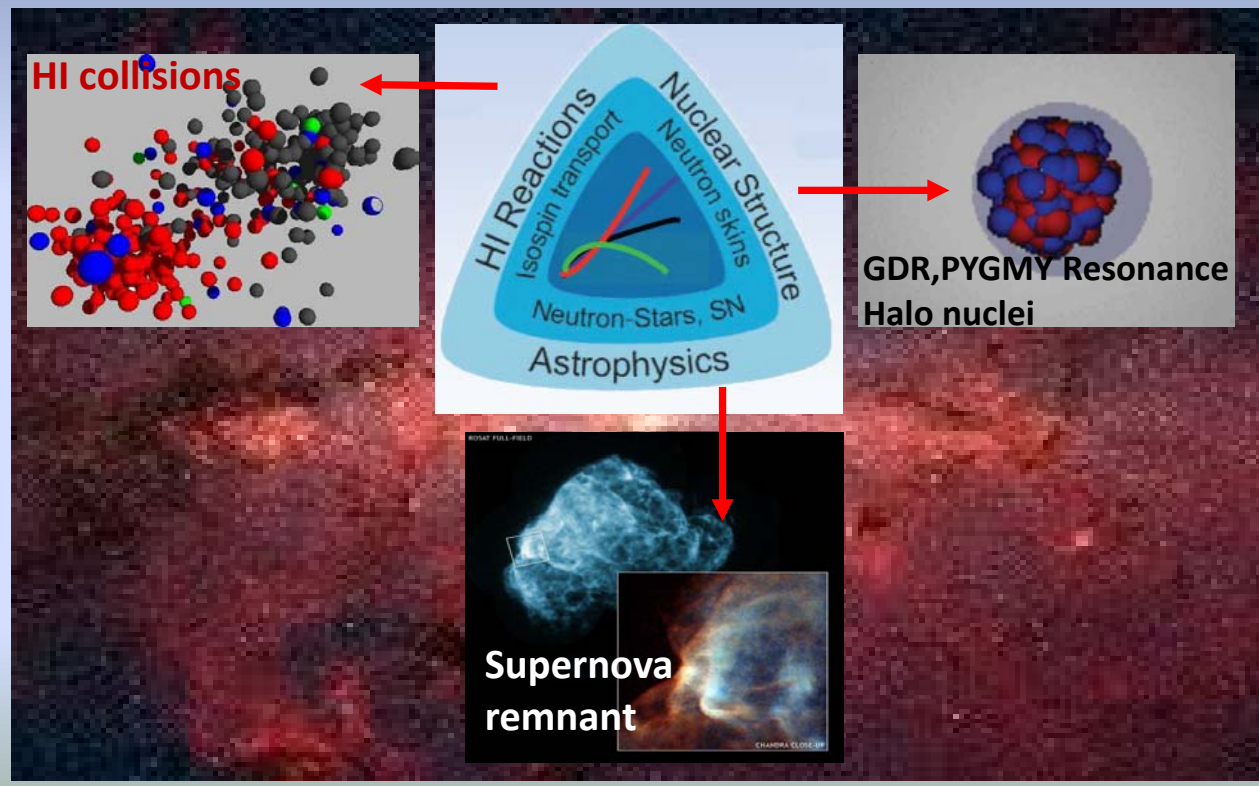
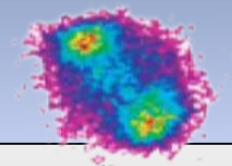


# Probing the nuclear symmetry energy with heavy ion collisions

The nuclear EOS describes the relation between pressure, density, temperature and isospin asymmetry. It is an essential ingredient in nuclear physics and astrophysics, but how  $E/A(\rho, \delta)$  depends on the density  $\rho$  and isospin asymmetry  $\delta$  ?



The density dependence of symmetry energy should be determined in a coherent way between astrophysical observations and heavy ion phenomenology



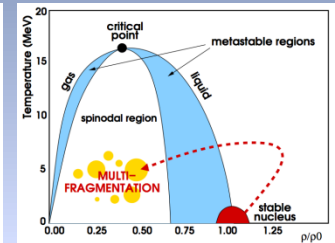
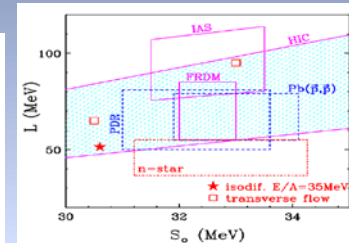
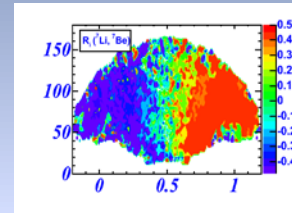
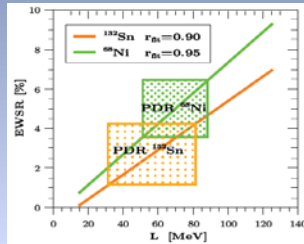
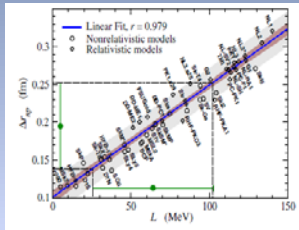
# The role of isospin asymmetry in nuclear processes in the laboratory and in the cosmos

From laboratory

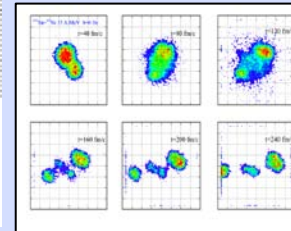
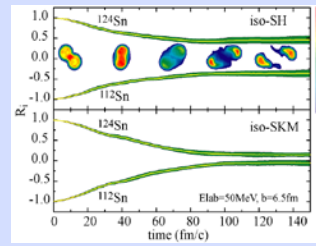
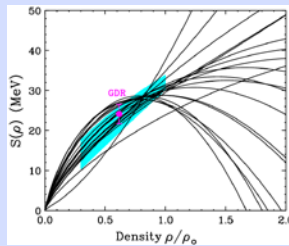
Nuclear structure

Nuclear reactions

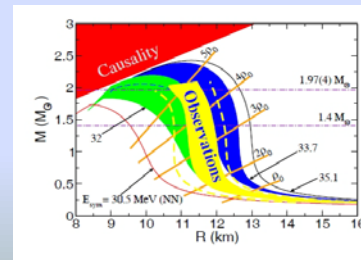
Experimental Heavy ion reactions



Theory



Models



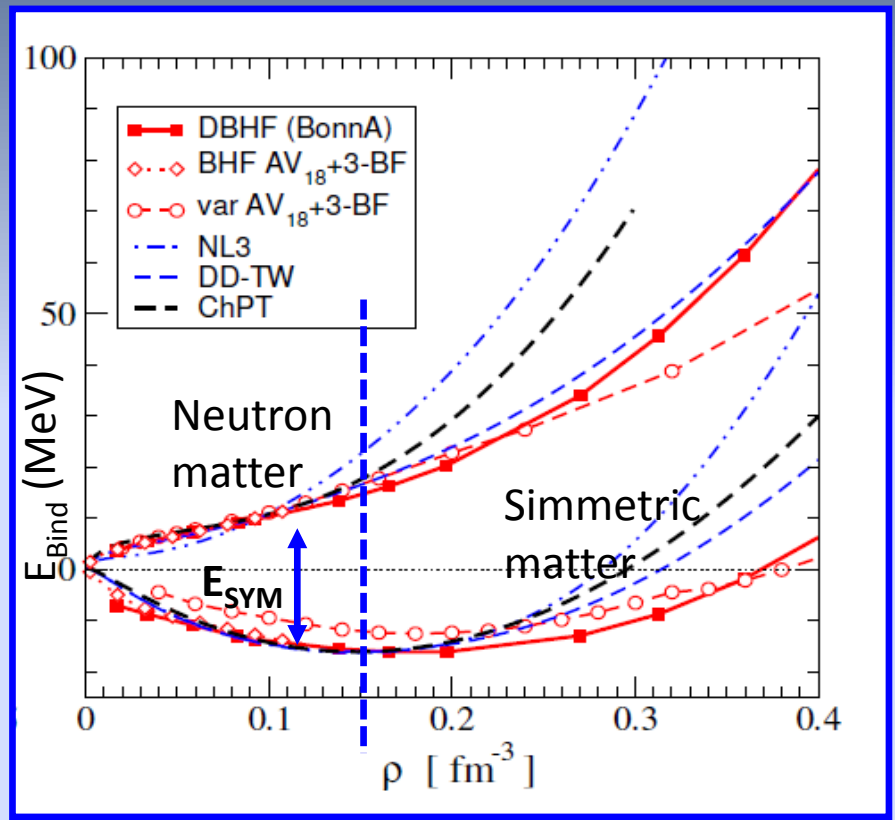
To compact stars

The key problem: the **symmetry energy** as a function of the **barionic density**

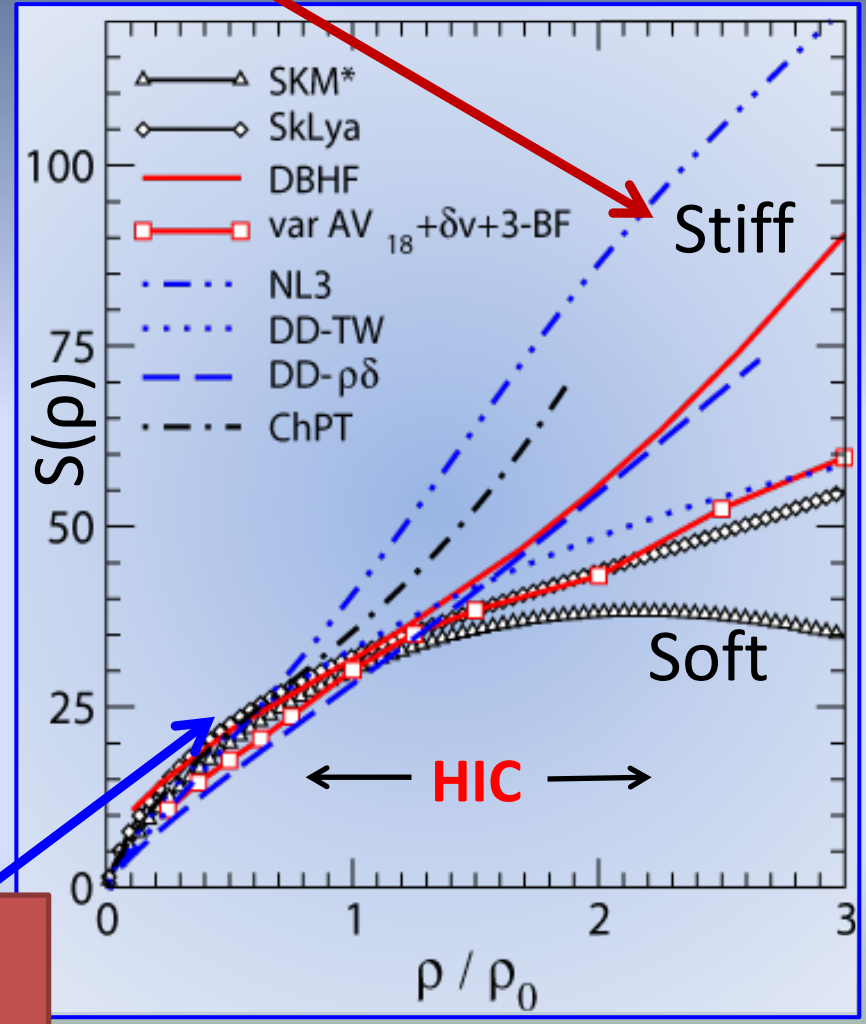
$$E(\rho, \delta) = E(\rho, \delta = 0) + S(\rho)\delta^2$$

$$\delta = \frac{\rho_n - \rho_p}{\rho_n + \rho_p} = \frac{N - Z}{A}$$

Large deviations at high densities, lack of experimental probes



Fuchs and Wolter, EPJA 30, 5 (2006)



Sensitivity to observables based on N/Z asymmetry

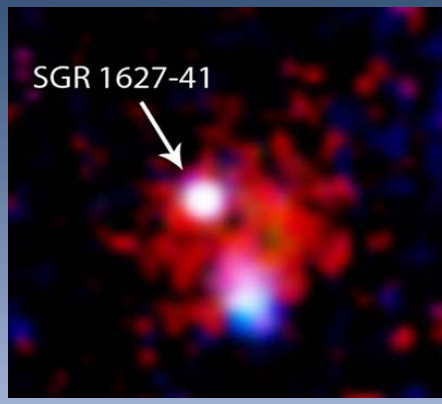
# Symmetry energy in neutron stars and neutron skin radius

$$S(\rho) = S_0 + \frac{L}{3} \left( \frac{\rho - \rho_0}{\rho_0} \right) + \frac{K_{sym}}{18} \left( \frac{\rho - \rho_0}{\rho_0} \right)^2 + \dots$$

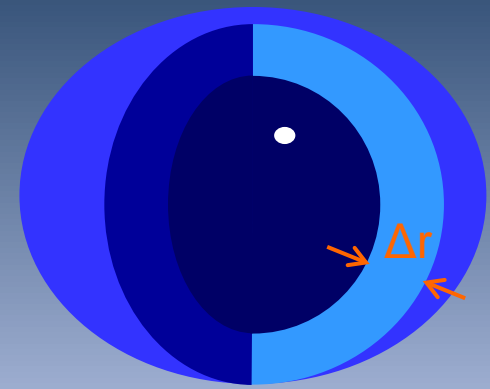
$$L = 3\rho_0 \frac{dS(\rho)}{d\rho} \quad \text{Slope}$$

$$P_{SYM} = \rho^2 \left( \frac{dS}{d\rho} \right)_{\rho=\rho_0} = \frac{\rho_0}{3} L$$

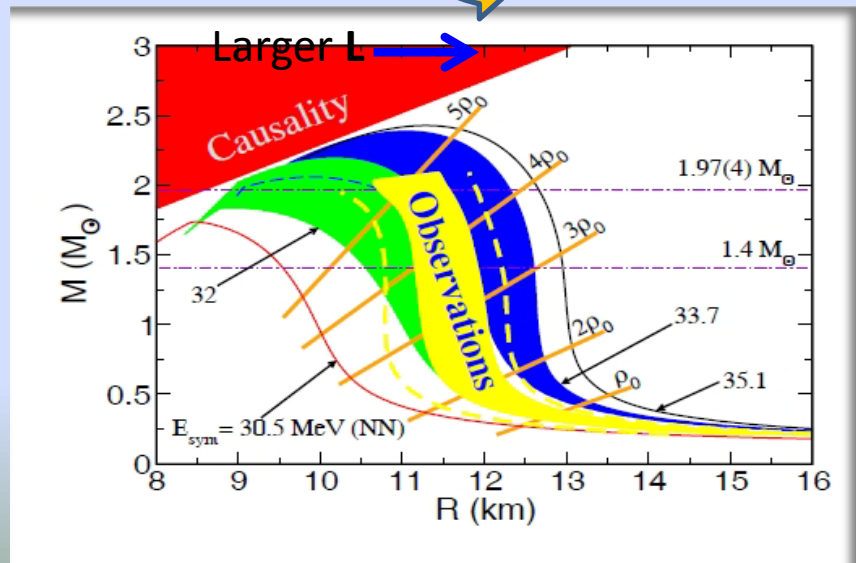
Pressure



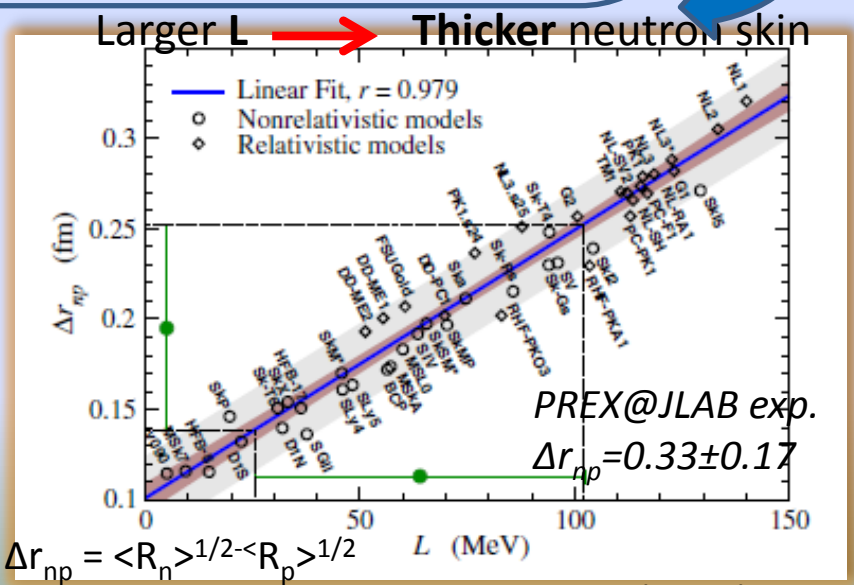
Neutron star  
 $\approx 10^4$  m



Neutron skin in  $^{208}\text{Pb}$   
 $\approx 10^{-15}$  m



S. Gandolfi et al. EPJA 50:10 (2014)



Roca-Maza et al., PRL 106, 252501 (2011)



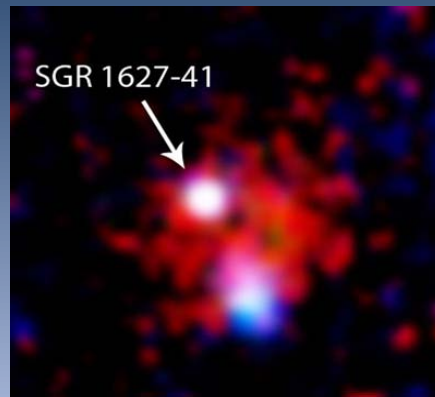
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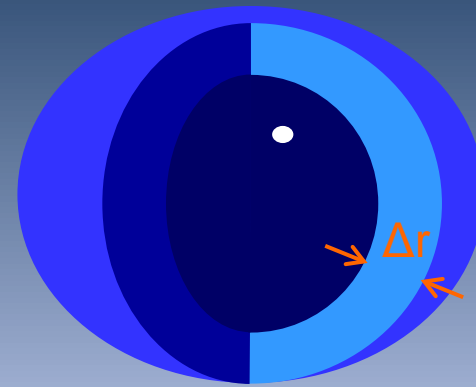
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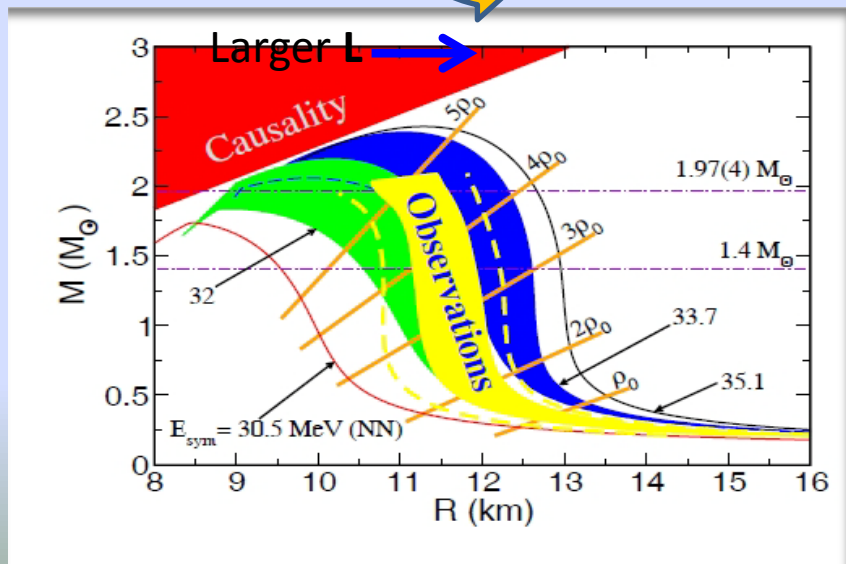
Pressure



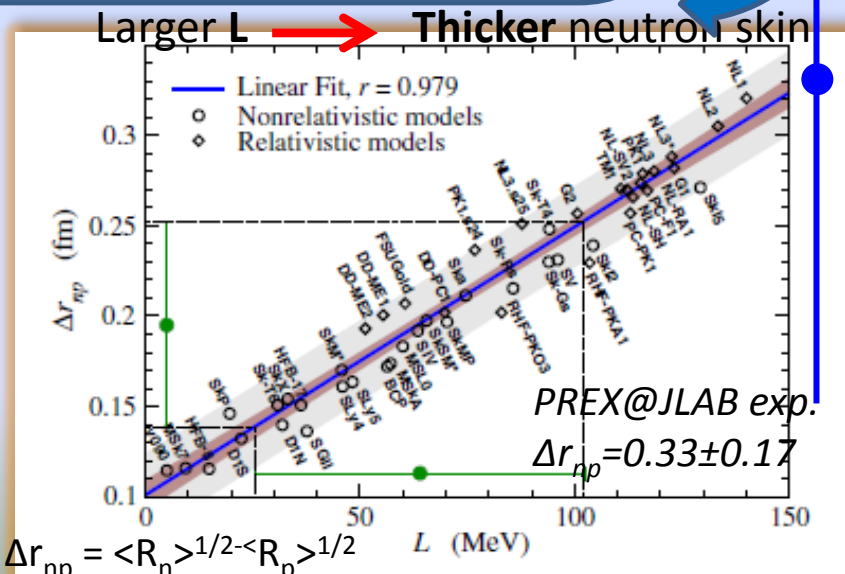
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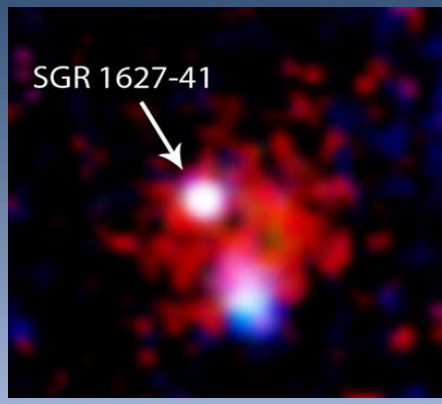
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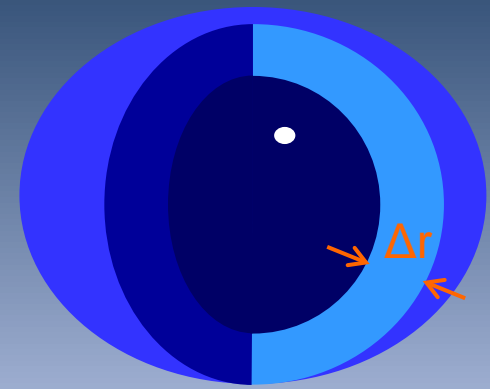
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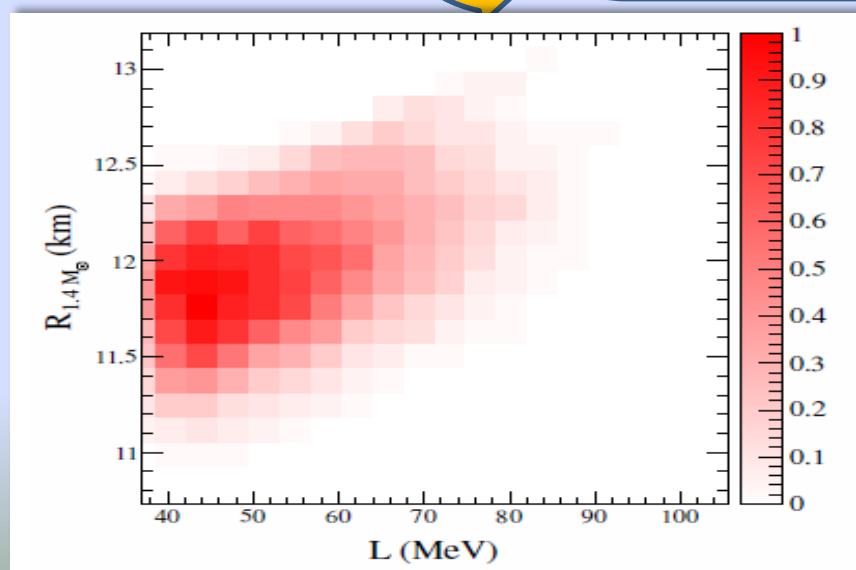
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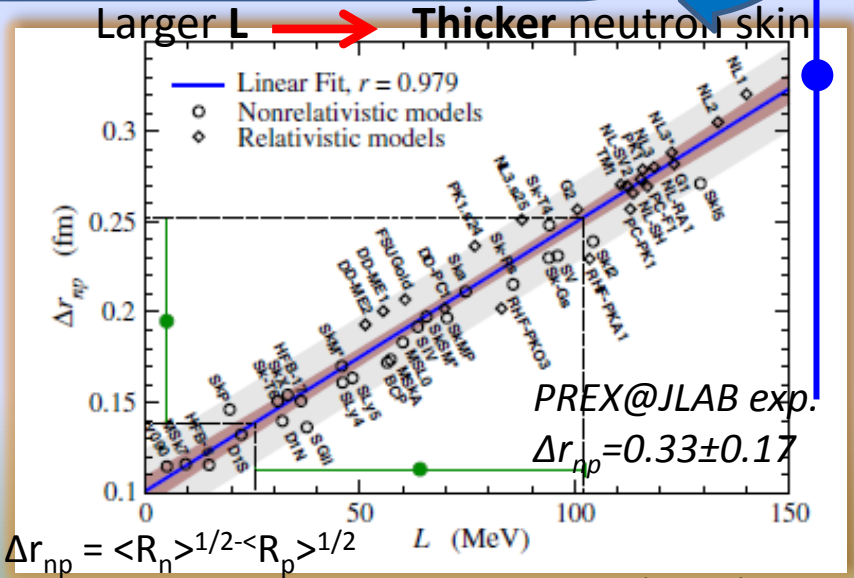
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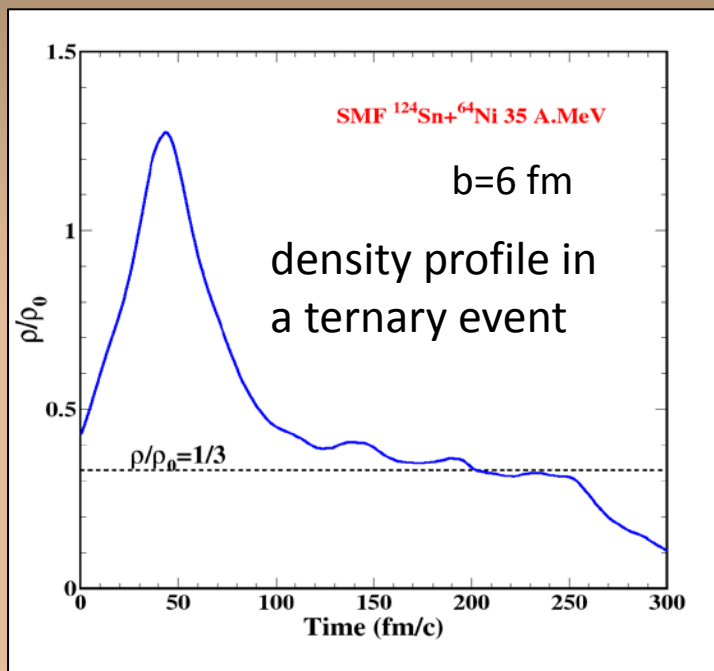


Roca-Maza et al., PRL 106, 252501 (2011)

# Symmetry energy and heavy ion collisions (HIC): Why ?

With heavy ion collisions it is possible to access nuclear matter from low densities ( $\rho \leq \rho_0$ , Fermi energies) to high densities ( $\rho = 2-3\rho_0$ )

SMF  $^{124}\text{Sn} + ^{64}\text{Ni}$  35 A.MeV

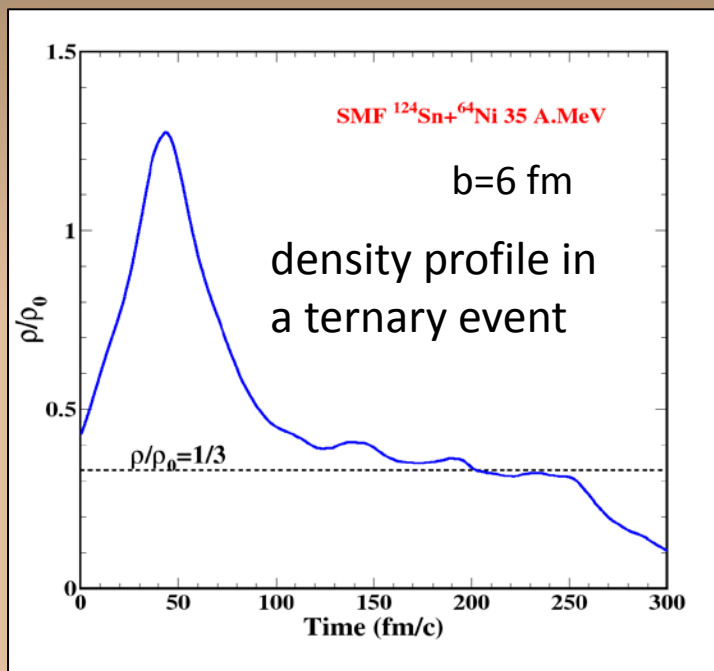


With HIC large density variations (density gradients) in nuclear matter can be obtained in a short timescale.

