Galactic cosmic rays phenomenology:

nuclei, antimatter, dark matter

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1. What are cosmic rays (CRs)

2. Searches for dark matter in CRs

3. Cross sections for CR phenomenology

CHARGED (GALACTIC) COSMIC RAYS

are charged particles (nuclei, isotopes, leptons, antiparticles)

diffusing in the galactic magnetic field

Observed at Earth with E~ 10 MeV/n - 10³ TeV/n

1. SOURCES

<u>PRIMARIES</u>: directly produced in their sources <u>SECONDARIES</u>: produced by spallation reactions of primaries on the interstellar medium (ISM)

2. ACCELERATION

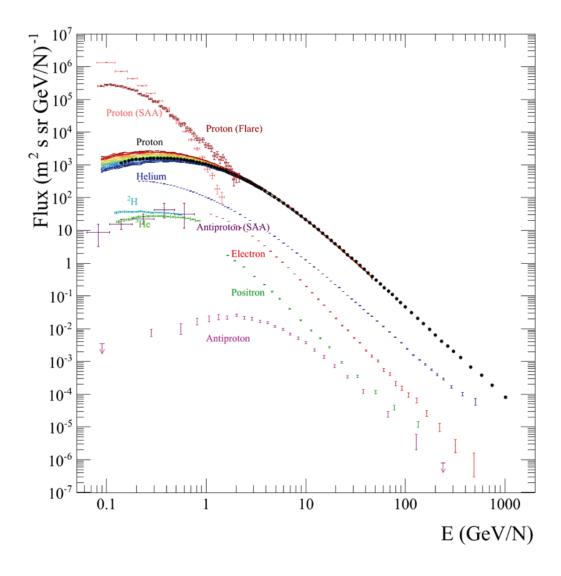
SNR are considered the powerhouses for CRs. They can accelerate particles at least up to 10^2 TeV

3. PROPAGATION

CRs are diffused in the Galaxy by the inhomogeneities of the galactic magnetic field.

+ loose/gain energy with different mechanisms

All particle spectra (from Pamela experiment)



Credits: Valerio Formato & Mirko Boezio, Pamela Collaboration, 2013

Transport equation in diffusion models

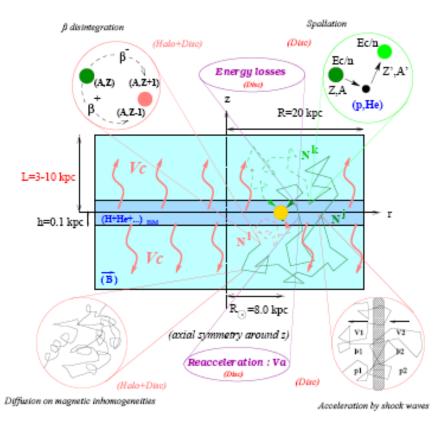
$$\begin{array}{c|c} \text{Diffusion} & \textit{Convection} \\ -\vec{\nabla} \left[K \vec{\nabla} N^j(E) - \vec{V_c} N^j(E) \right] - \Gamma^j N^j \\ \\ -\frac{(\vec{\nabla}.\vec{V_c})}{3} \frac{\partial}{\partial E} \left[\frac{p^2}{E} N^j(E) \right] = \mathcal{Q}^j(E) + \\ \\ \frac{\partial}{\partial E} \left[-b_{\text{tot}}(E) N^j(E) + \beta^2 K_{pp} \frac{\partial N^j(E)}{\partial E} \right] \\ \\ \text{Eneegy losses (EM)} & \text{Reacceleration} \end{array} \tag{CR sources: primaries, secondaries} \\ \text{(spallations)}$$

- DESTRUCTION: $\Gamma = n_{ISM} v \sigma_R$, $\sigma_{R} = \sigma^{tot} \sigma^{tot}_{el}$
- 2. SOURCES: $Q^j \equiv q_0^j Q(E) \hat{q}_i + \sum_k^{m_k > m_j} \tilde{\Gamma}^{kj} N_i^k(0)$

production in SNR

Primary Secondary production by fragmentation of heavier nuclei

Cosmic antimatter fluxes from DM annihilation in the Milky Way halo

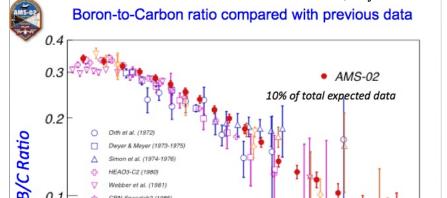


AMS data on CRs: great step forward for fixing Propagation and source models!

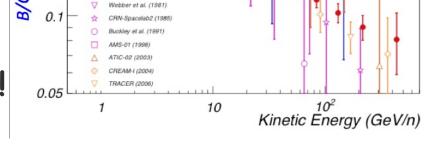
Diffusive models for CR propagation in the Galaxy

Jopikii & Parker 1970; Ptuskin & Ginzburg, 1976; Ginzburg, Khazan & Ptuskin 1980; Weber, Lee & Gupta 1992,;

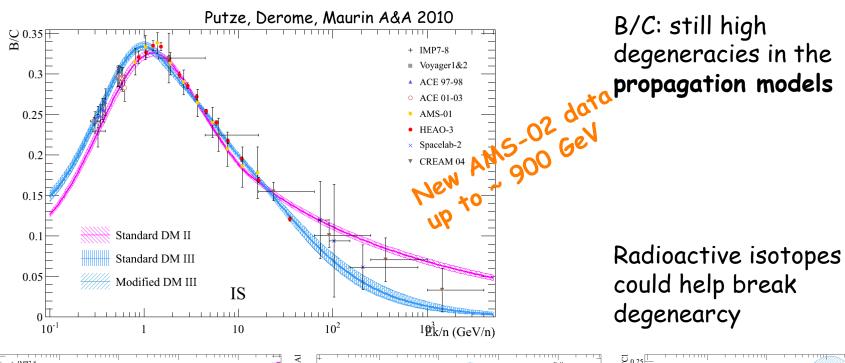
Maurin, FD, Taillet, Salati 2001; Maurin, Taillet, FD 2002; Putze, Derome, Maurin 2010; Strong & Moskalenko 1998; Moskalenko, Strong, Ormes, Potgieter, 2002; Shibata, Hareyama, Nakazawa, Saito 2004; 2006;); Evoli, Gaggero, Grasso, Maccione 2008; Di Bernardo et al. 2010; ...



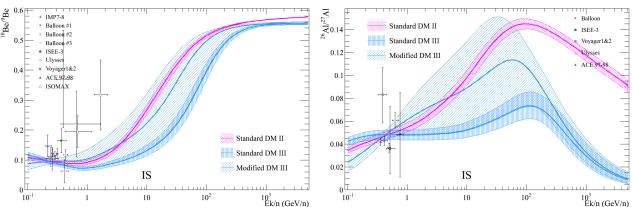
AMS Coll. ICRC July 2013

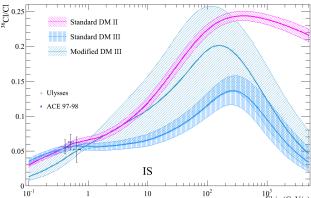


Propagation of CRs: DATA and MODELS BORON/CARBON (B/C): A "STANDARD CANDLE"



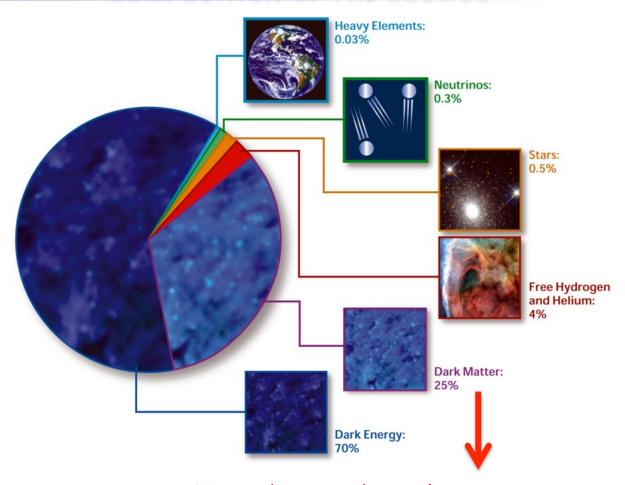
Radioactive isotopes could help break degenearcy





