



Cluster features of stable and unstable nuclei in p-shell region

Y. Kanada-En'yo (Kyoto)

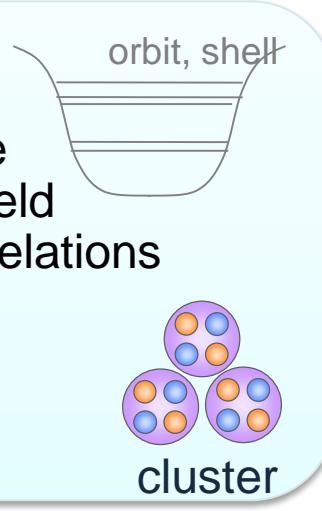
- 1. Introduction**
- 2. Cluster gas, chain states**
- 3. Cluster structures in Be isotopes**
- 4. Summary**

1. Introduction

Cluster & Mean field

Nuclear system

1. Independent-particle feature
in self-consistent mean-field
2. Strong nucleon-nucleon correlations
3. Saturation properties
 $\text{Energy/nucleon} \sim \text{constant}$

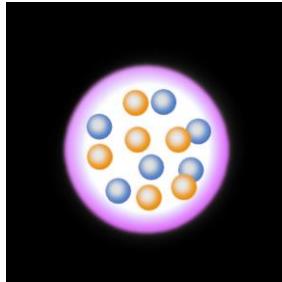


Single-particle motion
v.s.
Many-body correlation

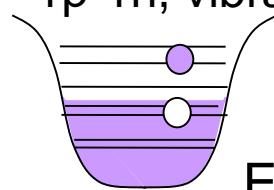


**Rich phenomena
in ground and excited
states**

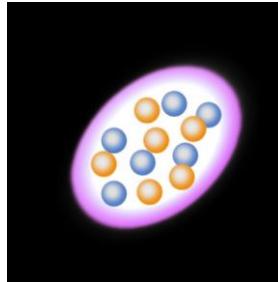
s.p. in mean field



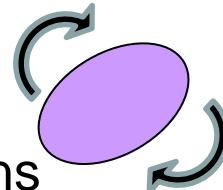
1p-1h, vibration



deformation

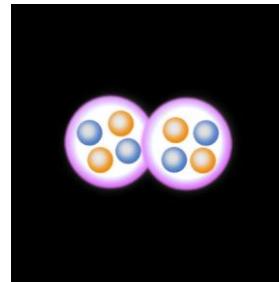


rotation

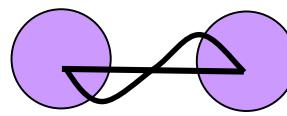


Excitations

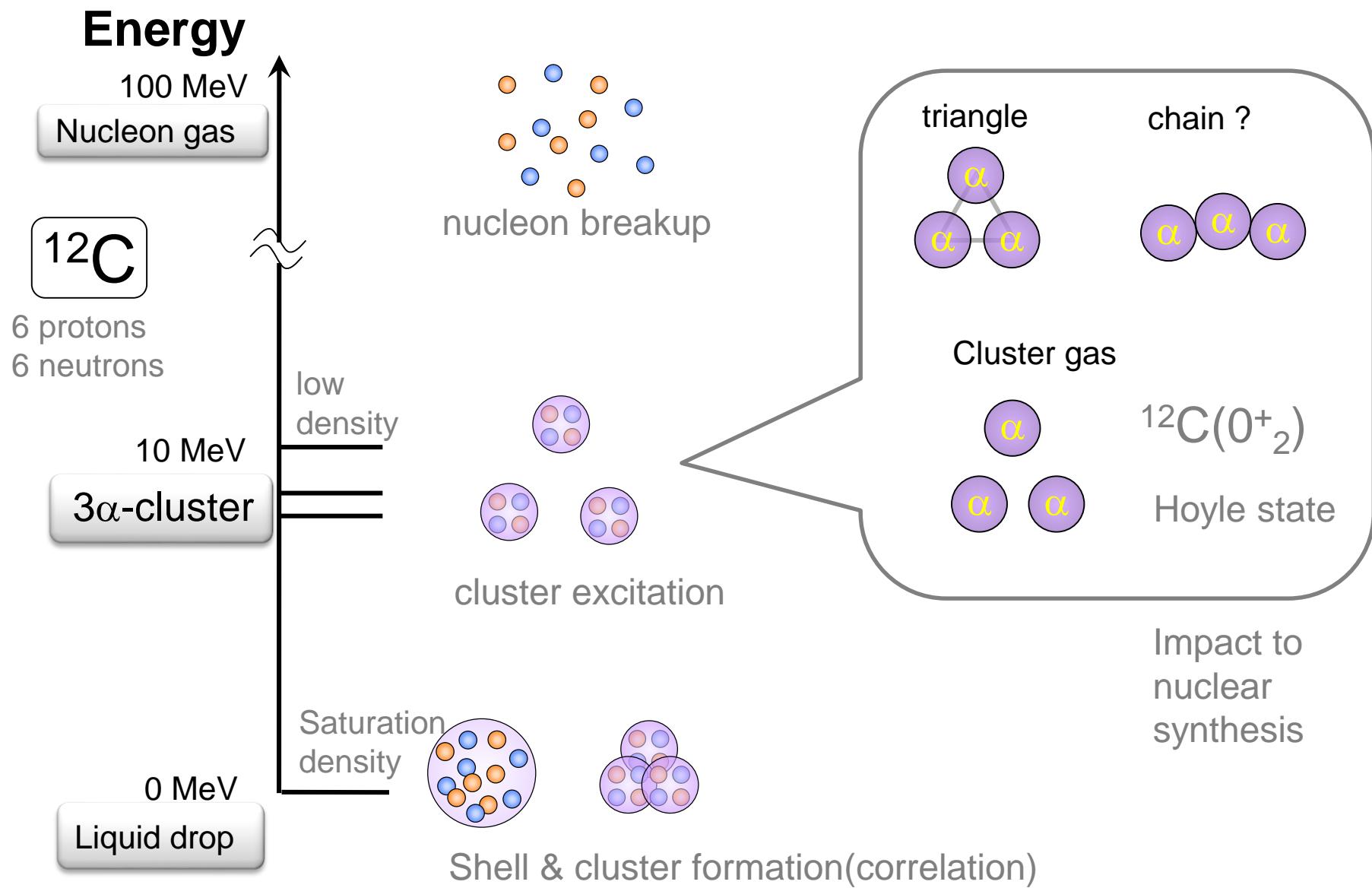
cluster



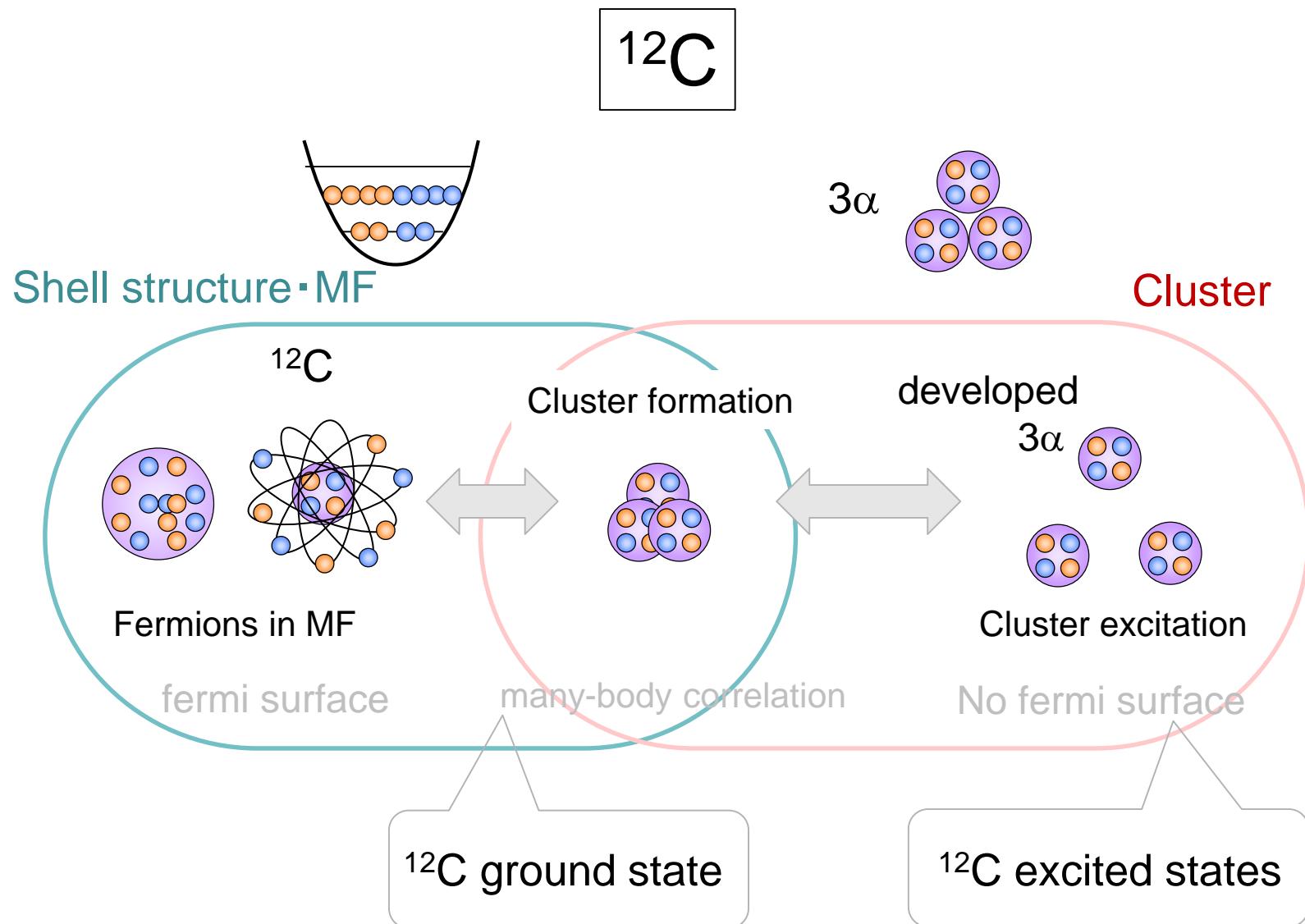
relative motion



Cluster states in low energy



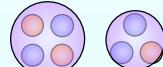
Coexistence of cluster and MF features



Cluster structures in stable and unstable nuclei

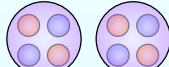
Typical cluster structures known in stable nuclei

