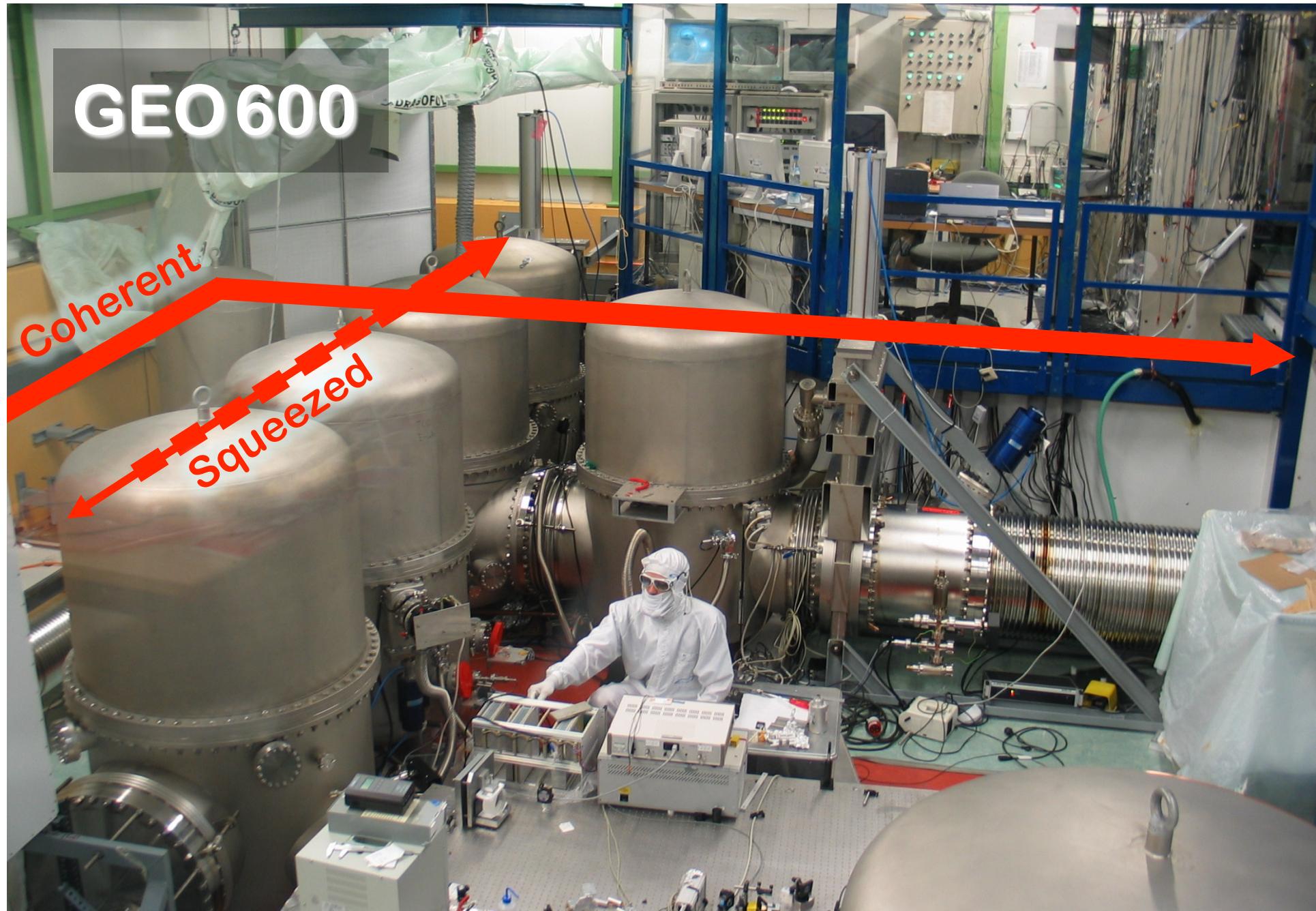


# Light Sources and Interferometer Topologies

Roman Schnabel

Albert-Einstein-Institut (AEI)  
Institut für Gravitationsphysik  
Leibniz Universität Hannover





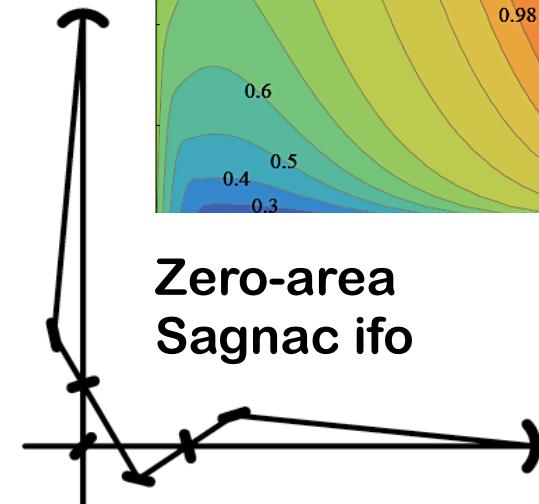
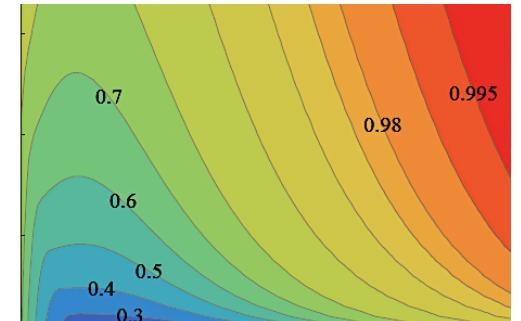
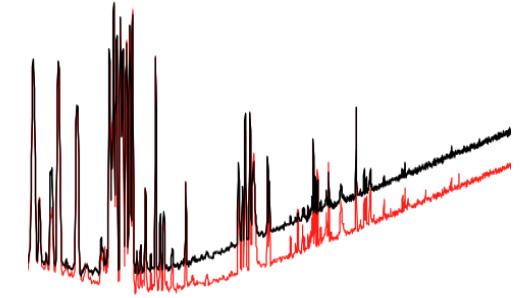
Albert-Einstein-Institut



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# Outline

- Optimality of the “coherent state – squeezed state approach”
- Further aspect: radiation pressure noise
- Ponderomotive Squeezing
- Squeezed vacuum generation  
    @ 1064nm, @ 1550nm, @ 532nm
- Avoiding radiation pressure noise:  
    Sagnac interferometer
- Dynamic back-action and optical springs



## Quantum-mechanical noise in an interferometer

Carlton M. Caves

*W. K. Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, California 91125*

(Received 15 August 1980)

The interferometers now being developed to detect gravitational waves work by measuring the relative positions of widely separated masses. Two fundamental sources of quantum-mechanical noise determine the sensitivity of such an interferometer: (i) fluctuations in number of output photons (photon-counting error) and (ii) fluctuations in radiation pressure on the masses (radiation-pressure error). Because of the low power of available continuous-wave lasers, the sensitivity of currently planned interferometers will be limited by photon-counting error. This paper presents an analysis of the two types of quantum-mechanical noise, and it proposes a new technique—the “squeezed-state” technique—that allows one to decrease the photon-counting error while increasing the radiation-pressure error, or vice versa. The key requirement of the squeezed-state technique is that the state of the light entering the interferometer’s normally unused input port must be not the vacuum, as in a standard interferometer, but rather a “squeezed state”—a state whose uncertainties in the two quadrature phases are unequal. Squeezed states can be generated by a variety of nonlinear optical processes, including degenerate parametric amplification.

### Introduction of „squeezed states“ to electro-magnetic fields:

H. P. Yuen, *Two-photon coherent states of the radiation field*,  
Phys. Rev. A **13**, 2226–2243 (1976)



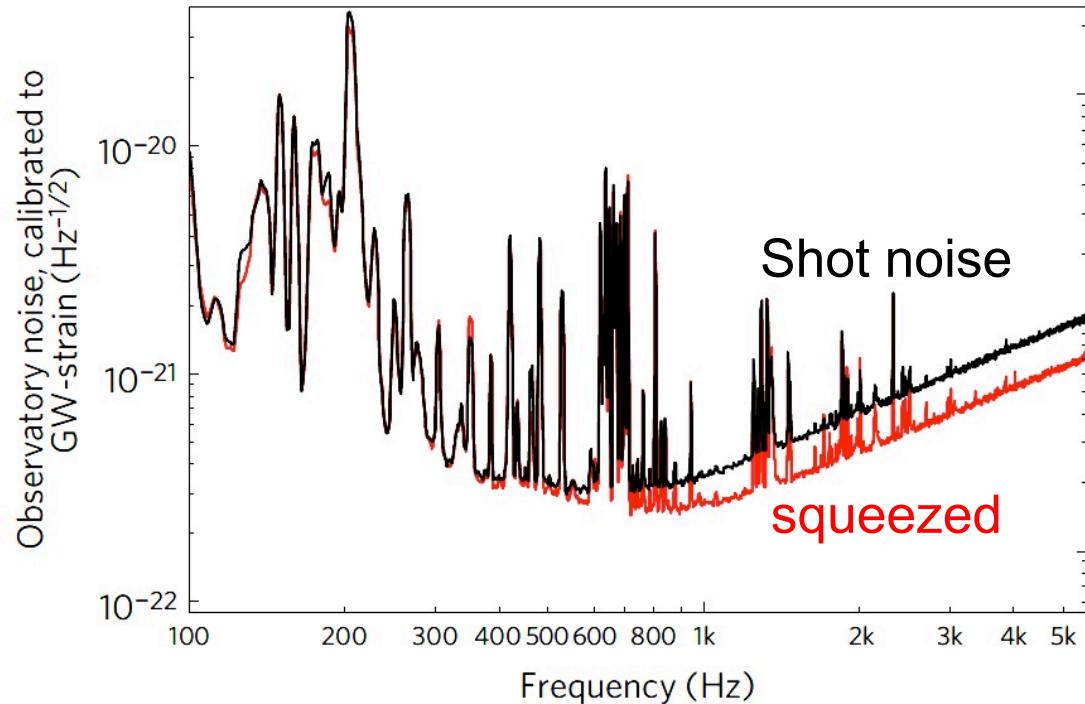
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# A gravitational wave observatory operating beyond the quantum shot-noise limit

The LIGO Scientific Collaboration <sup>†\*</sup>



GEO600 now regularly uses squeezed light and has acquired 205 days of squeezed science data.

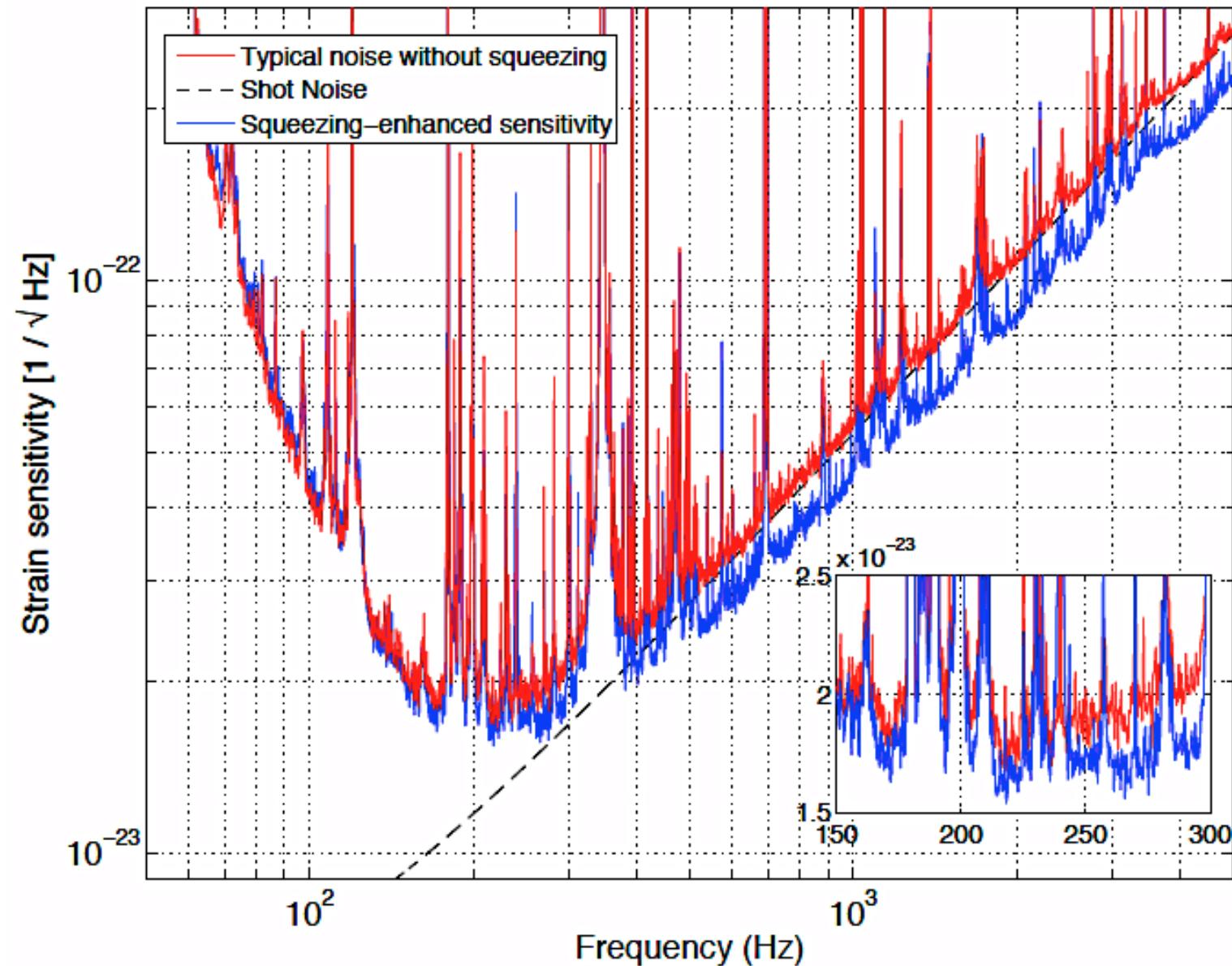
[Grote, Danzmann, Dooley, Schnabel, Slutsky, Vahlbruch, Phys. Rev. Lett. 110, 181101(2013)]