The composition of the Universe

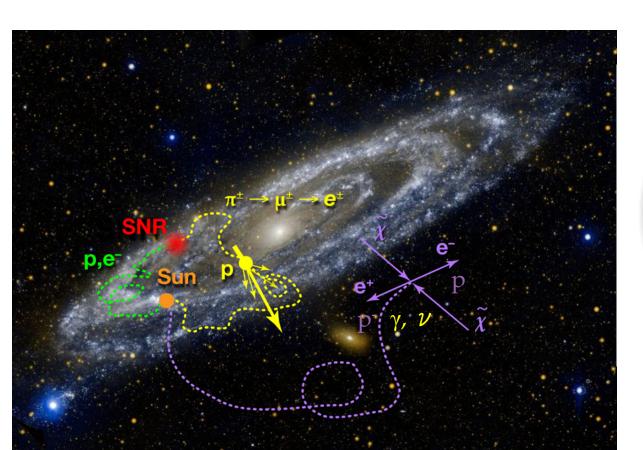
COMPOSITION OF THE COSMOS

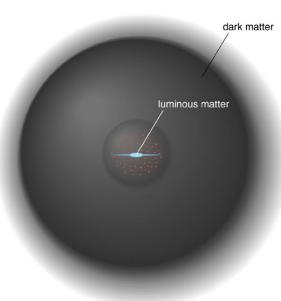


Hypothesis: the solution is a particle, a WIMP (weakly interacting massive particle)

Indirect DARK MATTER searches

Dark matter can annihilate in pairs with standard model final states. Low background expected for ANTIMATTER, and for neutrinos and gamma rays coming from dense DM sites





WIMP Dark Matter Indirect Searches

Annihilation inside celestial bodies:

$$\rightarrow$$
 ν at ν telescopes as up-going μ 's

$$\Phi_{\mu}^{(\text{Earth,Sun})} \propto <\sigma_{\text{ann}}v>\frac{\rho_{\chi}}{m_{\chi}}$$

Annihilation in the galactic halo(s):

$$\rightarrow$$
 Photons (γ -rays, radio,...)

$$\rightarrow e^+, \ \overline{p}, \ \overline{D}$$

$$\Phi^{(\bar{p},\bar{D},e^+,\gamma)} \propto <\sigma_{\rm ann}v> \left(\frac{\rho_\chi}{m_\chi}\right)^2$$

v and γ keep directionality

can be detected only if emitted from high χ density regions

Clue is DM space distribution $\rho(r)$

Charged particles diffuse in the galactic halo

antimatter searched as rare components in cosmic rays (CRs)

Clue is the astrophysics of charged cosmic rays

N.B. New particles are searched at colliders but we cannot say anything about being the solution to the **DM** in the Universe!

The case for

antiprotons

Cosmic antiprotons

Antiprotons are produced in the Galaxy by <u>fragmentation</u> of proton and He (and marginally heavier nuclei) on the ISM (secondary antiprotons).

These antiprotons would be the background to an exotic component due to

dark matter annihilation

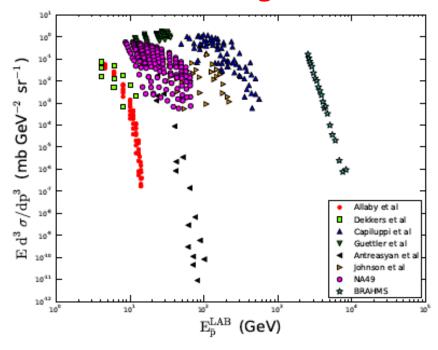
in the galactic halo (primary antiprotons).

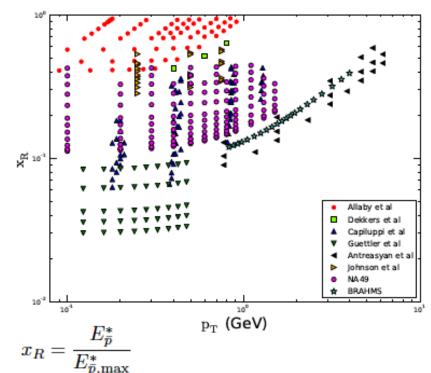
N. B. Thousands of cosmic antiprotons have already been detected by balloon-borne (Bess, Caprice,...) or satellite experiments (Pamela), and AMS-01, and 290000 (out of 54 billion events) from AMS-02 on the ISS

New analysis of p-p-ppbar data Di Mauro, FD, Goudelis, Serpico PRD 2014, 1408.0288; Kappl, Winkler 1408.0299, JCAP2014

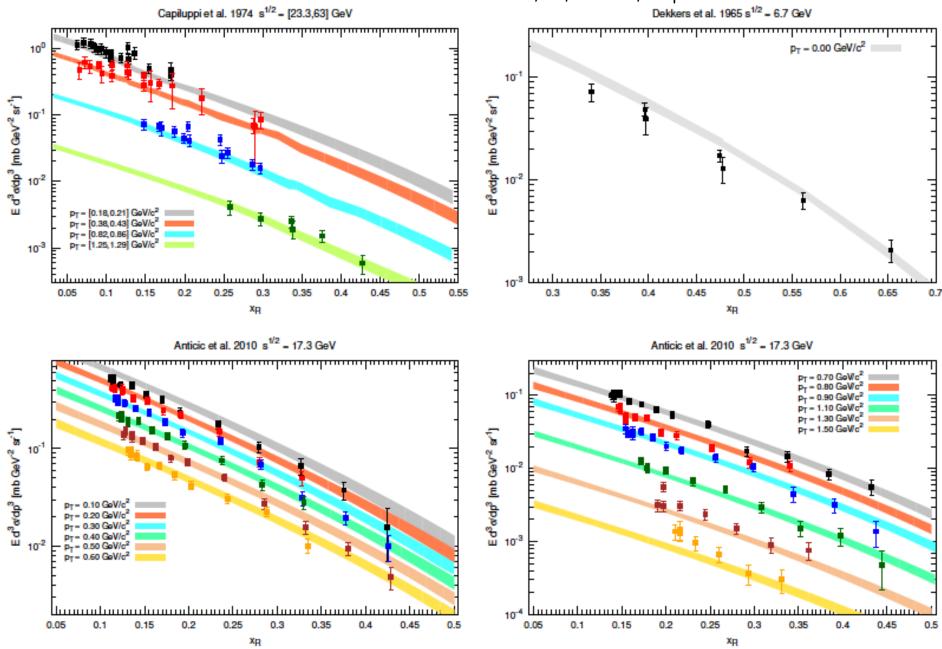
$$q_{\bar{p}}^{pp}(E_{\bar{p}}) = \int_{E_{\text{th}}}^{+\infty} \frac{d\sigma_{p\,p\to\bar{p}}}{dE_{\bar{p}}} (E_p, E_{\bar{p}}) n_H (4\pi\Phi_p(E_p)) dE_p$$

