

Theoretical Astroparticle Workshop

Contribution to PRIN 2012 - Midterm Review Workshop

*" Looking for Dark Matter in
Dwarf Spheroidal Galaxies "*



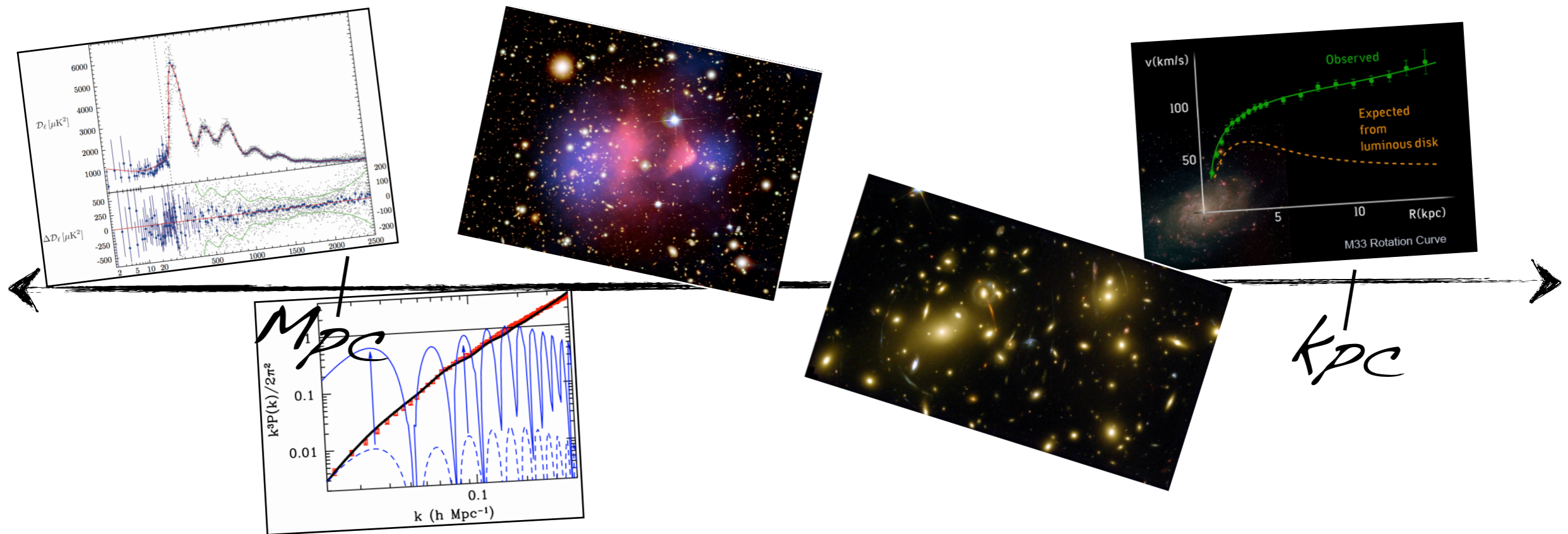
M. Valli



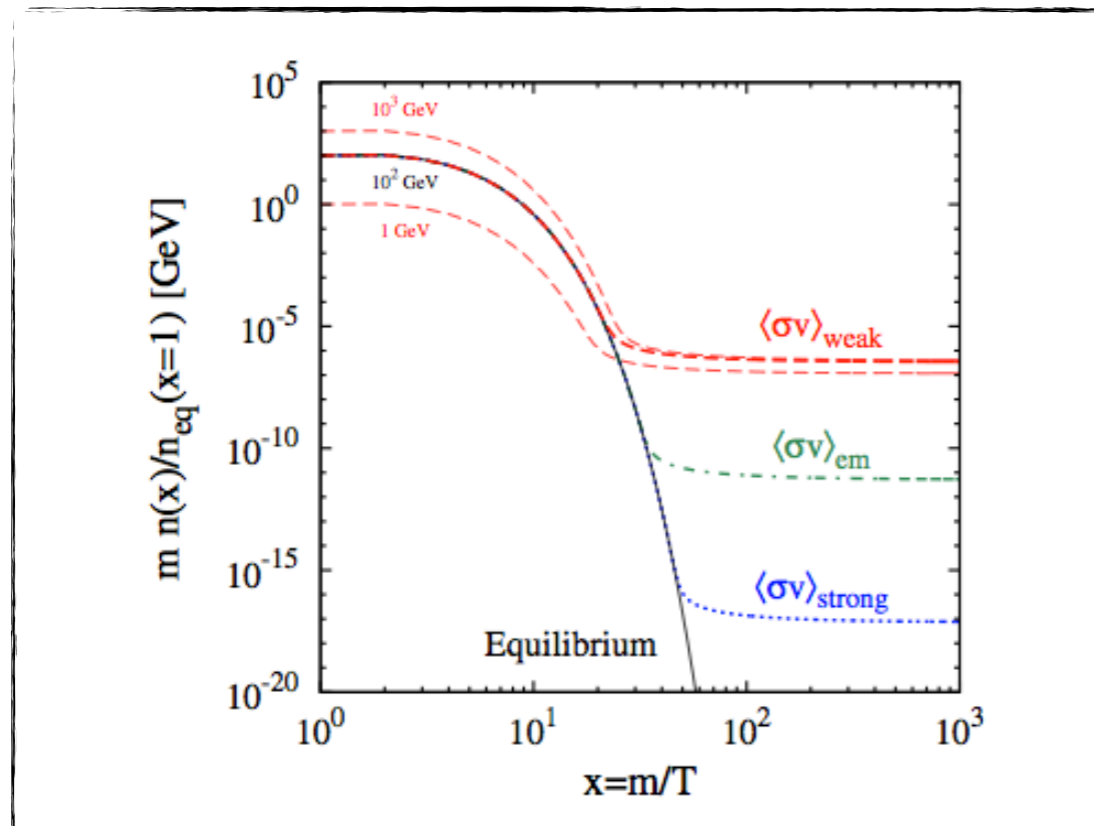
In collaboration with *Piero Ullio*

10 July 2015, University of Turin

Evidence in favour of Dark Matter existence @ different scales ...



(Steigman et al. '12)

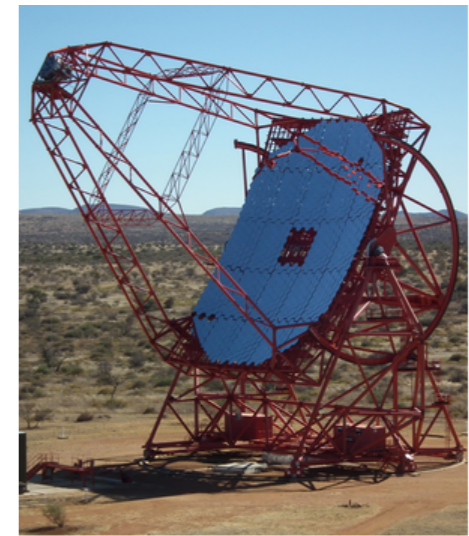
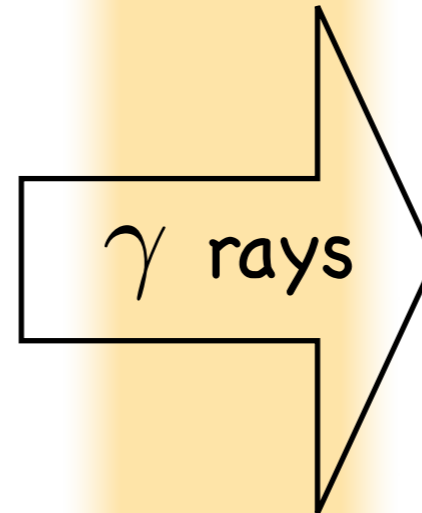
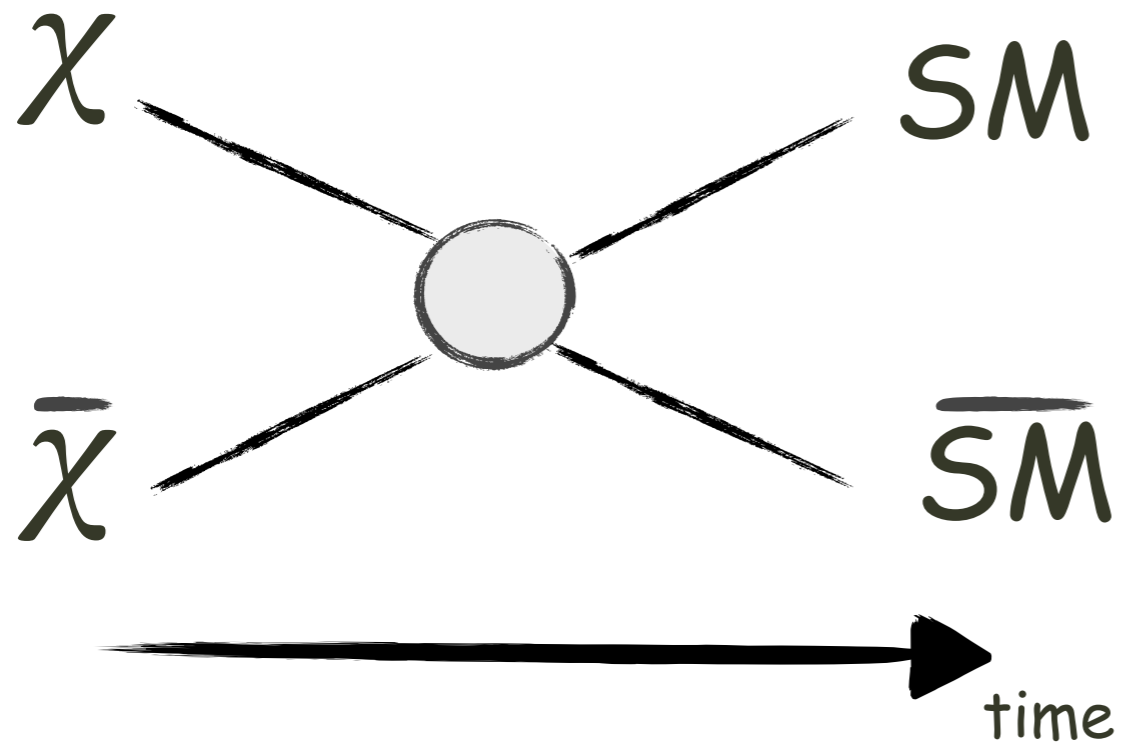


