

Clustering in Dilute Matter with Medium Effects

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TECHNISCHE
UNIVERSITÄT
DARMSTADT

International Workshop on Multi facets of EoS and Clustering

Dipartimento di Fisica e Astronomia
& Laboratori Nazionali del Sud
Catania, Italy
May 22 – 25, 2018

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IN SCIENCE AND TECHNOLOGY





- ▶ **Introduction**
- ▶ **Theoretical Model**
 - ▶ Generalized Relativistic Density Functional for Nuclei and Compact Star Matter
- ▶ **Systematics of Cluster Formation and Dissolution**
 - ▶ Predictions for Compact Star Matter
 - ▶ Experimental Tests
 - ▶ Dependence on Symmetry Energy
- ▶ **Problems**
- ▶ **Conclusions**



Introduction

development of a unified phenomenological description of

▶ atomic nuclei

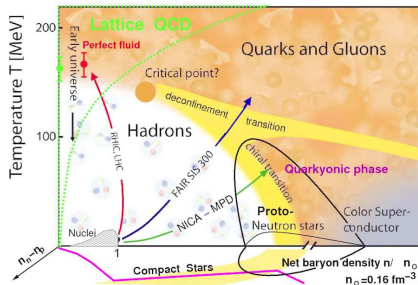
- ▶ light to (super-) heavy, stable and exotic

▶ nuclear matter

- ▶ all relevant degrees of freedom
- ▶ with phase transitions

▶ compact star matter

- ▶ for all densities, temperatures, and isospin asymmetries
- ▶ with inhomogeneities, clustering
- ▶ for neutron stars, their mergers and core-collapse supernovae

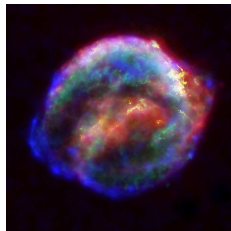


essential ingredient in astrophysical model calculations

- ▶ static properties of **neutron stars**
- ▶ dynamical evolution of **core-collapse supernovae, neutron star mergers**
- ▶ conditions for **nucleosynthesis**
- ▶ energetics, **chemical composition**, transport properties



X-ray: NASA/CXC/J.Hester (ASU)
Optical: NASA/ESA/J.Hester & A.Loll (ASU)



NASA/ESA/R.Sankrit & W.Blair (Johns Hopkins Univ.)

Equation of State (EoS) and Astrophysics I

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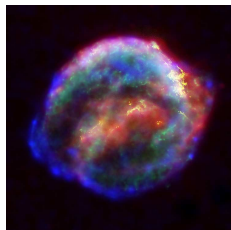
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timescale of reactions \ll timescale of system evolution

- ▶ **equilibrium** (thermal, chemical, ...)
- ▶ application of **EoS** reasonable



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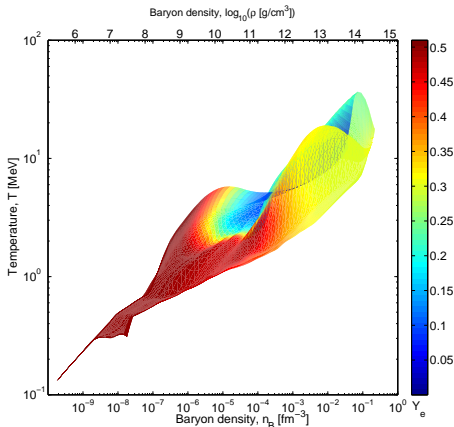
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Equation of State (EoS) and Astrophysics II

wide range of thermodynamic variables

- ▶ **temperature** T
- ▶ **baryon density** n_b
- ▶ **hadronic charge fraction** Y_q or isospin asymmetry $\beta = 1 - 2Y_q$

simulation of core-collapse supernova



T. Fischer, Uniwersytet Wroclawski

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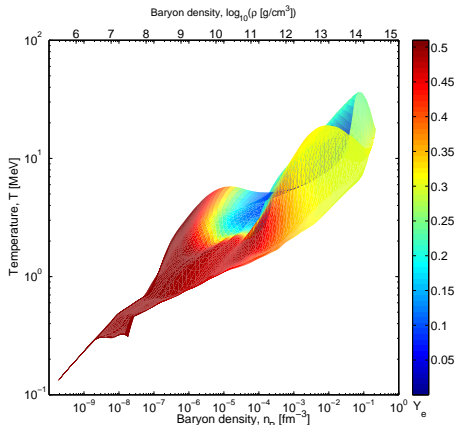
modeling of nuclear matter
and stellar matter

- ▶ different systems and conditions

⇒ **global, multi-purpose EoS** required

EoS review: M. Oertel et al.,
Rev. Mod. Phys. 89 (2017) 015007

simulation of core-collapse supernova



T. Fischer, Uniwersytet Wroclawski

▶ hadronic 'ab-initio' methods with realistic interactions

- ▶ interactions: potential models, meson-exchange, chiral forces, RG evolved (Argonne, Urbana, Tucson-Melbourne, Nijmegen, Paris, Bonn, ...)
⇒ two-body NN interaction (in vacuum) well constrained by experiment, three-body forces less, large uncertainties for YN, YY, etc.
- ▶ many-body methods: BHF/DBHF, SCGF, CBF, VMC, GFMC, AFDMC, ...

▶ QCD-based/inspired descriptions

- ▶ Lattice QCD, pQCD, DS, (P)NJL, bag models, ...

▶ effective field theories (EFT)

- ▶ chiral EFT, nuclear lattice EFT, ...

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- ▶ methods not always applicable (methodological/technical limitations)
- ▶ many EoS for neutron matter & neutron star matter, but no global EoS for astrophysical applications available from these approaches
⇒ only **phenomenological models** for global EoS at present



- ▶ **constituents:** mostly considered are nucleons, nuclei (light/heavy/representative), leptons, photons, ...)
- ▶ **models:** often combination of different approaches (Skyrme/Gogny/relativistic mean-field models, NSE, virial EoS, density functionals, classical/quantum molecular dynamics, ...)



