

$$\frac{d\sigma_{\text{M}}(v, E_{\text{R}})}{dE_{\text{R}}} = \frac{d\sigma_{\text{M}}^{\text{SI}}(v, E_{\text{R}})}{dE_{\text{R}}} + \frac{d\sigma_{\text{M}}^{\text{SD}}(v, E_{\text{R}})}{dE_{\text{R}}} =$$

$$\propto \lambda_{\chi}^2 \left\{ Z^2 \left[\frac{1}{E_{\text{R}}} - \frac{1}{v^2} \left(\frac{2m_{\mathcal{N}} + m_{\chi}}{2m_{\mathcal{N}}m_{\chi}} \right) \right] F_{\text{SI}}^2(E_{\text{R}}) + \frac{1}{v^2} \left(\frac{\bar{\lambda}_{\text{nuc}}}{\lambda_p} \right)^2 \frac{m_{\mathcal{N}}}{3m_p^2} F_{\text{SD}}^2(E_{\text{R}}) \right\}$$