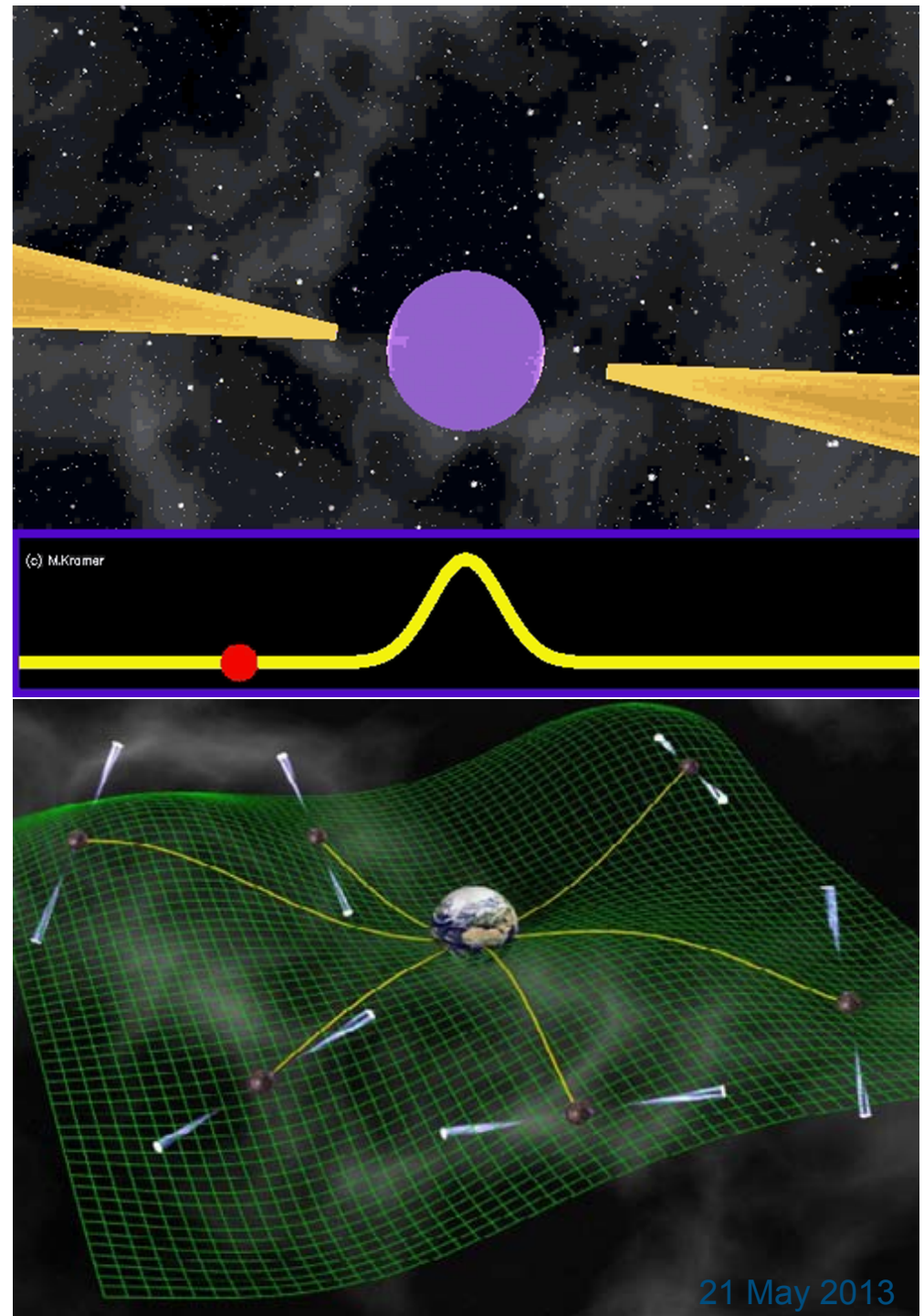


# Building a Galactic Scale Gravitational Wave Observatory: Increasing the Sensitivity of the NANOGrav PTA

Maura McLaughlin  
West Virginia University



GWADW2013

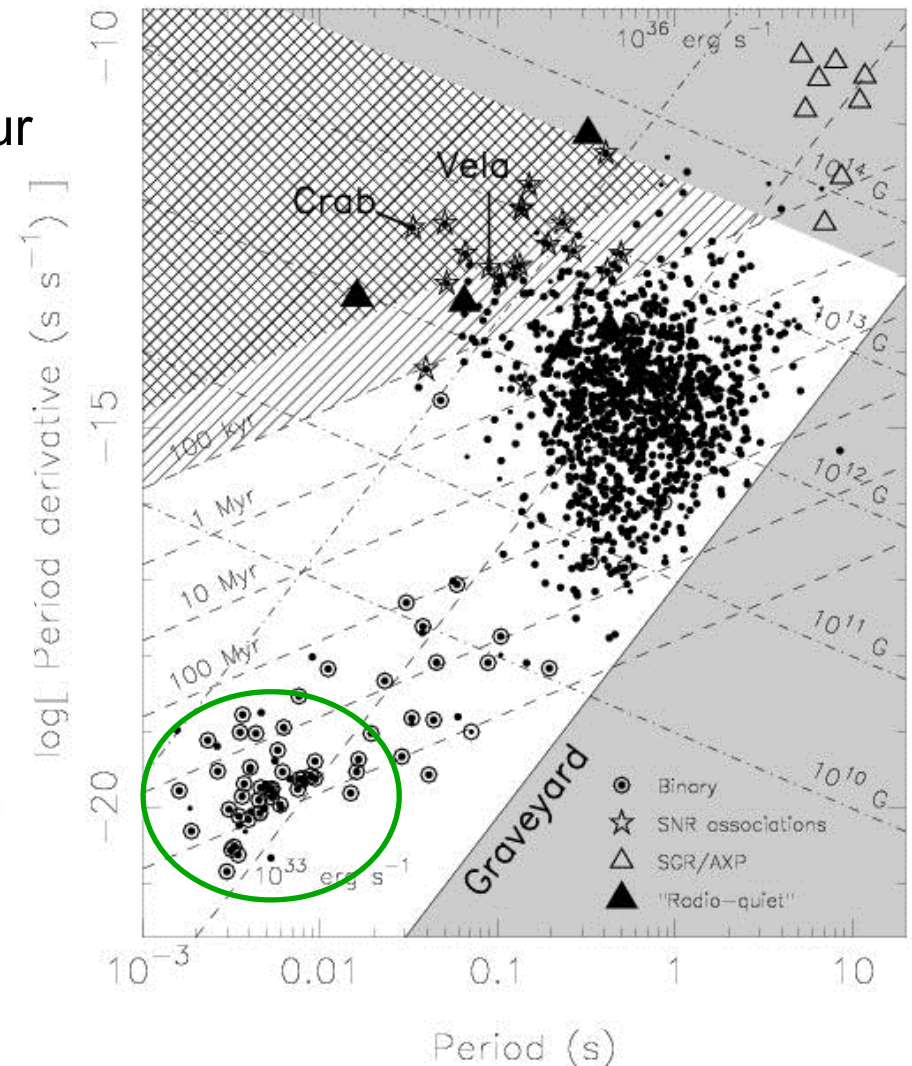
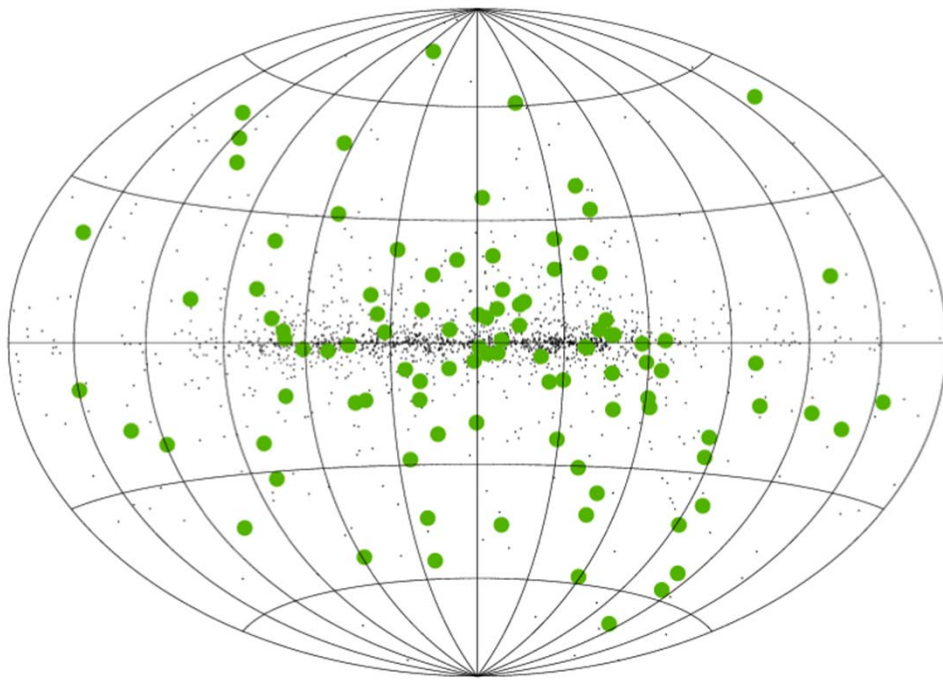


# Outline

- Introduction
  - millisecond pulsar properties
  - millisecond pulsar timing
- Gravitational Wave Detection with Pulsars
  - pulsar timing arrays
  - analysis techniques
  - current stochastic background limit
- Improving Our Detector
  - new instrumentation
  - new algorithms
  - more pulsars
- Summary
  - dramatic increases in PTA sensitivity expected over next several years

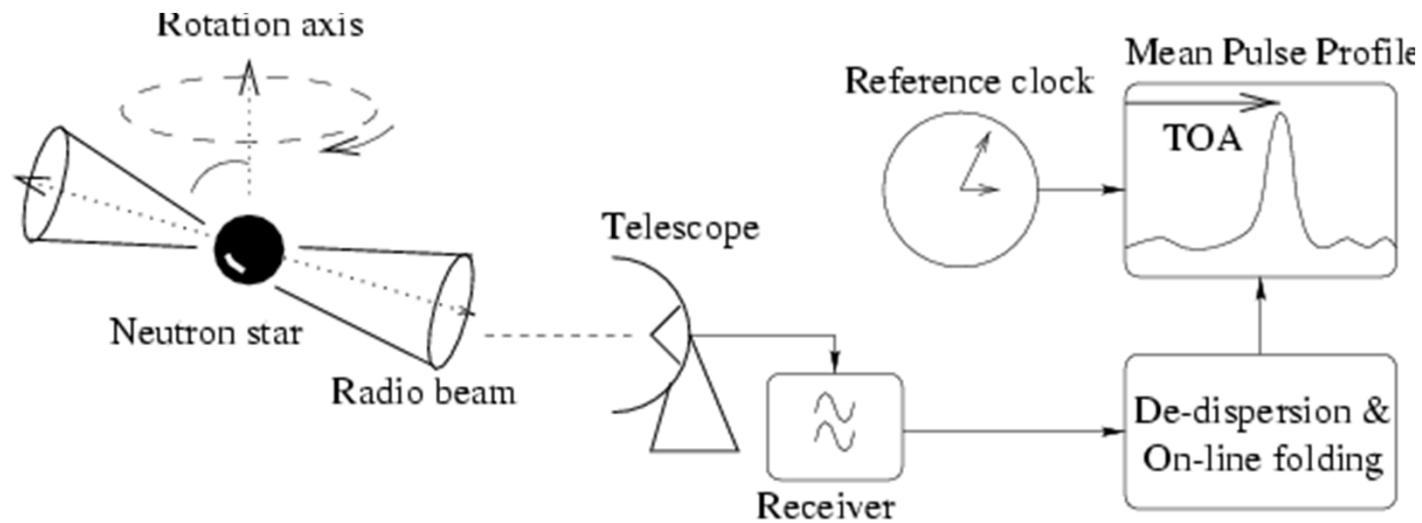
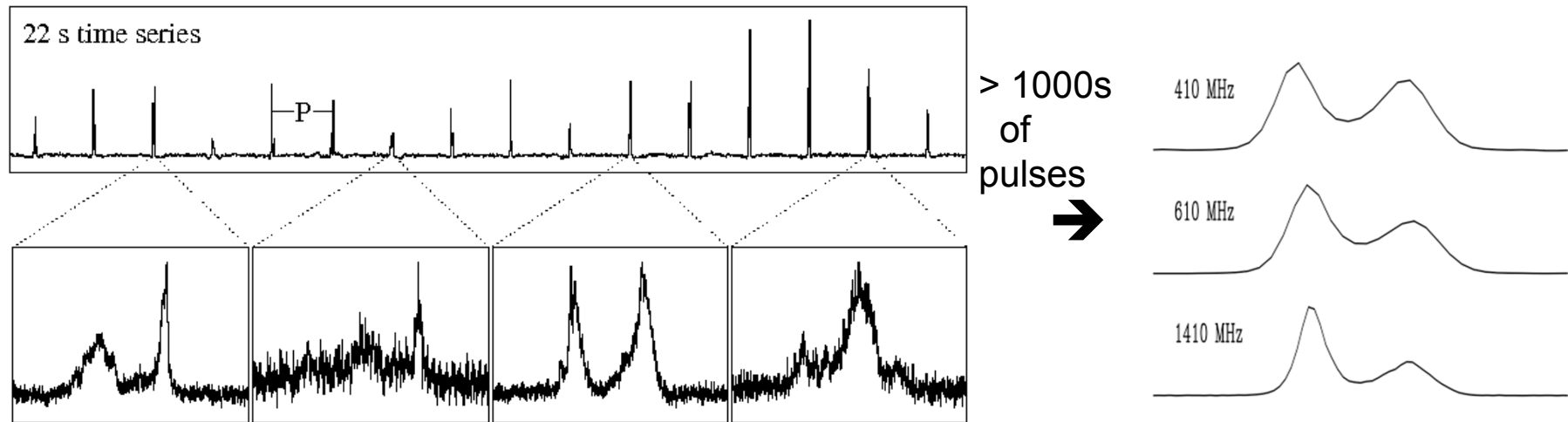
# Millisecond Pulsars

Nearly 200 known MSPs ( $P < 20$  ms) in our Galaxy, out of roughly 30,000 detectable. Galactic MSPs are local ( $d \sim \text{kly}$ ) and roughly isotropically distributed.



