

Gaius Valerius Catullus, Carma 31

*Paene insularum, Sirmio, insularumque
ocelle, quascumque in liquentibus stagnis
marique vasto fert uterque Neptunus,
quam te libenter quamque laetus inviso,
vix mi ipse credens Thuniam atque Bithunos
liquisse campos et videre te in tuto.
O quid solutis est beatius curis,
cum mens onus reponit, ac peregrino
labore fessi venimus larem ad nostrum,
desideratoque acquiescimus lecto?
Hoc est quod unum est pro laboribus tantis.
Salve, o venusta Sirmio, atque ero gaude
gaudente, vosque, o Lydiae lacus undae,
ridete quidquid est domi cachinnorum.*



Advanced topics in the physics of Thomson/Compton scattering

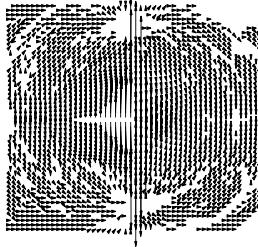
Vittoria Petrillo

Thanks to: Cesare Maroli, Illya Drebota, Alberto Bacci, Cristina Vaccarezza, Andrea Renato Rossi, Pino Dattoli, Titti Ronsivalle, Paolo Tomassini, Camilla Curatolo, Michela Venturelli, Federico Nguyen, Anna Giribono, Alessandro Variola,
Luca Serafini

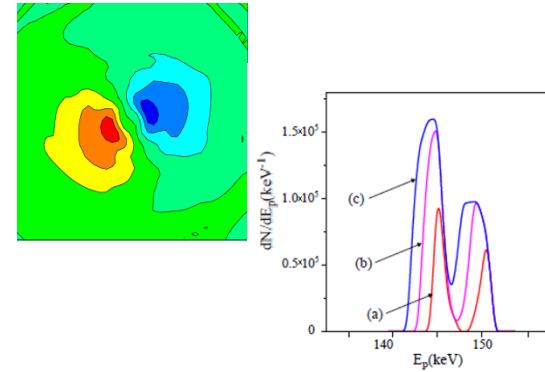
And also to all the  and ELI-NP groups

Presentation Outline

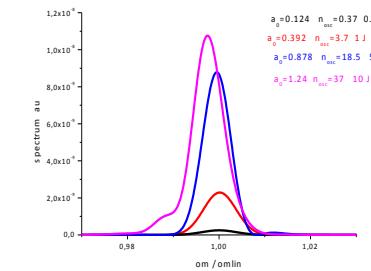
Introduction on Thomson/Compton scattering



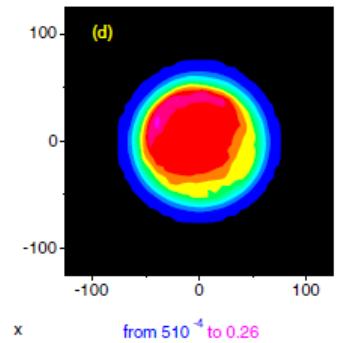
Polarization



Orbital angular momentum

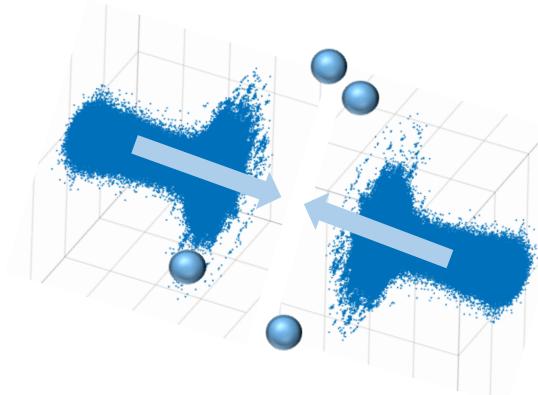


Two-color and multibunch

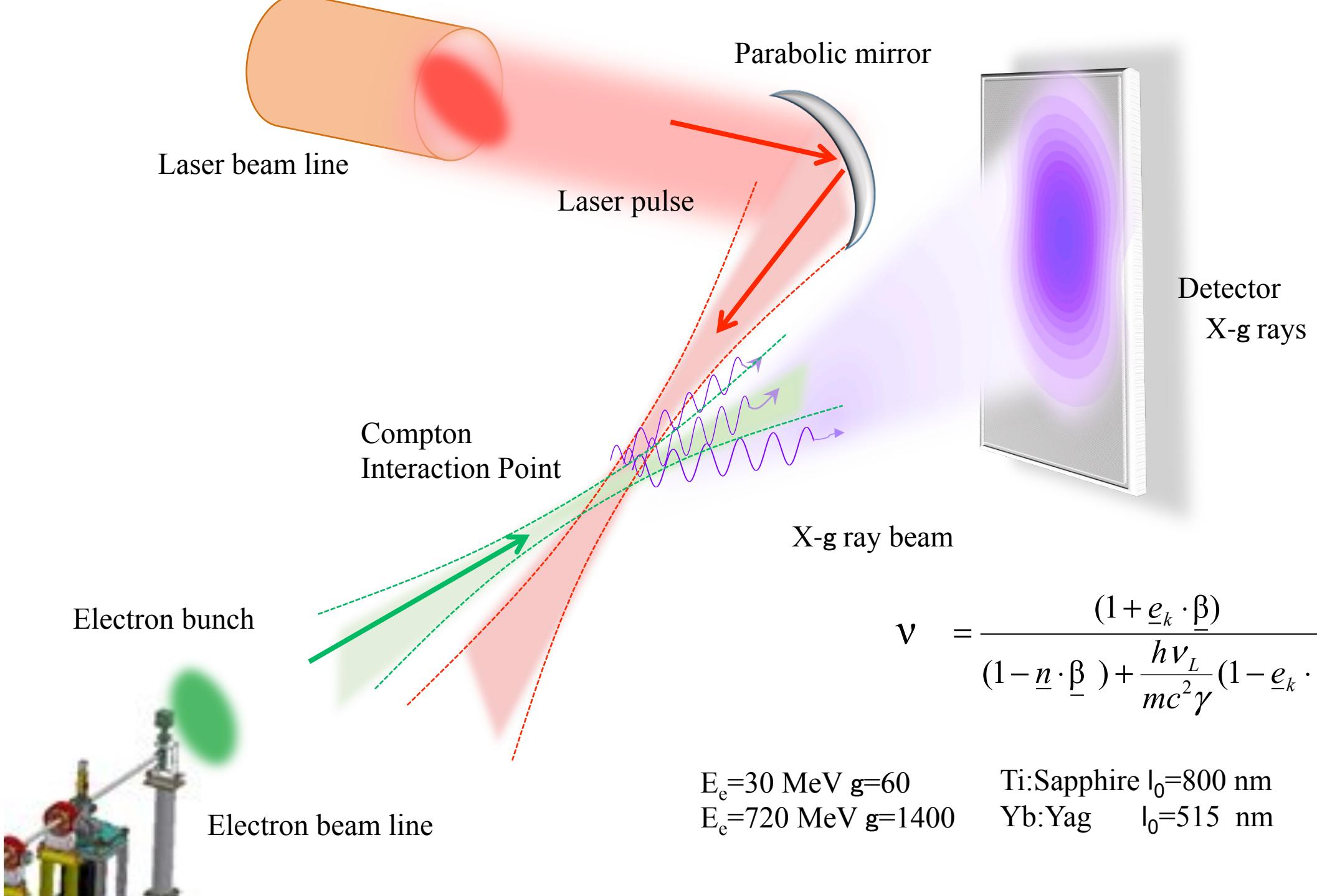


For increasing the spectral density: the chirp

For increasing spectral density, flux and coherence: the collective effects.



Gamma-gamma source



$$v = \frac{(1 + \underline{e}_k \cdot \underline{\beta})}{(1 - \underline{n} \cdot \underline{\beta}) + \frac{h\nu_L}{mc^2\gamma}(1 - \underline{e}_k \cdot \underline{n})} v_L \approx 4\gamma^2 v_L$$

$E_e = 30 \text{ MeV}$ $g = 60$
 $E_e = 720 \text{ MeV}$ $g = 1400$

Ti:Sapphire $\lambda_0 = 800 \text{ nm}$
Yb:Yag $\lambda_0 = 515 \text{ nm}$

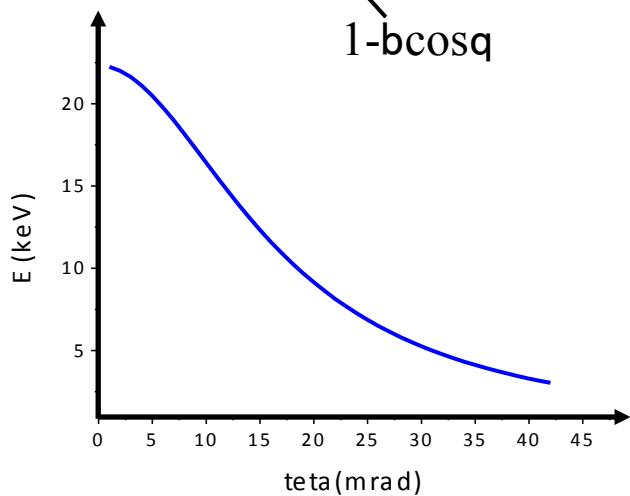
$E_{ph} = 22 \text{ keV}$
 $E_{ph} = 19 \text{ MeV}$

Generalities on Compton scattering

Compton radiation is frequency-angle correlated

Frequency of the radiation in a direction \underline{n}

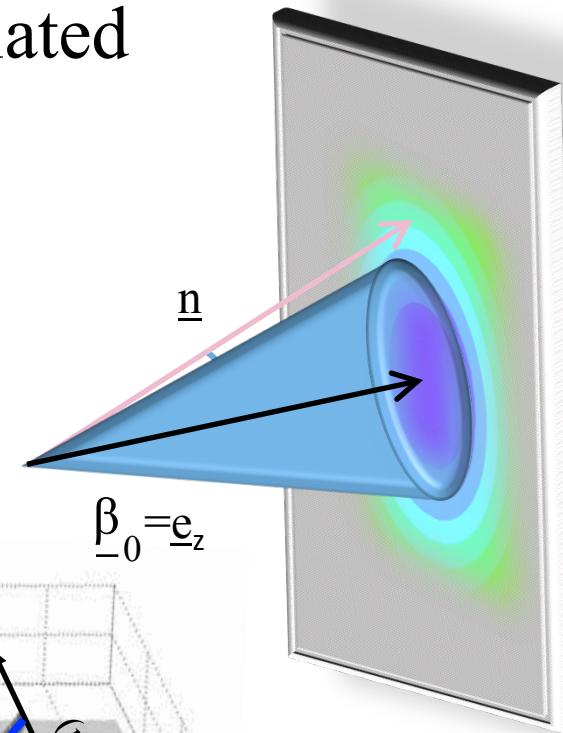
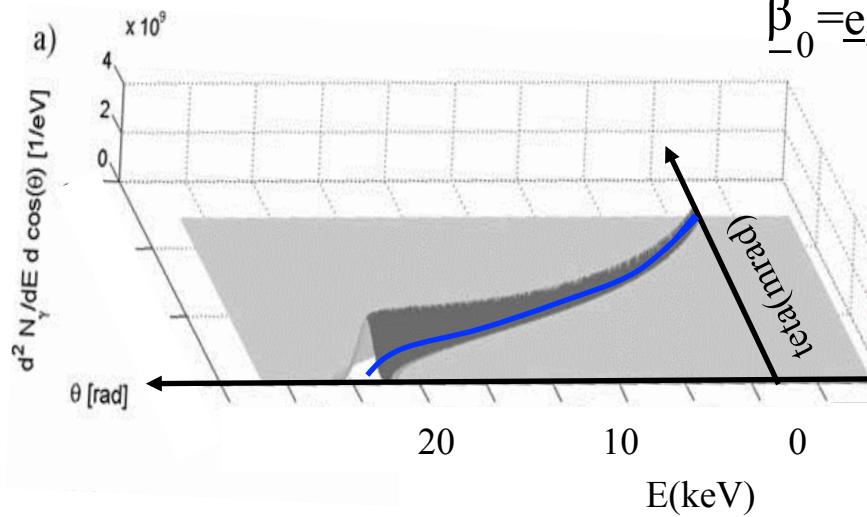
$$\nu = \nu_L \frac{1 - \underline{e}_k \cdot \underline{\beta}_0}{1 - \underline{n} \cdot \underline{\beta}_0} \approx 4\gamma_0^2 \nu_L$$



Total acceptance

$$Y_{\max} = g q_{\max} = 1$$

$$q_{\max} = 1/g$$



Higher frequencies close to axis

Lower frequencies in the outer part

PRL 111, 114803 (2013) PHYSICAL REVIEW LETTERS week ending 13 SEPTEMBER 2013

High Resolution Energy-Angle Correlation Measurement of Hard X Rays from Laser-Thomson Backscattering

A. Jochmann,^{1,2,*} A. Irman,¹ M. Bussmann,¹ J. P. Couperus,^{1,2} T. E. Cowan,^{1,2} A. D. Debus,¹ M. Kuntzsch,^{1,2} K. W. D. Ledingham,³ U. Lehnert,¹ R. Sauerbrey,^{1,2} H. P. Schlenvoigt,¹ D. Seipp,^{1,4} Th. Stöhlker,^{4,5} D. B. Thom,⁵ S. Trotsenko,^{4,5} A. Wagner,¹ and U. Schramm^{1,2}

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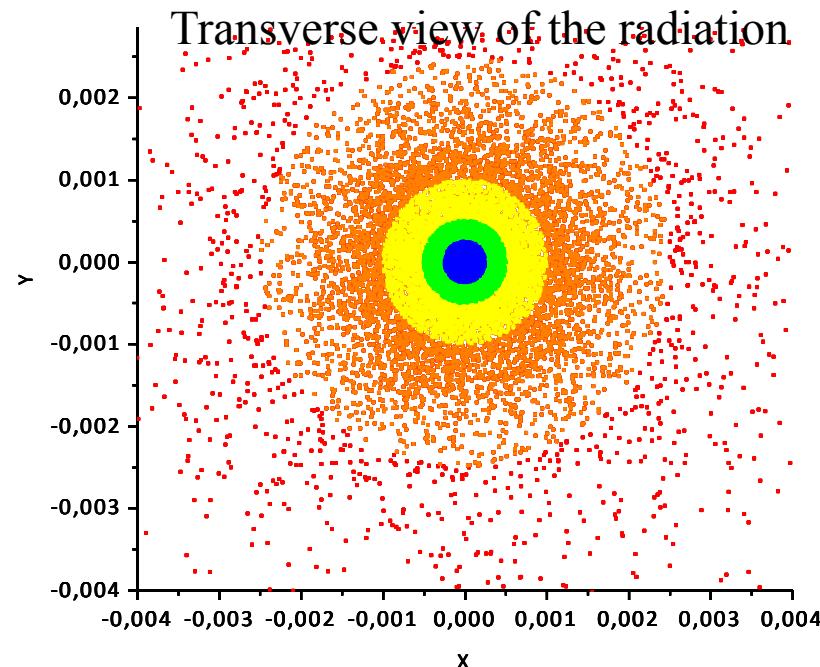
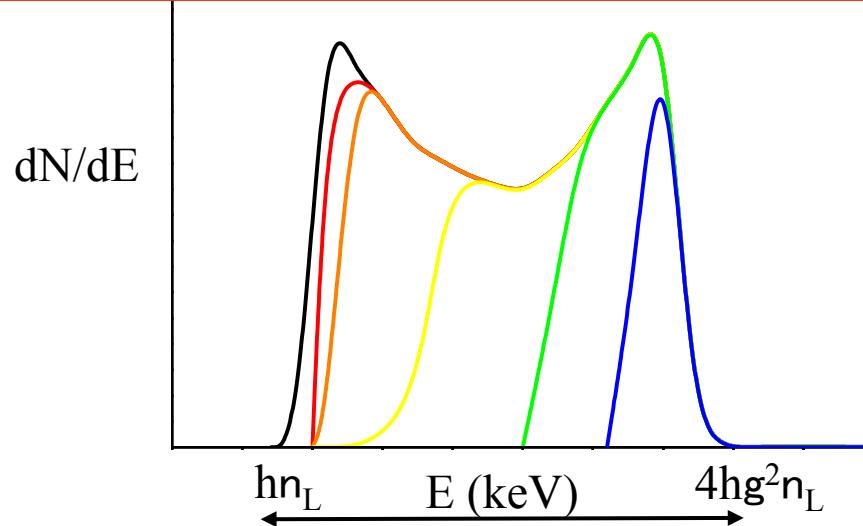
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(Received 6 May 2013; published 13 September 2013)

Thomson backscattering of intense laser pulses from relativistic electrons not only allows for the

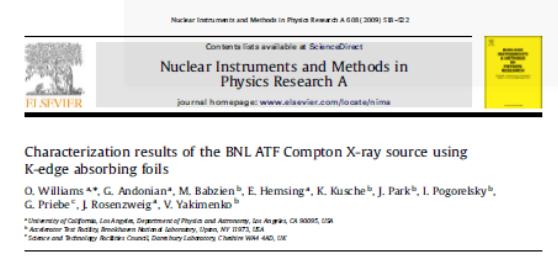
Generalities on Compton scattering



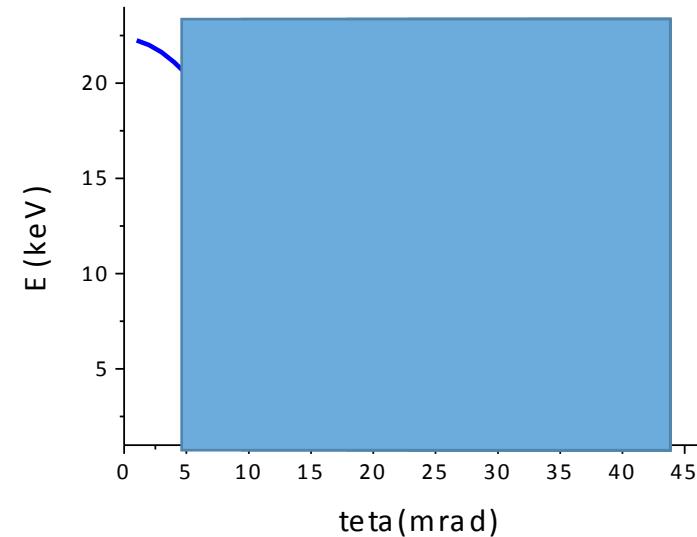
Large natural spectrum

The energy-angle correlation permits the control of bandwidth and divergence

By introducing irides or collimators one can diminish the bandwidth, by selecting the photons close to the axis