Existing data on the production cross section

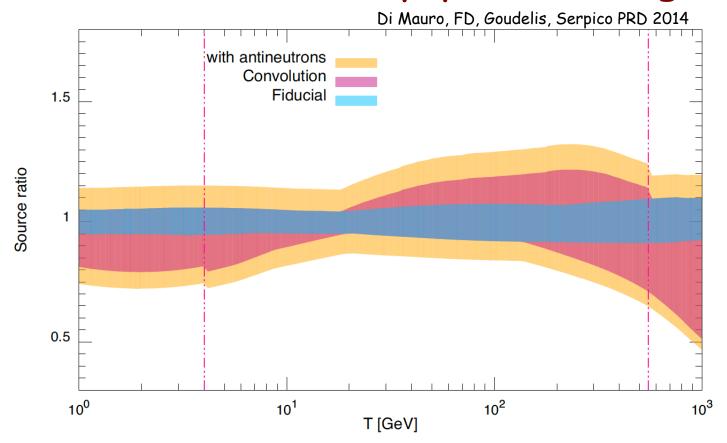




Di Mauro, FD, Goudelis, Serpico PRD 2014



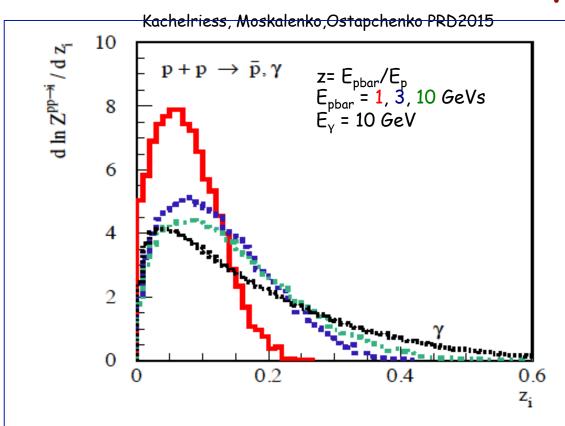
Uncertainties due p-p scattering



Uncertainties in the pbar production spectrum from p-p scattering are at least 10%.

Conservative: 20% at low energies (GeV) up to 50% (TeV) (data expected at least up to ~ 500 GeV)

Protons → antiprotons



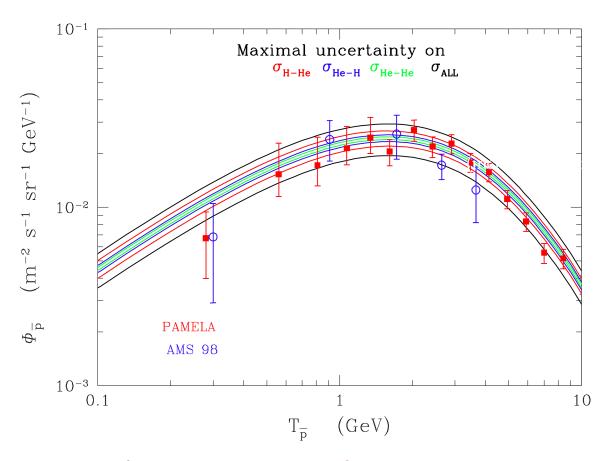
The bulk of antiprotons is produced by **protons** with kinetic energy 10-30 times greater

AMS energies ~ 1-500 GeV in $E_{pbar} \rightarrow$

Proton energies with ~ few GeV - 10 TeV

Uncertainties on the antiproton flux from nuclear cross sections

(Donato+ ApJ 2001, PRL 2009)

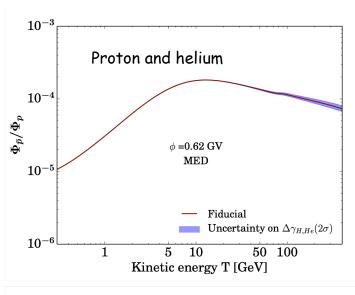


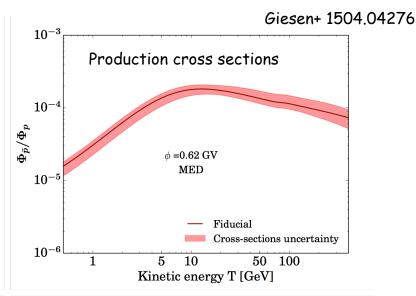
- pp: Tan& Ng
- H-He, He-H, He-He: DTUNUC MC
- Functional form for the cross section derived from other reactions, given
 NO DATA!!

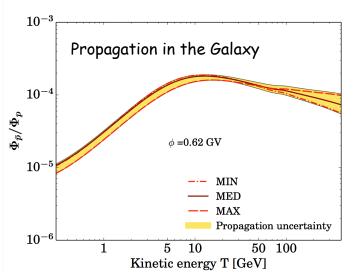
Maximal uncertainty from p-He cross sections: 20-25%!

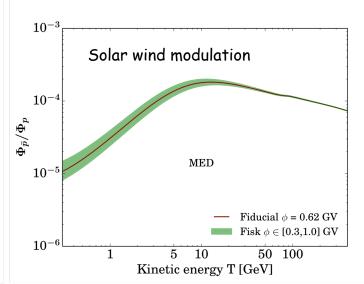
Data from AMS-02 on cosmic antiprotons are at ~ 10% accuracy

Secondary antiprotons: theoretical uncertainties

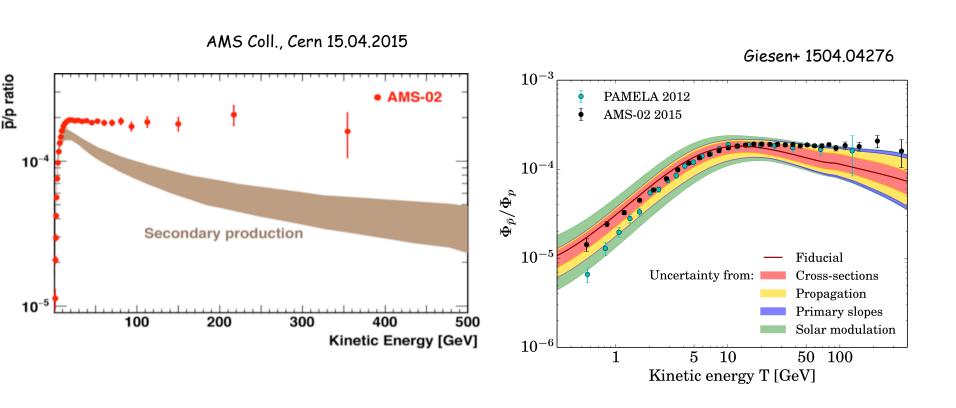








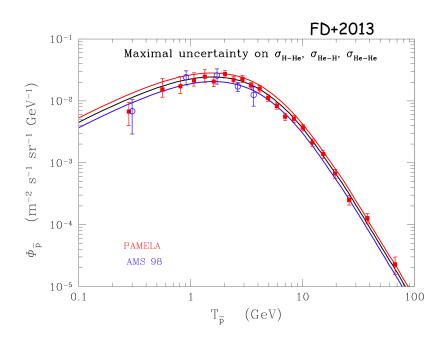
Prediction and AMS data



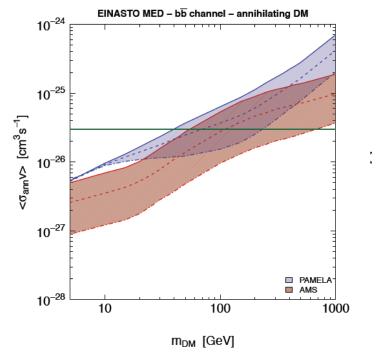
Very recent AMS-02 results up to 450 GeV
Can be explained by secondary production in the Milky Way,
considering several theoretical uncertainties

He cross sections: effect on DM interpretation

Uncertainties due to helium reactions range 40-50% on Secondary CR flux



Effect of cross section uncertainty on DARK MATTER interpretation Fornengo, Maccione, Vittino JCAP2014



AMS-02 is providing data with much higher precision up to hundreds of GeV!!! Their interpretation risks to be seriously limited by nuclear physics

The case for

positrons

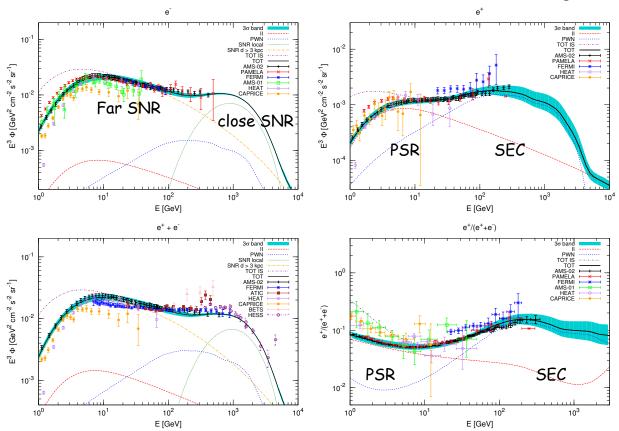
Sources of positrons in the Milky Way

Sources of e^+ and e^- in the Galaxy:

