

# Transport properties of nuclear matter in the Fermi energy domain

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# Content

- Study of the **stopping reached in central collisions** for HIC between  $15A$  and  $100A$  MeV
- Analysis of **exclusive data** recorded with **INDRA  $4\pi$  array** :  
Large scale analysis :  $42$  symmetric systems from  $72$  to  $476$  *uma*
- **Energy and mass dependence** for stopping
- Determination of **in-medium properties** of nucleons in nuclear matter :  $\lambda_{NN}$  and  $\sigma_{NN}$

# Motivations

- Aspects connected to the **transport properties in the nuclear medium : energy dissipation and isospin diffusion**
- 
- Transport properties are mandatory for :
  - the description of **supernova collapse** and formation of **neutron stars**
  - the determination of the **nuclear EOS** via the underlying properties of the **nuclear interaction**
  - **microscopic descriptions** as one of the fundamental ingredient for the dissipative features: **EOS** and **collision term**

# Theoretical background

- Mean-Field effects : **1-body dissipation** and **viscosity/friction**  
Collective properties : **nuclear** degrees of freedom (Mean-Field)
- $NN$  collisions : **2-body dissipation** and  $\lambda_{NN}, \sigma_{NN}$   
Individual properties : **nucleonic** degrees of freedom (collisions)
- **Crossover** in incident energy should be observed where  
MF weakens and  $NN$  collisions become more and more likely
- **In-medium effects** for  $NN$  collisions :
  - **Renormalization** of  $\sigma_{NN}$  as compared to vacuum: **quenching factor**
  - Due to **Pauli blocking** (2-body) but also to **higher-order correlations** (density effects *via* many-body correlations).

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**Mean free path is (quite) constrained both theoretically and experimentally above  $E_{inc}/A > 100$  MeV:  $\lambda_{NN} = 4-5$  fm but not below...**

See A. Rios and V. Soma, PRL **108**, 012501 (2012)

# Experimental background

Overview of **degree of stopping** between 10A MeV and 2000A MeV

- **FOPI data** for Au+Au between 90A and 1930A MeV : **saturation** for the maximal stopping around 200A-400A MeV

A. Andronic *et al.*, Eur. Phys. J. A **30**, 31-46 (2006)

- **INDRA data** for Ar+KCl/Ni+Ni/Xe+Sn/Au+Au between 15A and 100A MeV : **minimum** around  $E_{inc} = 35A$  MeV, **transition** from 1b to 2b dissipation

G. Lehaut *et al.* (INDRA and ALADIN coll.), Phys. Rev. Lett. **104**, 232701 (2010)

## Goal of the present study :

- **Extend the former analysis for the full set of INDRA data for symmetric systems : Ta+Au, Gd+U, U+U**
- **Relate the stopping properties to NN collisions : in-medium  $\lambda_{NN}$  and  $\sigma_{NN}$  at high incident energy, *i.e.* above the transition energy**

# Event selection

- Study the **isotropy ratio** for complete (forward) events :

$$R_E = \frac{\sum_i^N E_i^\perp}{2\sum_i^N E_i^{\parallel}}$$

- Use of the total charged particle multiplicity  $M_{ch}$  (*scalar quantity*)
- Select events by  $M_{ch}$  such as  $\langle R_E \rangle$  is **maximal** in  $\langle R_E \rangle \otimes M_{ch}$
- Cross sections around  $50-150 \text{ mb}$  :  $b=0-2 \text{ fm}...$

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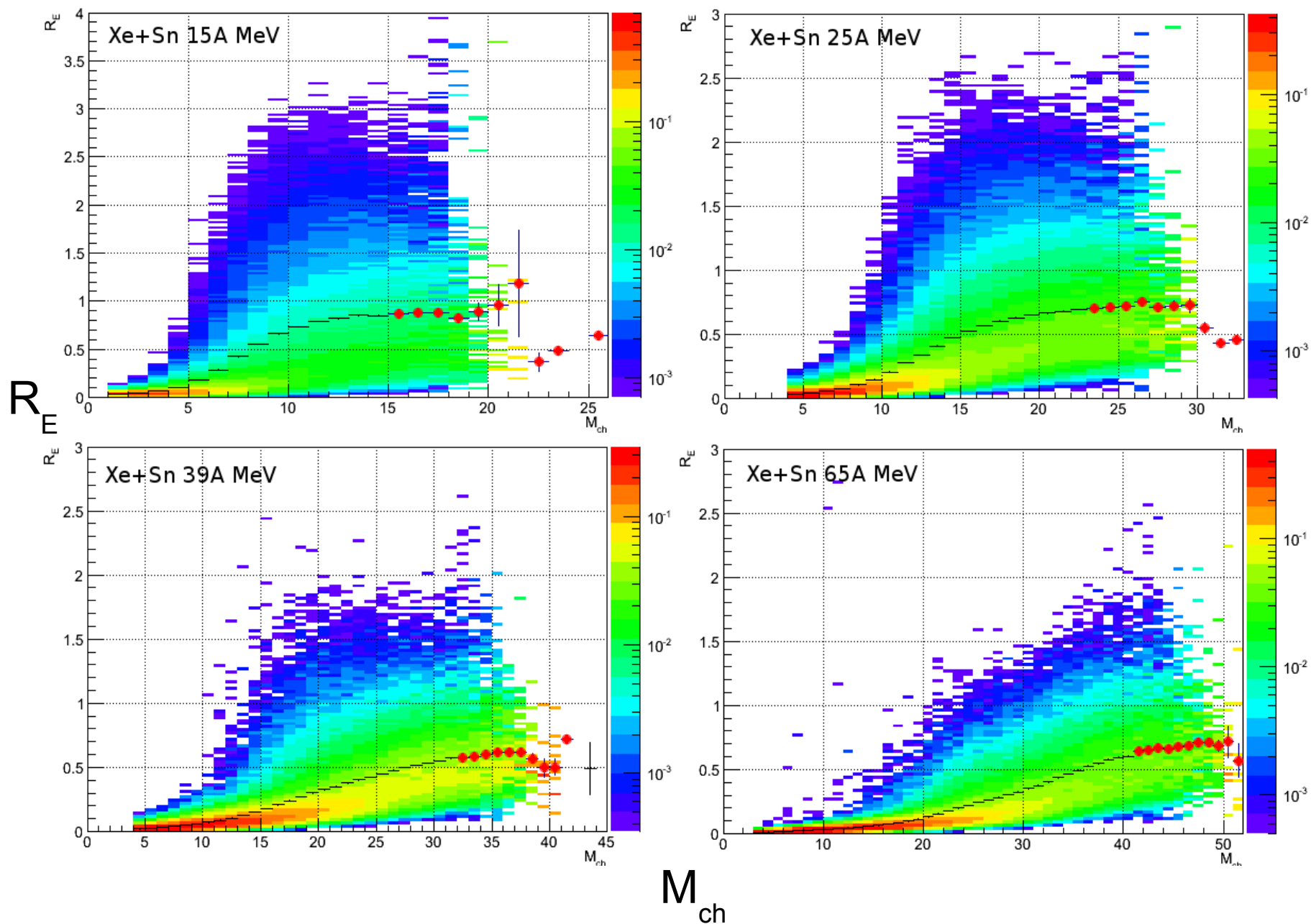
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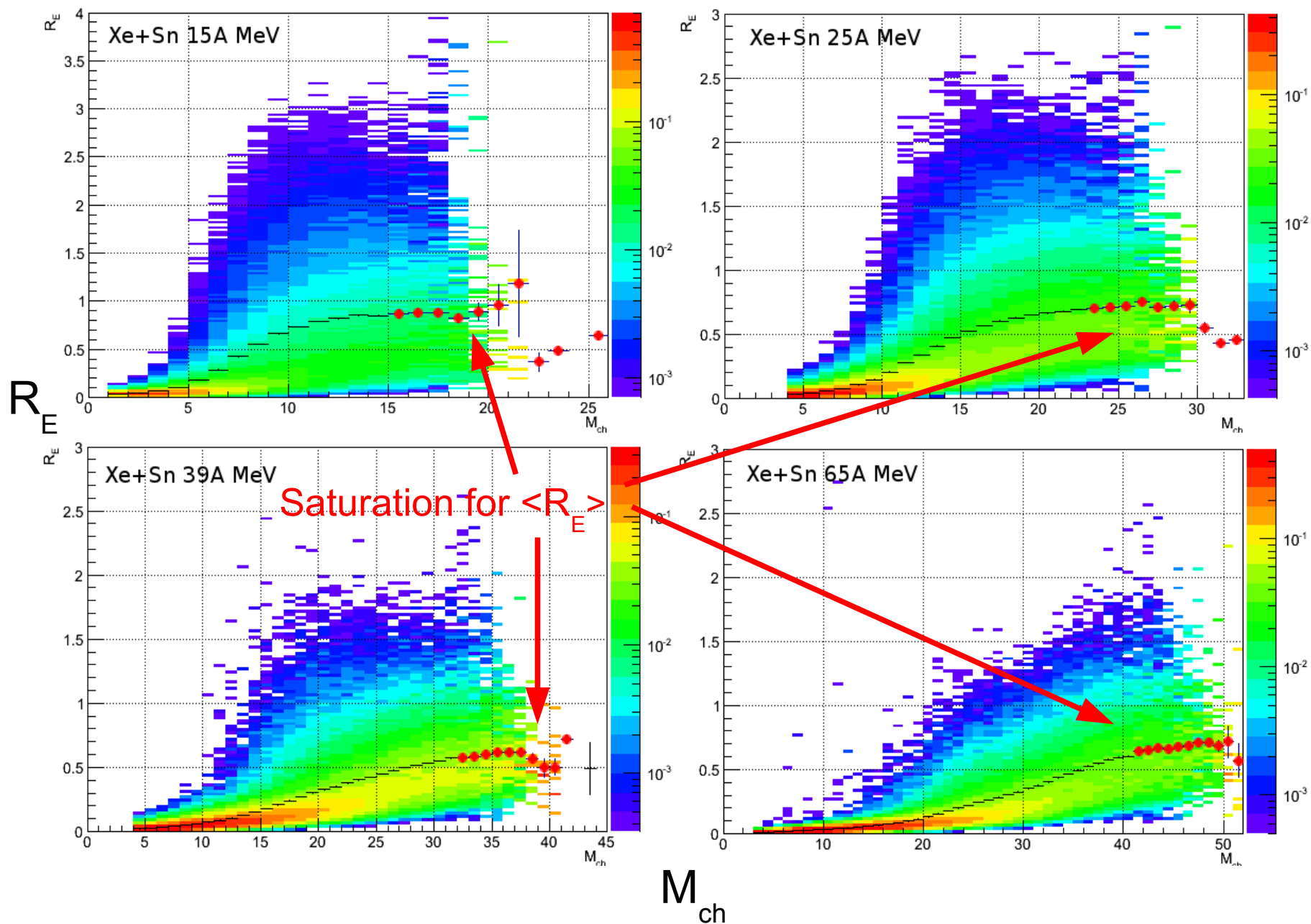
**We want here to insure a minimum bias measurement for  $R_E$  concerning the selected events ( $b < 2 \text{ fm}$ )**