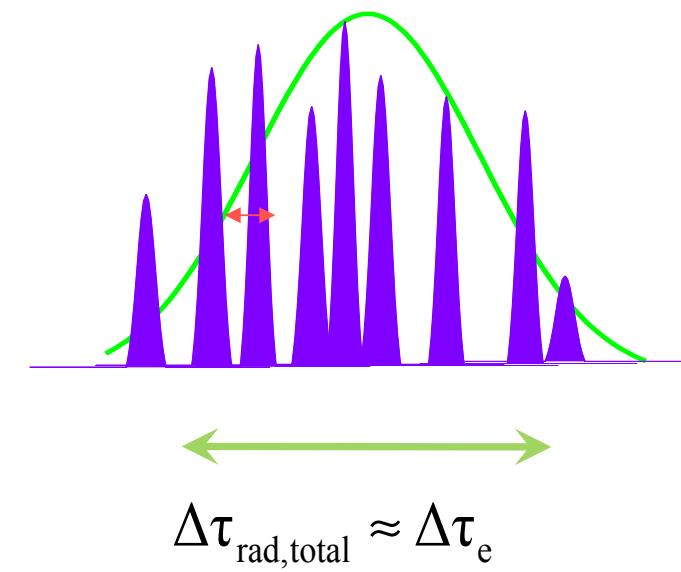
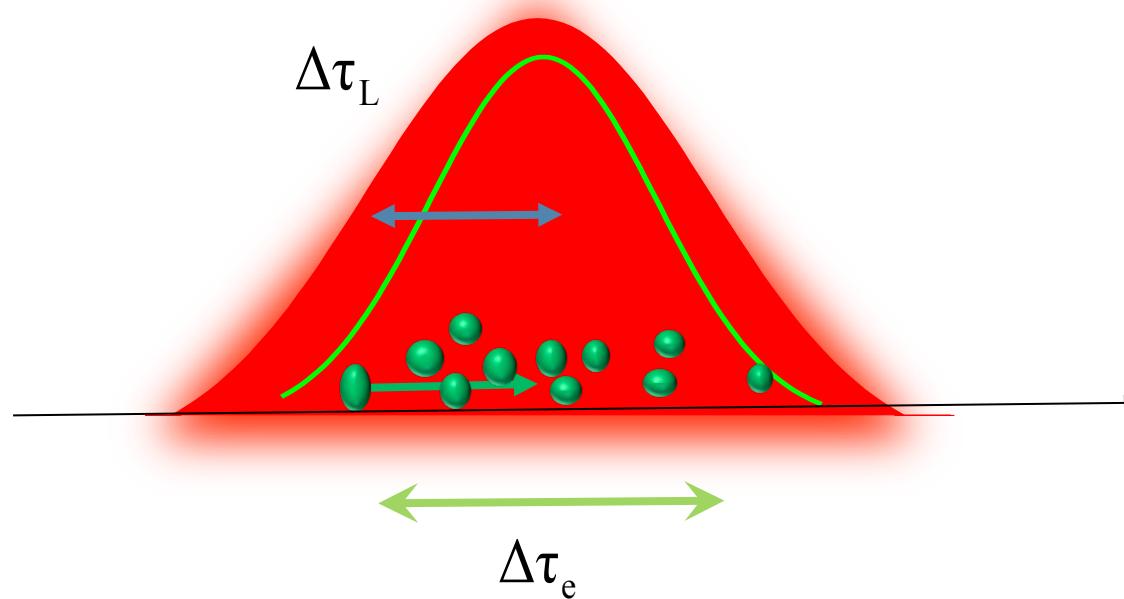
Effect of the collimator



Generalities on Compton scattering

Temporal structure of the radiation

All electrons emit out of phase and the longitudinal structure of the radiation is totally incoherent



Generalities on Compton scattering

Transverse coherence

Transverse structure of spectral components

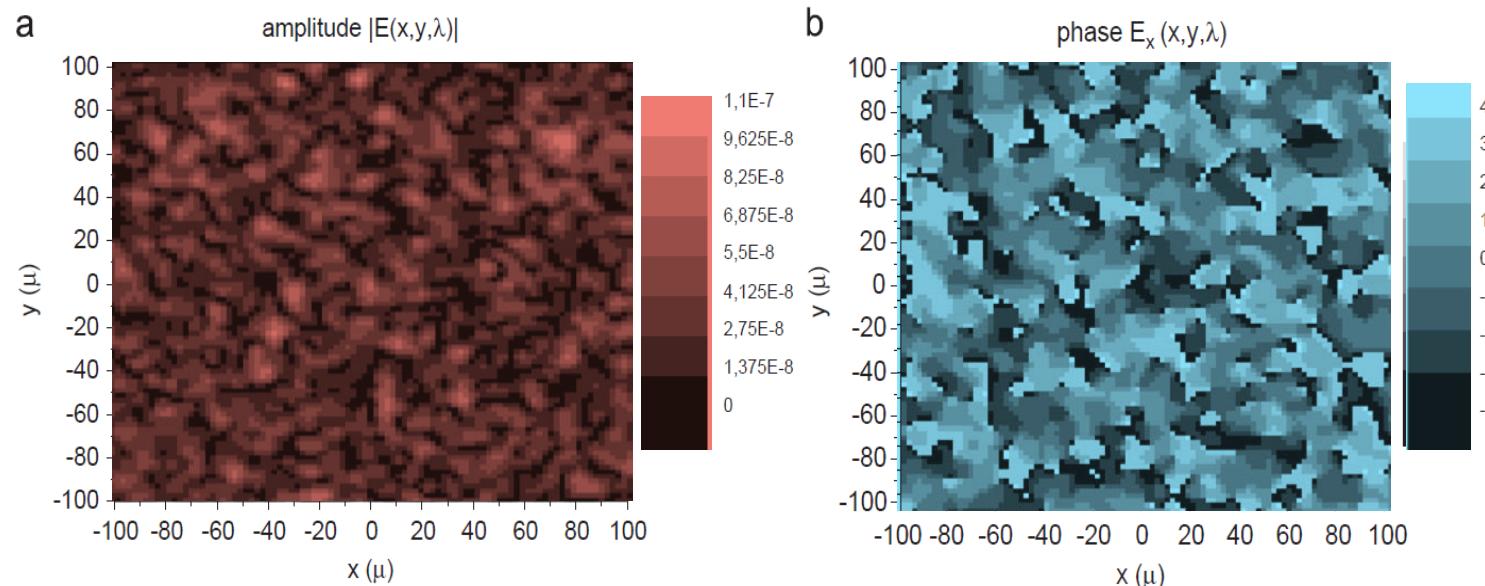


Fig. 3. Amplitude $|E(x,y,\lambda)|$ (a) and phase of $E_x(x,y,\lambda)$ (b) for $\lambda = 0.7 \text{ \AA}$ at $r = 10 \text{ m}$ from the source. Coordinates x and y in microns, Fourier time-transform of electric field in V/m .

Coherence length=|R/s

$$\begin{aligned} E_e &= 30 \text{ MeV} & g &= 60 \\ E_e &= 720 \text{ MeV} & g &= 1400 \end{aligned}$$

$$\begin{aligned} \text{Ti:Sapphire } l_0 &= 800 \text{ nm} \\ \text{Yb:Yag } l_0 &= 515 \text{ nm} \end{aligned}$$

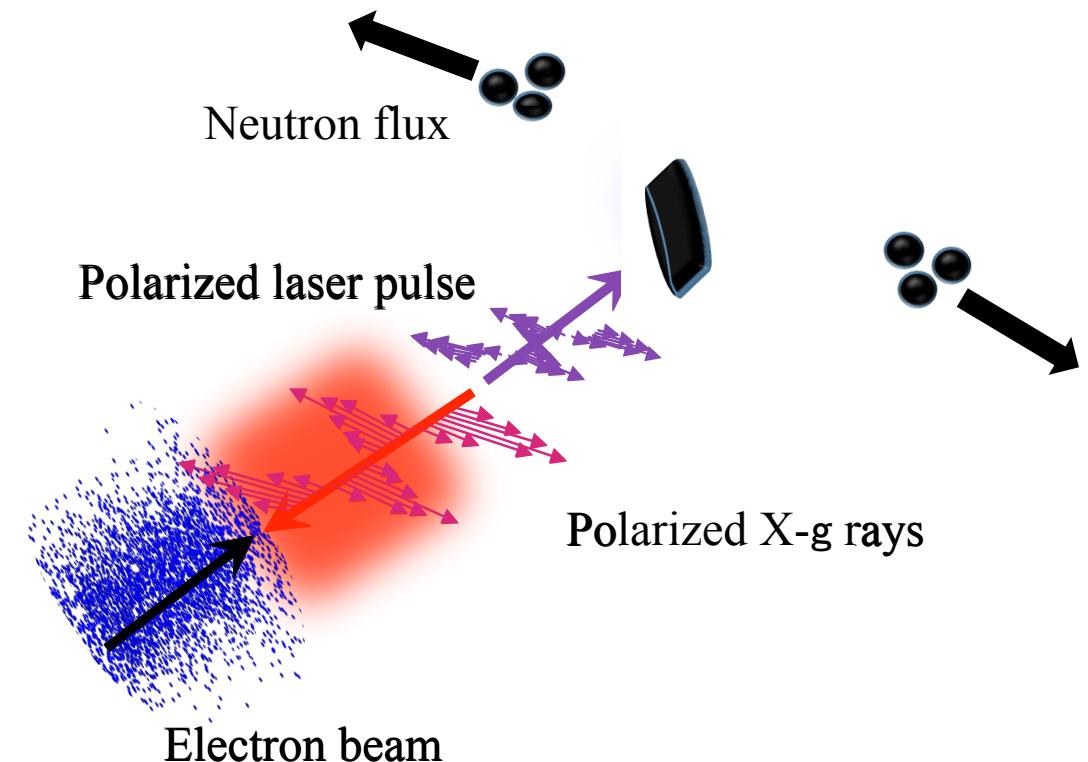
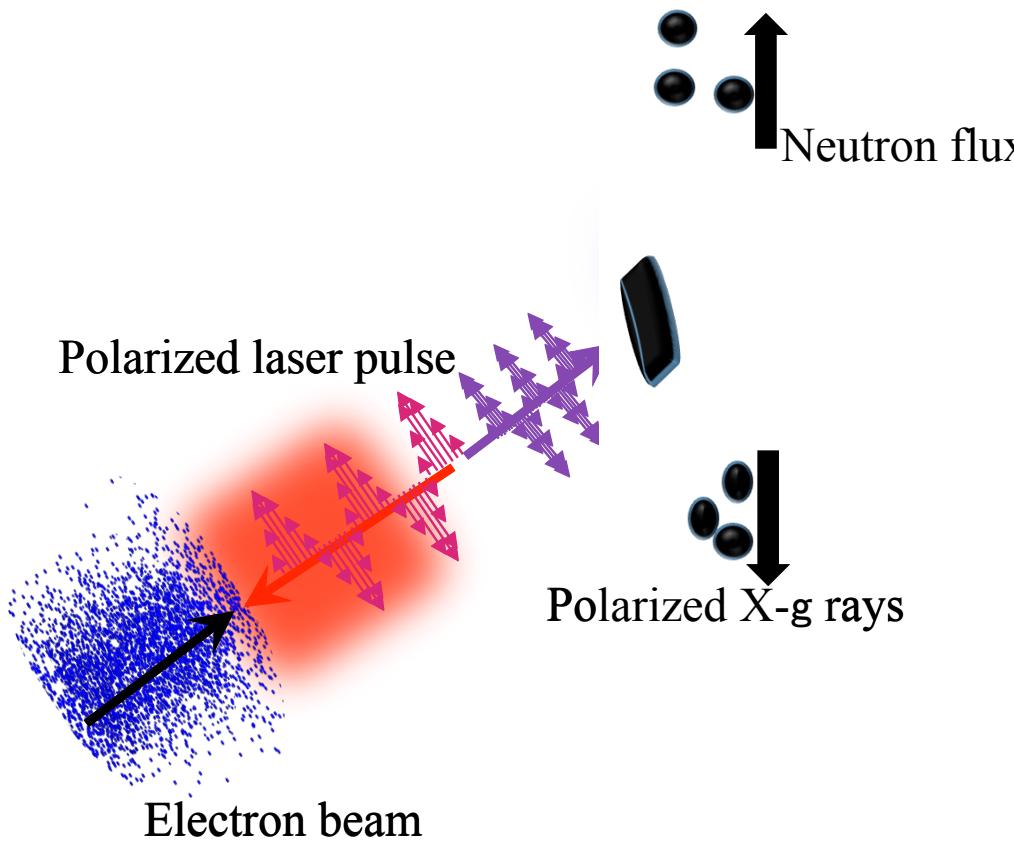
$$\begin{aligned} E_{\text{ph}} &= 22 \text{ keV} \\ E_{\text{ph}} &= 19 \text{ MeV} \end{aligned}$$

$$\begin{aligned} L &= 8 \text{ micron at } 1 \text{ m} \\ L &= 10^{-2} \text{ micron at } 1 \text{ m} \end{aligned}$$

Polarization

Why studying gamma ray polarization?

In nuclear photonics experiments, the kinematics of neutrons is strongly influenced by the polarization of the gamma rays



PHYSICAL REVIEW SPECIAL TOPICS - ACCELERATORS AND BEAMS 14, 044701 (2011)

Theoretical and simulation studies of characteristics of a Compton light source

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(Received 25 January 2011; published 21 April 2011)

Polarization: ELI-NP case

PHYSICAL REVIEW SPECIAL TOPICS—ACCELERATORS AND BEAMS 18, 110701 (2015)

Polarization of x-gamma radiation produced by a Thomson
and Compton inverse scattering

V. Petrillo,^{1,2} A. Bacchini,³ C. Curatolo,^{1,2} L. Dabrot,² A. Grigorio,² C. Maroli,¹ A. R. Rossi,²

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(Received 24 June 2015; published 19 November 2015)

ELI-NP Parameters

$E=234\text{-}529 \text{ MeV}$

$Q=250 \text{ pC}$

$e=0.5 \text{ mm mrad}$

$\Delta E/E=7 \cdot 10^{-4}$

$l=520 \text{ nm}$

$E_L=0.2\text{-}0.4 \text{ J}$

$d=8^\circ$

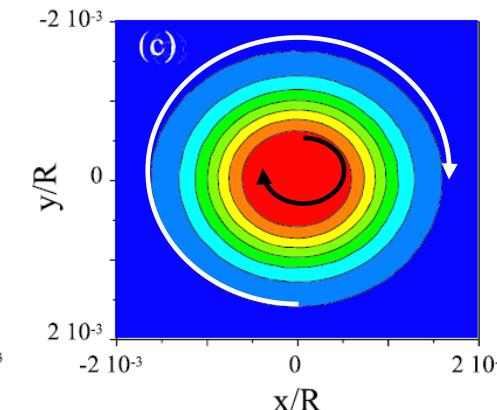
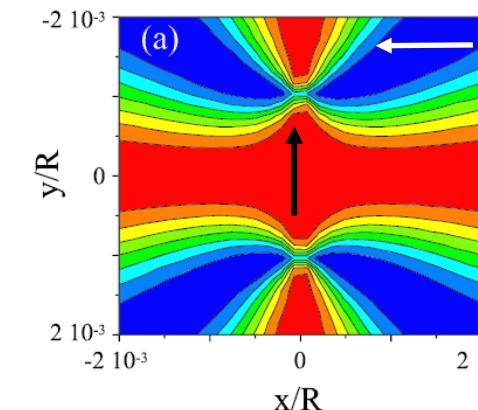
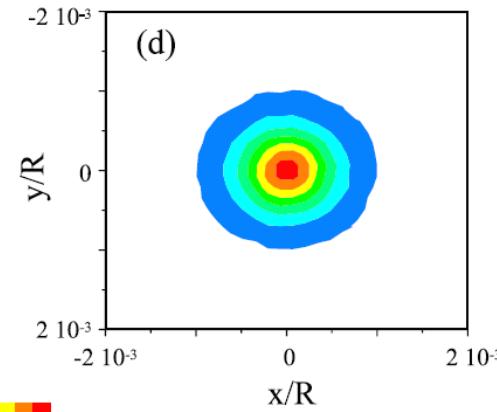
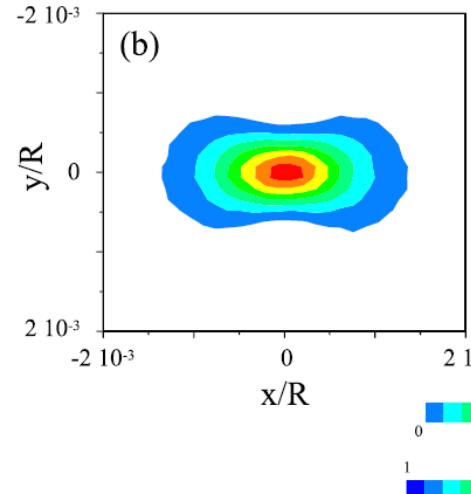
$w_0=28 \text{ mm}$

$E_{\text{ph}}=2\text{-}10 \text{ MeV}$

Total intensity I
on the screen at 1 m
 $E_{\text{ph}}=10 \text{ MeV}$

Stokes parameter
$$\frac{(|E_x|^2 - |E_y|^2)}{(|E_x|^2 + |E_y|^2)}$$

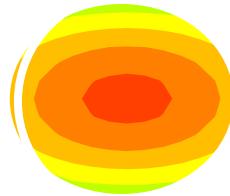
Linear polarization
of the laser ↑



Circular polarization
of the laser ↗

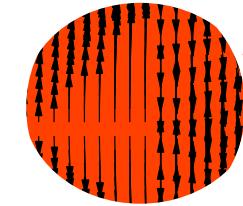
Polarization: ELI-NP case

With a **linear polarization** of the laser:



