

# HOUGH TRANSFORMATION ALGORITHM FOR THE TRACKING IN THE CGEM-IT

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# OUTLINE

## Introduction

- CGEM-IT software
- Hough transformation

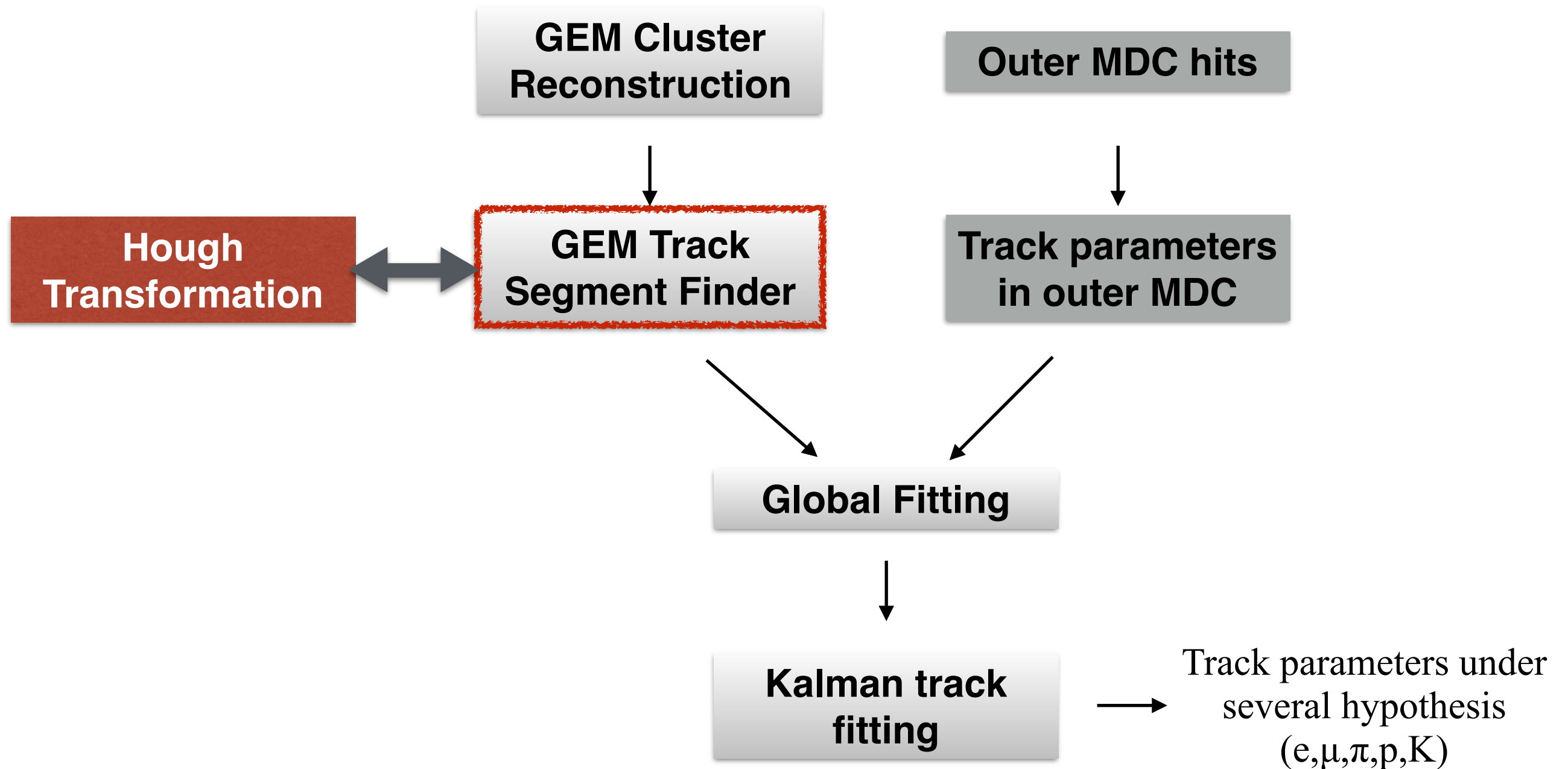
## The Hough algorithm

- how to find a track

## Summary and conclusions

- status of the code and plans

# Reconstruction with CGEM-IT



# Introduction: the HOUGH transformation

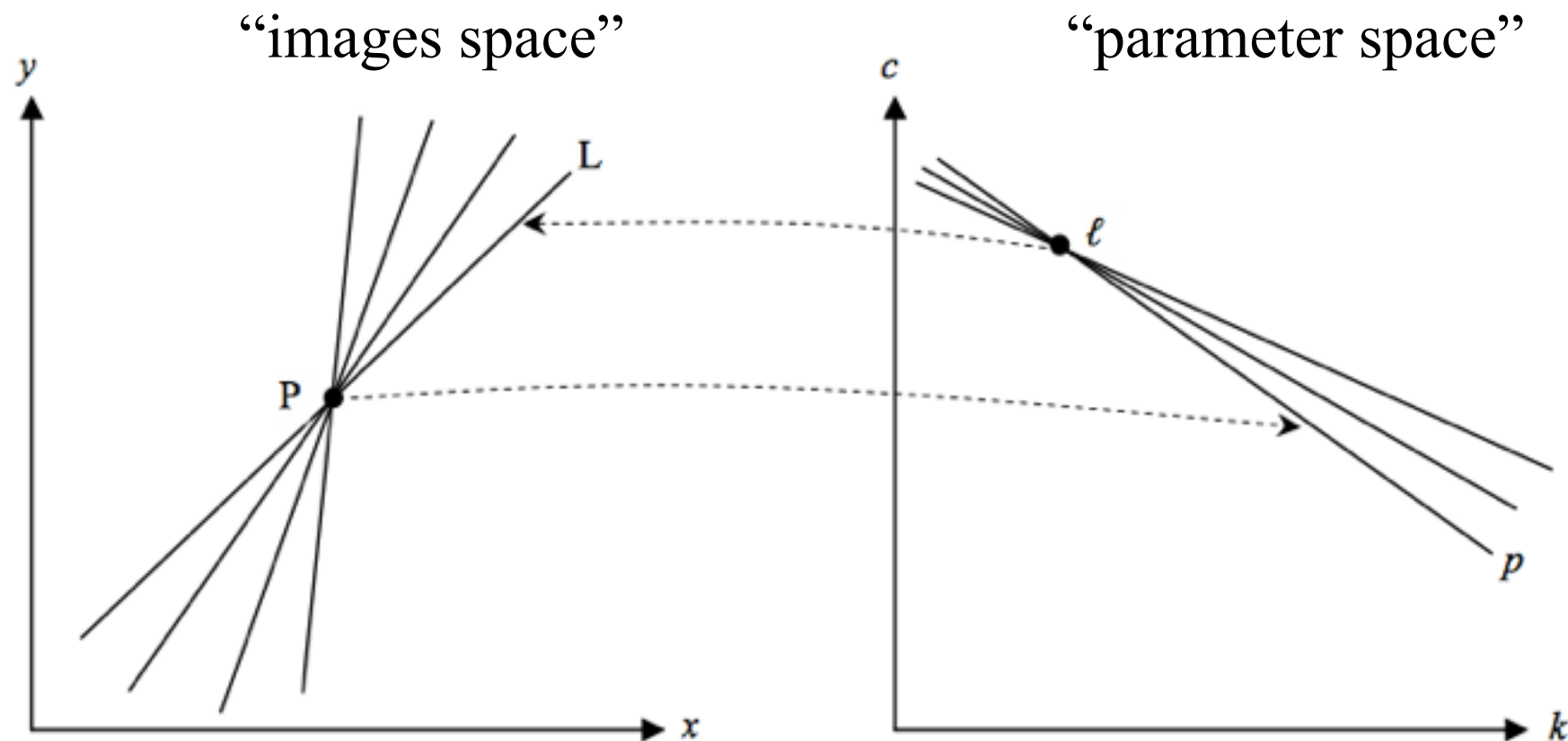
- The Hough transformation (HT) can be used to detect lines, circles or other parametric curves
- It was introduced in the 1962, and first used one decade later to find lines in an image
- It can detect lines, circles, and other structures if their parametric equation is known
- HT can be used as track finder method
  - global tracking method: all hits enter into the algorithm at the same time and in the same way
  - also used in many experiments: ATLAS, PANDA, ...
  - first version developed for the MDC tracking in BESIII (Zhang Jin, Zhang Yao, Liu Huaimin) to improve the tracking for low momentum particles ( $p_t < 120$  MeV)