Beyond the Standard Model of Particle Physics opportunity!

$$\Omega_{\chi} h^2 \sim \frac{3 \times 10^{-27} \text{ cm}^3 \text{ s}^{-1}}{\langle \sigma v \rangle_{f.o.}}$$

W eakly I nteracting M assive P articles miracle

WIMP annihilation in the Sky



Expected flux of prompt gamma to be detected ?

$$\phi_{\gamma} \propto \langle \sigma v \rangle \times J \rightarrow \sim \int dl \rho_{\chi}^2(r(l)) / m_{\chi}^2$$

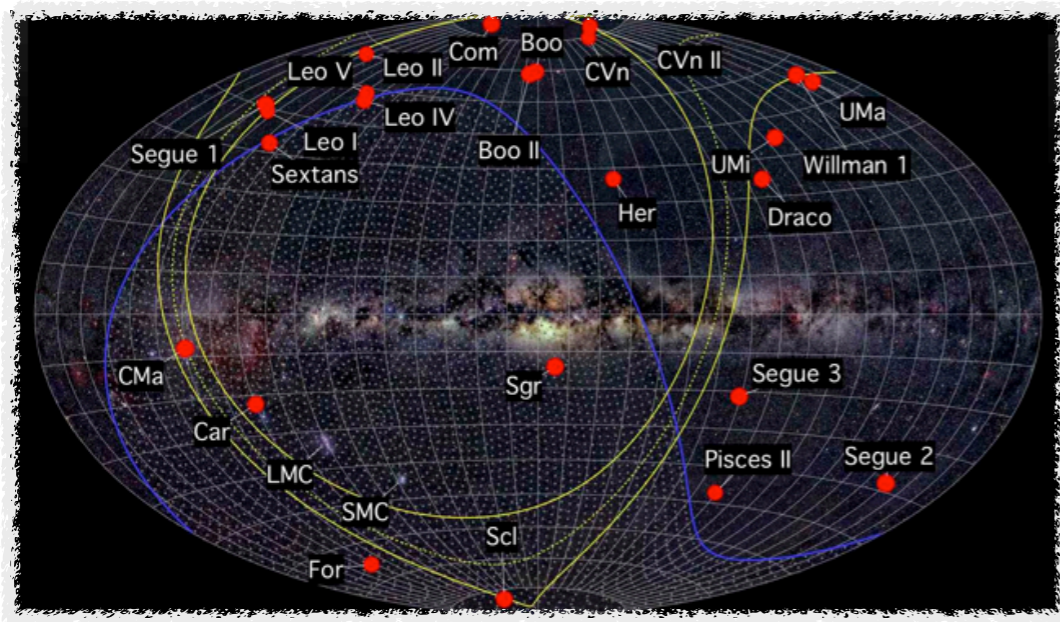
Milky Way (MW) Galactic Center: $J \sim 10^{23} \text{ GeV}^2/\text{cm}^5$
 high J-factor value, but also complicated background!

Dwarf spheroidal galaxies (dSphs) are the ideal targets!

$$\frac{M}{L} \sim 10^{2-3} \times \frac{M_{\odot}}{L_{\odot}}$$

very faint objects with large mass-to-light ratio!

In particular, for Milky Way satellites:



high latitude position
suppressed gamma-ray flux
from standard processes

heliocentric distances
about 70 - 250 kpc

high
J-value

- ✓ photometry for stellar density profile , $I(R)$
- ✓ spectroscopy for line-of-sight kinematics , $\sigma_{los}(R)$
- ✗ full 3D kinematical knowledge , $\beta(r) \equiv 1 - \sigma_t^2(r)/\sigma_r^2(r)$

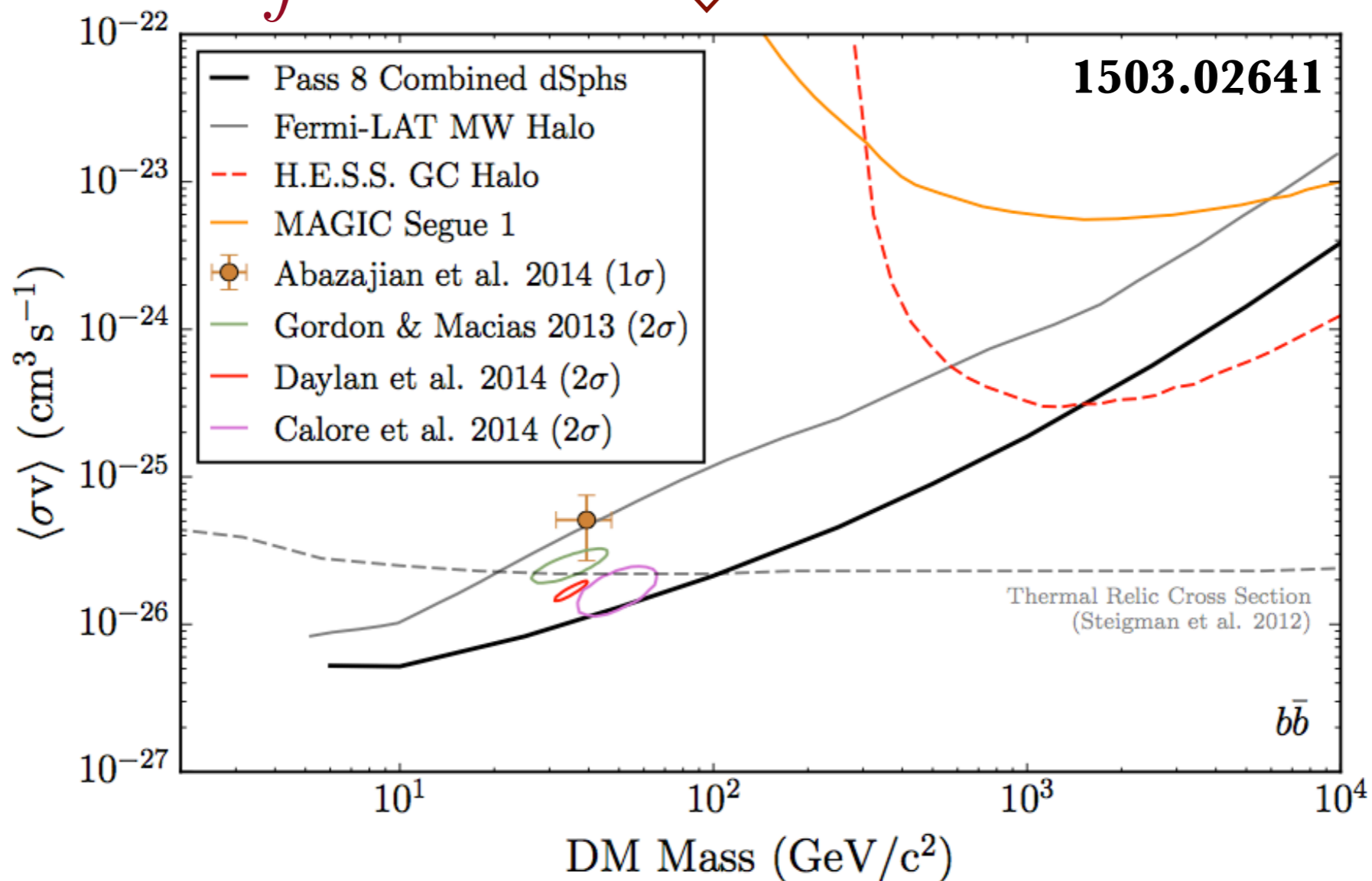
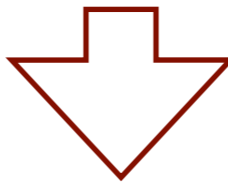
dSph \equiv collisionless spherical system in dynamical equilibrium