^7Li



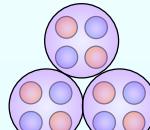
$\alpha + t$

^8Be



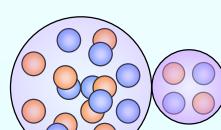
$\alpha + \alpha$

^{12}C



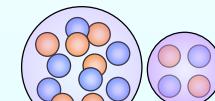
3α

^{20}Ne



$^{16}\text{O} + \alpha$

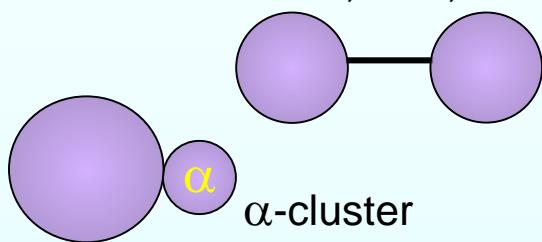
$^{16}\text{O}^*$



$^{12}\text{C} + \alpha$

Heavier nuclei

Si-C, O-C, O-O

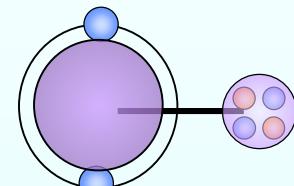


$^{36}\text{Ar}-\alpha$, $^{24}\text{Mg}-\alpha$, $^{28}\text{Si}-\alpha$

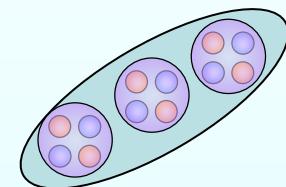
$^{40}\text{Ca}^*$, $^{28}\text{Si}^*$, $^{32}\text{S}^*$

Unstable nuclei (neutron-rich)

α -cluster
excitation

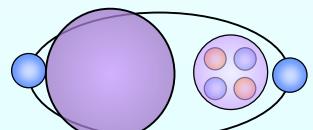


3α linear chain



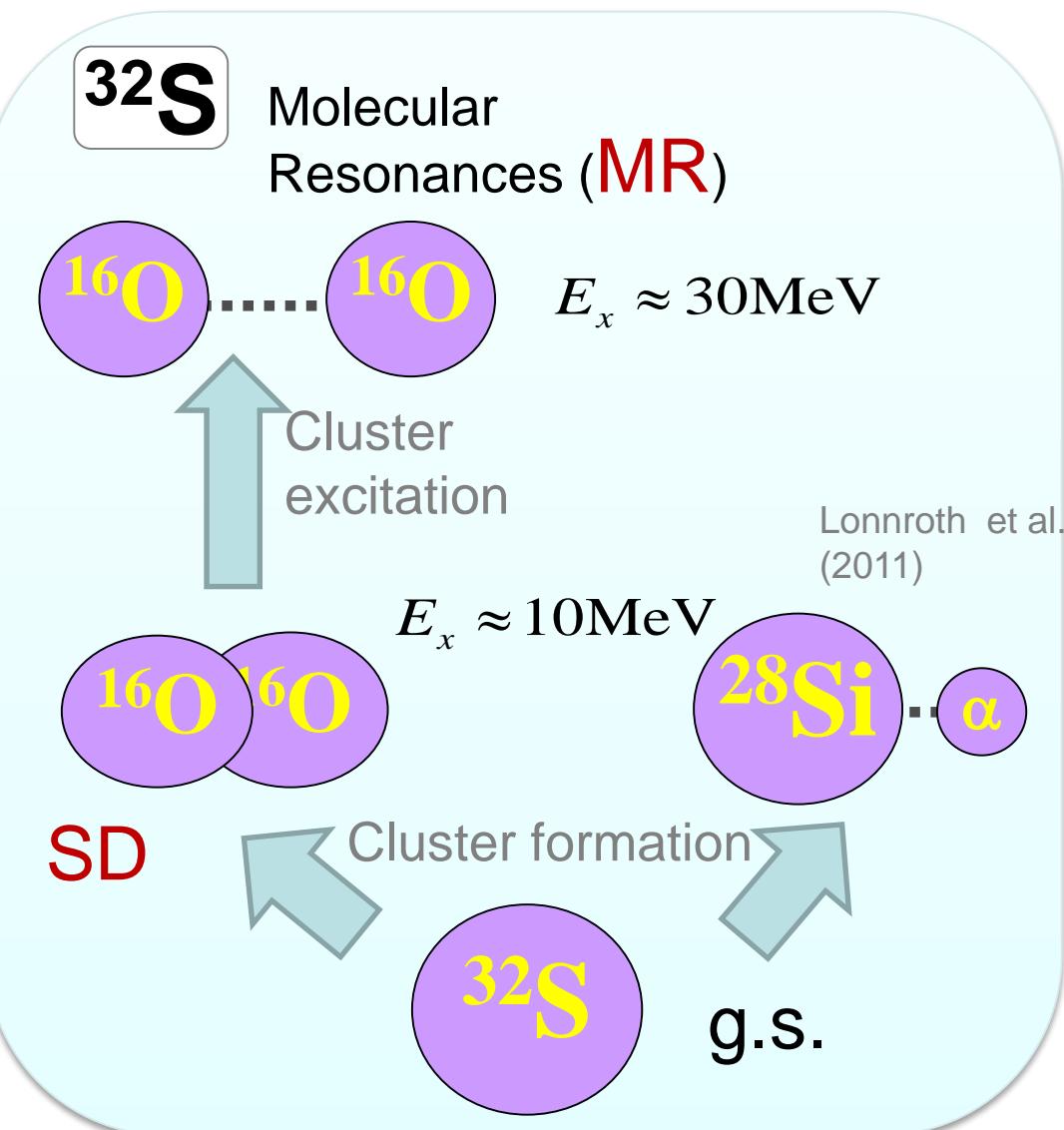
$^{14}\text{C}^*$

Molecular
orbital



Be, C, O, Ne, F

In heavier-mass nuclei



- ✓ SuperDeformation(SD)
- ✓ Molecular Resonance
- ✓ α -cluster

^{32}S : O-O, Si- α

^{40}Ca : Si-C, Ar- α

^{44}Ti : Si-O, Ca- α

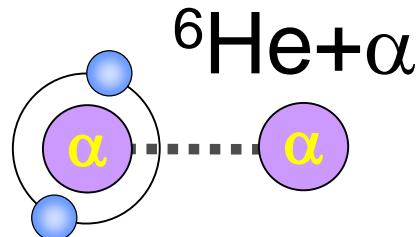
^{28}Si : Si-C (MR)

^{56}Ni : Si-Si (MR)

In neutron-rich nuclei

neutron-rich Be isotopes

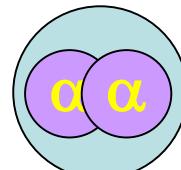
Seya, Von Oerzten, Descouvemont et al.,
Itagaki et al., K-E et al. M. Ito et al.



Atomic (resonance)

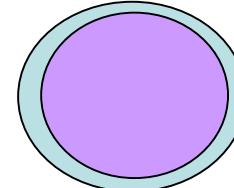
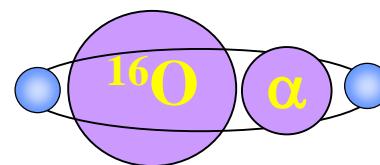
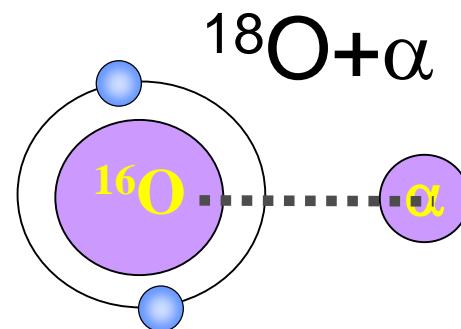


molecular Bond



shell model-like

^{10}Be



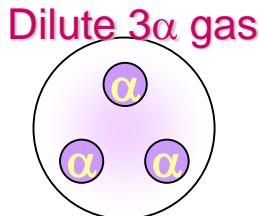
Ne, F, O isotopes

Kimura et al.,
Yoshida et al.,
Furutachi et al.

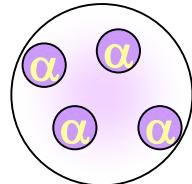
Cluster gas, linear chain

α -cluster gas

$^{12}\text{C}^*(0_2^+)$



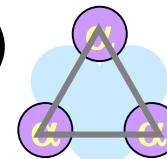
$^{16}\text{O}^*$



Tohsaki et al.,
Yamada et al.,
Funaki et al.
Wakasa et al.,

cluster crystallization

$^{14}\text{C}^*(3^-_2)$



triangle

Itagaki et al.,
Von Oertzen et al.

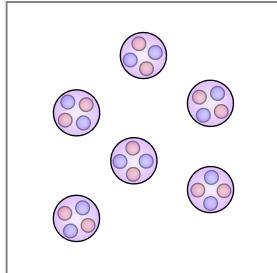
Price et al.
Suhara et al



$^{12,14,15,16}\text{C}^*$ linear chain

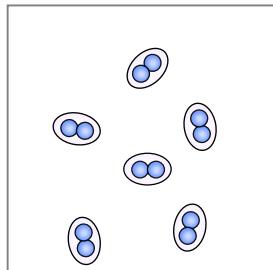
Nuclear matter

α -condensation

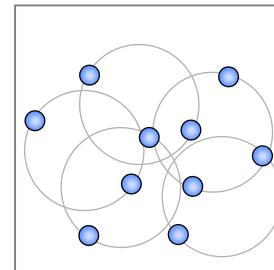


Roepche et al.

dineutron-cond.



BEC-BCS matsuo et al.



Rich cluster phenomena in nuclear systems

as functions of proton&neutron numbers and excitation energy

- ✓ Cluster formation/breaking in low-lying states
- ✓ Cluster excitation and resonances
- ✓ Molecular Bond in neutron-rich nuclei
- ✓ Many clusters : cluster gas, chain
- ✓ New types of cluster

t, ${}^4\text{He}$, ${}^{12}\text{C}$, ${}^{16}\text{O}$,

${}^{6,8}\text{He}+\text{He}$ in Be, ${}^{10}\text{Be}+\alpha$ in ${}^{14}\text{C}$,

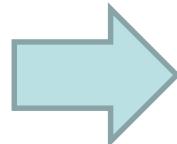
${}^{14}\text{C}+\alpha$ in ${}^{18}\text{O}$, ${}^{18}\text{O}+\alpha$ in ${}^{22}\text{Ne}$

Rich cluster phenomena in nuclear systems

as functions of proton&neutron numbers and excitation energy

- ✓ Cluster formation/breaking in low-lying states
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- ✓ Many clusters : cluster gas, chain
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Theoretical framework that can describe those
Cluster phenomena



AMD: antisymmetrized molecular dynamics

2. A theoretical model: AMD

AMD method for structure study

AMD wave fn.

$$\Phi = c\Phi_{\text{AMD}} + c'\Phi'_{\text{AMD}} + c''\Phi''_{\text{AMD}} + \dots$$

$$\Phi_{\text{AMD}} = \det \{\varphi_1, \varphi_2, \dots, \varphi_A\}$$

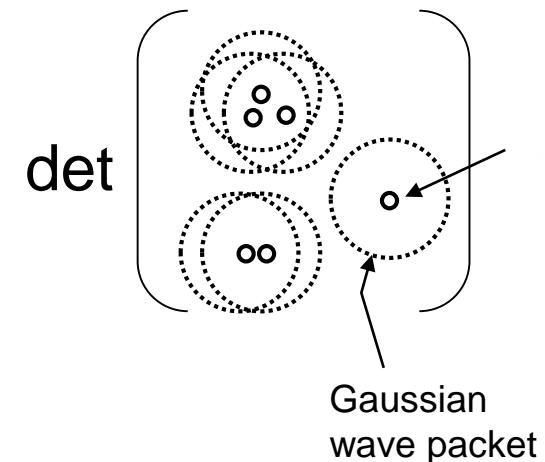
Slater det.

