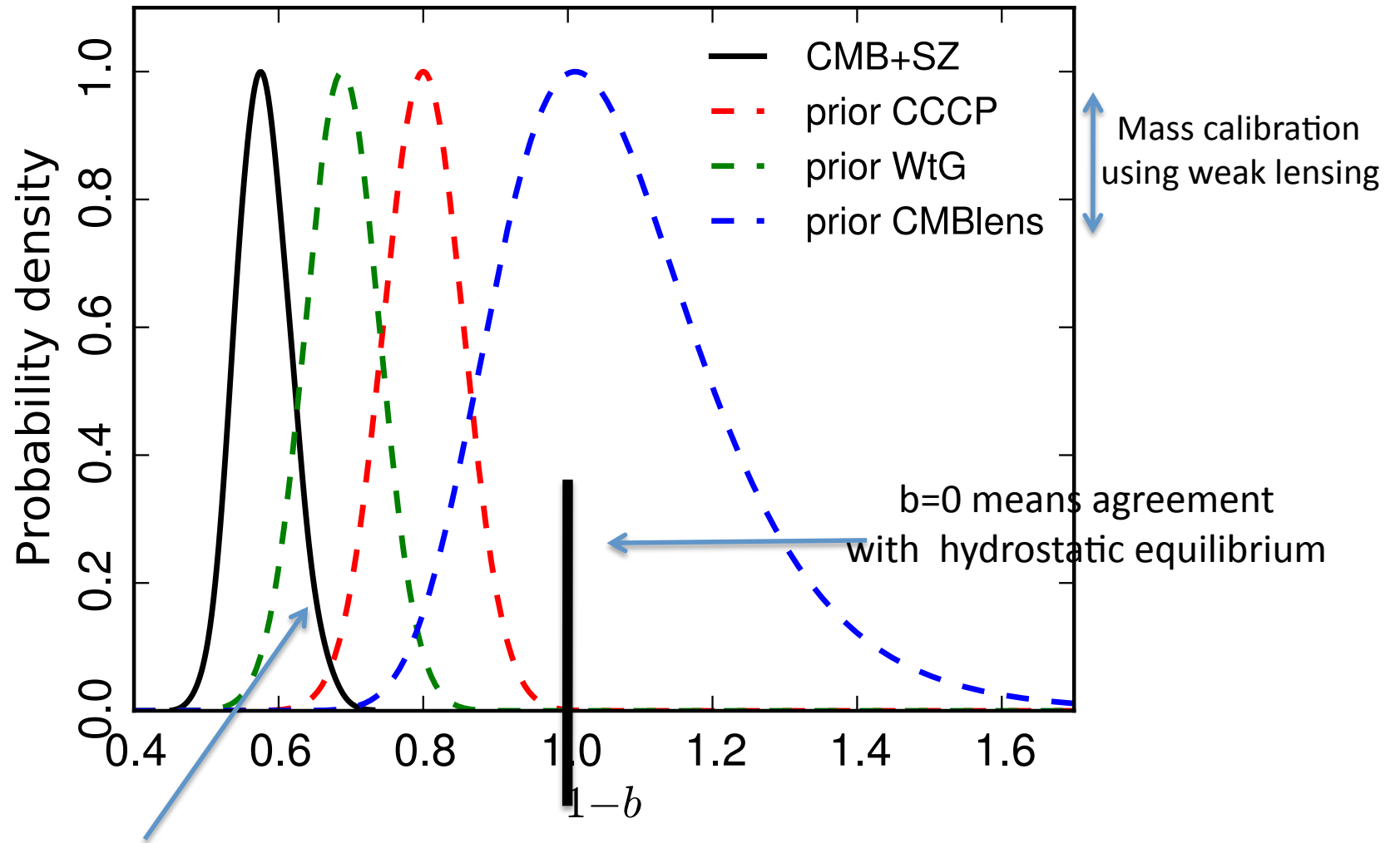
Planck 2015 : 439 clusters with $S/N > 6$