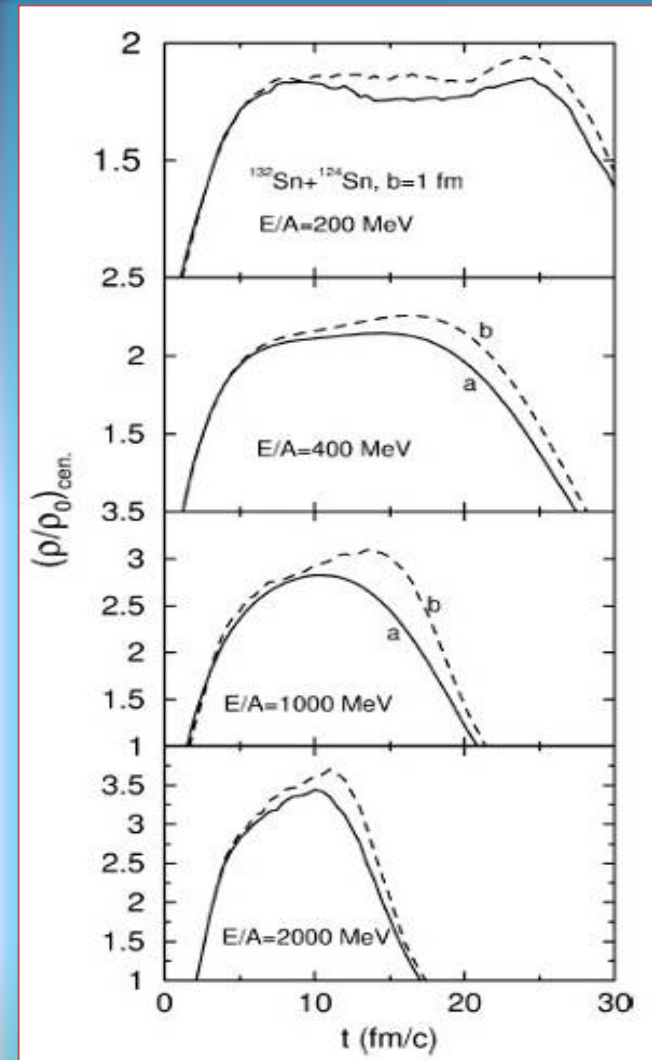
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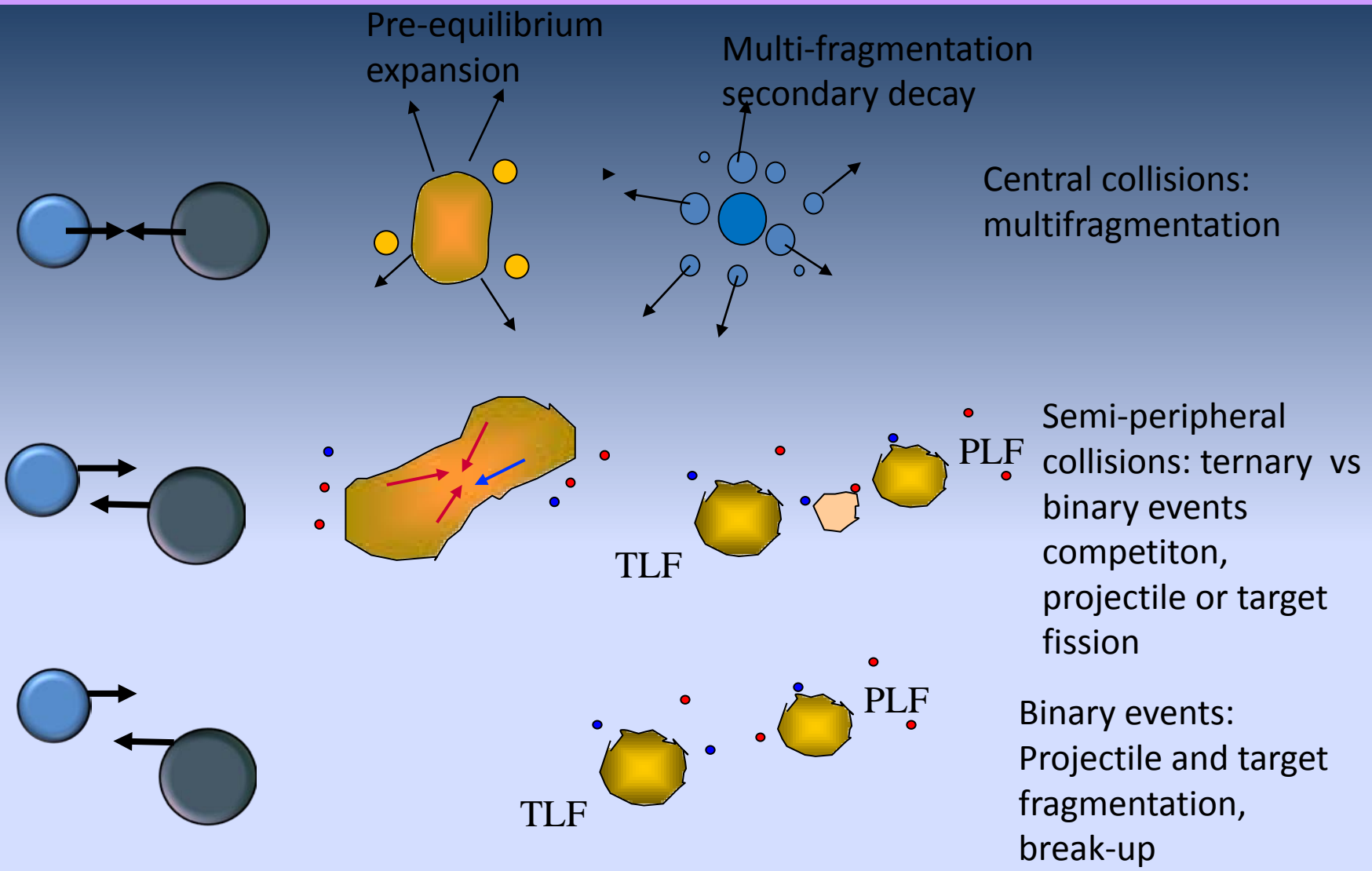
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Bao-An Li, NPA 708 365 (2002)

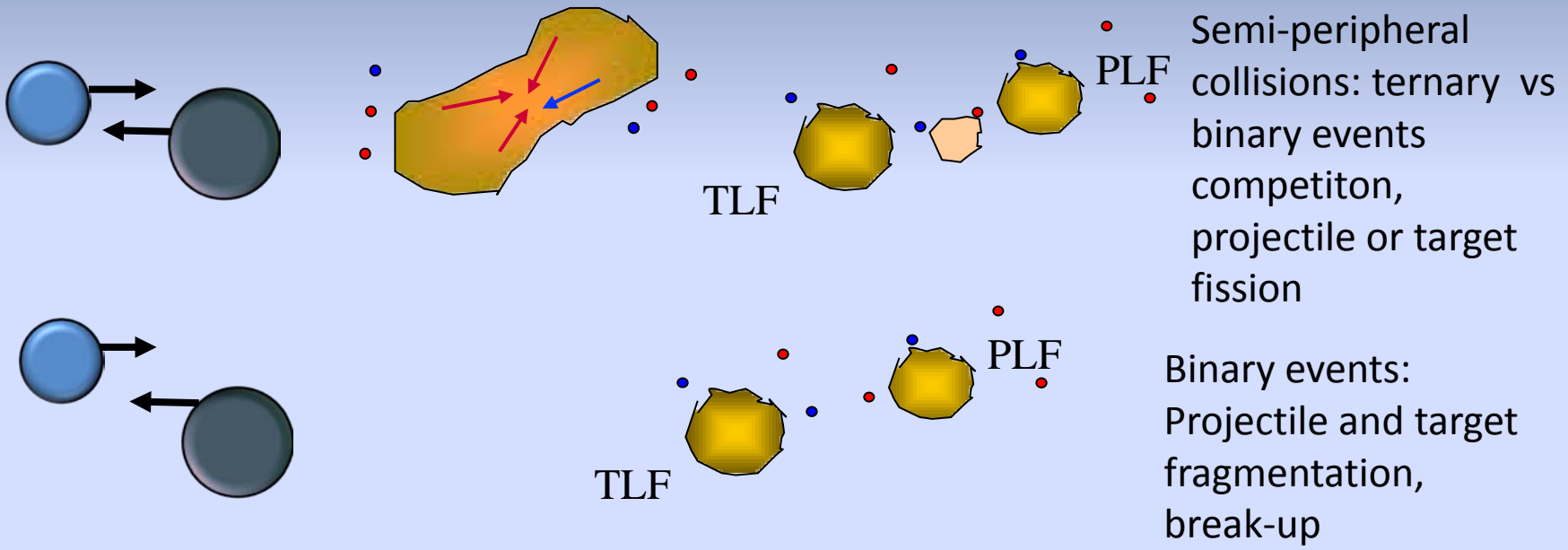
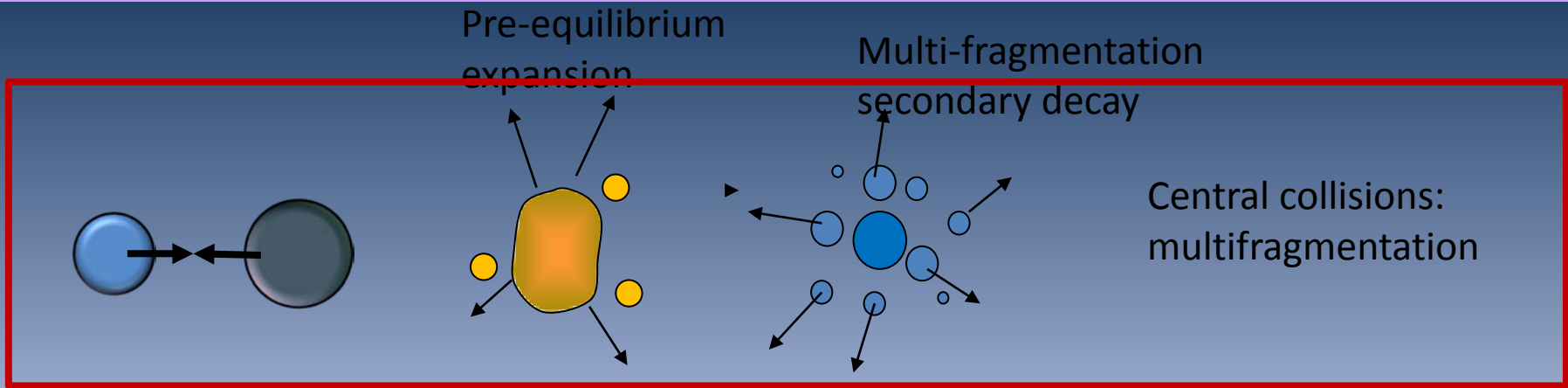


# Heavy ion collisions at Fermi energies: **different scenarios and mechanisms**



Particle emissions from the early phase of the dynamical evolution (**few fm/c**) up to later stages of statistical decay (**several hundreds of fm/c**) have been measured and are expected to coexist in the reaction products.

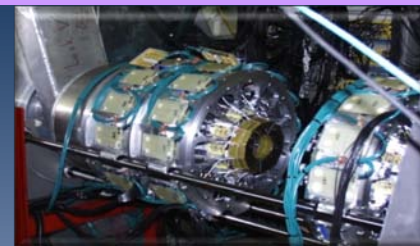
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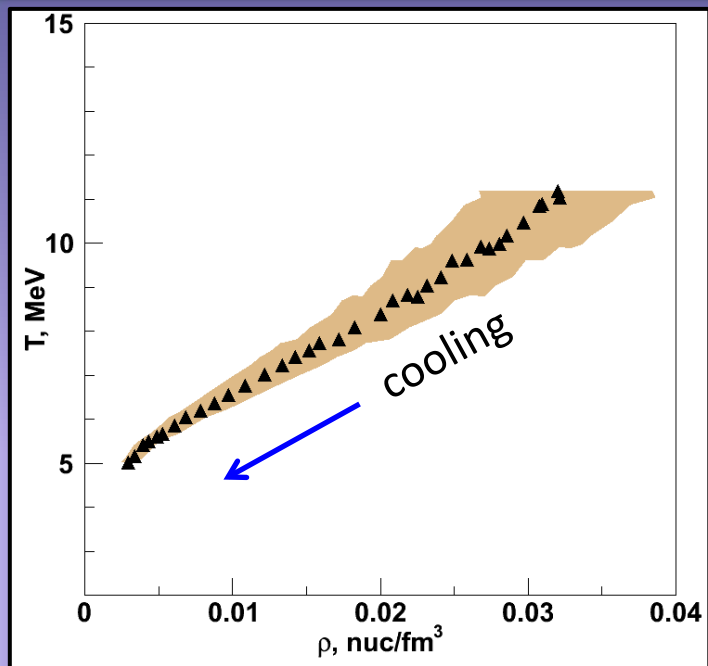
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# Nuclear matter symmetry energy at low density ( $\rho/\rho_0 \leq 0.2$ )

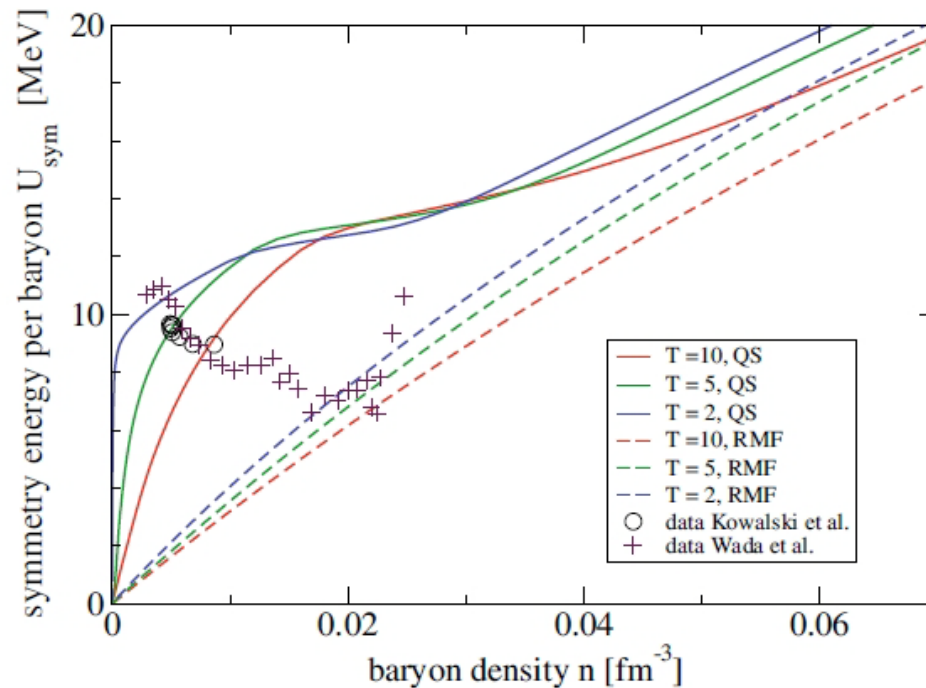
Temperature and density determination from intermediate velocity source in  $^{40}\text{Ar}, ^{64}\text{Zn} + ^{112,124}\text{Sn}$  at 47 A.MeV



NIMROD@TAMU



## Formation of light clusters at very low densities



- R. Wada et al., PRC85, 064618 (2012)
- J.B. Natowitz et al., PRL 104 202501 (2010)
- K. Hagel et al., EPJA 50:39 (2014)

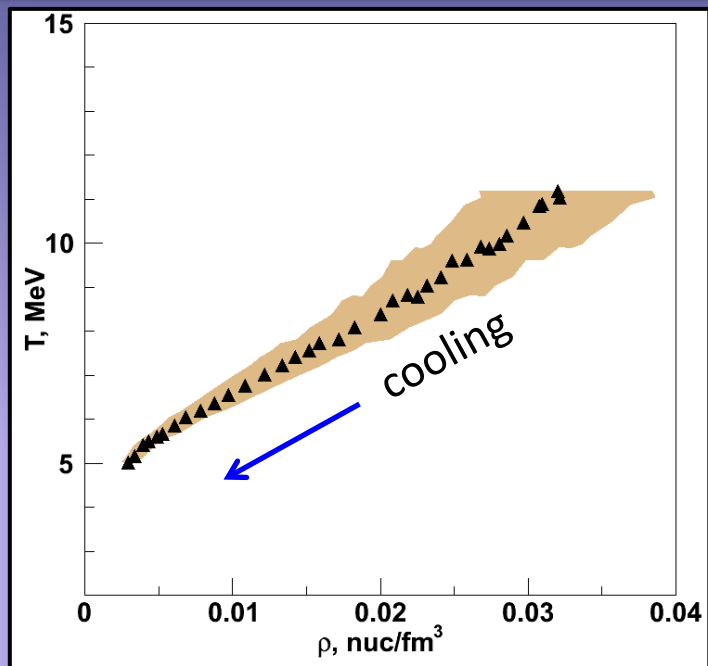
QS = Quantum Statistical model including clusterization by Typel, Roepke et al.,  
RMF = Relativistic mean field approaches

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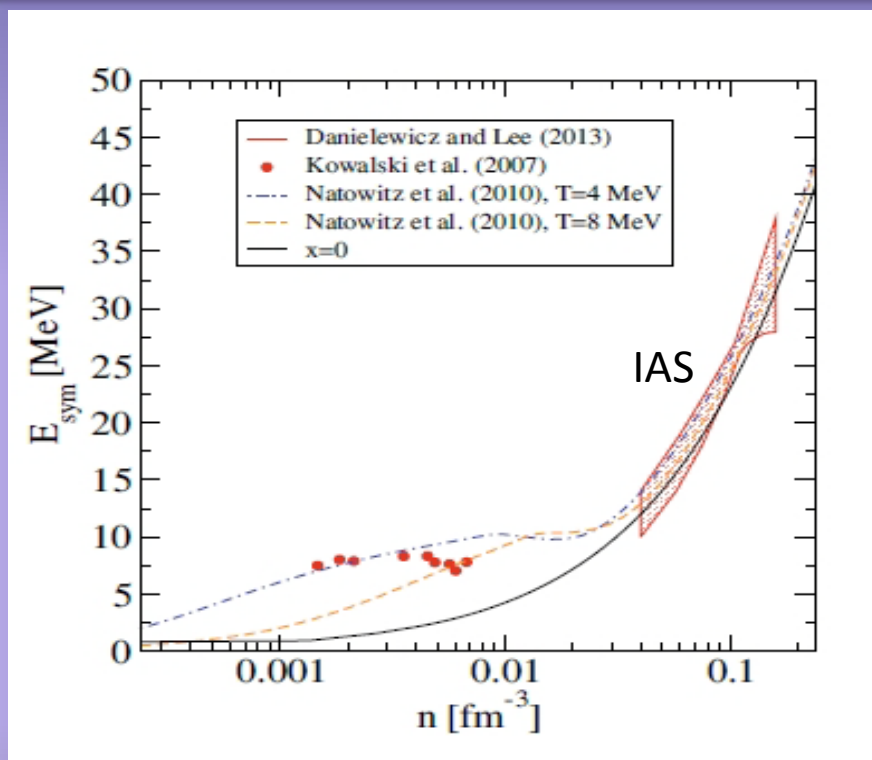
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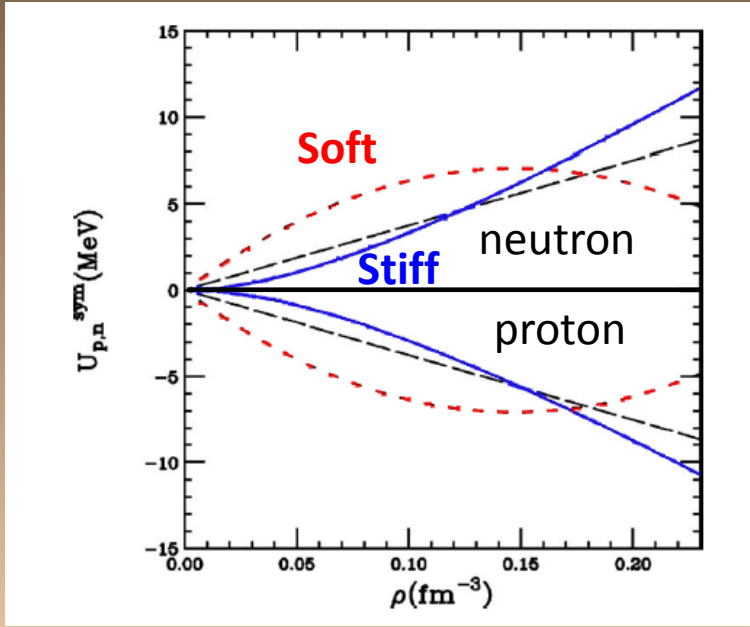
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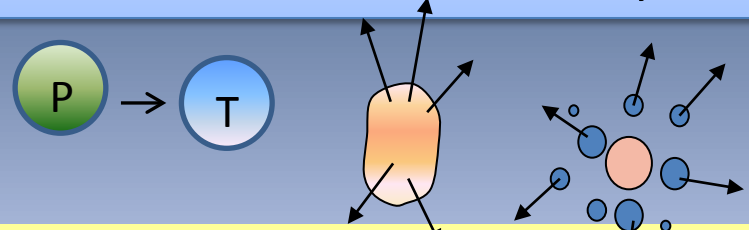
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# Pre-equilibrium nucleons: n/p and scalings laws for clusters



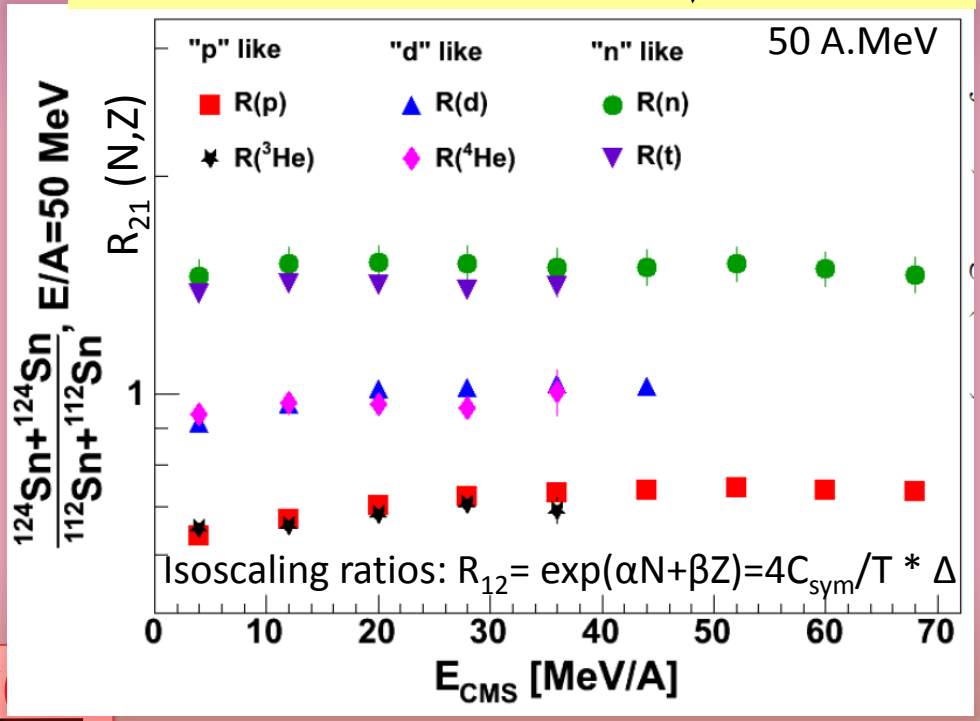
The idea is to look to the ratio of neutron/proton yield in central collisions (energy spectra of transversely emitted nucleons around  $90^\circ$  in the c.m. system.)



