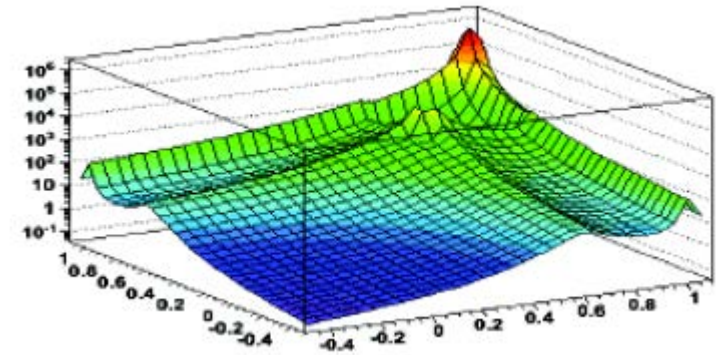
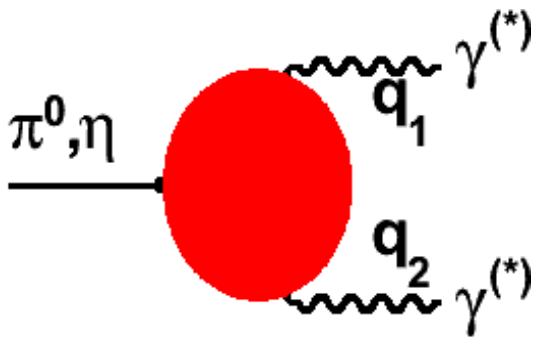


# Transition form factors of light mesons



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FCCP2015, Anacapri, September 11<sup>th</sup>, 2015

# Outline

- $\pi^0, \eta, \eta', \omega, \phi$  meson factories/data samples  
(pN,  $\gamma p$ ,  $e^+e^-$ )

## Transition Form Factors / Anomalous processes

- $\gamma^*\gamma \rightarrow \eta, \pi^0$  ( $\Gamma_{\gamma\gamma}$ )
- $\eta, \pi^0 \rightarrow e^+e^-\gamma$
- $e^+e^- \rightarrow \eta\gamma$
- $\eta \rightarrow e^+e^-e^+e^-$
- $\phi \rightarrow \eta/\pi^0 e^+e^-$  (TFF)
- $P \rightarrow e^+e^-$
- $\eta, \eta' \rightarrow \pi^+\pi^-\gamma, e^+e^- \rightarrow \eta\pi\pi, \pi\pi\pi$
- Belle  $\gamma^*\gamma \rightarrow \pi^0\pi^0$  arXiv:1508.06757

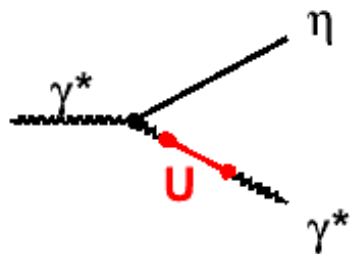
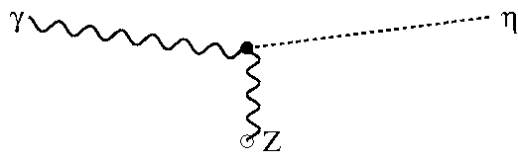
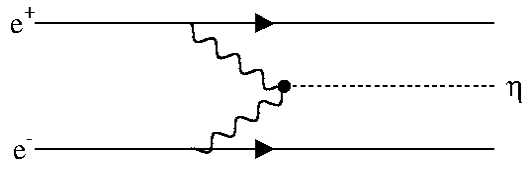
# Meson Transition Form Factors (TFF)

Structure of light mesons

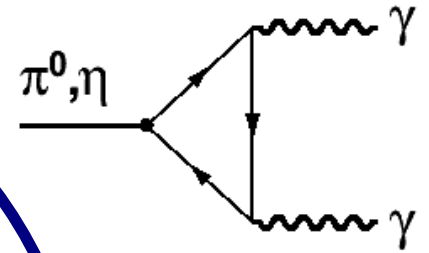
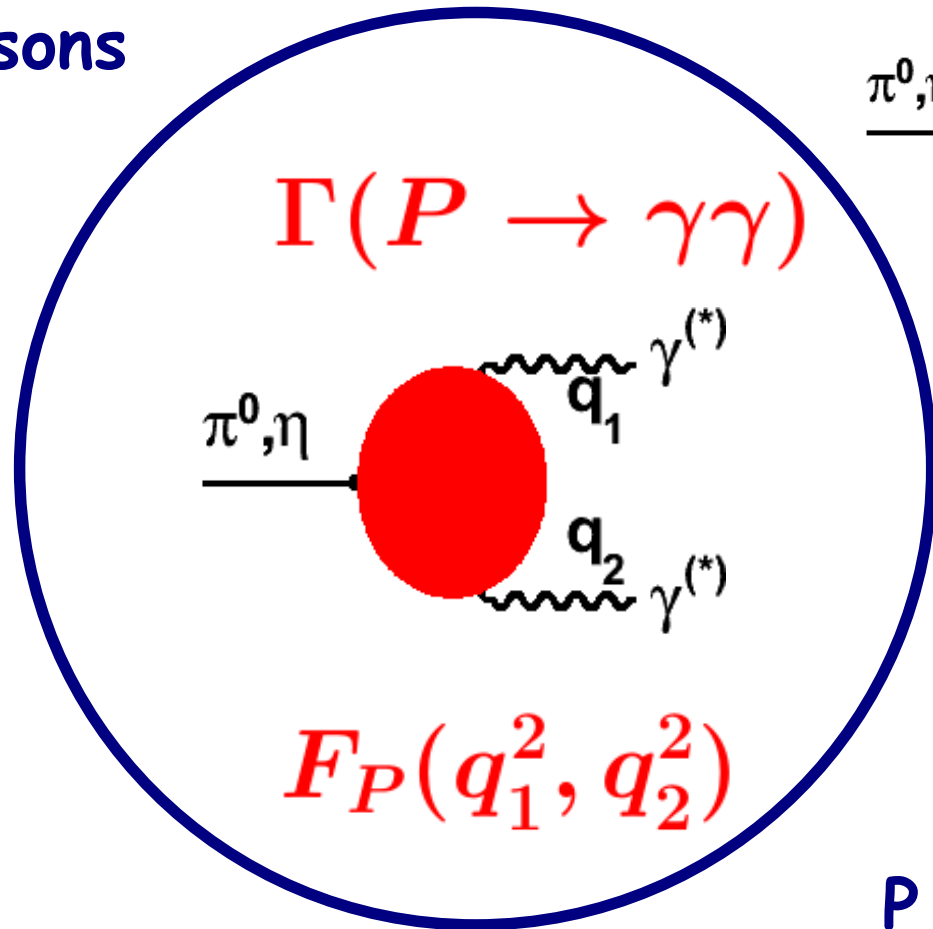
L/H energy QDC LAB

$l^+l^-$  spectra in HIon

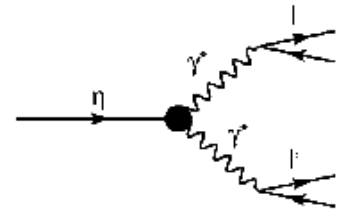
$F_{\pi^0} q^2 \rightarrow \infty$  puzzle



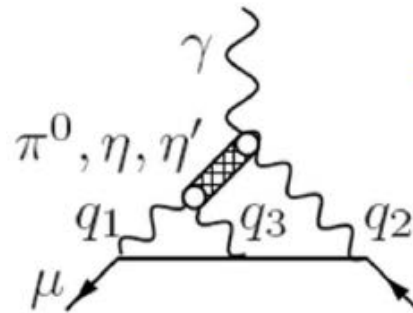
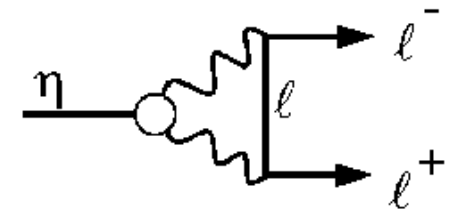
Dark photon



$\eta: \Gamma_{\gamma\gamma}$   
 $m_u/m_d$



$P \rightarrow l^+l^-$



$g-2$  HLbL

# Radiative widths of $\eta, \pi^0$

$\eta, \pi^0$  : narrow and short lived

$$\Rightarrow \Gamma_{\text{tot}} = \Gamma_{\gamma\gamma} / \text{BR}_{\gamma\gamma}$$

$$\eta: 5 \times 10^{-19} \text{ s}; \Gamma = 1.3 \text{ keV} \quad \eta \rightarrow \gamma\gamma$$

$$\pi^0: 8 \times 10^{-17} \text{ s}; c\tau = 25 \text{ nm} \quad \pi^0 \rightarrow \gamma\gamma$$

Two exp. techniques:

$\gamma Z \rightarrow \eta, \pi^0$  Primakoff

$$\delta\Gamma(\pi^0 \rightarrow \gamma\gamma) \sim 2.8\%$$

PrimEx PRL 106,162303(2011)

$e^+e^-: \gamma\gamma \rightarrow \eta, \pi^0$

KLOE-2 Taggers

$$5\text{fb}^{-1} \Rightarrow \delta\Gamma(\pi^0 \rightarrow \gamma\gamma) \sim 1\%$$

Details: [EPJC 72, 1917 (2012)]