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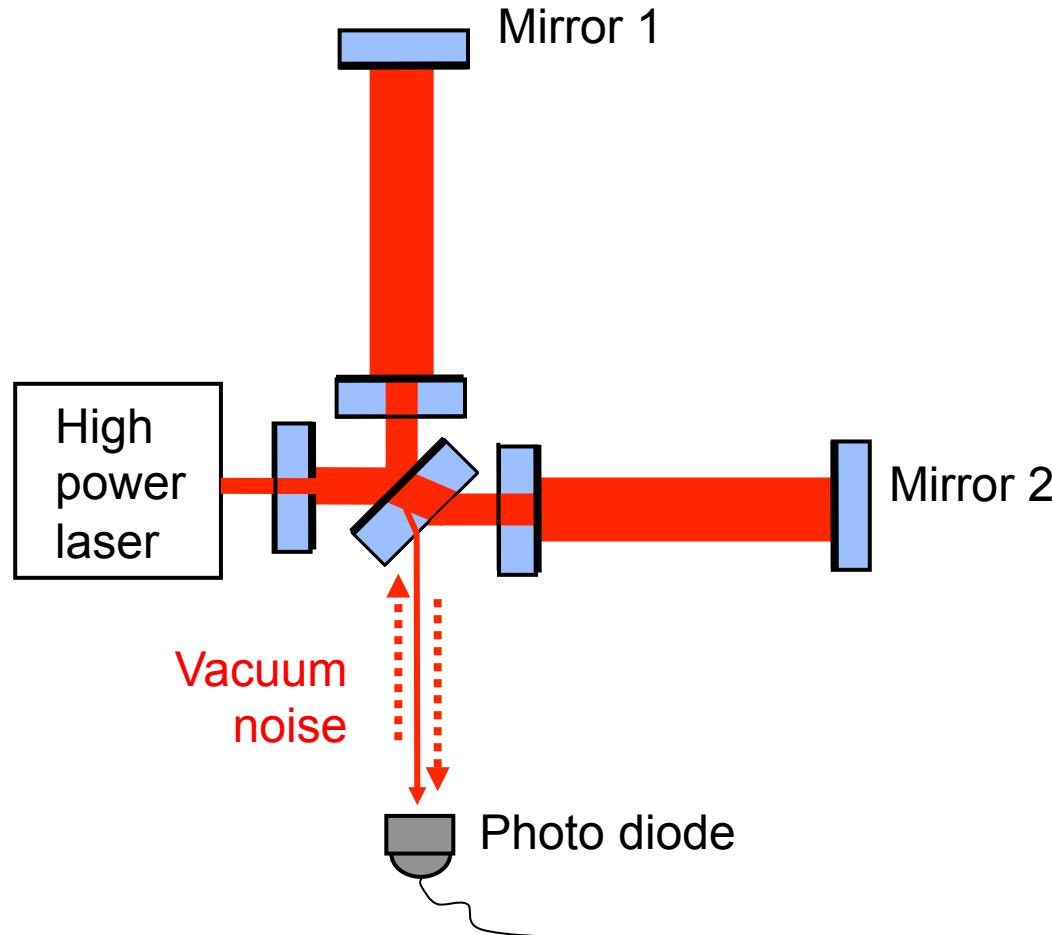
Roman Schnabel, 23 / May / 2013



# Shot Noise / Vacuum Noise

C. M. Caves  
(1981):

Vacuum noise  
that enters at  
the dark port is  
responsible for  
shot-noise on  
photo diode



[Caves, Phys. Rev. D 23, 1693 (1981)]



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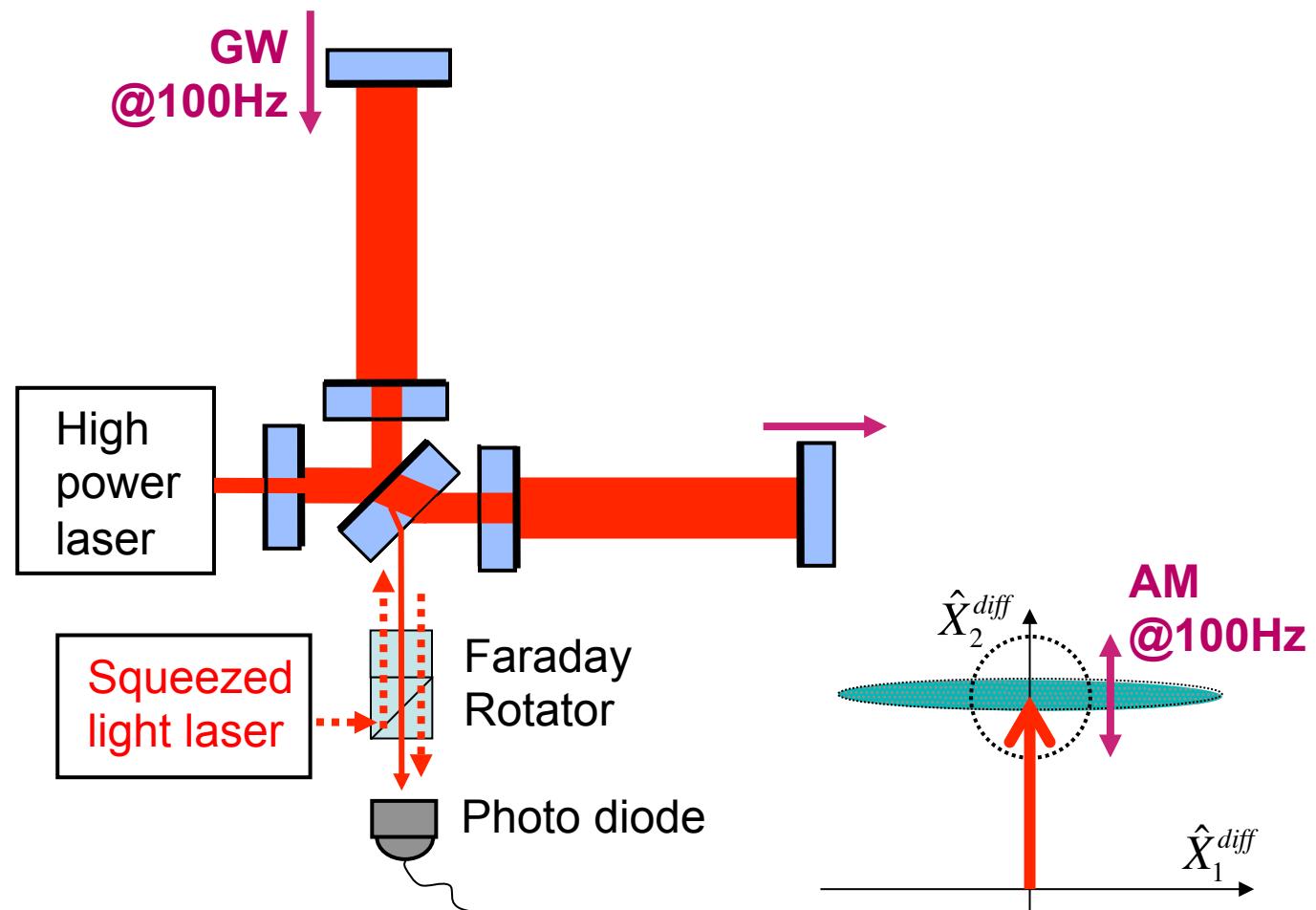


Roman Schnabel, 23 / May / 2013

# Squeezing the Shot-Noise: “Optimal”?

C. M. Caves  
(1981):

Vacuum noise  
that enters at  
the dark port is  
responsible for  
shot-noise on  
photo diode



[Caves, Phys. Rev. D 23, 1693 (1981)]



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# Optimality of Phase Sensing

Well-known: “Light power should be high and optical loss low!  
(And radiation pressure noise needs to be evaded.)”

What is the optimum approach to measure a small phase  $\Delta\Phi$  for a  
given photon rate and for a given decoherence rate (loss)?

For just a few photons (per integration time) and low optical loss,  
Fock states ( $N00N$ -states) are optimal:

$$\Delta\Phi_{|N00N\rangle} = \frac{1}{N}$$

$$\Delta\Phi_{|\alpha\rangle} = \frac{1}{\sqrt{N}}$$

$$\Delta\Phi_{|\alpha,r\rangle} \approx \frac{e^{-r}}{\sqrt{N}}$$

“Heisenberg Scaling”

[J. Rarity *et al.*, *Two-photon interference in a Mach-Zehnder interferometer*,  
Phys. Rev. Lett. 65, 1348 (1990)]

[M. Mitchell *et al.*, *Superresolving phase measurements with a multiphoton entangled state*, Nature 429, 161 (2004)]



# Optimality of Phase Sensing

For many photons ( $N > 10^{12}$  per second) and some optical loss ( $1-\eta > 1\%$ ), the combination of bright coherent states and squeezed vacuum states is optimal!  
(Current GW detectors:  $N \approx 10^{22}/s$ ,  $(1-\eta) \approx 40\%$ )

Cramér–Rao bound,  $\eta < 1$ :

⇒

$$\Delta\Phi_{|\psi\rangle} \geq \sqrt{\frac{1-\eta}{\eta N}}$$

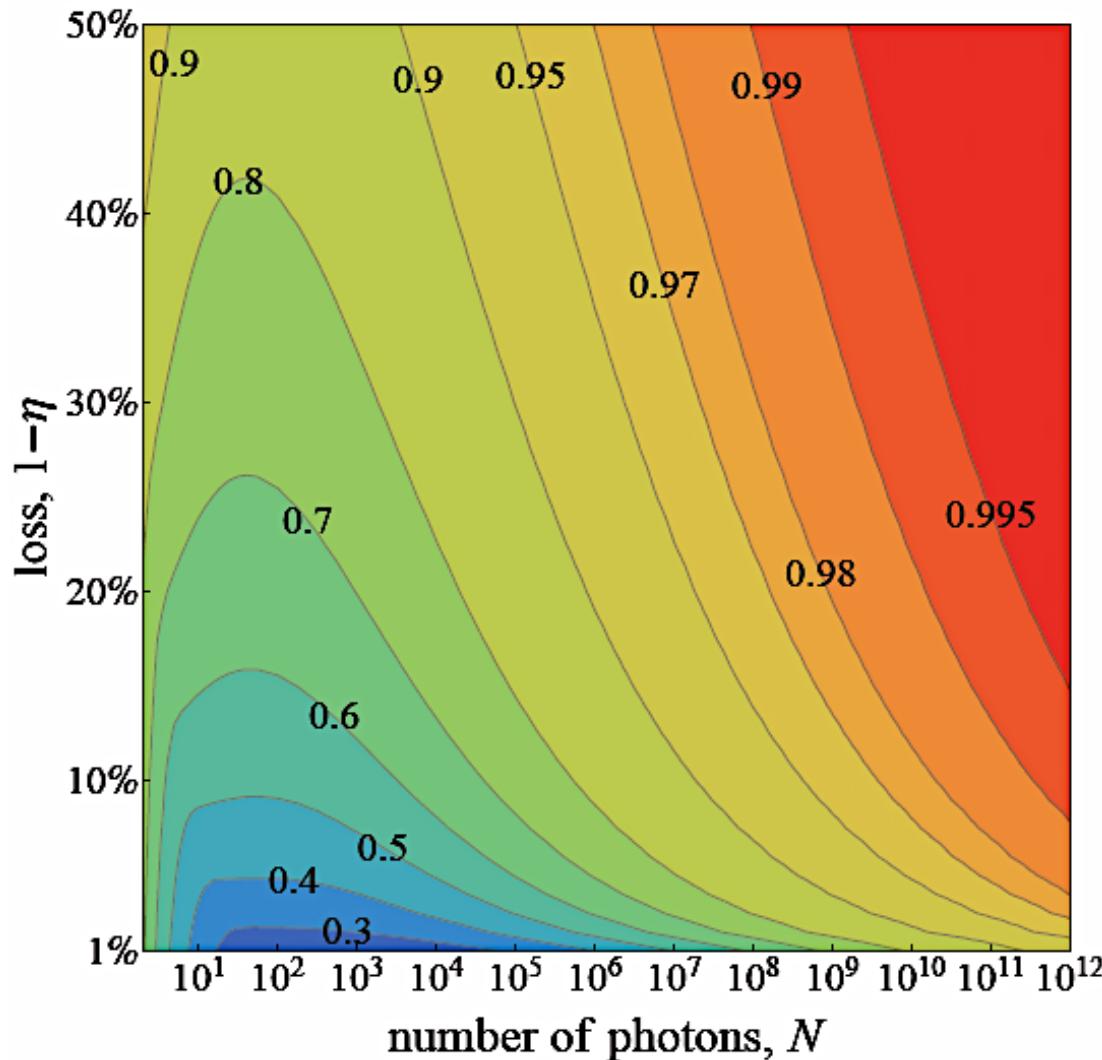
Caves 1981:

$$\Delta\Phi_{|\alpha,r\rangle} \approx \sqrt{\frac{1-\eta + \eta e^{-2r}}{\eta N}}$$