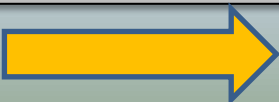
Adapted from Z Chajecki et al., ArXiv:1402:521 (2014)

V. Baran et al. *Phys. Rep.* 410, (2005)  
 Skyrme-like form for mean-field potential seen by protons and neutrons for  $^{124}\text{Sn}$

**Double Ratio  $R(n/p)$  minimizes systematic errors, efficiency problems, etc**

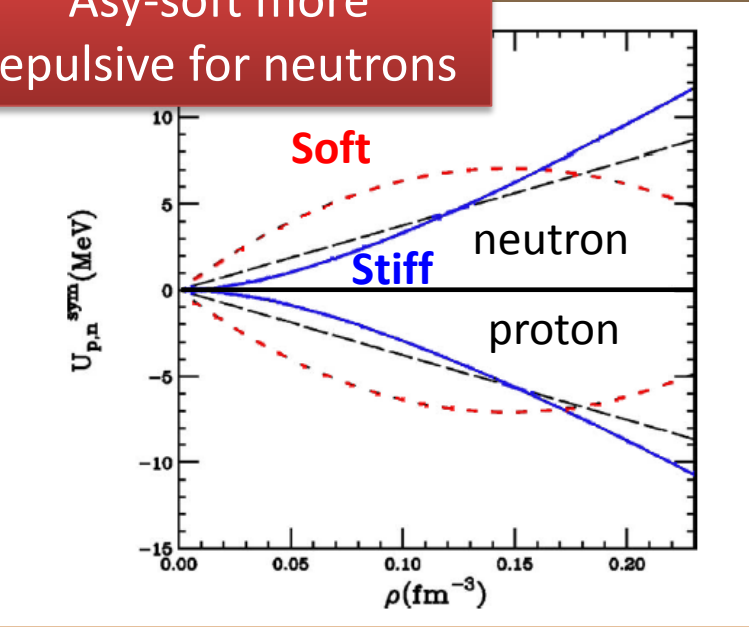


Neutron rich  $Y(n)/Y(p)$   
 Neutron poor  $Y(n)/Y(p)$

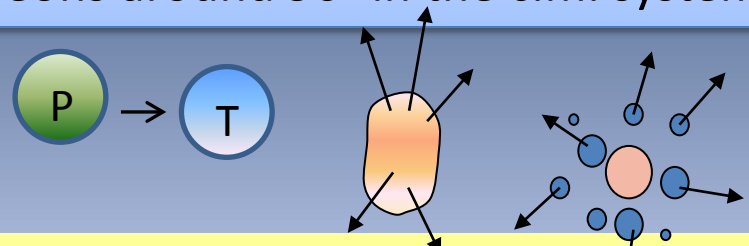


# Pre-equilibrium nucleons: n/p and scalings laws for clusters

Asy-soft more repulsive for neutrons



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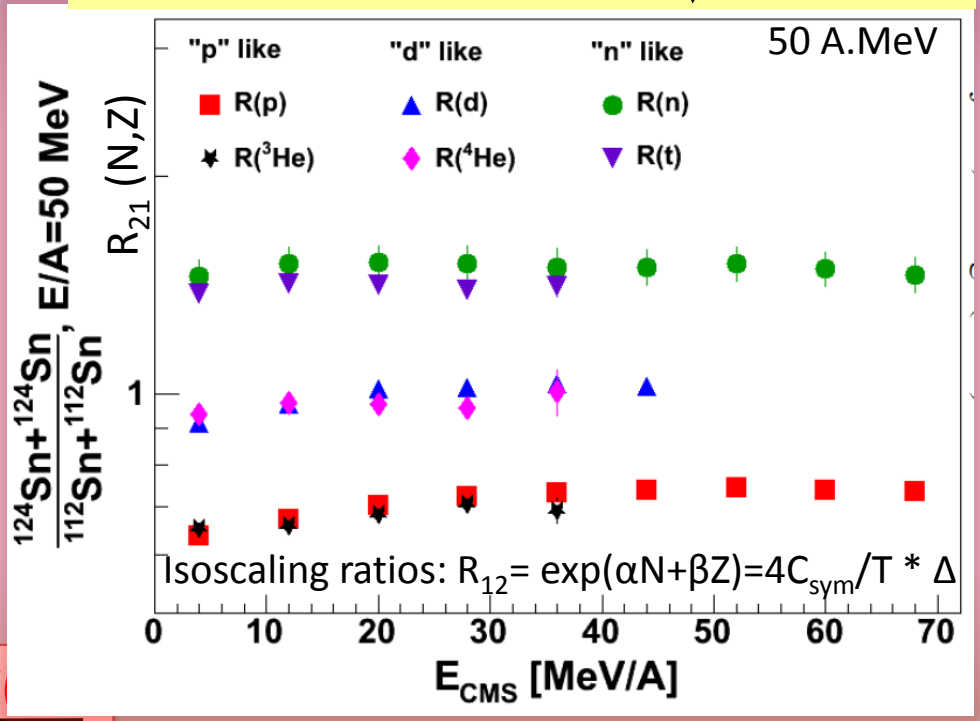


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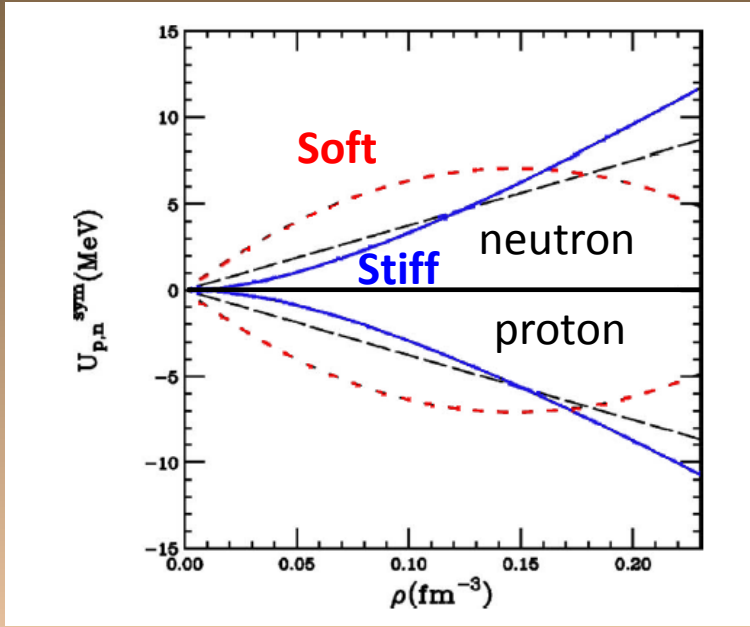
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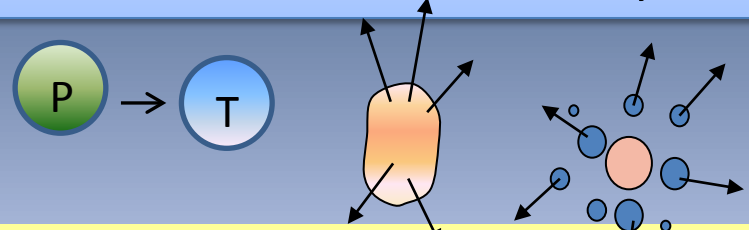
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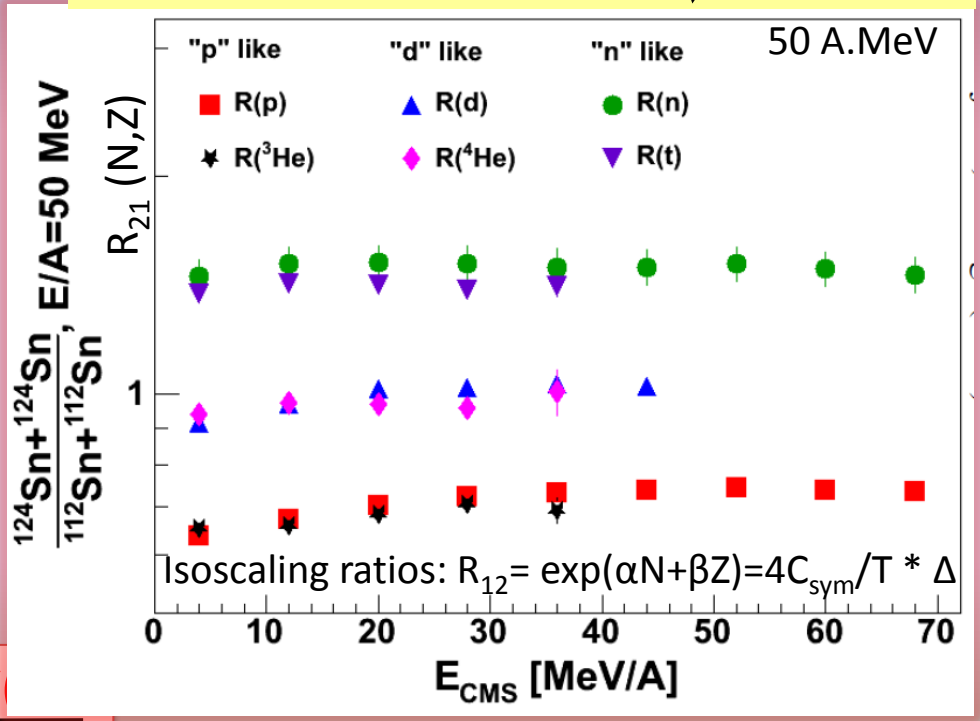
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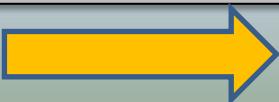
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# Neutron – Protons ratio (pre-equilibrium nucleons)

Nucleons are mostly emitted when system expands and breaks-up at subsaturation densities.

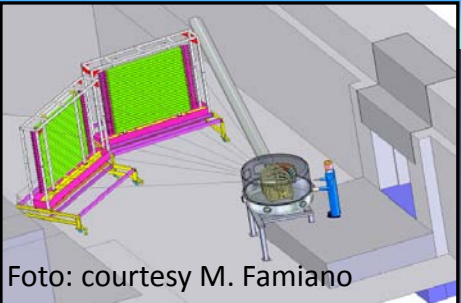
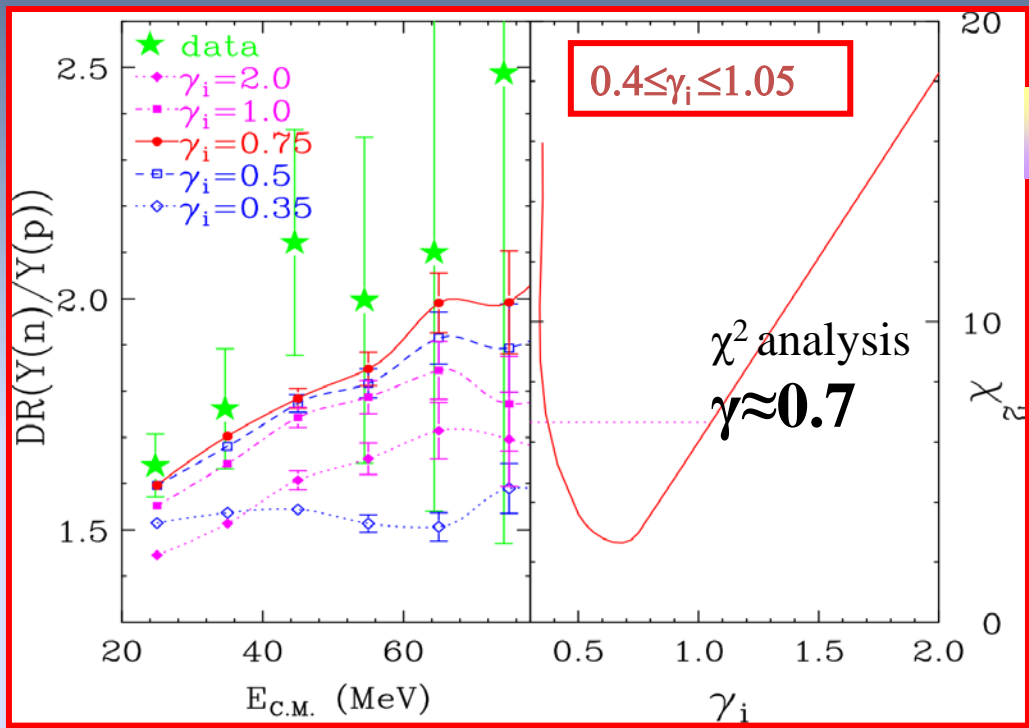


Foto: courtesy M. Famiano

LASSA+MBall + NEUTRON WALL@MSU

M. Famiano et al. data



$$S(\rho) = 12.3 \cdot (\rho / \rho_0)^{2/3} + 17.6 \cdot (\rho / \rho_0)^\gamma$$

M.B. Tsang et al., PRL 102 122701 (2009)

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**ImQMD** model with  $\gamma$  between 0.35 and 2.0 (momentum dependent mean field)



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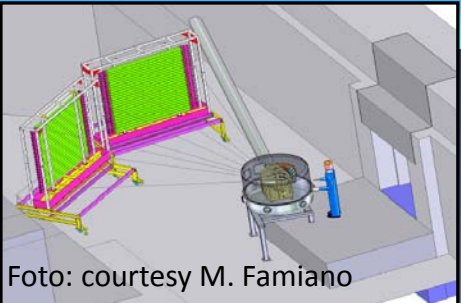
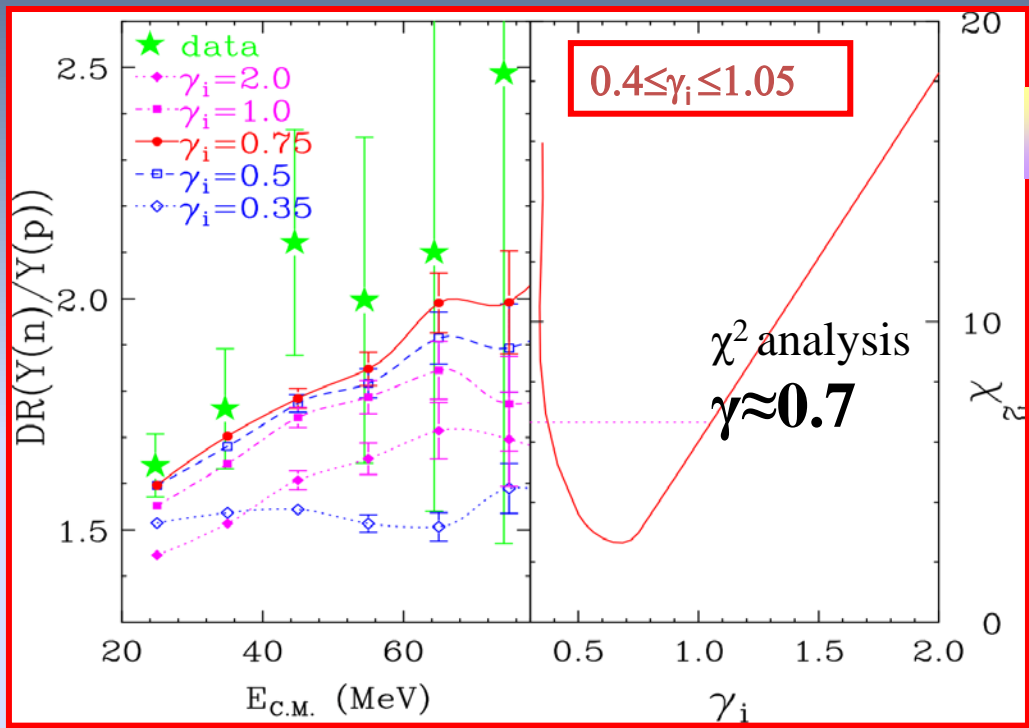


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see J. Rizzo et al., PRC72 064609

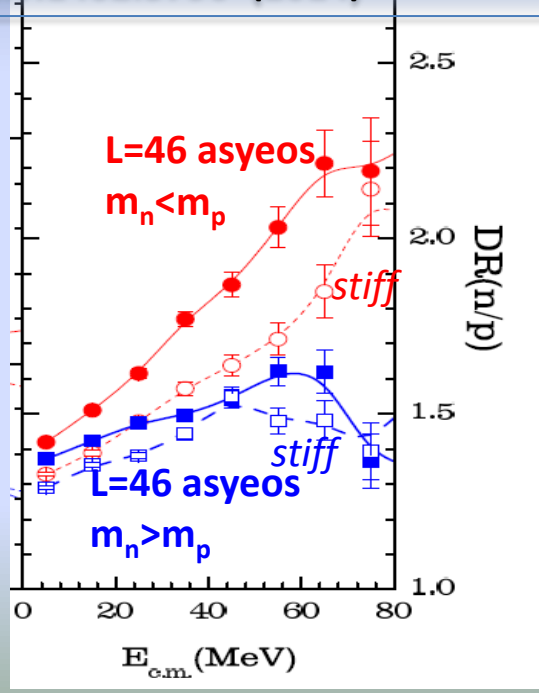
Adapted from Zhang et al  
ArXiv:1402.3790 (2014)

M.B. Tsang et al., PRL 102 122701 (2009)

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ImQMD model with  $\gamma$  between 0.35 and 2.0 (momentum dependent mean field)

But: **WARNING!!**  
The role of effective masses can give effects comparable to that of symmetry energy



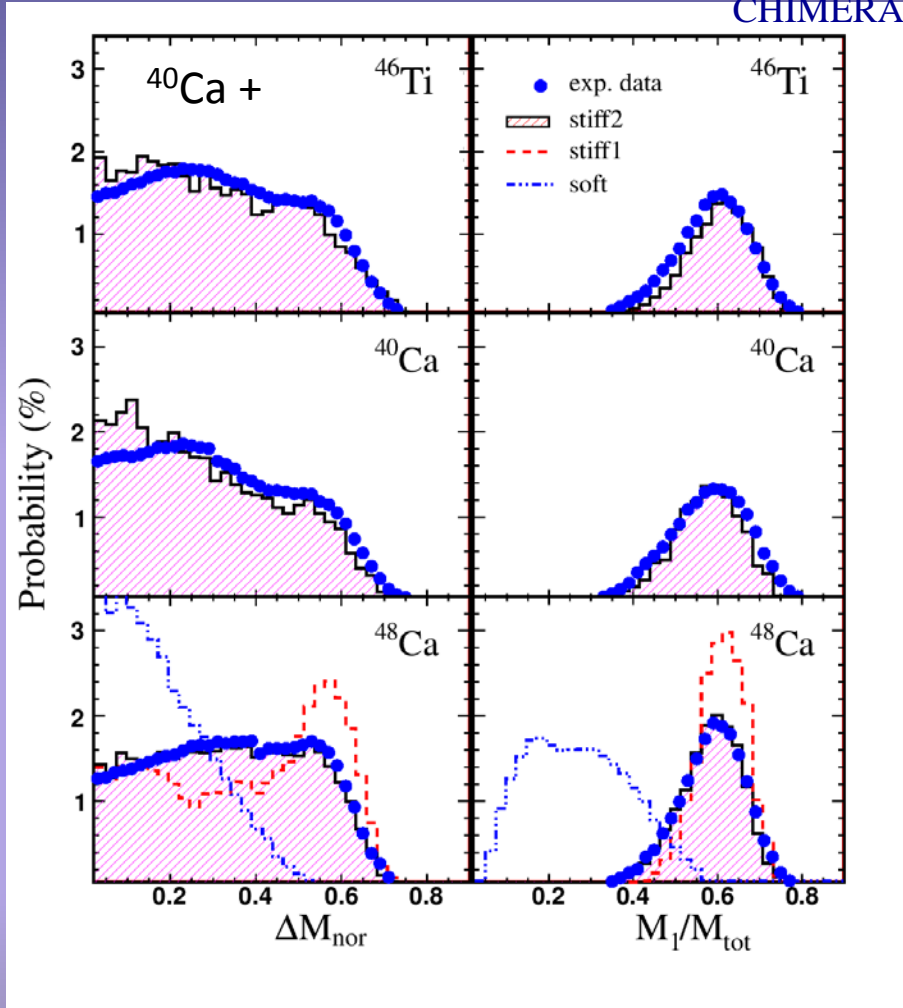
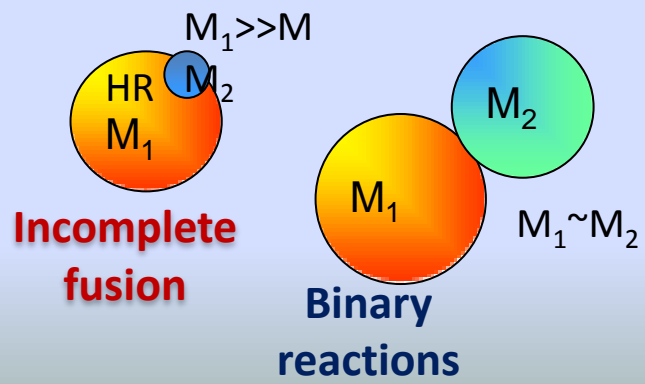
# Competition of reaction mechanisms

N/Z effects in competition between binary reactions and incomplete fusion. Higher probability for fusion using neutron rich systems

$^{48}\text{Ca}+^{48}\text{Ca}$   $^{40}\text{Ca}+^{48}\text{Ca}$   
 $^{48}\text{Ca}+^{40}\text{Ca}$   $^{40}\text{Ca}+^{40}\text{Ca}$   
 25 A.MeV



CHIMERA @ LNS



G. Cardella et al., PRC 85 084609 (2012)  
 F. Amorini et al., PRL102, 112, 701 (2009)

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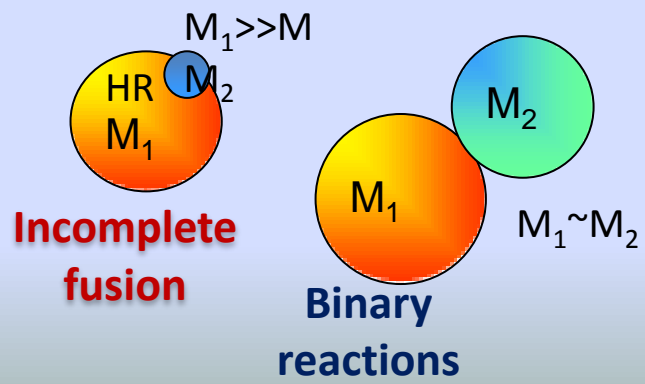
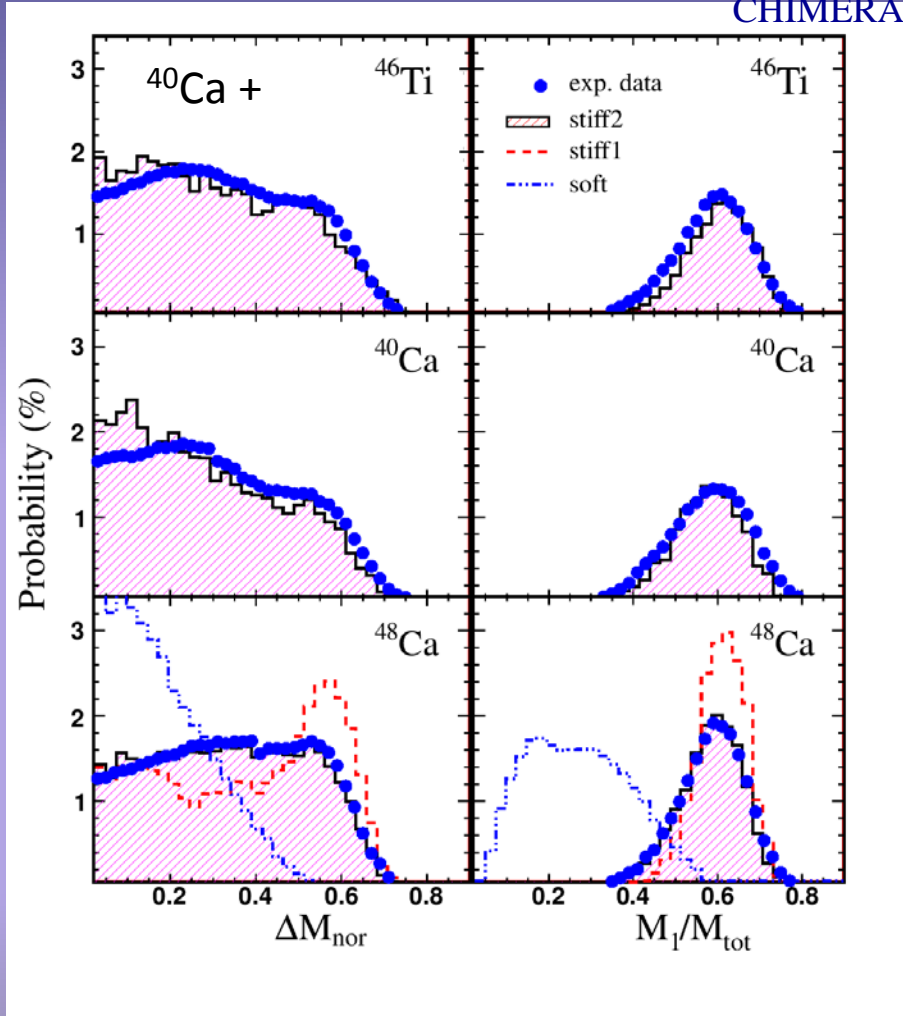
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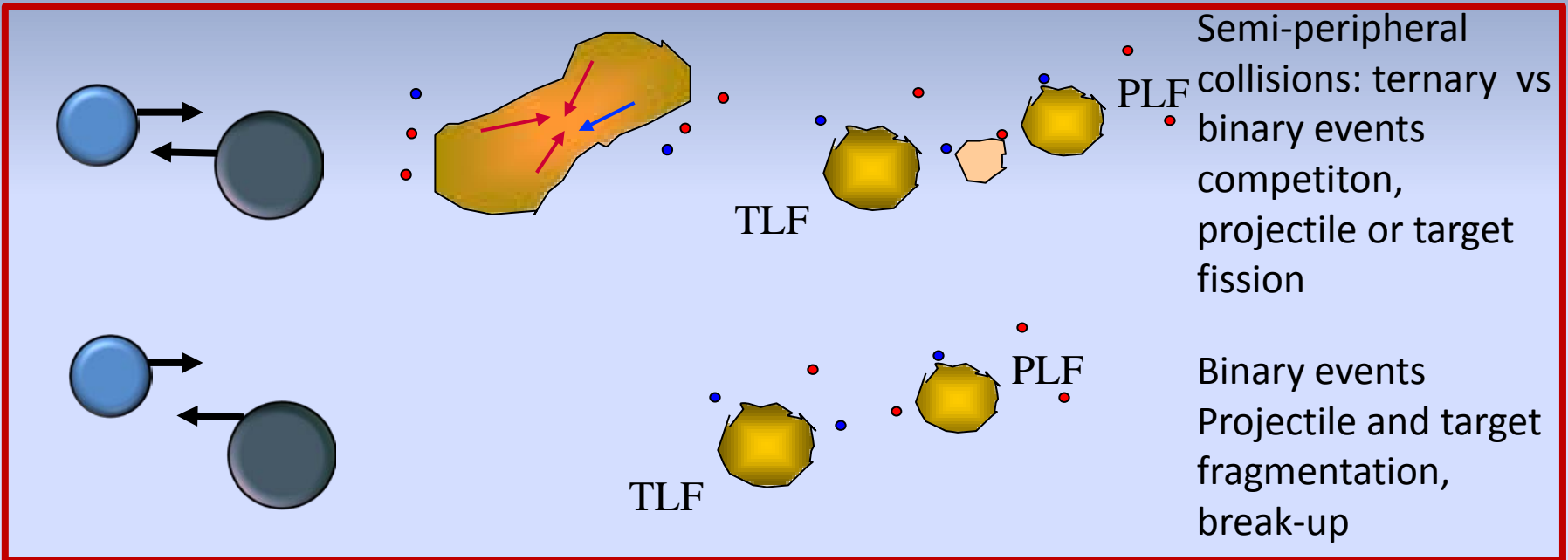
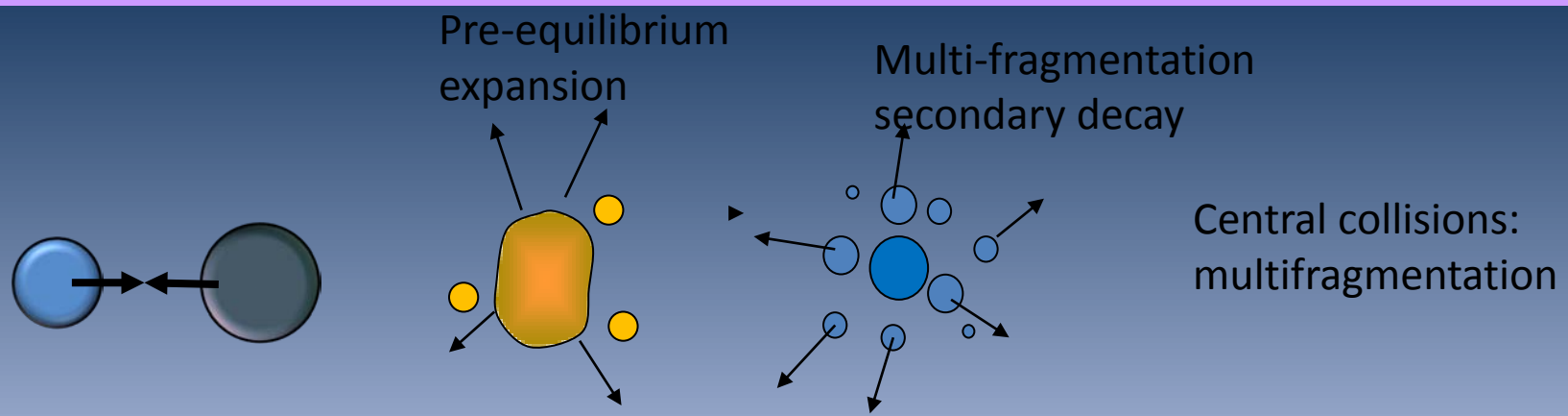
CHIMERA @ LNS

Comparison with **CoMD** model (*M. Papa et G. Giuliani, EPJA 39, 17 (2009)*): the good matching with experimental data is obtained by a stiff symmetry energy term ( $\gamma = 1.1 \pm 0.1$ )



*G. Cardella et al., PRC 85 084609 (2012)*  
*F. Amorini et al., PRL102, 112, 701 (2009)*

# Heavy ion collisions at Fermi energies: different scenarios and mechanisms

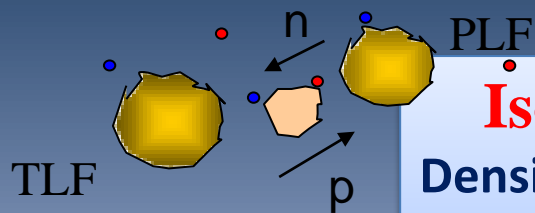


Semi-peripheral events are characterized by binary reactions where projectile and target nuclei experience a substantial overlap of matter.