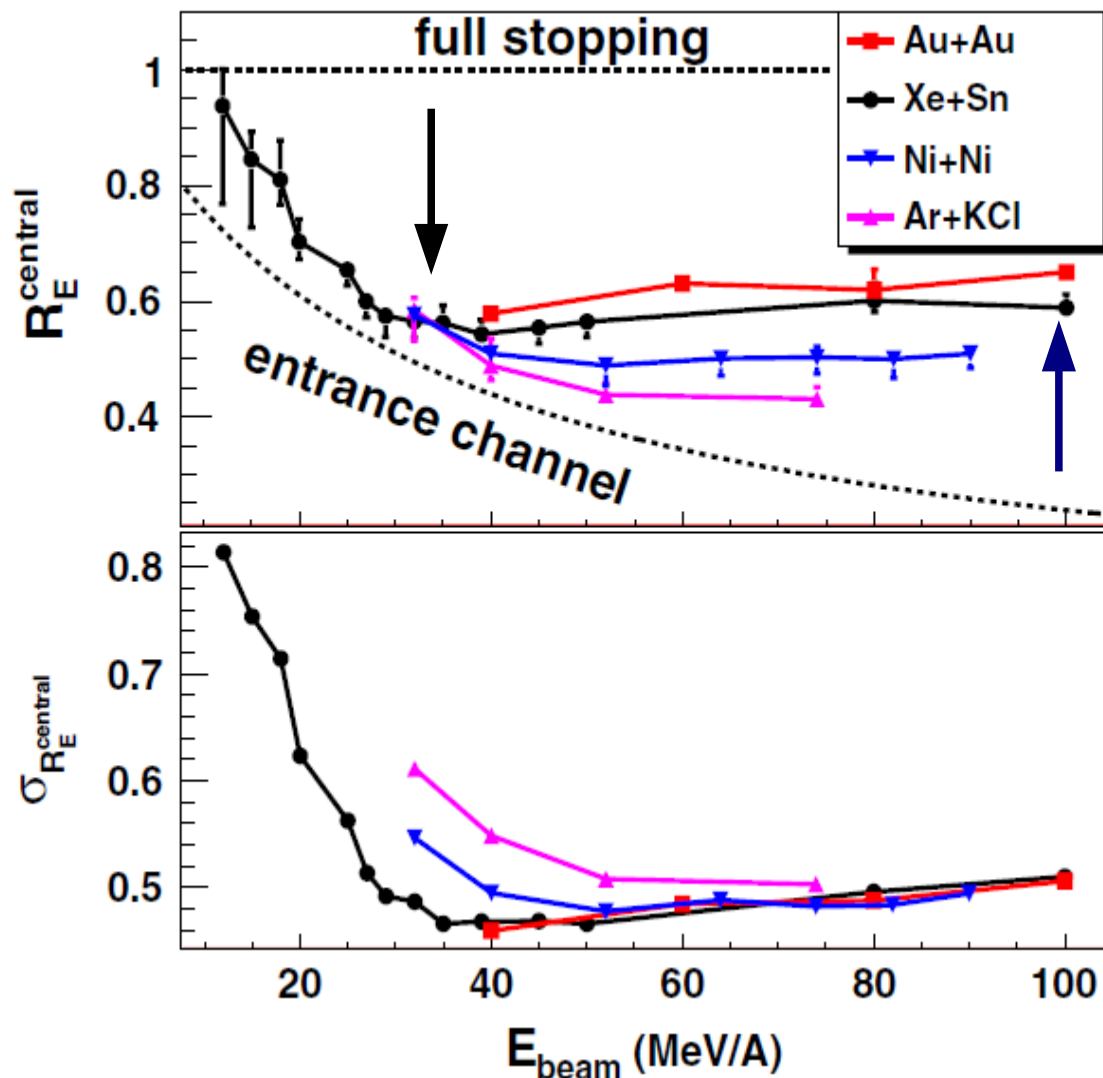
# Event selection



# Event selection



# From previous studies...



G. Lehaut *et al.* (INDRA coll.),  
Phys. Rev. Lett. **104**, 232701 (2010)

$$R_E = \frac{\sum_i^N E_i^\perp}{2\sum_i^N E_i^{\parallel}}$$

- Minimum of stopping around 35A MeV
- Mass hierarchy at high energy : attributed to NN (elastic) collisions

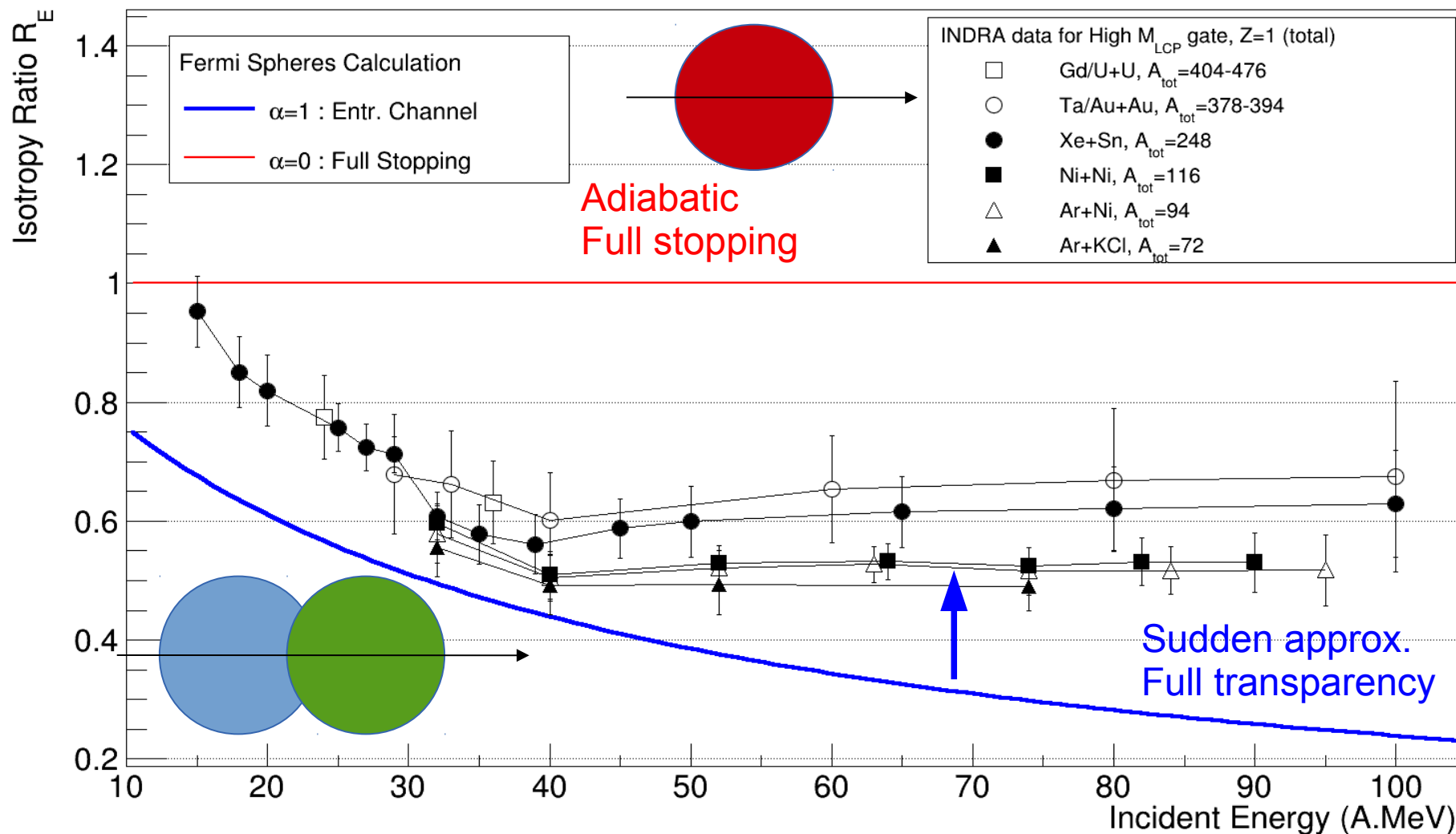
Here  $R_E$  is calculated with all charged products...