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- ▶ **global EoSs used in astrophysical simulations:**
 - ▶ H&W: W. Hillebrandt, K. Nomoto, R.G. Wolff, A&A 133 (1984) 175
 - ▶ LS180/220/375: J.M. Lattimer, F.D. Swesty, NPA 535 (1991) 331
 - ▶ STOS (TM1): H. Shen, H. Toki, K. Oyamatsu, K. Sumiyoshi, NPA 637 (1998) 435, PTP 100 (1998) 1013
 - ▶ HS (TM1,TMA,FSUgold,NL3,DD2,IUFSU): M. Hempel, J. Schaffner-Bielich, NPA 837 (2010) 210
 - ▶ SHT (NL3): G. Shen, C.J. Horowitz, S. Teige, PRC 82 (2010) 015806, 045802, PRC 83 (2011) 035802
 - ▶ SHO (FSU1.7, FSU2.1): G. Shen, C.J. Horowitz, E. O'Connor, PRC 83 (2011) 065808
 - ▶ SFHo/SFHx: A.W. Steiner, M. Hempel, T. Fischer, ApJ 774 (2013) 17
 - ▶ recently many more, also with additional degrees of freedom (hyperons, quarks)



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- ▶ **challenge:**
covering of full range of thermodynamic variables in a unified model
⇒ here: generalized relativistic density functional



Generalized Relativistic Density Functional for Nuclei and Compact Star Matter



- ▶ **objective:** development of improved EoS model with
 - ▶ extended set of constituent particles
 - ▶ *nuclear matter*: nucleons, nuclei/clusters, . . . , mesons, hyperons, . . . , quarks
 - ▶ *stellar matter*: add electrons, muons, photons
 - ▶ more serious consideration of correlations
 - ▶ *nucleon-nucleon correlations*: clustering, pairing
 - ▶ *Pauli principle*: dissolution of composite particles in medium (Mott effect)
 - ▶ *electromagnetic correlations*: essential for solidification/melting



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 - ▶ better constrained model parameters
 - ▶ *constraints*: properties of nuclei, compact stars, heavy-ion collisions, theory
 - ▶ correct treatment of phase transitions
 - ▶ distinguish nuclear matter and stellar matter
 - ▶ “non-congruent” phase transitions, gas/liquid/solid(crystal) phases

only a selection from these topics considered here



basic approach: relativistic mean-field (RMF) models

- ▶ **energy density functional**
 - ▶ origin: field theoretical description
 - ▶ derived from Lagrangian density, mean-field approximation
 - ▶ phenomenological description

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- ▶ interaction: exchange of scalar and vector mesons ($\sigma, \omega, \rho, \dots$)
 - ▶ minimal coupling of mesons to nucleons
 - ▶ with nonlinear self-interactions
 - ▶ with density dependent couplings
- ▶ without explicit meson fields
 - ▶ point-coupling models



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▶ many parametrizations

- ▶ different purposes (finite nuclei, excitations, EoS, ...)

(see, e.g., M. Dutra et al., Phys. Rev. C 90 (2014) 055203)



► interaction contribution to Lagrangian

- nonlinear (NL) RMF models with meson self-interactions

$$\mathcal{L}_{\text{int}} = \bar{\psi} g_{\sigma} \sigma \psi - \frac{A}{3} \sigma^3 - \frac{B}{4} \sigma^4 - \bar{\psi} g_{\omega} \omega_{\mu} \gamma^{\mu} \psi + \frac{C}{4} (\omega_{\mu} \omega^{\mu})^2 - \bar{\psi} g_{\rho} \vec{\rho}_{\mu} \cdot \vec{\tau} \gamma^{\mu} \psi$$

with constants g_{σ} , g_{ω} , g_{ρ} , A , B , C , ...

(usually scalar and vector contributions not coupled, cross terms added later)

- density dependent (DD) RMF models

$$\mathcal{L}_{\text{int}} = \bar{\psi} \Gamma_{\sigma} \sigma \psi - \bar{\psi} \Gamma_{\omega} \omega_{\mu} \gamma^{\mu} \psi - \bar{\psi} \Gamma_{\rho} \vec{\rho}_{\mu} \cdot \vec{\tau} \gamma^{\mu} \psi$$

with functionals Γ_{σ} , Γ_{ω} , Γ_{ρ} , ... depending on Lorentz scalars constructed from nucleon fields $\bar{\psi}$, ψ
(motivated by Dirac-Brueckner calculations, more flexible than NL models)

dependence of couplings Γ_i on

- vector density $\varrho^{(v)} = \sqrt{j^{\mu} j_{\mu}}$ with current $j^{\mu} = \bar{\psi} \gamma^{\mu} \psi \Rightarrow$ standard choice
- scalar density $\varrho^{(s)} = \bar{\psi} \psi \Rightarrow$ not really explored so far



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- **phenomenological approach** \Rightarrow model parameters determined from fits
(properties of finite nuclei, characteristic nuclear matter parameters)

Relativistic Density Functionals with Density Dependent Couplings

- ▶ first DD-RMF parametrization fitted to energies of selected nuclei:

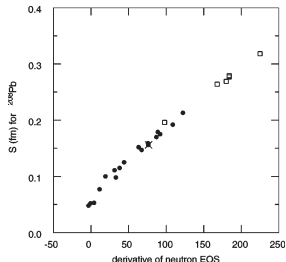
TW99 (S. Typel, H.H. Wolter, Nucl. Phys. A 656 (1999) 331)

- ▶ functional form of couplings: $\Gamma_i(\varrho) = \Gamma_i(\varrho_{\text{ref}})f_i(x)$
with $f_i(x) = a_j \frac{1+b_j(x+d_j)^2}{1+c_j(x+d_j)^2}$ or $f_i(x) = \exp[-a_j(x-1)]$ $x = \frac{\varrho}{\varrho_{\text{ref}}}$
- ▶ two parameters for isovector part of effective interaction (only one in standard NL-RMF models)
 - ⇒ improved nuclear matter parameters, similar to Skyrme Hartree-Fock models
 - ⇒ correlation of neutron skin thickness with slope of neutron matter EoS

| | K [MeV] | J [MeV] | L [MeV] |
|---------|--------------|--------------|--------------|
| TM1 [1] | 285 | 36.9 | 110.8 |
| NL3 [2] | 272 | 37.4 | 118.5 |
| TW99 | 240 | 32.8 | 55.3 |

[1] Y. Sugahara and H. Toki, NPA 579 (1994) 557

[2] G.A. Lalazissis et al., PRC 55 (1997) 540



S. Typel and B.A. Brown, PRC 64 (2001) 027302

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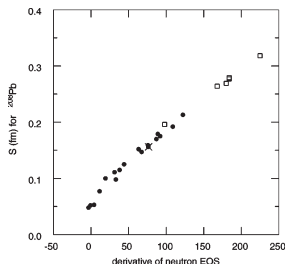
- ▶ many DD-RMF parametrizations in the following

- ▶ DD-ME1 (T. Nikšić et al., PRC 66 (2002) 024306)
- ▶ DDH δ (T. Gaitanos et al., NPA 732 (2004) 24)
- ▶ DD (S. Typel, PRC 71 (2005) 064301)
- ▶ DD-ME2 (G.A. Lalazissis et al., PRC 71 (2005) 024312)
- ▶ DD-F (T. Klähn et al., PRC 74 (2006) 035802)
- ▶ DD2 (S. Typel et al., PRC 81 (2010) 015803)
- ▶ DD-ME δ (X. Roca-Maza et al., PRC 84 (2011) 054309)
- ▶ DD+++ – DD $^{--}$ (S. Typel, PRC 89 (2014) 064321)
- ▶ ...

