

PRIN 2012
Theoretical astroparticle physics

Phenomenology of ν masses and mixings (Bari Unit)



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Research activity - Bari group

- **Phenomenology of neutrino oscillations and mass hierarchy**
- **Neutrinoless double beta decay**
- **Collective effects in supernova neutrinos**

Neutrino oscillations

In the 3ν framework, the mixing matrix U is:

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U^* \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

where $c_{ij} = \cos\theta_{ij}$ and $s_{ij} = \sin\theta_{ij}$

3 mixing angles

$\theta_{12}, \theta_{13}, \theta_{23}$

1 phase δ

(CPV for $\delta \neq 0, \pi$)

Oscillations depend on mass differences. Assuming $m_2 > m_1$:

$$\delta m^2 = m_2^2 - m_1^2 > 0 \ll \Delta m^2 = m_3^2 - \frac{m_2^2 + m_1^2}{2}$$

“SOLAR”

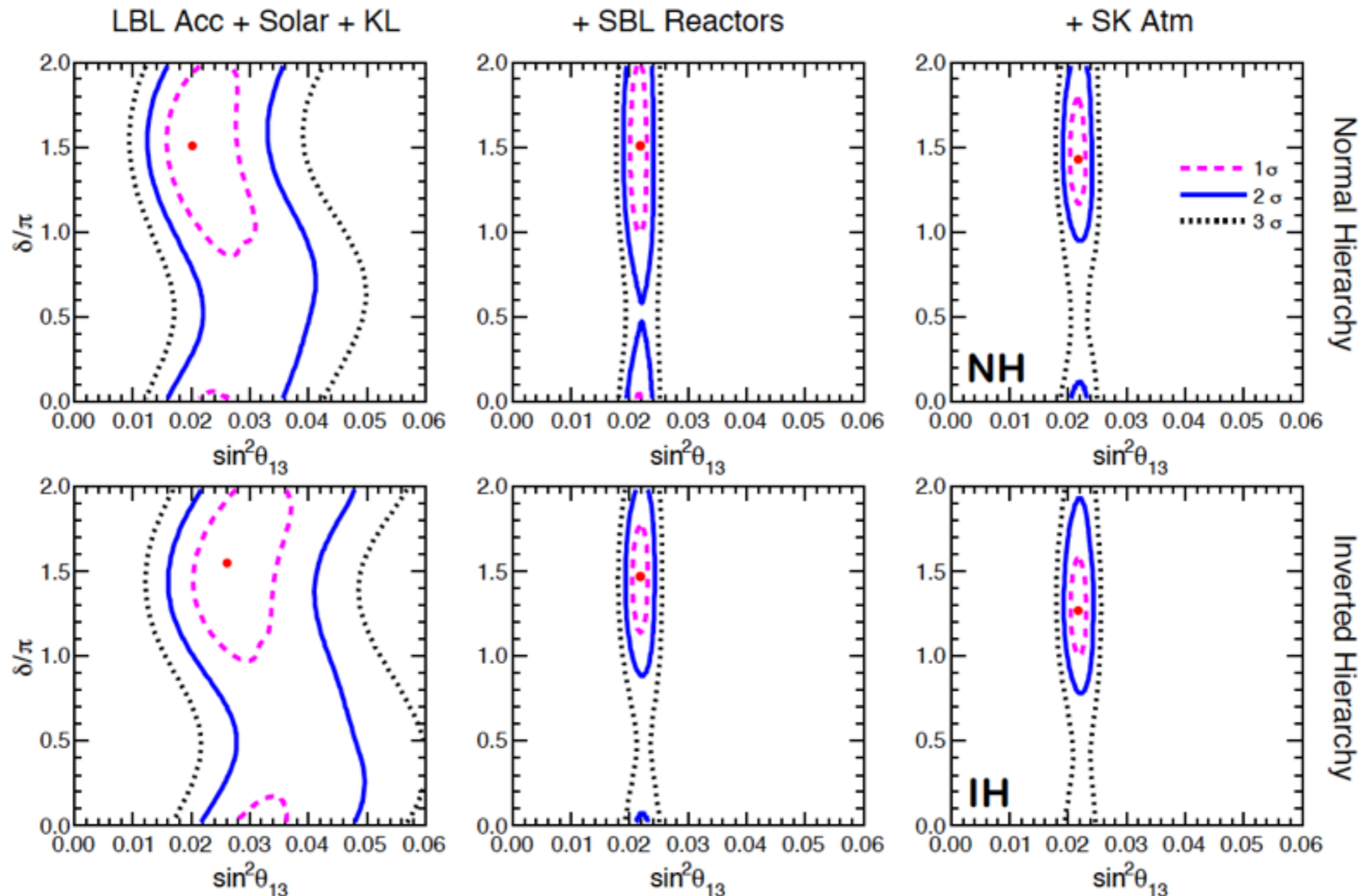
“ATMOSPHERIC”

If $\Delta m^2 > 0$ we are in **NORMAL HIERARCHY**

If $\Delta m^2 < 0$ we are in **INVERTED HIERARCHY**

Global analysis

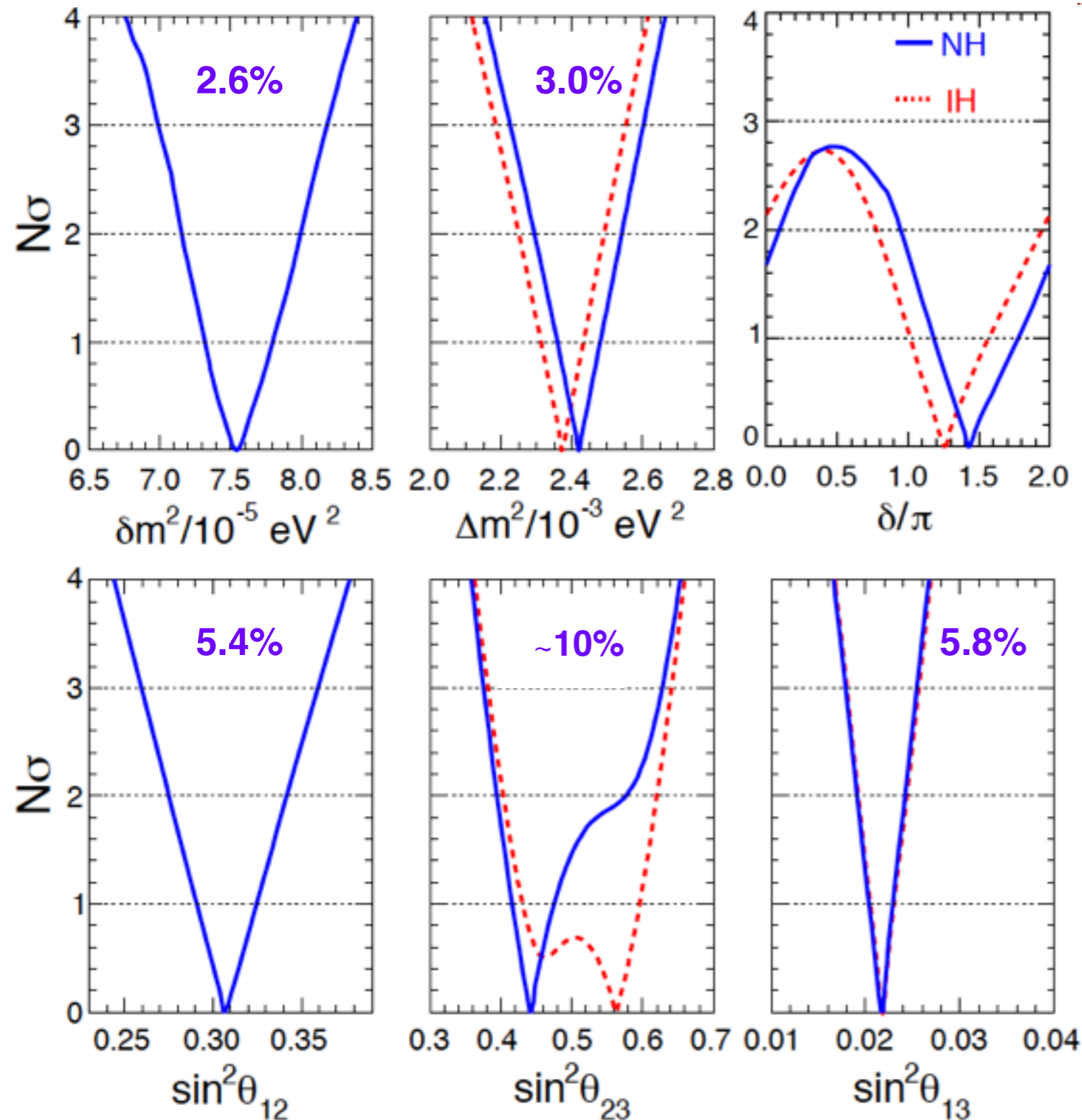
(based on arXiv:1312.2878, F. Capozzi, G. L. Fogli, E. Lisi, A. Marrone, D. Montanino, A. Palazzo)



