

# Thermal devices based on Josephson quantum nanocircuits: The era of *coherent* caloritronics

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**COMANCHE**



# Outline

1. Motivations & mission
2. Principle of phase-coherent heat flux control
3. Behavior of a temperature-biased Josephson tunnel junction
4. Josephson heat interferometer
5. Quantum diffractor for thermal flux
6. An ultraefficient thermal rectifier
7. Perspectives

## NEWS & VIEWS

THERMAL PHYSICS

### Quantum interference heats up

A thermal effect predicted more than 40 years ago was nearly forgotten, while a related phenomenon stole the limelight. Now experimentally verified, the effect could spur the development of heat-controlling devices. [SEE LETTER P.401](#)

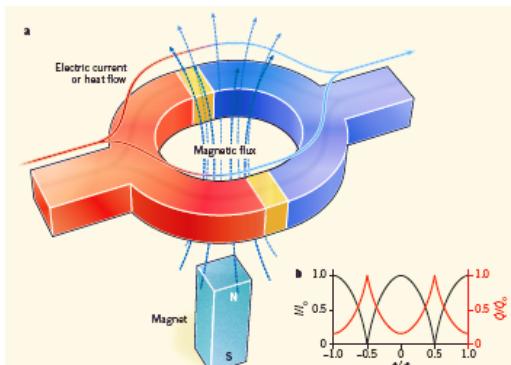
RAYMOND W. SIMMONDS

Wouldn't it be strange to have a material whose thermal conductivity could be changed by a magnetic field? Imagine holding the end of a rod made of this material with the other end placed in a hot fire. As long as a friend keeps a bar magnet away from the rod, you wouldn't burn your hand, but as soon as they apply a magnetic field — ouch! As odd as this seems, the rules of quantum mechanics predict this type of situation for heat transported across a pair of Josephson junctions (devices that consist of two superconductors separated by a thin insulating gap). Writing on page 401, Giazotto and Martinez-Pérez<sup>1</sup> report experiments confirming that this strange phenomenon can actually occur.

In 1962, Brian Josephson made a remarkable discovery<sup>2</sup> as a graduate student, while investigating what would happen if two superconducting metals were placed very close together without touching. He found that the 'Cooper pairs' of electrons that make up the supercurrent (a current that flows without resistance) in superconductors could miraculously jump, or 'tunnel', across the gap without needing an applied electric voltage.

The size of the supercurrent flowing through this 'tunnel barrier' depends on whether the superconductors at either edge of the gap have the same or a different phase — a property of the quantum-mechanical wavefunction that describes the behaviour of Cooper pairs. In a bulk superconductor, any phase changes in the wavefunction between local regions give rise to supercurrent flow. Alternatively, forcing a supercurrent to flow produces phase differences, even across a thin non-conducting or insulating barrier.

Consider also what happens when superconductors form closed circuits, such as loops. Now the total phase that accumulates around the loop when supercurrent flows must be an integer multiple of  $2\pi$ , to maintain the continuity of the wavefunction. This causes magnetic flux in the system to be quantized. The Josephson effect can be combined with this flux quantization to produce a superconducting direct-current quantum interference device<sup>3</sup> (d.c.-SQUID). In these devices, a split



**Figure 1 |** A direct-current superconducting quantum interference device (d.c.-SQUID). **a**, In d.c.-SQUIDs, a superconducting loop contains two Josephson junctions — thin insulating barriers (yellow) sandwiched between the two superconductors (red and blue). **b**, The maximum electrical current ( $I$ , black, left axis) flowing through the device from left to right can be fully modulated by the amount of magnetic flux ( $\Phi$ ) passing through the loop.  $I_c$  is the maximum current that can flow through the d.c.-SQUID;  $\Phi_0$  is the magnetic flux quantum,  $2.07 \times 10^{-15}$  webers. Giazotto and Martinez-Pérez<sup>1</sup> have observed an interference effect for heat flow ( $Q$ , red, right axis).  $Q_0$  is the maximum total heat-flow current through a d.c.-SQUID; the total amount of heat passing through the device can also be modulated by an applied magnetic flux.

superconducting path with two Josephson junctions can sustain a maximum supercurrent, the amplitude of which can be modulated by the amount of magnetic flux piercing the loop (Fig. 1). Such d.c.-SQUIDS are among the most sensitive detectors of magnetic flux ever created and have found many practical applications<sup>4</sup>.

In addition to the phase-dependent supercurrent, Josephson discovered<sup>2</sup> two other currents that are present when a finite voltage difference exists across a junction. These currents were caused by the tunnelling of quasiparticles (lone electrons from broken Cooper pairs) or of quasiparticles with Cooper pairs. The first type was similar to the flow of electrons through normal metal–metal junctions, but the second type of current was rather odd: it involved a dynamic

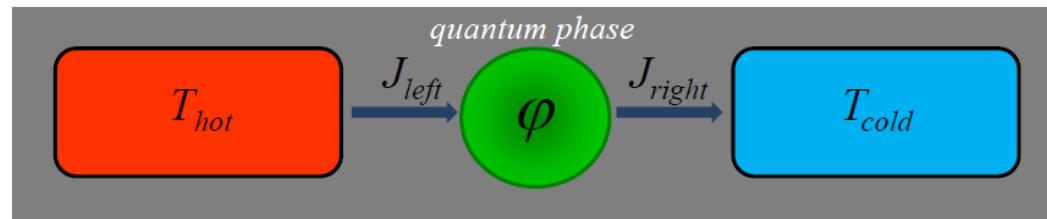
process in which the tunnelling occurred in conjunction with processes for breaking and recombining Cooper pairs. Because Cooper pairs are involved, this current should exhibit interference effects analogous to those seen in d.c.-SQUIDS (in which differences in the wavefunction's accumulated phase along the two paths of a loop create constructive or destructive interference). But electrical experiments that clearly quantify the behaviour of this 'interference current' have remained elusive<sup>5</sup>.

What does all this talk of electrical currents have to do with thermal properties? Well, according to the Wiedemann–Franz law, a metal's thermal conductivity is proportional to its electrical conductivity (and to temperature). This is because electrons can transport some of the heat in a metal. Only three years after

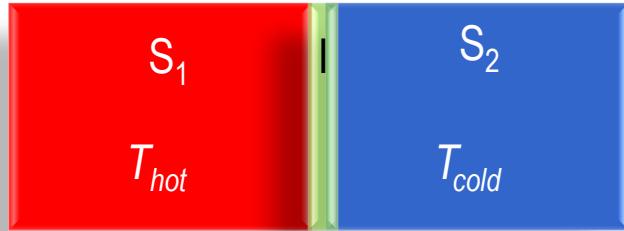
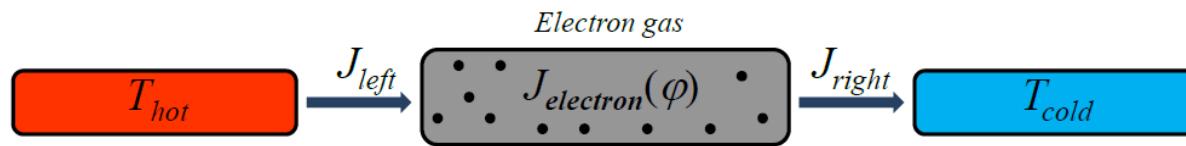
## Motivations & mission

- Set the experimental ground for a challenging **new branch of science**: the *coherent caloritronics*, i.e., the complementary of coherent electronics
- Phase-manipulate & master heat transfer in a solid-state environment
- Provide **original & novel approaches** to realize thermal devices (heat transistors, splitters, diodes, refrigerators, exotic quantum circuits)
- Address & understand **fundamental energy- and heat-related phenomena** at nanoscale (coherent dynamics, heat interference, time-dependent effects, thermodynamics, decoherence)

# Principle of phase-dependent heat current control



Exploitation of quantum phase to control heat current flow



Temperature-biased Josephson tunnel junction

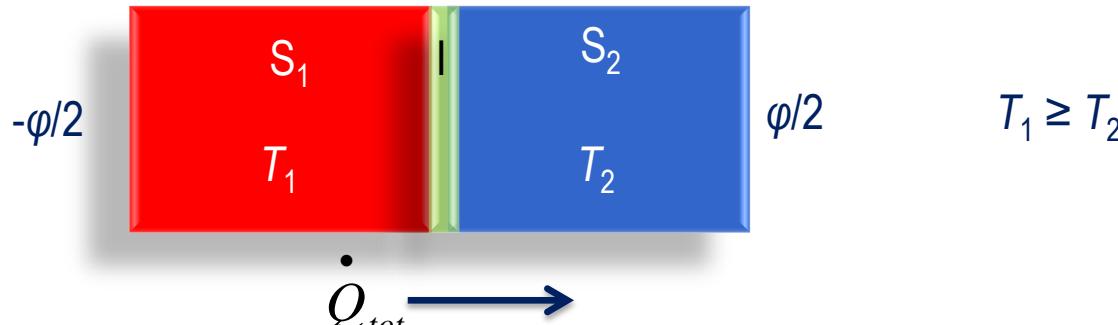


Heat current is predicted to be **phase dependent** and **stationary**

Maki and Griffin, PRL 15, 921 (1965);  
 Zhao et al., PRL 91, 077003 (2003);  
 Zhao et al., PRB 69, 134503 (2004)

Roma, 20/05/2015

# Heat current in $T$ -biased Josephson tunnel junctions: theory (i)



$$\dot{Q}_{tot} = \dot{Q}_{qp}(T_1, T_2) - \dot{Q}_{int}(T_1, T_2) \cos(\varphi)$$

$$\dot{Q}_{qp}(T_1, T_2) = \frac{2}{e^2 R_J} \int_0^\infty d\varepsilon \varepsilon \mathcal{N}_1(\varepsilon, T_1) \mathcal{N}_2(\varepsilon, T_2) [f_1(\varepsilon, T_1) - f_2(\varepsilon, T_2)] \quad \text{Quasiparticles heat current}$$

$$\dot{Q}_{int}(T_1, T_2) = \frac{2}{e^2 R_J} \int_0^\infty d\varepsilon \varepsilon \mathcal{M}_1(\varepsilon, T_1) \mathcal{M}_2(\varepsilon, T_2) [f_1(\varepsilon, T_1) - f_2(\varepsilon, T_2)] \quad \text{Interference heat current}$$

$$\mathcal{N}_{1(2)}(\varepsilon, T) = |\varepsilon| / \sqrt{\varepsilon^2 - \Delta_{1(2)}(T)^2} \Theta[\varepsilon^2 - \Delta_{1(2)}(T)^2]$$

$$\mathcal{M}_{1(2)}(\varepsilon, T) = \Delta_{1(2)}(T) / \sqrt{\varepsilon^2 - \Delta_{1(2)}(T)^2} \Theta[\varepsilon^2 - \Delta_{1(2)}(T)^2]$$

$$f_i(\varepsilon, T_i) = [1 + \exp(\varepsilon/k_B T_i)]^{-1}$$

$$\begin{cases} \dot{Q}_{qp} = 0 & \text{if } T_1 = T_2 \\ \dot{Q}_{int} = 0 & \end{cases}$$

$$\dot{Q}_{int} = 0 \quad \text{if } S_1 \text{ or } S_2 \text{ are in the normal state}$$

Maki and Griffin, PRL **15**, 921 (1965);  
 Guttman et al., PRB **55**, 12691 (1997);  
 Zhao et al., PRL **91**, 077003 (2003)

