



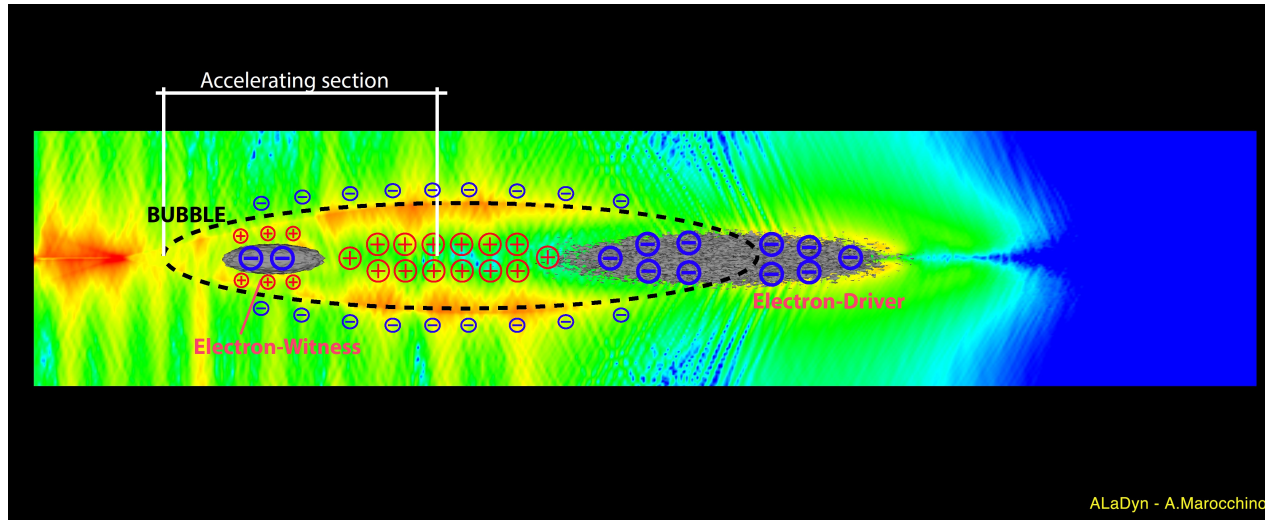
# PhD activity Report

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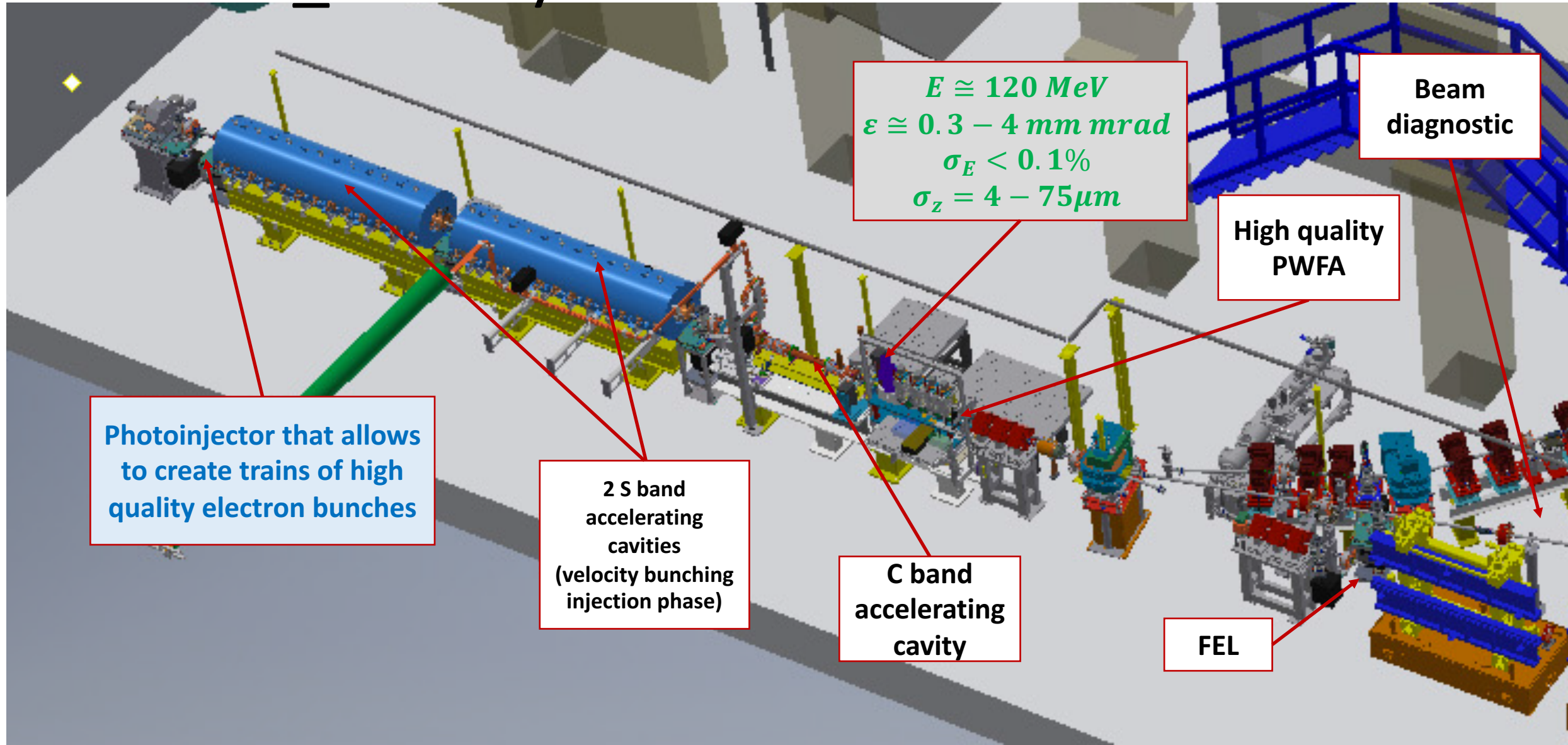
# Plasma Wakefield Acceleration Beam Driven



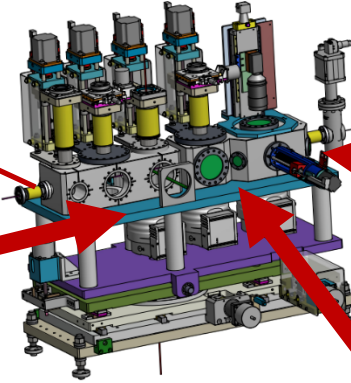
- Plasma Wakefield acceleration is a new kind of device that utilizes the wakefield produced by an electromagnetic pulse inside plasma to accelerate a beam

- In PWFA beam driven the wakefield is generated by the coulombian repulsion of a charged beam
- The beam driven acceleration scheme consist in a driver (or multiple drivers) that looses energy inside plasma and a witness gaining energy

# SPARC\_LAB Layout



# Acceleration experiment @SPARC\_LAB



$E \cong 150 \text{ MeV}$   
 $\varepsilon \cong 1 - 2 \text{ mm mrad}$   
 $\sigma_E < 1\%$

$\sigma_x < 3 \mu\text{m}$

Permanent  
magnets final  
focus system

Effective  
accelerating  
gradient  
 $\cong 1 \text{ GV/m}$

Low energy  
beams

Pre ionized plasma  
(gas inside a capillary  
ionized by discharge)