# Stopping in central *HIC*

42 (quasi)-symmetric systems,  
Only protons for  $\langle R_E \rangle \dots$

Nuclear Stopping

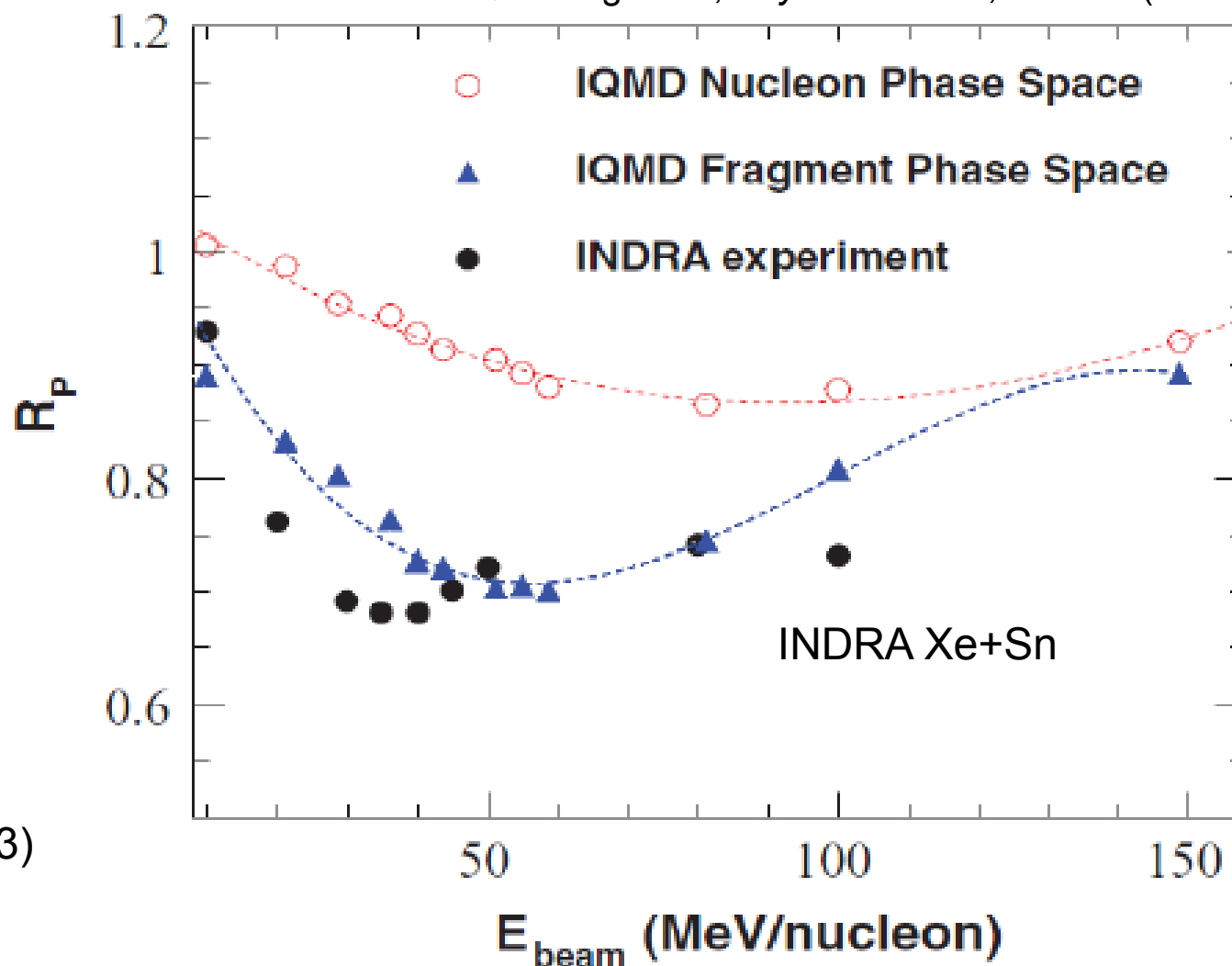
$$R_E(\alpha) = \frac{1}{1 + 5(\alpha P_{rel}/P_{Fermi})^2}$$



# Why using only protons ? (1)

From *IQMD* calculations :  $R_E$  ( $R_p$ ) is strongly influenced by the clusterization

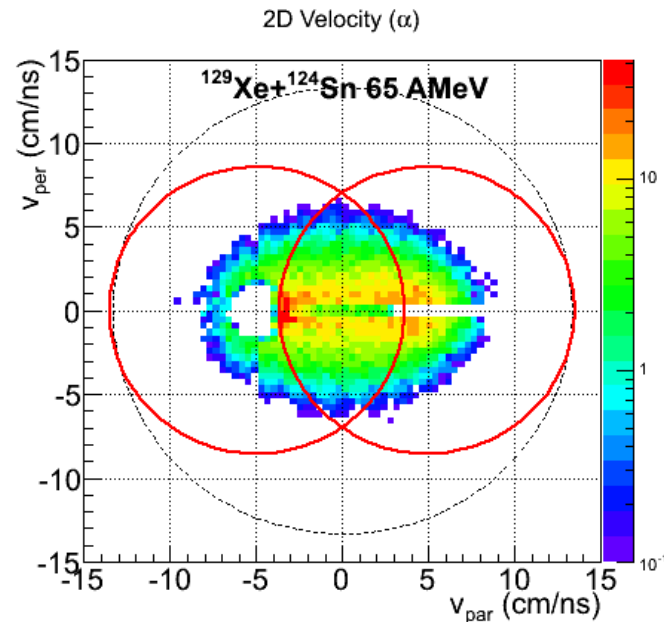
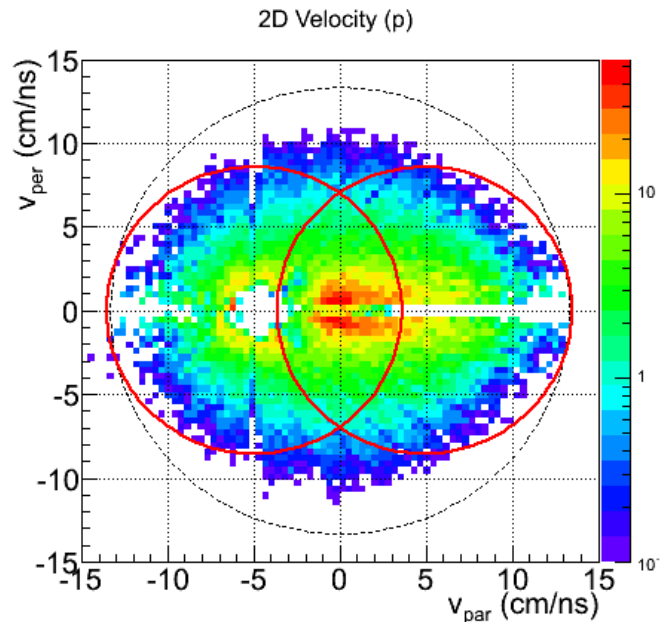
G.Q. Zhang *et al.*, *Phys Rev. C* **84**, 034612 (2011)



See also :  
 J. Su and F.S. Zhang,  
*PRC* **87**, 017602 (2013)

# Why using only protons ? (2)

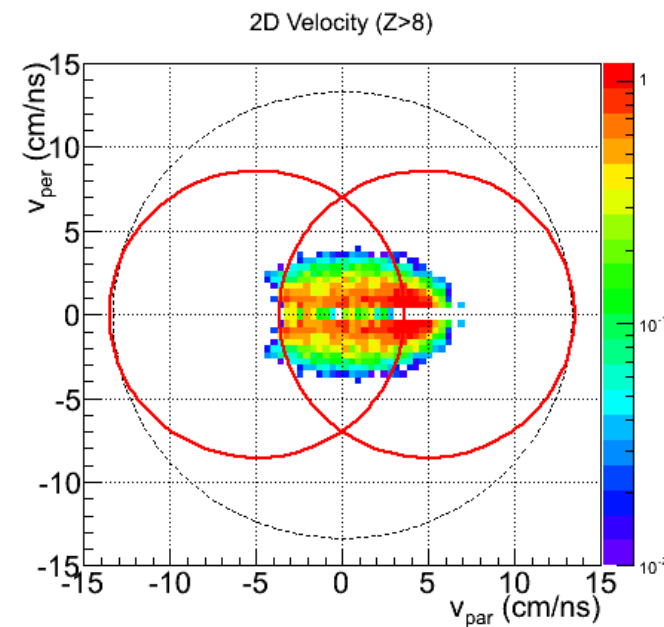
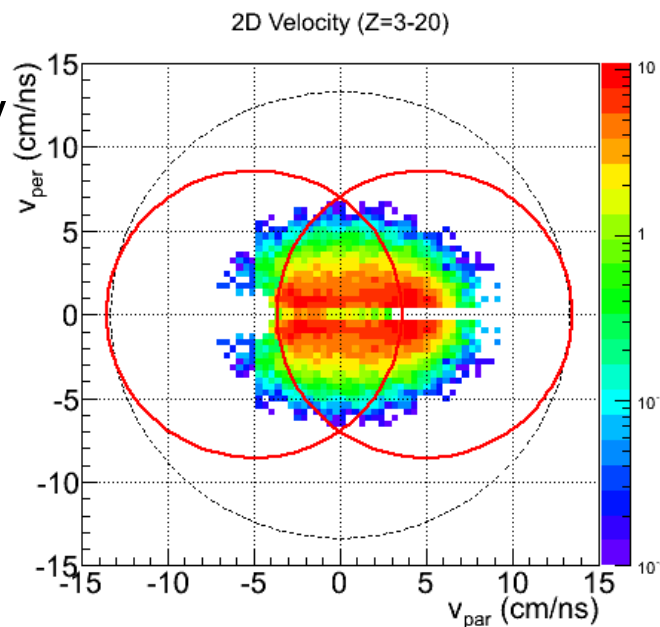
- Velocity plots for protons are significantly different from  $\alpha$  or composite particles/IMFs
- Mid-rapidity and transverse velocity components are dominant : preequilibrium effects



- Contribution from secondary decay are rather small :