# Isospin transport through the "neck"

V. Baran et al., PRC 72 064620 (2005)

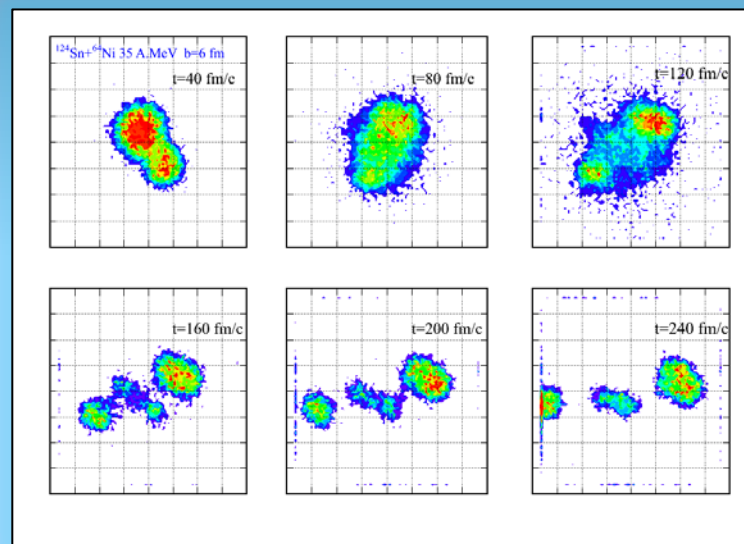
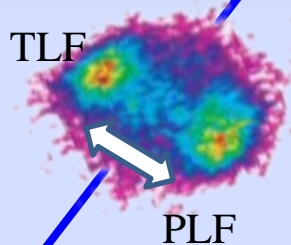


## Isospin drift (fast timescale: around 100 fm/c)

### Density gradient

Depending on slope of the symmetry energy  
Migration of neutrons in low density region

$$j_n - j_p \propto E_{sym}(\rho) \nabla I + \frac{\partial E_{sym}(\rho)}{\partial \rho} I \nabla \rho$$



## Isospin diffusion

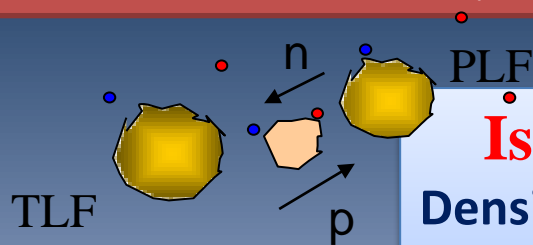
**Isospin gradient** (N/Z asymmetry in the initial system)

Depending on absolute value of the symmetry energy

Isospin equilibration between projectile and target

# Isospin transport through the “neck”

V. Baran et al., PRC 72 064620 (2005)

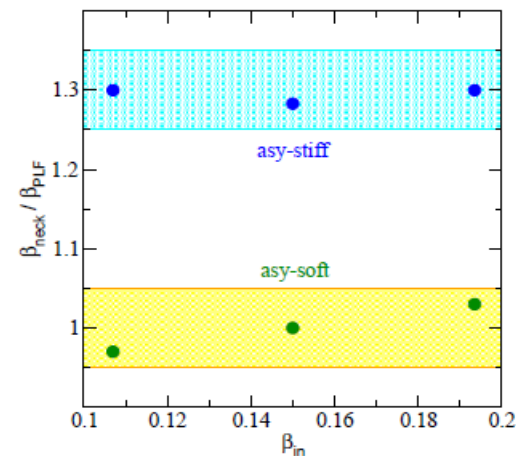
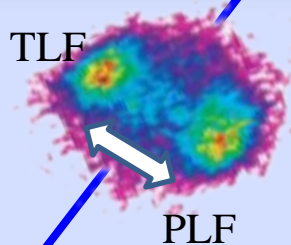


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M. Colonna et al., J. Phys. CS, 413, 012018 (2013)

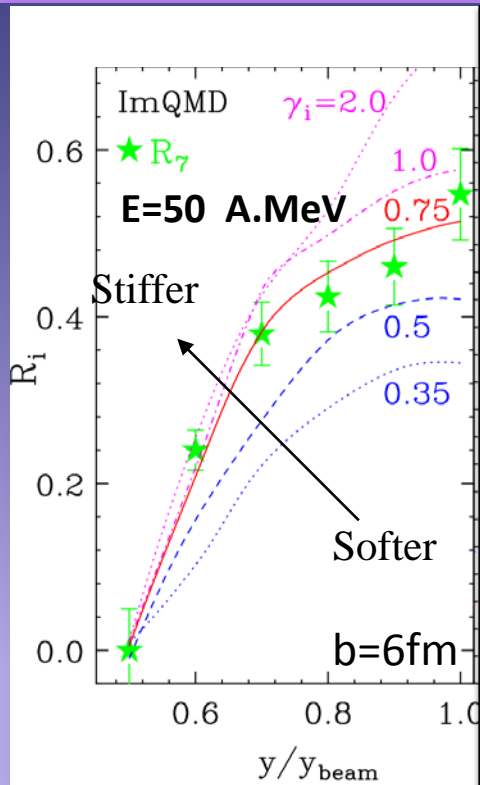
## Isospin diffusion

**Isospin gradient** (N/Z asymmetry in the initial system)

Depending on absolute value of the symmetry energy

Isospin equilibration between projectile and target

# Isospin diffusion → diffusion of neutrons and protons across the neck



Comparison with ImQMD model (Best fit obtained with  $\gamma=0.75$  at  $b=6$  fm.

Results of  $\chi^2$  analysis on compared isospin diffusion and n/p ratios data:

$0.45 \leq \gamma \leq 1$   
 $50 \leq L \leq 85$  MeV

$^{124}\text{Sn} + ^{112}\text{Sn}$  (AB) mixed → diffusion

$^{112}\text{Sn} + ^{124}\text{Sn}$  (BA) mixed → diffusion 50 A.MeV

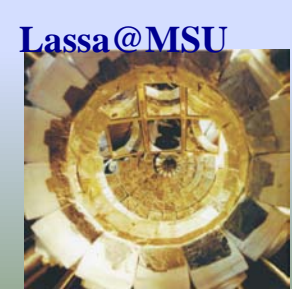
$$R_i(x_{AB}) = 2 \cdot \frac{x_{AB} - (x_{AA} + x_{BB})/2}{x_{AA} - x_{BB}}$$

$R_i = \pm 1$  no diffusion;  $R_i = 0$  equilibration

$X$  is an "isospin" observable and is rescaled according to  $R_i$  (transport ratio)

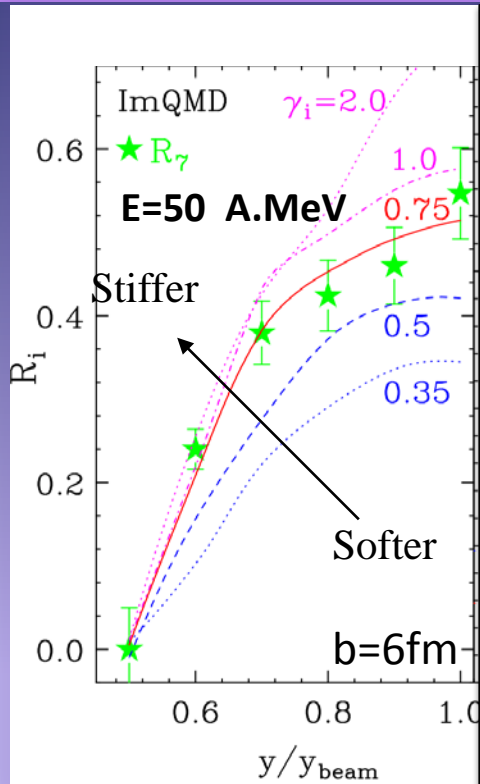
$$R_7 = f(Y(^7\text{Li})/Y(^7\text{Be}))$$

Isospin equilibration depends from  $S(\rho)$  value at subsaturation density and is favoured by a **SOFT** term of ASY-EOS. Less mixing with a **STIFF** asy-EOS.



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$$E_{\text{sym}} = E_{\text{sym}}^{\text{kin}} + E_{\text{sym}}^{\text{pot}}$$

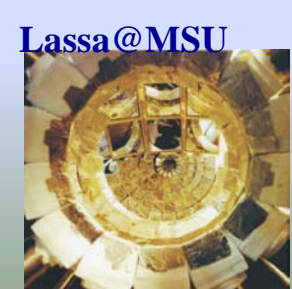
$$= 12\text{MeV} \cdot (\rho/\rho_0)^{2/3} + 22\text{MeV} \cdot (\rho/\rho_0)^\gamma$$

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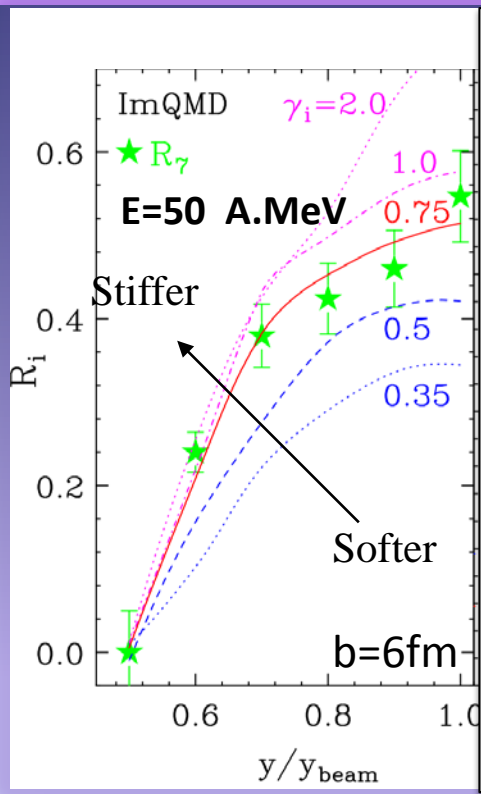
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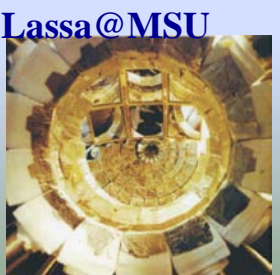
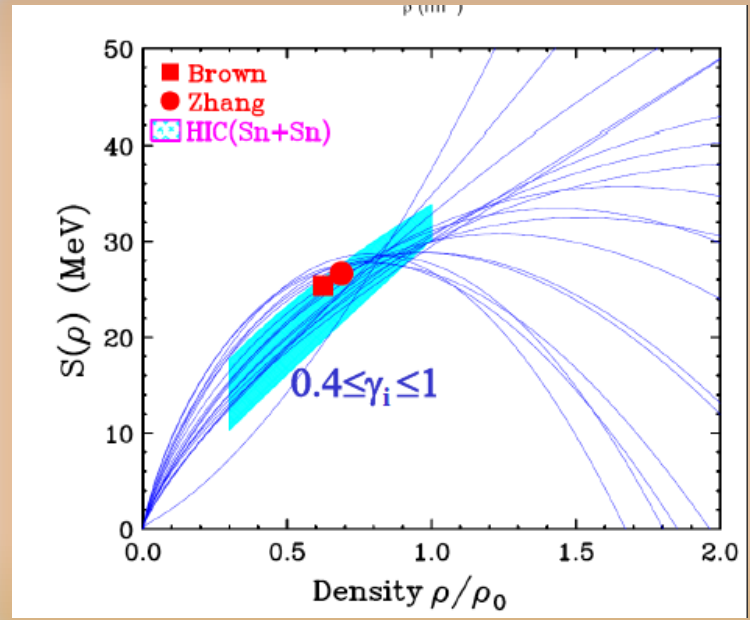
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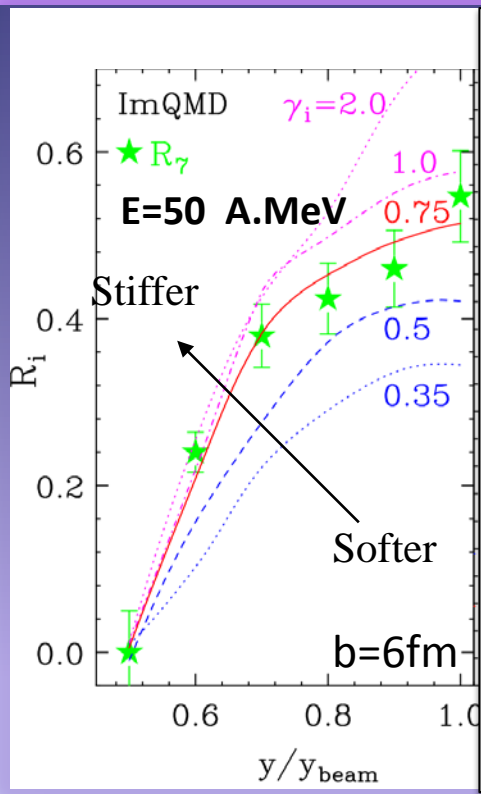
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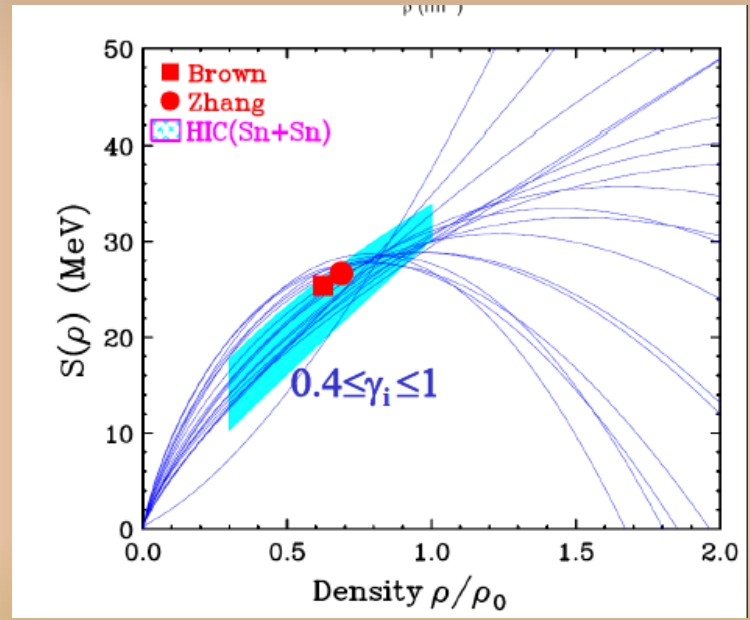
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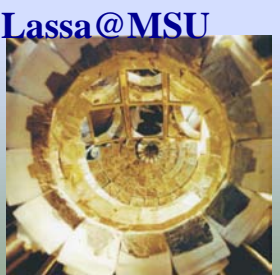
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Improvement with RIBS



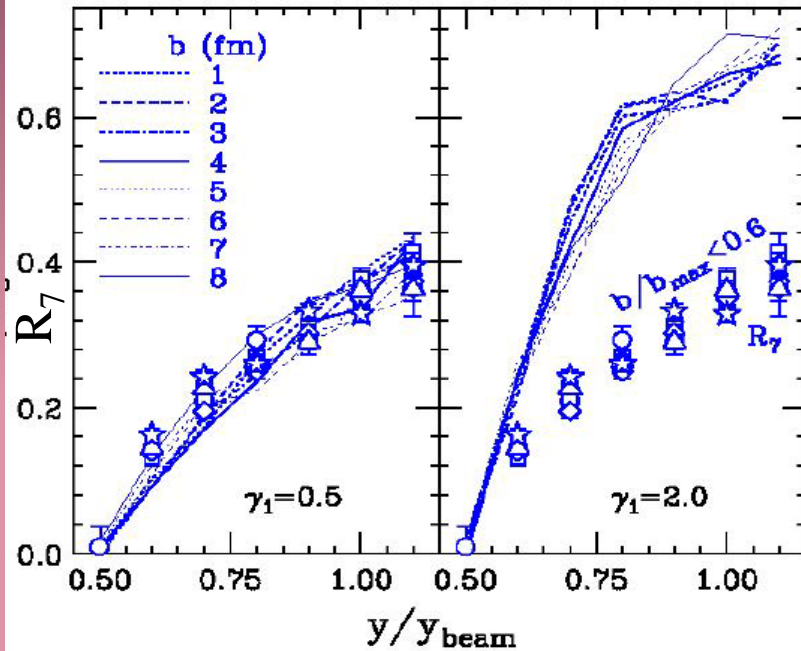
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# Isospin diffusion: Sn+Sn@35 A.MeV

Z.Y. Sun et al, CHIMERA-MSU  
collaboration PRC82, 051603 (2011)



CHIMERA@LNS

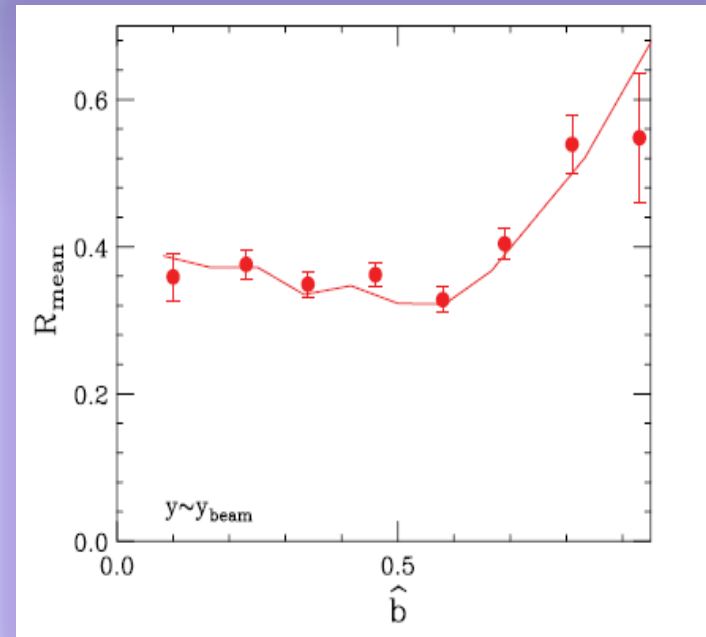
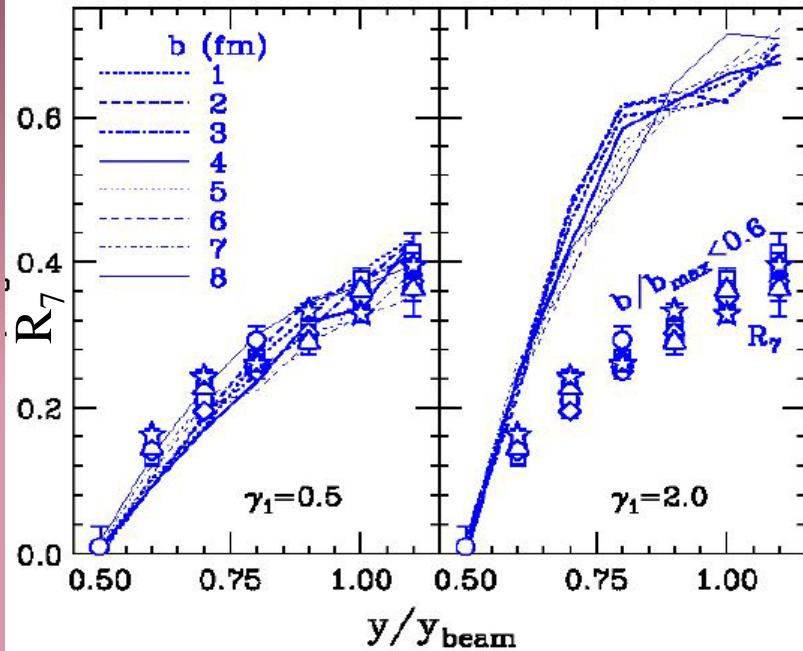


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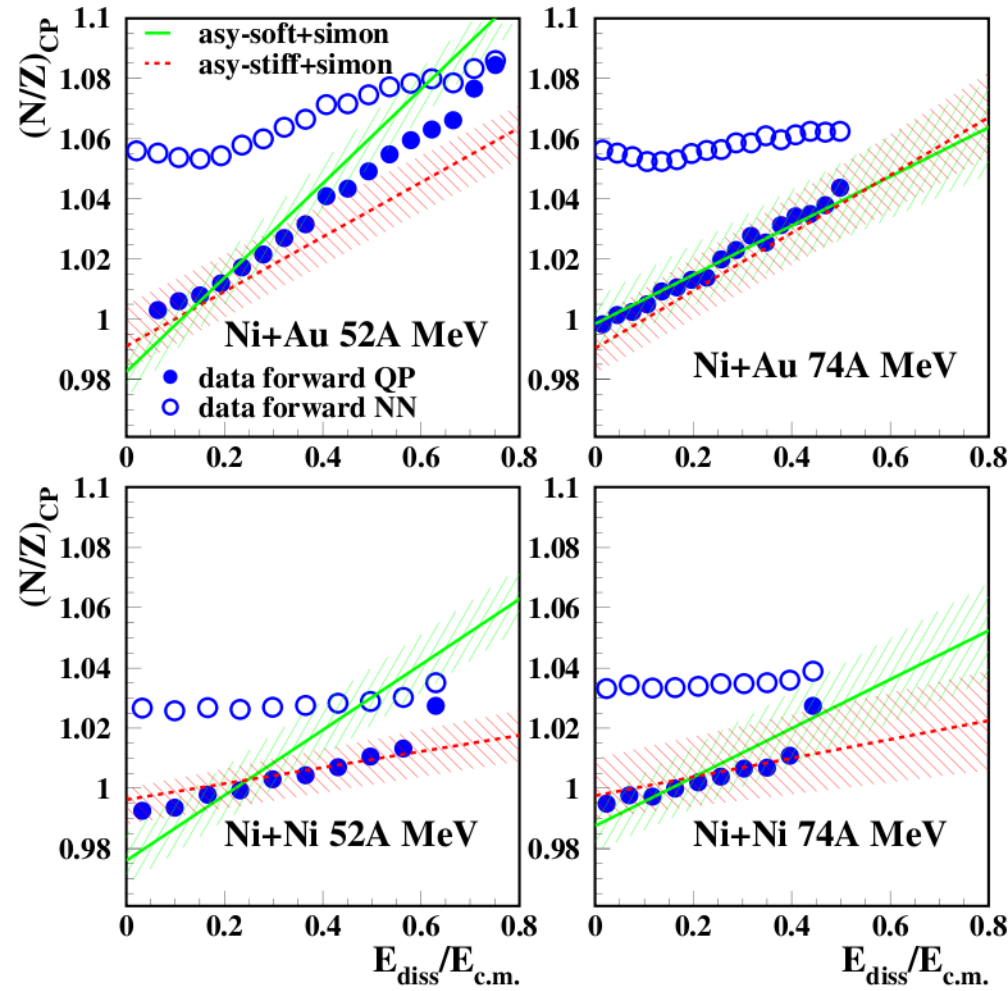
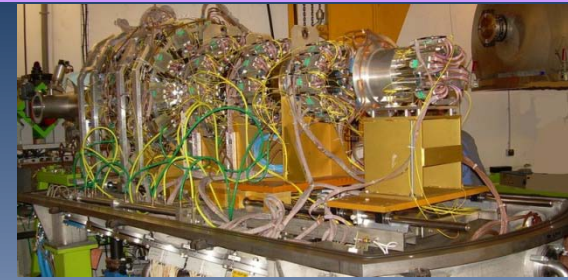
CHIMERA@LNS

Z.Y. Sun et al, CHIMERA-MSU  
collaboration PRC82, 051603 (2011)

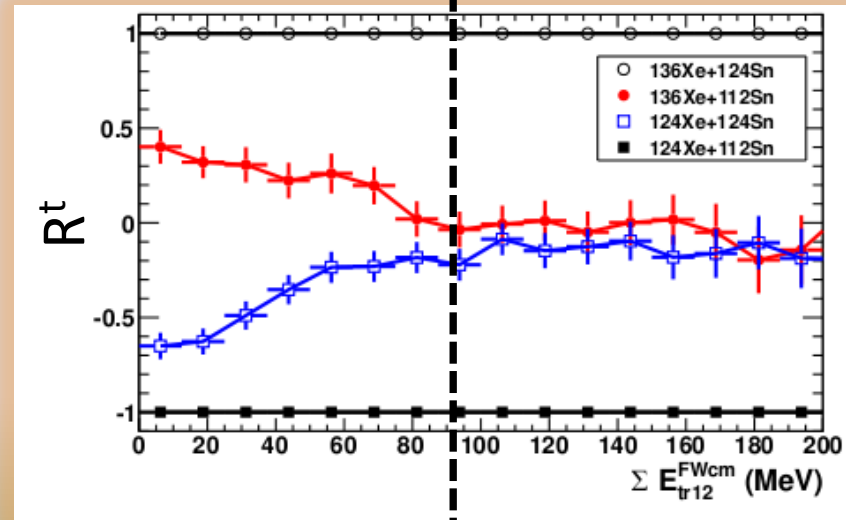


# Isospin transport by looking at the quasi-projectile

Indra@GANIL



Isospin equilibration is reached for more dissipative collisions. Here  $X$  (isospin variable in  $R^t$ ) = **triton multiplicity**



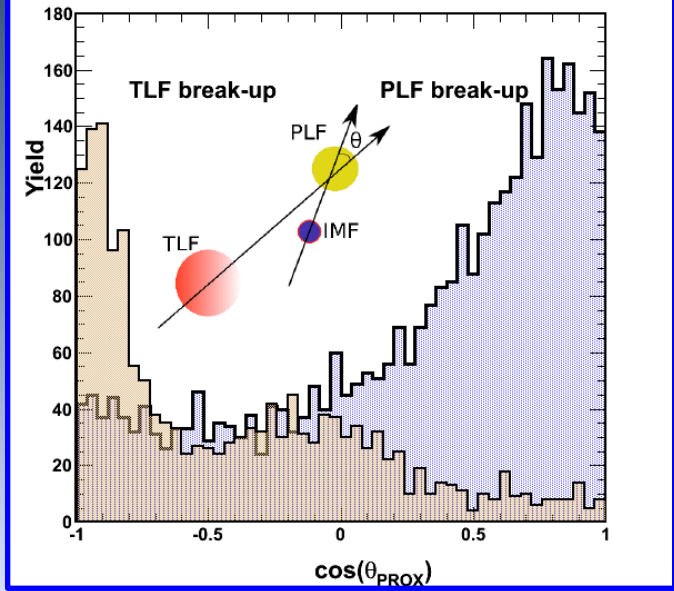
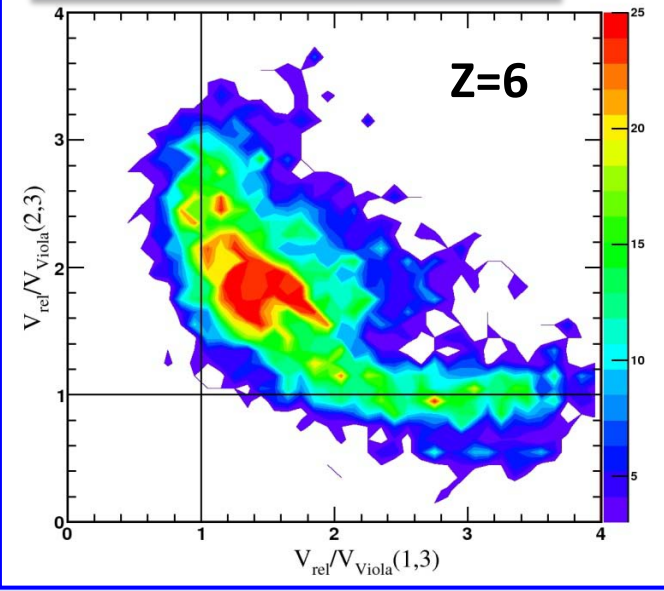
Data compared to Stochastic Mean Field (SMF) Asy-stiff parametrization better reproduce data

see E. Galichet et al., PRC79 064615 (2009)  
G. Ademard et al., EPJA 50:33 (2014)

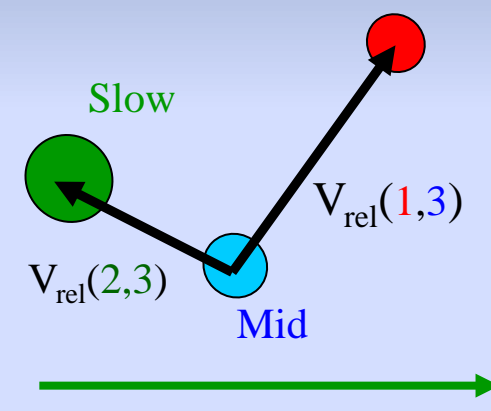
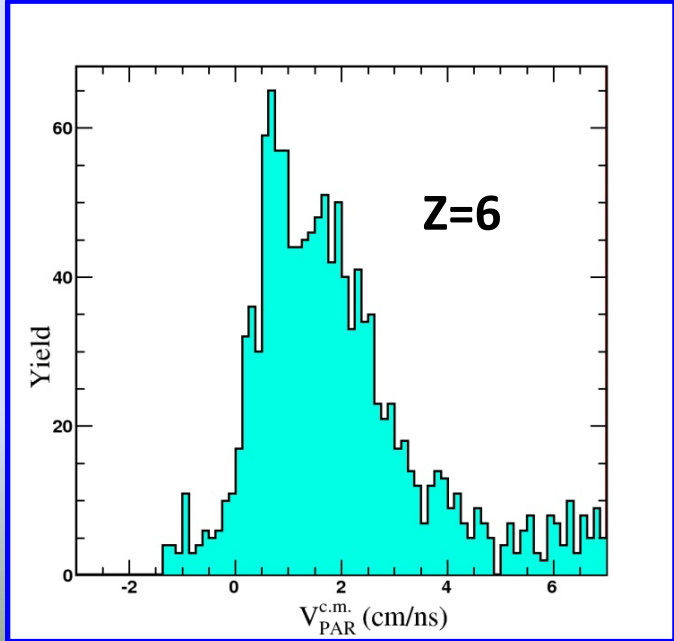
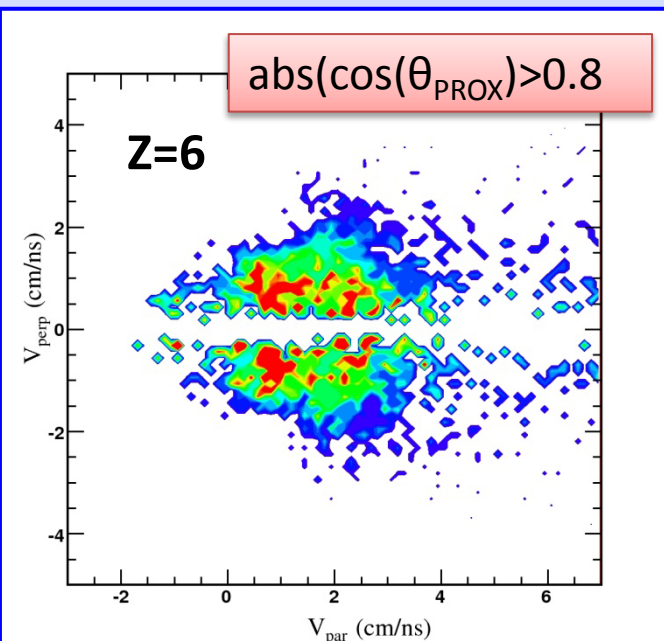


