

Exotic baryons as a hadronic molecule in the heavy quark region

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**Yasuhiro Yamaguchi and Elena Santopinto ,
arXiv:1606.08330 [hep-ph].**

QCD@Work - International workshop on QCD Theory and Experiment
27-30 June 2016, Martina Franca, Italy

Hidden-charm pentaquarks as **a molecules**

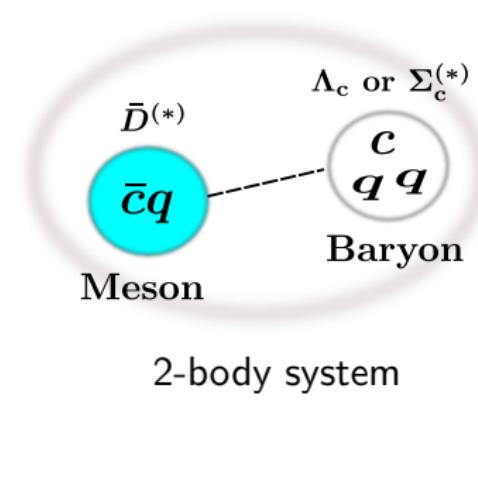
① Introduction

- Observed Pentaquarks
- Heavy Quark Spin Symmetry
- Coupled channels

② Meson-Baryon molecules:

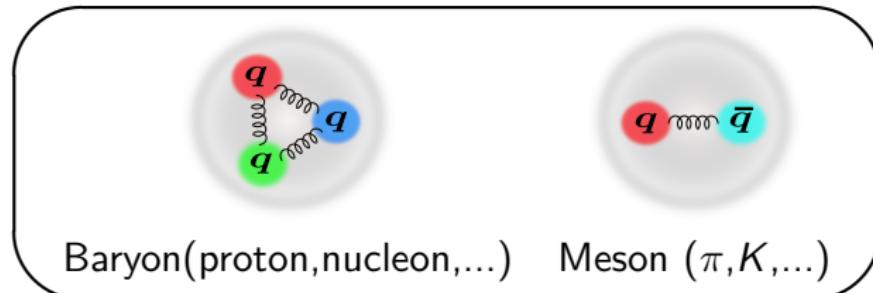
$$\bar{D}^{(*)}\Lambda_c^{(*)} - \bar{D}^{(*)}\Sigma_c^{(*)}$$

③ Summary



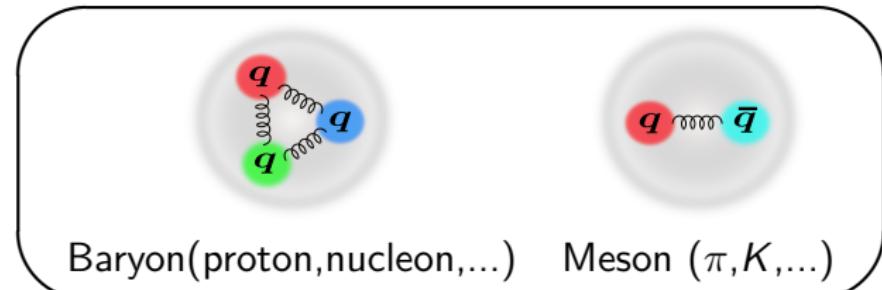
Hadrons in the heavy quark region

- Hadron: Composite particle of **Quarks** and **Gluons**
- Constituent quark model (Baryon(qqq) and Meson $q\bar{q}$) has been successfully applied to the hadron spectra!

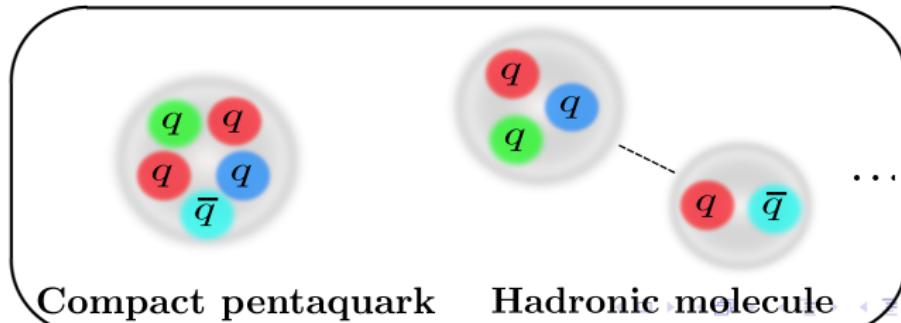


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- **Exotic hadrons?** → Multiquark state



Observation of two hidden-charm pentaquarks !!

Introduction

PRL 115, 072001 (2015)

PHYSICAL REVIEW LETTERS

WCK CHUNG
14 AUGUST 2015



Observation of $J/\psi p$ Resonances Consistent with Pentaquark States in $\Lambda_b^0 \rightarrow J/\psi K^- p$ Decays

R. Aaij *et al.*^{*}

(LHCb Collaboration)

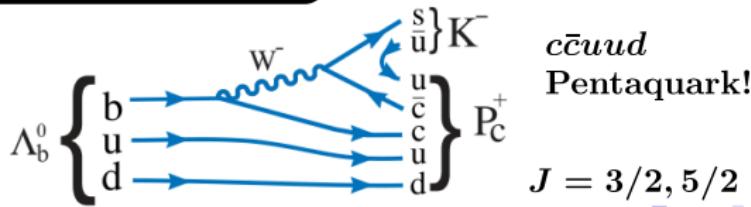
(Received 13 July 2015; published 12 August 2015)