Cluster Number Counts from Planck



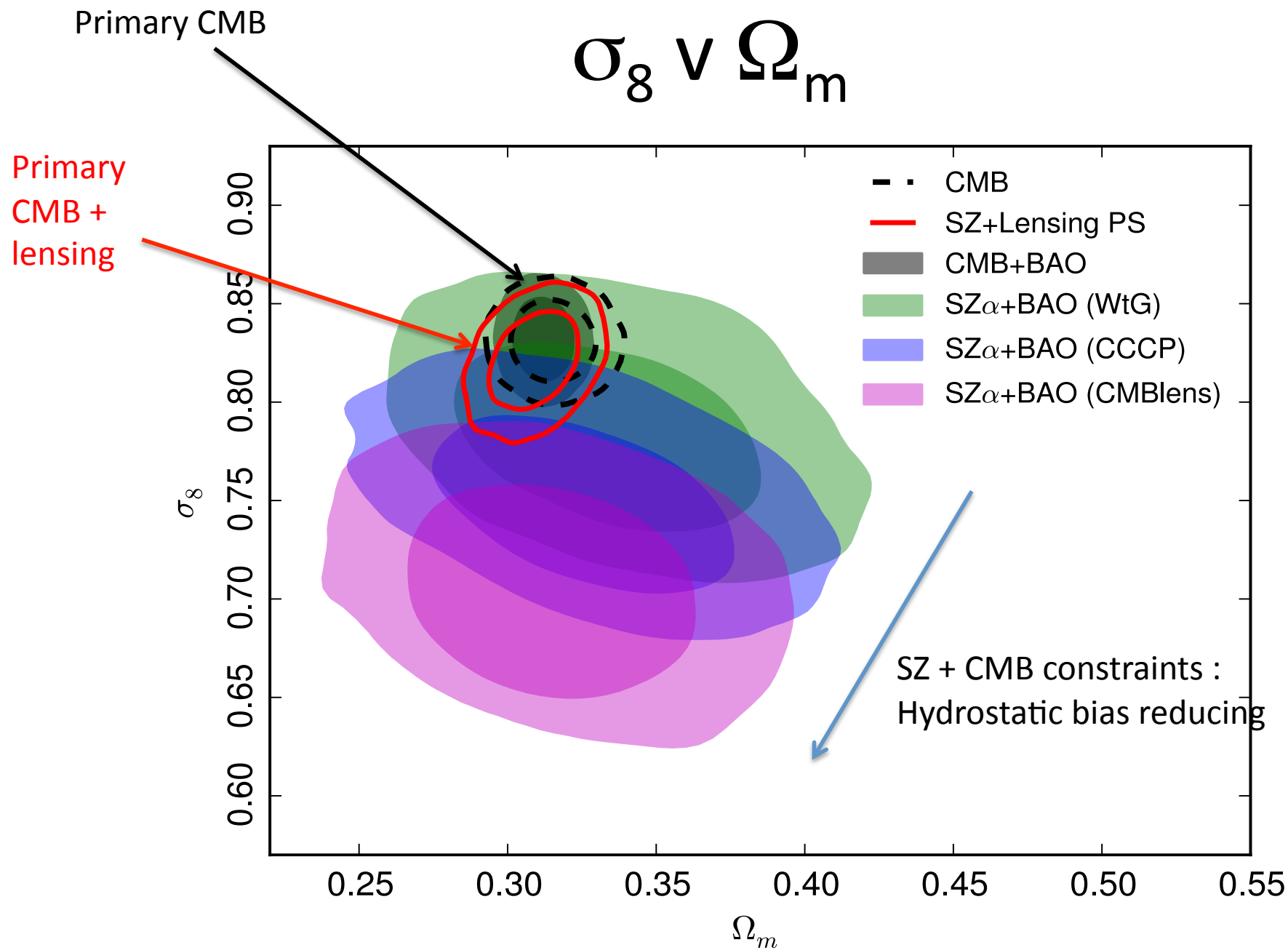
Number of clusters as a function of redshift