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Properties of Homogeneous Nuclear Matter

▶ **parametrisation: DD2 with very reasonable nuclear matter parameters**

S. Typel et al., PRC 81 (2010) 015803

▶ **neutron matter EoS consistent with chiral EFT(N³LO) calculations**

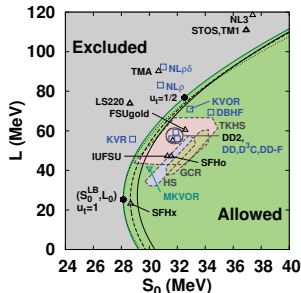
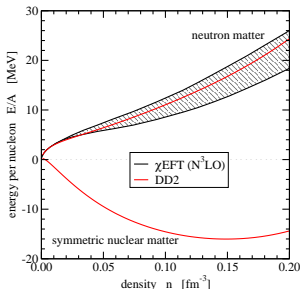
I. Tews et al., PRL 110 (2013) 032504, T. Krüger et al., PRC 88 (2013) 02580

▶ **nuclear symmetry energy consistent with unitary gas constraint**

E. E. Kolomeitsev, J. M. Lattimer, A. Ohnishi, I. Tews, Astrophys. J. 848 (2017) 105

- ▶ $n_b^{\text{sat}} = 0.149 \text{ fm}^{-3}$
- ▶ $a_V = 16.02 \text{ MeV}$
- ▶ $K = 242.7 \text{ MeV}$
- ▶ $J = 31.67 \text{ MeV}$
- ▶ $L = 55.04 \text{ MeV}$

- ▶ $M_{\text{max}} = 2.42 M_{\odot}$
- ▶ $R_{1.4} = 13.2 \text{ km}$





- ▶ **generalized relativistic density functional (gRDF)**
 - ▶ **extended set of particle species**
 - ▶ nucleons, electrons, muons, photons, hyperons (optional), . . .
 - ▶ light nuclei (^2H , ^3H , ^3He , ^4He) and heavy nuclei ($A > 4$)
 - ▶ AME2012/AME2016 mass tables (M. Wang et al., Chin. Phys. C 36 (2012) 1603; Chin. Phys. C 41 (2017) 030003)
 - ▶ extension with DZ10/DZ31 masses (J. Duflo and A.P. Zuker, Phys. Rev. C 52 (1995) R23)
- ⇒ shell effects included, full distribution, not only average heavy nucleus
- ▶ two-nucleon scattering states
- ⇒ consistency with virial EoS at low densities



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 - ▶ **excited states of nuclei**
 - temperature dependent degeneracy factors with density of states
 - ▶ **medium dependence of particle properties**
 - quasiparticle picture, mass shifts (coupling to mesons, effective Pauli principle)
- details: S. Typel et al., Phys. Rev. C 81 (2010) 015803; M. D. Voskresenskaya et al., Nucl. Phys. A 887 (2012) 42; M. Hempel et al., Phys. Rev. C 91 (2015) 045805; S. Typel, arXiv:1504.01571; H. Pais et al., arXiv:1612.07022; H. Pais et al. Nuovo Cim. C 39 (2016) 393



- ▶ **concept applies to composite particles: clusters**
 - ▶ light and heavy nuclei
 - ▶ nucleon-nucleon correlations in continuum
- ▶ **effective change of masses/binding energies**

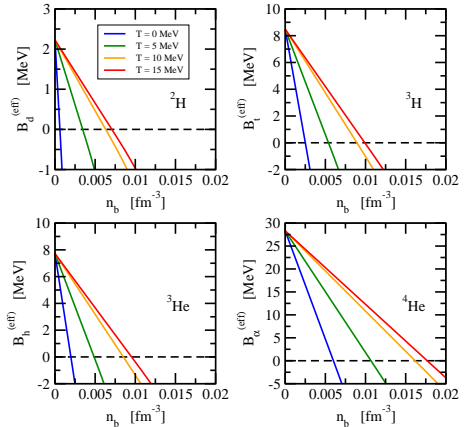


- ▶ **concept applies to composite particles: clusters**
 - ▶ light and heavy nuclei
 - ▶ nucleon-nucleon correlations in continuum
- ▶ **effective change of masses/binding energies**
- ▶ **two major contributions** $\Delta m_i = \Delta m_i^{\text{strong}} + \Delta m_i^{\text{Coul}}$
 - ▶ strong shift $\Delta m_i^{\text{strong}} = \Delta m_i^{\text{meson}} + \Delta m_i^{\text{Pauli}}$
 - ▶ effects of strong interaction (coupling to mesons)
 - ▶ Pauli exclusion principle: blocking of states in the medium
 - ⇒ reduction of binding energies
 - ⇒ cluster dissolution at high densities: Mott effect
 - ⇒ replaces traditional excluded-volume mechanism
 - ▶ electromagnetic shift Δm_i^{Coul} (in stellar matter)
 - ▶ electron screening of Coulomb field
 - ⇒ increase of binding energies

Light Nuclei and NN Scattering states

- ▶ **parametrization from G. Röpke**
simplified and modified for high
densities and temperatures
- ▶ scattering states:
mass shifts as for deuteron

effective binding energies $B_i^{(\text{eff})} = B_i^{(0)} - \Delta m_i^{\text{Pauli}}$



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- ▶ dependence of $\Delta m_i^{\text{Pauli}}$ on temperature T and effective density