They are incredibly stable rotators, making them excellent fundamental physics laboratories.

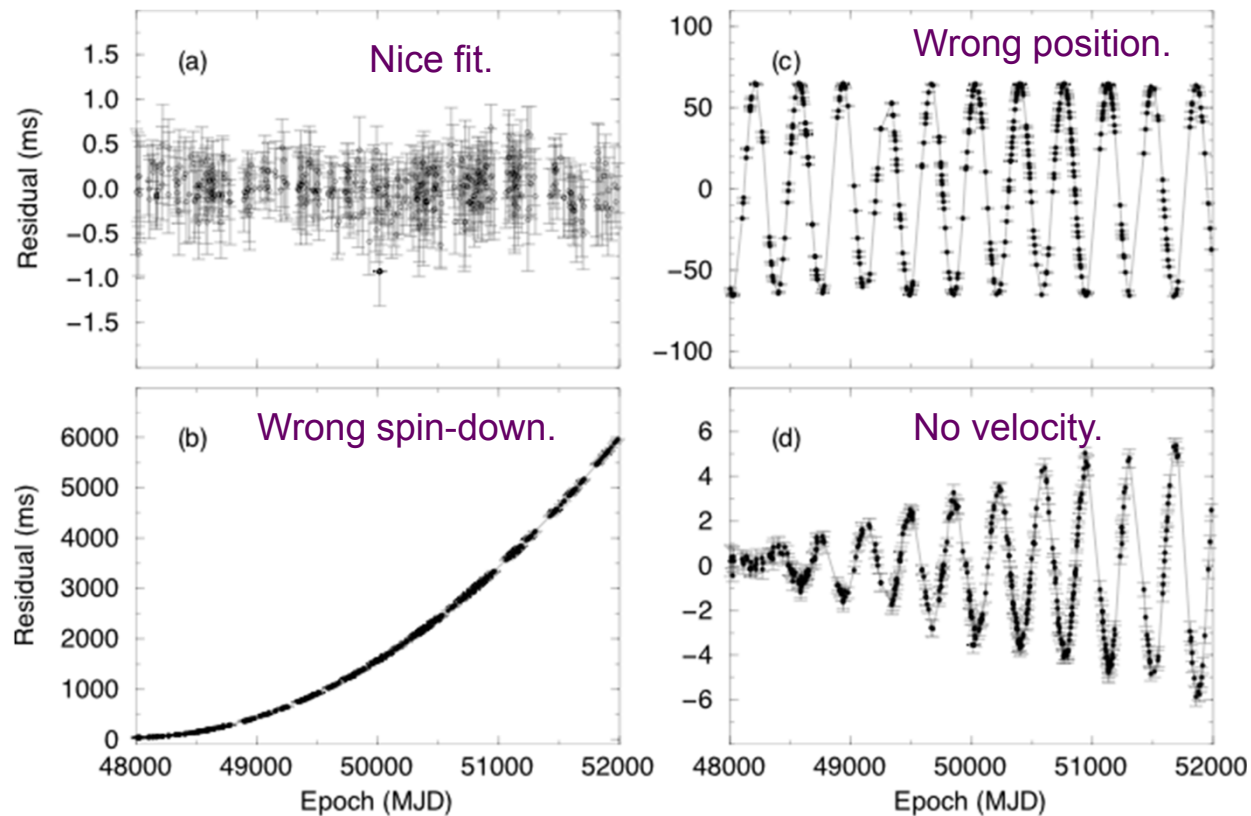
# Measuring a pulse time-of-arrival (TOA)



Lorimer & Kramer, 2005, "Handbook of Pulsar Astronomy"

# Obtaining a Timing Model and Residuals

Timing Residuals = Model – Measured TOAs

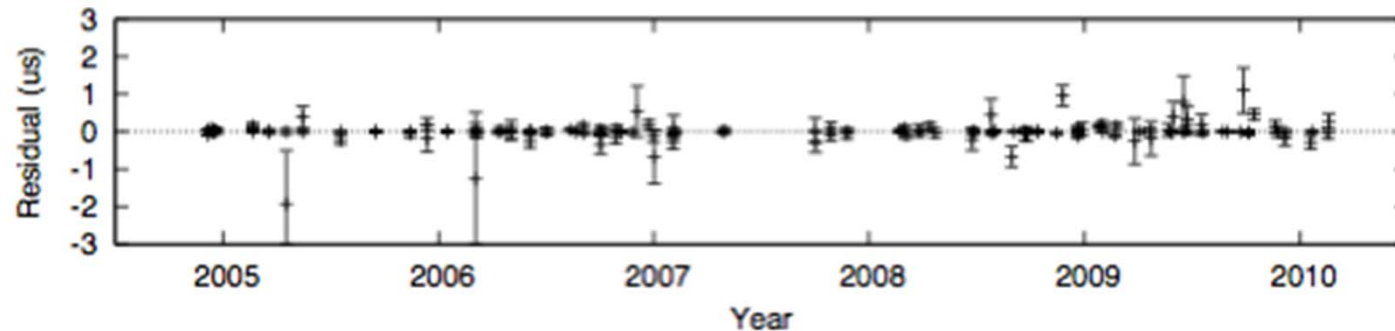




# Typical Residuals for a Millisecond Pulsar

J1713+0747

P = 4.57 ms



Demorest et al. 2013, ApJ, 762, 94

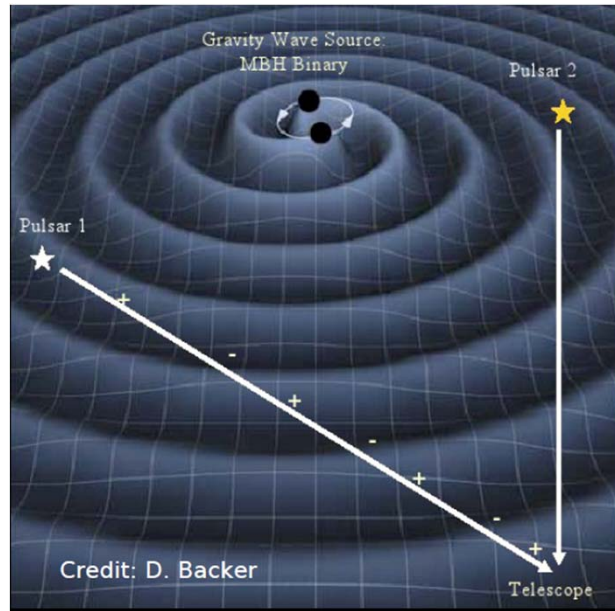
$\sigma_{\text{RMS}}$  = root-mean-square residual = 30 ns ( $6 \times 10^{-6} P$ )

after fitting for spin, astrometric, Keplerian, and post-Keplerian parameters  
and time-variable dispersion measure changes.

Today at 4:40 pm, the spin period of this pulsar is

4.57013631538007(4) milliseconds.

# Pulsars as GW Detectors



First discussed by Detweiler (1979, ApJ, 234,1100) and Sazhin (1978,SA,22,36).

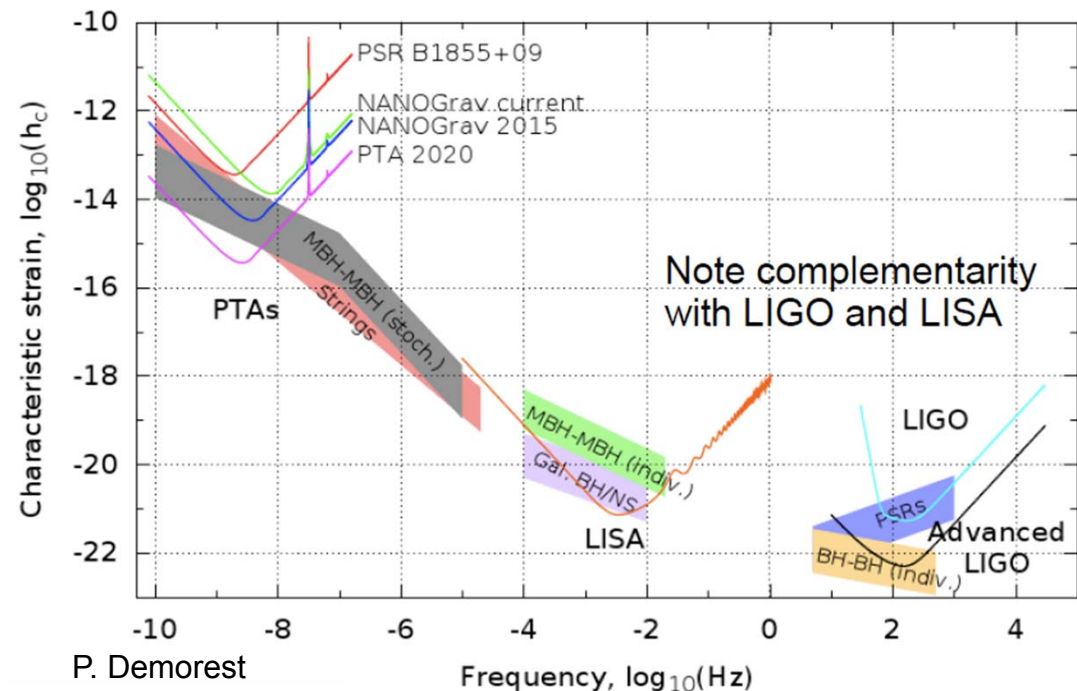
$f \sim 1/\text{weeks to } 1/\text{years } (10^{-6} - 10^{-9} \text{ Hz})$

$$\Delta t \propto n_i n_j \int_0^d h_{ij}(x, t) dr$$

$\Delta t \sim h/f$  and will have pulsar and Earth terms

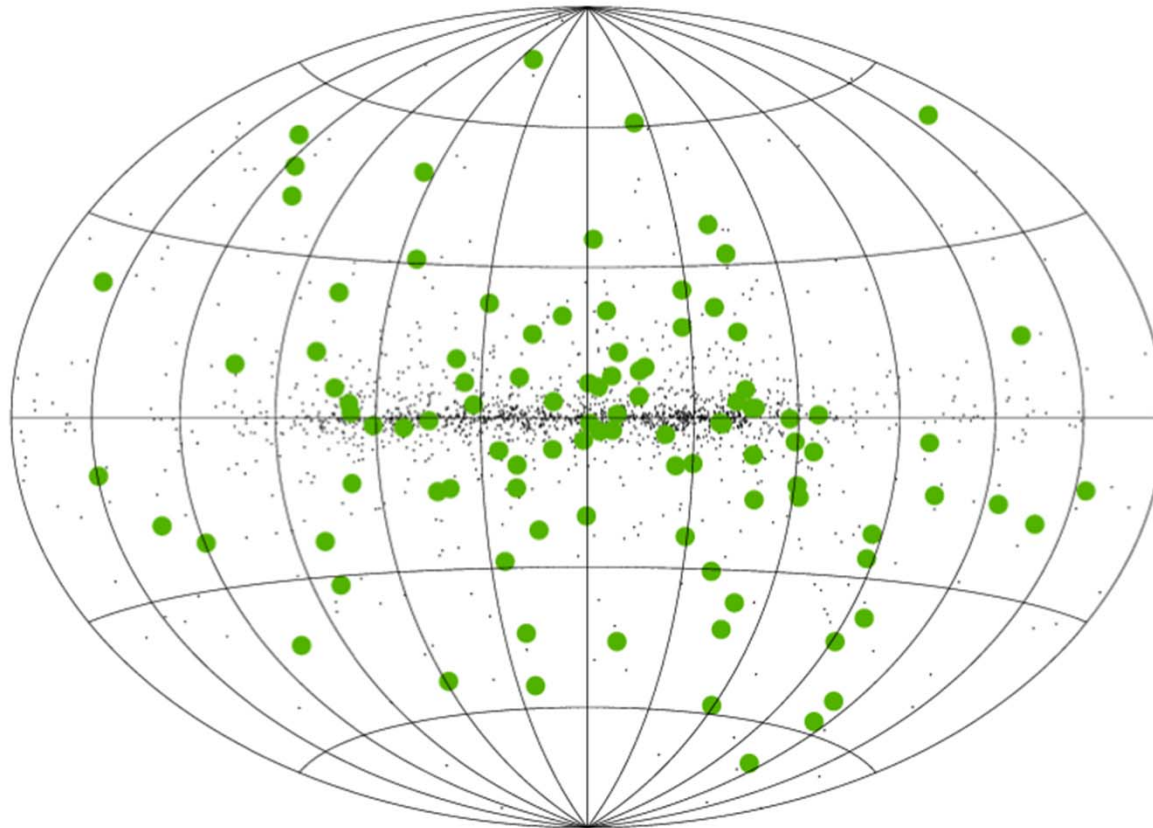
$h \sim \sigma_{\text{rms}}/T \sim 100 \text{ ns}/5 \text{ years} \sim 10^{-15}$

$\lambda_{\text{gw}} \sim 1\text{-}10 \text{ lyr}; D_{\text{psr}} \sim 1000 \text{ lyr}$



# Pulsar Timing Array

A network of pulsars that can be used to measure various effects that produce correlations in the arrival times of pulses from the members of the array.



First proposed by Foster and Backer (1990).



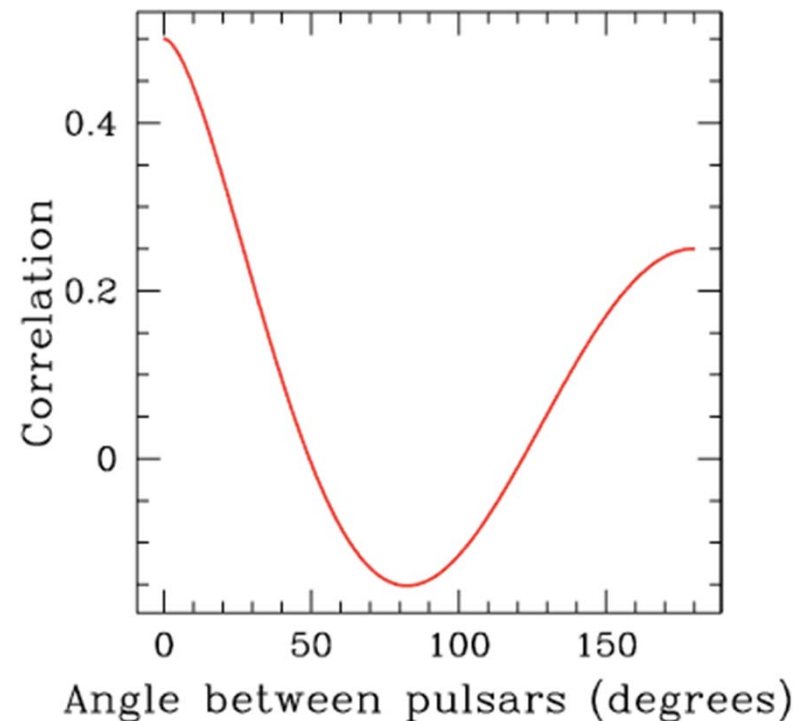
# Stochastic Background Limits from a PTA

Expected correlation of residuals for pairs of pulsars versus angular separation on sky. “Pulsar” terms uncorrelated. “Earth” terms correlated.

$$C_{y,ij}^{(ab)} = E \{y_a(t_i)y_b(t_j)\} :$$

$$= C_y(t_i - t_j)\zeta(\theta_{ab})$$

Clock errors monopole.  
Ephemeris errors dipole.  
GWs quadrupole.



