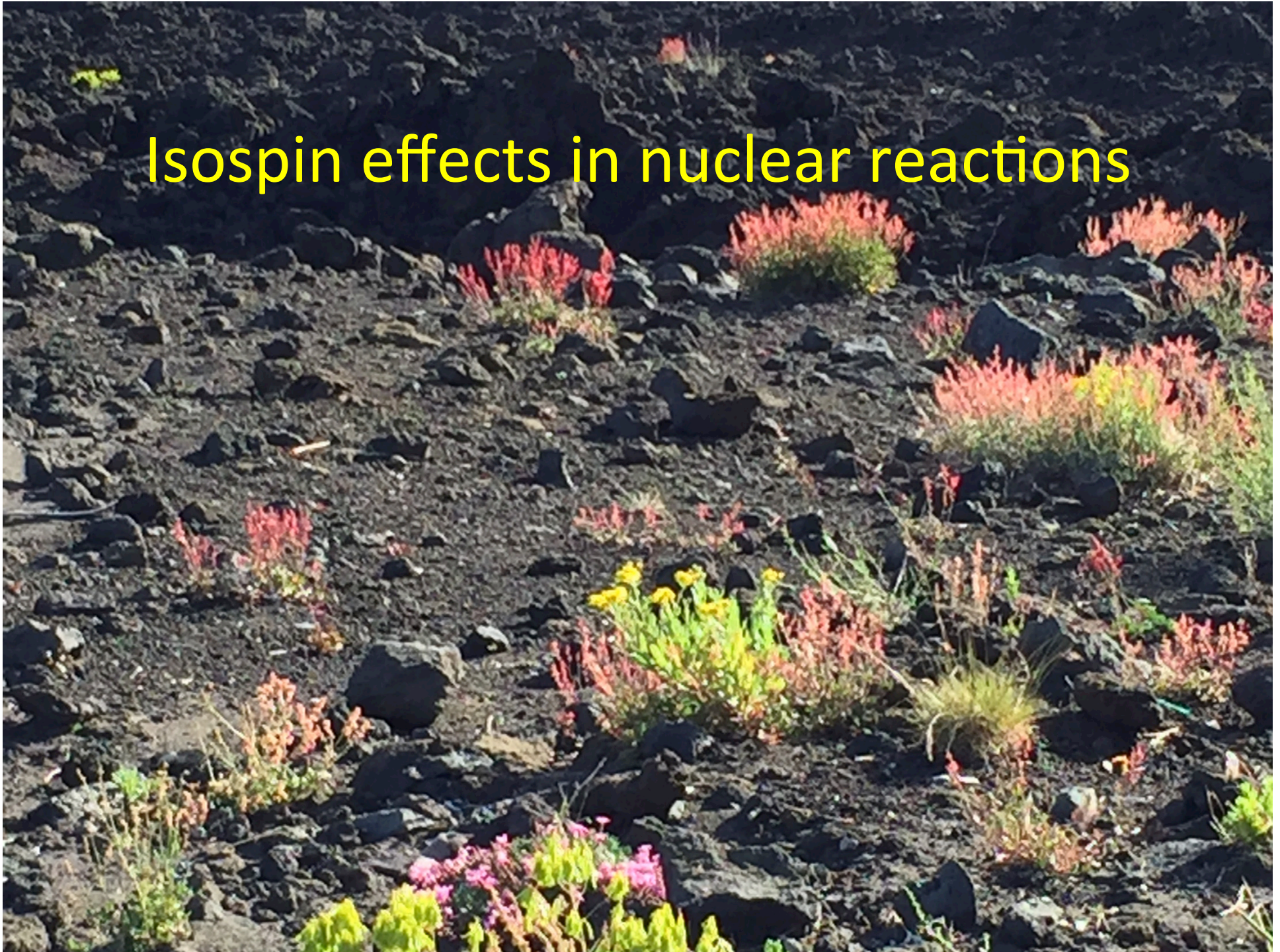
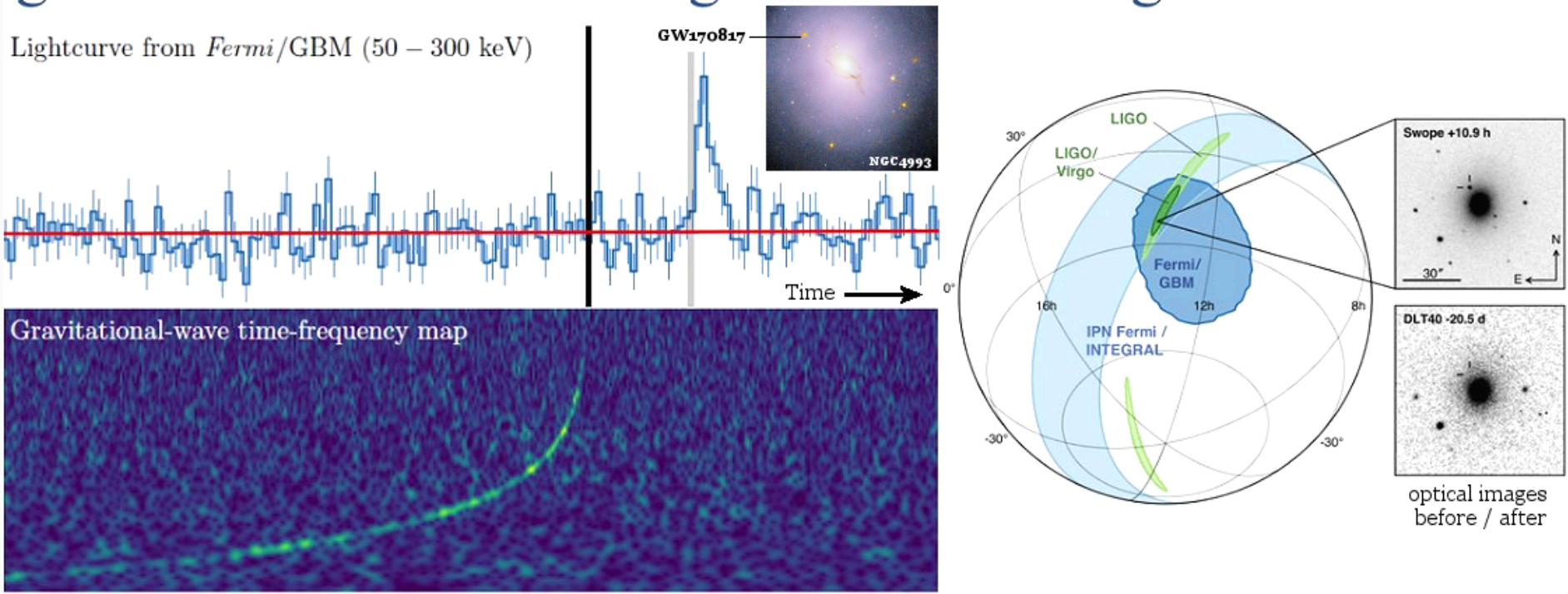


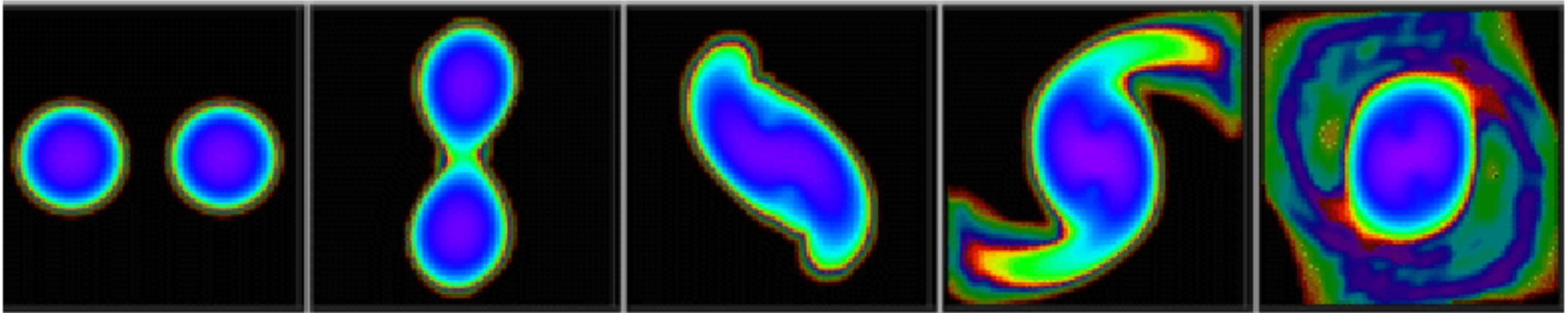
Isospin effects in nuclear reactions



Science Magazine's Breakthrough of the Year 2017:

LIGO, Virgo, and partners make first detection of gravitational waves and light from colliding neutron stars





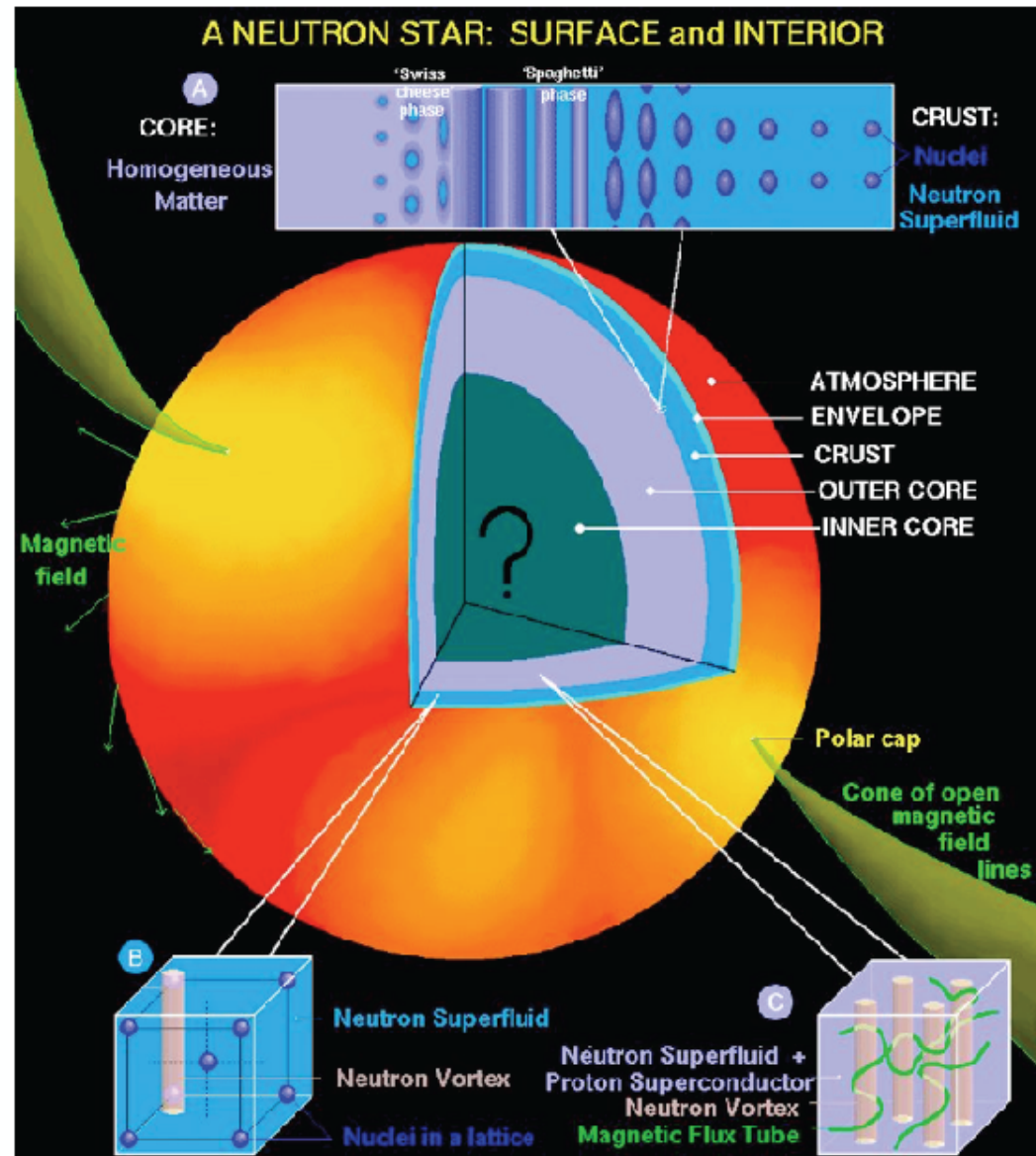
EOS – Asymmetry energy

- » Heat capacity
- » Partitioning of nuclear material - fragmentation
 - Clustering – particularly at low density
 - Inhomogeneous distribution of isospin
 - Pasta
- » Equilibration
- » Deformation – tidal effects



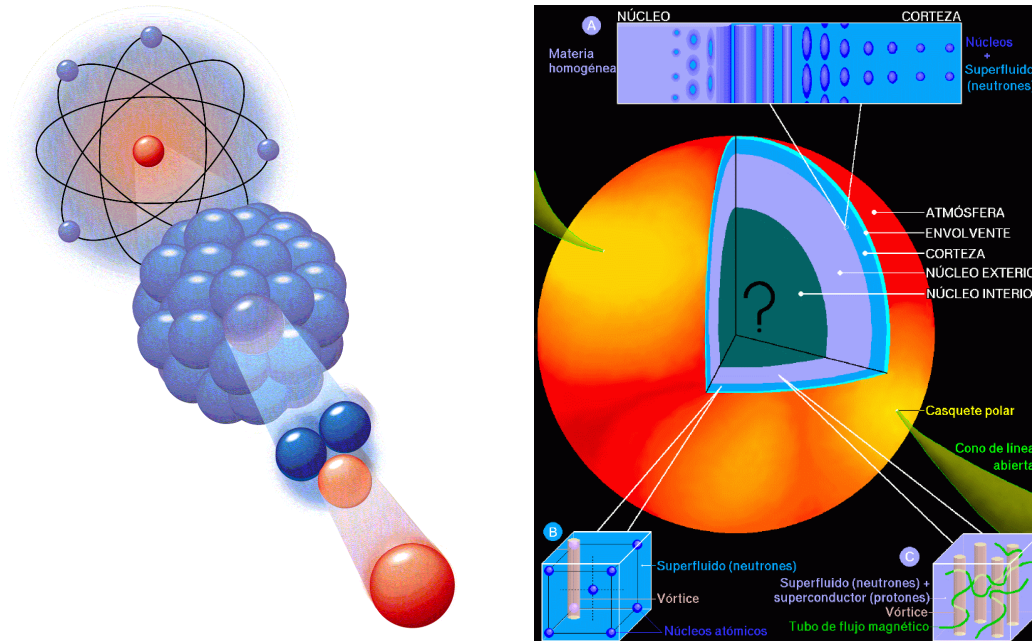
Neutron stars

- Neutron stars are formed from the collapse of a massive star in a supernova explosion.
- Mass $\sim 1.4 M_{\text{sun}}$, Radius ~ 10 km
- Solid crust ~ 1 km thick ($\sim 10^{12}$ g/cm³) over liquid outer core of neutron rich matter ($\sim 10^{15}$ g/cm³).
- Possible exotic phase in center: de-confined quark matter; strange matter; meson condensates, color superconductor...
- Structure determined by Equation of State (pressure vs density) of n rich matter.
- Figure: **Dany Page**, UNAM



Atomic nuclei & Neutron star (two vastly different systems)

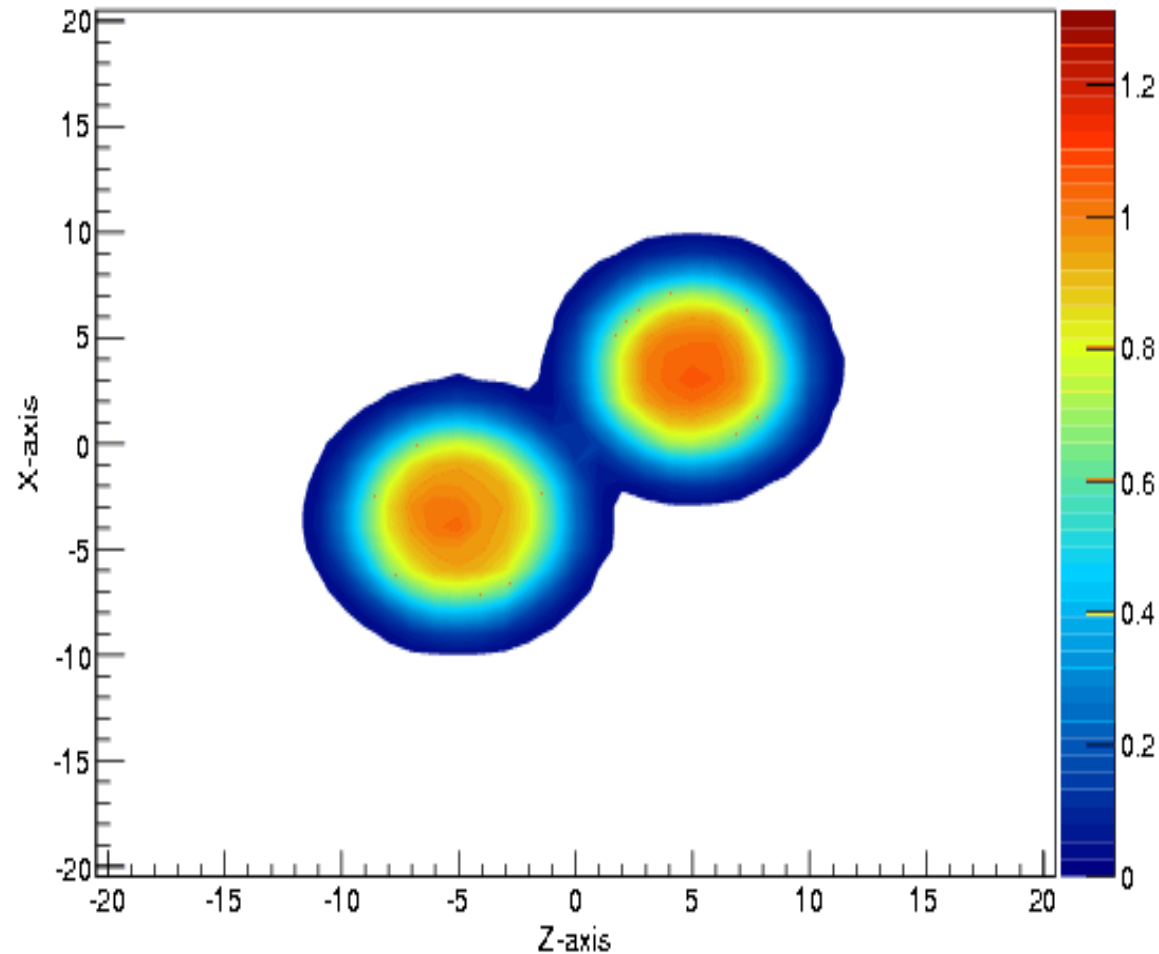
A heavy nucleus (like ^{208}Pb) is 18 orders of magnitude smaller
and 55 orders of magnitude lighter than a neutron star !



Yet bounded by a common entity, the nuclear Equation Of State (EOS) !



Experimental constraints on the nuclear equation-of-state from heavy-ion collisions



Observables sensitive to the EOS ?

Neutron-skin thicknesses

Pygmy resonances

Fragment isotope distribution, isotopic & isobaric yield ratios

Isospin distillation/fractionation, relative n & p densities

Isospin transport / diffusion / migration

Nuclear stopping & NZ equilibration

Pre-equilibrium emission

Particle - particle correlation

Light cluster production

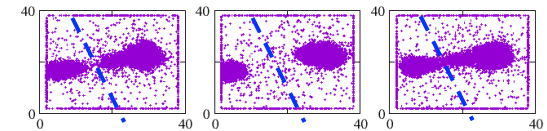
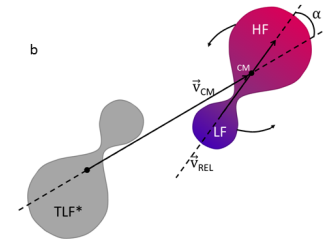
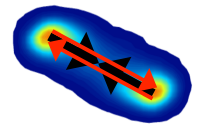
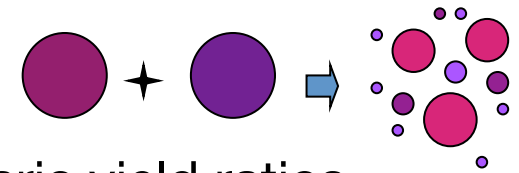
Collective Flow

Neck emission

Fusion vs Deep Inelastic reactions

Subthreshold particle production

...



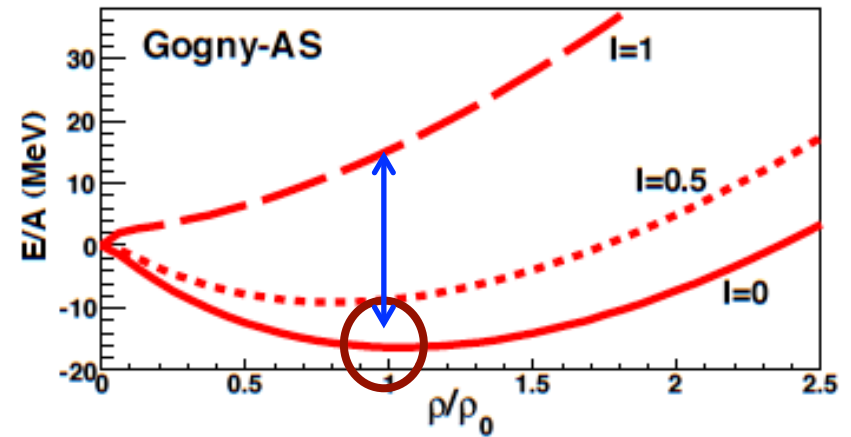
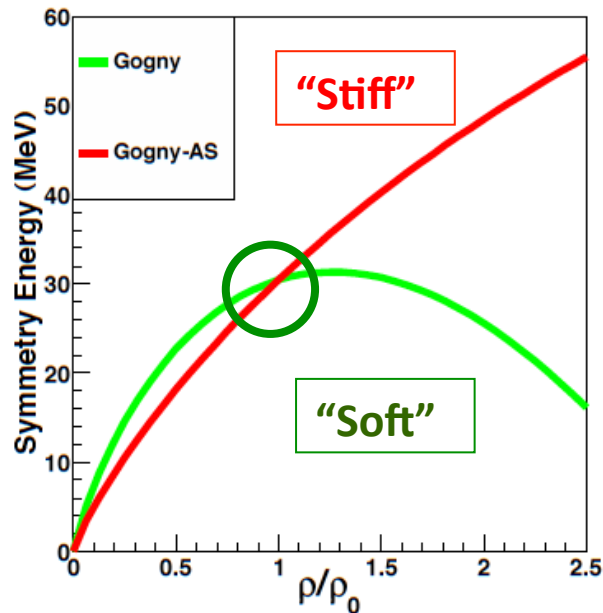
$$E_B = a_v A - a_s A^{2/3} - a_c \frac{Z^2}{A^{1/3}} - a_A \frac{(A - 2Z)^2}{A} - \delta(A, Z)$$

$$E(\rho, I) = E(\rho) + E_{sym}(\rho) I^2$$

with $I = \frac{\rho_n - \rho_p}{\rho_{Total}} \approx \frac{N - Z}{A}$

Binding Energy of Symmetric Nuclear Matter

Symmetry Energy Term for Asymmetric Matter

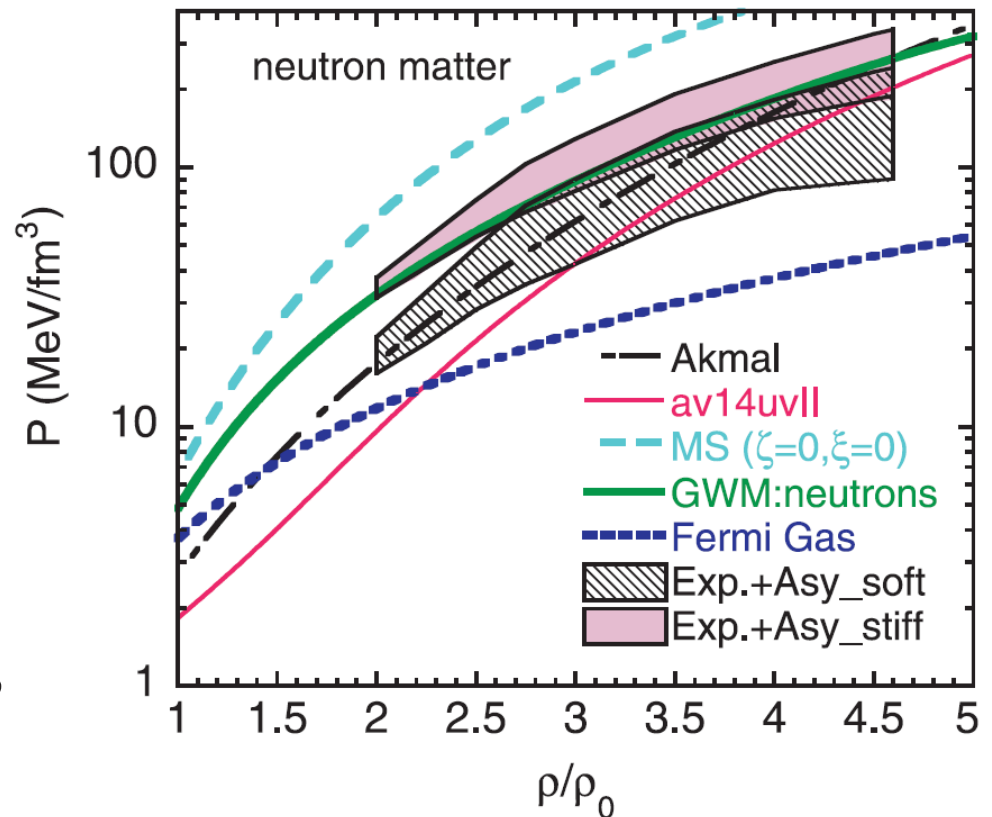
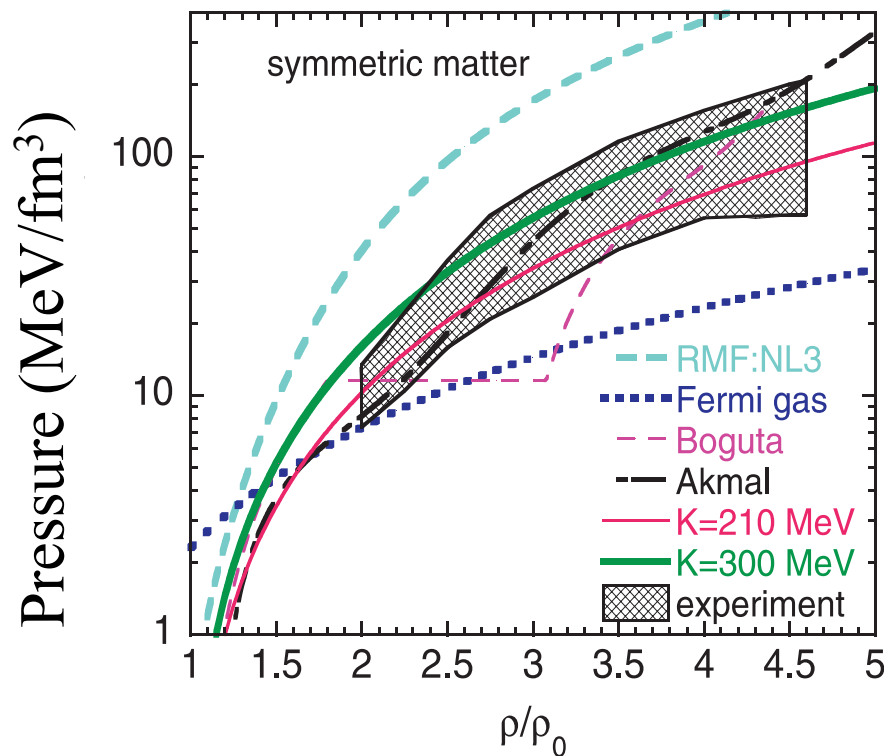


$$E_{sym}(\rho) = E(\rho, 1) - E(\rho, 0)$$



Constraining EOS from the flow measurements (Probing the high density dependence)