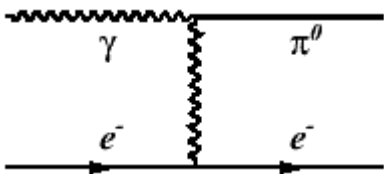
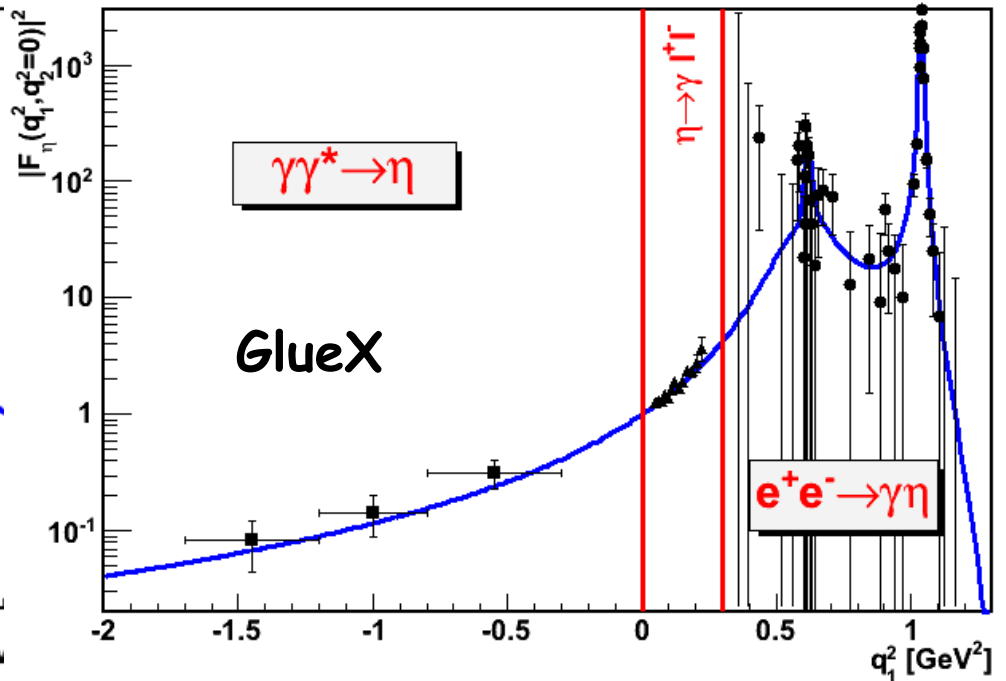
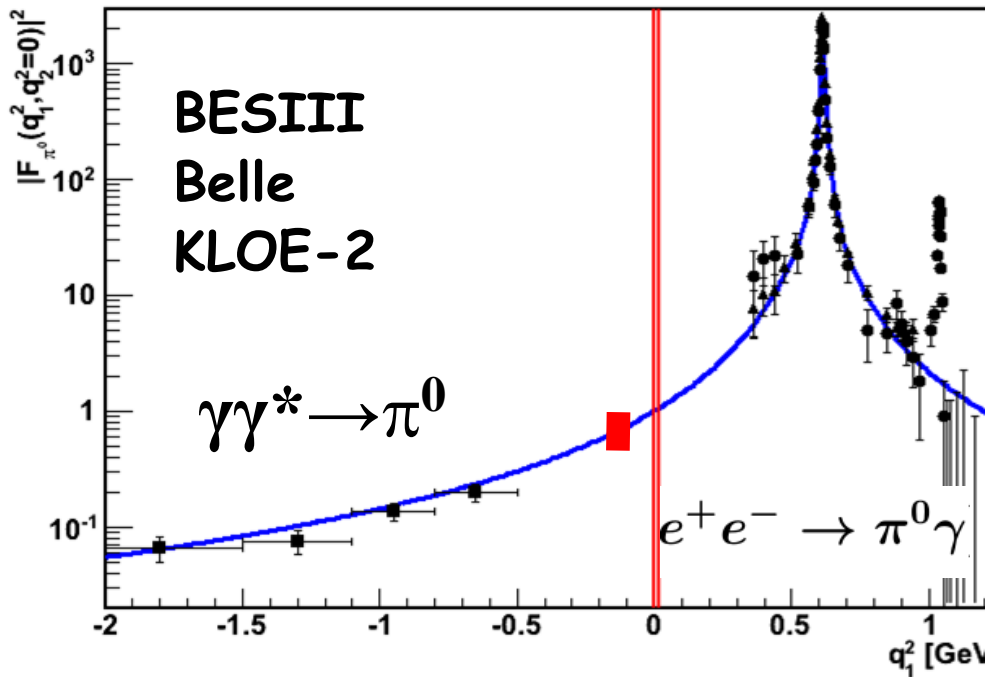
VALUE (keV)	EVTS	DOCUMENT ID	TECN	COMMENT
0.510 ± 0.026	OUR FIT	$\delta\Gamma(\eta \rightarrow \gamma\gamma) \sim 5\%$		
0.510 ± 0.026	OUR AVERAGE			
0.51 ± 0.12 ± 0.05	36	BARU	90 MD1	$e^+e^- \rightarrow e^+e^-\eta$
0.490 ± 0.010 ± 0.048	2287	ROE	90 ASP	$e^+e^- \rightarrow e^+e^-\eta$
0.514 ± 0.017 ± 0.035	1295	WILLIAMS	88 CBAL	$e^+e^- \rightarrow e^+e^-\eta$
0.53 ± 0.04 ± 0.04		BARTEL	85E JADE	$e^+e^- \rightarrow e^+e^-\eta$
*** We do not use the following data for averages, fits, limits, etc. ***				
0.476 ± 0.062		<sup>1</sup> RODRIGUES	08 CNTR	Reanalysis
0.64 ± 0.14 ± 0.13		AIHARA	86 TPC	$e^+e^- \rightarrow e^+e^-\eta$
0.56 ± 0.16	56	WEINSTEIN	83 CBAL	$e^+e^- \rightarrow e^+e^-\eta$
0.324 ± 0.046		BROWMAN	74B CNTR	Primakoff effect
1.00 ± 0.22		<sup>2</sup> BEMPORAD	67 CNTR	Primakoff effect

$$\sigma(e^+e^- \rightarrow e^+e^-\eta, \sqrt{s}=1\text{GeV})$$

$$\Gamma_{\gamma\gamma} = 520 \pm 20_{\text{stat}} \pm 13_{\text{syst}} \text{ eV}$$

[KLOE JHEP1301 (2013) 119]

# $\eta, \pi^0$ single off shell TFF

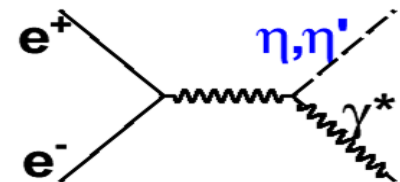


$$\frac{d\sigma}{dt}(e^- \gamma \rightarrow e^- P) = \frac{16 \pi \alpha}{3 s m_P^3} \Gamma_{\gamma\gamma} |F_P(t, 0)|^2 \frac{s - m_P^2 + t}{t}$$

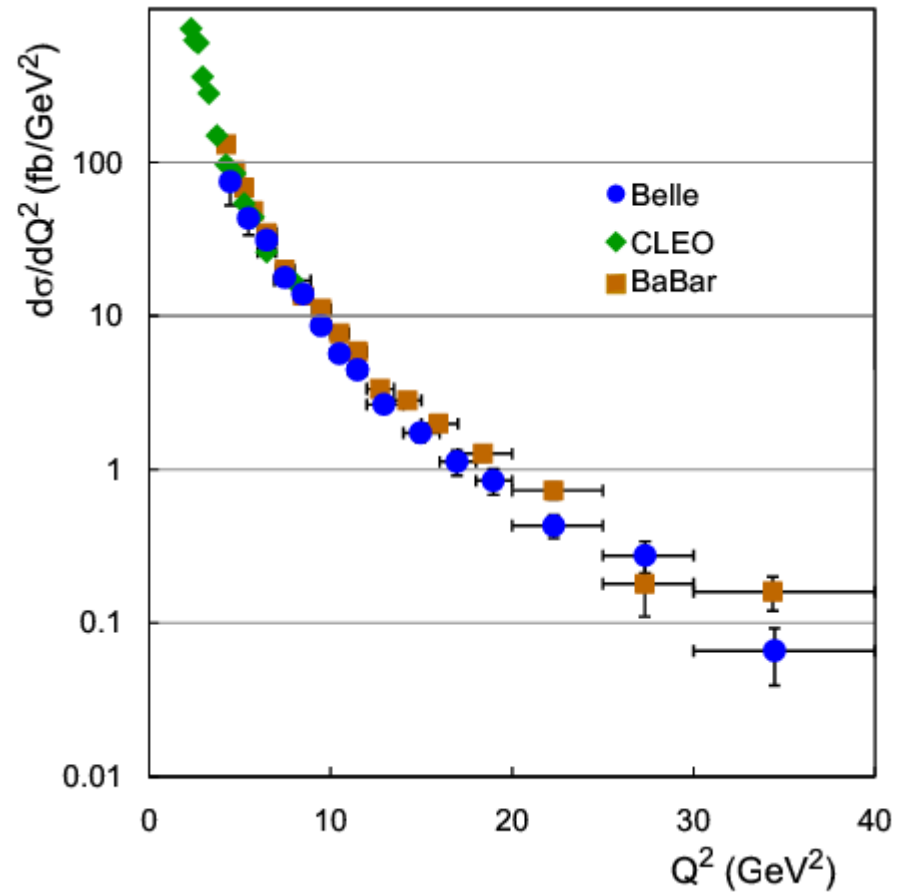
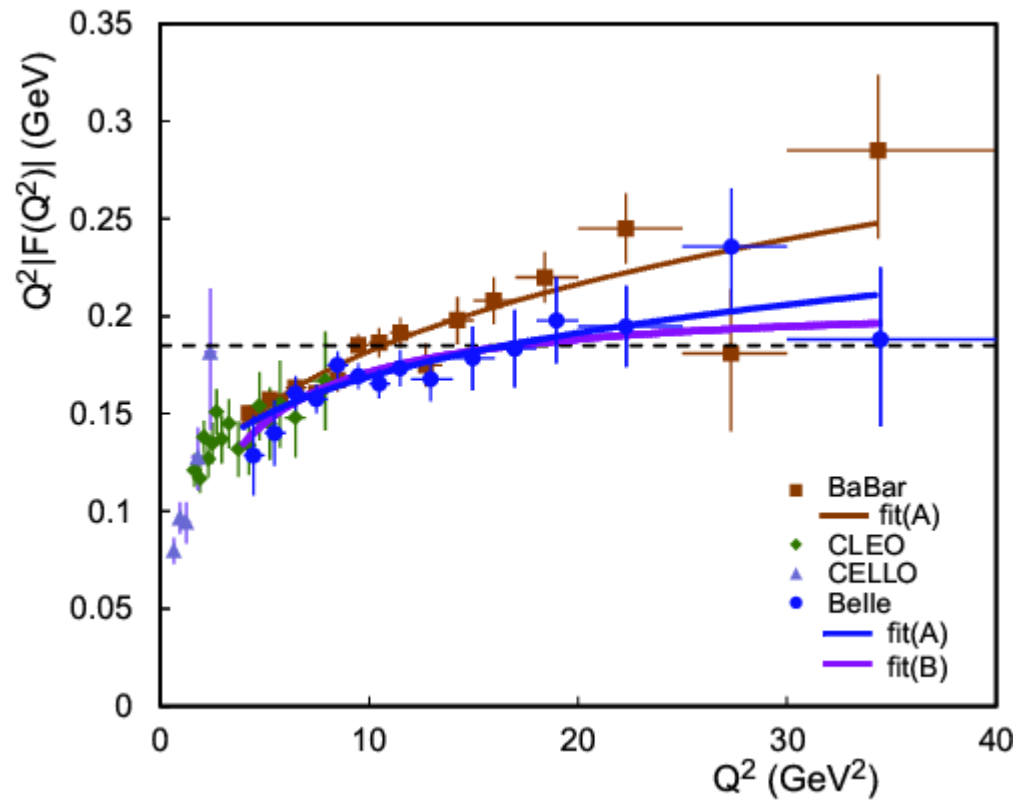
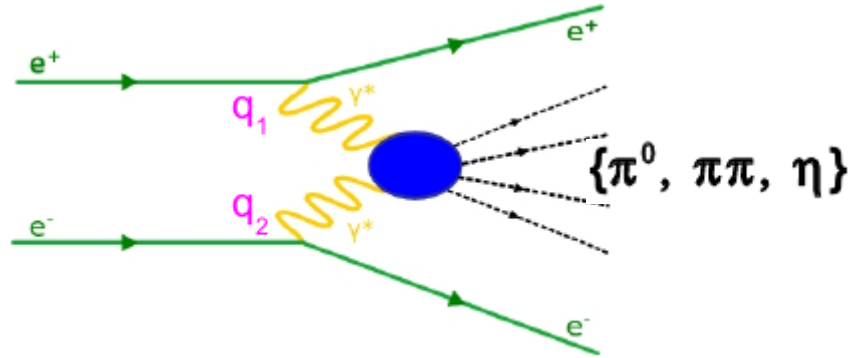
$P \rightarrow \gamma^* \gamma$   
Dalitz decays:  
KLOE, WASA, CBall, BESIII  
CLAS, NA48