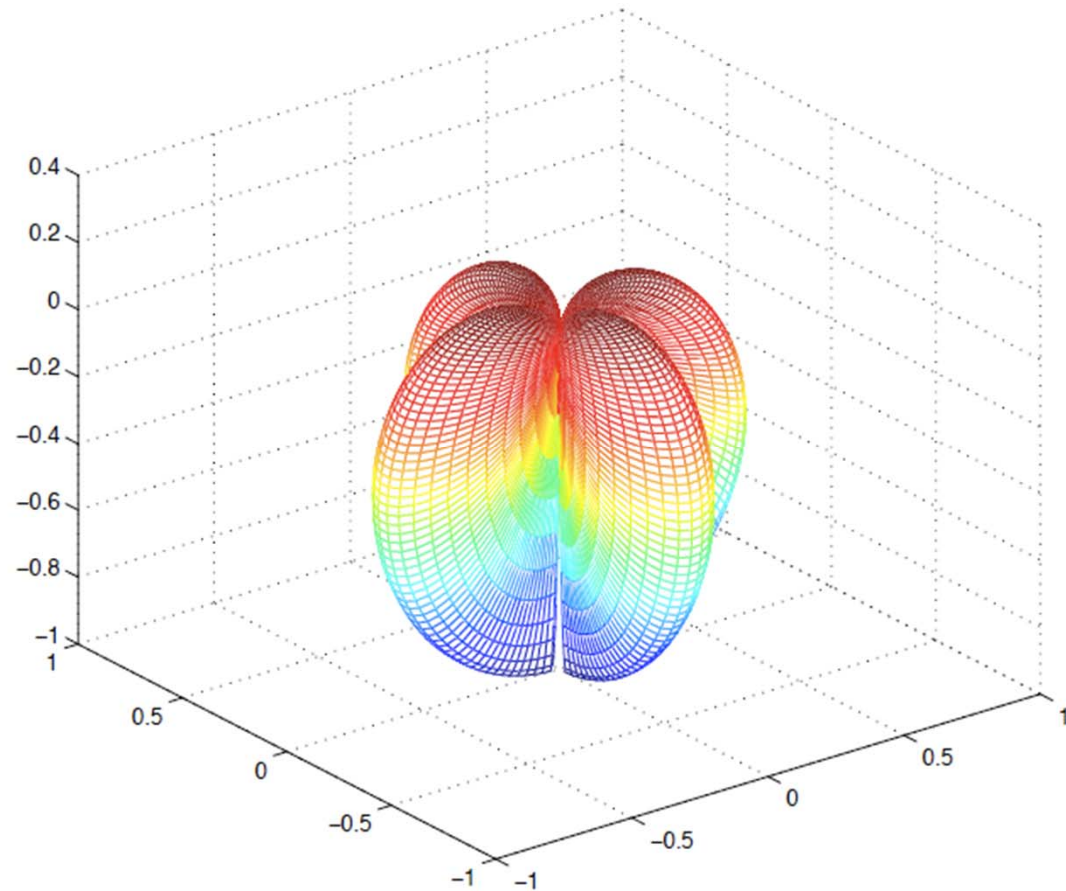
Hellings & Downs, 1983, ApJ, 265, L39

# Can use a PTA for single sources too

We can of course search for single sources too!

$$\begin{aligned} z(t, \hat{z}) &\equiv \frac{\nu_0 - \nu(t)}{\nu_0} \\ &= \frac{\alpha^2 - \beta^2}{2(1 + \gamma)} (h_+^p - h_+^e) \\ &\quad + \frac{\alpha\beta}{1 + \gamma} (h_\times^p - h_\times^e) \end{aligned}$$

Anholm et al. 2009, PhRvD, 79, 8



Antenna response for the pulsar-Earth system.

# North American Nanohertz Observatory for GWs



11 U.S. and 2 Canadian Institutions

GWADW2013

[nanograv.org](http://nanograv.org)

21 May 2013



# Current Status



37 MSPs being timed with Arecibo and the GBT.  
 2-3 frequencies at each telescope.  
 Roughly bi-monthly observations.  
 First all-NANOGrav paper on 17 pulsars published.

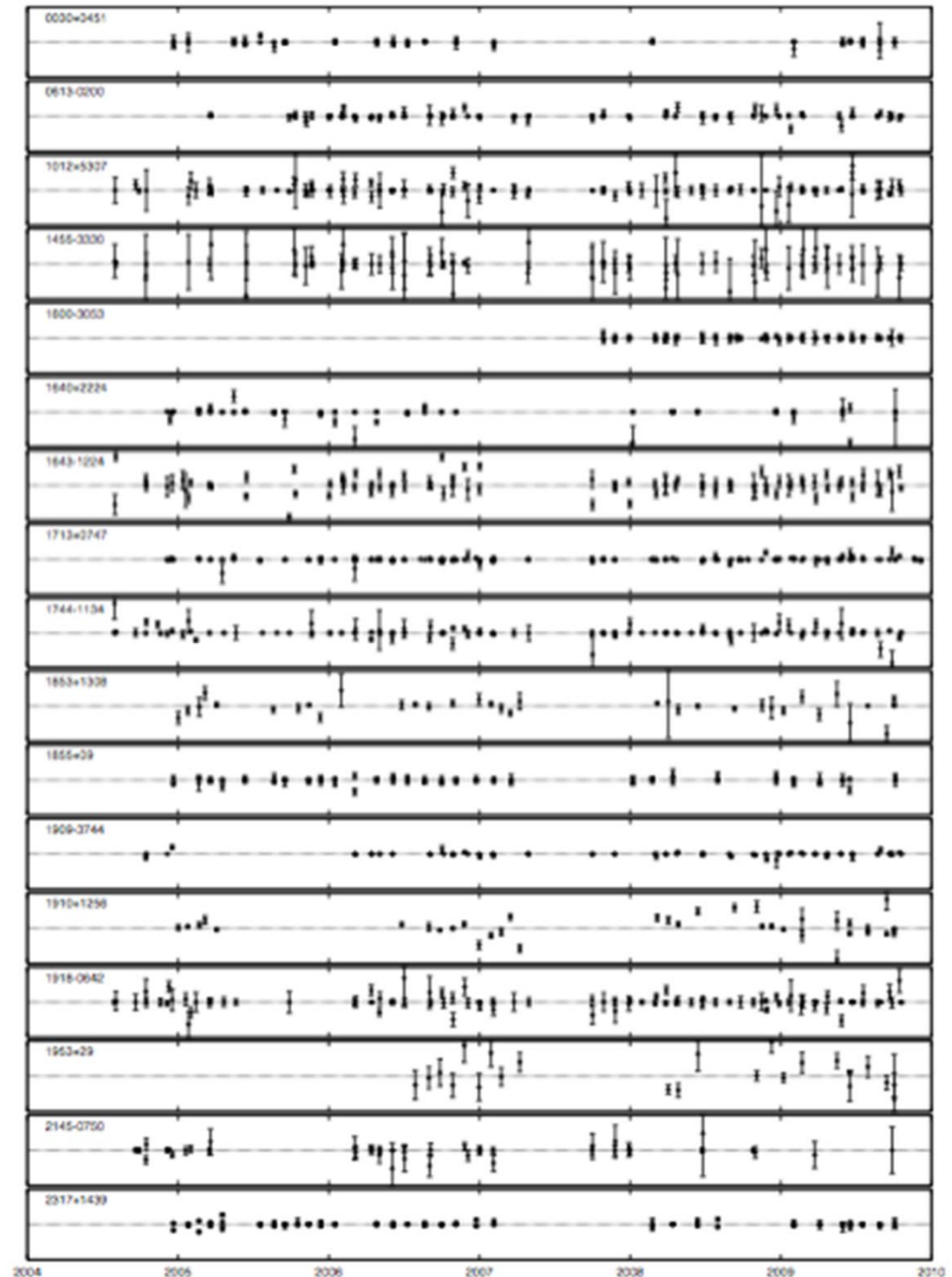
OVERVIEW AND RESULTS FROM TIMING MODEL FITS.

Source	# of TOAs <sup>a</sup>	# of parameters			RMS ( $\mu$ s)	Fit $\chi^2$	Epoch-averaged RMS ( $\mu$ s) <sup>c</sup>		
		DM	Profile	Other <sup>b</sup>			Low-band <sup>d</sup>	High-band	Combined
J0030+0451	545	20	26	7	0.604	1.44	0.019	0.328	0.148
J0613-0200	1113	34	45	12	0.781	1.21	0.021	0.519	0.178
J1012+5307	1678	52	53	14	1.327	1.40	0.192	0.345	0.276
J1455-3330	1100	37	53	12	4.010	1.01	0.363	1.080	0.787
J1600-3053	625	21	31	14	1.293	1.45	0.233	0.141	0.163
J1640+2224	631	23	26	12	0.562	4.36	0.057	0.601	0.409
J1643-1224	1266	40	48	13	2.892	2.78	0.589	1.880	1.467
J1713+0747	2368	50	111	15	0.106	1.48	0.092	0.025	0.030
J1744-1134	1617	54	49	7	0.617	3.58	0.139	0.229	0.198
J1853+1308	497	0	34	12	1.028	1.16	0.271	0.096	0.255
B1855+09	702	29	21	14	0.395	2.19	0.277	0.101	0.111
J1909-3744	1001	31	37	14	0.181	1.95	0.011	0.047	0.038
J1910+1256	525	0	34	14	1.394	2.09	0.712	0.684	0.708
J1918-0642	1306	49	37	12	1.271	1.21	0.129	0.211	0.203
B1953+29	208	0	27	12	3.981	0.98	1.879	0.543	1.437
J2145-0750	675	20	37	12	1.252	1.97	0.068	0.494	0.202
J2317+1439	458	30	12	15	0.496	3.03	0.373	0.150	0.251

# Residuals

RMS residuals for 17 NANOGrav pulsars range from 30 ns to 1.5 microseconds over timespans of  $\sim 5$  years. Most of these residuals are consistent with white noise, but two have significant red noise components.

We must (most likely) reduce RMS residuals to  $\sim 100$  ns for all of these (and more!) MSPs for gravitational wave detection within the next  $\sim 10$  years.



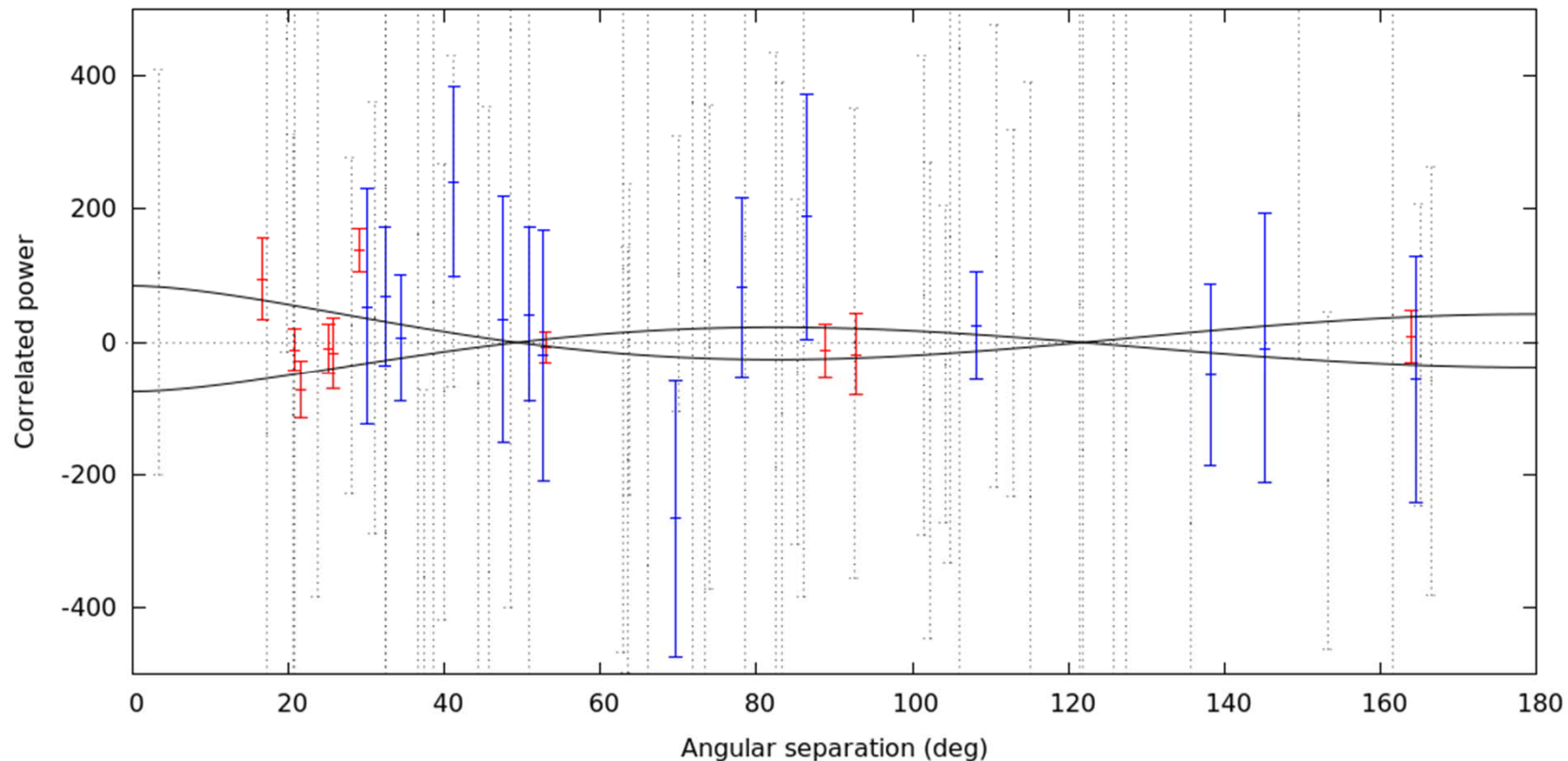


# Limit from Correlation Analysis

$$h_c < 7 \times 10^{-15} \text{ (f=1 yr}^{-1}\text{)}$$



$$\rho_{ab} = \frac{\sum_{ijkl} r_i^{(a)} (C^{tot(a)})_{ij}^{-1} C_{jk}^{GW(a,b)} (C^{tot(b)})_{kl}^{-1} r_l^{(b)}}{\sum_{ijkl} (C^{tot(a)})_{ij}^{-1} C_{jk}^{GW(a,b)} (C^{tot(b)})_{kl}^{-1} C_{il}^{GW(a,b)}}$$