JEANS
EQUATION



$$\sigma_{los}(R) = f(I, \rho_\chi, \beta)$$

$$\int d\beta p(\beta)$$



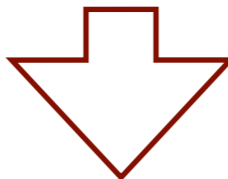
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JEANS EQUATION



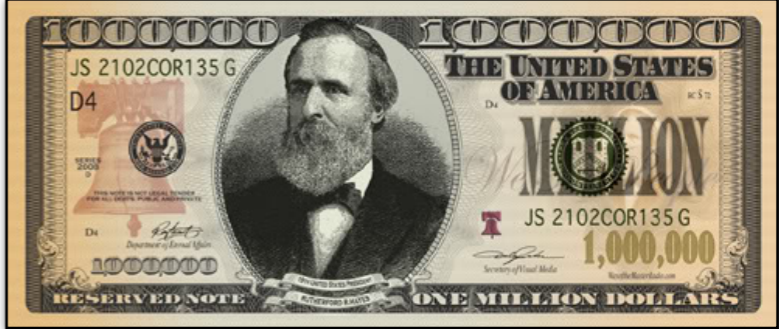
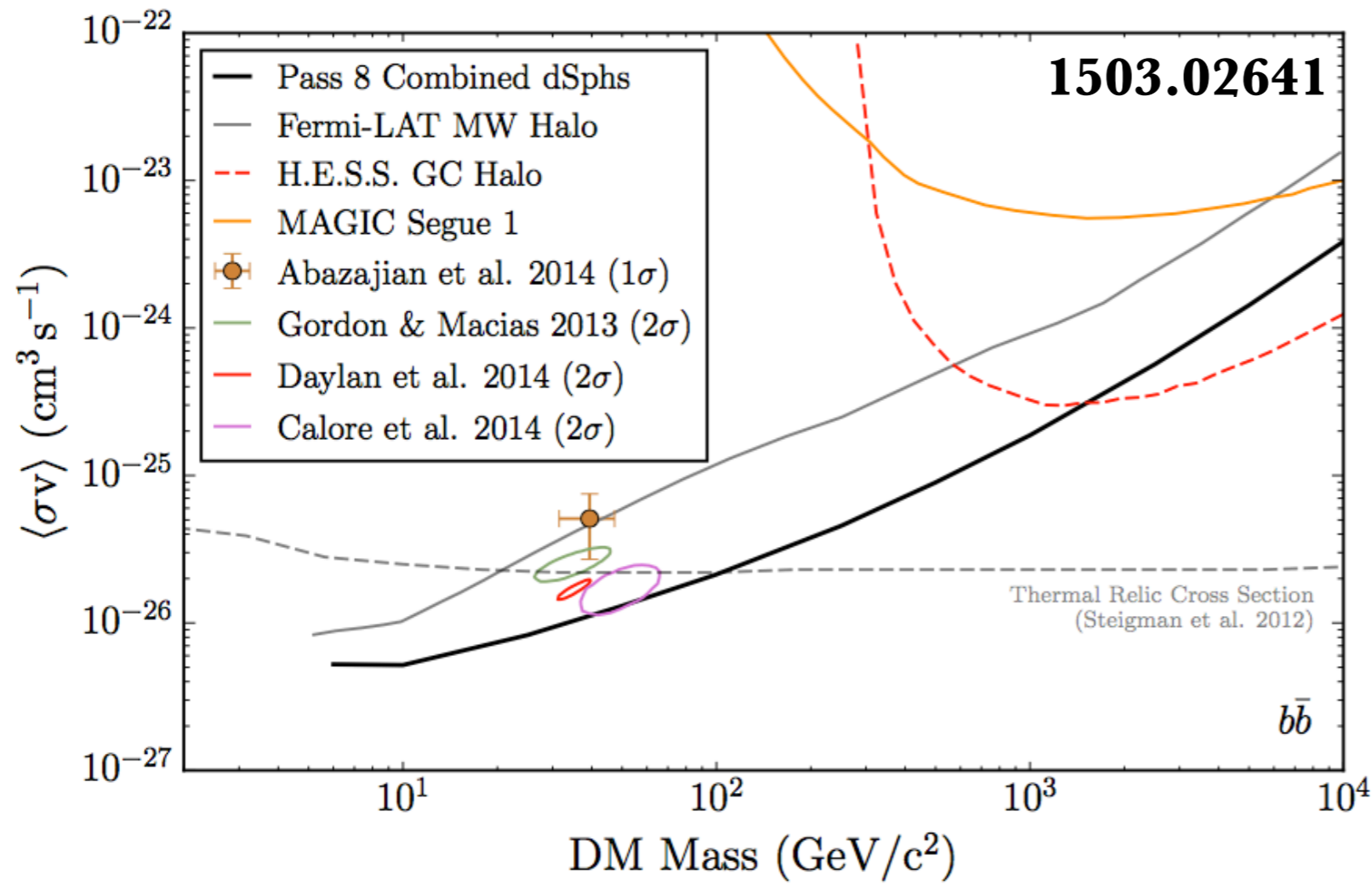
$$\sigma_{los}(R) = f(I, \rho_\chi, \beta)$$

$$\int d\beta p(\beta)$$



$$-\infty < \beta(r) \leq 1$$

1 Million Dollar Question



How do you marginalize on something you do not know?