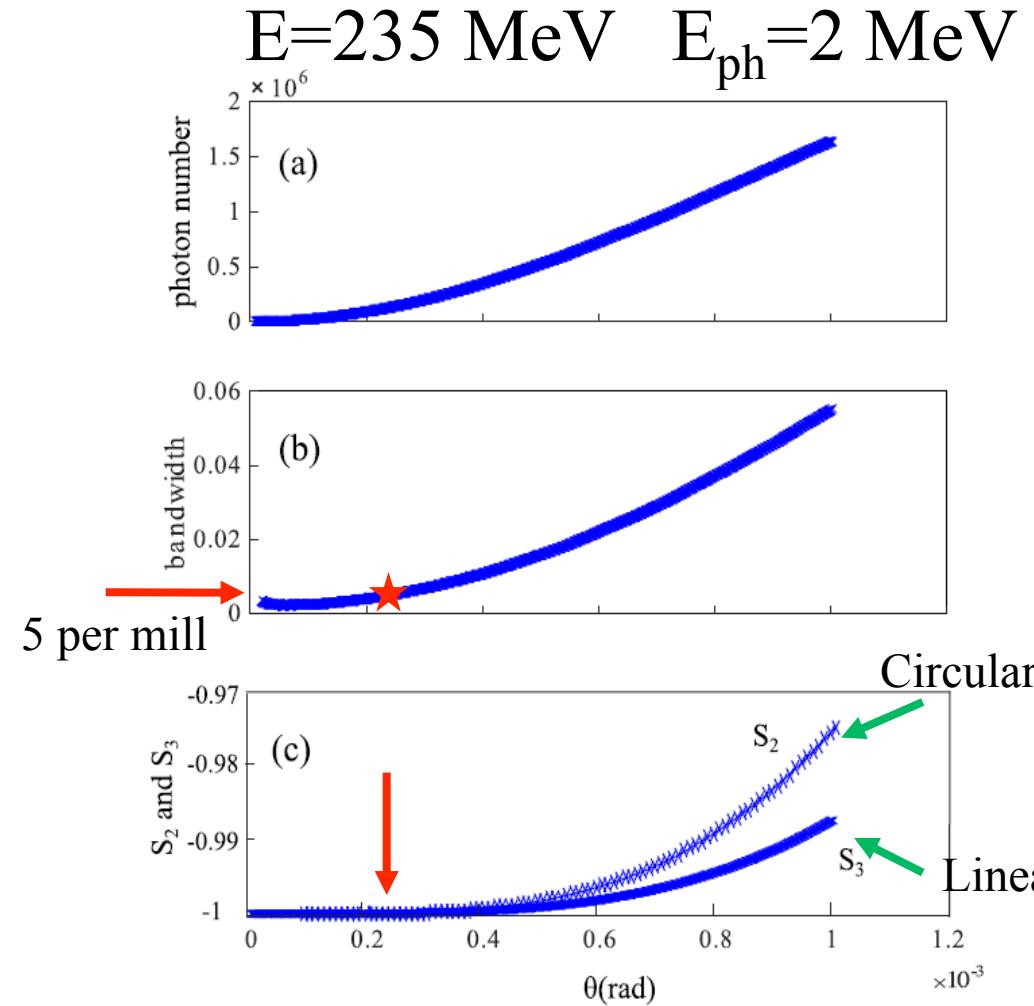
Total intensity

on the screen at 1 m,
the circle is 1/g



Stokes parameter
 $(|E_x|^2 - |E_y|^2) / (|E_x|^2 + |E_y|^2)$

Polarization: ELI-NP case, calculations by Illya Drebot



Bandwidth 5 per mill

Polarization 100%

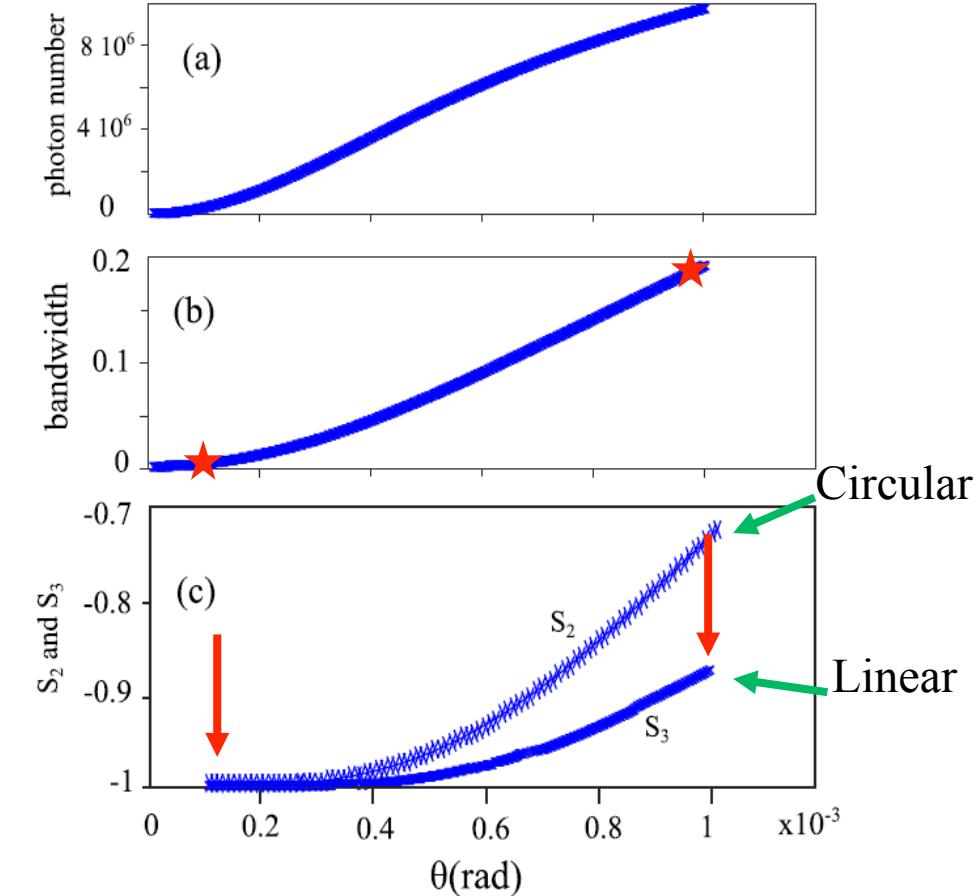
ELI-NP e-beam optimized in emittance

Photon number

Bandwidth

Polarization

$E=530 \text{ MeV}$ $E_{\text{ph}}=10 \text{ MeV}$



Bandwidth 20 %

Polarization 85-70%

Polarization: typical plasma accelerated beam

NATURE PHOTONICS | LETTER



All-optical Compton gamma-ray source

K. Ta Phuoc, S. Corde, C. Thaury, V. Malka, A. Tafzi, J. P. Goddet, R. C. Shah, S. Seban & A. Rousse

Affiliations | Contributions | Corresponding authors

Nature Photonics 6, 308–311 (2012) | doi:10.1038/nphoton.2012.82

Received 15 November 2011 | Accepted 16 March 2012 | Published online 22 April 2012

$Q=120 \text{ pC}$
 $e=1 \text{ mm mrad}$
 $s=1.5 \text{ mm}$
 $DE/E=1 \cdot 10^{-2}$
 $l=520 \text{ nm}$
 $E_L=0.2-0.4 \text{ J}$
 $d=8^\circ$
 $w_0=28 \text{ mm}$
 $E_{\text{ph}}=2-10 \text{ MeV}$

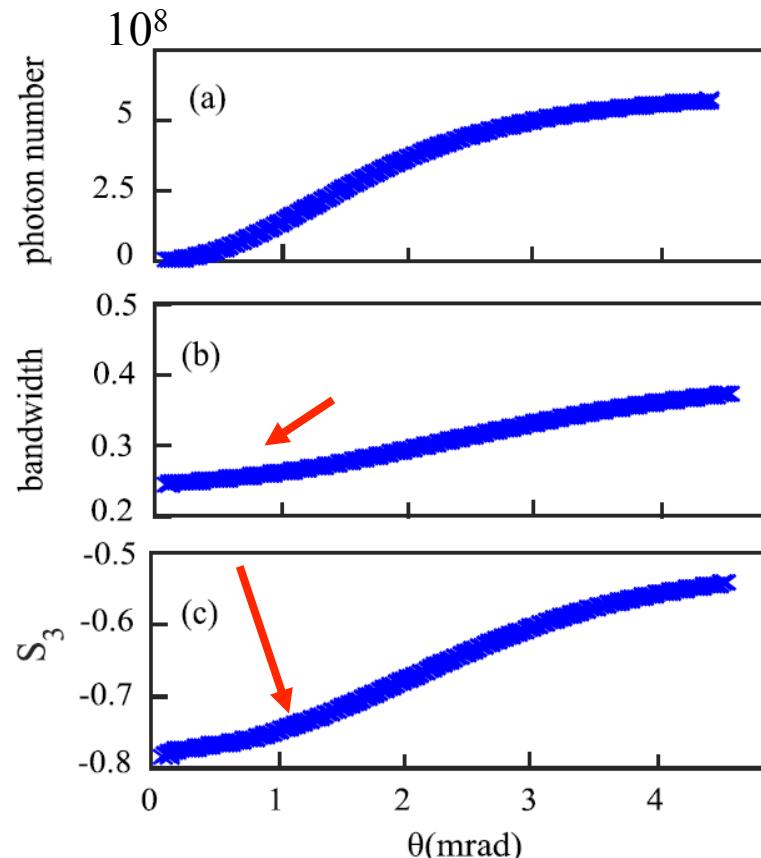
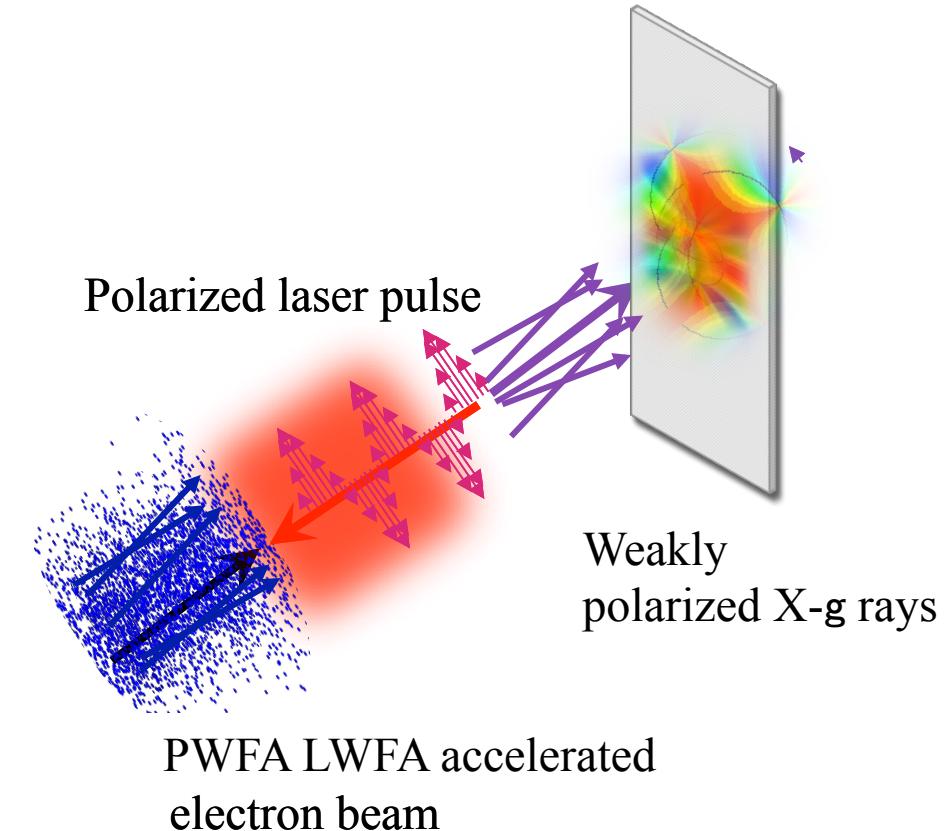


FIG. 10. (a) Photon flux, (b) bandwidth, and (c) Stokes parameter S_3 vs acceptance angle for a typical plasma beam.

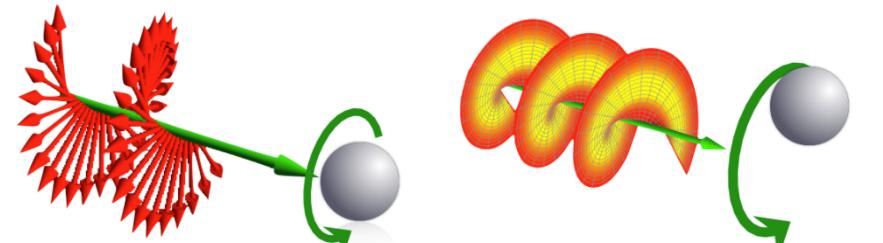


Bandwidth $> 25\%$, polarization < 0.75

Orbital Angular Momentum (OAM)

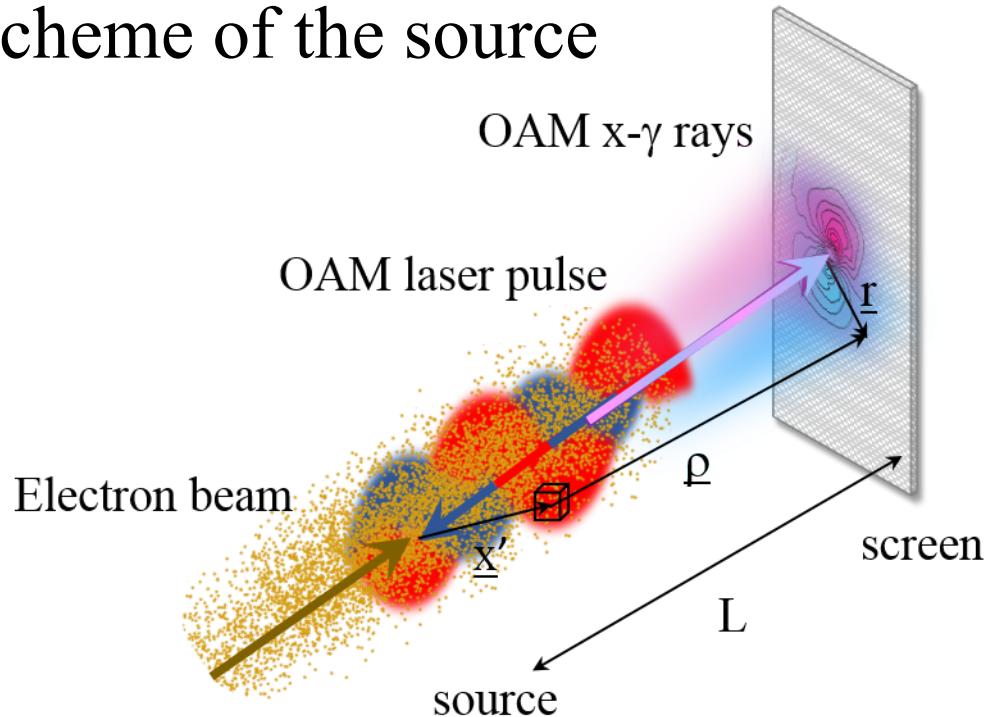
Why studying radiation with orbital angular momentum?

In exp. of photoinization forbidden decays can be excited, molecules in rotational states can resonate in vortex,dipolar and quadrupolar transition can be distinguished.



Spin Ang Mom interaction Orb Ang Mom interaction

Scheme of the source



'Wild type' electron beam generated by linac

$$s = \frac{1}{2}\hbar \quad j = s + m\hbar$$

Proposals for OAM X-beams are based on manipulation of electrons in FEL emission. The electrons are treated in such a way that they carry OAM and transfer it to the radiation.

Compton Scattered X-Gamma Rays with Orbital Momentum

V. Petrillo, G. Dattoli, I. Drebot, and F. Nguyen
Phys. Rev. Lett. **117**, 123903 (2016) – Published 16 September 2016
[Show Abstract](#)

Orbital Angular Momentum, laser structure

Expression and propagation of an OAM laser mode

L. Allen, M. W. Beijersbergen, R. J. C. Spreeuw, and J. P. Woerdman, Phys. Rev. A **45**, 8185 (1992).

$$\tilde{E}_L(x, y, z, t) = \underline{e}_y f(z + ct) E_m(x, y, z) e^{i(\omega t + k_z z)}$$

$$E_m(x, y, z) = \pi \left(\frac{w_0}{w_z} \right)^2 H_m(\xi, \alpha) e^{-\frac{x^2+y^2}{2w_z^2}}$$

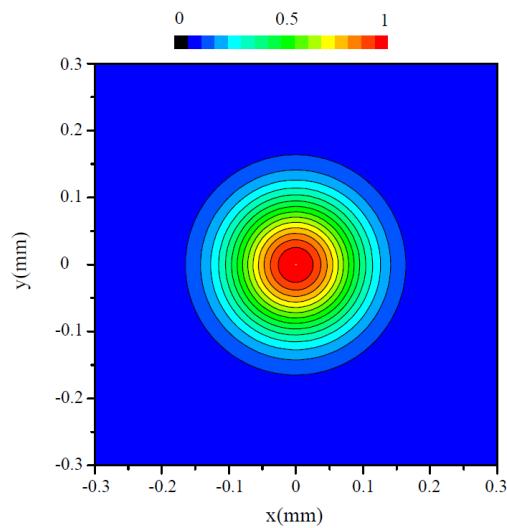
$$H_m(\xi, \alpha) = m! \sum_{r=0}^{[m/2]} \frac{\alpha^r \xi^{m-2r}}{r!(m-2r)!}$$

$$\xi = \frac{1}{w_0} \left[\left(\frac{w_0}{w_z} \right)^2 (x + i\varepsilon y) - (x_0 + i\varepsilon y_0) \right]$$

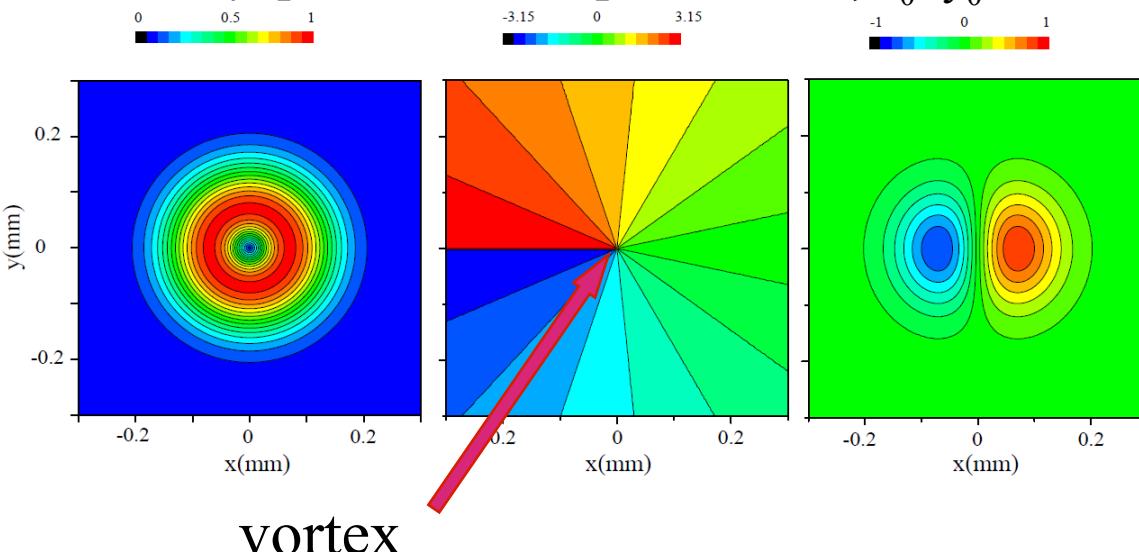
$$\alpha = \frac{i}{2}(1 - \varepsilon^2) \frac{\lambda z}{w_z^2}$$