Observations of exotic structures in the $J/\psi p$ channel, which we refer to as charmonium-pentaquark states, in $\Lambda_b^0 \rightarrow J/\psi K^- p$ decays are presented. The data sample corresponds to an integrated luminosity of 3 fb^{-1} acquired with the LHCb detector from 7 and 8 TeV pp collisions. An amplitude analysis of the three-body final state reproduces the two-body mass and angular distributions. To obtain a satisfactory fit of the structures seen in the $J/\psi p$ mass spectrum, it is necessary to include two Breit-Wigner amplitudes that each describe a resonance state. The significance of each of these resonances is more than 9 standard deviations. One has a mass $\mathbf{1} 4380 \pm 8 \pm 29 \text{ MeV}$ and a width of $205 \pm 18 \pm 86 \text{ MeV}$, while the second is narrower, with a mass $\mathbf{2} 4449.8 \pm 1.7 \pm 2.5 \text{ MeV}$ and a width of $39 \pm 5 \pm 19 \text{ MeV}$. The preferred J^P assignments are of opposite parity, with one state having spin $3/2$ and the other $5/2$.

DOI: [10.1103/PhysRevLett.115.072001](https://doi.org/10.1103/PhysRevLett.115.072001)

PACS numbers: 14.40.Pq, 13.25.Gv

$\Lambda_b^0 \rightarrow K^- P_c^+$ decay



What is the structure of the pentaquarks?

Introduction

Theoretical discussions

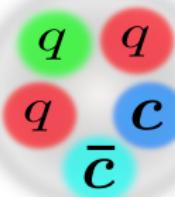
- Compact pentaquark?

▷ Quark model

W.L.Wang *et al.*, PRC**84**(2011)015203

G. Yang and J. Ping, (2015), arXiv:1511.09053

...



Pentaquark
(Compact)

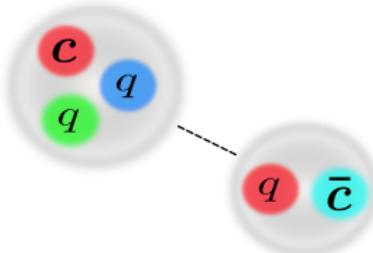
- Hadronic molecule?

▷ SU(4) flavor symmetry

J.-J.Wu *et al.*, PRL**105**(2010)232001

C.W.Xiao *et al.*, PRD**88**(2013)056012

...

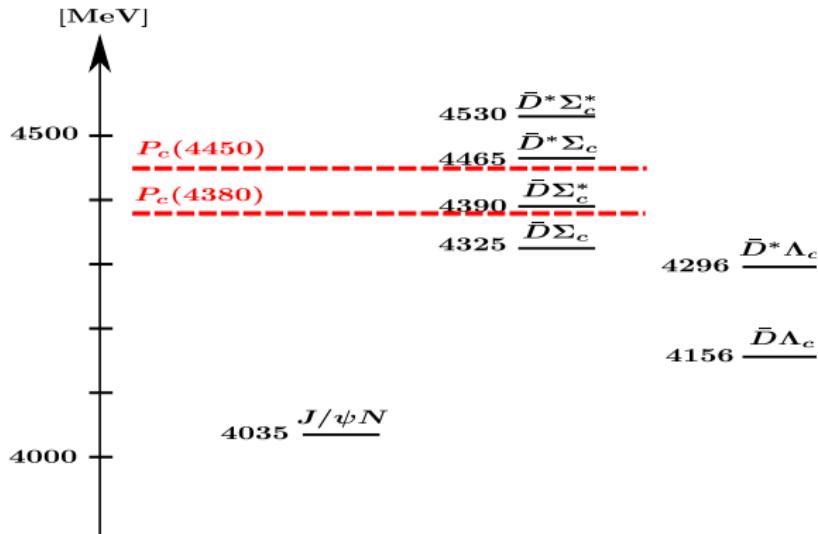


Hadronic molecule

Important issue of the heavy pentaquarks

Introduction

- Pentaquarks are close to **the meson-baryon thresholds**
⇒ **Hadronic molecules** appears near the thresholds!



- Heavy Quark Spin Symmetry**

⇒ SU(4) symmetry is broken in the charm quark sector.

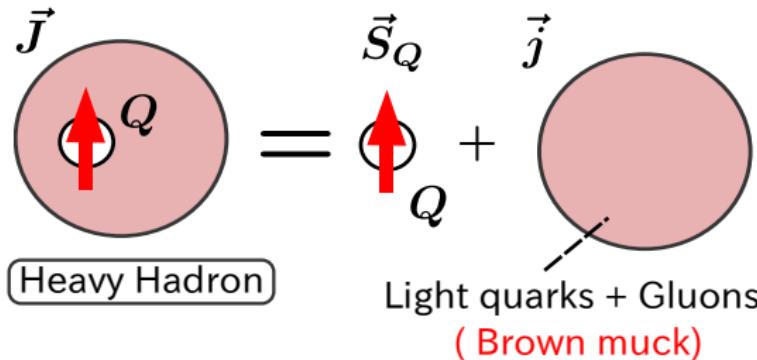
Heavy Quark Spin Symmetry and Mass degeneracy

Introduction

Heavy Quark Spin Symmetry (HQS)

