
Amorphous Dielectric Coatings

M.M. Fejer

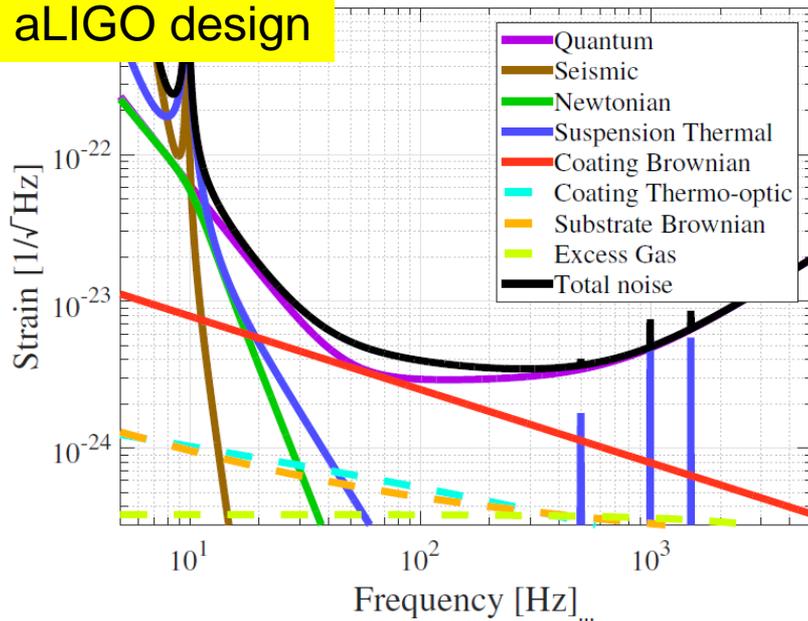
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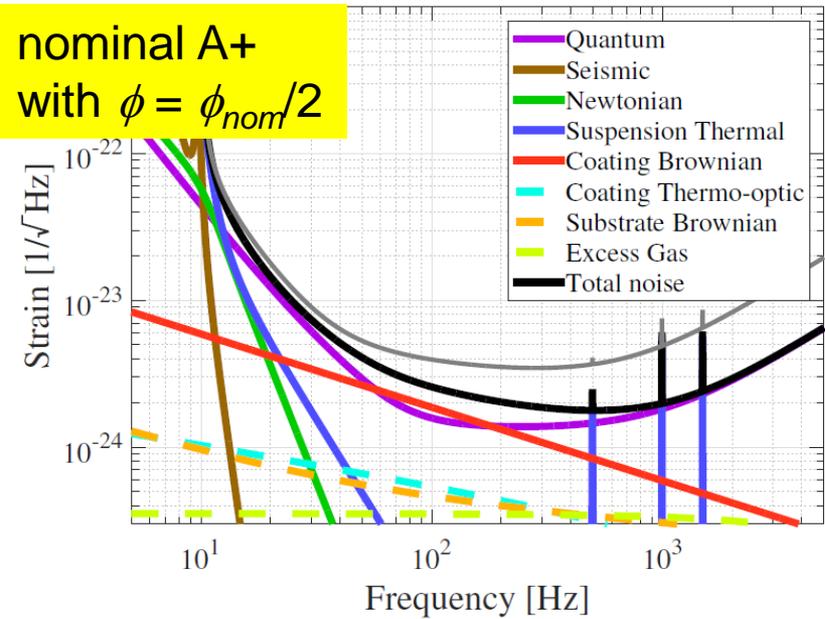
GWADW 2016

Reduced Elastic Loss in LIGO Mid-Band

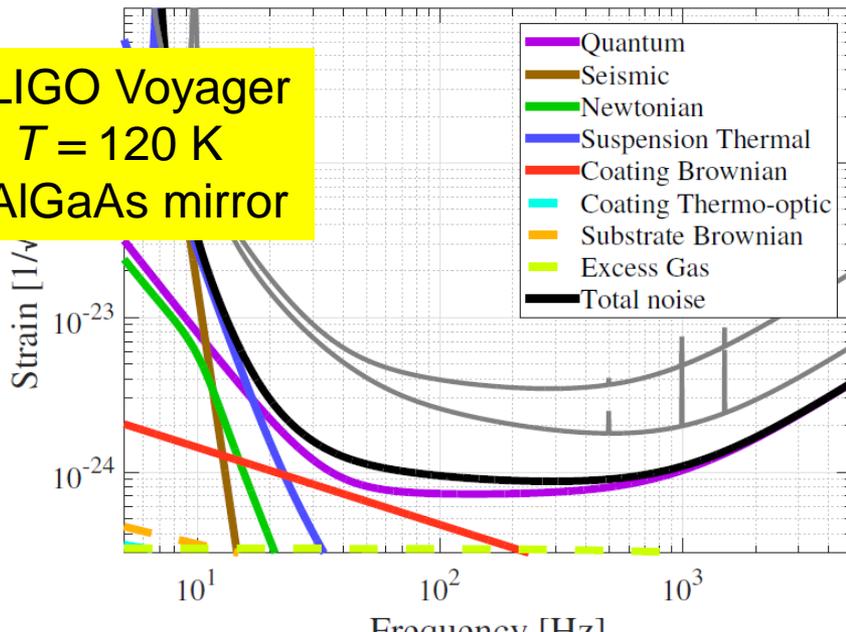
aLIGO design



nominal A+
with $\phi = \phi_{nom}/2$



LIGO Voyager
 $T = 120$ K
AlGaAs mirror



coating elastic loss
coating thickness

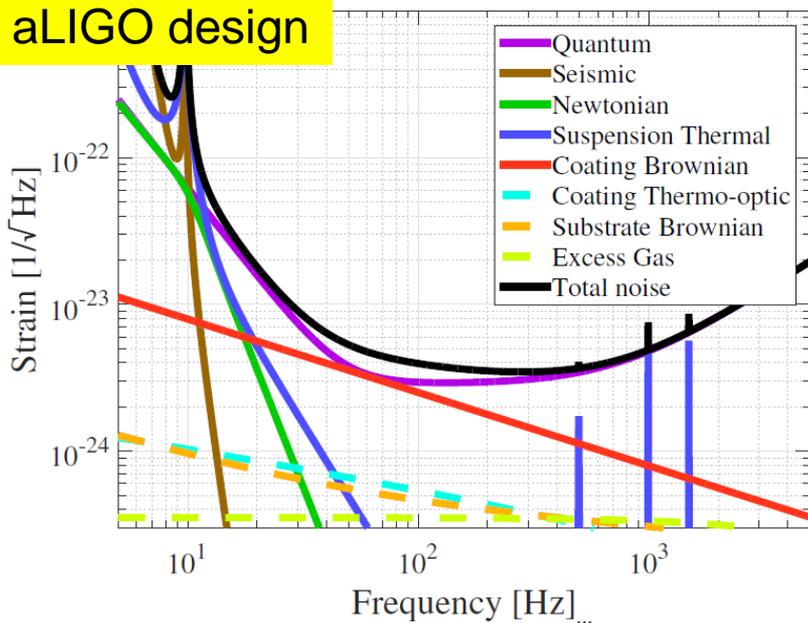
$$S_x(f, T) \approx \frac{2k_B T}{\pi^2 f} \frac{d}{w^2 Y} \phi \left(\frac{Y'}{Y} + \frac{Y}{Y'} \right)$$

beam radius

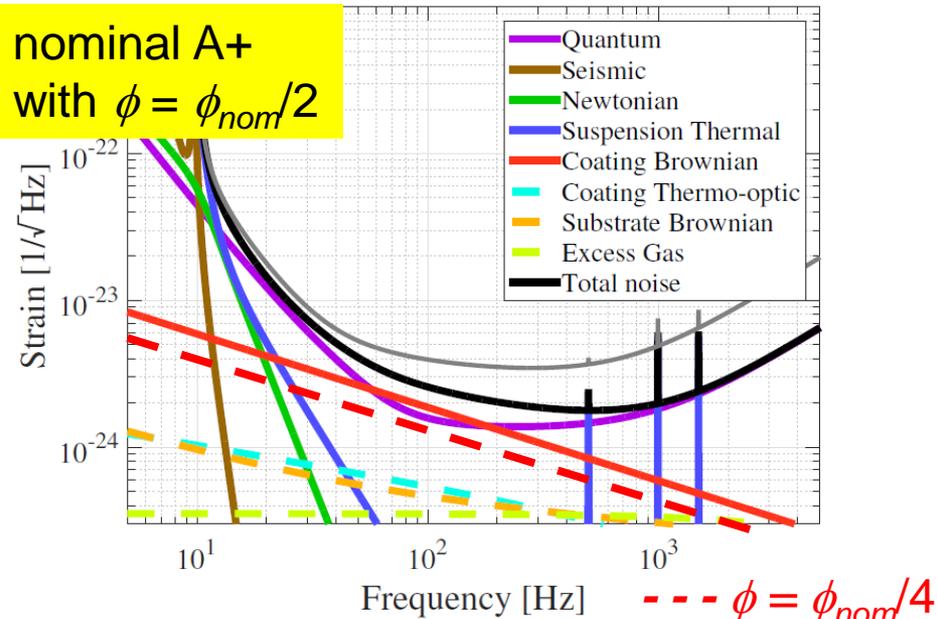
$$\begin{aligned} \phi_{\text{TiO}_2:\text{Ta}_2\text{O}_5} &= 2 \times 10^{-4} \\ \phi_{\text{SiO}_2} &= 4 \times 10^{-5} \\ \phi_{\text{AlGaAs}} &= 2.4 \times 10^{-5} \end{aligned}$$

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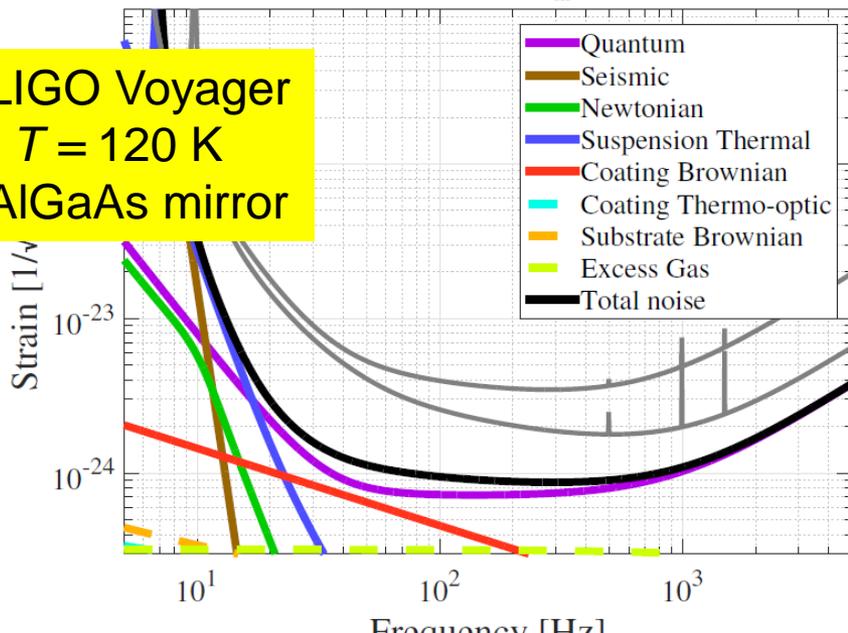
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Plausible Goals

- A+ LIGO
 - room temperature $\phi < 1 \times 10^{-4}$
- LIGO Voyager (cryogenic)
 - 120 K $\phi < 2 \times 10^{-5}$
- While maintaining optical properties over 34 cm diameter
 - at 1.06 μm for A+-LIGO
 - at $\sim 1.5 - 2 \mu\text{m}$ for cryo LIGO Voyager
 - optical absorption ~ 0.5 ppm
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 - micro-roughness scatter ~ 1 ppm
- Useful topic for discussion:
 - tighten up these numbers and required timeline

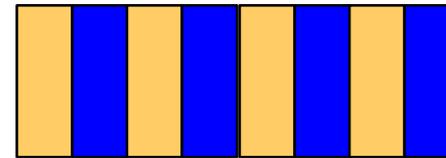
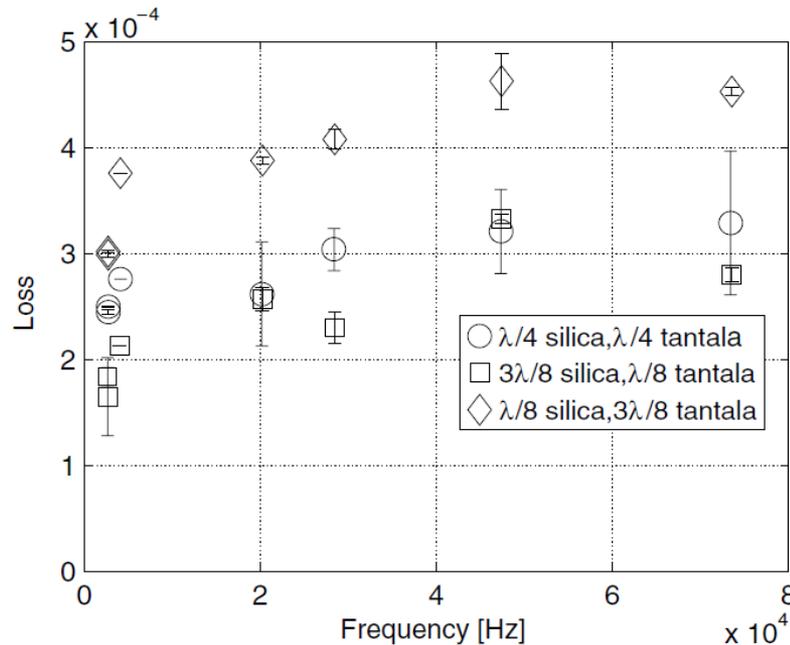
Outline

- Quick sketch of what we (think we) know
- Two-level system (TLS) model for internal friction
- Theoretical guidance
 - molecular dynamics
- Amorphous silicon
 - potential material for A+ⁿ and LIGO Voyager
 - model system for ultra-stable glass
- More theory
 - “Ultra-stable glasses” from high-temperature deposition
- Structural characterization
- Some thoughts on strategy going forward

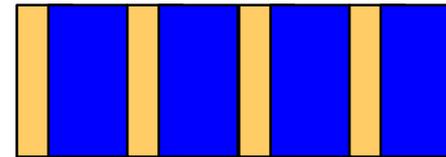
General Observations About Coating Elastic Loss

Volume and Interface Effects

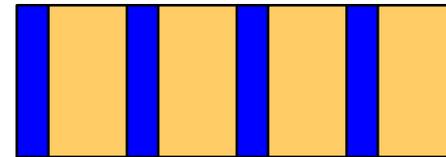
- Volume rather than interface losses dominate in tantala/silica mirror