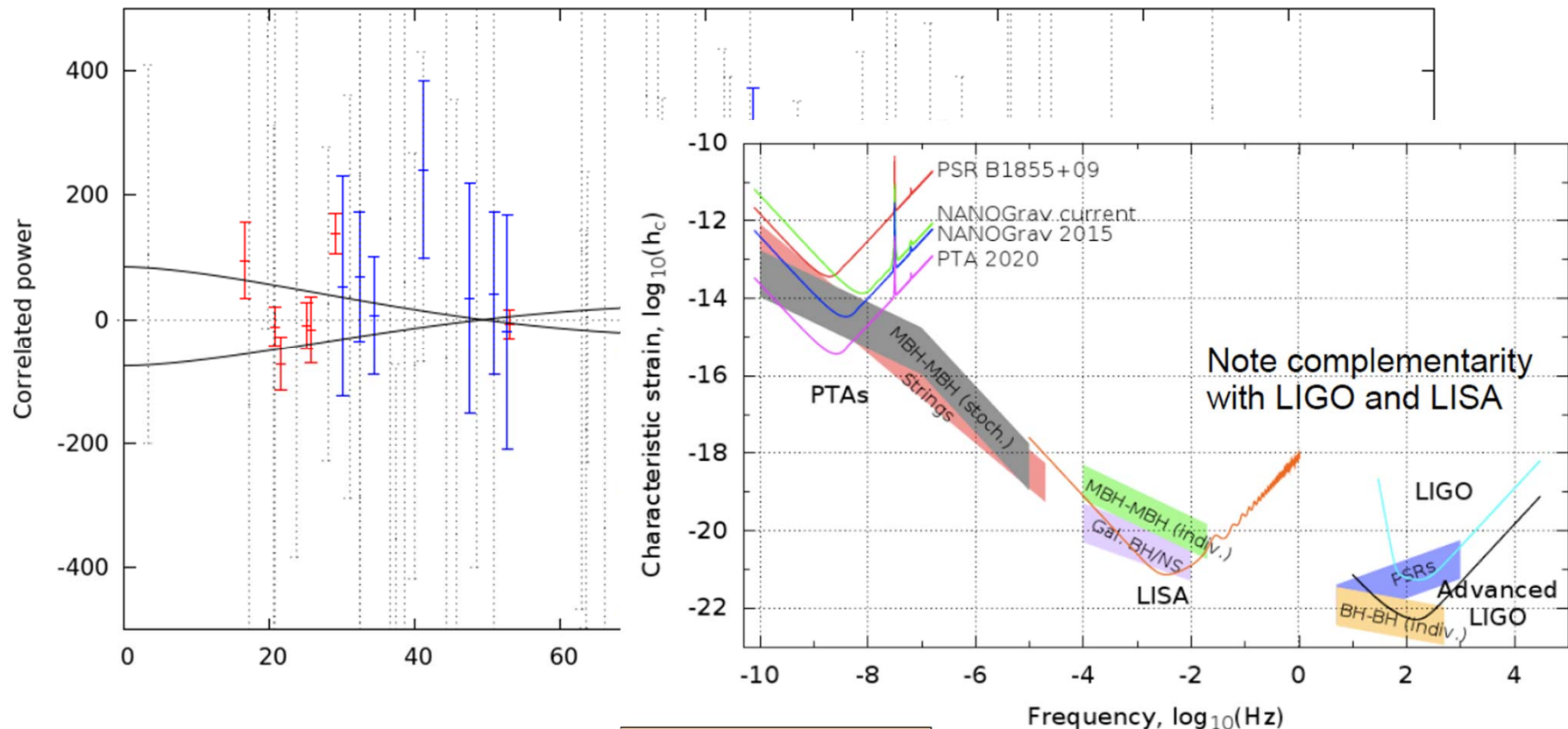


# Limit from Correlation Analysis

$$h_c < 7 \times 10^{-15} \text{ (f=1 yr}^{-1}\text{)}$$

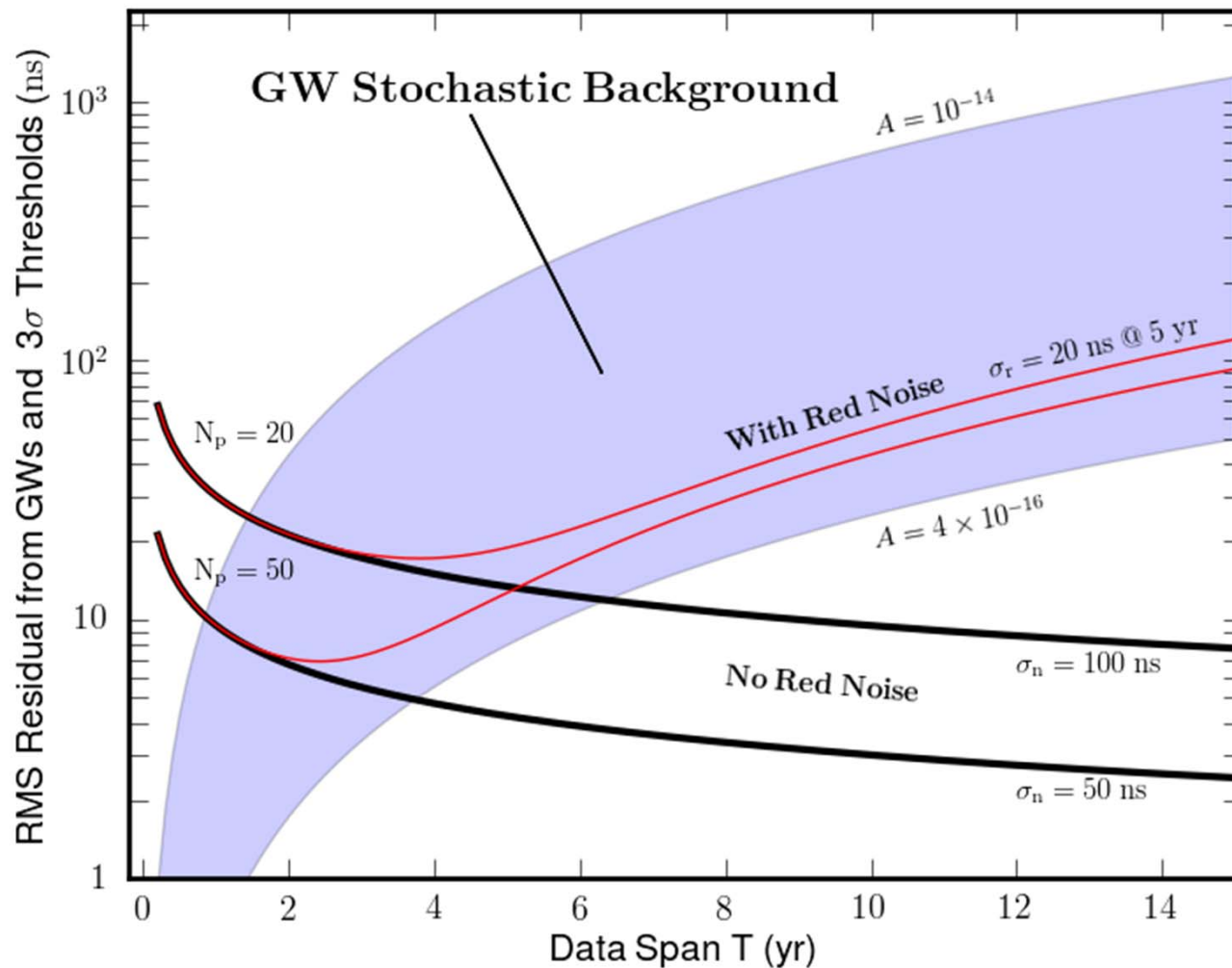


$$\rho_{ab} = \frac{\sum_{ijkl} r_i^{(a)} (C^{tot(a)})_{ij}^{-1} C_{jk}^{GW(a,b)} (C^{tot(b)})_{kl}^{-1} r_l^{(b)}}{\sum_{ijkl} (C^{tot(a)})_{ij}^{-1} C_{jk}^{GW(a,b)} (C^{tot(b)})_{kl}^{-1} C_{il}^{GW(a,b)}}$$



How do we improve the sensitivity of our detector?

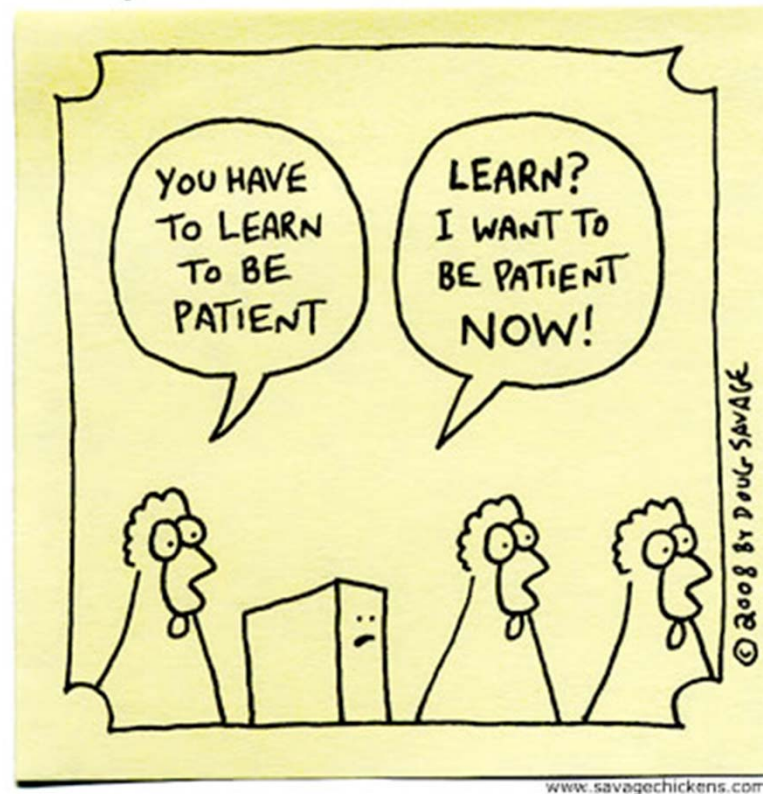
# Projected Sensitivity



J. Cordes

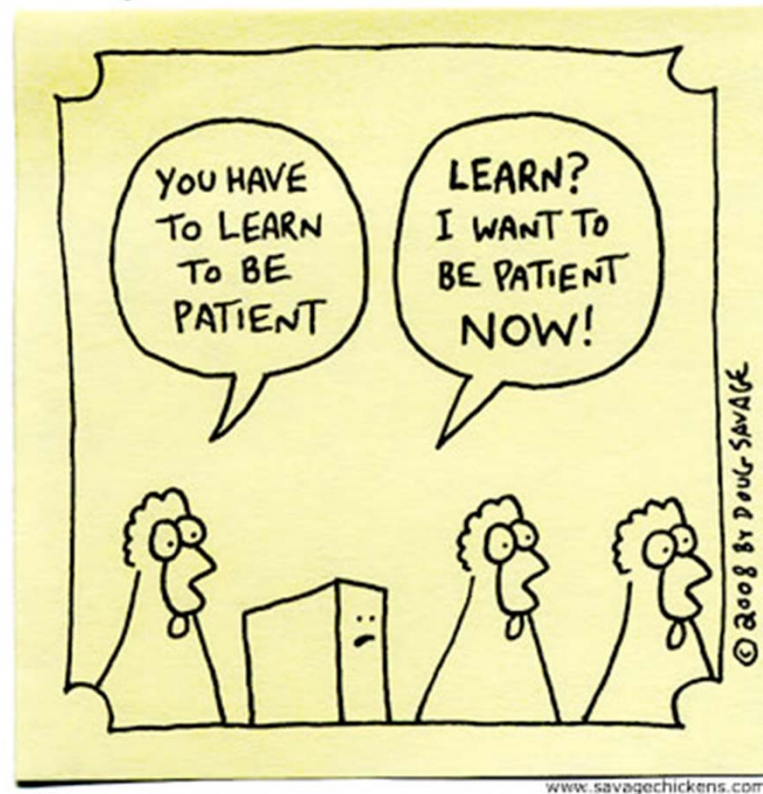
In the strong source regime, sensitivity scales as  $T^{1/2}$ ,  $N_p^{1/2}$ , and  $N_{\text{TOA}}^{1/2}$ . GWs grow as  $T^{5/3}$ . Assumes similar spectrum for GWs ( $f^{-13/3}$ ) and red noise ( $f^{-5}$ ).