For the relatively “low” value $\sin^2\theta_{13}\sim 0.02$ preferred by SBL reactors (and Solar + KL) data, the appearance signal in T2K is maximized by CP violating $\delta\approx 1.5\pi$. SK Atm lowers a bit this value.

Global analysis

(based on arXiv:1312.2878, F. Capozzi, G. L. Fogli, E. Lisi, A. Marrone, D. Montanino, A. Palazzo)



- Preference for CP violating $\delta \sim 1.4\pi$ and $\sin\delta < 0$.

- Preference for non-maximal θ_{23} (octant instability).

- $\chi^2_{\min}(\text{NH}) - \chi^2_{\min}(\text{IH}) = -0.3$.
No hierarchy information yet.

Mass hierarchy from atmospheric ν (PINGU)

(based on arXiv:1503.01999, F. Capozzi, E. Lisi, A. Marrone)

Mass hierarchy from matter effects in Earth core and mantle (NH for ν_e IH for $\bar{\nu}$): $\theta_{13}(\text{matter}) \gg \theta_{13}(\text{vacuum})$.

PINGU measures ν_α spectrum ($\alpha=e,\mu$) which depends on E (energy) and θ (zenith angle)

Osc. independent

$$N_{ij}^\alpha(E_\nu, \theta) = \underbrace{V_{\text{eff}}^\alpha(E_\nu)}_{\text{volume}} \otimes \underbrace{\sigma(E_\nu)}_{\text{cross sec.}} \otimes \underbrace{\Phi^\alpha(E_\nu, \theta)}_{\text{flux}} \otimes \underbrace{P^\alpha(E_\nu, \theta)}_{\text{Osc. prob.}} \otimes \underbrace{R^\alpha(E_\nu, \theta)}_{\text{Res. function (gaussian)}}$$

CHALLENGES

Can't distinguish ν and $\bar{\nu}$
($\sigma_\nu \neq \sigma_{\bar{\nu}}$)

Spectral shape systematics

Not perfect resolution on E, θ

Mass hierarchy from atmospheric ν (PINGU)

(based on arXiv:1503.01999, F. Capozzi, E. Lisi, A. Marrone)

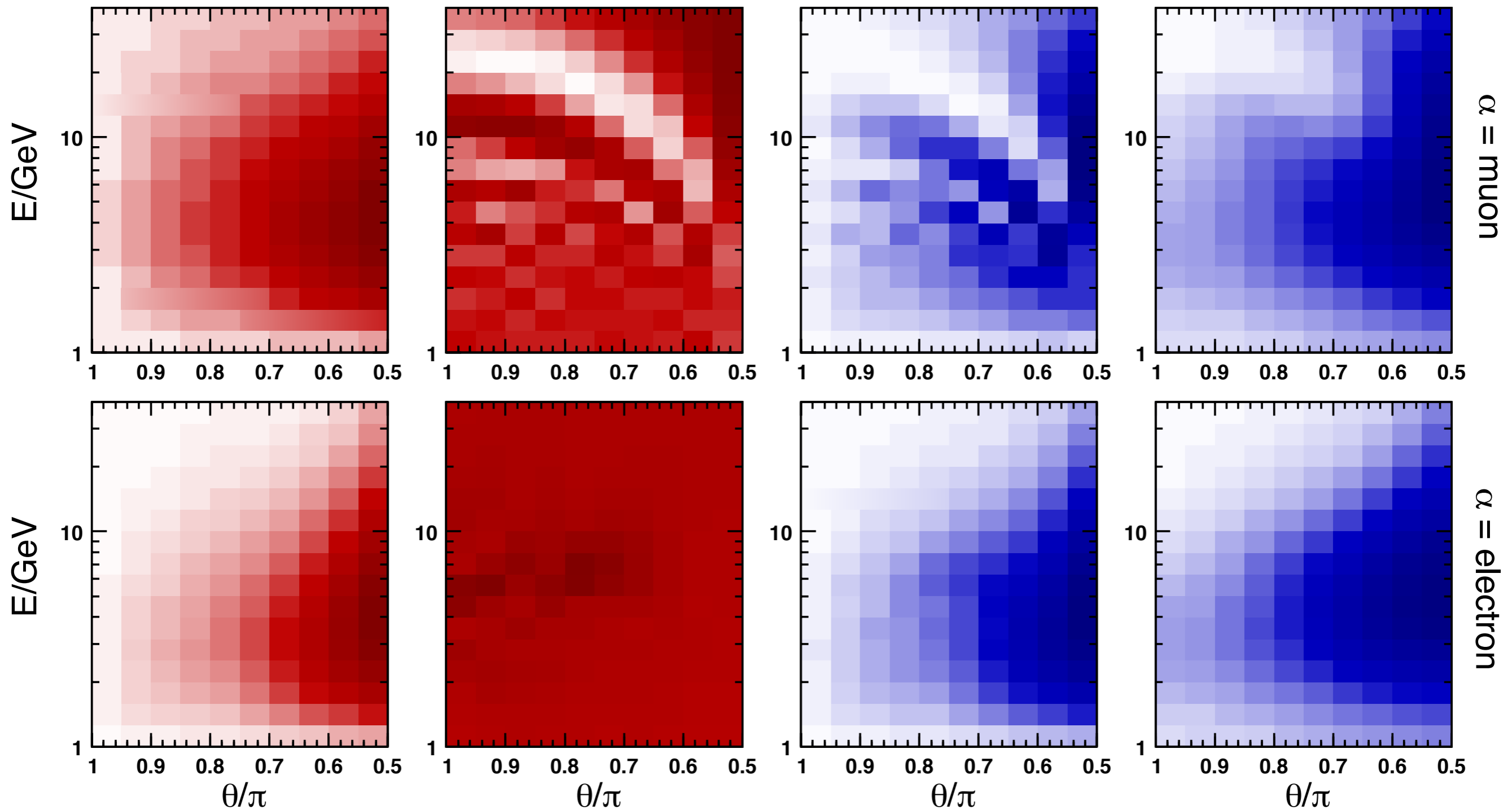
Normal hierarchy

V_{eff}^α Φ^α $\sigma_{\text{CC}}^\alpha$

P_{NH}^α ($s_{23}^2=0.5$)