Beam driven  
acceleration

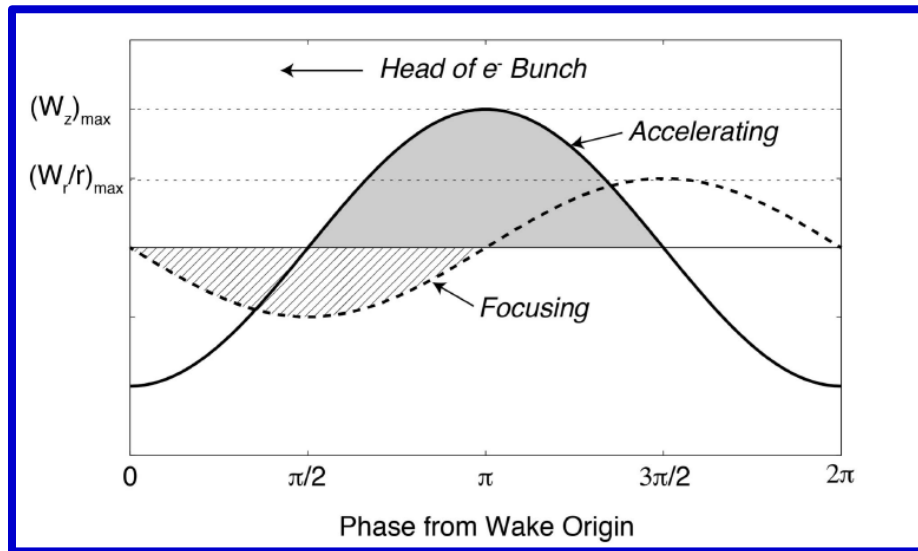
Resonant  
Wakefield  
Acceleration  
Scheme

High quality  
beams

Quasi non  
linear regime

# Linear/Bubble regime

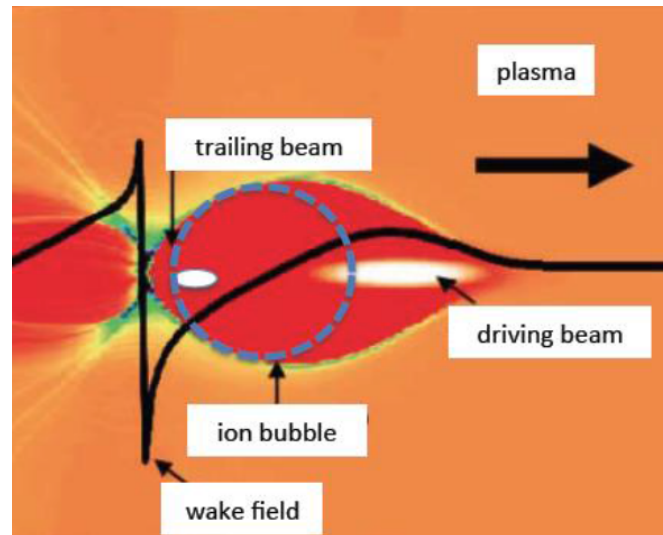
$$n_b \ll n_0$$



## Linear field

- It is possible to inject a beam in the crest region
- Non linear dependency of the focusing
- Accelerating field depends on transverse position
- Lower field

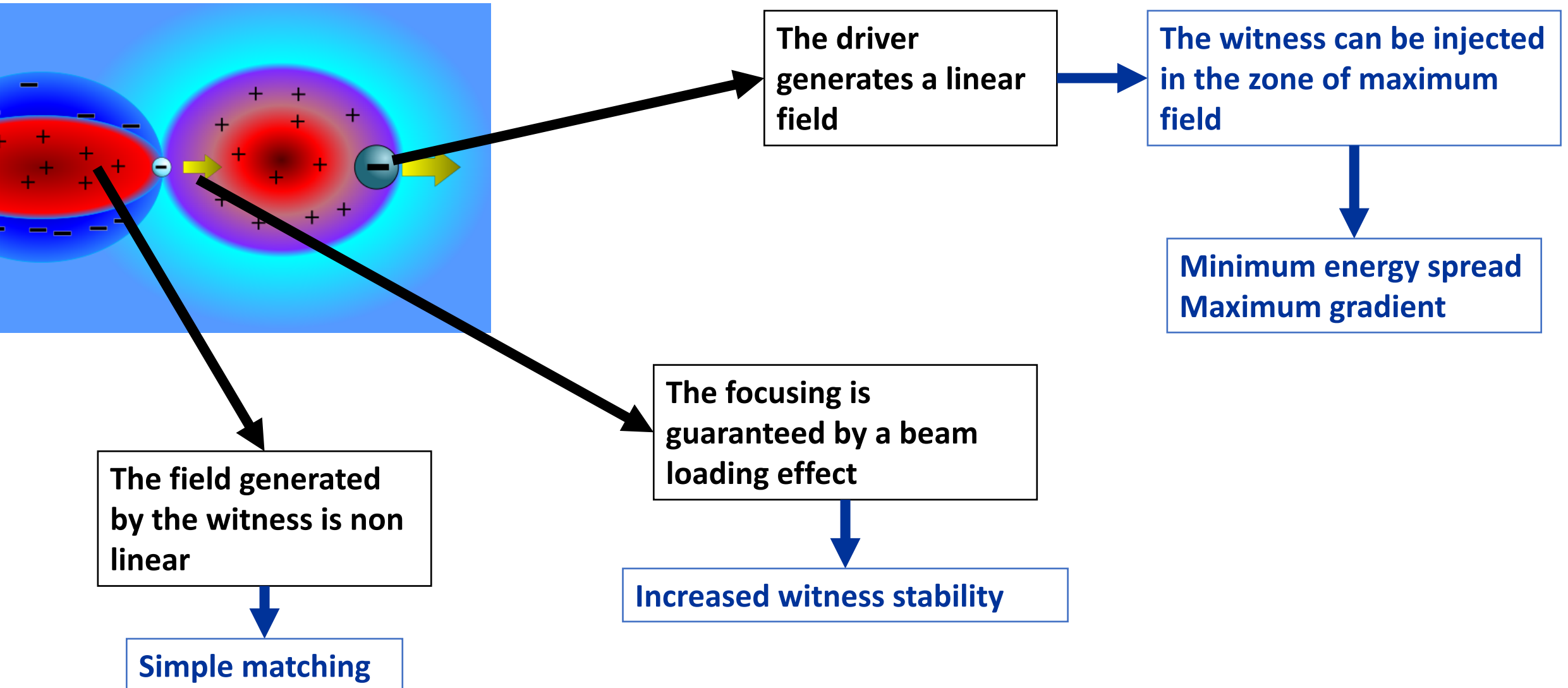
$$n_b > n_0$$



## Blow out field

- No crest region -> Spike on field
- Linear dependency of the focusing
- Accelerating field doesn't depend on transverse position
- Higher field