[R. Demkowicz-Dobrzanski, K. Banaszek, R.S., *Fundamental quantum interferometry bound for the squeezed-light-enhanced GW detector GEO600, LIGO-P1300059-v2*]



# Optimality of Phase Sensing

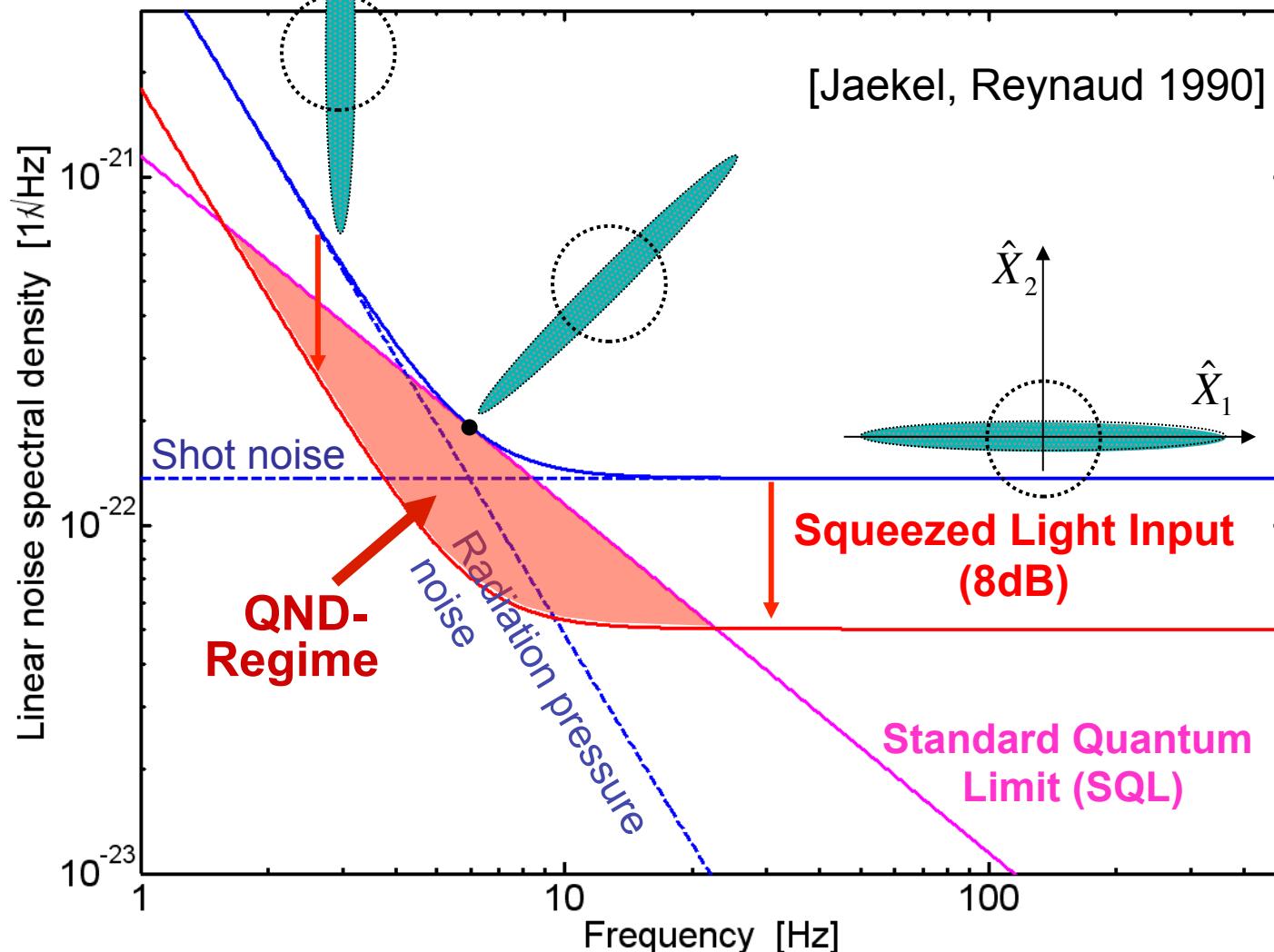


For  $N \approx 10^{22}/s$  and 40% loss, 16 dB instead of the currently used 10 dB of input squeezing would achieve 99.9996% of the ultimate phase sensitivity.

→ “No need for other than coherent and squeezed states in GW detection!”



# Squeezing | SN and RPN



*Europhys. Lett.*, 13 (4), pp. 301-306 (1990)

## Quantum Limits in Interferometric Measurements.

M. T. JAEKEL (\*) and S. REYNAUD (\*\*)

(\*) *Laboratoire de Physique Théorique de l'Ecole Normale Supérieure* (§)

24 rue Lhomond, F-75231 Paris Cedex 05

(\*\*) *Laboratoire de Spectroscopie Hertzienne* (§§), *Université Pierre et Marie Curie*  
4 place Jussieu, F-75252 Paris Cedex 05

“Photon counting noise and radiation pressure  
noise in a GW detector can **both** be squeezed!”

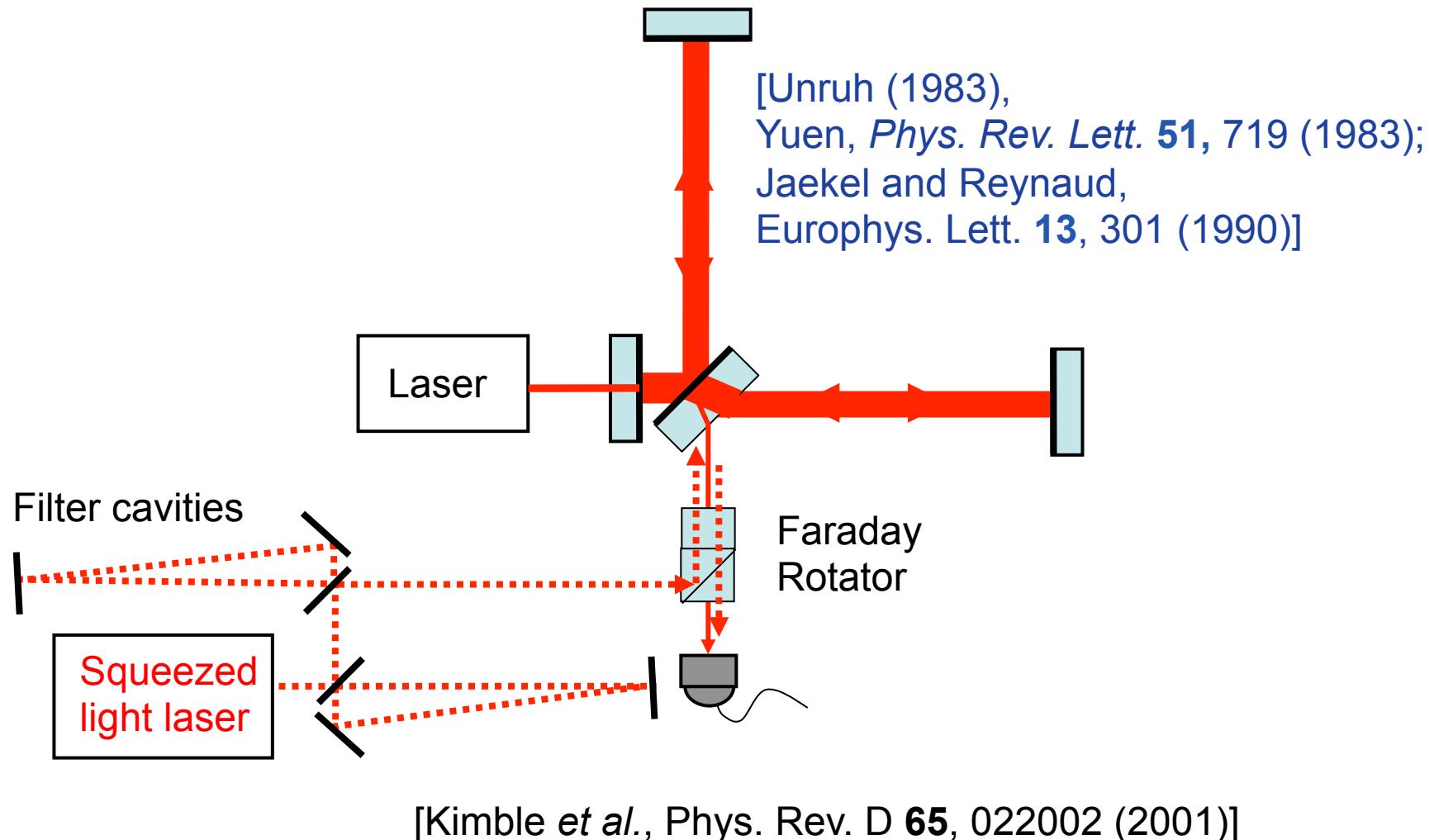
First doubts on the free-mass SQL as the ultimate limit:

W. G. Unruh, in *Quantum Optics, Experimental Gravitation, and Measurement Theory* 647–660 (Plenum, 1983),

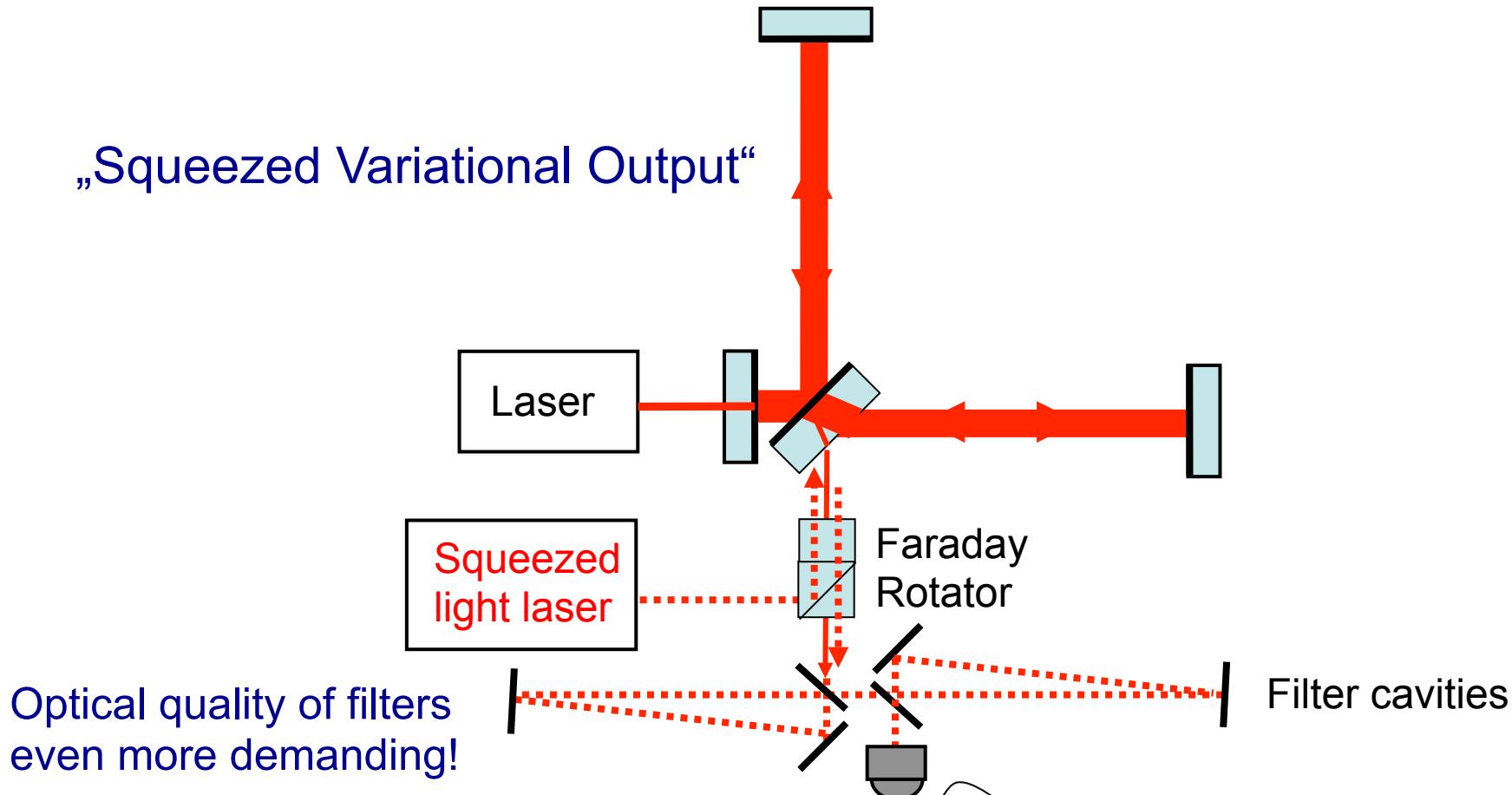
H. P. Yuen, *Phys. Rev. Lett.* **51**, 719 (1983)