Cluster Hydrostatic Bias

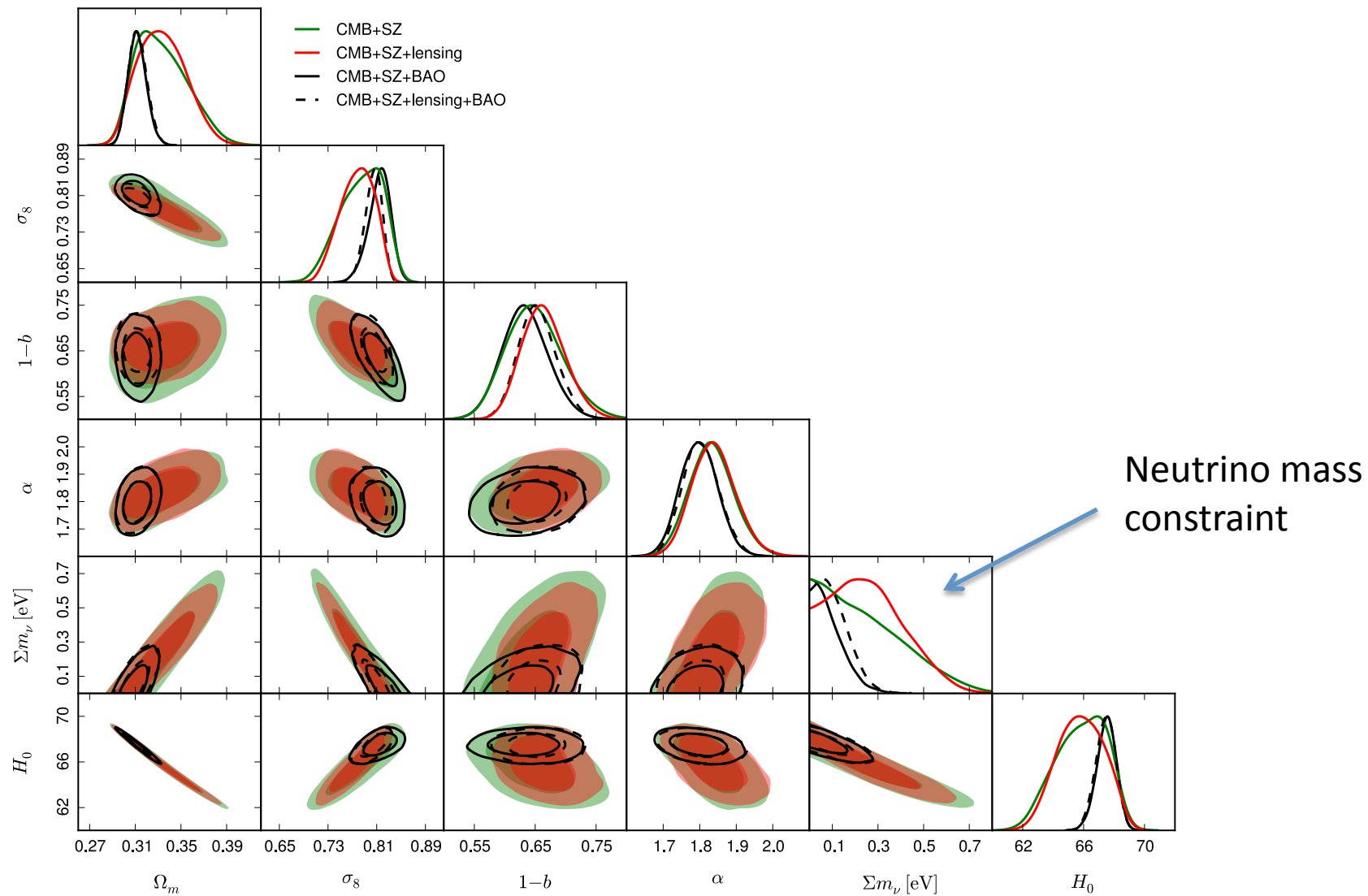


Suggests SZ counts may not be in agreement with other determinations

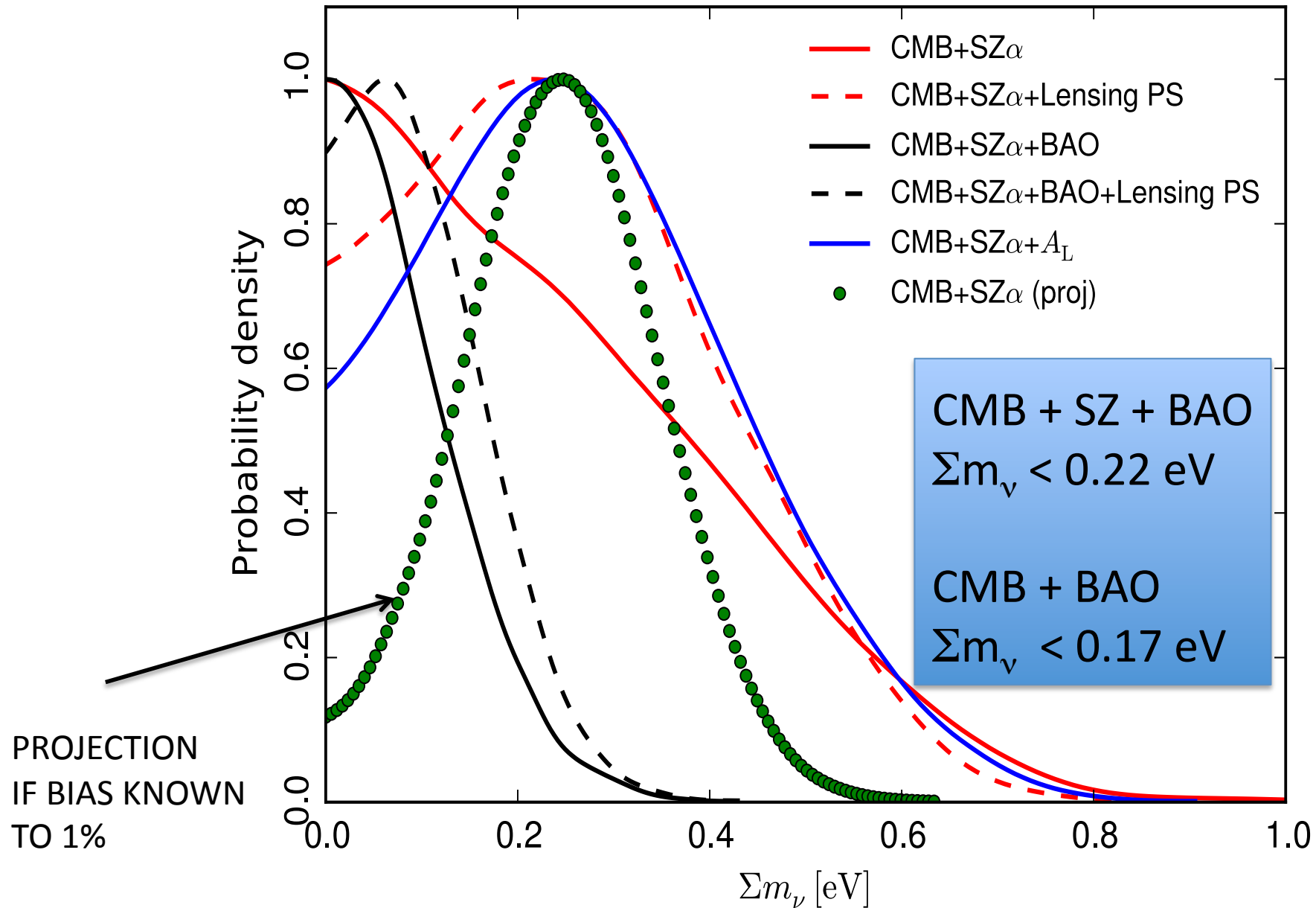
$$\sigma_8 \text{ v } \Omega_m$$



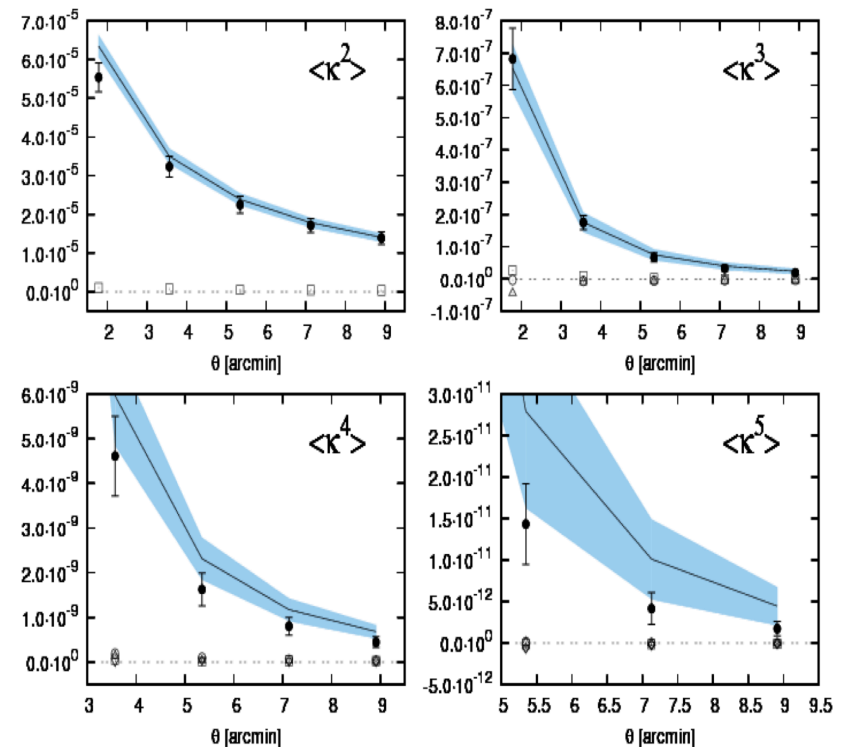