OAM laser modes are generated with fork holograms or phase masks



Transverse shape of a laser with OAM, intensity, phase and real part

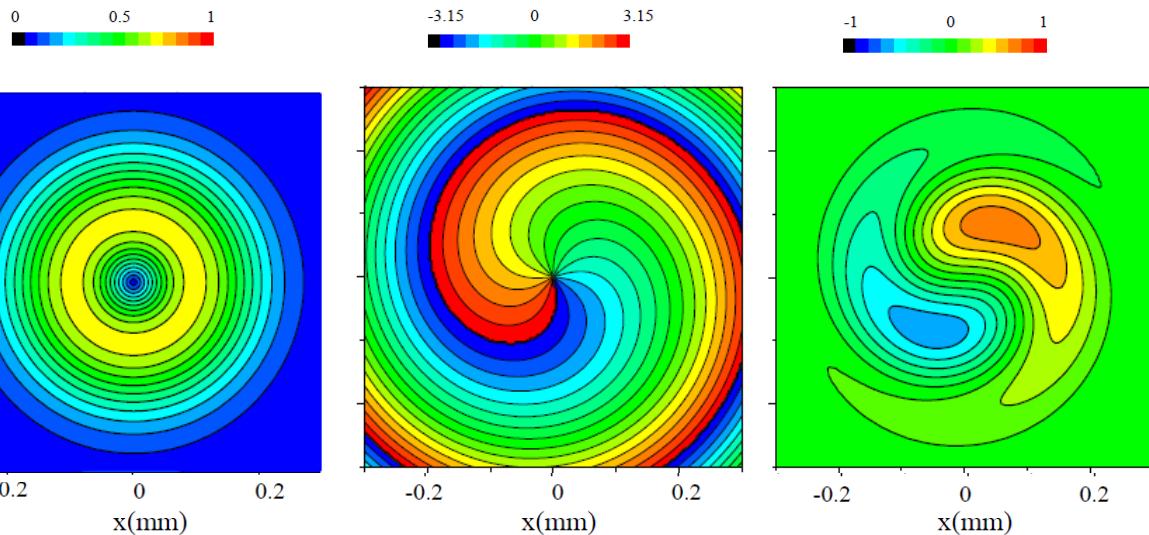


Gaussian mode

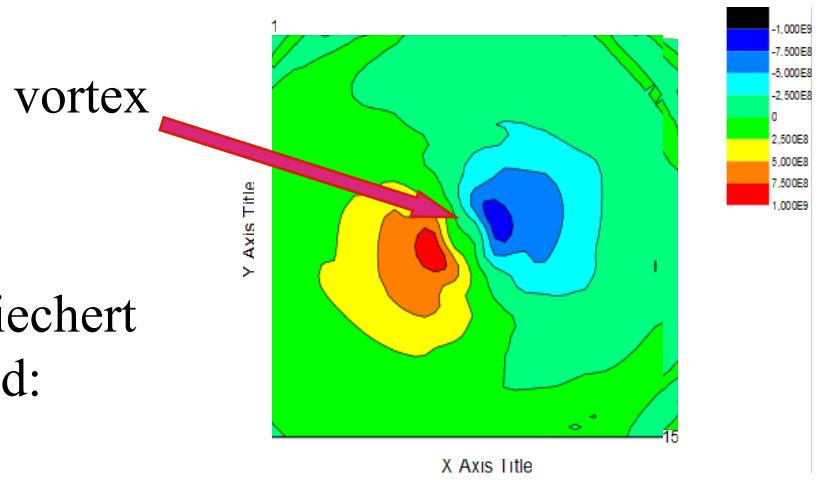
$$m=1, x_0=y_0=0$$

Orbital Angular Momentum, radiation calculation

Propagation of the laser:



X radiation the screen,
classical treatment:

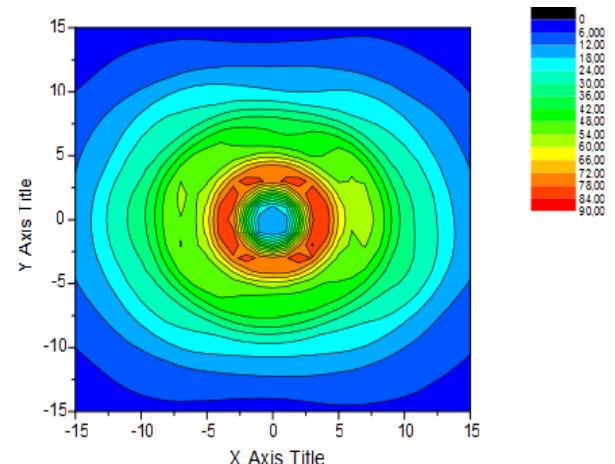


Lienard-Wiechert
electric field:

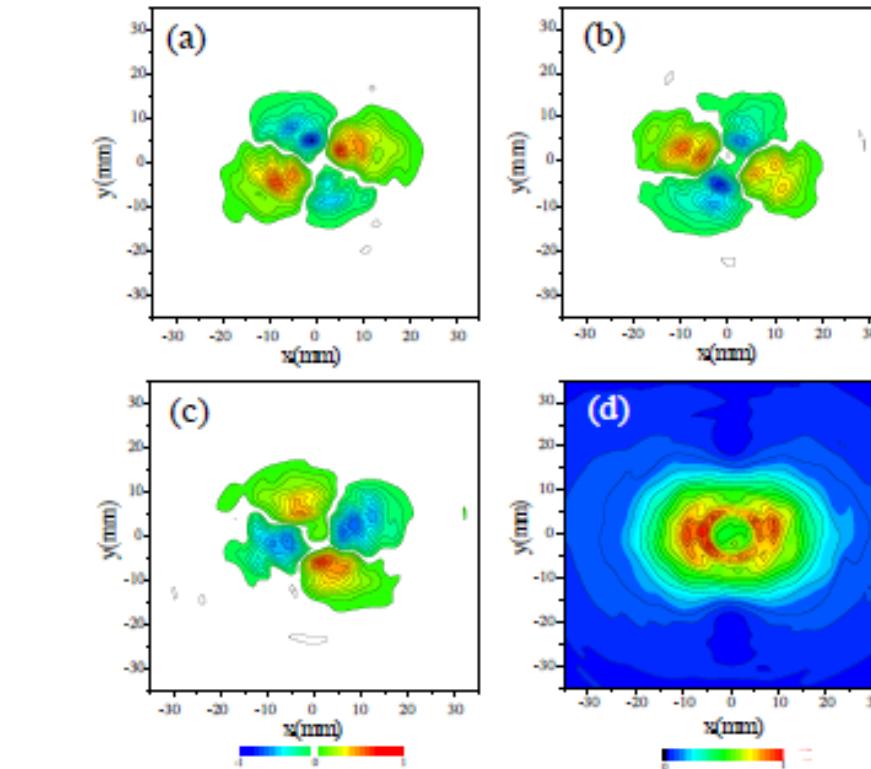
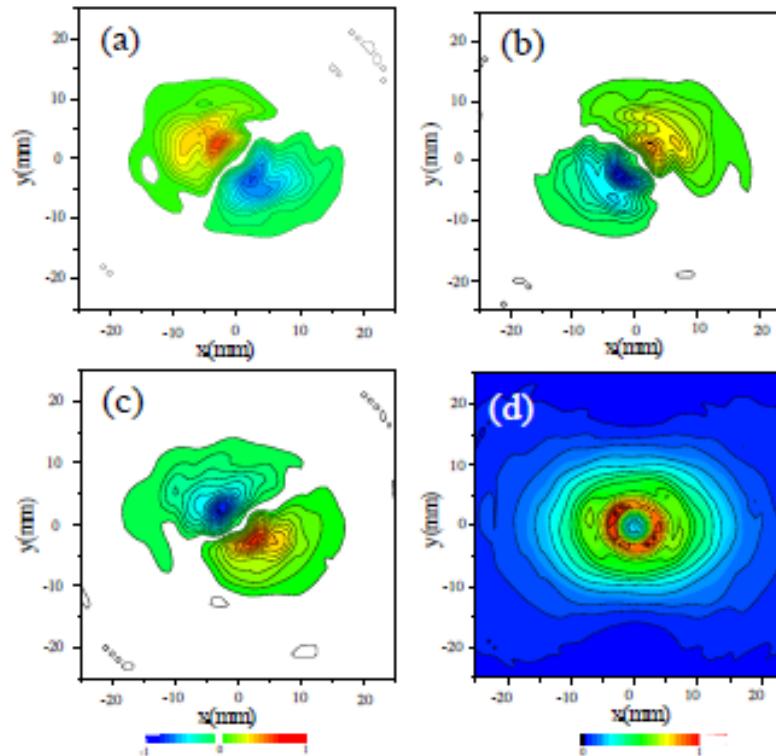
$$\underline{E} = \frac{e}{c} \sum_j \left[\frac{\underline{n} \times ((\underline{n} - \underline{\beta}_j) \times \dot{\underline{\beta}}_j)}{(1 - \underline{\beta}_j \cdot \underline{n})^3 R} \right]_{ret}$$

$$\dot{\underline{\beta}}_j = -\frac{e}{mc\gamma_j} \left[\underline{E}_L \left(1 - \underline{\beta}_j \cdot \underline{e}_k \right) + \dots + \underline{\beta}_j \left[\underline{E}_L (\underline{e}_k - \underline{\beta}_j) \right] \right]$$

Quantum treatment:



Orbital Angular Momentum, radiation structure

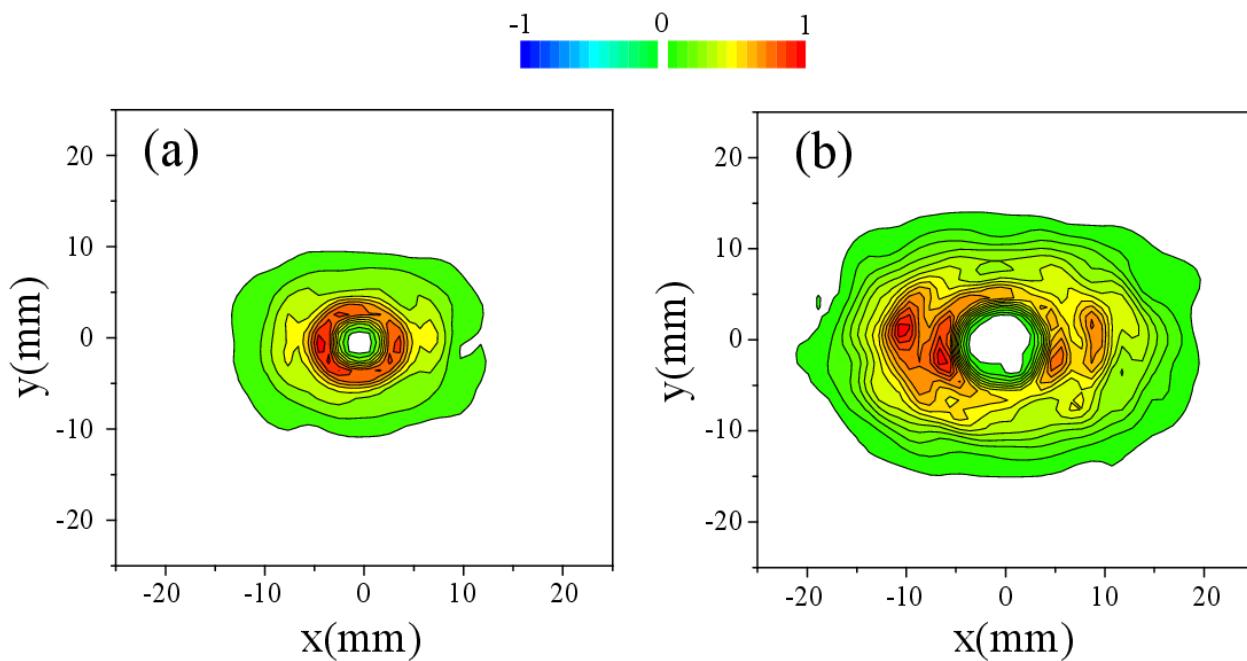


Electric field at different time and averaged intensity on the screen

$m=1$

$m=2$

Orbital Angular Momentum



Orbital Angular Momentum on the screen

$m=1$

$m=2$

$$N_{ph} = 6 \cdot 10^6$$
$$E_{ph} = 8 \text{ keV}$$

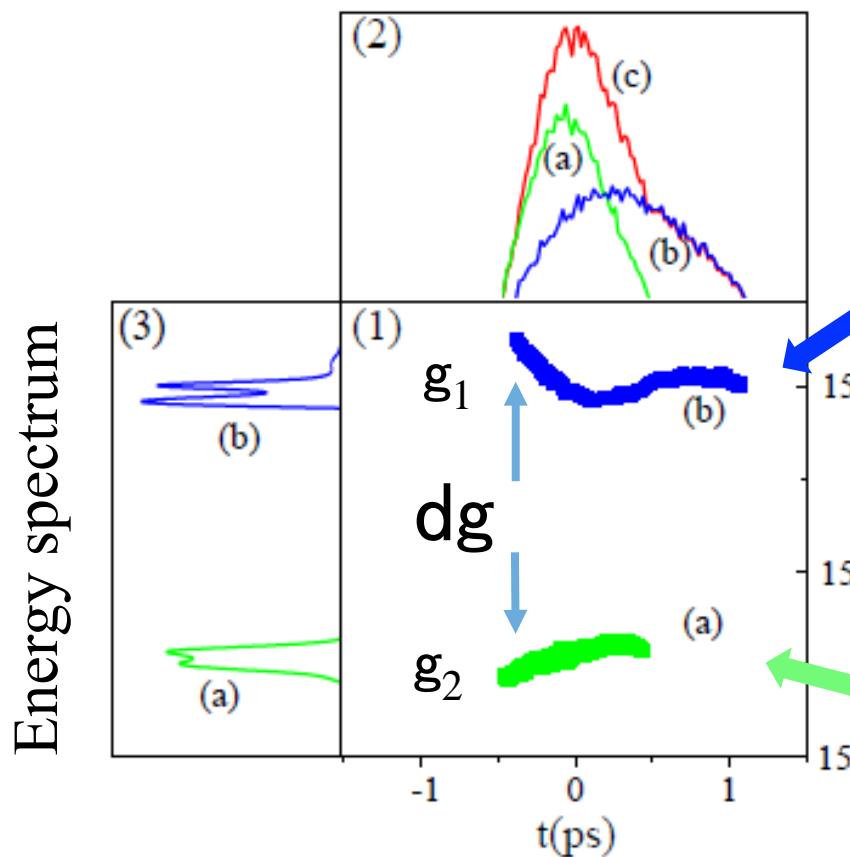
$$\frac{dL_z^{OM,rad}}{dV} \approx \frac{m}{4\pi\omega} |E_y|^2$$

$$L_z^{OM,rad} = 1.7 \times 10^{-27} \text{ J}\cdot\text{s}$$

Electron Energy	25 MeV
Electron Charge	1 nC
Electron Radius	0.1 mm
Electron Length	1 mm
Laser wavelength	800 nm
Laser energy	1 J
Laser waist	0.02 mm
Laser duration	1 ps
Repetition rate	10 Hz

Two color with a two energy e-beam

Electronic current



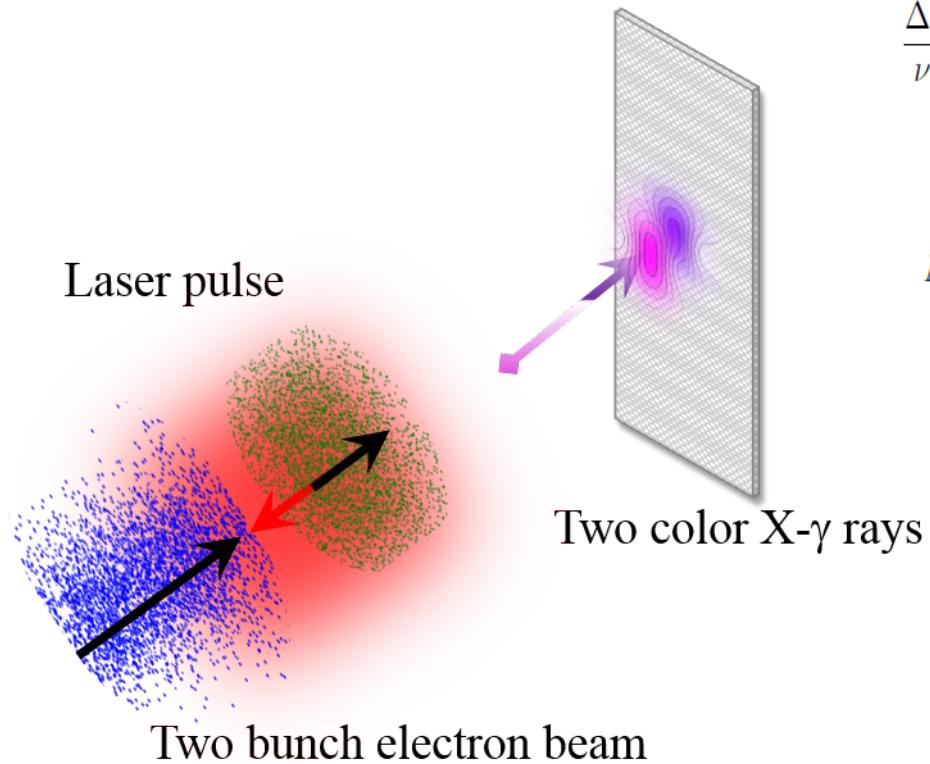
Typical electron phase space of an e-beam
with two energies

$$n_{p,1} = 4n_L g_1^2$$

The total radiation spectrum
is the superposition of the
spectra of the two beamlets

$$n_{p,2} = 4n_L g_2^2$$

Two color: condition on acceptance $Y=qg$

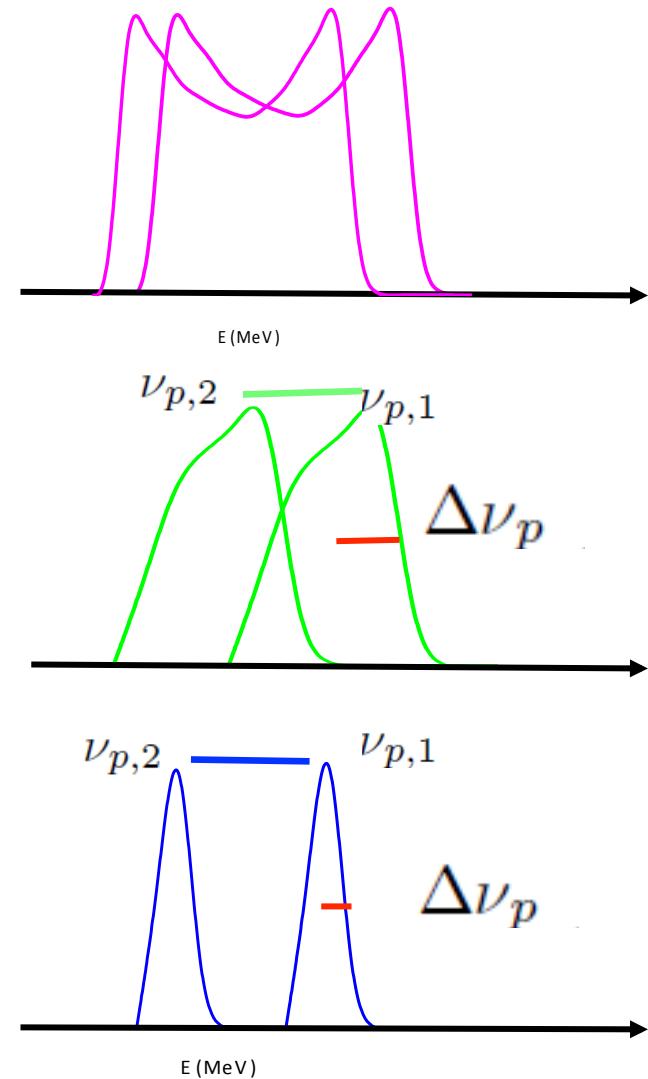


$$\frac{\Delta\nu_p}{\nu_p} \approx \sqrt{0.09\Psi_{max}^4 + \left[\frac{\epsilon_n}{\sigma_x}\right]^4 + \left[\frac{\Delta\gamma}{\gamma}\right]^2 + \left[\frac{\Delta\nu_p}{\nu_p}\right]_L^2}$$