# Squeezing SN and RPN: Filter cavities

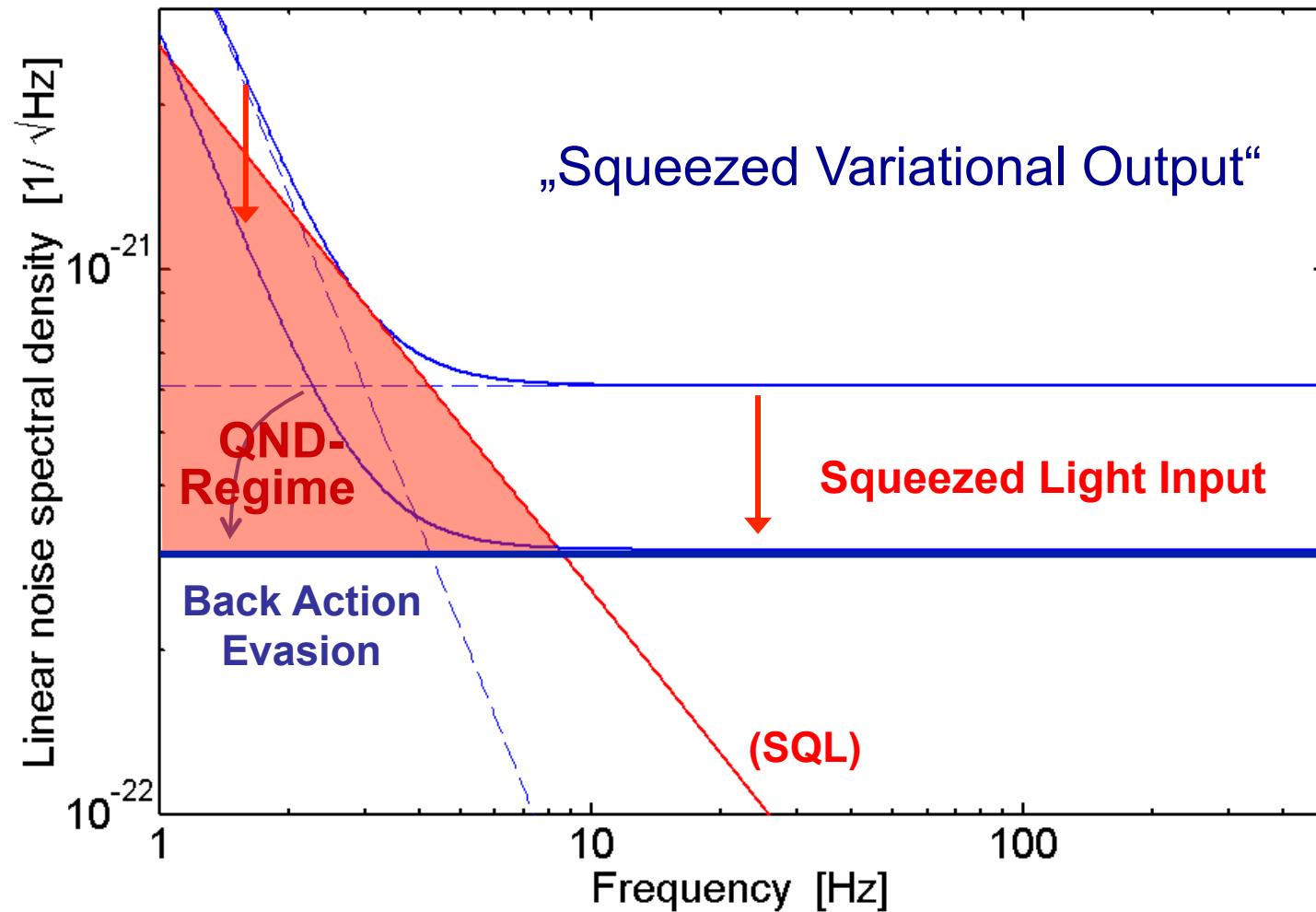


# Squeezing and Full Evasion of RPN

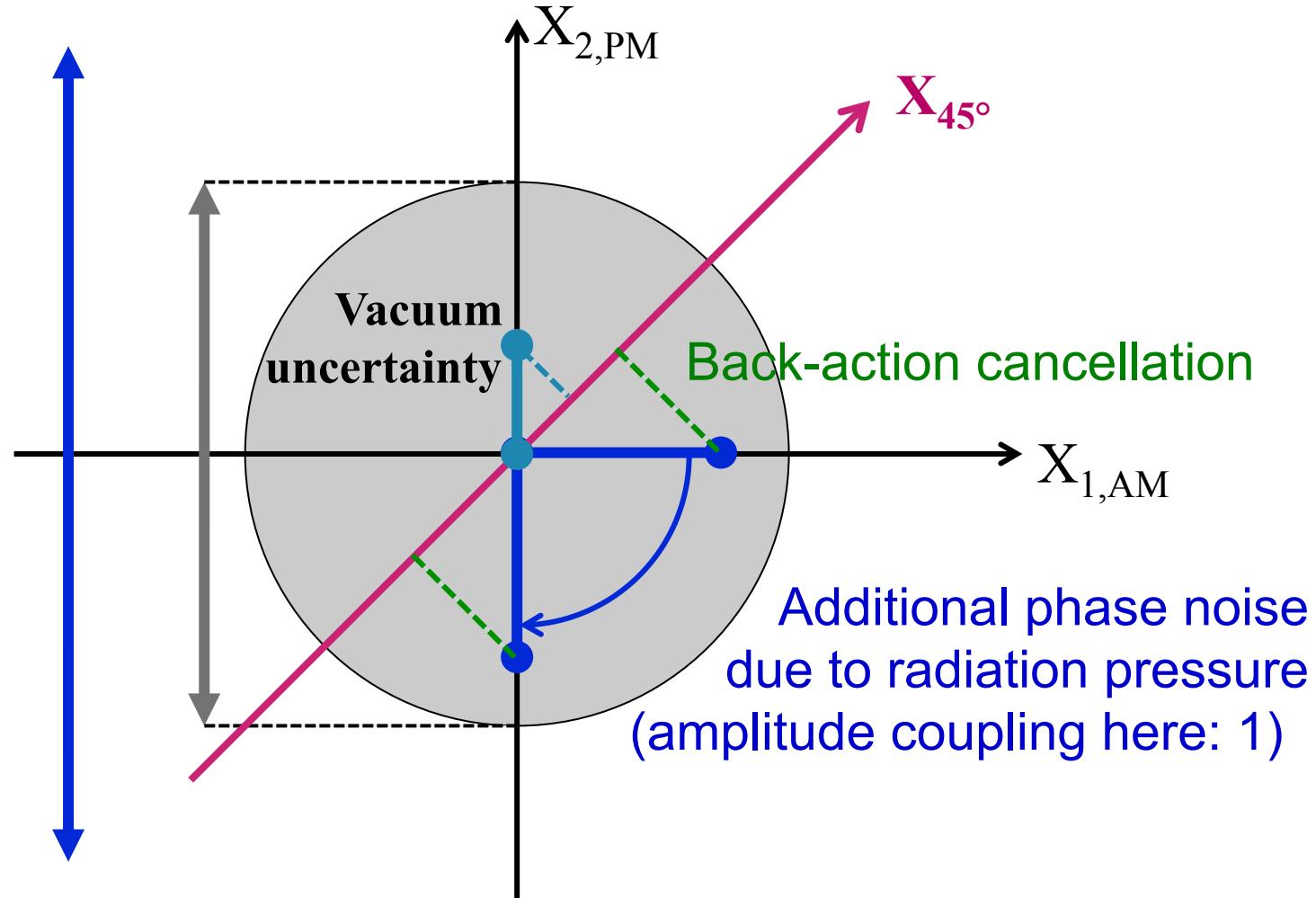


[Kimble *et al.*, Phys. Rev. D 65, 022002 (2001)]

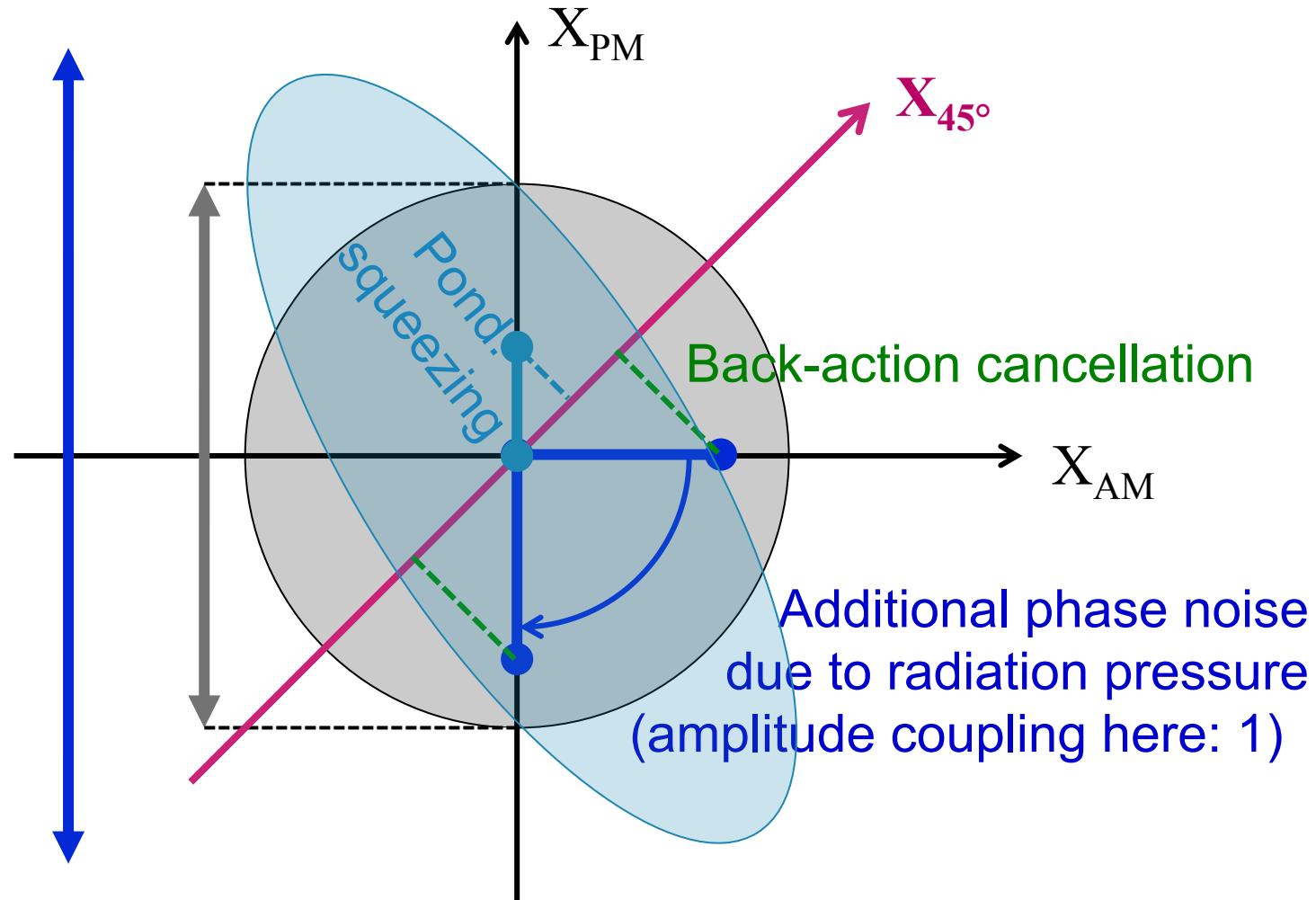
# Squeezing and Full Evasion of RPN



# Ponderomotive Squeezing



# Ponderomotive Squeezing



# Ponderomotive Squeezing

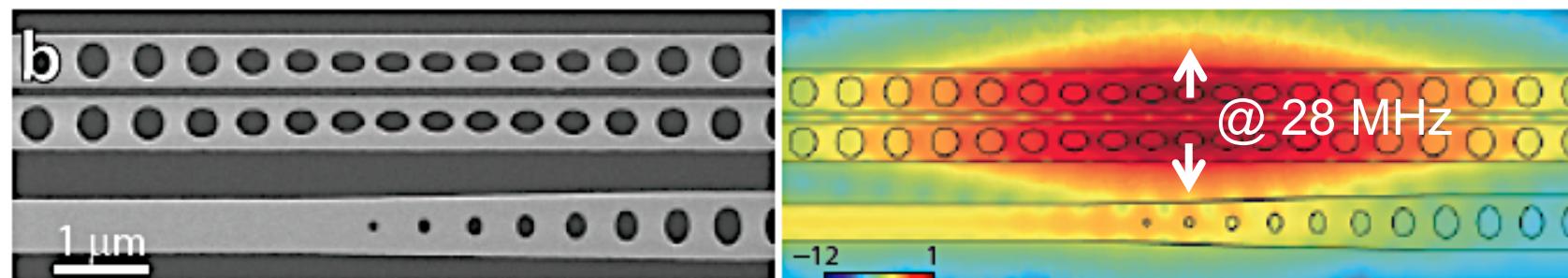
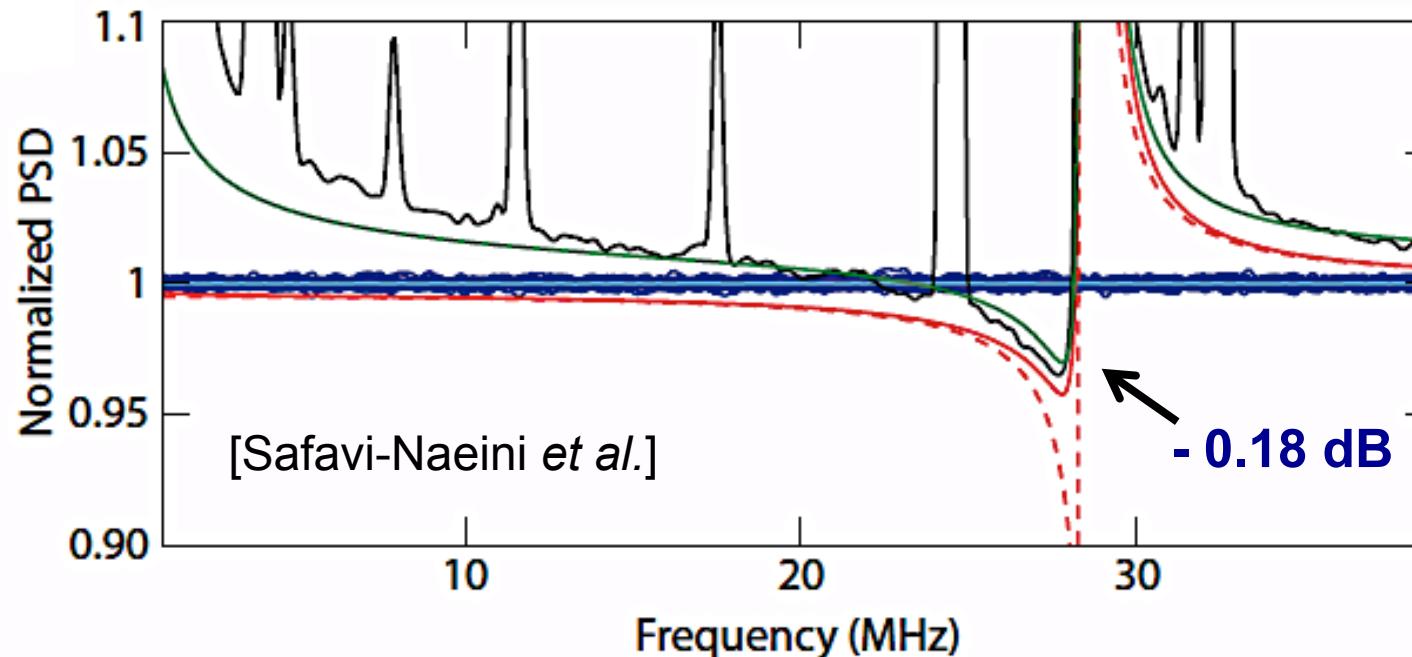
- Is of limited strength (requires an increasingly dominating RPN)
- Has a frequency dependent angle (and strength)
- Good to cancel back-action (less good as a squeezing source)