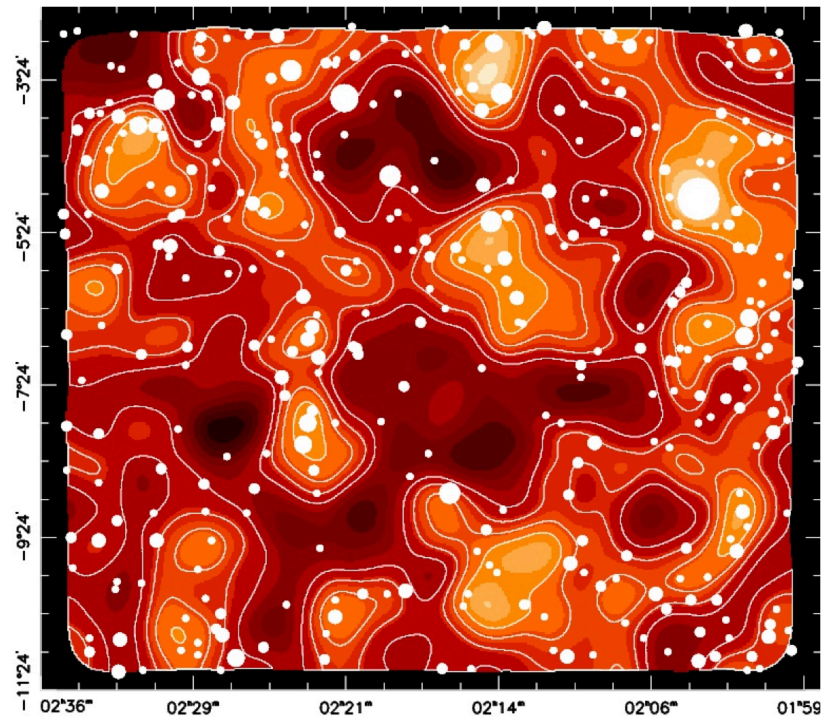
CMB + SZ + CCCP



Constraints on neutrino mass

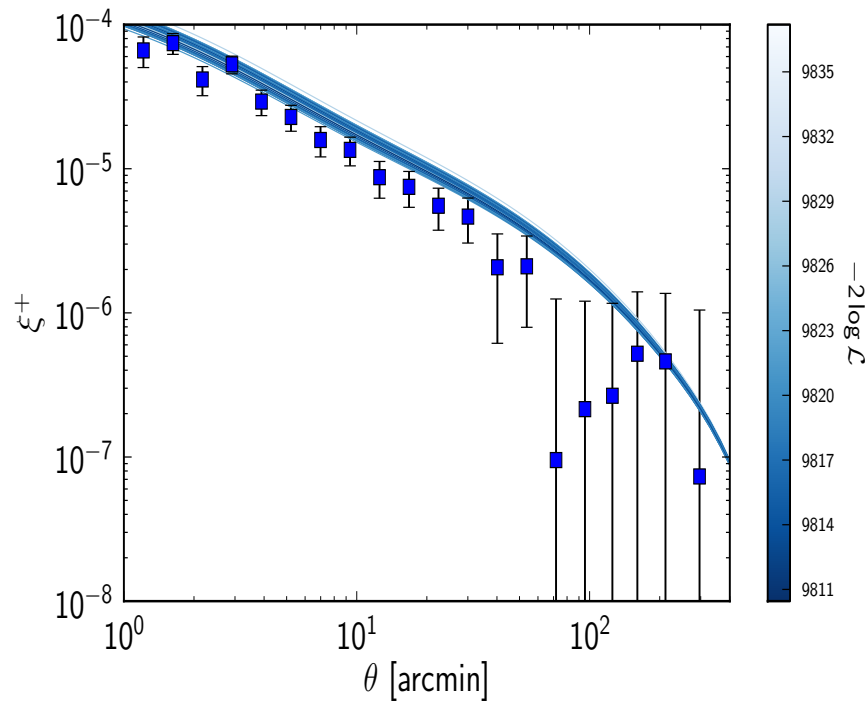


CFHTLenS

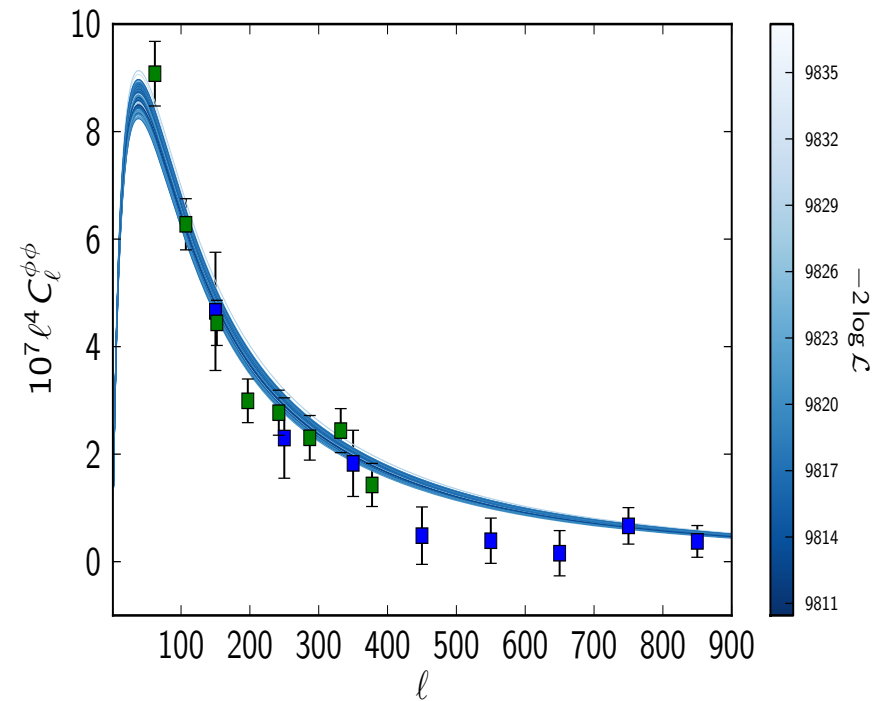


Around $\sim 150 \text{ deg}^2$ survey using CFHT with high source density for weak lensing