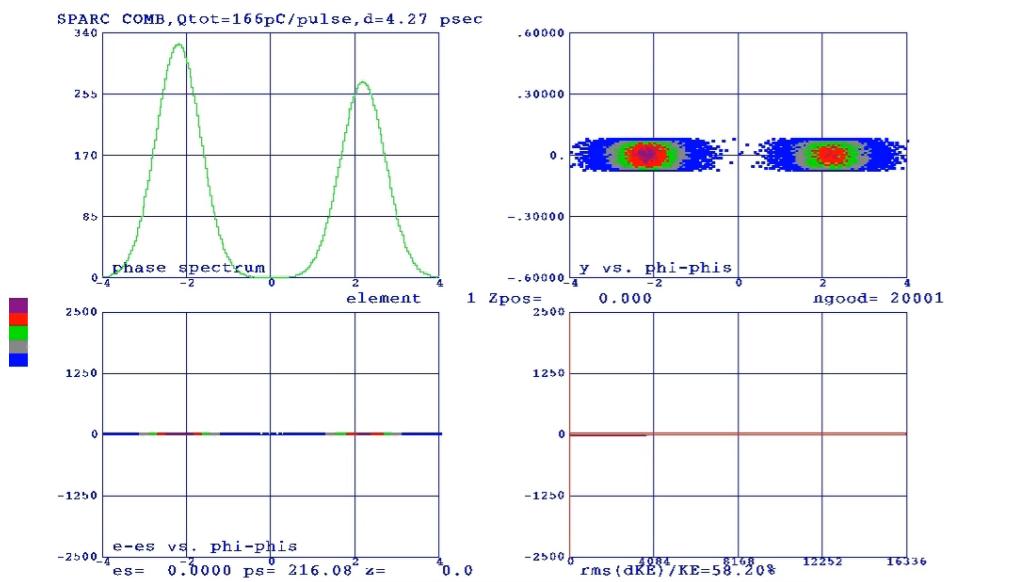
$$N \approx \frac{2 \cdot 10^8 E_L Q \Psi_{max}^2}{h\nu_L \sigma_x^2}$$

$$\frac{2|\delta\gamma|}{\langle\gamma\rangle} \geq \left[\frac{\Delta\nu_p}{\nu_p} \right]_{FWHM}$$

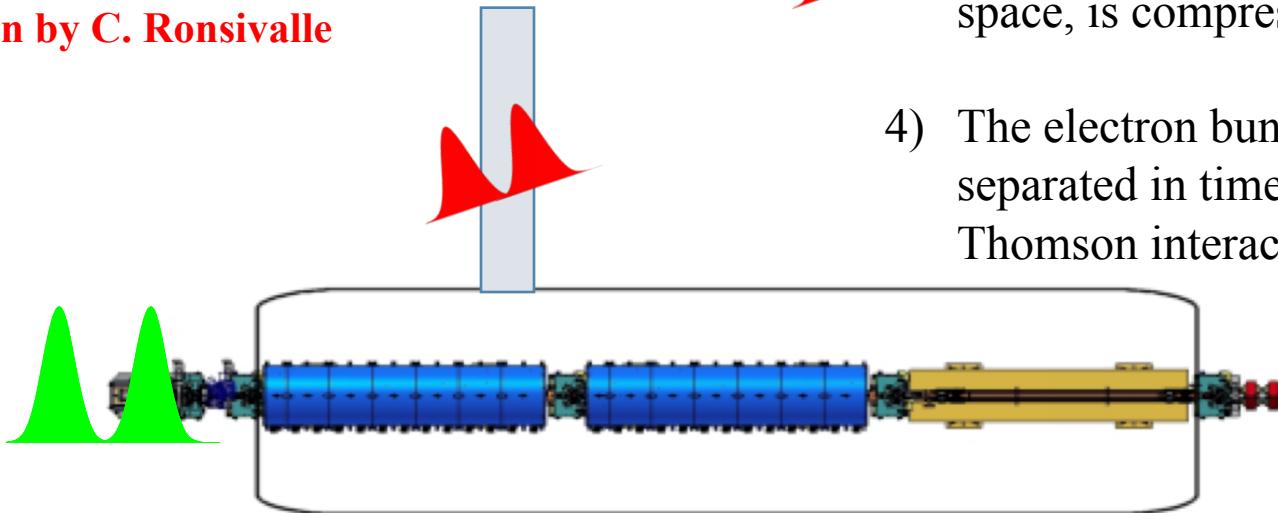
$$\frac{2|\delta\gamma|}{\langle\gamma\rangle} \geq 0.68\Psi_{max}^2$$



Two color: TSTEP simulation



TSTEP simulation by C. Ronsivalle



- 1) Generation of a combed laser pulse by passing the Ti:Sapphire pulse through a birefringent crystal that decomposes the two orthogonal polarizations and introduces a time delay of few ps between them.
- 2) The combed radiation illuminates the cathode and extracts an electron packet with two beamlets.
- 3) The electron bunch is injected in the linac for velocity bunching (injection off crest) and, rotating in the phase space, is compressed and accelerated.
- 4) The electron bunch, composed by two beamlets differently separated in time and energy, could be transported to the Thomson interaction point (IP).

To the Thomson IP

Two color: e-beam data, experiment at SPARC_LAB

Combination of multipulse laser techniques and velocity bunching in the linac

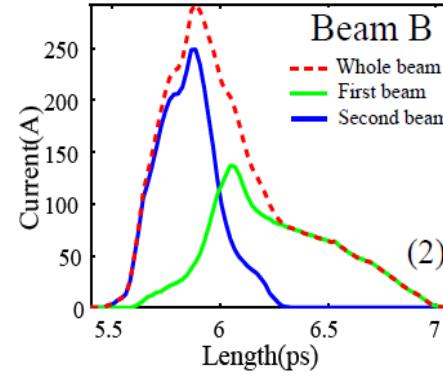
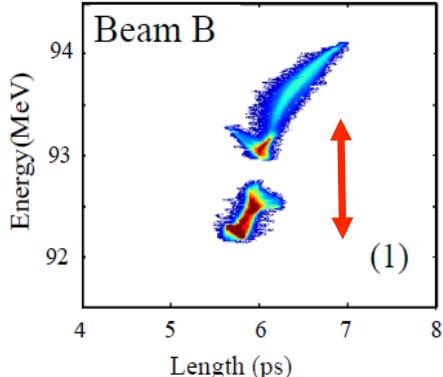
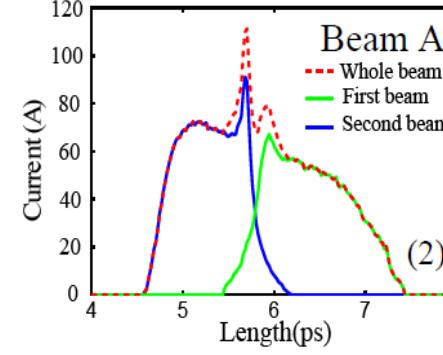
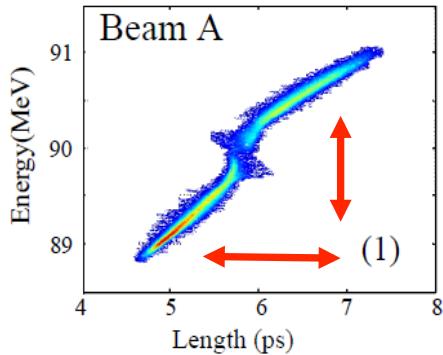
Whole beam

	Beam A	Beam B
Energy	90 MeV	93 MeV
Charge	150 pC	160 pC
Current	120 A	300 A
Energy spread	0.6%	0.6%
Emittance	1.6 mm mrad	1.7 mm mrad
Duration	630 fs	300 fs

Single bunch

Energy separation	1.01 MeV	1.1 MeV
Time separation	0.7 ps	0.4 ps
Energy spread	0.2%	0.3%
Duration Dt	250-400 fs	100-250 fs

Data from  experiments



Large-bandwidth two-color free-electron laser driven by a comb-like electron beam

C. Roncaglia,¹ M.P. Arnone,² A. Bacci,³ M. Bellampalli,⁴ E. Chiarò,⁵ A. Cianchi,⁶ P. Coello,⁷ G. D'Amato,⁸ G. D'Onise,⁹ O. Di Girolamo,¹⁰ G. Di Perio,¹¹ M. Ferrario,¹² G. Gatti,¹³ G. Gatti,¹⁴ L. Giannessi,¹⁵ A. Giudiceo,¹⁶ P. Giordano,¹⁷ L. Palumbo,¹⁸ A. Petrucci,¹⁹ V. Pellegrini,²⁰ P. Picci,²¹ F. Pino,²² G. Rinaldi,²³ J. Rodriguez,²⁴ C. Vaccarezza,²⁵ and P. Vilà²⁶

Nature Institutions and Metrics in Particle Physics A 2017, 2017, 1–10



Laser comb with velocity bunching: Preliminary results at SPARC
M. Ferrario,^{1,2} D. Almeri,³ A. Bacci,³ M. Bellampalli,⁴ P. Calore,⁵ M. Cannillo,⁶ C. Chiarò,⁵ A. Cianchi,⁶ L. Colletta,⁷ G. D'Amato,⁸ P. Faccione,⁹ A. Filippetto,¹⁰ G. Gatti,¹¹ G. Gatti,¹² L. Giannessi,¹³ A. Giudiceo,¹⁴ P. Giordano,¹⁵ L. Palumbo,¹⁶ A. Petrucci,¹⁷ V. Pellegrini,¹⁸ P. Picci,¹⁹ F. Pino,²⁰ G. Rinaldi,²¹ J. Rodriguez,²² C. Vaccarezza,²³ and P. Vilà²⁴

PRB 95, 114108 (2017)

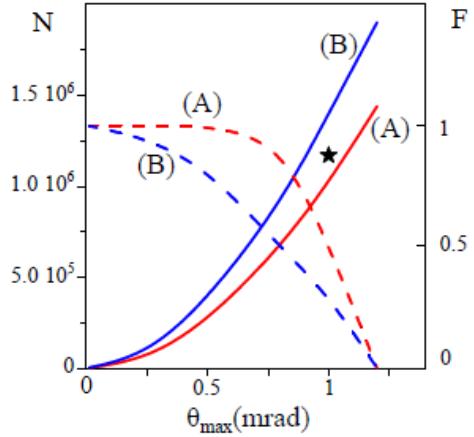
Observation of Time-Domain Modulation of Free-Electron Laser Pulses

by Multipulse Electron Beam Spectroscopy
V. Pellegrini,¹ M.P. Arnone,² A. Bacci,³ M. Bellampalli,⁴ E. Chiarò,⁵ A. Cianchi,⁶ T. Giordano,⁷ G. Gatti,⁸ D. Di Girolamo,⁹ G. Di Perio,¹⁰ M. Ferrario,¹¹ G. Gatti,¹² L. Giannessi,¹³ A. Giudiceo,¹⁴ P. Giordano,¹⁵ R. Pepe,¹⁶ V. Pellegrini,¹⁷ M. Quaranta,¹⁸ C. Roncaglia,¹⁹ A.R. Rossi,²⁰ J. Rodriguez,²¹ L. Senni,²² M. Settina,²³ S. Spatola,²⁴ C. Vaccarezza,²⁵ and P. Vilà²⁶

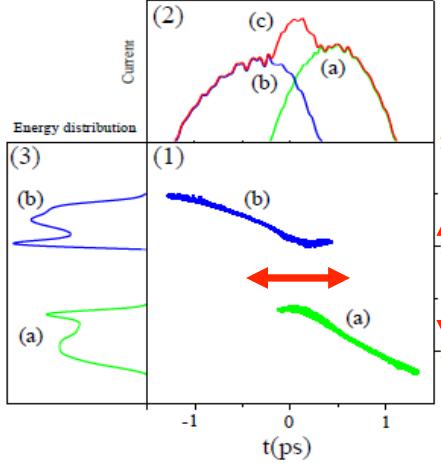
Over compression

Maximum compression

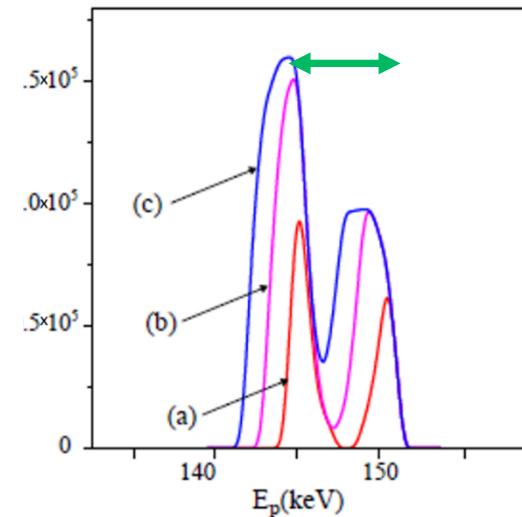
Two color: X rays spectra



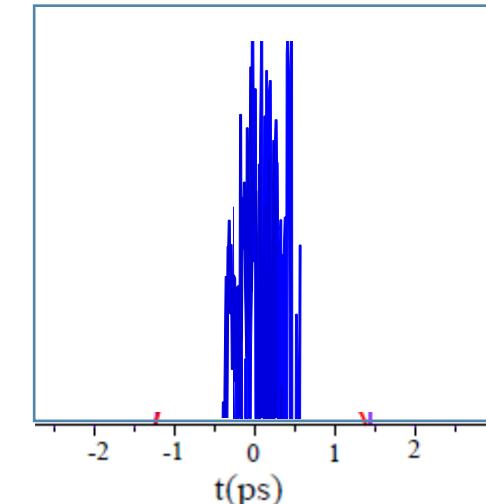
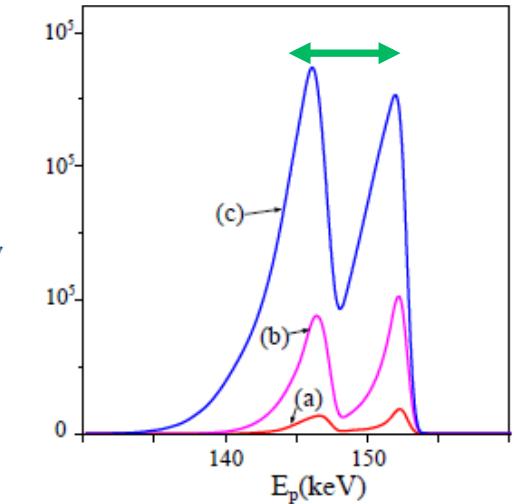
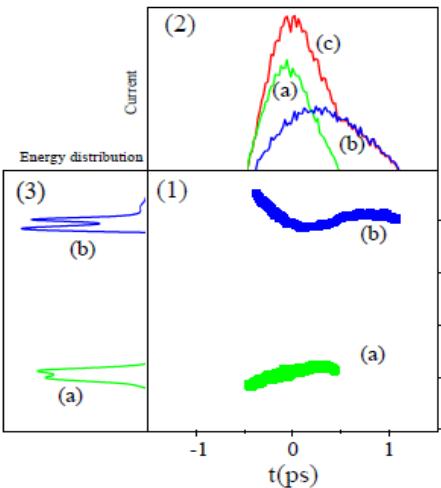
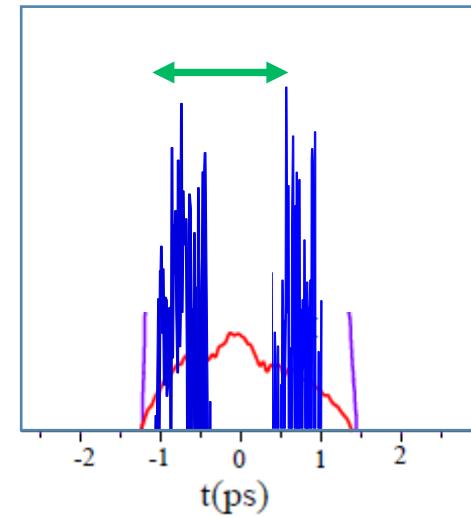
Laser energy	1 J
Waist	25 mm
Time duration	4 ps
Wavelength	800 nm
Photon energy	150 KeV
Photon number	$1.5 \cdot 10^6$
Angle	<1 mrad
Visibility	>80%