# New concept: Linear/non Linear

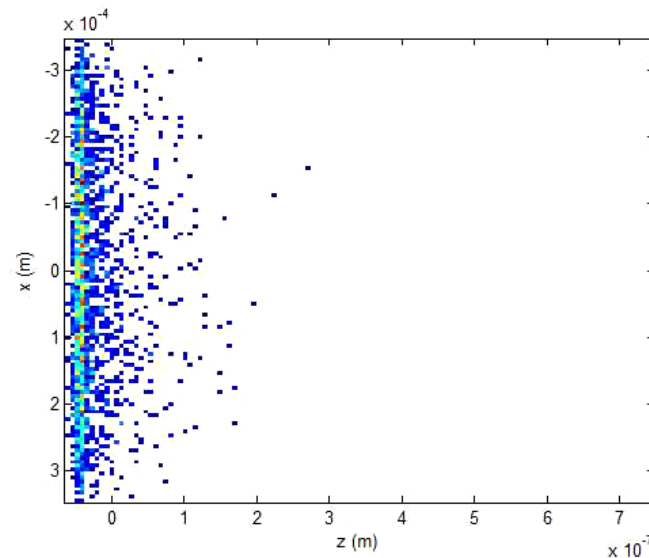
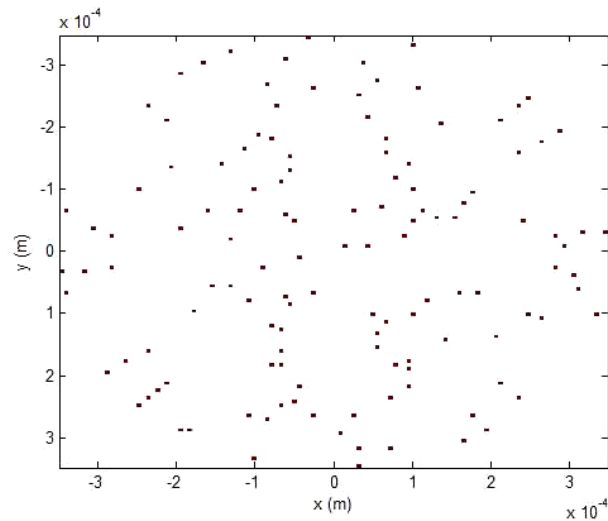




# Hollow driver scheme

- **Short witness** → Witness compression by velocity bunching

**Velocity bunching** → Witness emittance growth  
Lower compression



**Hollow Driver**

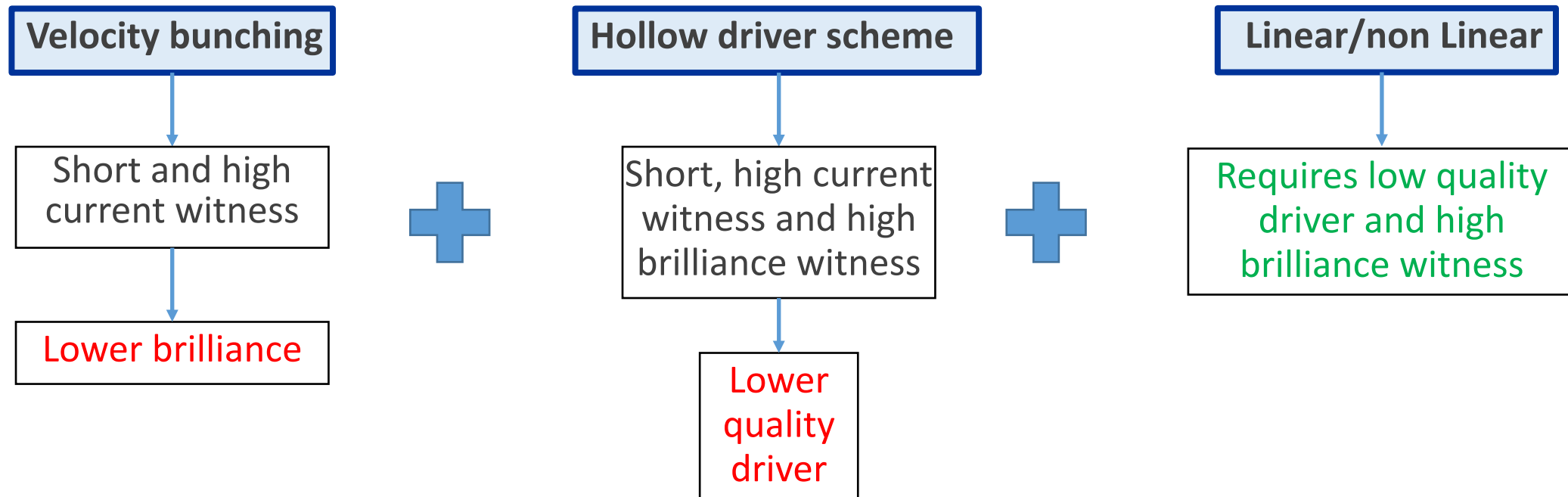
Very short and low emittance witness

High emittance driver

**Courtesy of R. Pompili**

# Proposal:

## Hollow driver scheme+Linear/non Linear





# High quality witness requirements: Driver

A driver that follows the matching conditions guarantee a field that varies slowly (with a frequency very lower than the betatron frequency of witness)

- **Driver transverse matching**

Ion column (non linear)  $\sigma_x = \sqrt[4]{\frac{2}{\gamma}} \sqrt{\frac{\varepsilon_n}{k_p}} \longrightarrow \beta_x = \frac{\sqrt{2\gamma}}{k_p}$

1D-linear theory (linear)  $\sigma_x = \sqrt[4]{\frac{2}{\alpha\gamma Z(0)}} \sqrt{\frac{\varepsilon_n}{k_p}} \longrightarrow \beta_x = \frac{1}{k_p} \sqrt{\frac{2\gamma}{\alpha Z(0)}}$

$$Z(\xi) = \sqrt{\frac{\pi}{2}} k_p \sigma_z e^{k_p^2 \sigma_z^2 / 2} \text{Im} \left[ e^{ik_p \xi} \text{erfc} \left( \frac{\xi}{\sqrt{2} \sigma_z} + i \frac{k_p \sigma_z}{\sqrt{2}} \right) \right]$$

# High quality witness requirements: Driver

Matched beams

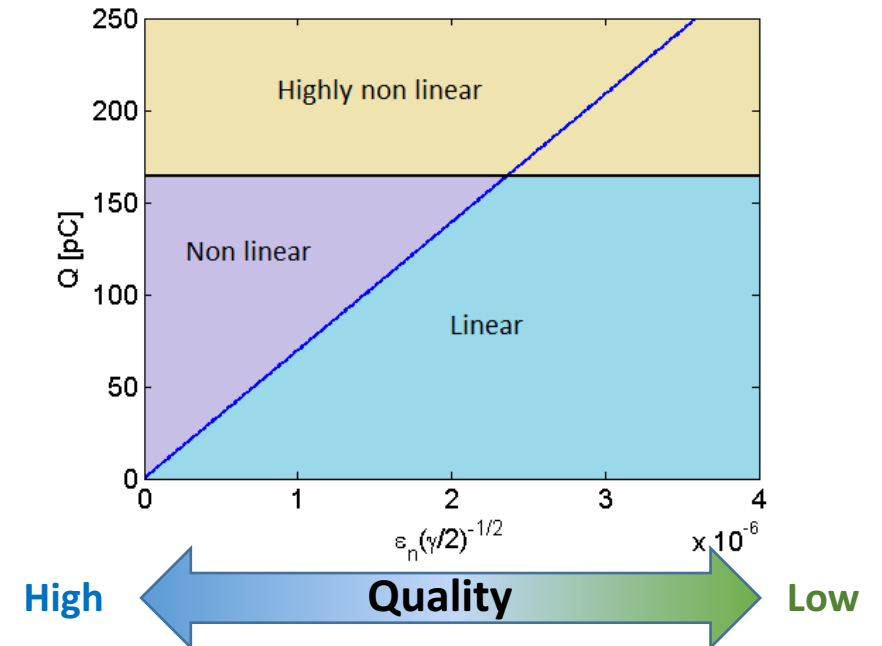
- **Non linear driver threshold**  $\ell = \frac{Q}{e} \frac{k_p}{(2\pi)^{3/2} \sigma_z \varepsilon_n n_0} \sqrt{\gamma}$   $\longrightarrow$   $\ell \gg 1$  non linear field  
 $\ell \ll 1$  linear field