$$\varphi_i = \phi_{Z_i} \chi_i$$

$$\begin{cases} \text{spatial} \\ \phi_{Z_i}(\mathbf{r}_j) \propto \exp \left[-\nu \left(\mathbf{r} - \frac{\mathbf{Z}_i}{\sqrt{\nu}} \right)^2 \right] \\ \text{Intrinsic spins} \\ \chi_i = \begin{pmatrix} \frac{1}{2} + \xi_i \\ \frac{1}{2} - \xi_i \end{pmatrix} \times \begin{array}{l} p \text{ or } n \\ \text{isospin} \end{array} \end{cases}$$

Gaussian

Variational parameters:
Gauss centers, spin orientations



Energy Variation

$$\delta \frac{\langle \Phi | H | \Phi \rangle}{\langle \Phi | \Phi \rangle} = 0$$

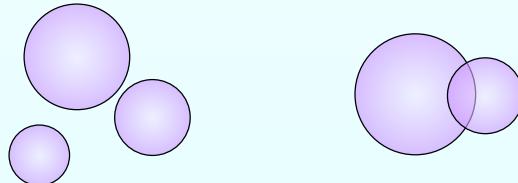
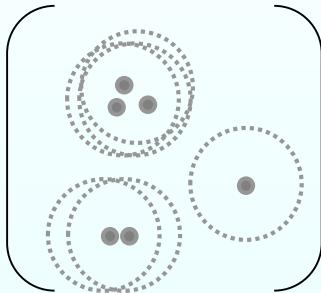
Model wave fn. Φ

Effective nuclear force
(phenomenological)

$$H^{\text{eff}} = \sum_{i=1} t_i + \sum_{i < j} v_{ij}^{\text{eff}} + \sum_{i < j < k} v_{ijk}^{\text{eff}}$$

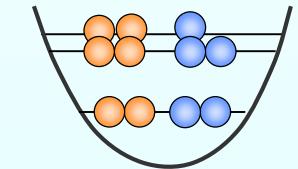
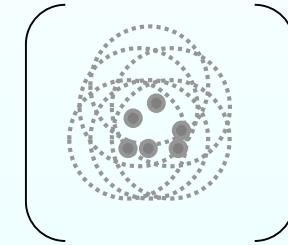
AMD model space

det



a variety of cluster st.

det

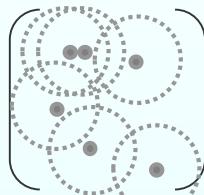
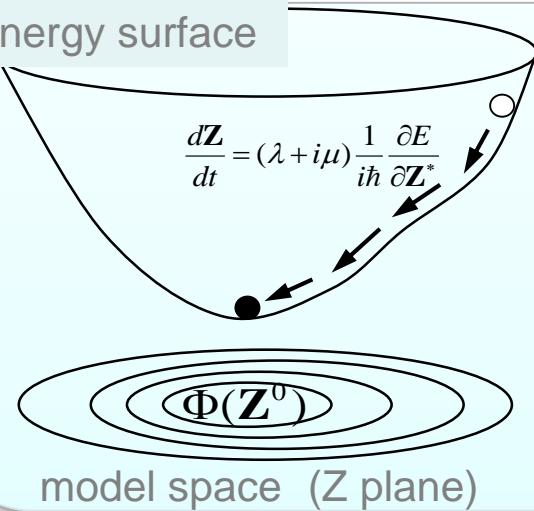


shell model state

Energy variation

Energy surface

$$\frac{d\mathbf{Z}}{dt} = (\lambda + i\mu) \frac{1}{i\hbar} \frac{\partial E}{\partial \mathbf{Z}^*}$$



randomly chosen
initial state

$$\delta \frac{\langle \Phi | H | \Phi \rangle}{\langle \Phi | \Phi \rangle} = 0$$

optimum solution
is obtained

AMD wave function is
similar to FMD wave function.
Difference is effective
interaction

3. Some topics of cluster phenomena

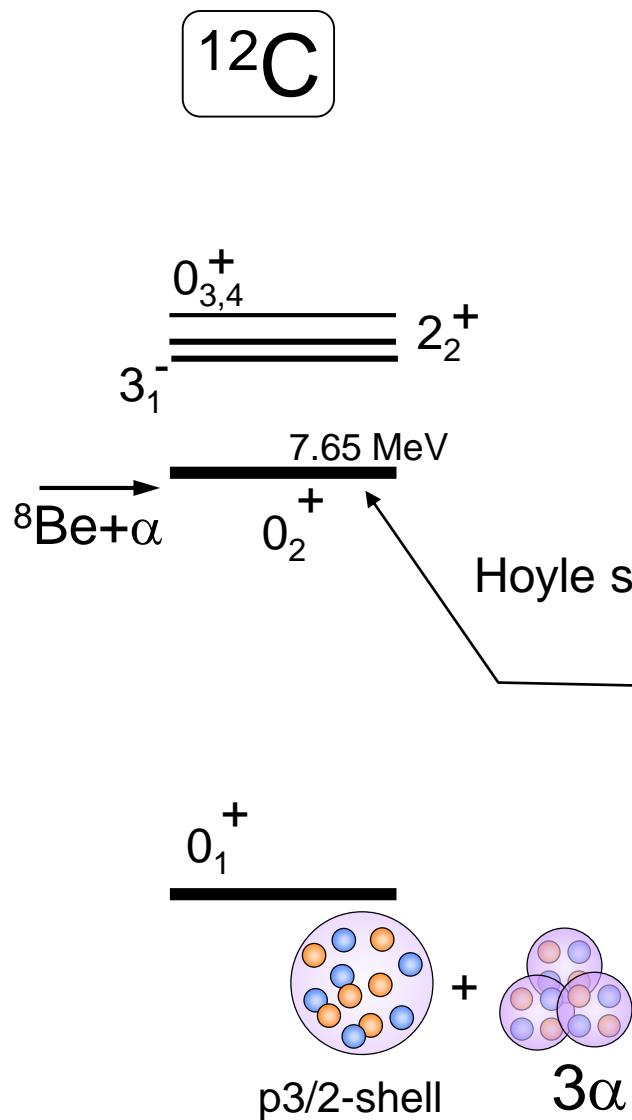
Topics of cluster phenomena

- Cluster gas, chain states
- Cluster structures in Be isotopes

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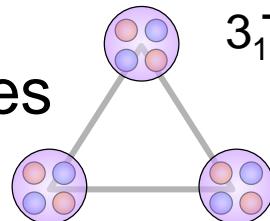
Cluster states in excited states



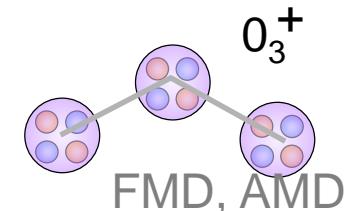
Various modes of cluster excitation,
and their rotation

Geometric ?

triangles

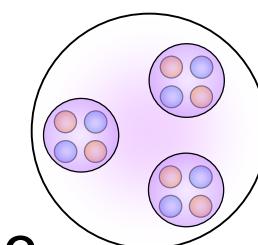


Bending chain?



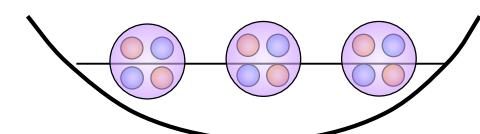
dilute cluster gas

Uegaki et al. (1977)
Tohsaki et al. (2001)



bosonic behavior

Funaki et al. (2003)



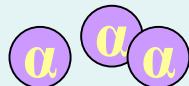
analogy to **BEC**
in nuclear matter
Roepke et al., PRL(1998)

Cluster gas

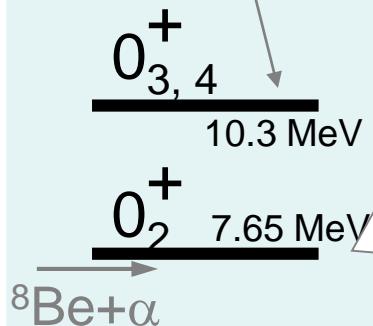
^{12}C

^{16}O

Tohsaki et al., Yamada et al.,
Funaki et al. Wakasa et al.,

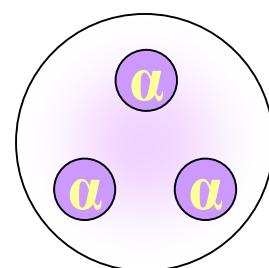


chain ?

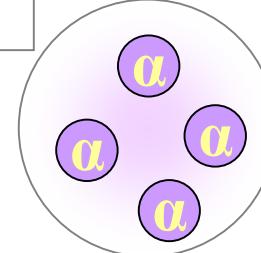


A.Tohsaki et al., (2001)
Funaki et al.(2003)