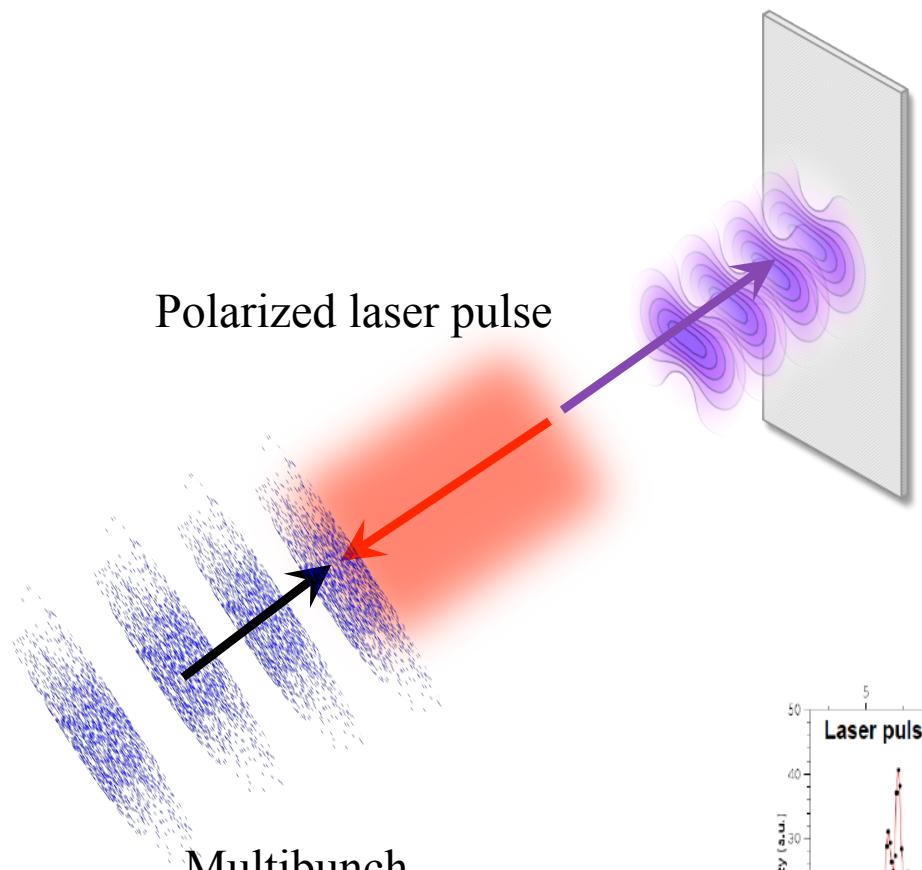
Spectral domain



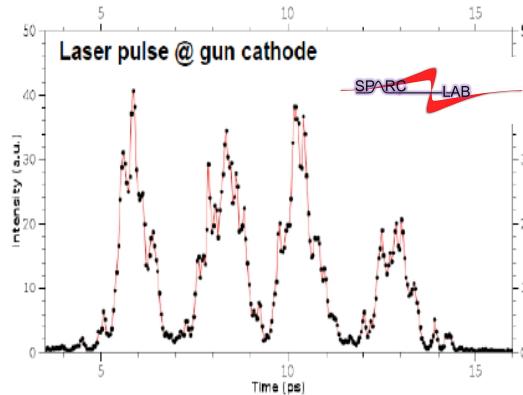
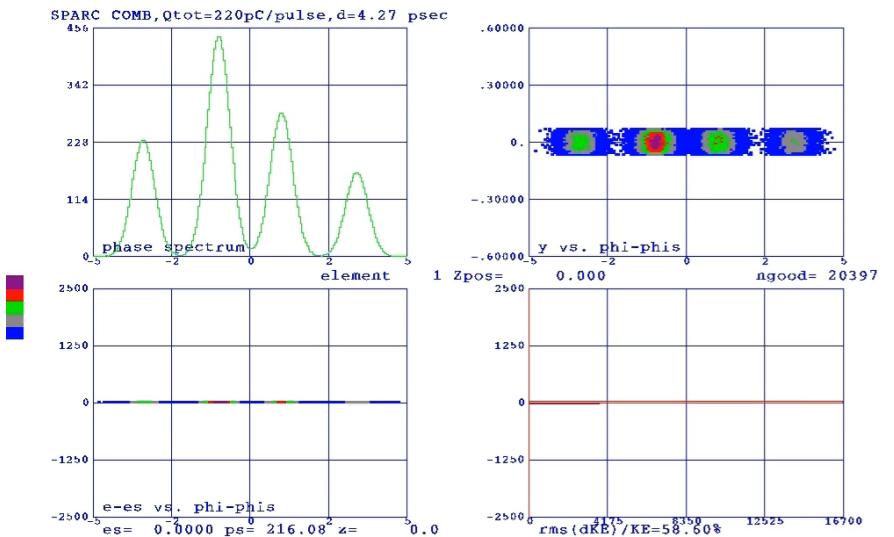
Time domain



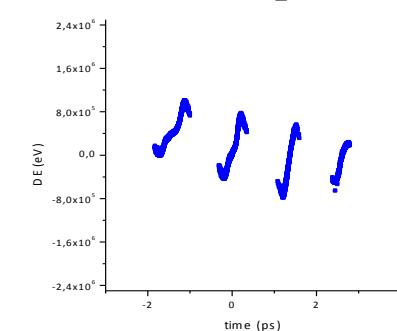
Two color: four bunches



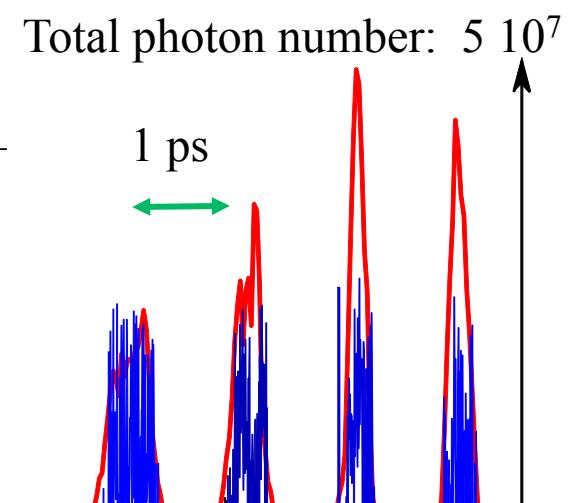
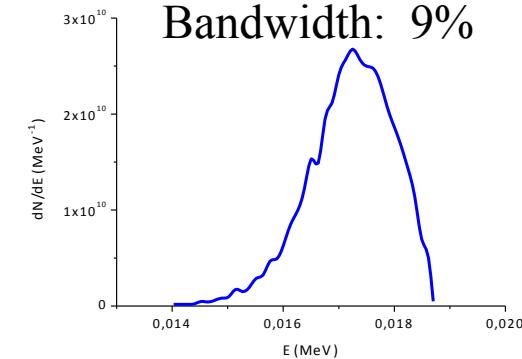
TSTEP simulation by C. Ronsivalle



Electron phase space

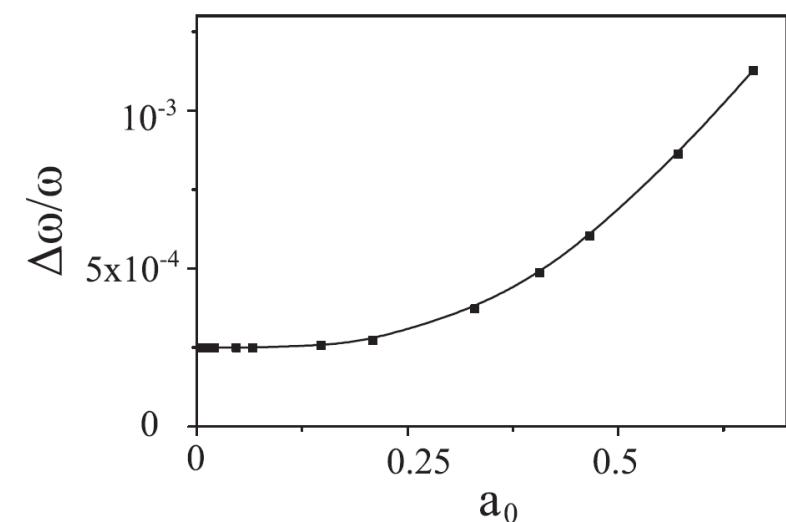
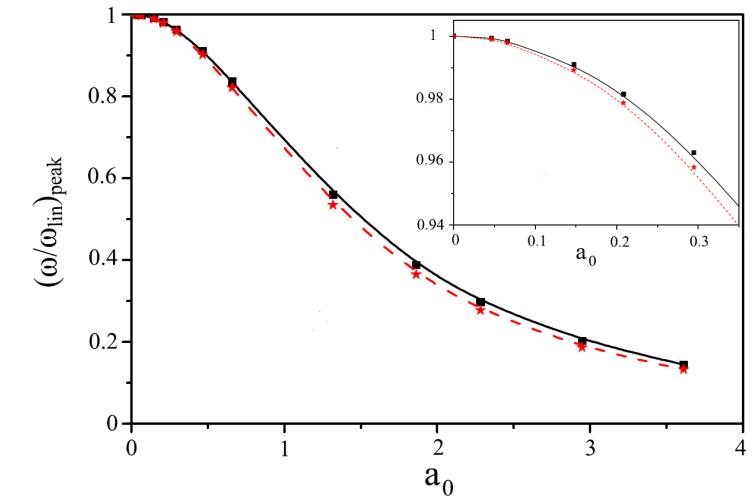
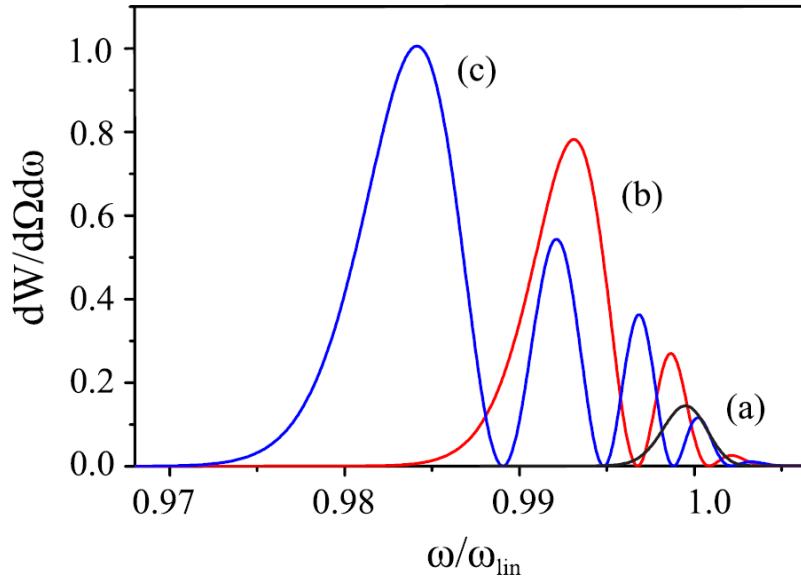
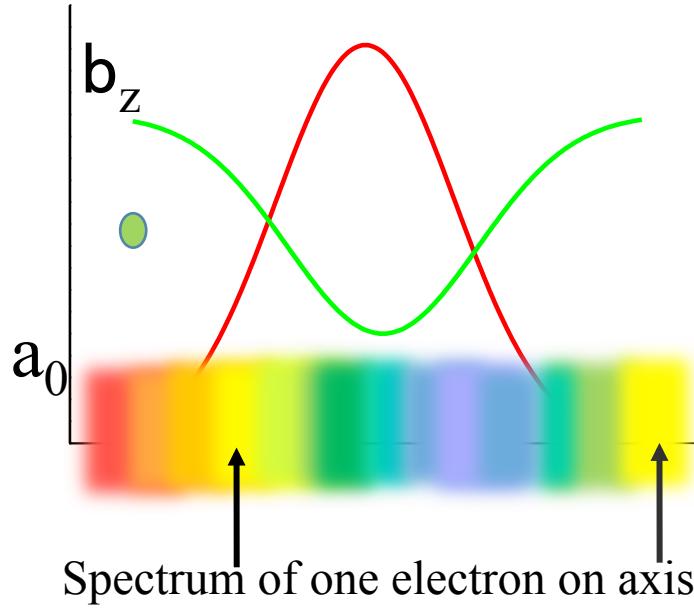


Radiation spectrum



Chirping the laser for enhancing the spectral density

Increasing the laser intensity, the peak frequency shifts towards lower values, the spectrum broadens and secondary peaks appear. $N_{\text{osc}}=240 a_0^2 \text{ Dt(ps)}$



The electron experiences a variable laser parameter

Its longitudinal velocity changes.

$$\omega = \frac{(1+\beta)}{(1-\beta)} \omega_L \quad a_0 = 0.85 I^{1/2}.$$

And therefore also the local emitted frequency changes.

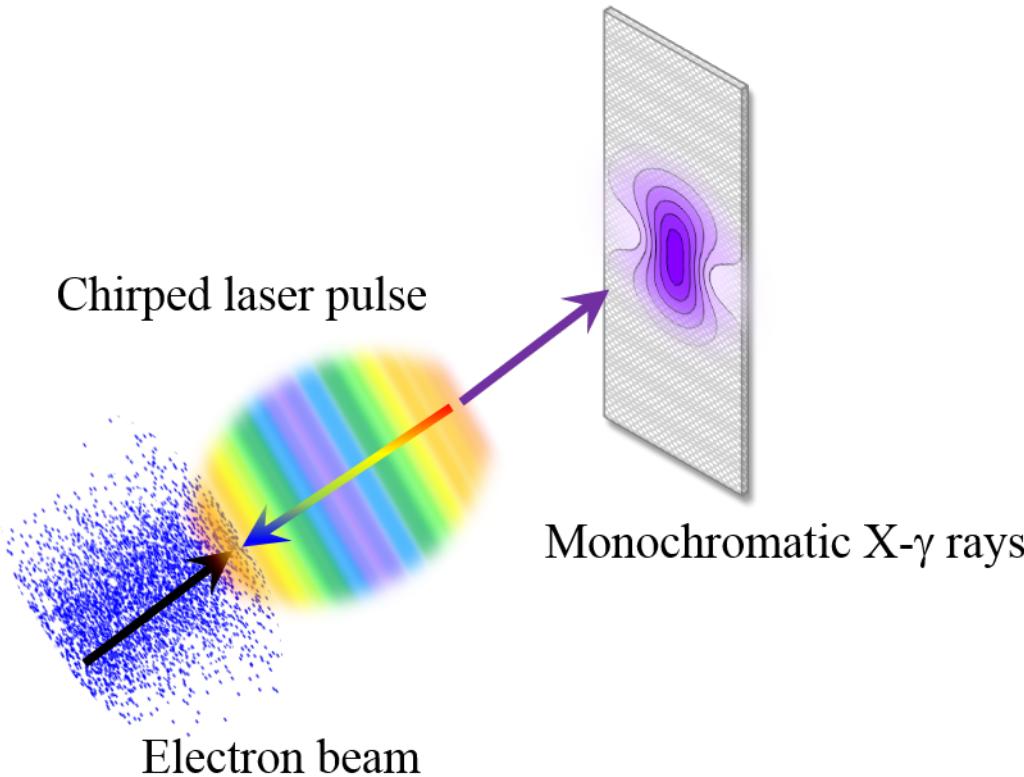
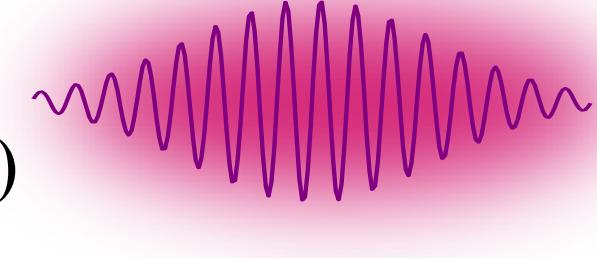
Chirp

The idea is to compensate the dependence on z of b_z by introducing in the laser a longitudinal dependence of $w_L(z+ct)$

$$E(\underline{x}, t) = E_0(\underline{x}, t) \sin \Gamma$$

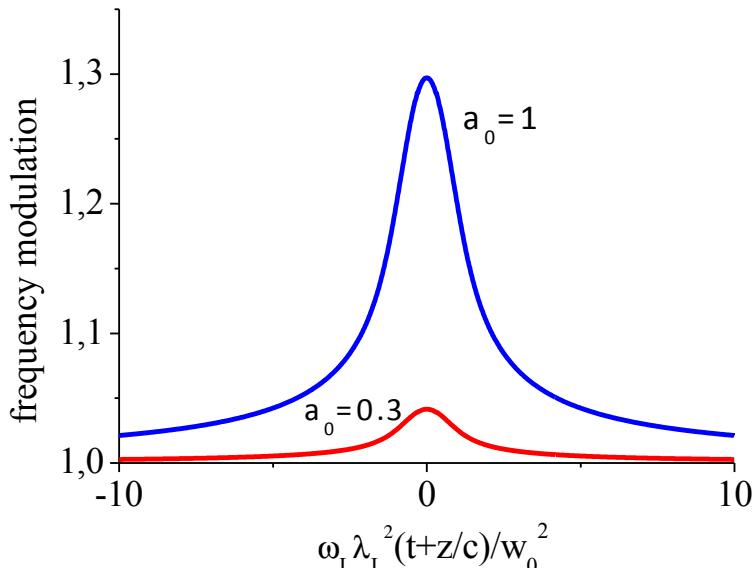
No chirp

$$\Gamma = k_L(z + ct)$$



Chirp

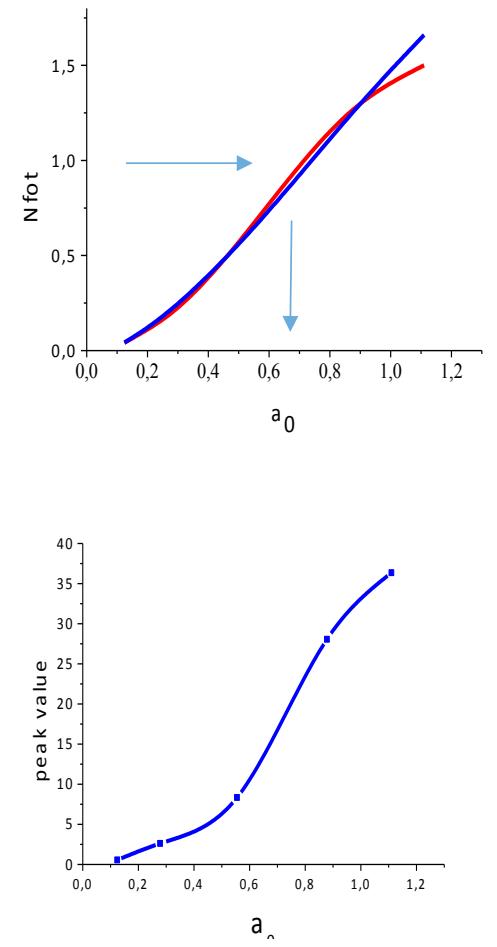
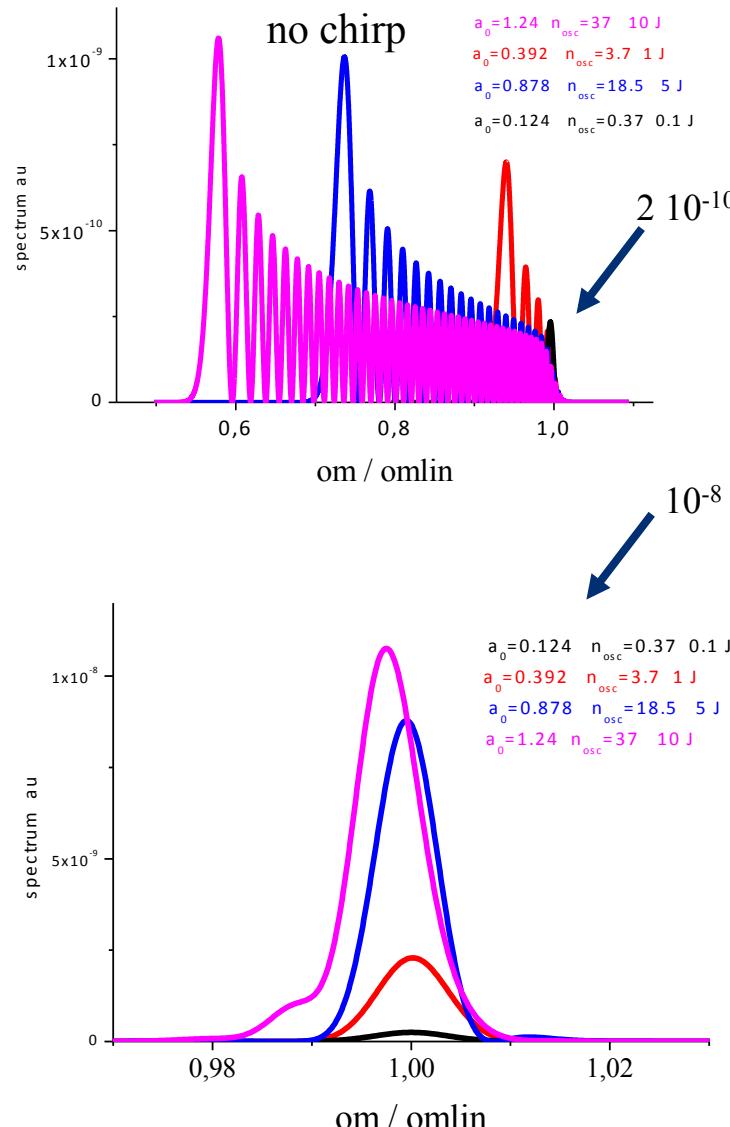
Calculations with the stationary phase method gives the optimum expression of $f(z+ct)$:



The total number of photon increases with a_0 , but is the same with and without chirp.