N_{NH}^α (unsmearred)

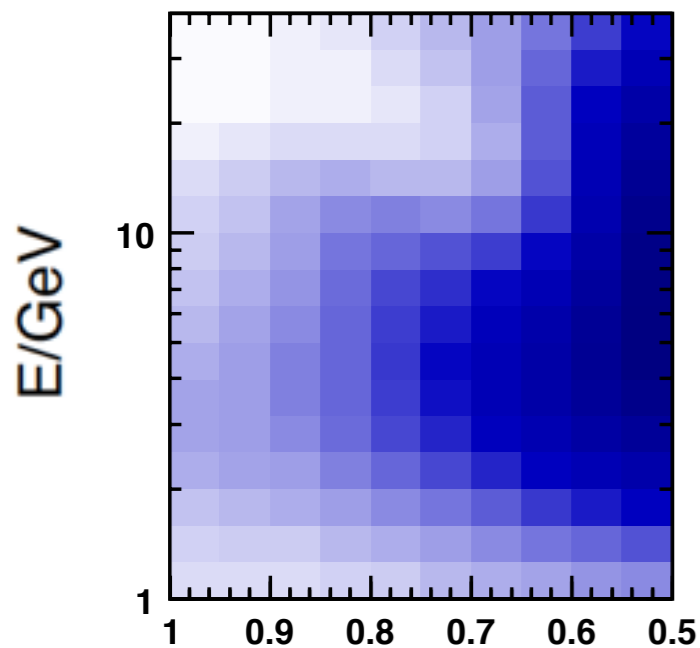
N_{NH}^α (smearred)



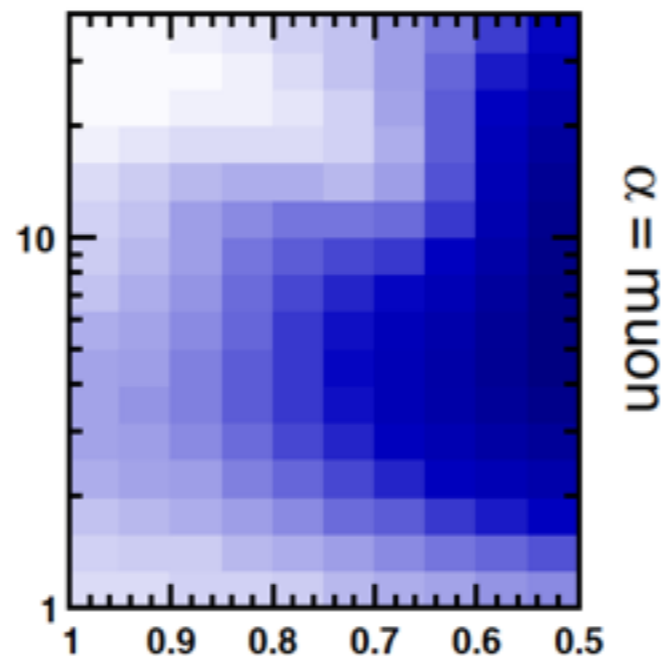
Mass hierarchy from atmospheric ν (PINGU)

(based on arXiv:1503.01999, F. Capozzi, E. Lisi, A. Marrone)

N_{NH}^α (smeared)



N_{IH}^α (smeared)



$\alpha = \mu$ on

Difference connected to mass hierarchy are O(few %).
Do we know spectral shape at the percent level?

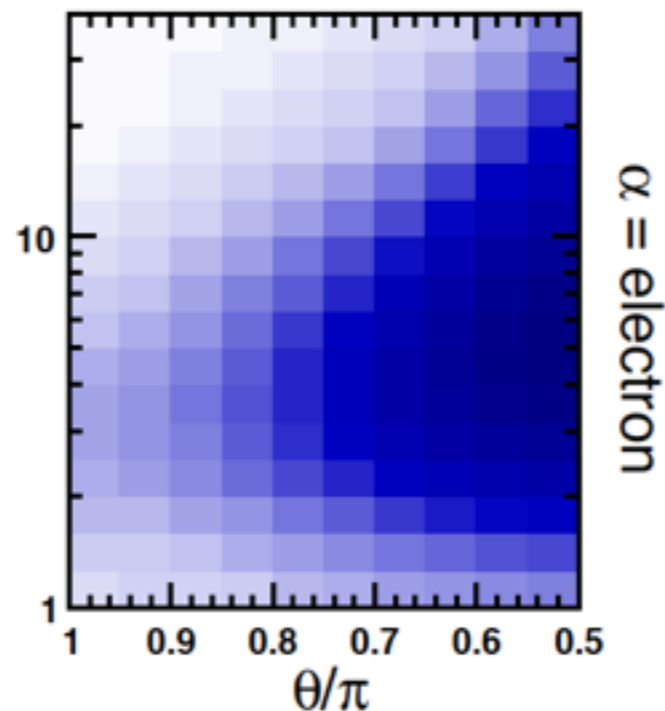
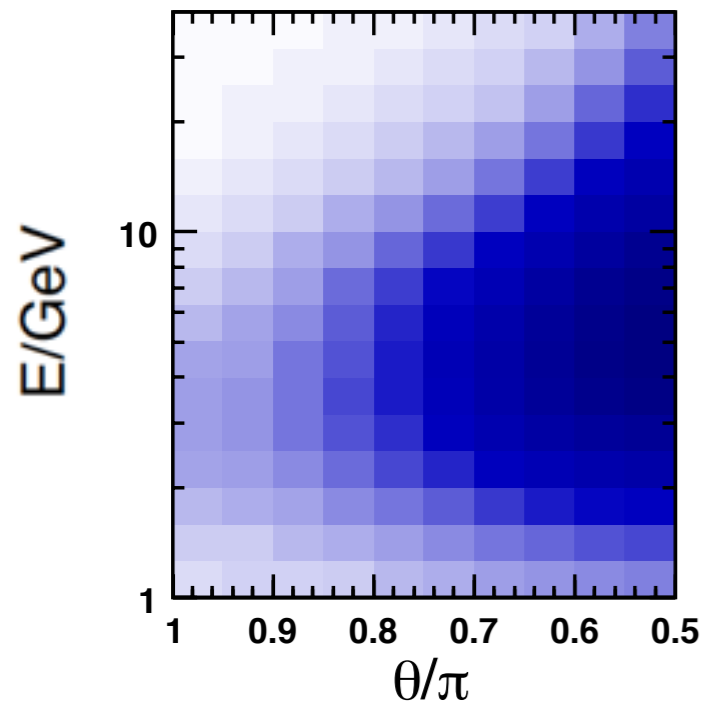
SYSTEMATICS

standard

OSCILLATIONS +
NORMALIZATION

known shape errors

+ RESOL (WIDTH, SCALE)