If we are white noise dominated, we could just wait

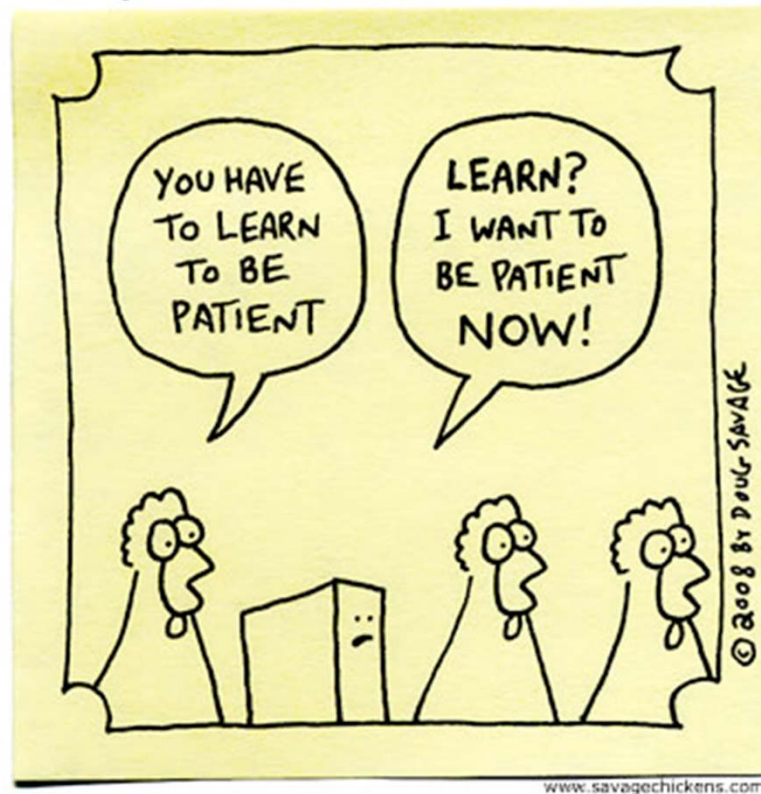




If we are white noise dominated, we could just wait  
..but we will get there faster with more precise TOA  
measurements and better algorithms.



If we are red noise dominated (or if red noise is ubiquitous), we may *need* to add pulsars to the array.



Based on studies of slow pulsars, it is likely that red noise due to rotational instabilities exists at some level for all MSPs.

How do we improve the sensitivity of our detector?

- 1) More precise TOA measurements
- 2) Better algorithms for timing and detection
- 3) More pulsars in the array

# 1) More precise TOA measurements

Minimum detectable strain proportional to average RMS residual ( $h \sim \sigma_{\text{RMS}}/T$  in simple model).

$$\sigma_{\text{RMS}} \sim \sigma_{\text{TOA}} \sim \frac{w}{\text{SNR}} \propto \frac{w}{S_{\text{PSR}}} \frac{T_{\text{sys}}}{A} \frac{1}{\sqrt{BT}}$$

Therefore, we want *bright pulsars* with *narrow pulses* observed with *sensitive receivers* with *large telescopes* over *large bandwidths* and with *long integration times*.

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Therefore, we want *bright pulsars* with *narrow pulses* observed with **sensitive receivers** with **large telescopes** over *large bandwidths* and with **long integration times**.

105 m  
Green Bank Telescope



We are steadily increasing our amount of observing time on the two largest telescopes in the world, equipped with sensitive receivers.

305 m  
Arecibo Telescope





# 1) More precise TOA measurements

Minimum detectable strain proportional to average RMS residual ( $h \sim \sigma_{\text{RMS}}/T$  in simple model).

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105 m  
Green Bank Telescope



New instrumentation on both telescopes is dramatically increasing our available bandwidth. But we must preserve narrow pulsar shapes over those bandwidths!

305 m  
Arecibo Telescope



# 1) More precise TOA measurements

Frequency-dependent refractive index  
leads to frequency-dependent time delay

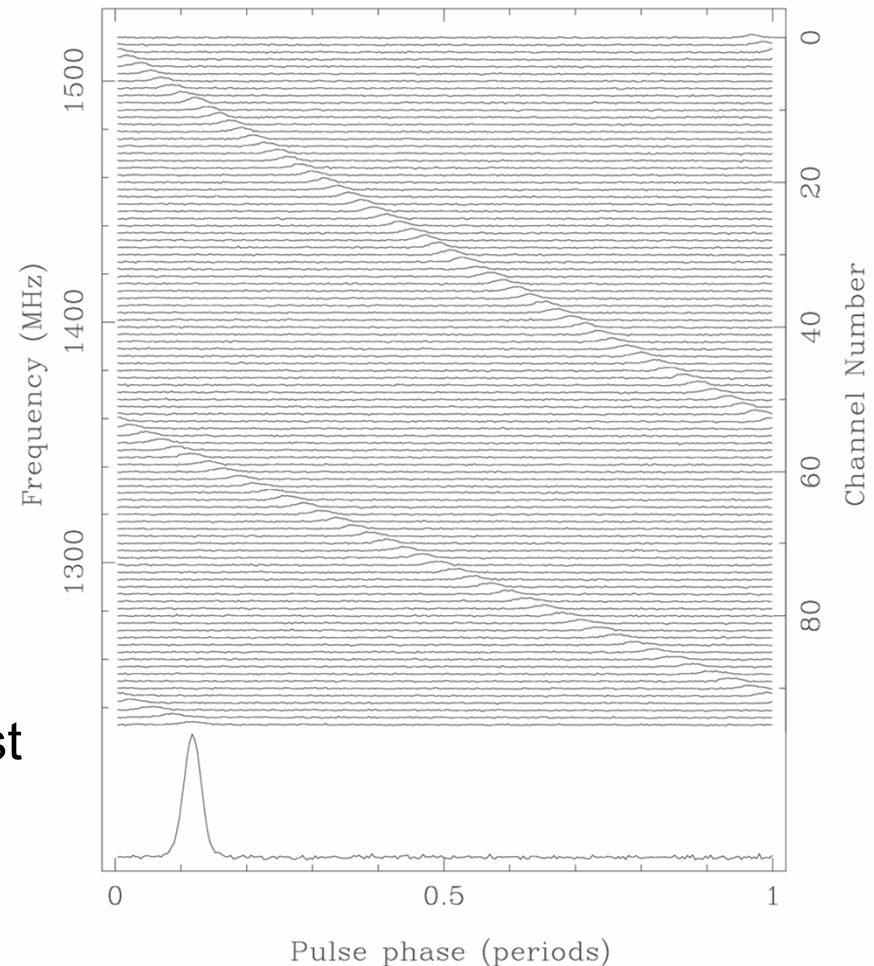
$$\Delta t \simeq 4.15 \times 10^6 \text{ ms} \times (f_1^{-2} - f_2^{-2}) \times \text{DM}$$

where  $\text{DM} = \int_0^d n_e dl$

DMs range from roughly 3 to 100 pc cm<sup>-3</sup>  
for delays of 1 to 30 ms over a 100 MHz  
bandwidth at 1.4 GHz.

To preserve narrow pulse shapes, we must  
*coherently dedisperse*, or convolve raw  
signal voltages with inverse of interstellar  
medium transfer function.

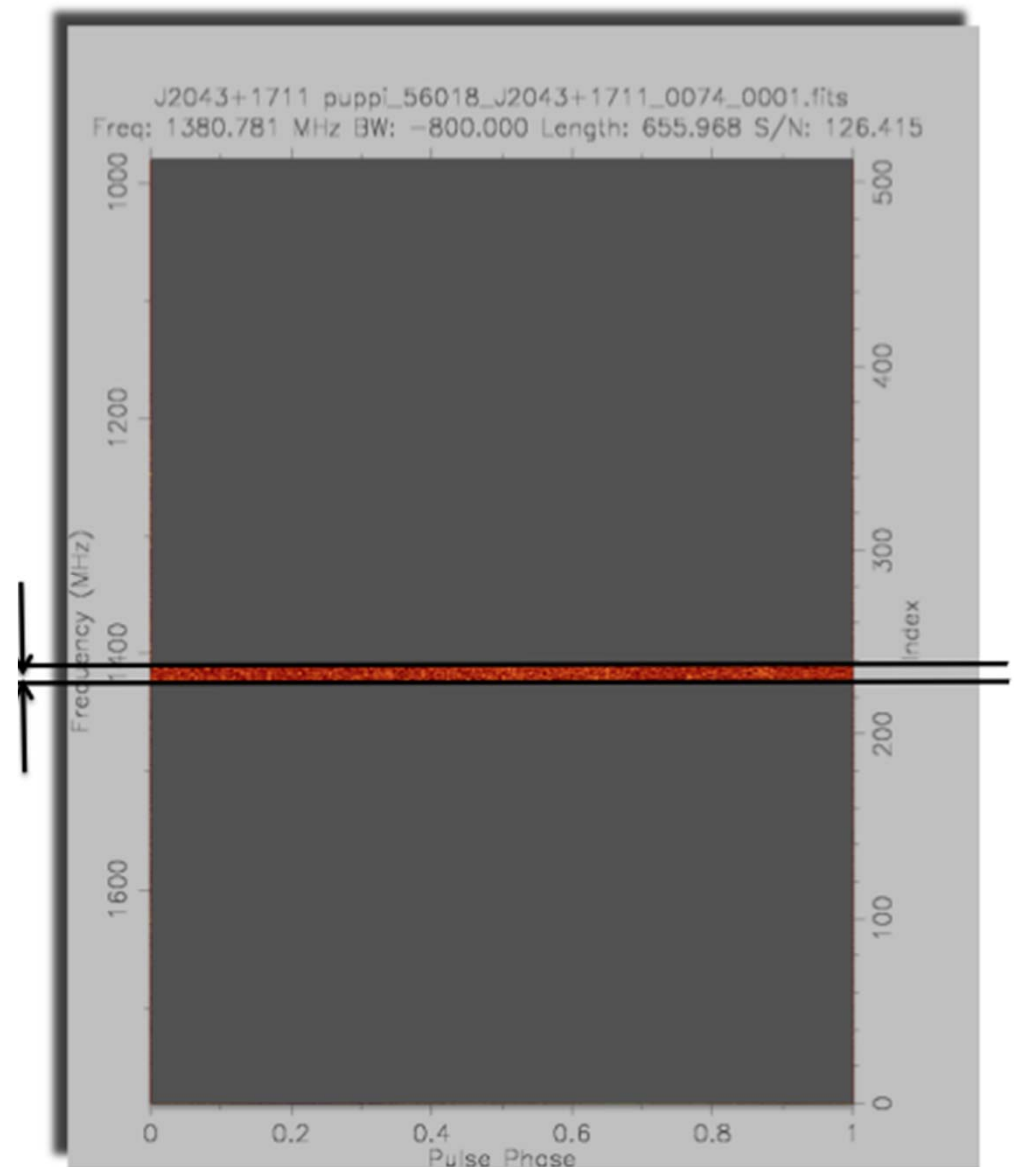
Computationally expensive!!



# 1) More precise TOA measurements

$$\sigma_{\text{TOA}} \sim \frac{w}{\text{SNR}} \propto \frac{w}{S_{\text{PSR}}} \frac{T_{\text{sys}}}{A} \frac{1}{\sqrt{BT}}$$

Arecibo 1998-2006:  
10 MHz bandwidth

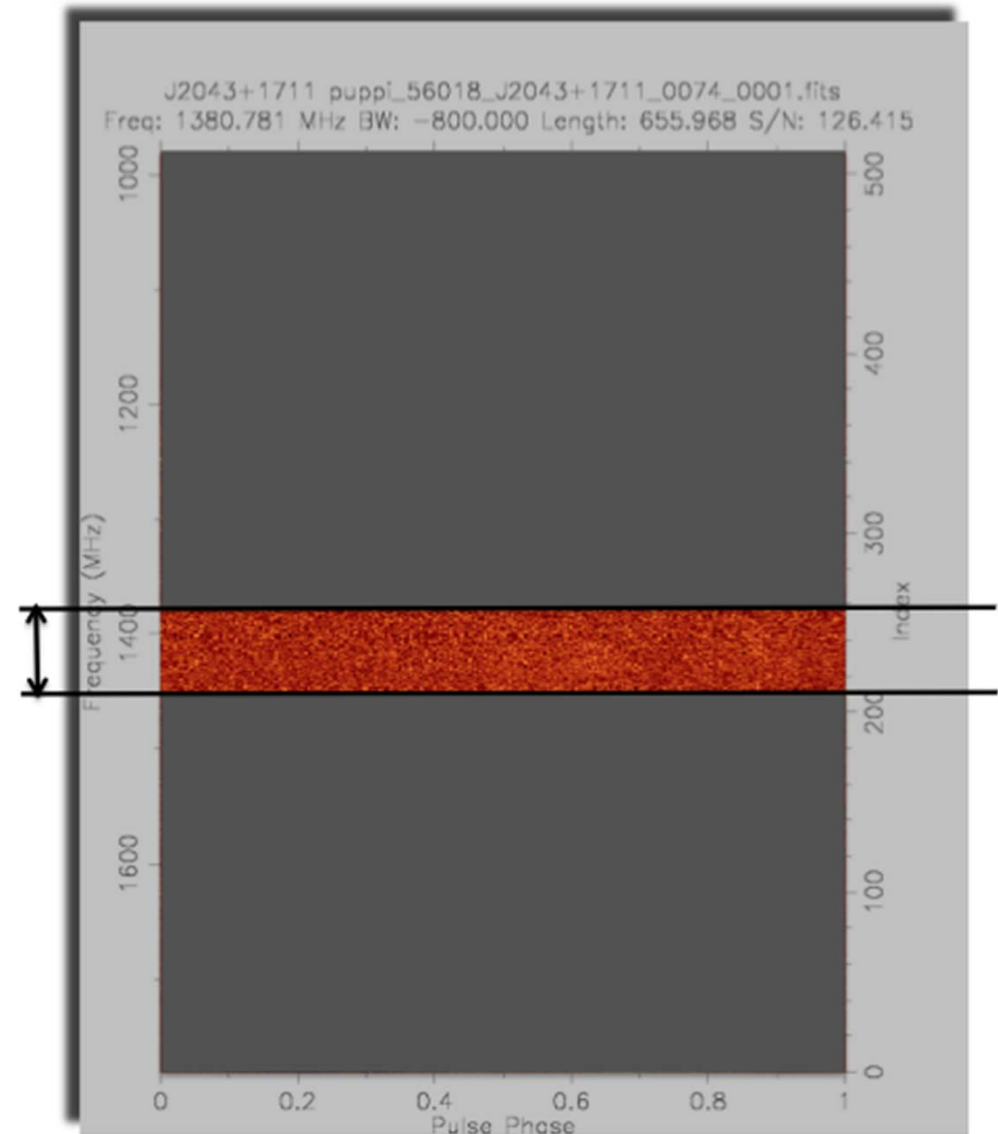


# 1) More precise TOA measurements

$$\sigma_{\text{TOA}} \sim \frac{w}{\text{SNR}} \propto \frac{w}{S_{\text{PSR}}} \frac{T_{\text{sys}}}{A} \frac{1}{\sqrt{BT}}$$

Arecibo 2005-2012:  
64 MHz bandwidth  
available with ASP  
backend.