Within the acceleration  
 $\frac{\sqrt{\gamma}}{\varepsilon_n}$  decreases for:

- Deceleration
- Beam depletion
- Head erosion

QNL threshold  $\frac{Q}{e} \frac{k_p^3}{n_0} < 1$

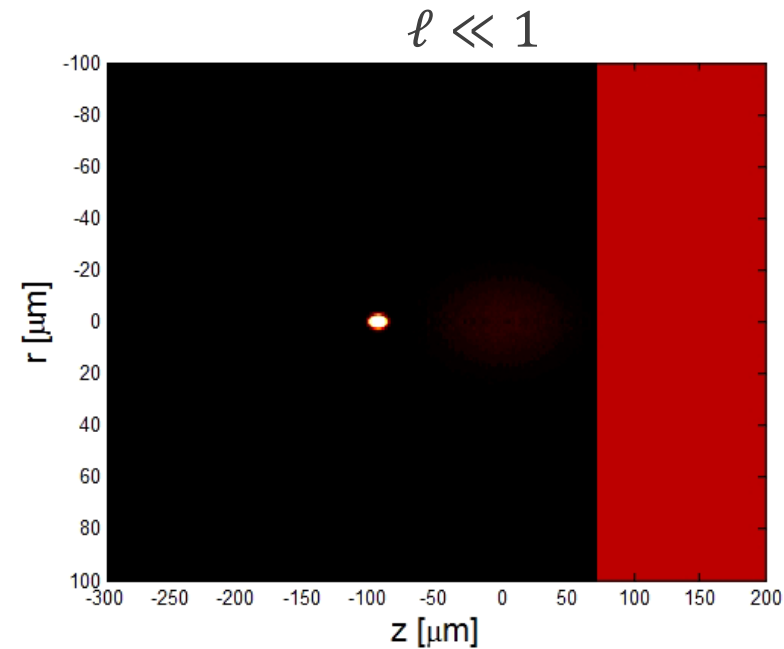
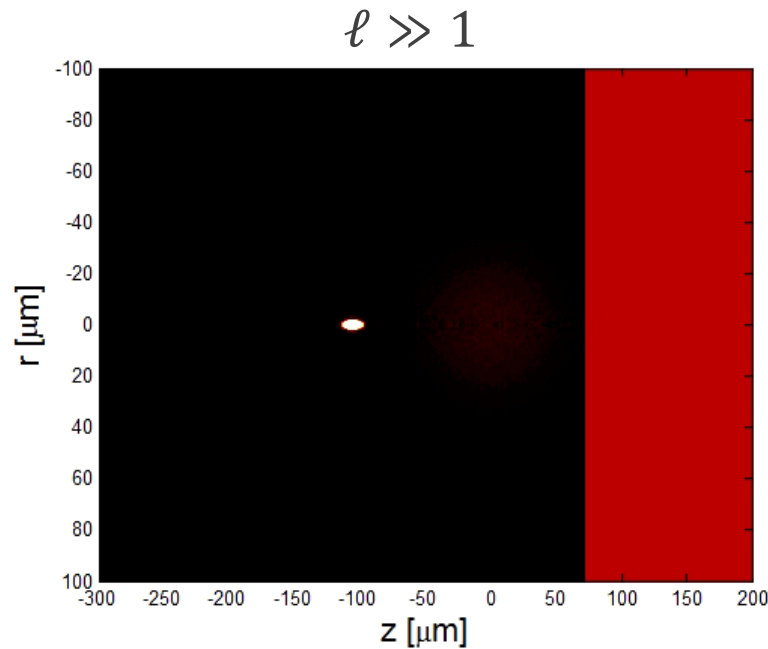
Within acceleration  
 the bubble can be  
 destroyed by driver  
 erosion



# High quality witness requirements: Driver outside of matching

- It is difficult to inject both the driver and the witness at the matching conditions

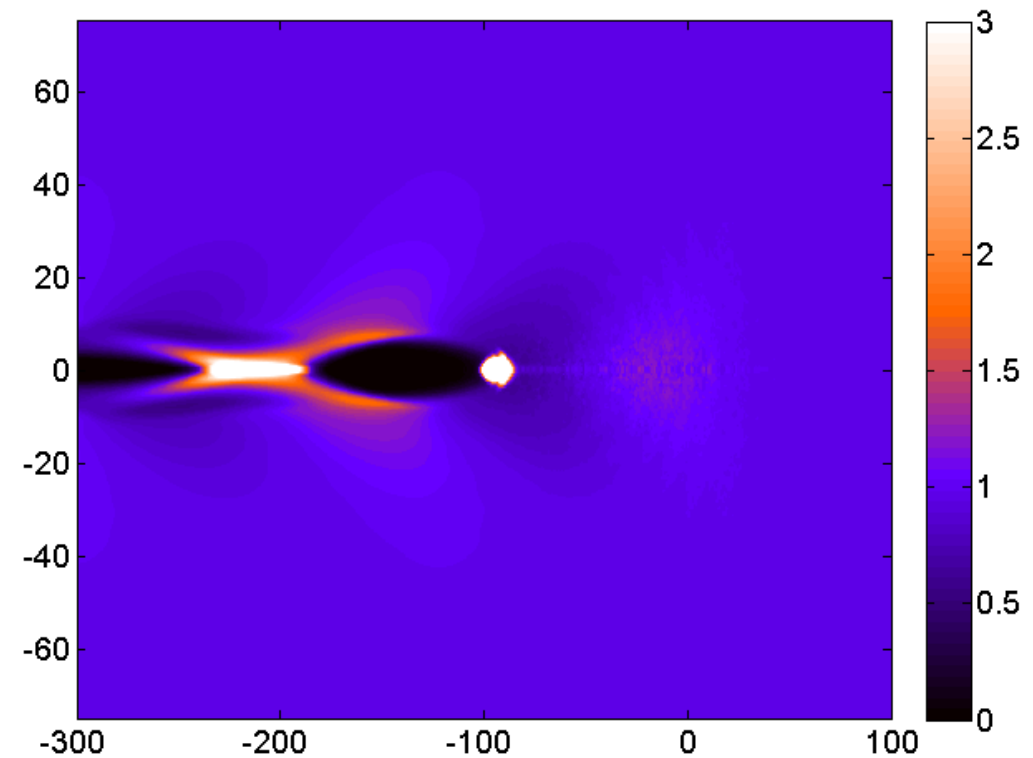
Driver is usually injected with a spot size that is higher than the matching condition