N.Isgur,M.B.Wise,PLB232(1989)113

- **Suppression of Spin-spin force** in $m_Q \rightarrow \infty$.
- ⇒ Decomposition of **Heavy quark spin** and **Light components**
 $\vec{J} = \vec{L} + \vec{S} = \vec{S}_Q + \vec{j}$



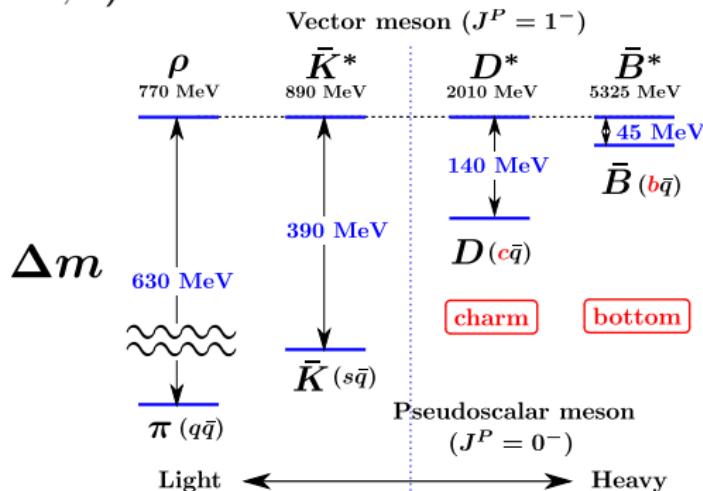
⇒ **Mass degeneracy** of hadrons with the different J

- Mass degeneracy of $\{D, D^*\}(Q\bar{q})$, $\{\eta_c, J/\psi\}(Q\bar{Q})$, $\{\Sigma_c, \Sigma_c^*\}(Qqq)$ (baryons)...

Mass degeneracy of heavy hadrons

Introduction

- Mass difference between vector and pseudoscalar mesons.
 $(Q\bar{q}, q = u, d)$

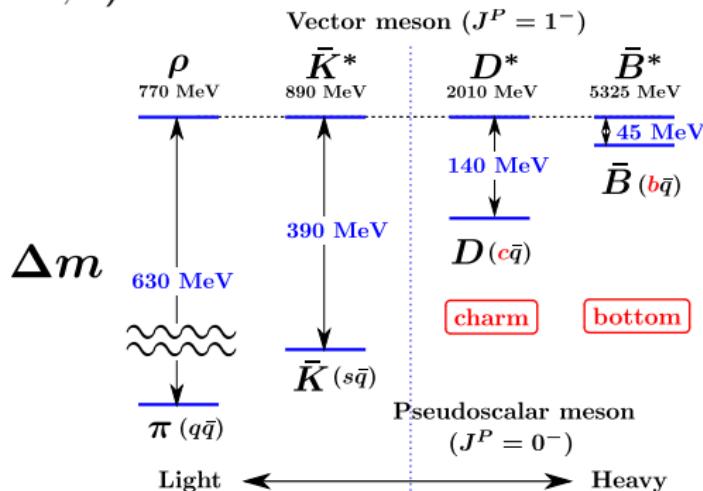


- Δm decreases when the quark mass increases.
- Mass degeneracy of heavy baryons $\{\Sigma_c, \Sigma_c^*\}$ also appears.

Mass degeneracy of heavy hadrons

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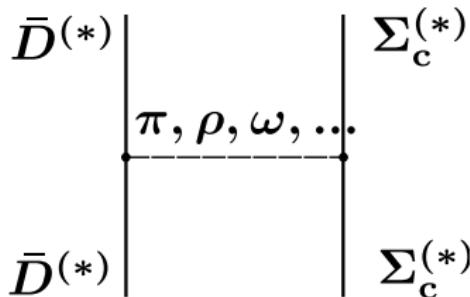
⇒ Degeneracy of $\bar{D}\Sigma_c, \bar{D}\Sigma_c^*, \bar{D}^*\Sigma_c, \bar{D}^*\Sigma_c^*$

Coupled channels of the hidden-charm pentaquark

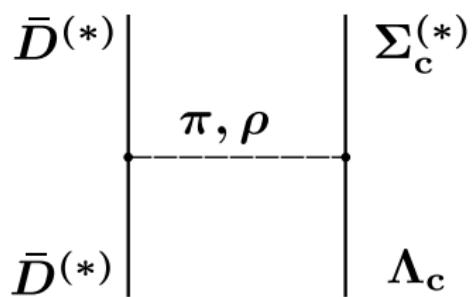
Introduction

- $\bar{D}^{(*)}\Lambda_c - \bar{D}^{(*)}\Sigma_c^{(*)}$ mixing (analogous to $\Lambda N - \Sigma N$)
 $m_{\Sigma_c} - m_{\Lambda_c} \sim 170$ MeV