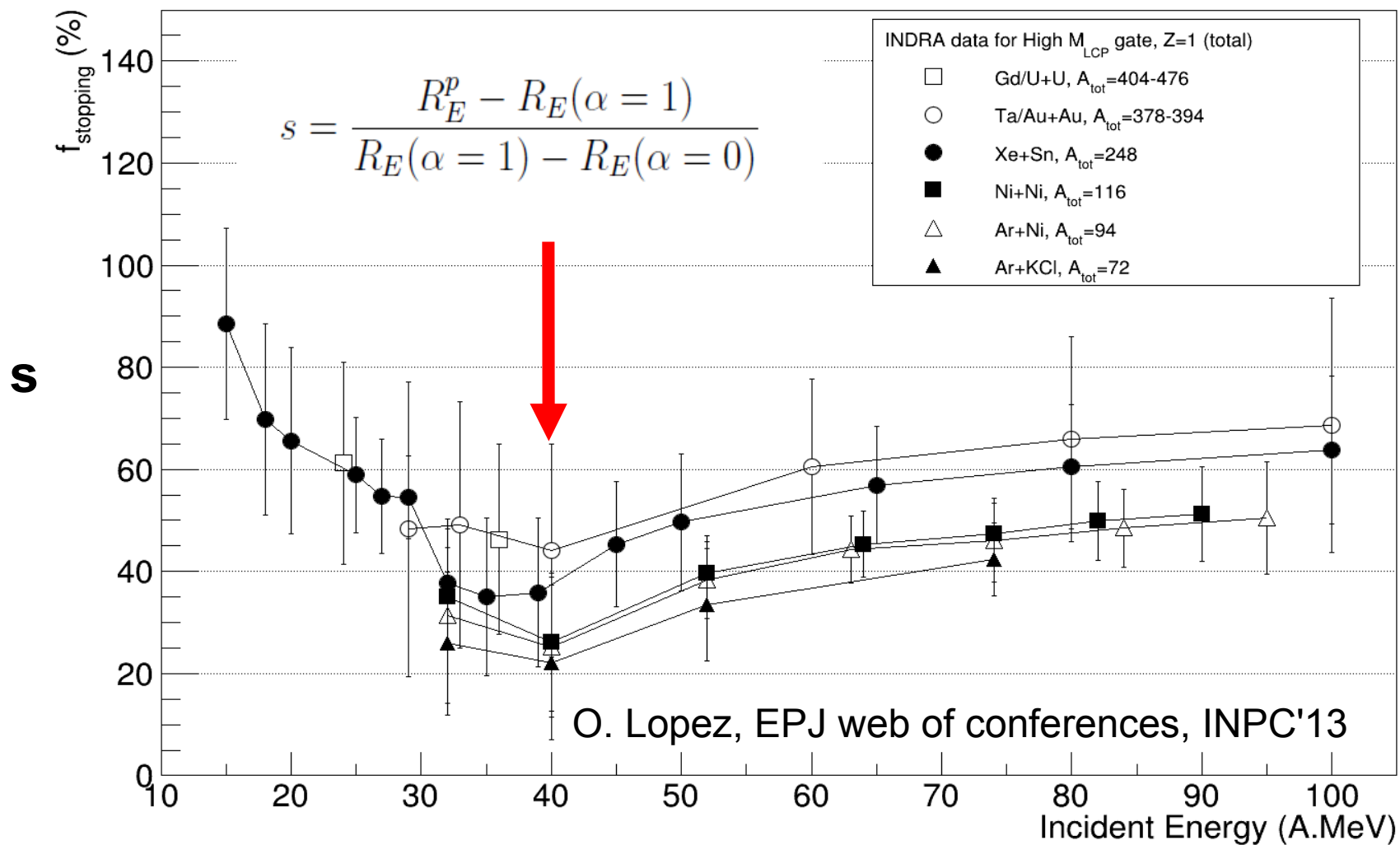
~20 % for Xe+Sn at 50A MeV

S. Hudan et al. (INDRA coll.),  
Phys. Rev. C 67, 064613 (2003)



# Stopping ratio

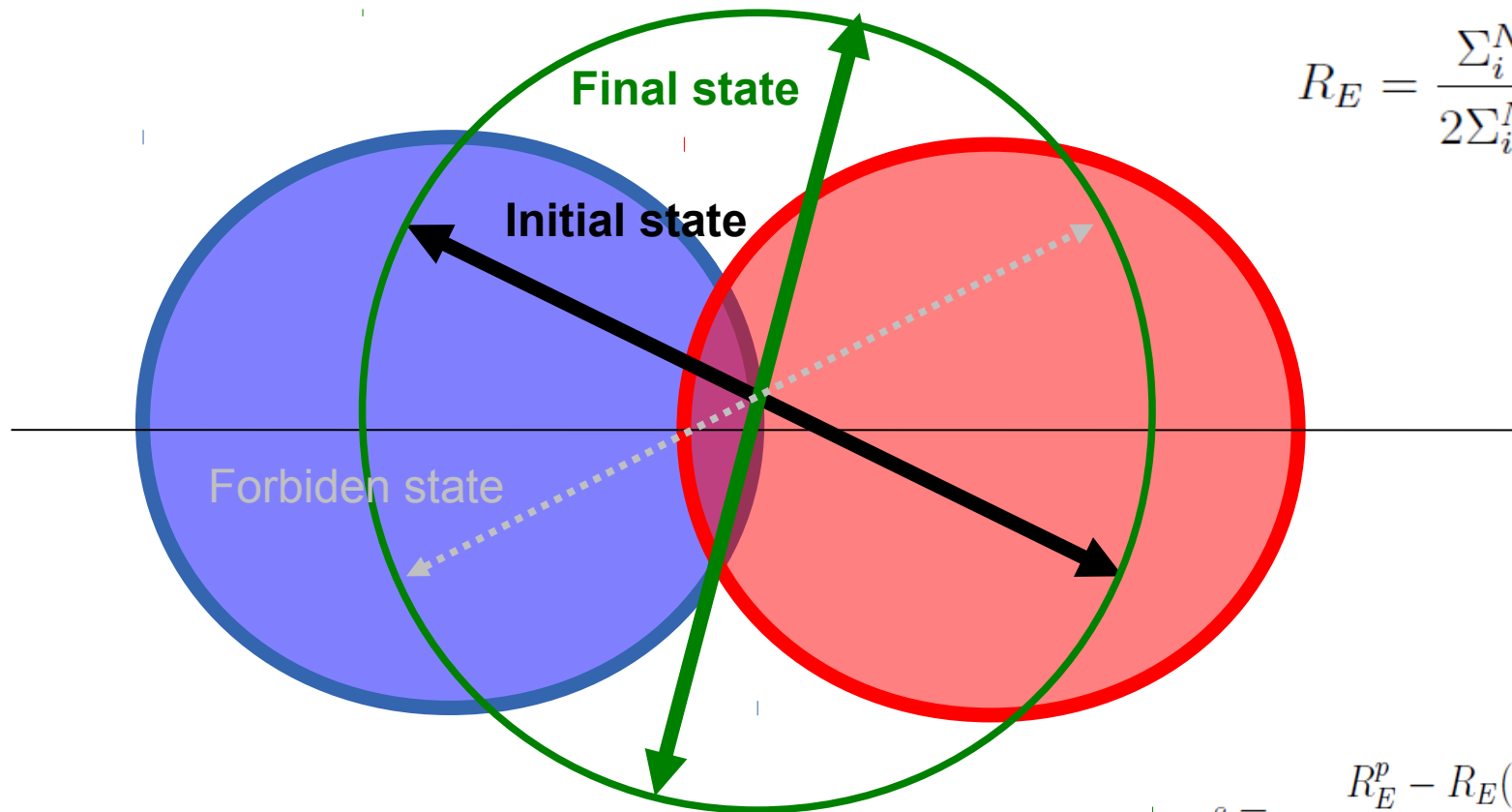
Distance to non-relaxed Fermi spheres



➤ **Stopping ratio and NN collisions ?**

# Phase space : 2 Fermi spheres + $NN$ collisions

% of  $NN$  collisions : random choice of nucleons in the 2 Fermi spheres



$$R_E = \frac{\sum_i^N E_i^\perp}{2\sum_i^N E_i^{\parallel}}$$

Elastic  $NN$  collision (semi-classical) : rotation in  $p$ -space

*Pauli* exclusion principle (fermions) : some rotations are forbidden

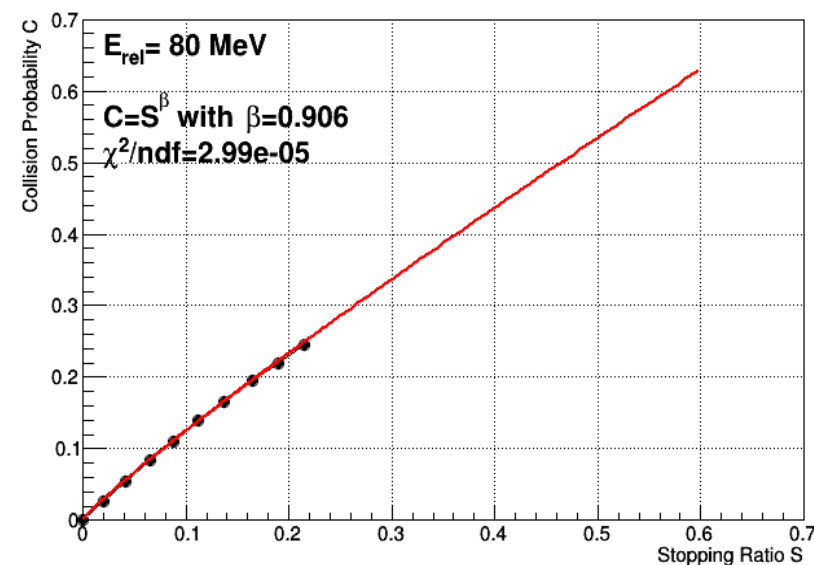
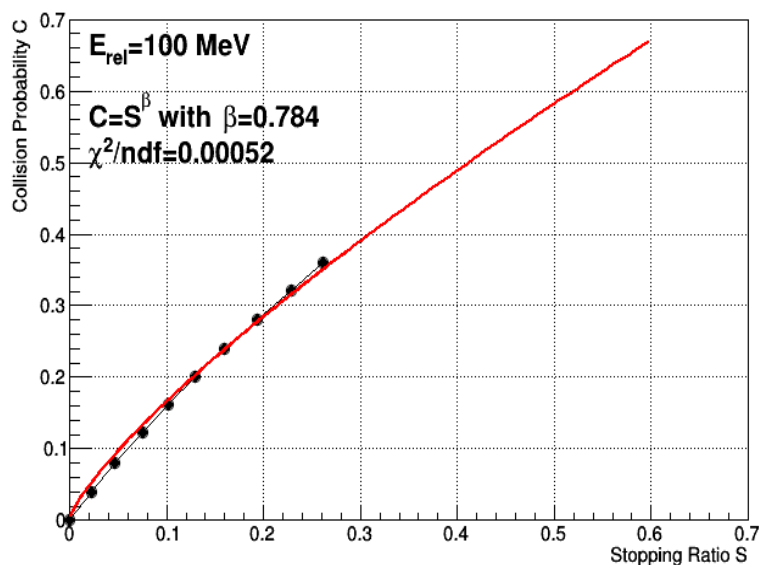
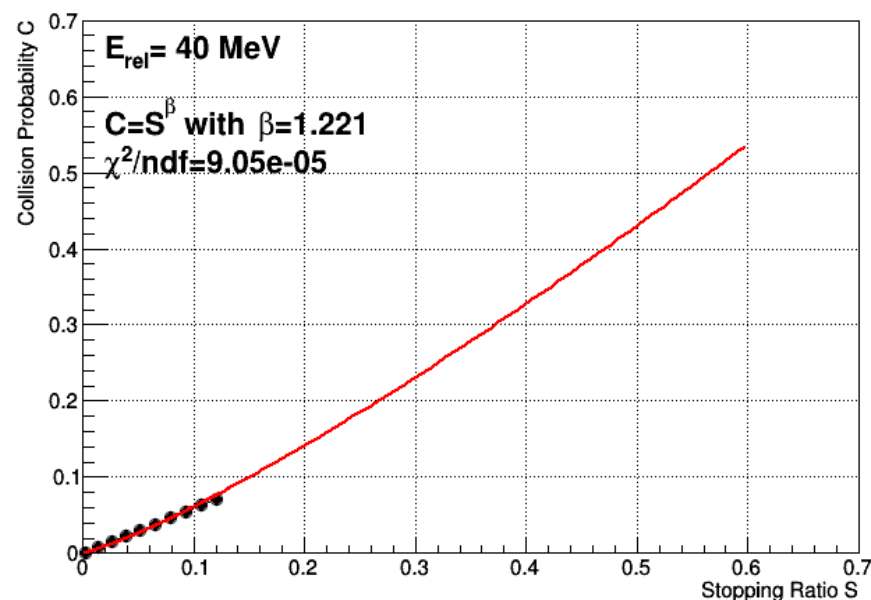
$$s = \frac{R_E^p - R_E(\alpha = 1)}{R_E(\alpha = 1) - R_E(\alpha = 0)}$$