# Disentangling dynamical vs. statistical emission in ternary events

$^{64}\text{Ni} + ^{124}\text{Sn}$  35 A.MeV



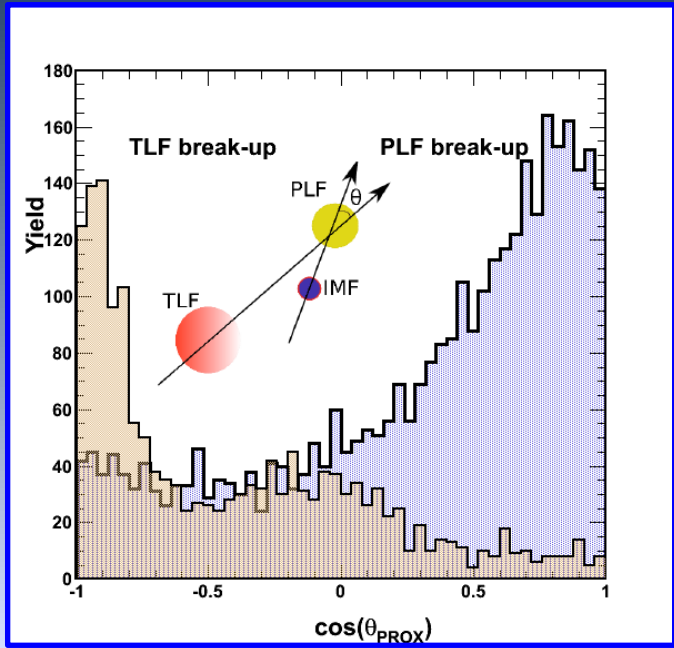
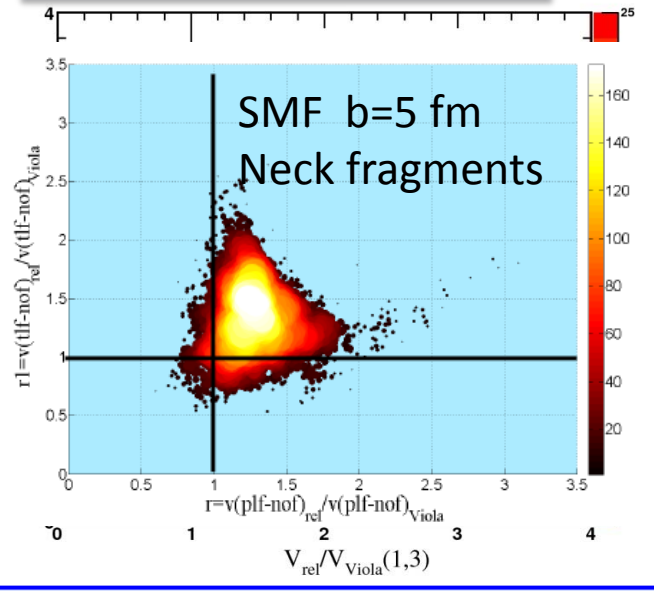
$\cos(\theta) \approx \pm 1$   
aligned emission of the lighter fragment in the backward hemisphere of **PLF** (+1) and **TLF** (-1) towards midrapidity



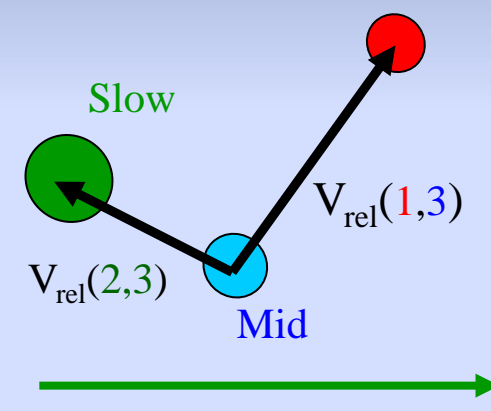
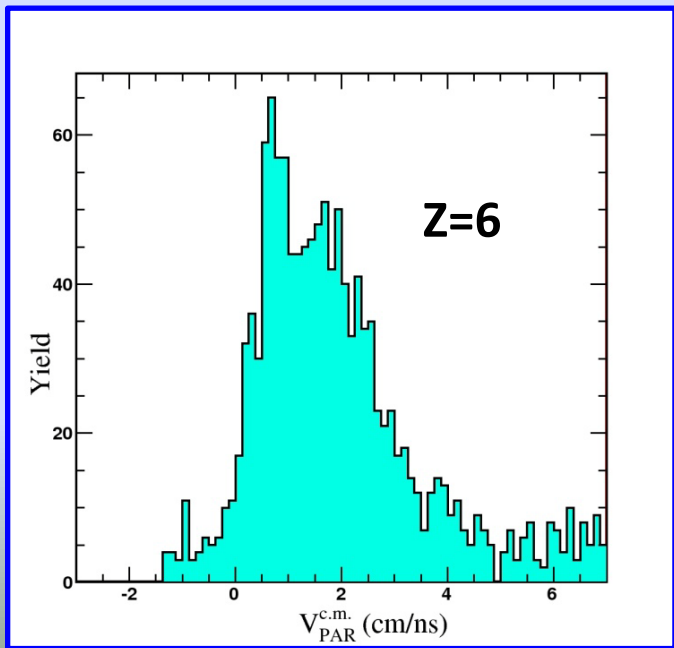
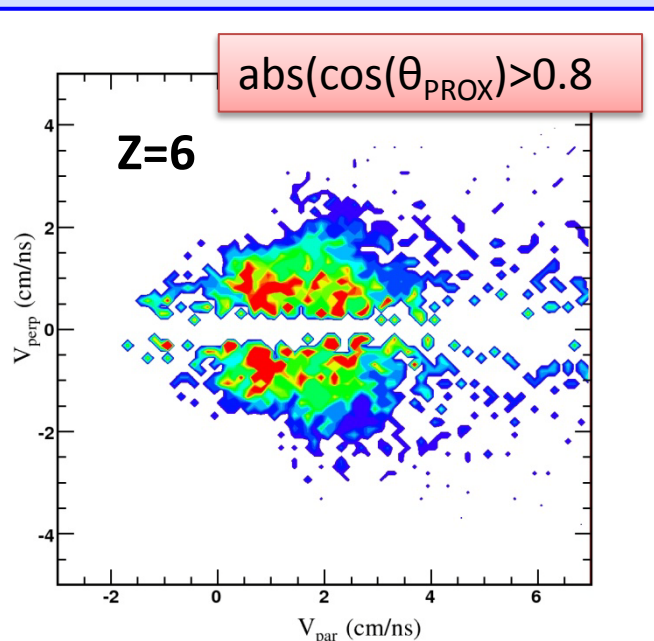
The three heaviest fragments are ordered according to decreasing value of parallel velocity.

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$^{64}\text{Ni} + ^{124}\text{Sn}$  35 A.MeV



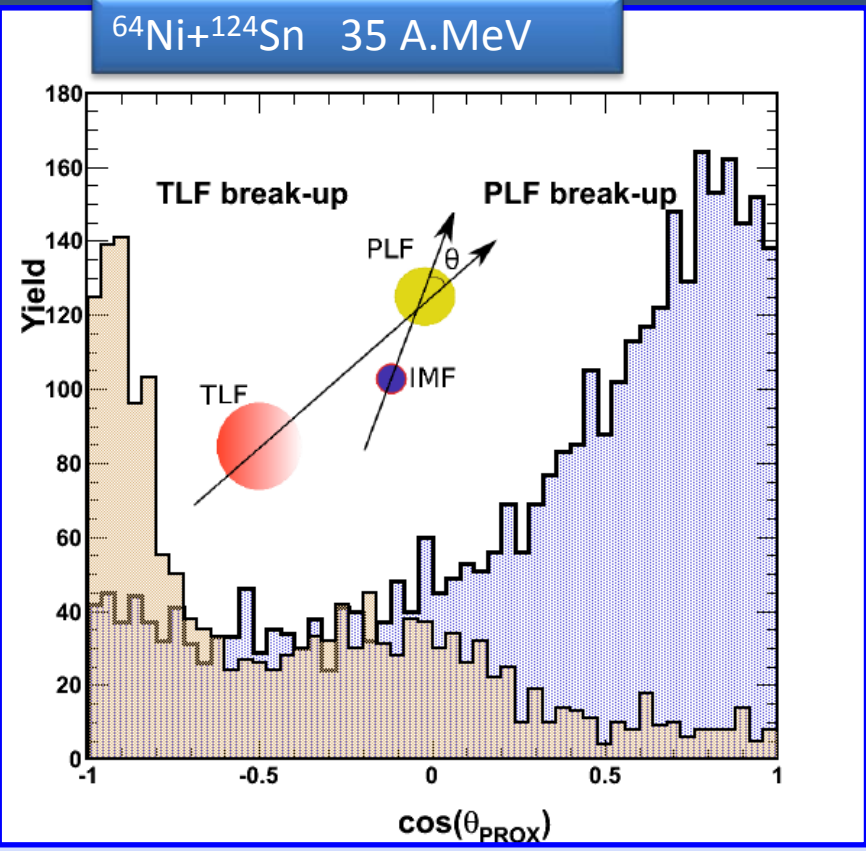
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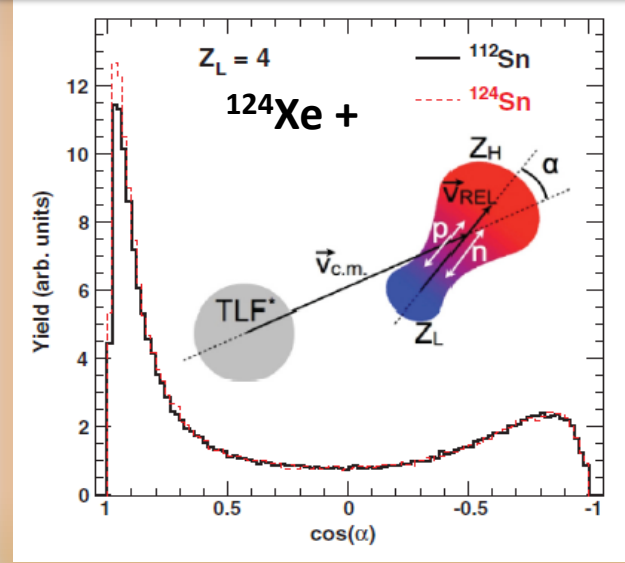


# Disentangling dynamical vs. statistical emission in ternary events



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 aligned emission of the lighter fragment in the backward emisphere of **PLF (+1)** and **TLF (-1)** towards midrapidity

Enhancement of backward fragment yield relative to the forward component



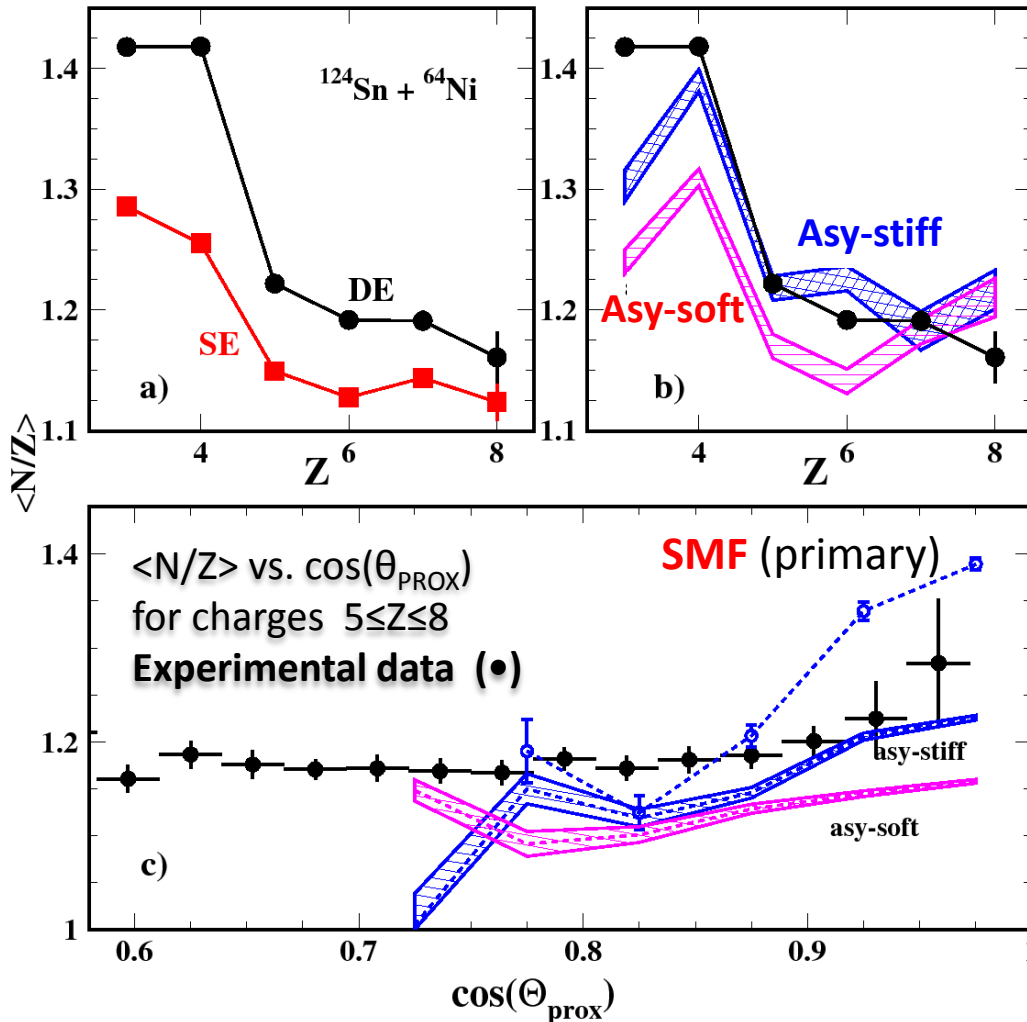
S. Hudan et al., PRC **86** 021603 (2012)  
 R. Brown et al., PRC **87** 061601 (2013)

# Stochastic Mean Field (SMF) + GEMINI calculation



CHIMERA @ LNS

$^{124}\text{Sn} + ^{64}\text{Ni}$  35 A.MeV



Experimental  $\langle N/Z \rangle$  distribution of IMFs as a function of their atomic number compared with results **SMF+GEMINI** calculations (hatched area) for two different parametrizations of the symmetry potential (**asy-soft** and **asy-stiff**)

- Dynamically emitted particles
- Statistically emitted particles

See also: S. Hudan et al., PRC **86** 021603(R) 2012.

K. Brown et al., PRC **87** 061601 (2013)

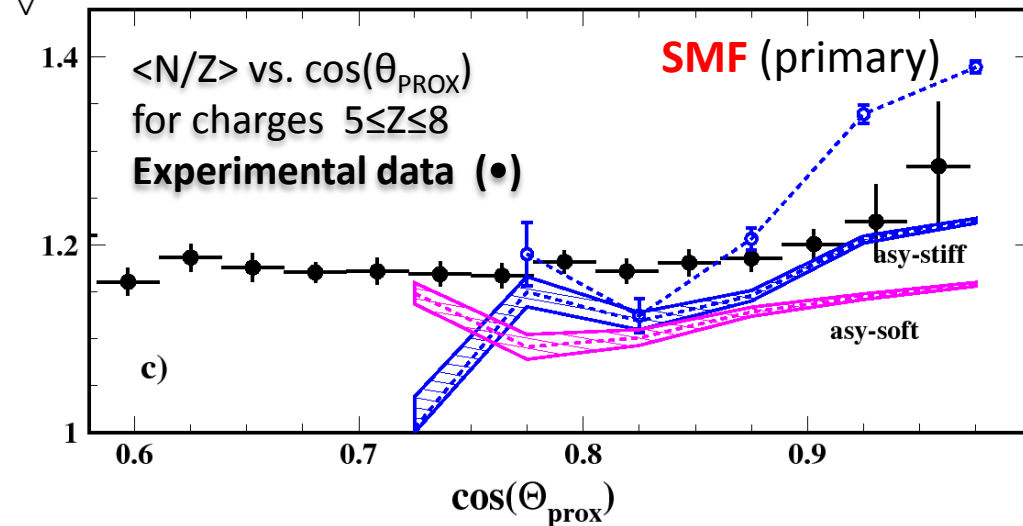
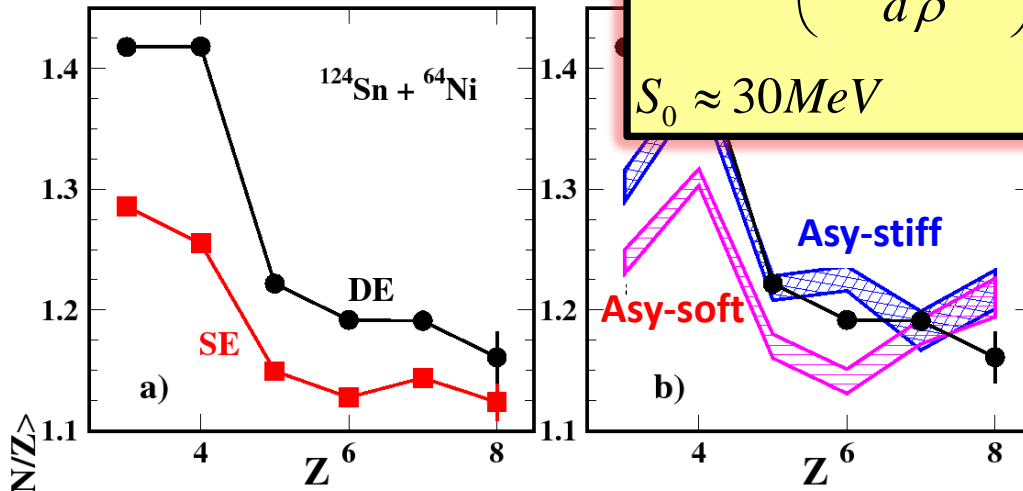
# Stochastic Mean Field (SMF) + GEMINI calculation



$^{124}\text{Sn} + ^{64}\text{Ni}$  35 A.MeV

$$L = 3\rho_0 \left( \frac{dE_{\text{sym}}(\rho)}{d\rho} \right)_{\rho=\rho_0} = \begin{aligned} &\approx 80 \pm 10 \text{ MeV for the asy-stiff} \\ &\approx 25 \text{ MeV for the asy-soft} \end{aligned}$$

$$S_0 \approx 30 \text{ MeV}$$



function of their atomic number compared with results **SMF+GEMINI** calculations (hatched area) for two different parametrizations of the symmetry potential (**asy-soft** and **asy-stiff**)

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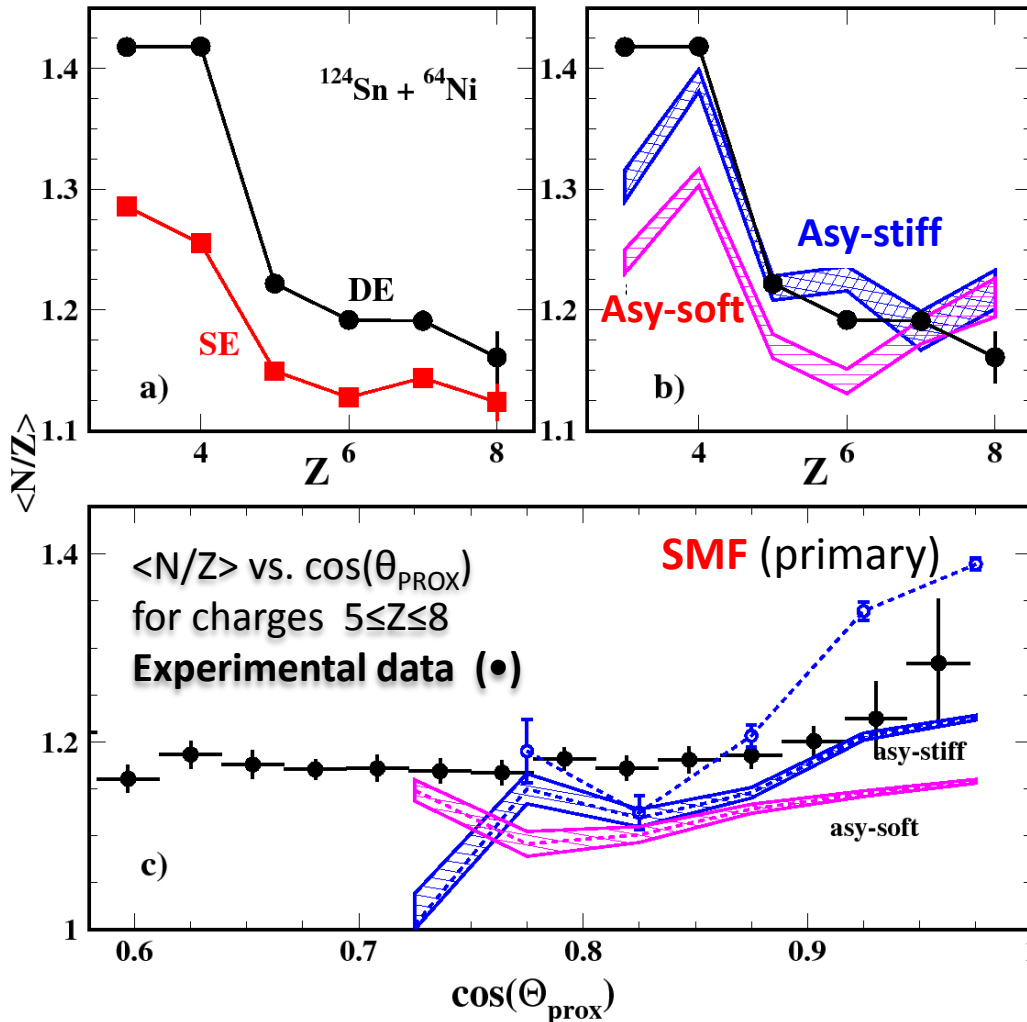
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CHIMERA @ LNS

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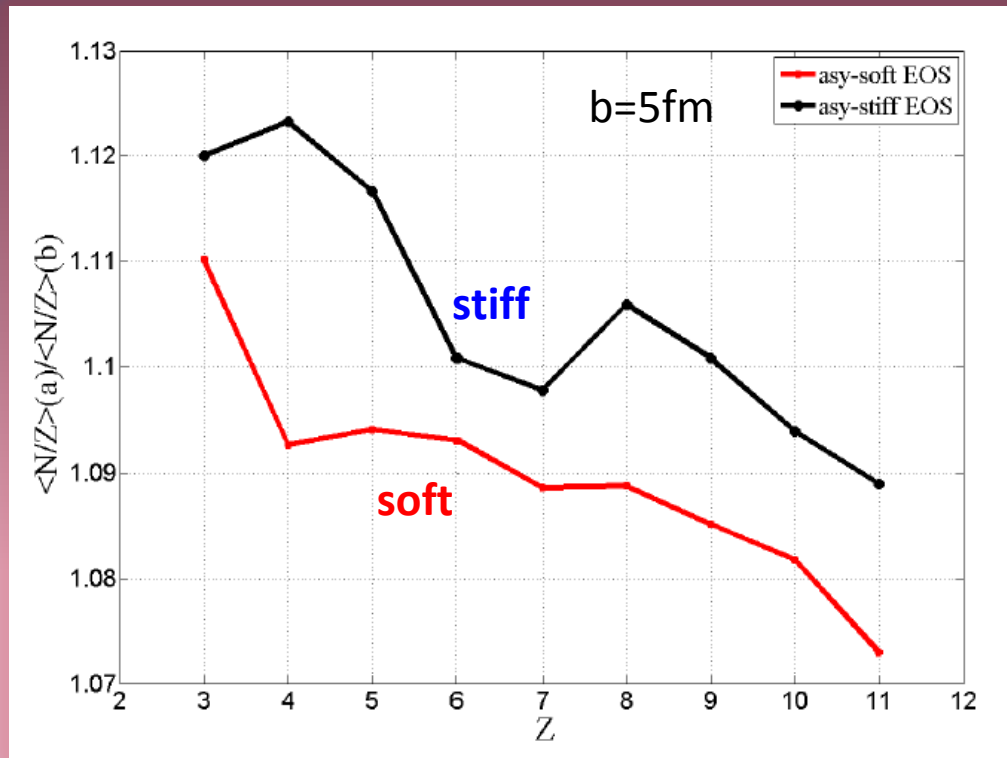
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K. Brown et al., PRC **87** 061601 (2013)

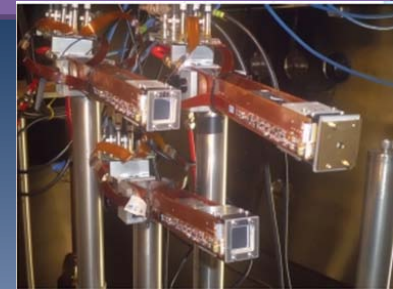
# Stochastic Mean Field (SMF) : ratio (a) $^{124}\text{Sn}+^{64}\text{Ni}$ / $^{124}\text{Xe}+^{64}\text{Zn}$