$\bar{D}^{(*)}\Sigma_c^{(*)}$ coupling



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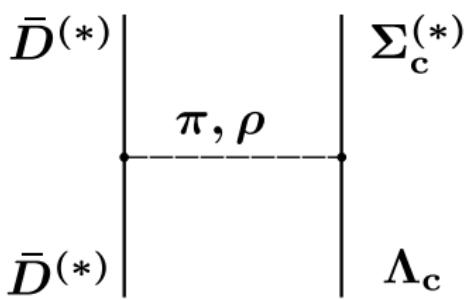
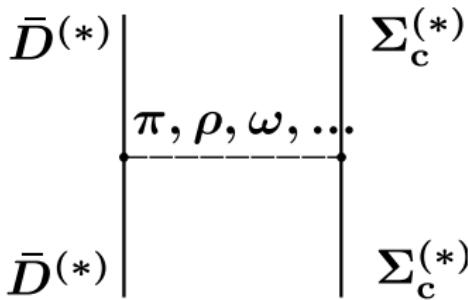
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⇒ $\bar{D}\Lambda_c, \bar{D}^*\Lambda_c, \bar{D}\Sigma_c, \bar{D}\Sigma_c^*, \bar{D}^*\Sigma_c, \bar{D}^*\Sigma_c^*$ (**6 thresholds!**)

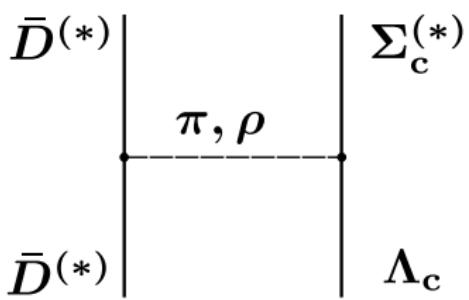
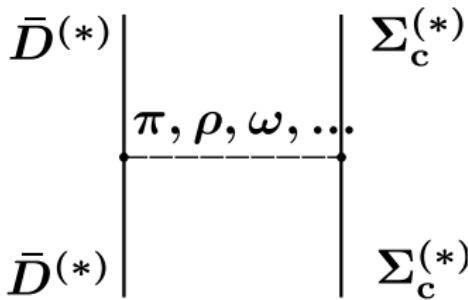
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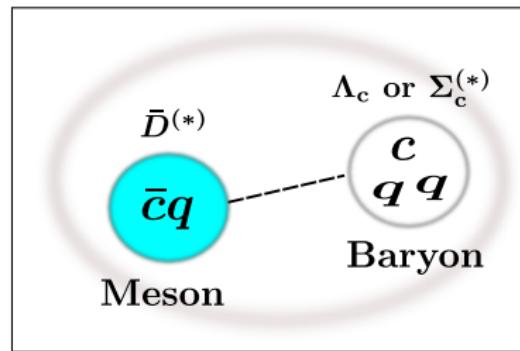


⇒ $\bar{D}\Lambda_c, \bar{D}^*\Lambda_c, \bar{D}\Sigma_c, \bar{D}\Sigma_c^*, \bar{D}^*\Sigma_c, \bar{D}^*\Sigma_c^*$ (**6 thresholds!**)

- Coupling to a state with $\ell \neq 0$ (D -wave,...)
⇒ **Tensor force producing a strong attraction!**

Main Subject: Pentaquarks

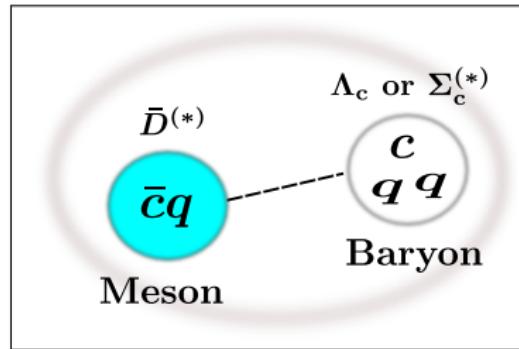
- Hadronic molecules formed by **hidden-charm meson-baryon**.



- Bound and resonant states of $\bar{D}^{(*)}\Lambda_c - \bar{D}^{(*)}\Sigma_c^{(*)}$
- ▷ Coupling to $\bar{D}^{(*)}\Lambda_c$ and $\bar{D}^{(*)}\Sigma_c^{(*)}$
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- ▷ Coupling to the state with $\ell \neq 0$

The full-coupled channel analysis has never performed so far !

$\bar{D}^{(*)}B$ Interaction: Meson exchange potential

- Effective Lagrangian with heavy quark symmetry

R. Casalbuoni *et al.*, Phys.Rept.**281** (1997)145, Y.-R.Liu and M.Oka, PRD**85**(2012)014015

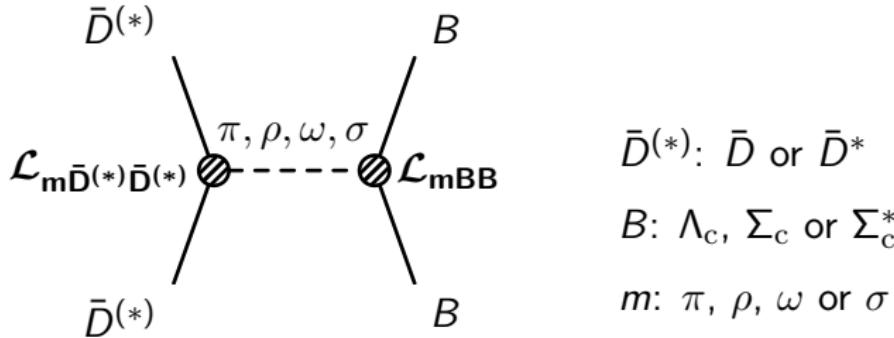


Fig: Meson exchange diagram

$$V_{\bar{D}^{(*)}B - \bar{D}^{(*)}B}^\pi = G \left[\vec{\mathcal{O}}_1 \cdot \vec{\mathcal{O}}_2 C(r) + S_{\mathcal{O}_1 \mathcal{O}_2} T(r) \right]$$