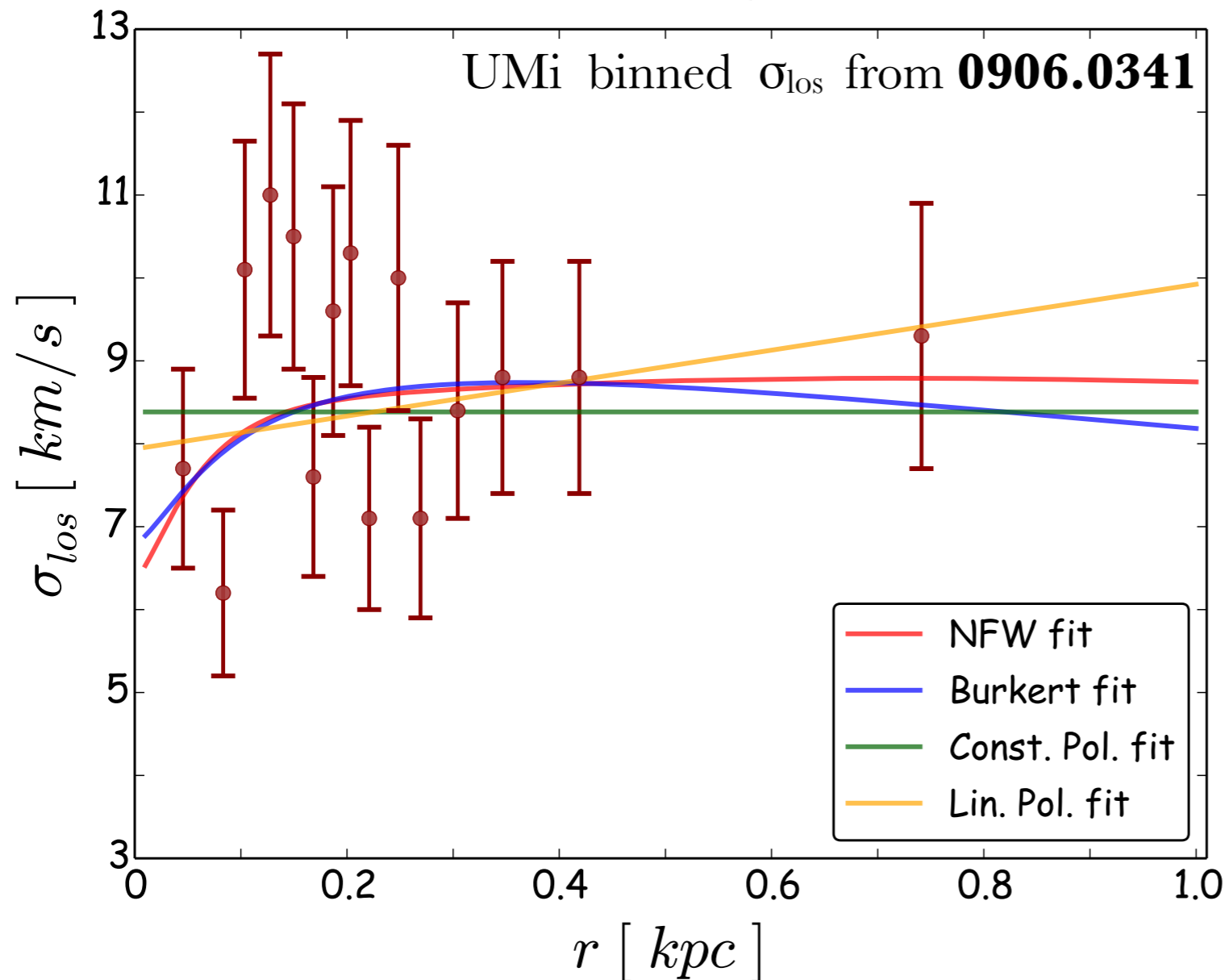
**OUR NOVEL
APPROACH**

to attack the problem in a different way
it may be worth inverting standard logic!

Jeans Inversion

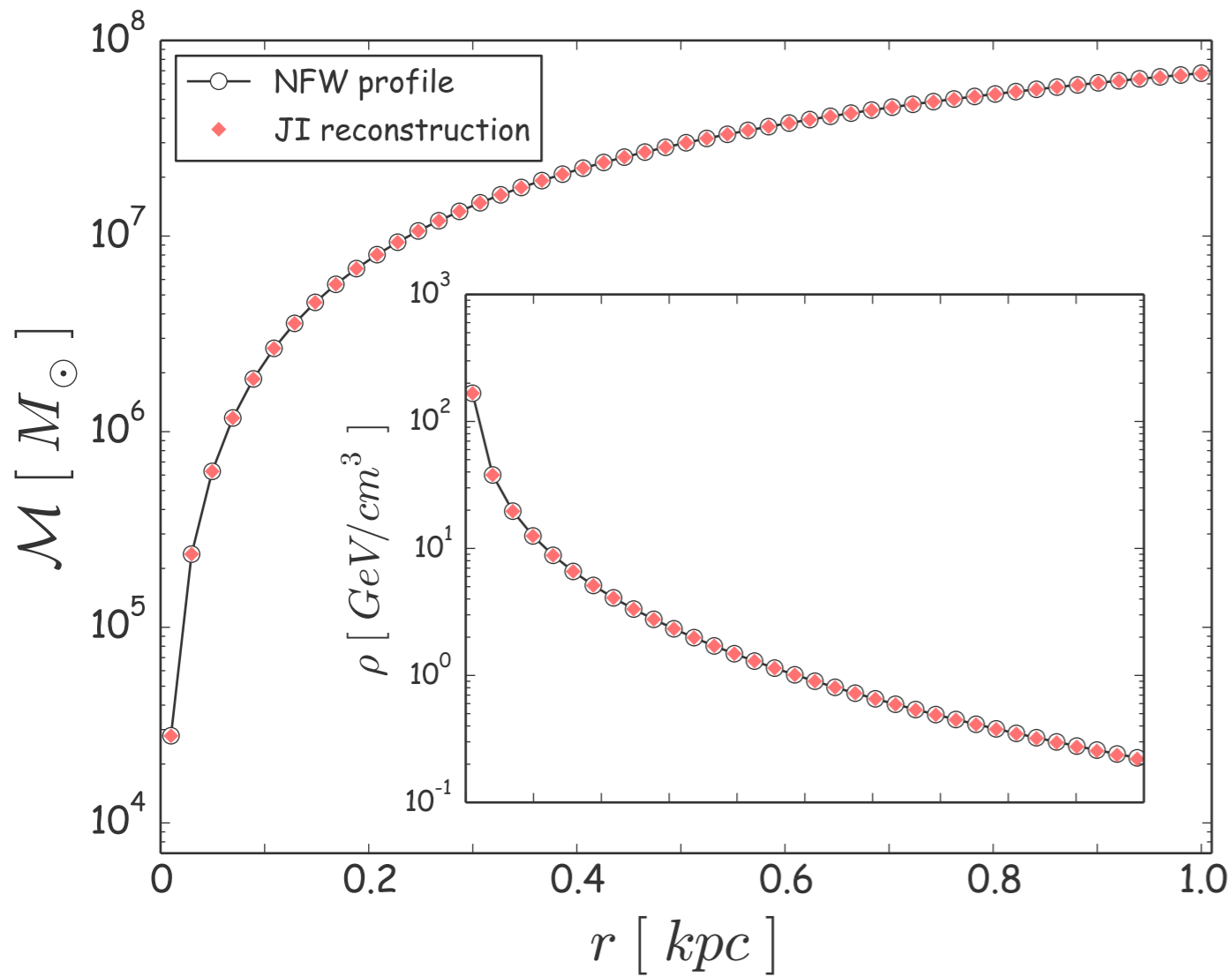
$$\sigma_{los}(R) = f(I, \rho_x, \beta)$$

$$\mathcal{M}_\beta(r) = \mathcal{F}(\sigma_{los}, I, \beta)$$



FOR A GIVEN FIT
OF LINE-OF-SIGHT
DISPERSION DATA
ONE GETS ACCESS TO
A MASS PROFILE
IN TERMS OF $\beta(r)$

**WE BREAK
MASS-ANISOTROPY
DEGENERACY!**



The inversion works pretty well also for the halo density.

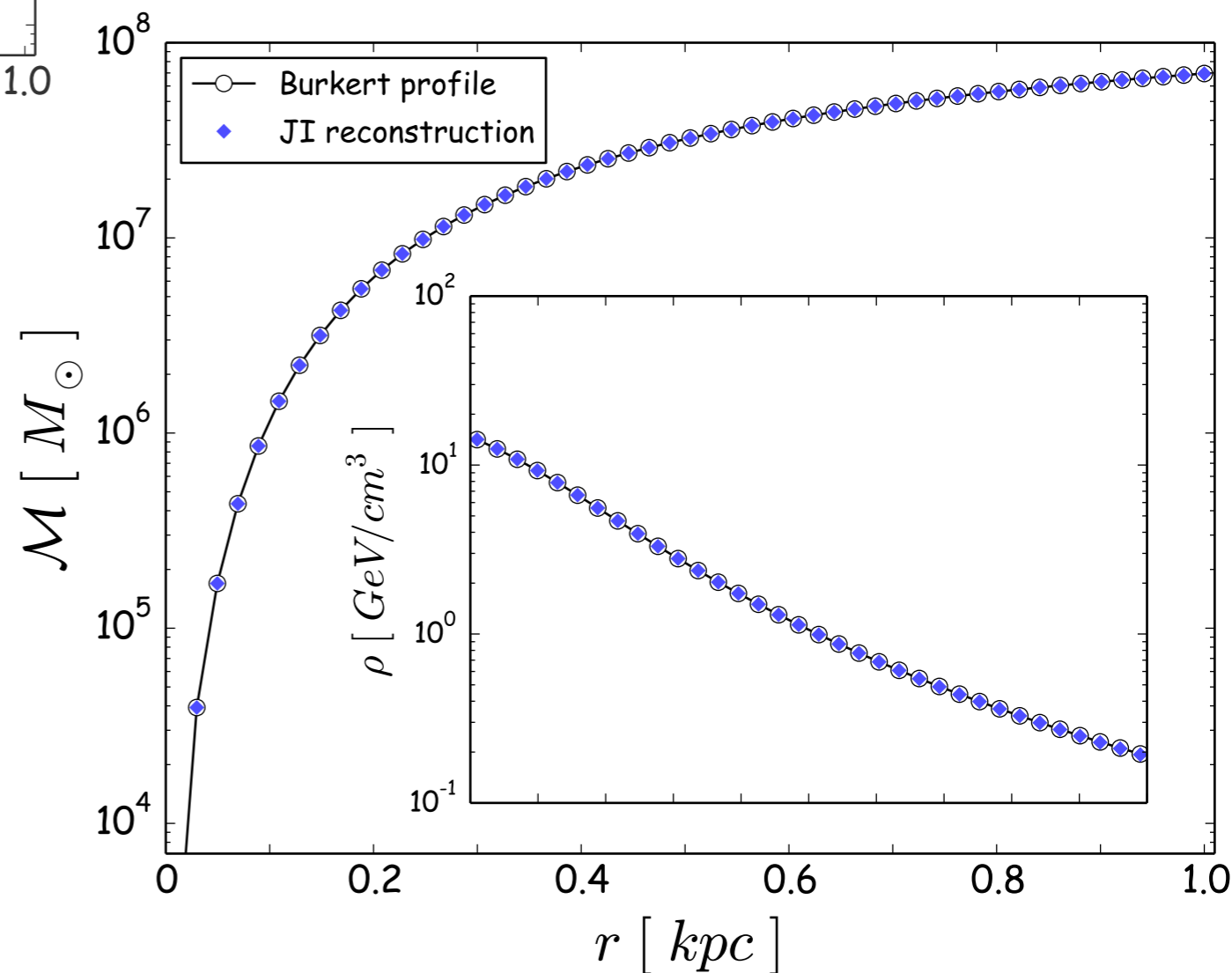
$$\rho_{\chi\beta} = \frac{1}{4\pi r^2} \frac{d\mathcal{M}_{\beta}}{dr}$$