# High quality witness requirements: Driver outside of matching

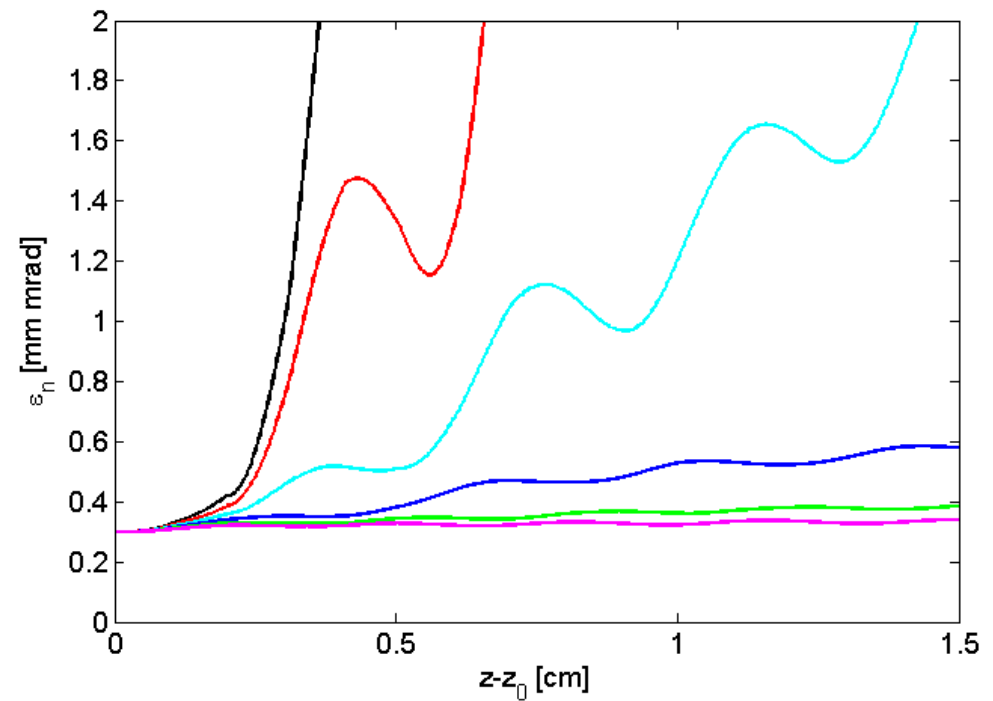
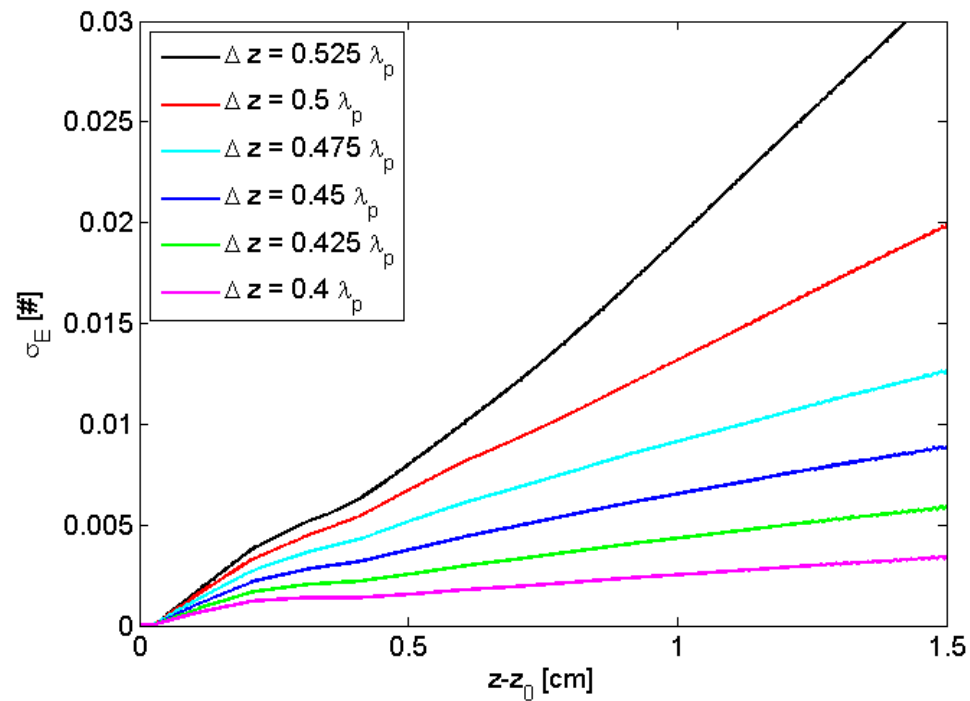
- **Linear field crest zone:**
- Guarantees the maximum accelerating field
- Has a local electron plasma density that is independent from bunch density
- Has a negligible focusing field
- Enhanced witness beam loading creates a focusing field such that matching condition is

$$\sigma_x = \sqrt[4]{\frac{1}{\gamma}} \sqrt{\frac{2\varepsilon_n}{k_p}} \longrightarrow \beta_x = \frac{2\sqrt{\gamma}}{k_p}$$



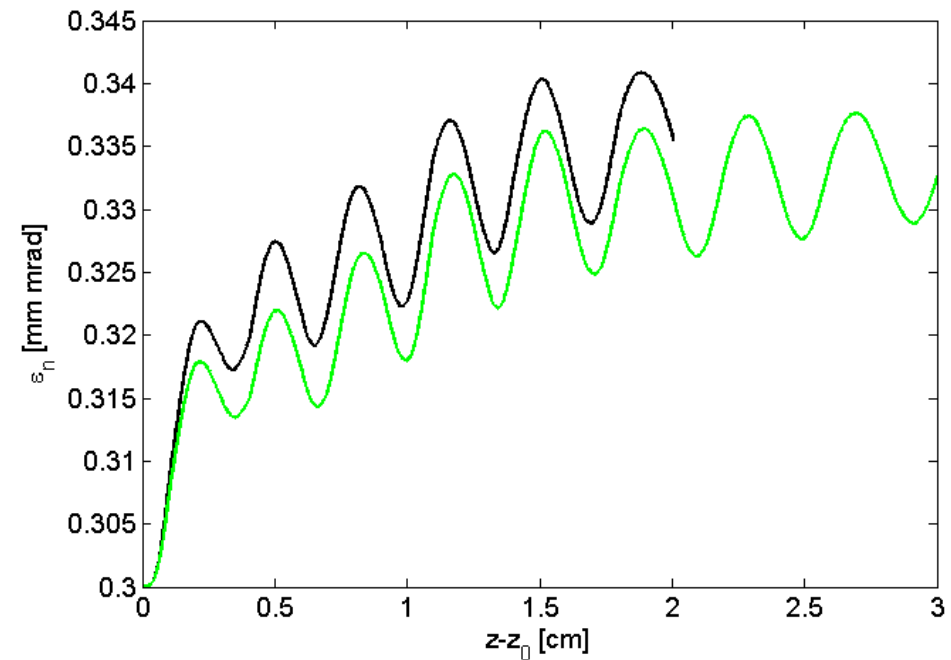
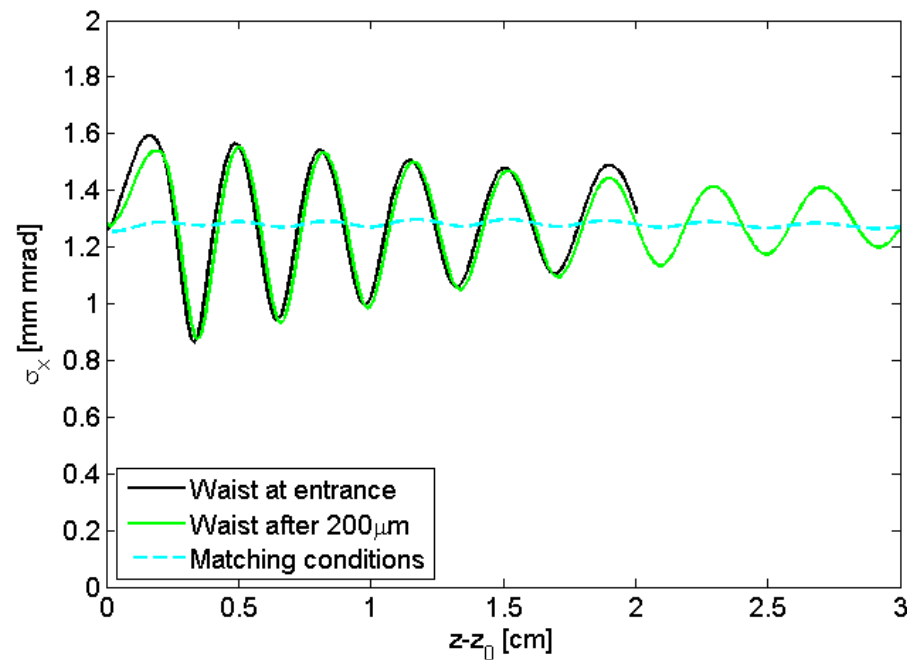
# High quality witness requirements: Witness matching