Dilute cluster gas



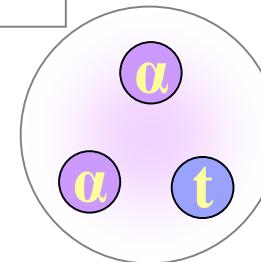
Bosonic behavior



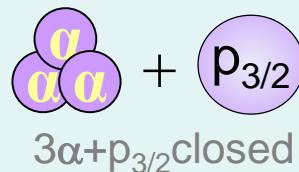
$^{16}\text{O}(0^+_6) ?$

$^{11}\text{C}, ^{11}\text{B}$

K-E. et al., Suhara et al



0_1^+

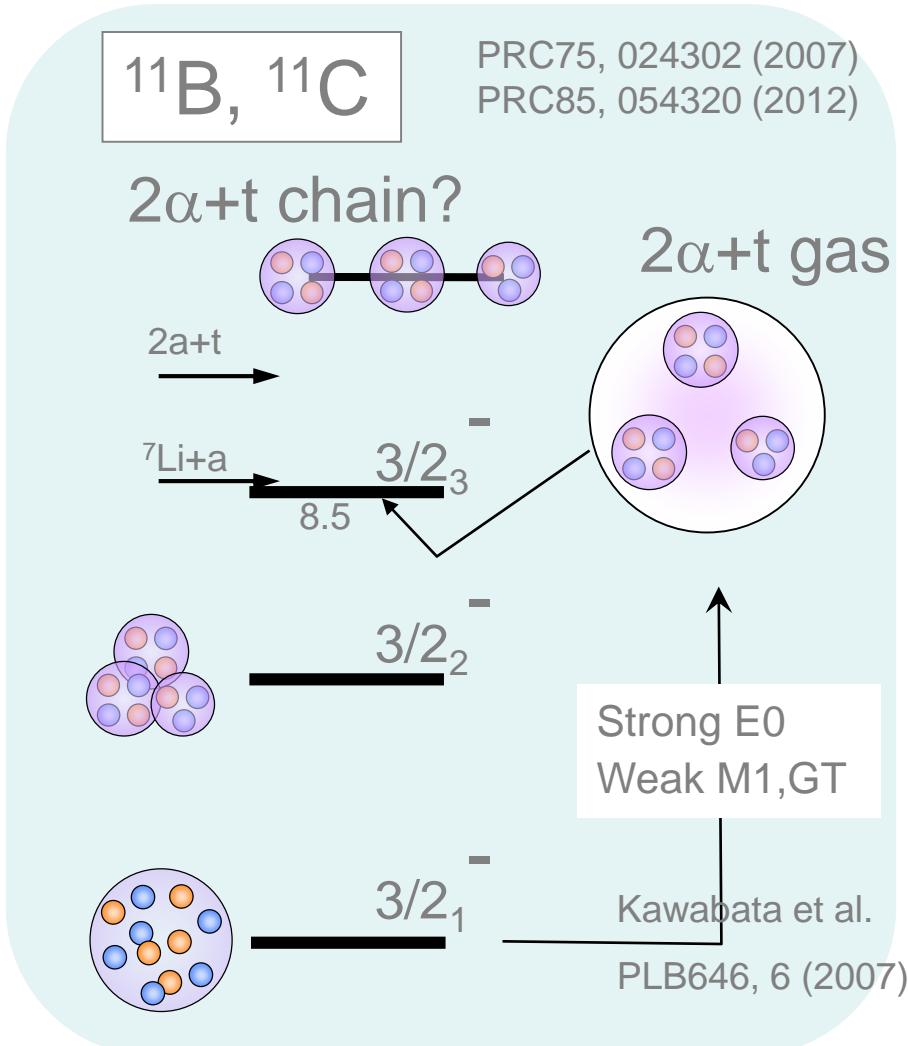
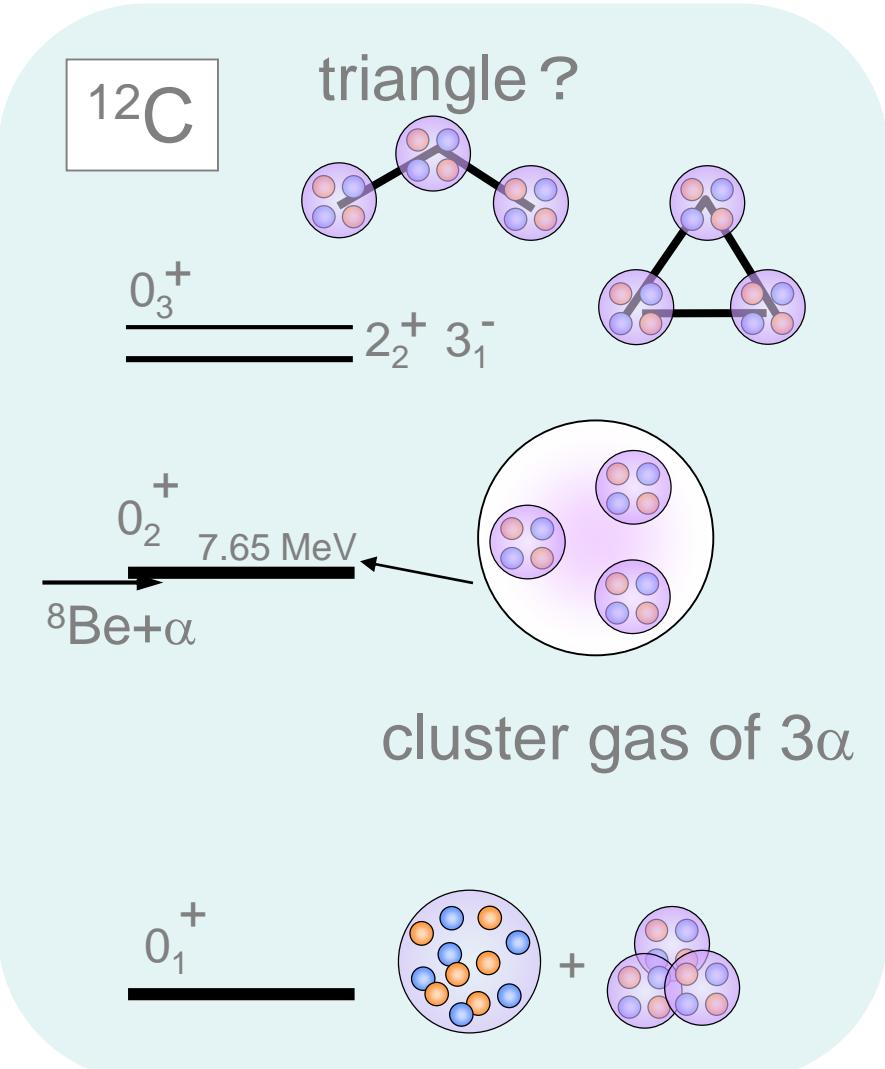


Problems

- ✓ Cluster gas in other nuclei
- ✓ rotation of clusters gas?

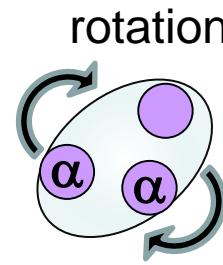
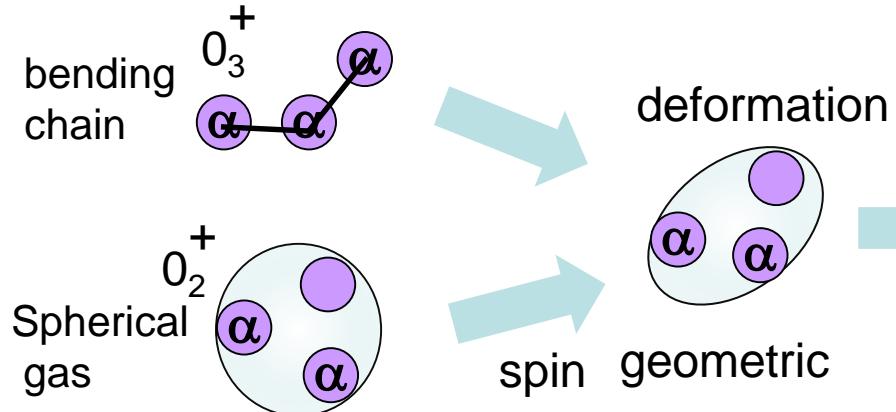
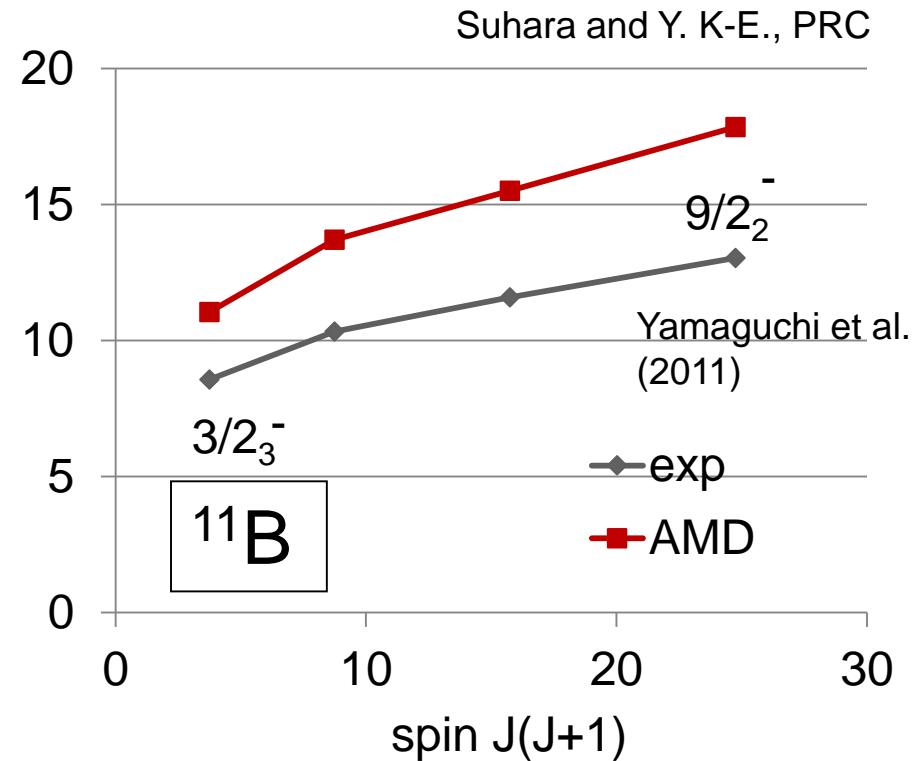
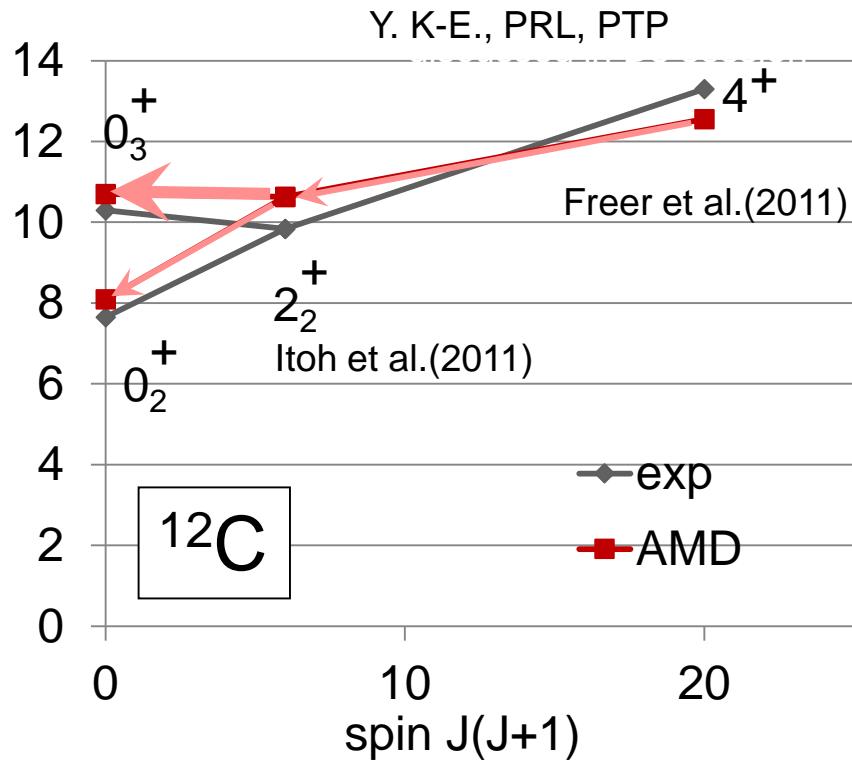
$2\alpha+t$ cluster in $^{11}\text{B}(3/2^-_3)$