$C(r)$: Central force, $T(r)$: Tensor force

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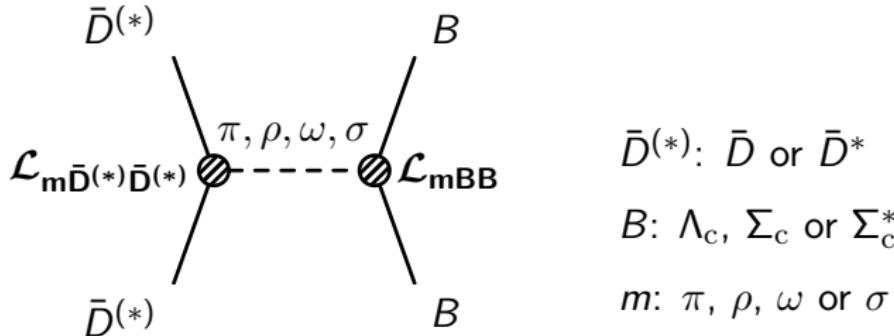


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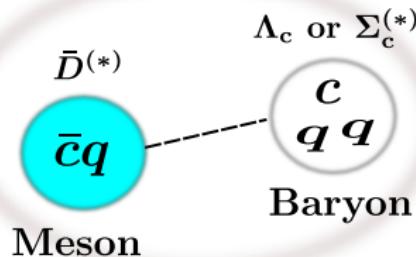
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- Form factor with common cutoff $\Lambda \leftarrow$ Free parameter

$$F(\Lambda, \vec{q}) = \frac{\Lambda^2 - m_\alpha^2}{\Lambda^2 + |\vec{q}|^2} \quad (\text{fixed by the observed mass of } P_c)$$

Results of $\bar{D}^{(*)}B$ states (2-body)



$$\bar{D}^{(*)}\Lambda_c - \bar{D}^{(*)}\Sigma_c^{(*)}$$

Exotic states ($c\bar{c}qqq$)

Bound state and Resonance

- We solve the coupled-channel Schrödinger equations with $J^P = 3/2^\pm, 5/2^\pm$ and isospin $I = 1/2$.
- Interaction: $\pi\rho\omega\sigma$ exchange potentials

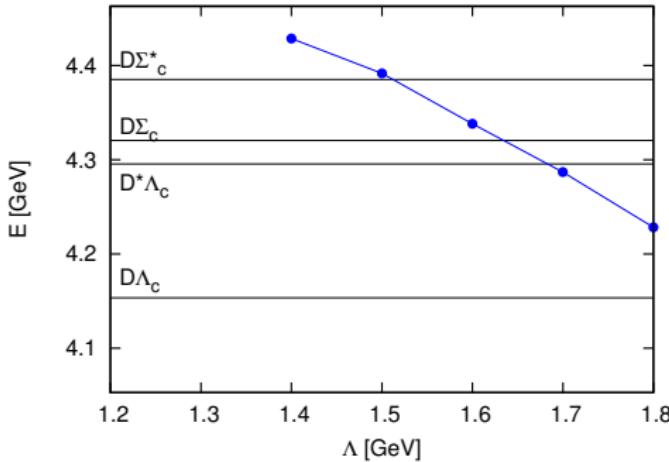
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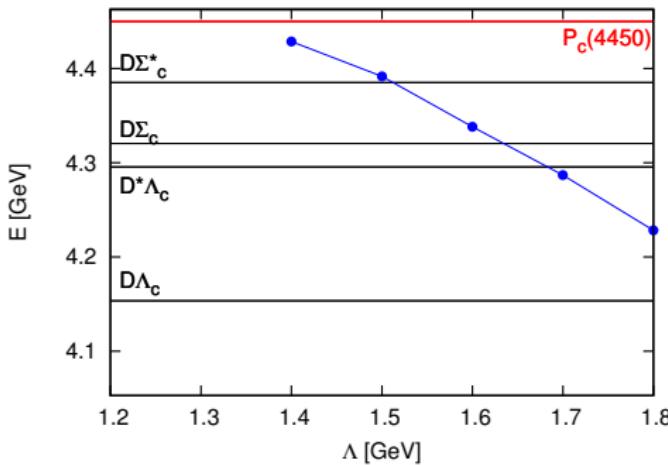
→ In our results, only **the $J^P = 5/2^-$ state** appears above the $\bar{D}\Sigma_c^*$ threshold!



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$P_c^+(4450)$:

$$M = 4449.8 \pm 1.7 \pm 2.5 \text{ MeV}$$

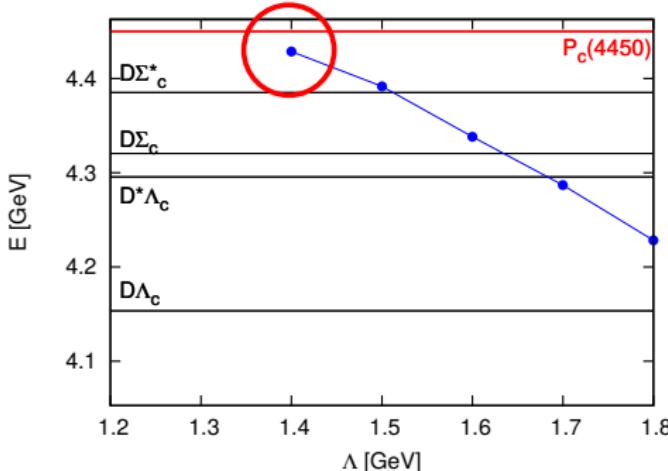
$J^P = 5/2^-$ state:

