

# Background to the search for dark photon

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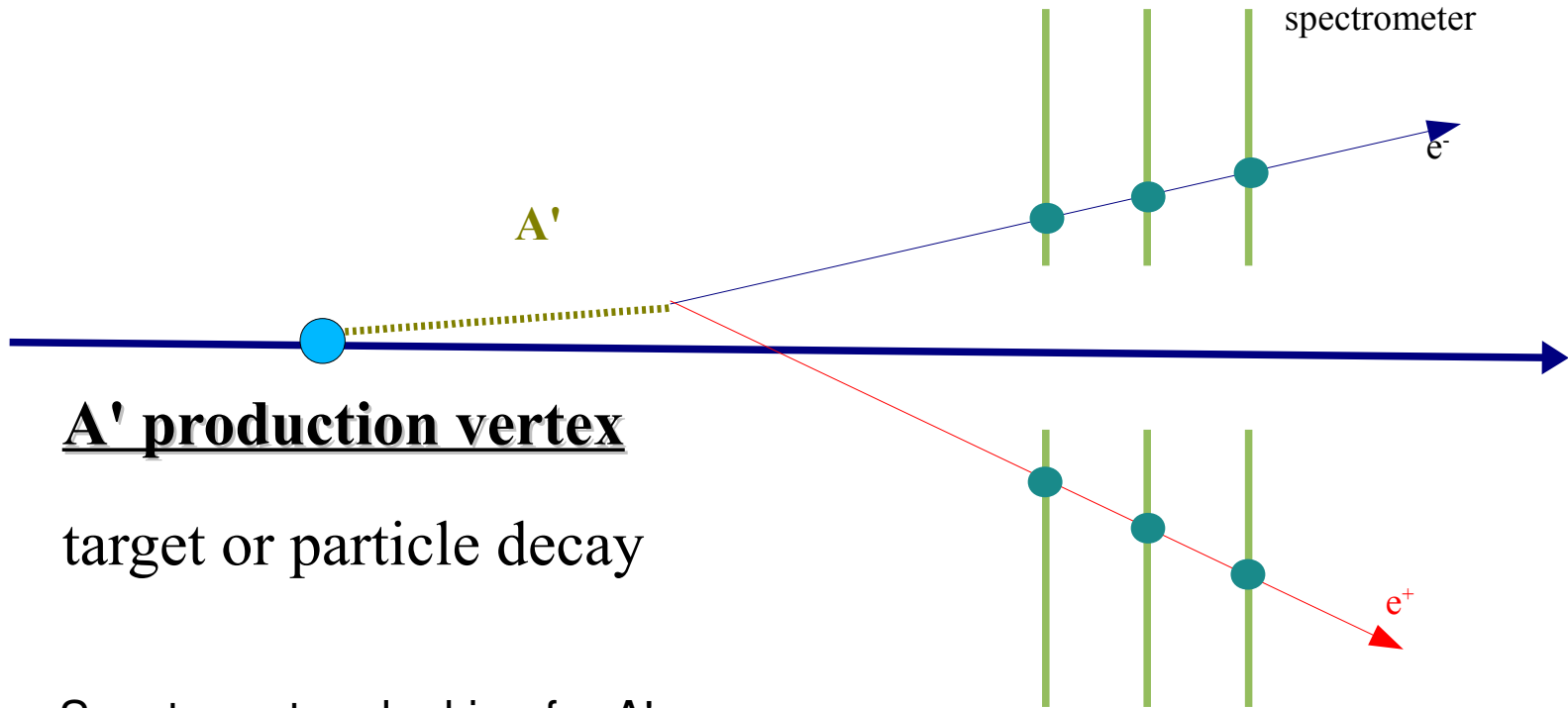
*\*partially supported by LNF-SU 70-06-497/07-10-2014  
and SU-FNI 39/2016*



# Overview

- Overview of annihilation experiments
- Dark photon production
- Multiphoton annihilation
- Bremsstrahlung
- Radiative
- Conclusions/open questions