## ADVANTAGES:

- global method (in a local method the pattern recognition starts with a seed of track consisting of a few hits, then more hits are added step by step)
- noise resistant
- resistant to the hits inefficiency

# Principle of the Hough transformation

## LINE/POINT DUALITY



The line in the “images space” is defined by points whose coordinate satisfy the equation:  $y=kx+c$

- A point P in the “images space” defines a lines (p) in the “parameters space”

Each point in the “parameter space” can be defined by the bundle of lines passing through it

- each point (l) on the line p defines a line L in the “image space” in the bundle of lines passing through P

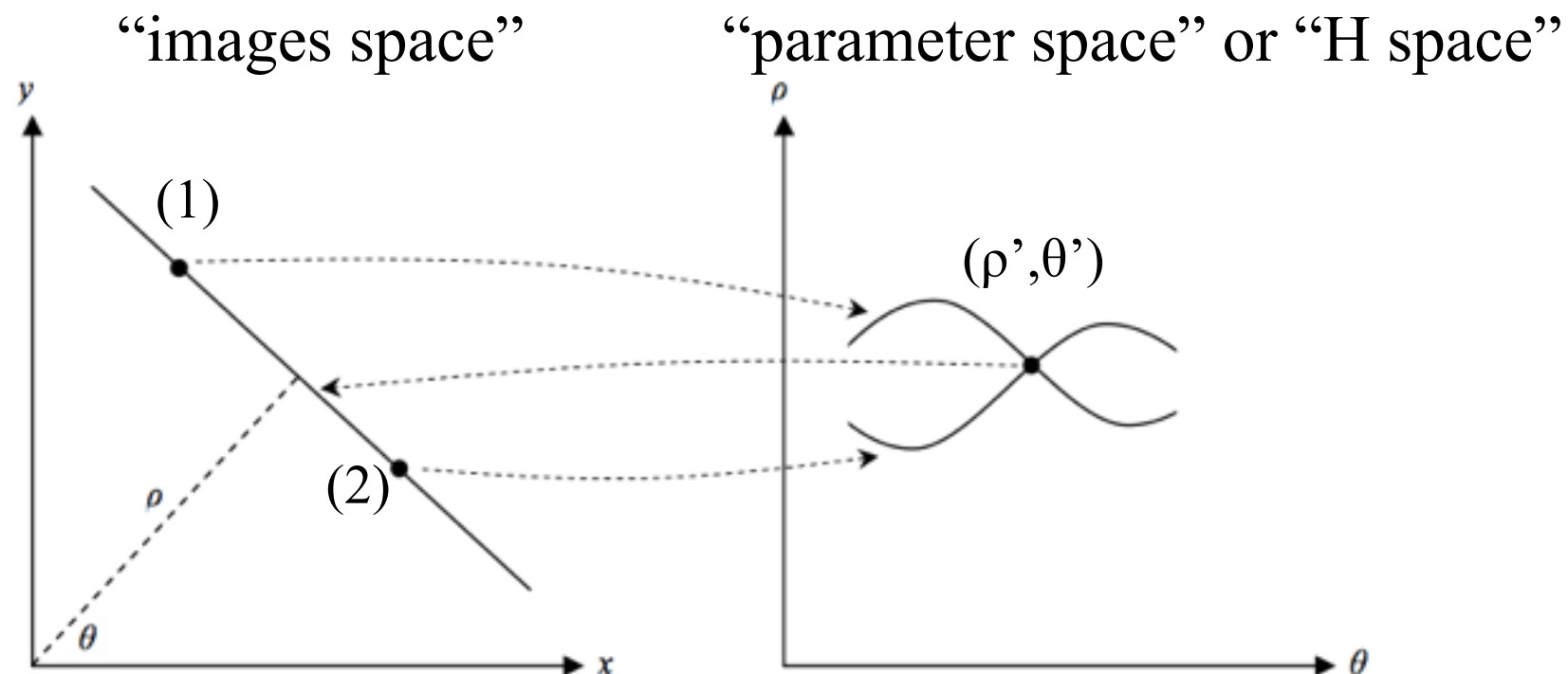
1. Coordinates of  $l$  are the parameters of line L  $\Rightarrow$  this method can be thought as a transform between “images space” and “parameters space”.
2. **If the hits are on a straight line, the lines in the “parameters space” intersect in one point , and the intersection gives the parameters of the line the hits are on.**



# Polar parameterization of lines

To avoid singularities arising from the infinite slope for vertical lines, Duda and Hart (Comm. ACM 15, pp.11-15, 1972) introduces a singularity free alternative:

$$\rho = x \cdot \cos(\theta) + y \cdot \sin(\theta)$$



Each point in the  $yx$ -plane gives a sinusoid in the "H space"  $\implies$  the intersection point  $(\rho', \theta')$  correspond to the line that passes through the two points (1) and (2)