$$M = 4428.6 \text{ MeV} \text{ in } \Lambda = 1400 \text{ MeV}$$

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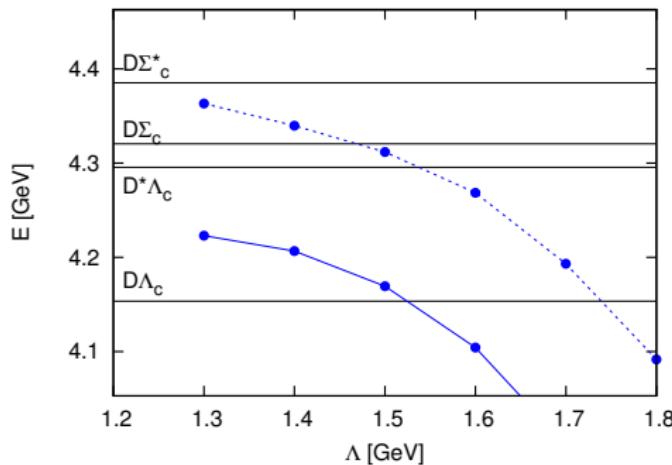
Cutoff $\Lambda = 1400$ MeV, J^P of $P_c^+(4450) = 5/2^-$

What is J^P of $P_c^+(4380)$?

- ▷ $P_c^+(4450)$: $J^P = 5/2^- \Rightarrow J^P$ of $P_c^+(4380)$ is **3/2⁺!**

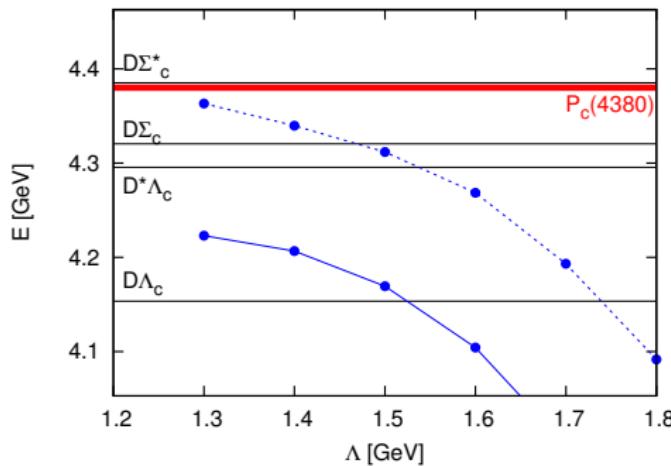
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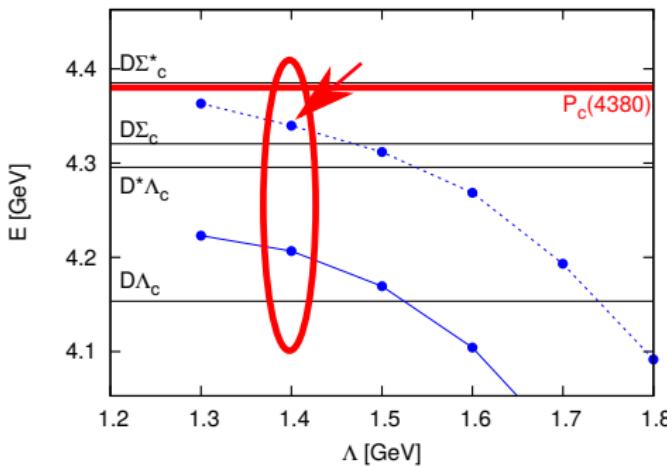


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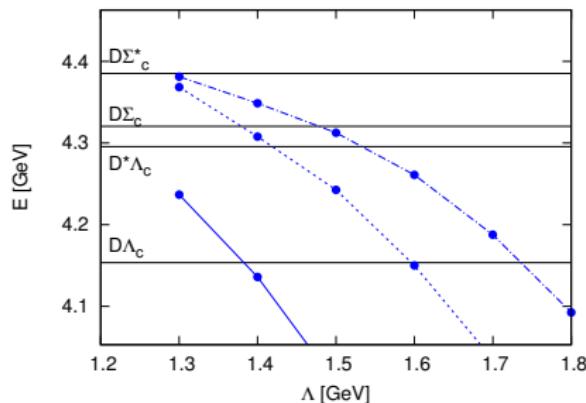
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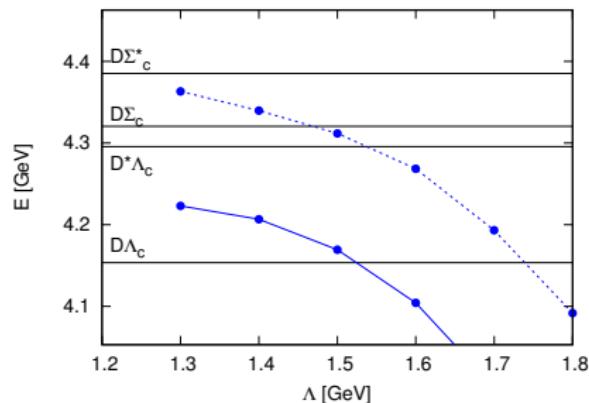
Cutoff $\Lambda = 1400$ MeV