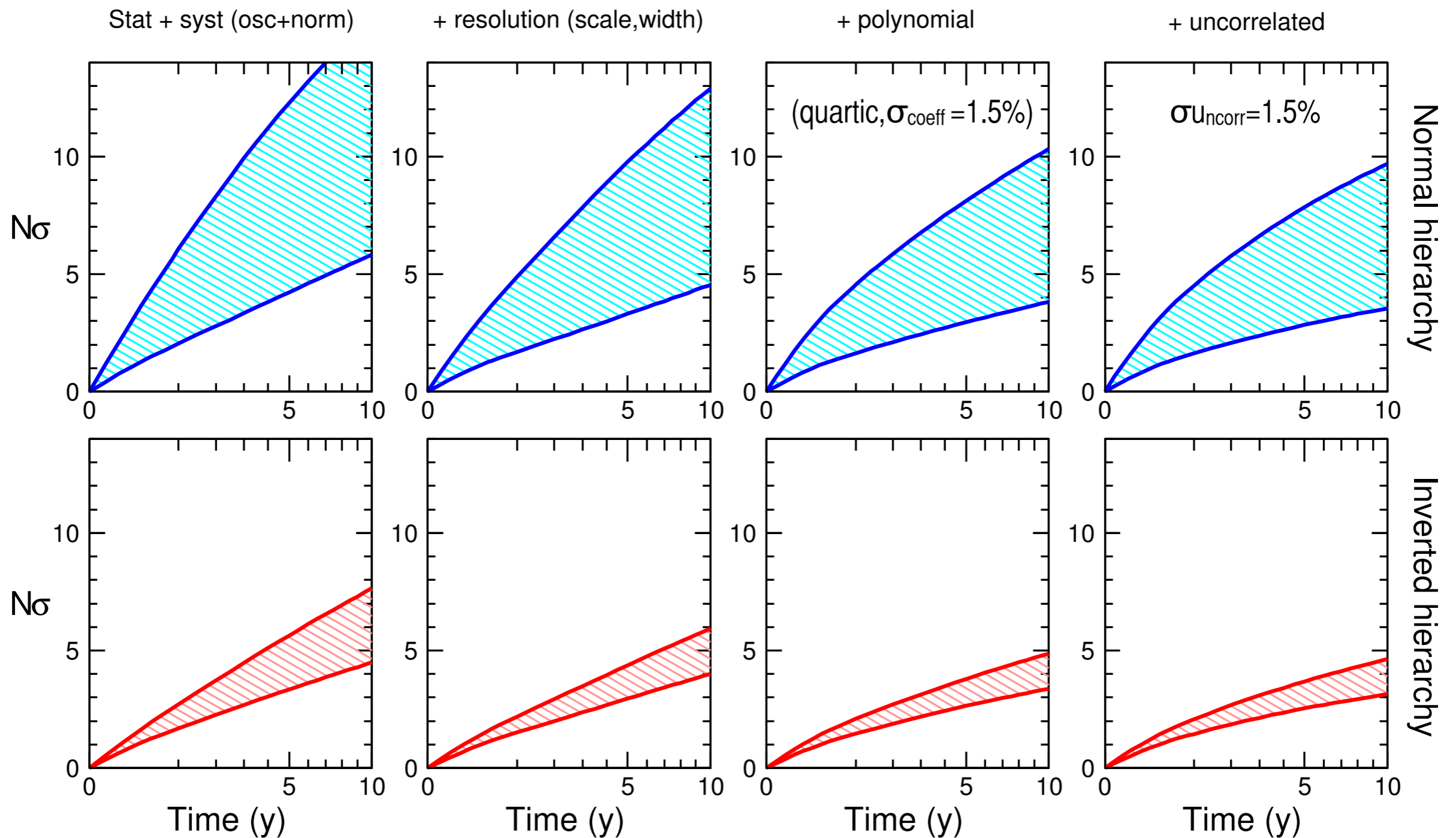
$\alpha = e$ lectron

In the limit of high statistics we must take into account possible residual correlated and uncorrelated uncertainties, which may not have a definite parametrization. For correlated, we use quartic polynomial in (E, θ)

Mass hierarchy from atmospheric ν (PINGU)

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Bands $\longleftrightarrow \sin^2\theta_{23} \in [0.4, 0.6]$



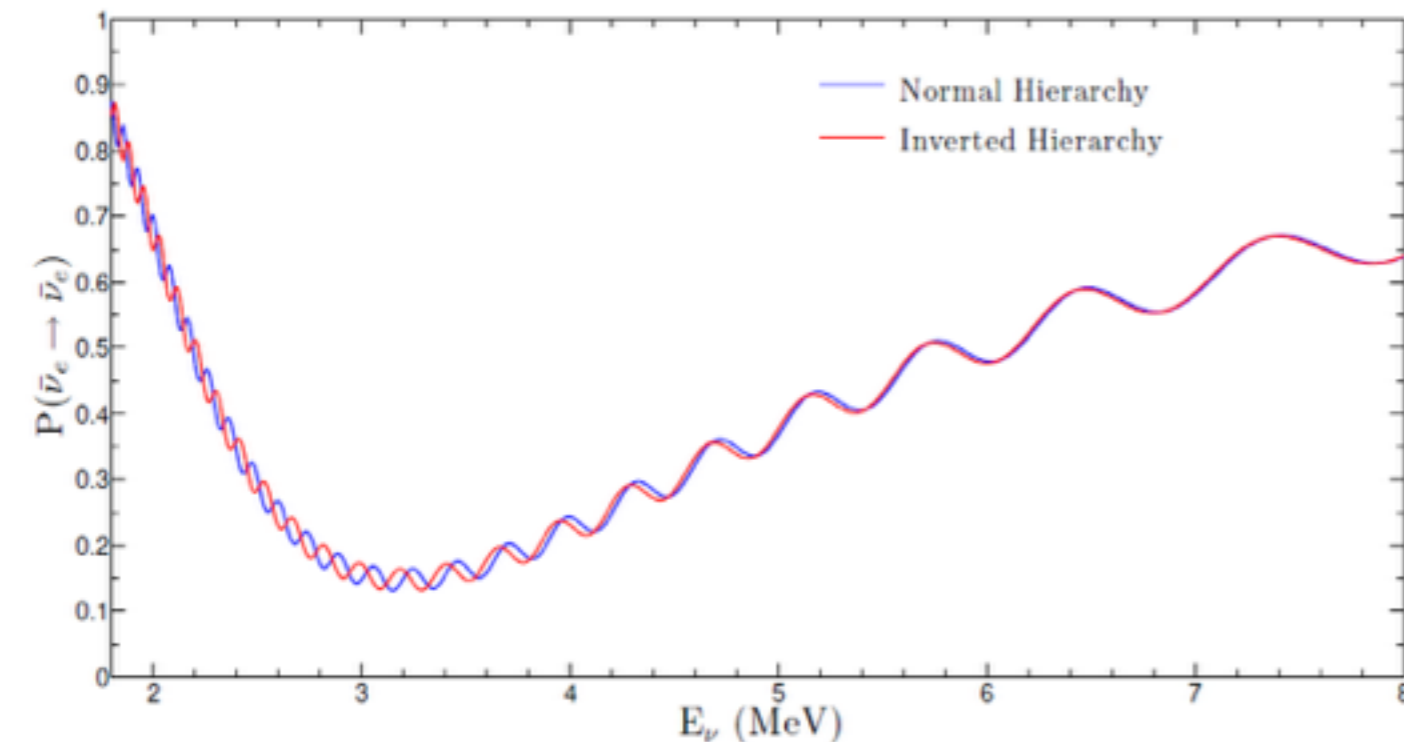
Including all systematics (right panel) there is a **reduction in hierarchy sensitivity of ~35% (~40%) after 5 (10) years** with respect to the left panel, which refers to standard systematics. Further studies are needed.