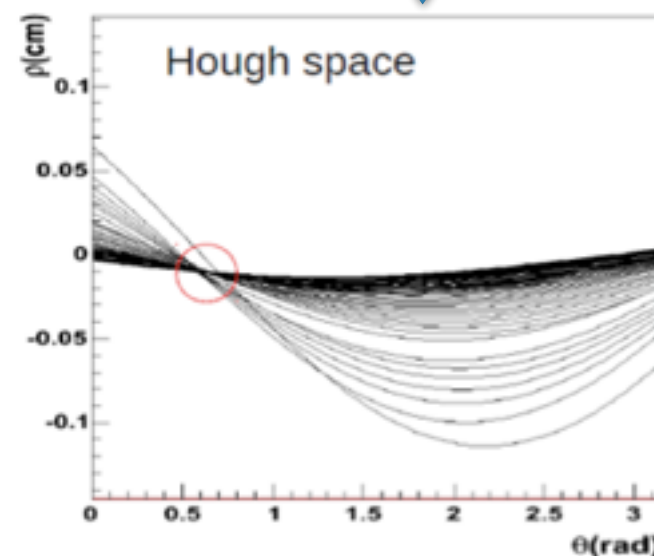
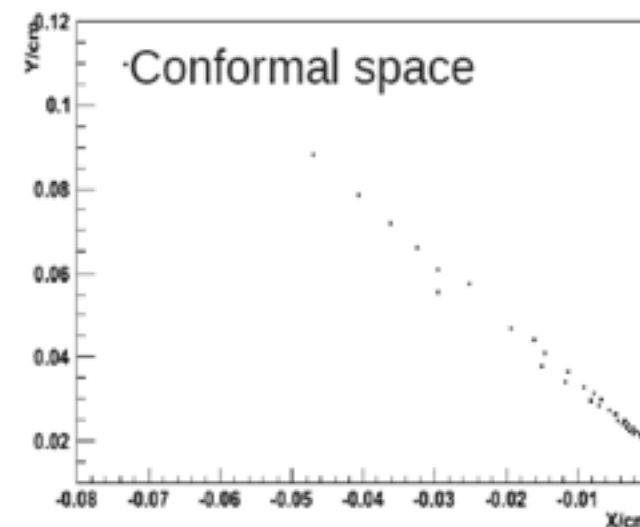
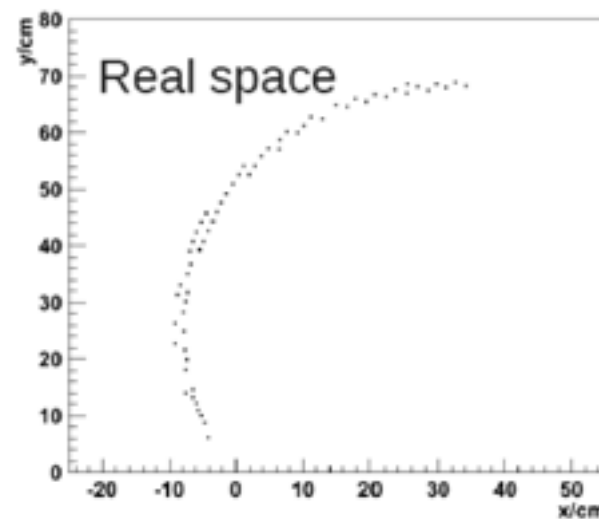
**Basic idea of HT:** parametric shapes can be detected by looking for accumulation points in the parameter space. If a particular shape is present in the image, then the mapping of all its points into the parameter space must cluster around the parameter values which correspond to that shape (two parameters for a line)

# Conformal transformation

The conformal mapping method (Hansroul *et al.*, 1988) for track finding is based on the fact that circles going **through the origin** of a two-dimensional xy-coordinate system maps onto straight lines in a XY coordinate system by the transformation:

$$(x,y) \rightarrow (X,Y) \quad X=2x/(x^2+y^2) \quad \text{and} \quad Y=2y/(x^2+y^2)$$

Find a straight line is  
less complicate than  
find a circle



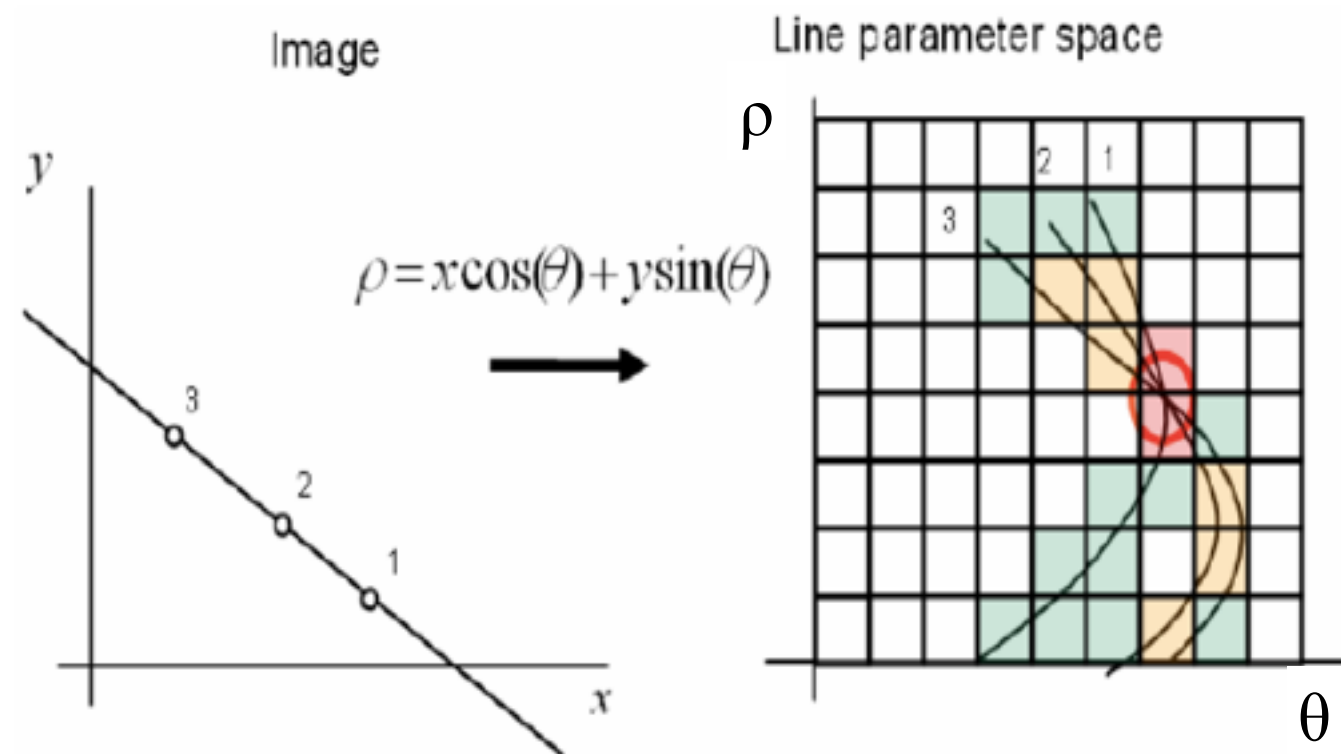
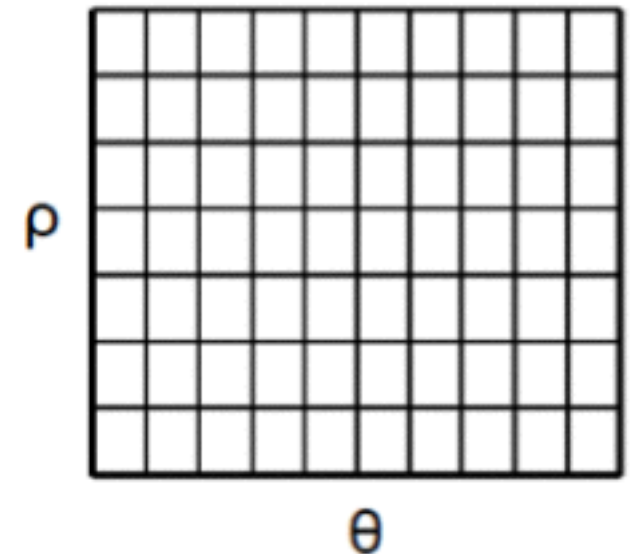
A peak in the 2D histogram  
corresponds to a track

[\*MDC-HT, Z. Jin, Z.  
Yao, L. Huaimin]