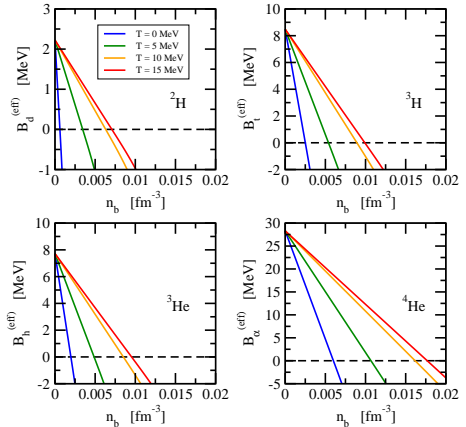
$$n_i^{\text{eff}} = \frac{2}{A_i} [Z_i Y_q + N_i (1 - Y_q)] n_b$$

⇒ asymmetry of medium

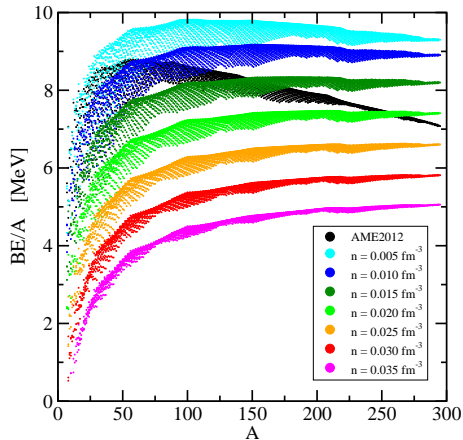
- ▶ Δm_i^{Coul} in Wigner-Seitz approximation

- ▶ full coupling of nucleons in clusters to meson fields

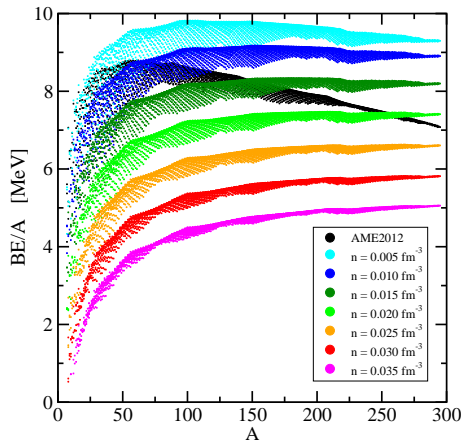
effective binding energies $B_i^{(\text{eff})} = B_i^{(0)} - \Delta m_i^{\text{Pauli}}$



- ▶ simple heuristic parametrization



- ▶ simple heuristic parametrization
- ▶ dependence of $\Delta m_i^{\text{Pauli}}$ only on effective density
$$n_i^{\text{eff}} = \frac{2}{A_i} [Z_i Y_q + N_i(1 - Y_q)] n_b$$
 \Rightarrow asymmetry of medium
- ▶ Δm_i^{Coul} in Wigner-Seitz approximation
- ▶ reduced coupling of nucleons in heavy clusters to meson fields (proportional to surface)

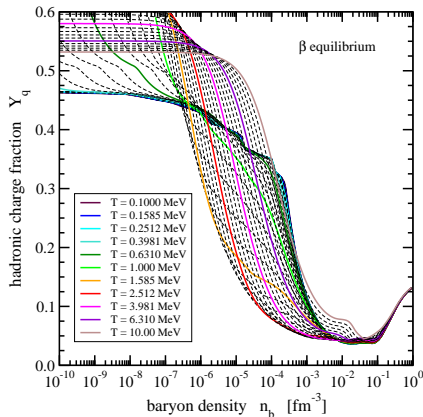
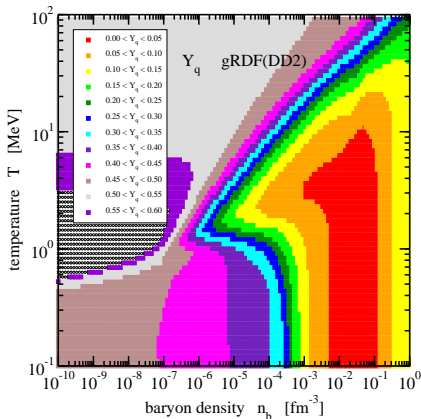




Predictions for Compact Star Matter Experimental Tests Dependence on Symmetry Energy

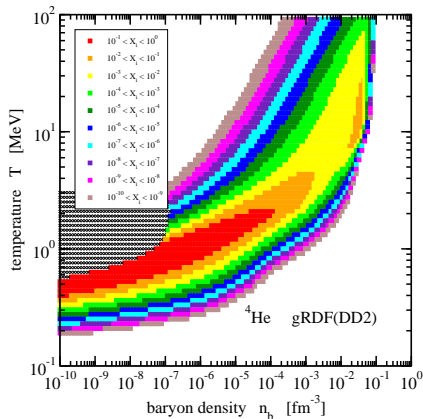
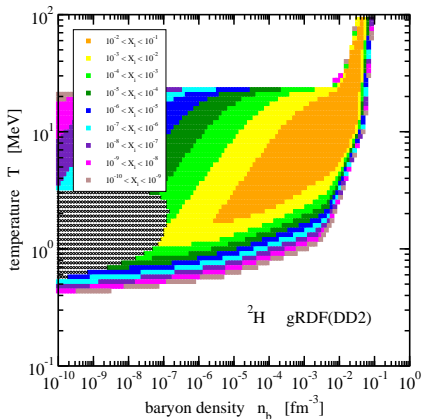
Compact Star Matter Hadronic Charge Fraction

► neutronisation with increasing baryon density



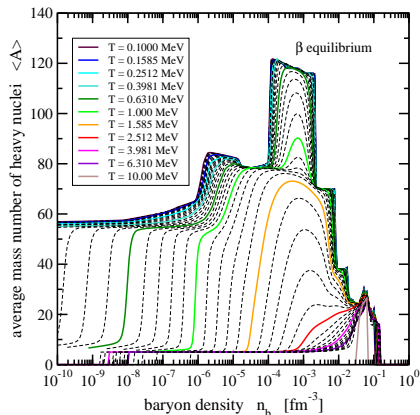
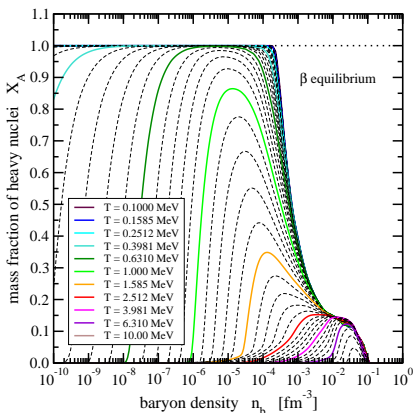
Compact Star Matter Light Clusters