Recent experiments:

- Observation of radiation pressure noise on a membrane at NIST  
[T. P. Purdy, R. W. Peterson, C. A. Regal, *Science* **339**, 801 (2013)]
- Observation of ponderomotive squeezing at Caltech  
[A.H. Safavi-Naeini, S. Gröblacher, J.T. Hill, J. Chan, M. Aspelmeyer, O. Painter, arXiv:1302.6179]

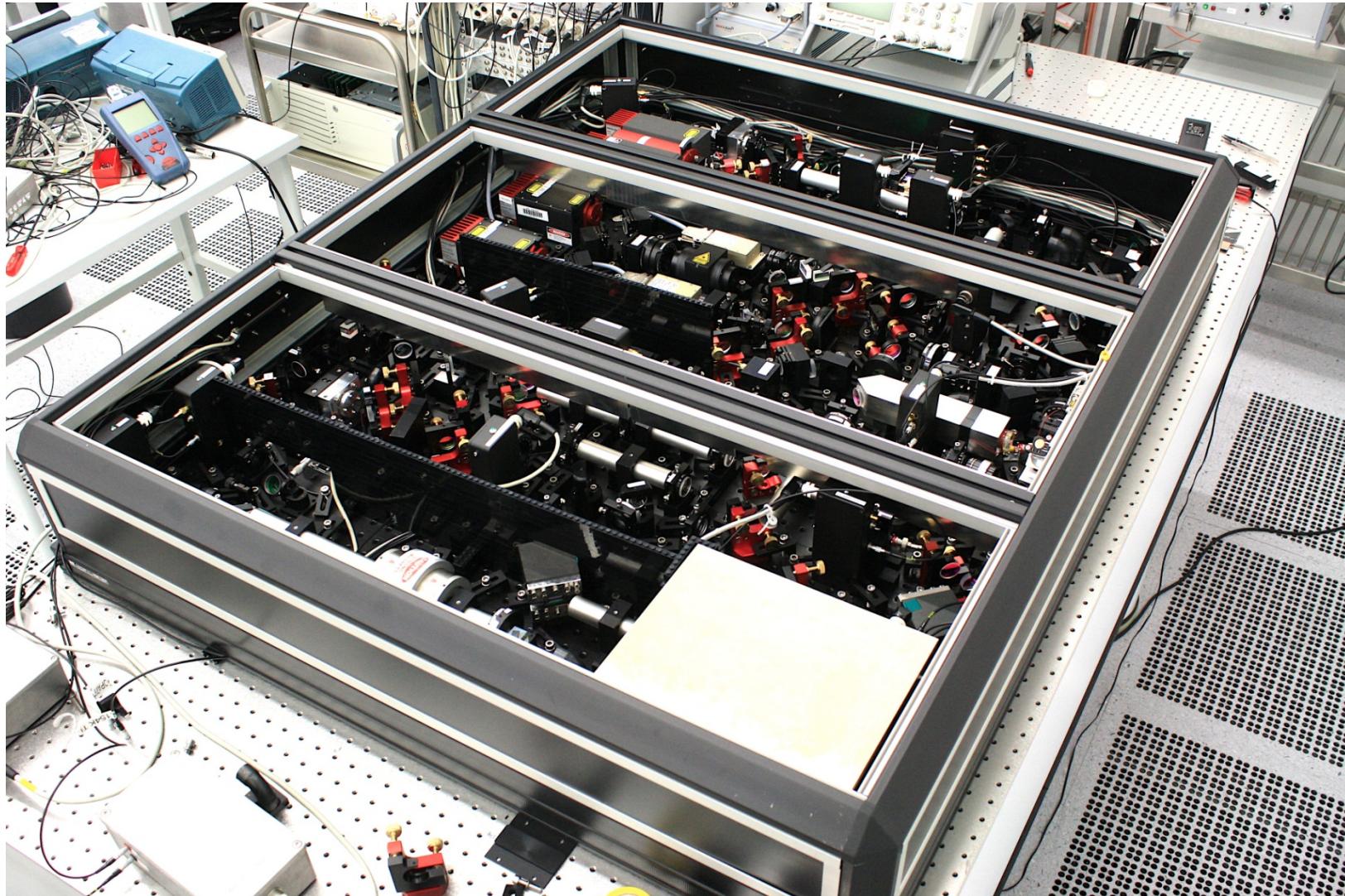


# Ponderomotive Squeezing: Experiment



Waveguide coupled opto-mechanical cavity from Si, at 10 K

# The GEO600 Squeezed Light Source

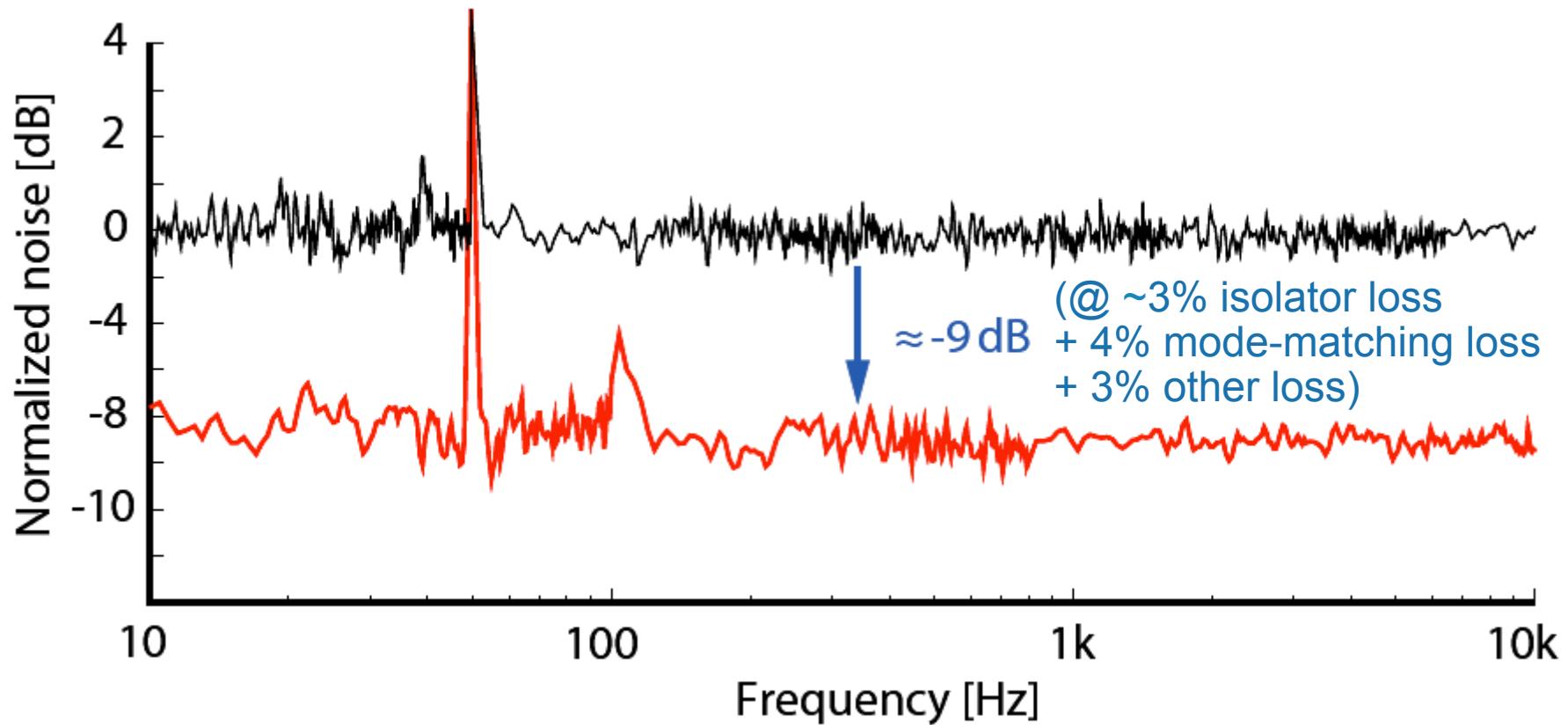


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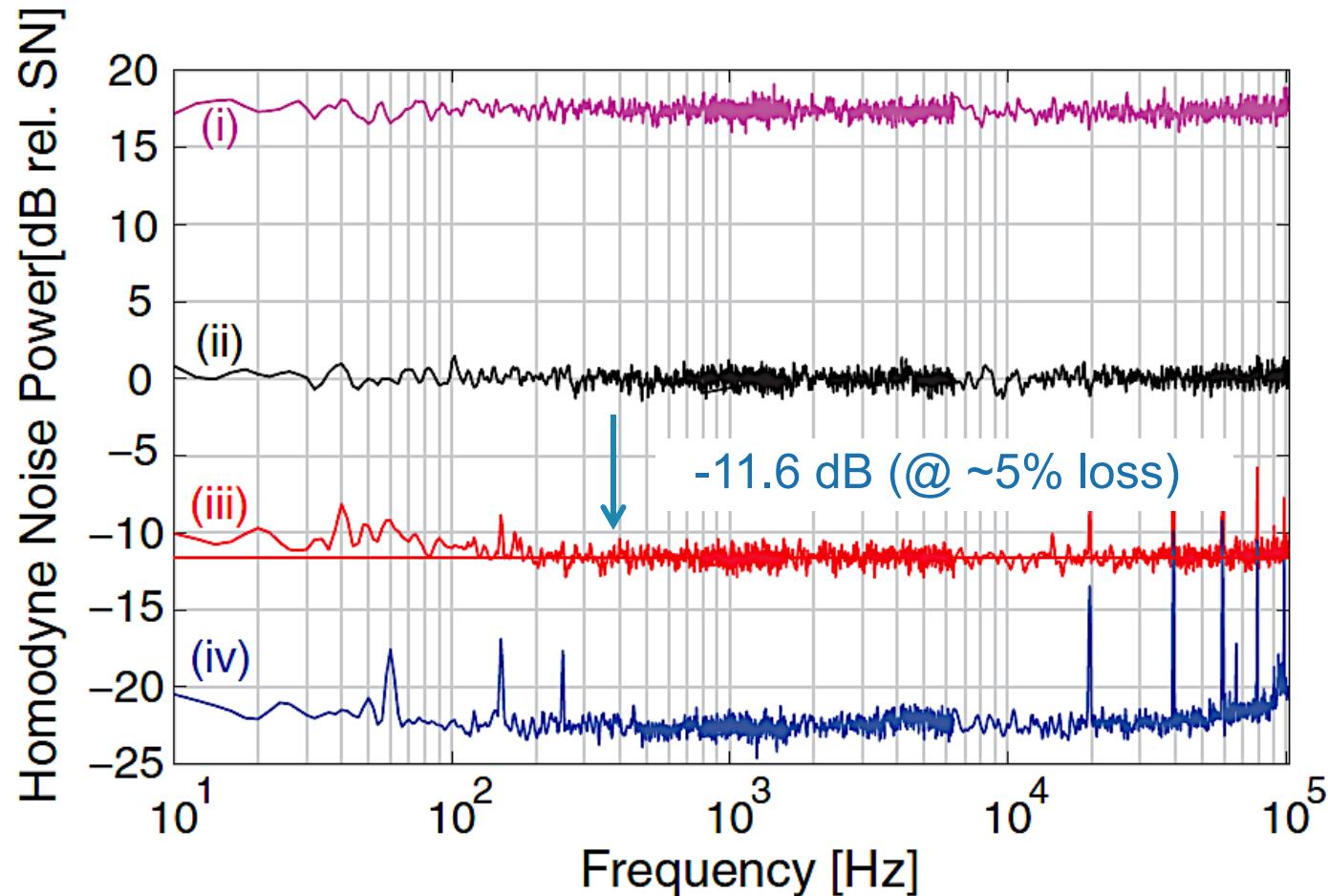
# The GEO600 Squeezed Light Source



[H. Vahlbruch, A. Khalaidovski, N. Lastzka, C. Gräf, K. Danzmann, and R. Schnabel,  
*The GEO600 squeezed light source*, Class. Quantum Grav. **27**, 084027 (2010).]