- **2 required scans:**
- Injection phase optimizes energy spread and emittance (rough

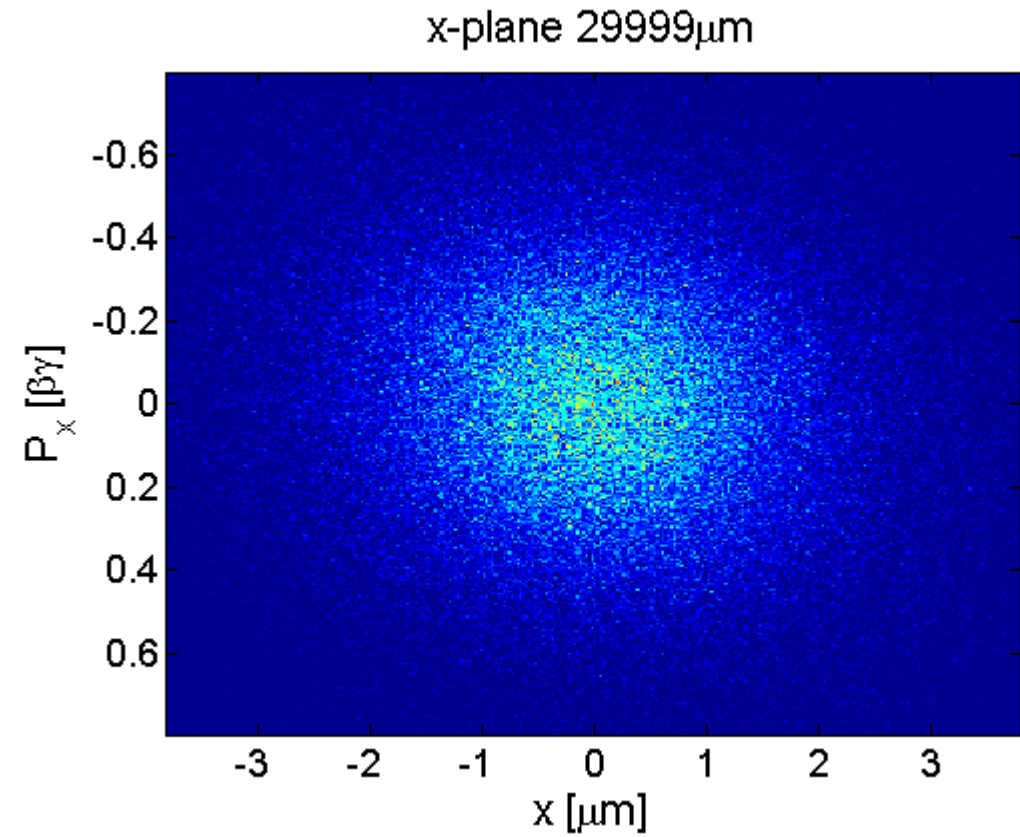
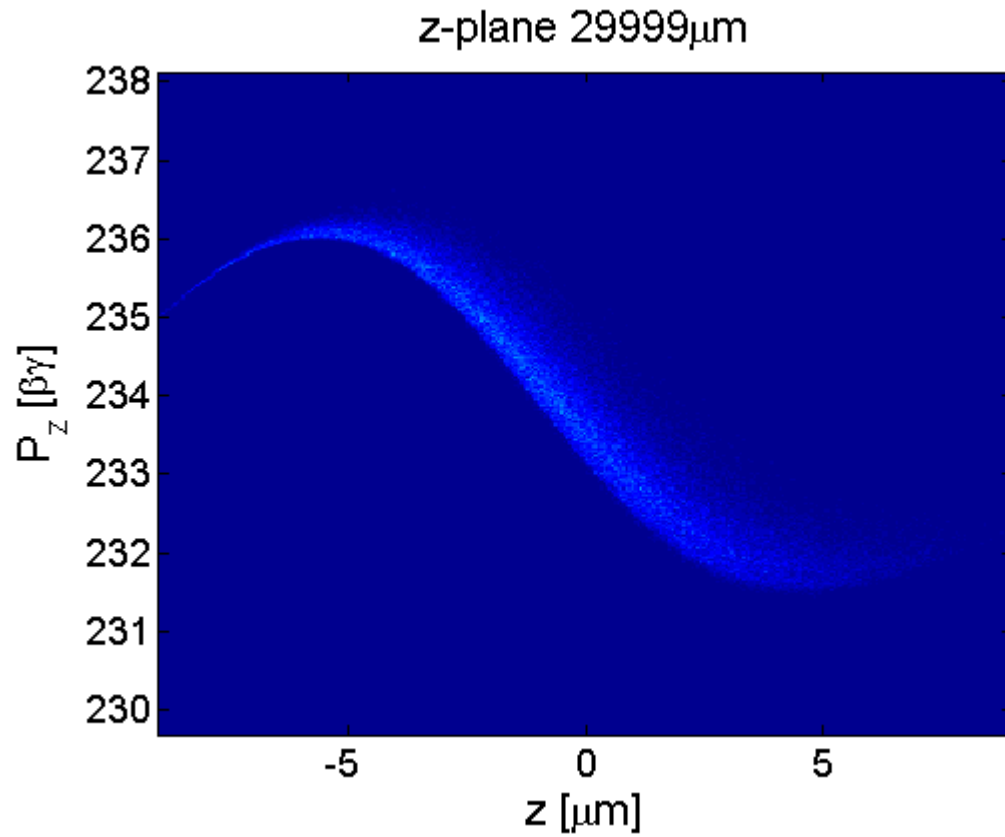


# High quality witness requirements: Witness matching

- Witness waist position optimizes emittance (fine tune)