# Visible dark photons



## $A'$ production vertex

target or particle decay

## Spectrometers looking for $A'$ :

- produced in a thin target
- decaying to leptons

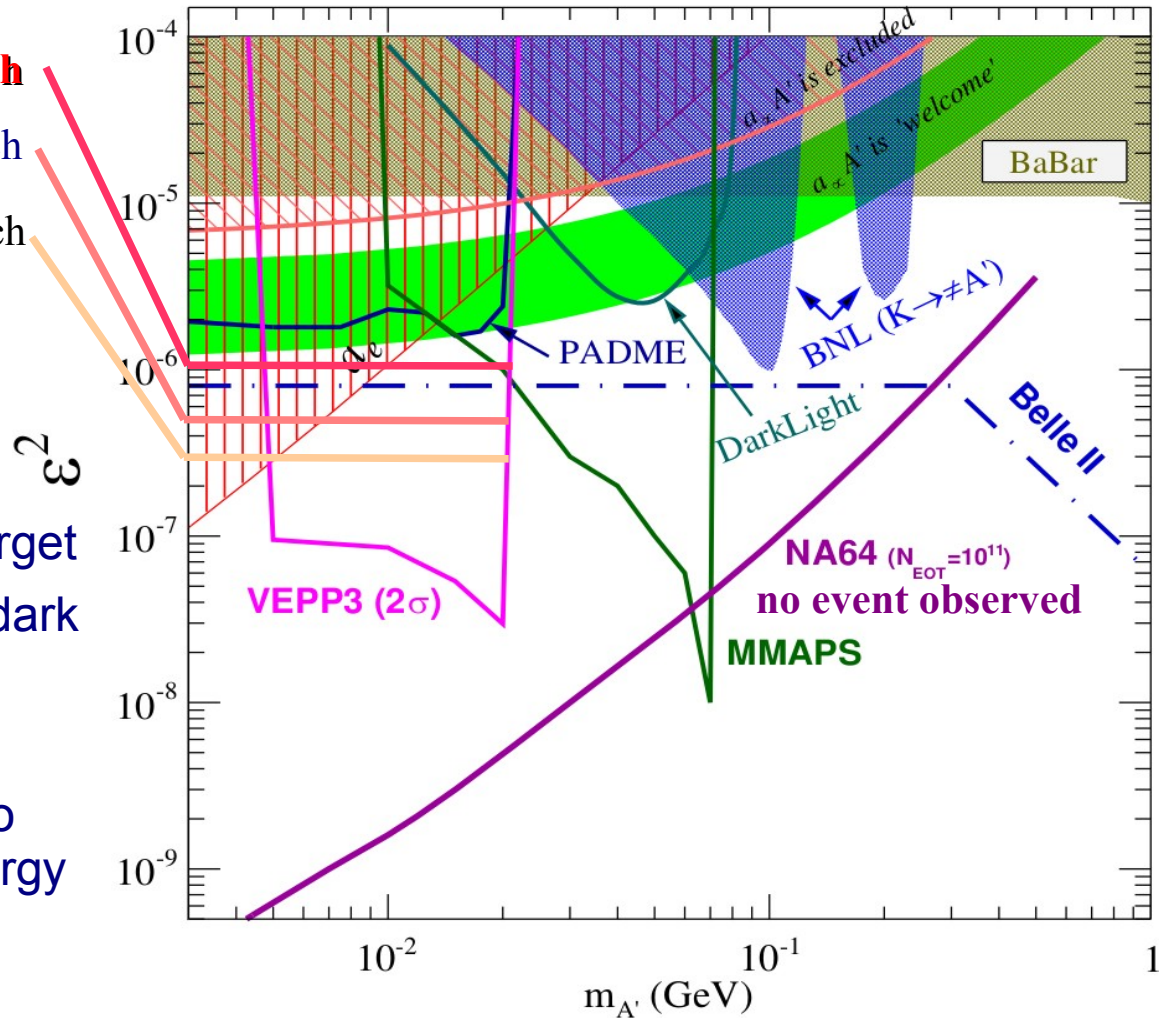
# Invisible dark photons

**PADME 40 ns bunch**

PADME 160 ns bunch

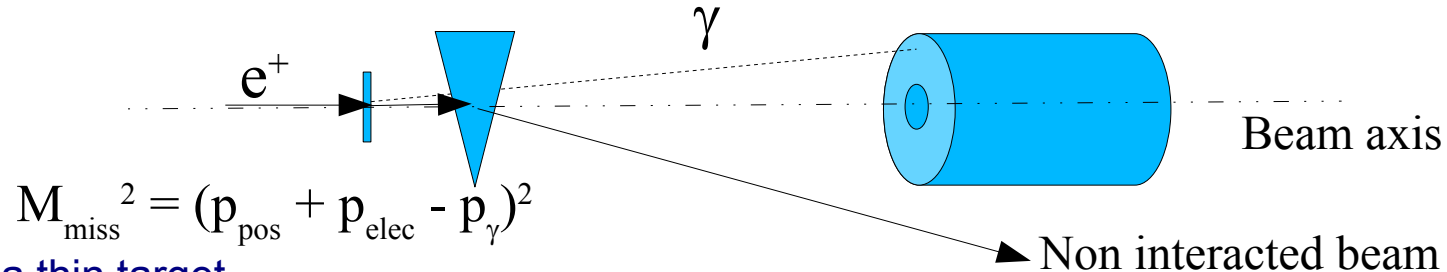
PADME 480 ns bunch

- Addressing the missing mass
  - PADME@Frascati, VEPP3@Novosibirsk, MMAPS@Cornell
  - Positron beam on a thin target
  - Annihilation production of dark photons
- Missing energy
  - NA64: leakage of energy to the dark sector in high energy shower development
- Dark matter scattering
  - BDX