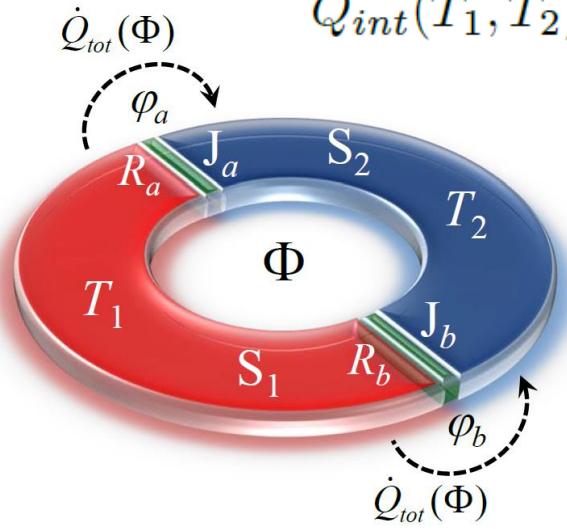
Roma, 20/05/2015

# Temperature-biased DC-SQUID: theory (i)

$$\dot{Q}_{tot} = \dot{Q}_{qp}(T_1, T_2) - \dot{Q}_{int}(T_1, T_2, \varphi_a, \varphi_b)$$

$$\dot{Q}_{qp}(T_1, T_2) = \dot{Q}_{qp}^a(T_1, T_2) + \dot{Q}_{qp}^b(T_1, T_2)$$

$$\dot{Q}_{int}(T_1, T_2) = \dot{Q}_{int}^a(T_1, T_2) \cos \varphi_a + \dot{Q}_{int}^b(T_1, T_2) \cos \varphi_b$$



$$\varphi_a + \varphi_b + 2\pi\Phi/\Phi_0 = 2k\pi$$

$$I_J^a \sin \varphi_a = I_J^b \sin \varphi_b$$

$$\cos \varphi_a = \frac{r + \cos(2\pi x)}{\sqrt{1 + r^2 + 2r\cos(2\pi x)}}$$

$$\cos \varphi_b = \frac{1 + r\cos(2\pi x)}{\sqrt{1 + r^2 + 2r\cos(2\pi x)}}.$$

$$x = \Phi/\Phi_0$$

$$r = I_J^a / I_J^b$$

(with  $0 \leq r \leq 1$ )

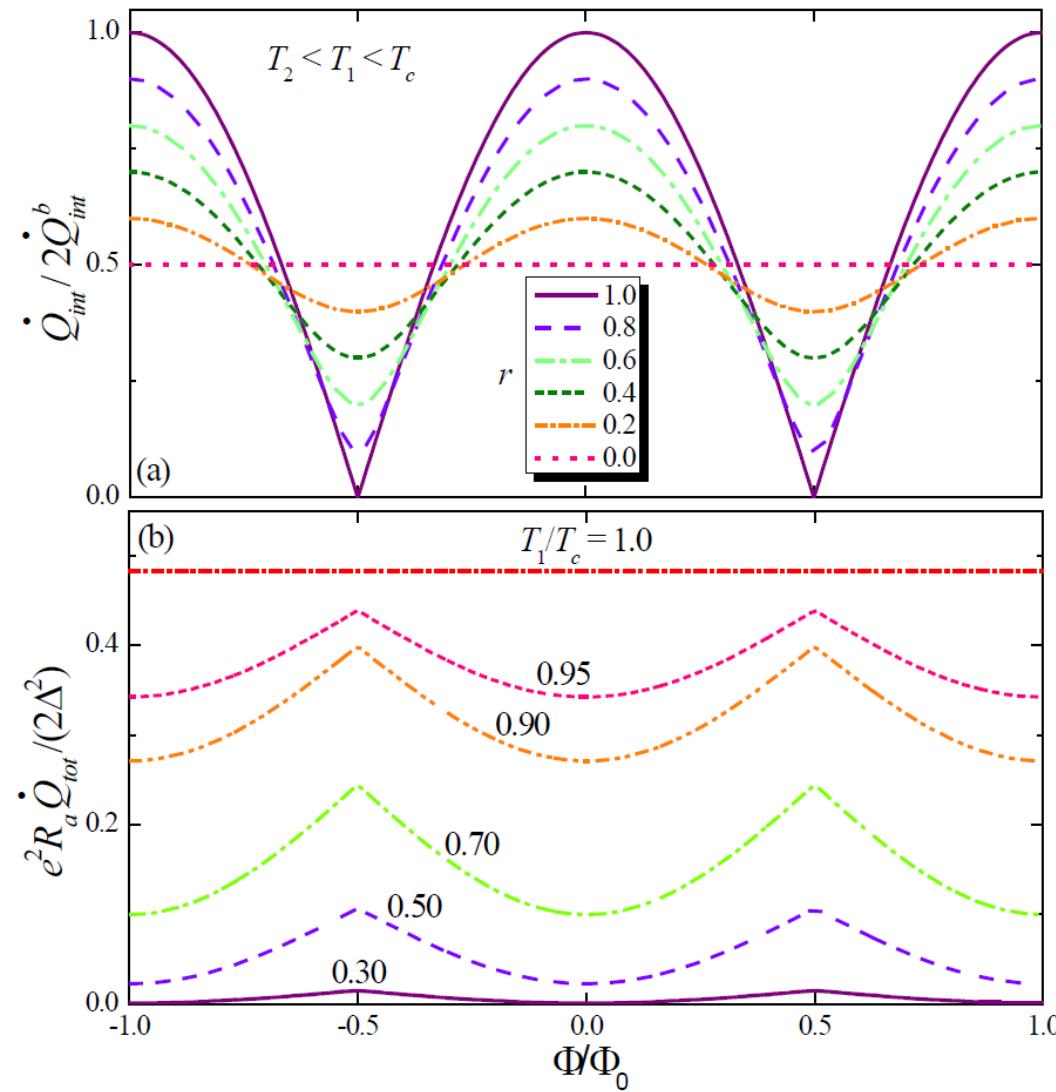
Symmetric SQUID

$$\dot{Q}_{int} = \dot{Q}_{int}^b(T_1, T_2) \sqrt{1 + r^2 + 2r\cos\left(\frac{2\pi\Phi}{\Phi_0}\right)}$$



$$\dot{Q}_{int} = 2\dot{Q}_{int}^b(T_1, T_2) \left| \cos\left(\frac{\pi\Phi}{\Phi_0}\right) \right|$$

# Temperature-biased DC-SQUID: theory (ii)



Role of critical current asymmetry

Maximum

$$\dot{Q}_{int}^b(1 + r)$$

Minimum

$$\dot{Q}_{int}^b(1 - r)$$

Total heat current behavior  
(symmetric SQUID)

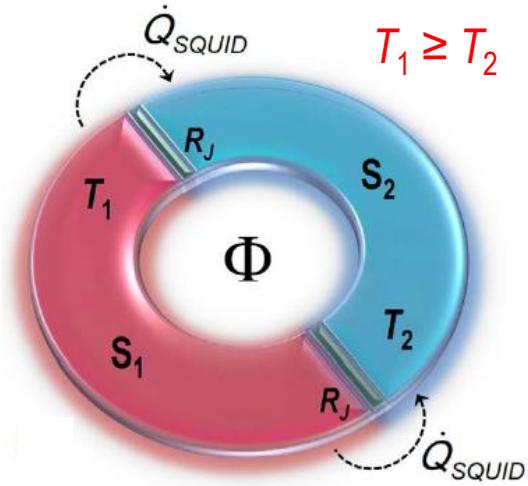
$$T_2 = 0.1 T_c$$

# “Josephson heat interferometer”: setup (i)

## LETTER

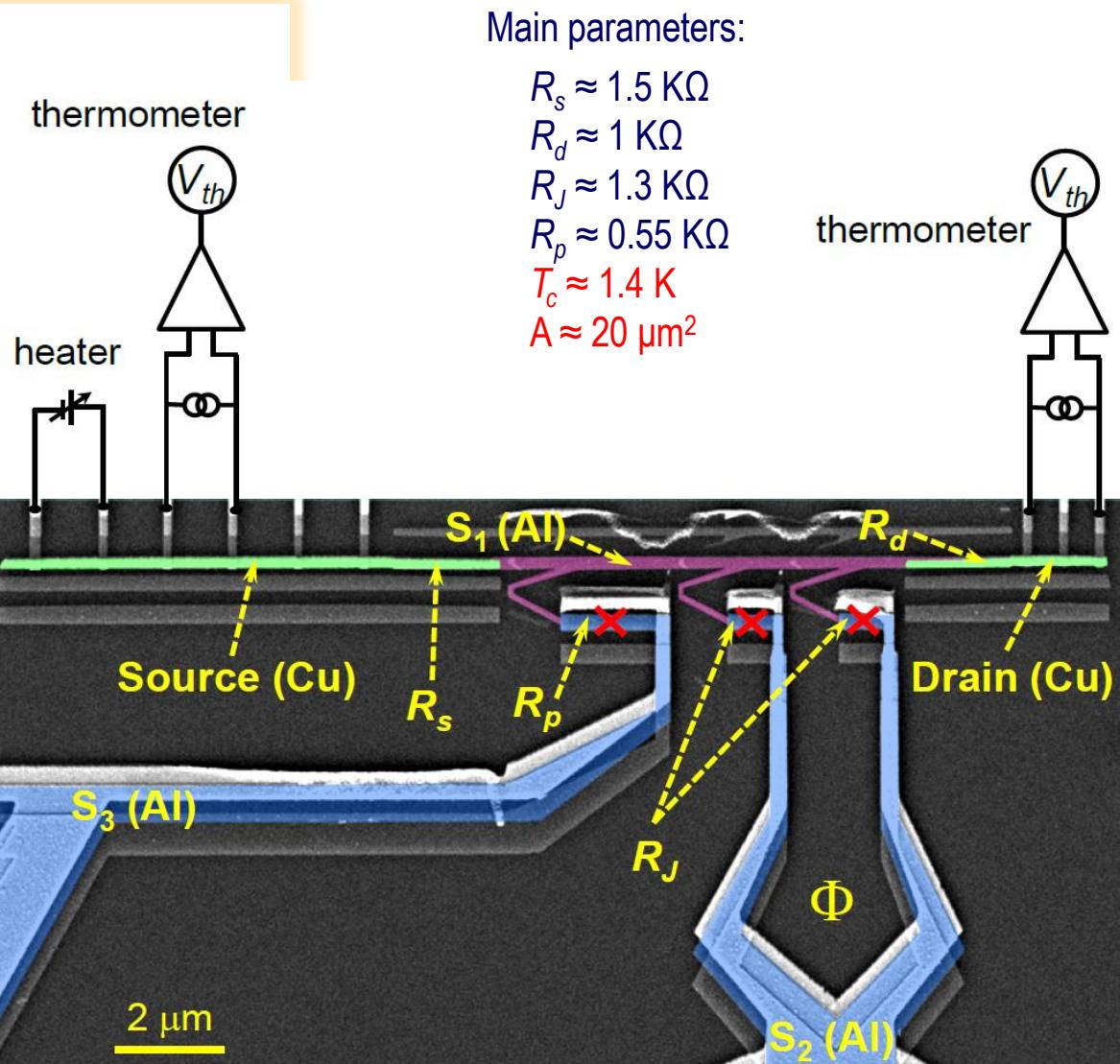
### The Josephson heat interferometer

Francesco Giazotto<sup>1</sup> & María José Martínez-Pérez<sup>1</sup>



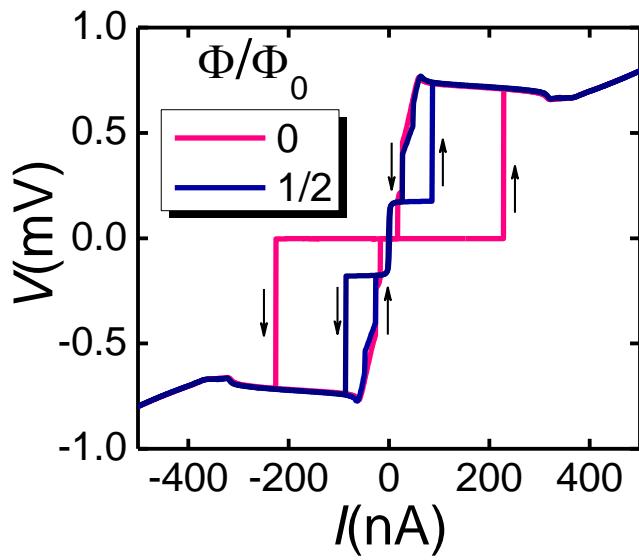
Symmetric SQUID ( $r = 1$ )

$$\dot{Q}_{SQUID}(\Phi) = 2\dot{Q}_{qp} - 2\dot{Q}_{int} \left| \cos \left( \frac{\pi\Phi}{\Phi_0} \right) \right|$$