# Witness phase space after acceleration



- **Accelerating gradient: 600 MV/m**



# 1 GV/m working point

## Driver

$$Q = 200pC$$

$$\sigma = \begin{pmatrix} 13 & 0 & 0 \\ 0 & 13 & 0 \\ 0 & 0 & 38 \end{pmatrix} \mu m$$

$$\varepsilon = \begin{pmatrix} 20 & 0 \\ 0 & 20 \end{pmatrix} \text{mm mrad}$$

$$\gamma = 200$$

$$\sigma_E = 0.1\%$$

## Witness

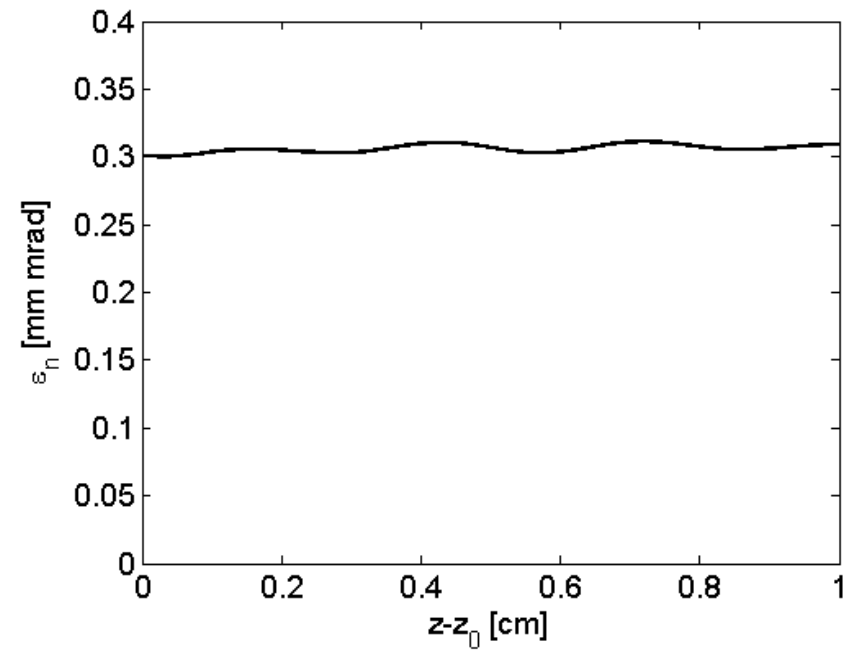
$$Q = 15pC$$

$$\sigma = \begin{pmatrix} 1.25 & 0 & 0 \\ 0 & 1.25 & 0 \\ 0 & 0 & 5.3 \end{pmatrix} \mu m$$

$$\varepsilon = \begin{pmatrix} 0.3 & 0 \\ 0 & 0.3 \end{pmatrix} \text{mm mrad}$$

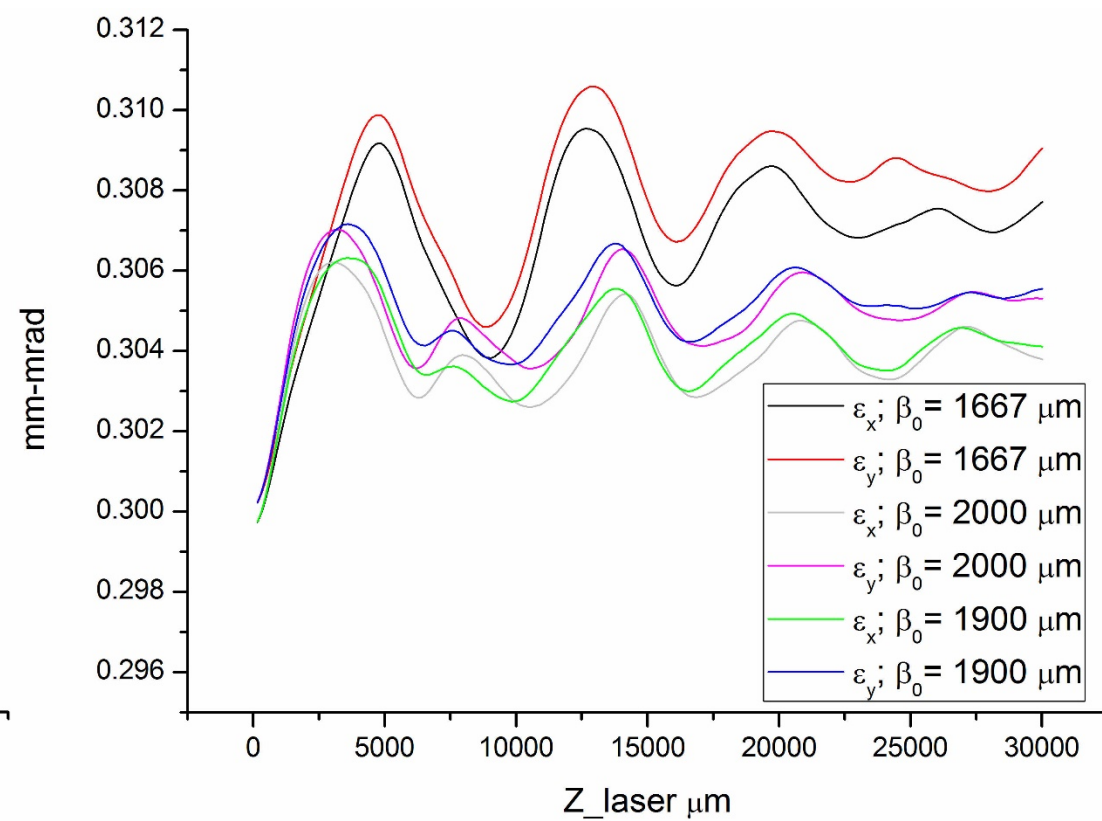
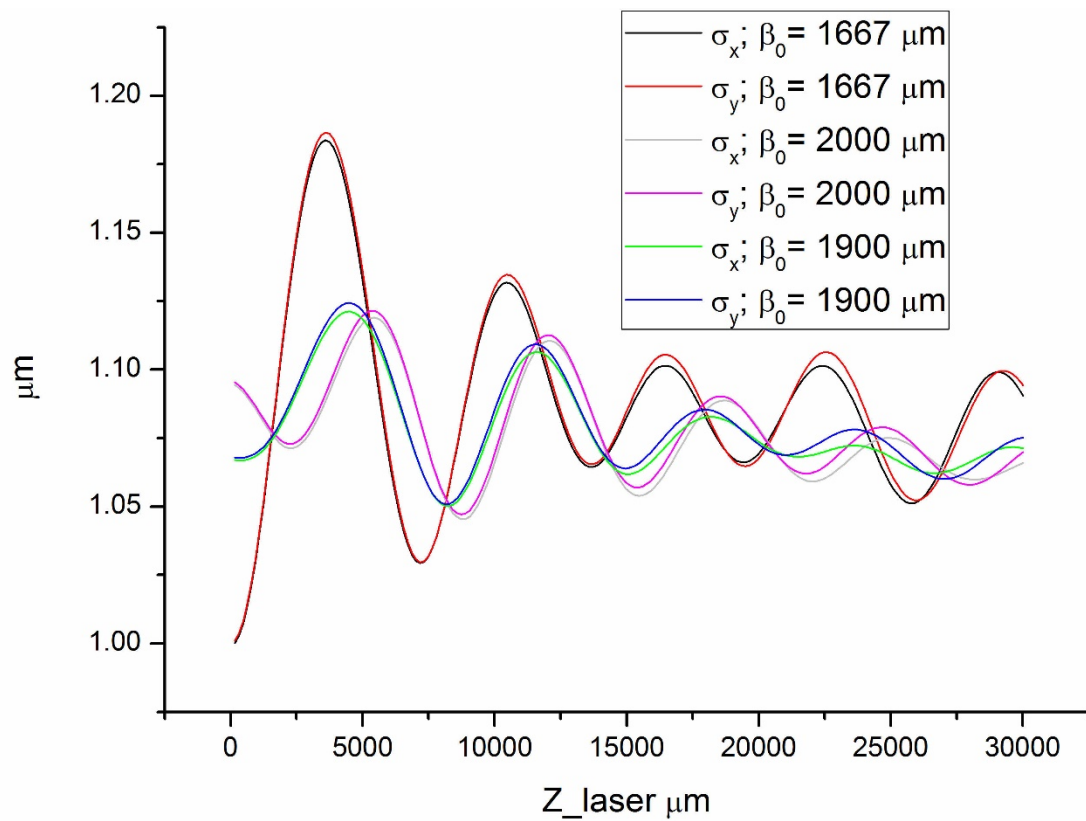
$$\gamma = 200$$