# Missing mass technique

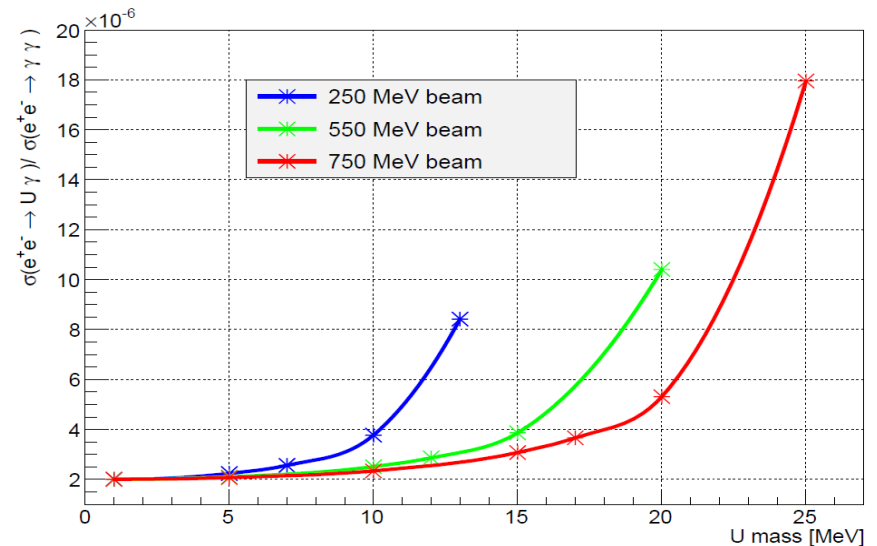
## Study only the recoil photon



- Positron beam on a thin target
- Positron momentum is determined by the accelerator characteristics
- Missing mass resolution: annihilation point,  $E_{\gamma}$ ,  $\phi_{\gamma}$

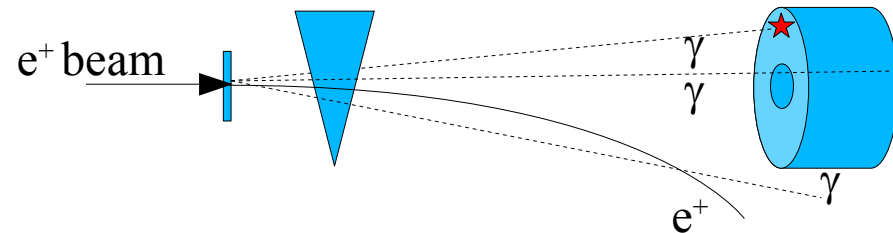
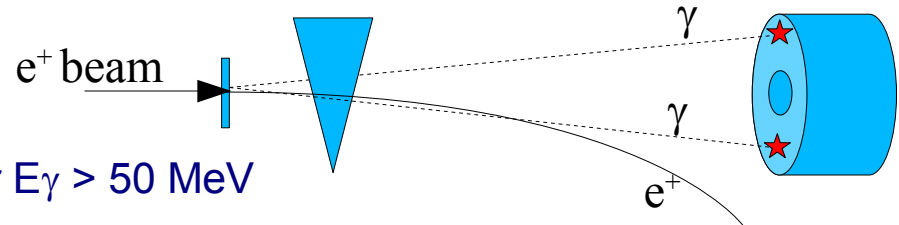
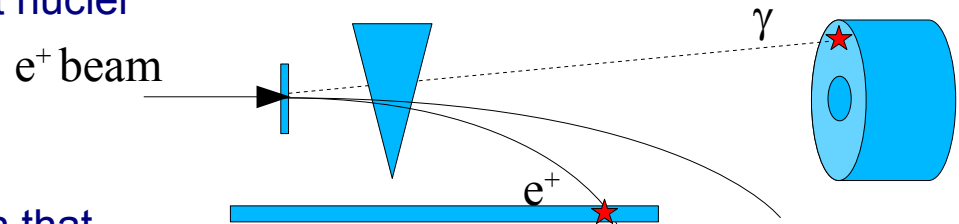
$$\frac{\sigma(e^+e^- \rightarrow U\gamma)}{\sigma(e^+e^- \rightarrow \gamma\gamma)} = \frac{N(U\gamma)}{N(\gamma\gamma)} * \frac{Acc(\gamma\gamma)}{Acc(U\gamma)} = \epsilon^2 * \delta,$$