**Very Preliminary**

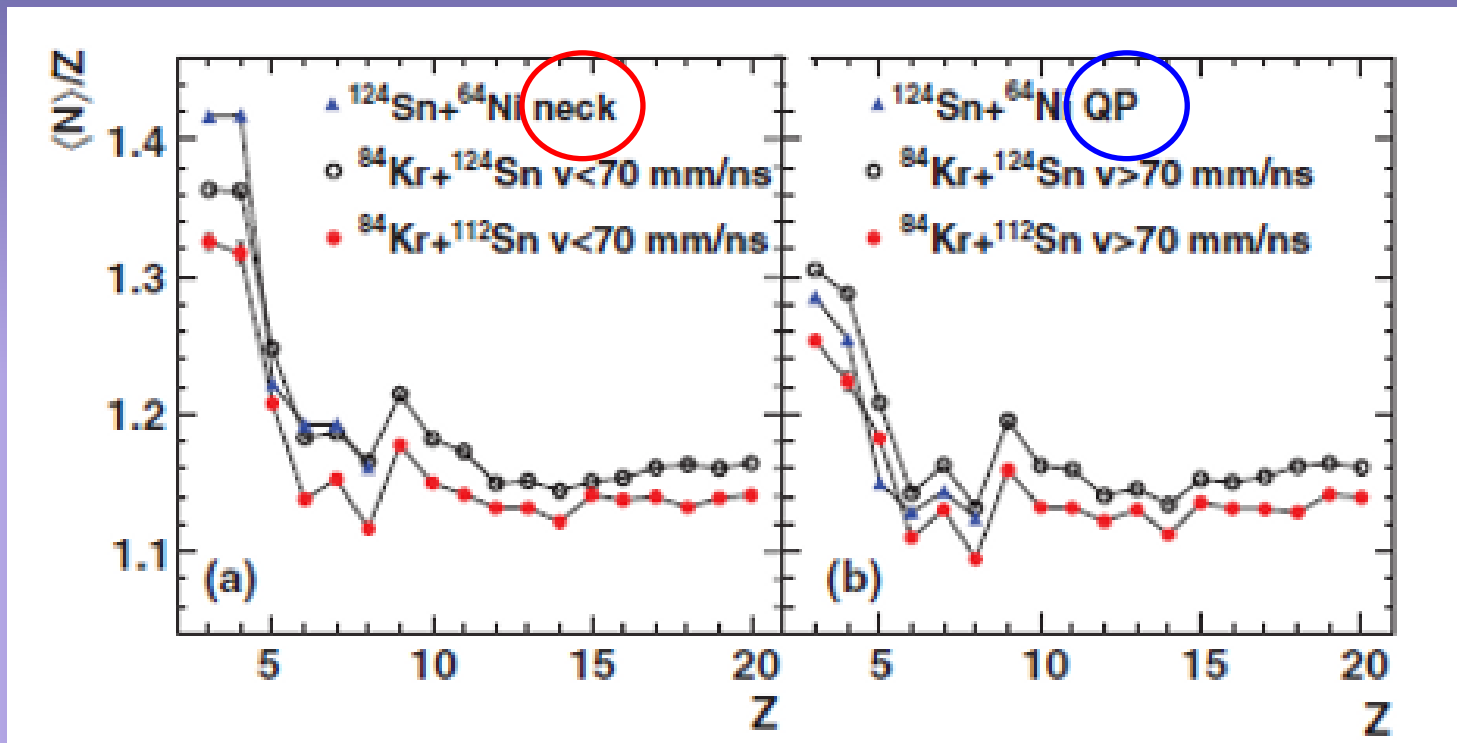
V. Baran, M. Marciu

# Comparison with FAZIA data $^{84}\text{Kr} + ^{112,124}\text{Sn}$ data 35 A.MeV



Fazia@LNS

**FAZIA data:  $^{84}\text{Kr} + ^{112,124}\text{Sn}$**   
Selection based on particles velocity



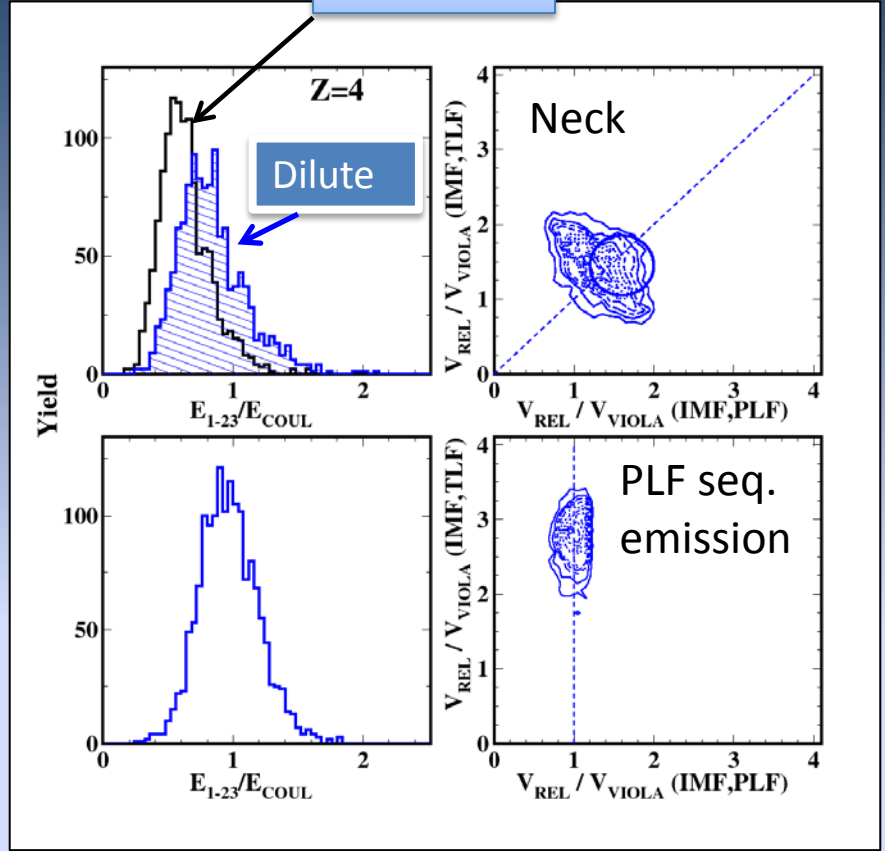
**Chimera data (triangles):  $^{124}\text{Sn} + ^{64}\text{Ni}$**   
Selection based on angular correlations



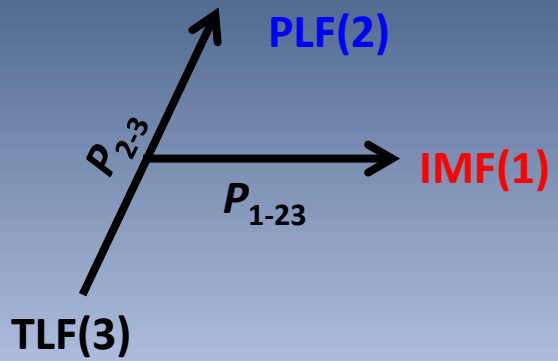
# Density determination: three body analysis in the experimental data



Compact

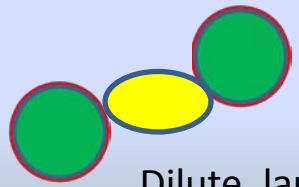


In the 3-bodies center-of-mass system:

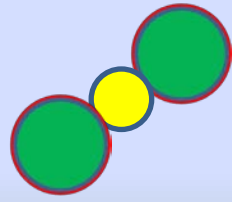


$$E_{TOT}^{c.m.} = E_1 + E_2 + E_3 = \frac{p_{1-23}^2}{\mu_{1-23}} + \frac{p_{23}^2}{\mu_{23}} = E_{1-23} + E_{23}$$

$^{124}\text{Sn} + ^{64}\text{Ni}$  35 A.MeV



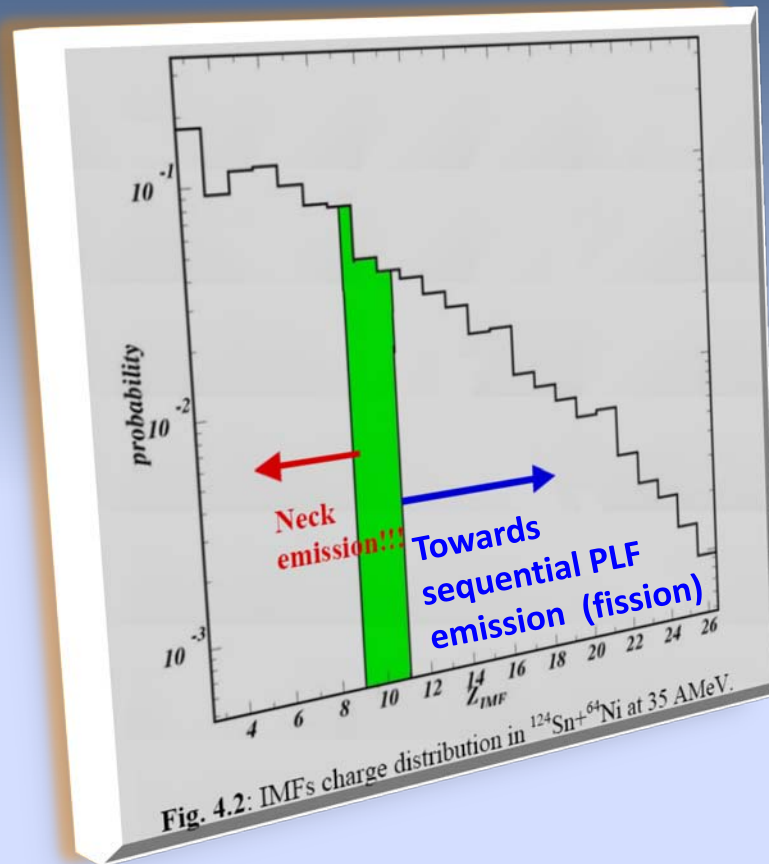
Dilute, large radius



Compact, normal radius

The ratio  $E_{1-23}/E_{COULOMB}$  is calculated considering for the IMFs a dilute configuration with  $r_0=1.8A^{1/3}$  fm (filled histogram corresponding to about  $0.05 \rho_0$ ) resulting from average values of SMF calculation ( $\rho=0.05-0.06$   $1/\text{fm}^3$ )

# From early prompt neck fragmentation to PLF dynamical fission



The time-scale of the process as a function of the incident energy and impact parameter could be the main signature among different mechanisms:

- 1) Early neck fragmentation (40-120 fm/c)
- 2) Dynamical fission (120-300 fm/c)
- 3) Equilibrated fission (>1000 fm/c)

With respect to the prompt neck emission, the emission of heavy IMFs from projectile-like fragment break-up appears at a later stage

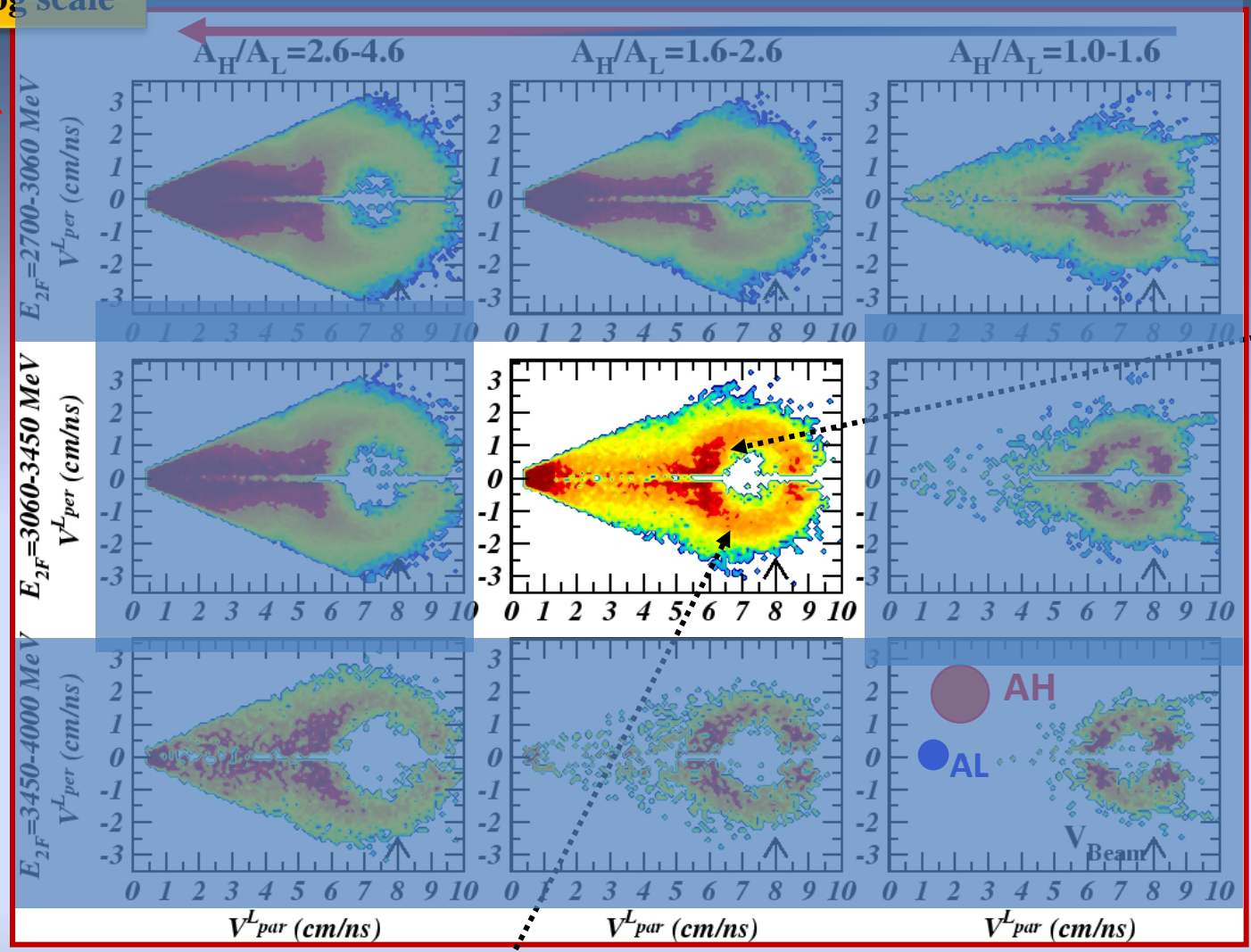
# The inset of quasi-projectile dynamical fission

$^{124}\text{Sn} + ^{64}\text{Ni}$  35 A MeV  
neutron rich

$A_H/A_L$  Mass asymmetry

log scale

Collision violence



The lighter fragments are emitted preferentially backwards in the PLF reference system, i.e., towards the target nucleus:  
***Dynamical Fission***  
→ fast and non-equilibrated fission

E. De Filippo et al., PRC 71 064604 (2005)  
P. Russotto et al., PRC 81, 064605 (2010)

Coulomb ring  $5 \lesssim V_{\text{beam}} = 8$ . cm/ns → Well defined PLF source: scattering of PLF followed by its splitting in H&L fragments → sequential mechanism!!!

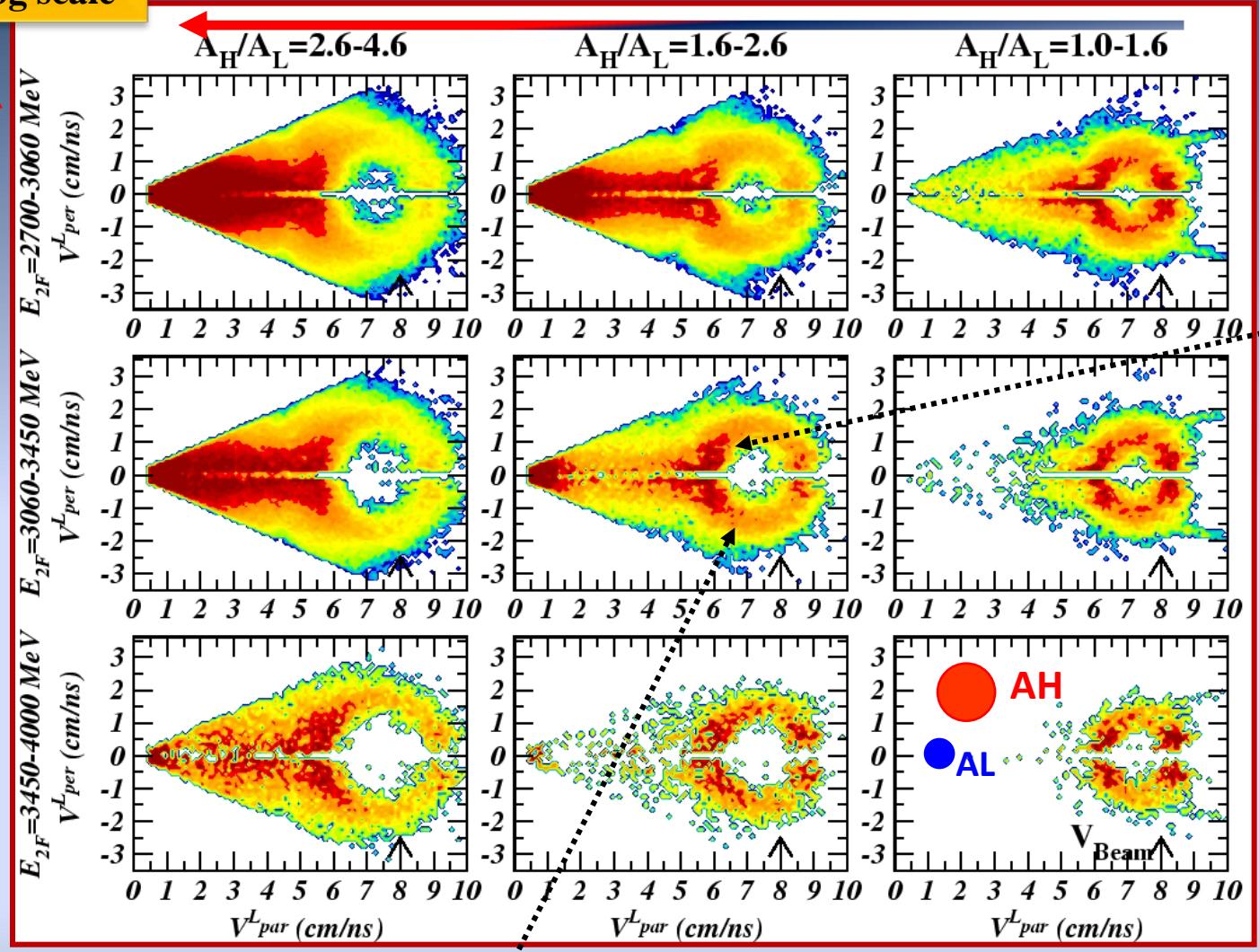
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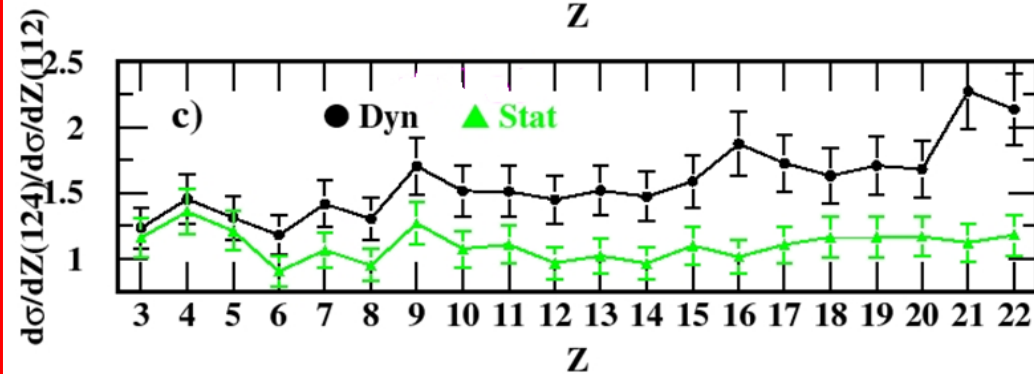
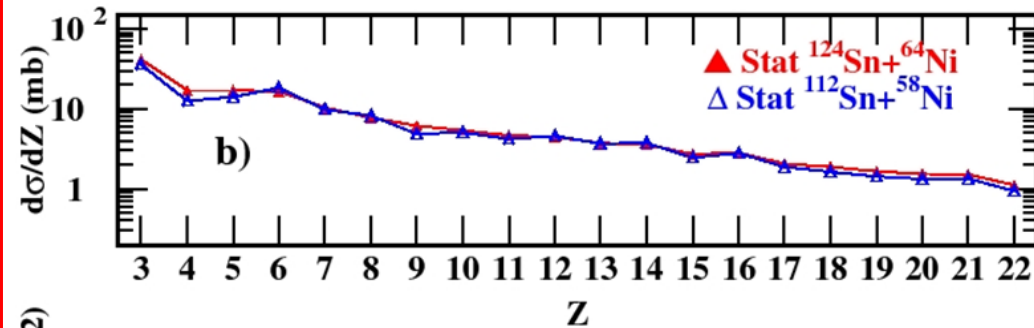
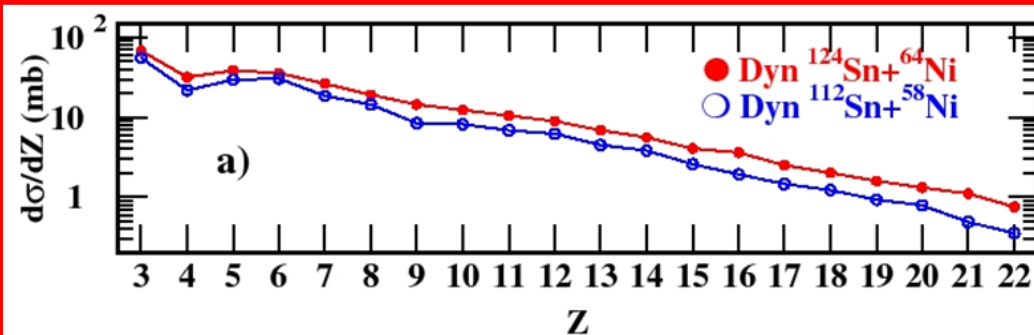
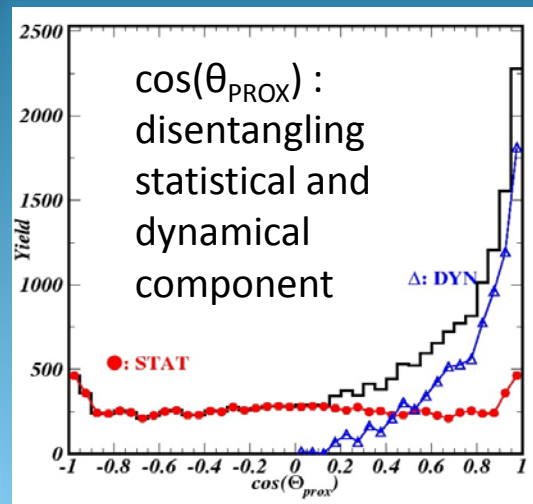
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# Comparison of IMFs cross sections for $^{124}\text{Sn}+^{64}\text{Ni}$ and $^{112}\text{Sn}+^{58}\text{Ni}$



P. Russotto et al. , to be submitted, PRC (2014)  
 P. Russotto et al., PRC 81, 064605 (2010)  
 E.De Filippo et al., PRC 71 064604 (2005)

- Dynamical component: enhanced in the neutron rich
- Statistical component: almost equal (ratio:  $\sim 1.1$ )

# Comparison of IMFs cross sections for $^{124}\text{Sn}+^{64}\text{Ni}$ and $^{112}\text{Sn}+^{58}\text{Ni}$

Main experimental result: the dynamical component is enhanced for the neutron rich system.

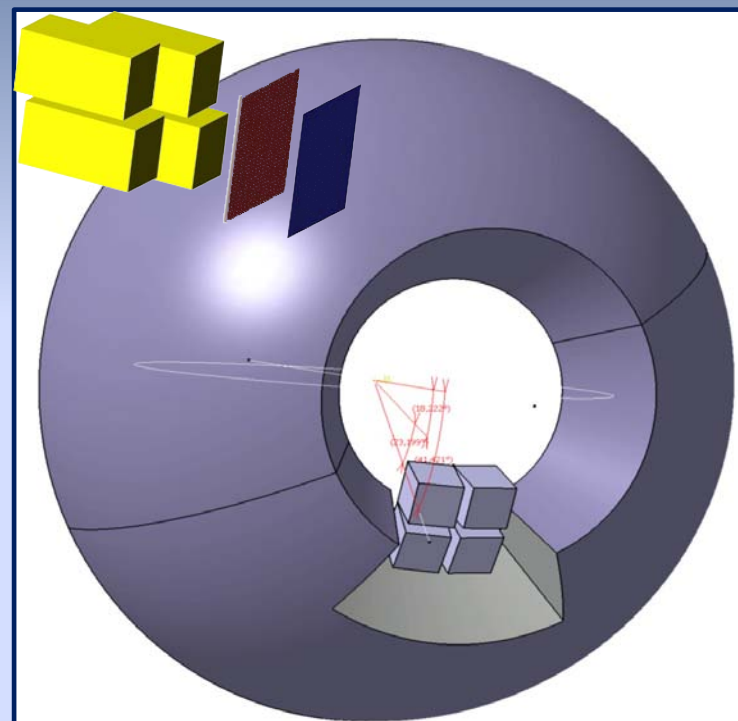
Is it a **size (mass)** effect or **isospin** effect ?

## The Inkiissy experiment at LNS

System	N/Z Projectile	N/Z target	N/Z compound
$^{124}\text{Sn}+^{64}\text{Ni}$	1.48	1.29	1.41
$^{124}\text{Xe}+^{64}\text{Zn}$	1.30	1.13	1.24
$^{112}\text{Sn}+^{58}\text{Ni}$	1.24	1.07	1.18

see Lucia Quattrocchi poster for details

the  $4\pi$  CHIMERA +  
a module of FARCOS  
prototype



4 telescopes 25 cm from the target  
 $\theta_{\text{lab}} \sim 16\text{-}44$  deg,  $\Delta\phi \sim 45$  deg

See E.V. Pagano talk



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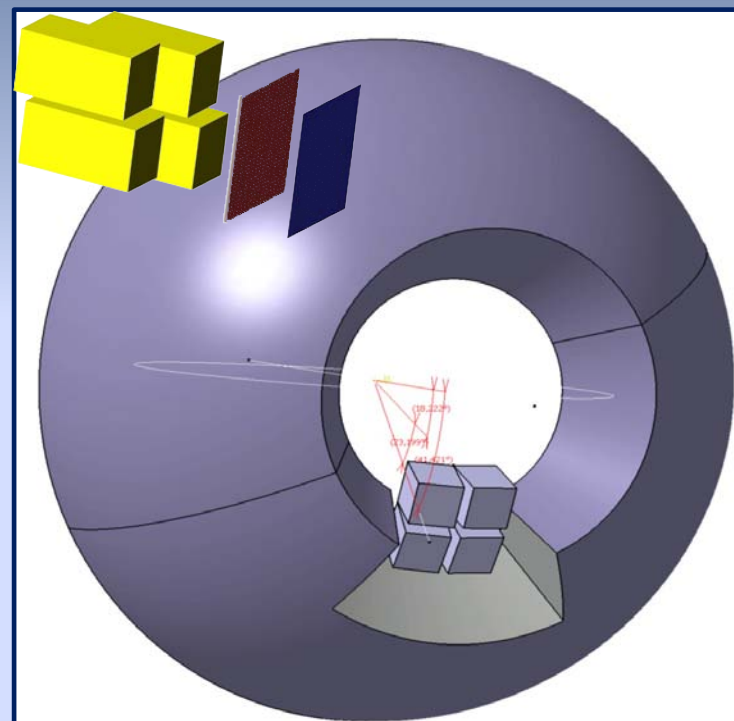
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SPES letter of intent 2014

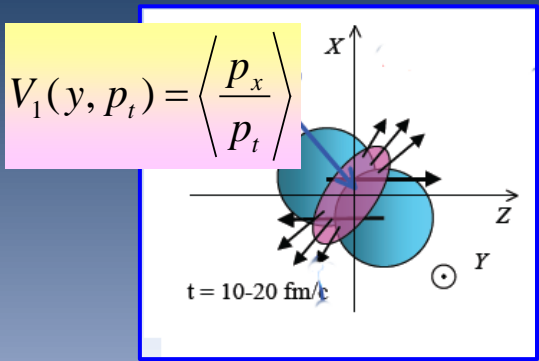


4 telescopes 25 cm from the target  
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See E.V. Pagano talk

# Transverse flow of IMFs and symmetry energy

$^{70}\text{Zn}+^{70}\text{Zn}$ ,  $^{64}\text{Zn}+^{64}\text{Zn}$ ,  $^{64}\text{Ni}+^{64}\text{Ni}$   $E/A=35$  MeV

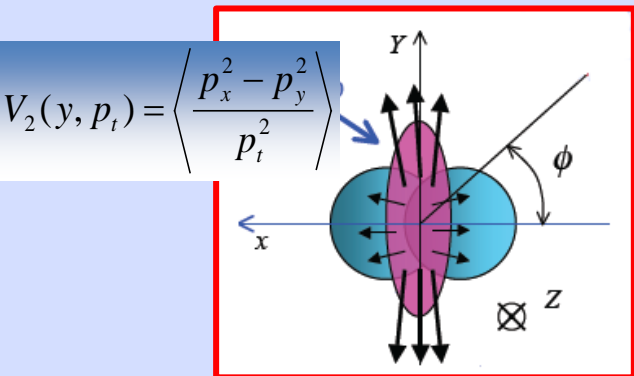
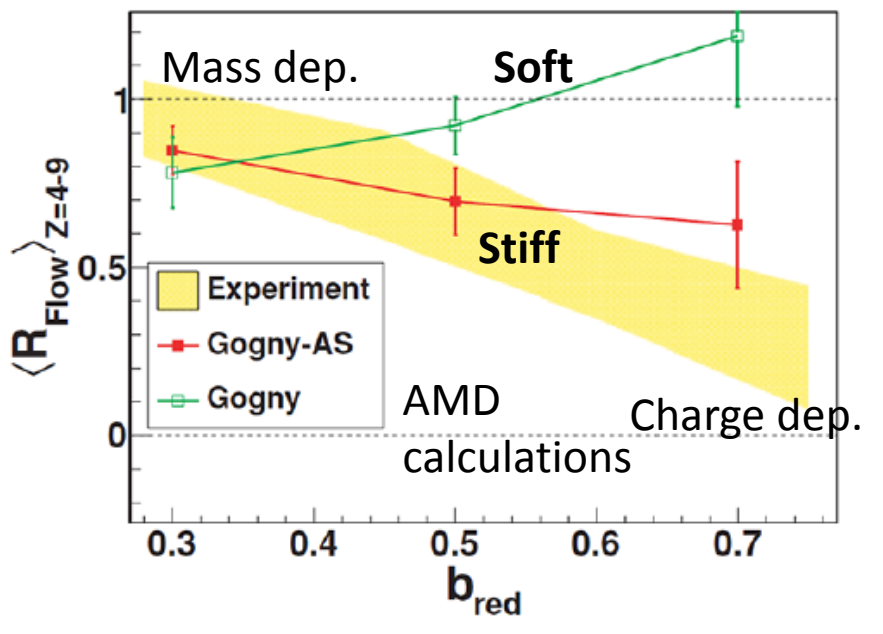