- 1. Secondary e⁺ e⁻: spallation of cosmic p and He on the ISM (H, He) * p+H(He) \rightarrow p+ Δ^+ \rightarrow p+ π^0 & n+ π^+ (mainly below 3 GeV) * p+H(He) \rightarrow p+n+ π^+ * p+H(He) \rightarrow X + K[±]
- 2. Primary e- and e+ from Pulsars (PSR): pair production in the strong <u>PULSAR</u> magnetoshpere
- 3. Primary e- from SNR: 1° type Fermi acceleration mechanism
- 4. Primary e⁺ e⁻ from exotic sources (DARK MATTER)

AMS lepton data: an astrophysical interpretation

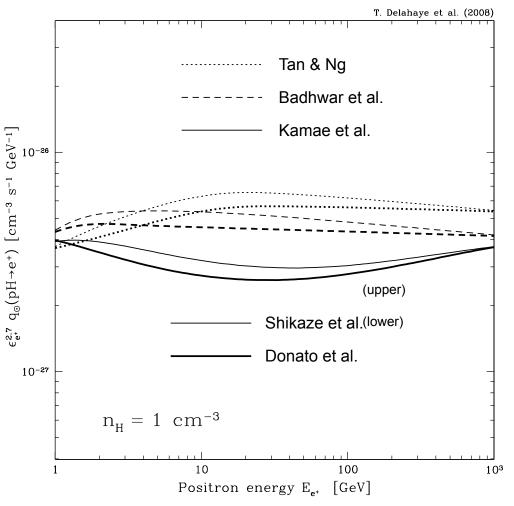
Di Mauro, FD, Fornengo, Vittino JCAP 2014



TH: Secondaries + supernovae + pulsars EXP: Ams data precise + wide range > Small features can bring strong information!

The secondary positron source term: effect of cross sections

Delahaye, FD, Fornengo, Lavalle, Lineros, Salati, Taillet A&A 2009



Effect of proton flux determination - negligible

Effect of production cross sections is not negligible!!

Up to factor 2 in p-p!

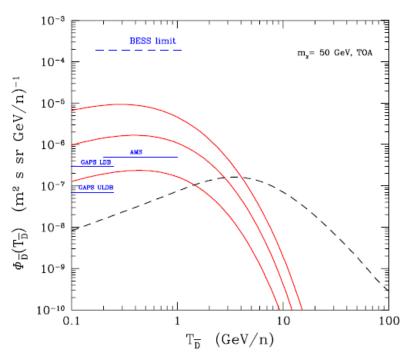
The case for

antideuterons

COSMIC ANTIDEUTERONS

FD, Fornengo, Maurin PRD 2001; 2008; Kadastik, Raidal, Strumia PLB2010; Ibarra, Wild JCAP2013; Fornengo, Maccione, Vittino JCAP 2013; ...

In order for fusion to take place, the two antinucleons must have low kinetic energy



Kinematics of **spallation** reactions prevents the formation of very low antiprotons (antineutrons).

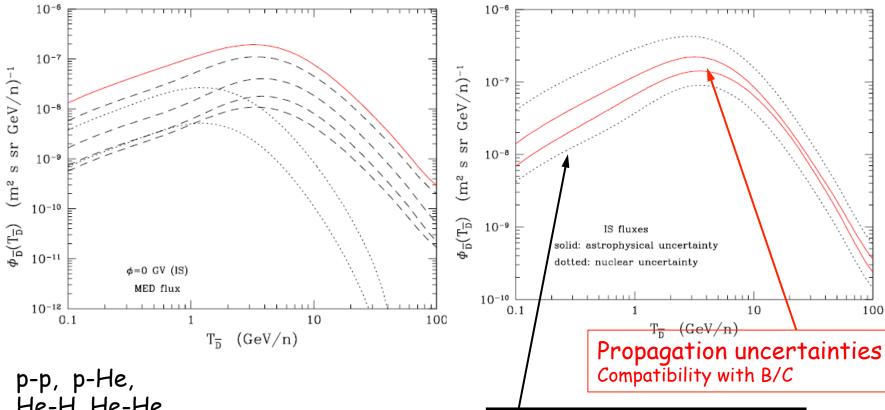
At variance, dark matter annihilate almost at rest

N.B: Up to now, NO ANTIDEUTERON has been detected yet. Several expreriments are on the road: AMS/ISS, BESS-Polar, GAPS ...

Secondary antideuterons

FD, Fornengo, Maurin PRD 2008

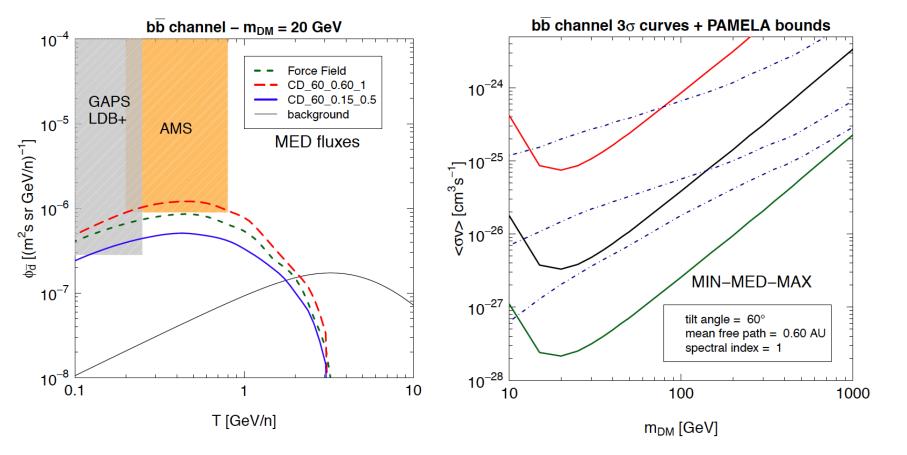
Contributions to secondaries



p-p, p-He, He-H, He-He H-pbar, He-pbar

Nuclear uncertainties Production cross sections & P_{coal} Production from antiprotons Non-annihilating cross sections

Antideuterons: Dark matter detection perspectives Fornengo, Maccione, Vittino 1306.4171



 3σ expected sensitivities

Prospects for 3 σ detection of antideuteron with GAPS (dotted lines are Pamela bounds from antiprotons)

Few final remarks

The astrophysics of cosmic rays is entering an era of remarkable precision (AMS-02/ISS)

ANTIMATTER is a key element for testing galactic models and searching for DARK MATTER signals

Propagation uncertainties confined to less than 20%, close to be < 10%

The (production, total inelastic, inelastic non-annihilating, ...) cross sections from Fe down, including isotopes and antimatter, rely on very few or (often) NO lab data!!