Au+Au flow ($E/A \sim 1-8$ GeV)

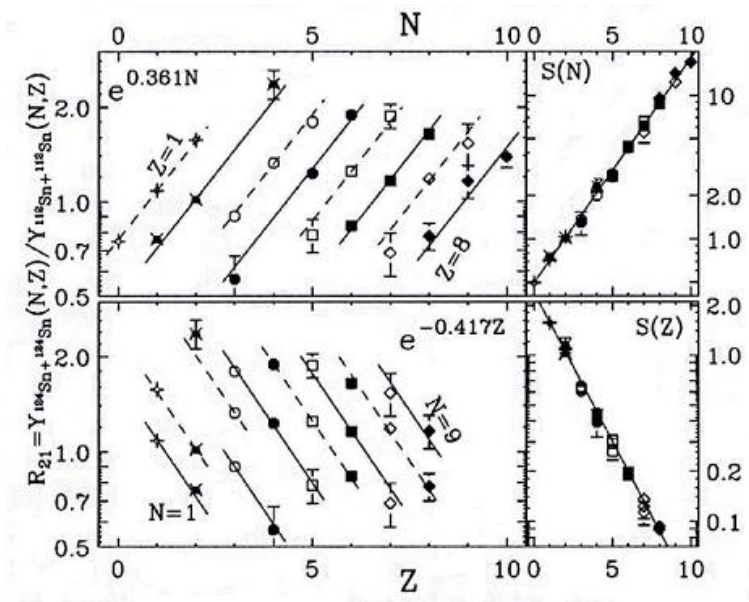
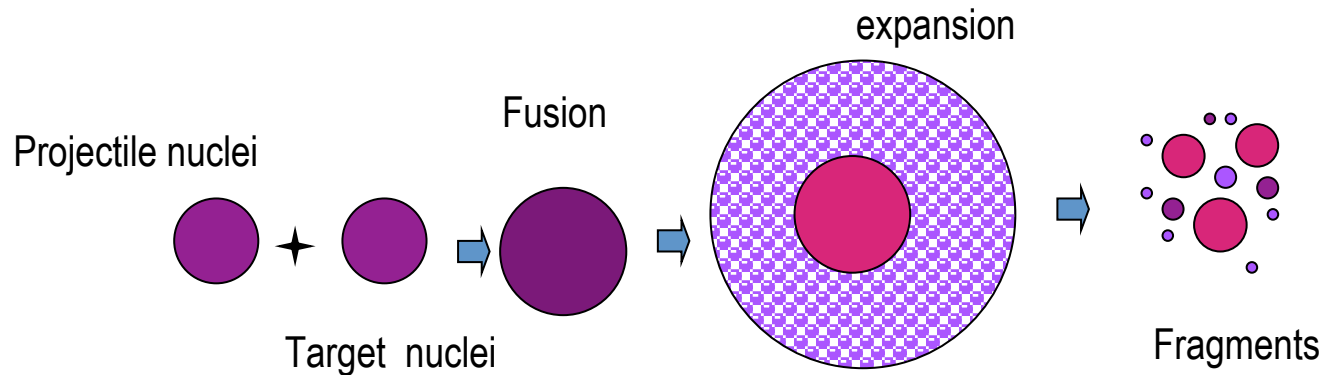


Danielewicz, Lacy, Lynch, Science 298,1592 (2002)



CYCLOTRON INSTITUTE
TEXAS A & M UNIVERSITY

Studying density dependence of symmetry energy : Multifragmentation



$$\alpha = \frac{4C_{sym}}{T} \left(\frac{Z_1^2}{A_1^2} - \frac{Z_2^2}{A_2^2} \right)$$

α – Scaling parameter

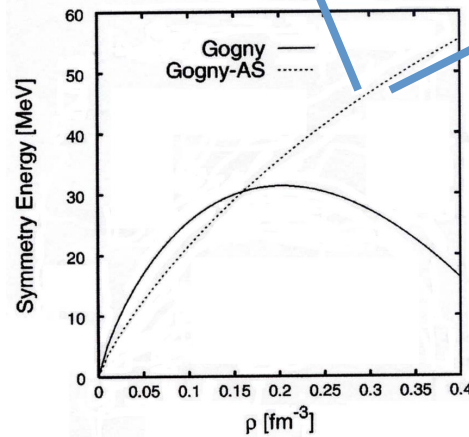
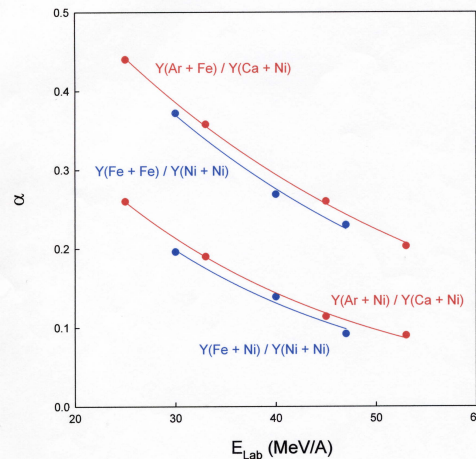
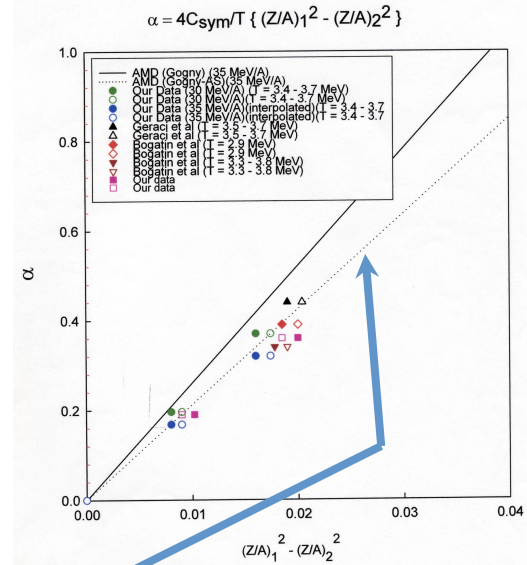
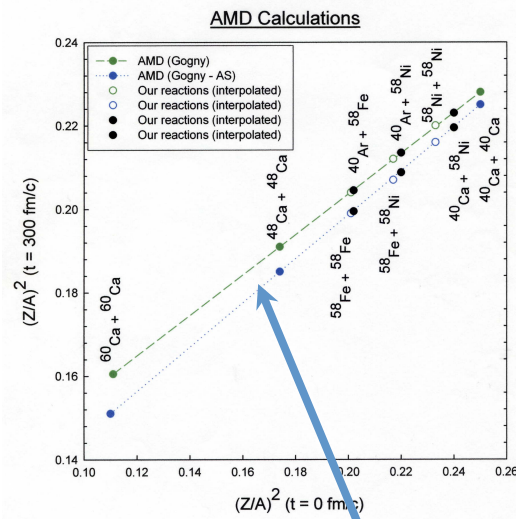
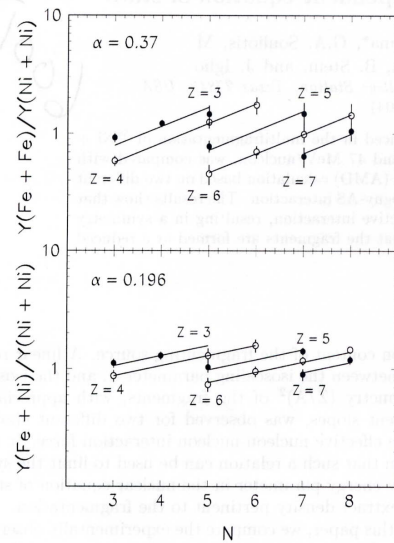
C_{sym} – Symmetry energy

M.B. Tsang et al, Phys. Rev. Lett 68 (2001) 5023



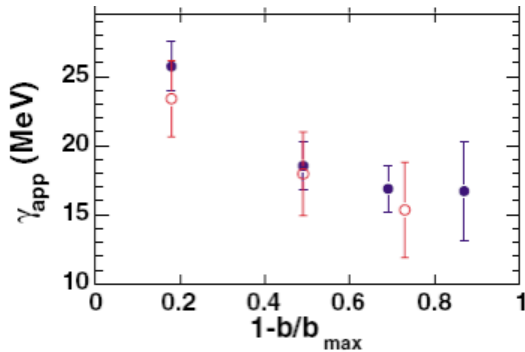
CYCLOTRON INSTITUTE
TEXAS A & M UNIVERSITY

Symmetry energy and the scaling parameter α

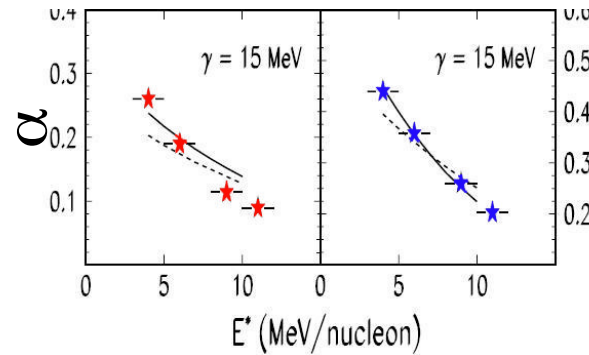


$$\alpha T = 4C_{\text{sym}} \left(\frac{Z_1^2}{A_1^2} - \frac{Z_2^2}{A_2^2} \right)$$

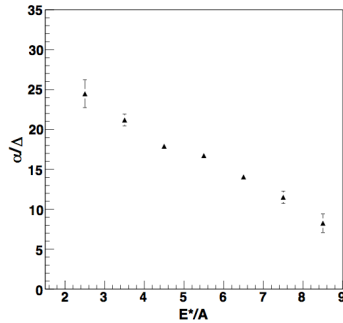
Decrease in Asymmetry energy (Expt. Observation)



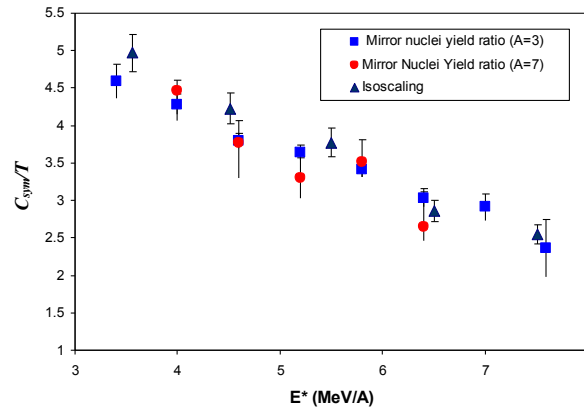
A. Le Fevre et al., PRL 94 (2005) 162701



J. Iglio et al., PRC 74 (2006) 024605

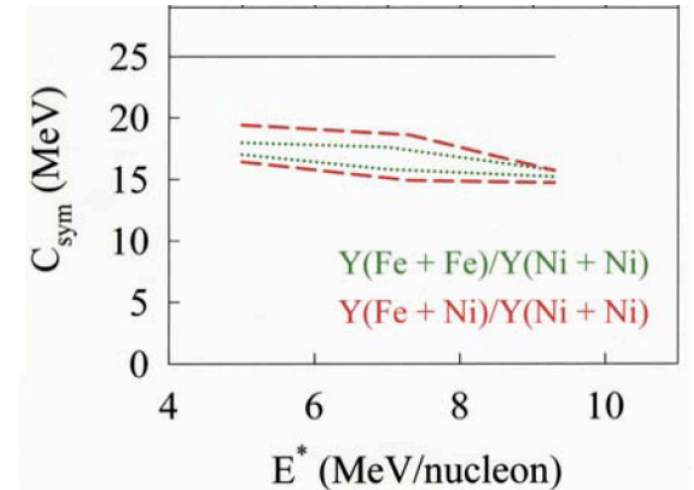
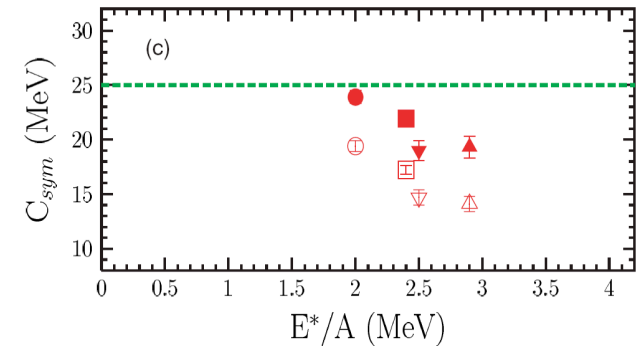


S. Wuenschel, Phys. Rev. C 79, 061602(R) (2009)



R. Tripathi, Phys. Rev. C **83**, 054609 (2011).
Int. J. Mod. Phys. E 21, 1250019 (2012)

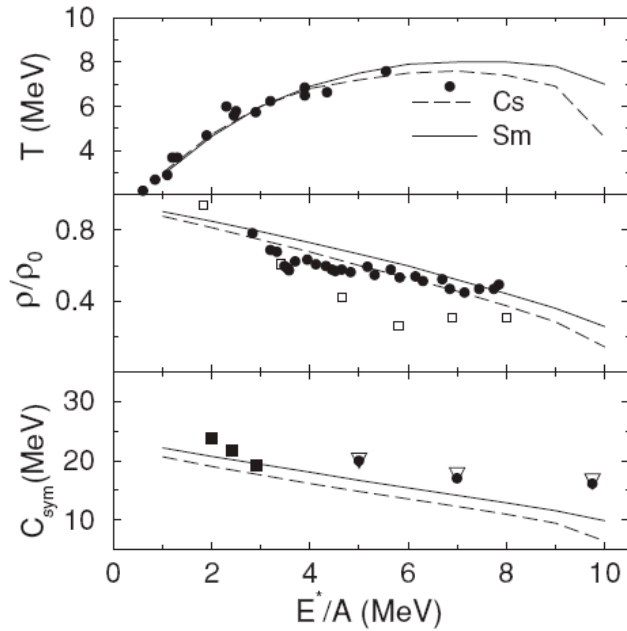
G.A. Souliotis et al., PRC 73 (2006) 024606
G.A. Souliotis et al., PRC 75 (2007) 011601



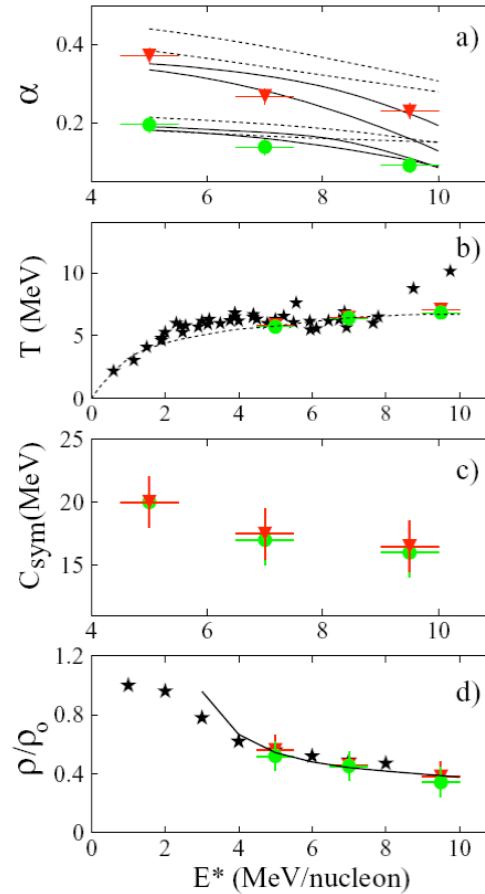
D.V. Shetty et al., PRC 74 (2005) 024602

Decrease in E_{sym} related to thermal expansion

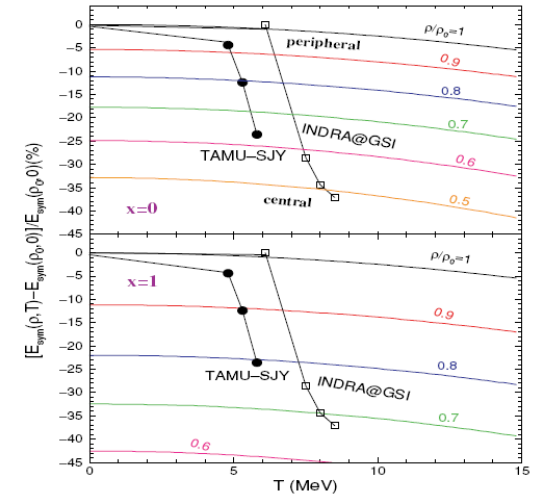
- Finite T Thomas-Fermi Seyler Blanchard interaction



S.K. Samaddar et al., PRC 76 (2007) 041602



D.V. Shetty et al., PRC 76 (2007) 024606



B.A. Li et al., PRC 74 (2006) 034610



Determination of symmetry energy through dependence of fragment yield ratios on source isospin

Landau expansion of free energy near the critical point

$$\frac{F}{T} = \frac{1}{2}am^2 + \frac{1}{4}bm^4 + \frac{1}{6}cm^6 - \frac{H}{T}m$$

$m (=N-Z)/A$: Order parameter

H : External field

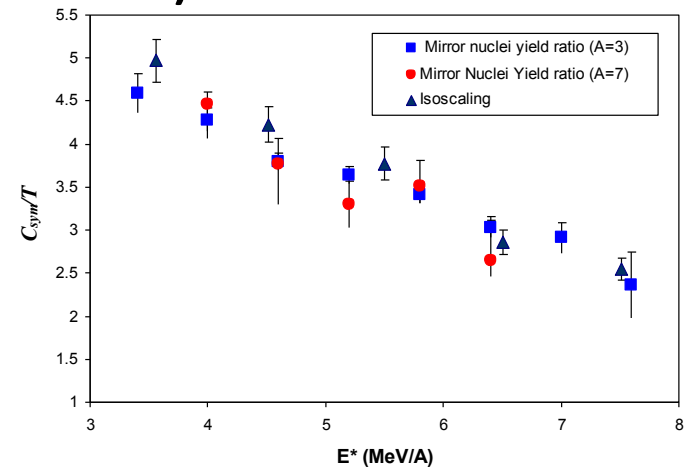
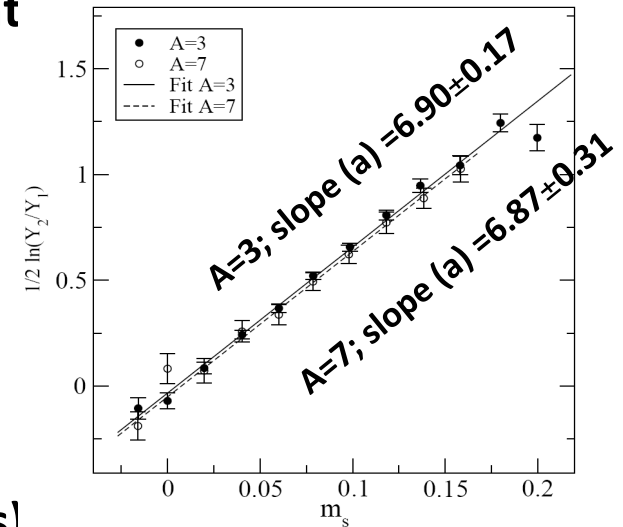
$$\frac{H}{T} = am_s (1 + \text{Higher order terms in 'm' and 'm_s'})$$

For mirror nuclei yield ratio (ignoring higher order terms)

$$\frac{1}{2} \ln \left(\frac{Y_2}{Y_1} \right) = am_s$$

Source Isospin

$$\frac{C_{Sym}}{T} \approx \frac{1}{2} a$$

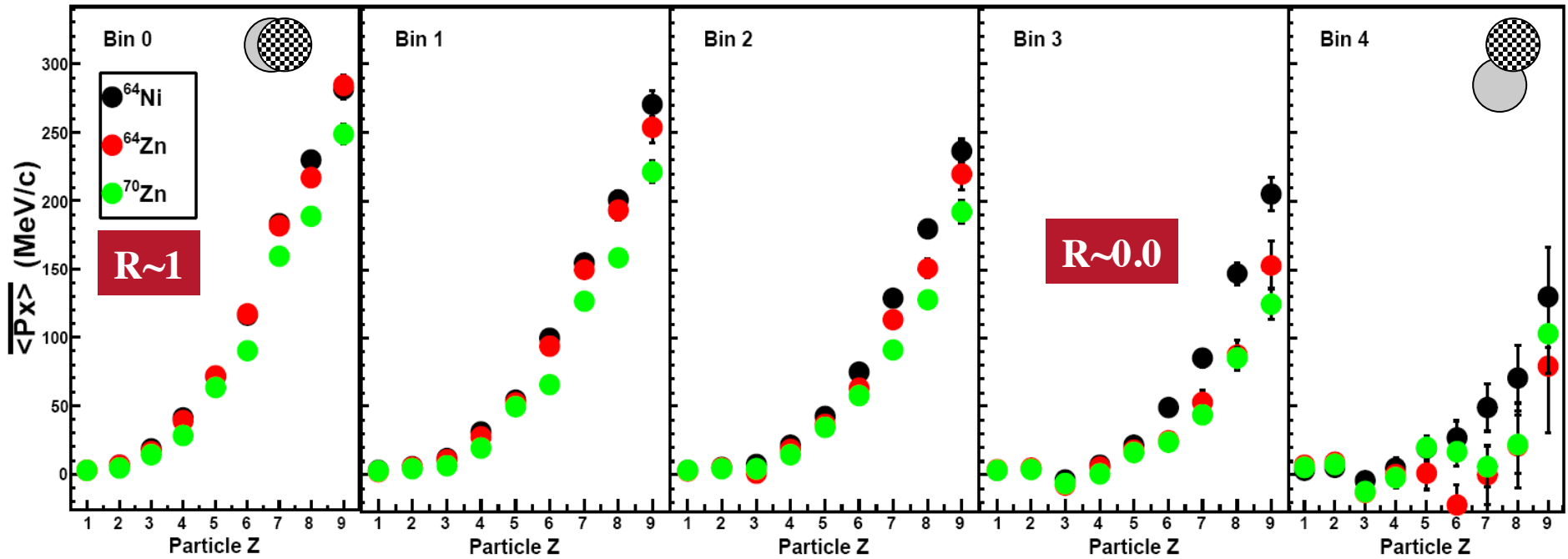


R. Tripathi, Phys. Rev. C **83**, 054609 (2011).
Int. J. Mod. Phys. E 21, 1250019 (2012)



CYCLOTRON INSTITUTE
TEXAS A & M UNIVERSITY

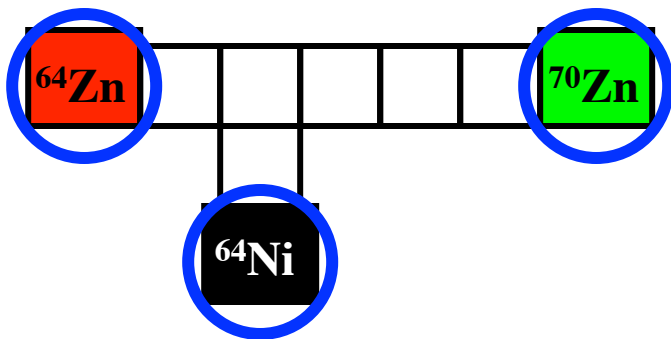
IMF Transverse Flow



Mass Dependence



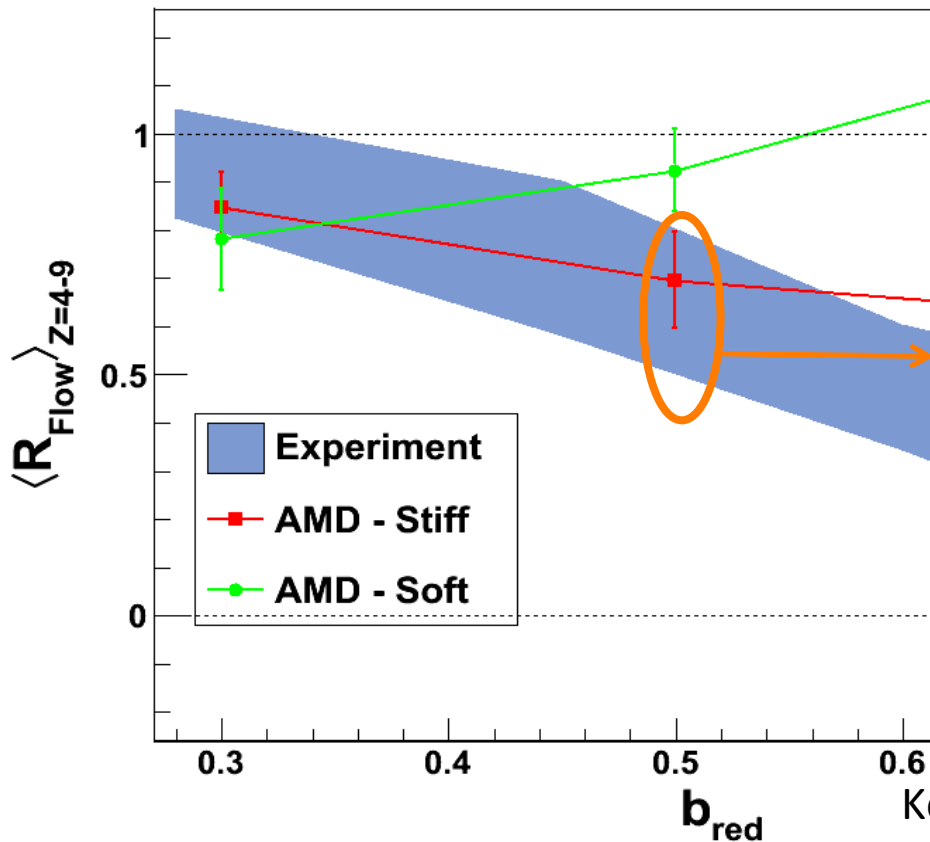
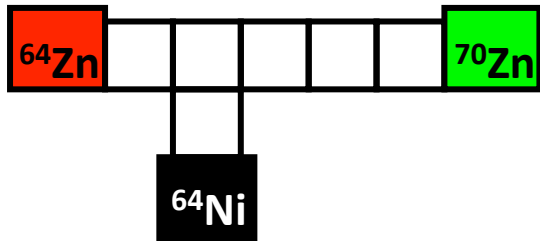
Charge Dependence