$\lambda/4 - \lambda/4$



$3\lambda/8 - \lambda/8$



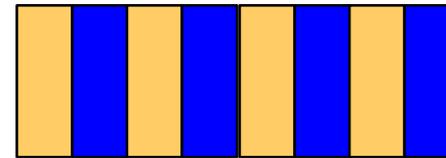
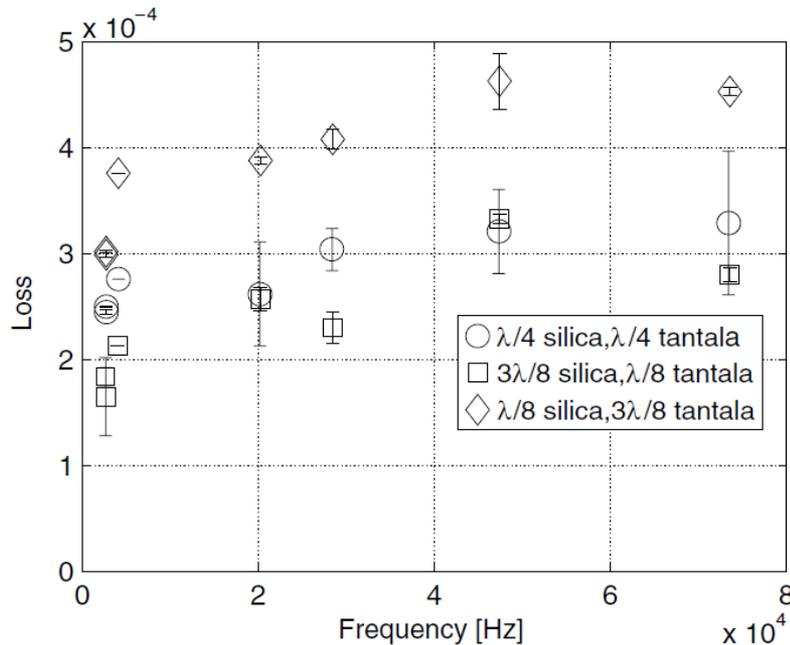
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D. Crooks, *Class. Quantum Grav.* 23 (2006) 4953–4965

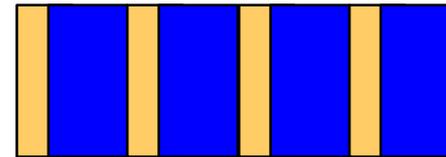
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- thickness independent
 - some suggestion of thickness dependence in a-Si

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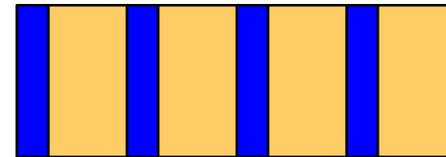
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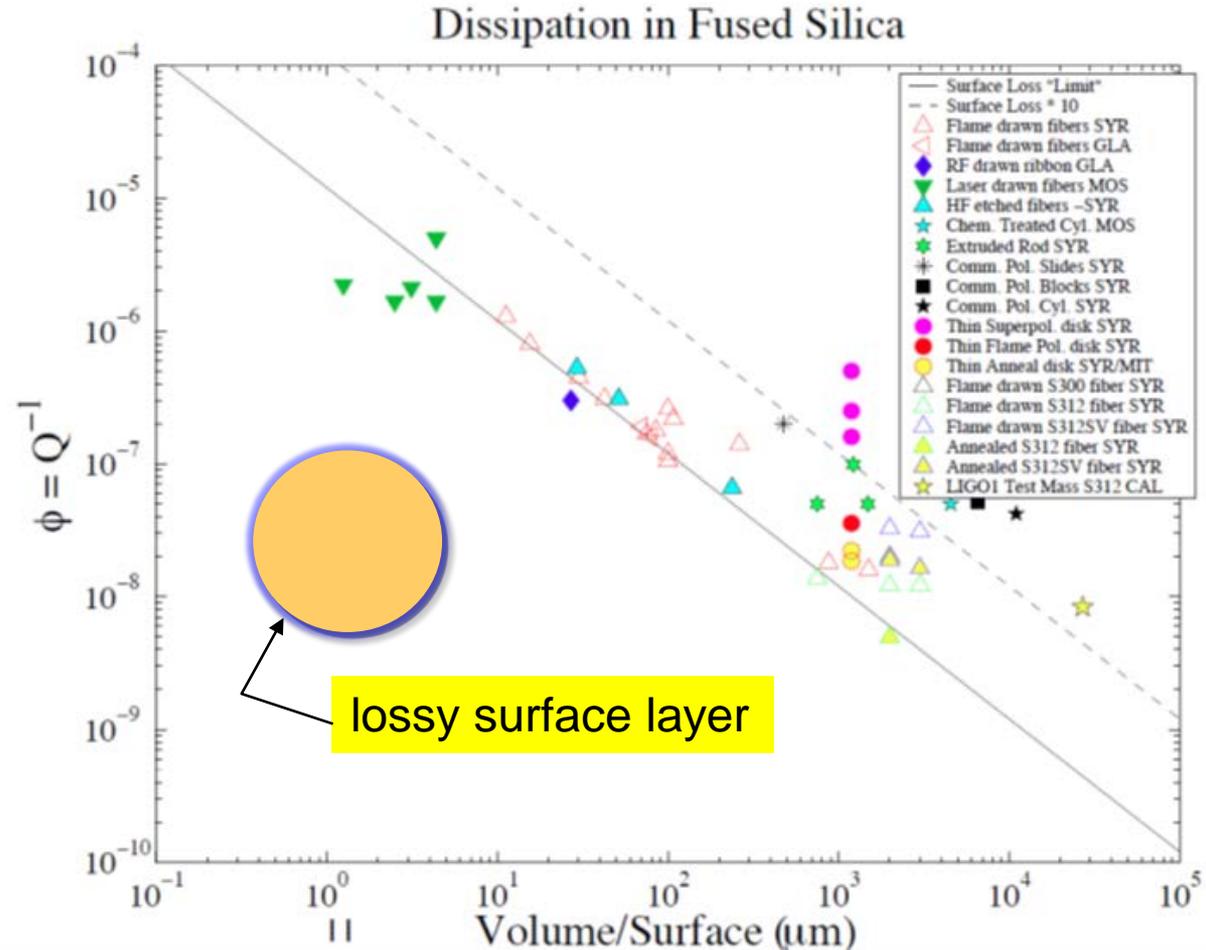
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health warning:
new thoughts from Geppo
talk Wednesday

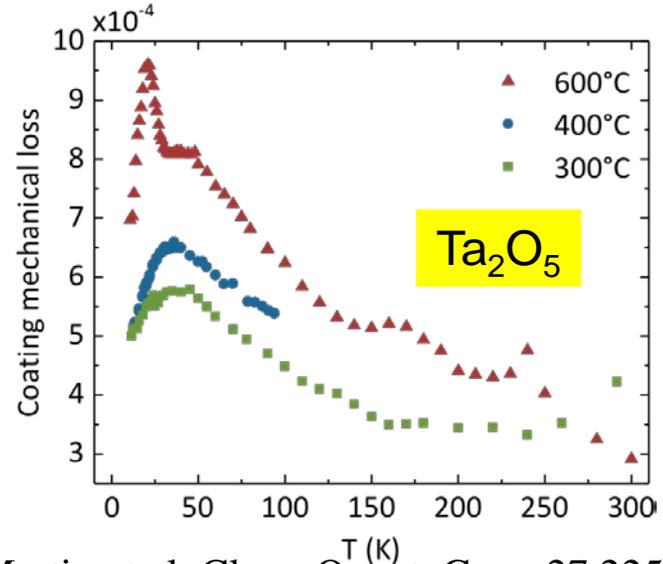
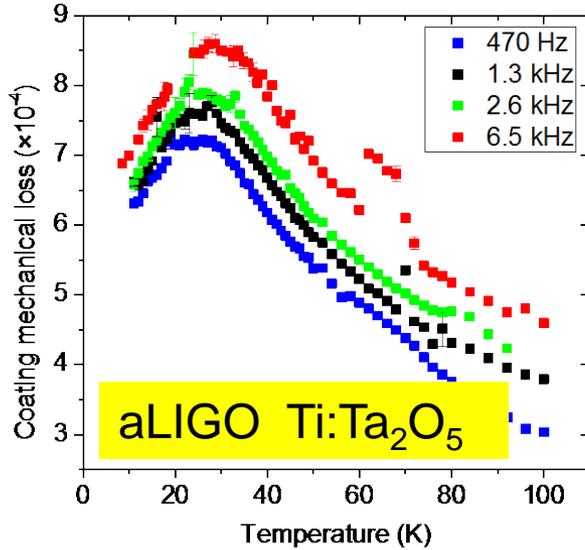
Surface and Volume Loss in Bulk Silica

- Bulk and surface loss
- Decrease with:
 - annealing temp. up to $\sim 900^\circ\text{C}$
 - annealing time
- Rayleigh scattering also decreases with annealing
 - \Rightarrow density fluctuations reduced



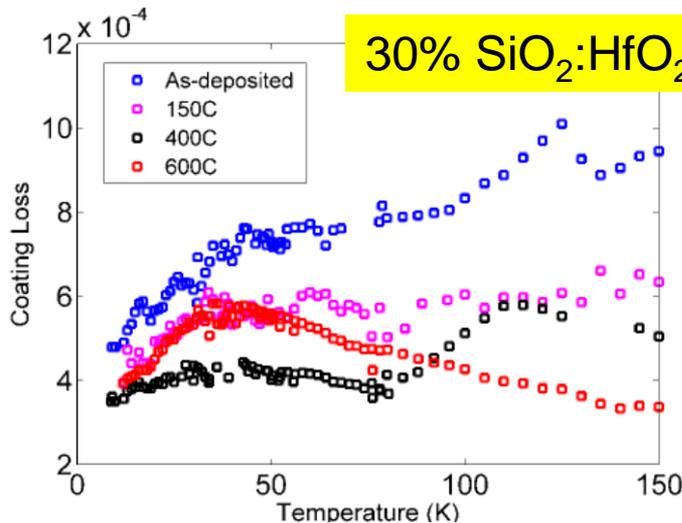
Temperature and Frequency Dependence

- Typical behavior vs T and f

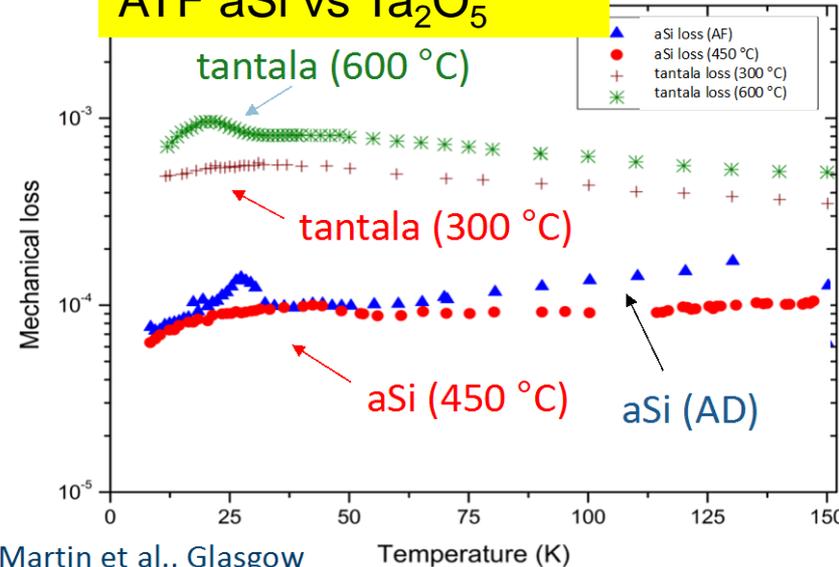


[I W Martin et al, Class. Quant. Grav. 27 225020, 2010]

- Other materials behave differently



ATF aSi vs Ta₂O₅

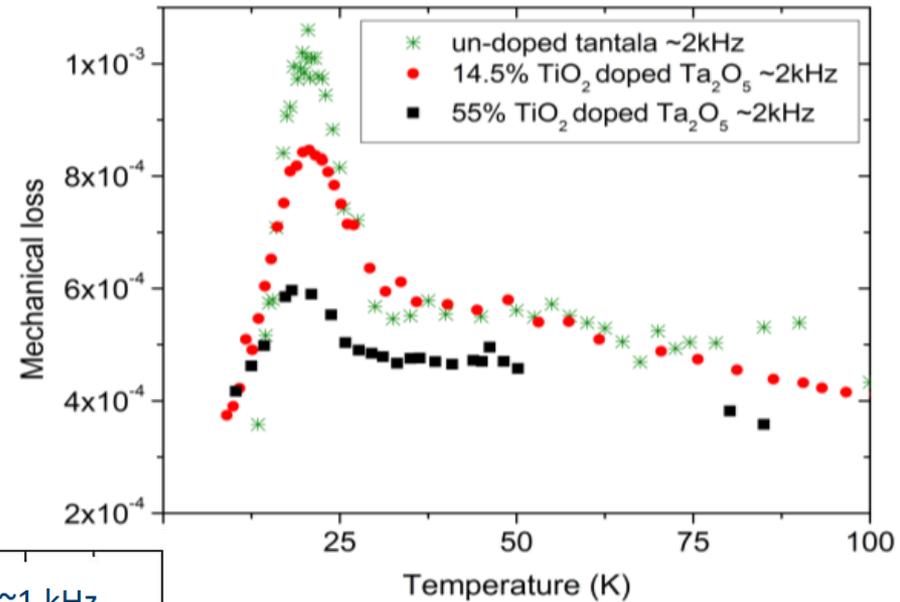


[I. Martin et al., Glasgow

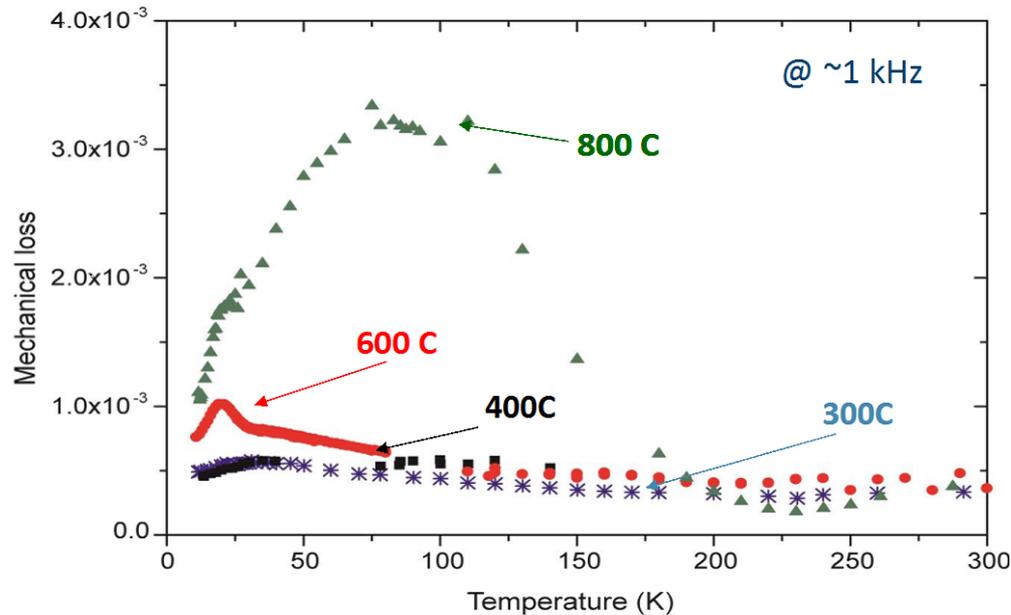
Temperature (K)

Doping and Annealing Alter Dissipation

- Loss modified by dopants
 - TiO_2 doping reduces losses in Ta_2O_5



- Annealing modifies loss spectra



P. Murray et al, U. Glasgow
- (Unpublished)

- can improve at some temperatures while worsened at others

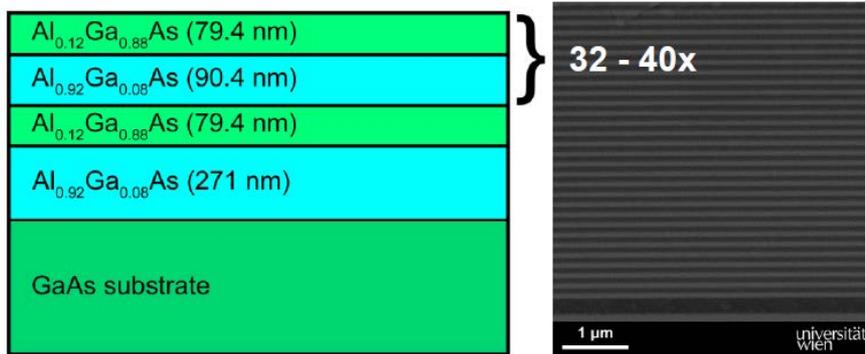
How to Find Better Amorphous Oxides?