The general expression for Jeans inversion is of the form

$$\mathcal{M}_{\beta} = \mathcal{A}_{\beta}(I) \int_r^{\infty} dR \frac{d^2 P}{(dR^2)^2} W_{\beta}(R, r)$$

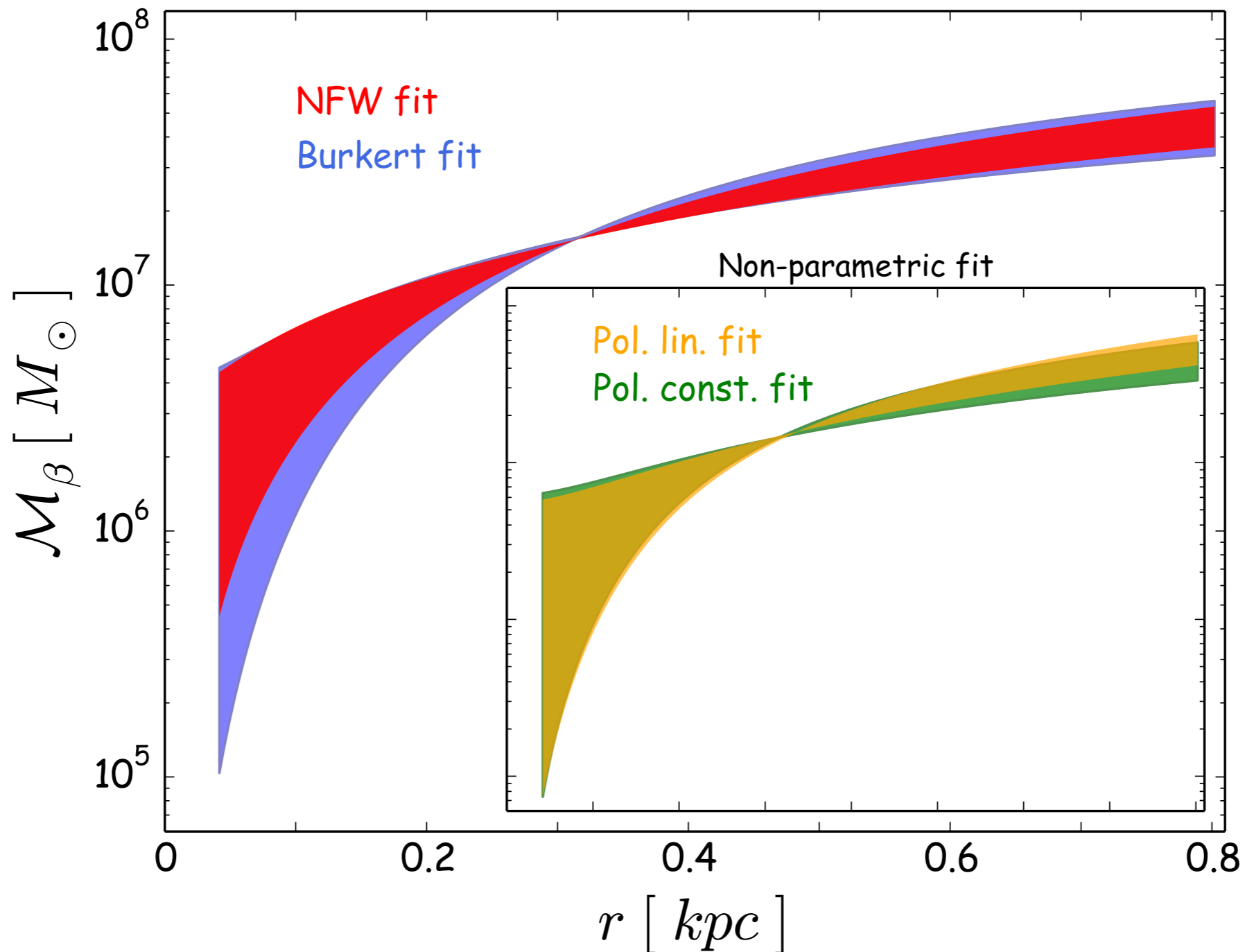
where the pressure P is defined as

$$P = I \sigma_{los}^2$$



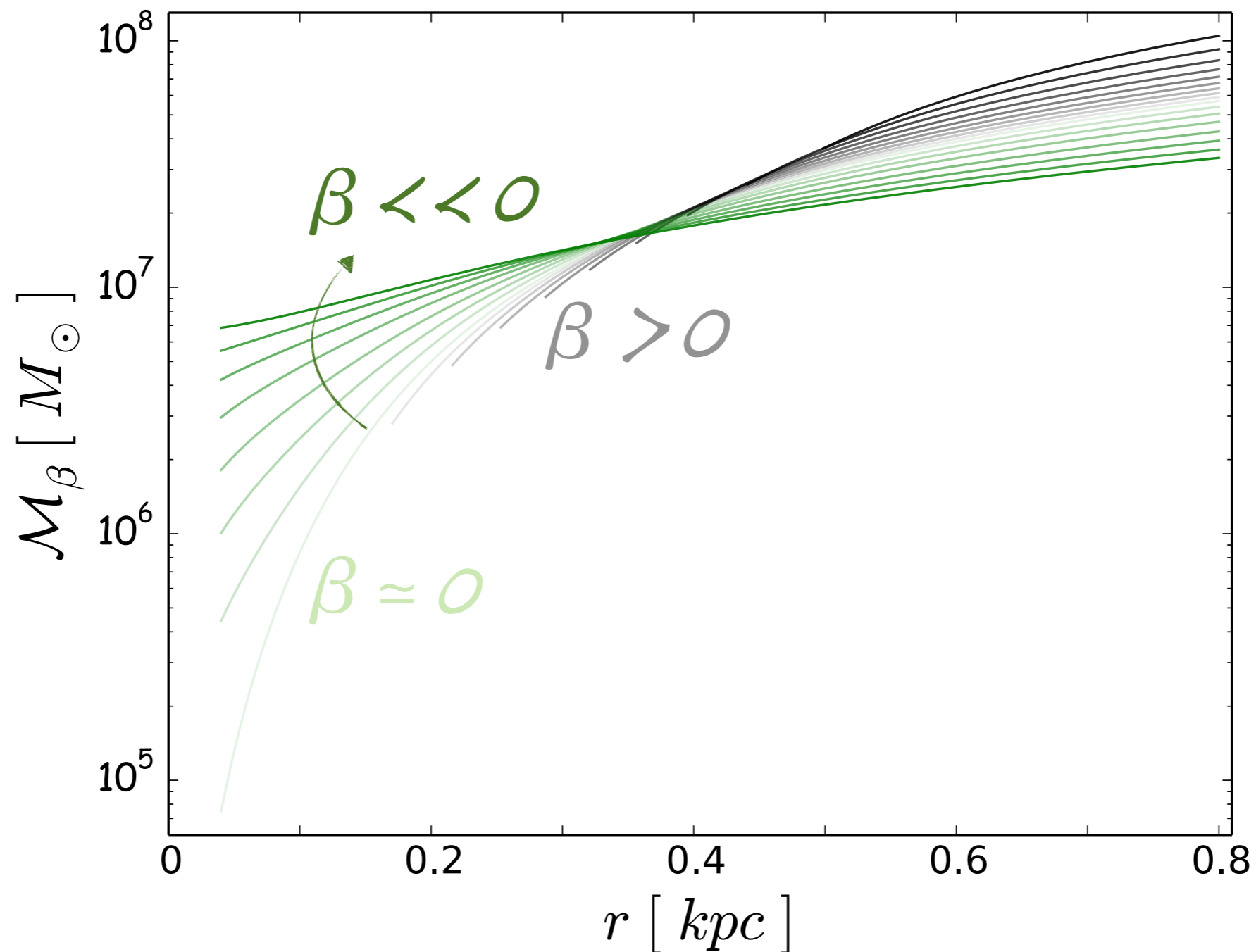
Let's get started with the simplest case: $\beta(r) = \text{const}$