Mass hierarchy from MBL reactor $\bar{\nu}_e$ (JUNO)

(based on arXiv:1309.1638, F. Capozzi, E. Lisi, A. Marrone)

If baseline ~ 50 km, we can probe neutrino mass hierarchy through the study of the channel $\bar{\nu}_e \rightarrow \bar{\nu}_e$

The experiments are sensitive to short wavelength oscillations (θ_{13} , Δm^2), to long wavelength oscillations (θ_{12} , δm^2), and to their tiny interference (mass hierarchy)



REQUIREMENTS

EXPERIMENTAL:
High statistics,
High resolution

THEORETICAL:
Very accurate
theoretical calc.

PHENOMENOLOGICAL:
Refined stat/syst analysis

Mass hierarchy from MBL reactor ν (JUNO)

(based on arXiv:1309.1638, F. Capozzi, E. Lisi, A. Marrone)

THEORETICAL CALCULATIONS

Accurate and analytical expression for $P(\bar{\nu}_e \rightarrow \bar{\nu}_e)$ including matter effects and multiple reactors

Inclusion of nucleon recoil in the IBD

Background of geo- ν and ν from far reactors

SYSTEMATICS

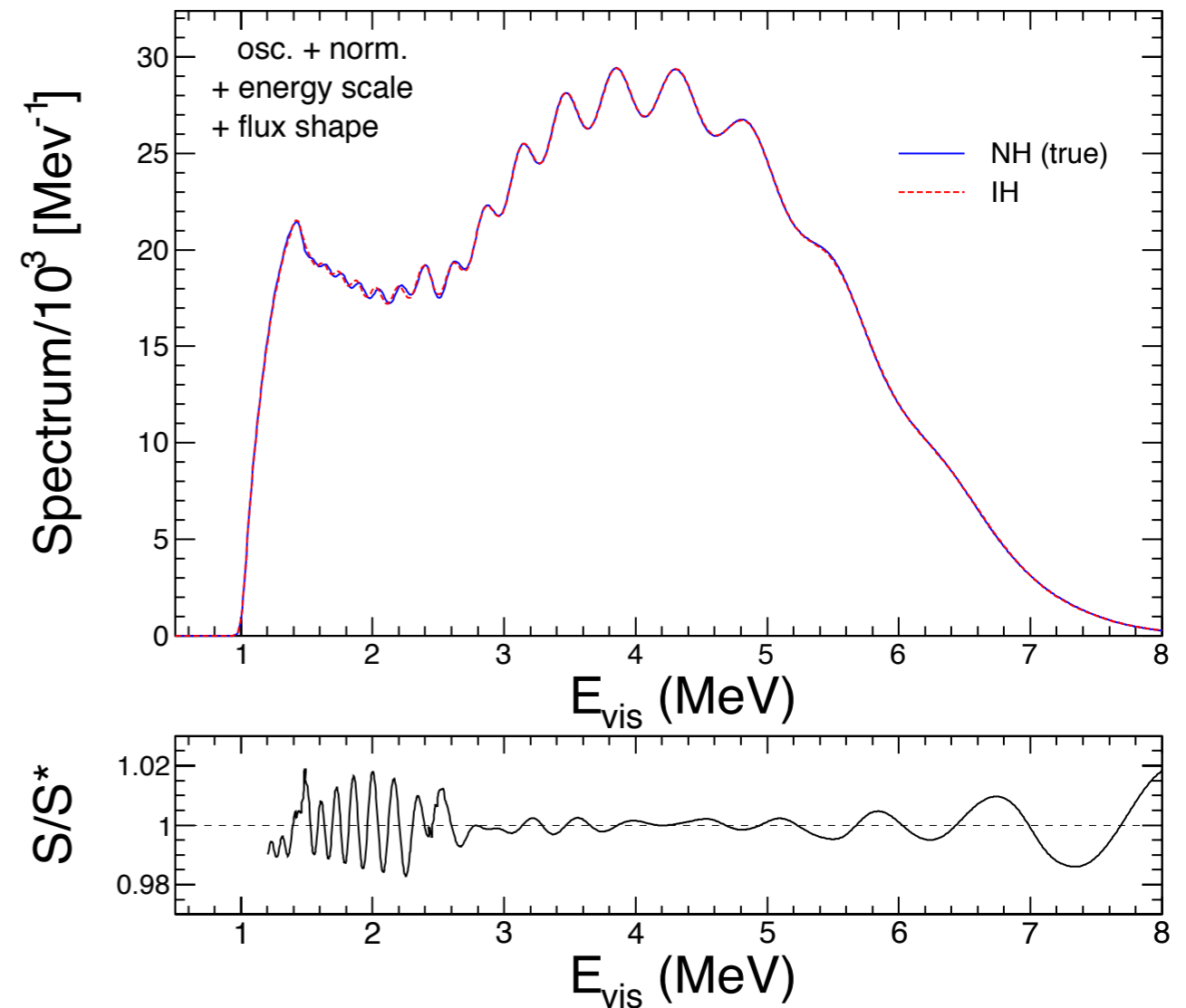
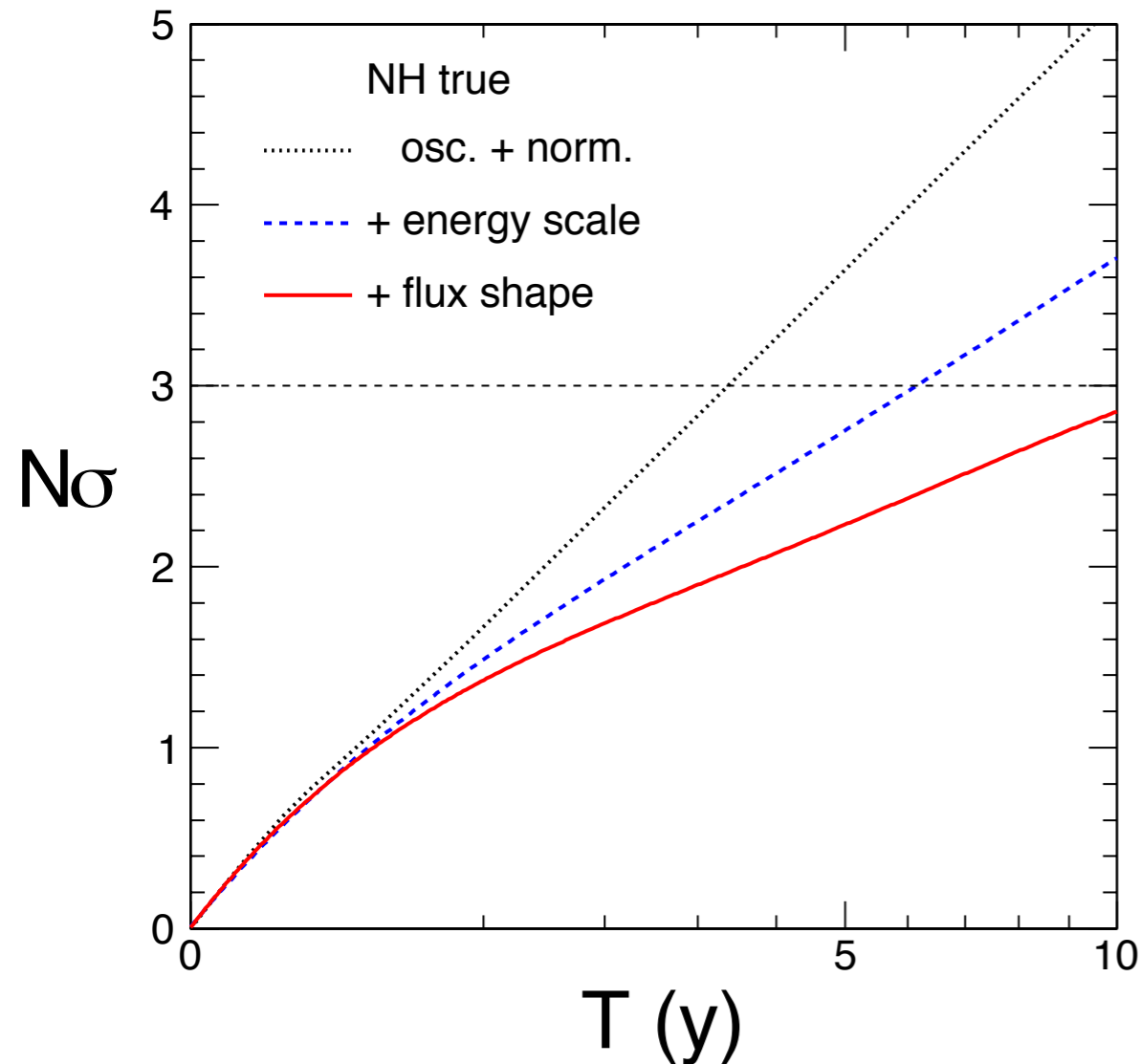
Variations of $\theta_{13}, \Delta m^2_{ee}, \theta_{12}, \delta m^2$ (current bounds)
Normalization: global (reactor), U and Th (geo- ν)