Cross section enhancement with the approach of the production threshold



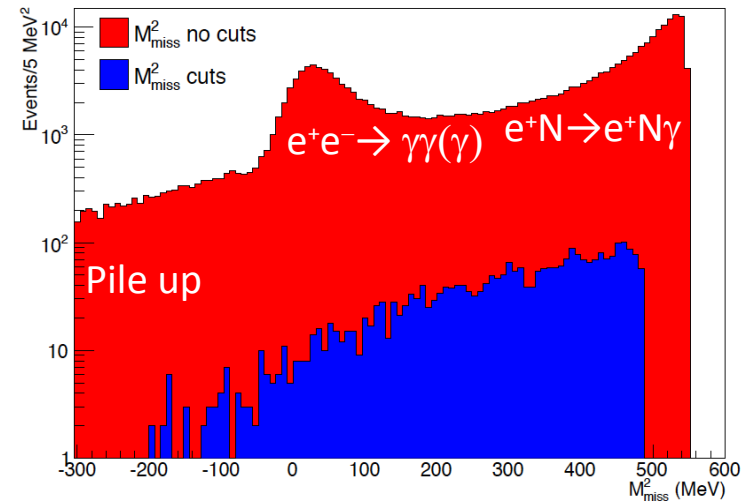
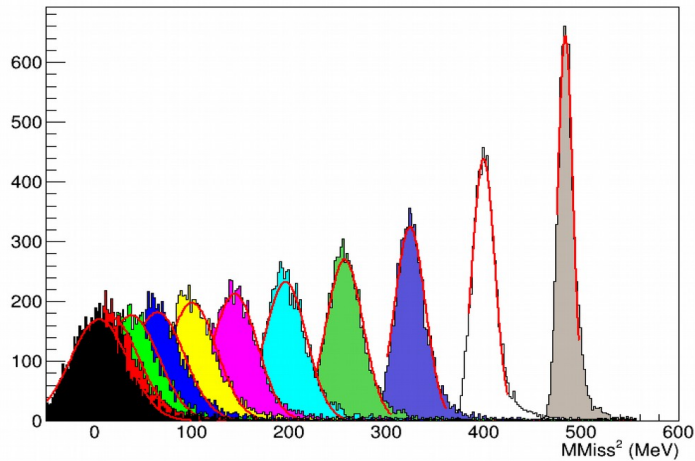
# Backgrounds

- Bremsstrahlung in the field of the target nuclei
  - Photons mostly @ low energy, background dominates the high missing masses
  - An additional lower energy positron that could be detected due to stronger deflection
- 2 photon annihilation
  - Peaks at  $M_{\text{miss}} = 0$
  - Quasi symmetric in gamma angles for  $E_\gamma > 50 \text{ MeV}$
- 3 photon annihilation
  - Symmetry is lost – decrease in the vetoing capabilities
  - Does not peak
- Radiative bhabha scattering
  - Topology close to bremsstrahlung
  - Could have higher energy loss by the incident positron



# Measurement strategy

M<sub>miss</sub><sup>2</sup> for different M<sub>A</sub>



- Background suppression

Background process	Cross section e <sup>+</sup> @550 MeV beam	Comment
$e^+e^- \rightarrow \gamma\gamma$	1.55 mb	
$e^+ + N \rightarrow e^+ N \gamma$	4000 mb	$E_\gamma > 1\text{MeV}$ , C
$e^+e^- \rightarrow \gamma\gamma\gamma$	0.16 mb	CalcHEP, $E_\gamma > 1\text{MeV}$
$e^+e^- \rightarrow e^+e^-\gamma$	180 mb	CalcHEP, $E_\gamma > 1\text{MeV}$

- Not a background free experiment!
- 3g and bremsstrahlung dominate and are of comparable size
- $O(10^4 - 10^5)$  foreseen background events for a given A' mass

# Missing mass searches status

	PADME	MMAPS	VEPP3
<b>Place</b>	LNF	Cornell	Novosibirsk
<b>Beam energy</b>	550 MeV	Up to 5.3 ( <b>6.0</b> ) GeV	500 MeV
<b><math>M_{A'}</math> limit</b>	23 MeV	74 MeV	22 MeV
<b>Target thickness</b>	$2 \times 10^{22}$ e <sup>-</sup> /cm <sup>2</sup>	$O(2 \times 10^{23})$ e <sup>-</sup> /cm <sup>2</sup>	$5 \times 10^{15}$ e <sup>-</sup> /cm <sup>2</sup>
<b>Beam intensity</b>	$8 \times 10^{-11}$ mA	$2.3 \times 10^{-6}$ mA	30 mA
<b><math>e^+e^- \rightarrow \gamma\gamma</math> rate [s<sup>-1</sup>]</b>	15	$2.2 \times 10^6$	$1.5 \times 10^6$
<b><math>\epsilon^2</math> limit (plateau)</b>	<b><math>10^{-6}</math> (<math>10^{-7}</math> SES)</b>	<b><math>10^{-6} - 10^{-7}</math></b>	<b><math>10^{-7}</math></b>
<b>Time scale</b>	2017 - 2018	?	2020 (ByPass)
<b>Status</b>	<b>Approved</b>	<b>Funds identification</b>	<b>Approved</b>

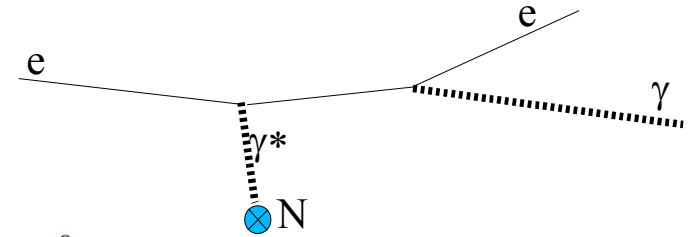


# Processes and tools

- Types of background
  - Multiphoton annihilation  
 $e^+e^- \rightarrow \gamma\gamma, e^+e^- \rightarrow \gamma\gamma\gamma, e^+e^- \rightarrow \gamma\gamma\gamma\gamma, \dots$
  - Bremsstrahlung in the field of the nuclei
  - Photon emission in the field of orbital electrons
- GEANT4
  - Bremsstrahlung, 2 photon annihilation
- CalcHEP
  - Cross-section calculation, 3 photon annihilation
- Different specialized MC generators
  - Babayaga
  - MCJPG