- $\forall \beta \in (-\infty, 1] :$
- 1) $\mathcal{M}_\beta > 0$
 - 2) $\mathcal{M}_\beta(r') - \mathcal{M}_\beta(r) \geq 0$ if $r' \geq r$



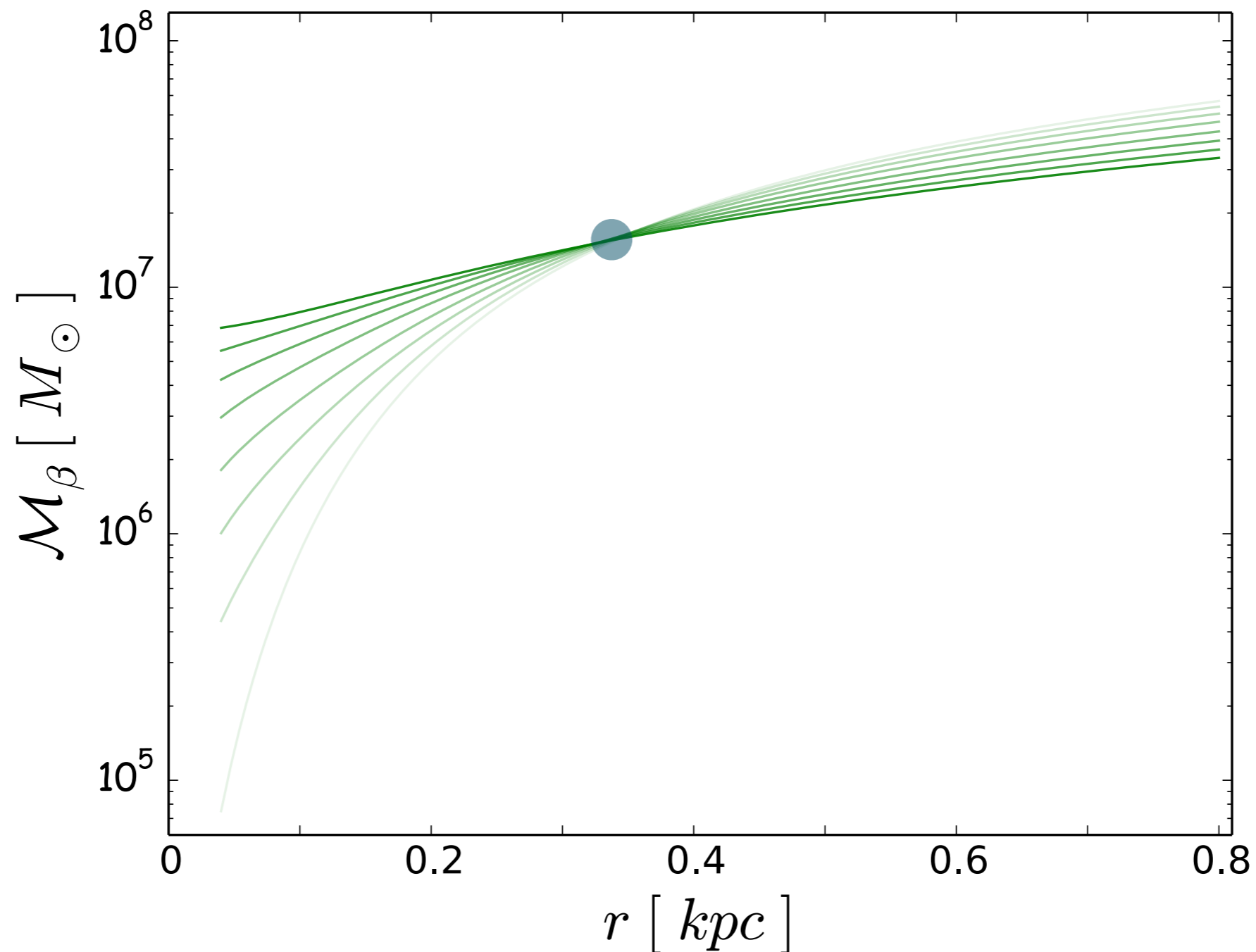
Fitting σ_{los} data with a constant fit yields an analytic expression in the case of constant orbital anisotropy within our Jeans inversion approach.

Taking a closer look @ this case :



Fitting σ_{los} data with a constant fit yields an analytic expression in the case of constant orbital anisotropy within our Jeans inversion approach.

We hit a special point where the dependence on the orbital anisotropy is minimized