Energy scale and flux shape (polynomial)

All parameters are floating with Markov chain Montecarlo

Mass hierarchy from MBL reactor ν (JUNO)

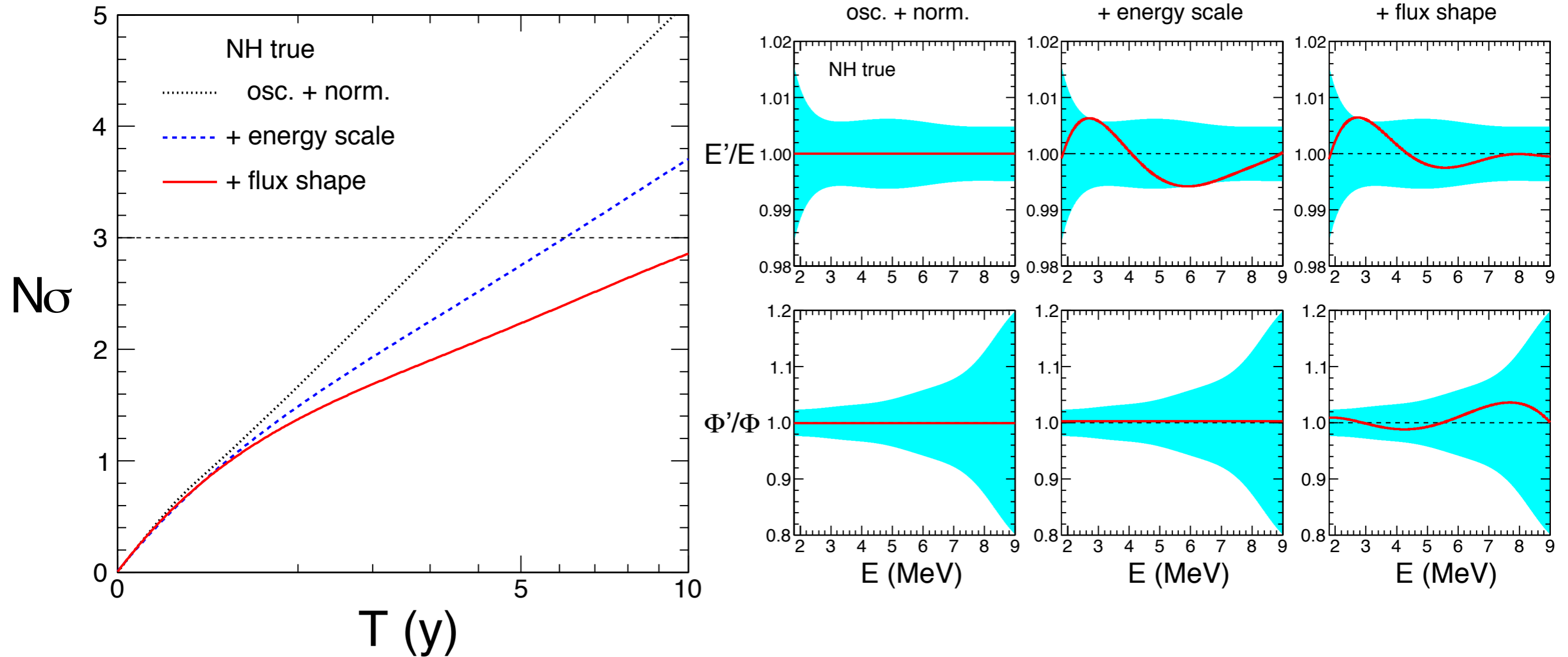
(based on arXiv:1309.1638, F. Capozzi, E. Lisi, A. Marrone)



Assuming the standard systematics (osc. + norm., dotted black curve) hierarchy sensitivity can reach about 5σ in 10 years. With current spectral uncertainties (red curve) hierarchy sensitivity may not reach 3σ after 10 years.

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DEGENERACIES IN $0\nu\beta\beta$

(based on arXiv:1506.04058, E. Lisi, A. M. Rotunno, F. Simkovic)

$$T_i^{-1} = G_i^j |M_i^j| (\lambda^j)^2$$

G_i^j = Kinematical phase space

M_i^j = Nuclear matrix element

λ^j = LNV parameter

The uncertainties on M_i^j make challenging the disentanglement of the particle physics mechanisms behind $0\nu\beta\beta$, even with multi-isotope data