# Bremsstrahlung

- Usually thoroughly simulated through GEANT4
- Different models exist
  - Parametric – up to version 9.4



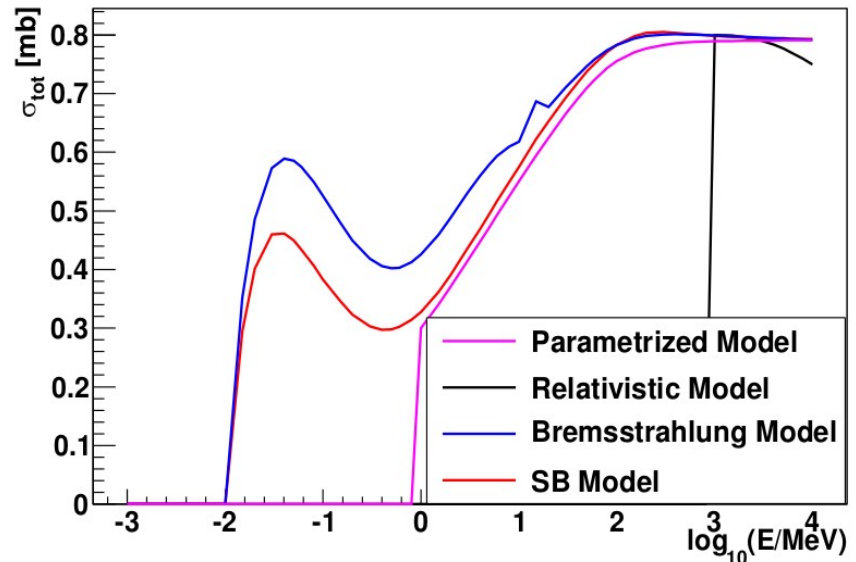
$$\sigma(Z, T, k_c) = Z(Z + \xi_\sigma)(1 - c_{sigh} Z^{1/4}) \left[ \ln \frac{T}{k_c} \right]^\alpha \frac{f_s}{N_{Avo}}$$

- Seltzer-Berger model (default)

$$\frac{d\sigma}{dk} = \frac{d\sigma_n}{dk} + Z \frac{d\sigma_e}{dk}$$

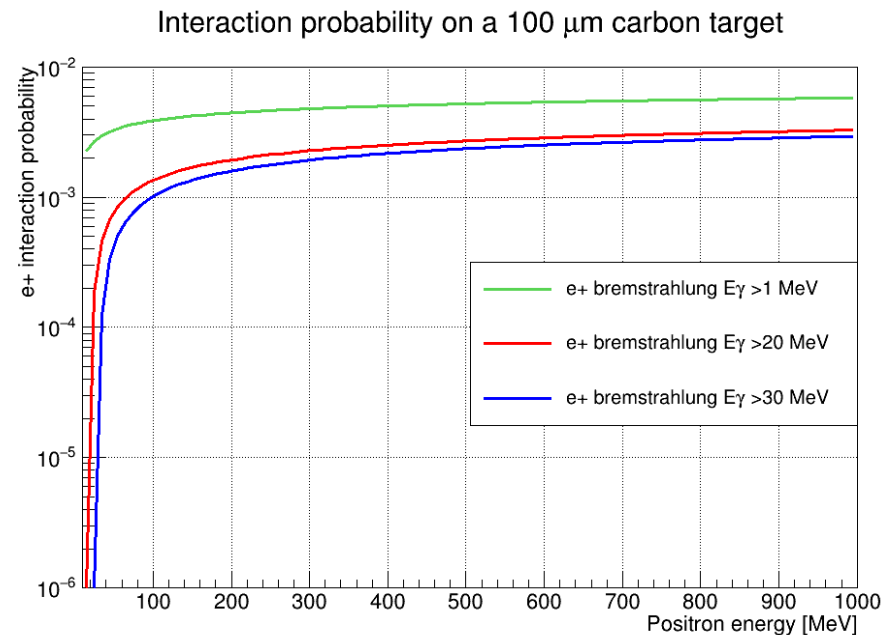
- Parametrization of tabulated data
- Takes into account e-N and e-e interactions
- Analytic – in the relativistic limit
  - Used for  $E > 1$  GeV

$$\frac{d\sigma}{dk} = \frac{4\alpha r_e^2}{3k} \left[ \{y^2 + 2[1 + (1 - y)^2]\} [Z^2(F_{el} - f) + ZF_{inel}] + (1 - y) \frac{Z^2 + Z}{3} \right]$$