- Don't bother: use crystalline coatings
- Random search through ternary oxides?
 - thousands of host/dopant combinations
 - thermal processing another degree of freedom
- *Ars longa, vita brevis* (Art is long, life is short)
 - Edisonian methods used to date may not scale gracefully
limited time and \$\$ available
- Understanding underlying mechanisms useful to guide experiment
 - two-level systems (TLS)
 - molecular dynamics modelling
 - atomic structure characterization

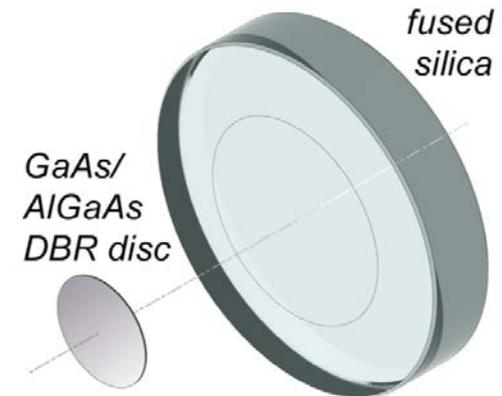
How to Eliminate TLS?: Crystalline Coatings

- GaAs/AlGaAs transferred to mirror substrate

$$\phi \sim 2 \times 10^{-5}, \alpha < 1 \text{ ppm}$$



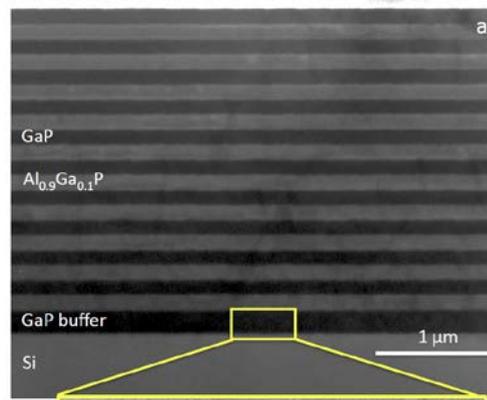
Garrett Cole talk, Friday 2:00



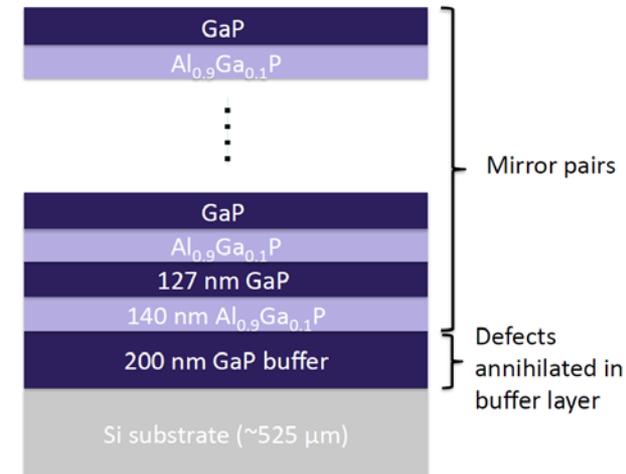
G. Cole, LIGO-G1401152

- GaP/AlGaP epitaxy on Si mirror substrate

$$\phi < 1 \times 10^{-4}, \alpha = ??$$



A. Lin, LIGO-G1200135

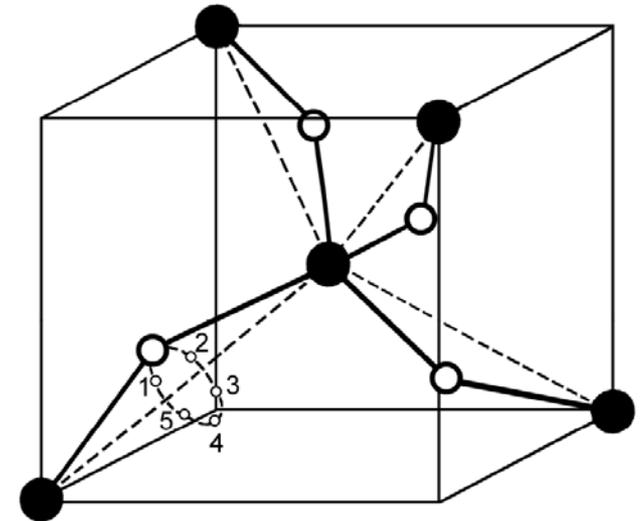
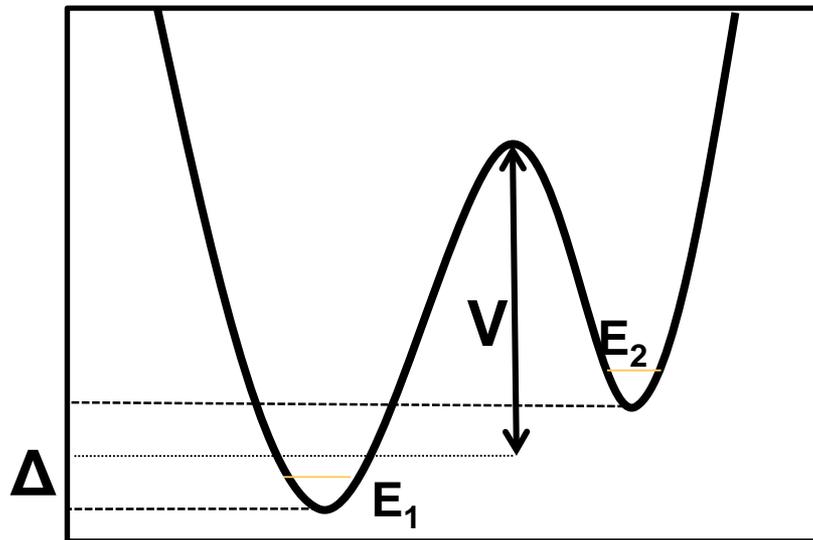


How to Reduce TLS: Find Better Amorphous Oxides?

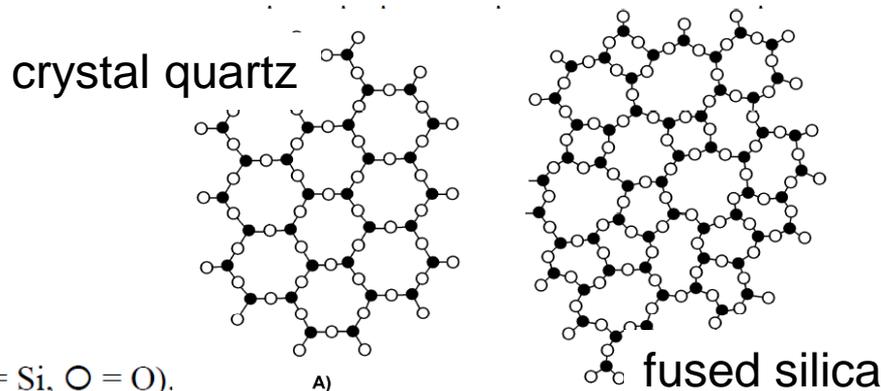
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 - molecular dynamics modelling
 - “ultra-stable” glasses
 - atomic structure characterization

Low-frequency losses in amorphous dielectrics

- Conventionally associated with low energy excitations (LEEs)
 - conceptualized as two-level systems (TLS)



Oversimple picture: bond flopping



Distribution of TLS in silica
due to disordered structure

figures from B.S. Lunin monograph

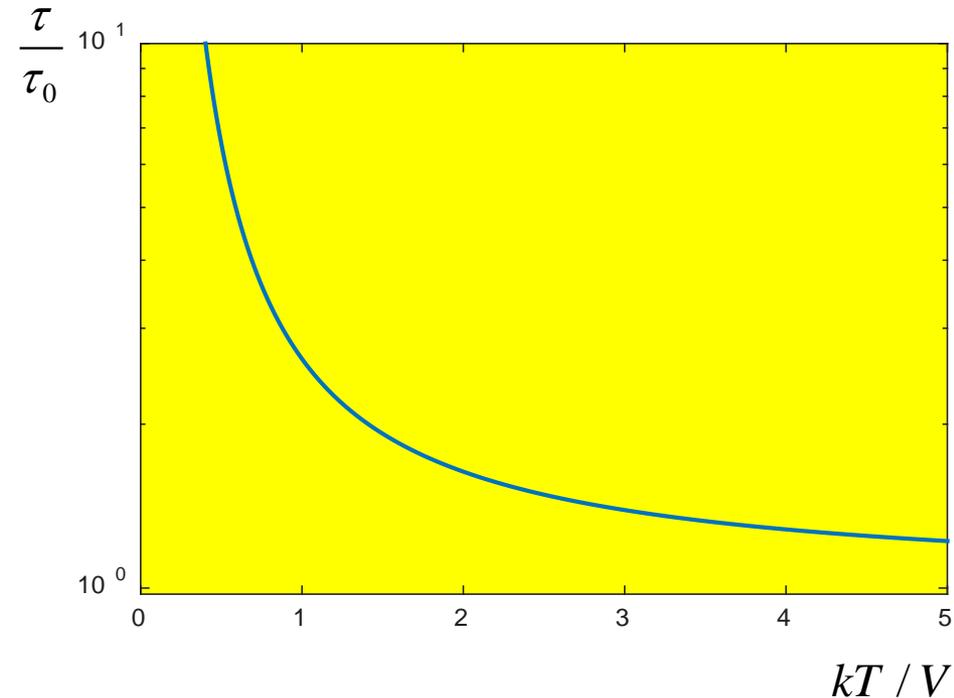
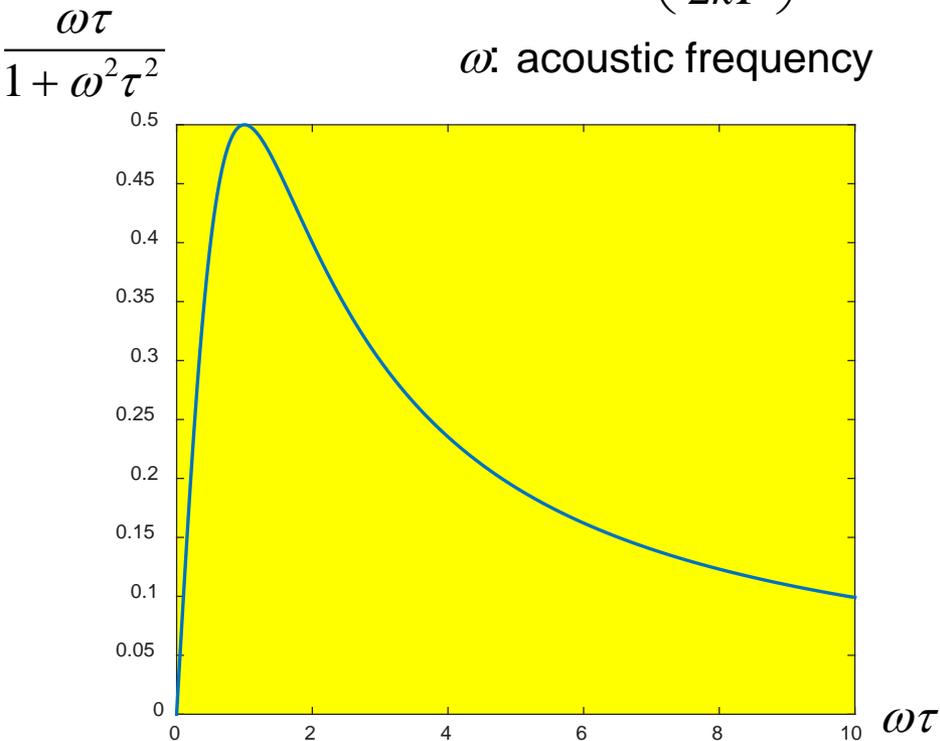
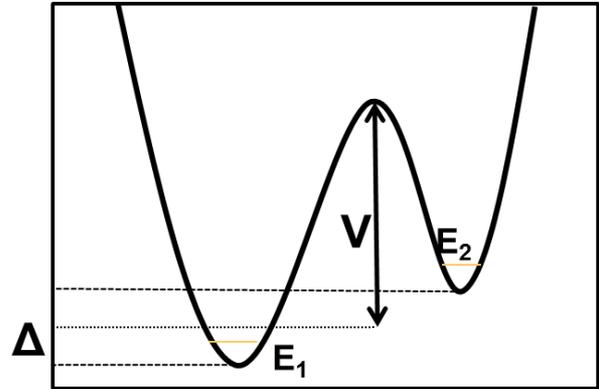
Elastic Dissipation by TLS

- Above ~5 K, thermally activated rather than quantum tunneling
 - for a single type of TLS:

$$Q^{-1} = N \frac{\gamma^2}{Y kT} \frac{\omega \tau}{1 + \omega^2 \tau^2} \operatorname{sech}^2 \left(\frac{\Delta}{kT} \right)$$