The brightness increases by 5 order of magnitude.

Spectrum on axis of one electron



Compton enhanced source: collective effects lead to FEL emission

What a challenge!!! So, why studying Optical Undulators ? Compactness of the set-up.
Dimension of the spot. Tunability at high frequency.

In the FEL emission: $\frac{\Delta\lambda}{\lambda} \approx \rho$.

$$\rho = \frac{1}{2\gamma} \left(\frac{I}{I_A} \frac{\lambda_L^2 a_{L0}^2}{4\pi^2 \sigma_x^2} \right)^{1/3} = \frac{Z_R}{L_g} \frac{\lambda_L^2 \gamma^2}{2\pi^2 \sigma_L^2}$$

Condition on emittance: Condition on energy spread:

$$\frac{\Delta\lambda}{\lambda} \approx \frac{\varepsilon_n^2}{\sigma_0^2}$$

$$\boxed{\varepsilon_n < \sigma_0 \sqrt{\rho}}$$

$$\frac{2\Delta\gamma}{\gamma} < \frac{\Delta\lambda}{\lambda} \approx \rho$$

$$\boxed{\frac{\Delta\gamma}{\gamma} < \frac{\rho}{2}}$$

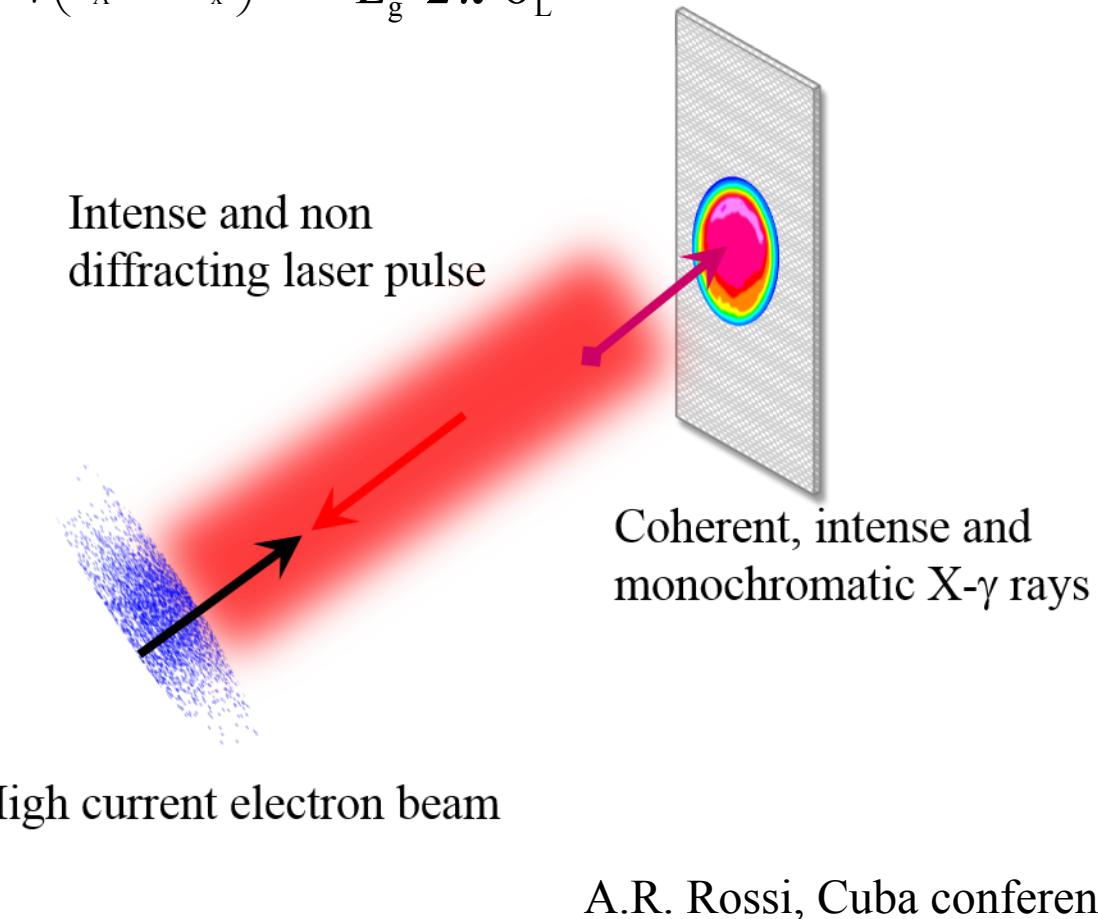
$$\approx \sqrt{\frac{Z_R}{L_g}} \frac{\lambda_L \gamma}{\sqrt{2\pi}} \text{ Pellegrini criterion}$$

Condition on laser profiles :

$$\boxed{\frac{\Delta a_0^2}{a_0^2} < \rho}$$

$$\frac{w_0}{\sigma_e} \geq \frac{\sqrt{2}}{\sqrt{\rho}}$$

$$N_{\text{period}} = \frac{\sigma_{\parallel}}{\lambda_w} \geq \frac{1}{\rho^{3/2}}$$

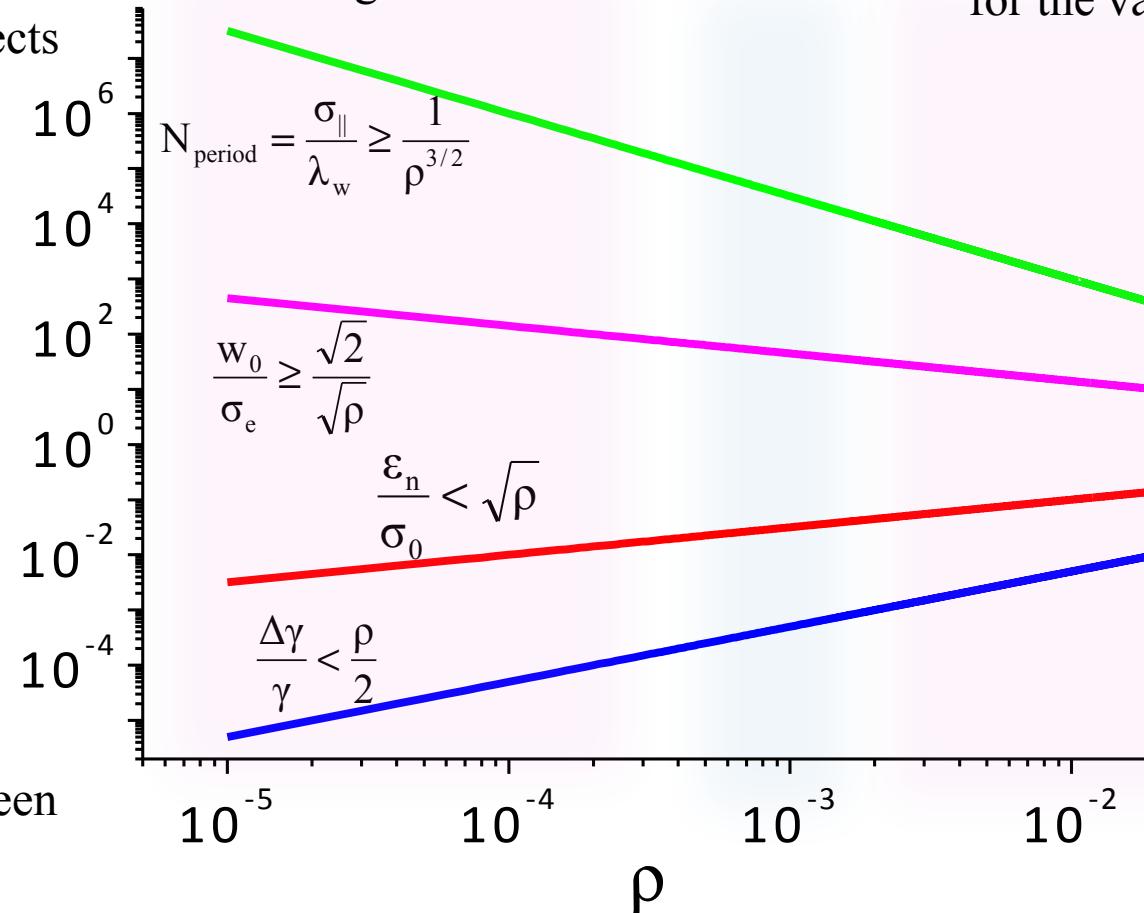


High current electron beam

A.R. Rossi, Cuba conference

High challenge for laser energy,
transverse and inhomogeneous
effects

A,B,C,D
tolerance
factors between
1 and 10



High challenge
for the value of rho

λ_R
laser
 I (A)
 r_b (μm)
 l_b (mm)
 ε_x
 $\Delta E/E$
 γ
 a_{L0}
 ρ (10^{-4})
 L_{1D}
 P (MW)

Linac accelerated beams

12 nm	0.75 m	1.08 Å	1 nm
CO ₂	CO ₂	Ti:Sa	Ti:Sa
150	1000	3000	600
30	25	7	10
1	1	0.3	1
1.06	0.3	0.26–0.8	0.26–0.8
1.3×10^{-4}	10^{-4}	10^{-4}	10^{-4}
16.5	60	55	18,11
0.2	0.3	0.8	0.8
7.01	2.91	3.82	5.36
654 μm	1.57 mm	121 μm	68 μm
0.1–10	1.93	9.4–1.5	1

Plasma accelerated beams

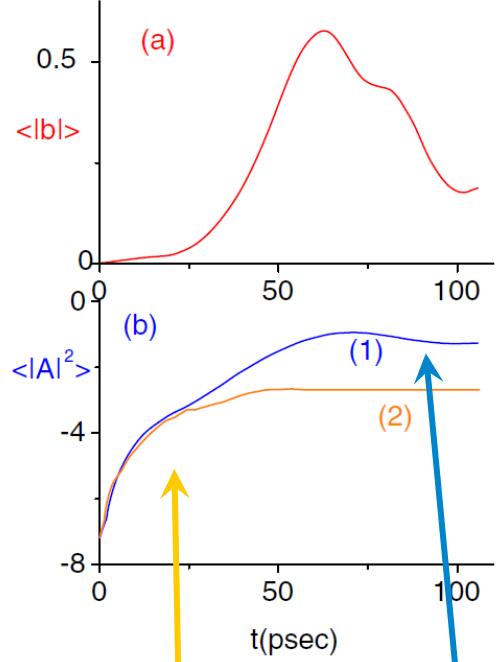
I(kA)	r	g	Dg/g total	s	e	Dg/g slice
20	$3 \cdot 10^{-3}$	55	$2 \cdot 10^{-2}$	5 mm	0.3mm	$3 \cdot 10^{-3}$

ρ	$\Delta\gamma/\gamma$	ε_n/σ_e	w_0/σ_e	$N_L(\text{Gauss}) = \sigma_{\parallel}/\lambda_w$
10^{-4}	$A \times 10^{-4}$	$B \cdot 10^{-2}$	$141/C$	$900000/D$
10^{-3}	$A \times 10^{-3}$	$B \cdot 0.03$	$43/C$	$30000/D$
10^{-2}	$A \times 10^{-2}$	$B \cdot 0.1$	$14/C$	$930/D$

TABLE II. Radiation parameters.

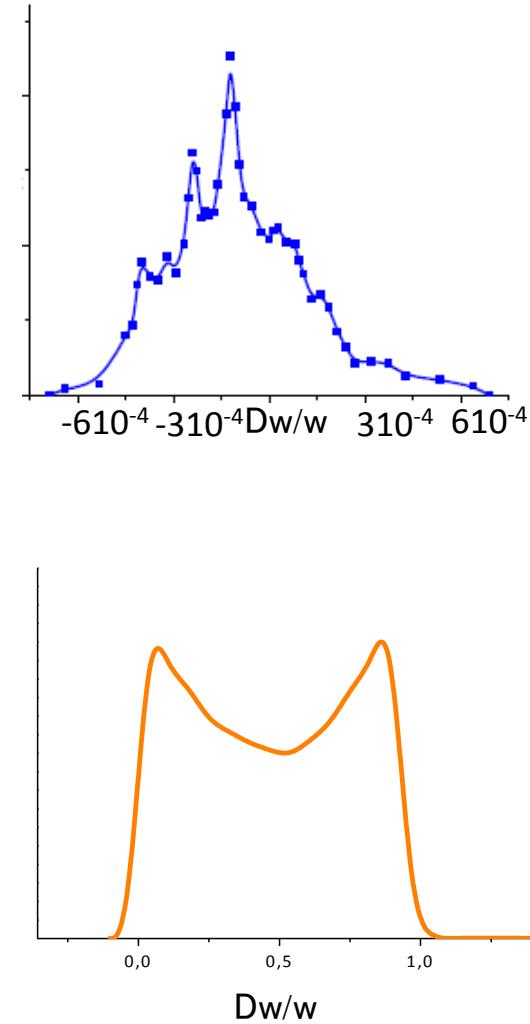
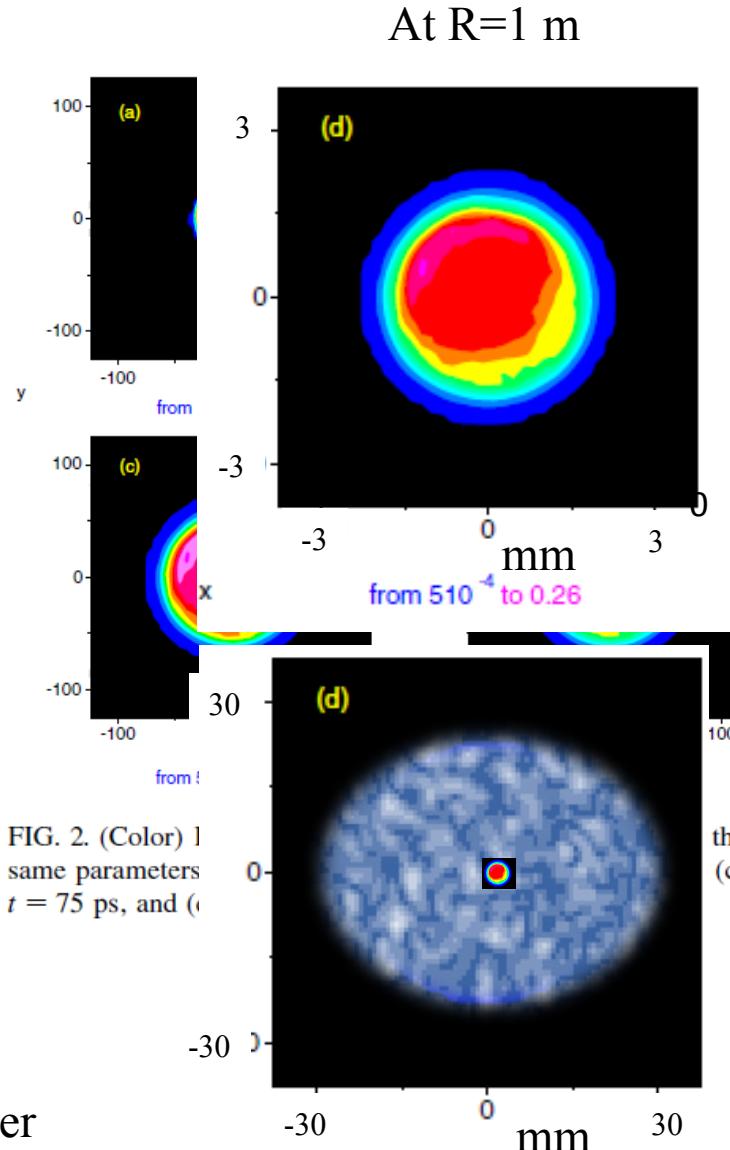
	P_{max} (W)	E (μJ)	L_R (μm)	L_{sat} (mm)	λ_R (nm)	$\delta\lambda_R/\lambda_R$
Case 1	7.5×10^8	0.4	0.5	2.5	1.36	0.82%
Case 2	6×10^8	0.5	0.6	2.7	1.43	0.16%
Case 3						
First peak	2×10^8	0.05	0.05	1	1.35	0.81%
Saturation	1.5×10^8	0.12	0.5	4.5		