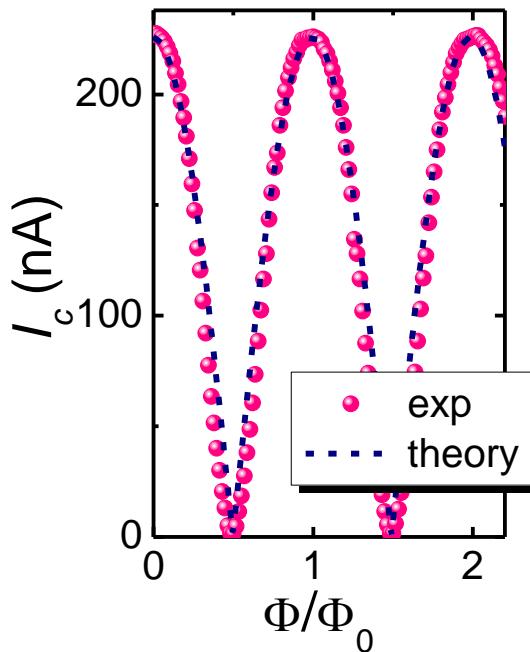
# “Josephson heat interferometer”: setup (ii)

$V$  vs  $I$  chars @ 240 mK



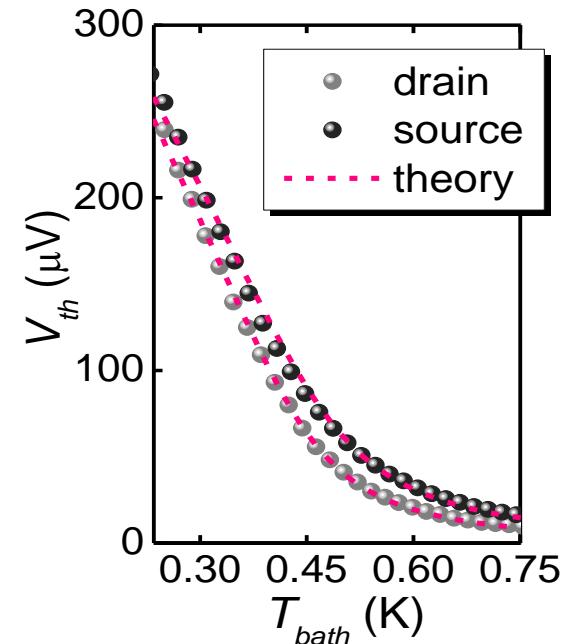
$$I_c \approx 226 \text{ nA}$$

Magnetic interference pattern



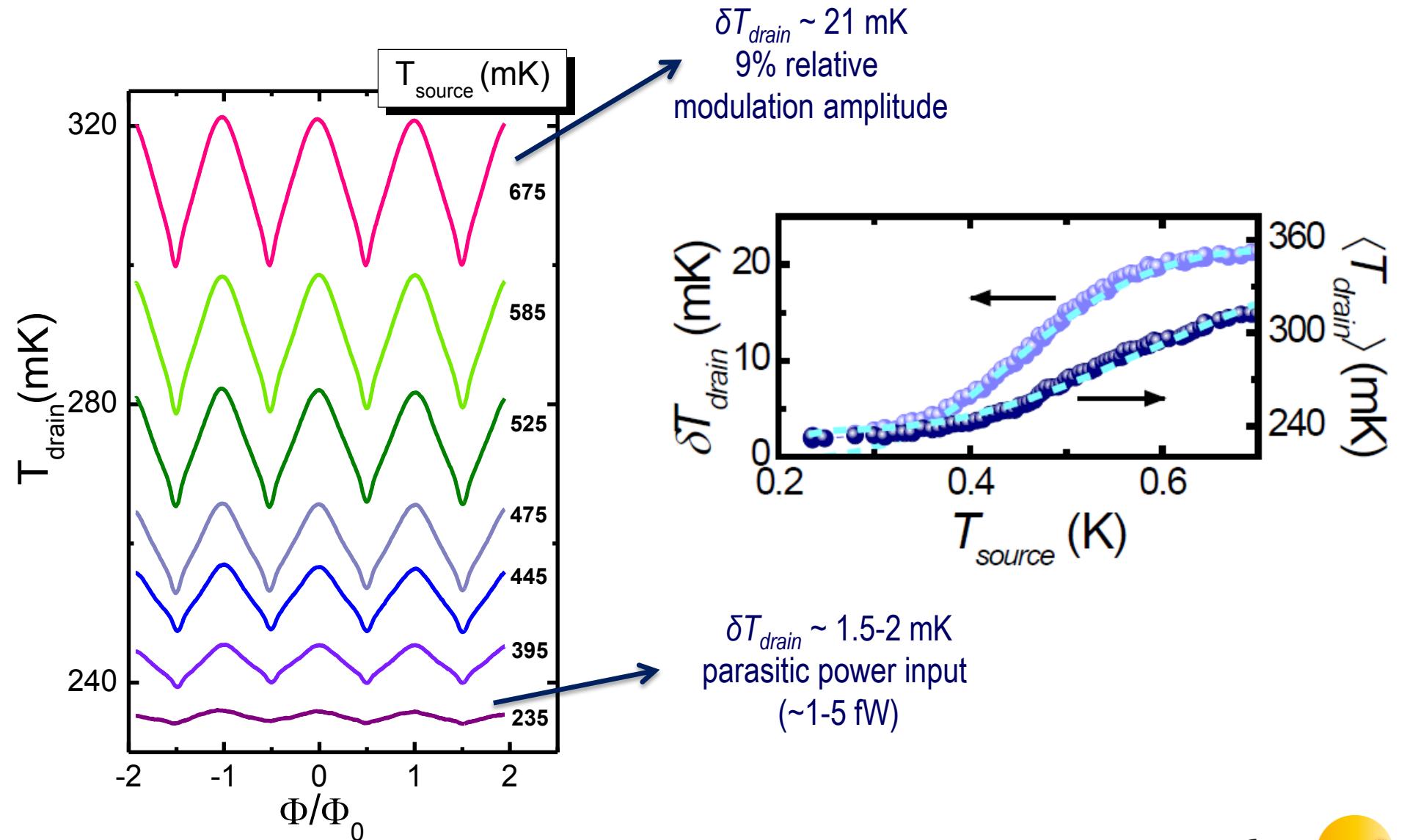
$$\begin{aligned} \alpha &\sim 0.3\% \\ \beta_L &\sim 1.6 \times 10^{-3} \ll 1 \\ L &\sim 15 \text{ pH} \end{aligned}$$

SINIS thermometers  
 $R_{thermo} \approx 25 \text{ K}\Omega$



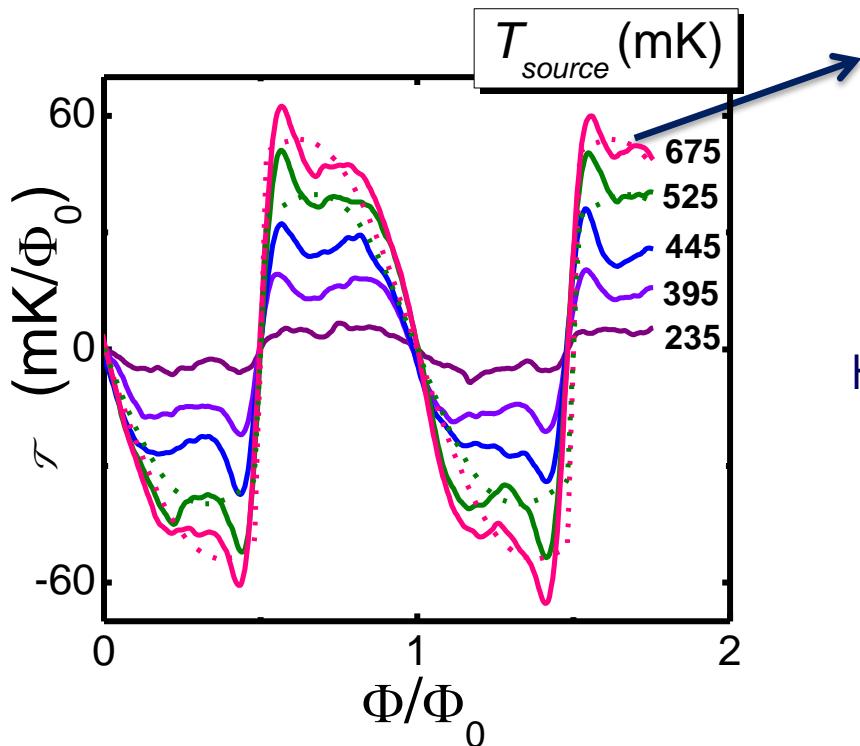
$$I_{bias} \sim 40-70 \text{ pA}$$

# Behavior @ 235 mK (i)



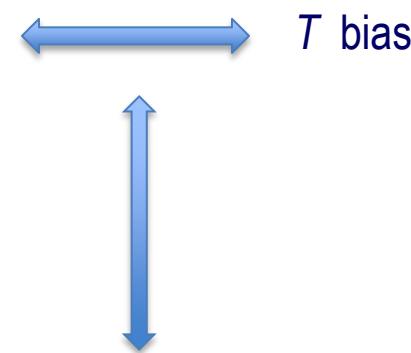
## Behavior @ 235 mK (ii)