Main observable:

$$R_{\text{flow}} = \frac{\overline{\langle P_x \rangle}_{^{64}\text{Zn}} - \overline{\langle P_x \rangle}_{^{70}\text{Zn}}}{\overline{\langle P_x \rangle}_{^{64}\text{Ni}} - \overline{\langle P_x \rangle}_{^{70}\text{Zn}}}$$

**Transverse flow:** provides information on the azimuthal anisotropy in the reaction plane .

Z. Kohley et al., PRC82, 064601 (2010)



**Elliptic flow:** measures the competition between in plane and out-of-plane emission

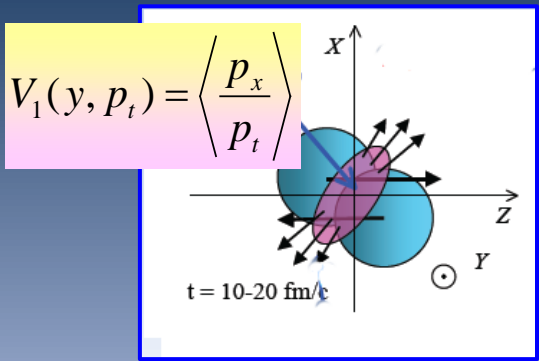
NIMROD-ISiS@TAMU



See P. Russotto talk for "flow" measurements at relativistic energies

# Transverse flow of IMFs and symmetry energy

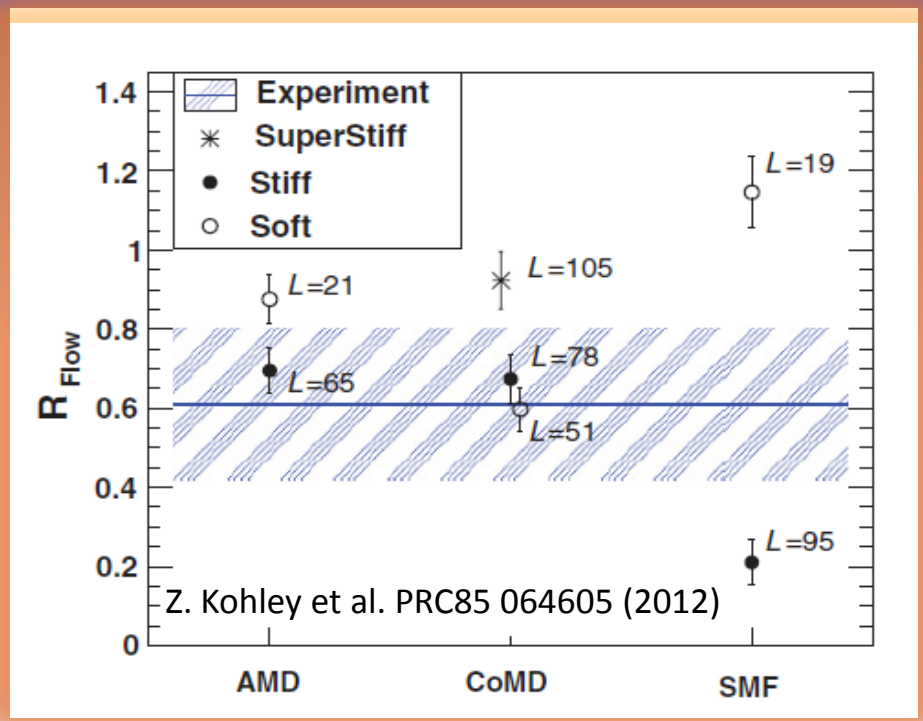
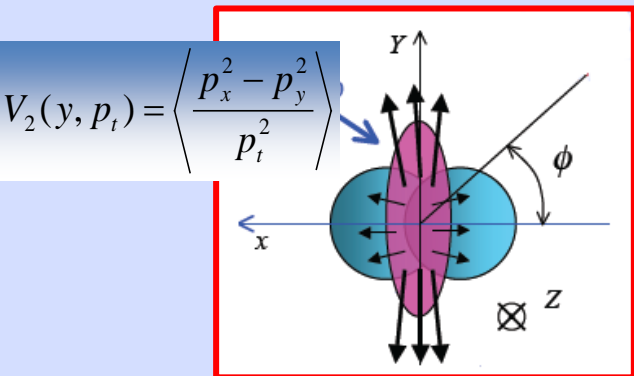
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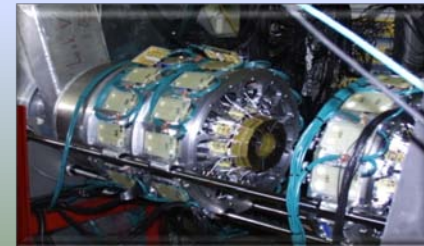
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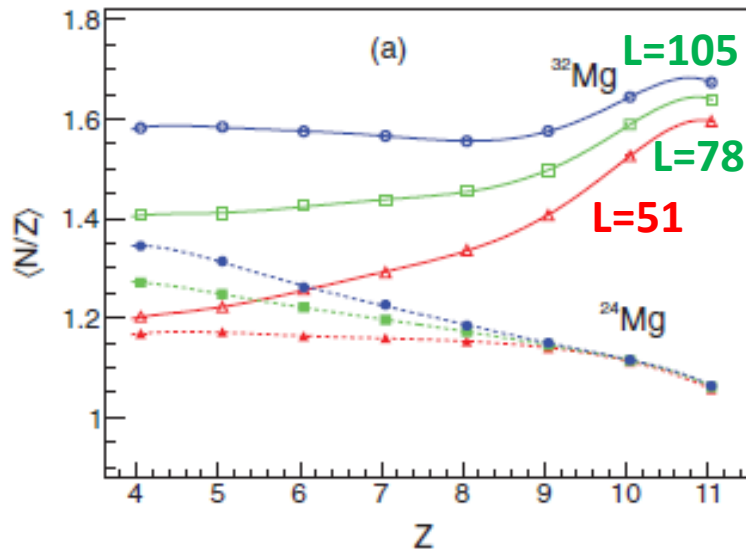
NIMROD-ISiS@TAMU



See P. Russotto talk for "flow" measurements at relativistic energies

# Exploiting RIBS and neutron detection (a way for the future ?)

CoMD calculation showing the sensitivity to  $L$  for the  $\langle N/Z \rangle$  of the quasi-projectile residue in  $^{32}\text{Mg} + ^9\text{Be}$  respect to  $^{24}\text{Mg} + ^9\text{Be}$  at 73 MeV/A

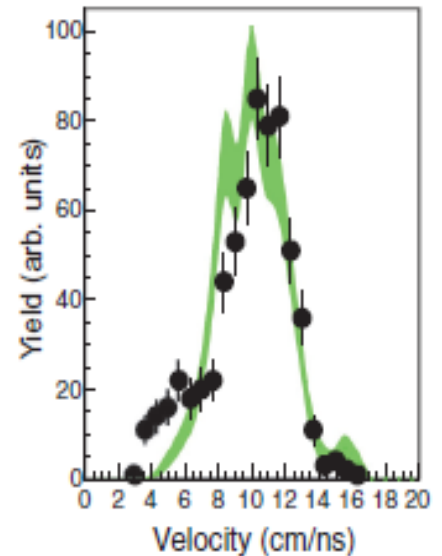
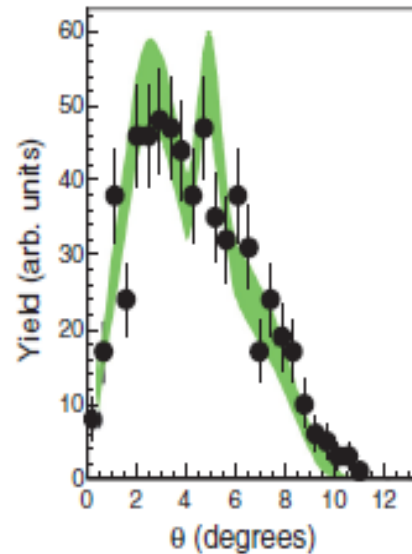


Adapted from Z. Kohley et al.,  
PRC **88** 041601 (2013)

MoNA@MSU

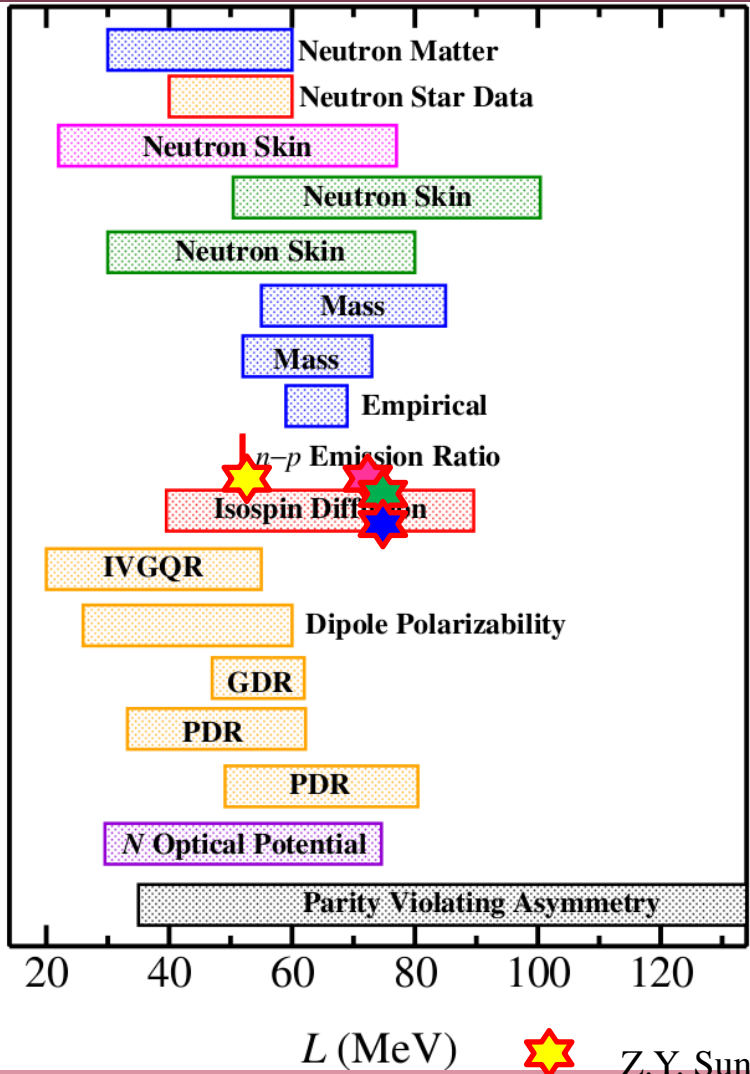


Neutron angular distributions and velocity in coincidence with  $Z=4$  fragments. CoMD calculations with  $L=78$  MeV are in green (Data from Z. Kohley et al. PRC88 with the MoNA Neutron Array).



# Collection of available estimates of the slope parameter L

- $\chi$  Lagrangian and Q. Montecarlo
- Neutron-Star Observations
- $p$  &  $\alpha$  scattering charge ex.
- Antiprotonic Atoms
- Nuclear Model Fit
- Heavy Ion Collisions
- Giant Resonances
- $N-A$  scattering Charge Ex. Reactions Energy Levels
- Parity Violating e-scattering



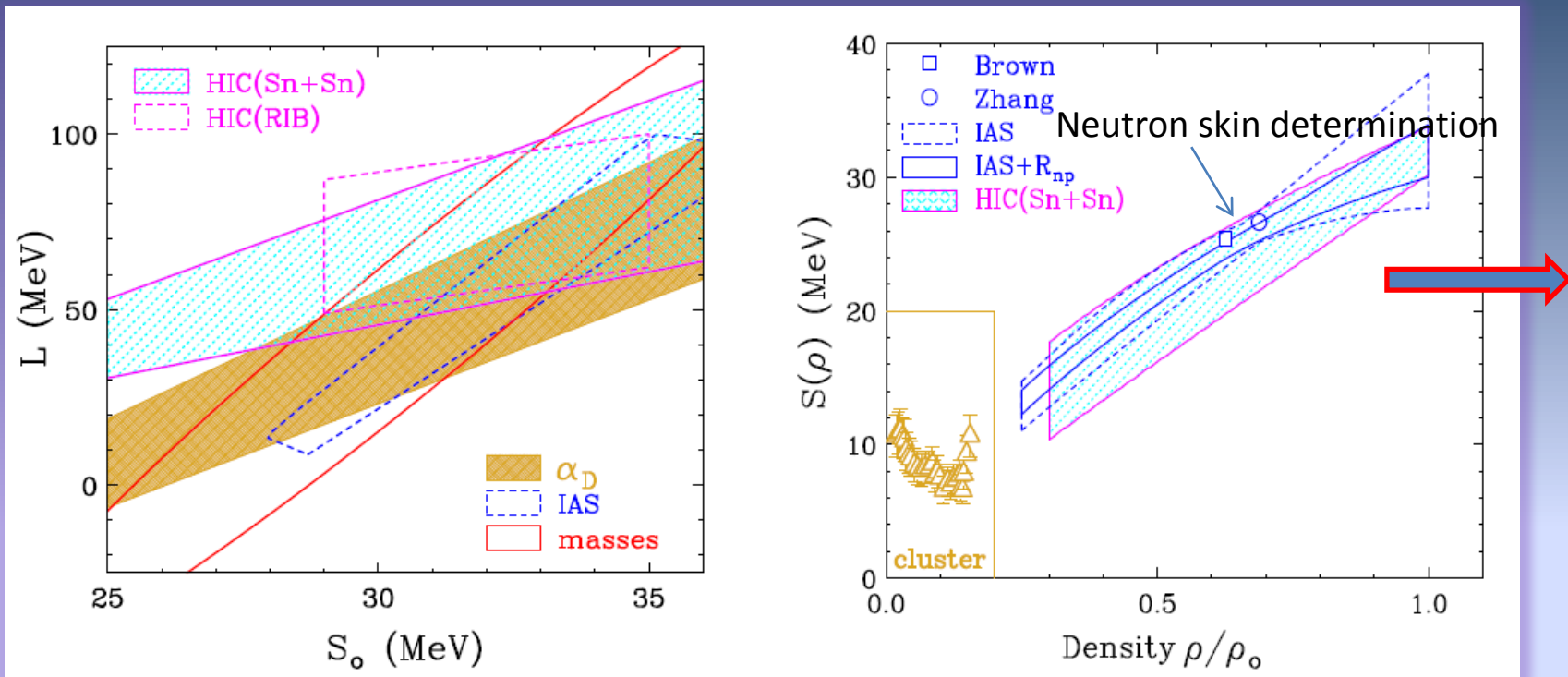
Hebeler *et al.* PRL105 (2010) 161102  
 and Gandolfi *et al.* PRC85 (2012) 032801 (R)  
 Steiner *et al.* Astrophys. J. 722 (2010) 33  
 Lie-Wen Chen *et al.* PRC 82 (2010) 024321  
 Centelles *et al.* PRL 102 (2009) 122502  
 Warda *et al.* PRC 80 (2009) 024316  
 Möller *et al.* PRL 108 (2012) 052501  
 Danielewicz NPA 727 (2003) 233  
 Agrawal *et al.* PRL109 (2012) 262501  
 Famiano *et al.* PRL 97 (2006) 052701  
 Tsang *et al.* PRL 103 (2009) 122701  
 Roca-Maza *et al.* PRC 87 (2013) 034301  
 Roca-Maza *et al.* PRC (2013), in press  
 Trippa *et al.* PRC 77 (2008) 061304(R)  
 Klimkiewicz *et al.* PRC 76 (2007) 051603(R)  
 Carbone *et al.* PRC 81 (2010) 041301(R)  
 Xu *et al.* PRC 82 (2010) 054607  
 PREX Collab. PRL 108 112502 (2012)

Adapted from X. Vinas et al., EPJA 50:27 (2014)

- ★ Z.Y. Sun et al., PRC82 051603 (2010) (Chimera/MSU data)
- ★ E. Galichet et al. PRC 79 064615 (2009) (INDRA data)
- ★ E.d.F. et al. PRC 86 014610 (2012) (Chimera data)
- ★ Z. Kohley et al., PRC 88 041601 (2013) (TAMU data)



# What we learn from **Heavy Ion collisions** and **nuclear structure probes** ?



Adapted from C.J. Horowitz et al., ArXiv 1401:5839 (2014)

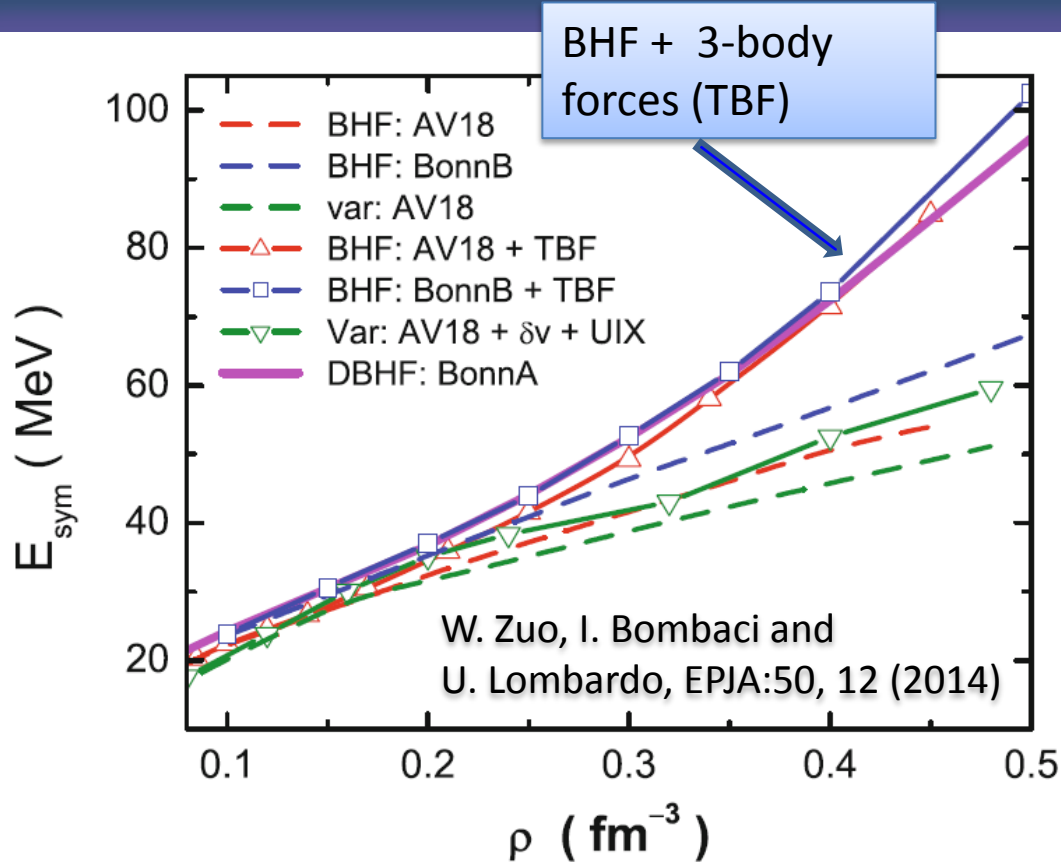
As a function of incident energy, impact parameter, isospin asymmetry, it is possible to span from low to high densities with HIC

A stringent test and constraint on transport model and dynamical theories

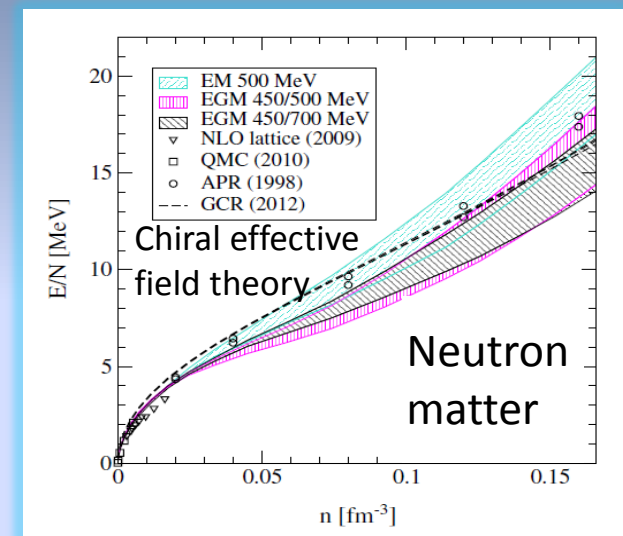
Unique possibility to explore the critical region at  $2-3\rho_0$



# High densities behaviour of symmetry energy: a controversial problem



The dependency on density of the potential part of symmetry energy term is largely unconstrained for the high density behaviour  $\rho \geq \rho_0$



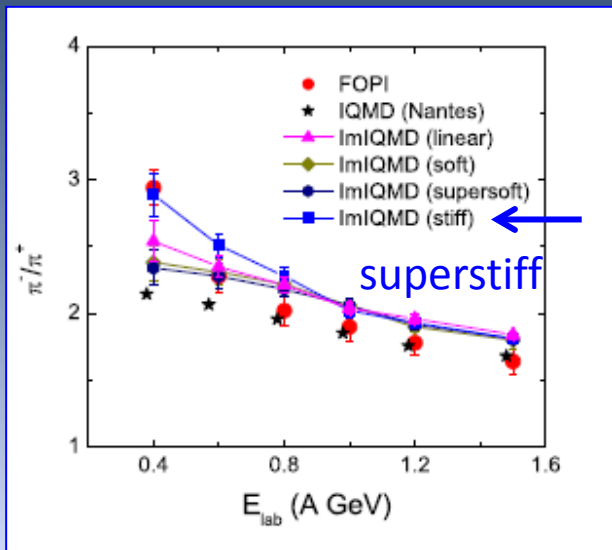
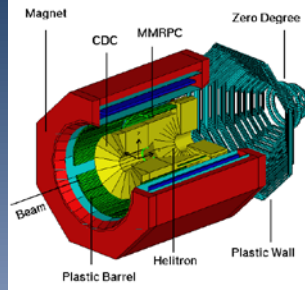
I. Tews et al., PRL110 032501 (2013)

The effect of three body forces (TBF) is weak at low density but at supra-saturation densities leads to a stiffening of the symmetry energy with density.

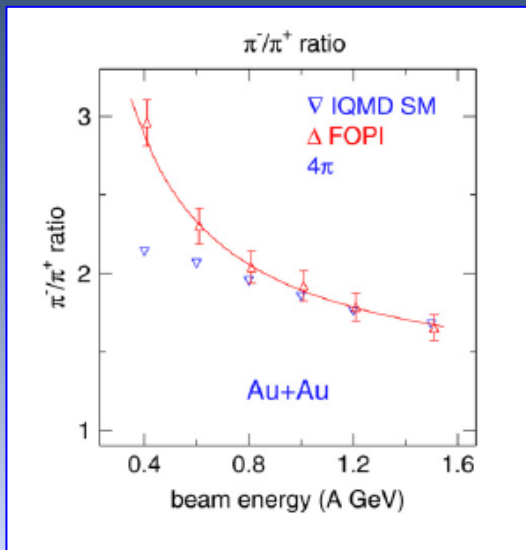
In neutron matter the short-range repulsive part of 3-body force is dominant.

# Using Pion and Kaon probes

FOPI@GSI



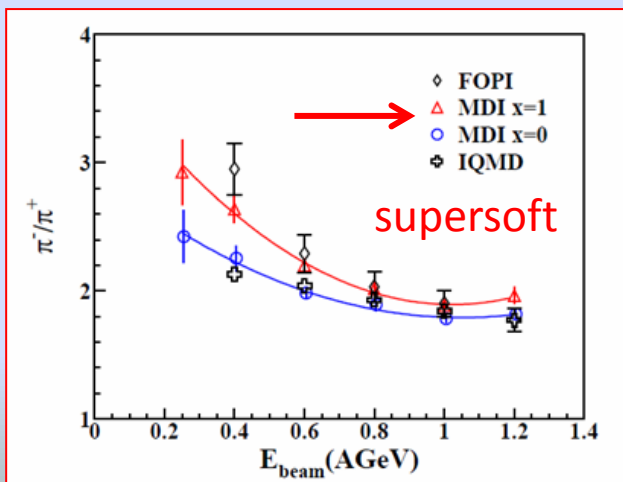
Z. Feng et al. PLB 683 140, 2010



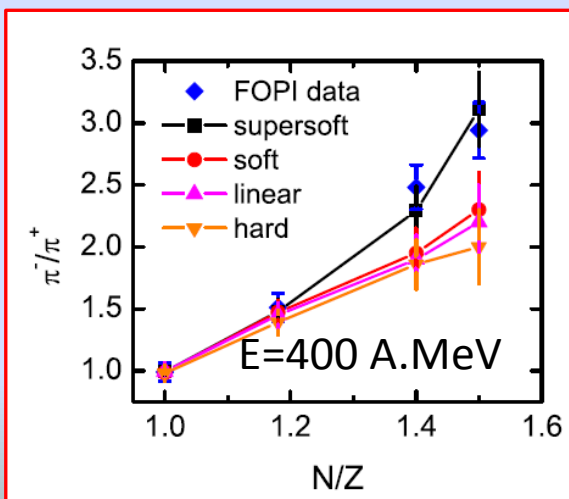
W. Reisdorf et al. NPA 781 459, 2007

$\Delta$  resonance:  
 $Y(\pi^-)/Y(\pi^+) \approx (N/Z)^2_{dense}$

Statistic model:  
 $\mu(\pi^+) - \mu(\pi^-) = 2 (\mu_p - \mu_n)$



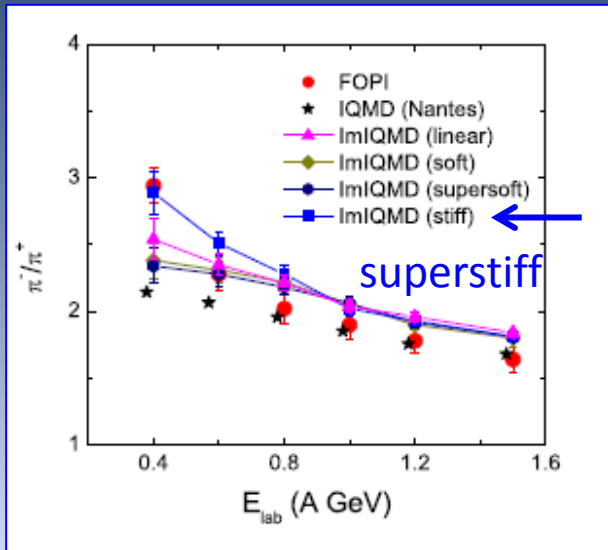
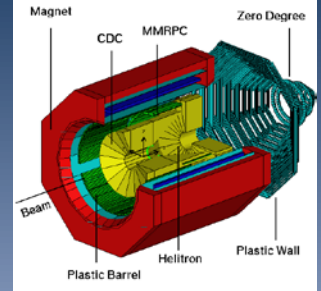
Z. Xiao et al. PRL 102 062509, 2009