Collective effects



Spontaneous emission

FEL emission factor 10^3 larger than SE



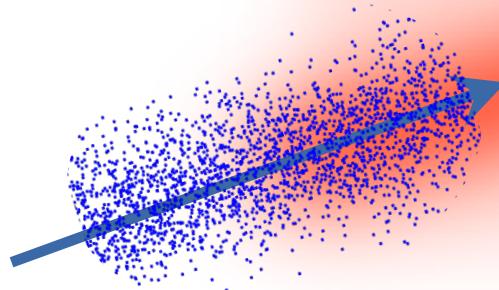
Collective effects

$$\rho = \frac{1}{\gamma} \left(\frac{\omega_p^2 a_{L0}^2}{16 \omega_L^2} \right)^{1/3} = \frac{1}{2\gamma} \left(\frac{I}{I_A} \frac{\lambda_L^2 a_{L0}^2}{4\pi^2 \sigma_x^2} \right)^{1/3}$$

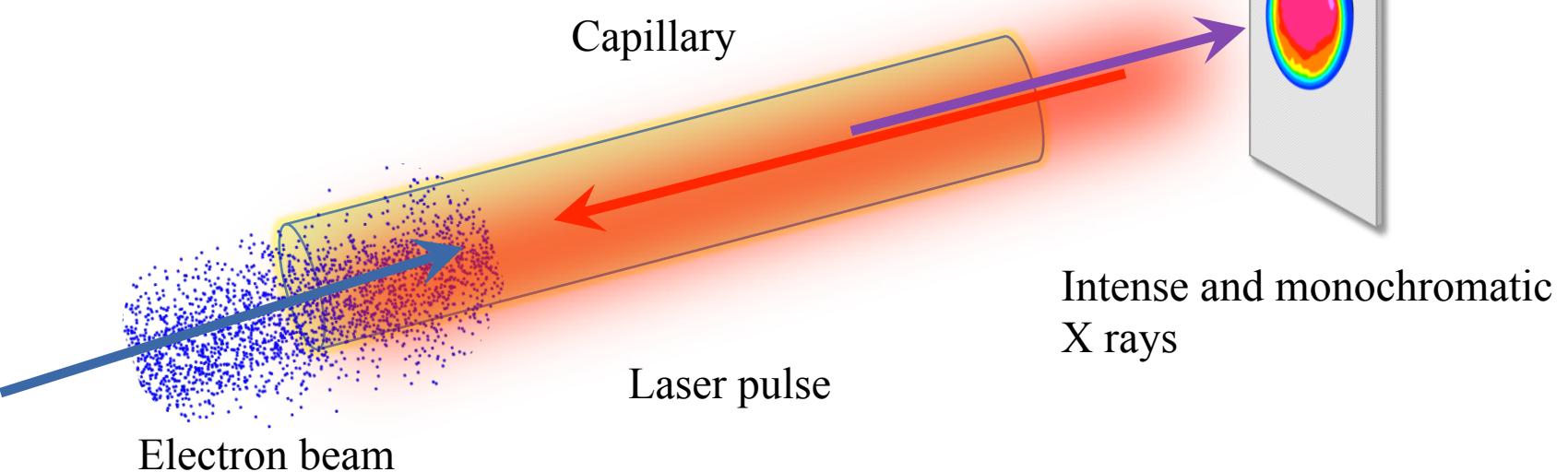
	Number of photons	Bandwidth	Spectral density	Longitudinal Coherence	Transverse Coherence	Divergence
Compton Spontaneous Emission	$N \approx \frac{2 \cdot 10^8 E_L Q \Psi_{max}^2}{h \nu_L \sigma_x^2},$	$\frac{\Delta \nu_p}{\nu_p} \approx \sqrt{0.09 \Psi_{max}^4}$	$\frac{dN}{db} \approx \frac{4.110^8 Q E_L}{h \nu_L \sigma_x^2}$	$L_c \approx \lambda$	$L_c \approx \frac{\lambda R}{\sigma}$	$\sigma' \approx \frac{1}{\gamma}$
Opt. Und. FEL regime	$N \approx \rho \frac{7.810^{11} Q}{h \nu_L 4\gamma}$	$\frac{\Delta \nu_p}{\nu_p} \approx \rho$	$\frac{dN}{db} \approx \frac{7.810^{11} Q}{h \nu_L 4\gamma}$	$L_c \approx \frac{\lambda}{4\pi\sqrt{3}\rho}$	$L_c \approx \frac{\lambda R}{4\pi\sqrt{3}\rho\sigma}$	$\sigma' \approx \frac{\lambda_L}{4\gamma^2 \sigma_e} + \frac{\epsilon_n}{\gamma \sigma_e}$

Ideas for optical undulators

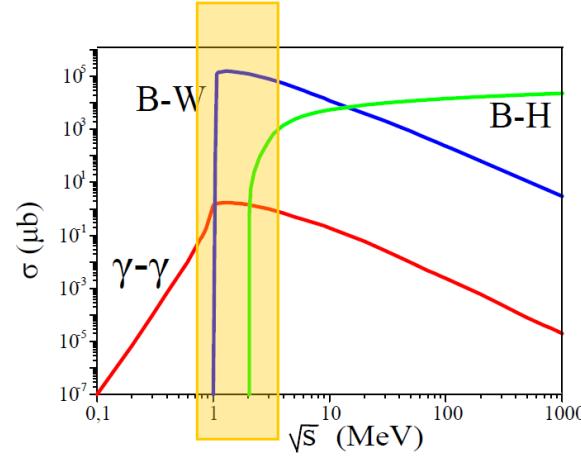
Tilted laser pulse



Electron beam



Electron beam



$g-g$: 1.5 mb @ 1.6 MeV **CAIN simulations**

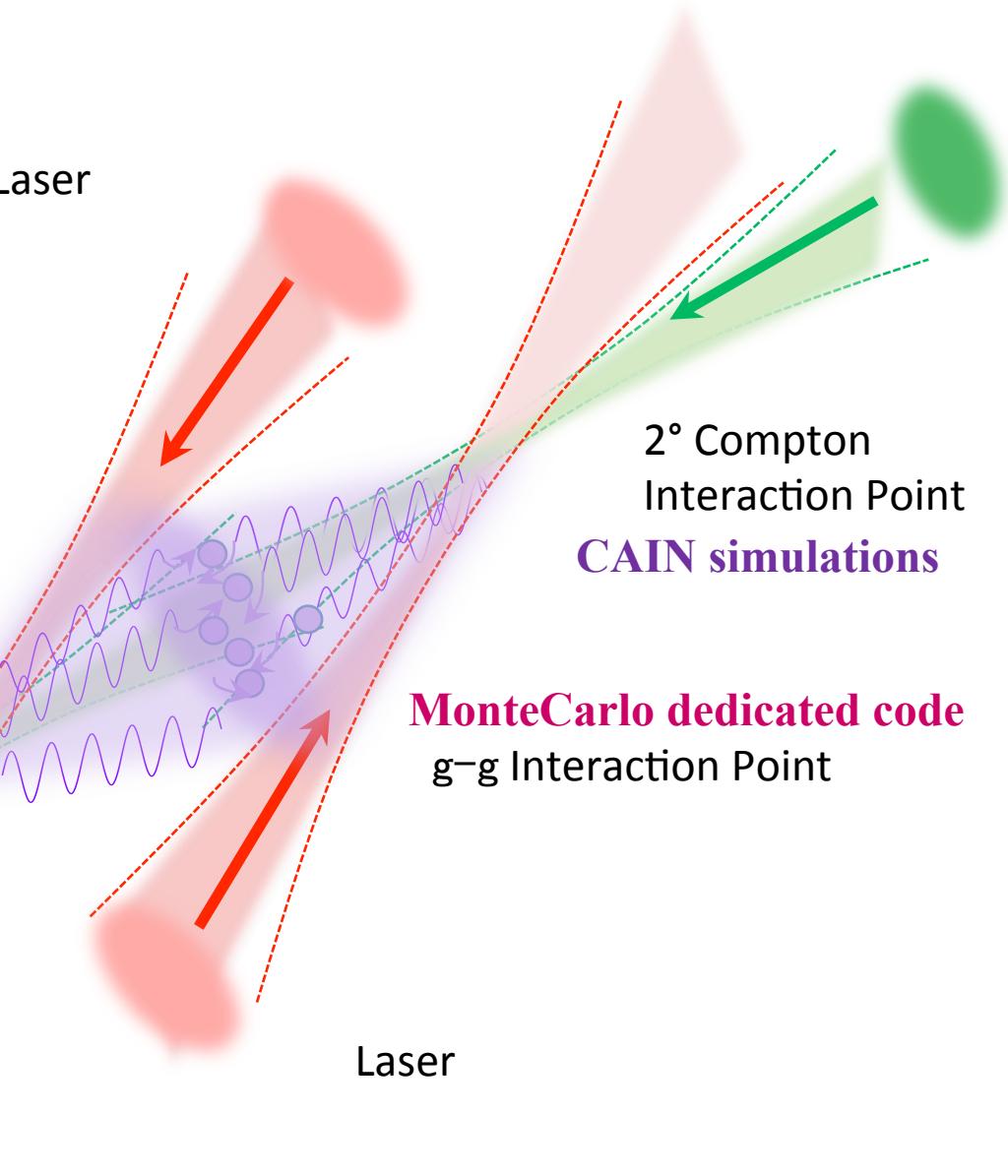
1° Compton
Interaction Point

Electrons

Astra simulations

Laser

Laser



2° Compton
Interaction Point
CAIN simulations

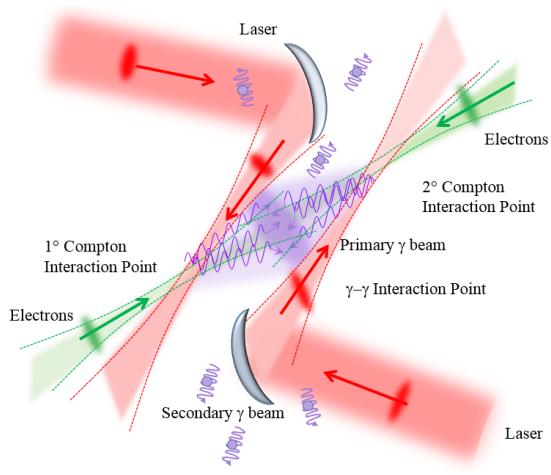
MonteCarlo dedicated code
 $g-g$ Interaction Point

Electrons
Astra simulations

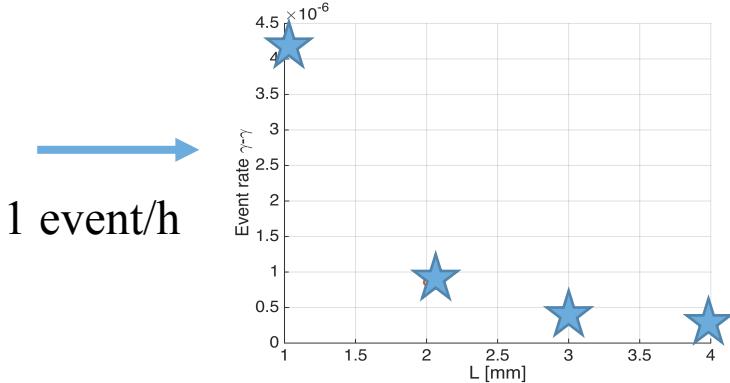
Conclusions

Thank You for the attention

Gamma-gamma collider for the study of g-g events generation



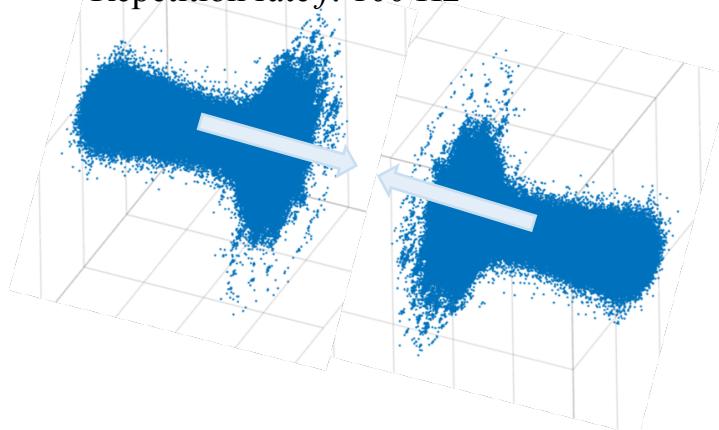
Results of a Monte Carlo dedicated code



$$L \approx 2.7 \cdot 10^{26} \text{ cm}^{-2}/\text{s}$$

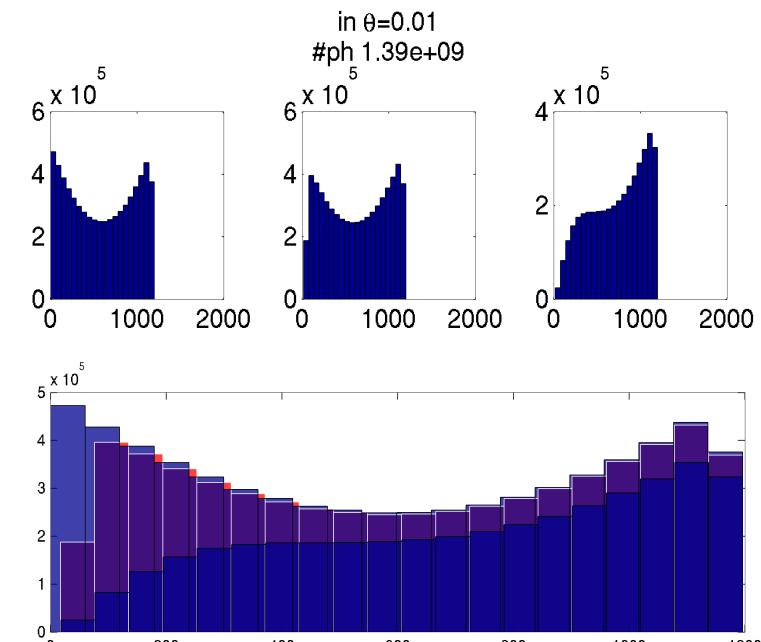
Parameter of the Compton sources

Total energy of the g-g system: 2 MeV
Electron energy: 250 MeV
Electron emittance: 0.4 mm mrad
Electron energy spread: $0.7 \cdot 10^{-4}$
Charge: 250 pC
Transverse electron width: 1 mm
Laser wavelength: 1000 nm
Laser waist: 10 micron
Laser Energy: 1 J
Photon energy: 1 MeV
Transverse photon beam dimension: 1 mm
Transverse photon beam dimension at IP: 10 mm
Repetition rate f : 100 Hz



See poster section

ELI-NP-like Compton sources focused at 1 mm give $1.5 \cdot 10^9$ primary photons at 1 MeV.



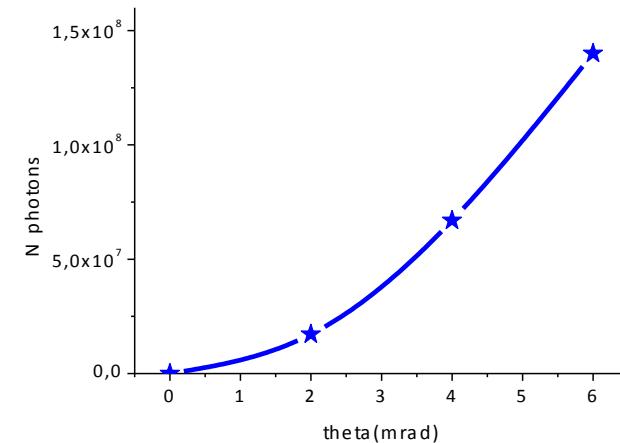
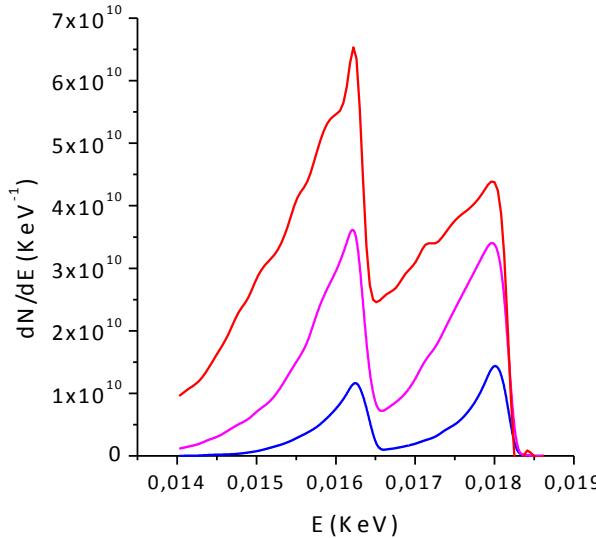
Two color: spectra at 30 MeV

$$N \approx \frac{2 \cdot 10^8 E_L Q \Psi_{\max}^2}{h\nu_L \sigma_x^2} \approx \frac{0.29 \cdot 10^9 E_L Q}{h\nu_L \sigma_x^2} \frac{|\nu_{p,1} - \nu_{p,2}|}{\langle \nu_p \rangle}$$

favourable scaling

Acceptance angle: 2 mrad, 4 mrad, 6 mrad

>95% linear polarization



Laser energy	5 J
Waist	25 mm
Time duration	6 ps
Wavelength	800 nm

Photon energy	18 KeV
Photon number	1 10⁸
Angle	<4 mrad
Visibility	>80%

The factor ρ is about 3.8×10^{-4} , and the radiation wavelength is about $\lambda_R = 1.1 \text{ \AA}$. In this case we are at the limit of validity of the classical model, because the quantum factor q is 0.9, and quantum effects, arising when $q > 1$, can play an important role [16,17]. However, the previous condition on q relies on one-dimensional models. Three-dimensional considerations [18] seem to point out a relaxation of the above condition due to the enlargement of the bandwidth associated to non-ideal and geometrical effects so that the requirement $q > 1$ should be rather replaced by $q\rho > \max(\rho, \Delta\gamma/\gamma, \epsilon_{n,x}^2/\sigma_x^2)$, where $q\rho$ is the relative energy separation between the quantum lines, ρ is the one-dimensional natural bandwidth and $\Delta\gamma/\gamma$ and $\epsilon_{n,x}^2/\sigma_x^2$ are, respectively, the inhomogeneous line broadening due to energy spread and emittance effects [19]. In our case, we have $q\rho = 3.5 \times 10^{-4}$, but for the case (a) $\epsilon_{n,x}^2/\sigma_x^2$ never goes under 7×10^{-4} . The cases with larger emittance are, in this sense, even less critical respect to the presence of quantum effects. The cases presented require an amount of laser power still outside the present status of the art, but achievable in the near future [20]. In fact, for instance, in the case (b) with emittance $\epsilon_x = 0.54 \text{ mm mrad}$, at saturation the beam has a maximum radius of about $15 \mu\text{m}$; assuming for the laser in the waist a spot size of $20 \mu\text{m}$, we obtain the needed laser power of more than 17 TW for at least 1.5 mm , corresponding to a total laser energy of about 85 J .

a.