$$\mathcal{T} \equiv \partial T_{\text{drain}} / \partial \Phi$$



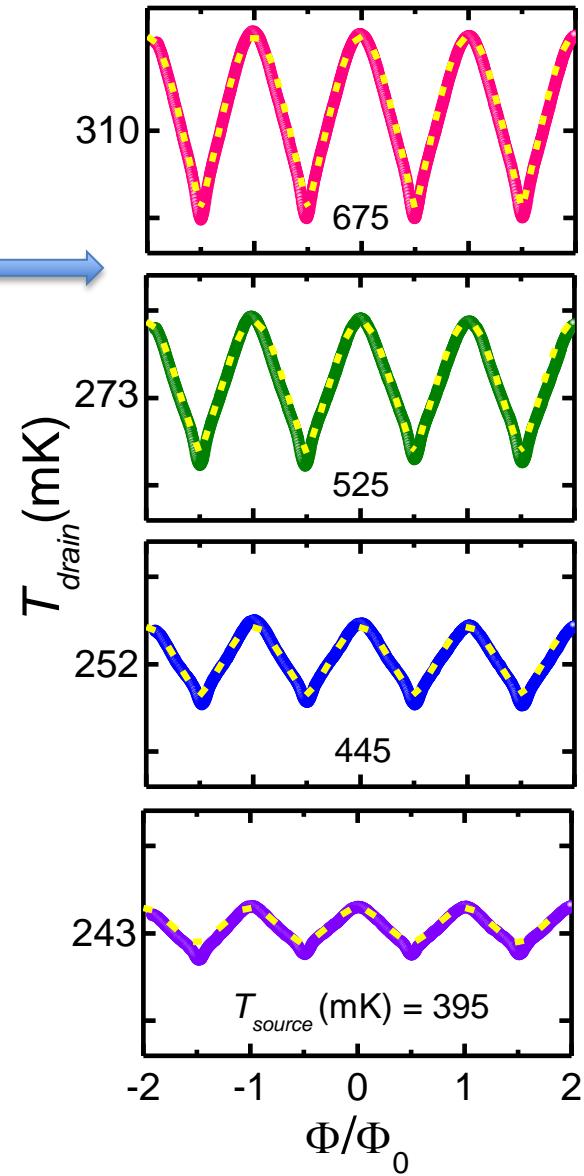
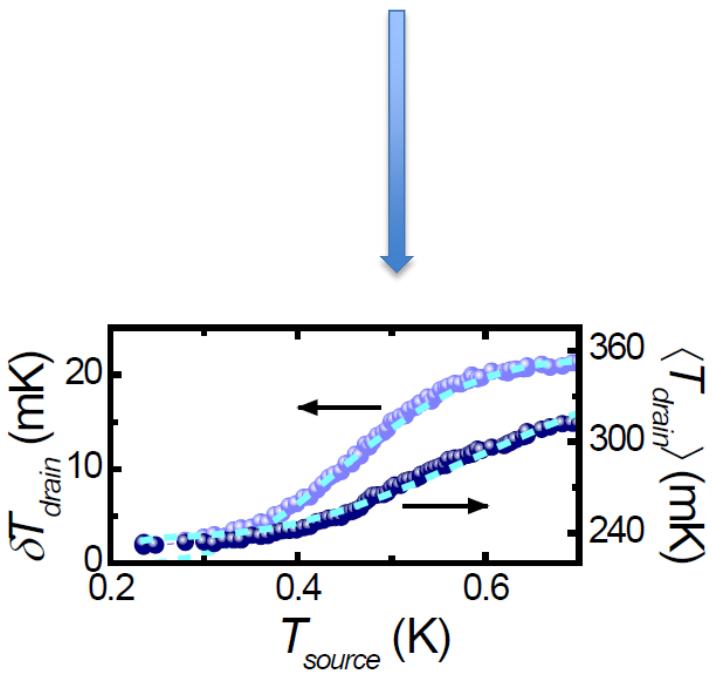
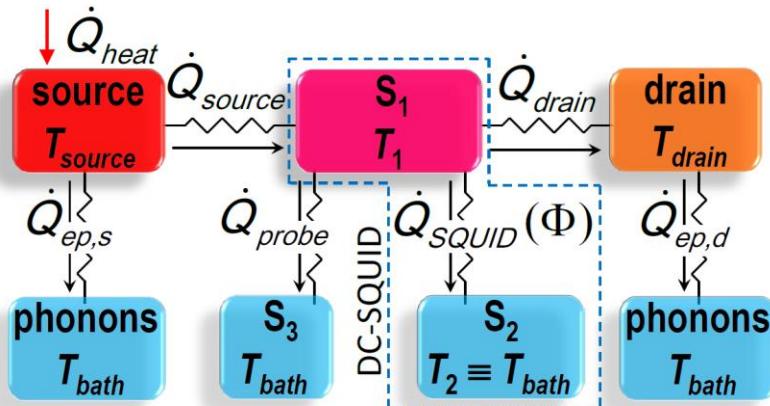
Flux-to-temperature transfer  
function up to  $\sim 60 \text{ mK}/\Phi_0$  @ 675 mK

Heat interference



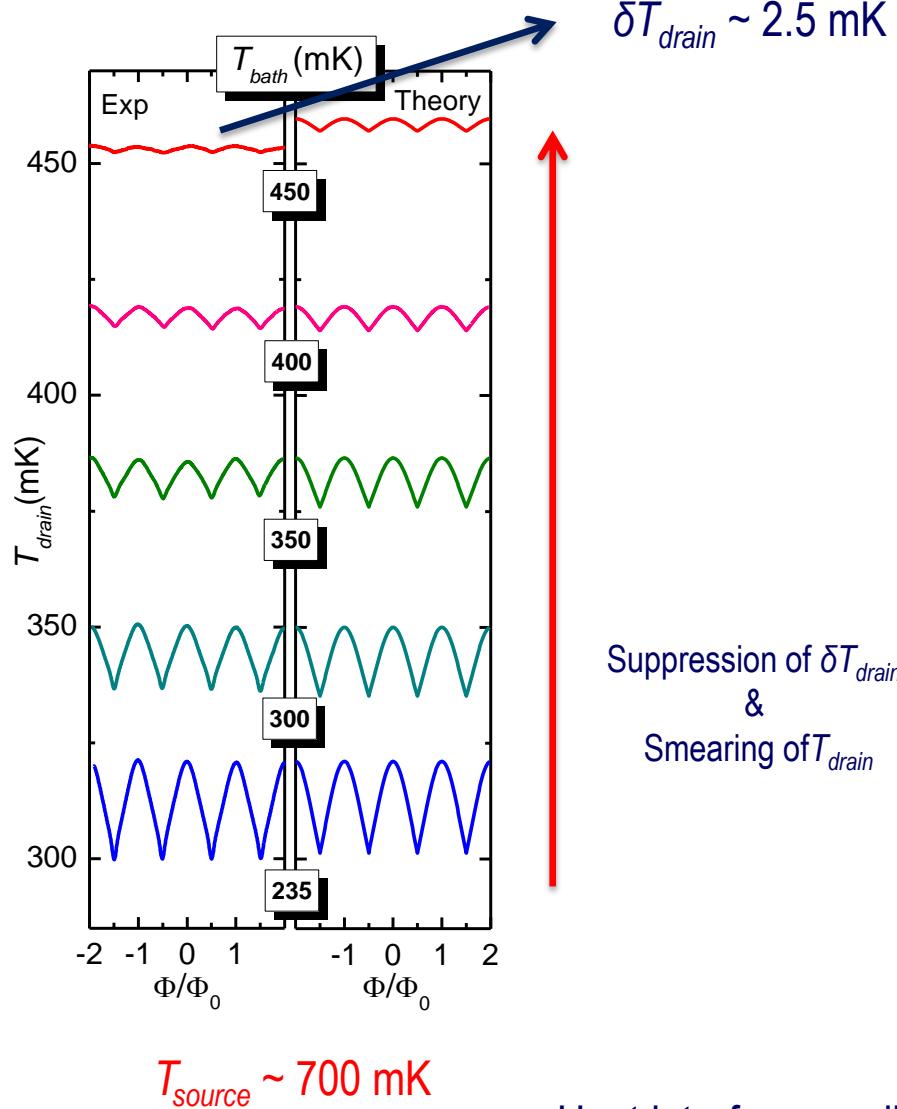
$$\cos(\varphi_0 + 2eV_{\text{SQUID}}t/\hbar) \longleftrightarrow \nu = V_{\text{SQUID}} / \Phi_0$$

# Comparison to theory



Good agreement with theoretical prediction

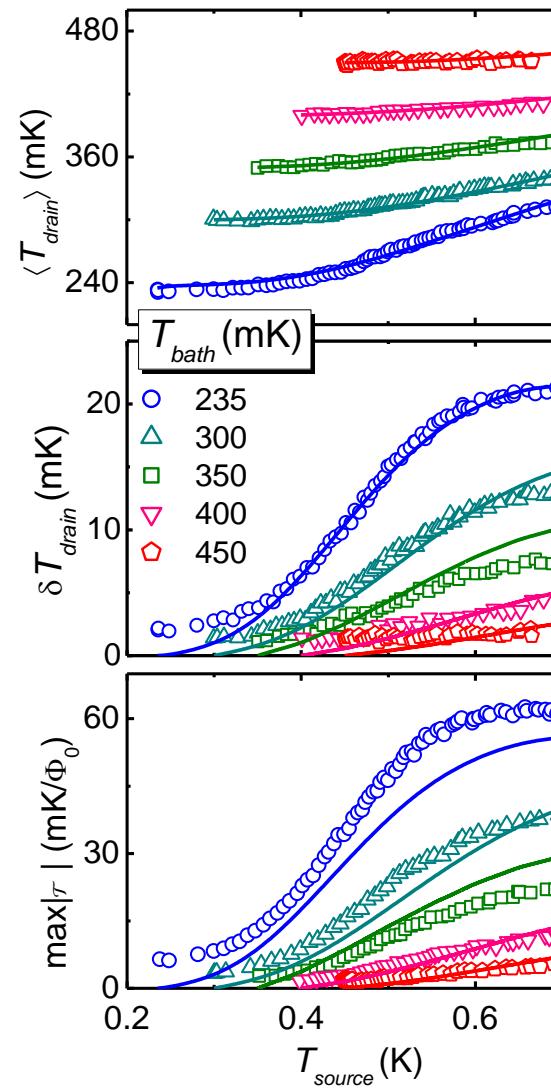
# Heat interferometer: bath temperature dependence



$\delta T_{drain} \sim 2.5 \text{ mK}$

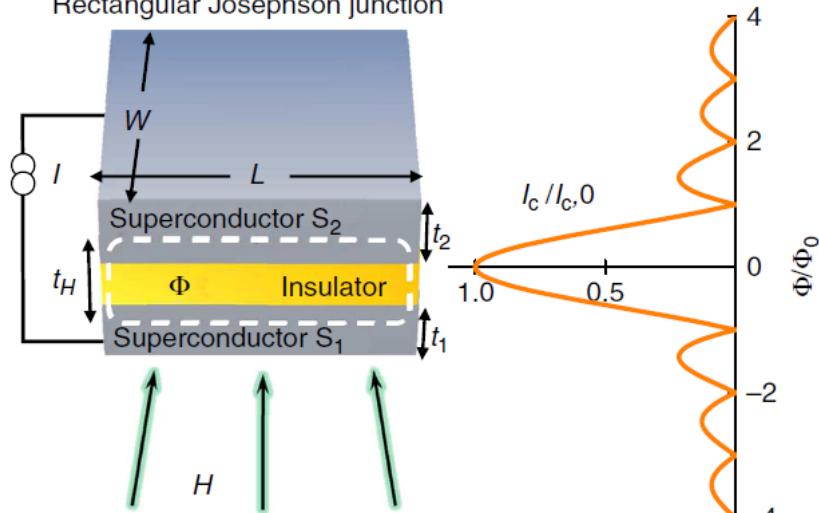
Suppression of  $\delta T_{drain}$   
&  
Smearing of  $T_{drain}$

Heat interference disappears at  $\sim 500 \text{ mK}$



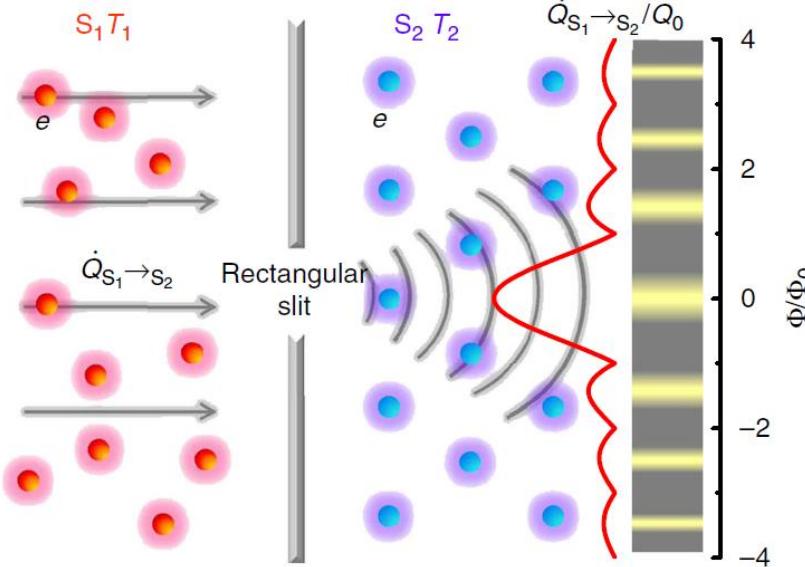
# Electric vs thermal quantum diffraction