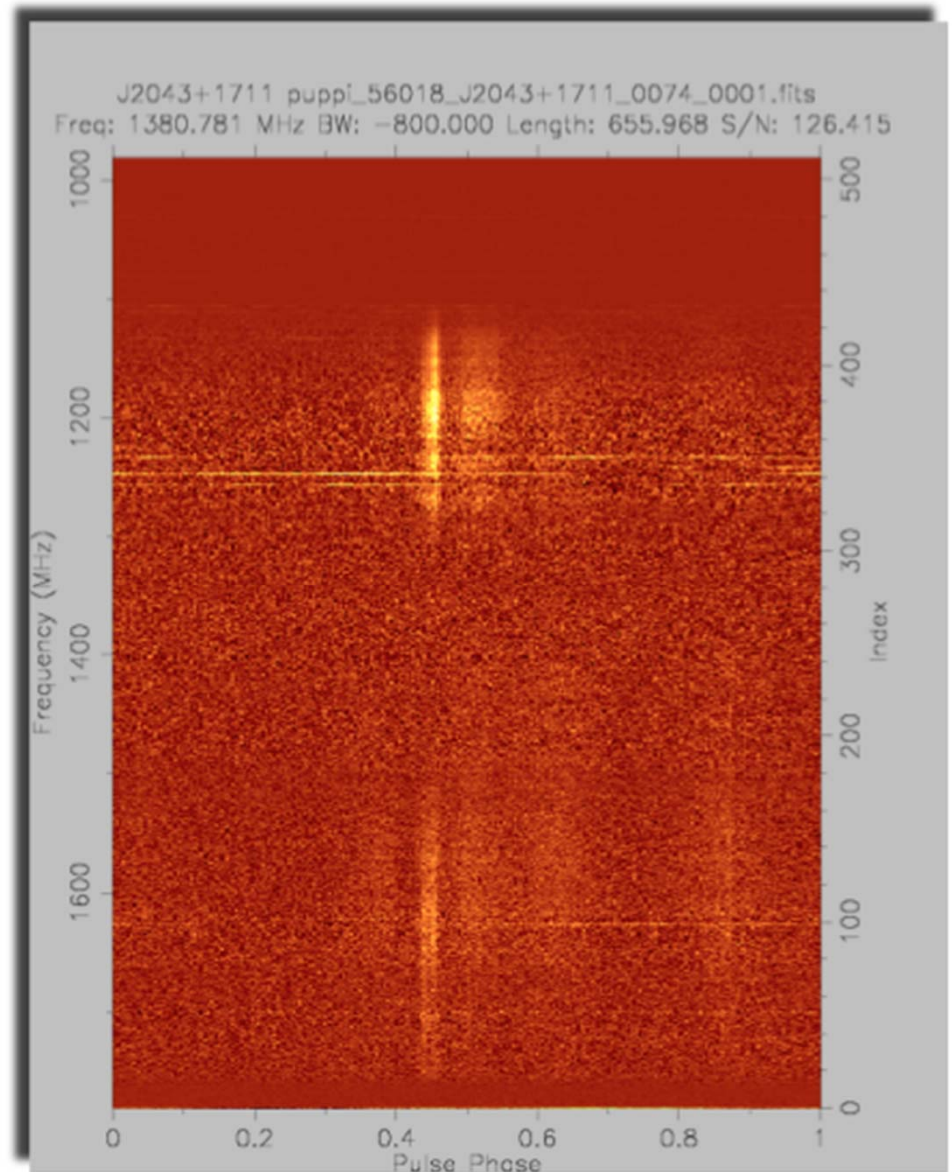
Used for recent upper  
limit paper.



# 1) More precise TOA measurements

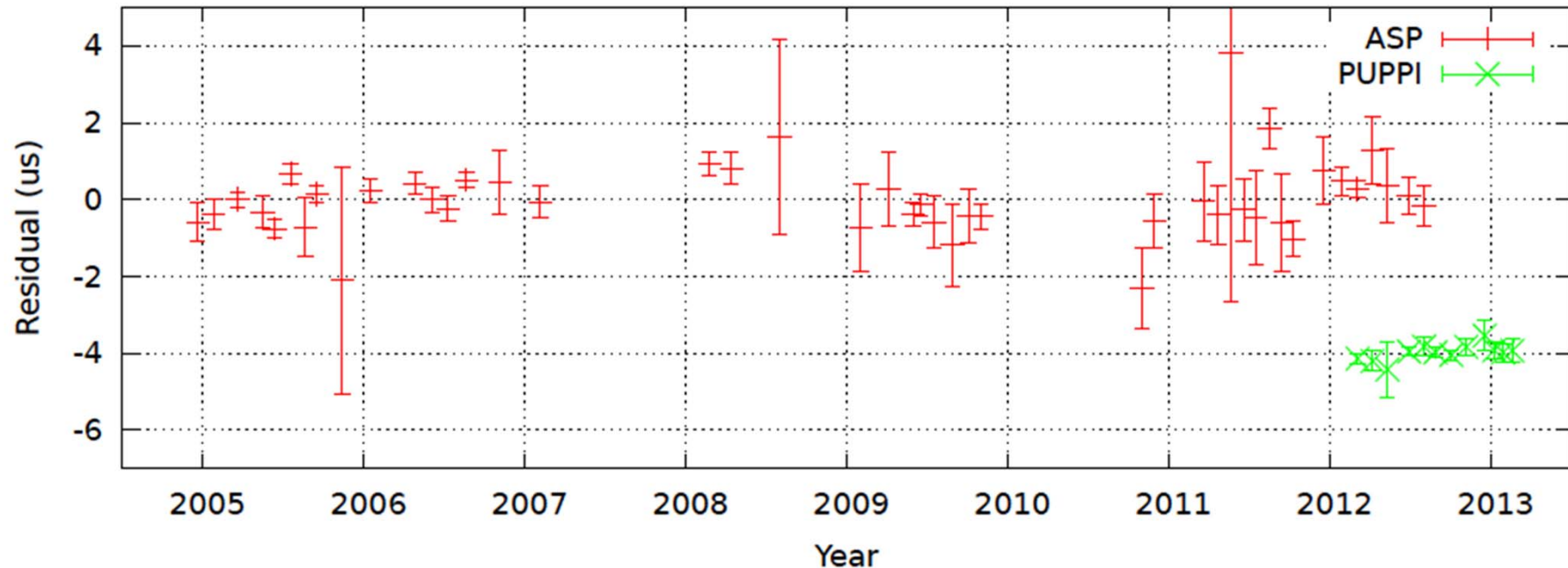
$$\sigma_{\text{TOA}} \sim \frac{w}{\text{SNR}} \propto \frac{w}{S_{\text{PSR}}} \frac{T_{\text{sys}}}{A} \frac{1}{\sqrt{BT}}$$

Arecibo 2012-present:  
800 MHz bandwidth  
available with new  
PUPPI backend. Made  
possible with cheap  
FPGA hardware.



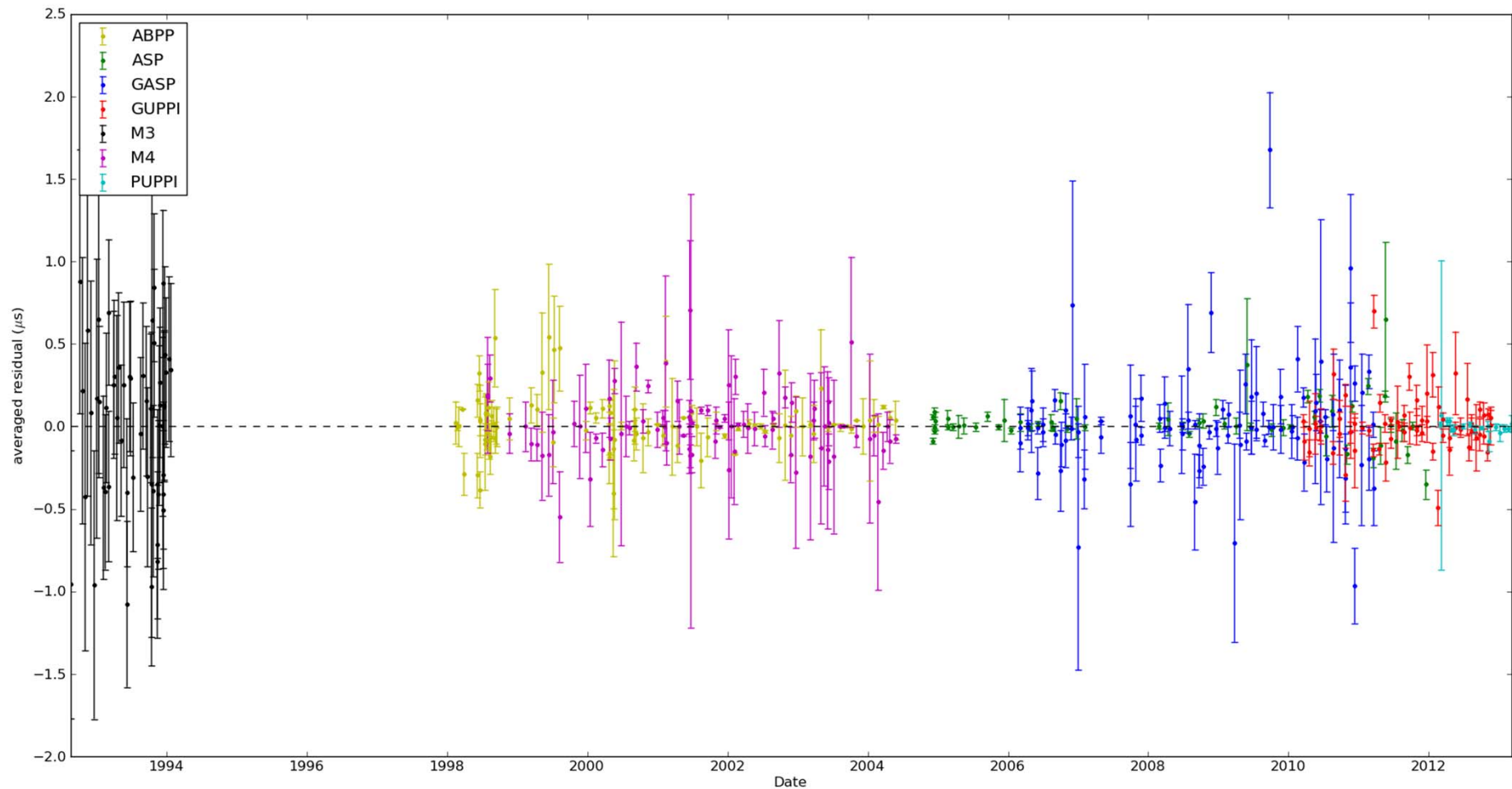


# 1) More precise TOA measurements



Additional bandwidth has resulted in RMS residuals a factor of three smaller, as expected.

# 1) More precise TOA measurements



Zhu et al. in preparation

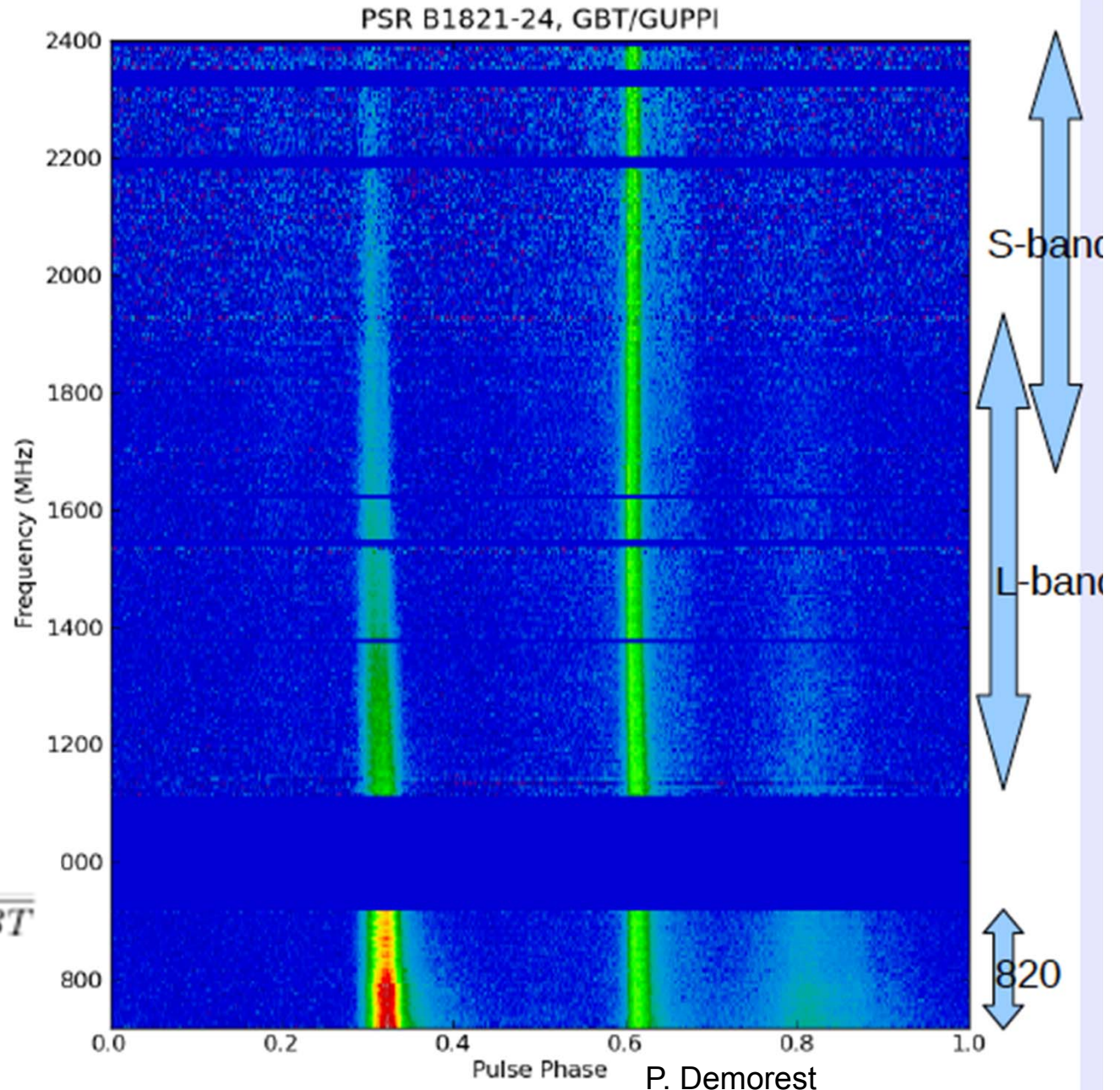
Additional bandwidth has resulted in RMS residuals a factor of three smaller, as expected (for the most part!)