Other predicted states

(i) $J^P = 3/2^-$



(ii) $J^P = 3/2^+$



- In $\Lambda = 1400$ MeV,

$J^P = 3/2^-$: 4136.0 MeV, 4307.9 MeV and 4348.7 MeV

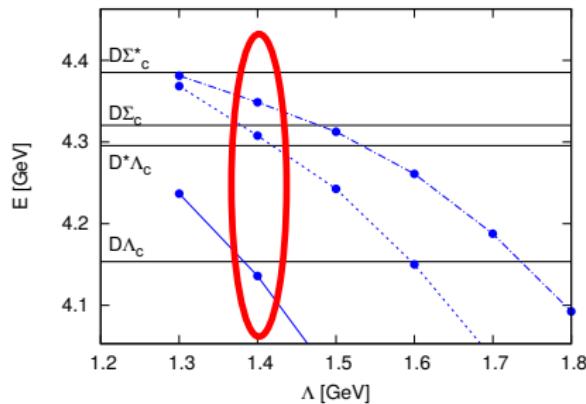
$J^P = 3/2^+$: 4206.7 MeV

New states are predicted!

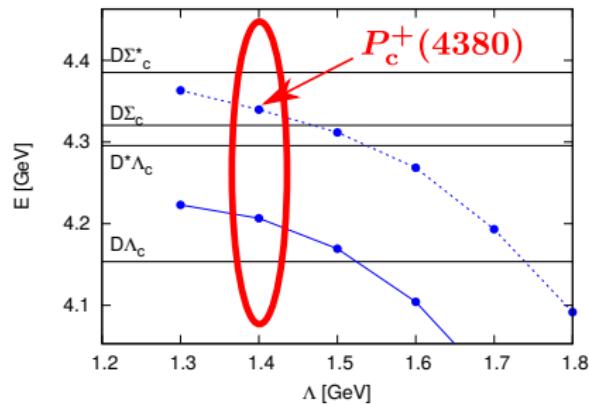
(can be decayed to $J/\psi p$, $\bar{D}^{(*)}\Lambda_c, \dots$)

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Summary

Subject: Hidden-charm meson-baryon molecules
with full-channel coupling



- **Meson-baryon thresholds** closed to the observed pentaquarks are considered.
→ **Full-coupled channel analysis** of $\bar{D}^{(*)}\Lambda_c - \bar{D}^{(*)}\Sigma_c^{(*)}$
- The meson exchange potential respecting to **the heavy quark spin symmetry** is employed.
- The J^P assignment of $P_c^+(4380)$ and $P_c^+(4450)$ is **$3/2^+$** and **$5/2^-$** , respectively.
- New states are predicted in $J^P = 3/2^\pm$.

Outlook

- Coupling to $J/\psi p$, cutoff Λ , $1/m_Q$ correction,...

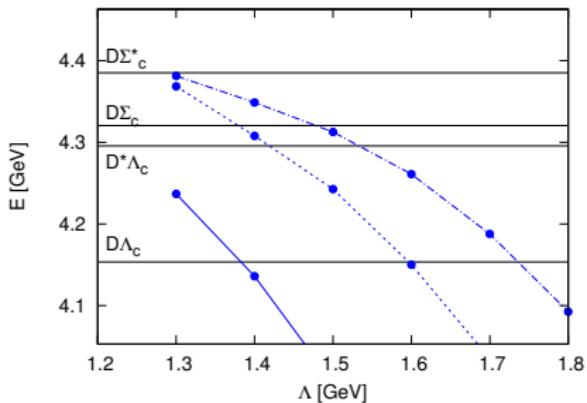
Yasuhiro Yamaguchi and Elena Santopinto , arXiv:1606.08330 [hep-ph]