$$\tau = \tau_0 \operatorname{sech} \left(\frac{\Delta}{2kT} \right) e^{V/kT}$$

ω : acoustic frequency



kT/V

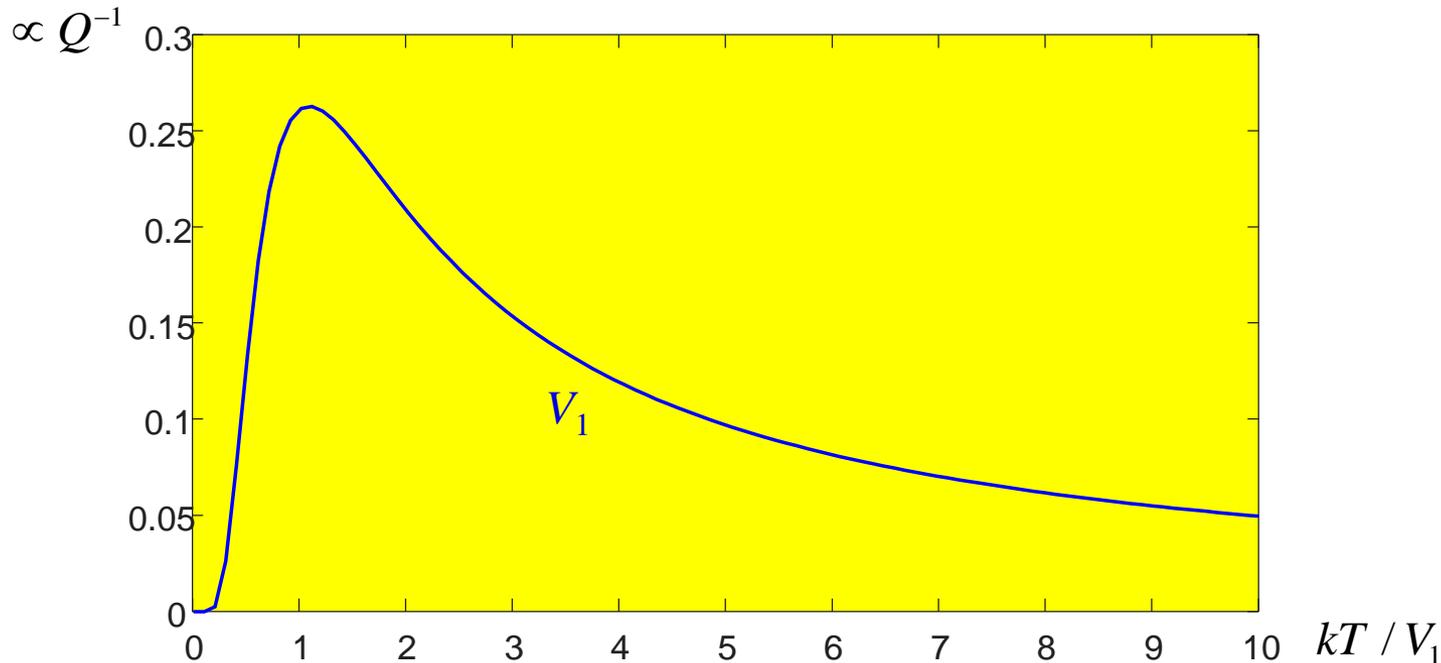
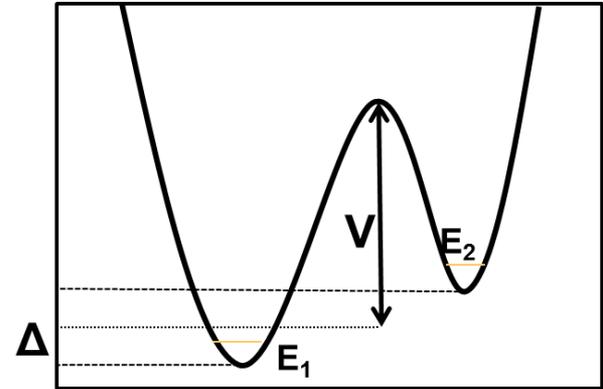
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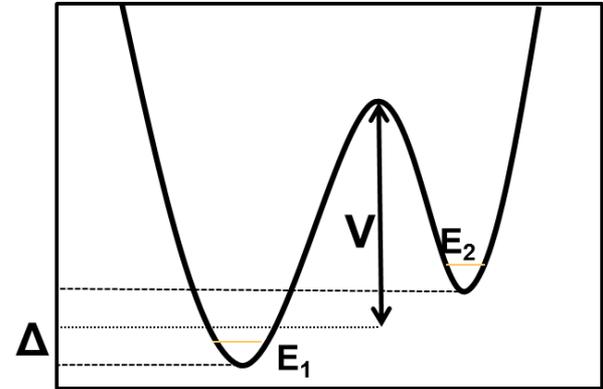
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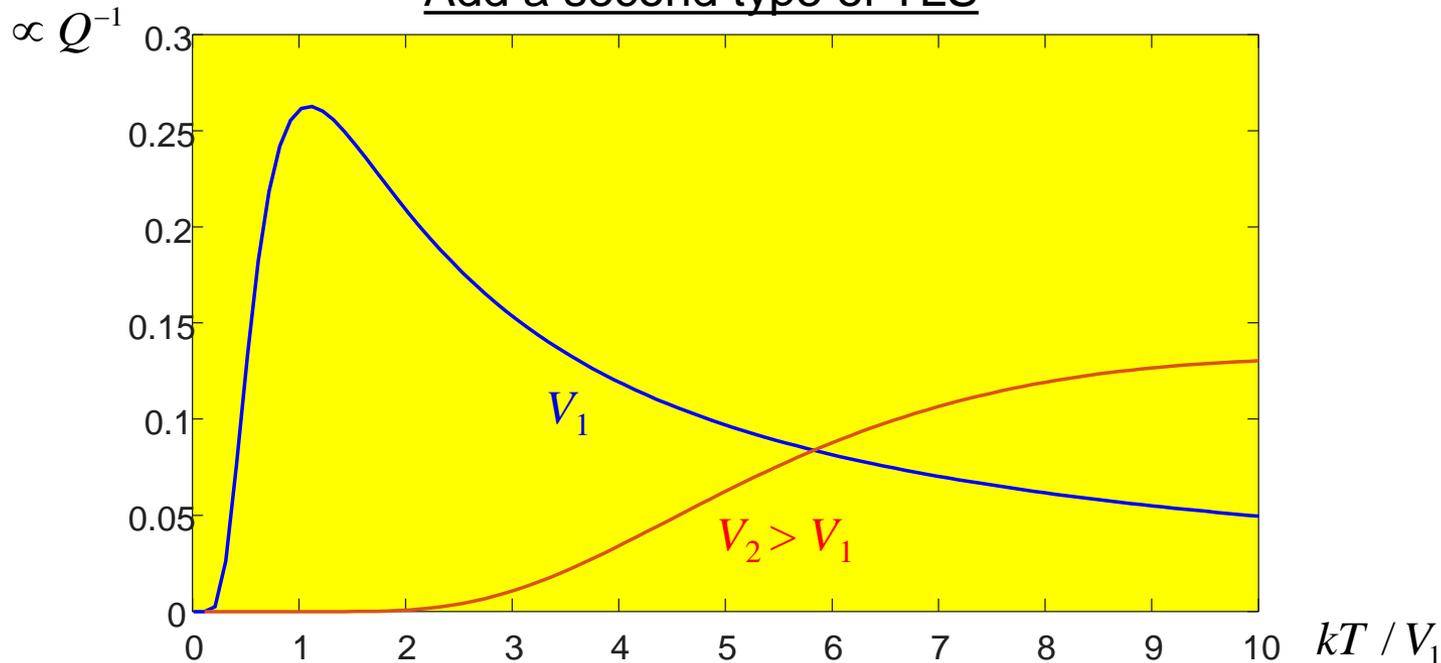
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Add a second type of TLS



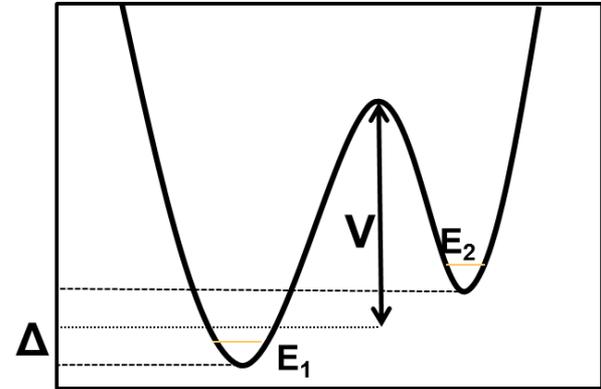
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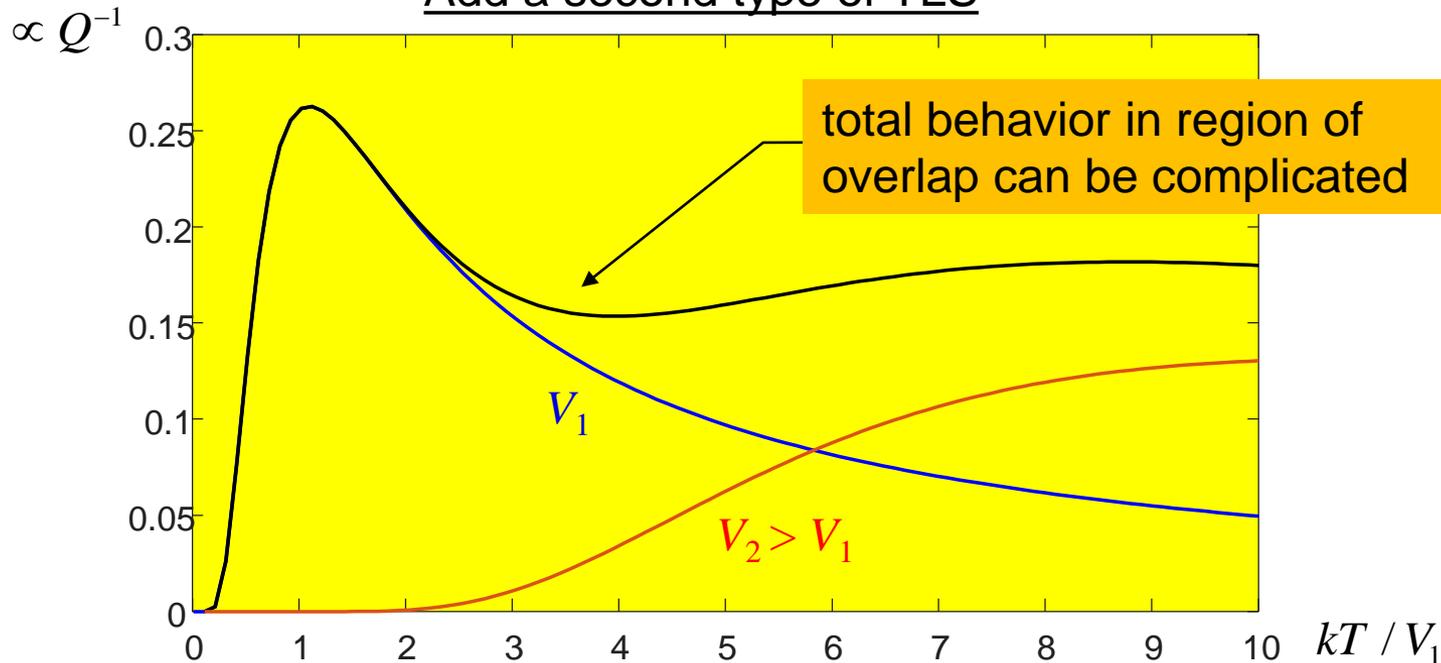
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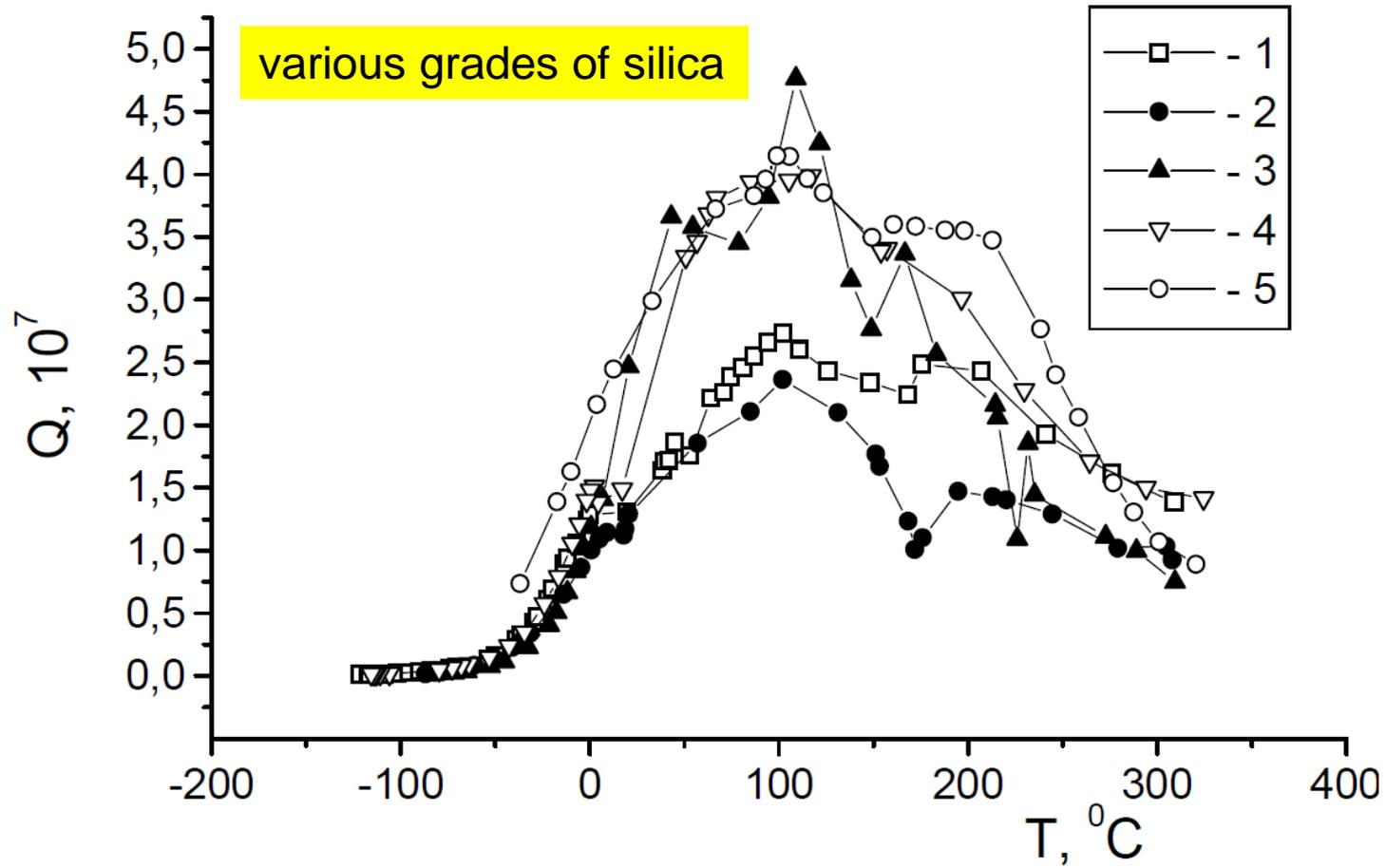
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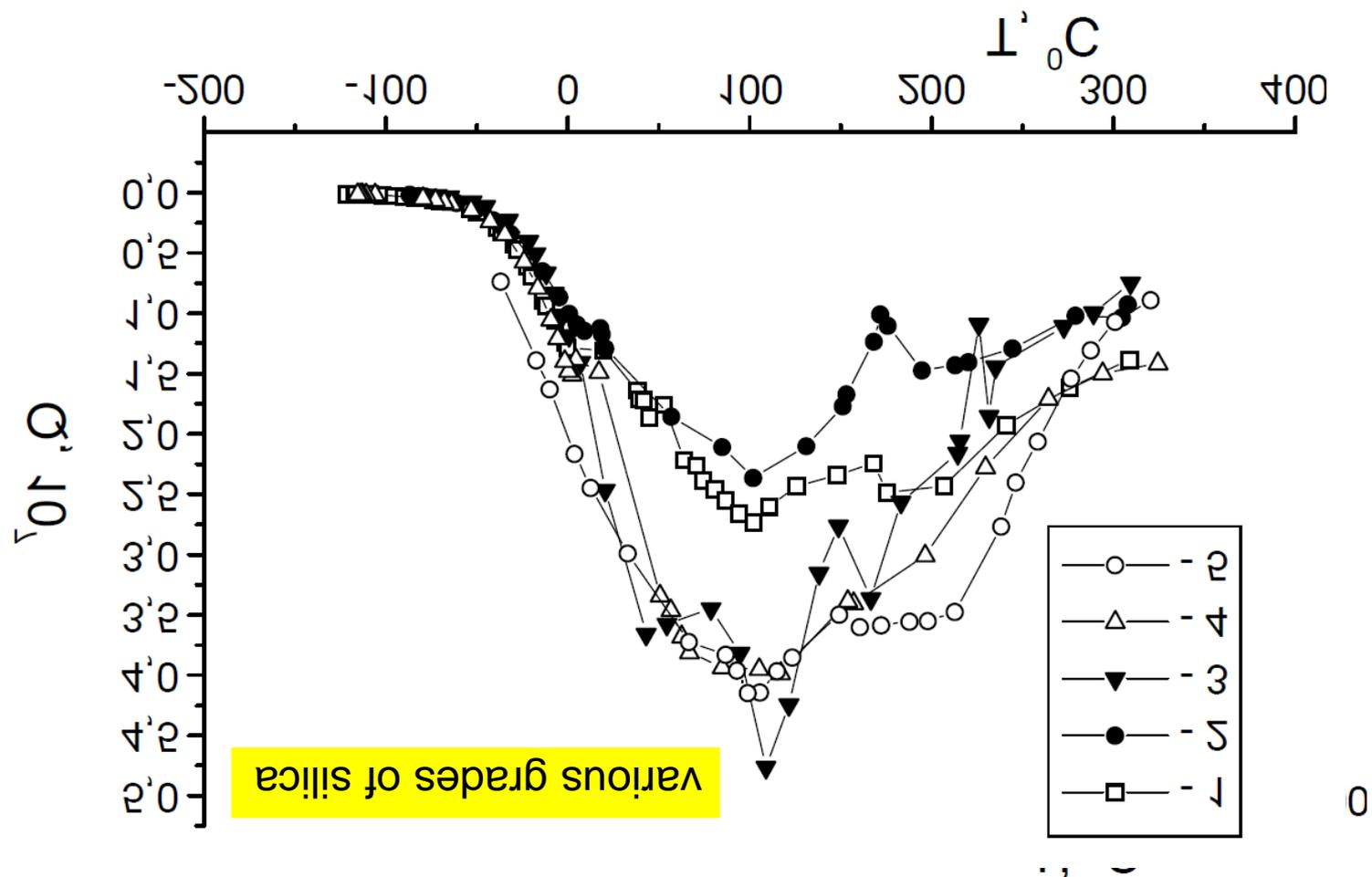
Add a second type of TLS