► mass fractions of ${}^2\text{H}$ and ${}^4\text{He}$



Compact Star Matter Heavy Clusters

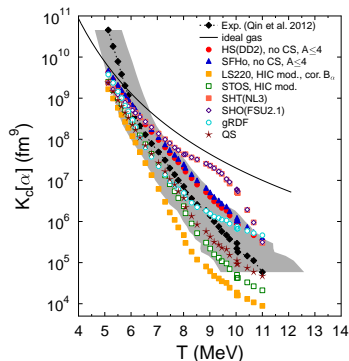
► mass fraction and average mass number



▶ emission of light nuclei in heavy-ion collisions

- ▶ study of particle yields \Rightarrow
chemical equilibrium constants
$$K_c[i] = n_i / (n_p^{Z_i} n_n^{N_i})$$

(L. Qin et al., PRL 108 (2012) 172701,
M. Hempel et al., PRC C 91 (2015) 045805)
- ▶ mixture of ideal gases not sufficient
 \Rightarrow medium effects



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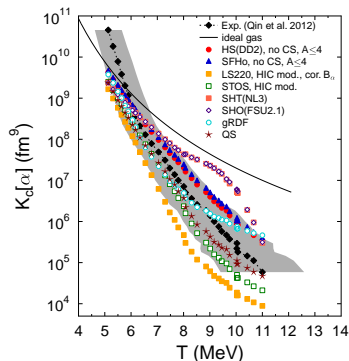
M. Hempel et al., PRC C 91 (2015) 045805)

- ▶ mixture of ideal gases not sufficient \Rightarrow medium effects

▶ cluster correlations at nuclear surface

- ▶ quasifree (p,p α) knockout reactions on Sn nuclei
- ▶ trend of α particle reduced widths in (d, ^6Li) pickup reactions on Sn nuclei \Rightarrow reduction with increasing neutron excess

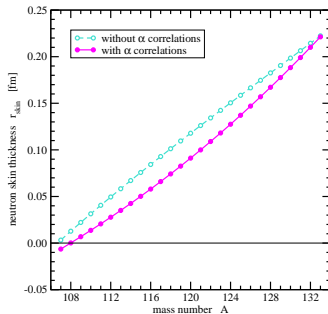
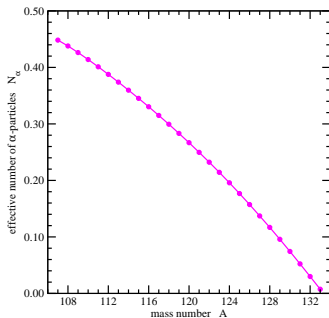
(A. A. Cowley, Phys. Rev. C 93 (2016) 054329)



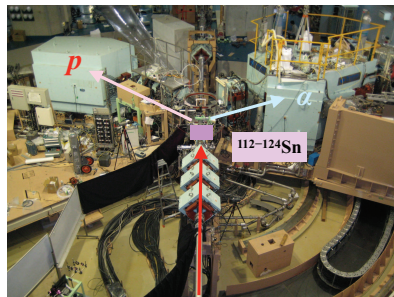
► application of gRDF with clusters to nuclei (zero temperature)

(S. Typel, PRC 89 (2014) 064321)

- α -particles at surface of Sn nuclei
- reduced probability with increasing neutron excess
- reduction of neutron skin thickness, effect depends on symmetry energy



- ▶ **quasifree ($p, p\alpha$) knockout reactions on Sn nuclei**
 - ▶ experimental signatures:
 - ▶ dependence of cross sections on neutron excess
 - ▶ localisation of α particles at surface
⇒ broad momentum distribution



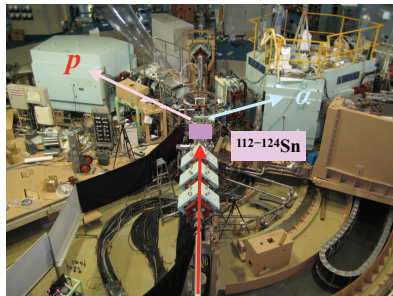
Cluster Correlations at Nuclear Surface II

▶ quasifree ($p,p\alpha$) knockout reactions on Sn nuclei

- ▶ experimental signatures:
 - ▶ dependence of cross sections on neutron excess
 - ▶ localisation of α particles at surface
⇒ broad momentum distribution

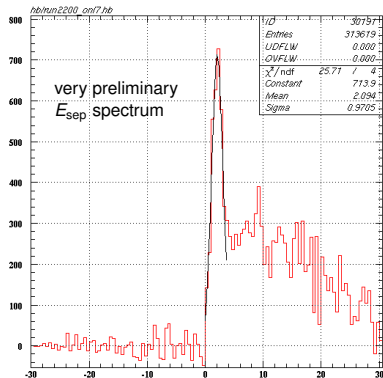
▶ experiments E461 at RCNP, Osaka

- ▶ targets: stable $^{112-124}\text{Sn}$ nuclei
- ▶ beam: 392 MeV protons, 100 pA
- ▶ proton detection: Grand Raiden
- ▶ α detection: LAS
- ▶ first experiment (June 2015):
failure of some detectors
- ▶ second experiment (February 2018):
successful, trend of observed α particles as expected



Cluster Correlations at Nuclear Surface III

- ▶ quasifree (p,p α) knockout reactions on ^{112}Sn (40 mg/cm 2)
- ▶ spectrometer setting: $\theta_{\text{lab}}(p) = 45.3$ deg, $\theta_{\text{lab}}(\alpha) = 60$ deg
- ▶ momentum coverage: $Q_{\alpha} \leq 80$ MeV/c
- ▶ clear identification of peak at the expected position, also for ^{116}Sn , ^{120}Sn , ^{124}Sn ,
- ▶ analysis ongoing (Yang Zaihong)

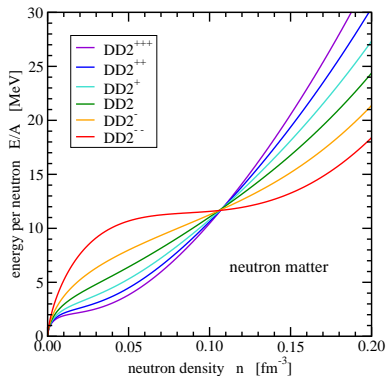


Dependence on Symmetry Energy

► variation of isovector interaction

| parametrisation | symmetry energy J [MeV] | slope coefficient L [MeV] |
|--------------------|------------------------------|--------------------------------|
| DD2 ⁺⁺⁺ | 35.34 | 100.00 |
| DD2 ⁺⁺ | 34.12 | 85.00 |
| DD2 ⁺ | 32.98 | 70.00 |
| DD2 | 31.67 | 55.04 |
| DD2 ⁻ | 30.09 | 40.00 |
| DD2 ⁻⁻ | 28.22 | 25.00 |