**a** Rectangular Josephson junction



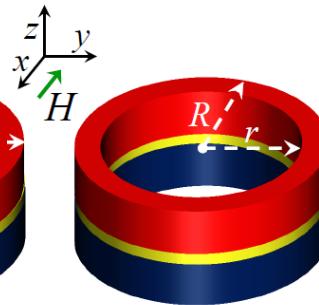
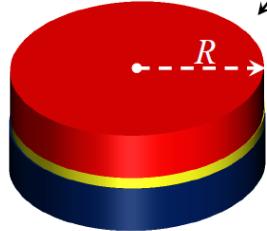
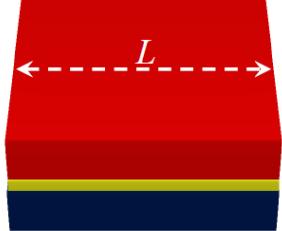
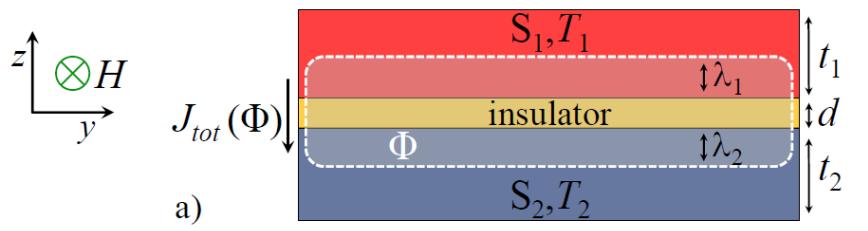
Electric diffraction through  
a rectangular slit

**b**



Diffraction of heat current  
through a rectangular slit

# Heat current quantum diffraction in extended short JJs



$$\tilde{t} = d + \lambda_1 \tanh \frac{t_1}{2\lambda_1} + \lambda_2 \tanh \frac{t_2}{2\lambda_2}$$

$$L \ll \lambda_J \equiv \sqrt{\frac{\Phi_0 WL}{2\mu_0 I_c \tilde{t}}}$$

Josephson critical current

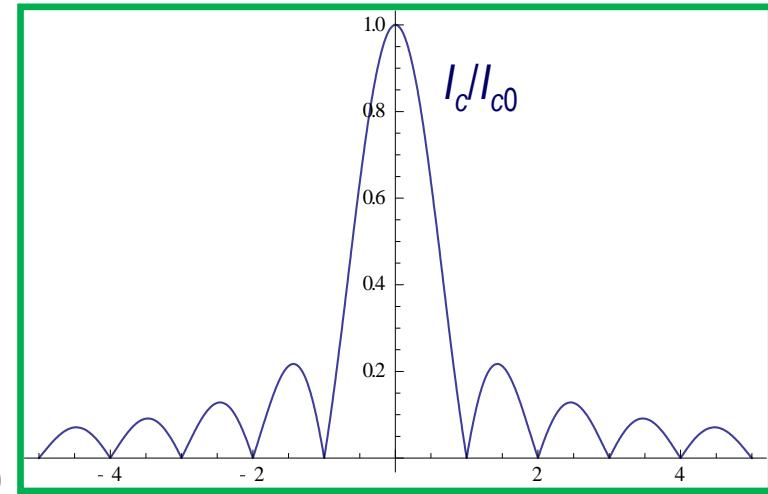
$$I_c(\Phi) = |2I_{c0} \int_{-\infty}^{\infty} f(y) \cos\left(\frac{2\pi\Phi}{\Phi_0} \frac{y}{L}\right) dy|$$

Critical current Fraunhofer pattern for a rectangular JJ

$$\frac{I_c}{I_{c0}} = |\sin(\pi\Phi/\Phi_0)/(\pi\Phi/\Phi_0)|$$

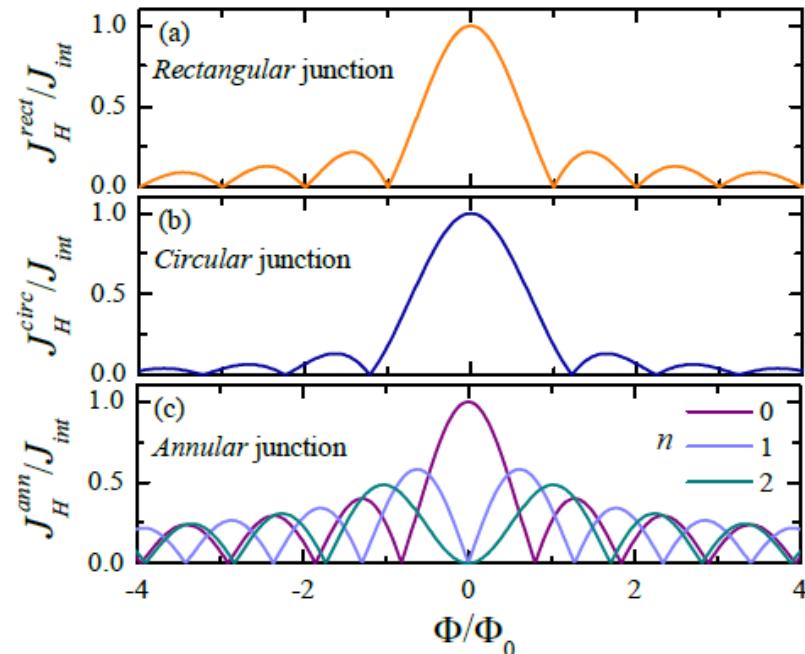


$\Phi/\Phi_0$



# Heat current quantum diffraction in short JJs

$$J_{int}(\Phi) \propto |J_0 \int_{-\infty}^{\infty} g(y) \cos\left(\frac{2\pi\Phi}{\Phi_0} \frac{y}{L}\right) dy|$$



Interference component of thermal current

$$\begin{aligned} I_H(T_1, T_2, H) &= \text{Im} \left\{ e^{i\varphi_0} \int_{-\infty}^{\infty} dy \mathcal{J}(y, T_1, T_2) e^{iky} \right\} \\ &= \sin \varphi_0 \int_{-\infty}^{\infty} dy \mathcal{J}(y) \cos ky, \end{aligned}$$

**Nulling** of the supercurrent

$$\begin{aligned} E_J(T_1, T_2, H) &= E_{J,0} - \frac{\Phi_0}{2\pi} \text{Re} \left\{ e^{i\varphi_0} \int_{-\infty}^{\infty} dy \mathcal{J}(y, T_1, T_2) e^{iky} \right\} \\ &= E_{J,0} - \frac{\Phi_0}{2\pi} \cos \varphi_0 \int_{-\infty}^{\infty} dy \mathcal{J}(y) \cos ky \end{aligned}$$

$$E_{J,0} = \Phi_0 I_c / 2\pi$$

**Minimization** of Josephson coupling energy



$\varphi_0 = m\pi$ , with  $m = 0, \pm 1, \pm 2, \dots$

$\varphi_0$  will undergo a  $\pi$  slip

S. V. Kuplevakhsky and A. M. Glukhov, Phys. Rev. B 73, 024513 (2006)

# A “quantum diffractor” for thermal flux: experimental setup



ARTICLE

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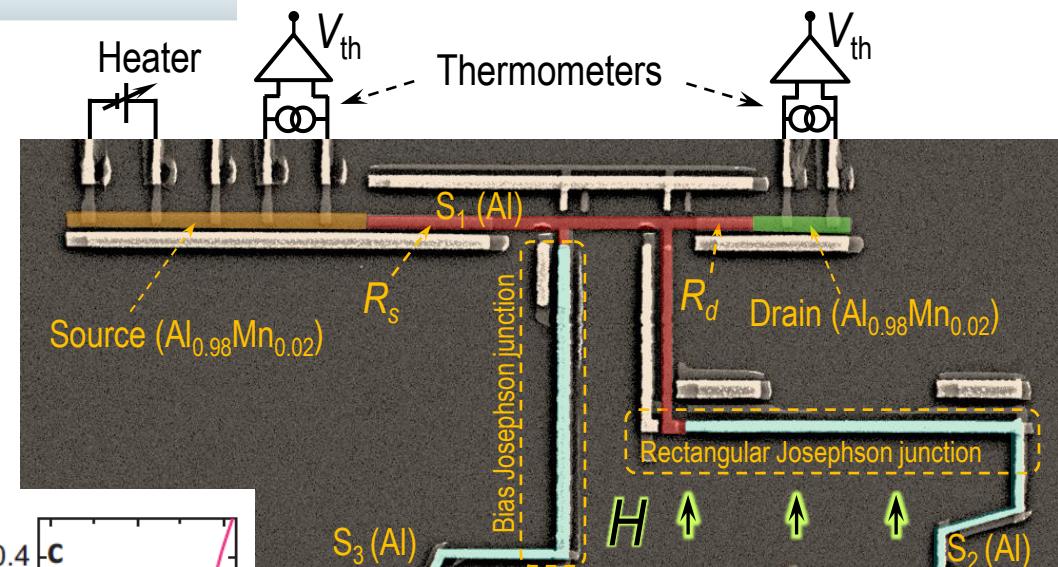
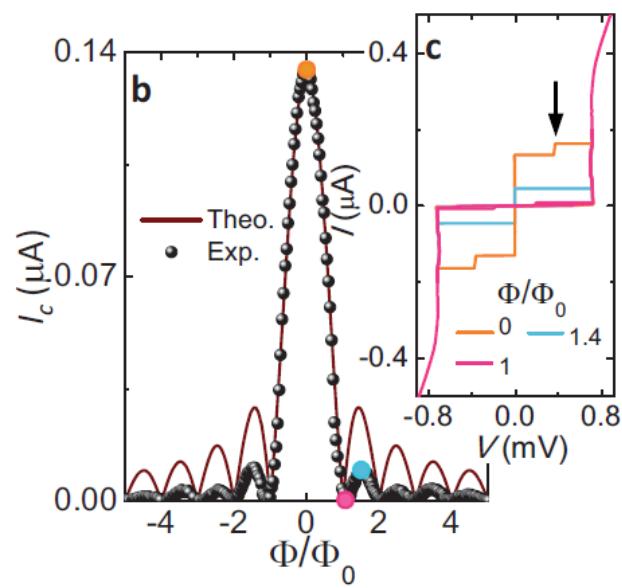
DOI: 10.1038/ncomms4579