→ A HUGE EXPERIMENTAL PROGRAM IS REQUIRED FOR A SIGNIFICANT REDUCTION OF UNCERTAINTIES

Proton-helium \rightarrow antiproton + X looks the most urgent case (contextually, measure of \rightarrow e+, γ , D-)

BACKUP SLIDES

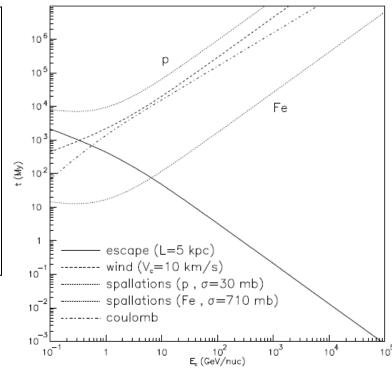
Characteristic times and distances

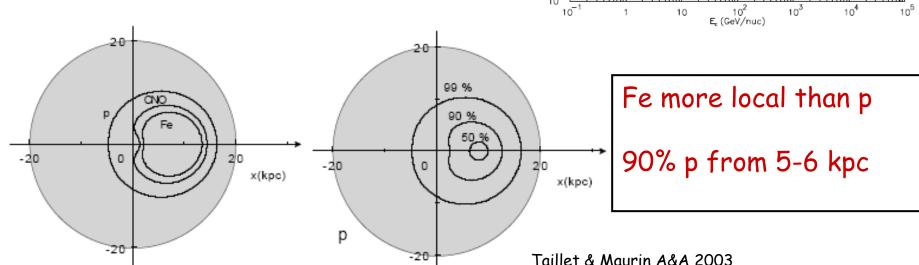
The smaller the time, the most effective the process is

Protons: escape E > 1 GeV

convection and e.m. losses E<1 GeV,

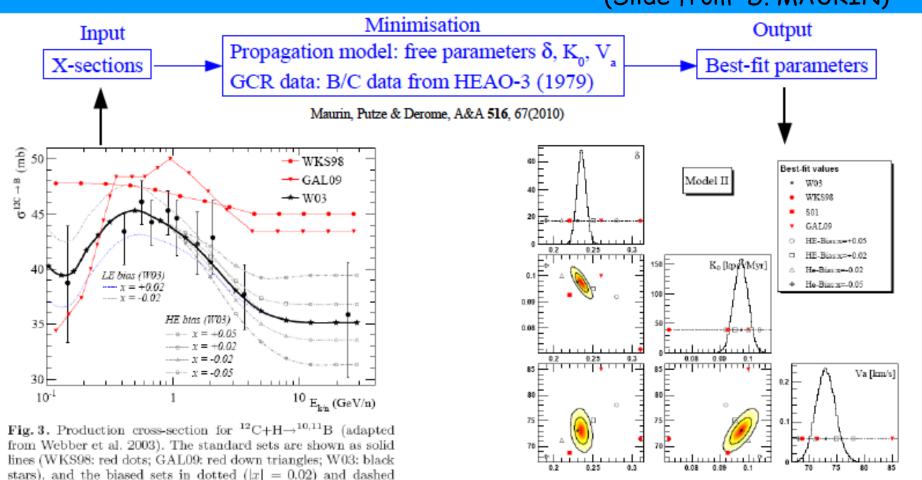
Iron: escape E > 1 GeV Spallations E<10 GeV/n





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Primaries
               = present in sources:
             Nuclei: H, He, CNO, Fe; e-, (e+) in SNR (& pulsars)
             e+, p+, d+ from Dark Matter annihilation
Secondaries = NOT present in sources, thus produced by
             spallation of primary CRs (p, He, C, O, Fe) on ISM
             Nuclei: LiBeB, sub-Fe, ...;
             e<sup>+</sup>, p<sup>+</sup>, d<sup>+</sup>; ... from inelastic scatterings
          30
          25
     Atomic Number (Z)
          20
          15
                                                    Primary Nuclei: >75% from source
          10
                                                   Mixed: 50-75% from source
                                                   Mixed: 25-50% from source
                                                           ·25% from source
                                                   Secondary: <5% from source
                                                   Propagation Clock Nuclei
                                                   Nucleosynthesis Clock Nuclei
                                                   K-Capture Secondary Nuclei
                               10
                                                 20
                                                                    30
                                                                                       40
                                     Number of Neutrons (N)
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X-sec uncertainties: impact on GCR model parameters (Slide from D. MAURIN)



- W03 and WKS98 are parameterisations of the same 'data' (energy bias)

(|x| = 0.05) lines.

- GAL09: modern nuclear codes normalised to LANL database [Moskalenko & Mashnik, astro-ph/0306367]
- → Systematics uncertainties (from X-sec) > statistical uncertainties (from GCR data) ... and AMS-02 is at least 100 better than HEAO-3!

III. Uncertainties are too large!

Inelastic cross sections $(\sigma_R = \sigma^{tot} - \sigma_{ela}^{tot})$ (Slide from D. MAURIN)

- Bradt & Peters (1950)

$$\sigma_R = \pi r_o^2 (A_{proj}^{1/3} + A_{cible}^{1/3} - b_0)^2$$

- Letaw et al. (1970-2000): accuracy <2% for 2<Z<30 and E>300MeV/n

S.Barshay & al, Phys.Lett 51B, 5 (1974)
J.R.Letaw & al, ApJSS 51, 271 (1983)
R.Silberberg & C.H Tsao, Phys.Rep. 191, 351 (1990)
L.Sihver & al, Phys.Rev.C 47, 1225 (1993)
H.P.Wellish & D.Axen, Phys.Rev.C 54, 1329 (1996)
R.Silberberg & al, ApJ 501, 911 (1998)
C.H.Tsao & al, ApJ 501, 920 (1998)

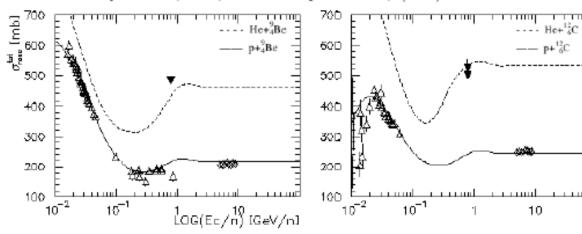
$$\alpha_R(E_k) = \sigma_R^{HE} \left[1 - 0.62 \exp[-E_k/200] \sin(10.9E_k^{-0.28}) \right] (mb)$$

$$\sigma_R^{HE} = 45A^{0.7} \left[1 + 0.016 \sin(5.3 - 2.63 \ln A) \right] (mb)$$

- Tripathi et al. (~2000): ~ or better (at low E) than Letaw et al., valid for all N+N reaction!

R.K.Tripathi & al, NASA, Technical Paper 3621, (1997)
 R.K.Tripathi & al, NASA, Technical Paper 3656, (1997)
 R.K.Tripathi & al, NASA, Technical Paper 209726, (1999)

$$\sigma_R = \pi r_0^2 \left(A_{proj}^{1/3} + A_{cible}^{1/3} + \delta_E\right)^2 \left(1 - R_c \frac{B}{E_{cm}}\right) X_m$$



Data from compilations: Bobchenko 79, Tanihata 85, Bauhoff 86, Carlson 96

→ Tripathi *et al.* is the one generally used in the field

Production cross sections (straight-ahead approx.)

$$\int_{0}^{\infty} n_{\rm H} v' N^{k}(T') \sigma^{kj}(T, T') dT' = \int_{0}^{\infty} n_{\rm H} v' N^{k}(T') \sigma^{kj}(T) \delta(T - T') dT' = n_{\rm H} v N^{k}(T) \sigma^{kj}(T)$$

- Semi-empirical approach [Silberberg et Tsao]
 - for any Proj. + Targ. → Frag.
 - better than Webber if extrapolation (Z>30)
- Empirical approach [Webber et al.]
 - for Proj. + H/He → Frag.
 - better than Silberberg on 'data' (Z<30)

P.Ferrando & al, Phys.Rev.C 37, 1490 (1988) W.R.Webber, J.C.Kish, D.A.Schrier, Phys.Rev C 4 W.R.Webber & al, ApJ 508, 940 (1998-a) W.R.Webber & al, ApJ 508, 949 (1998-b) W.R.Webber & al, Phys.Rev.C 58, 3539 (1998-c) W.R. Webber et al., ApJSS 144, 153 (2003)

D. MAURIN

- More recent empirical codes
 - EPAX2 http://www-w2k.gsi.de/hellstr/asp/gsi/epaxv21m.asp
 - PHITS phits.jaea.go.jp
- Microscopic description
 - LAOGSM (Los Alamos Quark Gluon String Model)
 - NUCFRG2 (semi-empirical abrasion-ablation model)

L.W. Townsend & al, NASA, Technical Paper 3310, (1993) F.A.Cucinotta, NASA, Technical Paper 3354, (1993) J.P.Bondorf & al, Phys.Rep. 257, 133 (1995) J.W.Wilson & al, NASA, Technical Paper 3533, (1995) F.A.Cucinotta & al. NASA, Technical Paper 3594, (1996) C.R.Ramsey & al, Phys.Rev.C 57, 982 (1998) Zeitlin et al., Phys. Rev. C 77, 034605 (2008) Zeitlin et al., AdSR 46, 728 (2010) Zeitlin et al., Phys. Rev. C 83, 034909 (2011)

R.Silberberg & C.H.Tsao, ApJSS 25, 315 (1973) R.Silberberg & C.H.Tsao, ApJSS 35, 129 (1977) R.Silberberg & C.H.Tsao, ApJSS 35, 137 (1977)

R.Silberberg & C.H Tsao, Phys.Rep. 191, 351 (1995lide from

R.Silberberg & al, ApJSS 58, 877 (1985)

L.Sihver & al, Phys.Rev.C 47, 1225 (1993).