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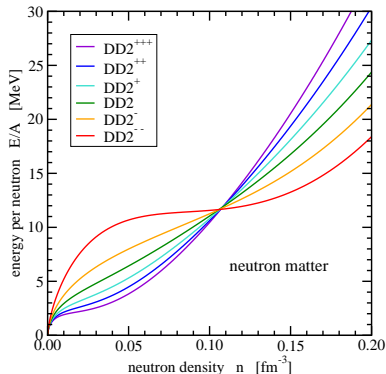
► new EoS tables for DD2⁺, DD2, DD2⁻

$$0.1 \text{ MeV} \leq T \leq 100 \text{ MeV}$$

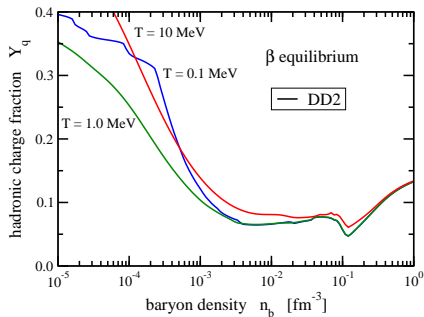
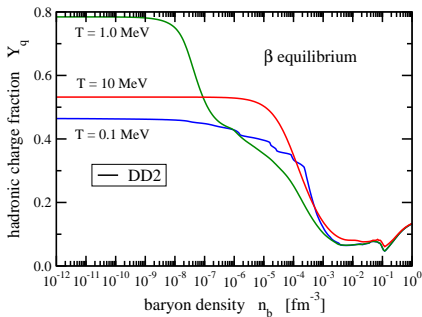
$$10^{-12} \text{ fm}^{-3} \leq n_b \leq 1 \text{ fm}^{-3}$$

$$0.01 \leq Y_q \leq 0.80$$

$$\Rightarrow 76 \times 301 \times 80 = 1830080 \text{ data points each}$$



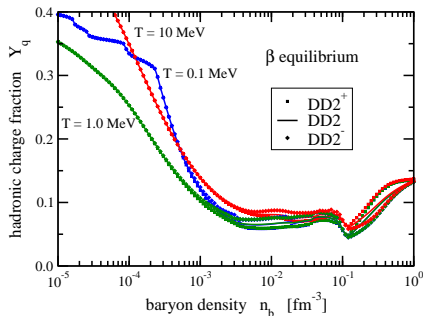
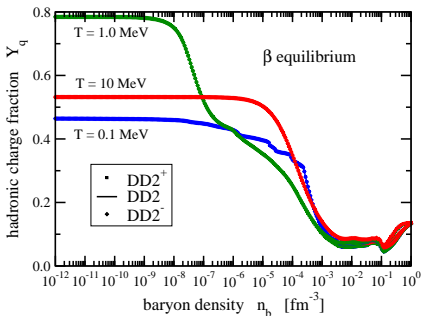
Compact Star Matter Hadronic Charge Fraction



Compact Star Matter

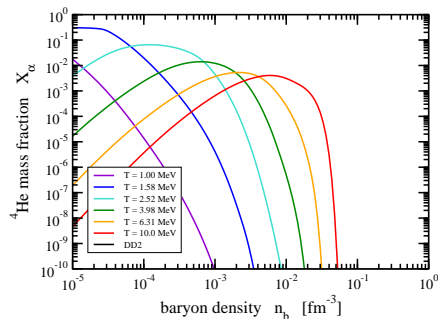
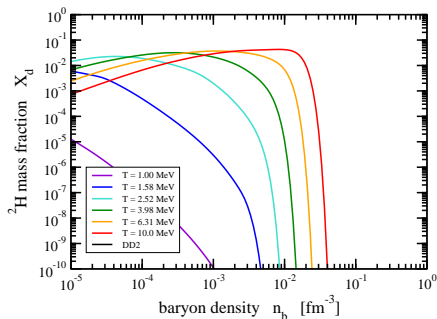
Hadronic Charge Fraction

- ▶ effects of modified symmetry energy only for baryon densities above approx. 10^{-3} fm^{-3}
⇒ sufficiently strong mesons fields needed
- ▶ Y_q smaller for larger L parameter below saturation density
- ▶ Y_q larger for larger L parameter above saturation density



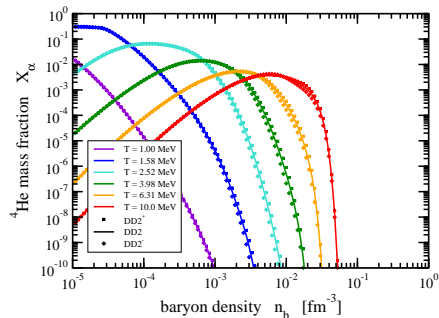
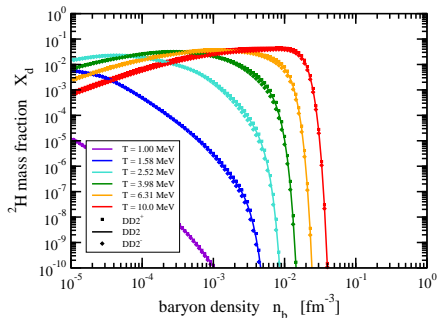
Compact Star Matter Light Clusters I

- ▶ mass fractions of ${}^2\text{H}$ and ${}^4\text{He}$
- ▶ temperature range from 1 MeV to 10 MeV
- ▶ original DD2 parametrisation



Compact Star Matter Light Clusters I

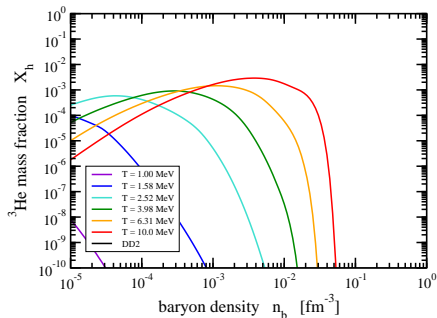
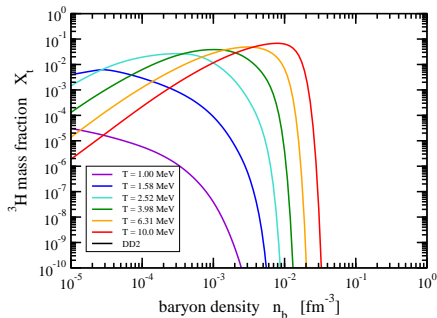
- ▶ mass fractions of ${}^2\text{H}$ and ${}^4\text{He}$
- ▶ temperature range from 1 MeV to 10 MeV
- ▶ parametrisations DD2⁺, DD2, and DD2⁻