## A quantum diffractor for thermal flux

Maria José Martínez-Pérez<sup>1</sup> & Francesco Giazotto<sup>1</sup>

Rectangular JJ

Magnetic interference pattern



$I$  vs  $V$  chars @ 240 mK

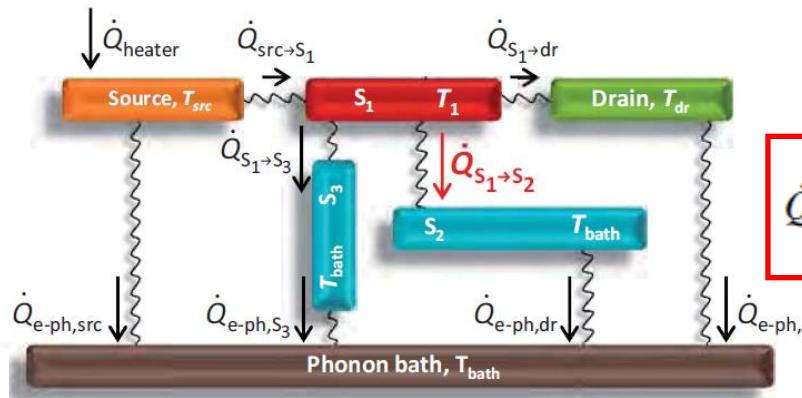
$I_{c,\max} \approx 140 \text{ nA}$

Josephson current behavior

# Thermal model & expected behavior

Negligible Kapitza  
Resistance

$$\downarrow \\ T_{phonon} = T_{bath}$$

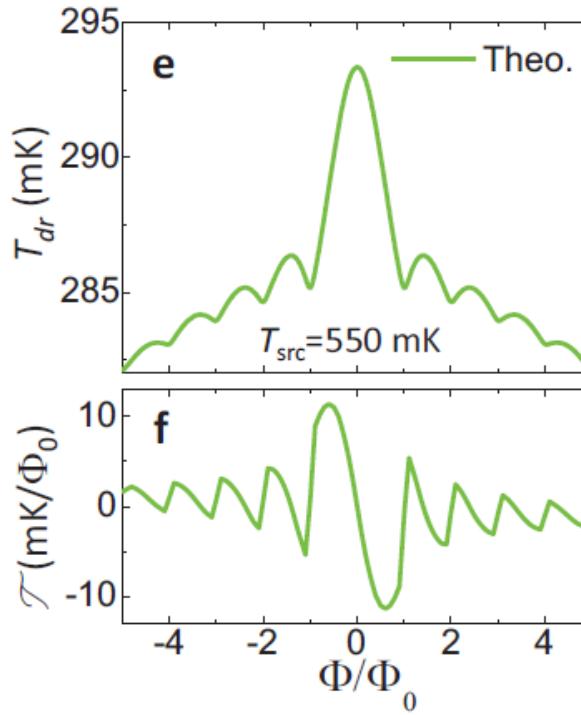


$$\dot{Q}_{S_1 \rightarrow S_2} = \dot{Q}_{qp} - \dot{Q}_{int} \left| \frac{\sin(\pi\Phi/\Phi_0)}{(\pi\Phi/\Phi_0)} \right|$$