C.J.Waddington, ApJ 470, 1218 (1996) R.Silberberg & al, ApJ 501, 911 (1998). C.H.Tsao & al, ApJ 501, 920 (1998) C.H.Tsao & al, ICRC 26, HE.1.1.04 (1999)

C.H.Tsao & al, Phys.Rev.C 47, 1257 (1993)

 \rightarrow Webber *et al.* is the one generally used in the field (but for Z<3 nuclei) with claimed uncertainties <10% (fragments from Li \rightarrow O) or <20% (from Fe)

<u>NB</u>: it is not straightforward to go from nuclear data/models to X-sec for GCRs

Transport equation in diffusion models

Diffusion Convection
$$-\vec{\nabla} \left[K \vec{\nabla} N^j(E) - \vec{V_c} N^j(E) \right] - \Gamma^j N^j$$

$$-\frac{(\vec{\nabla}.\vec{V_c})}{3} \frac{\partial}{\partial E} \left[\frac{p^2}{E} N^j(E) \right] = \mathcal{Q}^j(E) +$$
 CR sources: primaries, secondaries
$$\frac{\partial}{\partial E} \left[-b_{\rm tot}(E) N^j(E) + \beta^2 K_{pp} \frac{\partial N^j(E)}{\partial E} \right]$$
 (spallations) Eneegy losses (EM) Reacceleration

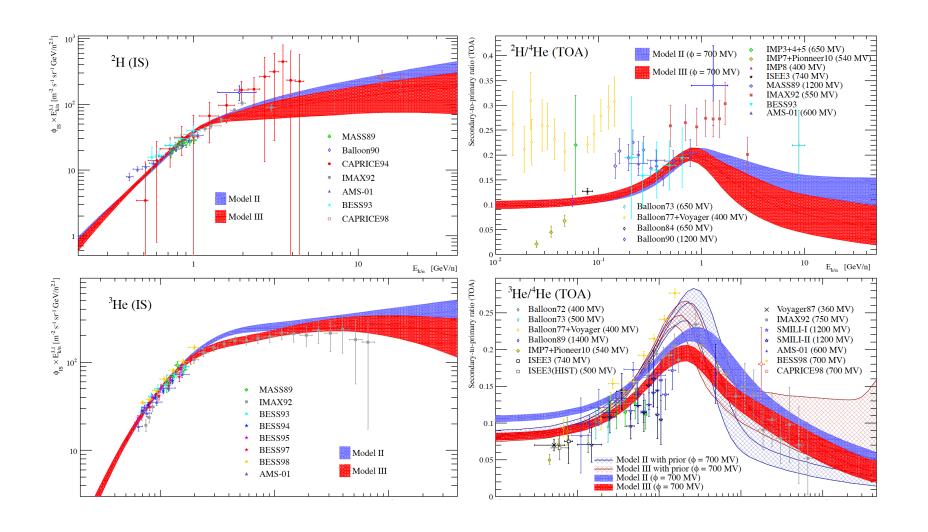
- DESTRUCTION: $\Gamma = n_{ISM} v \sigma_R$, $\sigma_{R} = \sigma^{tot} \sigma^{tot}_{el}$
- 2. SOURCES: $Q^j \equiv q_0^j Q(E) \hat{q}_i + \sum_k^{m_k > m_j} \tilde{\Gamma}^{kj} N_i^k(0)$

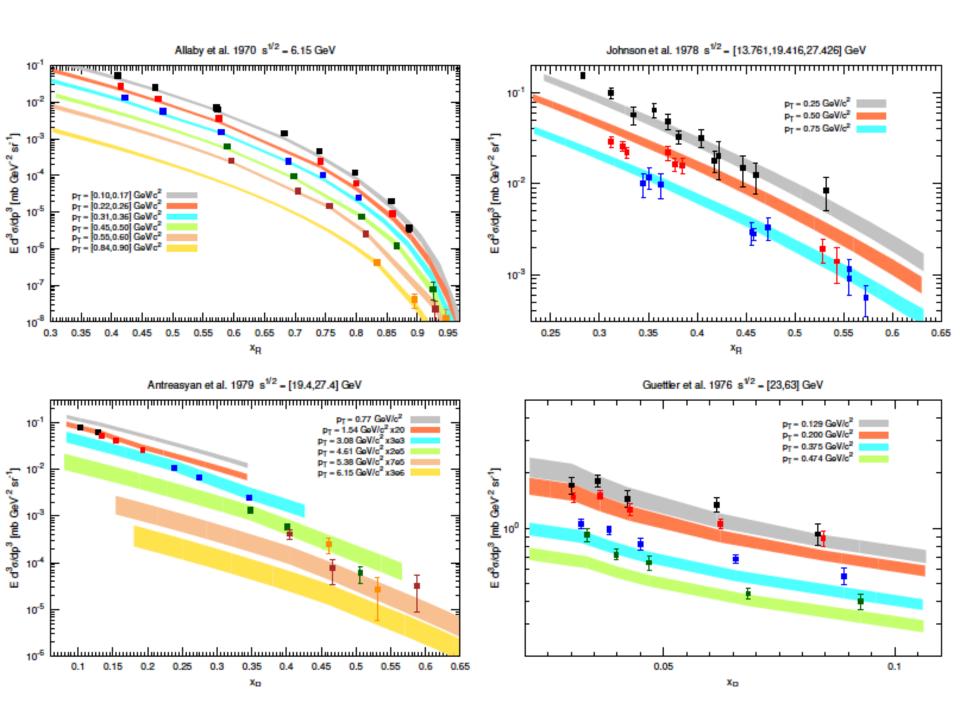
production in SNR

Primary Secondary production by fragmentation of heavier nuclei



¹H, ²H, ³He, ⁴He almost as powerful as B/C Noticeable effort on reliable cross sections