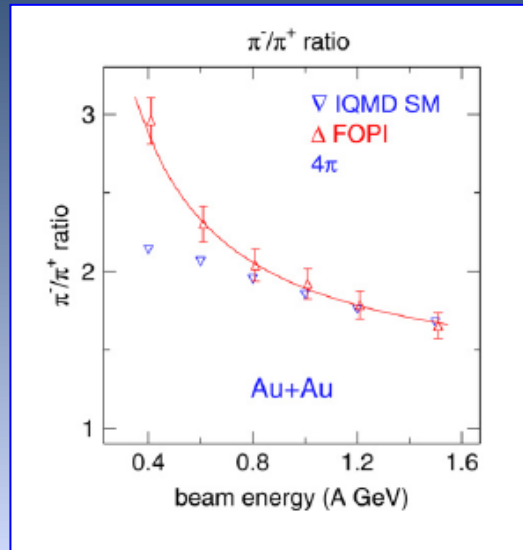
W. Xie et al. PLB 718 1510, 2013

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FOPI@GSI



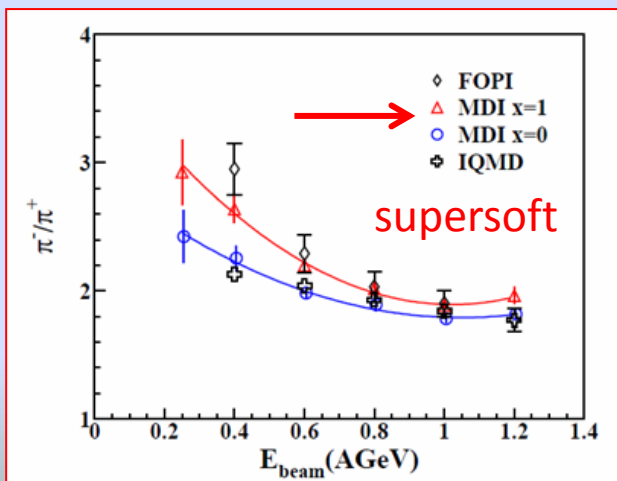
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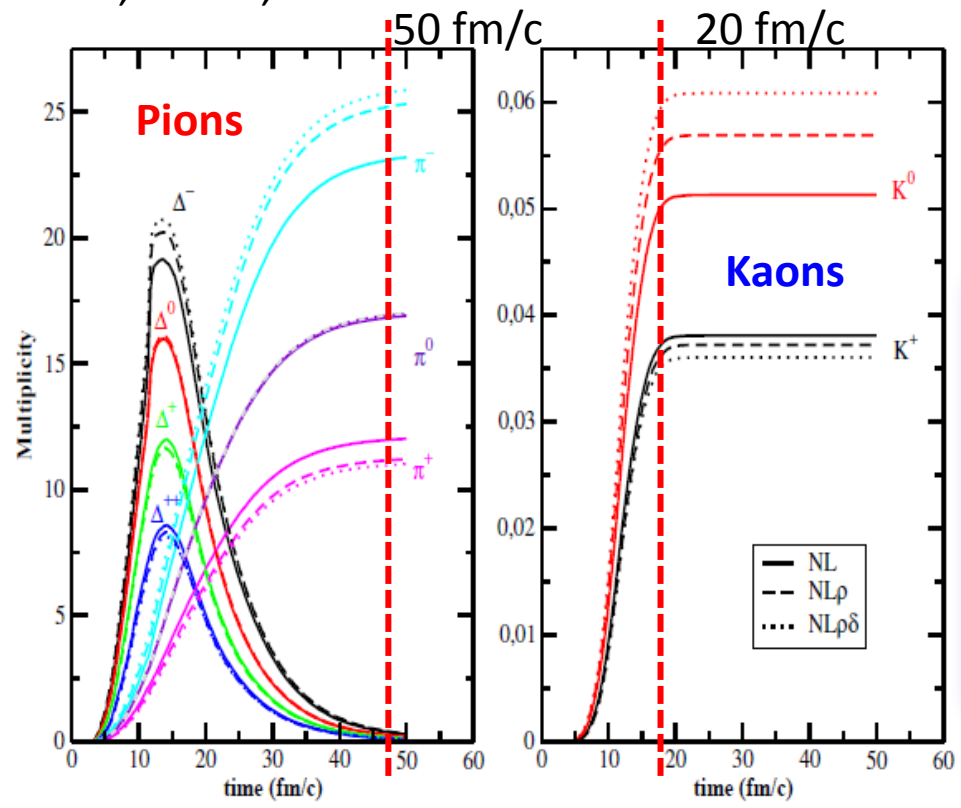
Z. Xiao et al. PRL 102 062509, 2009

	3.5	
Z. Xiao, B-An Li et al.	IBUU4	supersoft
Z. Feng et al.	IMQMD	superstiff
G. Ferini et al.	RMF	stiff (linear)
W. Reisdorf	IQMD	soft (or no influence)
W.J. Xie et al.	ImIBL	supersoft
	N/Z	

W. Xie et al. PLB 718 1510, 2013

# Using Pion and Kaon probes

G. Ferini et al., PRL97, 202301



Pions and Kaons:  
different freeze-out  
times

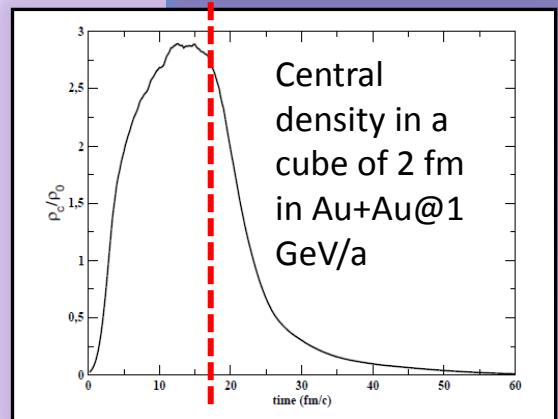
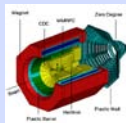


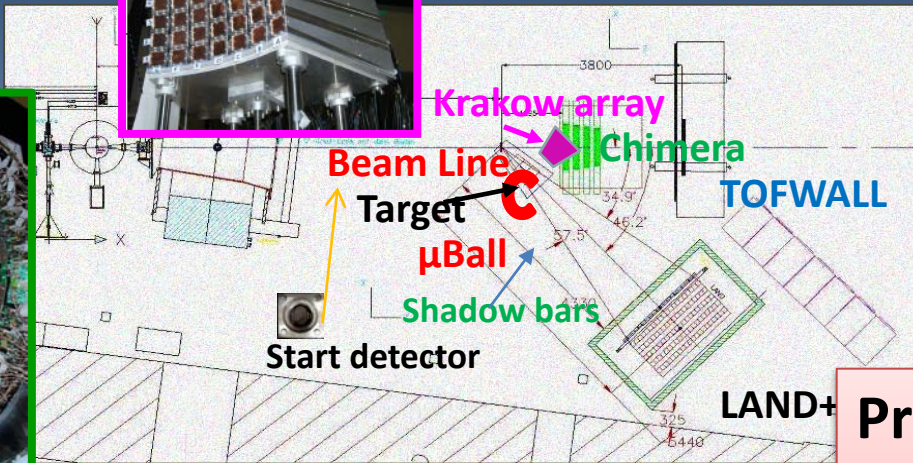
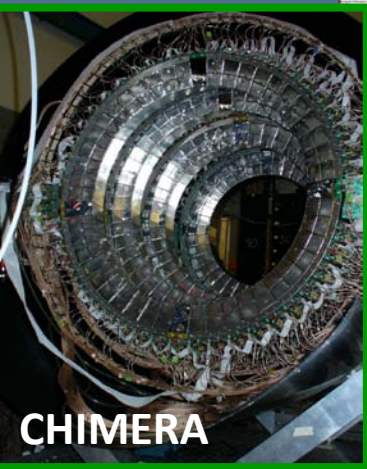
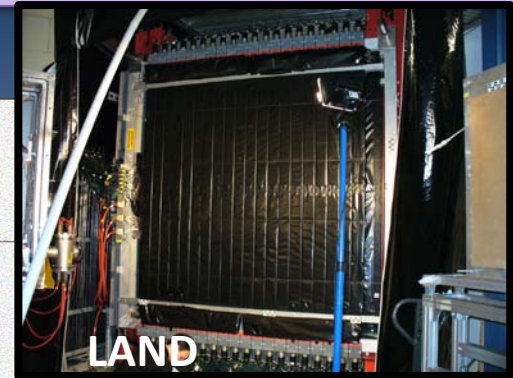
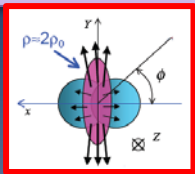
Figure 5.1: Time evolution of  $\Delta^{\pm,0,++}$  resonances and pions  $\pi^{\pm,0}$  (left) and kaons (right) for a central ( $b = 0$  fm impact parameter) Au+Au collision at 1 AGeV incident energy. Transport calculations using the  $NL$ ,  $NL\rho$  and  $NL\rho\delta$  models for the iso-vector part of the nuclear EoS are shown.

Experiment:   
X. Lopez et al., PRC **75**,  
011901 (2007).

New observables proposed : using  $\eta$  mesons or high energy photons  
(G.C. Yong and Bao-An Li Phys. Lett B 723, 388 (2013)).



# Neutron and proton elliptic flow: the AsyEos experiment at GSI



See next talk: **P. Russotto**

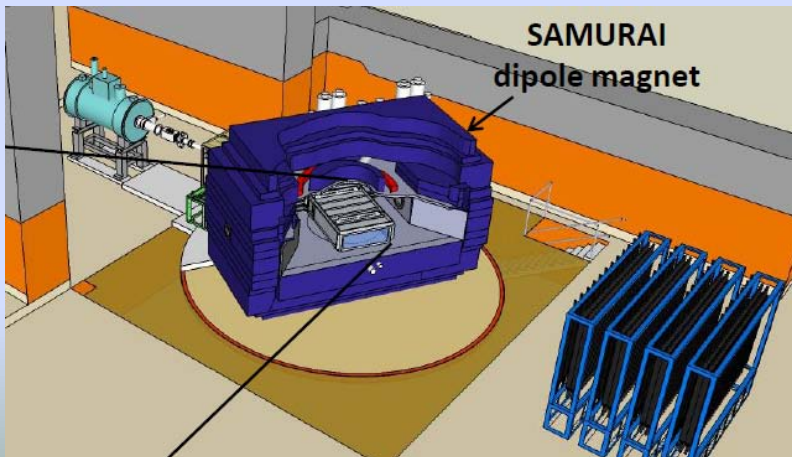
**Present:** the Asy-Eos experiment

**Future:** Fair beams

( $^{132}\text{Sn}$ ,  $^{106}\text{Sn}$ ) R3B/NeuLand, . . . . .

. . . . .

New projects at Riken with the SAMURAI TPC

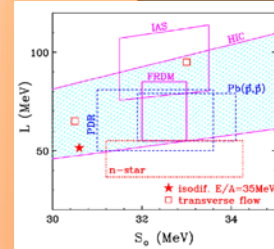


Measure differential flow and ratios for  $\pi^+/\pi^-$   $p/n$   $t/{}^3\text{He}$  at energies around or below 300 A.MeV with RIB beams like  $^{132}\text{Sn}$ ,  $^{108}\text{Sn}$ ,  $^{52}\text{Ca}$ ,  $^{36}\text{Ca}$

# WHAT NEXT ?

A relative consistence analysis have been obtained from HIC but with yet large uncertainties.

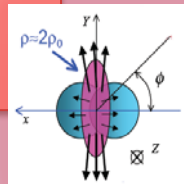
Use of new RIB facilities (exotic neutron rich, proton rich beams: isospin effects are enhanced by increasing the system asymmetry. Comparison with stable beam needed.



Measure different observables in the same experiment: Results have to be consistent for different observables. Different models should describe data in a consistent way.

Models: Look for discrepancies among different modes (the difference between the prediction between two models with the same Iso-parametrization can be larger than the difference between the results obtained by the same model with two different iso-parametrizations. It is important to compare multiple theoretical calculations to the same observable to validate the constraint.

Other signals: use of femtoscopy for a precise space-time sources characterization. Neutron signals (np correlations, n/p double ratios....). New detectors.



Experiment to measure the symmetry energy at supra saturation density are now fundamental. FOPI systematics and the ASYEOS@GSI experiment results are a good starting point for the future. Future efforts at RIKEN, FRIB (MSU), FAIR (GSI) with new devices (NEULAND, SAMURAI TPC, R3B) and new RIB facilities.



**FINE**

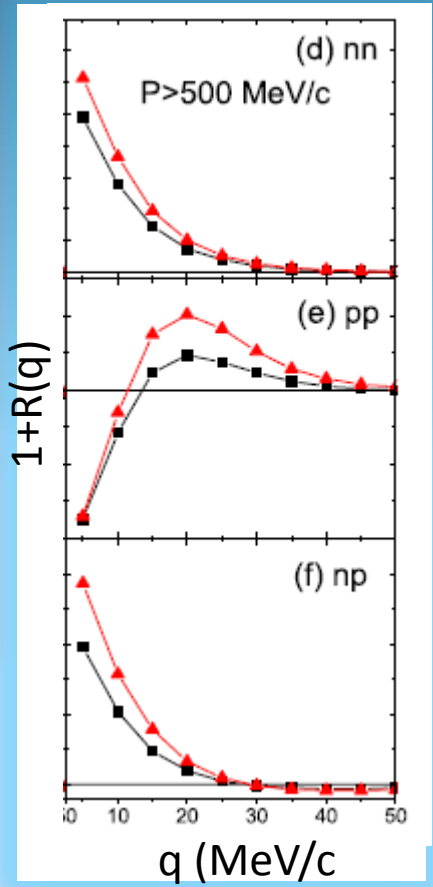
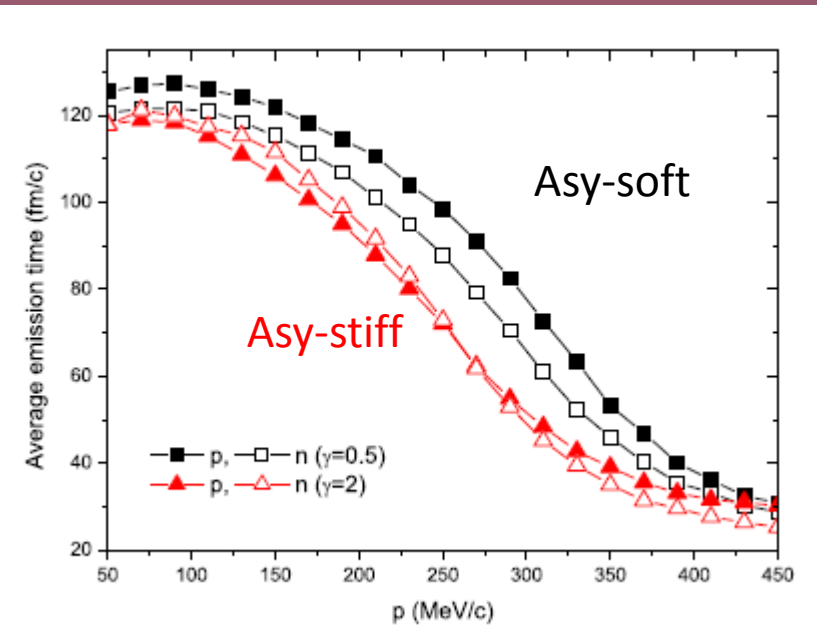
# Particle-particle correlations and symmetry energy: a difficult task

IBUU simulations

$^{52}\text{Ca} + ^{48}\text{Ca}$  E/A=80 MeV, Central collisions

L.W. Chen, V. Greco, C. Ko, B-An Li, PRC68, 014605(2003)

$$1 + R(q) = k \cdot \frac{\sum Y_{\text{coinc}}(\vec{p}_1, \vec{p}_2)}{\sum Y_{\text{ext.mixing}}(\vec{p}_1, \vec{p}_2)}$$



Shorter neutron and proton average emission times and more similar n and p emission times with  $E_{\text{sym}}$  - stiff

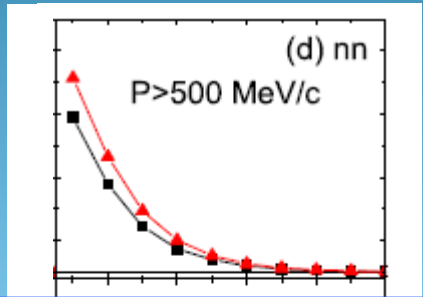
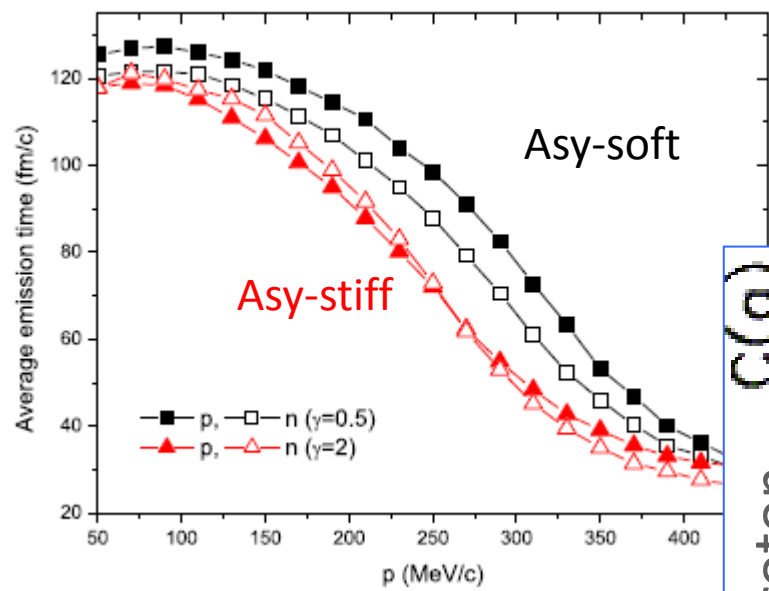
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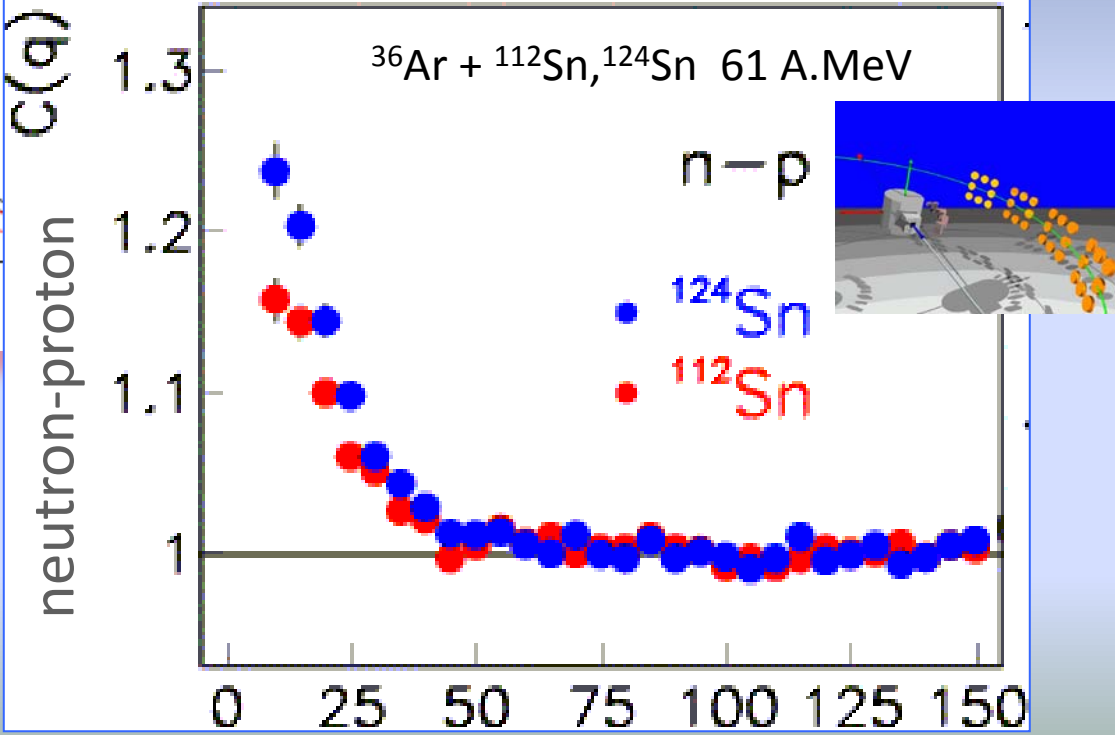
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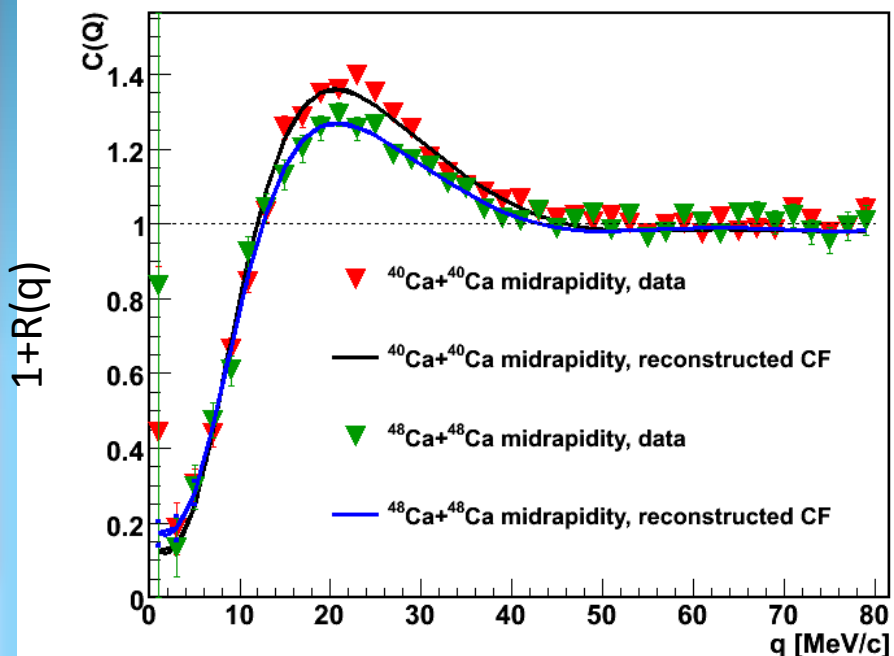
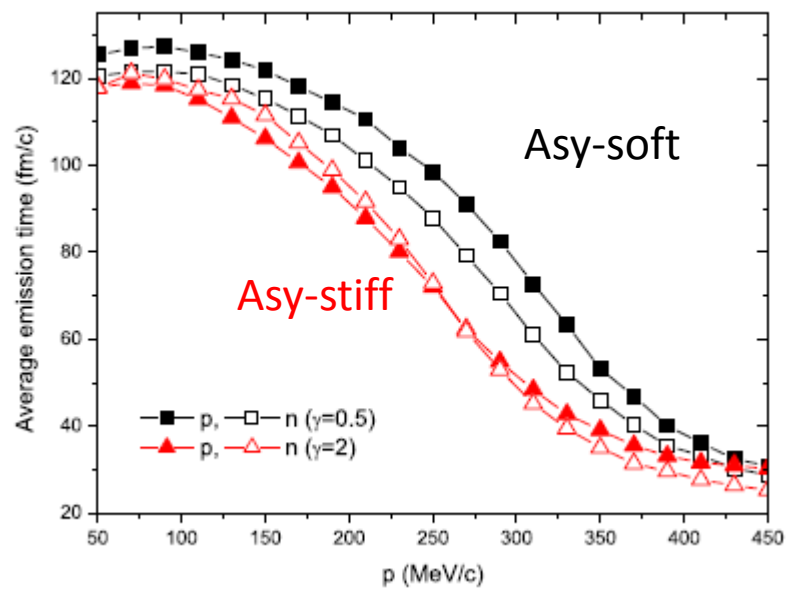
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Shorter neutron and proton average emission times and more similar n and p emission times with Esym - stiff

See Henzl et al., PRC85 014606 (2012)  
Larger source size for more n-rich systems: Asy-EOS, size effect... ?

# A new setup: the 4 $\pi$ CHIMERA + a module of FARCOS prototype

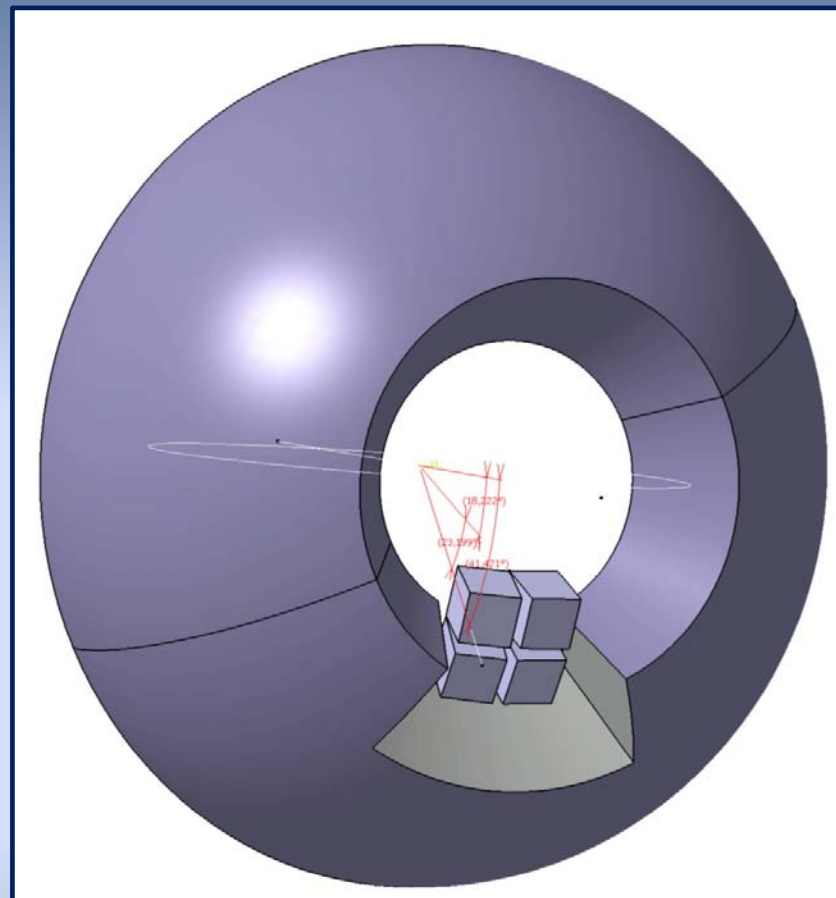
**FARCOS: Femtoscope Array for COrelations and Spectroscopy (INFN, Ganil, Huelva . . . )**

- Based on (62x64x64 mm<sup>3</sup>) clusters
- **1 square (0.3x62x62 mm<sup>3</sup>) DSSSD 32+32 strips**
- **1 square (1.5x62x62 mm<sup>3</sup>) DSSSD 32+32 strips**
- **4 60x32x32 mm<sup>3</sup> CsI(Tl) crystals**

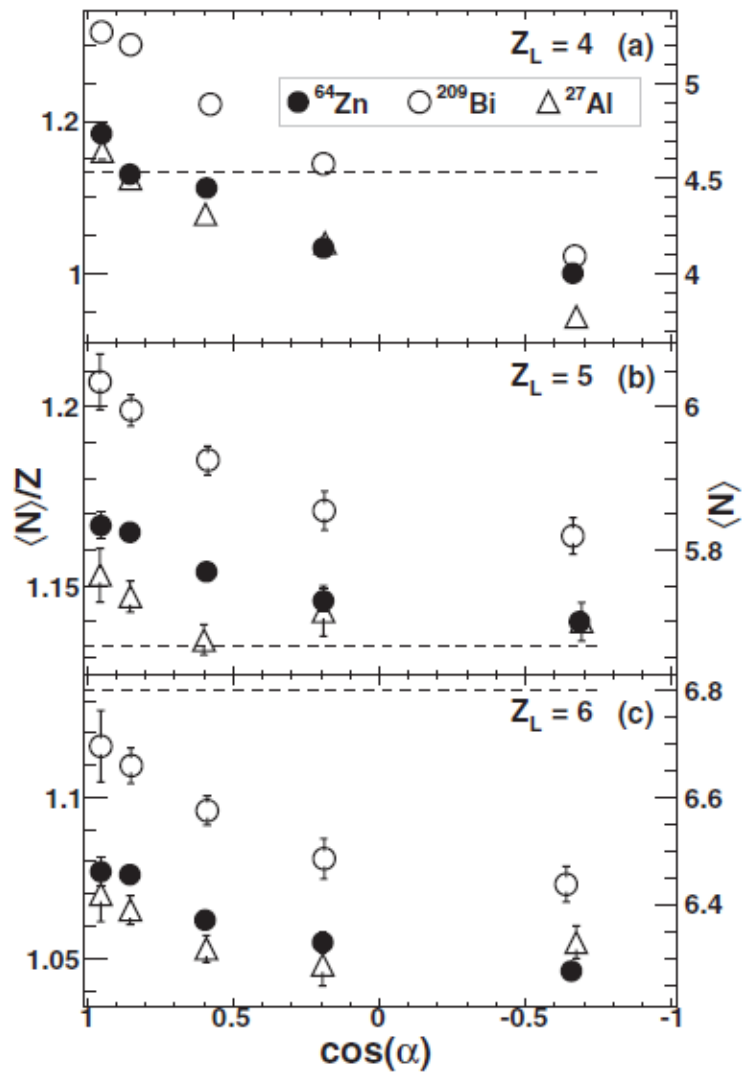


132 channels by each cluster

See T. Minniti talk (Wednesday)



4 telescopes 25 cm from the target  
 $\theta_{\text{lab}} \sim 16\text{-}44 \text{ deg}$ ,  $\Delta\phi \sim 45 \text{ deg}$



$^{64}\text{Zn}$  45 A.MeV.

Brown et al.,  
PRC87 (2013)