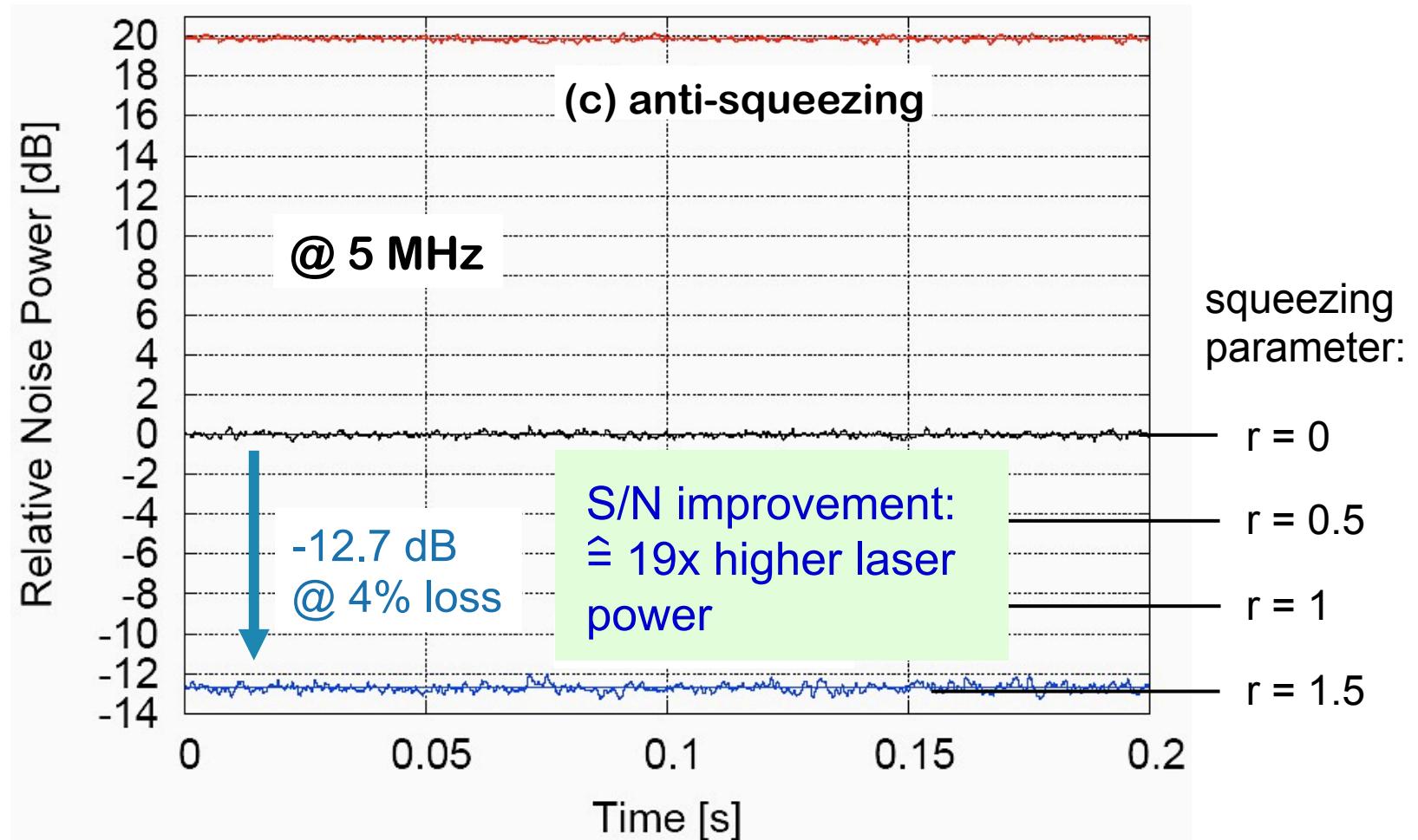
# ANU Squeezed Light Source



[M S Stefszky, C M Mow-Lowry, S S Y Chua, D A Shaddock, B C Buchler, H Vahlbruch, A Khalaidovski, R Schnabel, P K Lam, D E McClelland, CQG **29**, 145015 (2012)]

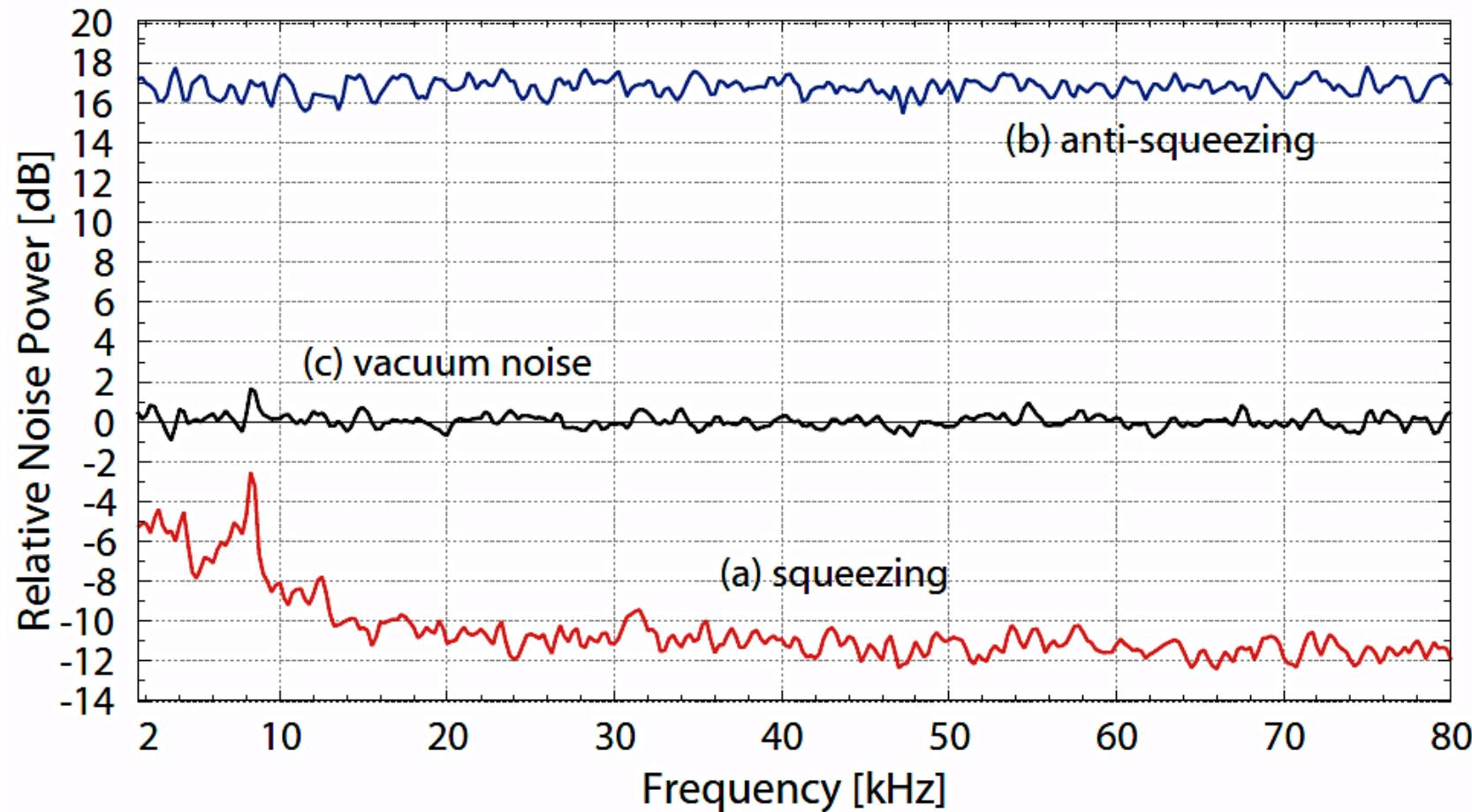


# 12.7 dB Squeezing @1064 nm



[T. Eberle *et al.*, PRL 104, 251102 (2010)]

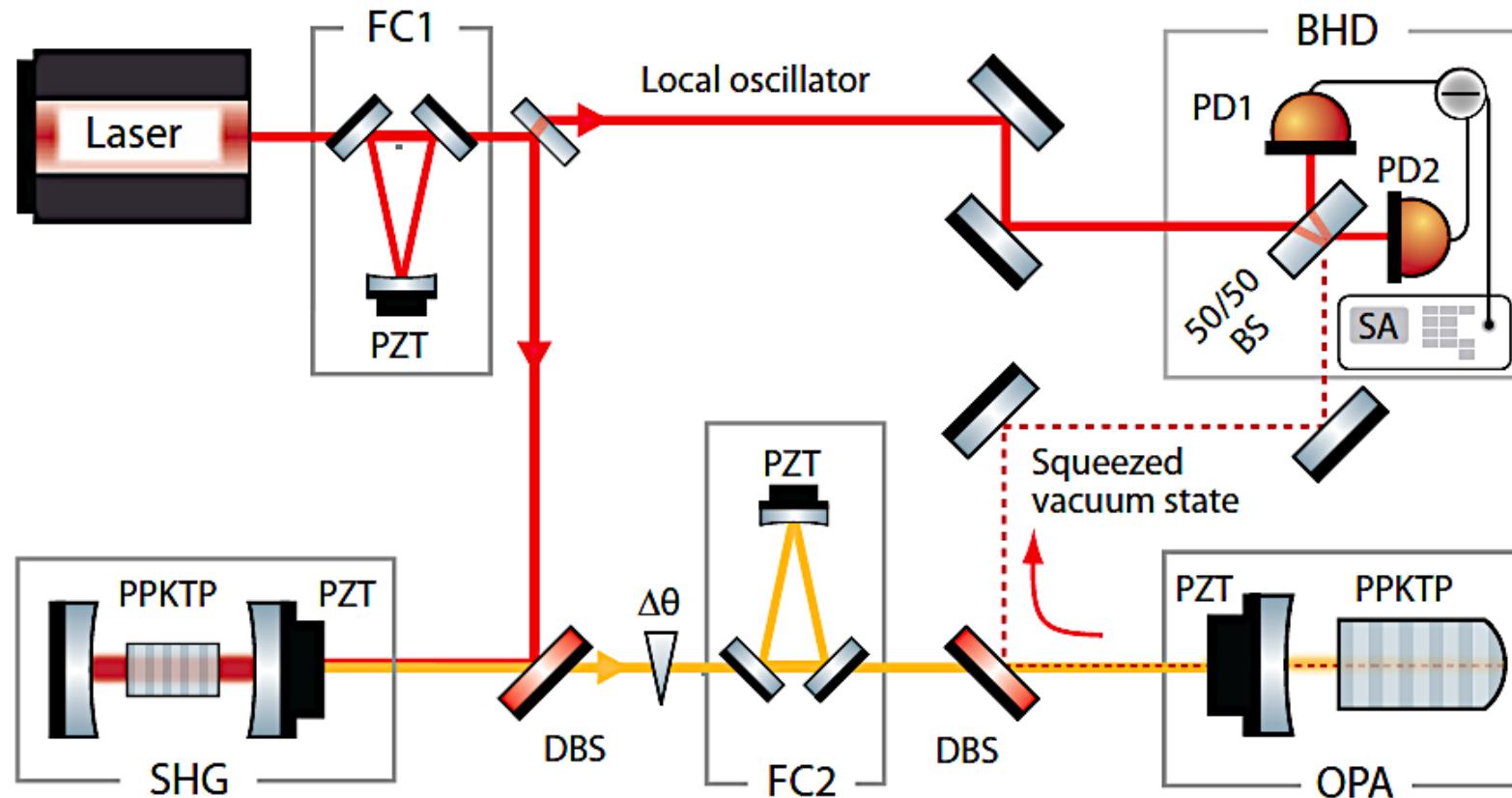
# Squeezing Spectrum @1550 nm



[M. Mehmet *et al.*, Opt. Exp. **25**, 25763 (2011)]



# Squeezed Light at 1064 nm / at 1550 nm



[M. Mehmet *et al.*, Opt. Exp. 25, 25763 (2011)]

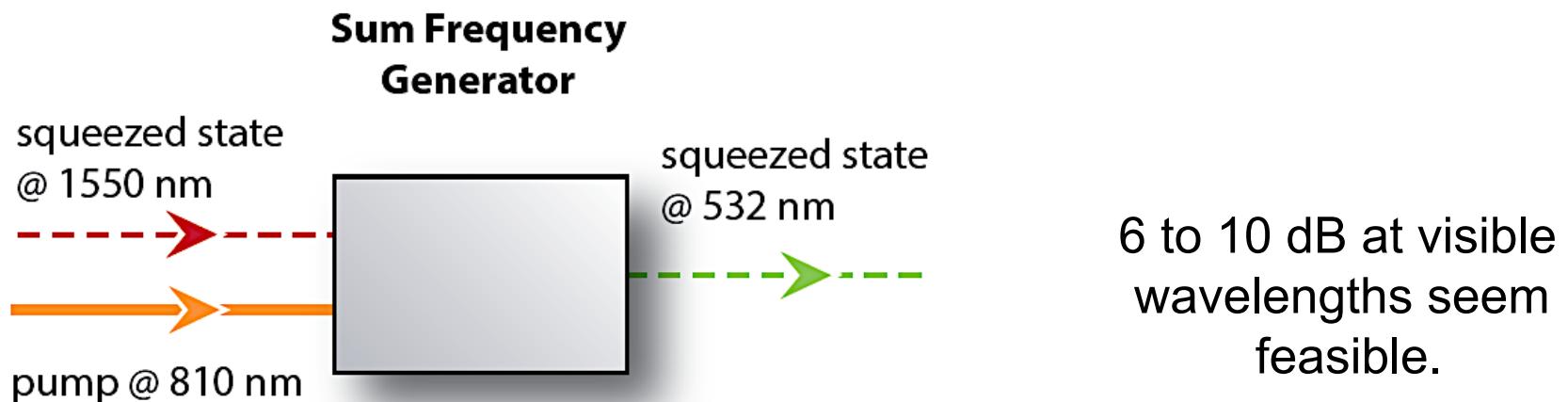


# Squeezing Light at Visible Wavelengths

Strongly (audio-band) squeezed vacuum states at visible wavelengths have not yet been demonstrated.