Lensing spectra v Planck best fit



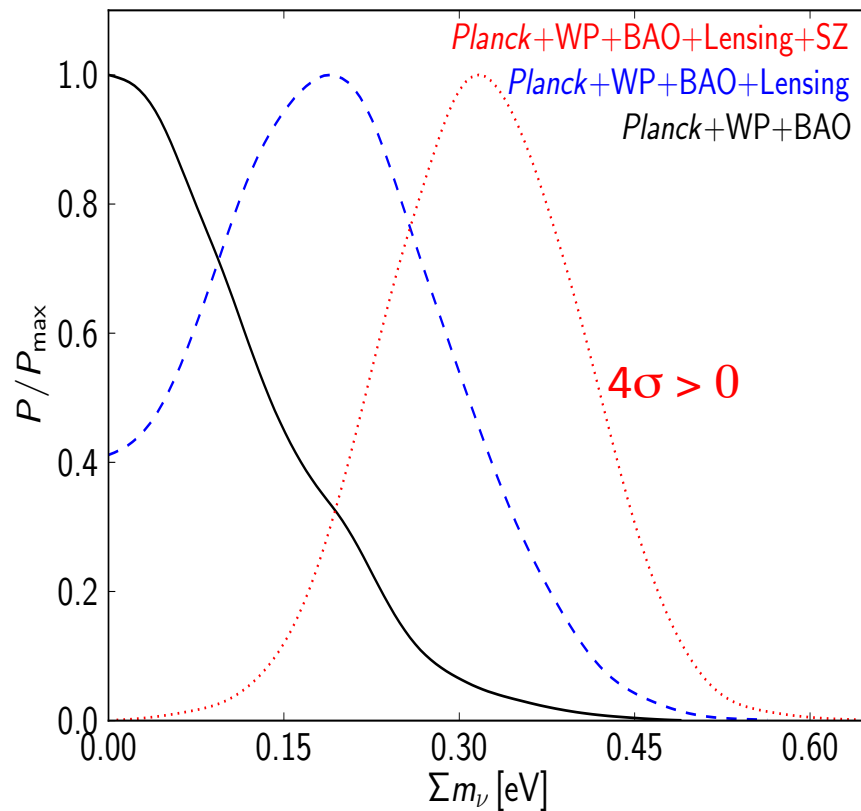
CFHTLenS



Planck & SPT CMB lensing

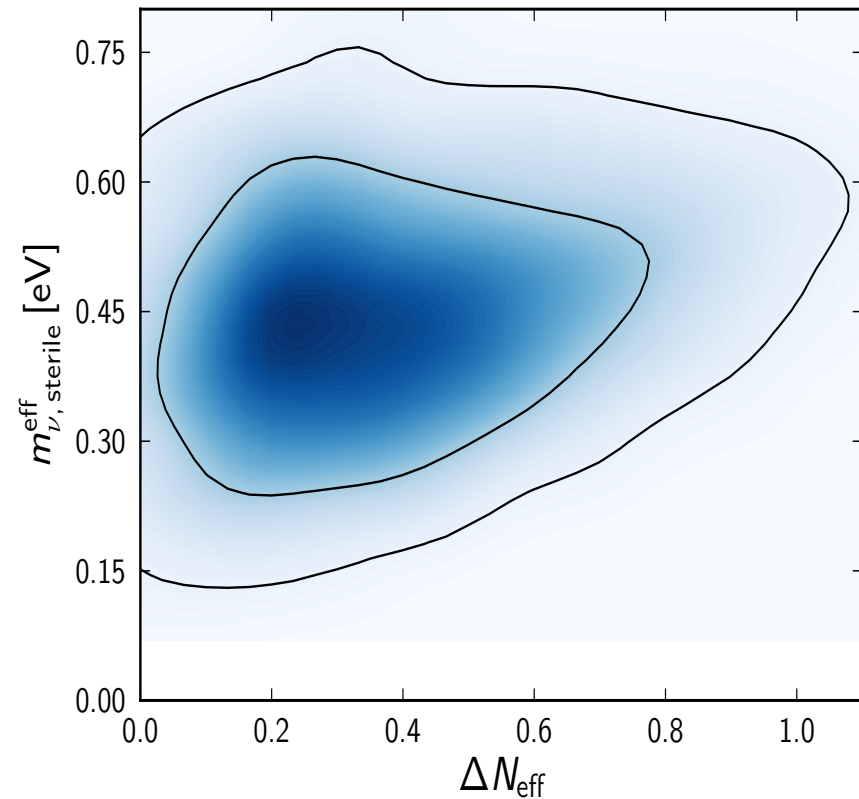
There is a discrepancy !

