

STRONG SECTOR IN NON-MINIMAL SUSY MODEL

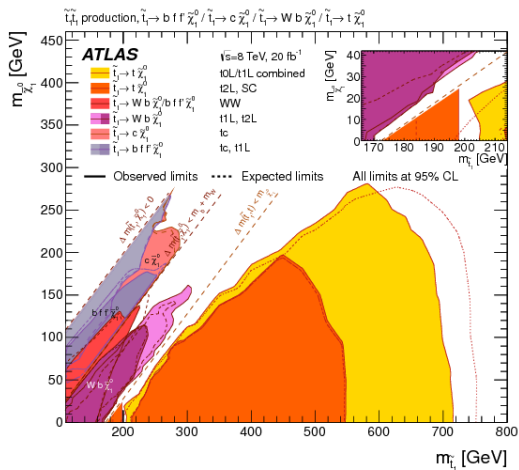
QCD@WORK 2016

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27 June 2016

Mass correlation plot of \tilde{t}_1 vs. $\tilde{\chi}_1^0$ Third-generation squark search from ATLAS Eur.Phys.J. C75 (2015) no.10, 510



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SQUARK IN THE MSSM

TNMSSM

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The superpotential of the Minimal Supersymmetric Standard Model is

$$\mathcal{W} = \mathcal{W}_{MSSM} + \mathcal{W}_{Higgs} \quad (1)$$

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and

$$\mathcal{W}_{Higgs} = \mu \hat{H}_u \cdot \hat{H}_d . \quad (3)$$

Higgs superfields are given by

$$\hat{H}_u = \begin{pmatrix} \hat{H}_u^+ \\ \hat{H}_u^0 \end{pmatrix} , \quad \hat{H}_d = \begin{pmatrix} \hat{H}_d^0 \\ \hat{H}_d^- \end{pmatrix} . \quad (4)$$

Stop and sbottom mass matrices are given respectively by

$$m_{\tilde{t}} = \begin{pmatrix} m_t^2 + m_{Q_3}^2 + m_Z^2 \cos(2\beta) \left(\frac{1}{2} - \frac{2}{3} \sin^2 \theta_w \right) & m_t(A_t - \mu \cot \beta) \\ m_t(A_t - \mu \cot \beta) & m_t^2 + m_{\tilde{u}_3}^2 - \frac{1}{3} m_Z^2 \cos(2\beta) \sin^2 \theta_w \end{pmatrix} \quad (5)$$

$$m_{\tilde{b}} = \begin{pmatrix} m_b^2 + m_{Q_3}^2 - m_Z^2 \cos(2\beta) \left(-\frac{1}{2} + \frac{2}{3} \sin^2 \theta_w \right) & m_b(A_b - \mu \tan \beta) \\ m_b(A_b - \mu \tan \beta) & m_b^2 + m_{\tilde{b}_3}^2 + \frac{2}{3} m_Z^2 \cos(2\beta) \sin^2 \theta_w \end{pmatrix} \quad (6)$$

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The mixing $\tilde{t}_R - \tilde{t}_L$ is relevant and \tilde{t}_1 is the lightest squark

$$\begin{aligned} m_{\tilde{t}_{1,2}}^2 &= \frac{1}{2} \left(m_t^2 + m_{Q_3}^2 + 2m_t^2 + \frac{1}{2} m_Z^2 \cos(2\beta) \right) \\ &\pm \sqrt{(m_{Q_3}^2 - m_{\bar{u}_3}^2 + \left(\frac{1}{2} - \frac{4}{3} \sin^2 \theta_w \right) \cos(2\beta) m_Z^2)^2 + 4m_t^2 (A_t - \mu \cot \beta)^2} \end{aligned}$$

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TRIplet & SINGLET

The superpotential of the model¹ is $\mathcal{W}_{TNMSSM} = \mathcal{W}_{MSSM} + \mathcal{W}_{TS}$ with

¹JHEP 1509 (2015) 045, JHEP 1512 (2015) 127, arXiv:1512.08651

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and

$$\mathcal{W}_{TS} = \lambda_T \hat{H}_d \cdot \hat{T} \hat{H}_u + \lambda_S \hat{S} \hat{H}_d \cdot \hat{H}_u + \frac{\kappa}{3} \hat{S}^3 + \lambda_{TS} \hat{S} \text{tr}[\hat{T}^2]. \quad (8)$$