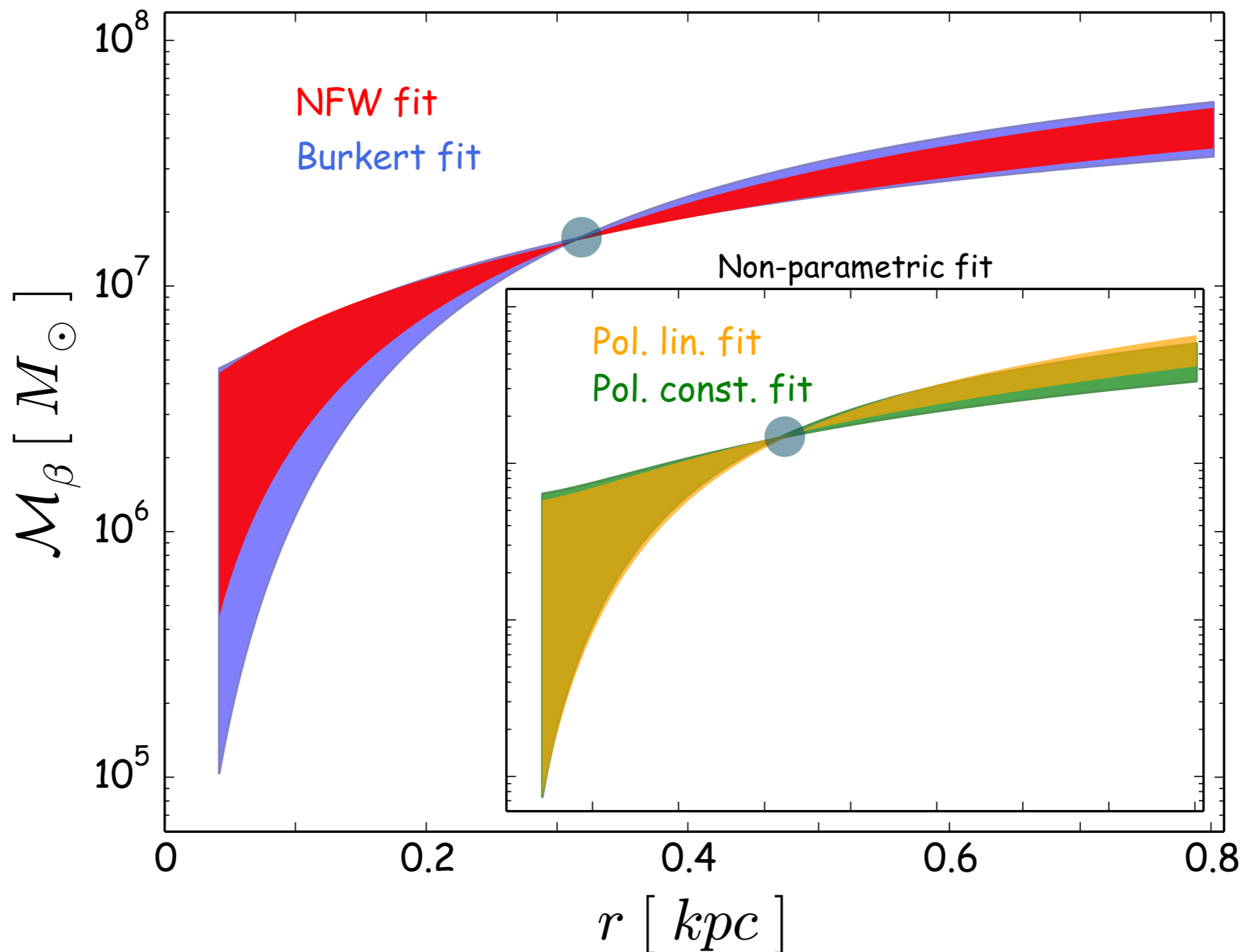


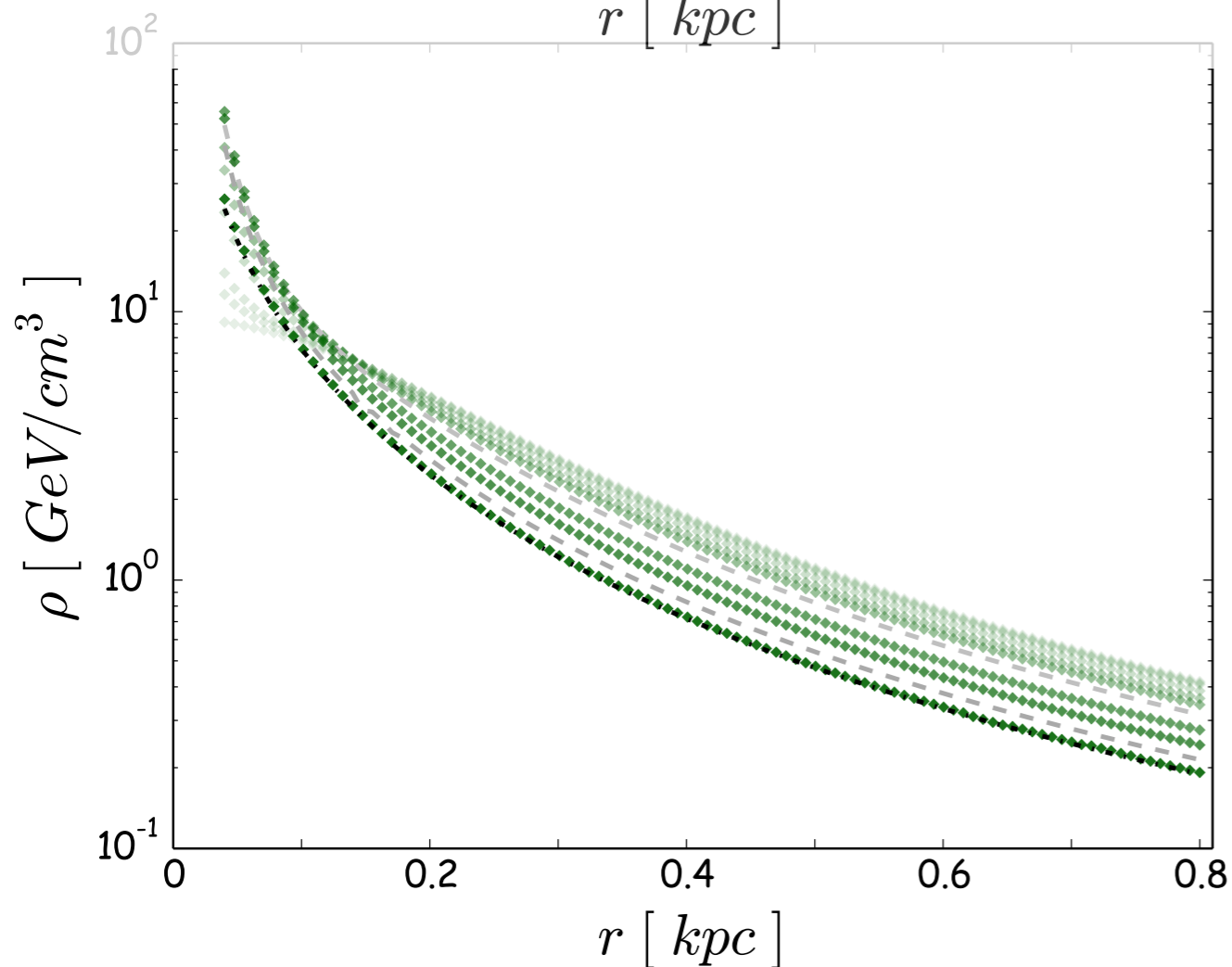
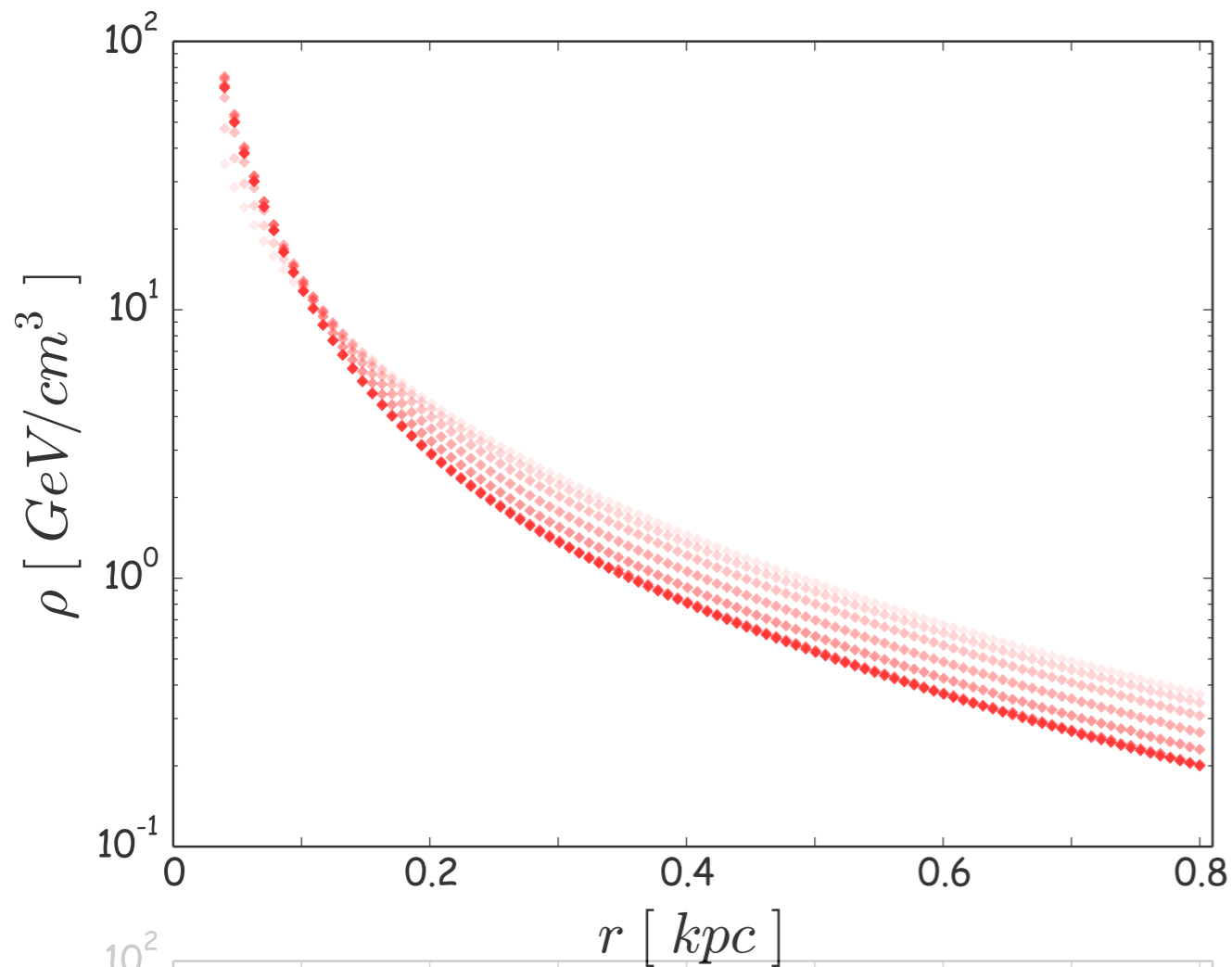
We give a proof of existence for a good (but not exact) mass estimator

(see e.g. **0908.2995**)