$$\sigma_E = 0\%$$

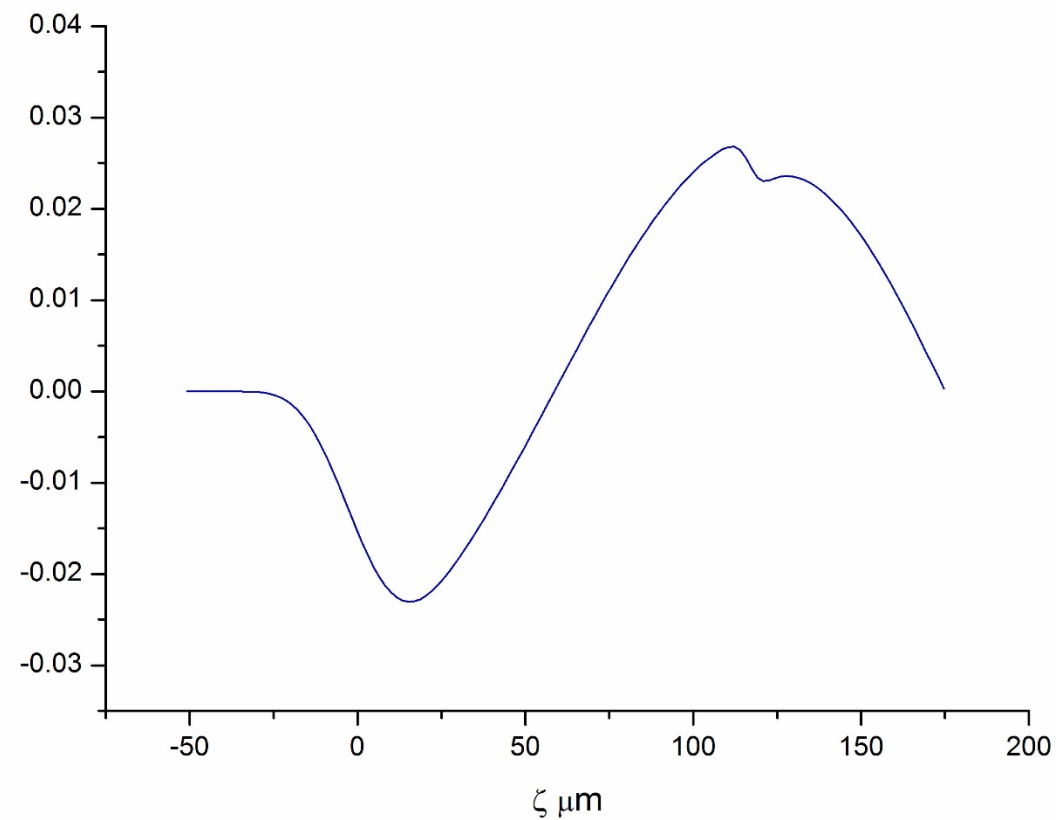
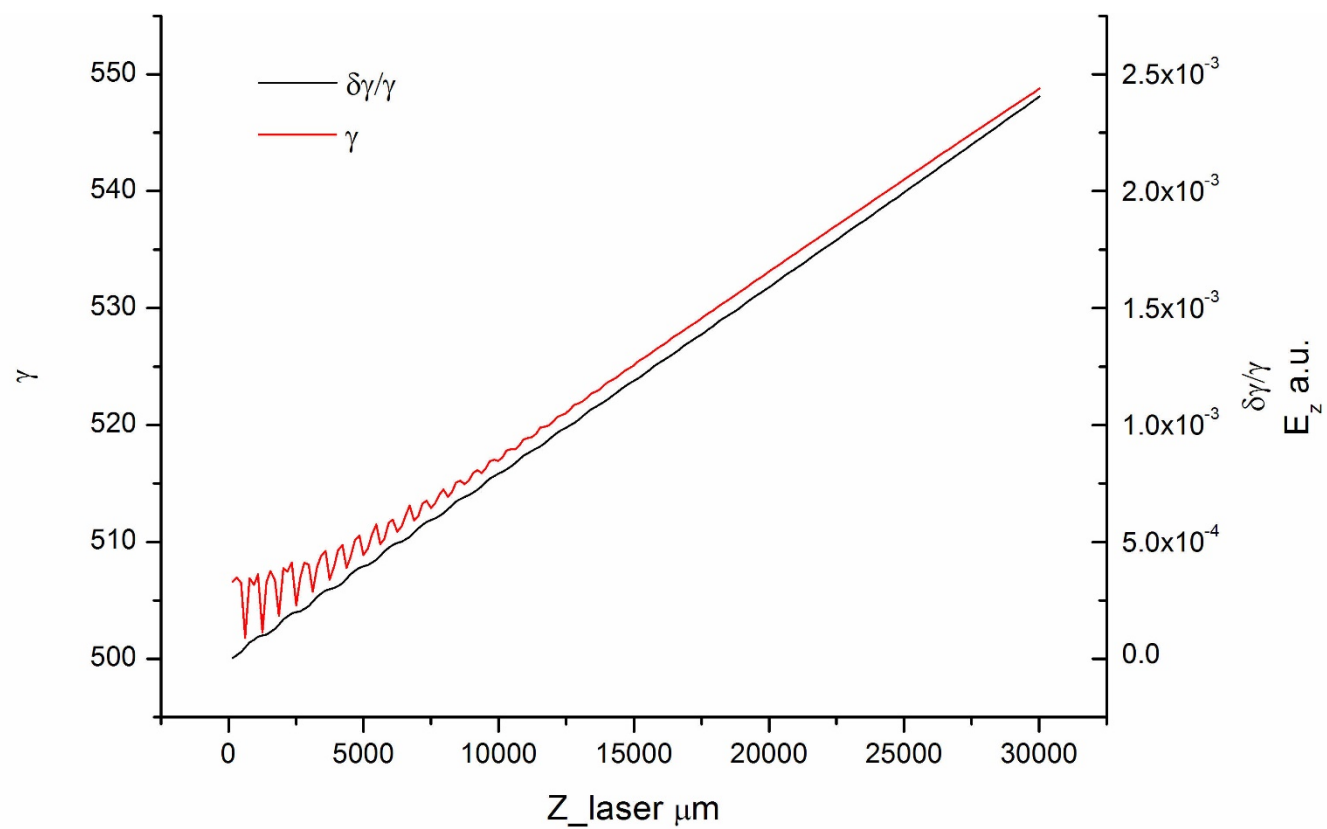


- **Accelerating gradient: 1 GV/m**

# LWFA ExIn



# LWFA ExIn



# Conclusions

- During my PhD work I focused on beam dynamics inside plasma in order to obtain high quality witness at the exit
- The study of beam dynamics required to develop scaling laws for PWFA
- Using the scaling laws I was able to find a way to create a new kind of PWFA scheme