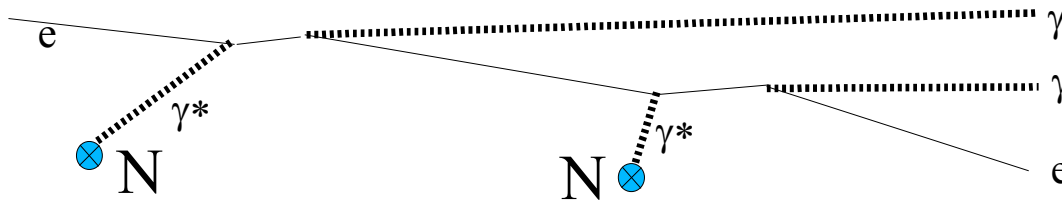


# The PADME and VEPP3 case

- Positron energy – 500 – 550 MeV
- The parametrized model seem to be well consistent with the SB model
  - Can be used for quick checks
- Using as a reference PADME
  - 100 um carbon target
- At  $E_\gamma \ll E_{e^+}$  the cross section depends mostly on  $E_\gamma$
- Bremsstrahlung probability @550 MeV
  - $E_\gamma > 1$  MeV: 0.55 %
  - $E_\gamma > 20$  MeV: 0.28 %
  - $E_\gamma > 30$  MeV: 0.25 %
- Almost every bunch has numerous bremsstrahlung emitted photons
  - Most at small angles with respect to the positron flight direction



# Double bremsstrahlung



- Non negligible probability for the two consequent bremsstrahlung by the same electron
  - $P(2\gamma)$  with  $E_\gamma > 20$  MeV @ 100 um carbon:  $\sim 10^{-5}$
  - Comparable with annihilation probability
- Possible background source
  - An event is rejected as signal only if  $E_\gamma + E_{e^+}$  is around the beam energy
    - Maximizes the acceptance for dark photon detection in the presence of pile-up bremsstrahlung
- BUT
  - Decreases the vetoing capabilities
- Should be able to perform at least two steps in the target volume

# Uncertainties

- The PADME sensitivity estimation relies on the knowledge of the background
  - Statistical uncertainty of the simulated background taken as a reference to determine the 90% (or 68 %) confidence level exclusion limits

$$\sigma_{\text{tot}}(N) \sim (\sqrt{N})_{\text{stat}} \oplus (\delta_{\text{model}} * N)$$

- We use  $\sigma_{\text{tot}}(N) / N(\gamma\gamma) / \text{Acc}(A')$  to describe the sensitivity
- GEANT4 model uncertainties
  - Parametric: 4-5 % for  $E_{e^+} > 1 \text{ MeV}$
  - SB model: 3-5% for  $E_{e^+} > 50 \text{ MeV}$
- @  $10^{13}$  events the number of background events due to bremsstrahlung per given  $A'$  mass interval varies from  $10^4 - 10^5$  ( $\sqrt{N}/N \leq 1\%$ )

**Already at that level the model uncertainty matters!**

*and even dominates...*

- Is it sufficient to extend the validity of the relativistic limit down to 300 MeV?

# Bremsstrahlung: open questions

- Can we use reliably the G4 bremsstrahlung simulation (and how)?
- Step modification to include possibility for double bremsstrahlung in the target? Or shall we introduce a custom double bremsstrahlung generator?
- How to decrease the bremsstrahlung uncertainty and tune the MC in the region  $100 \text{ MeV} < E_{e^+} < 1 \text{ GeV}$ 
  - Additional experimental measurements?
  - Might be possible also at LNF/BTF or elsewhere...
- Shall we employ data driven methods instead of MC ones for reliable bremsstrahlung background estimation?
  - Or a combination of both...