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Triplet and doublets superfields are given by

$$\hat{T} = \begin{pmatrix} \sqrt{\frac{1}{2}} \hat{T}^0 & \hat{T}_2^+ \\ \hat{T}_1^- & -\sqrt{\frac{1}{2}} \hat{T}^0 \end{pmatrix}, \quad \hat{H}_u = \begin{pmatrix} \hat{H}_u^+ \\ \hat{H}_u^0 \end{pmatrix}, \quad \hat{H}_d = \begin{pmatrix} \hat{H}_d^0 \\ \hat{H}_d^- \end{pmatrix}. \quad (9)$$

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In any scale invariant supersymmetric theory with a cubic superpotential, the complete Lagrangian with the soft SUSY breaking terms has an accidental Z_3 symmetry. Such terms are given by

$$\begin{aligned}
 V_{\text{soft}} = & m_{H_u}^2 |H_u|^2 + m_{H_d}^2 |H_d|^2 + m_S^2 |S|^2 + m_T^2 |T|^2 \\
 & + m_Q^2 |Q|^2 + m_U^2 |U|^2 + m_D^2 |D|^2 \\
 & + (A_S S H_d \cdot H_u + A_\kappa S^3 + A_T H_d \cdot T \cdot H_u \\
 & + A_{TS} S \text{Tr}(T^2) + A_U U H_U \cdot Q + A_D D H_D \cdot Q \\
 & + h.c.), \tag{10}
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 \end{aligned}$$

We have performed the scan using the following criteria for the couplings and the soft parameters

$$\begin{aligned}
 |\lambda_{T,S,TS}| &\leq 1, |\kappa| \leq 3, |v_s| \leq 1 \text{ TeV}, 1 \leq \tan \beta \leq 10, \\
 |A_{T,S,TS,U,D}| &\leq 1 \text{ GeV}, |A_\kappa| \leq 3 \text{ GeV}, \\
 65 \leq |M_{1,2}| &\leq 10^3 \text{ GeV}, 3 \times 10^2 \leq m_{Q_3, \bar{u}_3, \bar{d}_3} \leq 10^3 \text{ GeV}
 \end{aligned} \tag{11}$$

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The mass matrices for stop and sbottom in this model are

$$m_{\tilde{t}} = \begin{pmatrix} m_t^2 + m_{Q_3}^2 + \frac{1}{24} (g_Y^2 - 3g_L^2) (v_u^2 - v_d^2) & \frac{1}{\sqrt{2}} A_T v_u + \frac{y_t v_d}{2} \left(\frac{v_T \lambda_T}{\sqrt{2}} - v_S \lambda_S \right) \\ \frac{1}{\sqrt{2}} A_T v_u + \frac{y_t v_d}{2} \left(\frac{v_T \lambda_T}{\sqrt{2}} - v_S \lambda_S \right) & m_t^2 + m_{\tilde{u}_3}^2 + \frac{1}{6} (v_d^2 - v_u^2) g_Y^2 \end{pmatrix} \quad (12)$$

$$m_{\tilde{b}} = \begin{pmatrix} m_b^2 + m_{Q_3}^2 + \frac{1}{24} (g_Y^2 + 3g_L^2) (v_u^2 - v_d^2) & \frac{1}{\sqrt{2}} A_D v_d + \frac{y_b v_u}{2} \left(\frac{v_T \lambda_T}{\sqrt{2}} - v_S \lambda_S \right) \\ \frac{1}{\sqrt{2}} A_D v_d + \frac{y_b v_u}{2} \left(\frac{v_T \lambda_T}{\sqrt{2}} - v_S \lambda_S \right) & m_b^2 + m_{\tilde{d}_3}^2 + \frac{1}{12} (v_u^2 - v_d^2) g_Y^2 \end{pmatrix} \quad (13)$$

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In this model A_t is independent from y_t and the μ parameter of MSSM is dynamically generated through

$$\lambda_T \hat{H}_d \cdot \hat{T} \hat{H}_u + \lambda_S \hat{S} \hat{H}_d \cdot \hat{H}_u$$