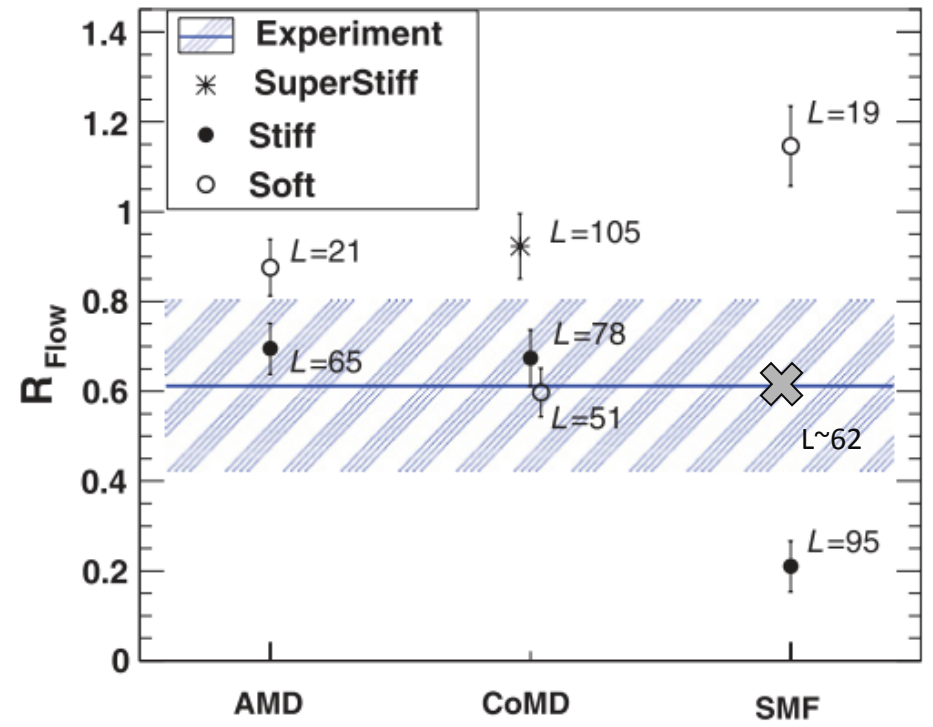
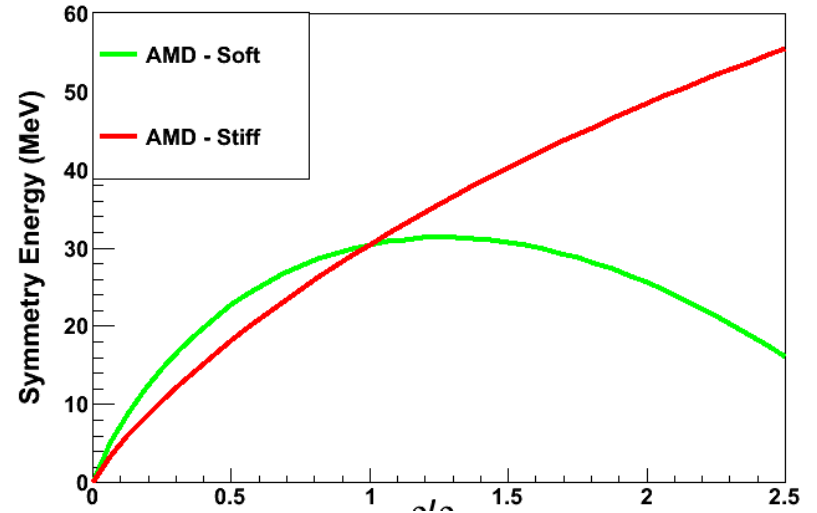
$$R_{Flow} = \frac{\overline{\langle Px/A \rangle}_{^{64}\text{Zn}} - \overline{\langle Px/A \rangle}_{^{70}\text{Zn}}}{\overline{\langle Px/A \rangle}_{^{64}\text{Ni}} - \overline{\langle Px/A \rangle}_{^{70}\text{Zn}}}$$

IMF Transverse Flow

$$R_{Flow} = \frac{\overline{\langle Px/A \rangle}_{64Zn} - \overline{\langle Px/A \rangle}_{70Zn}}{\overline{\langle Px/A \rangle}_{64Ni} - \overline{\langle Px/A \rangle}_{70Zn}}$$



Comparison to AMD Model



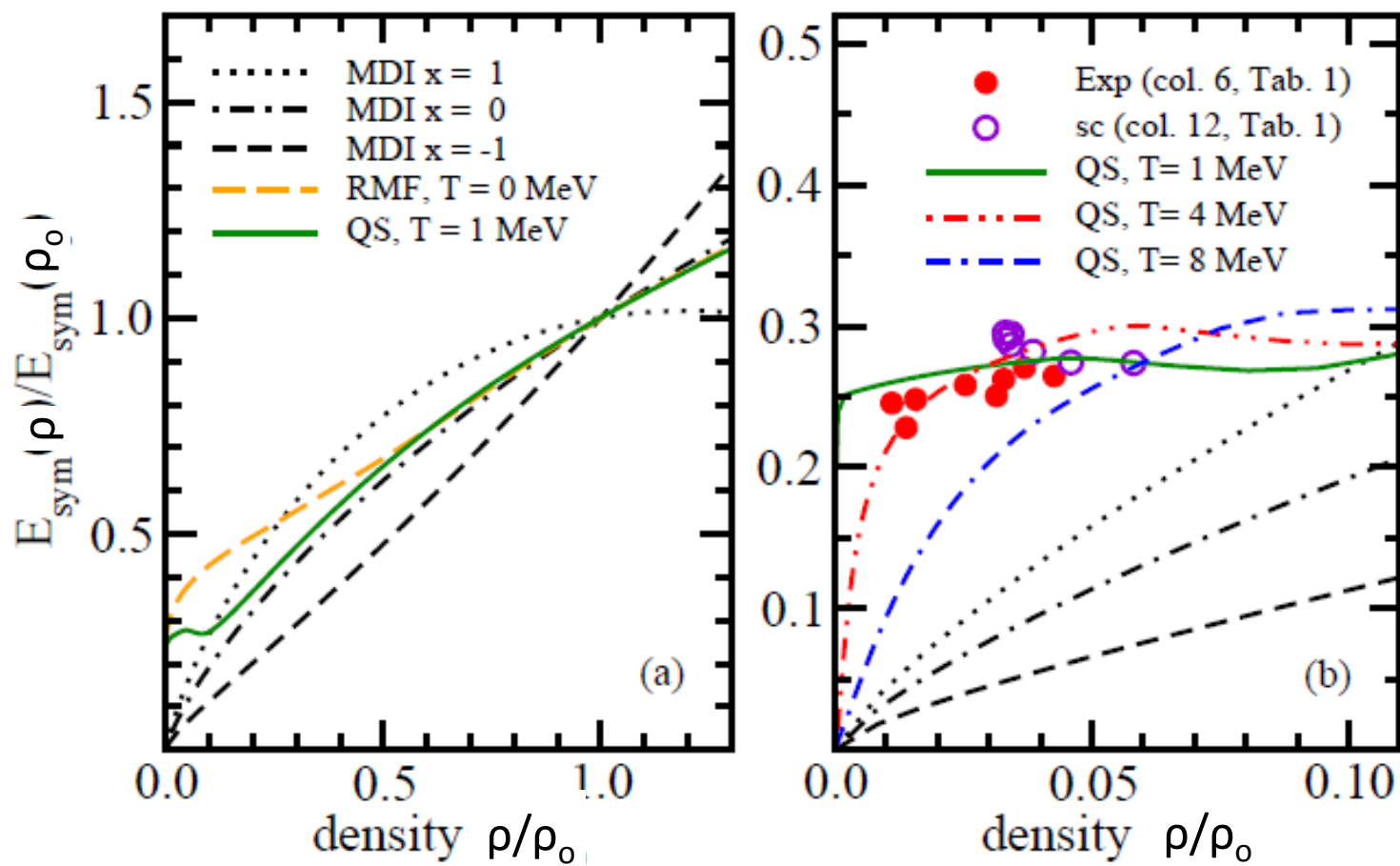
Kohley, PRC85(2012)



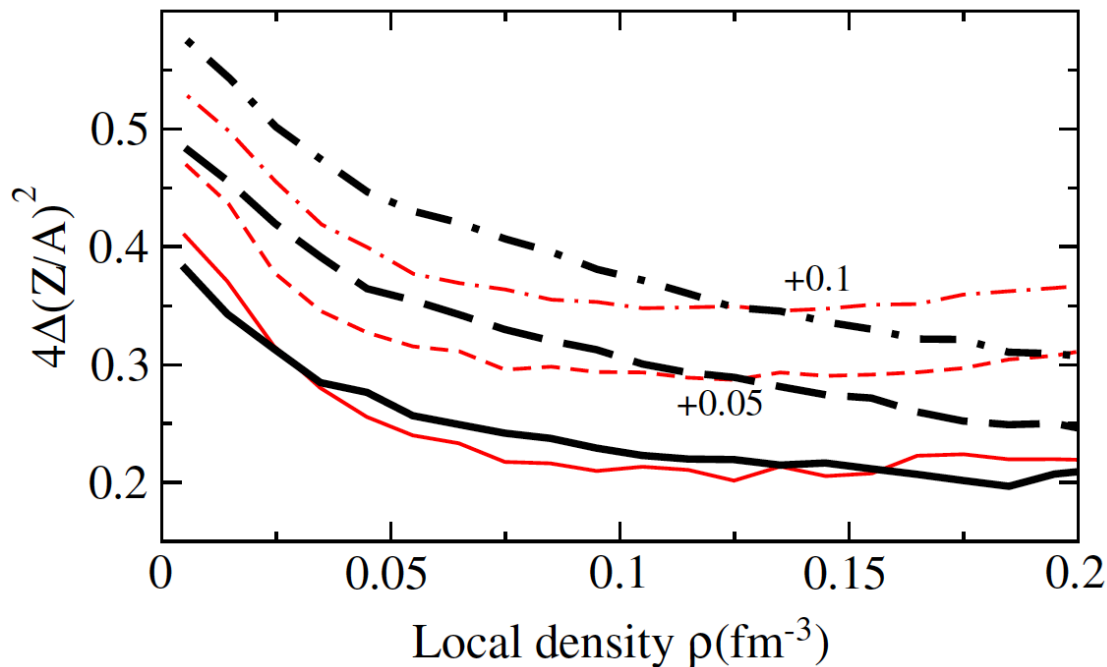
CYCLOTRON INSTITUTE
TEXAS A & M UNIVERSITY

Symmetry energy of dilute warm nuclear matter

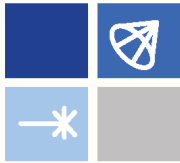
Clusters important for low density matter



Fluctuations and Symmetry Energy in Nuclear Fragmentation Dynamics



The amplitude of isovector fluctuations follows the evolution of the local density and approaches the corresponding local equilibrium value that is linked to the density-dependent symmetry free energy. Thus, fragment isospin fluctuations and isoscaling parameters are related to the symmetry energy at the fragment formation density.



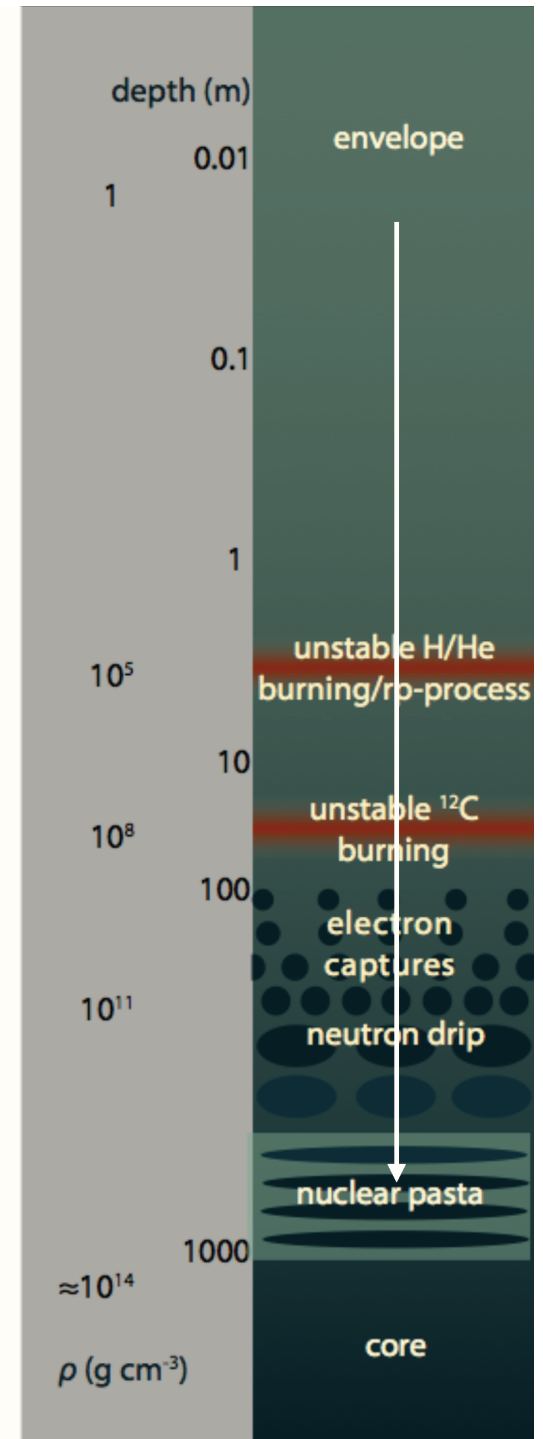
Why neutron star crusts?



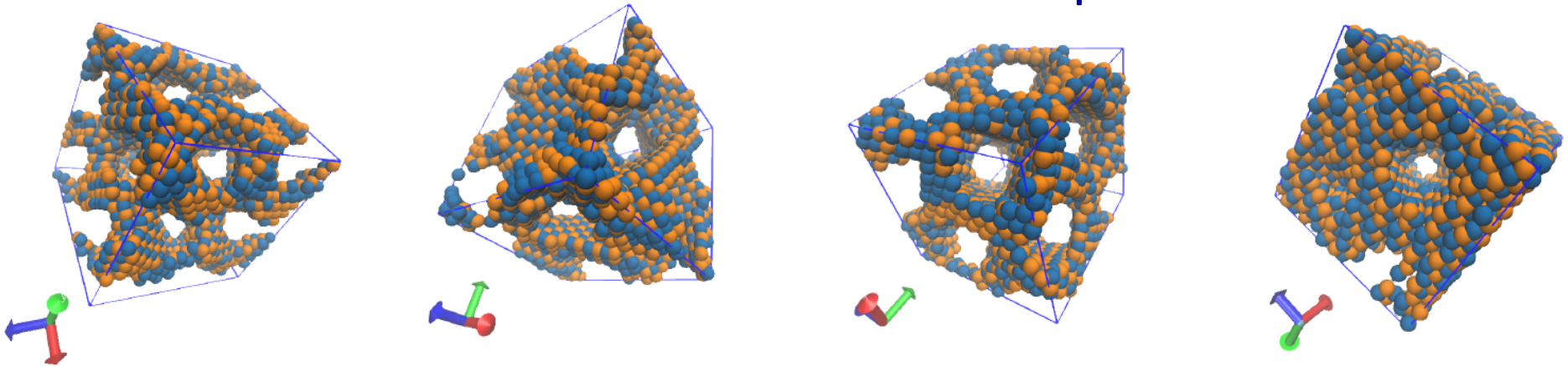
A. Piro, Carnegie Obs.

Accretion pushes matter through the crust and induces reactions.

These reactions produce a wealth of observable phenomena over a wide range of timescales.



Phase transitions in nuclear pasta

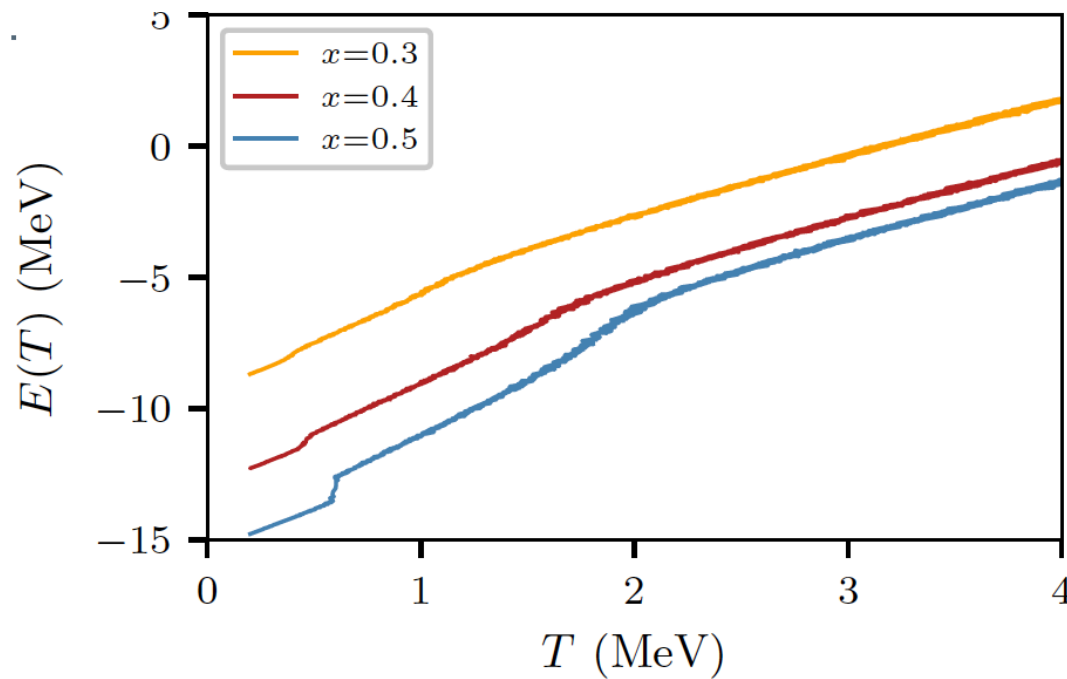


(a) $\rho = 0.05$

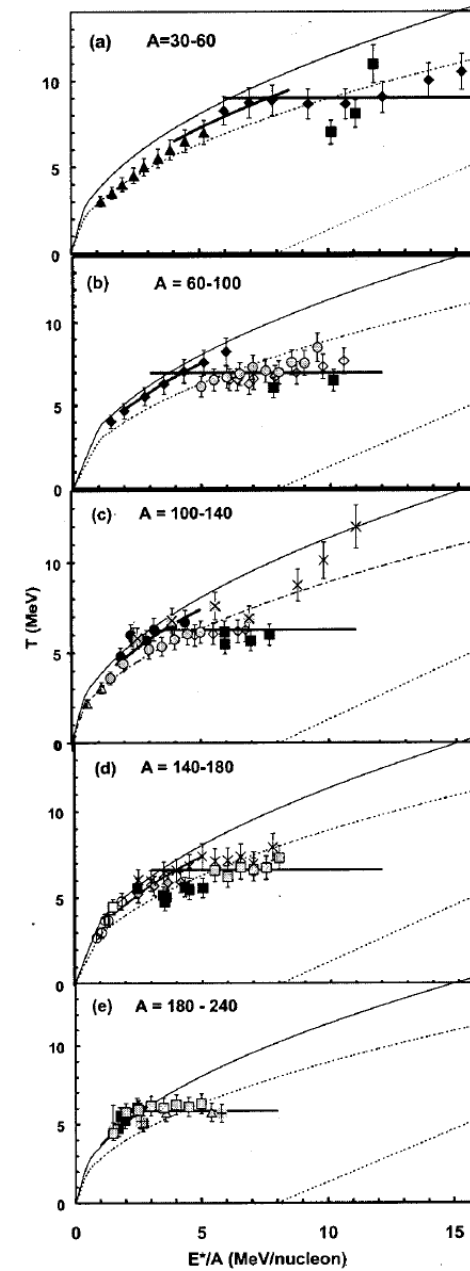
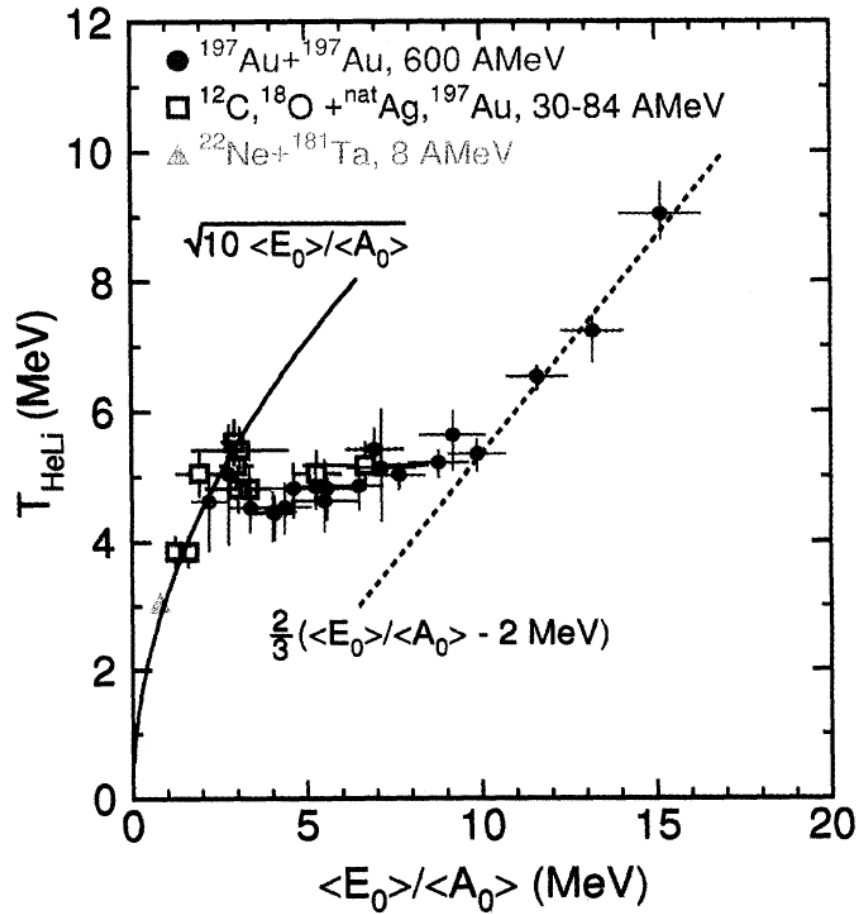
(b) $\rho = 0.06$

(c) $\rho = 0.07$

(d) $\rho = 0.085$



Nuclear Caloric Curve

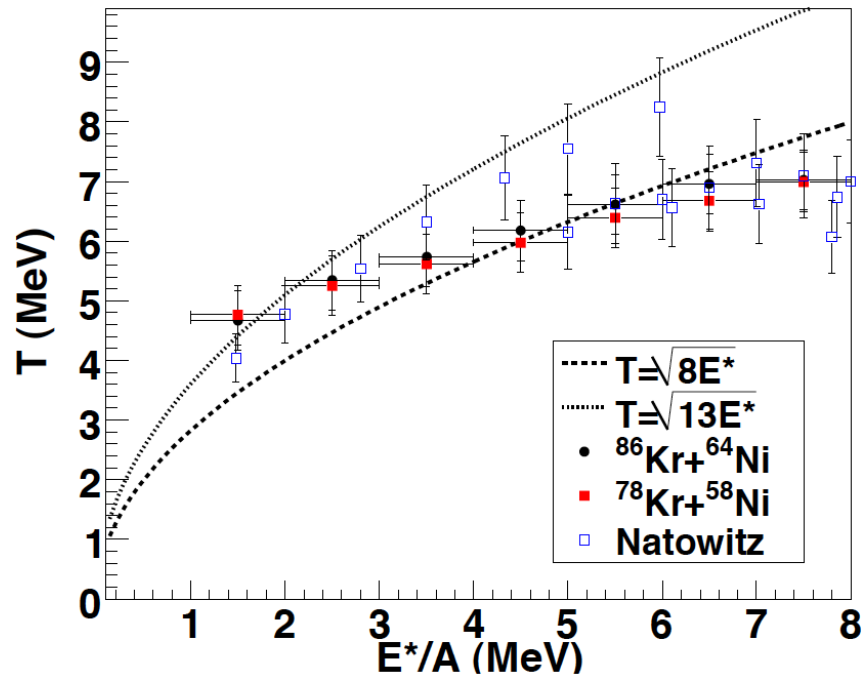


Pochodzalla et al. PRL 75, 1040 (1995)

Natowitz et al. PRC, 034618 (2002)

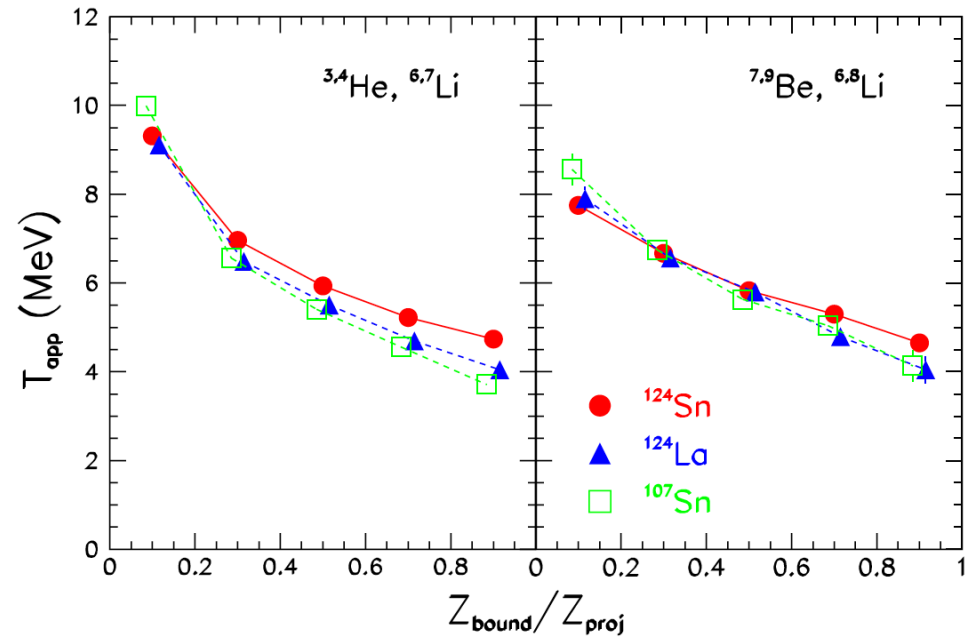
Caloric Curve: Asymmetry Dependence?

