

$$|\mathcal{M}_{\text{SI}}^N| =_{\text{out}} \langle N, \chi | \mathcal{L}_{\text{SI}}^N | N, \chi \rangle_{\text{in}} = 4 \lambda_{\text{SI}}^N m_\chi m_N \mathbf{1}$$