Compact Star Matter

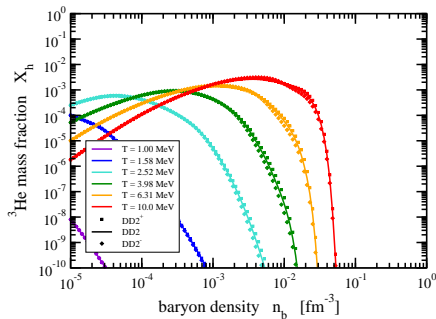
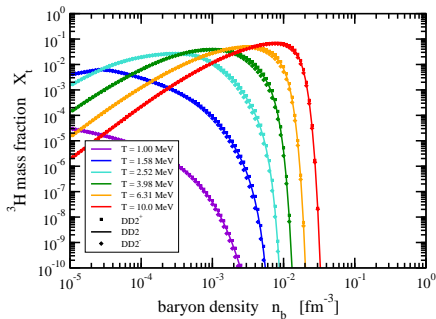
Light Clusters II

- ▶ mass fractions of ${}^3\text{H}$ and ${}^3\text{He}$
- ▶ temperature range from 1 MeV to 10 MeV
- ▶ original DD2 parametrisation



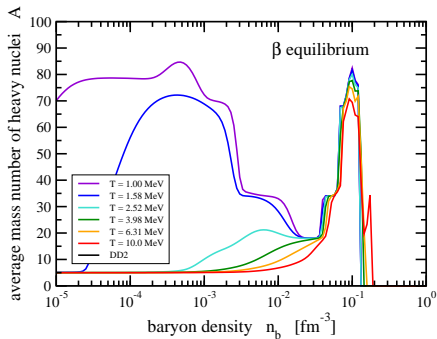
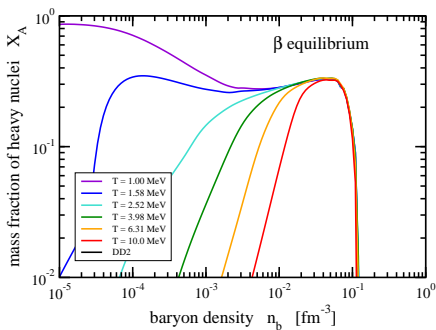
Compact Star Matter Light Clusters II

- ▶ mass fractions of ${}^3\text{H}$ and ${}^3\text{He}$
- ▶ temperature range from 1 MeV to 10 MeV
- ▶ parametrisations DD2⁺, DD2, and DD2⁻



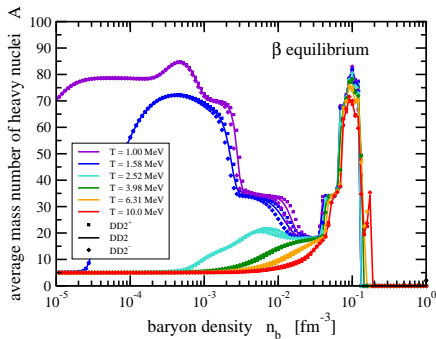
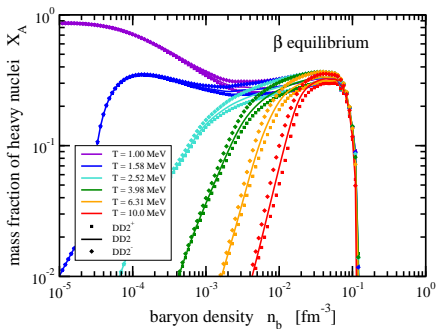
Compact Star Matter Heavy Clusters

- ▶ mass fractions and average mass number of heavy nuclei
- ▶ temperature range from 1 MeV to 10 MeV
- ▶ original DD2 parametrisation



Compact Star Matter Heavy Clusters

- ▶ mass fractions and average mass number of heavy nuclei
- ▶ temperature range from 1 MeV to 10 MeV
- ▶ parametrisations DD2⁺, DD2, and DD2⁻



Problems



- ▶ **vector density dependence:** slope of ω coupling $\left. \frac{d\Gamma_\omega}{dn_b} \right|_{n_b=0} \neq 0$ for DD2
 - ⇒ $n_b = 0$ does not correspond to $\mu_b = 0$ at finite temperature (rearrangement contribution in vector self-energy!)
 - ⇒ development of new parametrisations
- (S. Typel, Particles 1 (2018) 2)

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(S. Typel, Particles 1 (2018) 2)

- ▶ **transition to quark matter**

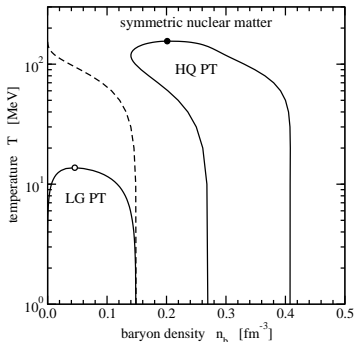
at high densities/temperatures:

not considered in present model

⇒ change of degrees of freedom

⇒ phenomenological description
with modified excluded-volume
mechanism?

(S. Typel and D. Blaschke, Universe 4 (2018) 32)





- ▶ population of **excited states** of heavy nuclei
 - ▶ temperature dependence of degeneracy factors
 - ▶ in EoS tables: $\left. \frac{\partial S}{\partial T} \right|_{n_b, Y_q} < 0$ in parts of the variable space
 - ▶ changes in density of states needed?



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 - ▶ changes in density of states needed?
- ▶ **single-nucleon momentum distributions**
above saturation density:
 - ▶ no clusters (\equiv correlations) by construction, n and p Fermi liquids
 \Rightarrow no population of single-particle momentum states above Fermi energy
 - ▶ experiment with (e,e'pp) knockout reactions:
 \Rightarrow NN short-range correlations, high-momentum tail
(O. Hen et al., Science 346 (2014) 614); PRC 91 (2015) 025803; RMP 89 (2017) 045002)
 - ▶ realisation in density functional?