Joint Constraints on Massive Neutrinos



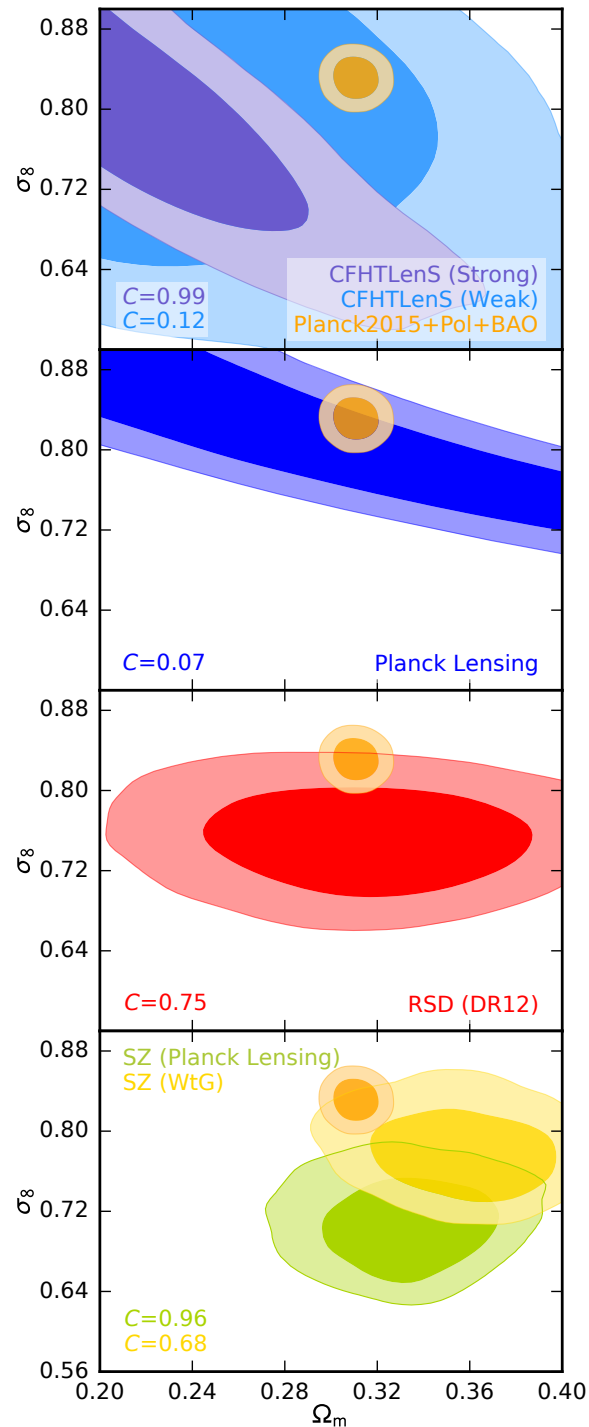
Active Neutrinos

Based on Planck 2013 results !!!