AMD by Y.K-E., Suhara



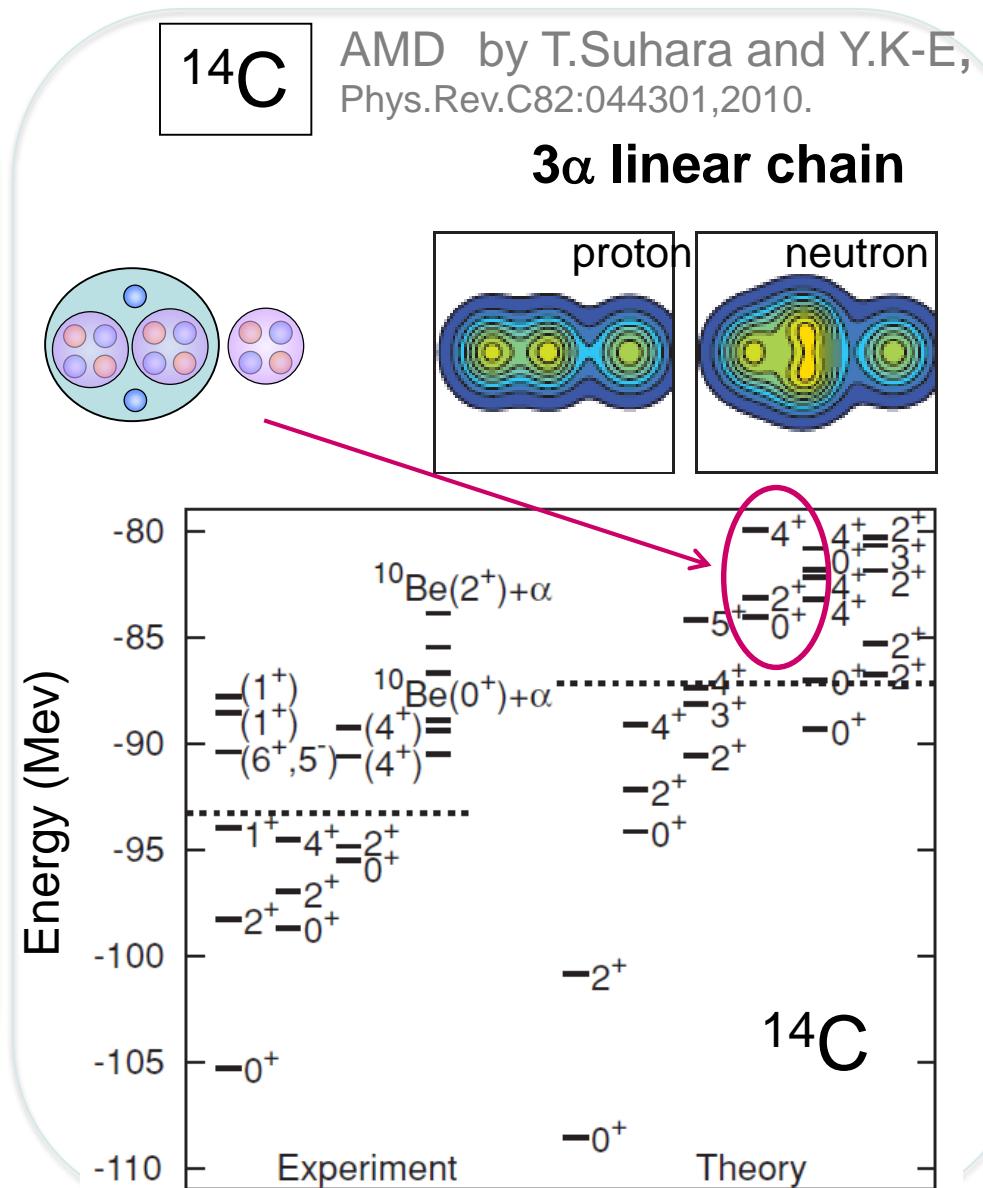
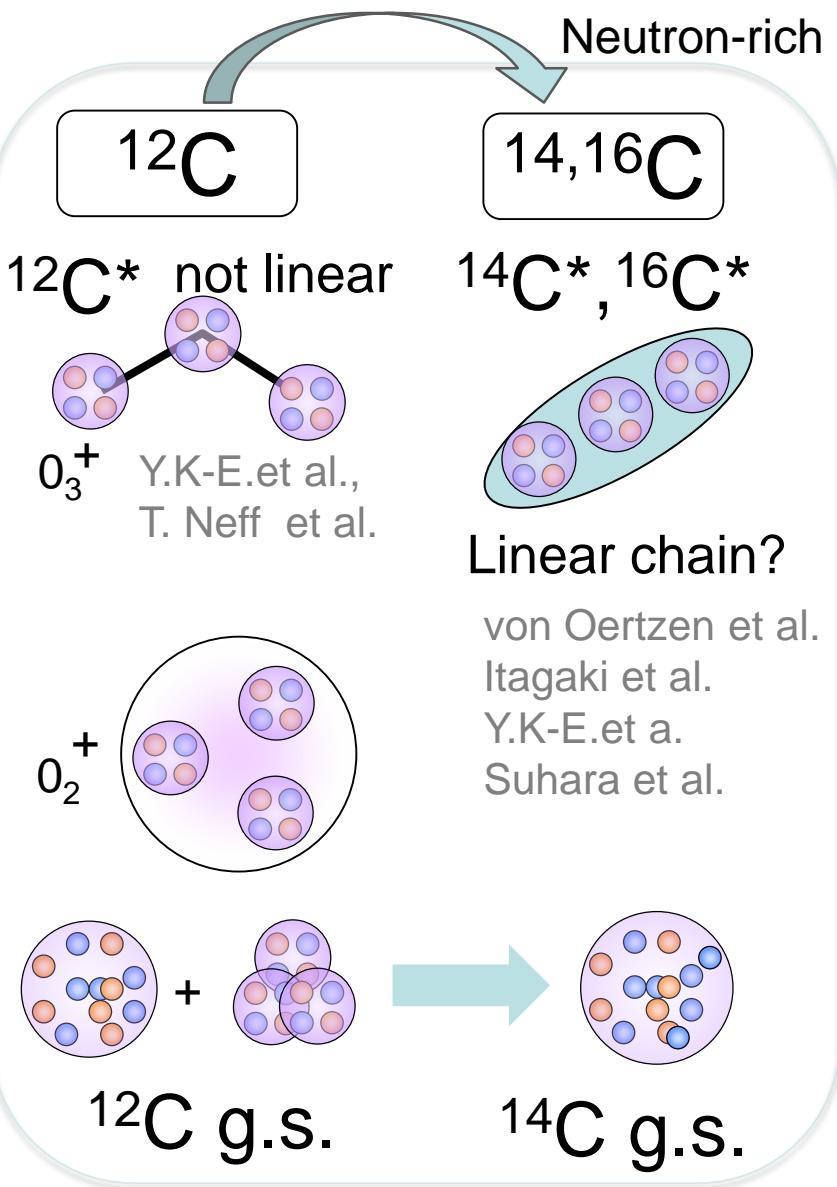
Rotational(?) band from cluster gas

Structure change with spin increasing -> change of moment of inertia



rotation of 3α , 4α gas
Ohkubo et al., PLB684(2010)
Funaki et al. PTPS196 (2012)

Linear chain state in $^{14}\text{C}^*$



Topics of cluster phenomena

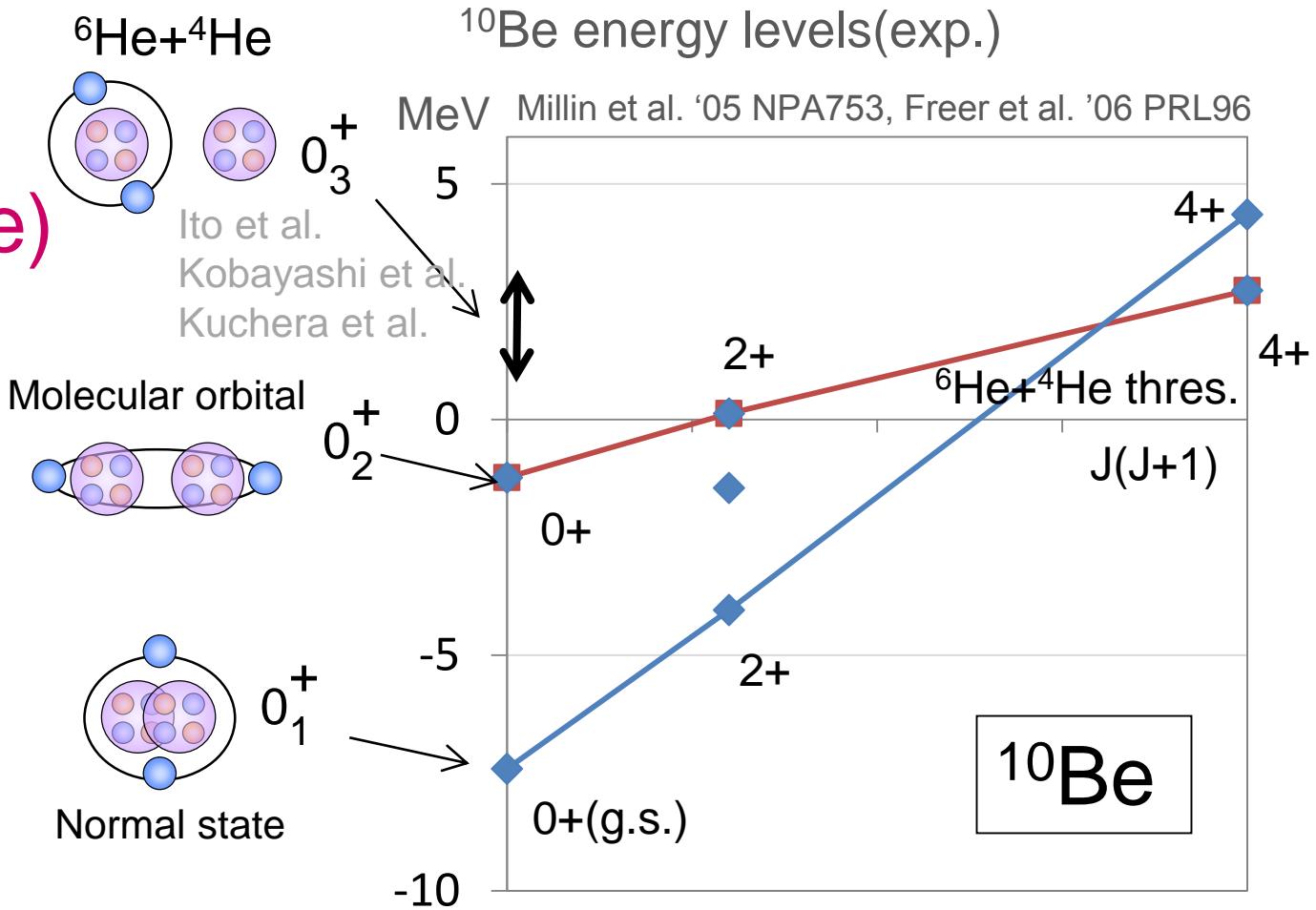
- Cluster gas, chain states
- Cluster structures in Be isotopes

Cluster structures in neutron-rich Be

Atomic
(cluster
Resonance)

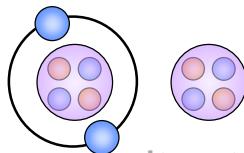
MO bond

Normal

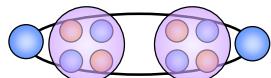


Cluster structures in neutron-rich Be

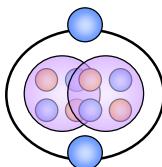
${}^6\text{He} + {}^4\text{He}$



Ito et al.
Kobayashi et al.
Kuchera et al.