$\gamma^* \rightarrow P\gamma$   
VEPP 2000 0.3-2GeV  
KLOE-2 ISR, BESIII

$$\sigma(e^+e^- \rightarrow P\gamma) = \frac{8}{3} \pi \alpha \Gamma_{\gamma\gamma} |F_P(s, 0)|^2 \left( \frac{s - m_P^2}{s m_P} \right)^3$$

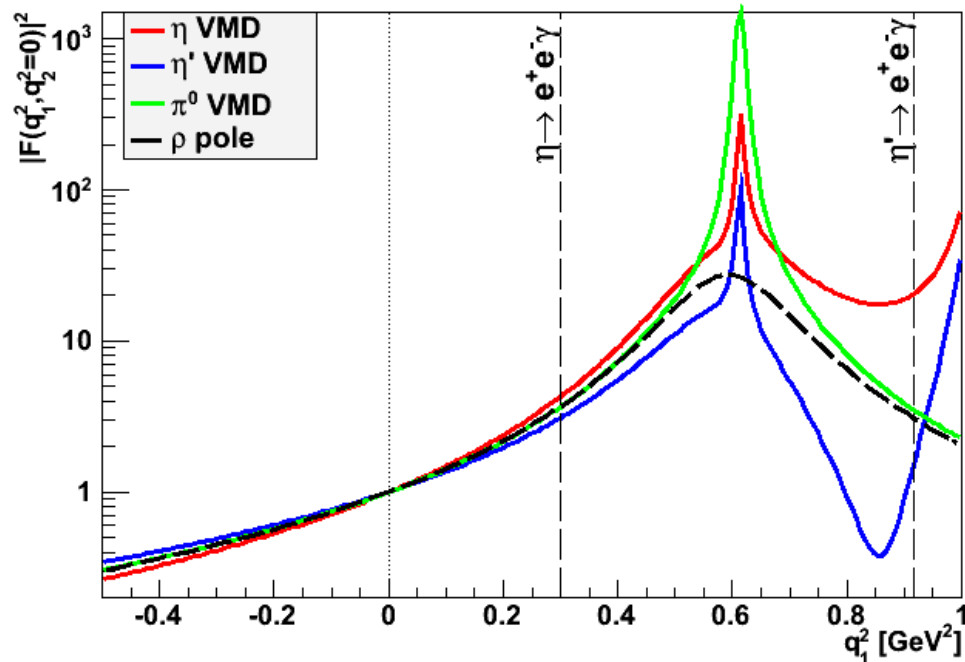
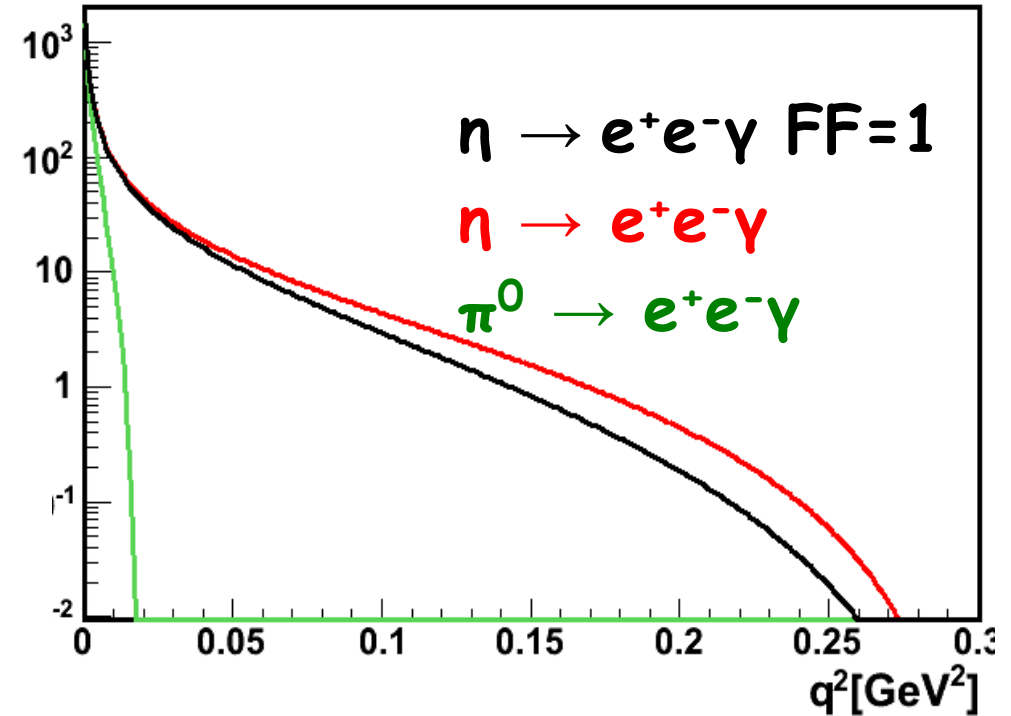
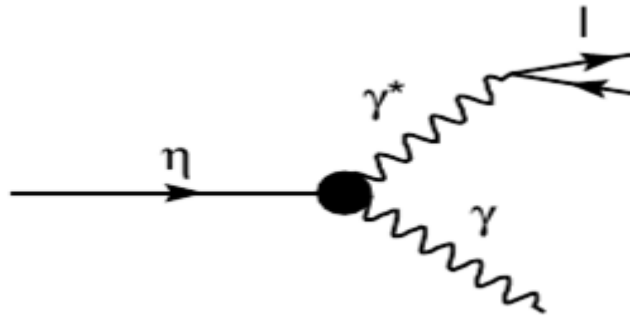


$$\gamma\gamma^* \rightarrow \pi^0$$



# Dalitz decays

$$\frac{d\Gamma(P \rightarrow l^+l^-\gamma)}{dq^2\Gamma_{\gamma\gamma}} = \frac{2\alpha}{3\pi} \frac{1}{q^2} \sqrt{1 - \frac{4m_l^2}{q^2}} \left(1 + \frac{2m_l^2}{q^2}\right) \left(1 - \frac{q^2}{M_P^2}\right)^3 |F_P(q^2, 0)|^2$$