# HT Algorithm

## ALGORITHM STRATEGY:

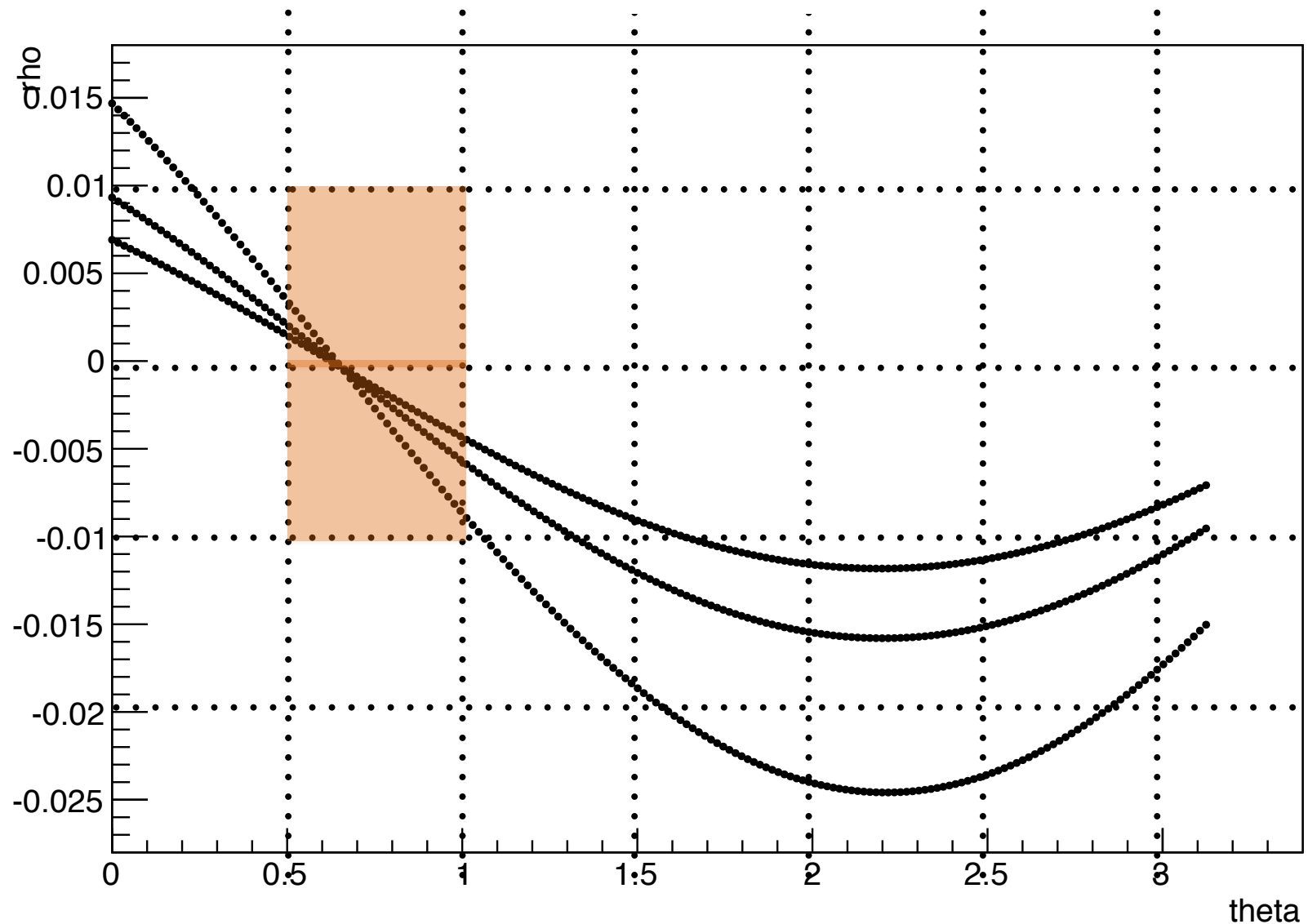
- conformal coordinates:  $(x,y) \Rightarrow (X,Y)$
- $0 < \theta_i < \pi$
- for each  $\theta_i$ , we calculate  $\rho_i$ :  $\rho_i = X \cos \theta_i + Y \sin \theta_i$
- each cell records the number of courses passing through it
  - we find the cells with the largest entries