**Isotropy ratio  $R_E$  and stopping ratio  $S$  are computed for all collisions (accepted or not)**



# Stopping ratio and $NN$ collisions

- 100,000 collisions are produced
- The number of accepted collisions is modulated from 0 (none) to 100 % (all accepted)
- $C$  is the ratio between attempted and accepted (realized) collisions

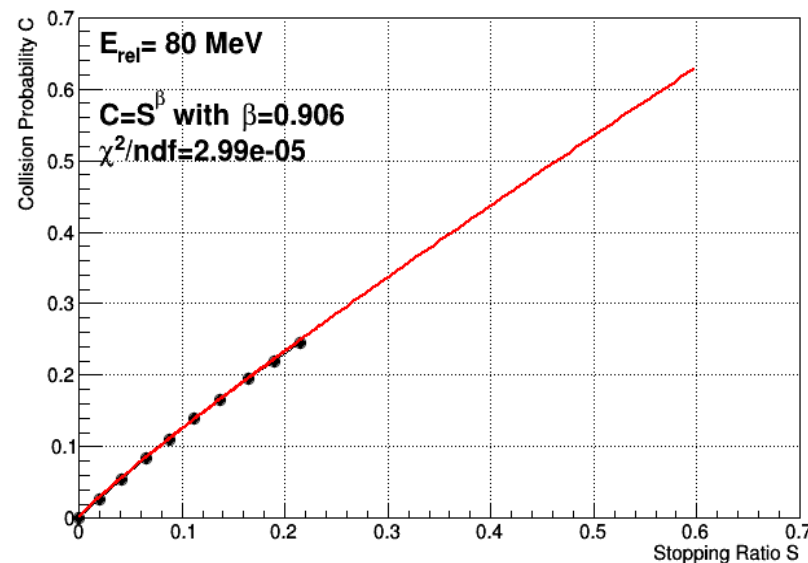
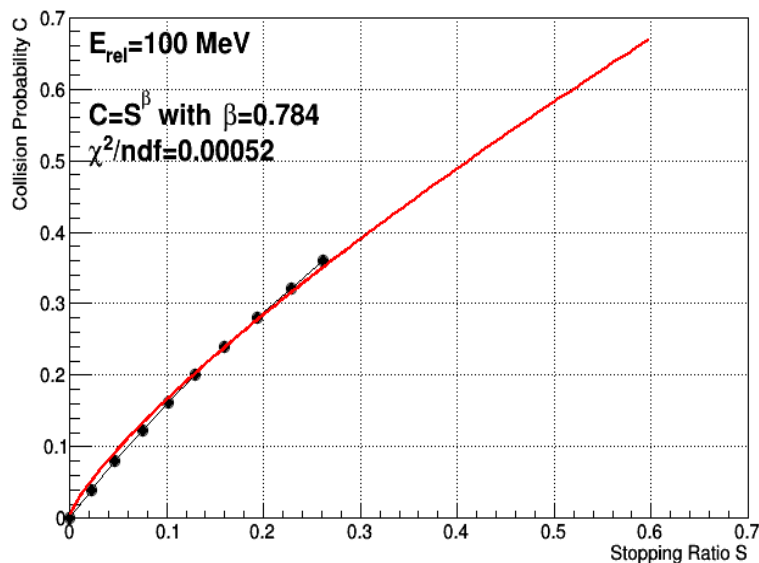
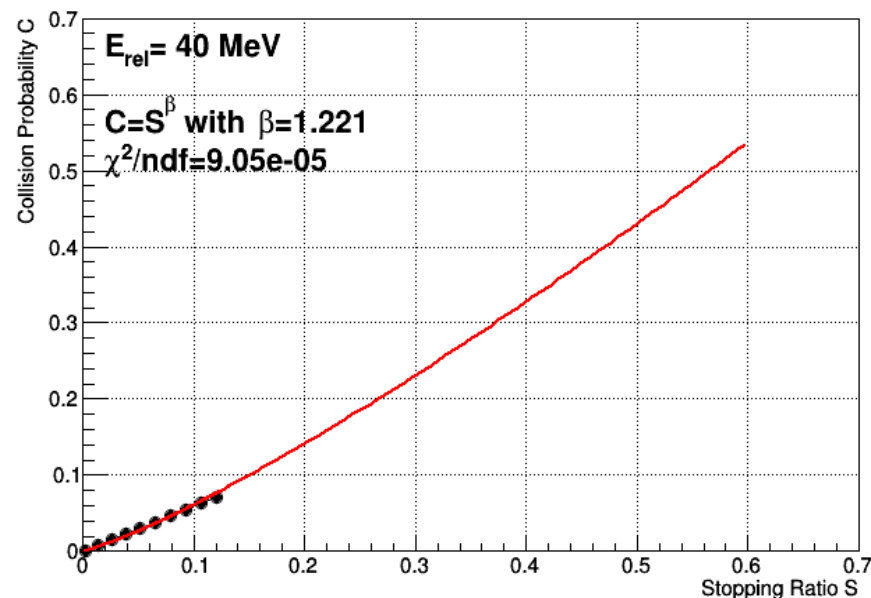


# Stopping ratio and NN collisions

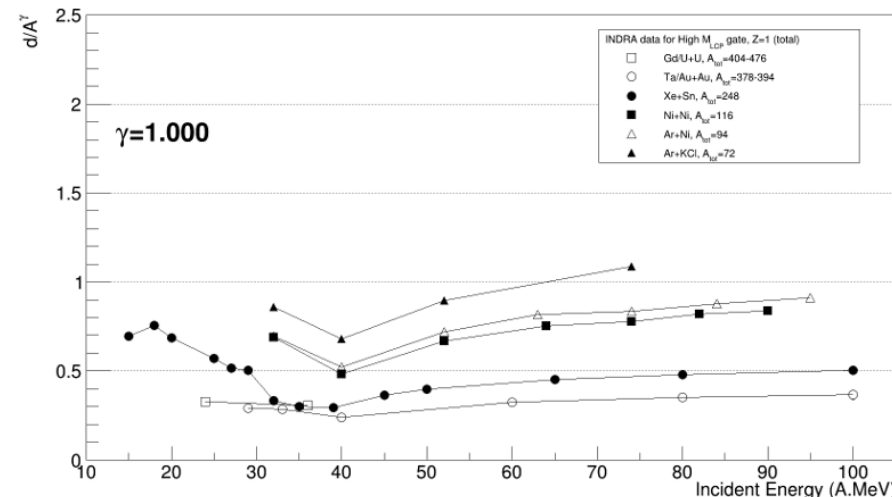
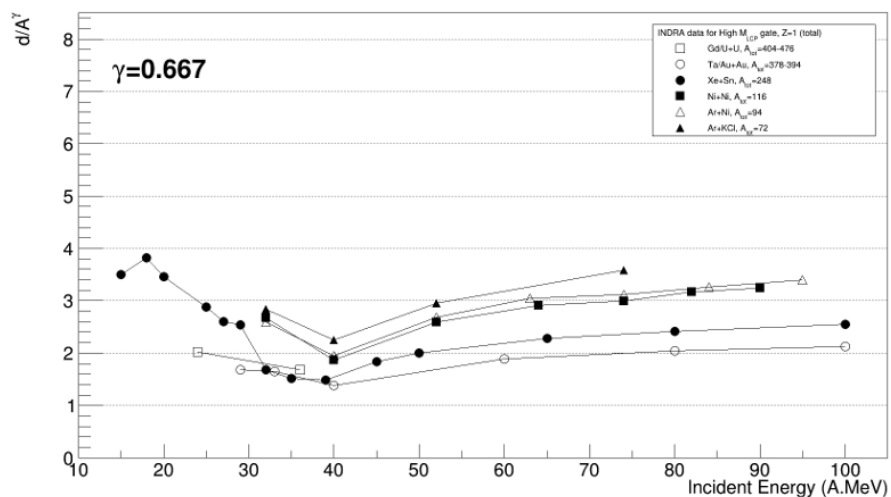
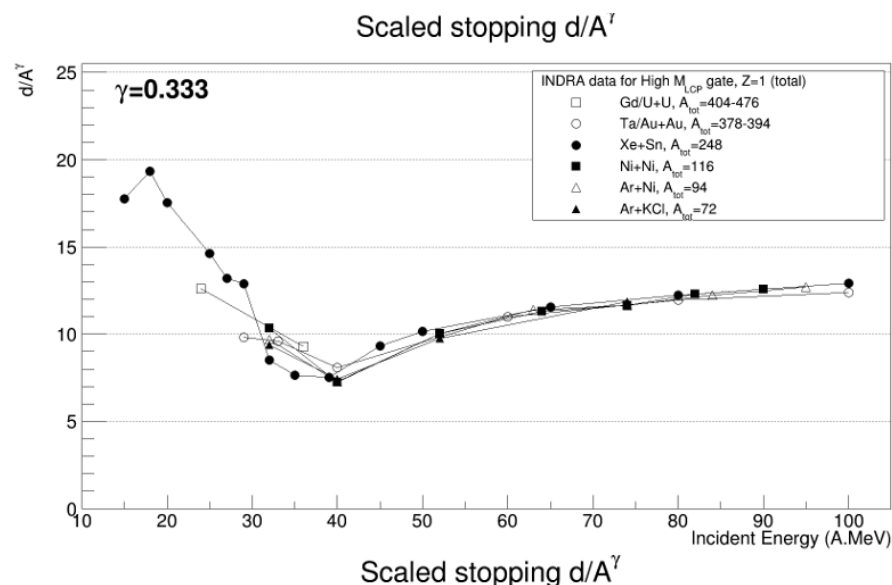
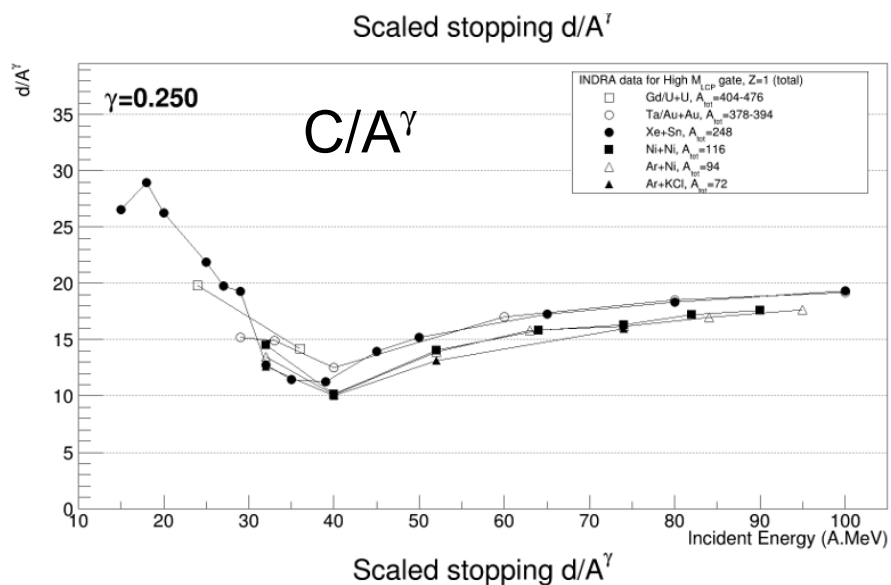
- 100,000 collisions are produced
  - The number of accepted collisions is modulated from 0 to 100 % (all accepted)
  - C is the ratio between attempted and accepted (realized) collisions
- From MC simulation, we get :