Sterile Neutrinos

Additional extra feature :
 H_0 agrees with HST



Weak lensing measured
from galaxy shapes

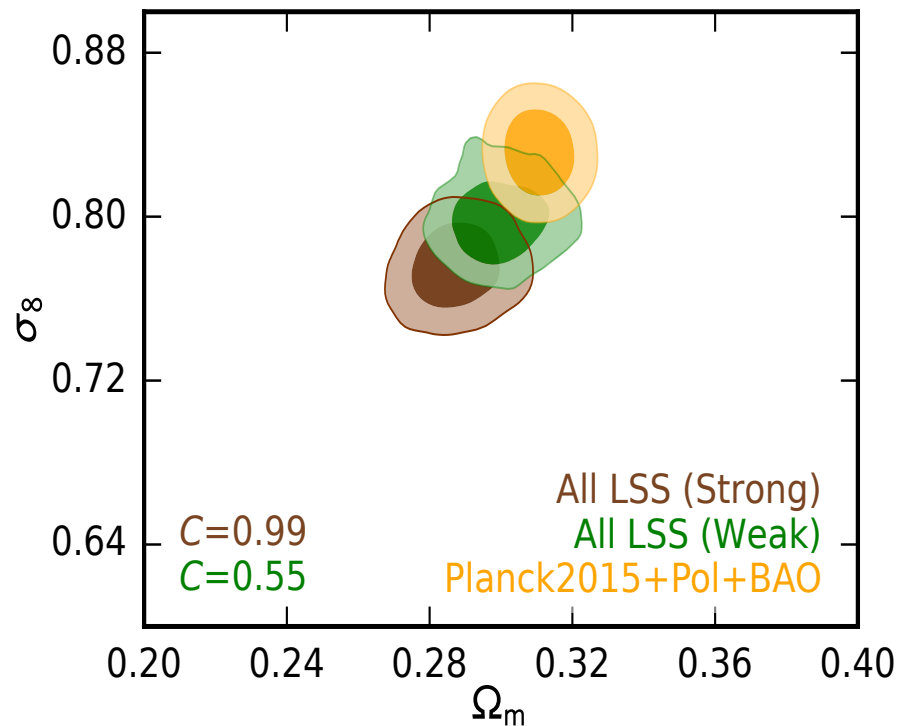
Weak lensing measured
from CMB

Redshift space distortions

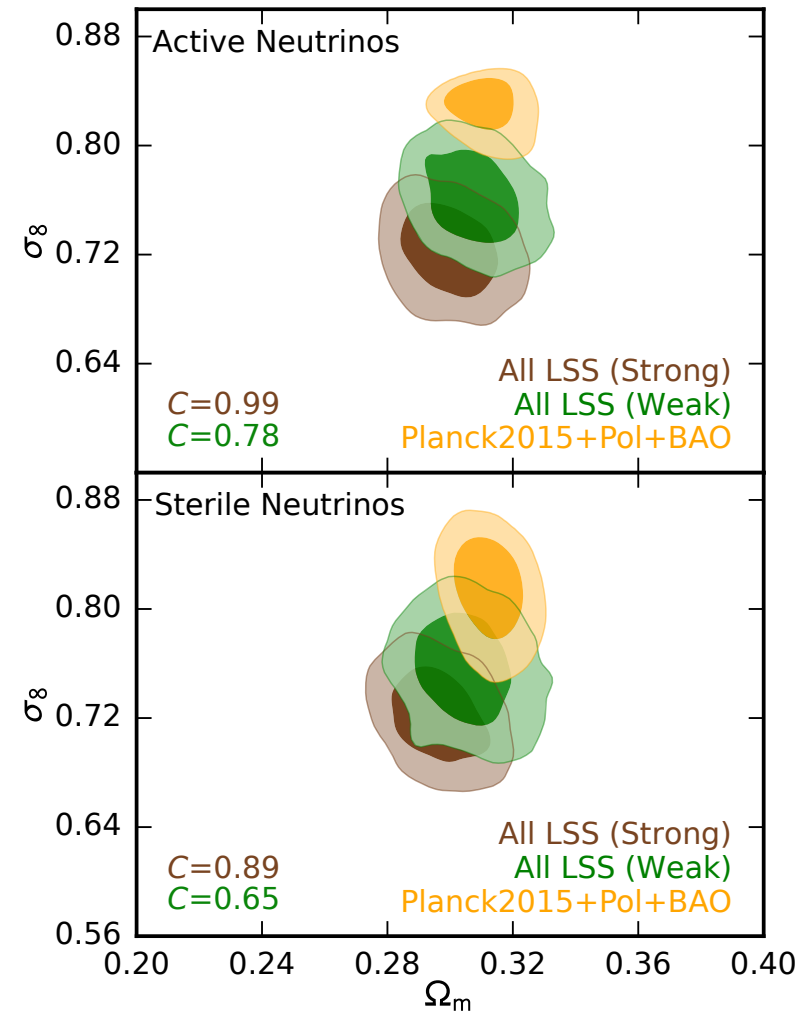
SZ cluster counts

ORANGE IS PRIMARY CMB + BAO

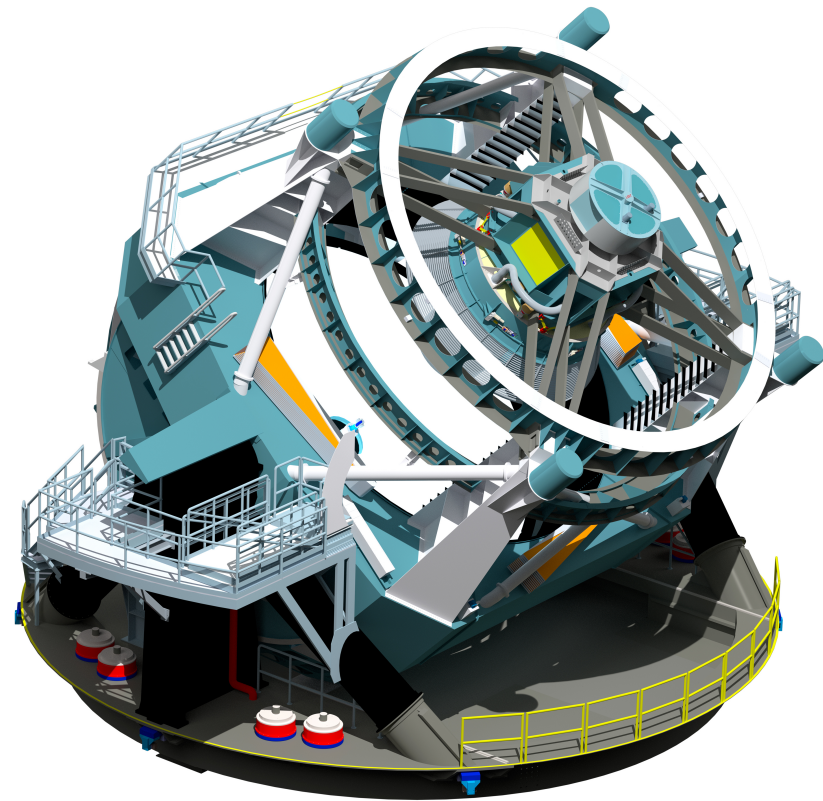
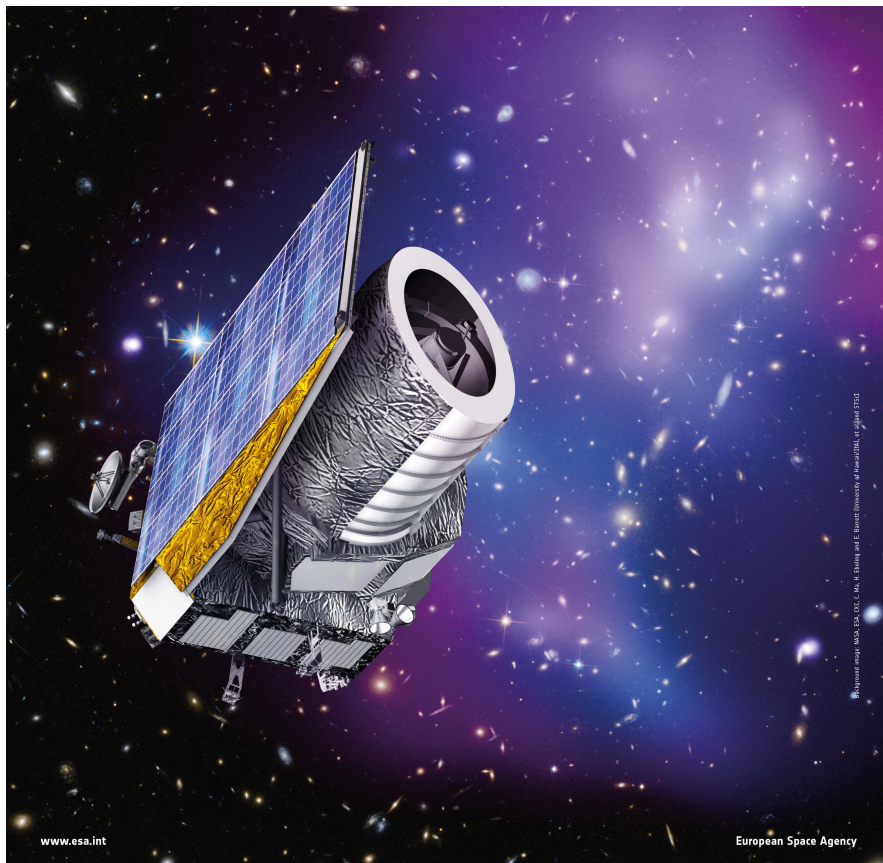
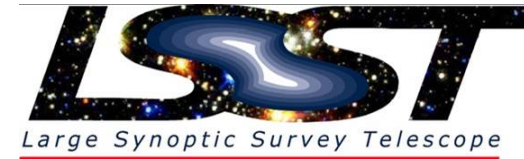
Present status of CMB/LSS tension