**ANALYSIS
METHOD**

Calculations in the QRPA approximation

$i = 1, 2, 3 = {}^{76}\text{Ge}, {}^{130}\text{Te}, {}^{136}\text{Xe}$

$j = 1, 2 =$ light, heavy Majorana neutrino exchange

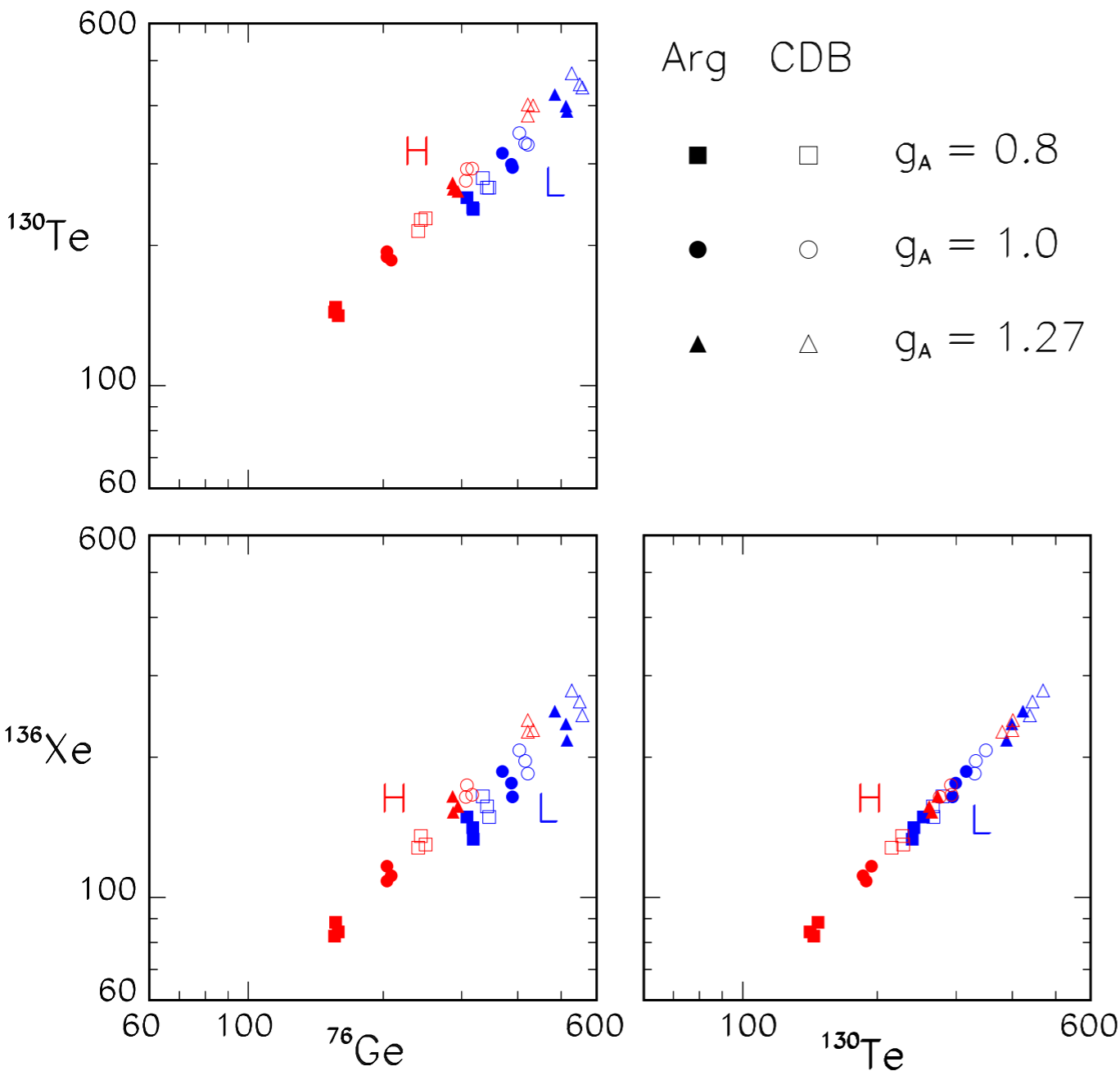
$g_A = 0.8, 1.0, 1.27$

potential = CD-Bonn, Argonne

DEGENERACIES IN $0\nu\beta\beta$

(based on arXiv:1506.04058, E. Lisi, A. M. Rotunno, F. Simkovic)

NME for Light ν ($\times 100$) and Heavy ν exchange



- For a given decay mechanism, the nuclear model uncertainties are degenerate with the LNV parameter λ_i

- The two different mechanisms (L and H) are largely degenerate with one another

Supernova neutrinos

(based on arXiv:1503.03485, A. Mirizzi, G. Mangano, N. Saviano)

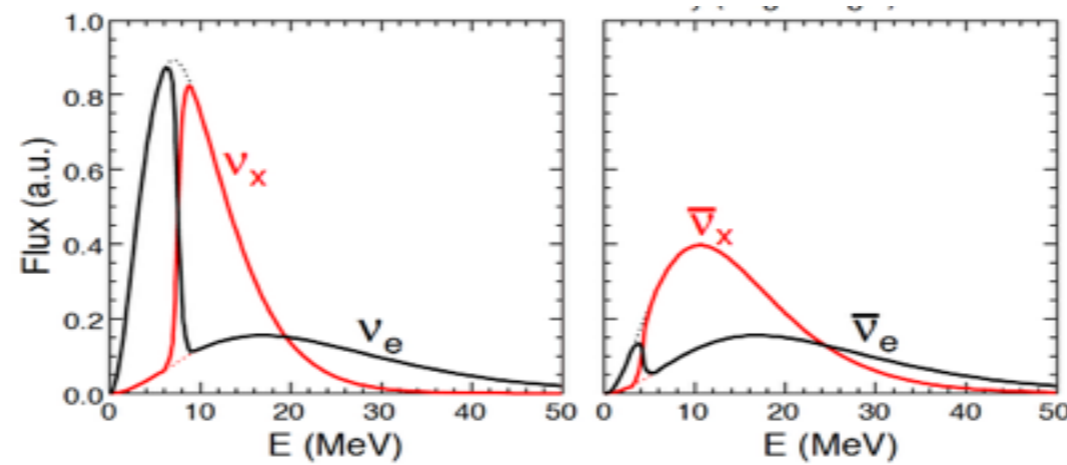
In high density SN regions, evolution becomes non linear. This locks the oscillations among modes in some energy ranges.

Collective phenomena take place.

$$H = H_{\text{vac}} + H_{\text{matter}} + H_{\nu\nu}$$

$$H_{\nu\nu} = \sqrt{2}G_F \int \frac{d^3q}{(2\pi)^3} (1 - \cos \theta_{pq}) (\rho(\vec{q}) - \bar{\rho}(\vec{q}))$$

- 1) Synchronized oscillations:** all neutrinos oscillate with the same frequency
- 2) Bipolar oscillations:** Coherent $\nu_e \bar{\nu}_e \leftrightarrow \nu_x \bar{\nu}_x$ oscillations even for extremely small mixing angle (only for inverted hierarchy)
- 3) Spectral splits:** ν_e and $\bar{\nu}_x$ (ν_e and $\bar{\nu}_x$) spectra interchange completely only within certain energy ranges (because of lepton number conservation)