# Annihilation

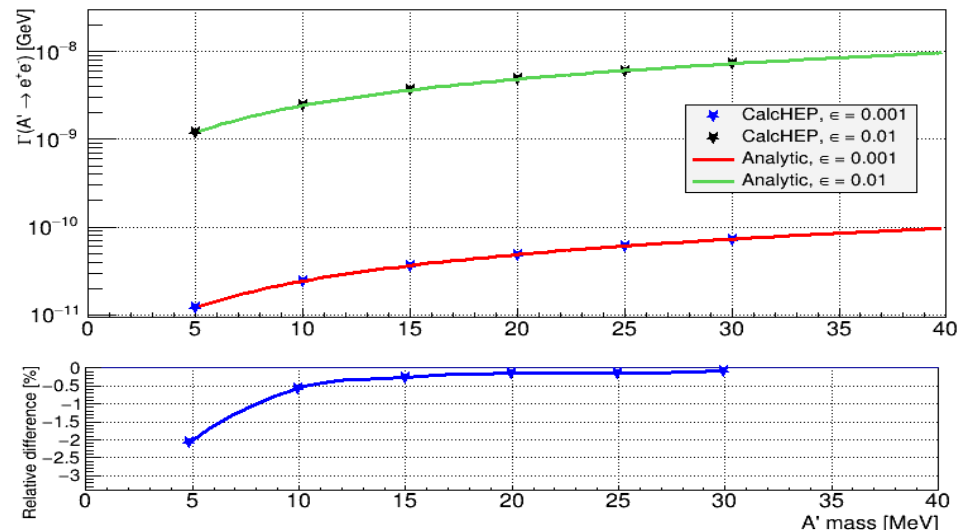
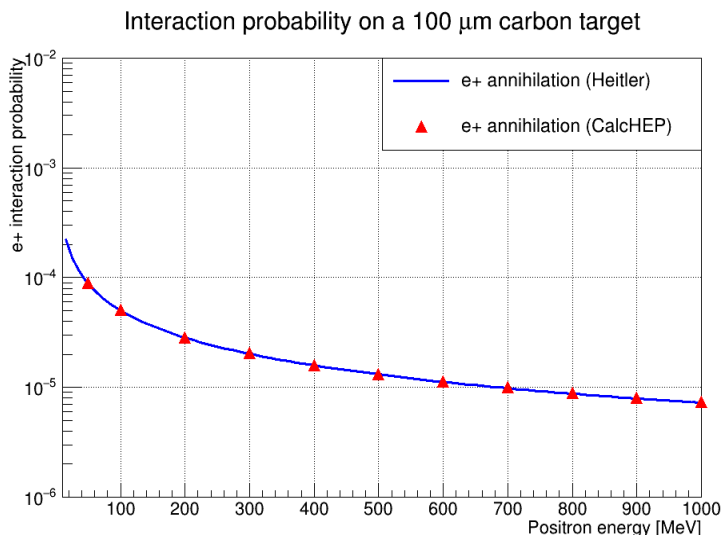
- $E_{e^+} = 550 \text{ MeV}$ , annihilation in flight
- Analytic expression for the cross section – Heitler formula

$$\sigma(Z, E) = \frac{Z\pi r_e^2}{\gamma + 1} \left[ \frac{\gamma^2 + 4\gamma + 1}{\gamma^2 - 1} \ln \left( \gamma + \sqrt{\gamma^2 - 1} \right) - \frac{\gamma + 3}{\sqrt{\gamma^2 - 1}} \right]$$

- The simulation is straight forward
  - GEANT4 includes the positron annihilation process
    - Sample the lab frame photon energy using  $d\sigma/dE_\gamma$
    - Isotropic azimuthal angle
  - Can be done with a custom event generator
    - 2-body  $\rightarrow$  2 body in the CM system, isotropic  $\gamma$  direction
    - Boost to the LAB-frame
- Well understood, background under control due to the strict kinematics

# Annihilation: 3 photon

- The process is not included by default in the simulation of positron interactions
- Can be assumed as a radiative correction to the  $2\gamma$  annihilation
- Different approaches to the treatment – from naive to “proper”
- CalcHEP – “a package for calculation of Feynman diagrams and integration over multi-particle phase space”
  - Development/support still active – last version 28.06.2016
  - Easy to use and modify – models, parameters, particle content, etc...

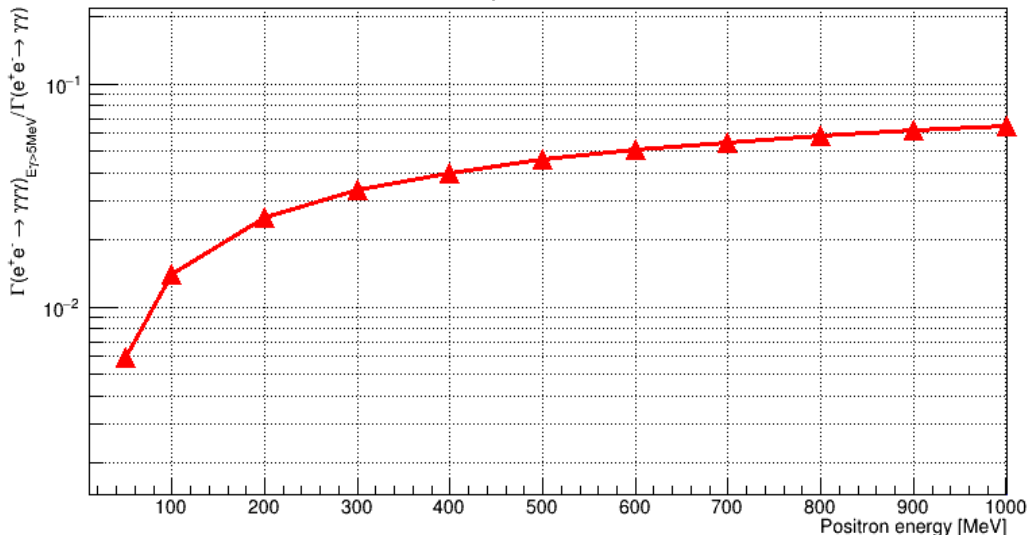




# Annihilation: 3 photon

- Thought to be negligible, but in-flight annihilation different from annihilation at rest
- Soft addition photon might be interpreted as initial state radiation (ISR)
- Cross section divergent with  $E_\gamma \rightarrow 0$ , a cut at  $E_\gamma > 5$  MeV
  - 1% of the nominal BTF beam energy for PADME
  - Seem consistent with the minimal detectable energy in the calorimeter
    - Seeding cell + shower