Back up

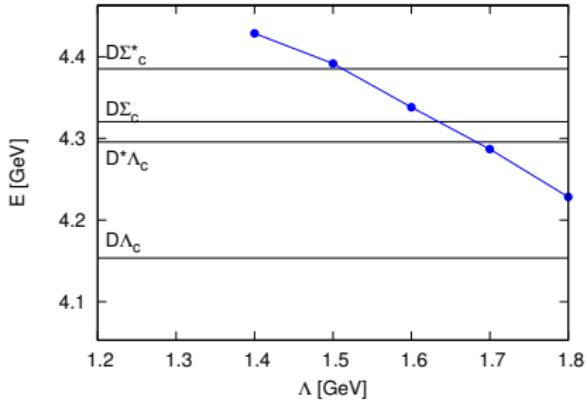
Coupled-Channels

J^P	Channels
$3/2^-$	$\bar{D}\Lambda_c(^2D)$, $\bar{D}^*\Lambda_c(^4S, ^2D, ^4D)$, $\bar{D}\Sigma_c(^2D)$, $\bar{D}\Sigma_c^*(^4S, ^4D)$, $\bar{D}^*\Sigma_c(^4S, ^2D, ^4D)$, $\bar{D}^*\Sigma_c^*(^4S, ^2D, ^4D, ^6D, ^6G)$
$3/2^+$	$\bar{D}\Lambda_c(^2P)$, $\bar{D}^*\Lambda_c(^2P, ^4P, ^4F)$, $\bar{D}\Sigma_c(^2P)$, $\bar{D}\Sigma_c^*(^4P, ^4F)$, $\bar{D}^*\Sigma_c(^2P, ^4P, ^4F)$, $\bar{D}^*\Sigma_c^*(^2P, ^4P, ^6P, ^4F, ^6F)$
$5/2^-$	$\bar{D}\Lambda_c(^2D)$, $\bar{D}^*\Lambda_c(^2D, ^4D, ^4G)$, $\bar{D}\Sigma_c(^2D)$, $\bar{D}\Sigma_c^*(^4D, ^4G)$, $\bar{D}^*\Sigma_c(^2D, ^4D, ^4G)$, $\bar{D}^*\Sigma_c^*(^6S, ^2D, ^4D, ^6D, ^4G, ^6G)$
$5/2^+$	$\bar{D}\Lambda_c(^2F)$, $\bar{D}^*\Lambda_c(^4P, ^2F, ^4F)$, $\bar{D}\Sigma_c(^2F)$, $\bar{D}\Sigma_c^*(^4P, ^4F)$, $\bar{D}^*\Sigma_c(^4P, ^2F, ^4F)$, $\bar{D}^*\Sigma_c^*(^4P, ^6P, ^2F, ^4F, ^6F, ^6H)$
	Thresholds (MeV)
	$\bar{D}\Lambda_c(4153.5)$, $\bar{D}^*\Lambda_c(4295.5)$, $\bar{D}\Sigma_c(4320.5)$, $\bar{D}\Sigma_c^*(4385.1)$, $\bar{D}^*\Sigma_c(4462.5)$, $\bar{D}^*\Sigma_c^*(4527.1)$

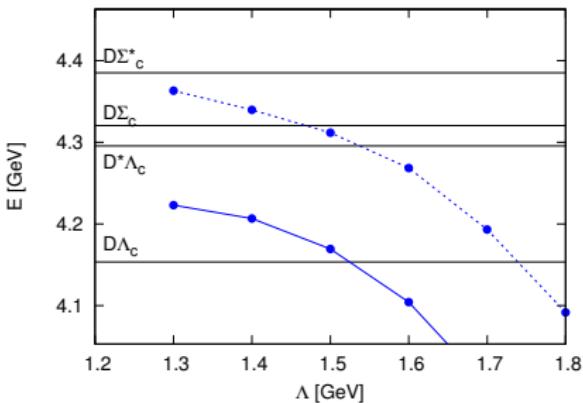
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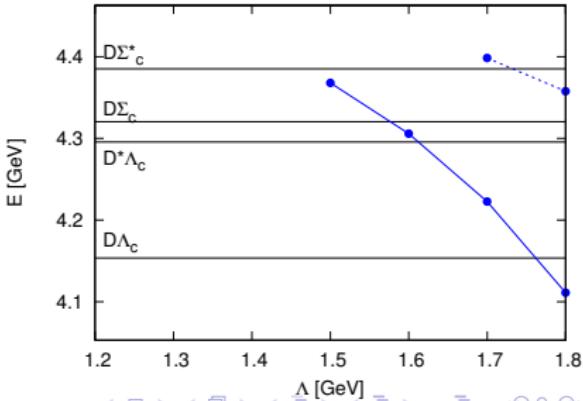


Table : Obtained masses with full channel coupling (Full), without $\bar{D}^{(*)}\Lambda_c$ (w/o $\bar{D}^{(*)}\Lambda_c$) and without large orbital angular momentum ℓ (w/o $\ell > 0$ or w/o $\ell > 1$) in $\Lambda = 1400$ MeV.

J^P	Channels	Mass [MeV]
$3/2^-$	Full	4136.0, 4307.9, 4348.7
	w/o $\bar{D}^{(*)}\Lambda_c$	4278.4, 4400.4
	w/o $\ell > 0$	4220.4, 4376.6
$3/2^+$	Full	4206.7, 4339.7
	w/o $\bar{D}^{(*)}\Lambda_c$	—
	w/o $\ell > 1$	4275.3
$5/2^-$	Full	4428.6
	w/o $\bar{D}^{(*)}\Lambda_c$	—
	w/o $\ell > 0$	—

Table : Comparison of the lowest mass of hidden-charm meson-baryon molecules with $I(J^P) = 1/2(3/2^-)$ by this work with the early works. The obtained masses are shown in the second column in the unit of MeV. The value of this work is in $\Lambda = 1400$ MeV. The third column gives the channels which are considered in those works.

Ref.	Mass [MeV]	Channels
This work	4136.0	$\bar{D}\Lambda_c, \bar{D}^*\Lambda_c, \bar{D}\Sigma_c, \bar{D}\Sigma_c^*, \bar{D}^*\Sigma_c, \bar{D}^*\Sigma_c^*$
PRL 105 (2010)232001	4415	$\bar{D}^*\Sigma_c, \bar{D}^*\Sigma_c^*$ with only <i>S</i> -wave
PRC 84 (2010)015202	4454	$\bar{D}^*\Sigma_c, \bar{D}^*\Sigma_c^*$ with only <i>S</i> -wave
PRD 88 (2013)056012	4334.5	$J/\psi N, \bar{D}^*\Lambda_c, \bar{D}^*\Sigma_c, \bar{D}\Sigma_c^*, \bar{D}^*\Sigma_c^*$ with only <i>S</i> -wave