► thermodynamic consistency

- local conditions:

e.g., for internal energy $E(S, V, \{N_i\}) = TS - pV + \sum_i \mu_i N_i$

with EoS $T = \left. \frac{\partial E}{\partial S} \right|_{V, N_i}$, $p = - \left. \frac{\partial E}{\partial V} \right|_{S, N_i}$, $N_i = \left. \frac{\partial E}{\partial \mu_i} \right|_{S, N_{j \neq i}}$

and Maxwell relations $\left. \frac{\partial T}{\partial V} \right|_{S, N_i} = - \left. \frac{\partial p}{\partial S} \right|_{V, N_i}$, ...

⇒ usually fulfilled



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and Maxwell relations $\left. \frac{\partial T}{\partial V} \right|_{S, N_i} = - \left. \frac{\partial p}{\partial S} \right|_{V, N_i}, \dots$

⇒ usually fulfilled

- global conditions:

e.g., convexity of $E(S, V, \{N_i\})$

⇒ phase transitions



coexistence of phases

- ▶ general construction with Gibbs conditions:
equal intensive variables
 - ▶ temperature
 - ▶ pressure
 - ▶ chemical potentials

⇒ **binodals**
(enclose phase coexistence regions)

coexistence of phases

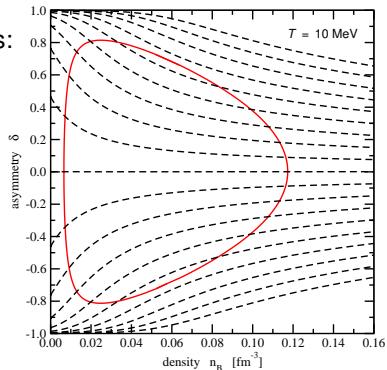
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equal intensive variables

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⇒ **binodals**
(enclose phase coexistence regions)

▶ nuclear matter

- ▶ consider lines of equal charge chemical potential
 $\mu_q = \mu_p - \mu_n$
⇒ standard Maxwell construction
- ▶ symmetry with respect to isospin asymmetry



coexistence of phases

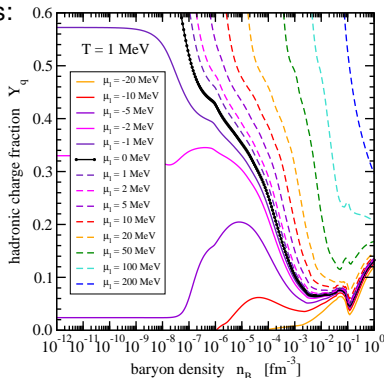
- ▶ general construction with Gibbs conditions:
equal intensive variables

- ▶ temperature
- ▶ pressure
- ▶ chemical potentials

⇒ **binodals**
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▶ compact star matter

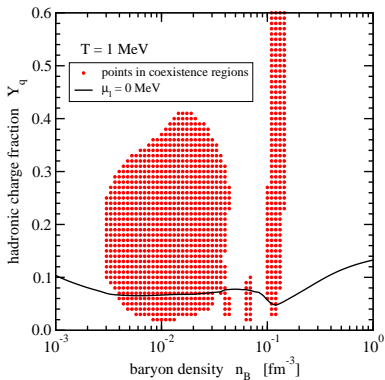
- ▶ specific condition of charge neutrality
- ▶ consider lines of equal lepton chemical potential
 $\mu_l = \mu_e + \mu_q$
⇒ standard Maxwell construction
- ▶ no symmetry with respect to isospin asymmetry



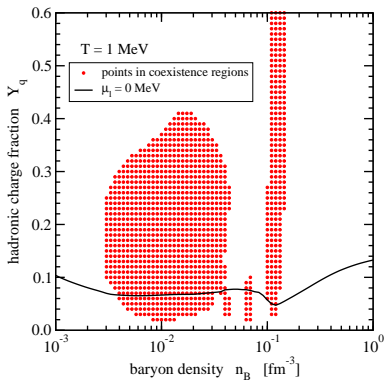
- ▶ full gRDF EoS table with DD2 parametrization
 - ▶ baryon density: $10^{-12} \text{ fm}^{-3} \leq n_B \leq 1 \text{ fm}^{-3}$
 - ▶ temperature: $0.1 \text{ MeV} \leq T \leq 100 \text{ MeV}$
 - ▶ hadronic charge fraction: $0.01 \leq T_q \leq 0.60$

⇒ **multiple phase transitions**

- ▶ coexistence of clustered and homogeneous phases
- ▶ coexistence of two clustered phases with different chemical composition



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 - ▶ baryon density: $10^{-12} \text{ fm}^{-3} \leq n_B \leq 1 \text{ fm}^{-3}$
 - ▶ temperature: $0.1 \text{ MeV} \leq T \leq 100 \text{ MeV}$
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- ⇒ **multiple phase transitions**
 - ▶ coexistence of clustered and homogeneous phases
 - ▶ coexistence of two clustered phases with different chemical composition
- ▶ global thermodynamic consistency of other EoS tables ?





Conclusions

▶ Formation and Dissolution of Clusters

- ▶ important aspect in compact star matter below nuclear saturation density
- ▶ changes chemical composition
- ▶ clusters as particular multi-nucleon correlations
- ▶ experimental observation in heavy-ion collisions, nuclear structure

▶ **Formation and Dissolution of Clusters**

- ▶ important aspect in compact star matter below nuclear saturation density
- ▶ changes chemical composition
- ▶ clusters as particular multi-nucleon correlations
- ▶ experimental observation in heavy-ion collisions, nuclear structure

▶ **Generalized Relativistic Density Functional**

- ▶ extension of relativistic mean-field model with well constrained parameters
- ▶ effects of strong & electromagnetic interaction and Pauli blocking
⇒ medium dependent mass shifts of clusters
- ▶ effects from density dependence of symmetry energy
- ▶ EoS tables for simulations of core-collapse supernovae and neutron star mergers
- ▶ several issues still to be solved

▶ **Massive Neutron Star in Compact Binary**

- ▶ PSR J2215+5135, 4.14 hr orbit
- ▶ $M_1 = 2.27^{+0.17}_{-0.15} M_{\odot}$ neutron star
- ▶ $M_2 = 0.33^{+0.03}_{-0.02} M_{\odot}$ companion star
- ▶ M. Linares, T. Shahbaz, J. Casares,
arXiv:1805.08799, ApJ 859 (2018) 54 (May 23, 2018)



Thank You For Your Attention