$$C = S^\beta$$

$$\beta(E_{rel}) = 1.42 - 0.0063 E_{rel}$$



# Mass scaling and Characteristic Length



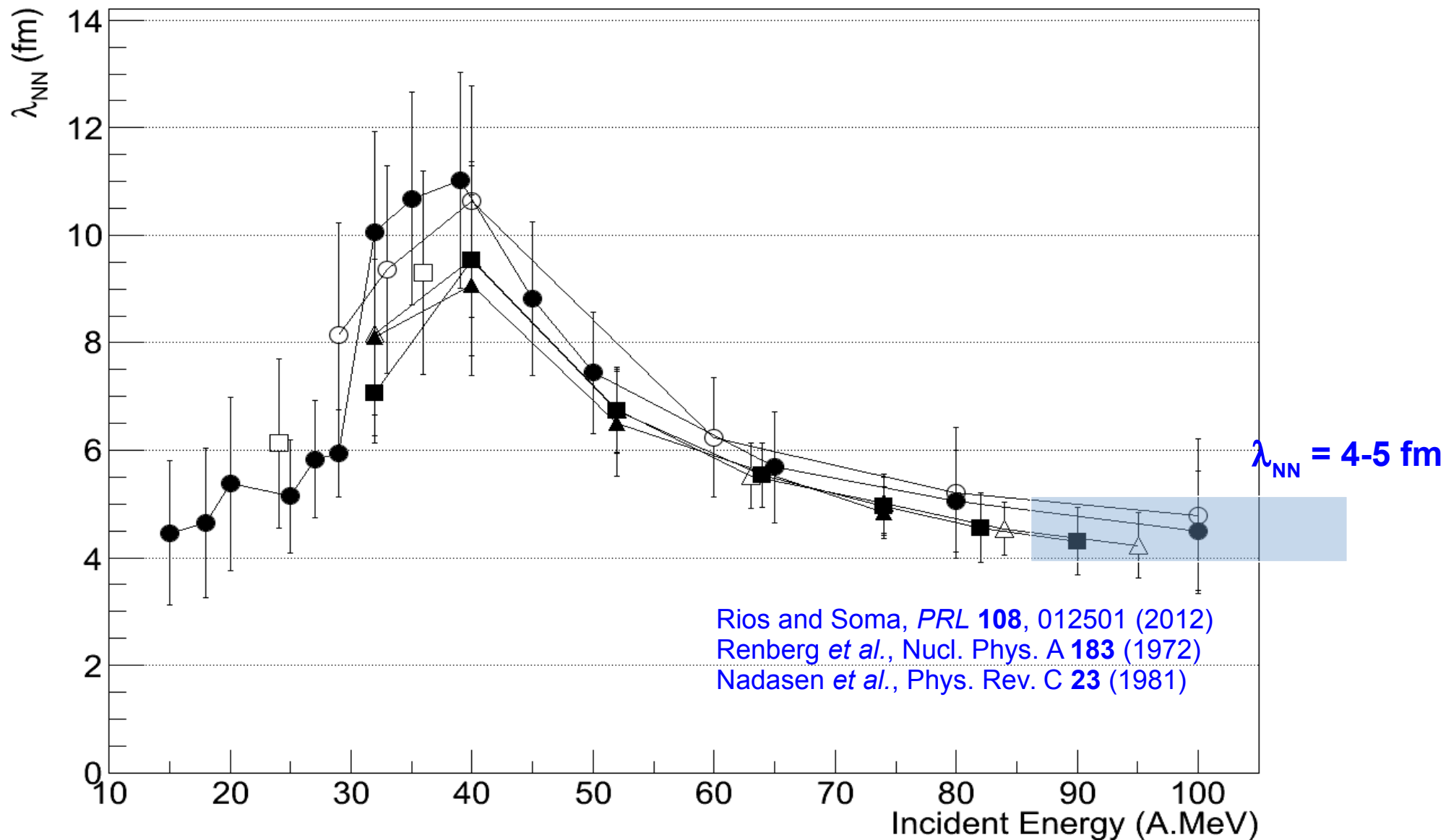
Mass scaling :  $C/A^\gamma$



Characteristic length :  $L \propto A^{1/3}$

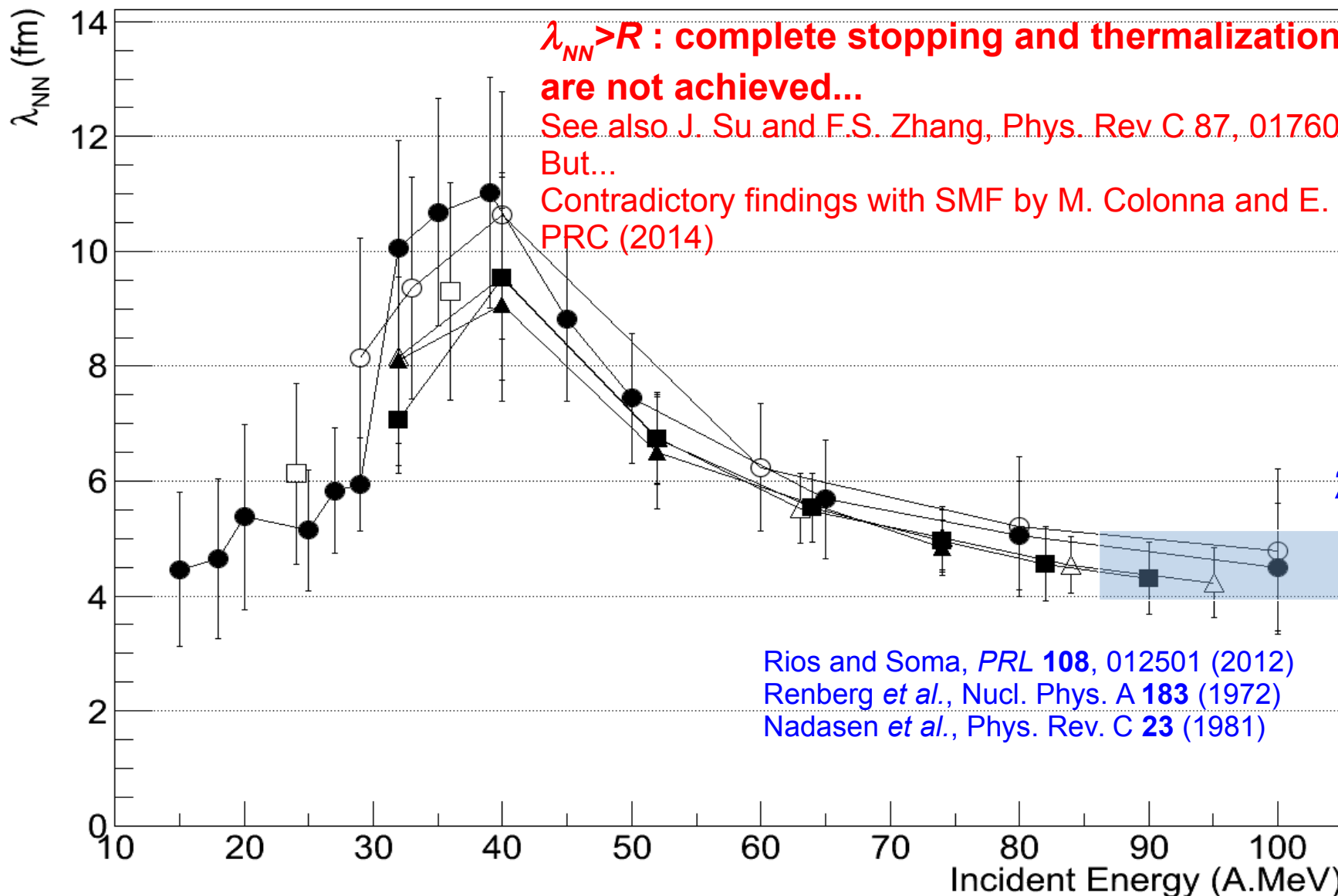
# Nucleon Mean Free Path

Assuming:  $C = L/\lambda_{NN}$

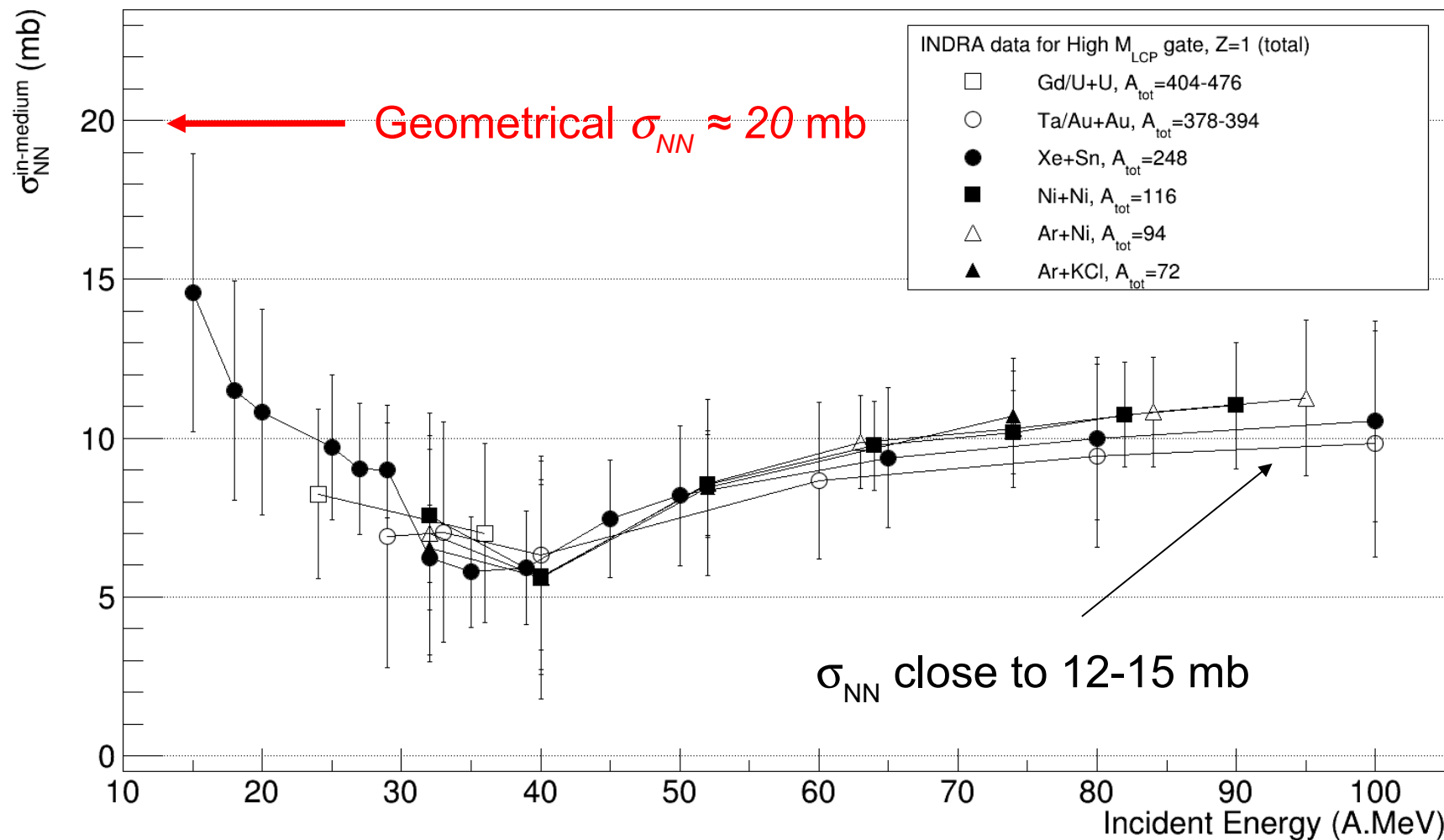