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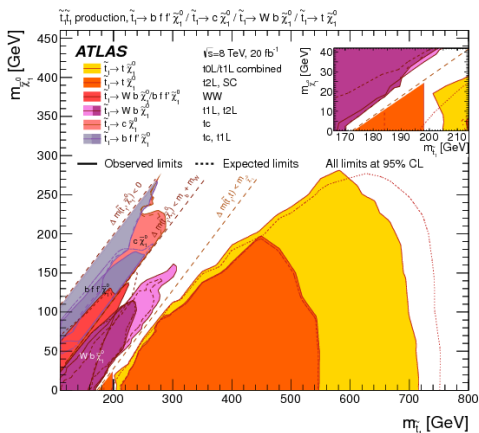
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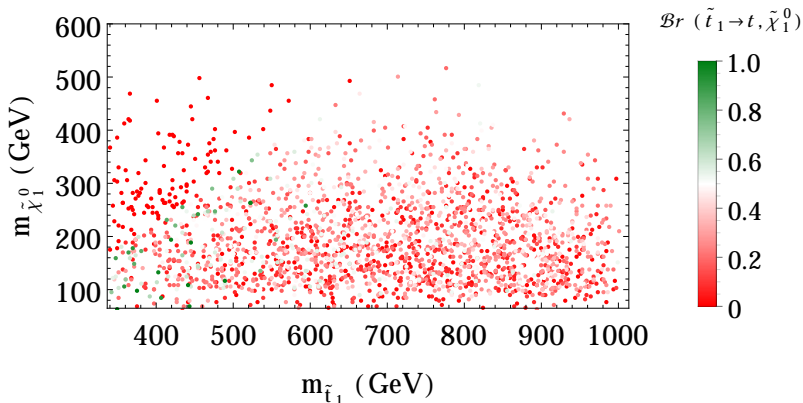
Squark searches are made usually under the assumption of

$$\mathcal{B}(\tilde{t}_1 \rightarrow t \tilde{\chi}_1^0) = 1$$



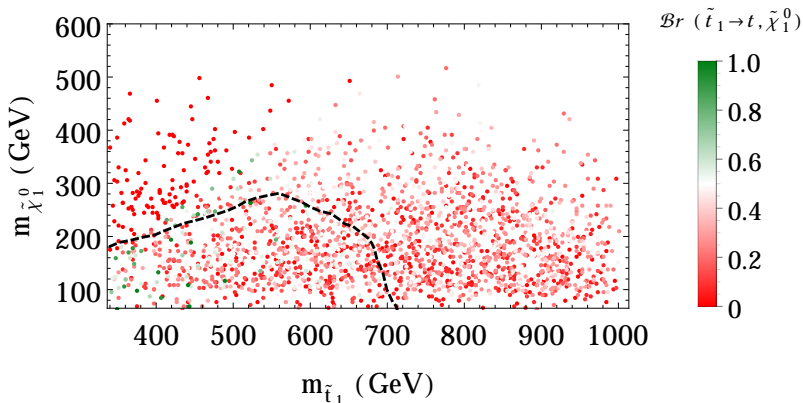
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However this is not always true in non-minimal SUSY theories, such as TNMSSM



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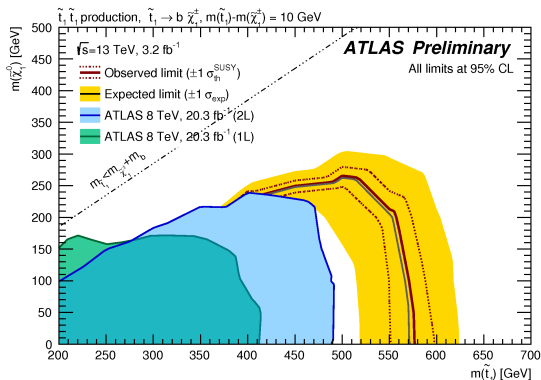
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$$\tilde{t}_1 \rightarrow b \tilde{\chi}_1^\pm$$

Another possibility for the squark decay is the channel

$$\tilde{t}_1 \rightarrow b \tilde{\chi}_1^\pm$$



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Again the channel

$$\tilde{t}_1 \rightarrow b \tilde{\chi}_1^\pm$$

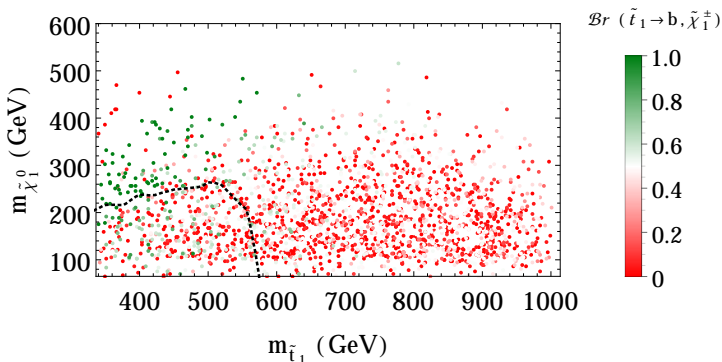
is assumed to have $\mathcal{B}\tau = 1$ and $m_{\tilde{t}_1} - m_{\tilde{\chi}_1^\pm} = 10$ GeV