# 1) More precise TOA measurements

Super-wideband receiver in development for both AO and GBT, covering 700 MHz – 3 GHz.

Challenge is getting low system temperature.

$$\sigma_{\text{TOA}} \sim \frac{w}{\text{SNR}} \propto \frac{w}{S_{\text{PSR}}} \frac{T_{\text{sys}}}{A} \frac{1}{\sqrt{BT}}$$

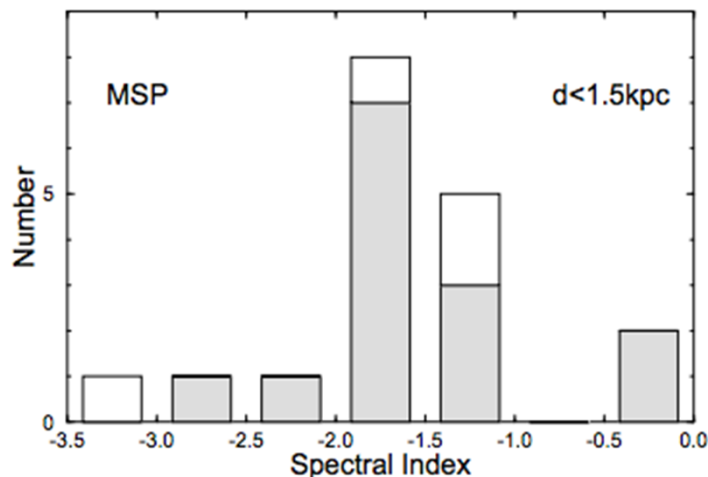


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Therefore, we want **bright pulsars** with **narrow pulses** observed with *sensitive receivers* with *large telescopes* over *large bandwidths* and with *long integration times*

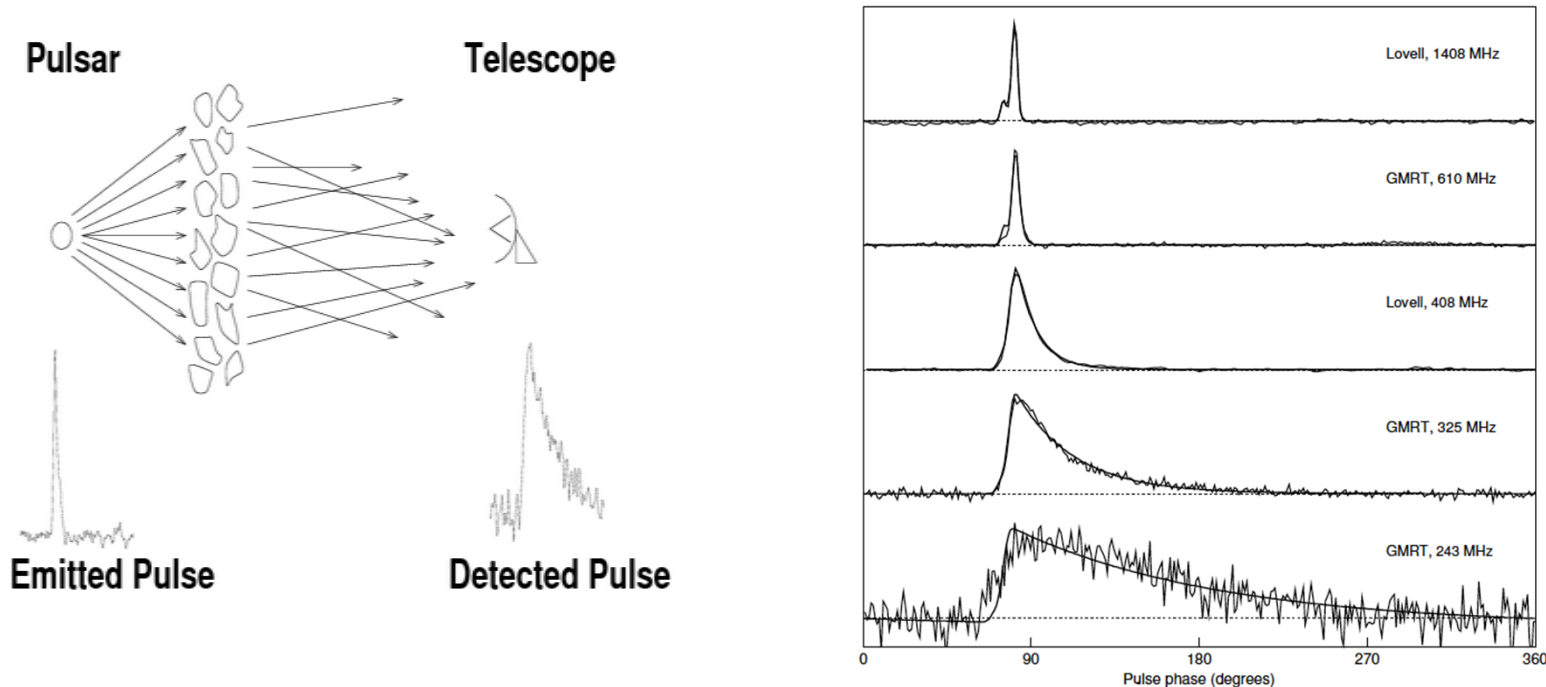


We want to observe at low frequencies where pulsars are brightest.

$$S \propto \text{freq}^{-1.6}$$

Kramer et al. 1998, ApJ, 501, 270,

# 1) More precise TOA measurements



Lorimer, Living Reviews in Relativity

From Lorimer & Kramer, 2005, "Handbook of Pulsar Astronomy"

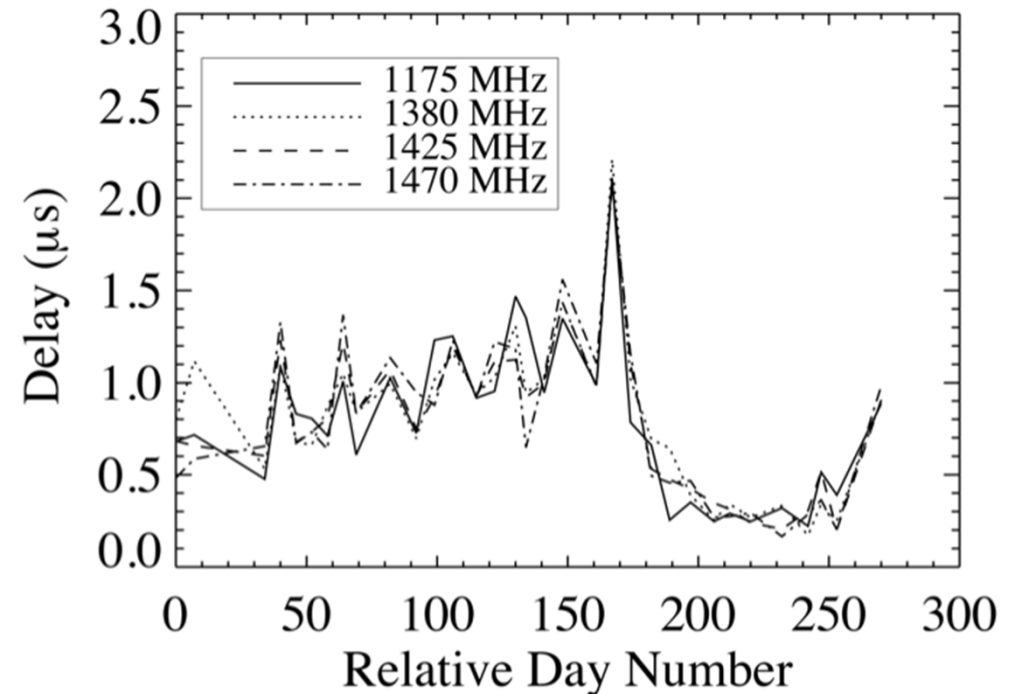
Pulsar signals are scattered by the interstellar medium with  $\tau_s \propto \text{freq}^{-4}$ , requiring either accepting fainter pulsars at high frequencies or the development of correction algorithms for scattering at low frequencies.



## 2) Better algorithms for timing and detection

Pulsar signals are also delayed by amounts greater than or comparable to GW perturbations.

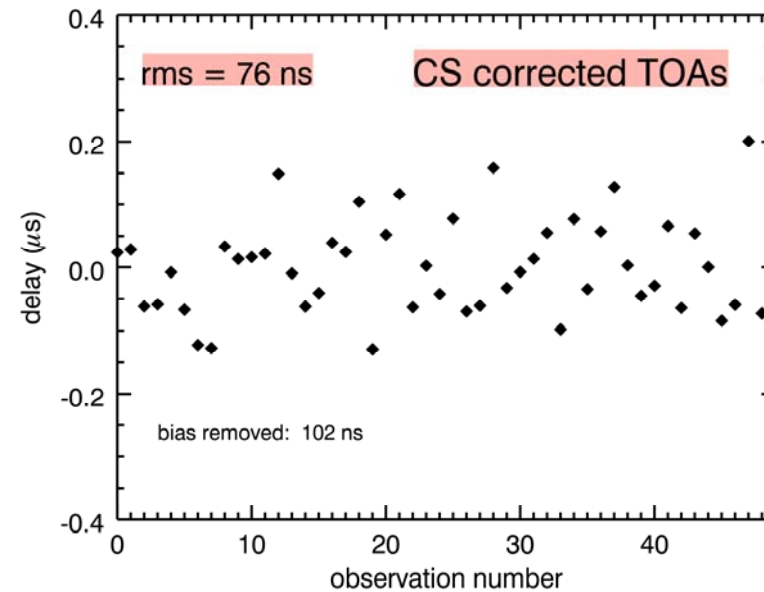
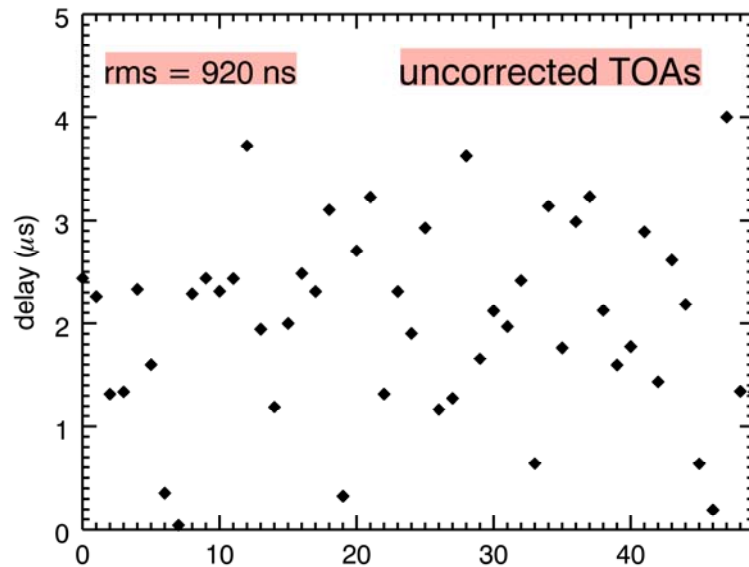
We are experimenting with correction techniques that preserve the phase information of the pulsar signal to recover the delay. This scheme requires baseband data and so we are working on GPU-based implementations (Jones et al. in preparation).



Hemberger & Stinebring, 2008, ApJ, 674, L37



## 2) Better algorithms for timing and detection



Palliyaguru et al. in preparation

Only works for a pulsed signals.

1) Take baseband data.

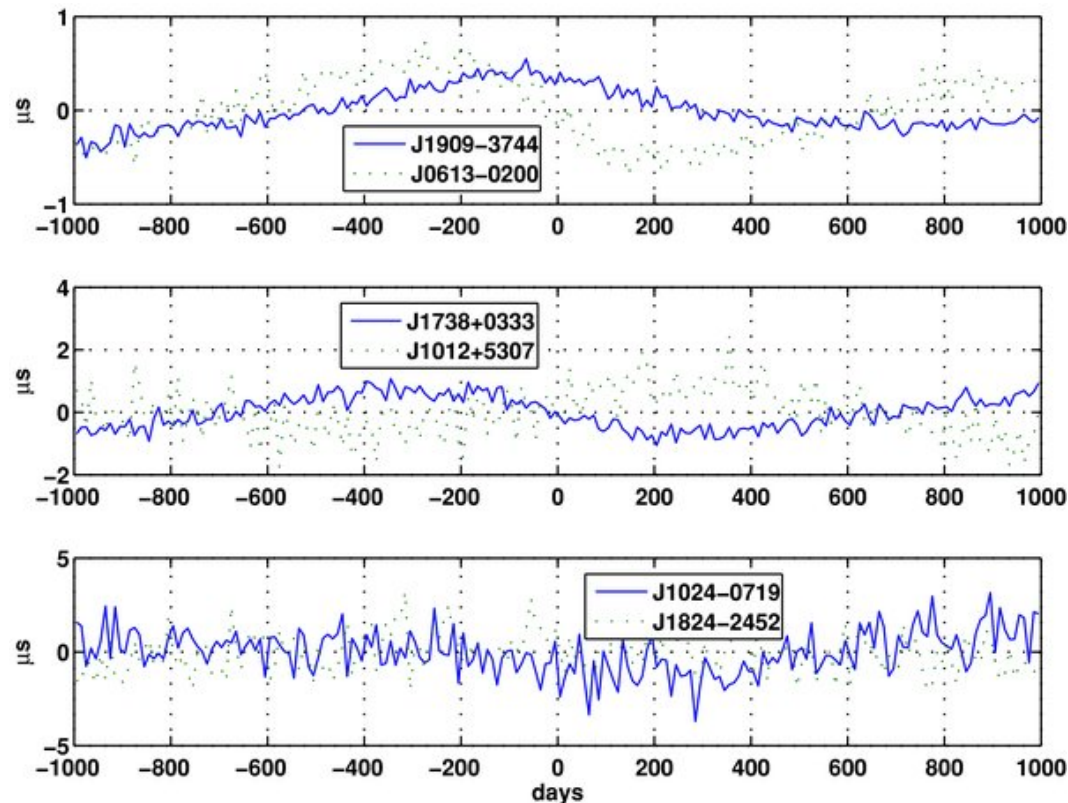
3) Shift FT and FT\* in opposite directions.