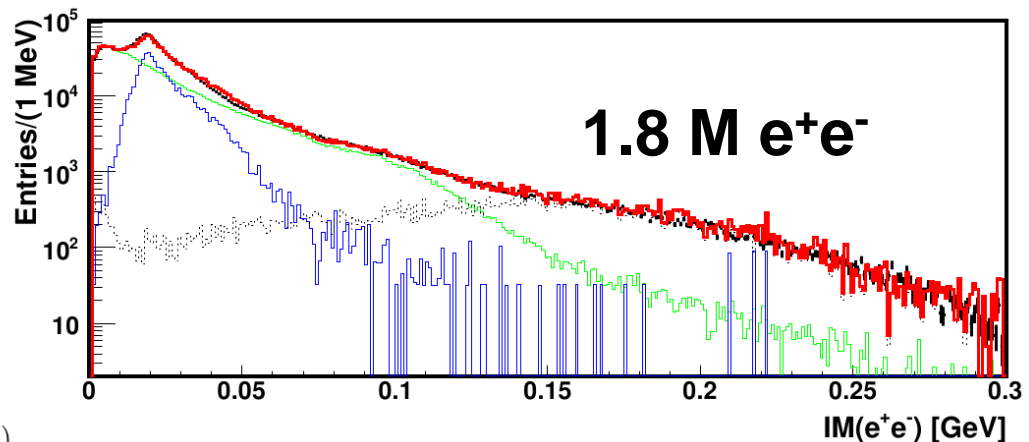




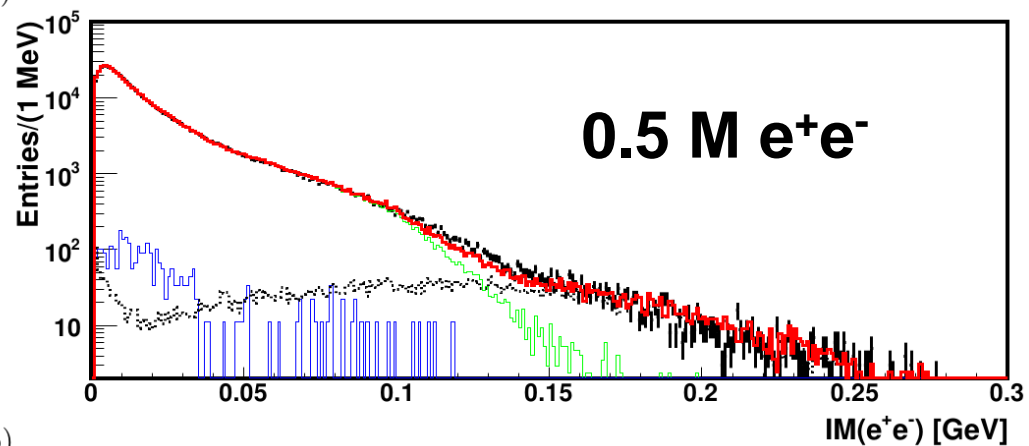
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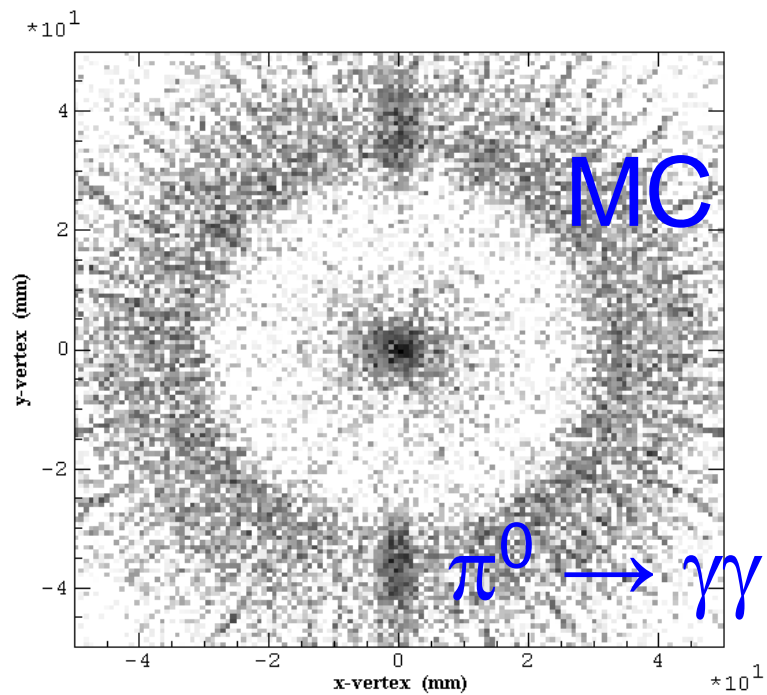
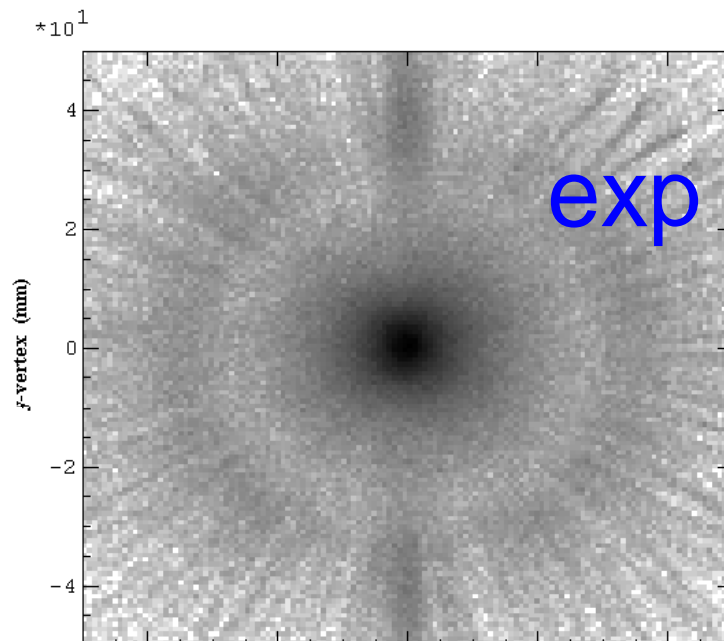
# Data analysis: $\pi^0 \rightarrow \gamma e^+ e^-$



a)

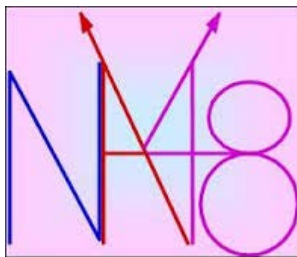
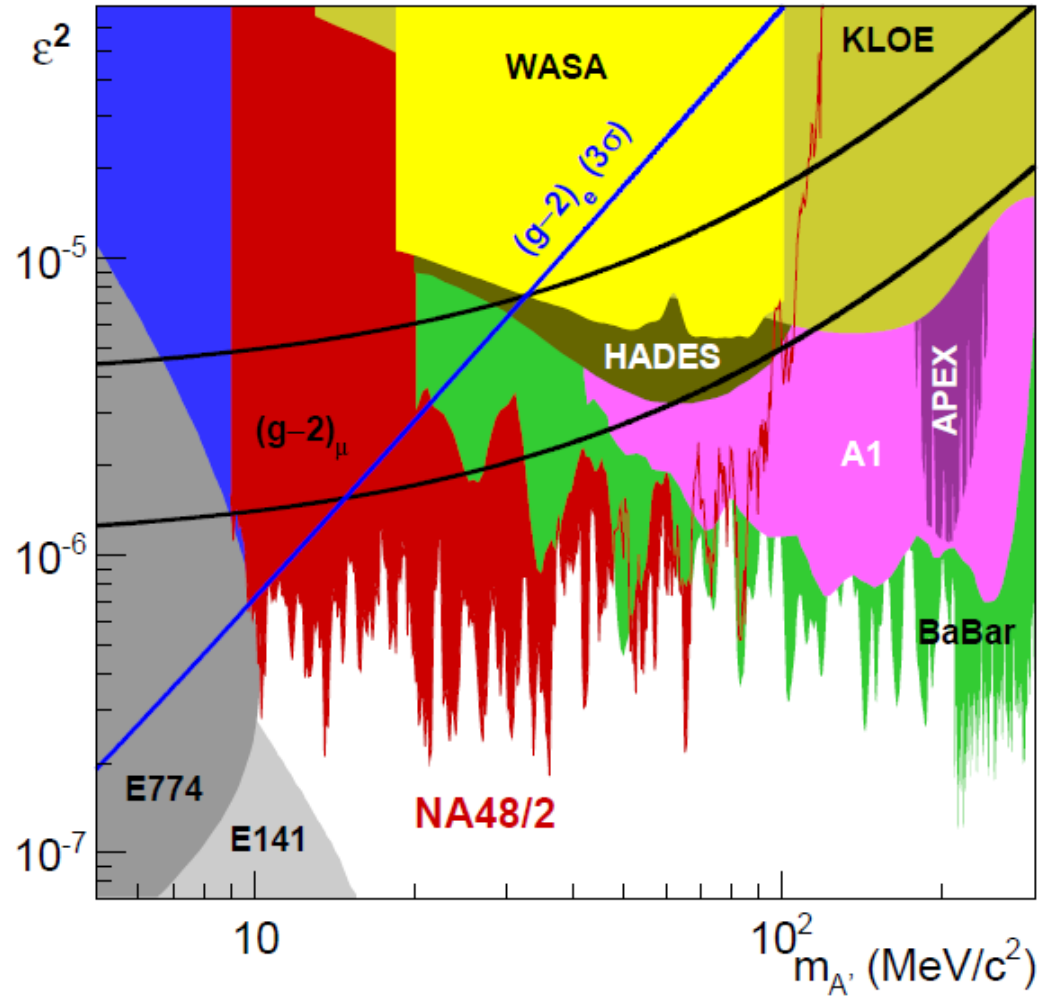
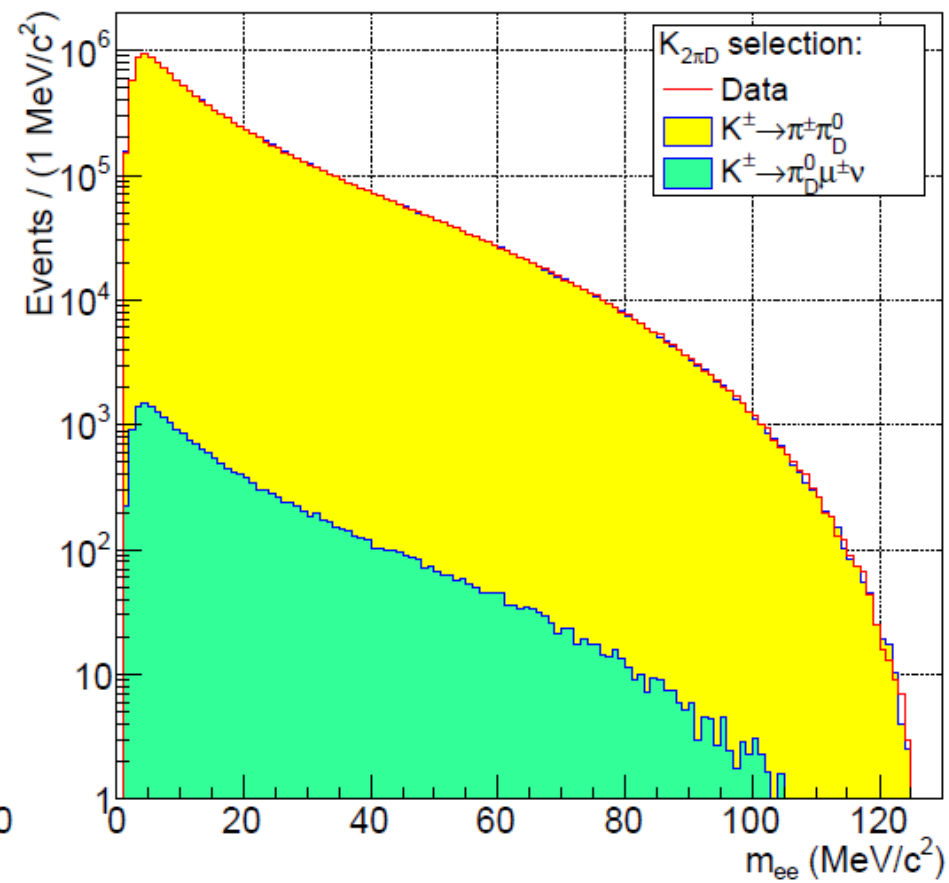


