## Earth-Moon Lagrangian points as a testbed for general relativity and effective quantum field theories of gravity: an experimental point of view

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\begin{aligned}
& \text { FQT-2015, INFN-LNF, Frascati (Italy) } \\
& \text { Sep. 24, } 2015
\end{aligned}
$$

## Outline

- Earth-Moon gravitational physics
- Lagrangian points
- Experimental approach to test new prediction
- SCF_Lab @ Frascati \& international context


## New generation lunar laser retroreflectors

## MoonLIGHT <br> Moon Laser Instrumentation for General relativity High accuracy Tests

Largest, optically most accurate Suprasil reflectors ever

MoonLIGHT (new, 100 mmm ) Apollo (old, 38 mm )


## Tests of General Relativity with MoonLIGHTs

| Precision test of violation of General Relativity | Time scale | Apollo/Lunokhod few cm accuracy* | $\begin{aligned} & \text { Moon } \\ & 1 \mathrm{~mm} \end{aligned}$ | IGHTs <br> 0.1 mm |
| :---: | :---: | :---: | :---: | :---: |
| Parameterized Post-Newtonian (PPN) | Few years | $\|\beta-1\|<1.1 \times 10^{-4}$ | $10^{-5}$ | $10^{-6}$ |
| Weak Equivalence Principle (WEP) | Few years | $\|\Delta a / a\|<1.4 \times$ | 10 | 10 |
| Strong Equivalence Principle (SEP) | Few years | $\|\eta\|<4.4 \times 10^{-4}$ | $3 \times 10$ | $3 \times 10$ |
| Time Variation of the Gravitational Constant (Gdot) | $\sim 5$ years | $\|\dot{\mathrm{G}} / \mathrm{G}\|<9 \times 10^{-13} \mathrm{yr}$ | $5 \times 10^{-14}$ | $5 \times 10^{-15}$ |
| Inverse Square Law (ISL) | $\sim 10$ years | $\|\alpha\|<3 \times 10^{-11}$ | $10^{-12}$ | $10^{-13}$ |
| Geodetic Precession (GP) | Few years | $\left\|\mathrm{K}_{\mathrm{GP}}\right\|<6.4 \times 10^{-3}$ | $6.4 \times 10^{-4}$ | $6.4 \times 10^{-5}$ |
| * PRL 93, 261101 (2004) <br> Gravity Probe $\mathrm{B}: \mid \mathrm{K}_{\mathrm{GP}}<2.8 \times 10^{-3}$ | * PRL 93, 261101 (2004) <br> Gravity Probe B: $\mid \mathrm{K}_{\mathrm{GP}}<2.8 \times 10^{-3}$ |  | Apolle 15 |  |

## Giuseppe Luigi Lagrange,

## born in Turin, Italy, on Jan. 25, 1736



## Earth-Moon Lagrangian points: New Physics

- E. Battista and G. Esposito, Phys. Rev. D 89, 084030 (2014)
- E. Battista and G. Esposito, Phys. Rev. D 90, 084010 (2014)
- Quantum effects on Lagrangian points and displaced periodic orbits in the Earth-Moon system
- E. Battista, S. Dell’Agnello, G. Esposito, and J. Simo
- Phys. Rev. D 91, 084041 (2015) - Published 20 April 2015
- Earth-Moon Lagrangian points as a testbed for general relativity and effective field theories of gravity
- E. Battista, S. Dell’Agnello, G. Esposito, L. Di Fiore, J. Simo, A. Grado
- Accepted for Phys. Rev.D 92 (2015) - To be published this week


## Low-energy test of quantum gravity with

Lunar-like Laser Ranging

$$
V_{Q}(r)=-\frac{G m_{A} m_{B}}{r}\left(1+\frac{k_{1}}{r}+\frac{k_{2}}{r^{2}}\right)+\mathrm{O}\left(G^{2}\right)
$$



$$
\begin{aligned}
& k_{1} \equiv \kappa_{1} \frac{G\left(m_{A}+m_{B}\right)}{c^{2}} \\
& k_{2} \equiv \kappa_{2} \frac{G \hbar}{c^{3}}=\kappa_{2}\left(l_{P}\right)^{2}
\end{aligned}
$$

$l_{\mathrm{p}}$ is the Planck length. $\mathrm{K}_{1}$ depends on $\varkappa_{2}$
$x_{1}$ and $x_{2}$ result from quantum loop diagrams.