# HT Algorithm: $(\theta, \rho)$ discretization (I)

Step 1

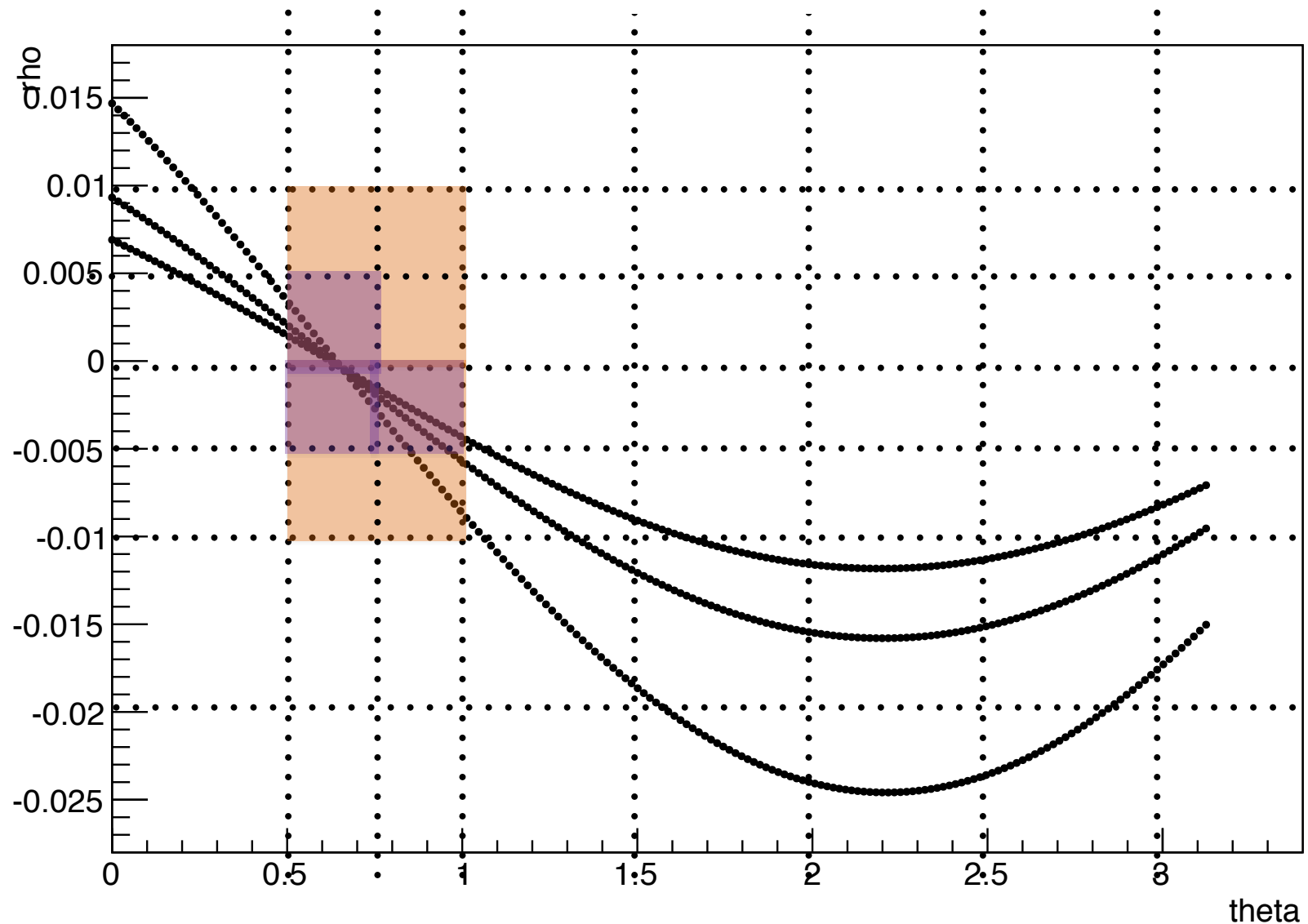


Discretization of the  $(\theta, \rho)$  space

- efficiency
- resolution
- computing time

# HT Algorithm: $(\theta, \rho)$ discretization (II)

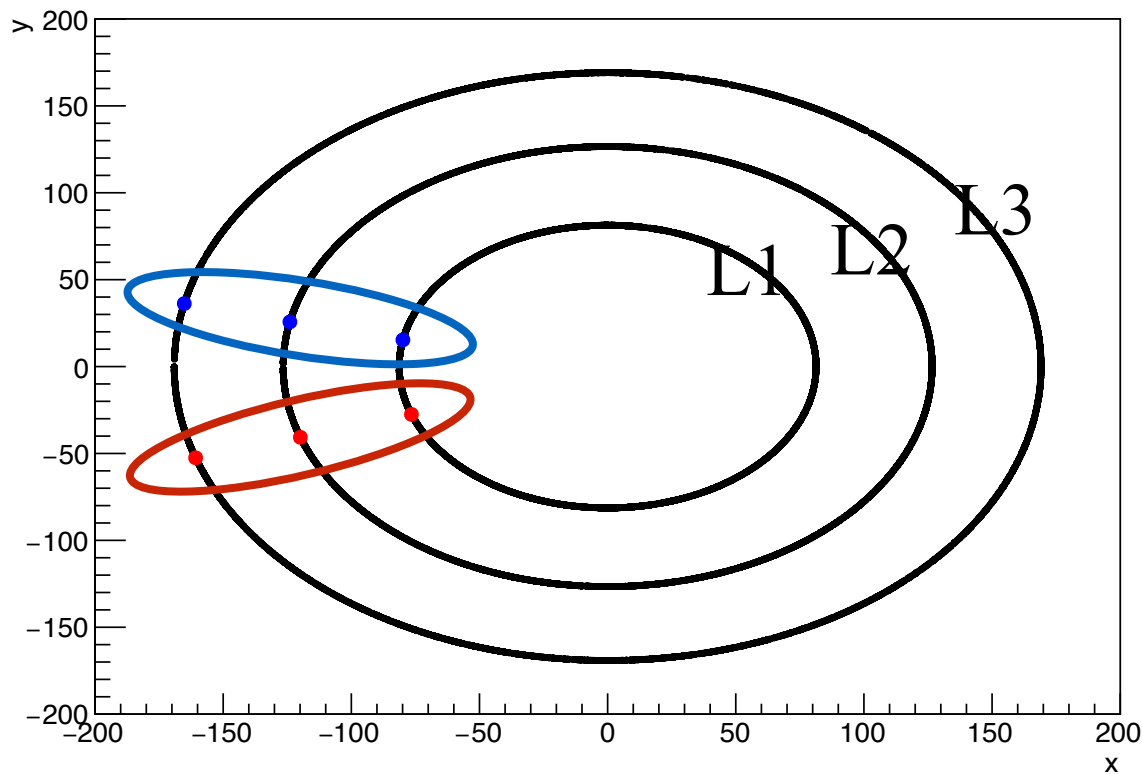
Step2



- Search for the  $(\rho, \theta)$  intervals with at least 3 hits
- Calculate the average  $\rho$  and  $\theta$  values
- Single decay mode test: excellent results

# HT Algorithm for the CGEM-IT

Image space



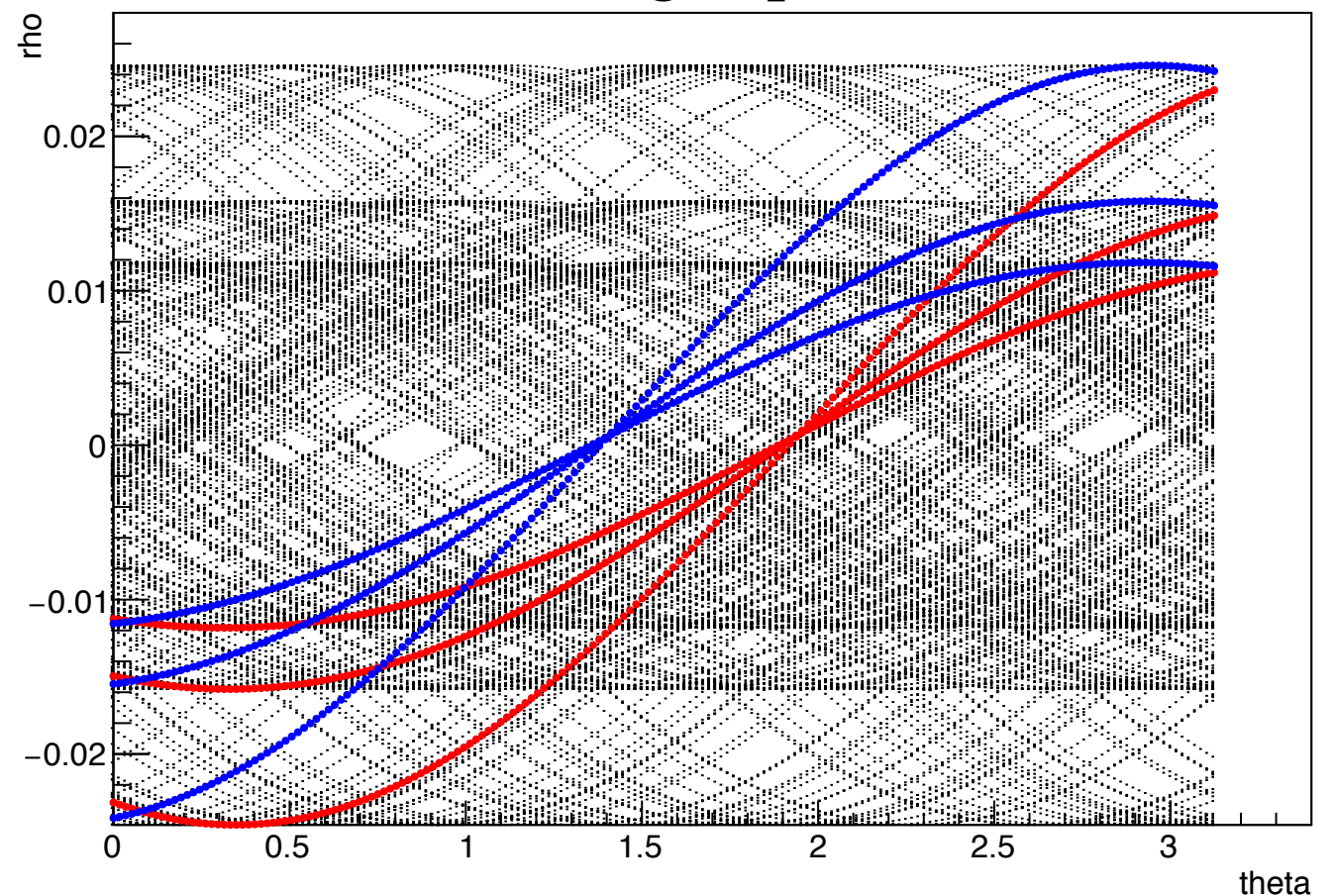
event 1 — blue —  
event 2 — red —

Simpler case: only one track for event  
and no noise simulated.