Experiment



S. Wuenschel, Ph.D. Thesis, 2009

Slight offset of neutron-rich system, but not statistically significant



Sfienti et al., PRL 102, 152701 (2009)

Possible dependence on asymmetry, depends on impact parameter and thermometer.

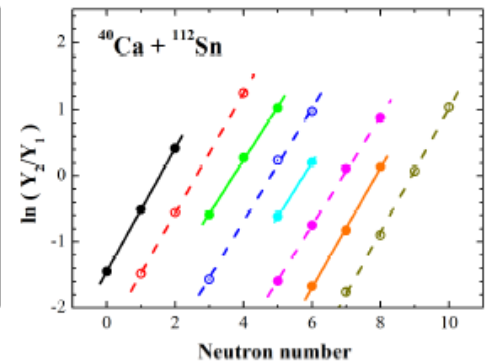
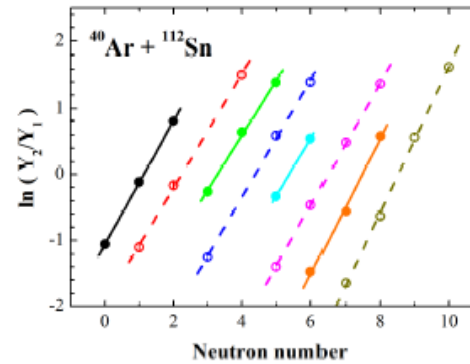
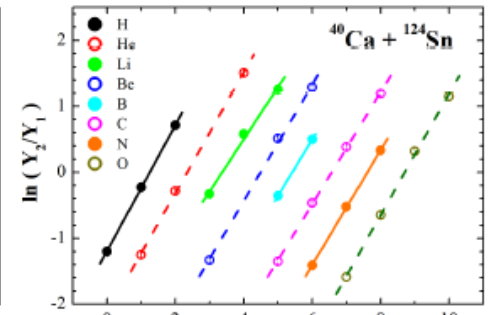
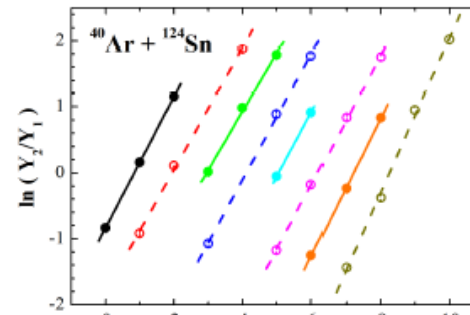
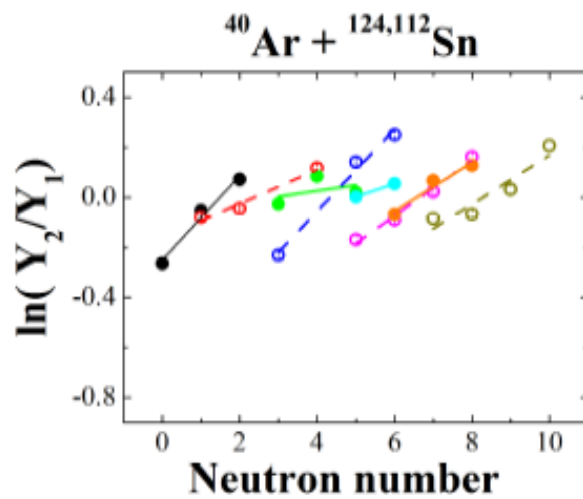
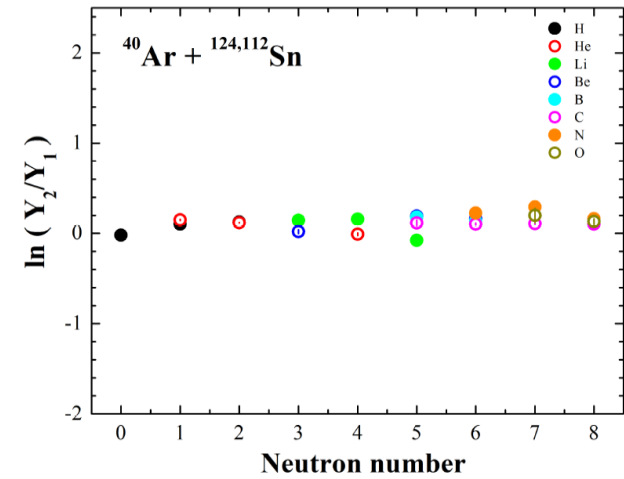
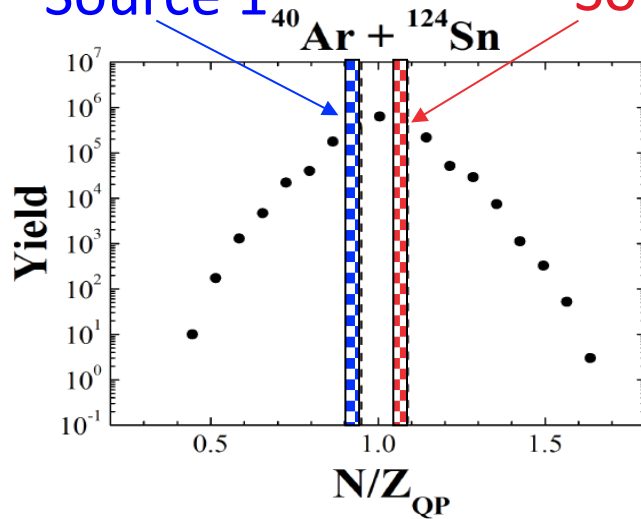
Selection was on the system composition.
Should use reconstructed-source composition



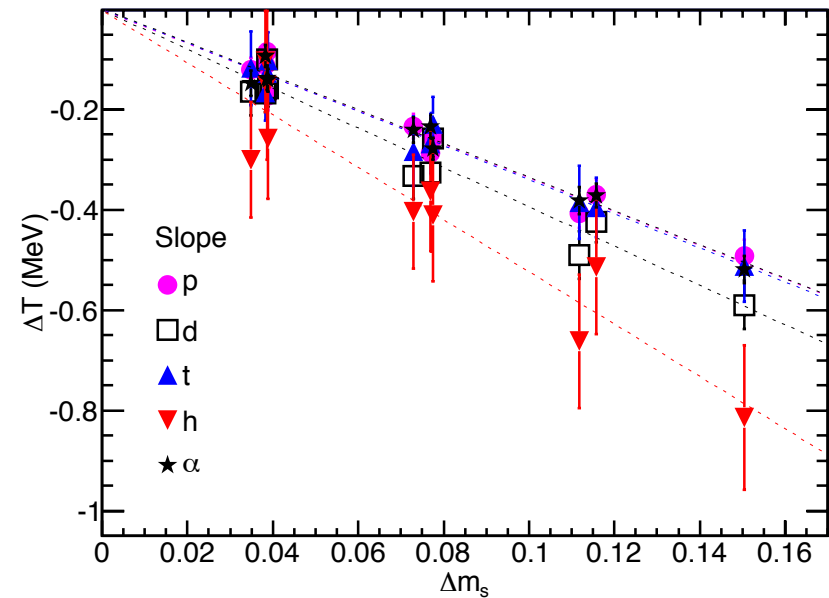
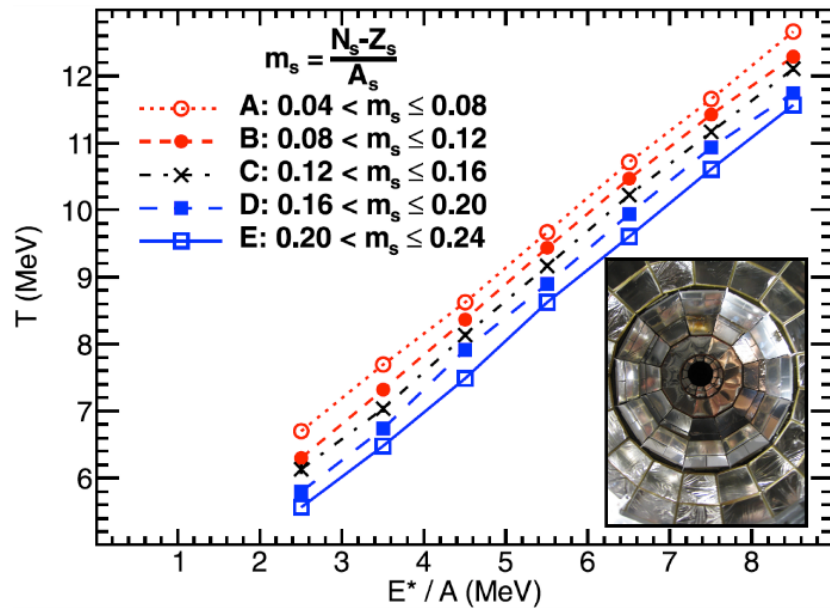
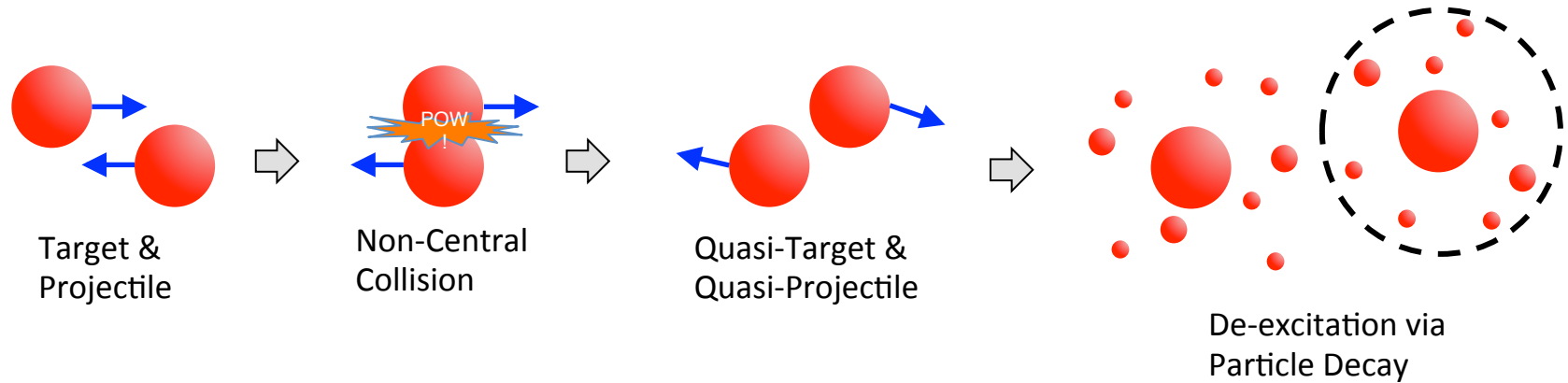
CYCLOTRON INSTITUTE
TEXAS A & M UNIVERSITY

Reconstructed PLFs

Source 1 Source 2



Asymmetry Dependence of the Nuclear Caloric Curve

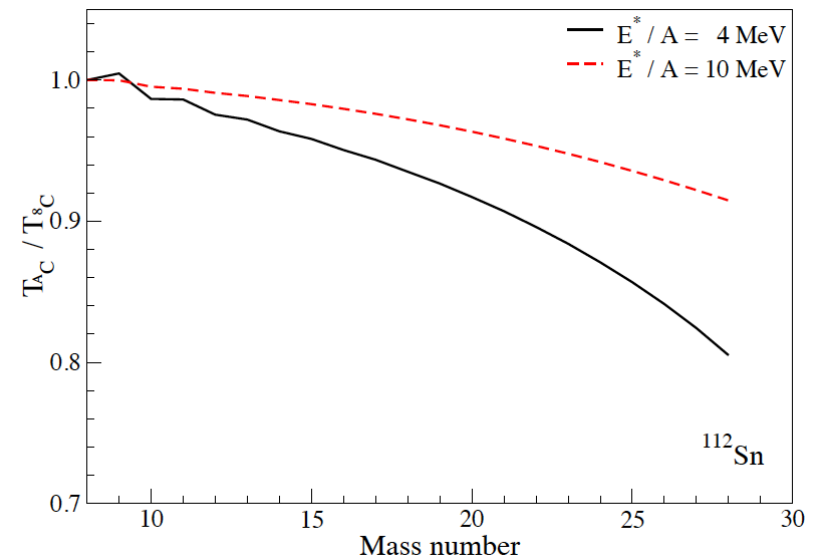
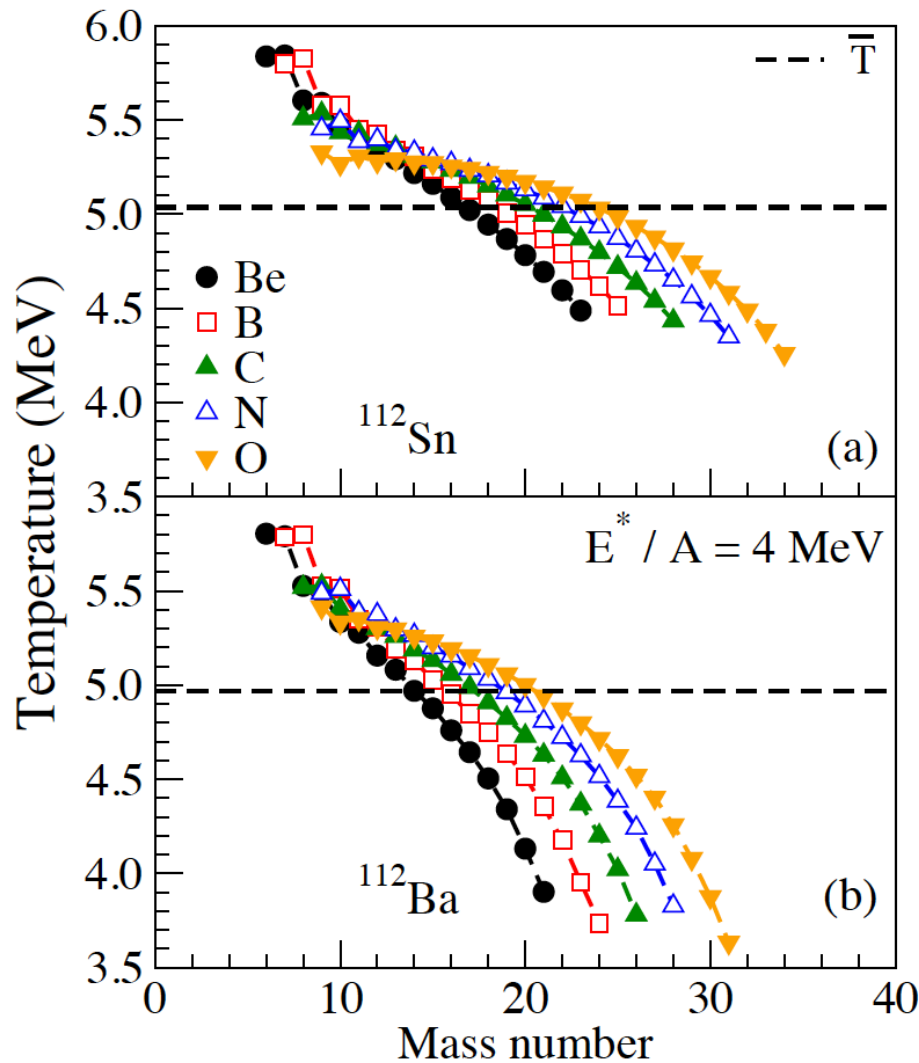


McIntosh, PLB **719**, 337 - 340 (2013)



CYCLOTRON INSTITUTE
TEXAS A & M UNIVERSITY

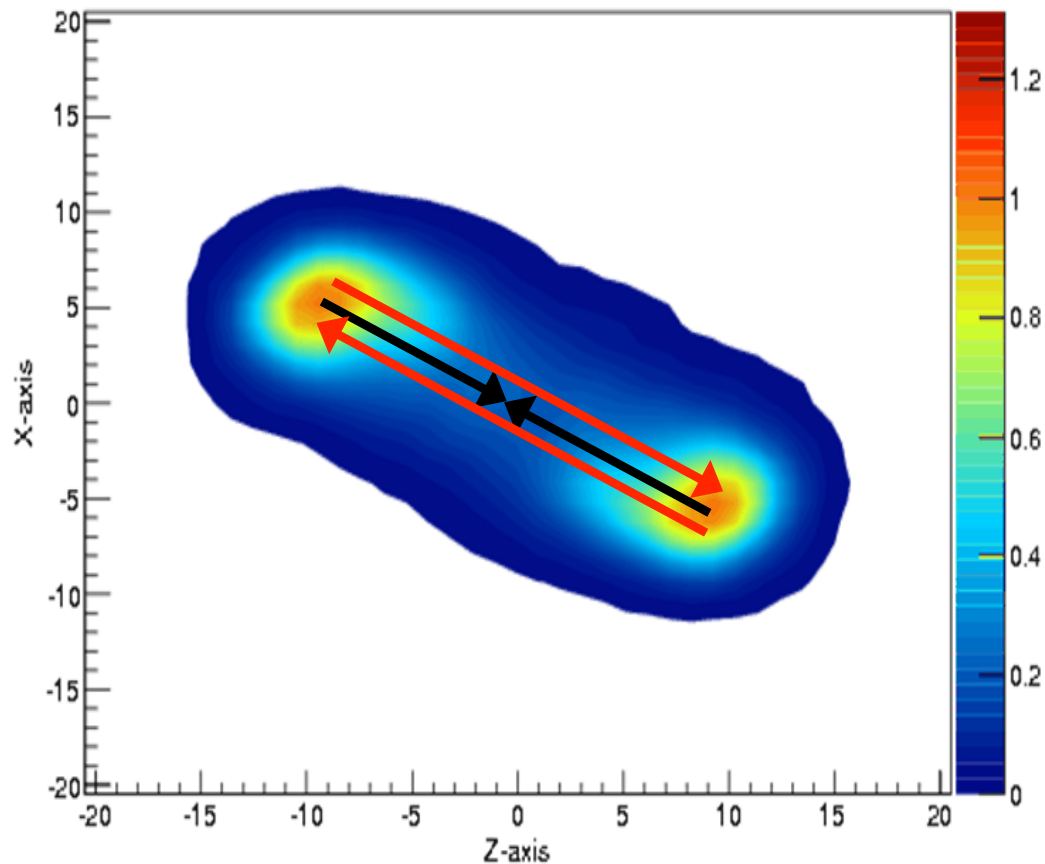
Isotopic dependence of the fragments' internal temperatures observed in multifragment emission



SMM-DE, emphasizing the discretization of the energy.

Isospin Transport

iBUU $^{70}\text{Zn} + ^{64}\text{Zn}$ $b = 7$ fm collision: density contour plots in XZ plane



$$D_q^\rho = ct \left(\frac{\partial \mu_q}{\partial \rho} \right)_{I,T}$$

$$D_q^I = -ct \left(\frac{\partial \mu_q}{\partial I} \right)_{\rho,T}$$

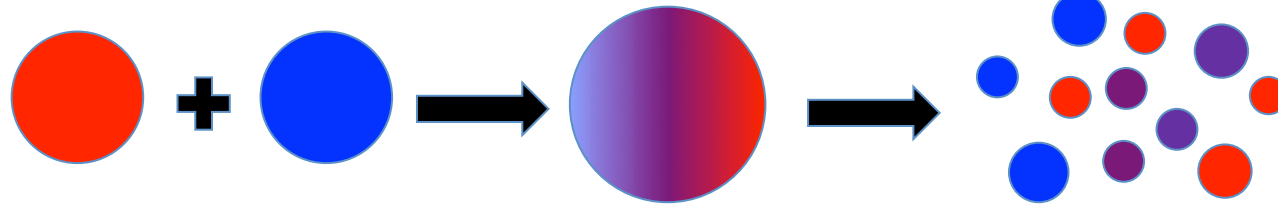
$(q = n, p)$

Drift (total nucleon density dependent)

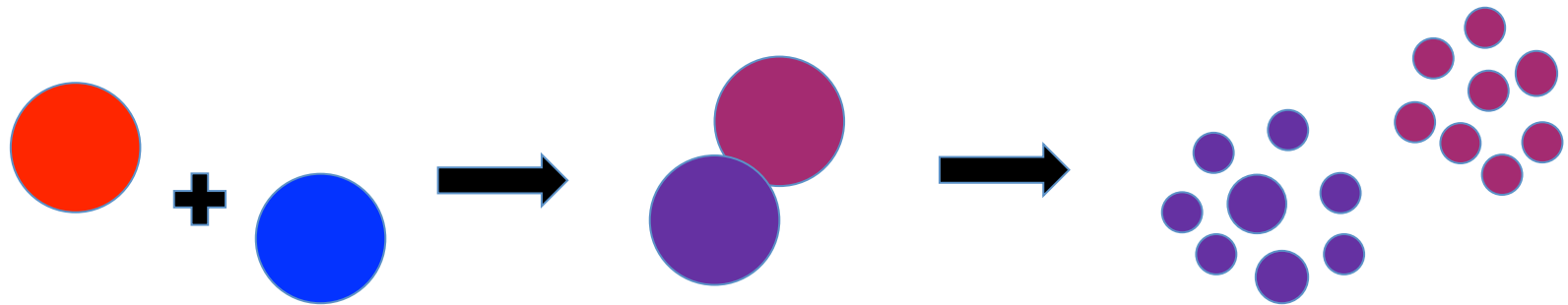
Diffusion (isospin concentration dependent)

Isospin Equilibration can be studied in multiple ways

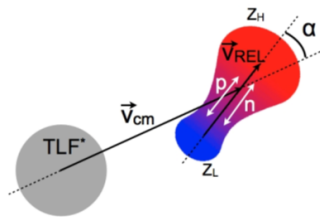
Translucency in central collisions



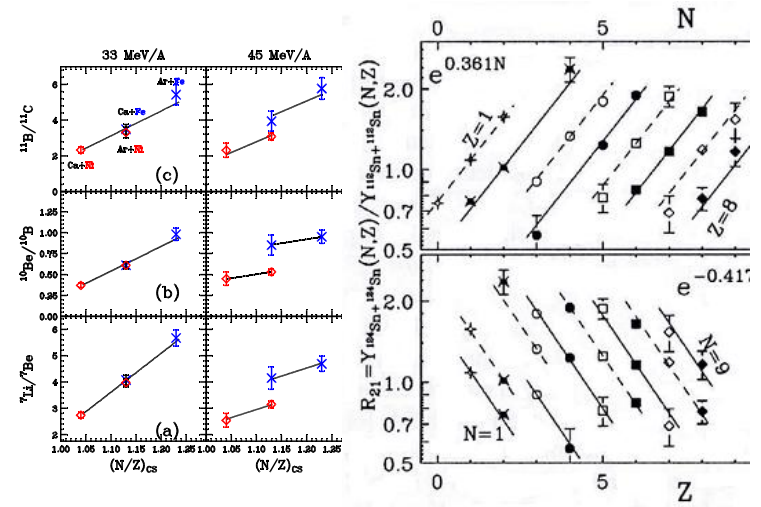
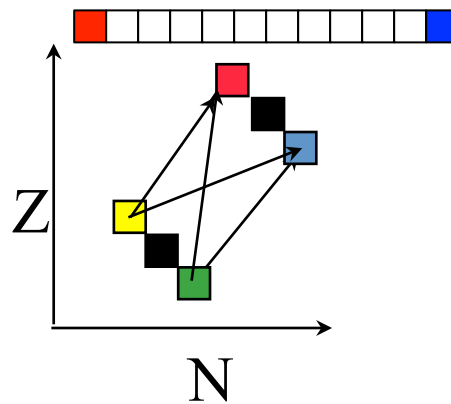
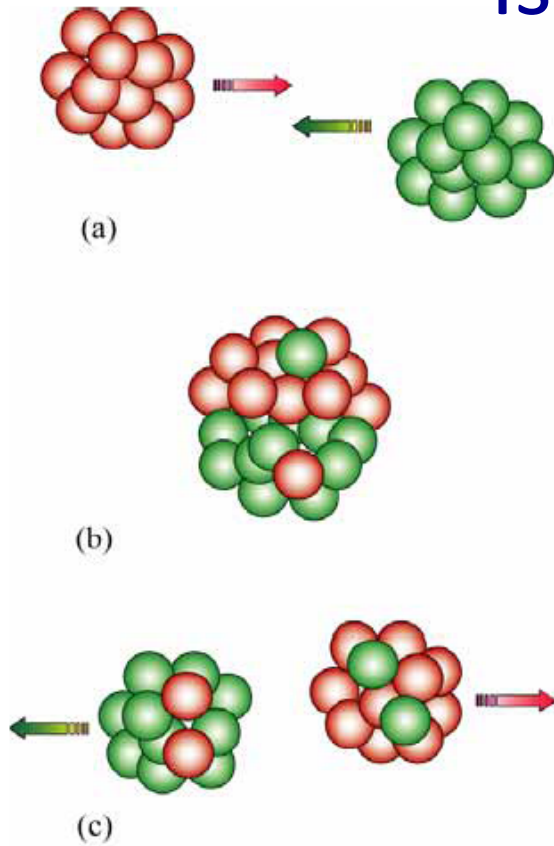
Diffusion between target and projectile in peripheral collisions