2) FT to frequency domain.

4) Multiply and accumulate.

## 2) Better algorithms for timing and detection

Optimal algorithms for stochastic, continuous, and burst source detection continually under development.

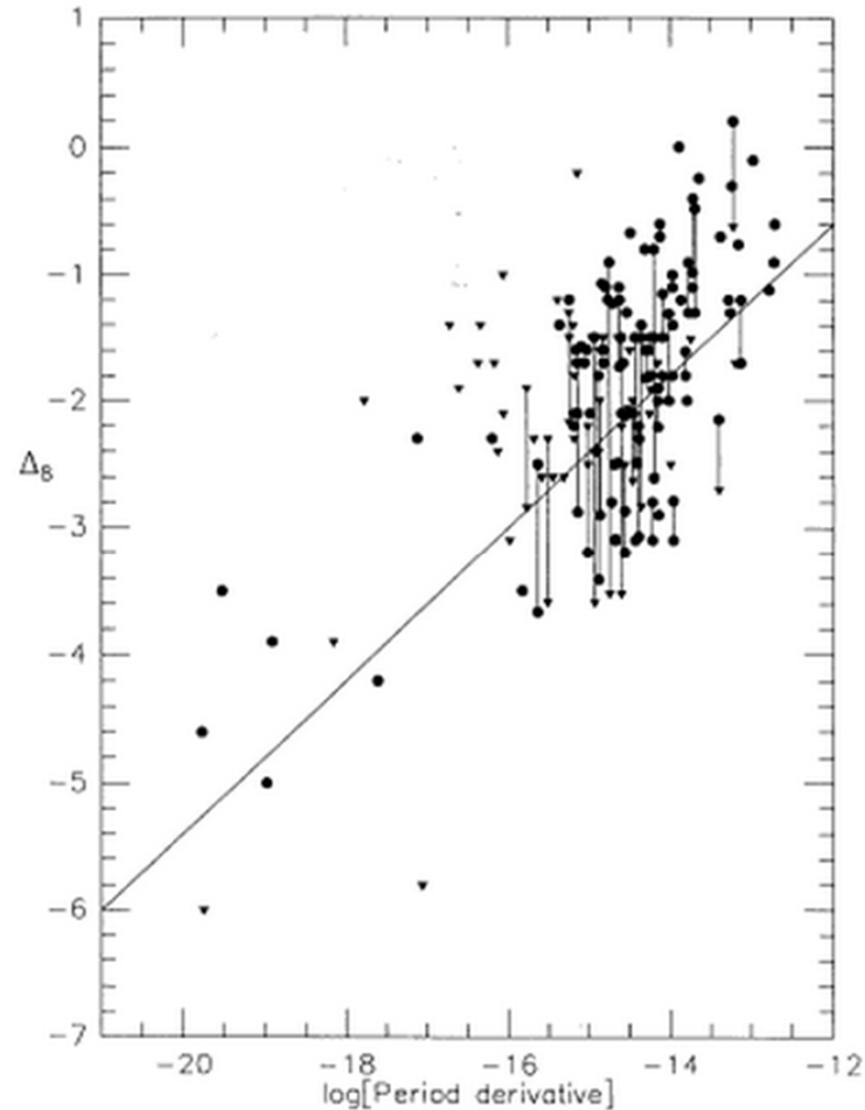


Finn & Lommen, ApJ, 718, 1400

### 3) New Pulsars!

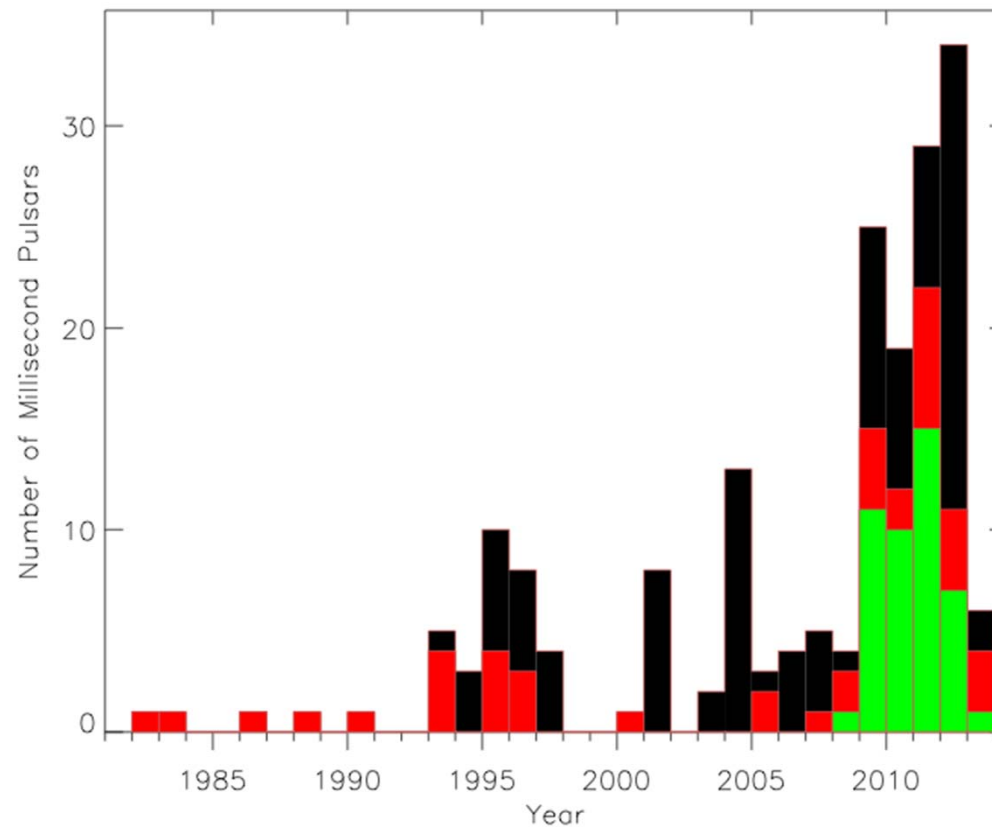
Timing noise is correlated with period derivative (or spin-down energy loss rate) but there is not a clear prediction for a specific pulsar.

Therefore, we must carry out searches and time pulsars for  $\sim$ year(s) to determine whether they are suitable for inclusion in the PTA.



Arzoumanian et al. 1994, ApJ, 422, 671

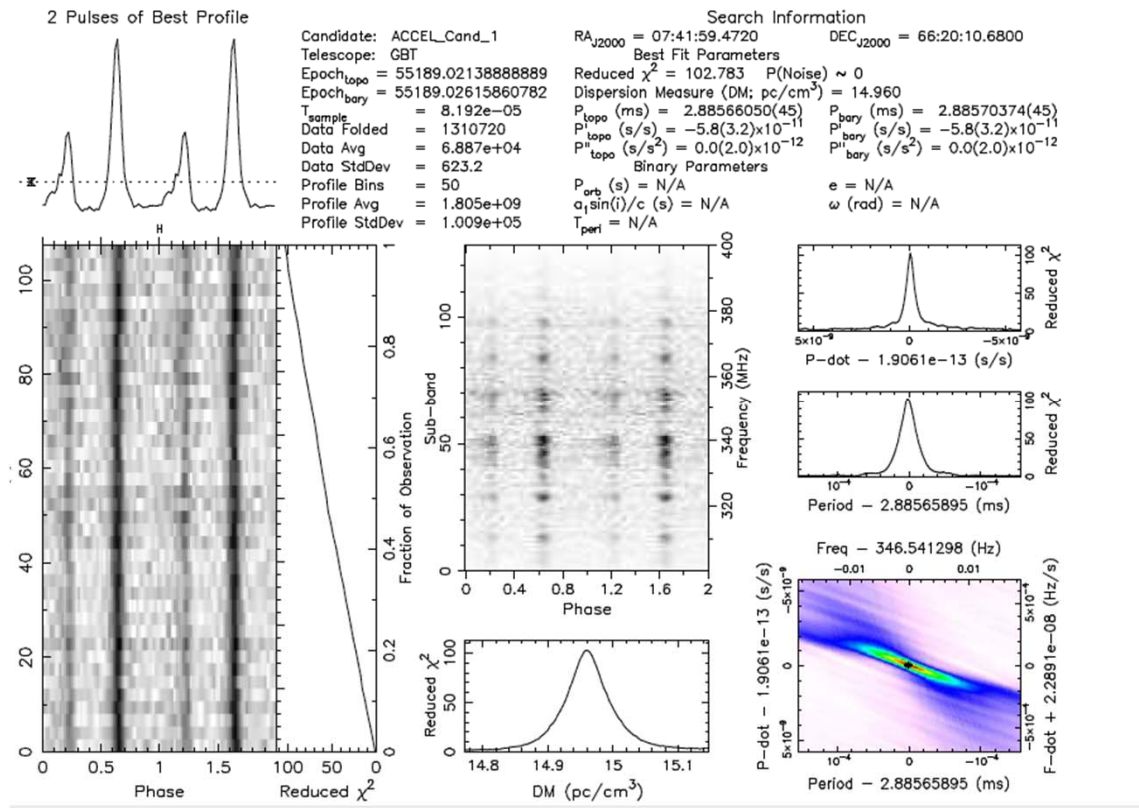
### 3) New Pulsars!



Searches underway with Arecibo and the GBT have revealed nearly 100 new MSPs over the past several years.

### 3) New Pulsars!

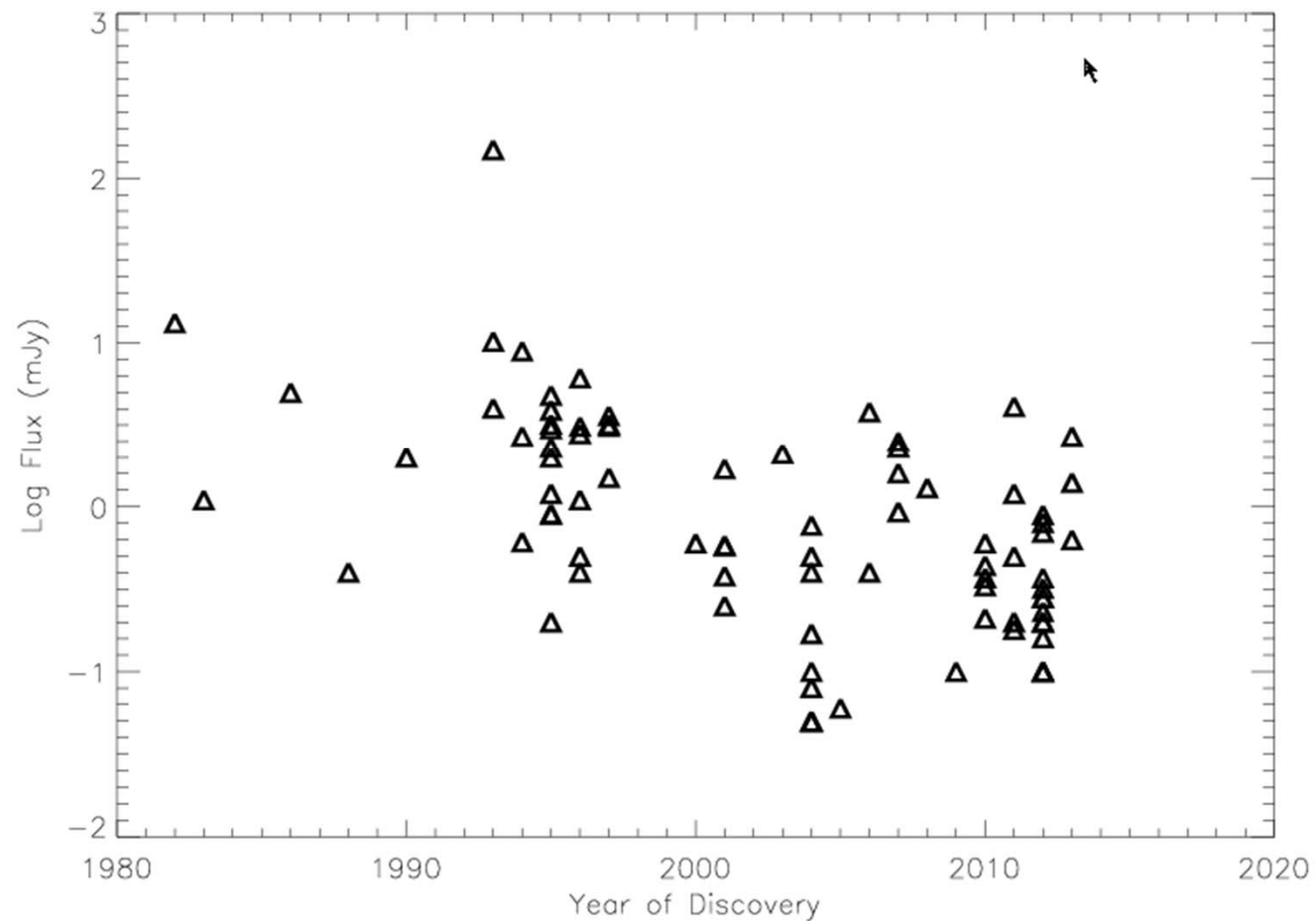
Many of these have the narrow, bright profiles required for PTAs.





### 3) New Pulsars!

Many bright MSPs remain to be found!



# Summary

- NANOGrav is timing nearly 40 pulsars with precisions of 30 ns – 1.5  $\mu$ s. This number has increased from 18 only 3 years ago.
- Limits are entering ranges that are constraining for SMBH and cosmic string models.
- Most of the pulsars are white noise dominated but red noise may become dominant in time.
- New instrumentation, more sophisticated scattering removal techniques, and adding new pulsars to the array are crucial for increasing our sensitivity.
- Arecibo and the GBT are essential for continuation of our program.
- Current searches are expected to discover ~100 MSPs over the next ~3 years.
- Ample additional science is enabled through these observations!