The role of helium nuclei

Kachelriess, Moskalenko & Ostapchenko 2015

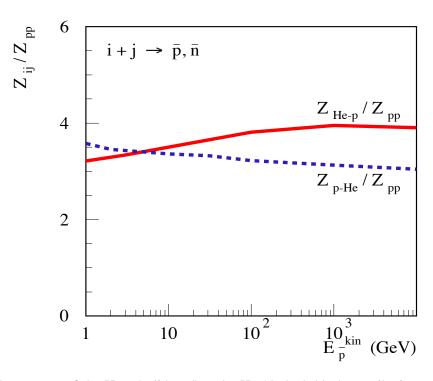
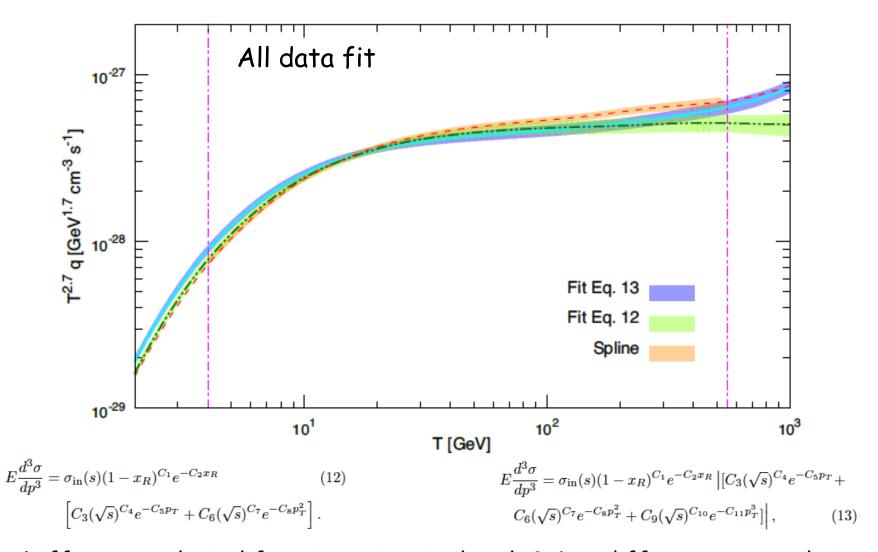


FIG. 7.— Energy dependence of the enhancement of the He p (solid, red) and p He (dashed, blue) contributions to the antiproton spectrum, relative to the pp-case, $Z_{\bar{p}}^{ij}(E_{\bar{p}},\alpha)/Z_{\bar{p}}^{pp}(E_{\bar{p}},\alpha)$ (plotted as a function of $E_{\bar{p}}^{kin}$), for $\alpha=2.6$.

Note: The cosmic p flux is ~ 10 times higher than He flux

Antiproton source spectrum from p-p channels

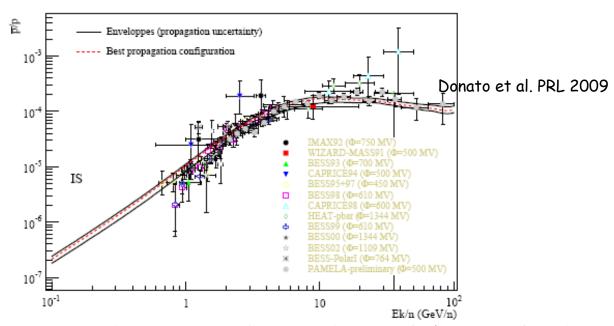


Different analytical functions give similar chi2, but different extrapolation out of validity ranges \rightarrow uncertainties at low and high energies

Antiproton in CRs: data and models

Theoretical calculations compatible with CR models

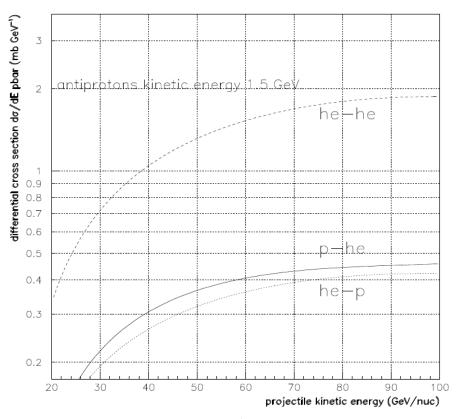
Powerful tool for DARK MATTER models



NO need for new phenomena (astrophysical / particle physics)

AMS-02 data now at high accuracy 1 - 450 GeV

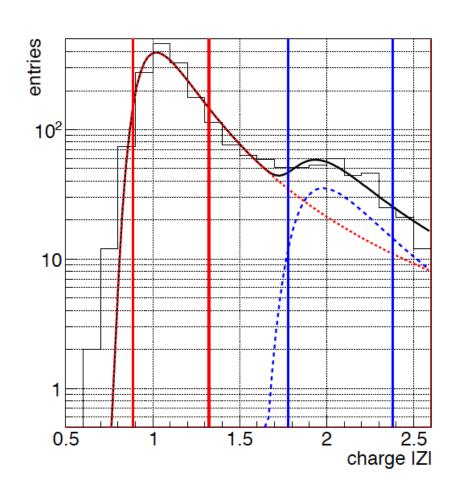
Differential antiproton cross section

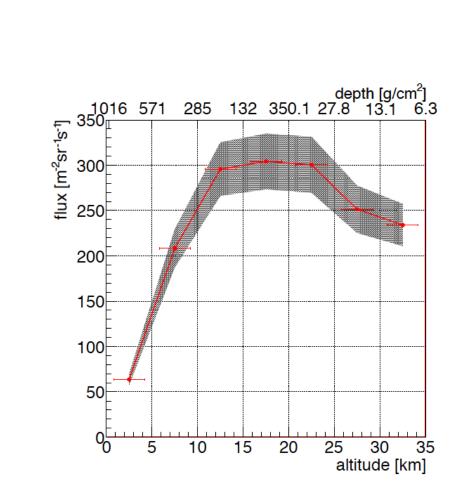


Given that:

- 1. In the ISM $n_H = 0.9/cm^3$, $n_{He} = 0.1/cm^3$,
- 2. the cosmic p flux is ~ 10 higher than He
- \rightarrow the main production channel involving He is p_{CR} -He $_{ISM}$

GAPS prototype flight P. von Doetinchem et al. 1307.3538





Propagation of e⁺ & e⁻

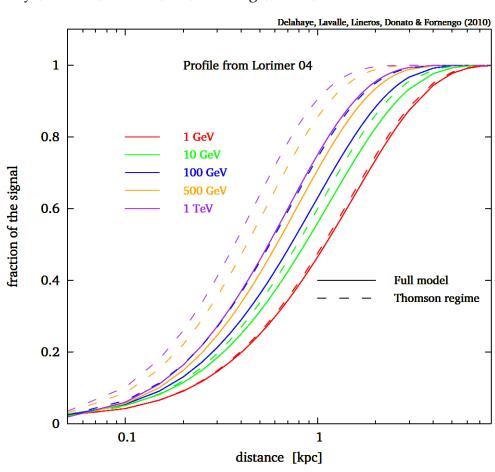
Delahaye, Lavalle, Lineros, FD, Fornengo, Salati, Taillet A&A 2009

Diffusive semi-analytical model: Thin disk and confinement halo Free parameters fixed by B/C

Above few GeV: only spatial diffusion and energy losses

Energetic positrons & electron are quite local

Relativistic (KN) energy losses induce a longer propagation scale



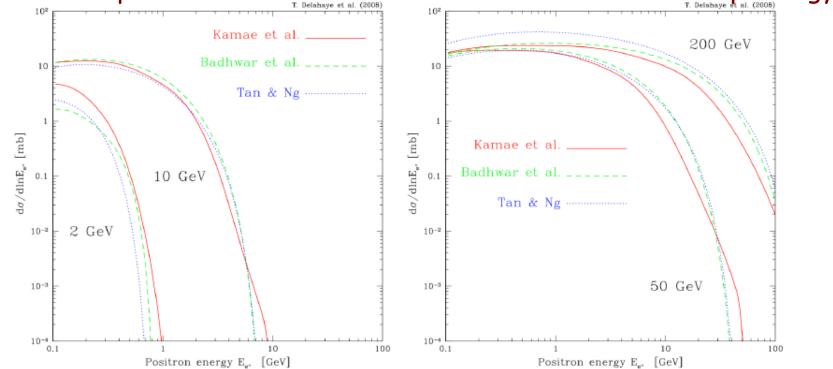
95%(80%) for 2kpc and E>100(10) GeV

Secondary positron production

Spallation of proton and helium nuclei on the ISM (H, He)