b)



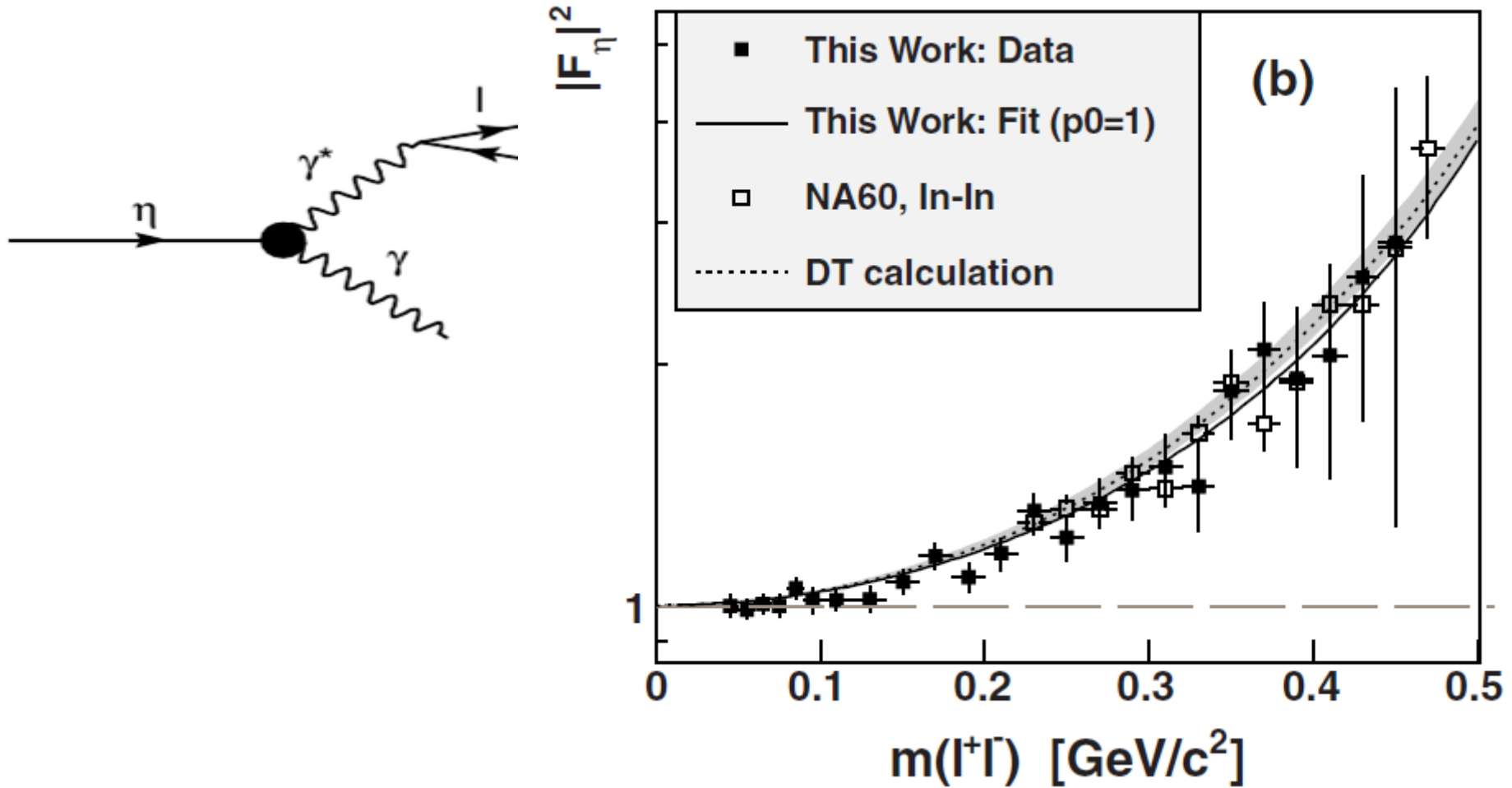


# NA48/2 $\pi^0 \rightarrow e+e-\gamma$



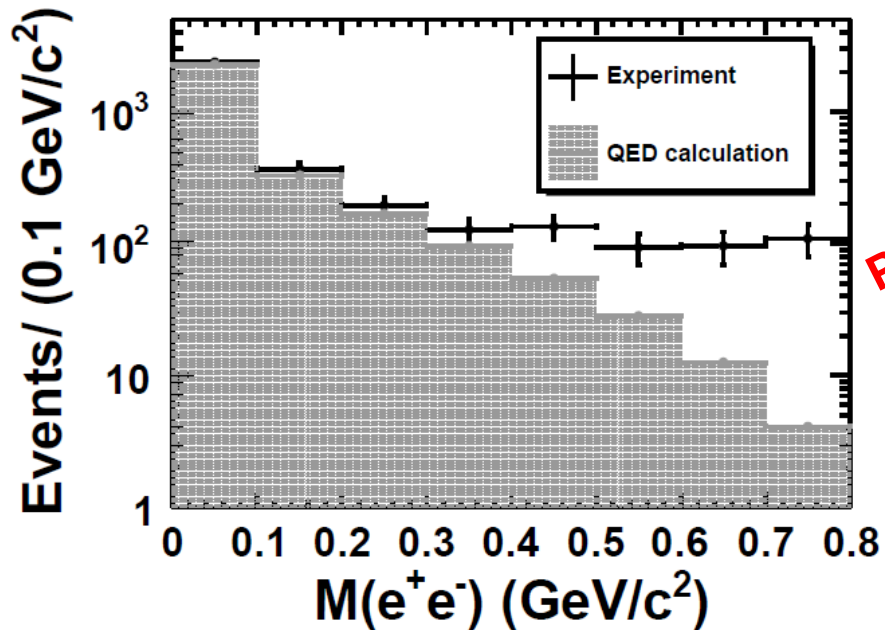
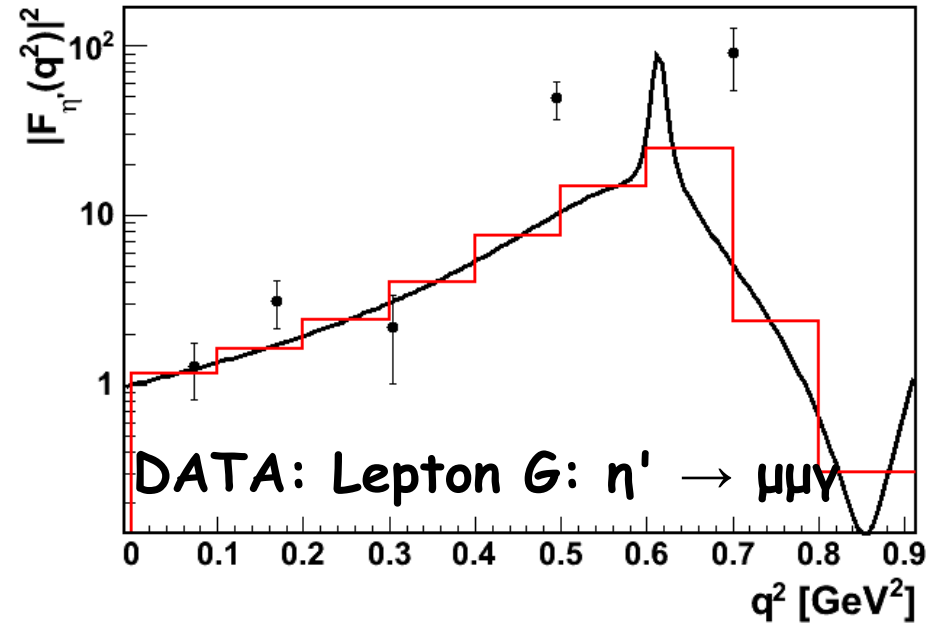
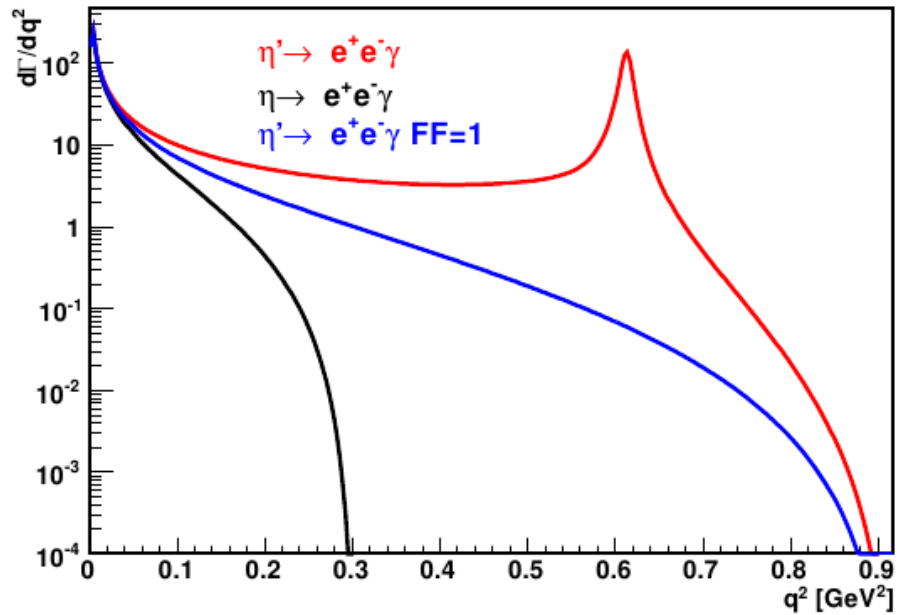
NA48/2: arXiv:1504.00607