The model neglects

- electron-photon coupling
- phonon heat current

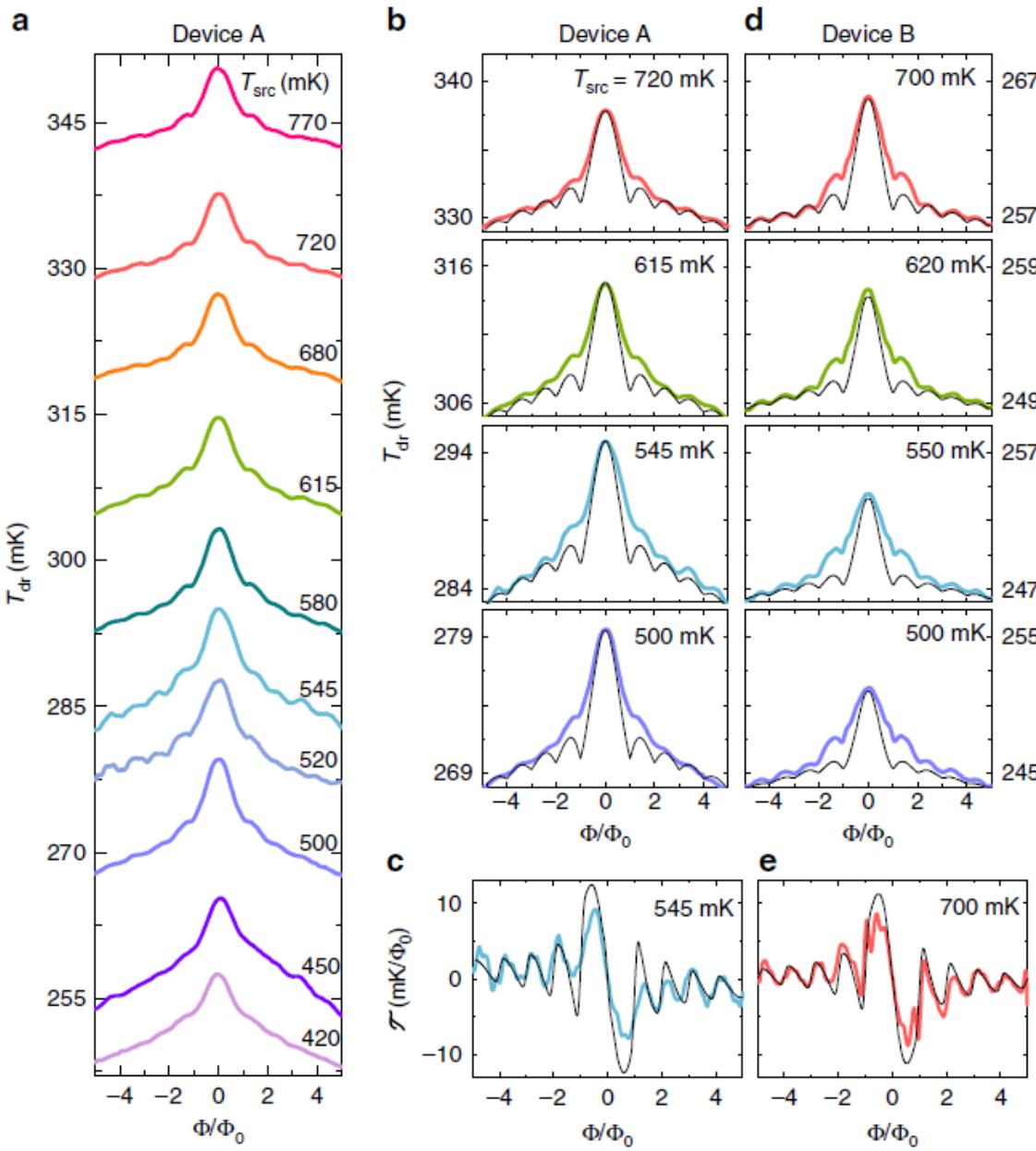
$T_{bath} = 240 \text{ mK}$



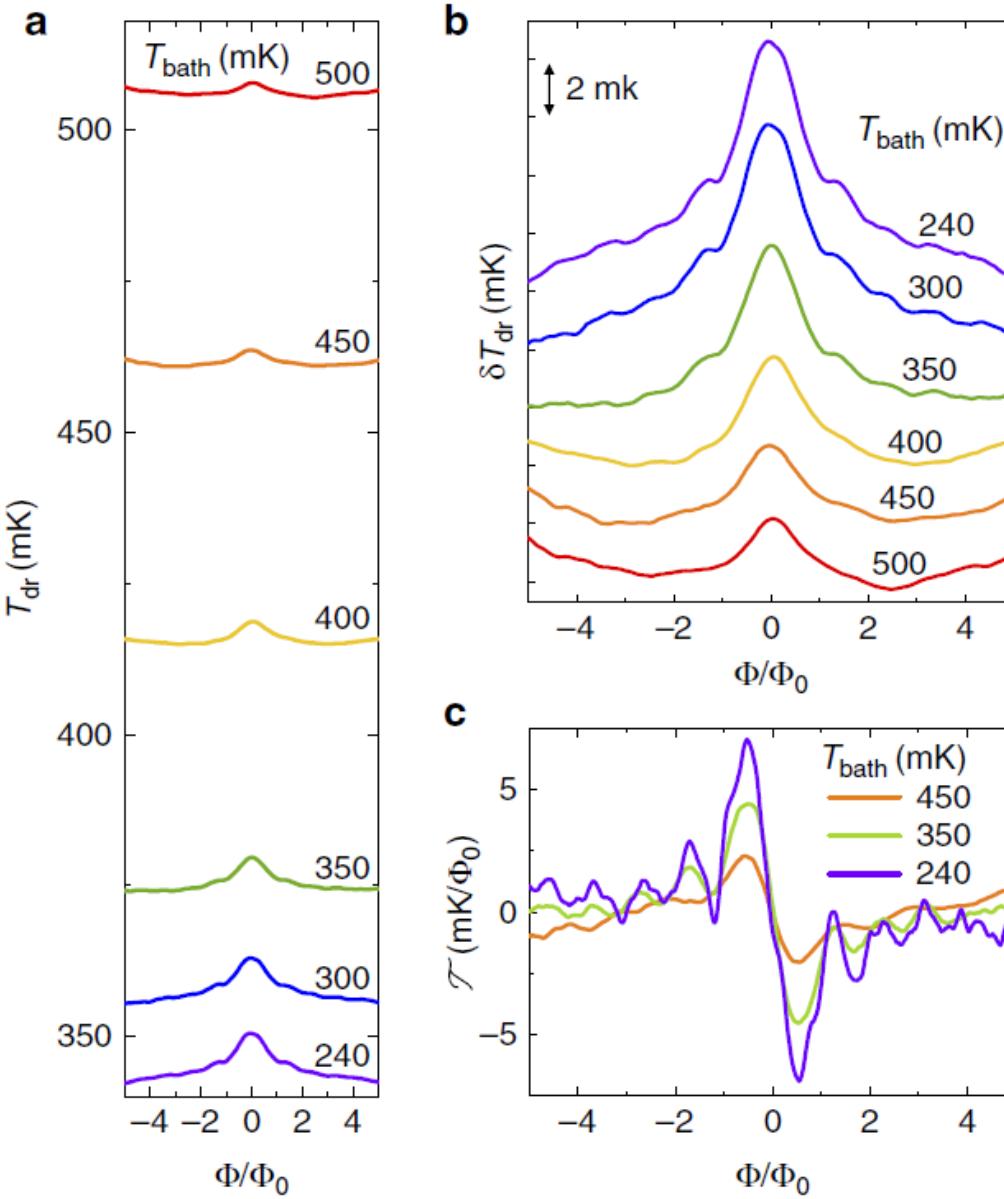
Drain temperature diffraction  
pattern

Flux-to-drain temperature  
transfer function

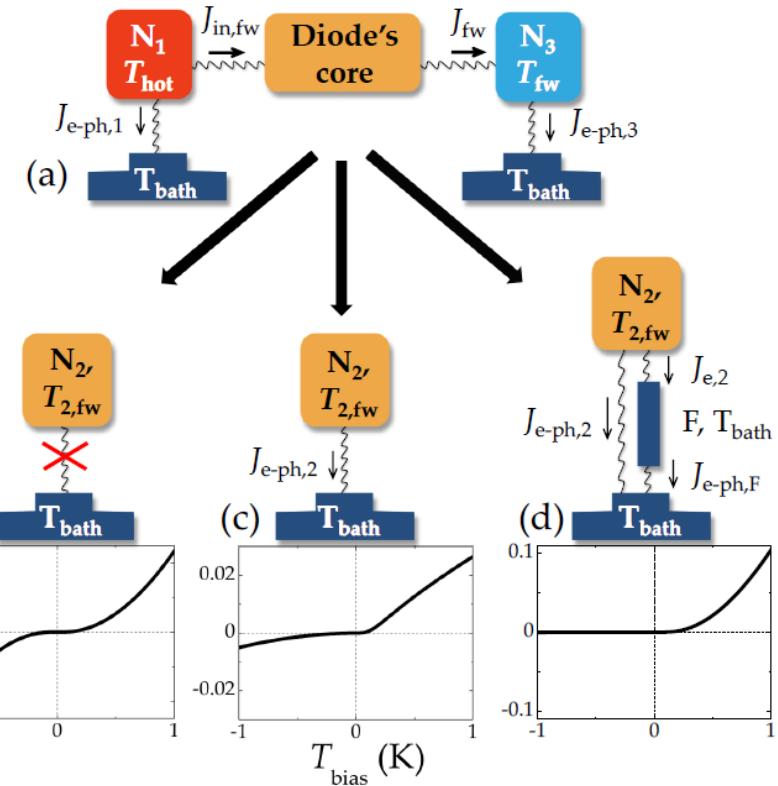
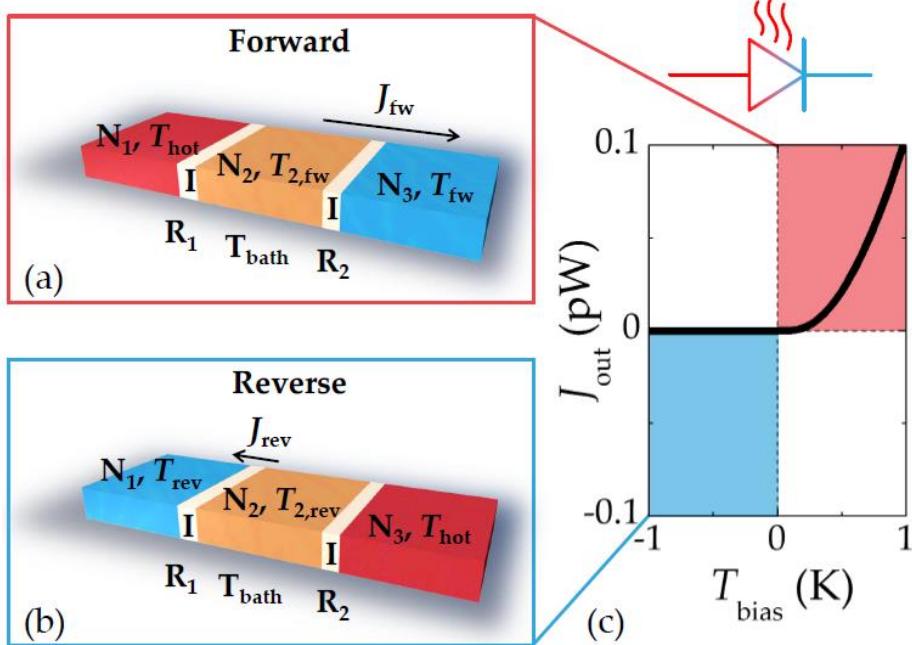
# Temperature diffraction pattern @ 240 mK



# Heat diffraction: Bath temperature dependence



# Thermal rectification with N tunnel junctions: principle



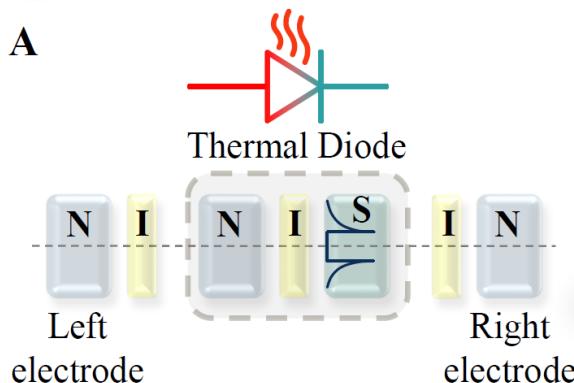
Conditions for thermal rectification:

- i) large tunnel resistance mismatch
- ii) N<sub>2</sub> must be coupled to phonon bath

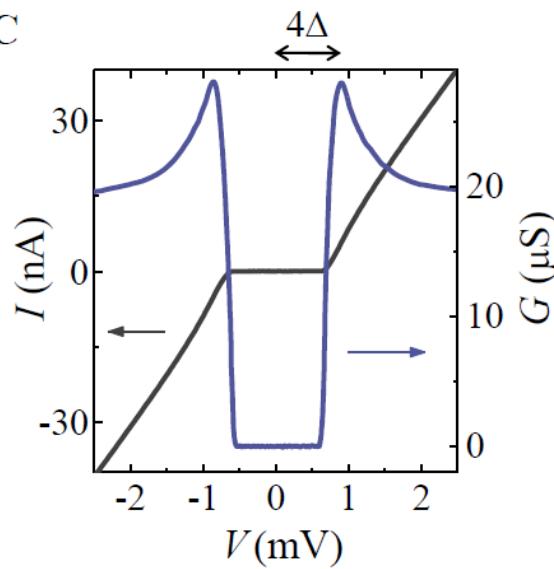


$$R = \frac{J_{fw}}{J_{rev}} \sim 10^3$$

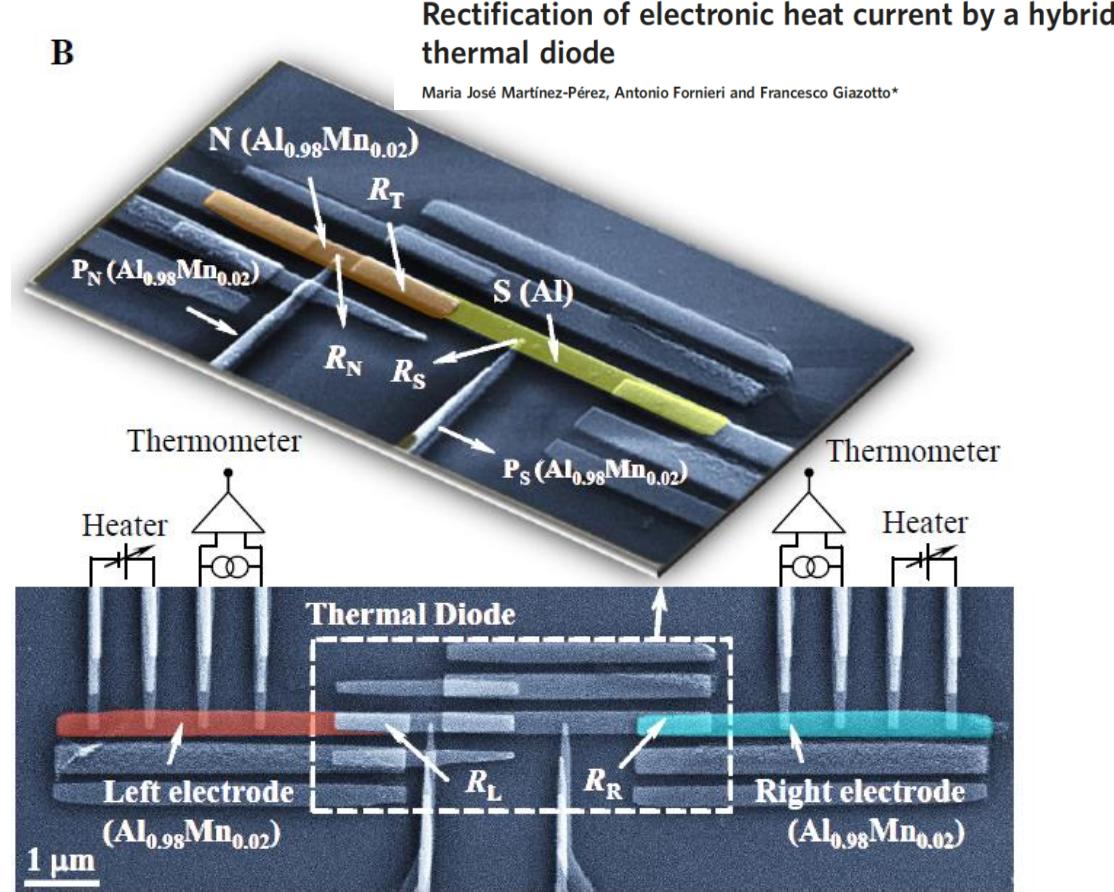
# An ultraefficient hybrid thermal rectifier

**A**

Hybrid heat diode concept

**C**

G vs V char @ 50 mK

**B**

Experimental structure

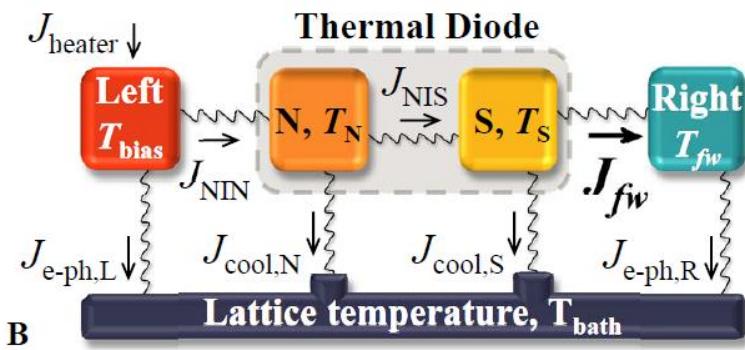
Full symmetry from the electrical point of view

M. J. Martinez-Perez, A. Fornieri, and FG, Nat. Nanotechnol. **10**, 303 (2015);  
FG and F. S. Bergeret, APL **103**, 242602 (2013); M. J. Martinez-Perez and FG, APL **102**, 182602 (2013).