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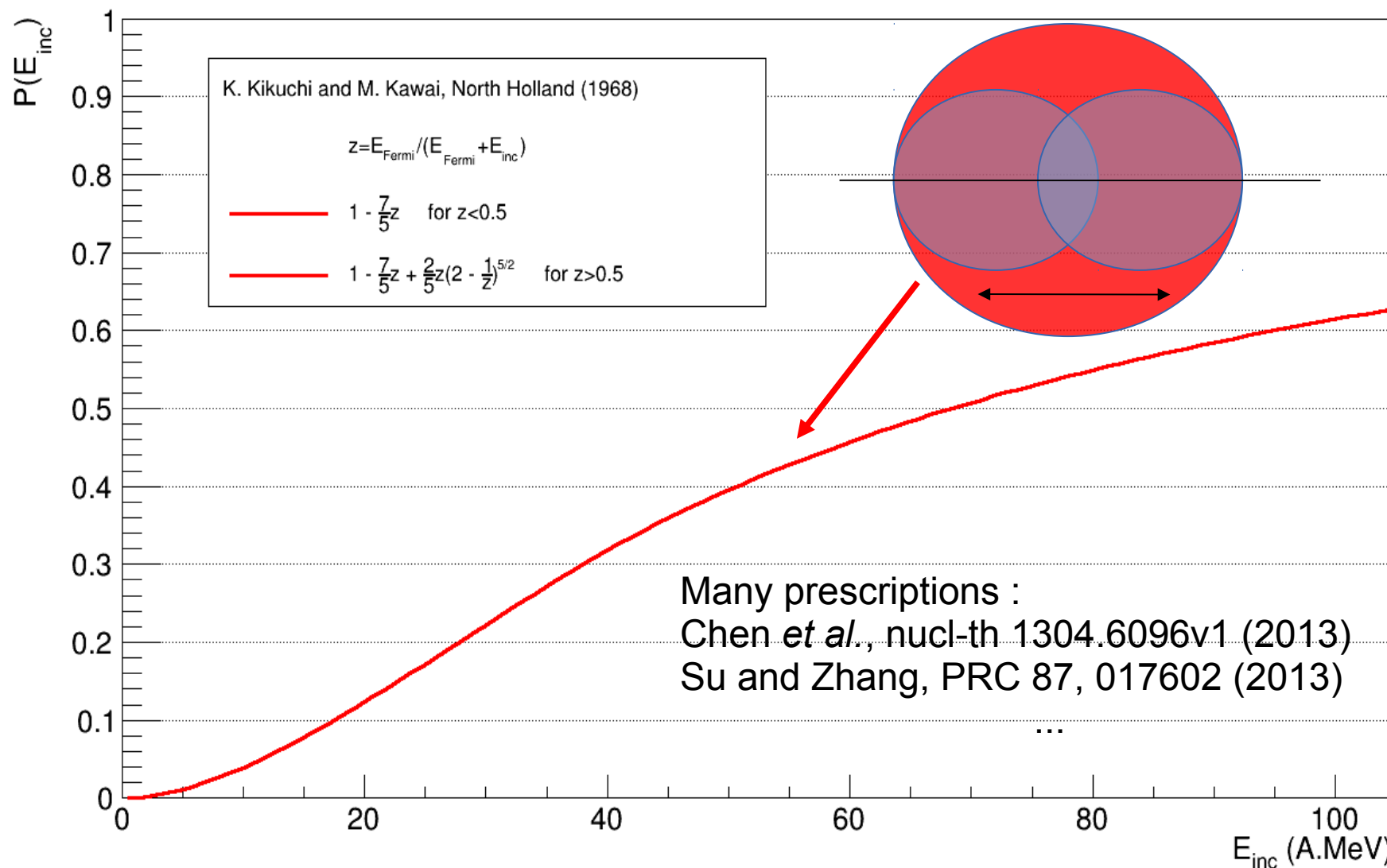
# NN cross section



$\sigma_{NN} \approx 1/\rho\lambda_{NN}$ , taking :  $\rho = 1.2\rho_0$  for central (overlapping) collisions

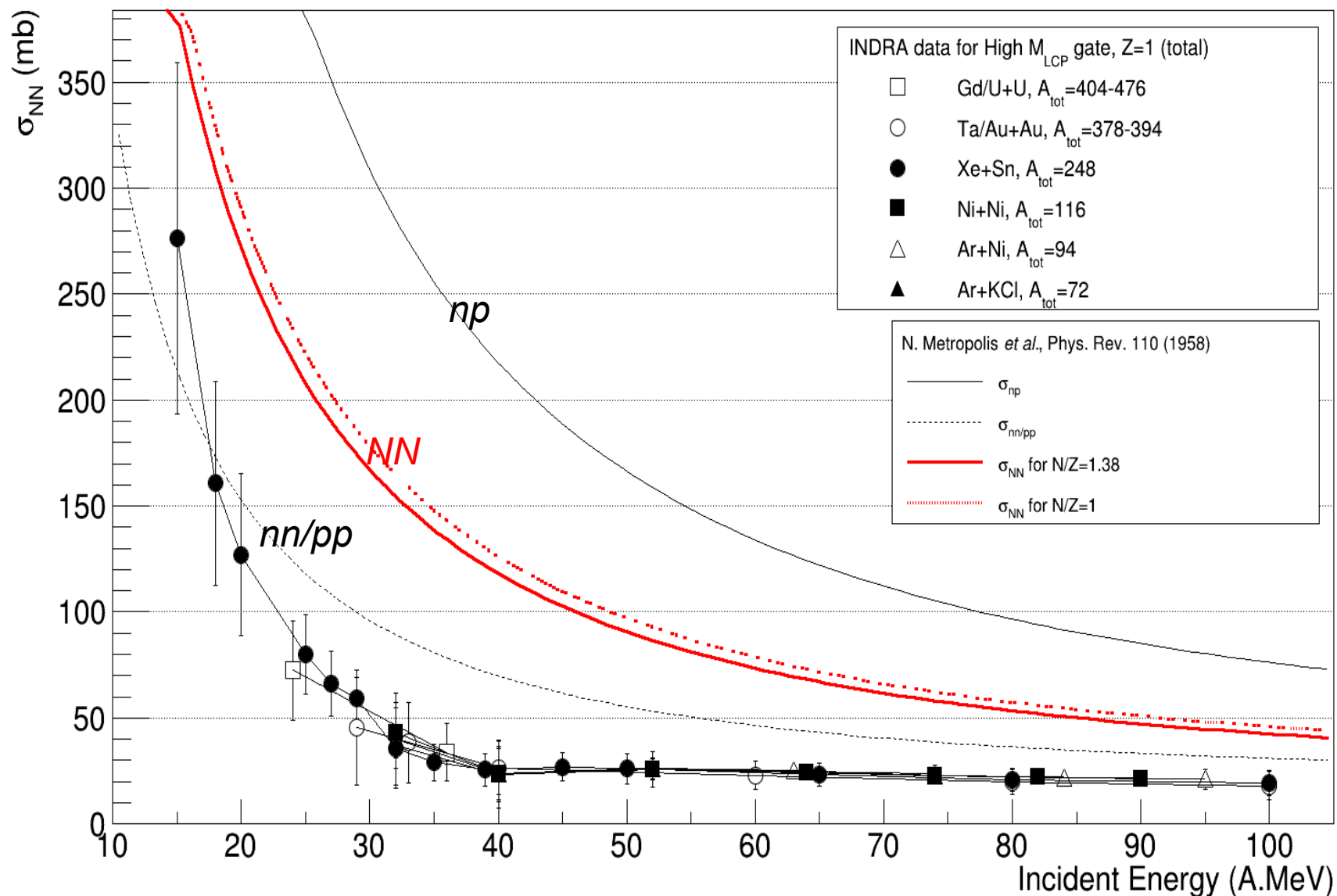
# In-medium effects : Pauli correction

Pauli Correction Factor  $P = \sigma_{NN}^{\text{in-medium}} / \sigma_{NN}^{\text{free}}$