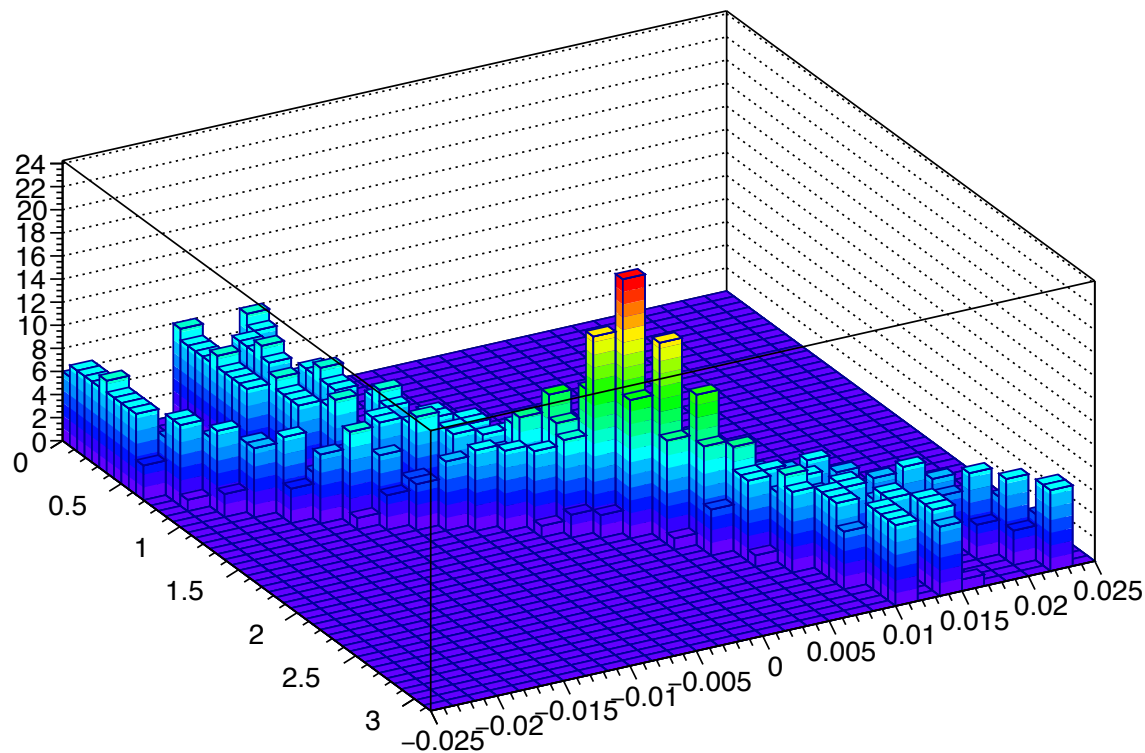
Using the BESIII framework, we simulate  
muons with  $p = 1 \text{ GeV/c}$  with  $|\cos\theta| < 0.8$

- the intersection point in the H space  
defines the segment passing through  
aligned points

Hough space



# HT Algorithm: binning effect

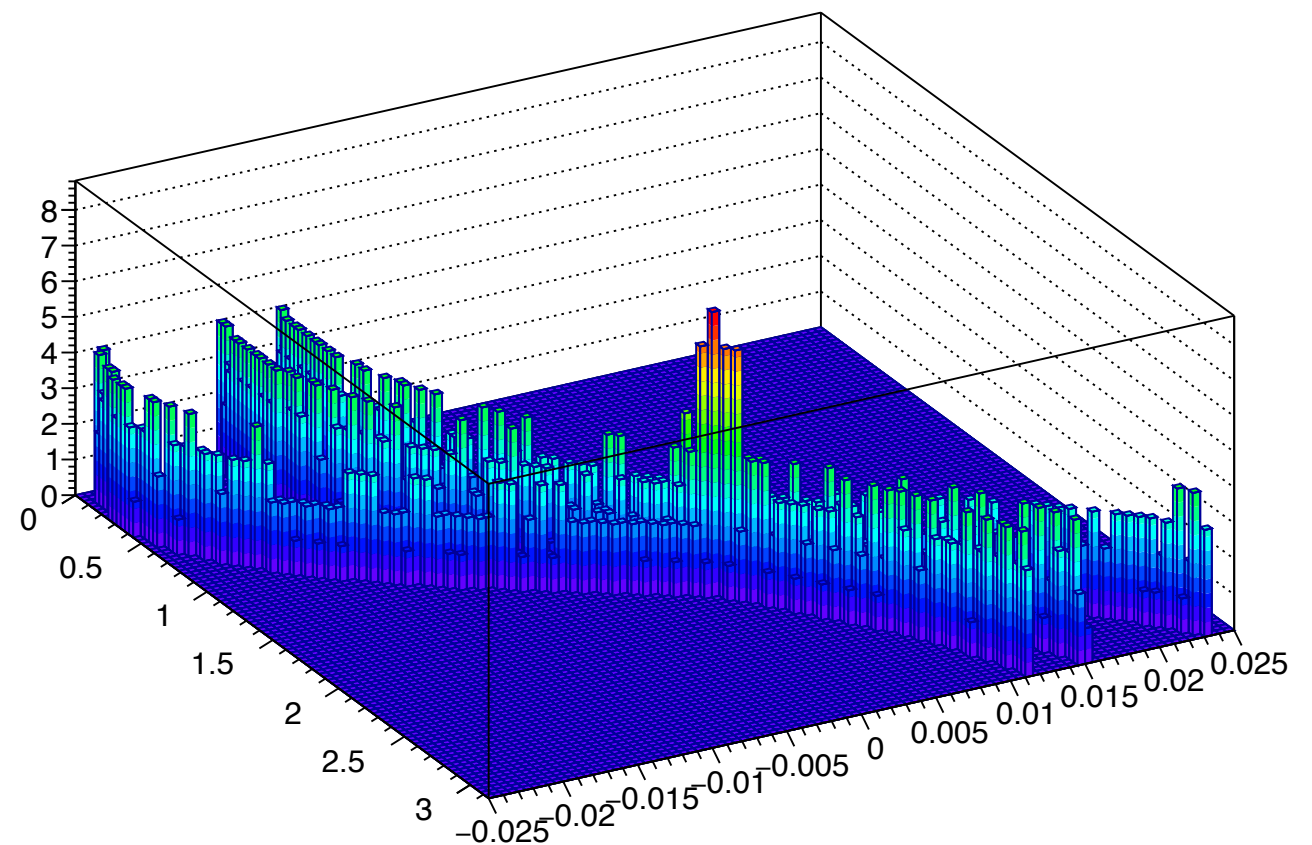


**50 × 30, small bins**

- high tracking efficiency
- worse resolution: two neighbor tracks can be mixed in the same peak