# Asymmetrical thermal transport

Directional thermal current mismatch

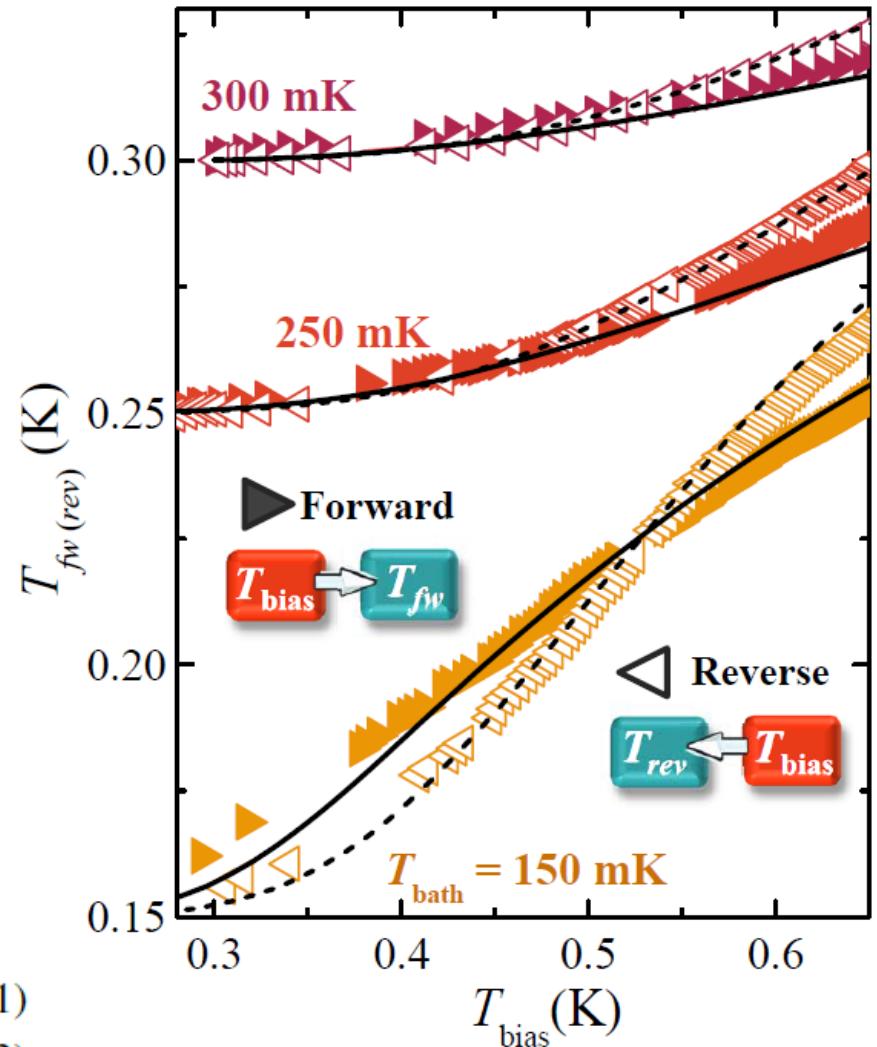
Thermal model



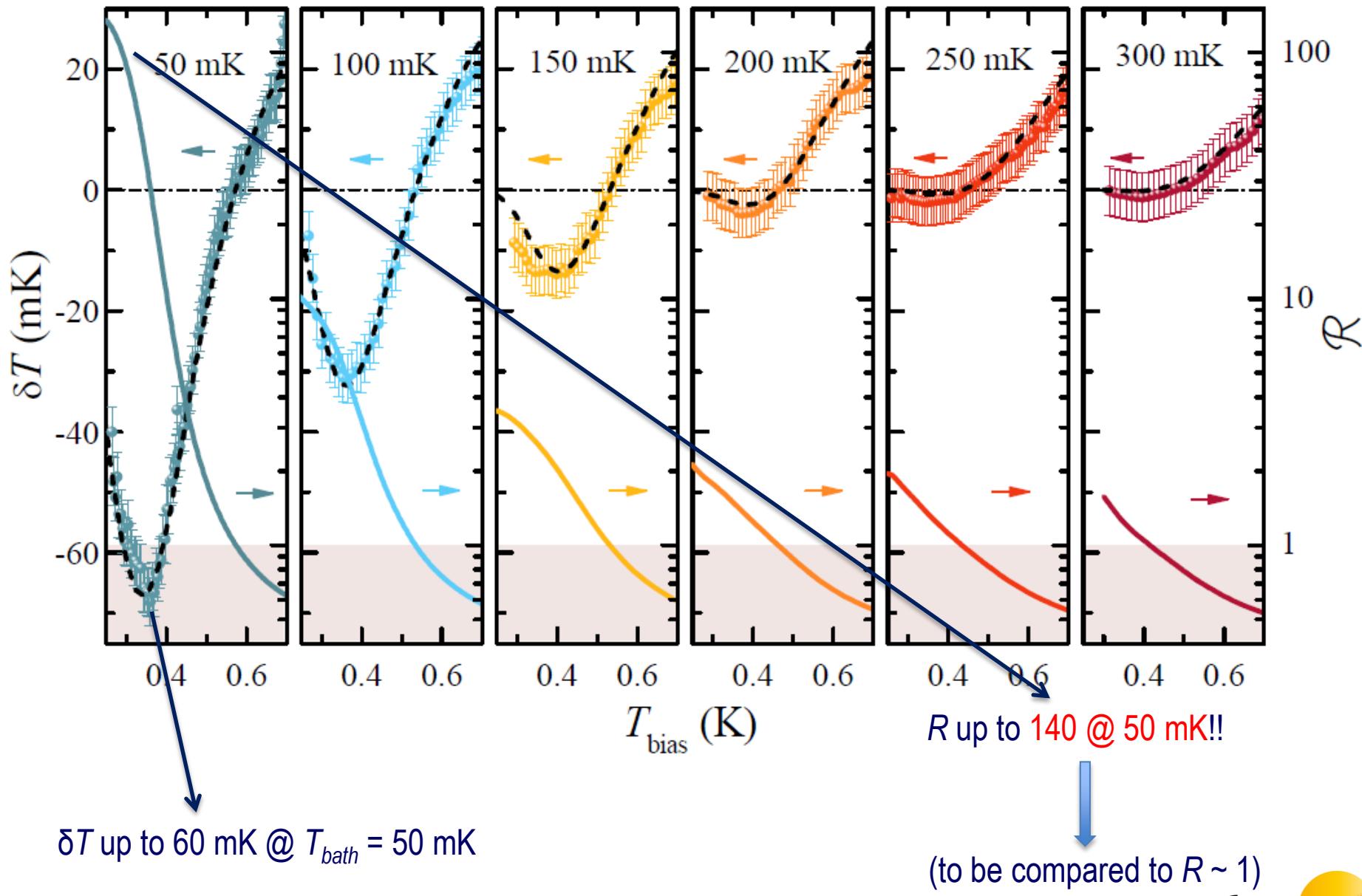
$$J_{\text{NIN}}(T_{\text{bias}}, T_N) - J_{\text{cool},N}(T_N, T_{\text{bath}}) - J_{\text{NIS}}(T_N, T_S) = 0, \quad (1)$$

$$J_{\text{NIS}}(T_N, T_S) - J_{\text{cool},S}(T_S, T_{\text{bath}}) - J_{\text{FW}}(T_S, T_{\text{FW}}) = 0, \quad (2)$$

$$J_{\text{FW}}(T_S, T_{\text{FW}}) - J_{\text{e-ph},R}(T_{\text{FW}}, T_{\text{bath}}) = 0. \quad (3)$$

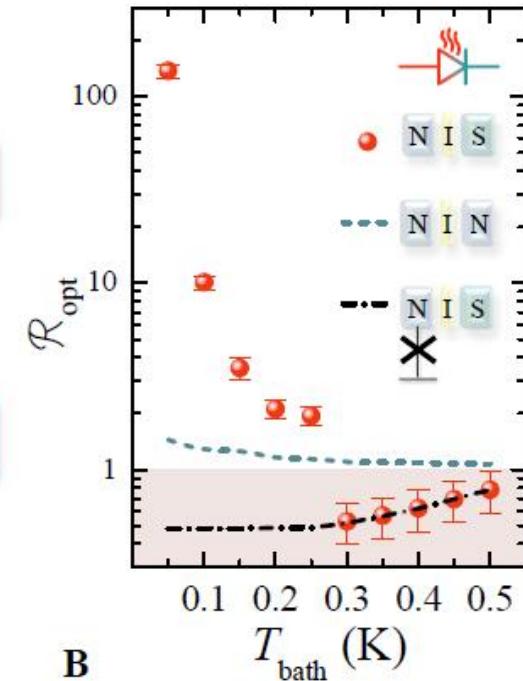
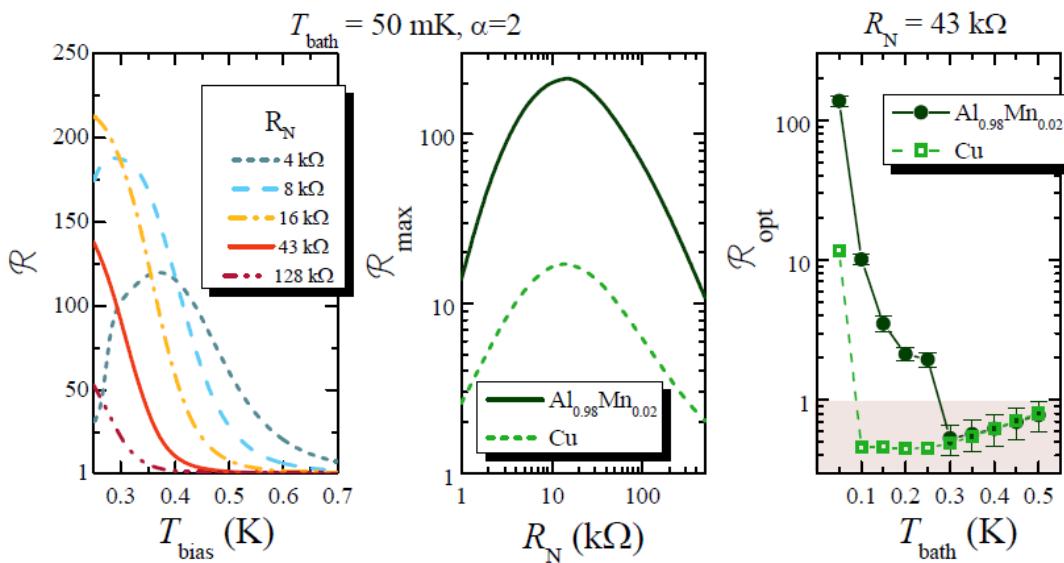
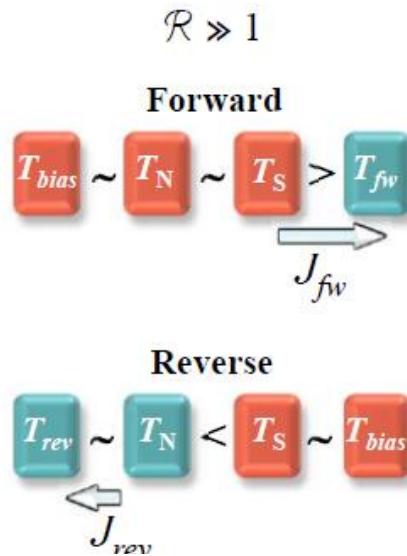


## Ultra-efficient thermal rectification



# Ultra-efficient thermal rectification: comparison

Mechanism & role of  
different structure elements

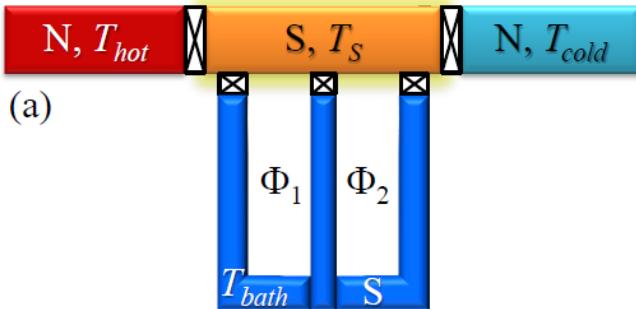


Role of probe & N material type

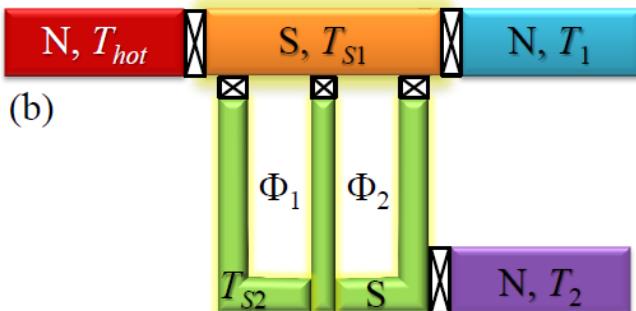
# Conclusions

1. Realization of a heat interferometer
2. Confirmation of the existence, magnitude and sign of the phase-dependent heat current
3. Realization of a quantum diffractor for thermal flux
4. Complementary proof of the “thermal” Josephson effect
5. Realization of an ultraefficient low-temperature hybrid thermal rectifier (with very large  $R \sim 140$ )
6. Novel “coherent caloritronic” devices

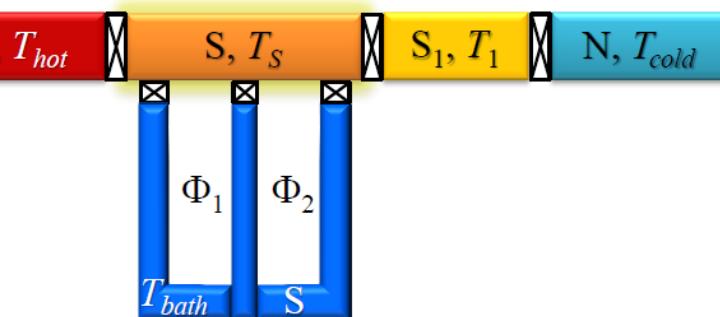
# Perspective for “coherent caloritronic” devices



Heat transistors or  
phase-tunable electron coolers



Heat splitters



Heat rectifiers (diodes)