Evidence of Such Behavior in Silica



Evidence of Such Behavior in Silica



Elastic Dissipation by TLS

- Real materials have distribution of TLS

Gilroy, K. S. and Phillips, W. A., Philos Mag. B, **38**, 735 (1981)

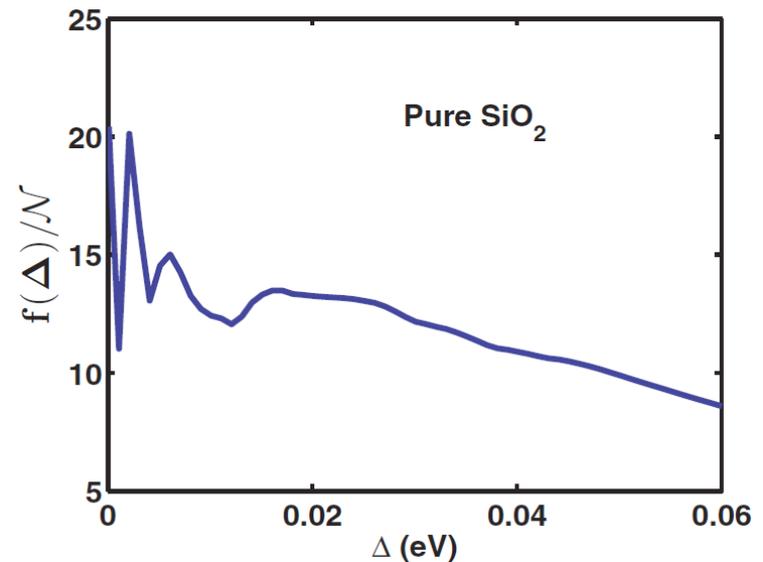
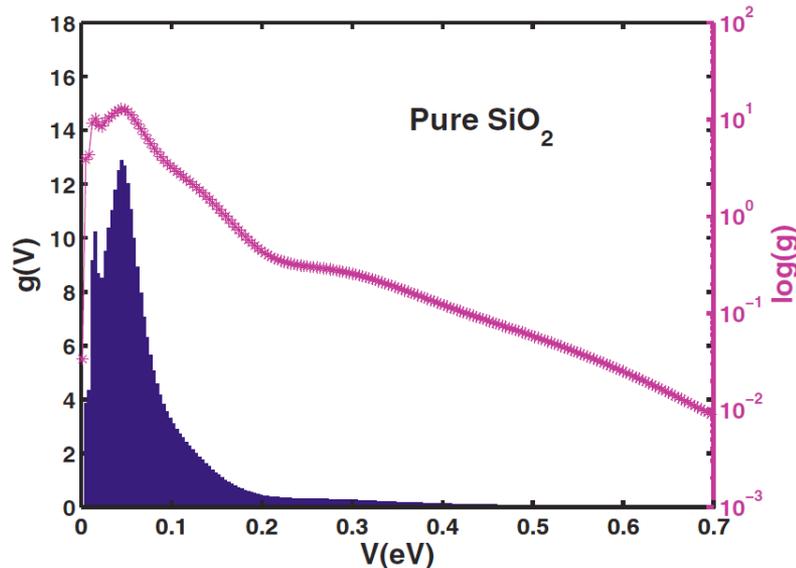
- Dissipation is weighted average of their contributions
 - smears out attenuation function

$$Q^{-1} = \frac{\gamma^2}{Y kT} \iint \frac{\omega\tau}{1 + \omega^2\tau^2} \operatorname{sech}^2\left(\frac{\Delta}{kT}\right) g(V) f(\Delta) dV d\Delta$$

barrier height distribution

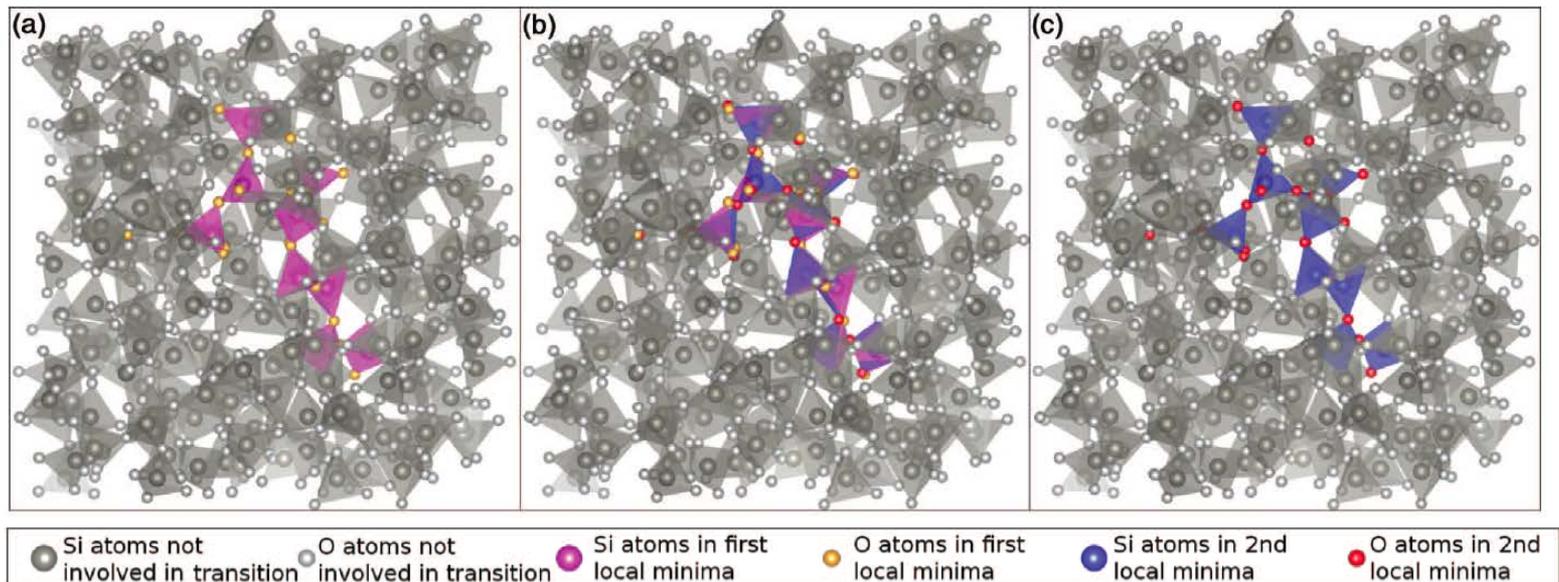
asymmetry distribution

$$\tau = \tau_0 \operatorname{sech}\left(\frac{\Delta}{2kT}\right) e^{V/kT}$$



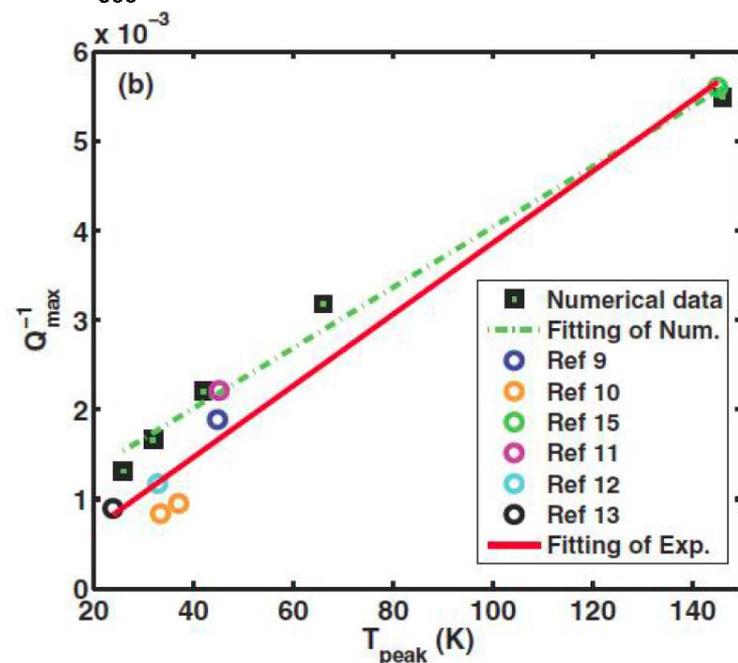
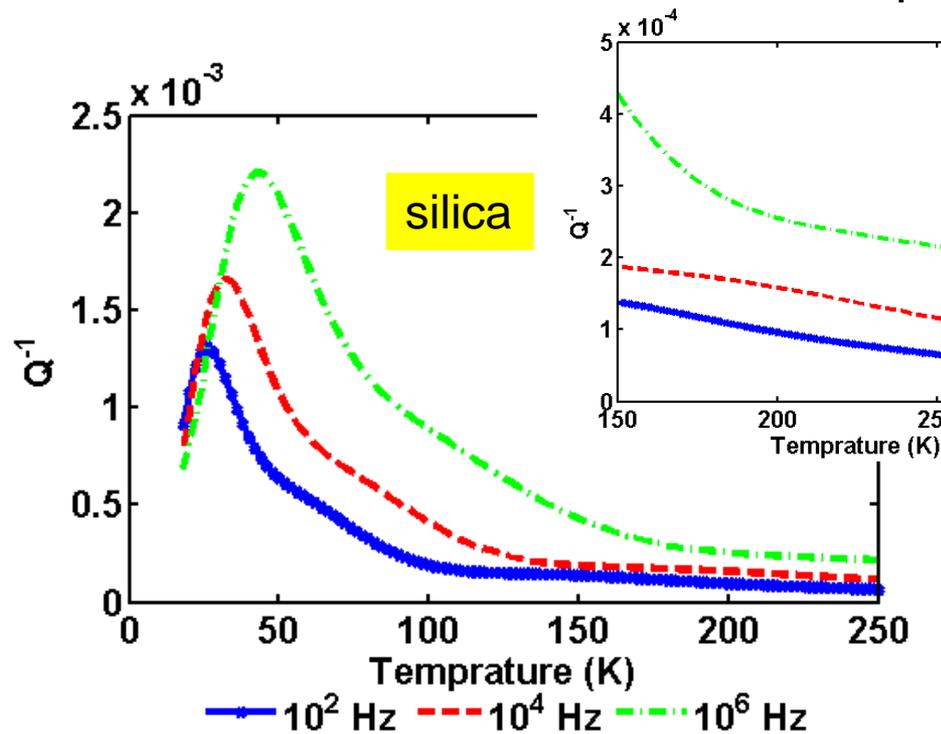
Theoretical Guidance: Molecular Dynamics

- Molecular dynamics calculations for amorphous materials
 - provide insight into dissipation mechanisms
 - can suggest promising material combinations
 - **Chris Billman** talk at 10:00 Tuesday
- Some observations:
 - TLS involves dozens of atoms in nm-scale configurations



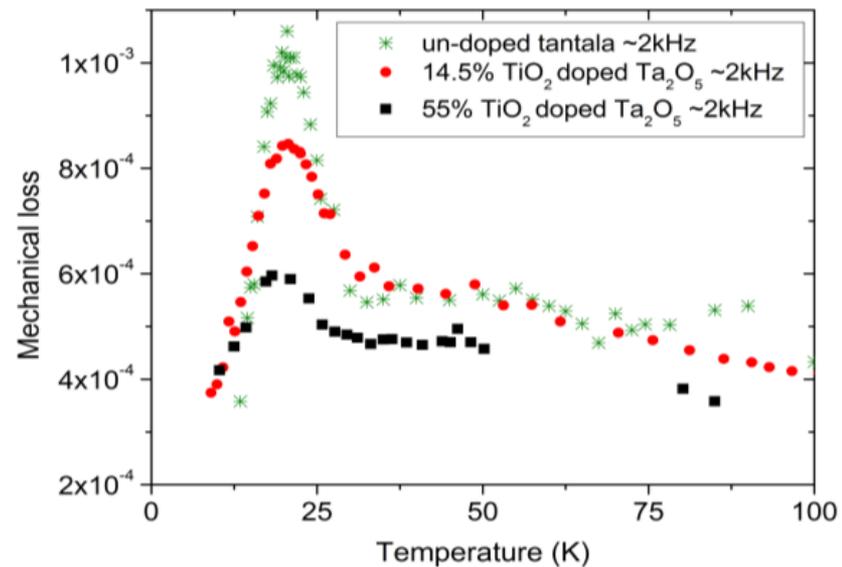
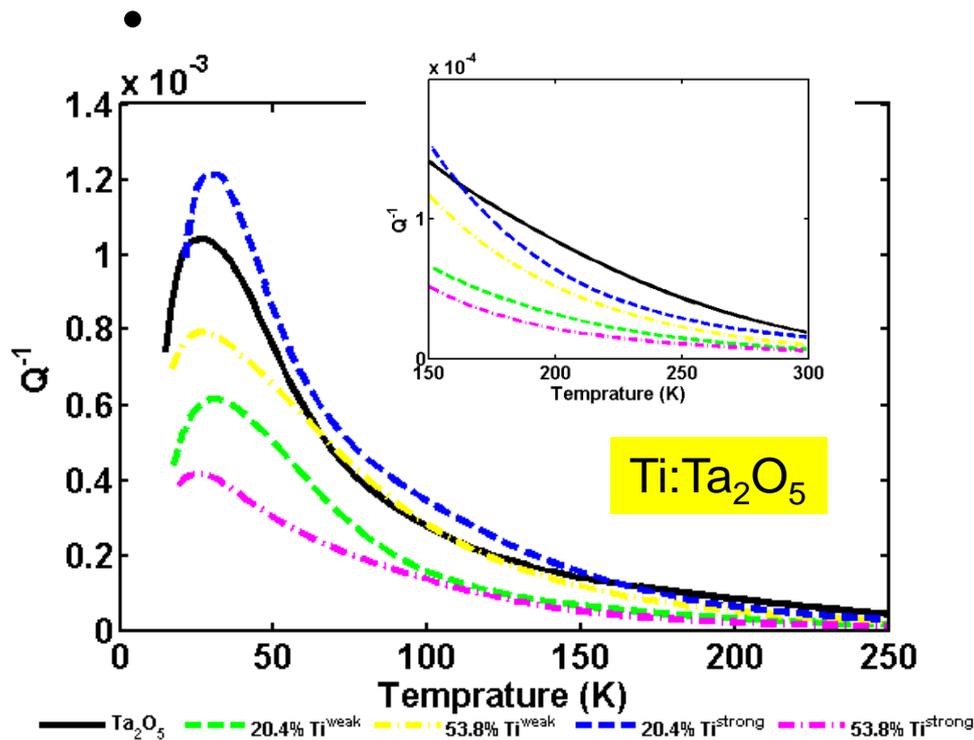
Theoretical Guidance: Molecular Dynamics