Transport in deformed nuclear systems



Isospin Equilibration / Diffusion



Non equilibration with Isotopically resolved fragments / ratios: Yennello, PLB321(94), Johnston, PLB 371 (1996), B.A. Li, PRC52(1995)

Isospin Tracer Method
Rami, et al, PRL84 (2000)

Diffusion coefficient connected to symmetry potential
L Shi & P Danielewicz, PRC68 (2003)

Measured isospin diffusion in Sn+Sn
Tsang, PRL92 (2004)

$$R_i = \frac{2\delta_i - \delta_{NR} - \delta_{NP}}{\delta_{NR} - \delta_{NP}}$$

where $\delta_i = I_i = \frac{(N_i - Z_i)}{(N_i + Z_i)}$

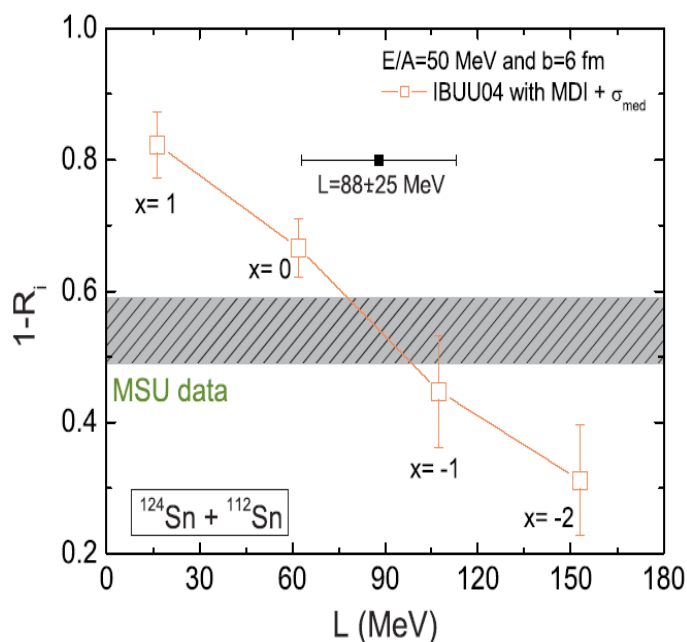


iBUU Isospin tracer results

- $^{70}\text{Zn} + ^{70}\text{Zn}$
- ▲ $^{70}\text{Zn} + ^{64}\text{Zn}$
- ▼ $^{64}\text{Zn} + ^{70}\text{Zn}$
- $^{64}\text{Zn} + ^{64}\text{Zn}$
- ◆ $^{64}\text{Zn} + ^{64}\text{Ni}$
- ◆ $^{64}\text{Ni} + ^{64}\text{Zn}$
- ◆ $^{64}\text{Ni} + ^{64}\text{Ni}$

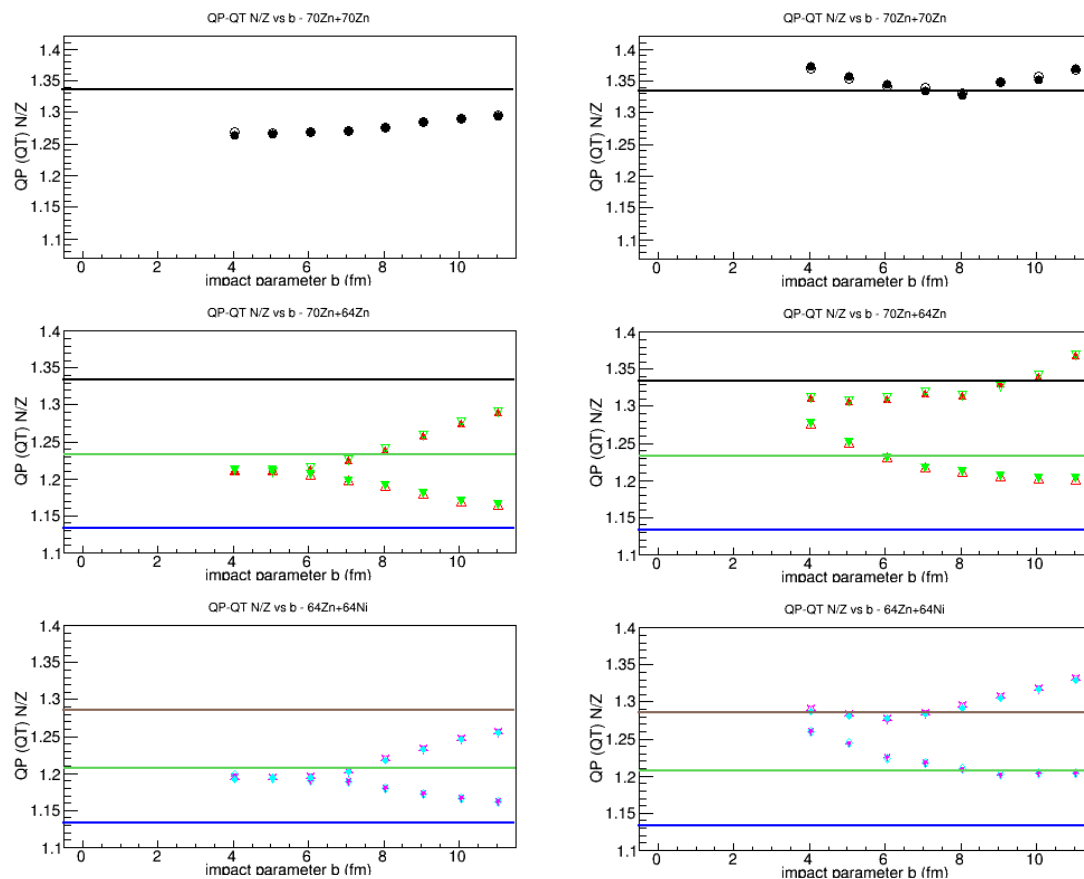
$^{112,124}\text{Sn} + ^{112,124}\text{Sn}$

Tsang, PRL 92 (2004)

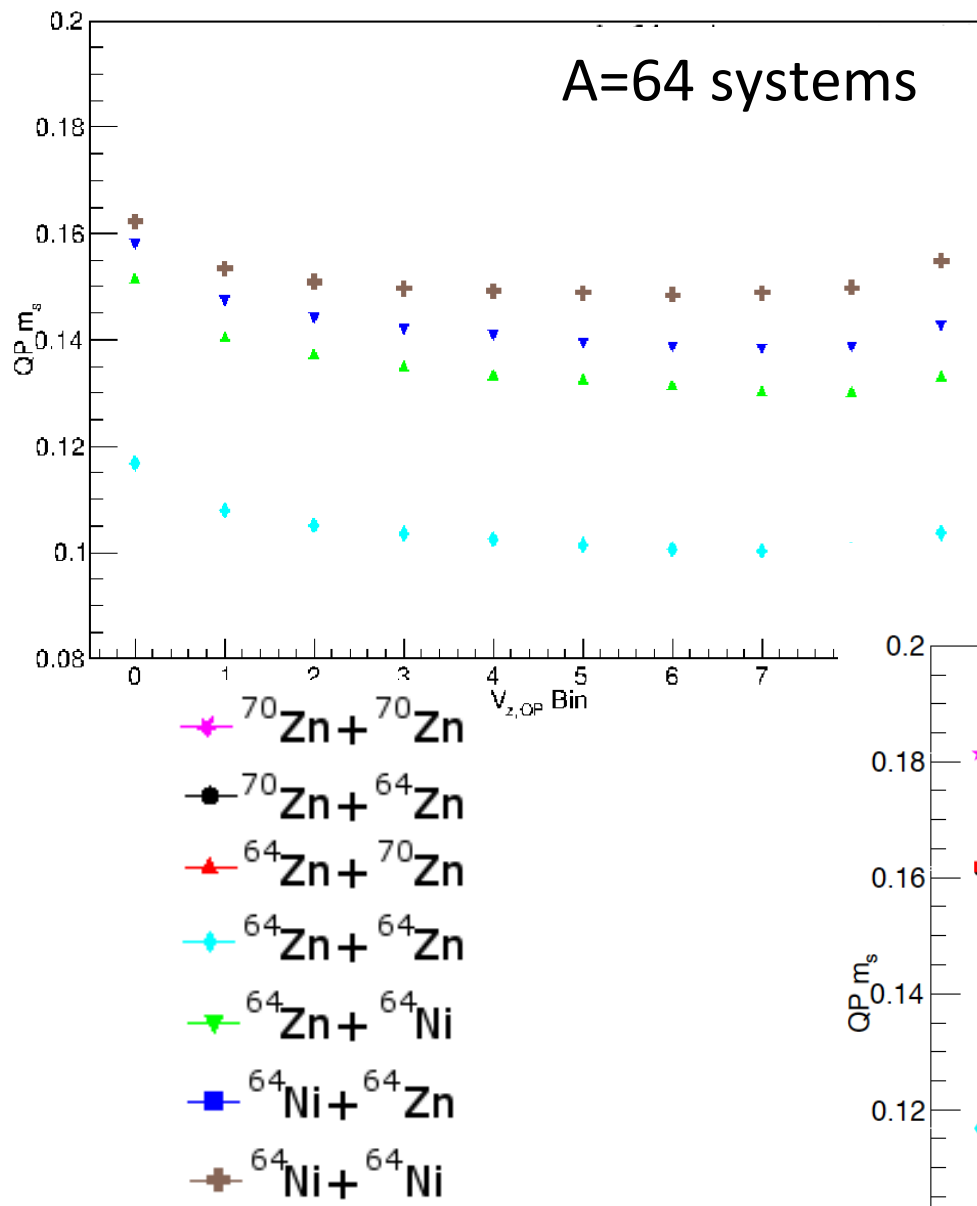


“asy-soft” $x=1$

“asy-stiff” $x=-2$



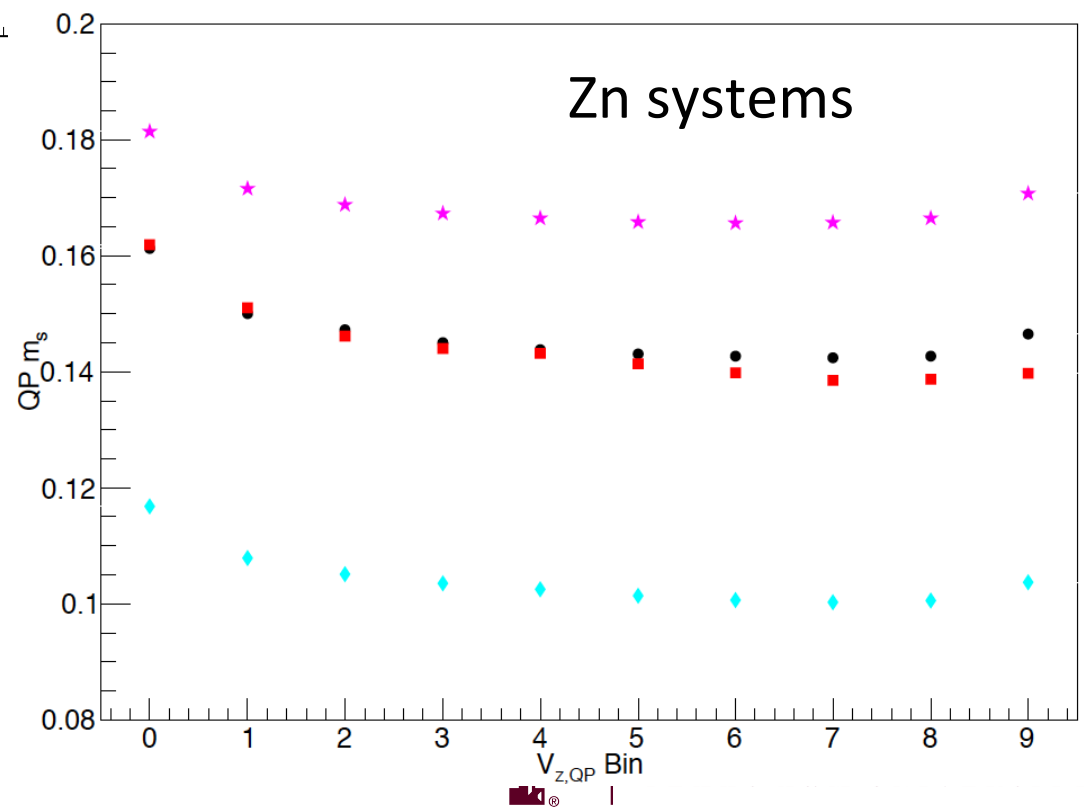
Lines are values for the composite system N/Z

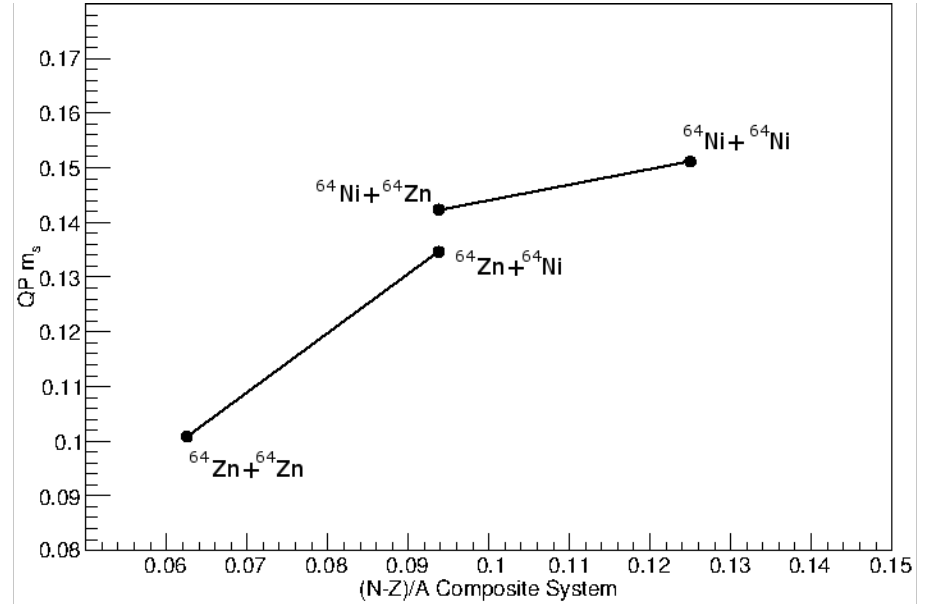
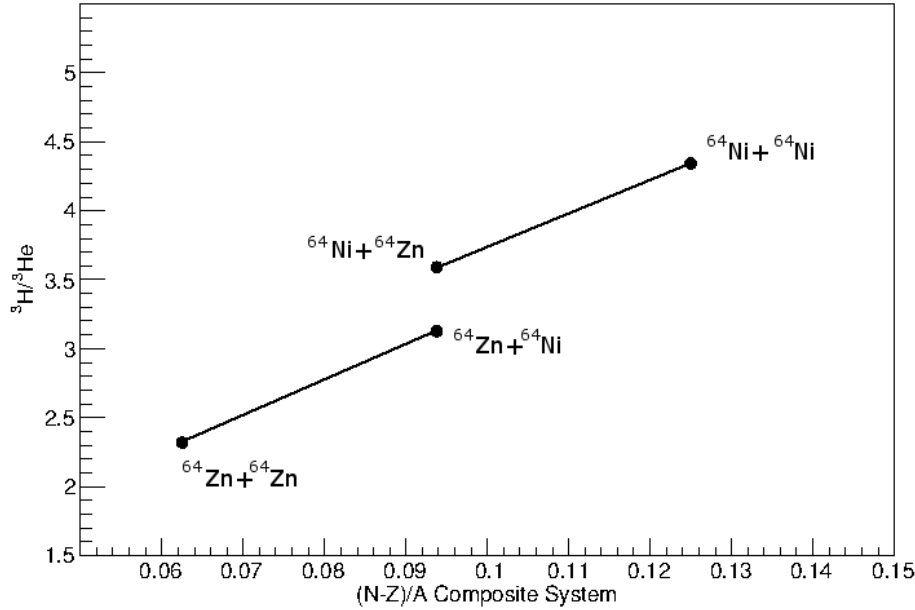


QP m_s

Zn systems show much more equilibration than A=64 systems

QP m_s vs $V_{z,QP}$

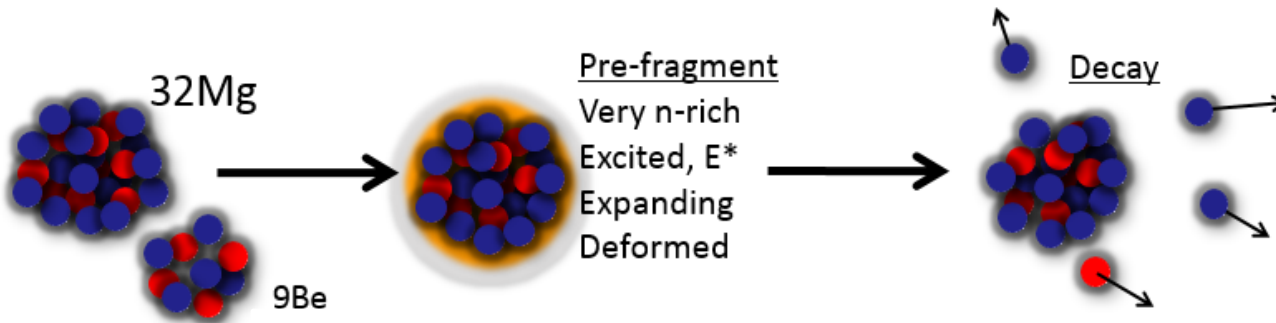




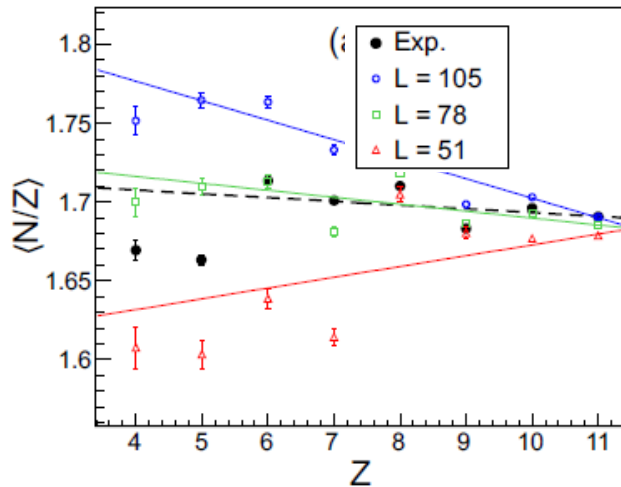
| Equilibration observable | 35 MeV/nucleon ${}^{70,64}\text{Zn}+{}^{70,64}\text{Zn}$ | 35 MeV/nucleon ${}^{64}\text{Zn,Ni}+{}^{64}\text{Zn,Ni}$ | 50 MeV/nucleon ${}^{124,112}\text{Sn}+{}^{124,112}\text{Sn}$ [20] |
|------------------------------------|---|---|--|
| Isoscaling α (Z=4-8) | $77\pm 5\%$ | $83\pm 5\%$ | 54% |
| Isoscaling α (Z=4-14) | $76\pm 7\%$ | $85\pm 7\%$ | - |
| ${}^3\text{H}/{}^3\text{He}$ ratio | $72\pm 4\%$ | $77\pm 4\%$ | - |
| QP m_s | $96\pm 5\%$ | $85\pm 5\%$ | - |

Detect PLF directly

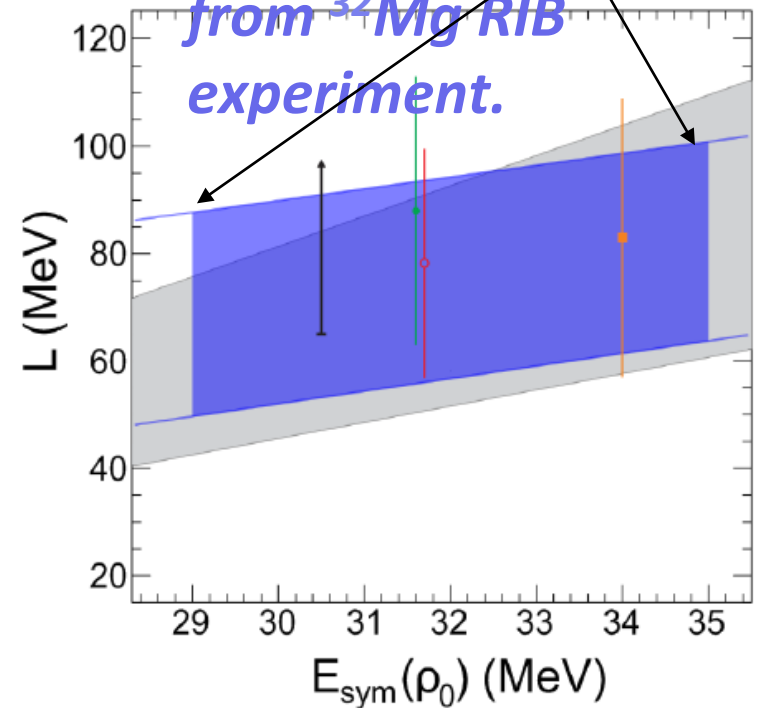
Measure neutrons and N/Z of PLF using MoNA-



Compared to Constrained Molecular Dynamics (CoMD-II) model: *M. Papa et al. PRC 64, 24612, (2001).*

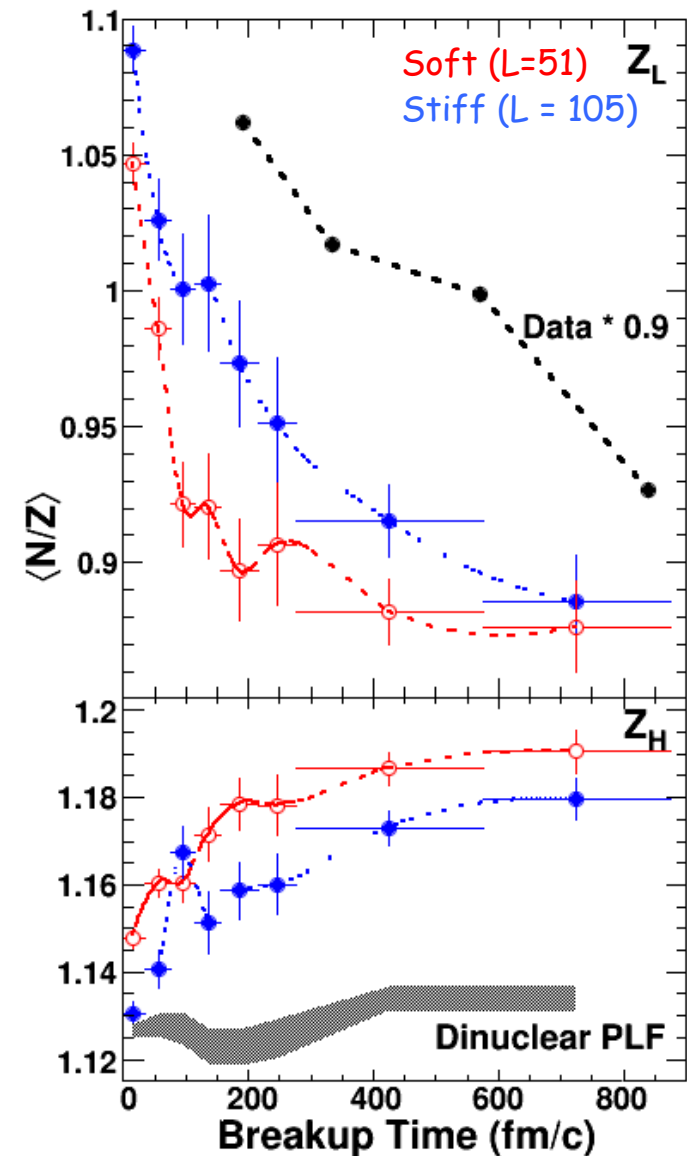
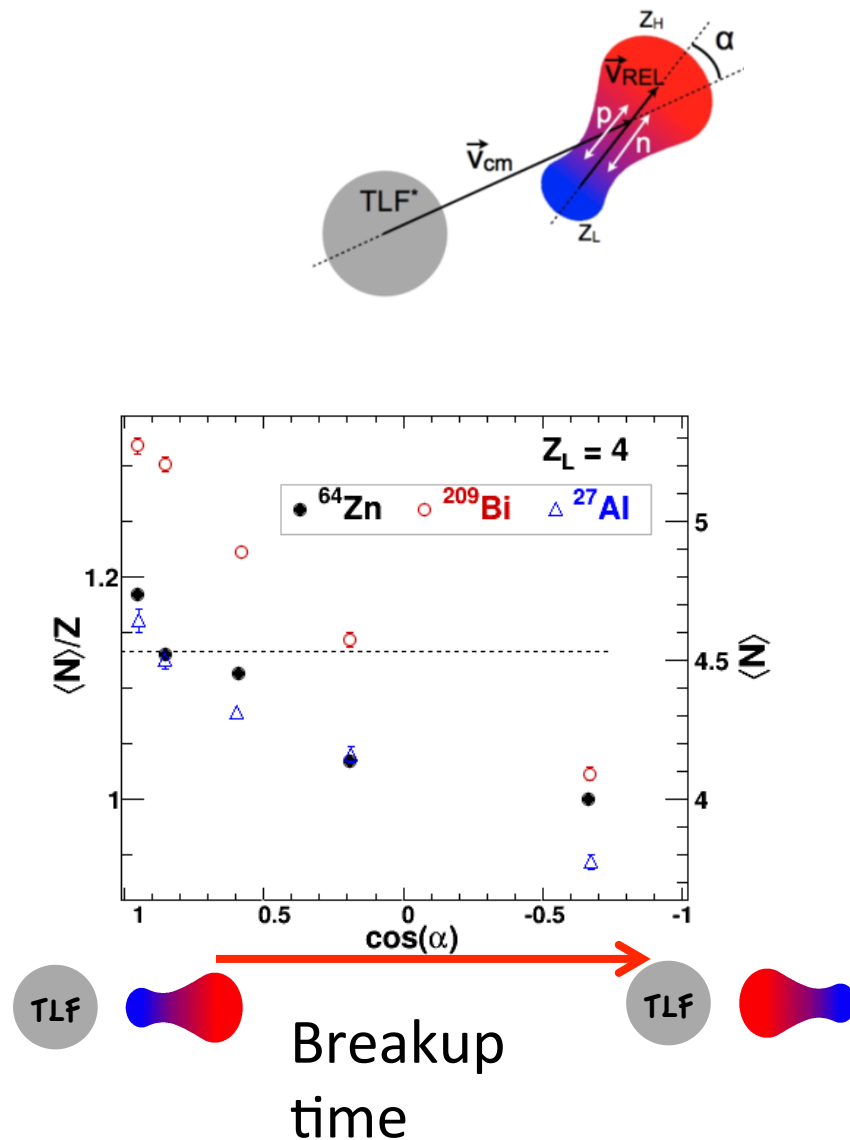


Purple area new constraints extracted from ^{32}Mg RIB experiment.