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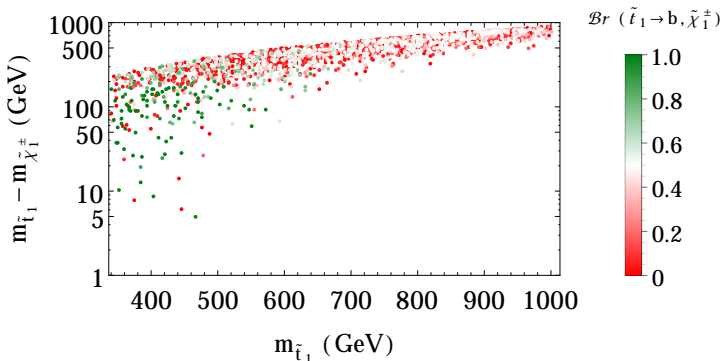
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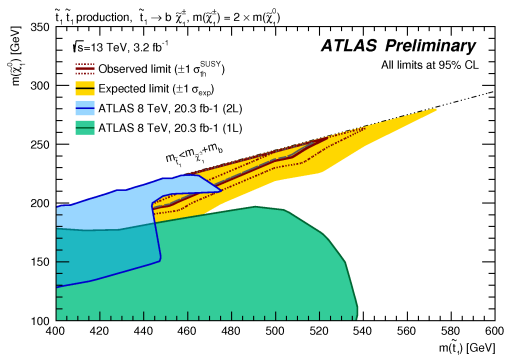


$$\tilde{t}_1 \rightarrow b \tilde{\chi}_1^\pm$$

It was also analyzed the case

$$\tilde{t}_1 \rightarrow b \tilde{\chi}_1^\pm$$

with $\mathcal{B}\tau = 1$ and $m_{\tilde{\chi}_1^\pm} = 2 m_{\tilde{\chi}_1^0}$



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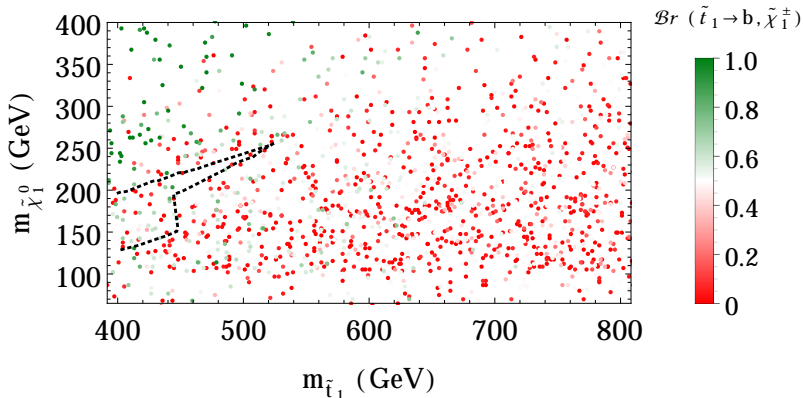
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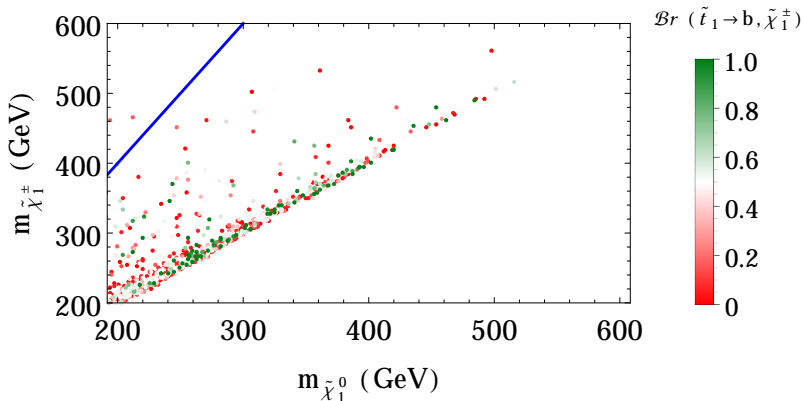


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- ▶ LHC is improving the previous searches for superpartners of the SM quarks
- ▶ most of the attention is devoted to MSSM-like scenarios
- ▶ extensions of MSSM can have different behavior in both strong and weak sectors

Thank You!