- Some observations:
 - some theoretical trends tie up with experiment



Theoretical Guidance: Molecular Dynamics

- Some observations:
 - some theoretical trends tie up with experiment
 - decrease in loss with titania doping in tantala



P. Murray et al, U. Glasgow
- (Unpublished)

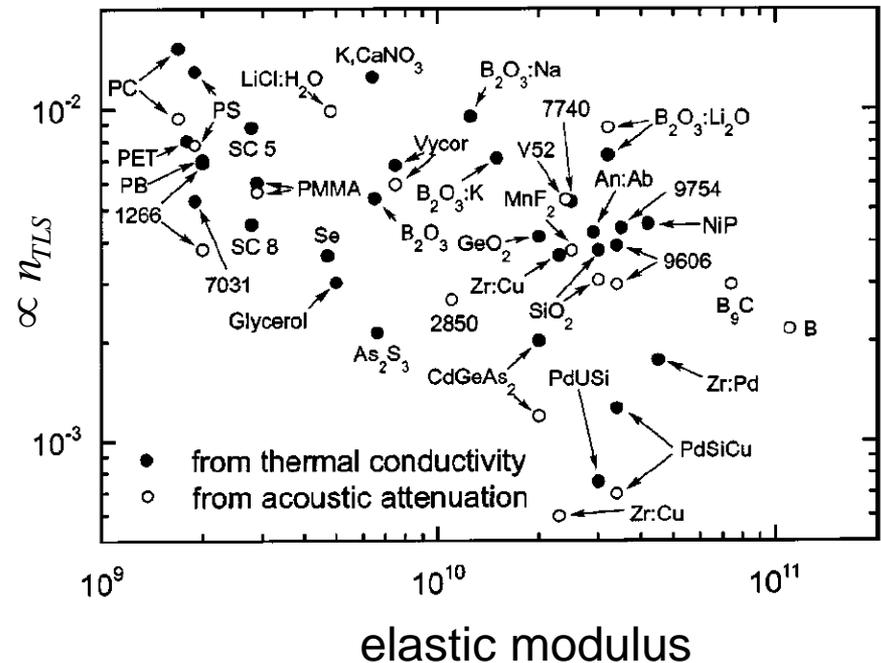
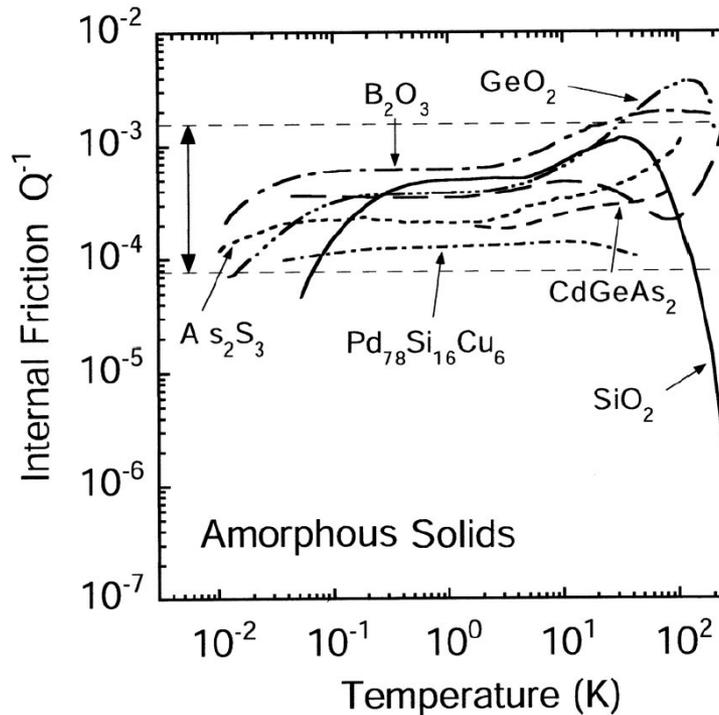
Theoretical Guidance: Molecular Dynamics

- Some issues:
 - absolute values not in close agreement with exp't
 - agreement worse at higher temperatures than cryogenic
- Possible sources:
 - surface effects
 - higher energy TLS
 - ??
- Correct trends already suggest potentially interesting materials
 - e.g. $\text{ZrO}_2:\text{Ta}_2\text{O}_5$

Chris Billman talk at 10:00 Tuesday

How to Reduce TLS? Synthesis and Annealing

- Universality of TLS in amorphous materials recently studied



- Has led to studies of elevated vapor deposition temperatures
 - very promising results

Several Properties \propto concentration of TLS

- At low temperatures several properties $\propto n_{TLS}$
- Internal friction (in tunneling regime)

$$\phi \propto \bar{P} \propto n_{TLS}$$

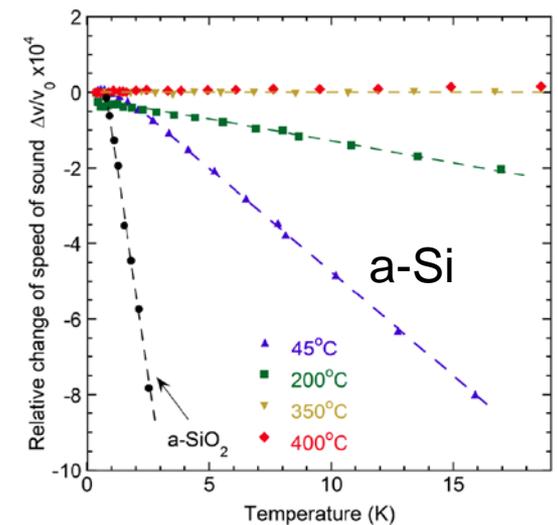
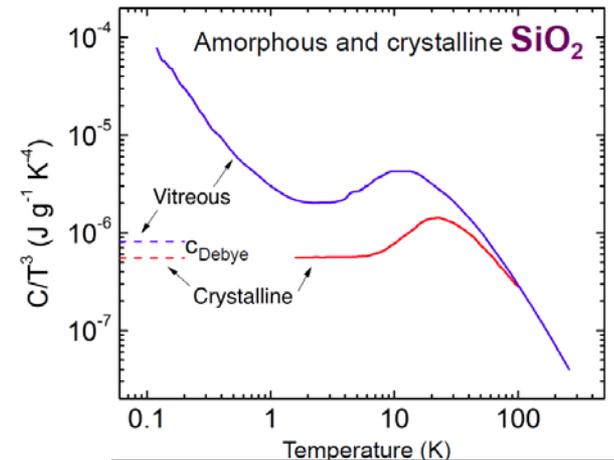
↙ spectral density of TLS

- Specific heat vs temperature T

$$C = c_1 T + c_3 T^3$$

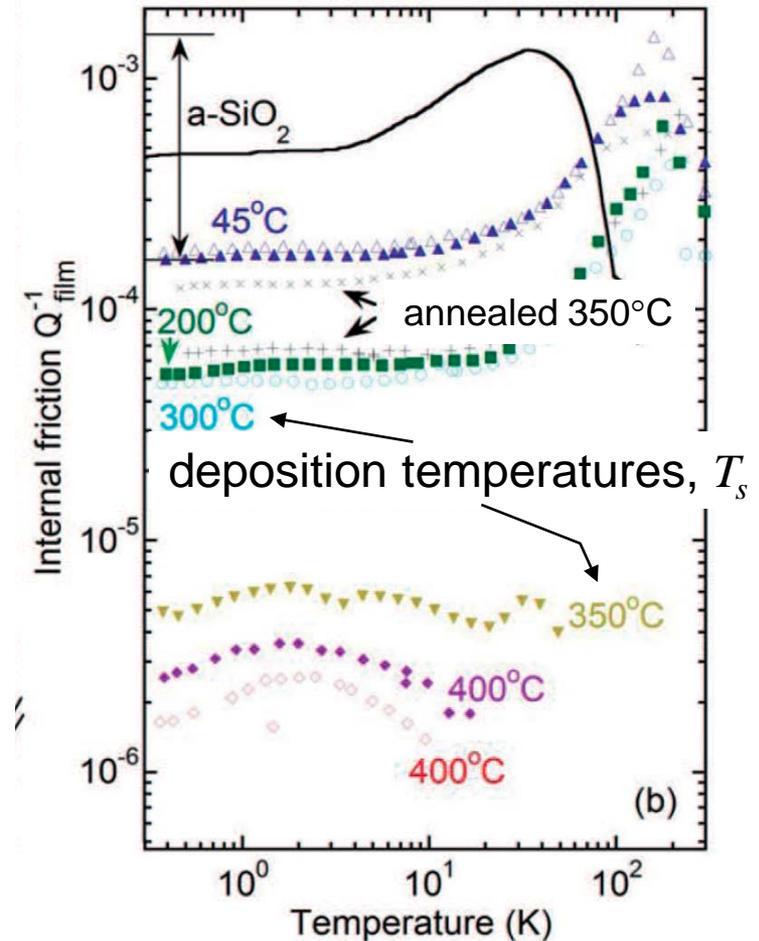
↙ $c_1 \propto n_{TLS}$ ↘ phonons

- Change in sound velocity vs T

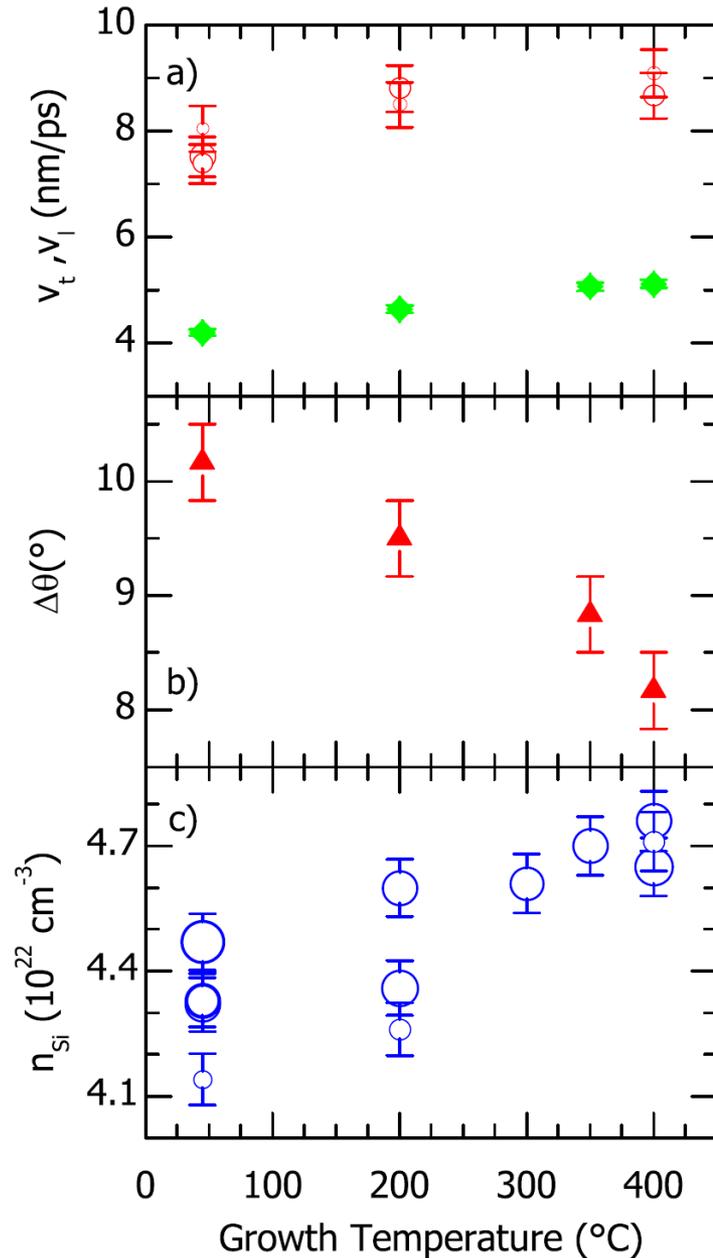


Experimental Observation for a-Si

- Internal friction of films deposited at high temperatures T_s
 - very different from film annealed at same temperature
 - $\phi \sim 2 \times 10^{-6}$ vs $\sim 10^{-4}$
- Improves steeply around $T_s \sim 400$ C



Other Properties of a-Si Modified for High T_s



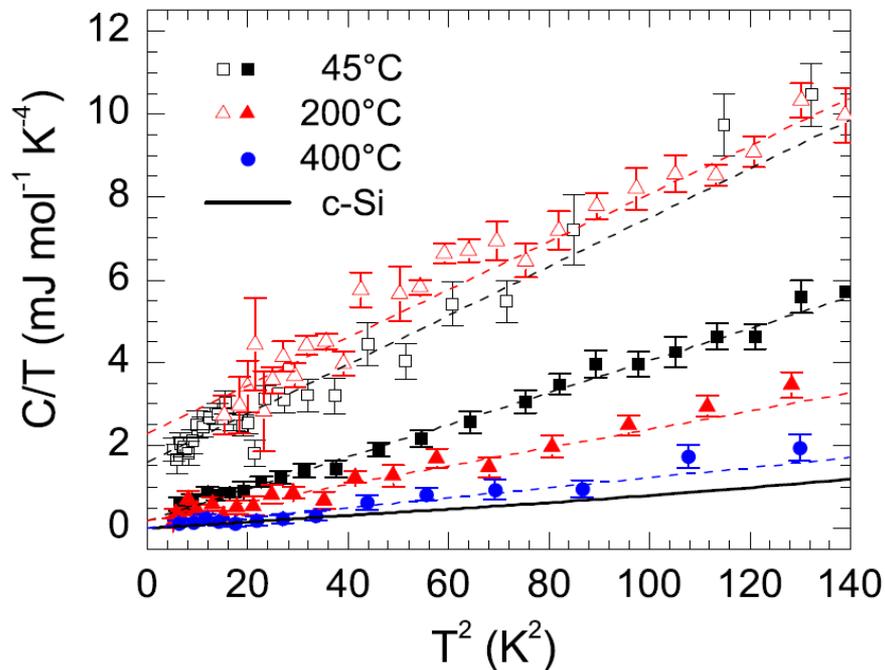
sound velocity approaches asymptote
(via paddle resonance)

distribution of bond angles narrows
(via Raman lineshape)

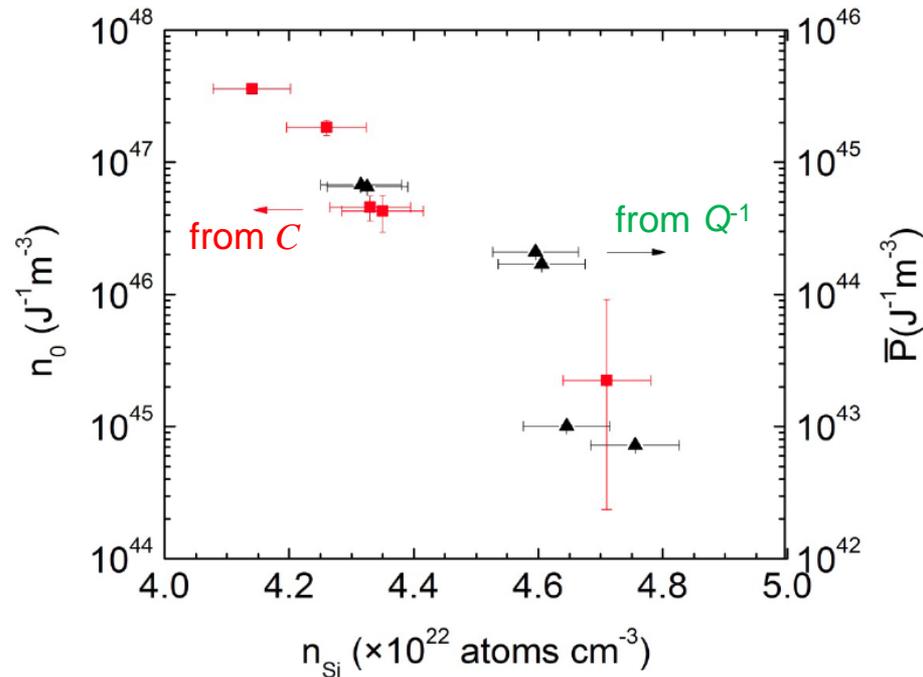
density increasing
(via RBS)