Kohley et al. PRC 88, 041601(R) (2013).

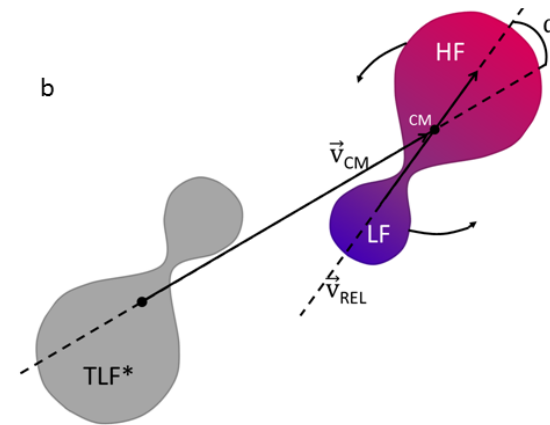
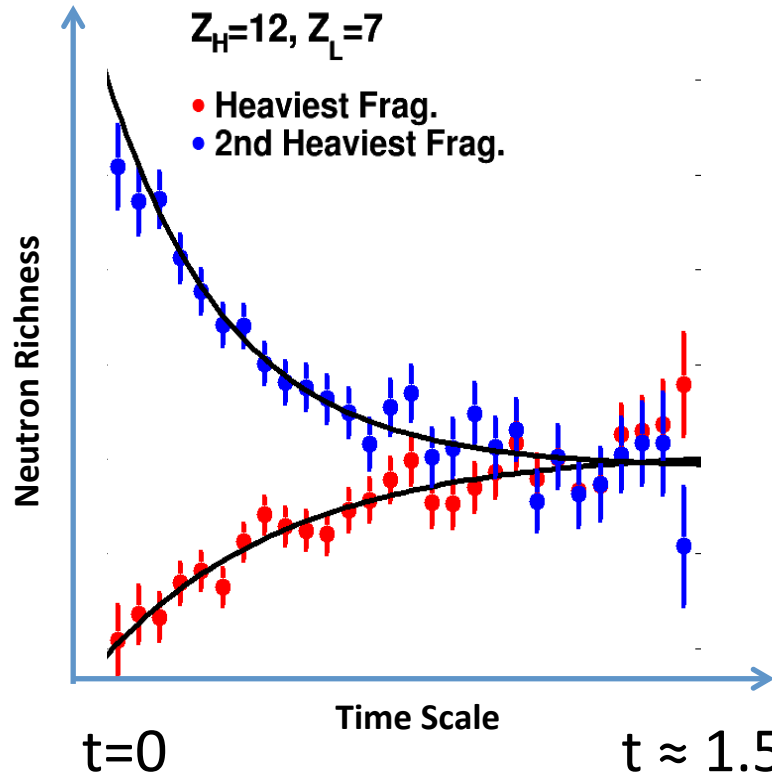
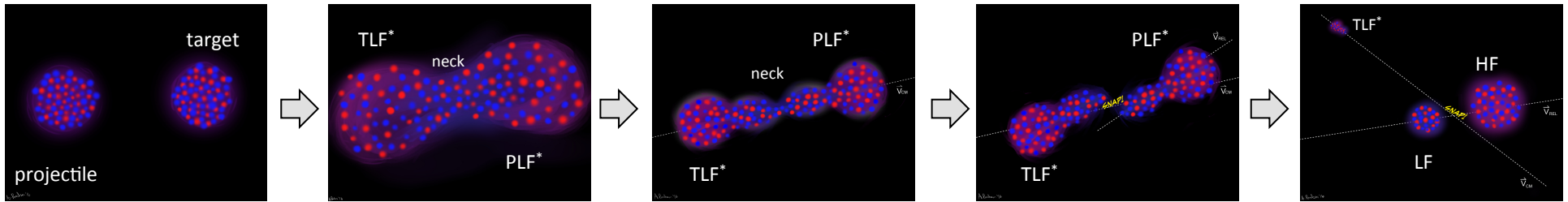
N/Z transport within a deformed nuclear system



K. Brown *et al.*, PRC87, 061601(R) (2013)
 K. Stiefel *et al.*, PRC90, 061605(R) (2014)

Equilibration Chronometry

Characterizing neutron-proton equilibration with sub-zeptosecond resolution

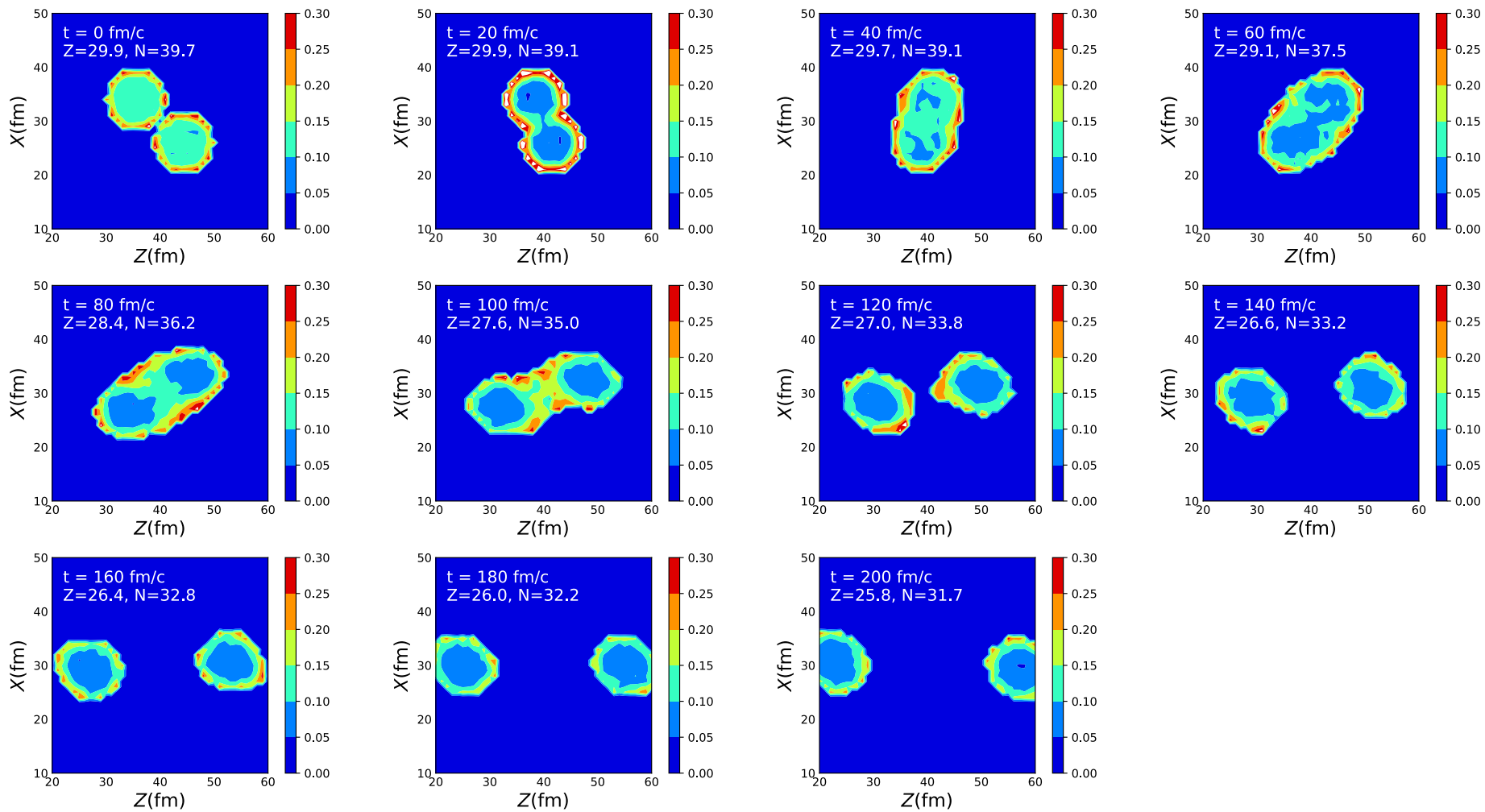


We observe N-Z equilibration as a function of time.

Equilibration curve is approximately exponential

→ First order kinetics

Zeptosecond timescale.



Private communication, Zhang & Ko



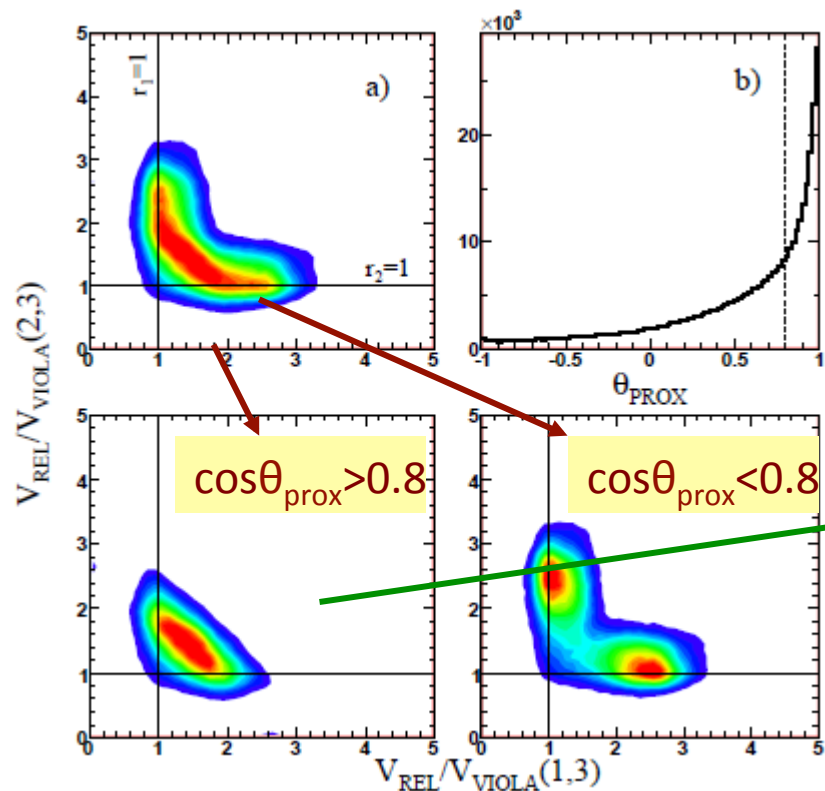
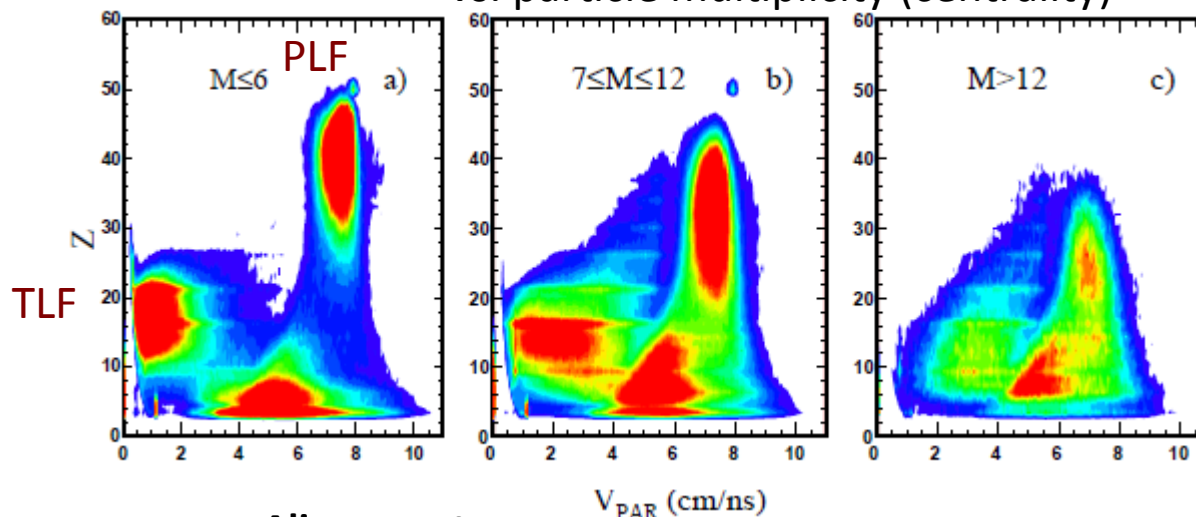
CYCLOTRON INSTITUTE
TEXAS A & M UNIVERSITY

$^{124}\text{Sn} + ^{64}\text{Ni}$ 35 AMeV:
CHIMERA data

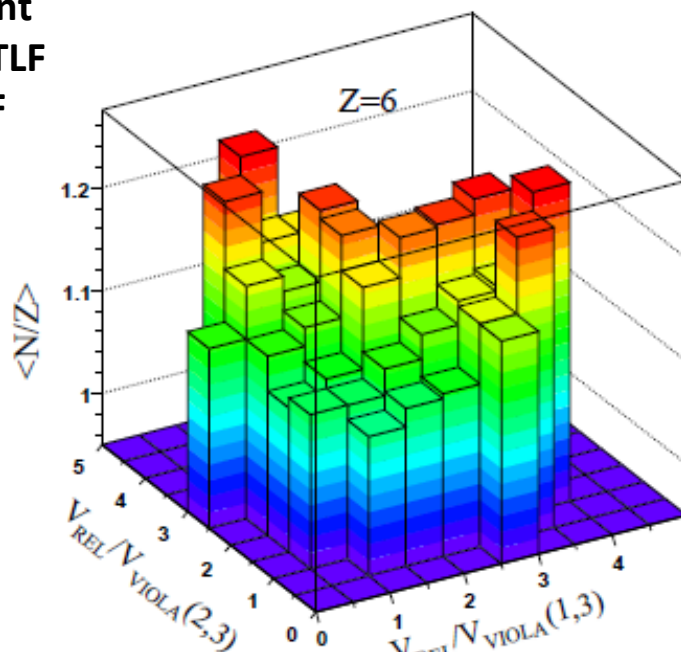
Semicentral (M=7)
v// selection of the 3
highest Z fragments:

- 1: PLF
- 2: TLF
- 3: Neck source

vs. particle multiplicity (centrality)



Alignment
IMF-PLF/TLF
vs PLF-TLF



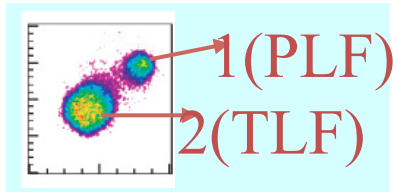
Neutron enrichment for the largest Viola deviations
and the highest degree of alignment :



Comparison with data: Isospin equilibration ?

GANIL Experiment: Ni + Au @ 52 MeV/A

Simulations: SMF + decay



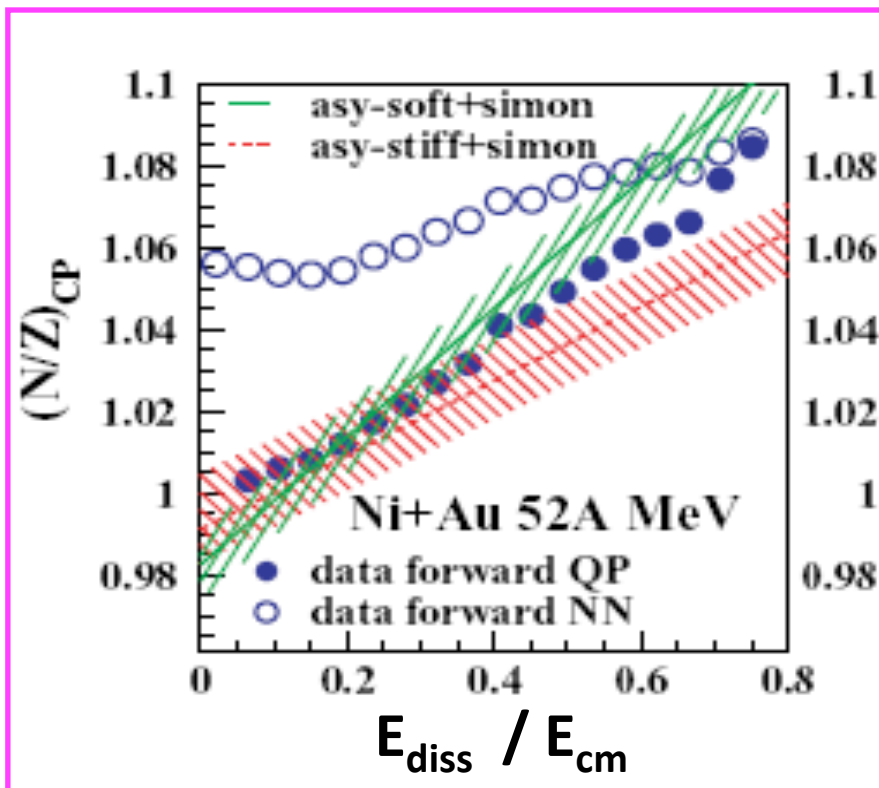
Isospin observables:

$(N/Z)_{CP} = N/Z$ of light charge particles

as a function of

Dissipated energy:
(contact time)

$$E_{diss} = E_{cm} - \frac{E_{kin} + E_{pot}^{Coul}}{A_{PLF} + A_{TLF}}$$



Data:

- forward PLF
- forward n-n c.m.
(include emission from neck region)

Galichet et al., PRC (2010)



CYCLOTRON INSTITUTE
TEXAS A & M UNIVERSITY

Isotopic Ratios For Light Fragments

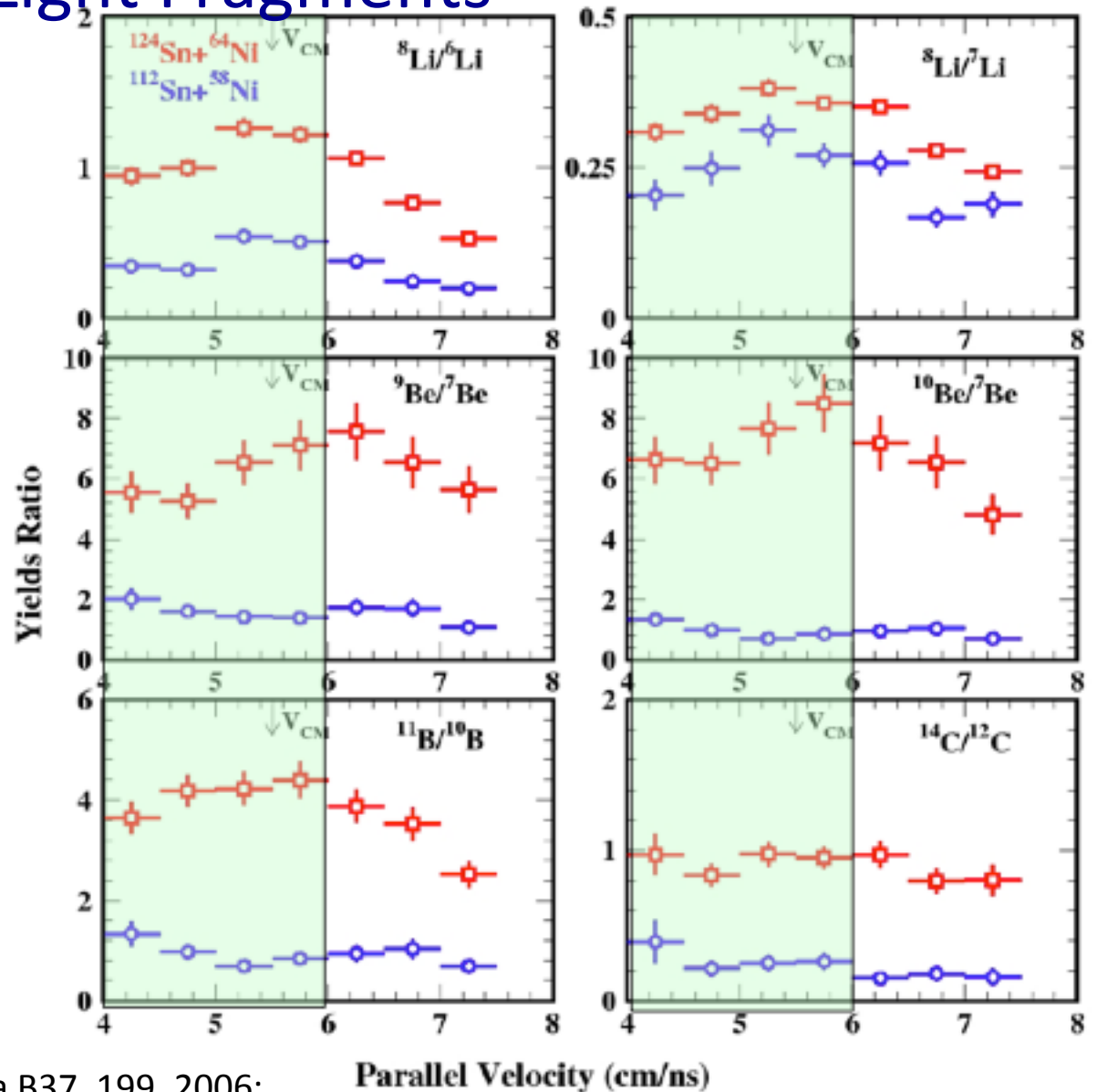
(Z=3-6) IN THE 35/A.MeV

NEUTRON RICH $^{124}\text{Sn}+^{64}\text{Ni}$ AND

NEUTRON POOR $^{112}\text{Sn} + ^{58}\text{Ni}$

REACTIONS

Enhancement
In n-rich fragments
for mid velocity



E. De Filippo et al., Acta Physica Polonica B37, 199, 2006;

P. Russotto, Procs of IWM 05, pp. 13, ed. SIF, 2006.



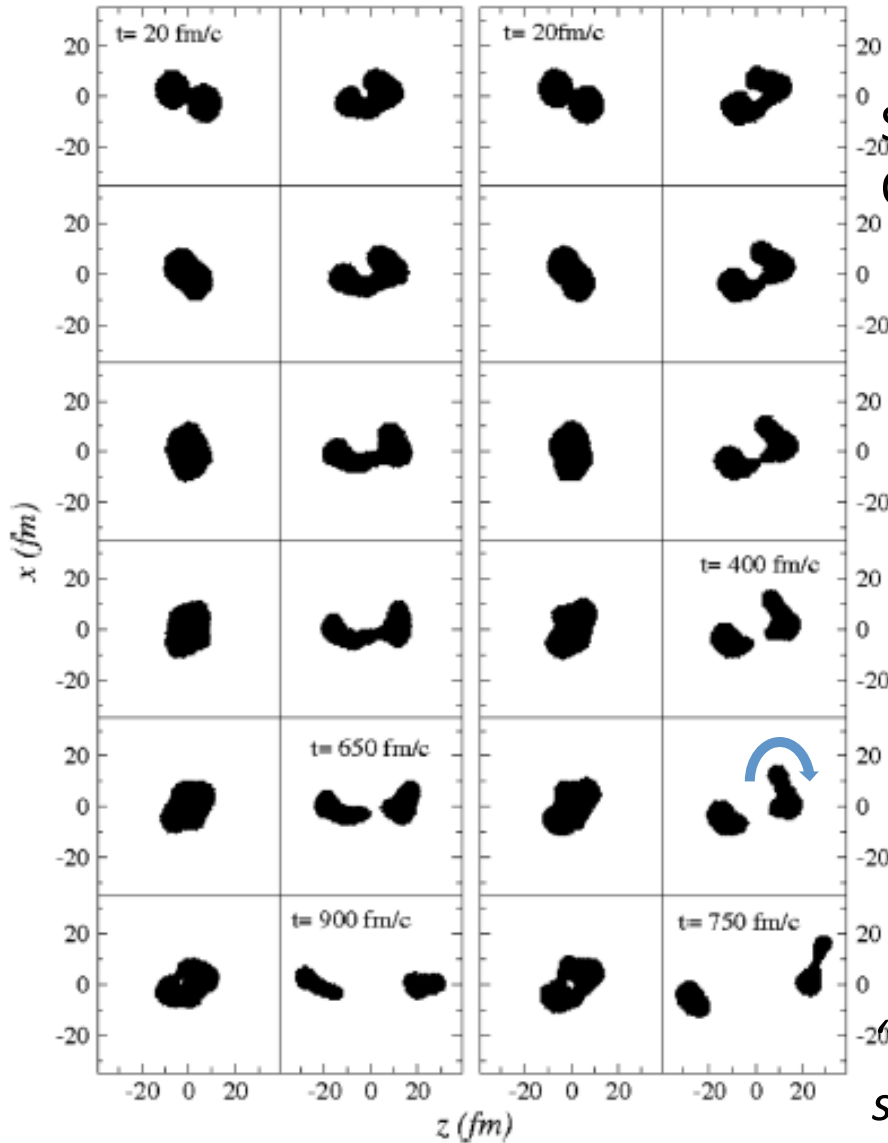
CYCLOTRON INSTITUTE
TEXAS A & M UNIVERSITY