Molecular orbital



Normal state

Atomic: cluster resonance

He+He resonances in Be
He+t res. In ${}^9\text{Li}$

MO bond

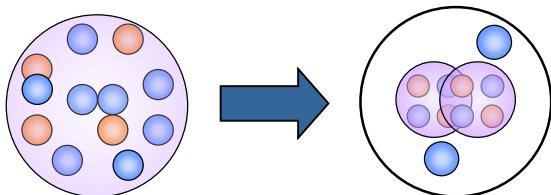
Vanishing of magic number
in ${}^{11}\text{Be}$, ${}^{12}\text{Be}$, ${}^{13}\text{Be}$

Normal: shell-model like

MO bond and vanishing of
magic number N=8 in Be

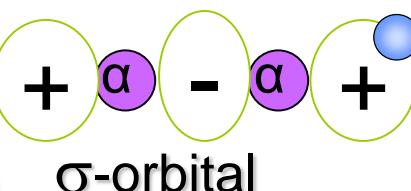
Molecular orbital(MO) bond in Be

2 α -core formation

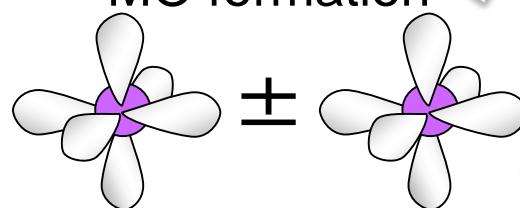


MO formation

Seya et al. Von Oertzen et al.,

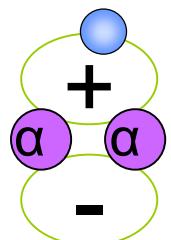


MO formation

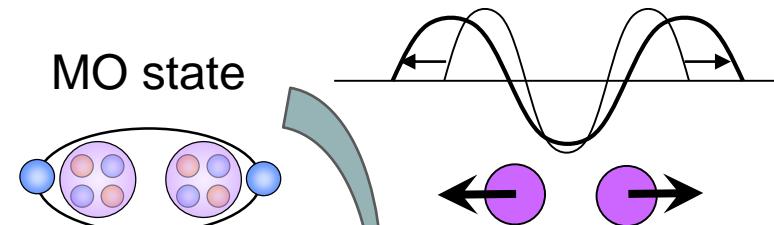


π -orbital

Normal state



MO state



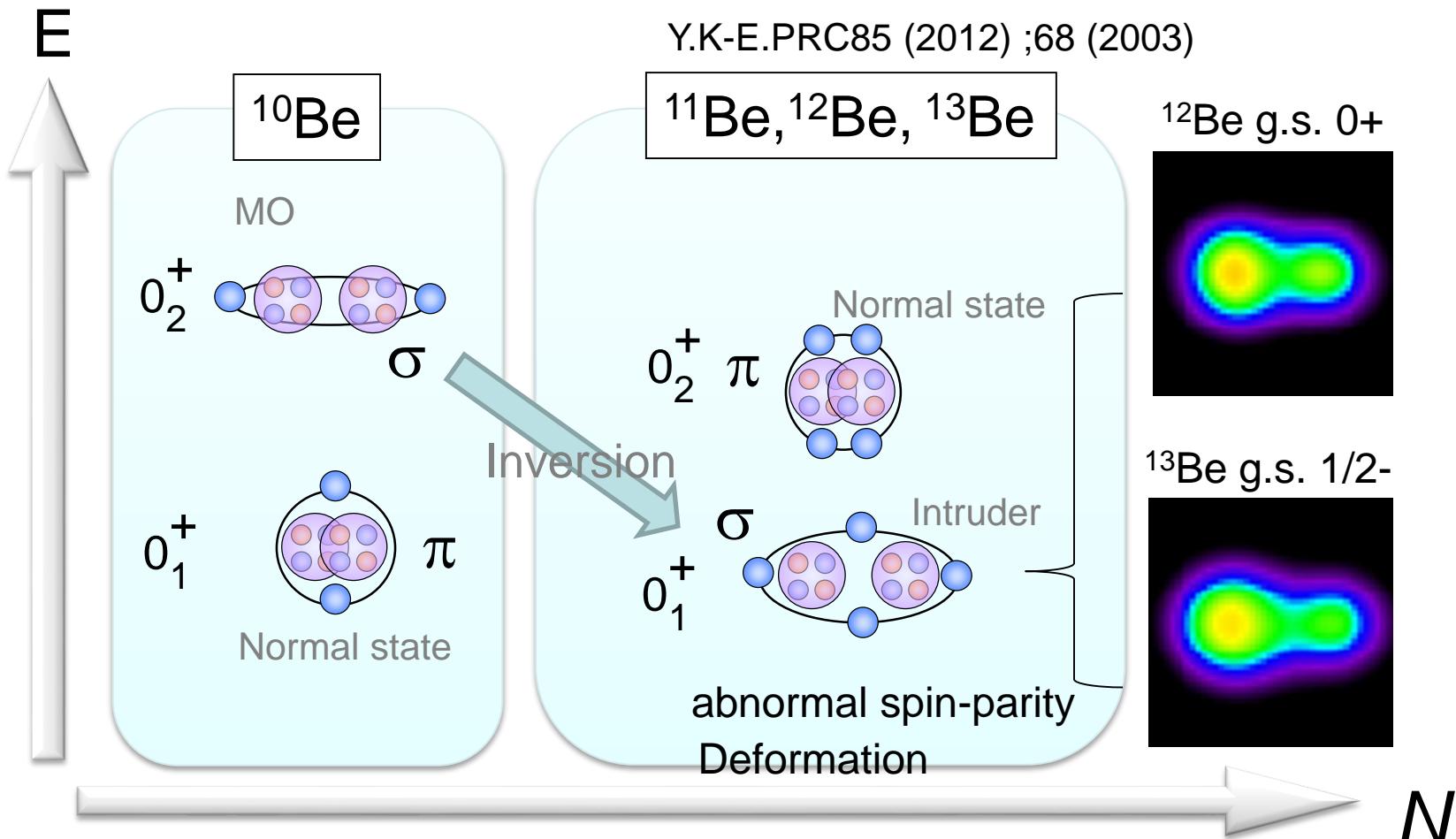
Gain kinetic energy
in developed 2 α system

Low-lying MO states
in $^{11,12,13}\text{Be}$

vanishing of magic number in ^{11}Be , ^{12}Be , ^{13}Be

Recent exp. for ^{13}Be
Kondo et al. PLB690(2010)

Vanishing of N=8 magic number in neutron-rich Be



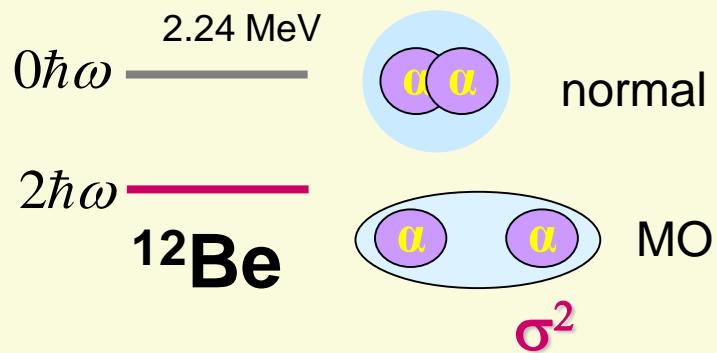
Exp:Iwasaki et al., Navin et al.,
Pain et all. Kondo et al.

^{12}Be :Vanishing of magic number N=8

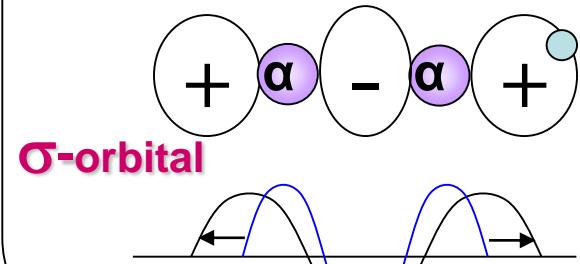
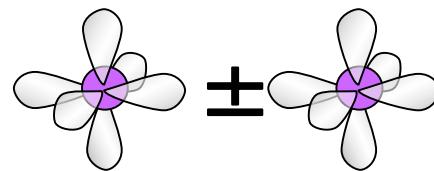
Breaking of magicity (N=8) in ^{12}Be

0_2^+ (2.24MeV) $0\hbar\omega$

0_1^+ intruder $2\hbar\omega$ state



Formation of 2α +molecular orbitals



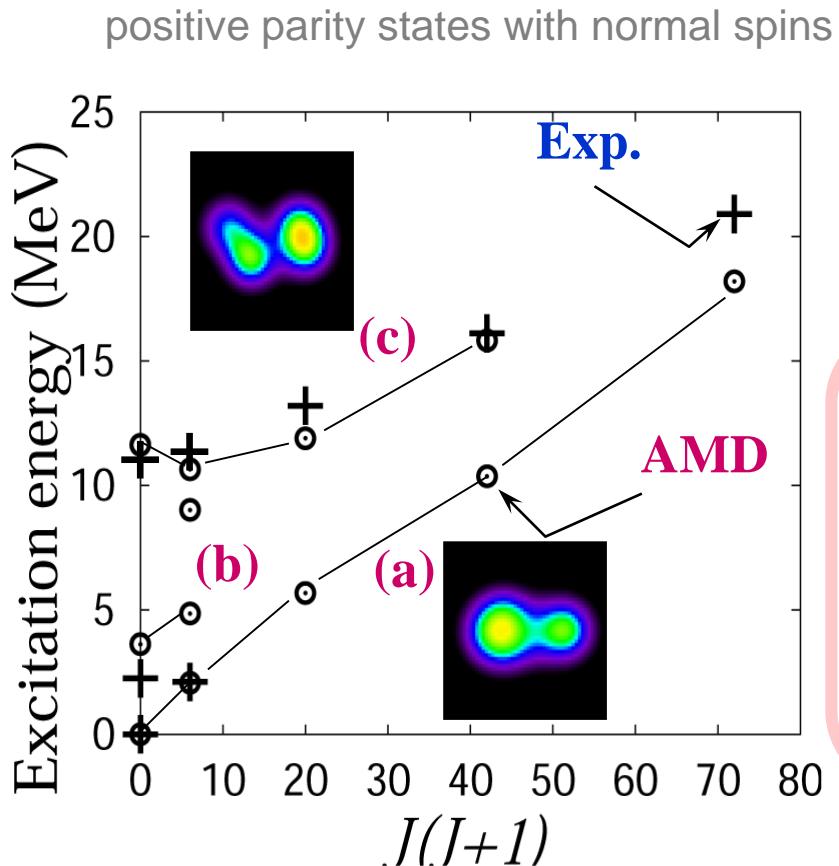
Deformed ground state with d-wave components

Experiments: Iwasaki et al.,
Navin et al., Pain et all.