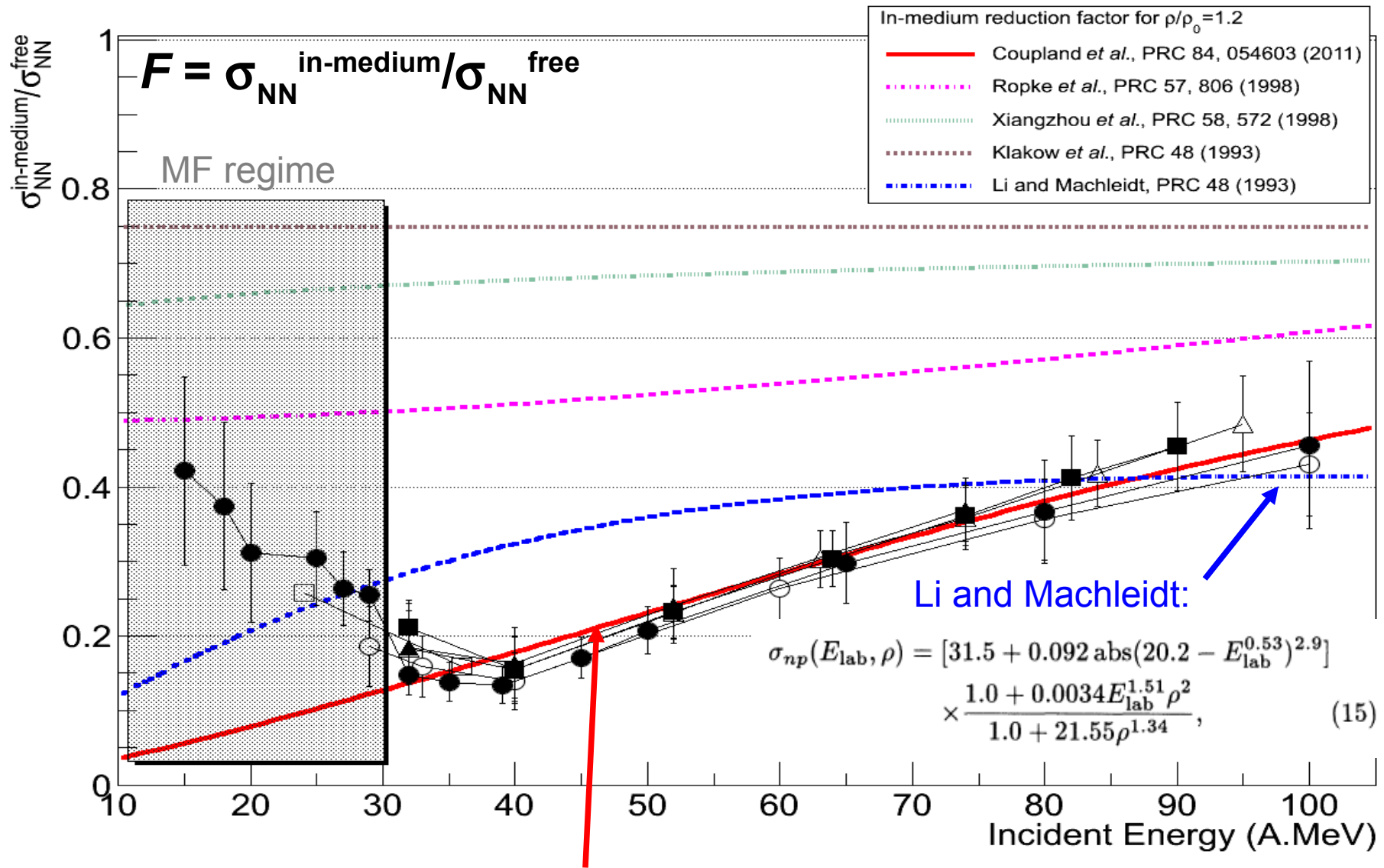
# In-medium effects : PB correction

'Free' NN cross section (Pauli-corrected),  $\sigma_{NN} = 1/(\lambda_{NN} \cdot \rho \cdot P(E_{inc}))$  with  $\rho = 1.5\rho_0$





# In-medium effects : quenching factor



Danielewicz (phenom. ):  $F = \sigma_0 \tanh(\sigma_{free} / \sigma_0)$ , with  $\sigma_0 = 8.5 / \rho^{2/3}$

# Conclusions

- **Mass scaling** is observed for  $R_E$  : size of the system => **characteristic length  $L$**
- **Mean Free Path** in nuclear matter, decrease by a factor of 2 between
- 40A and 100A MeV :

$$\lambda_{NN} = 11 - 5 \text{ fm}$$

**Complete stopping and thermalization are not achieved  
in this energy range for the selected central events... *tbc***

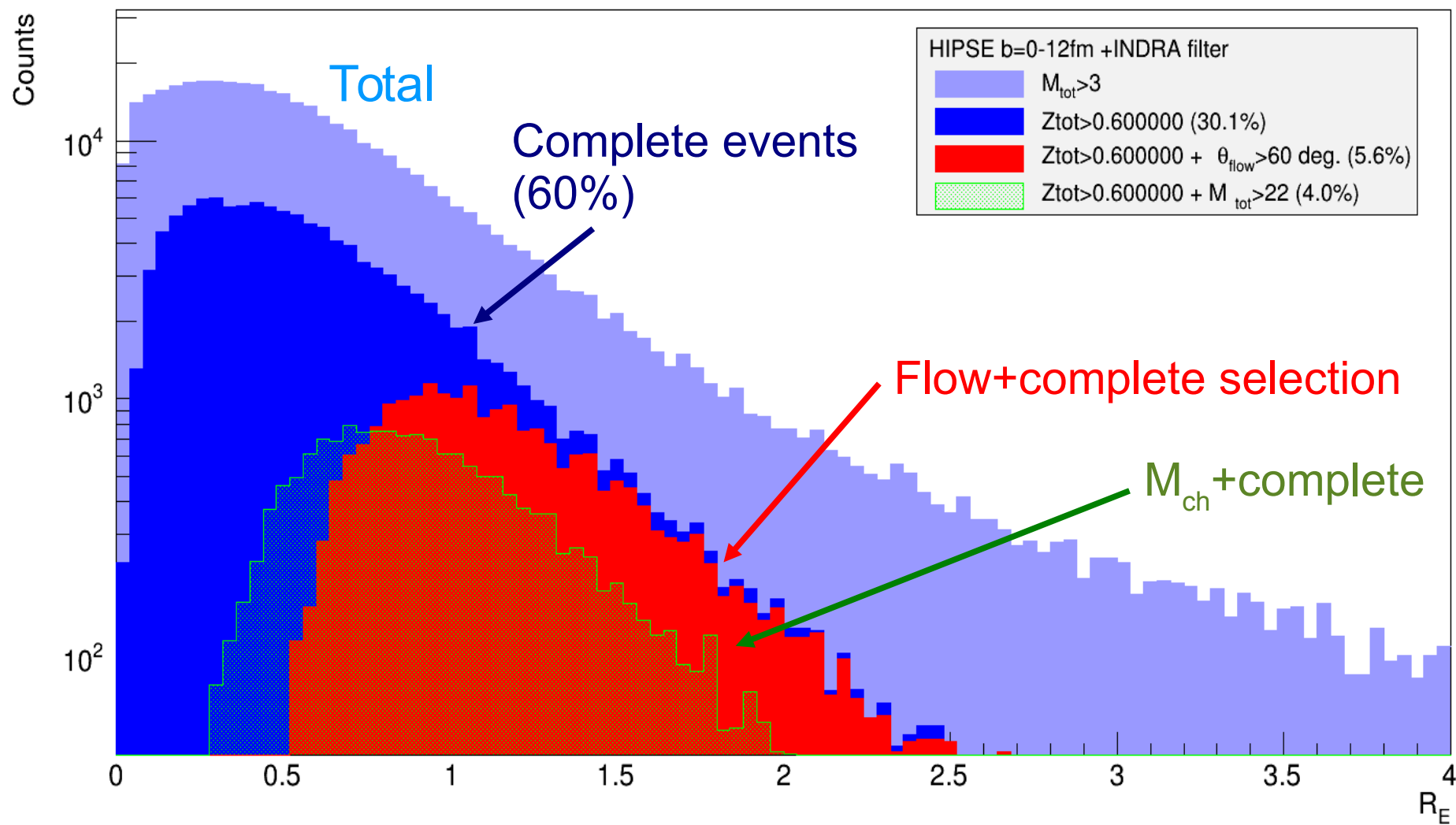
- 
- Study of **in-medium effects** :
  - Pauli effect is effective but ...
  - Density effects (**many-body correlations**) are also important and **cannot be neglected** in the Fermi energy range : **reduction x2-5**
  - Best description from **Danielewicz (Coupland) *et al.***
- Perspectives :
  - **Low incident energy** domain (<30A MeV) : **MF effects** to be evaluated properly
  - RIB : **isospin dependence** of the in-medium quantities and **isovector** properties of **NN interaction**

# Event selection...

*What can we learn from HIPSE ?*

# HIPSE Xe+Sn 32A MeV

## Isotropy Ratio $R_E$



# HIPSE Xe+Sn 32A MeV, $R_E \otimes b$

Entries 120844