Heat Capacity Approaches Crystalline Silicon Value

Heat Capacity Approaches Crystalline Silicon



same n_{TLS} from Q^{-1} and C

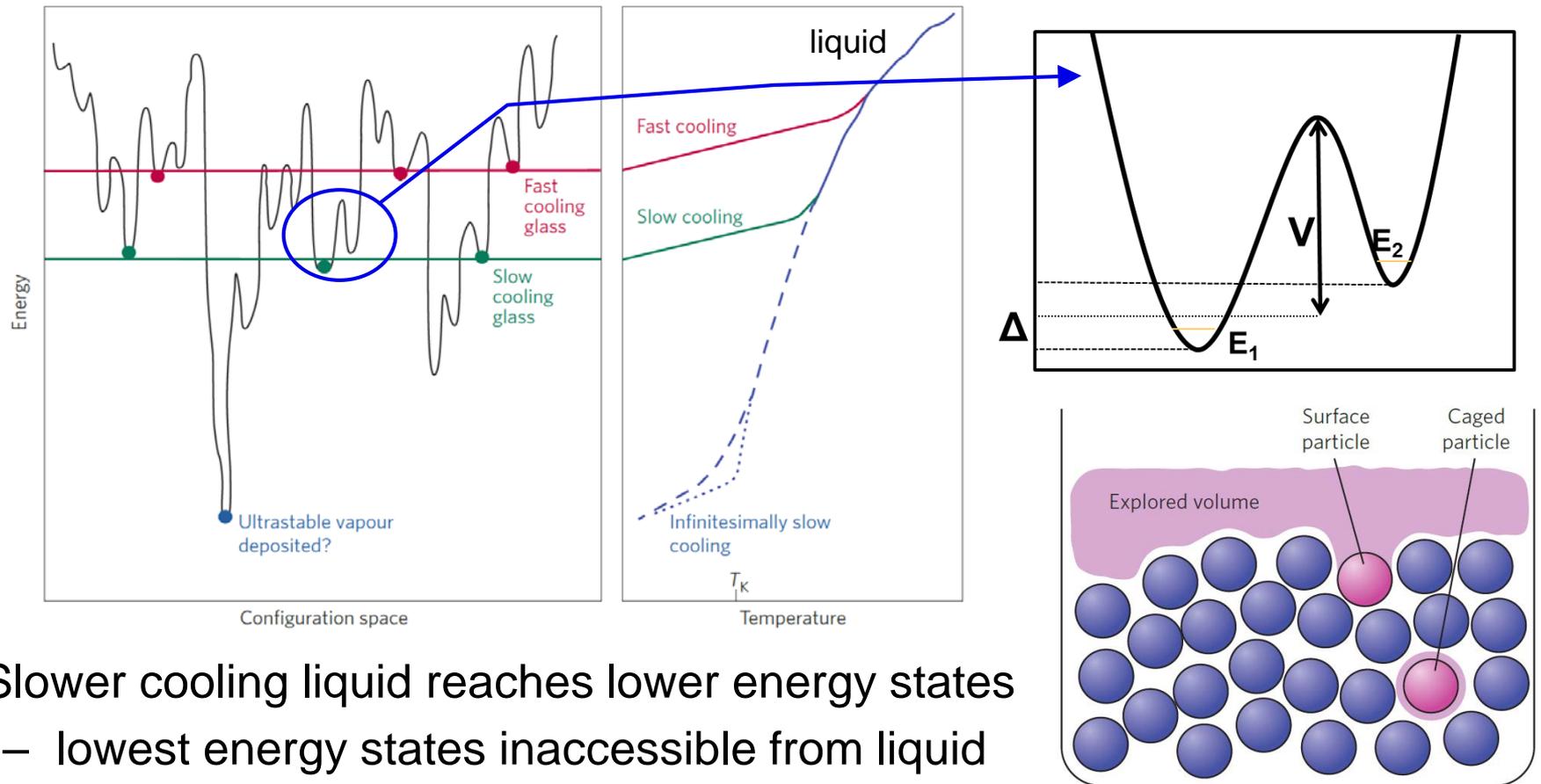


both correlate with film density

Material properties suggest greatly reduced n_{TLS} for high T_s

What is the mechanism?

Energy Landscape of Amorphous Materials

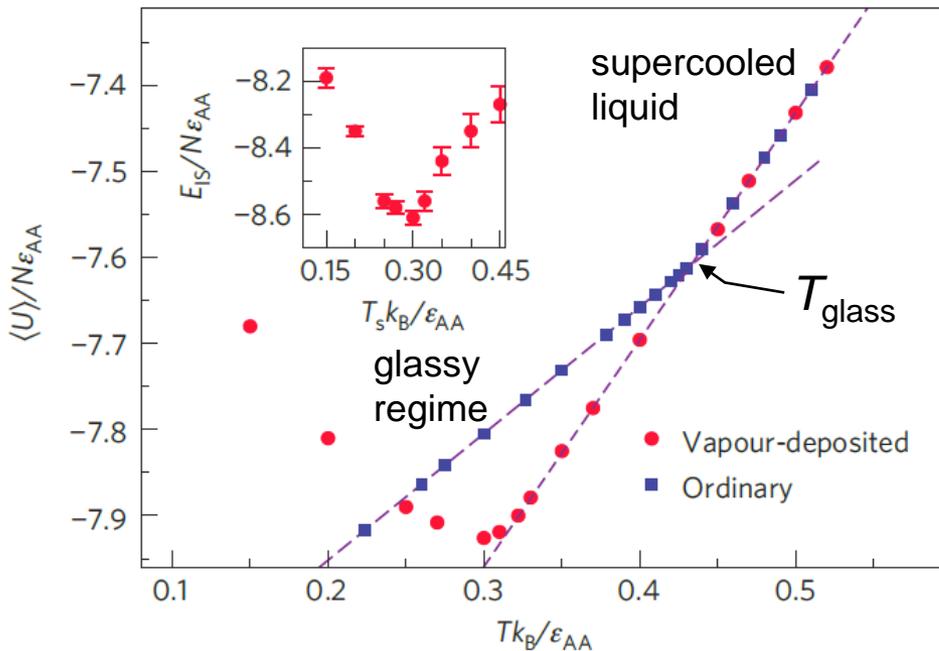
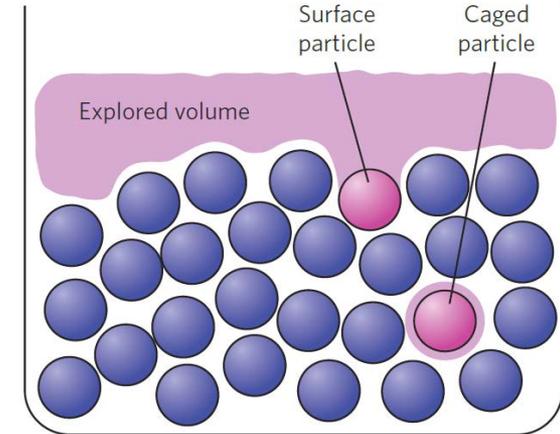


- Slower cooling liquid reaches lower energy states
 - lowest energy states inaccessible from liquid
- Vapor phase deposition accesses lower energies
 - simulations* suggest surface liquid layer has orders of magnitude higher mobility than caged particles in solid
 - deposition at high temperature more effective than post-annealing

Simulation of Model System

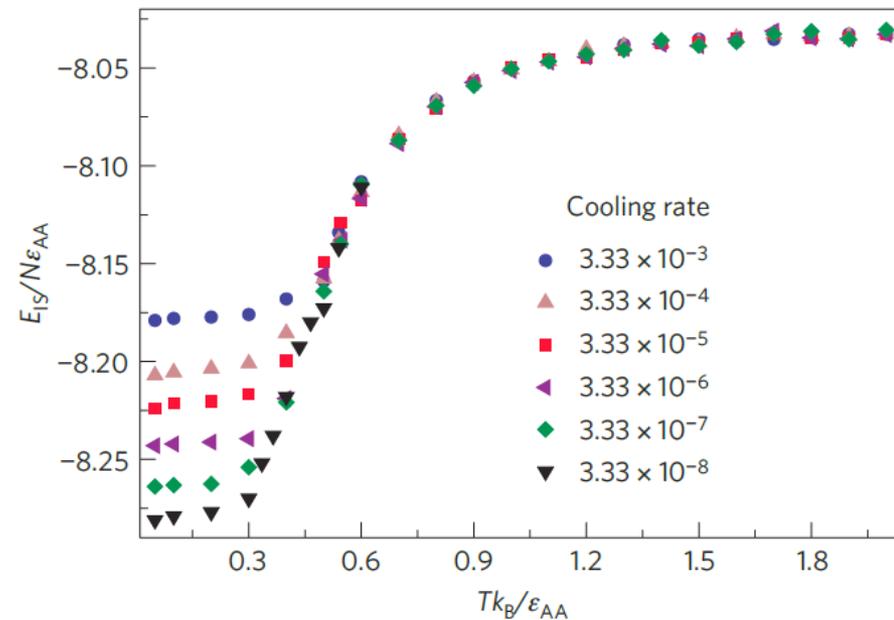
S. Singh, *Nature Mater.* **12**, 139 (2013)

- Add (numerically) Lennard-Jones particles
 - one-by-one onto free surface
 - ~5000 particles
 - explore effect of substrate temperature
 - compare to MD simulation of cooling liquidliquid vs vapor deposition



reach more stable glass from vapor

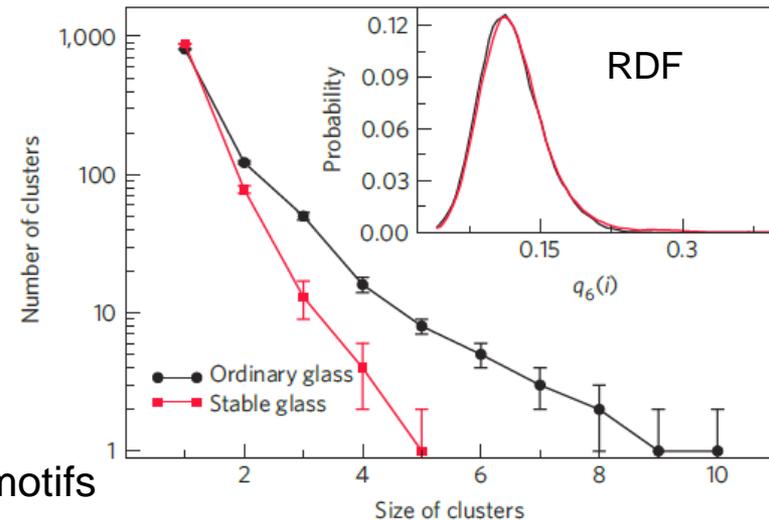
Structure energy (from cooled liquid)



slow cooling \Rightarrow more stable

“Ordinary” vs “Stable” Glass

- “Ordinary” glass: obtained by cooling liquid
- “Stable” glass: vapor deposited at T_s yielding lower energy configuration than ordinary glass
- Lowest energy obtained for $T_s \sim 0.8 T_{glass}$
 - unattainable from liquid at lab time scales
 - presumably also not from annealing film vapor deposited at a lower T_s
- Densities 1-2% higher than ordinary glass
- Structural features
 - radial distribution functions indistinguishable
 - more clustering of “ordered particles” in ordinary vs stable glass
 - stable glass more homogeneous
 - ordinary glass has wider range of packing motifs



Compare Model Calculations to Expt.

- a-Si expt.: steep improvement for $T_s \sim 400$ C
 - theoretical* $T_{\text{glass}} \sim 900$ K :
critical $T_s/T_{\text{glass}} \sim 0.75$ vs predicted $T_s \sim 0.8 T_{\text{glass}}$
 - similar trends seen in some organic glasses

* C.R. Miranda and A. Antonelli,
J. Chem. Phys. **120**, 11672 (2004)

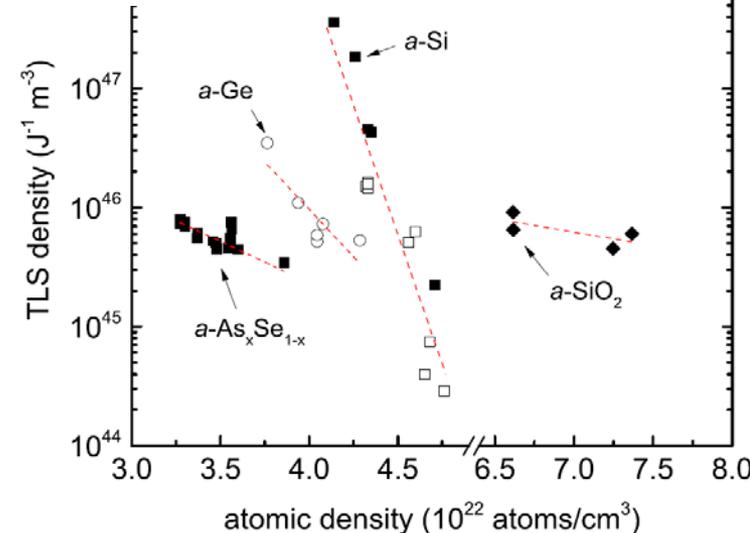
T. Perez-Castaneda, *PNAS* **111**, 11275 (2014)

- Low TLS correlates with high density
- Rayleigh scatter in SiO_2
 - decreases with anneal time
and anneal temperature