**100 × 100, large bins**

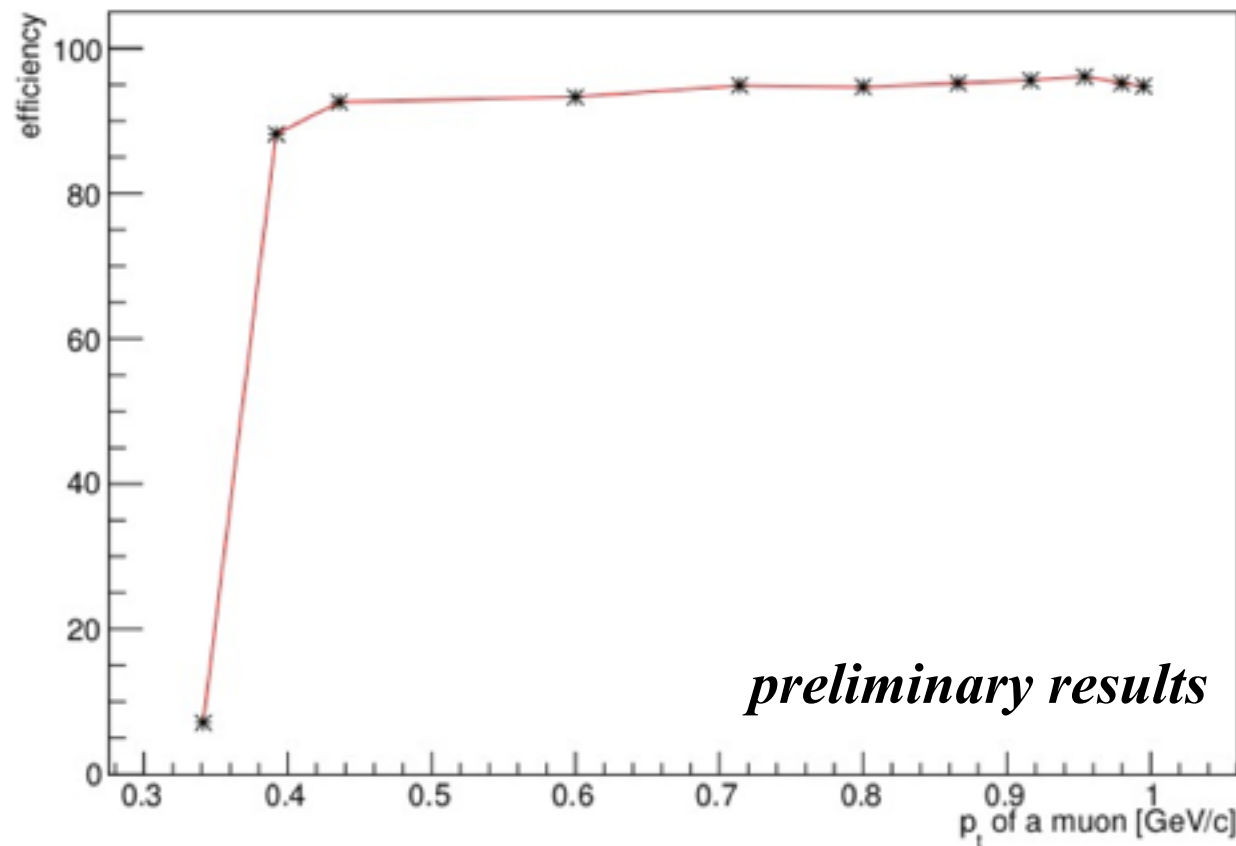
- the peak should be splitted into many packs
- worsening of the tracking efficiency





# Simulation studies (I)

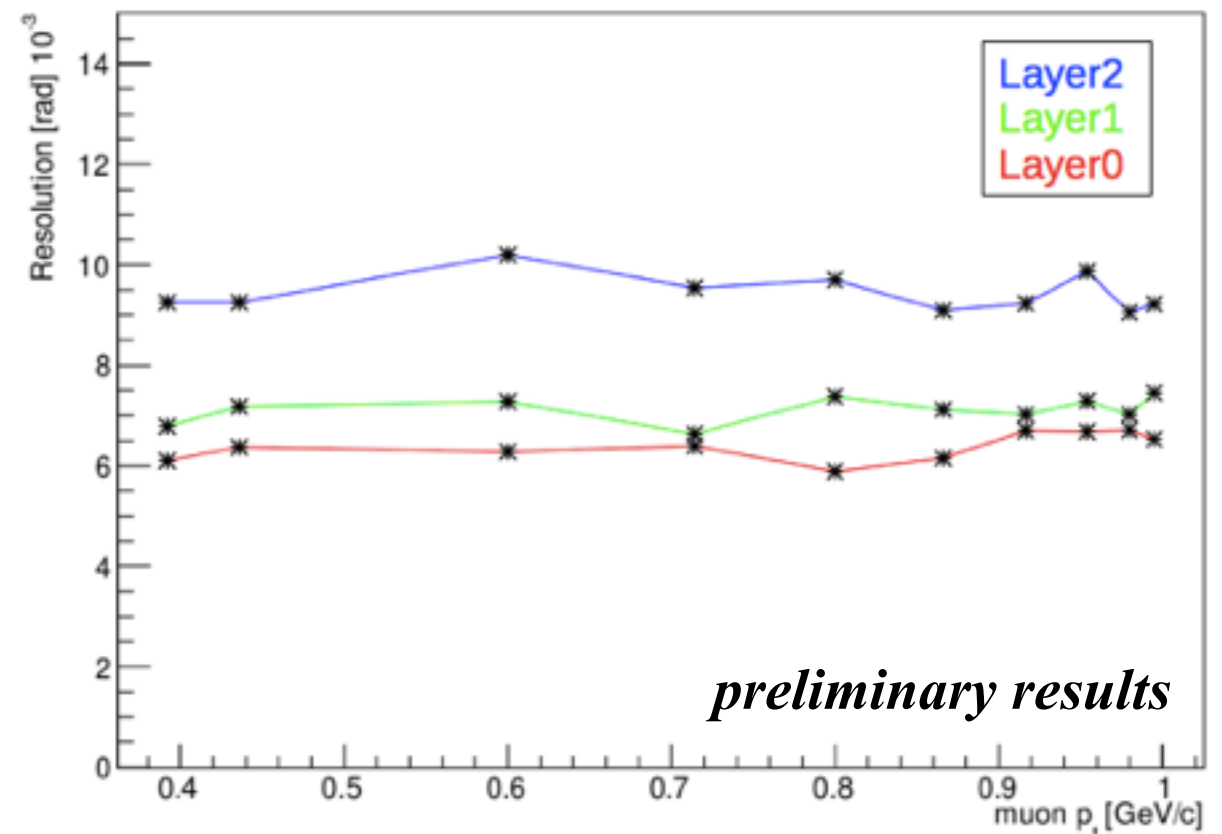
## Efficiency



- 1000 muons with fixed momentum  $p = 1 \text{ GeV}/c$
- $|\cos\theta| < 0.8$
- efficiency: number of tracks surviving the selection / total number of tracks selected

- Resolution: sigma from the gaussian fit to the distribution ( $\phi_{\text{MC-truth}} - \phi_{\text{rec-HT}}$ )