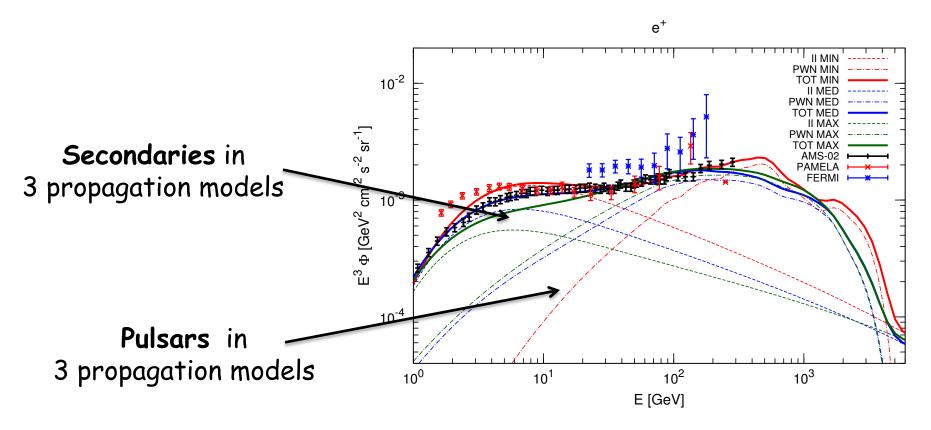
- p+H \rightarrow p+ Δ^+ \rightarrow p+ π^0 & n+ π^+ (mainly below 3 GeV)
- p+H \rightarrow p+n+ π^+
- $p+H \rightarrow X + K^{\pm}$

Different parameterizations of cross sections and incident p energy



Low energy positrons: the power of AMS precision data

Di Mauro, FD, Fornengo, Vittino JCAP 2014; Lavalle, Maurin, Putze PRD 2014



AMS POSITRON data at low energy are so precise to start constraining the Milky Way models (as well as B/C)!

The case for

gamma rays

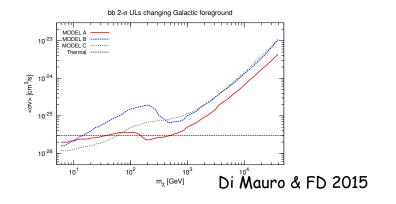
(very briefly)

p+He $\rightarrow \pi^0 \rightarrow 2\gamma$: galactic foreground in the Fermi-LAT data

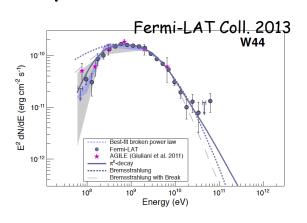
Contextually to p+He \rightarrow antiprotons, it would be of very interesting to measure also the photons (gamma rays) coming from the hadronization processes via π^0 decay.

This process occurs in the galactic disk and enters the calculation of the galactic emission, crucial for understanding:

 DARK MATTER annihilation (Galaxy, dwarf spheroidal galaxies, ..)

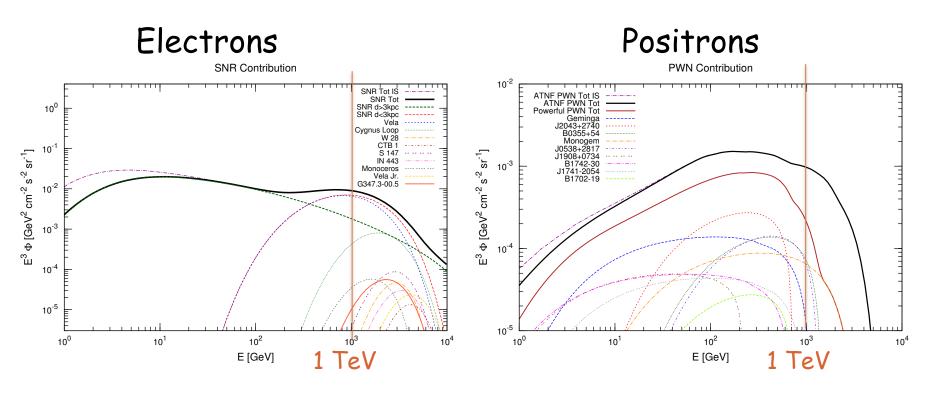


2. ORIGIN of COSMIC RAYS galaxy emission, SNRs, ..



Astrophysical sources of e+ e-

Di Mauro, FD, Fornengo, Vittino JCAP 2014



Supernova remnants

Pulsars

Partial contributions from CR nuclei

$$\epsilon_{ij}^{\bar{p}}(E_{\bar{p}}) = \frac{q_{\bar{p}}^{ij}(E_{\bar{p}})}{q_{\bar{p}}^{pp}(E_{\bar{p}})} \qquad \text{Kachelriß+2015}$$

$$q_{\bar{p}}^{ij}(E_{\bar{p}}) = n_j \int_{E_{\text{thr}}(E_{\bar{p}})}^{\infty} dE \, \frac{d\sigma^{ij \to \bar{p}}(E, E_{\bar{p}})}{dE_{\bar{p}}} \, I_i(E)$$

 $\begin{array}{c} \text{The distribution of the property of t$

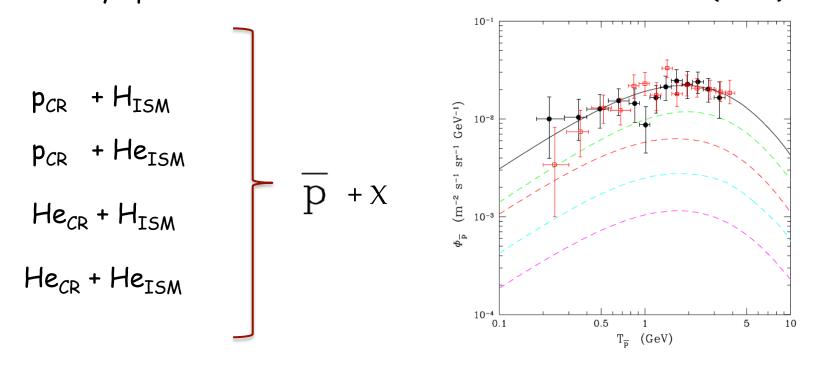
FIG. 8.— Energy dependence of partial contributions $\epsilon_{ij}^{\bar{p}}(E_{\bar{p}})$ to the nuclear enhancement factor from different interaction channels: p He (solid, red), He p (dashed, blue), He He (dot-dashed, green), and all others (dotted, black); the CR composition given in Table 2 is used.

The contribution of He nuclei, in CRs and in ISM, is similar (50%) of the p-p one

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Secondary antiprotons in cosmic rays (CR)

Produced by spallation reactions on the interstellar medium (ISM)



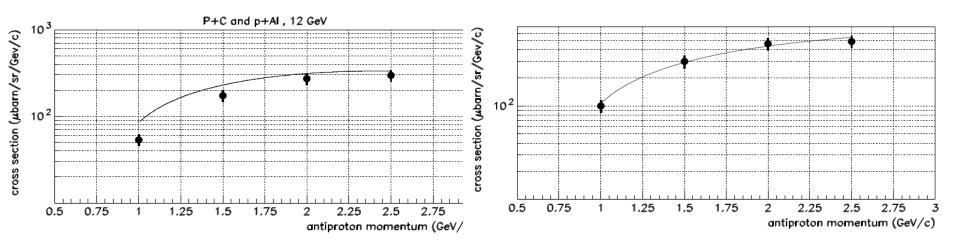
The only measured cross section is p-p $\rightarrow \overline{p}$ + X

ALL CROSS SECTIONS
INVOLVING He (projectile or target)
ARE DERIVED FROM OTHER DATA!!

Antiproton production from p and He

1. p+p: $\sigma_{p+p \to antiprotons}$ NA49 data analysis (Di Mauro, FD, Goudelis, Serpico PRD 2014; Kappl, Winkler JCAP 2014) or analytical expression (Tan & Ng, PRD26 1982, 1983

2. p+ He, He+p, He+He: σ(p + He → antiprotons): NO DATA
 → derived from MonteCarlo simulations, i.e. DTUNUC
 verified on p+C,p+Al and heavier nuclei (Duperray et al. 2003, 2005; Donato et al. ApJ 563 (2001)172)



Data from Sugaya+1998; fit: DTUNUC

Donato+ ApJ2001