$$\eta \rightarrow e^+e^-\gamma$$

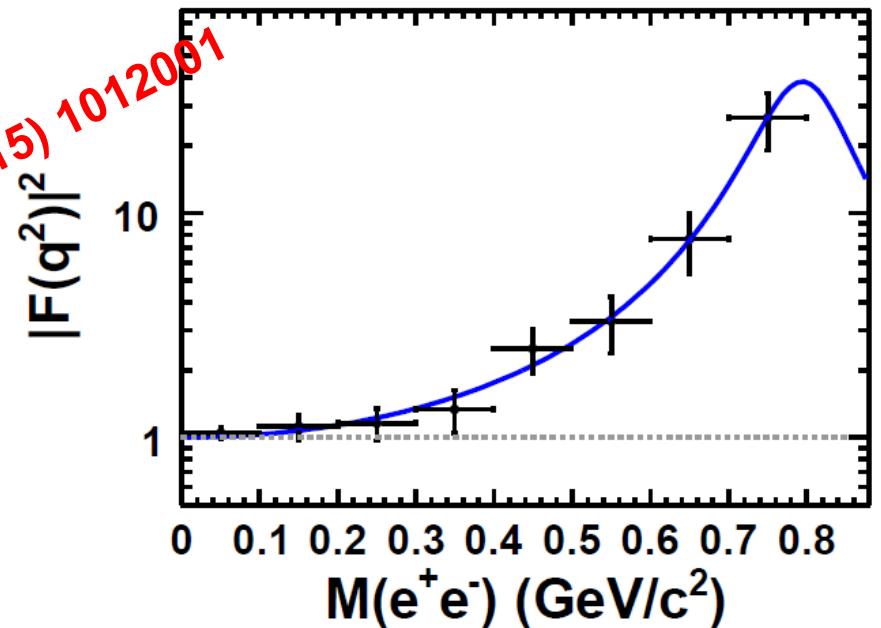


CB/TAPS: PRC89, 044608 (2014)

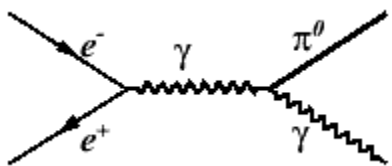
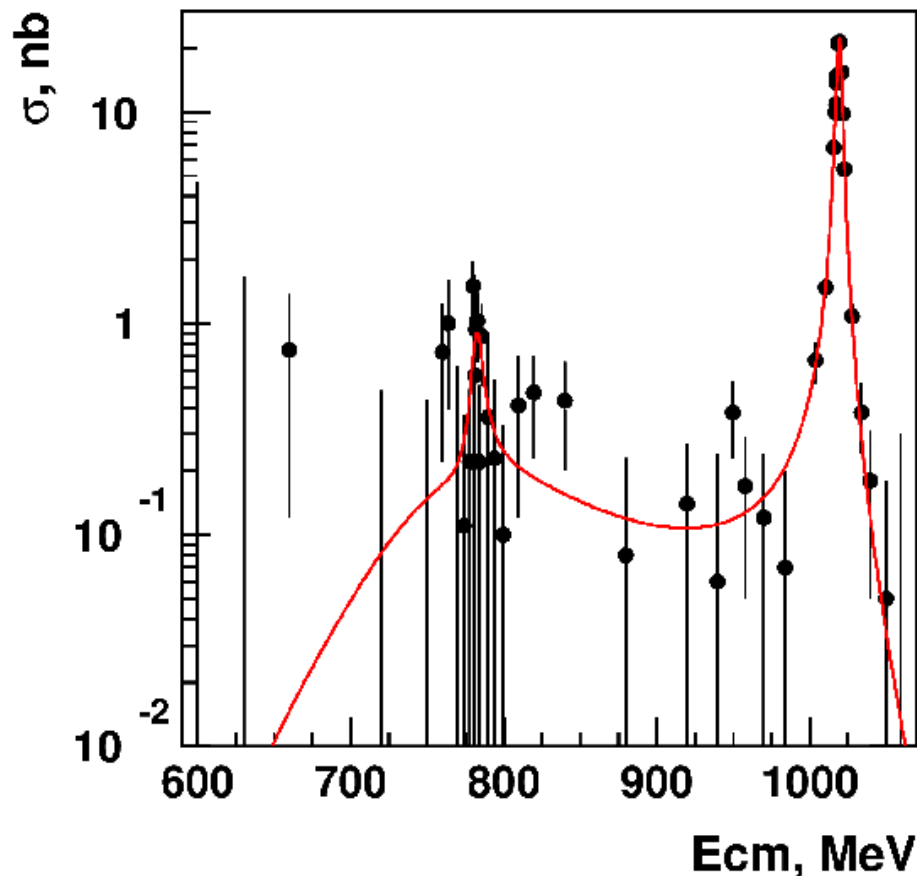
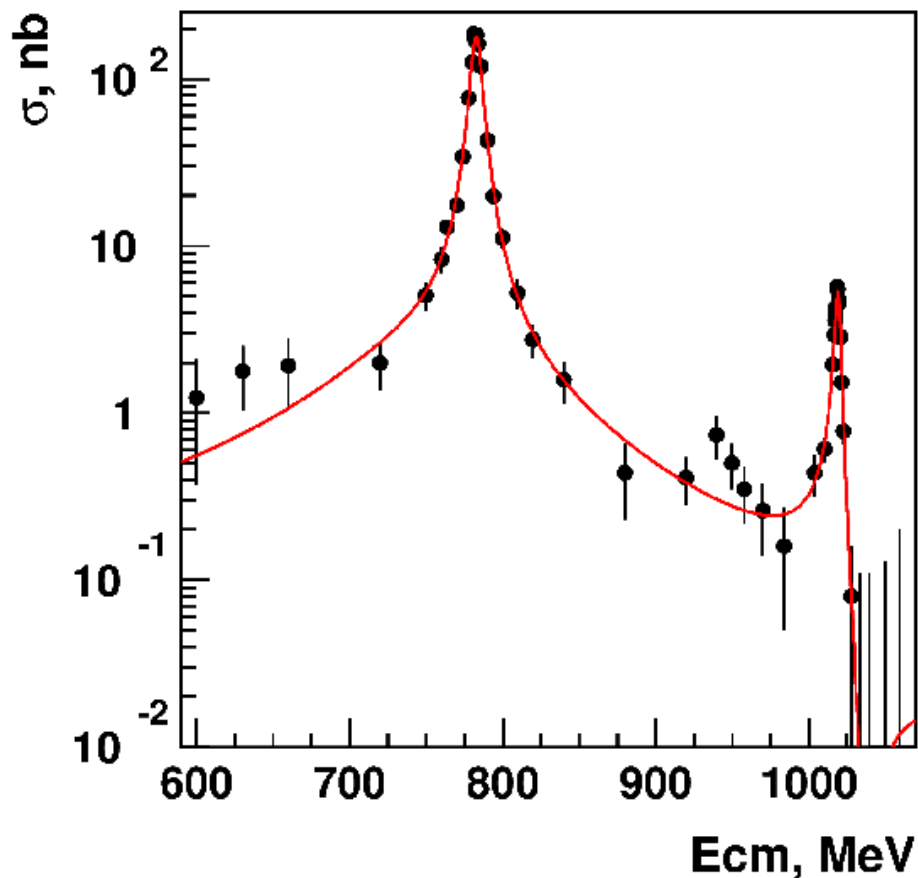
# BESIII: Observation of $\eta' \rightarrow \gamma e^+ e^-$