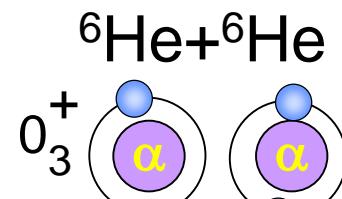
AMD result of ^{12}Be

VAP calculation with AMD method

^{12}Be

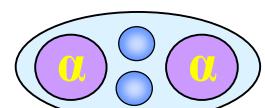


Highly excited states



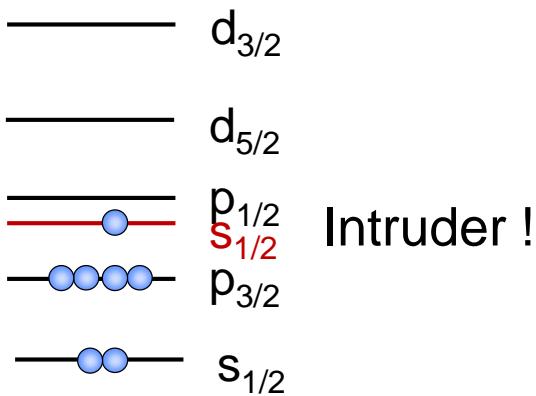
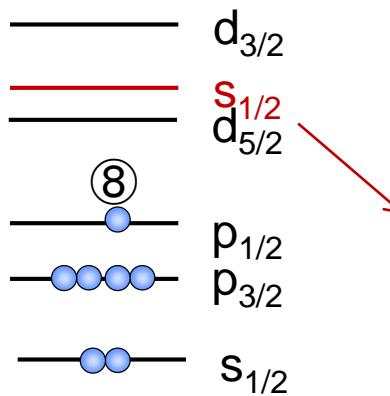
0_2^+ (2.24MeV) $0\hbar\omega$

0_1^+ intruder $2\hbar\omega$



Breaking of N=8 magicity
Formation of $2\alpha + \text{molecular orbitals}$

Parity inversion of $^{11}\text{Be}(1/2+, 1/2-)$



1/2- g.s.
Normal
N=7 nuclei

1/2+ g.s.
in ^{11}Be
Z=4, N=7

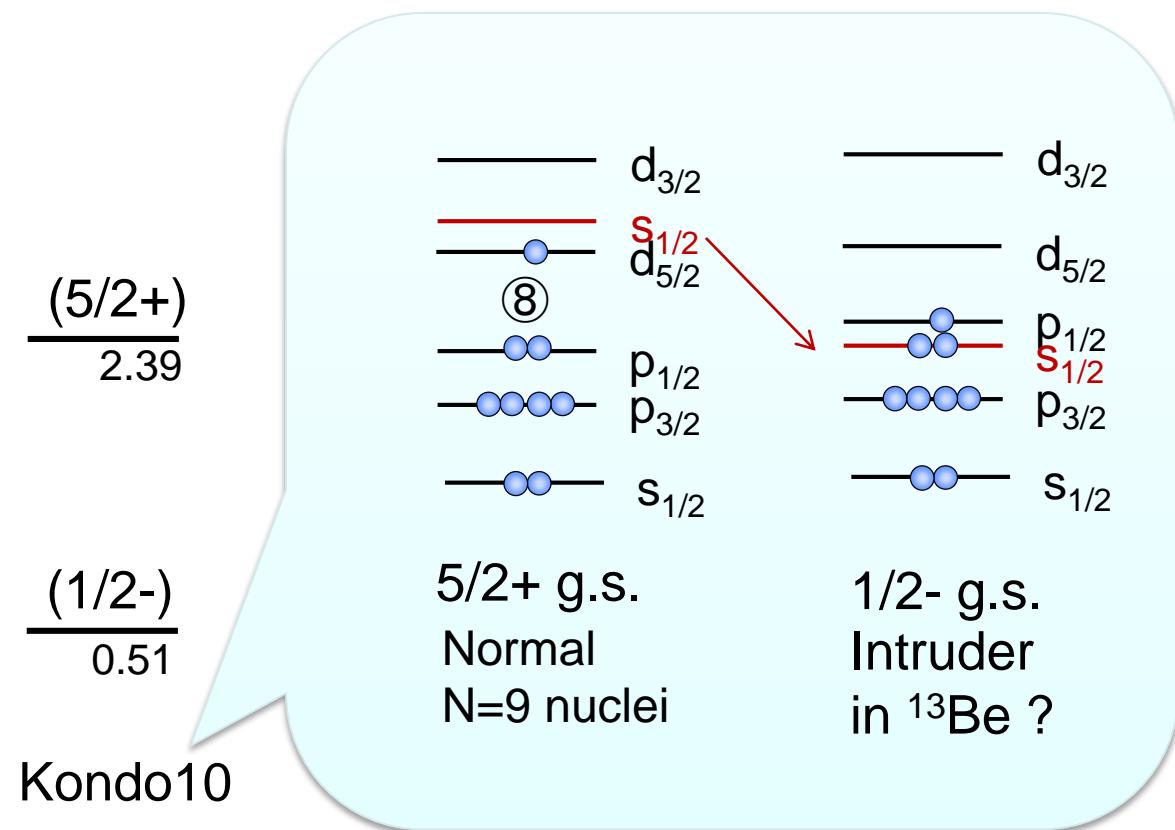
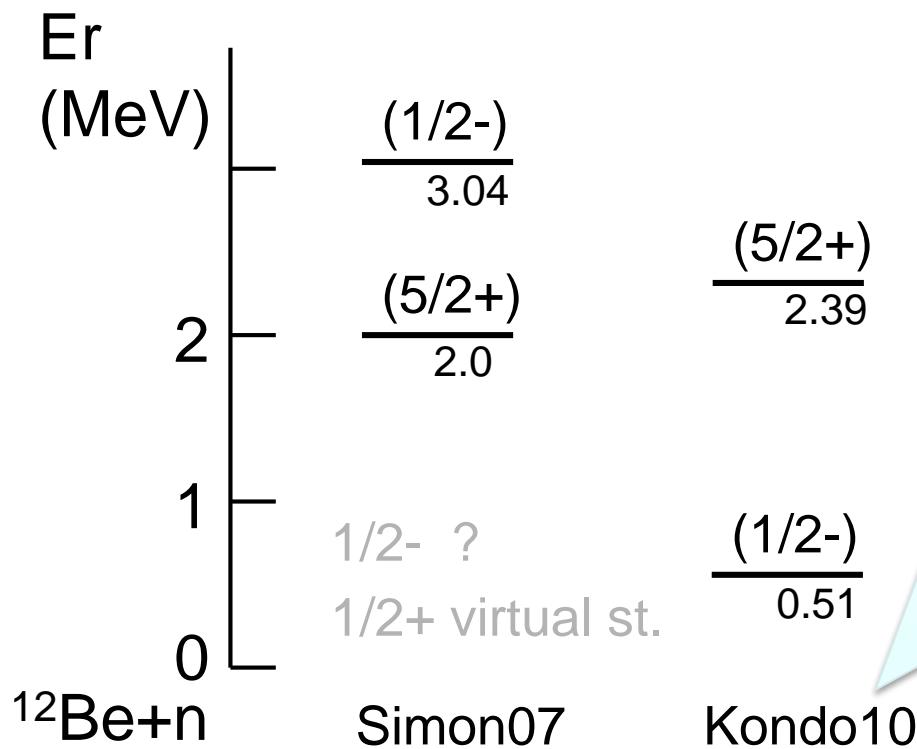
0.32 1/2-
g.s 1/2+

^{11}Be

^{13}Be spectra

^{13}Be : unbound

^{13}Be spectra has been measured by 1n knock-out reactions at GSI(Simon et al. 2007) and RIKEN(Kondo et al.,2010)



Be isotopes calculated with AMD+VAP

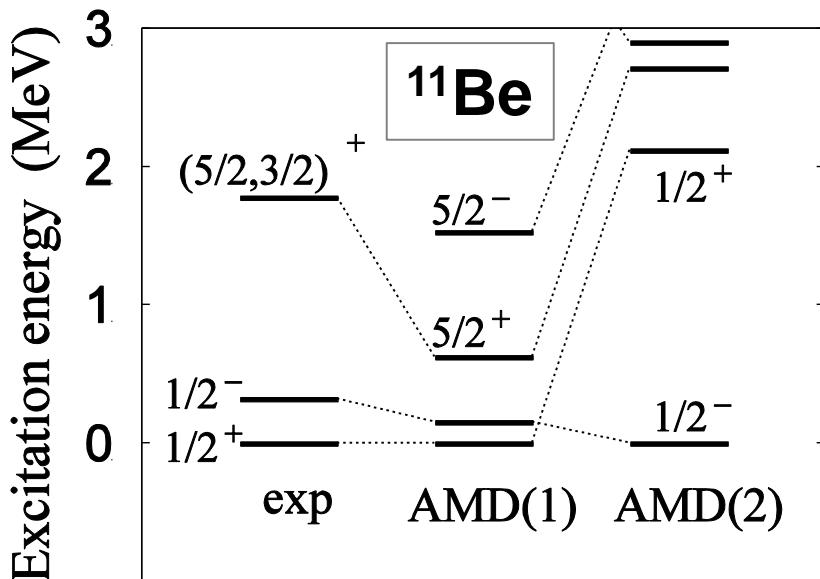
Eff. interactions

MV1($m=0.65$)+G3RS force

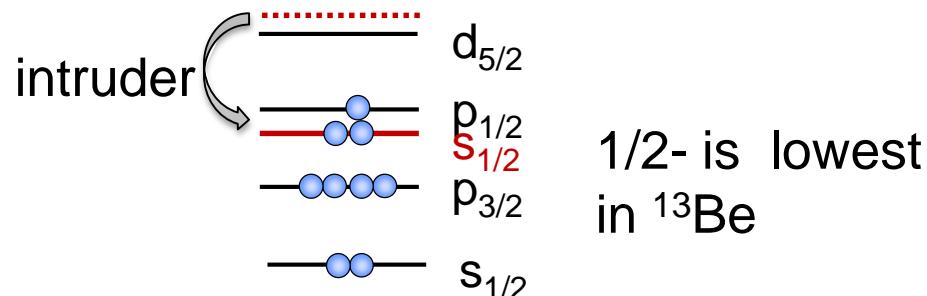
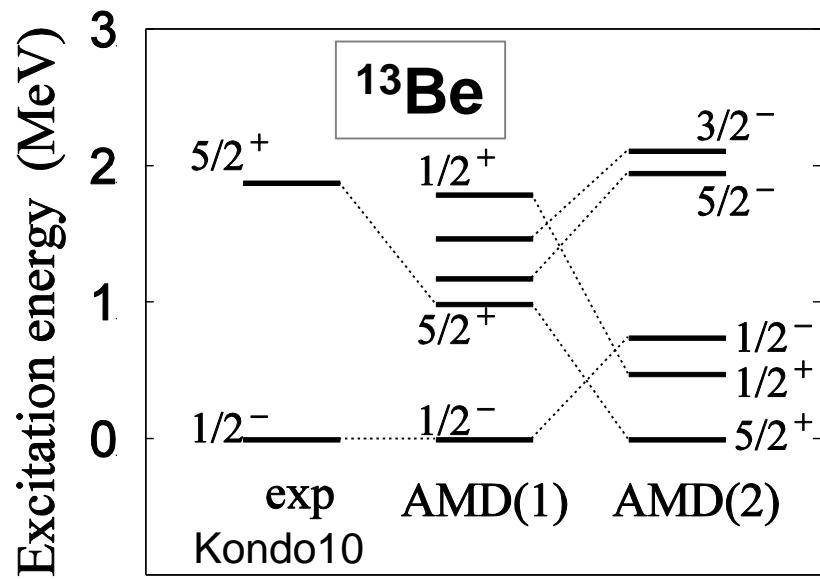
- set(1) : $u=3700$ MeV (ls force)
- set(2) : $u=2500$ MeV

AMD calculation using set(1) interaction:

- $1/2^+$ ground state in ^{11}Be .
- Intruder ground state in ^{12}Be .
- lowest $1/2^-$ state in ^{13}Be .