PLF-TLF shape properties

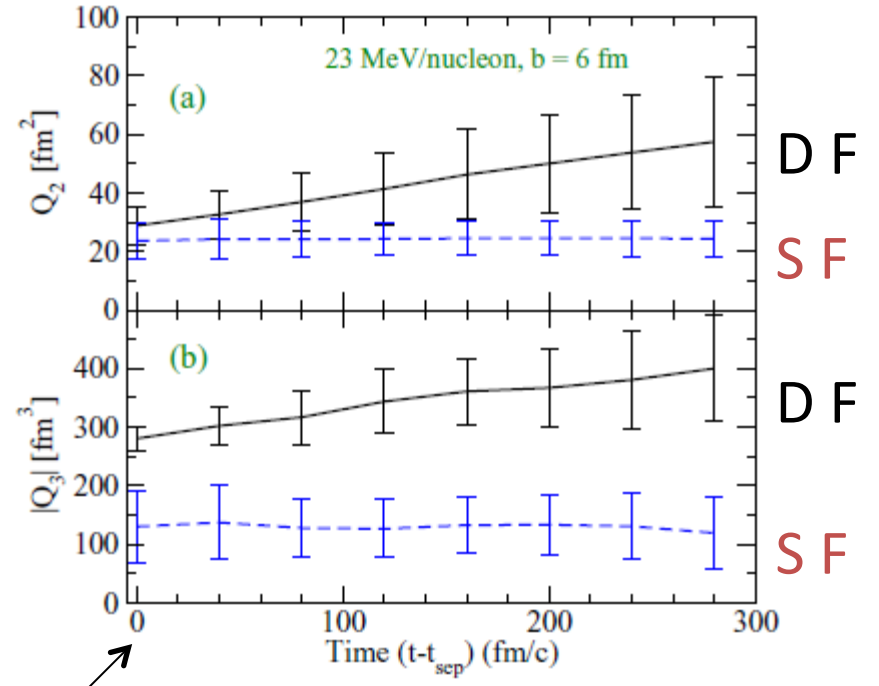
SMF
Skyrme forces

$^{197}\text{Au} + ^{197}\text{Au}$ 23 MeV/nucleon
b = 5 fm b = 6 fm

$^{197}\text{Au} + ^{197}\text{Au}$ collisions - 23 MeV/A



Shape Observables:
Quadrupole and Octupole moments



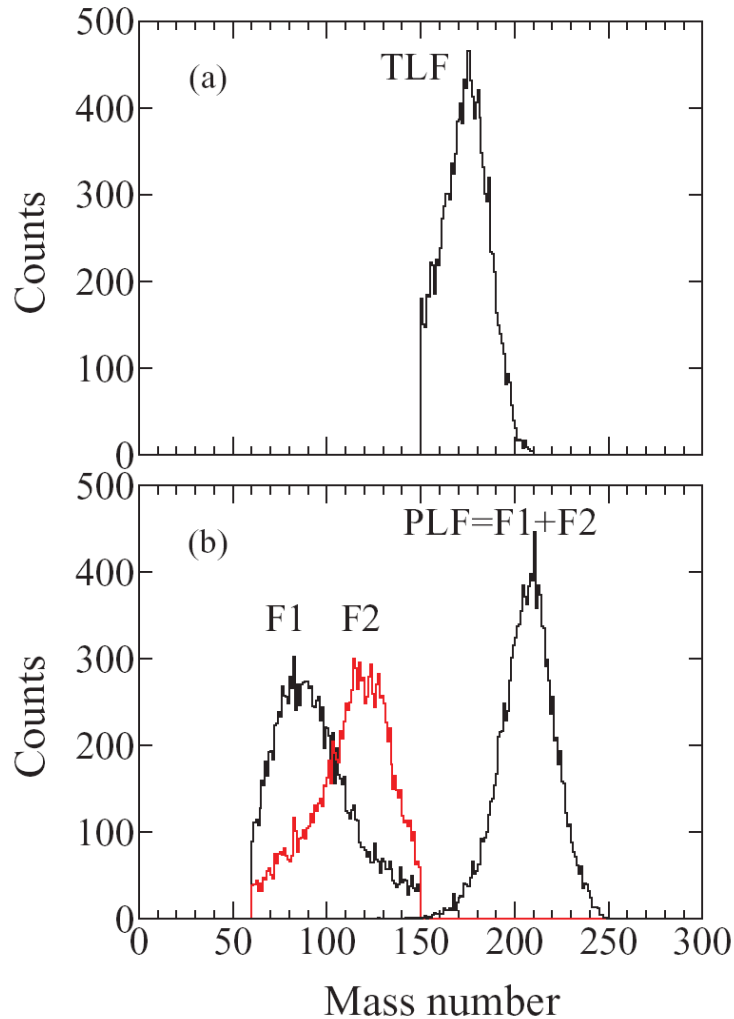
“PLF-TLF
separation time”

D F: deformed fragment

S F: “spherical” fragment

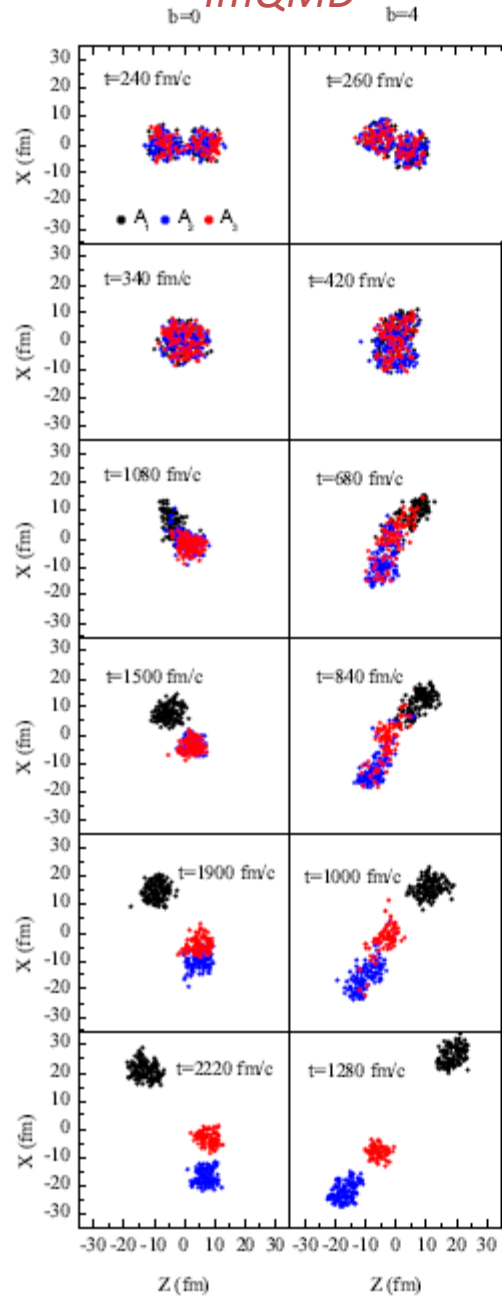
Ternary break-up

$^{197}\text{Au} + ^{197}\text{Au}$ collisions - 15 MeV/A
(Chimera@LNS data) *PRC 81, 024605 (2010)*



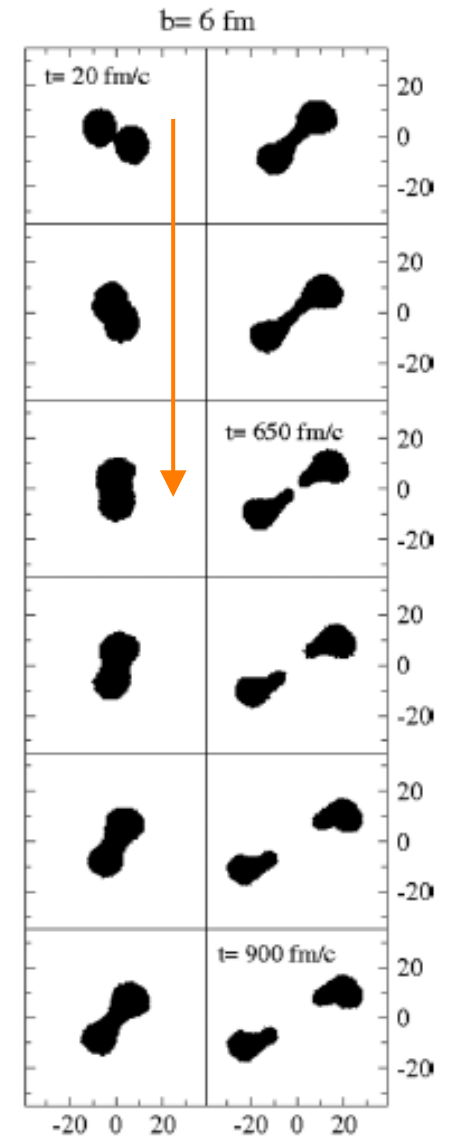
Y.Li et al., *NPA 902 (2013)*

ImQMD

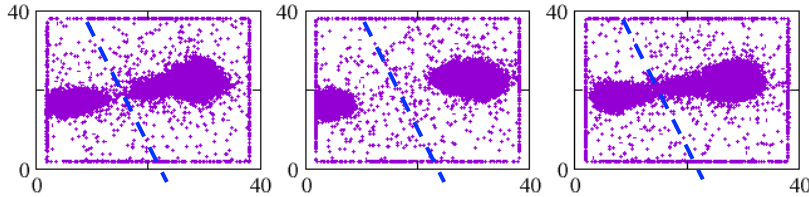


C.Rizzo et al., *PRC (2014)*

SMF



Ternary breakup in n-rich systems: Sensitivity to E_{sym}



$^{132}\text{Sn} + ^{64}\text{Ni}$, $E/A = 10$ MeV, $b = 7$ fm
 3 events, $t = 500$ fm/c

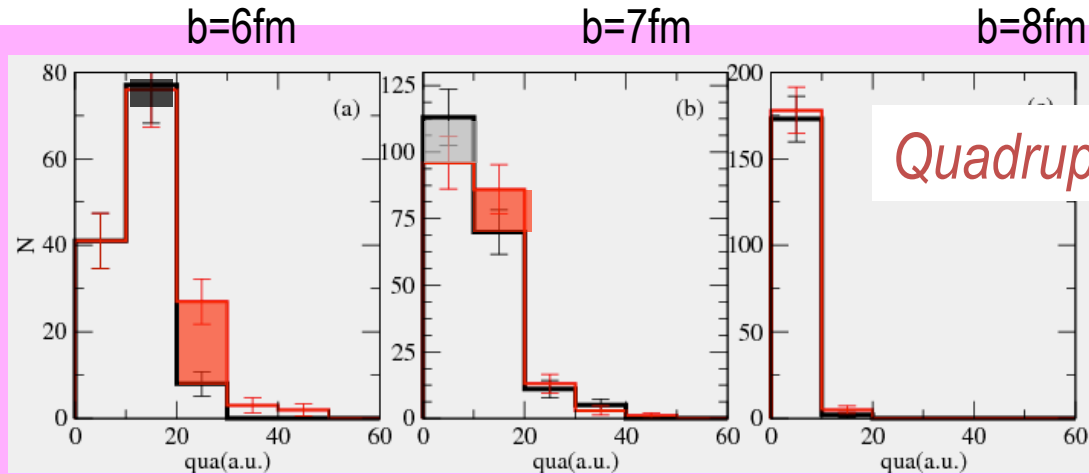
- Analysis of the deformation of the residues

200 runs each
 per impact parameter

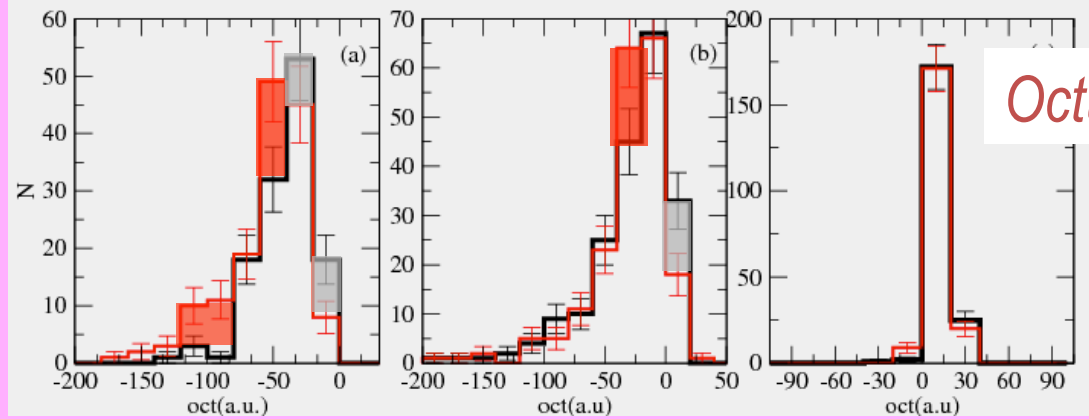
— *Asysoft*
 — *Asystiff*

- Larger residue deformations
 → more ternary events
 with *Asystiff*

Di Toro et al., NPA 787 (2007) 585c



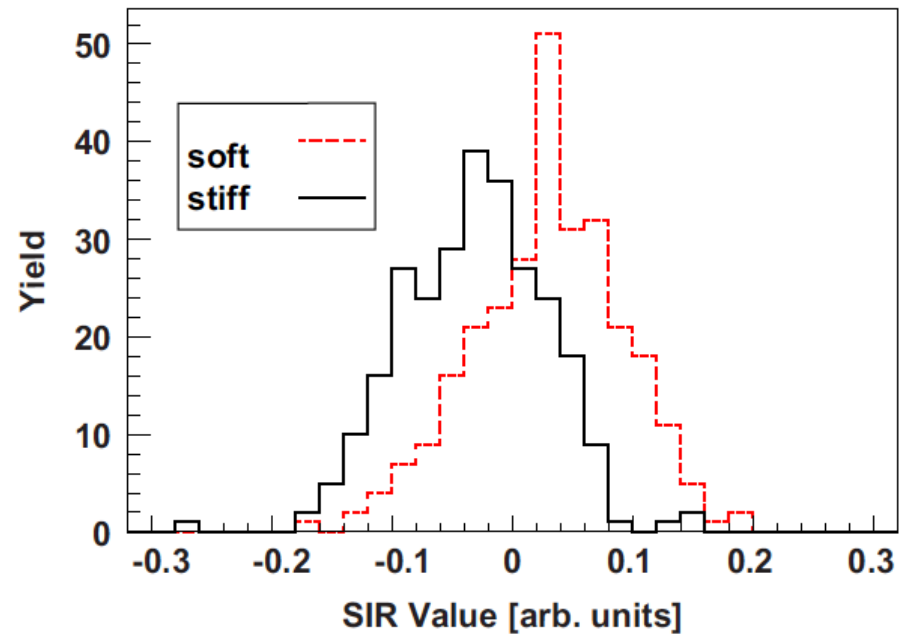
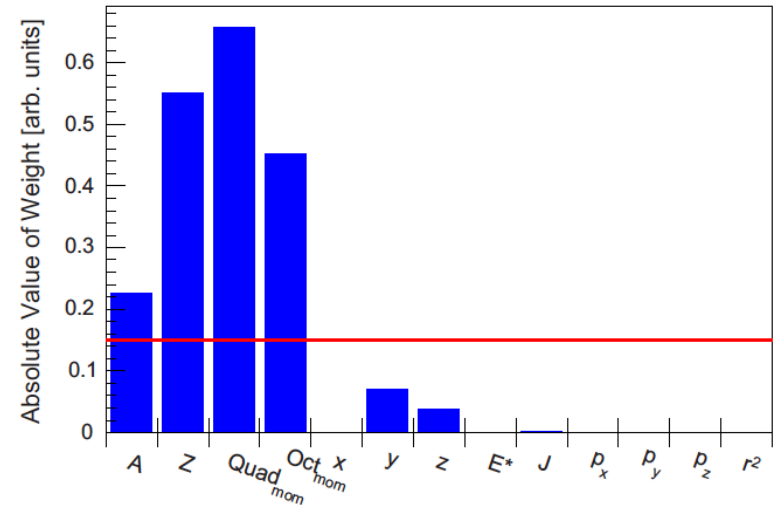
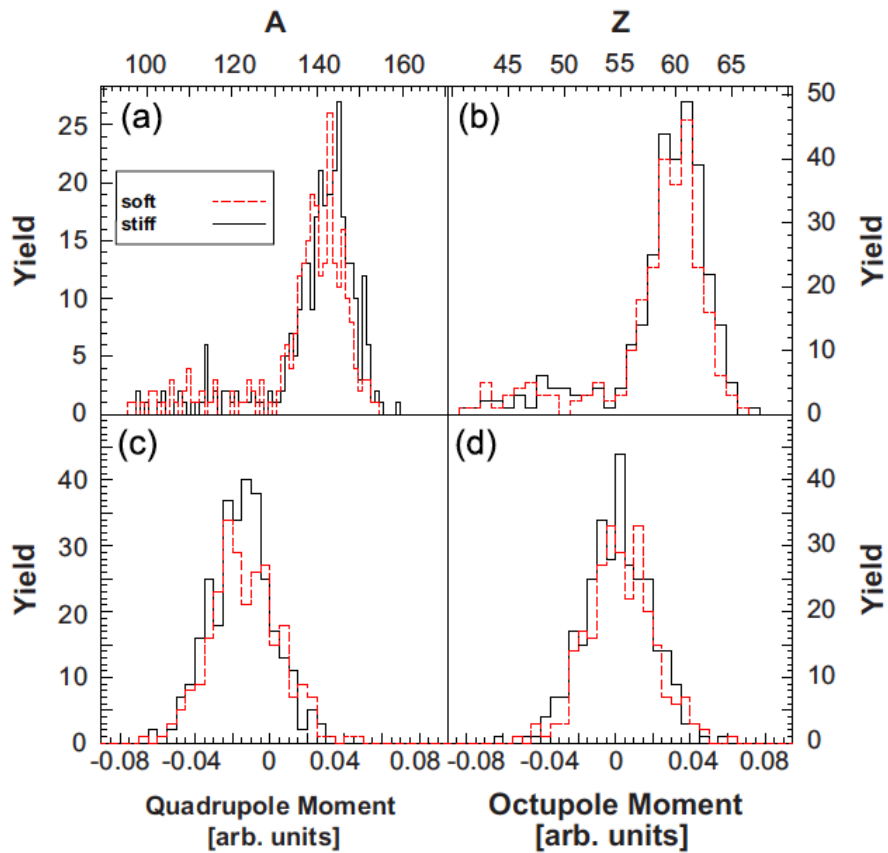
Quadrupole



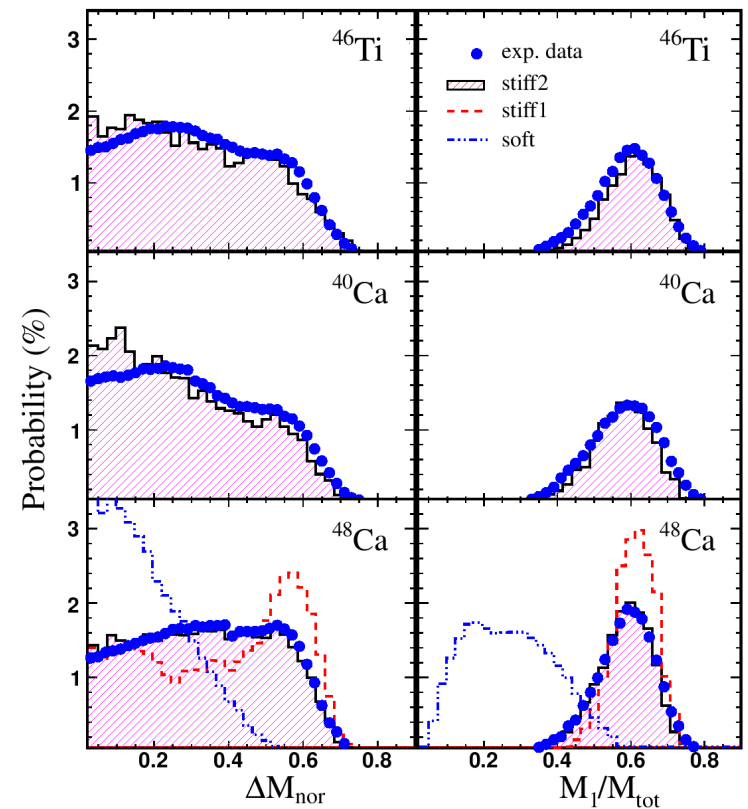
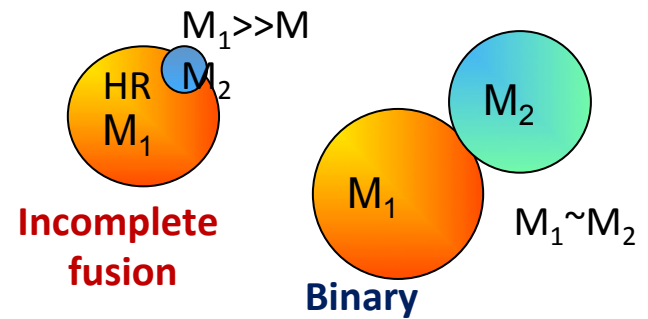
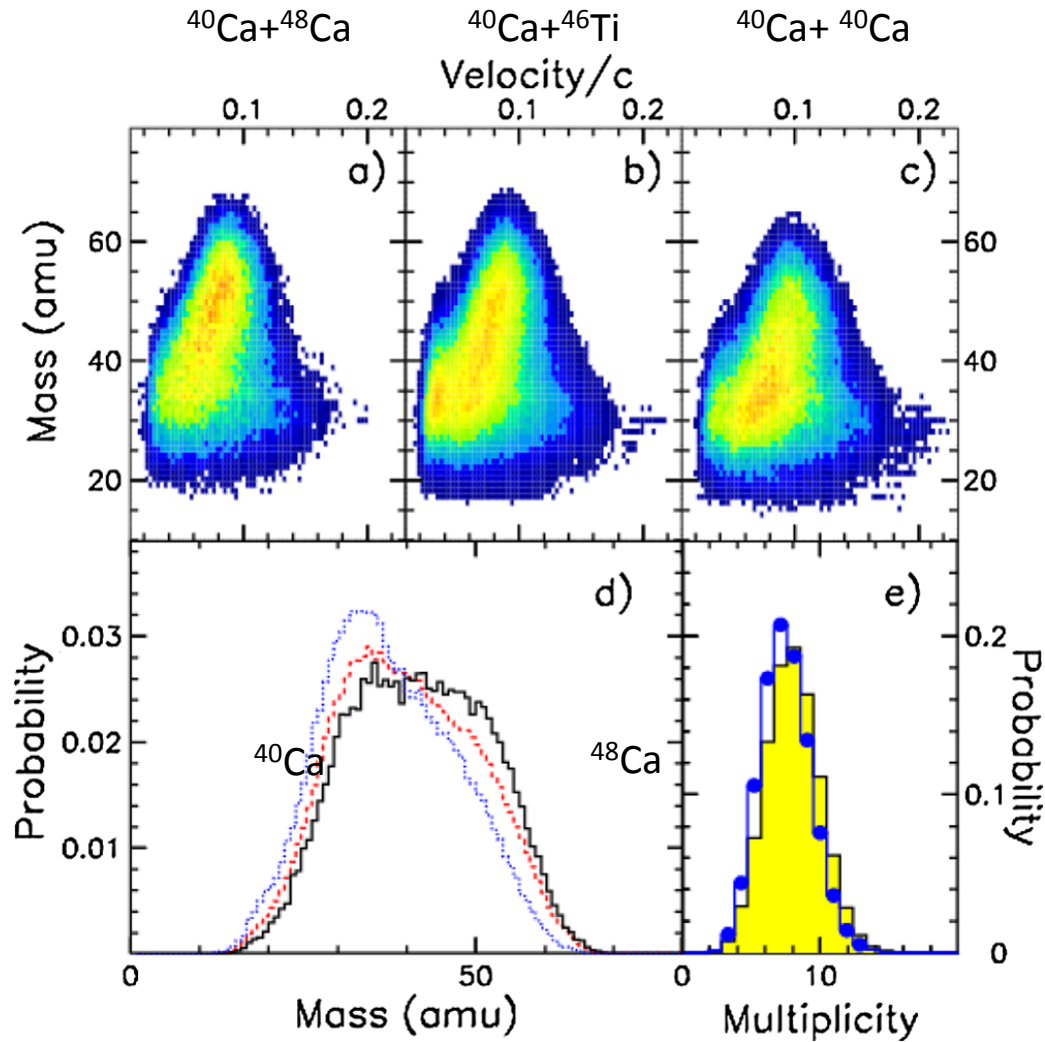
Octupole



sifting through the remnants



Isospin Dependence of Incomplete Fusion Reactions at 25 MeV/Nucleon

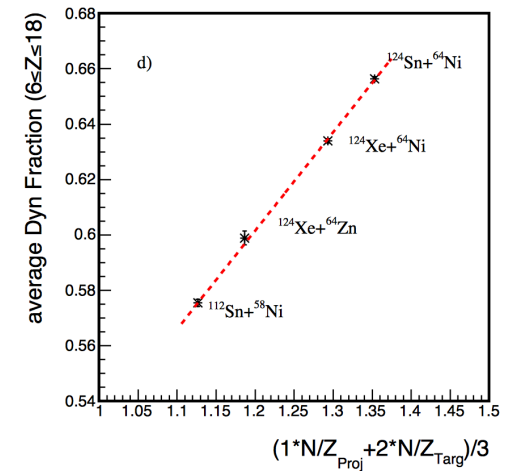
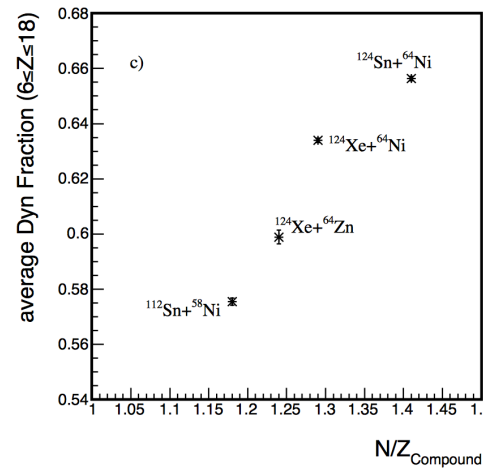
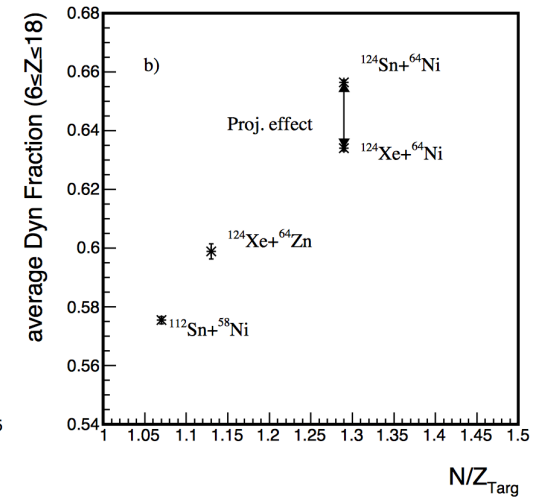
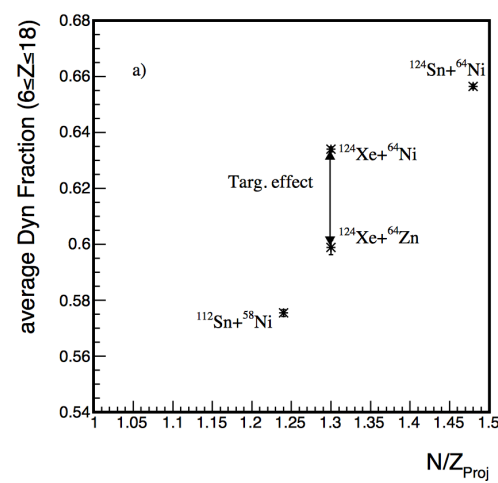
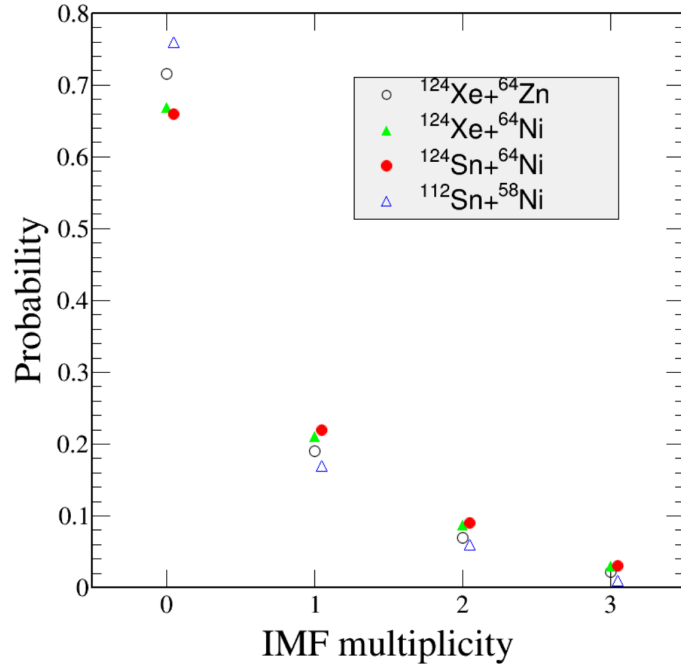