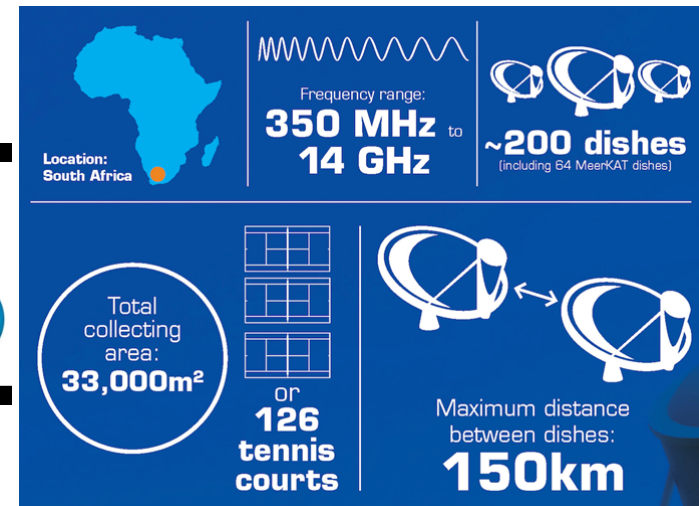
Strong LSS constraints are in tension with Planck at 2.5σ



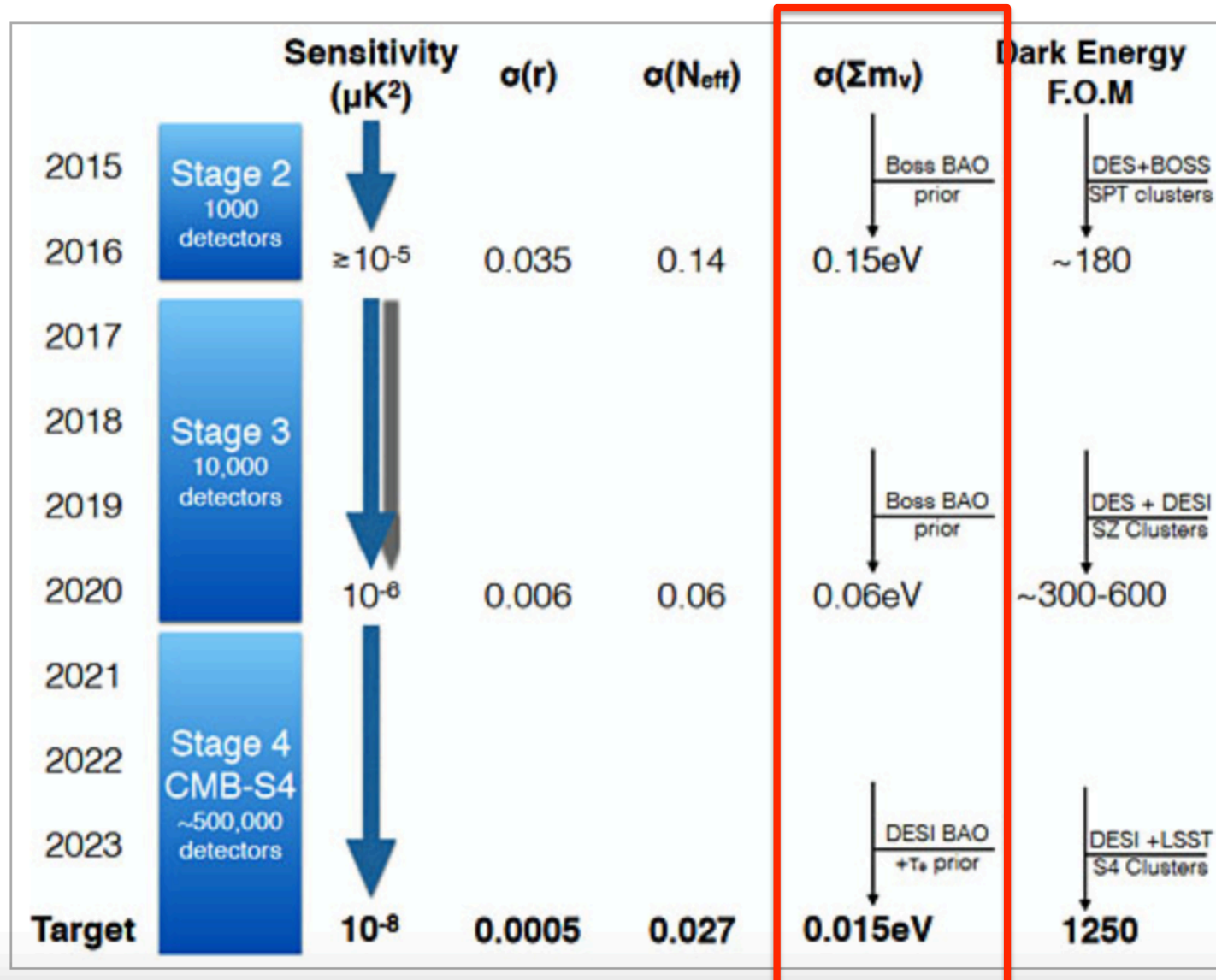
Stage 4 Cosmology Probes



Stage 4 Cosmology Probes



Future Probes



Conclusions

- Present safe limit : $\Sigma m_\nu < 0.6 \text{ eV}$ from CMB
- Most stringent limit : $\Sigma m_\nu < 0.2 \text{ eV}$
- needs input from other measurements eg BAO
- Issues with connecting with LSS – complex !
- Future : $\Sigma m_\nu < 60 \text{ meV}$ (2020ish)
 $\Sigma m_\nu < 15 \text{ meV}$ (2025ish)

At this level of
precision we can
start to think about
separating the masses