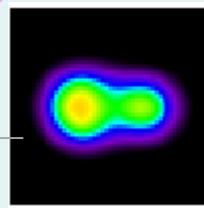
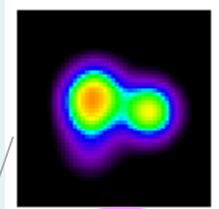
Y. K-E. et al. PRC66, 024305(2002);
PRC68, 014319 (2003)



Cluster structures in Be isotopes

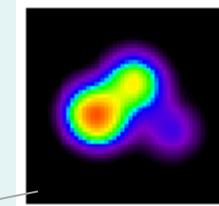
^{11}Be

$\underline{1/2^-} \quad 0\hbar\omega$
 $\underline{1/2^+} \quad 1\hbar\omega$

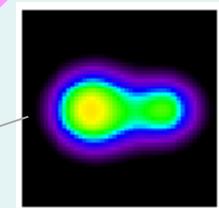


^{12}Be

$\underline{0+}_2 \quad 0\hbar\omega$



$\underline{0+}_1 \quad 2\hbar\omega$

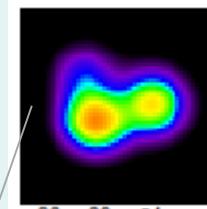


$^{12}\text{Be}(0\text{hw})$

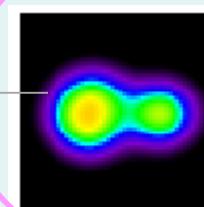
$^{12}\text{Be}(2\text{hw})$

^{13}Be

$\underline{5/2^+} \quad 0\hbar\omega$
 $\underline{1/2^-} \quad 1\hbar\omega$



$^{12}\text{Be}(0\text{hw})+\text{n}$

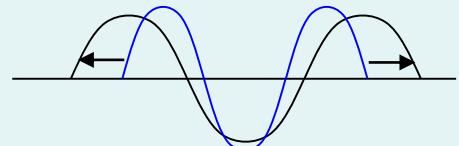
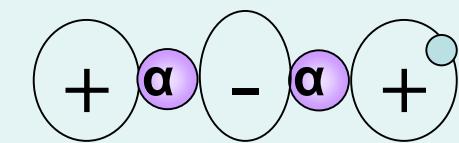


$^{12}\text{Be}(2\text{hw})+\text{n}$

Intruder states are well deformed states
with developed 2-alpha cores.
Similar structures in Be isotopes.

Molecular
 σ -orbital

von Oertzen et al.
Seya et al.



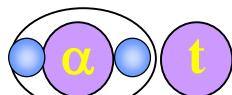
Cluster resonances in Be and ${}^9\text{Li}$

3. ${}^6\text{He} + t$ cluster states in ${}^9\text{Li}$

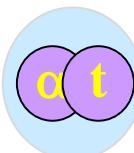
cluster resonances

Search for ${}^6\text{He}+\text{t}$ cluster state in ${}^9\text{Li}$

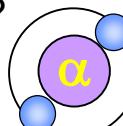
Cluster res. ?



MO bond ?



0^+_3 , 4?



Cluster res.

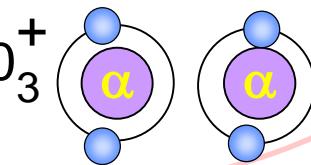
Kuchera et al.

Ito et al.

Kobayashi et al.



0^+_3



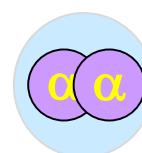
0^+_2



MO bond

Millin et al. '05 NPA753,
Freer et al. '06 PRL96
 $2+(7.54)$ and $4+(10.2)$

$K=0^+_1$



Normal

Normal

0^+_2

MO

0^+_1



von Oertzen '96, '97, ZPA 354,
Seya et al. '81 PTP65, 204



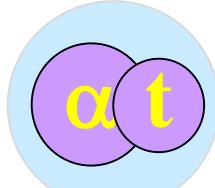
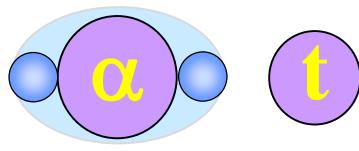
Freer et al. '99 PRL.82:1383

Freer et al. '06 PRL.042501

Developed ${}^6\text{He}+{}^3\text{H}$ cluster states in ${}^9\text{Li}$

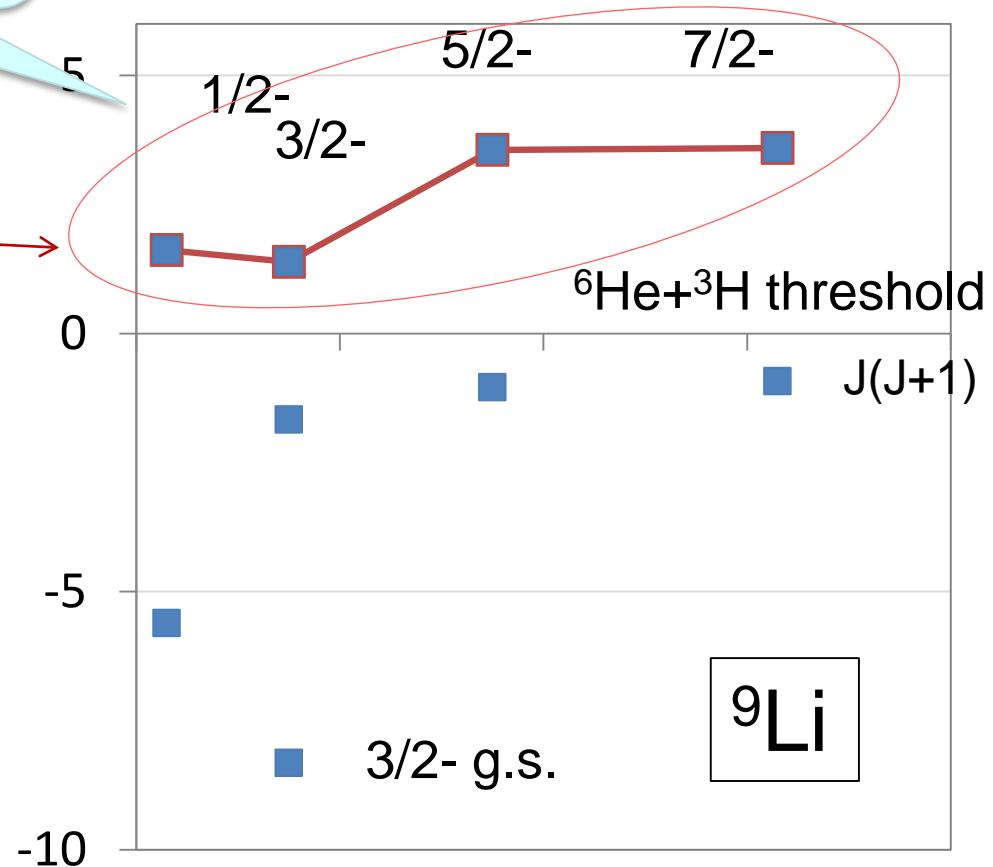
$K=1/2^-$ band with
 ${}^6\text{He}+{}^3\text{H}$ cluster
structure is suggested

${}^6\text{He}+{}^3\text{H}$ resonance

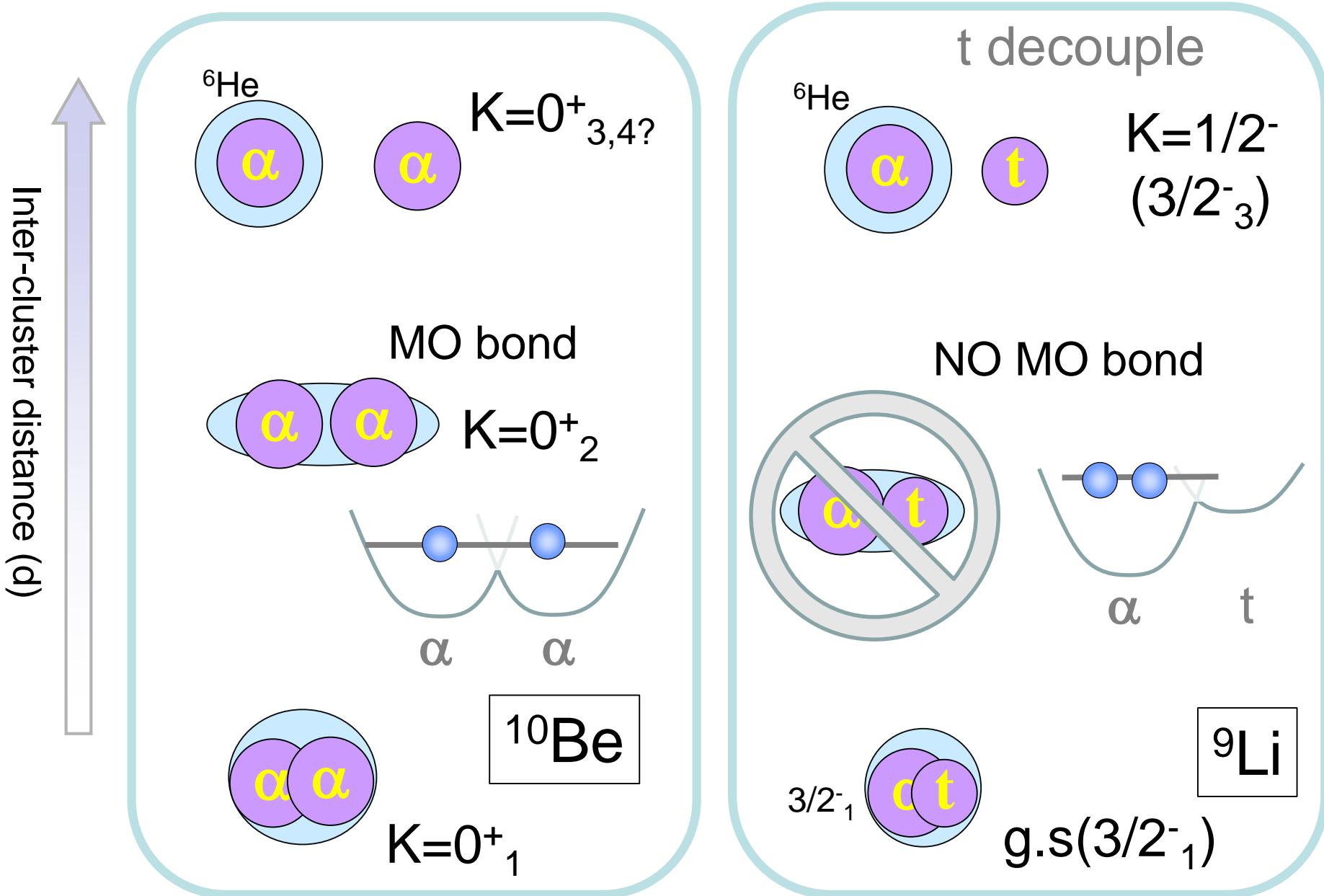


${}^9\text{Li}$

${}^9\text{Li}$: energy
levels(calculation)



Cluster structures in ^{10}Be and ^9Li



5. Summary

Cluster aspects in ground and excited states

◆ Cluster gas, chain states

- Cluster gas often appears in general nuclei
- Cluster gas is not stable in the rotation
- Chain structure of alpha clusters in neutron-rich C

◆ Cluster structures in Be isotopes

- 2α clusters and valence neutron
- MO bond structure and breaking of magic number N=8
- ${}^6\text{He}+\alpha$ Cluster resonances , and ${}^6\text{He}+t$ resonances