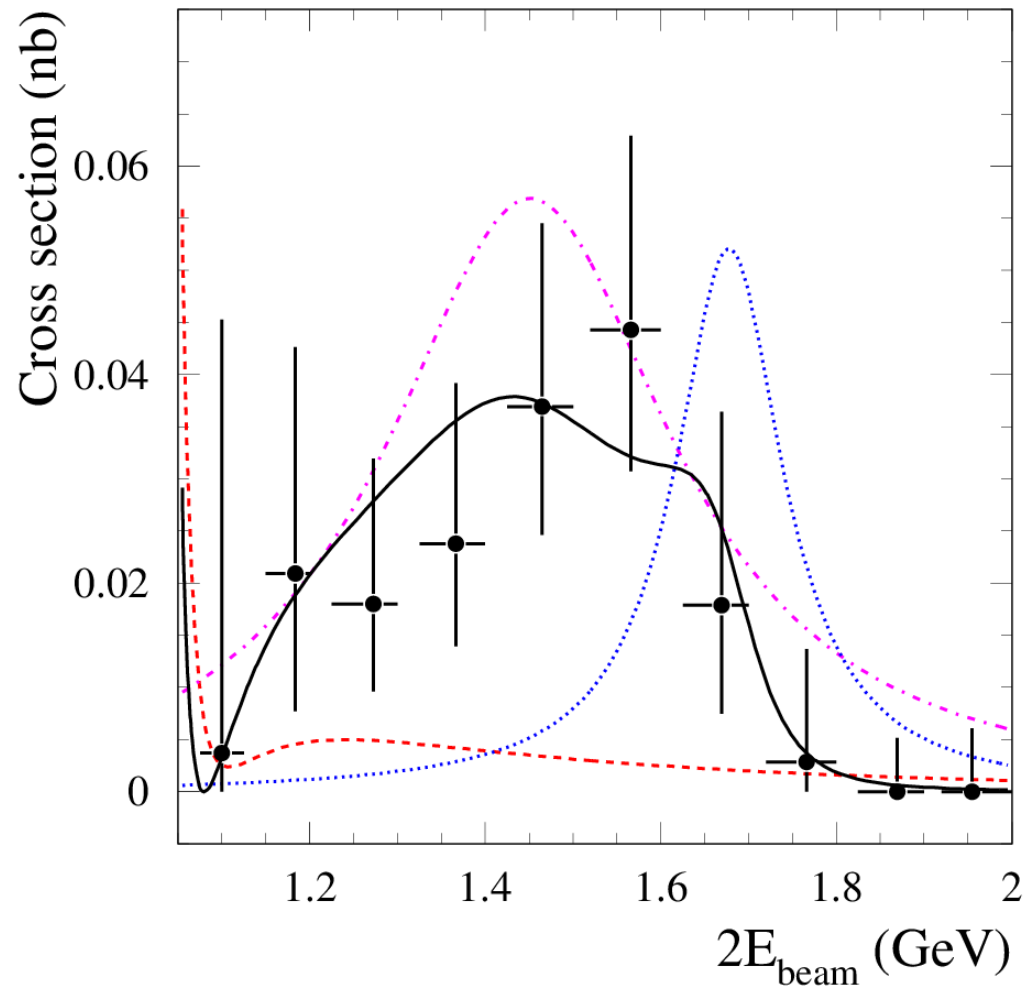
PRD92 (2015) 1012091



# $\sigma(e^+e^- \rightarrow \pi^0\gamma, \eta\gamma)$

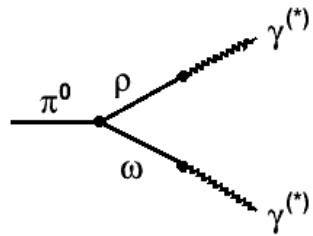


$$\sigma(e^+e^- \rightarrow P\gamma) = \frac{8}{3}\pi\alpha \Gamma_{\gamma\gamma} |F_P(s, 0)|^2 \left( \frac{s - m_P^2}{sm_P} \right)^3$$

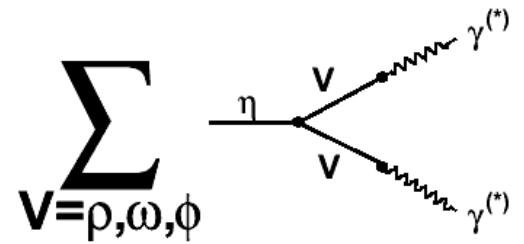
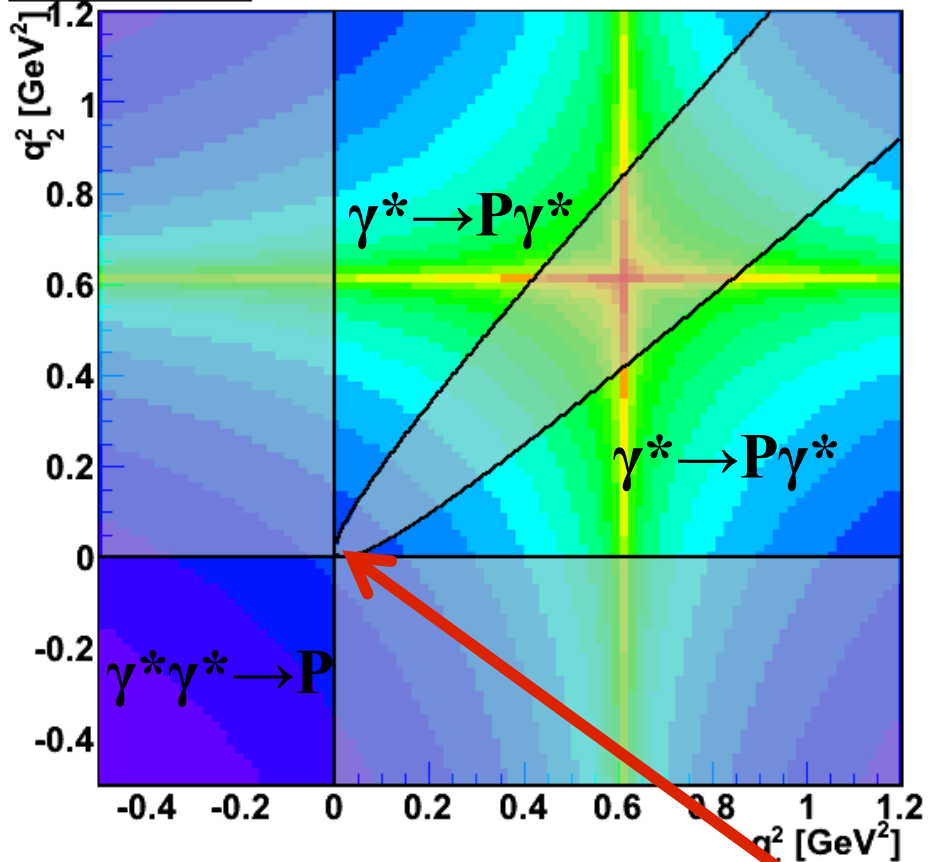