Problems: The 2<sup>nd</sup> harmonic (UV) pump field damages the crystal.  
(The Kerr-effect requires a bright field having excess noise).

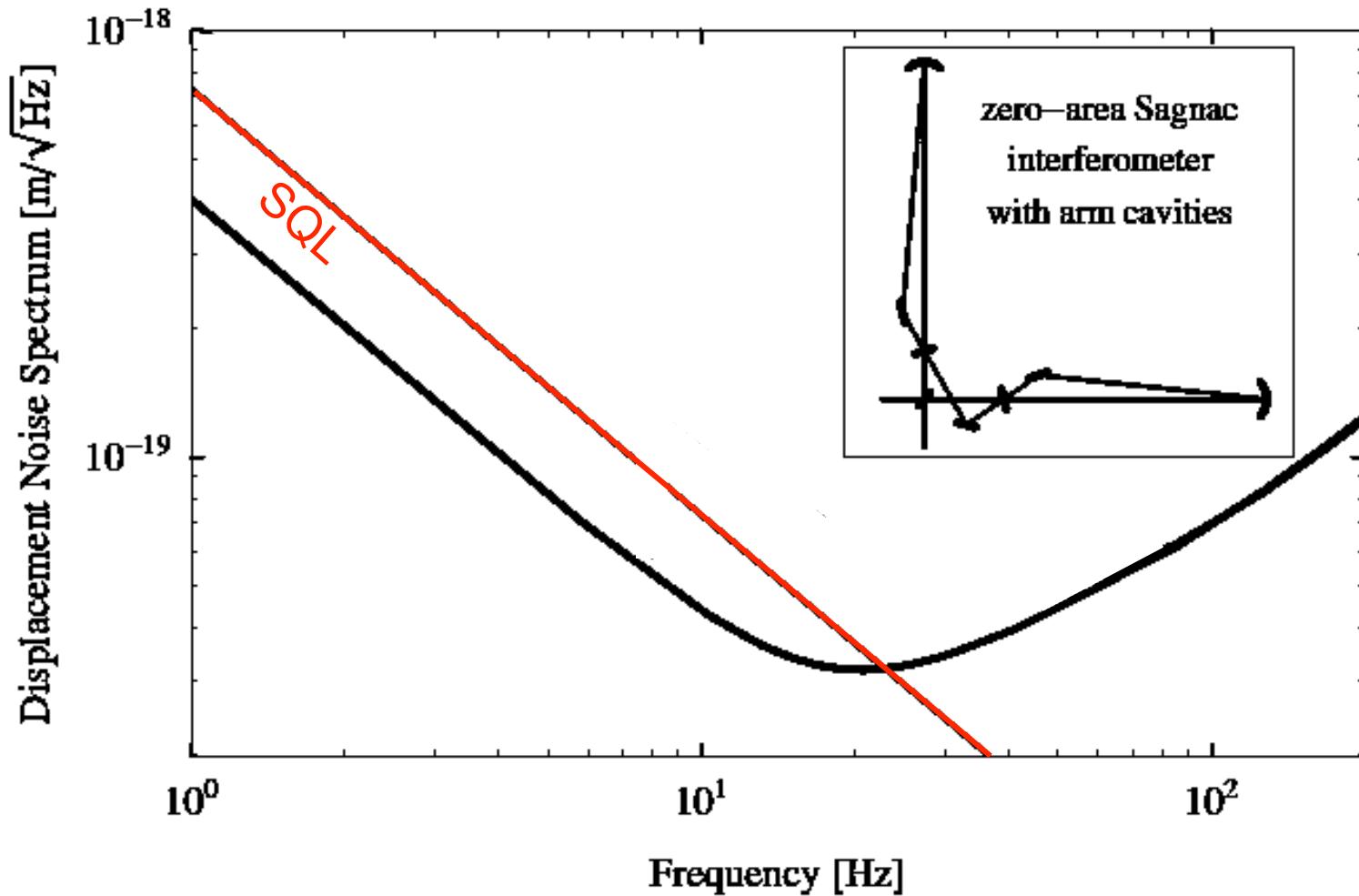
Solution: Up-conversion via sum frequency generation.



[C. Vollmer *et al.*, in preparation]



# Evading RPN: Sagnac Interferometer



[Y. Chen, PRA **67**, 122004 (2003)]



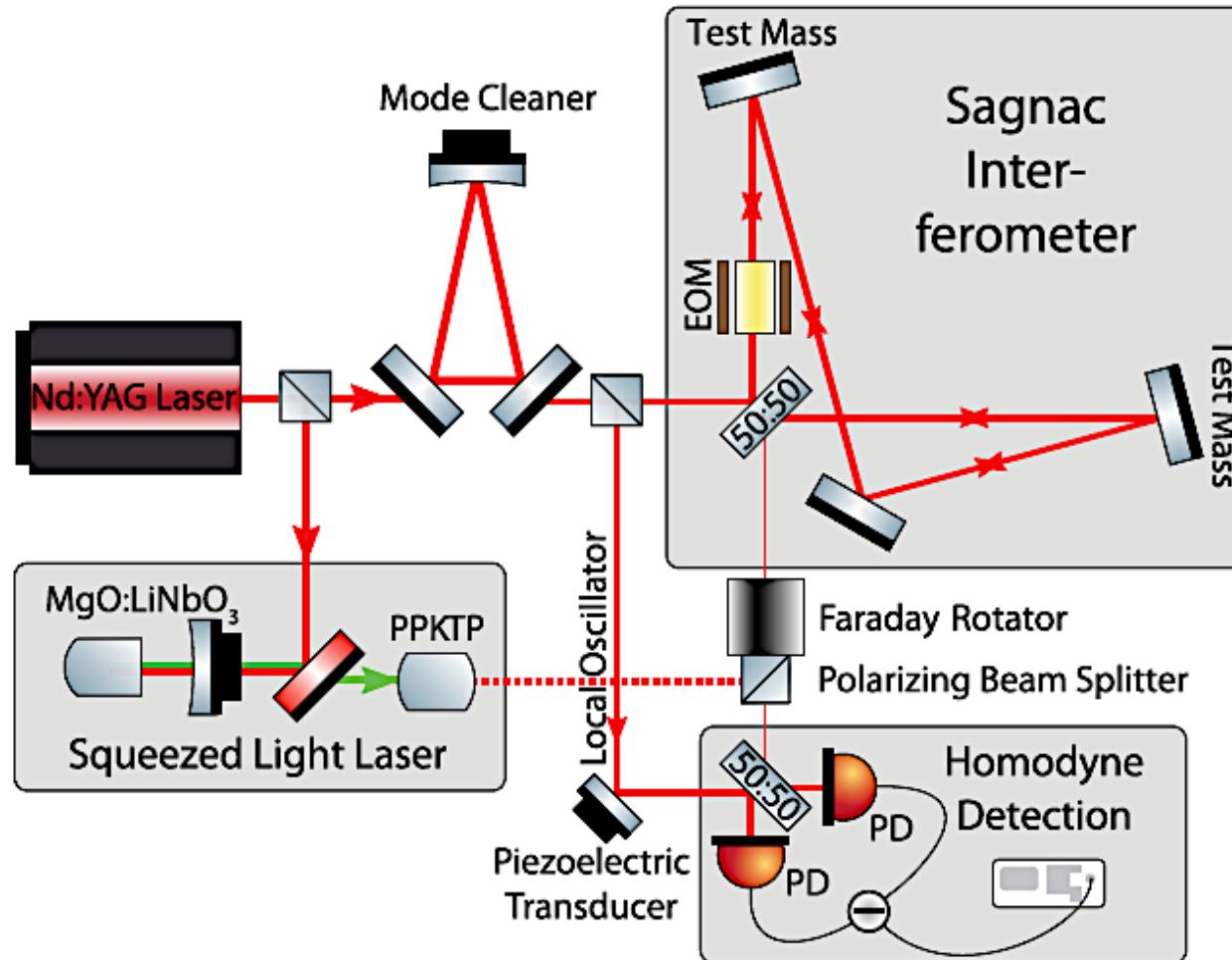
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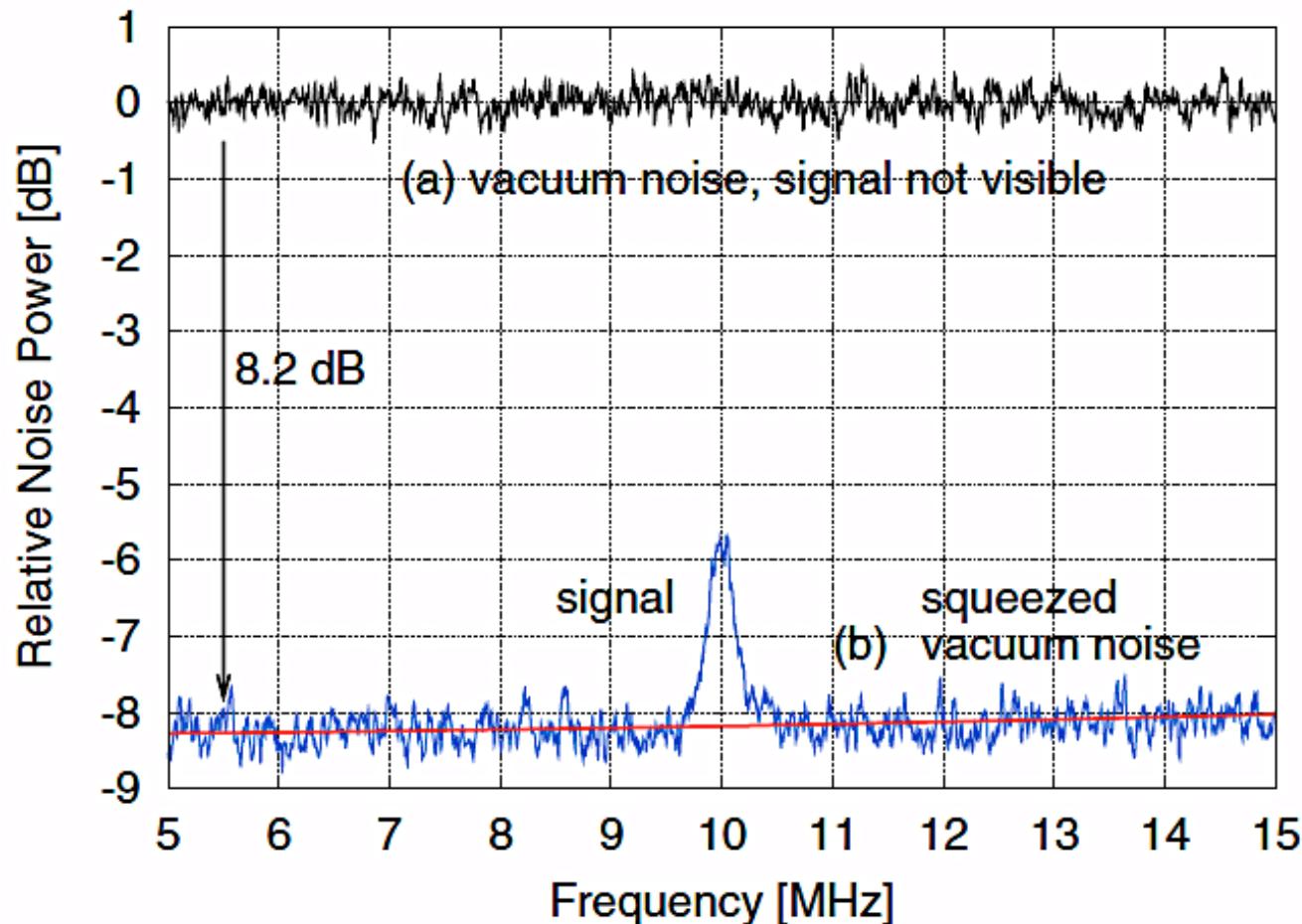
28