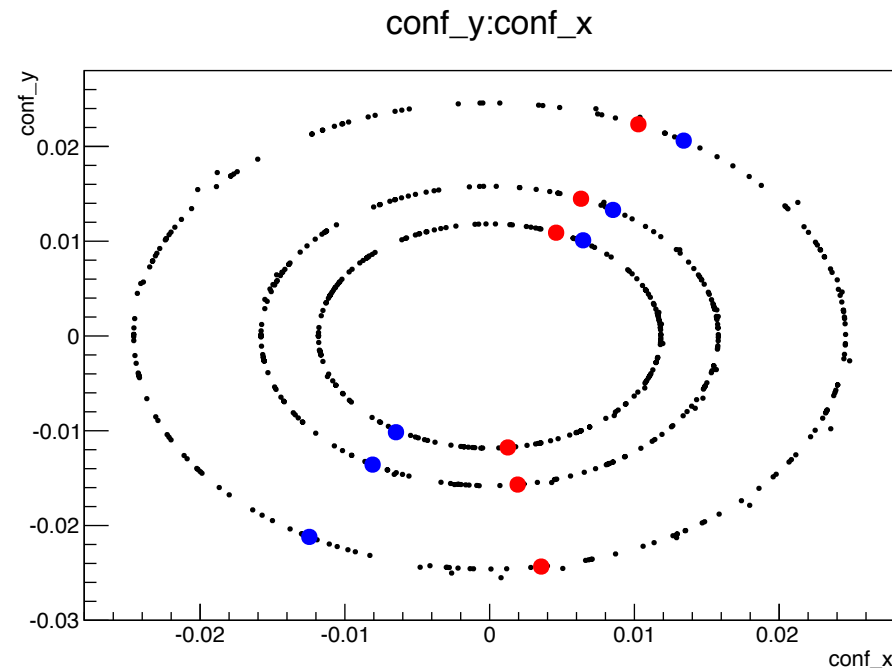
## Resolution





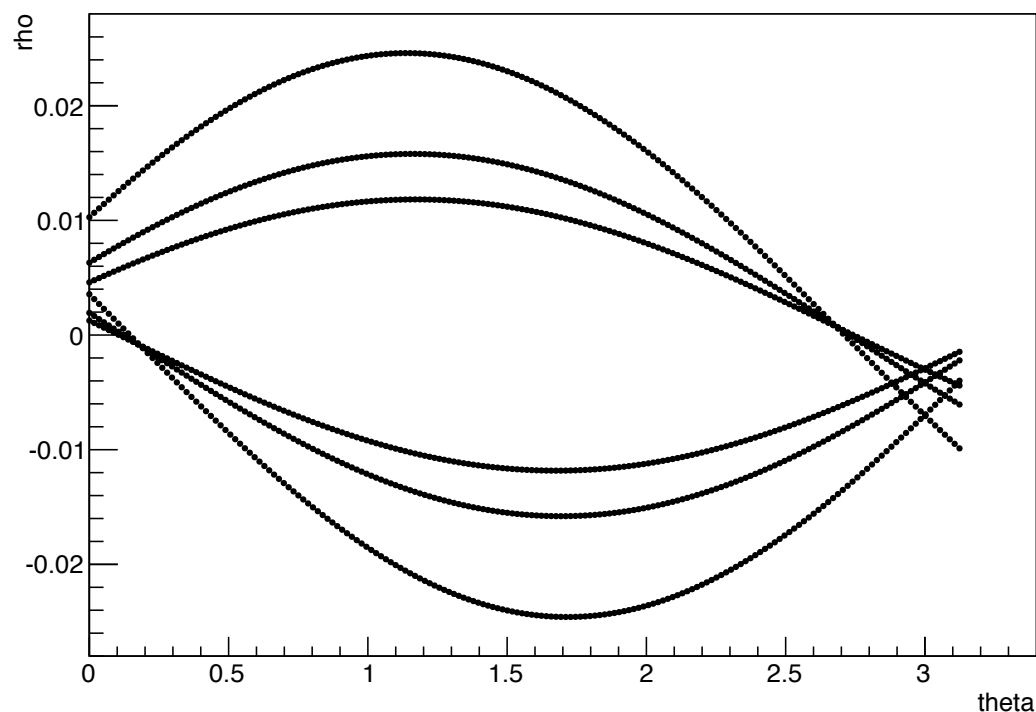
# Simulation studies (II)

- We simulate  $J/\Psi \rightarrow \rho^\pm \pi^\mp$

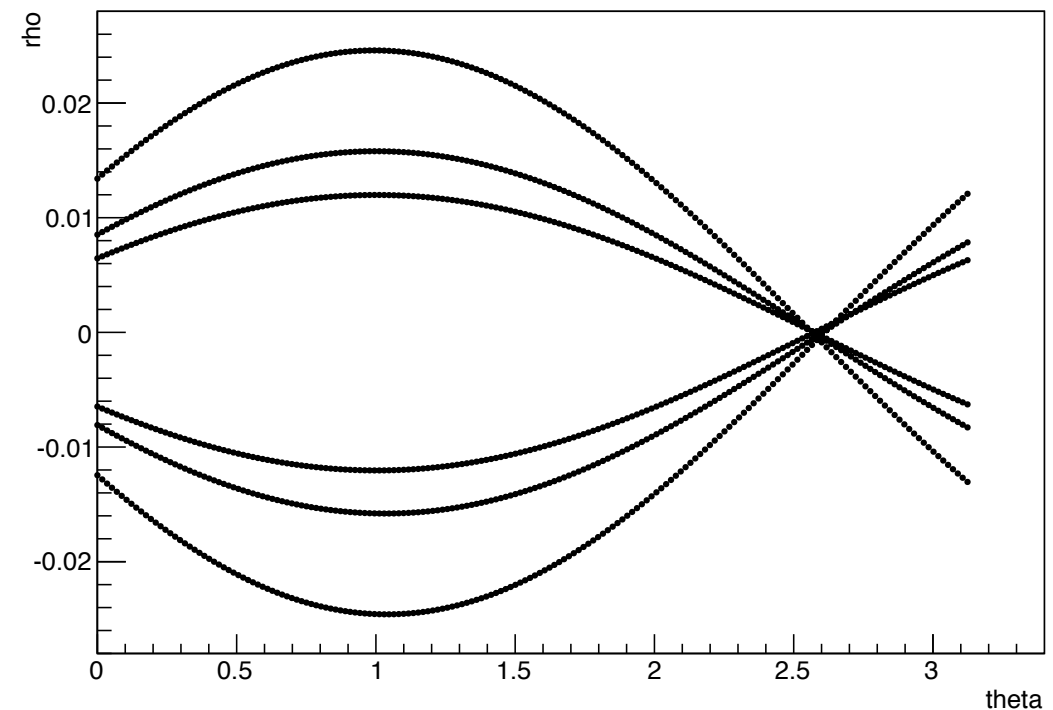


evt=99  
evt=86

rho:theta {evt==99}



rho:theta {evt==86}



We are able to discriminate the two peaks

We need additional information in order to disentangle the peaks: **slope**

# Summary and conclusion

- A first version of the Hough transformation for the CGEM-IT detector is implemented in the BESIII code and is under development
  - works well for single track simulation (no noise included)
  - discrimination of back-to-back tracks by using the slope information
- Efficiency and resolution studies are ongoing
- Future implementation
  - **Hough transformation using outer MCD point in order to increase the performances**
  - Study of physics benchmark channels, like  $\Lambda\bar{\Lambda}$  (secondary vertexes)

*Thanks for your attention*