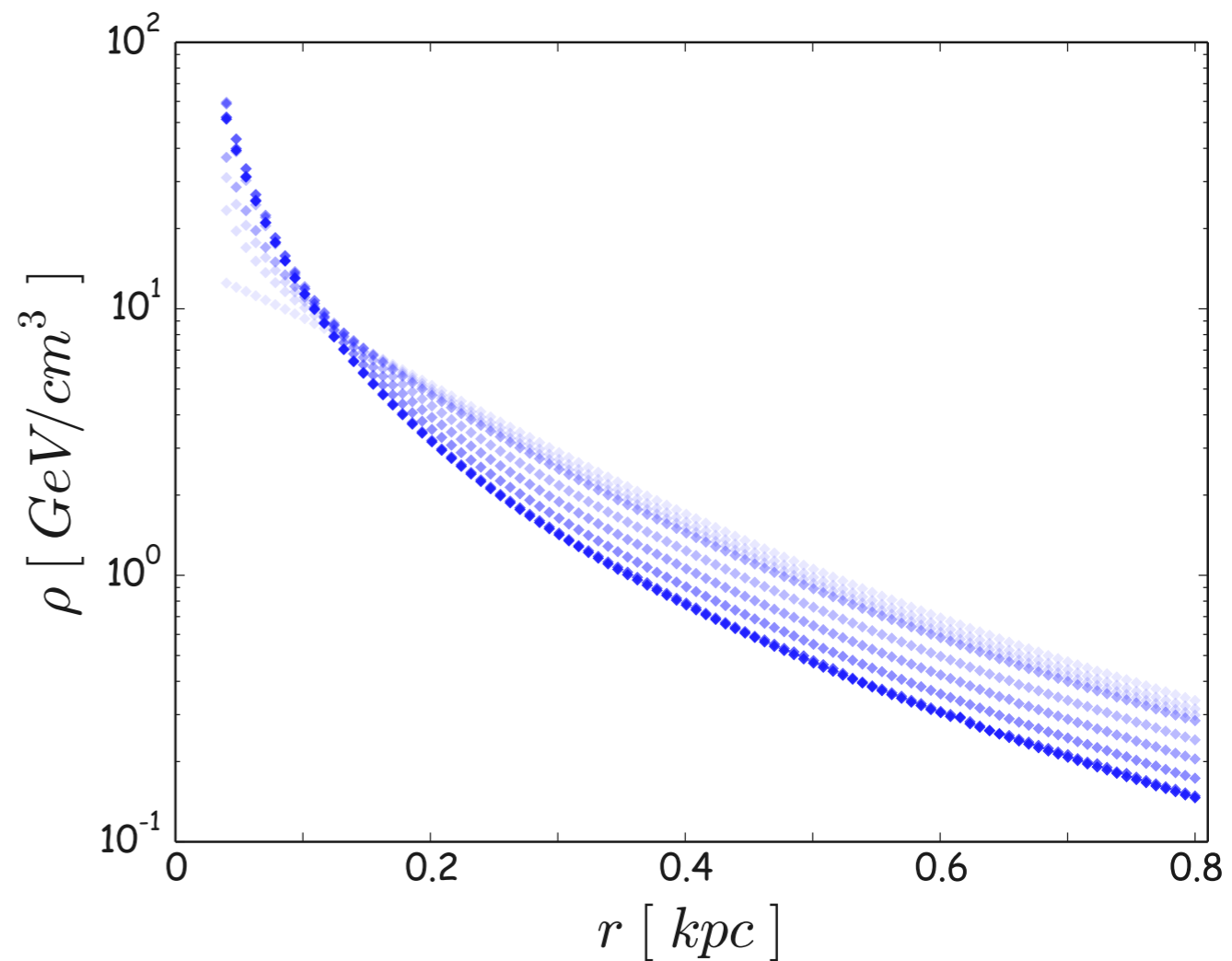
$$\mathcal{R}_{\bar{\beta}} \equiv 1 - \mathcal{M}_{\bar{\beta}} / \mathcal{M}_0 \longrightarrow \mathcal{R}_{\bar{\beta}}(r_{\star}) = 0, \quad r_{\star} = r_{\star \bar{\beta}}$$

$r_{\star} \cong r_{1/2}$
mild dependence
on β (% effect)





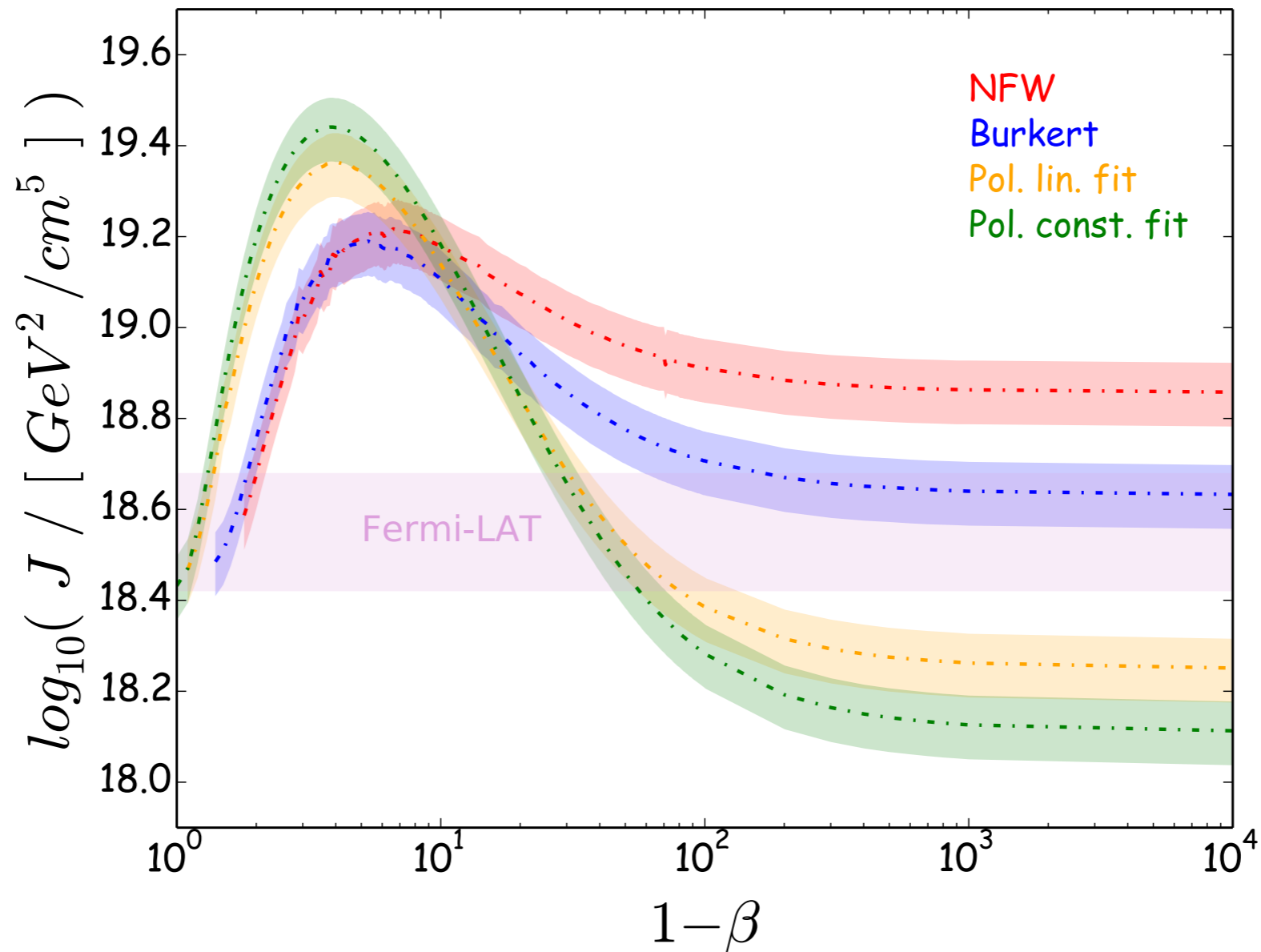
Negative anisotropy seems to require cuspier profiles.



$M_{1/2}$ constraint turns out to be slightly milder.

The halo density here can "shift down" a bit!

The integration of ρ^2_x along the line-of-sight yields the J-factor.



1.

In all the 4 cases, "J-sampling" is largely dominated by very negative orbital anisotropies.

2.

At face value, the minimum of J in parametric fits seems to agree with previous findings.

The non-parametric ones point to a few % of difference only.

Final Remarks

dSph galaxies represent a unique Dark Matter laboratory
(both for Indirect Searches as well as for N-body simulations)

They can confirm/falsify the Dark Matter
interpretation of the GeV excess @ the GC

In this work we actually probed the robustness of the
current tight upper-bound on $\langle \sigma v \rangle$ against what can be
considered the greatest theoretical bias in the modelling.

One last effort to get deeper physical insights on the orbital anisotropy

dSph constraints turned out to be quite solid ...
... maybe the milestone of Indirect Searches!

Thank You!