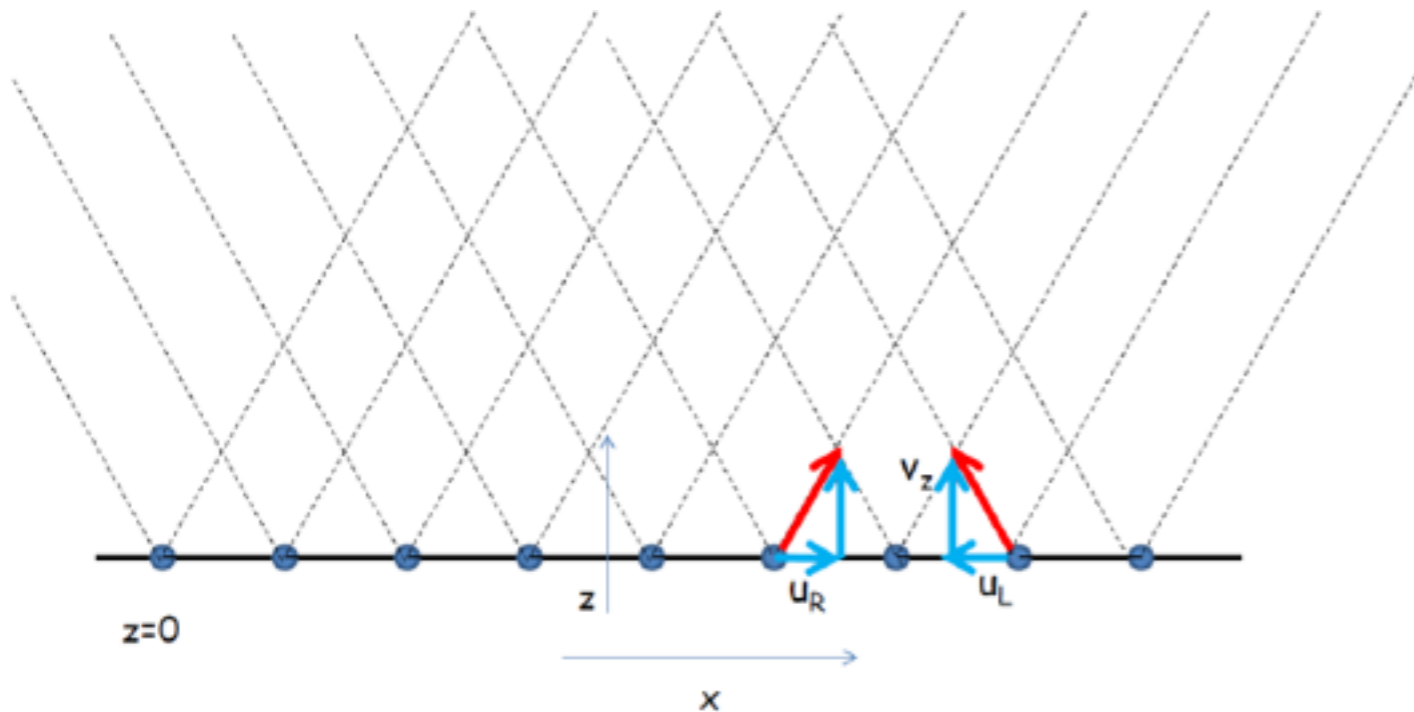


Supernova neutrinos

(based on arXiv:1503.03485, A. Mirizzi, G. Mangano, N. Saviano)

These phenomena are obtained assuming the bulb model (spherical, azimuthal and translational symmetry). Relaxing these hypotheses, instabilities may grow...

TOY MODEL



ν emitted by an infinite boundary at $z=0$, in only two directions (L,R). Assumed an excess of ν_e over $\bar{\nu}_e$ and normal hierarchy

$$P_{L,R}^3(x, 0) = \langle P_{L,R}^3(x, 0) \rangle + \epsilon \cos(k_0 x)$$

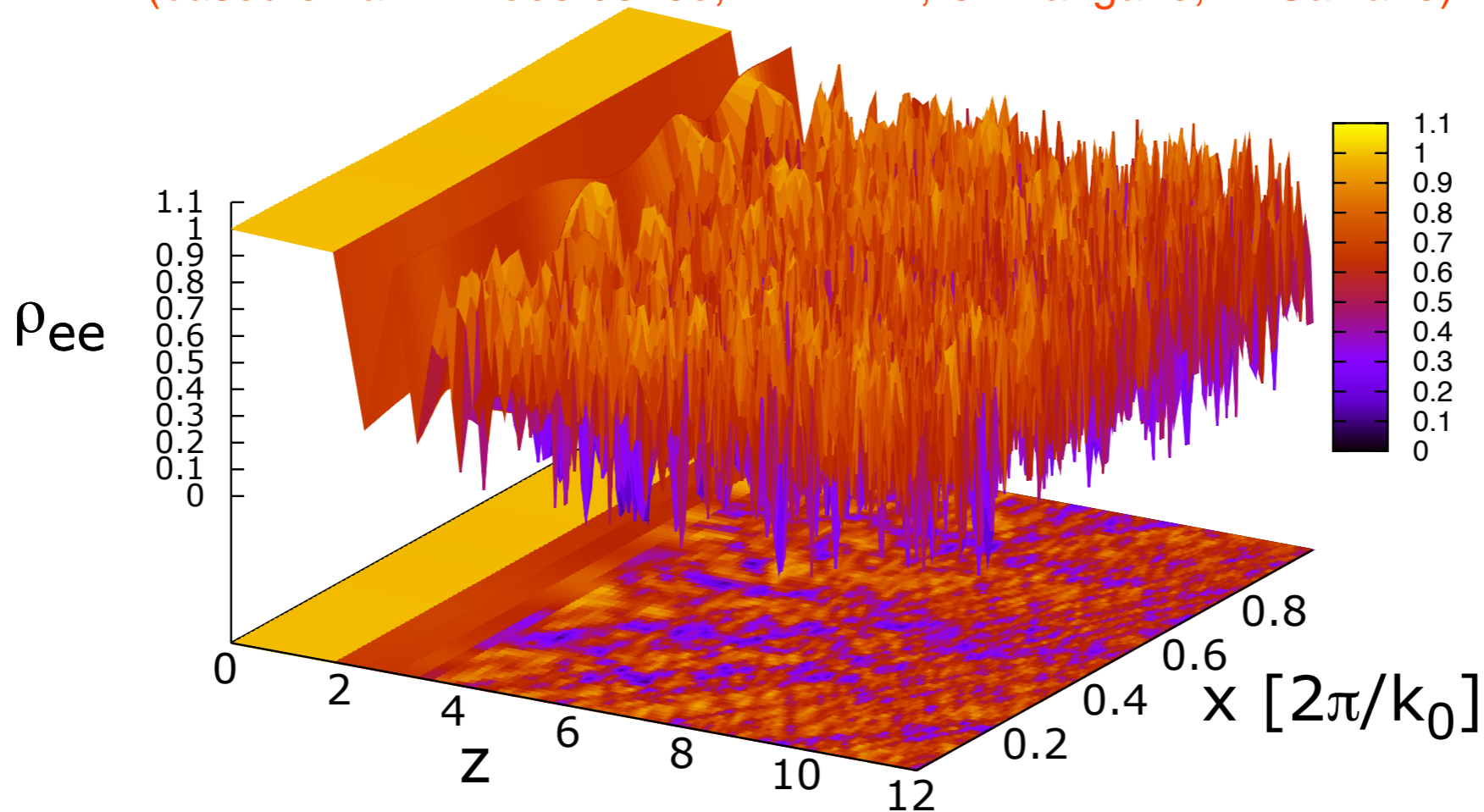
(Translational symmetry broken)

1% difference in the initial conditions of L and R modes

($L \longleftrightarrow R$ symmetry broken)

Supernova neutrinos

(based on arXiv:1503.03485, A. Mirizzi, G. Mangano, N. Saviano)



Till $z=2.5$ all the neutrinos oscillate in phase and the surfaces of equal phase are planes parallel to the radiating surface at $z = 0$. Then...

Large variations along the x direction at increasingly smaller scales

Coherent behavior of oscillations lost

$P^3_L(x,z) \neq P^3_R(x,z)$ (not shown)

Work in progress

- **(In)Stability and symmetry (breaking) of SN ν**
(F. Capozzi, A. Mirizzi *et al.*)
- **Refined Earth model for geo- ν analysis**
(E. Lisi in collaboration with PRIN-Ferrara)
- **Quenching of g_A in $0\nu\beta\beta$ and related weak processes**
(E. Lisi, A. Marrone, in collaboration with F. Simkovic *et al.*)
- **Updated global 3ν analysis of oscillation data after Summer 2015 Conferences**
(F. Capozzi, E. Lisi, A. Marrone, D. Montanino, A. Palazzo)
- **My PhD thesis**