Higher probability for fusion using neutron rich systems

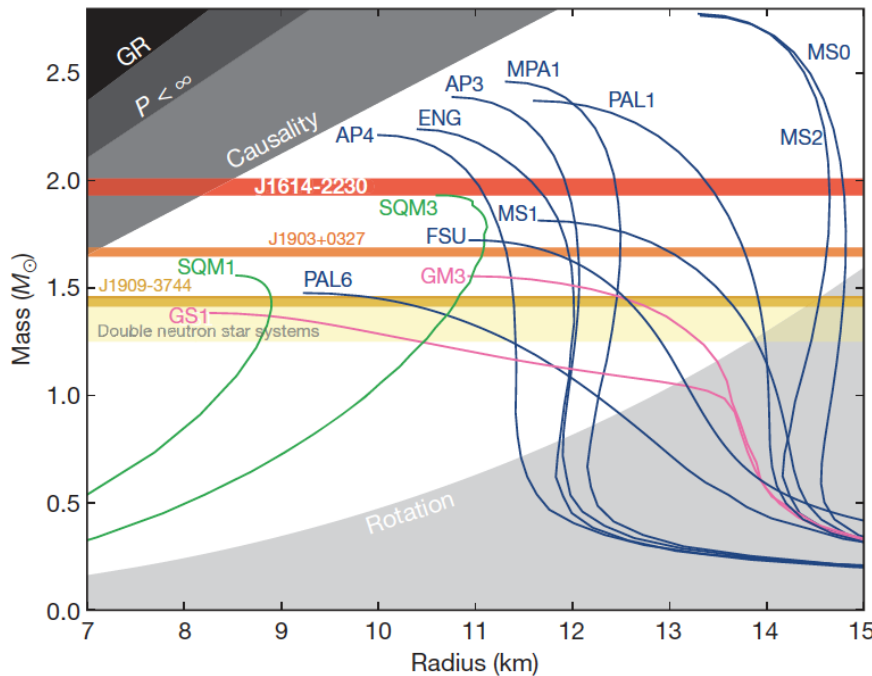
F. Amorini, G. Verde, PRL 102, 112701 (2009)
G. Cardella et al., PRC 85 084609 (2012)

Isospin influence on dynamical production of Intermediate Mass Fragments at Fermi Energies

$^{124}\text{Xe} + ^{64}\text{Ni}$ and ^{64}Zn
35 Mev/nuc

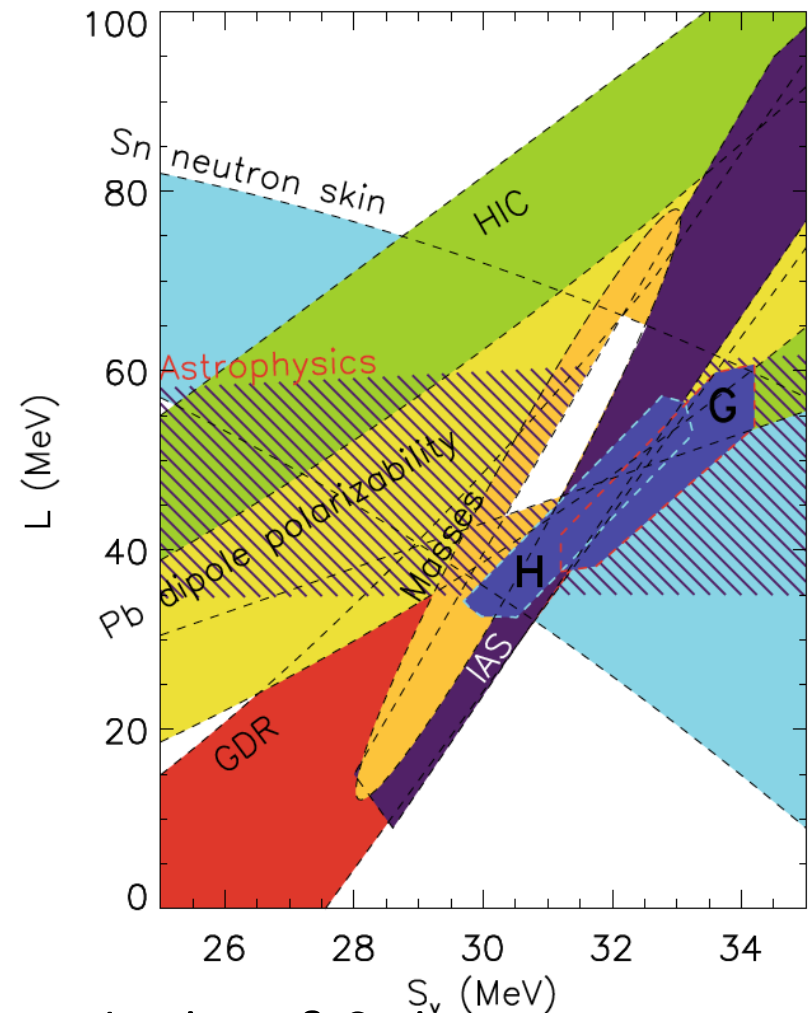


- » Many proposed observables
- » Various data sets
- » Need to understand differences in model predictions
- » New observables with increased power to discriminate welcome



Demorest, Nature 2010

EOS comparison



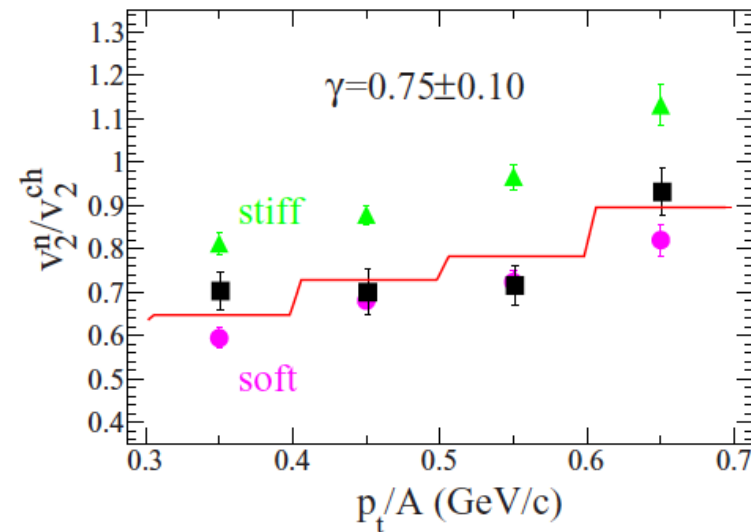
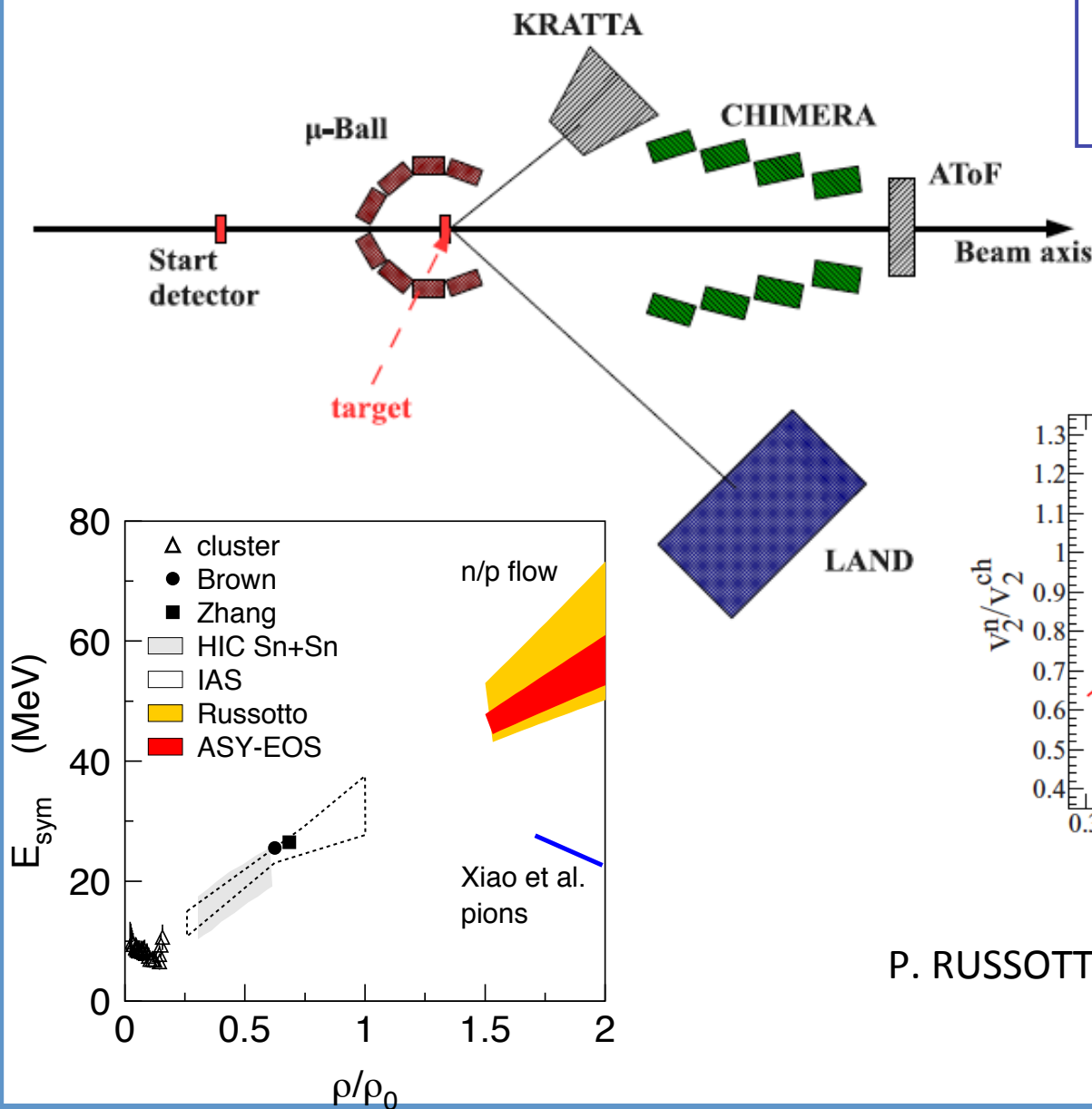
Lattimer & Steiner
Eur. Phys. J. A (2014)c



CYCLOTRON INSTITUTE
TEXAS A&M UNIVERSITY

Constraining the Symmetry Energy at Supra-Saturation Densities with Measurements of Neutron and Proton Elliptic Flows

$^{197}\text{Au} + ^{197}\text{Au}$ @ 400 A MeV
 $^{96}\text{Ru} + ^{96}\text{Ru}$ @ 400 A MeV
 $^{96}\text{Zr} + ^{96}\text{Zr}$ @ 400 A MeV

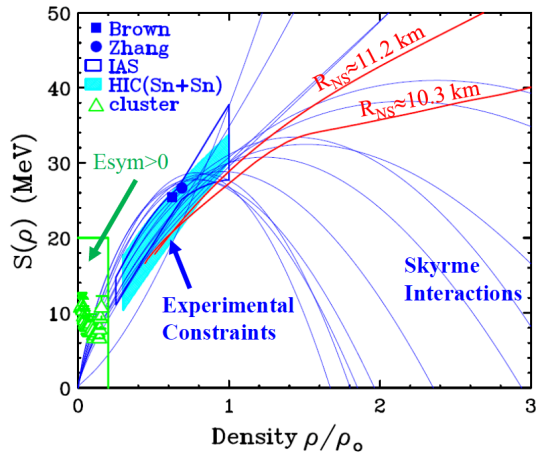


P. RUSSOTTO et al. PRC 94, 034608 (2016)



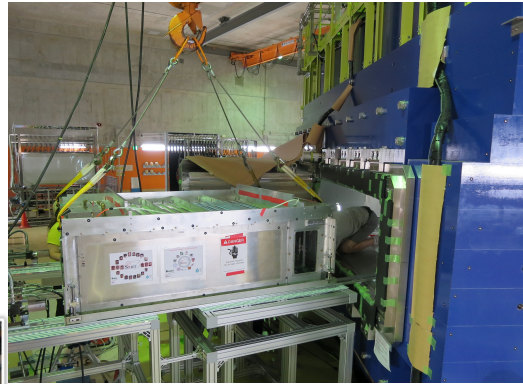
CYCLOTRON INSTITUTE
TEXAS A & M UNIVERSITY

SPIRIT TPC @ SAMURAI

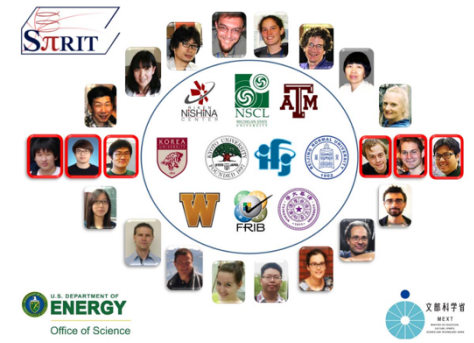
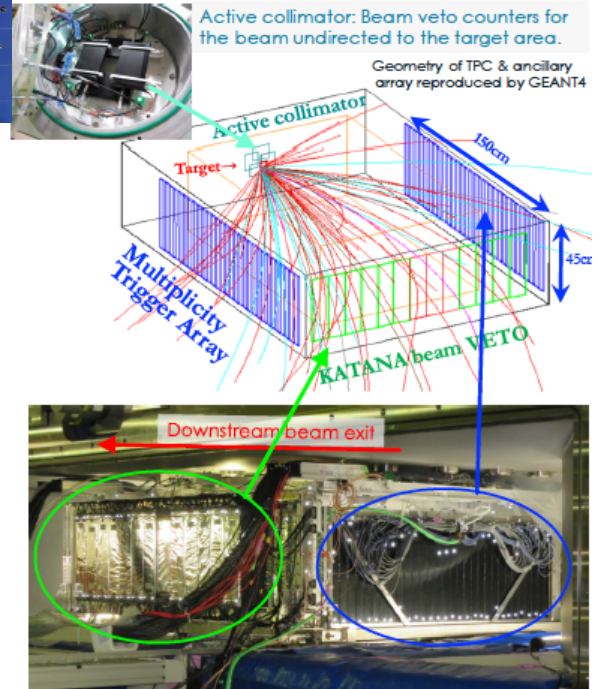
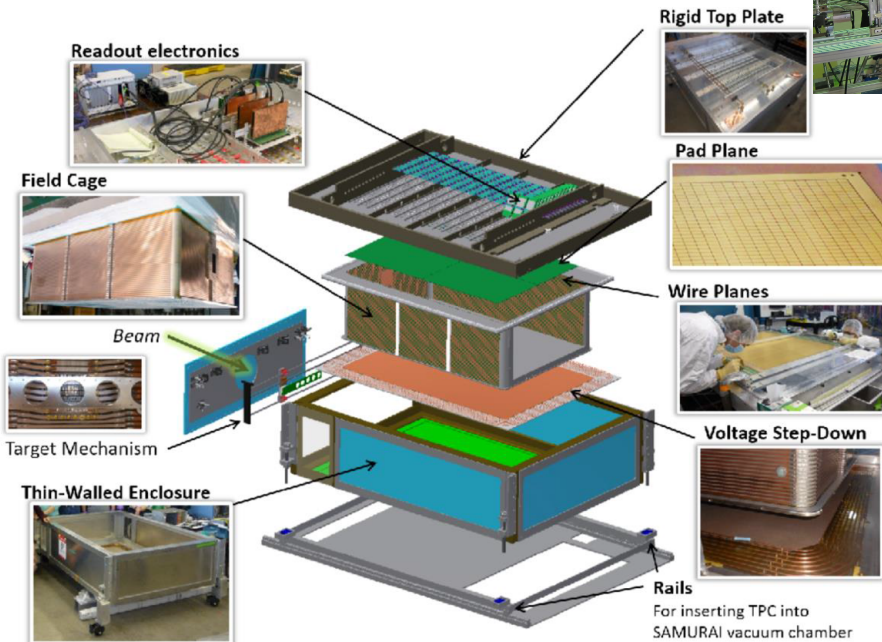


Constrain the Asymmetry Energy at **high density** through measurement of

- π^-/π^+ , n/p , $3H/3He$
- Differential Flow and Particle Yield Ratios
- $^{108}\text{Sn}+^{112}\text{Sn}$, $^{130}\text{Sn}+^{124}\text{Sn}$ @ $E/A \geq 200$ MeV



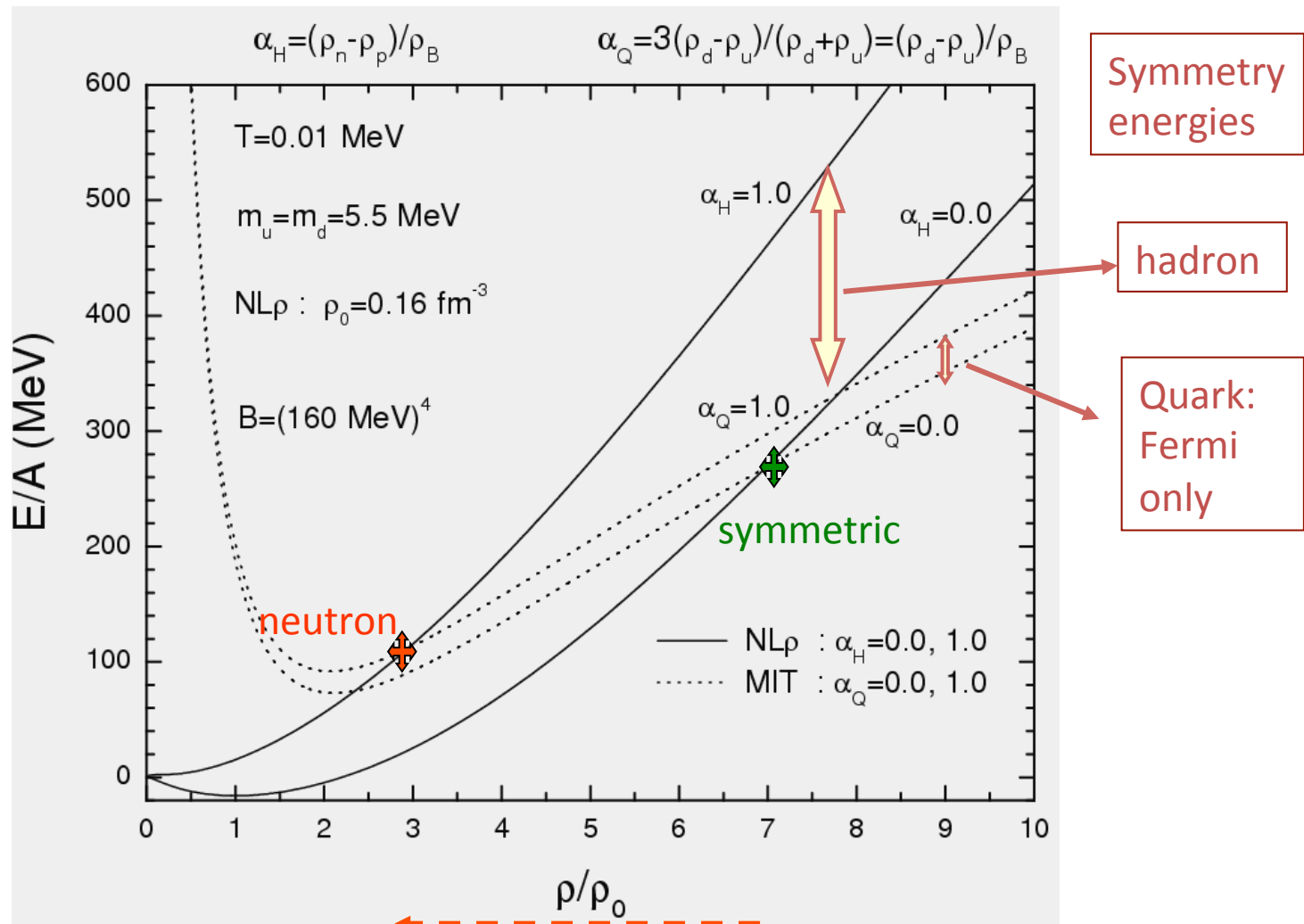
ed



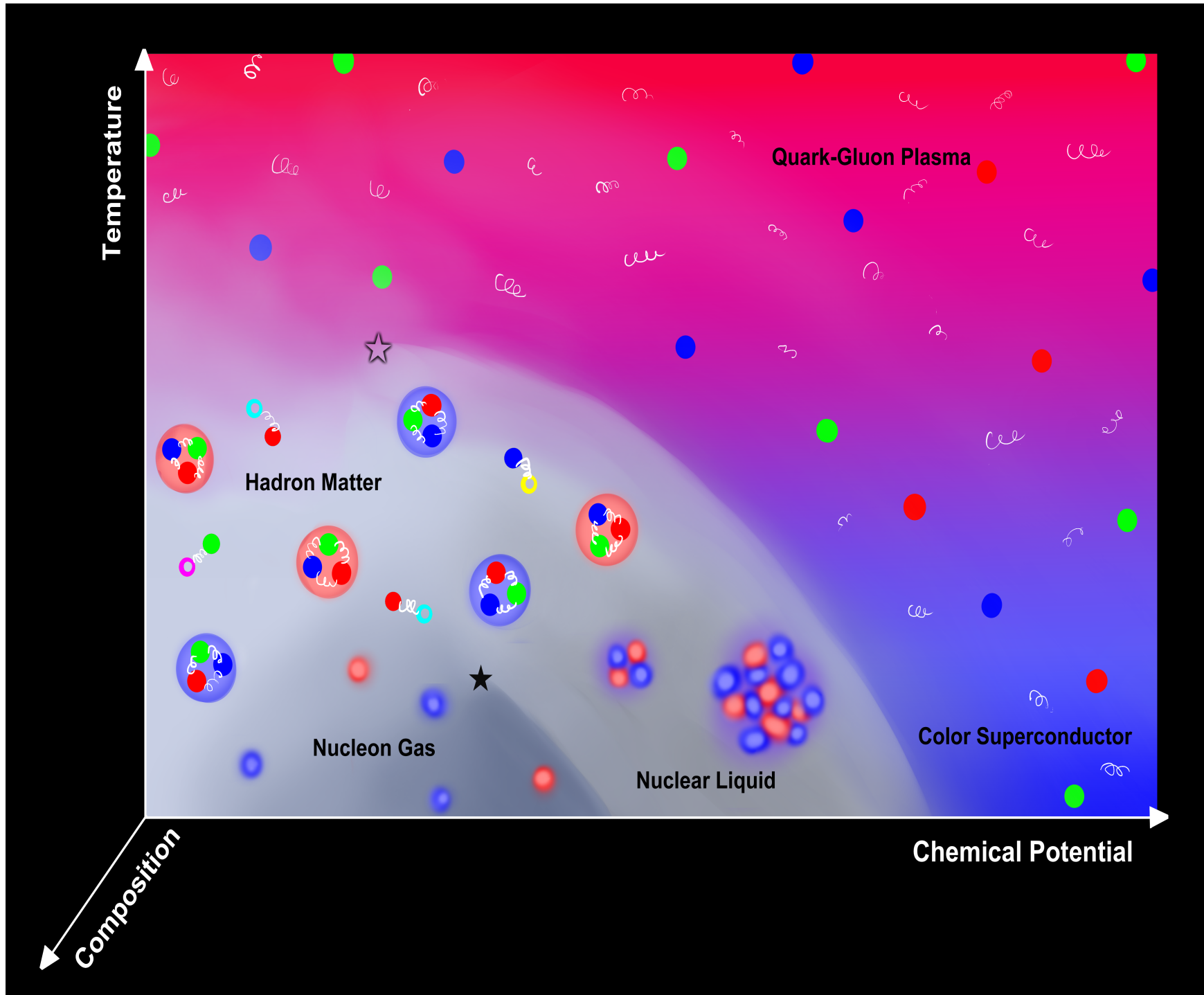
FA

Symmetry energy at high density and the transition to quark matter

MIT-Bag
Energy density:
 $\epsilon(\text{free gas}) + B$



For very isospin asymmetric matter we can expect a much earlier transition to the quark phase



Many Thanks

All the members of SJYGroup
The operations staff at the
Texas A&M Cyclotron Institute
DOE, Welch Foundation &
State of Texas



CYCLOTRON INSTITUTE
TEXAS A & M UNIVERSITY