A. Ageev, S. Penn, P. Saulson,
Class. Quantum Grav. **21** (2004) 3887–3892

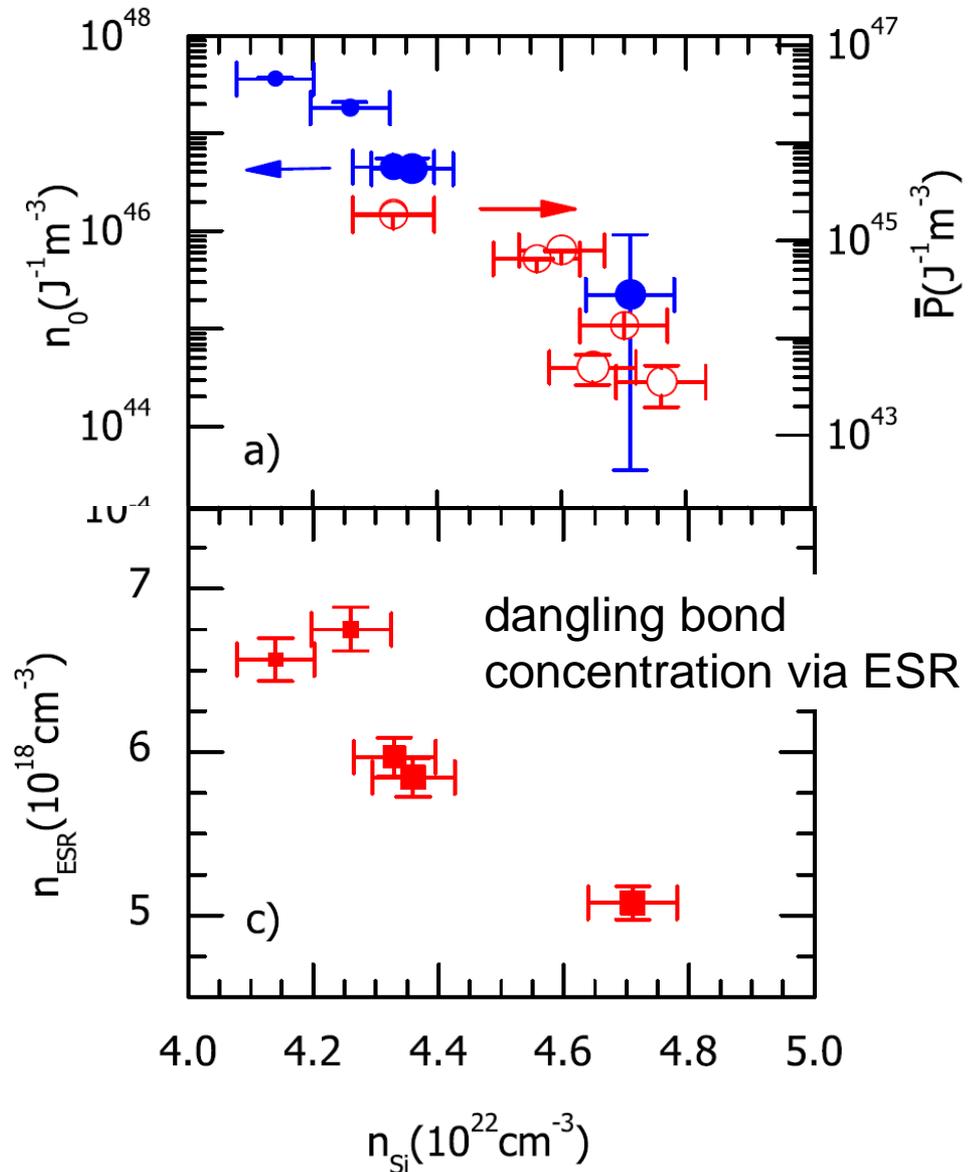
- Hellman posits evidence for heterogeneous structure:
 - dense backbone network surrounding low density regions
 - TLS and dangling bonds in the low density regions

D.R. Queen, F. Hellman, et al,
J. Non-Crystal. Solids **426** 19–24 (2015)



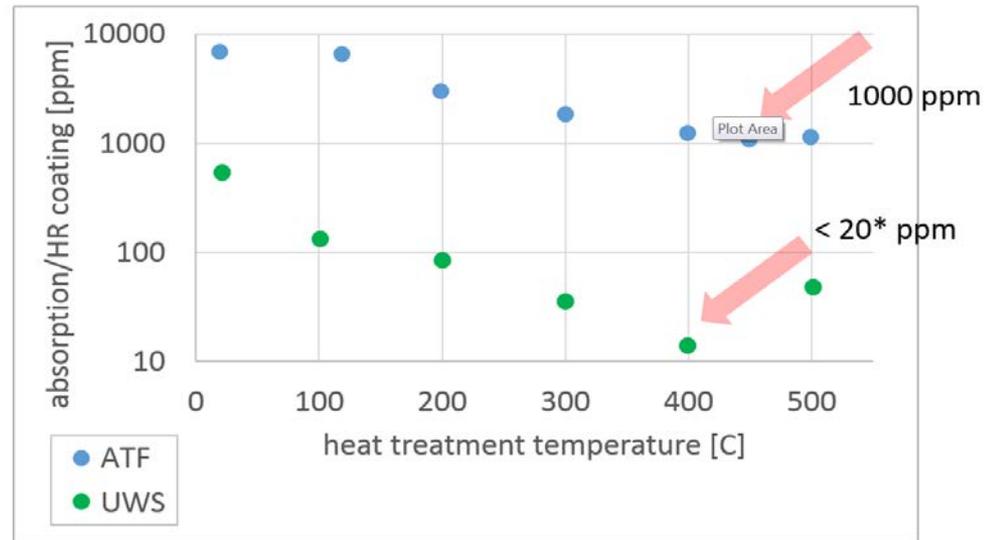
Optical Absorption in a-Si a Remaining Issue

- Absorption from dangling bonds too high
- Dangling bonds also reduced by high T_s
 - but $\sim 2x$, not 10^3x



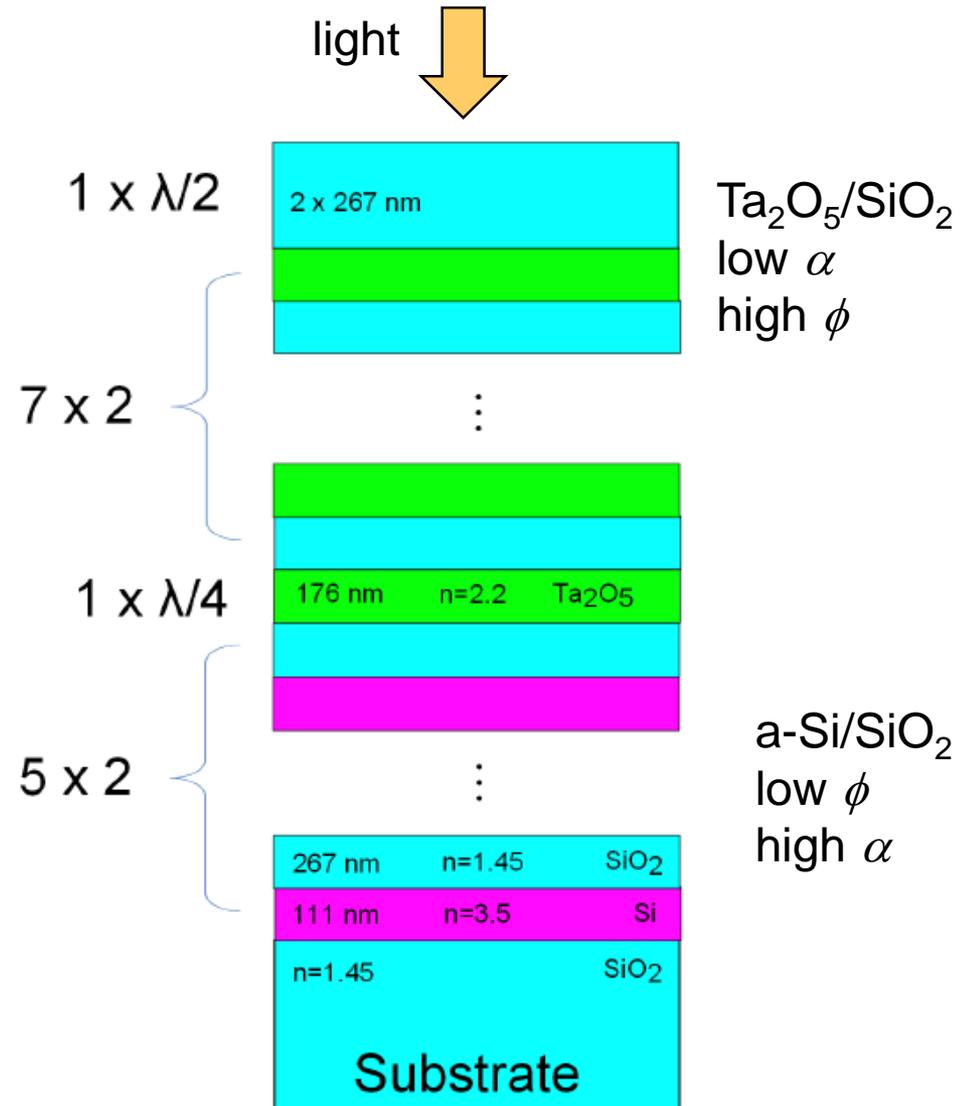
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- Recent IBS promising
 - alternative method to increase surface mobility
 - Stuart Reid 10:00 Wed.



Optical Absorption in a-Si a Remaining Issue

- Absorption from dangling bonds too high
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- Recent IBS promising
 - Stuart Reid 10:00 Wed.
- Multi-material coatings could mitigate absorption
 - Steinlechner poster

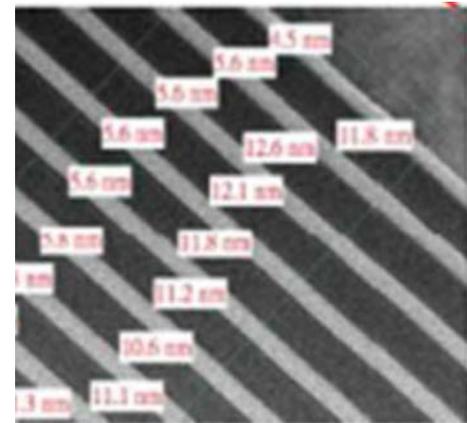


J. Steinlechner, et al , *Phys. Rev. D* **91** 042001 (2015)

W. Yam et al, *Phys. Rev. D* **91**, 042002 (2015)

Towards a Better Glass

- “Stable glass” concept
 - appears to apply for a-Si and organic glasses
- Extendable to amorphous oxides?
 - no data yet for high temperature deposition experiments in preparation
 - high glass temperatures potential challenge
 - Ion-beam sputter/assist
 - (controversial?) proposed alternative route to high surface mobility
- Alternative: higher annealing temperatures for oxide glasses
 - push toward more uniform glass
 - suppress devitrification
 - suitable stabilizing dopant, e.g. $\text{Zr:Ta}_2\text{O}_5$
 - nanolayers: poster A. Amato
 - suppress crystallization
 - interface scatter an issue?



Atomic Structure

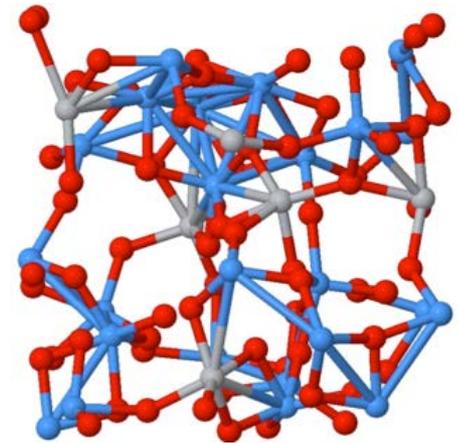
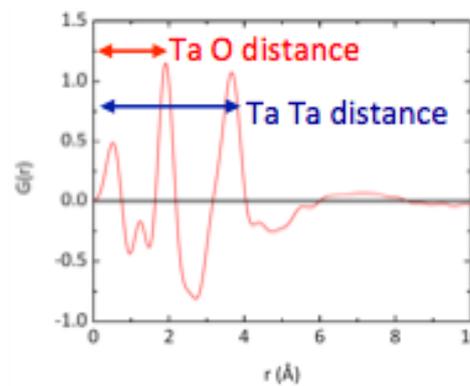
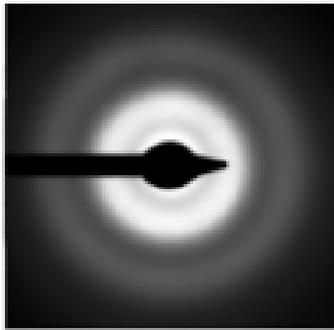
- Characterization of structure of amorphous materials more difficult than crystalline
 - several applicable techniques:
- Short-range order (<1 nm):
 - TEM (transmission electron microscopy)
 - Data: Nearest atomic neighbor distribution
 - Pro: Can be used on any amorphous coating, multi or single layer with layer dependent data
 - Con: Requires destructive sample prep
 - XAFS (X-ray absorption fine structure)
 - Data: Atomic species specific structure (around only Ta, Ti)
 - Pro: No sample prep
 - Con: Requires synchrotron with limited availability (3 X per year)
 - NMR (nuclear magnetic resonance)
 - Data: Local atomic co-ordination (predominantly O)
 - Pro: Provides direct measurement of coordination number
 - Con: Required destructive sample prep requires coatings on salt substrates
 - Raman spectroscopy
 - Data: Bond angle changes, Chemical ID, Phonon spectra
 - Pro: Probes vibrational modes vs static regime of other techniques
 - Con: Requires models to fully interpret

Atomic Structure

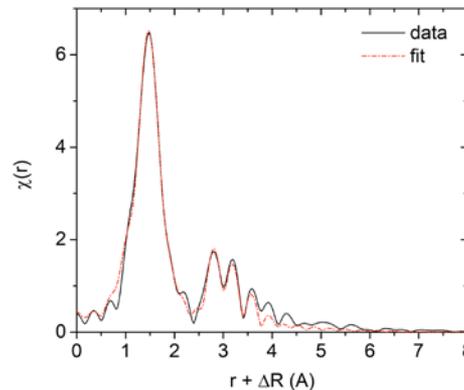
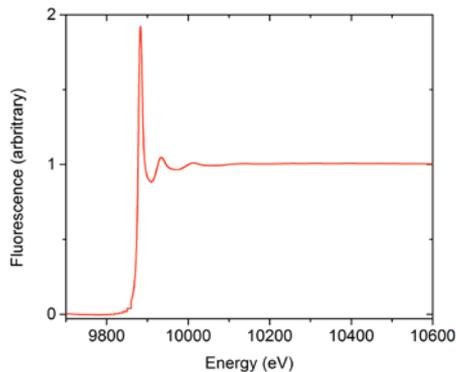
- Medium-range order (0.5 – 5 nm):
 - FEM (fluctuation electron microscopy)
 - Data: Quantifies the MRO by measuring variance in TEM diffraction patterns
 - Pro: MRO can be measured at various probe sizes (MRO at each set electron beam size)
 - Con: Destructive TEM sample prep, difficult to model
 - GI-XPDF (grazing incidence X-ray pair distribution function)
 - Data: Nearest neighbor distribution with resolution into medium range order
 - Pro: No sample prep required, depth dependence
 - Con: Requires synchrotron time
- talk by Riccardo Bassiri 9:40 Tuesday

Example of Atomic Structure Measurement

- Pair Distribution Function (PDF), $G(r)$, electron or X-ray diffraction



- Extended X-ray Absorption Fine Structure (EXAFS),
Ta L_{III} edge



How to Use Structural Characterization

- Some observations:
 1. structural changes with annealing and doping are subtle
 2. difficult to unambiguously invert from data to structure
- Some useful topics for discussion:
 - given progress in theoretical modeling, how to leverage data from structural probes?
 - forward vs inverse calculations for structural data

Some Current Directions in Coating Research

- Ultra-stable oxide glasses: experiments beginning
 - high temperature deposition
 - ion beam sputtering/ion assisted
 - slow deposition rates
- Other experimental approaches to synthesize lower loss coatings:
 - nanolayer stabilization
 - dopant-stabilized high-temperature annealing
 - multi-material coatings
- Atomic structure modeling/characterization
 - experiment and theory reaching maturity to usefully interact
 - tie-up loss and structure modeling with measurements
 - explore theoretically advantageous material/dopant combinations

Some Other Topics for Discussion

- Challenges
 - 4? year timeline to better coatings for A+
clarify performance goals and timeline
 - need to maintain long-range (cryo) research while targeting near-term (RT)
 - materials discovery not easily schedulable
 - need time for coating vendor to implement proposed coating once discovered
- How to tie up synthesis, loss measurements, structural models, coating design, and expts
 - more effective coordination across collaboration
 - complex decision space
 - how to reach decision points on what not to do?