# Squeezed Light Enhanced Sagnac IFO



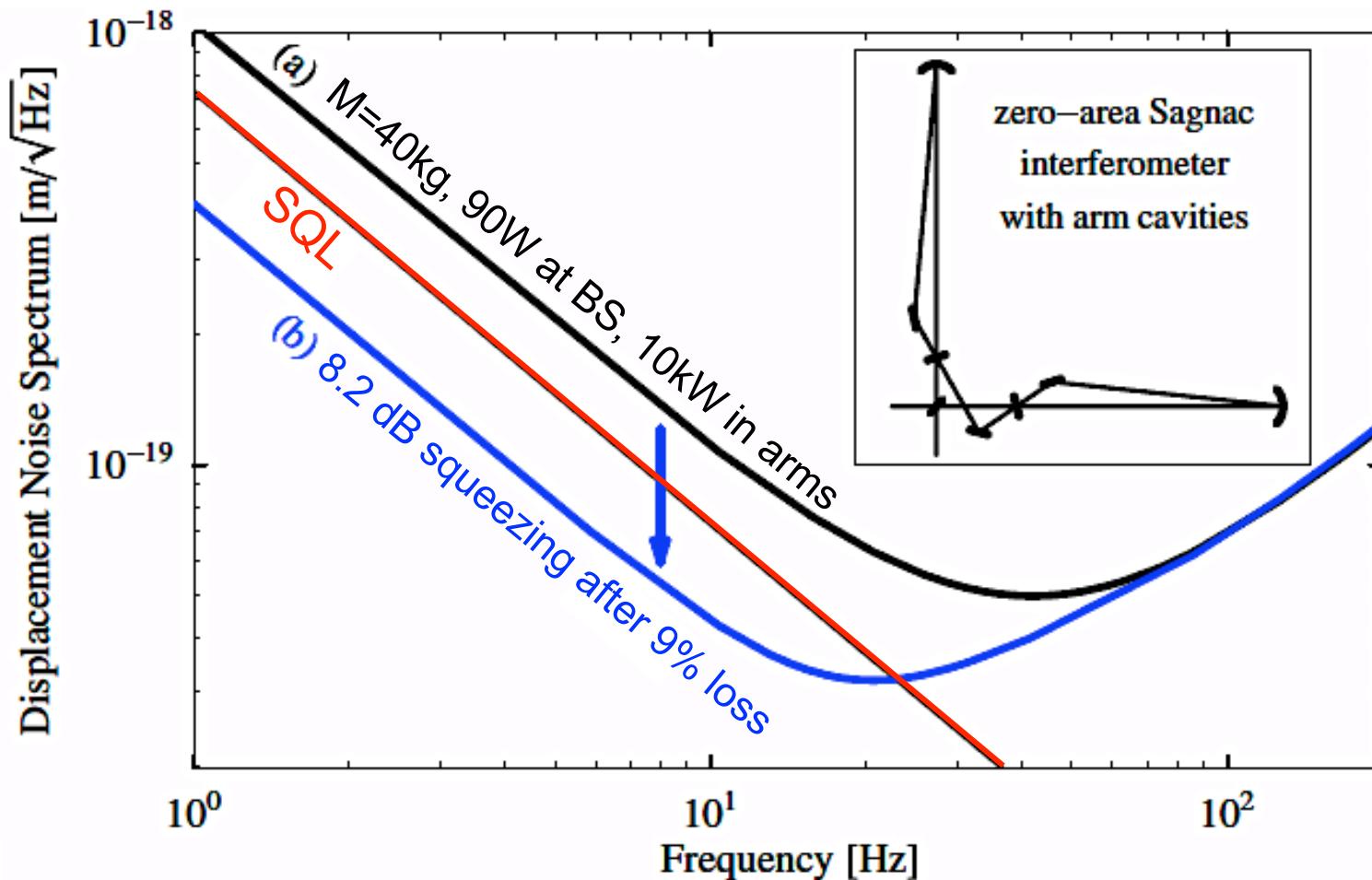
[T. Eberle *et al.*, PRL 104, 251102 (2010)]

# Squeezed Light Enhanced Sagnac IFO



[T. Eberle *et al.*, PRL 104, 251102 (2010)]

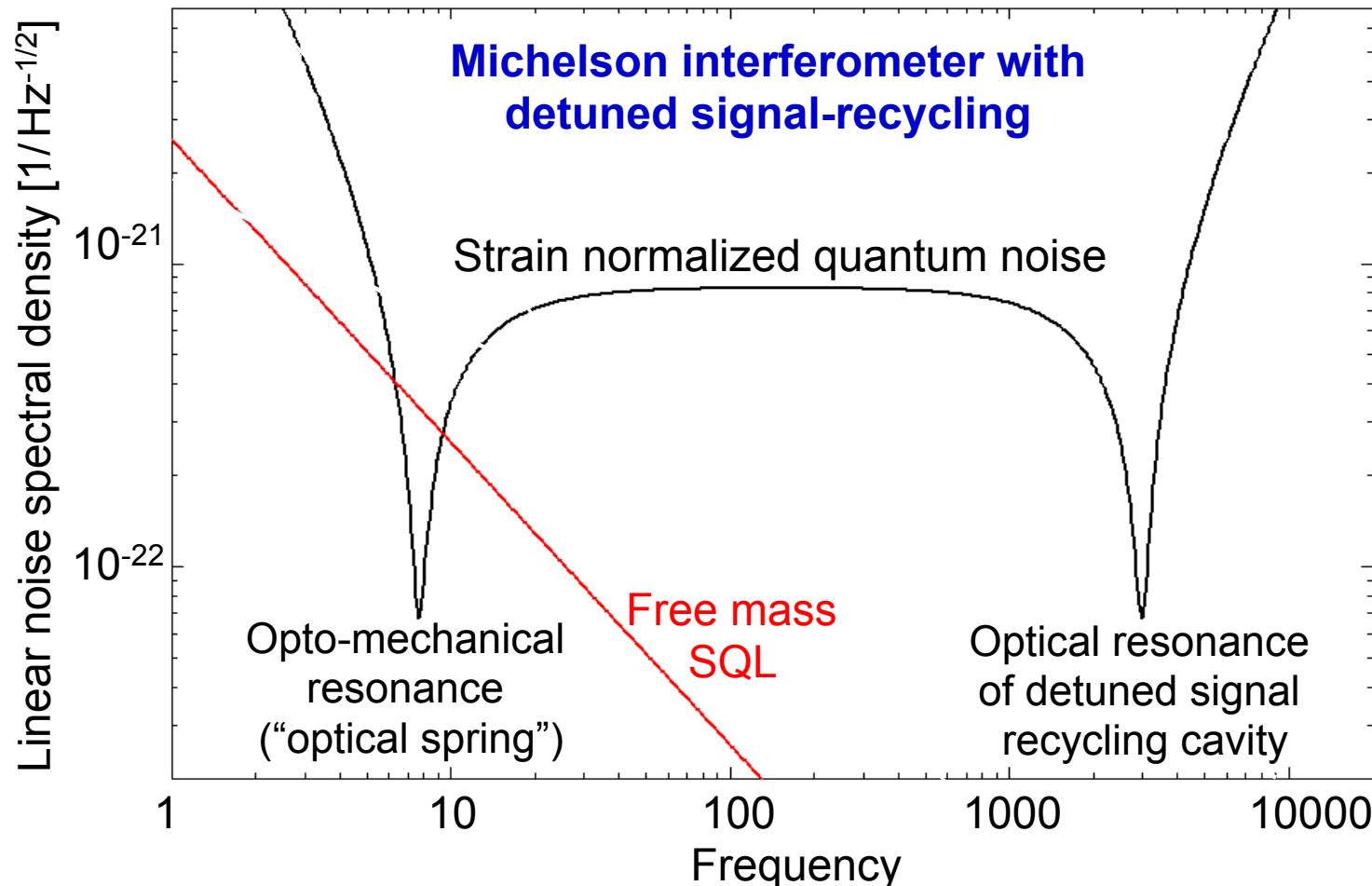
# Squeezed Light Enhanced Sagnac IFO



[T. Eberle S. Steinlechner, J. Bauchrowitz, V. Händchen,  
H. Vahlbruch, M. Mehmet, H. Müller-Ebhardt, R. Schnabel, PRL **104**, 251102 (2010)]

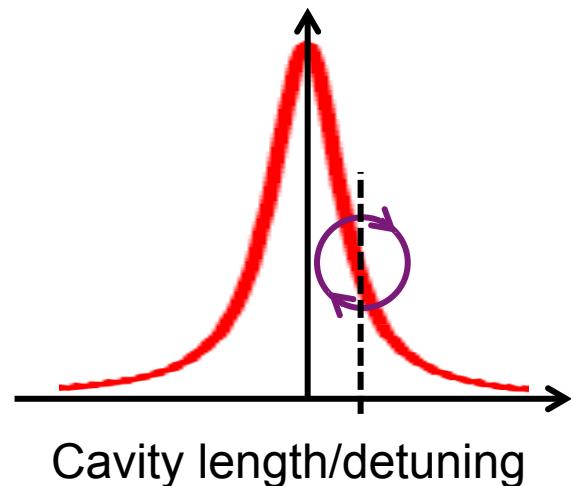


# Dynamical Back-Action: Optical Spring



[A. Buonanno and Y. Chen, Phys. Rev. D 65, 042001 (2002)]

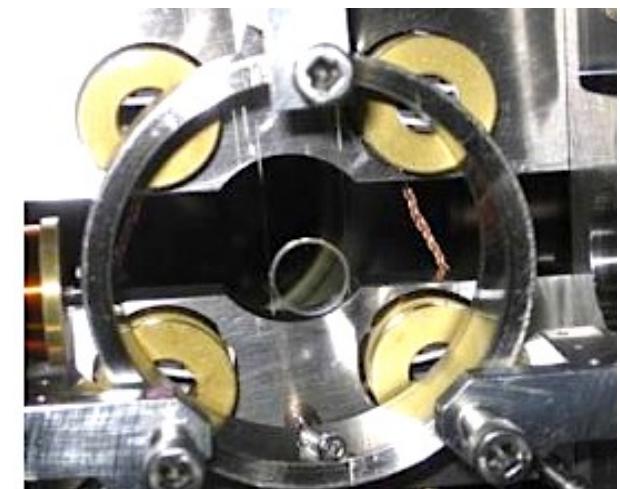
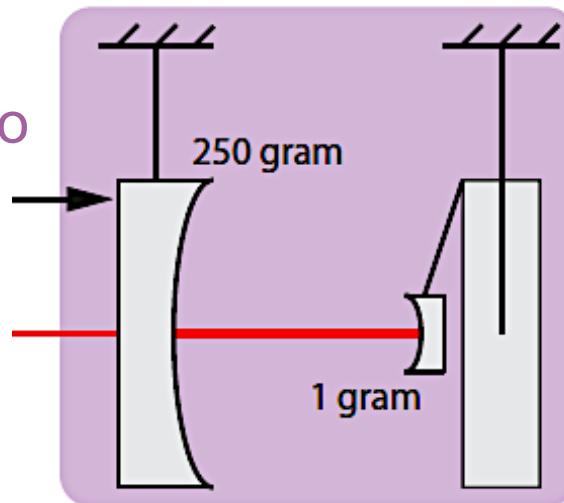
# Dynamical Back-Action – Optical Spring



[B. S. Sheard, M. B. Gray, C. M. Mow-Lowry, D. E. McClelland, S. E. Whitcomb, Phys. Rev. A, 69, 051801 (2004)]

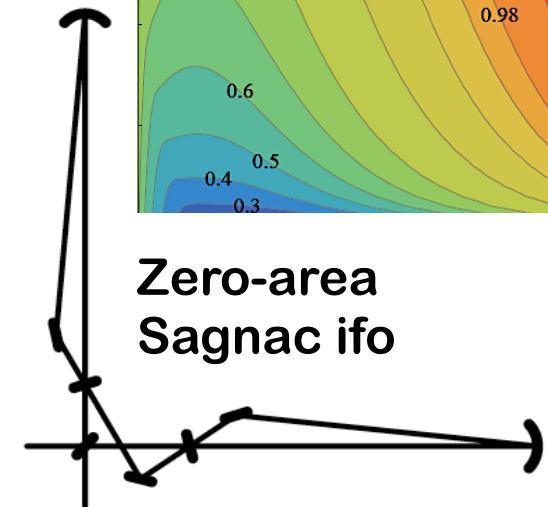
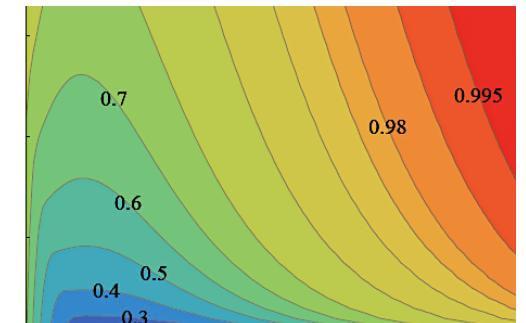
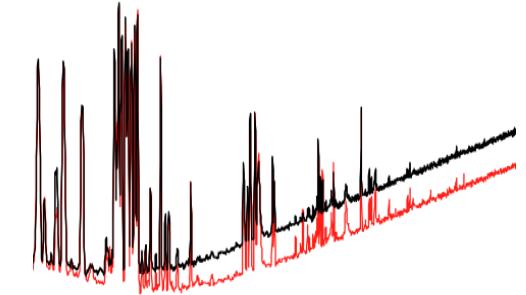
[T. Corbitt, C. Wipf, T. Bodiya, D. Ottaway, D. Sigg, N. Smith, S. E. Whitcomb, N. Mavalvala, Phys. Rev. Lett. 99, 160801 (2007)]

Feedback required to control instability



# Summary

- The combination of intense coherent light and squeezed vacuum is and will remain the optimum quantum approach for GW detectors
- Quantum radiation pressure effects have recently been observed in micro-mechanical setups
- “It's time to experimentally explore back-action evading techniques and also the potential of dynamical back-action”



# Light Sources and Interferometer Topologies

- 15:50 R. Schnabel    **Introduction to the Session**
- 16:30 S. Hild            **Sagnac Interferometer for GW Detection**
- 16:55 S. Danilishin    **Broadband Sagnac Interferometer with short Filter Cavities**
- 17:20 M. Wang          **A polarizing Sagnac topology with DC readout for future GW detectors**
- 17:45 Break**
- 18:15 S. Tarabrin      **Anomalous Dynamical Back-Action in Michelson Interferometer**
- 18:40 N. Gordon        **Multiple optical springs in coupled resonator system**