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VACUUM AND SCALAR SPECTRUM

To determine the tree-level mass spectrum, we consider the tree-level minimisation conditions,

$$\partial_{\Phi_i} V|_{\text{vev}} = 0; \quad V = V_F + V_D + V_{\text{soft}}, \quad \Phi_i = H_{u,d}^0, S, T^0. \quad (14)$$

Each field takes a vacuum expectation value (v.e.v.), which we choose to be real in order to preserve CP. V_F and V_D are the supersymmetric F-terms and D-terms extracted from the superpotential. V_{soft} is the scale invariant, soft-breaking part of the potential. The minimization conditions are solved w.r.t. the soft-breaking masses of the scalars. We then have

CP-even

h_1, h_2, h_3, h_4

CP-odd

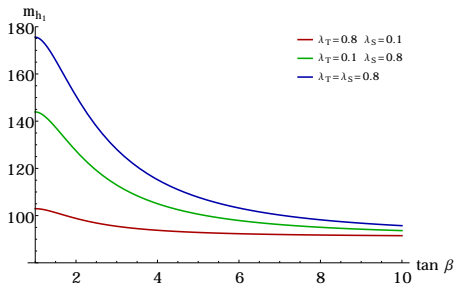
a_1, a_2, a_3

Charged

$h_1^\pm, h_2^\pm, h_3^\pm$

At tree-level the maximum value of the lightest neutral Higgs is

$$m_{h_1}^2 \leq m_Z^2 (\cos^2 2\beta + \frac{\lambda_T^2}{g_L^2 + g_Y^2} \sin^2 2\beta + \frac{2\lambda_S^2}{g_L^2 + g_Y^2} \sin^2 2\beta) \quad (15)$$



Tree-level lightest CP-even Higgs mass maximum values with respect to $\tan \beta$ for (i) $\lambda_T = 0.8$, $\lambda_S = 0.1$ (in red), (ii) $\lambda_T = 0.1$, $\lambda_S = 0.8$ (in green) and (iii) $\lambda_T = 0.8$, $\lambda_S = 0.8$ (in blue).

ONE-LOOP HIGGS MASSES

We calculate the one-loop Higgs mass for the neutral Higgs bosons via the Coleman-Weinberg effective potential

$$V_{\text{CW}} = \frac{1}{64\pi^2} \text{Str} \left[m^4 \left(\ln \frac{m^2}{\mu_r^2} - \frac{3}{2} \right) \right], \quad (16)$$

where m^2 are the field-dependent mass matrices, μ_r is the renormalization scale, and the supertrace includes a factor of $(-1)^{2J}(2J+1)$ for each particle of spin J in the loop.

Using the V_{CW} one-loop potential we have the following one-loop expression for the scalar Higgs boson mass matrix

$$\begin{aligned}
 (\Delta m_h^2)_{ij} &= \left. \frac{\partial^2 V_{\text{CW}}(\Phi)}{\partial \Phi_i \partial \Phi_j} \right|_{\text{vev}} - \frac{\delta_{ij}}{\langle \Phi_i \rangle} \left. \frac{\partial V_{\text{CW}}(\Phi)}{\partial \Phi_i} \right|_{\text{vev}} \\
 &= \sum_k \frac{1}{32\pi^2} \frac{\partial m_k^2}{\partial \Phi_i} \frac{\partial m_k^2}{\partial \Phi_j} \ln \frac{m_k^2}{\mu_r^2} \Big|_{\text{vev}} \\
 &\quad + \sum_k \frac{1}{32\pi^2} m_k^2 \frac{\partial^2 m_k^2}{\partial \Phi_i \partial \Phi_j} \left(\ln \frac{m_k^2}{\mu_r^2} - 1 \right) \Big|_{\text{vev}} \\
 &\quad - \sum_k \frac{1}{32\pi^2} m_k^2 \frac{\delta_{ij}}{\langle \Phi_i \rangle} \frac{\partial m_k^2}{\partial \Phi_i} \left(\ln \frac{m_k^2}{\mu_r^2} - 1 \right) \Big|_{\text{vev}} \quad (17)
 \end{aligned}$$

where we have included the one-loop correction to the minimization conditions.