Ratio between  $3\gamma$  ( $E_\gamma > 5$  MeV) and  $2\gamma$  annihilation

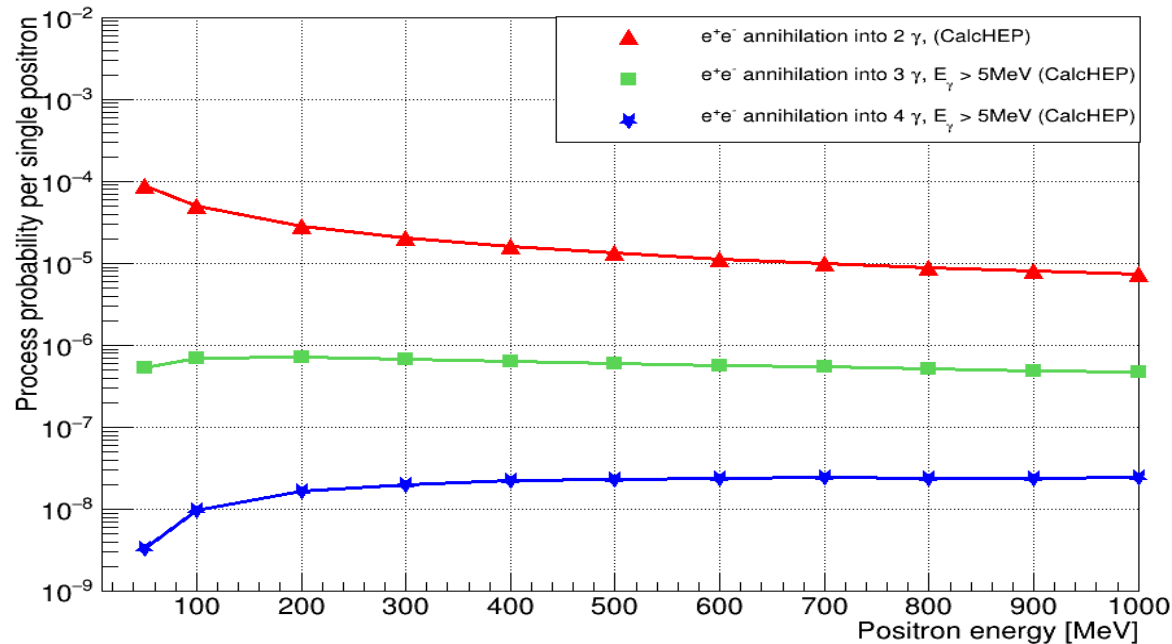


- $3\gamma$  events as much as  $\sim 4.5\%$  @550 MeV positron energy
- Should be custom generated and treated separately for background estimation
  - The third photon spoils the symmetry and veto capability of the calorimeter

# Annihilation: multi-photon

- We could even go further –  $e^+e^- \rightarrow N\gamma$

Interaction probability on a 100  $\mu\text{m}$  carbon target



- The low energy part of  $e^+e^- \rightarrow N\gamma$  is absorbed in the virtual corrections of  $e^+e^- \rightarrow (N-1)\gamma$

$$\Gamma(\text{annihilation}) = \Gamma(e^+e^- \rightarrow \gamma\gamma) + \Gamma(e^+e^- \rightarrow \gamma\gamma\gamma) + \Gamma(e^+e^- \rightarrow \gamma\gamma\gamma\gamma) + \dots \approx 1.05 \times \Gamma(e^+e^- \rightarrow \gamma\gamma)$$

The N+1 photon annihilation can introduce a sizable correction to the N photon rate

**Knowledge at better than % level necessary**

# Bhabha scattering

- Exists in G4
- Radiative correction to the Bhabha:  $e^+e^- \rightarrow e^+e^-\gamma$ 
  - In principle such a process is already considered in GEANT4 SB bremsstrahlung model – the inelastic cross section  $d\sigma_e/dk$  term
    - Is this the whole story?
  - Simulation can be performed through external libraries
    - MCJPG
      - Has to be upgraded since many formulas inside use  $m_e=0$  approximation (recall  $E_{CM}(\text{PADME/VEPP3}) \sim 23 \text{ MeV}$ )
    - Babayaga
      - No extra work necessary, ready to go
  - Should avoid double counting with GEANT4?
  - Take into account the screening from the atomic nuclei
- The specific treatment of this type of background has been neglected so far
  - Necessary to be tested and verified in consistent way

# Conclusions

- Background evaluation is a key ingredient to understand the sensitivity of the dark photon searching experiments
- Different techniques
  - MC based
  - Data driven – electron beam
  - Data driven – fit sidebands
  - A combination of all three
- Just EM processes included but still not all machinery and tools experienced at that low center of mass energy
- How to assure the knowledge of the background contribution at  $< 1\%$  level?