## New large effect, \& test, of General Relativity

| $L_{i}$ | General Relativity-Newton | Quantum-General Relativity | Quantum-Newton |
| :--- | :--- | :--- | :--- |
| $L_{1}$ | -7.61 m | -0.62 mm | -7.61 m |
| $L_{2}$ | 9.40 m | -0.39 mm | 9.40 m |
| $L_{3}$ | -1.13 m | -1.48 mm | -1.13 m |
| $L_{4}$ | $(2.73 \mathrm{~mm},-1.59 \mathrm{~mm})$ | $(-1.46 \mathrm{~mm},-0.86 \mathrm{~mm})$ | $(1.27 \mathrm{~mm},-2.45 \mathrm{~mm})$ |
| $L_{5}$ | $(2.73 \mathrm{~mm},-1.59 \mathrm{~mm})$ | $(-1.46 \mathrm{~mm},-0.86 \mathrm{~mm})$ | $(1.27 \mathrm{~mm},-2.45 \mathrm{~mm})$ |

## New large effect, \& test, of General Relativity

- Design a laser retroreflector to measure this new effect
- Design a suited mission and laser-guided propulsion system to reach and stop at Lagrangian points
- Study systematic effects: non-gravitational perturbations and multi-body gravitational effects
- Lagrangian-point Laser-ranging Gravity Eplorer (LaGrEx)
- $1^{\text {st }}$ generation experiment for a new test of GR

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## Key remarks

- The 7.61 m correction looks measurable, hence encouraging
- L2 is behind the Moon, L3 not a 'popular' destination
- It is possible to conceive a new laser ranging test of general relativity by measuring this correction to the L1 Lagrangian point, an observable never used before in the Sun-Earth-Moon system. Such an experiment requires controlling the propulsion to precisely reach L1, an instrumental accuracy comparable to the measurement of the lunar geodesic precession, understanding systematic effects resulting from solar radiation pressure and heating of the satellite that leads to photon emission, and multi-body gravitational perturbations.
- Much harder task: to measure the tiny deviations of effective gravity from GR in the Sun-Earth-Moon system.


## Tasks of INFN-Napoli

- Napoli contribution is mainly devoted to Theoretical modeling

Analysys of gravitational perturbation

- Computation of the propulsion needed to stay precisely at $\mathrm{L}_{1}$ or $\mathrm{L}_{4}$.
- Analysis of effects due to the presence of many bodies.

Analysys of non gravitational perturbation

- Deep study of solar radiation pressure.
- Heating Effects of satellites with consequent photons emission.


## SCF_Lab @Frascati \& international context

INFN and ASI, NASA
Partnership


SERV SOLAR SYSTEM EXPLORATIOM RESERRCH

VIRTUALINSTITUTE

Formerly the NASA LUNAR S(IENCE INSTITUTE


## International Partnerships

Eight international partnerships collaborate with U.S. based SSERVI researchers on a no-exchange-of-funds basis.


## $3^{\text {rd }}$ European Lunar Symposium

## EUROPEAN LUNAR SYMPOSIUM

 FRASGATTtall- Berlin (2012), London (2014), Frascati (2015)
- Science of the Moon
- Science on the Moon
- Science from the Moon
- Future Lunar / Cislunar Missions


# Moon Express Announces First International Multi-Mission Payload Agreement with The INFN National Laboratories of Frascati and the University of Maryland 

"MoonLIGHT" Lunar Laser Ranging Array Will Bring New Insights into General Relativity
Frascati, Italy (May $\mathbf{1 5}^{\mathbf{t h}}$, 2015) - Moon Express, Inc. (MoonEx) has announced a multi-mission payload agreement with The National Laboratories of Frascati (INFN-LNF) and the University of Maryland to deliver a new generation of lunar laser ranging arrays to the Moon. Under the agreement, "MoonLIGHT" instruments will be carried on the first four Moon Express missions and used in conjunction with Apollo Cube Corner (CCR) Retroreflector arrays to test principles of Einstein's General Relativity theory, add to international scientific knowledge of the Moon, and increase lunar mapping precision that will support the company's future lander missions. right after the European Lunar Symposium, during a Global

"MoonLIGHT" Payload Agreement Announcement in
Frascati, Italy. L-R: Jack Burns, CU; Doug Currie, UMD;
Simone Dell'Agnello, INFN-LNF; Bob Richards, Moon Express Exploration Roadmap workshop of the International Space Exploration Coordination Group (ISECG), attended by officials national space agencies and lunar scientists from around the world.