$e^+e^- \rightarrow \eta\gamma$  SND PRD 90 (2014) 032002

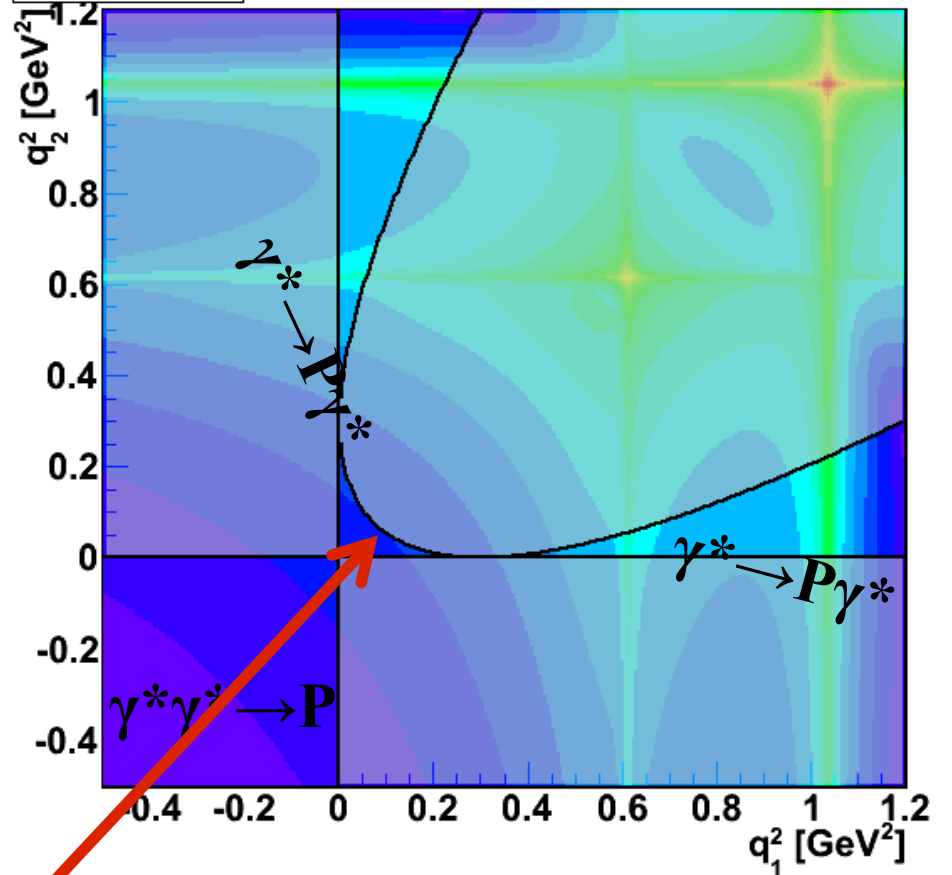
# TFF kinematic regions: $\pi^0, \eta$



$$|F_{\pi^0}(q_1^2, q_2^2)|^2 \quad \pi^0$$

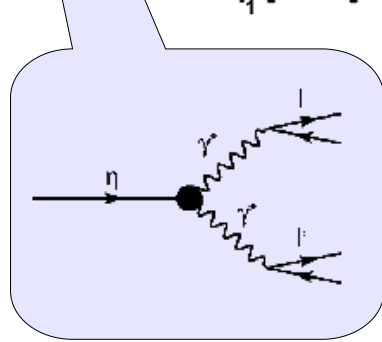
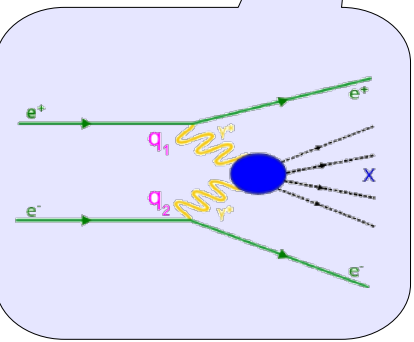
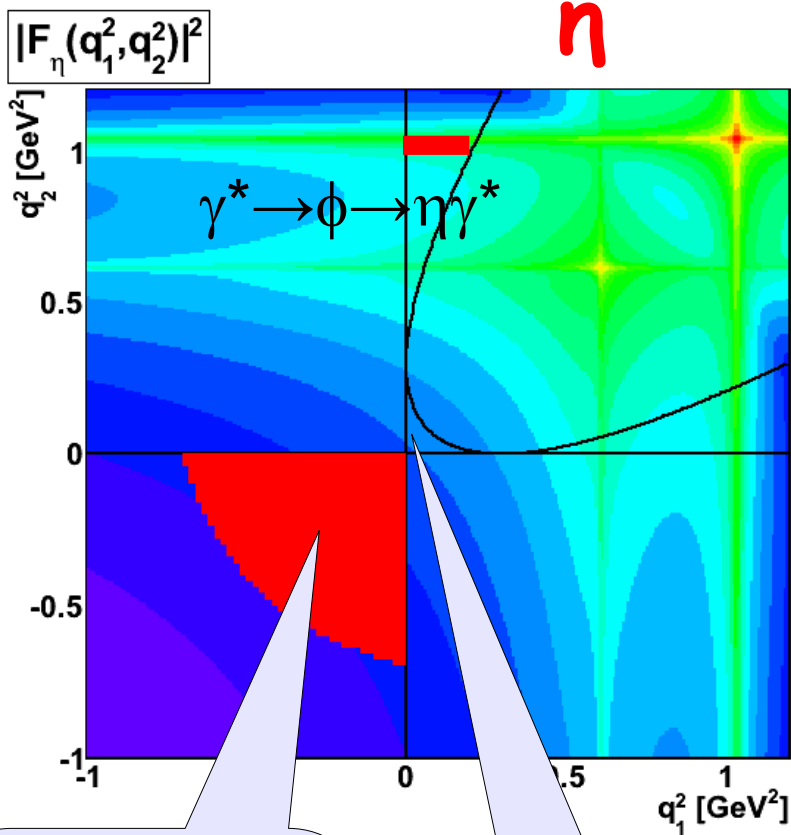


$$|F_{\eta}(q_1^2, q_2^2)|^2 \quad \eta$$

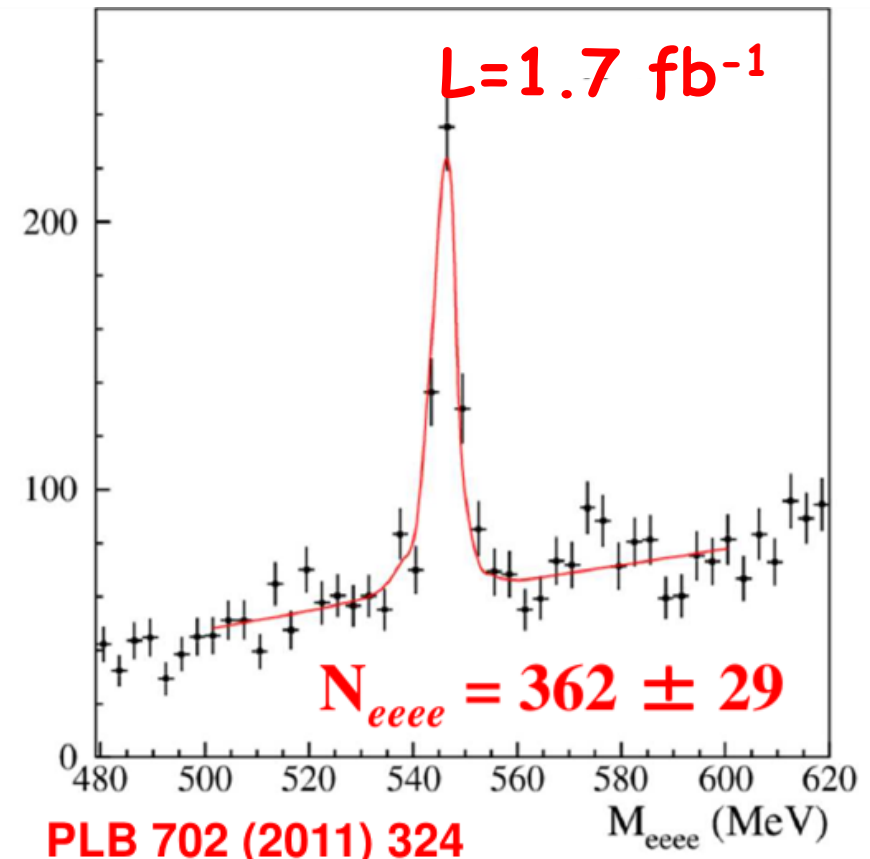


$$P \rightarrow \gamma^*\gamma^*$$

# Double off shell TFF at KLOE



$\eta \rightarrow e^+ e^- e^+ e^-$



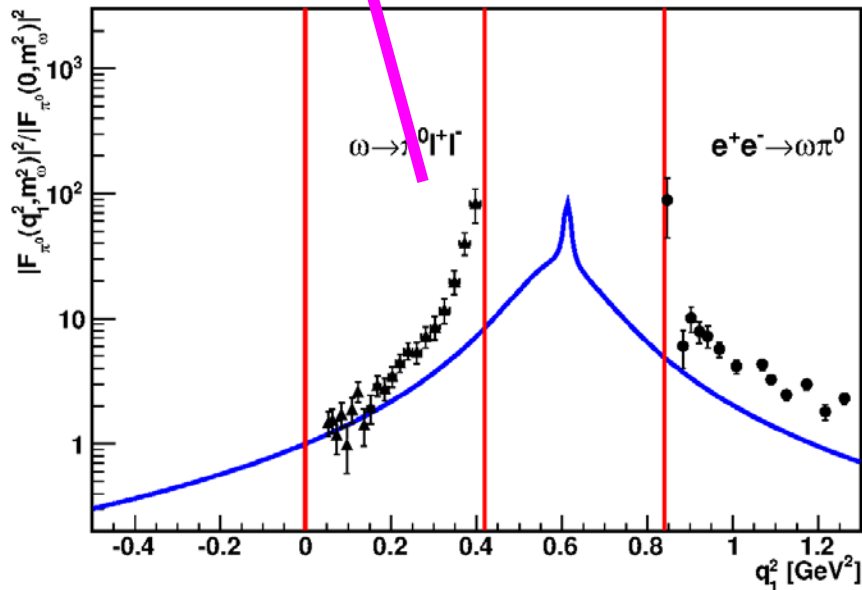
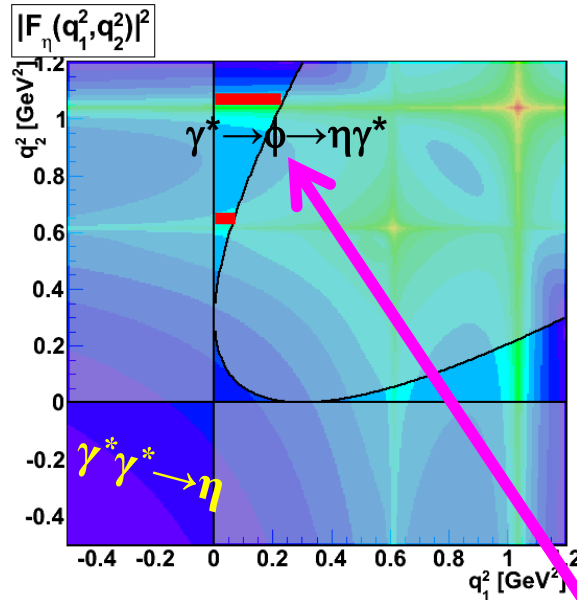
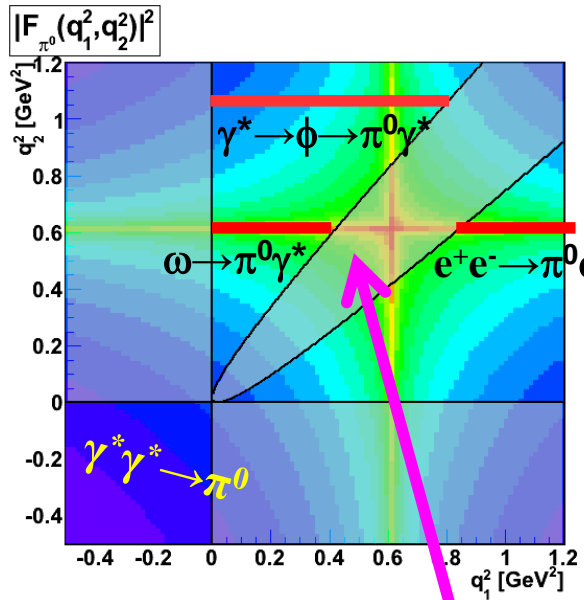
PLB 702 (2011) 324

$BR(\eta \rightarrow e^+ e^- e^+ e^- (\gamma)) = (2.4 \pm 0.2_{\text{stat}} \pm 0.1_{\text{syst}}) \times 10^{-5}$

TFF=1  $\Rightarrow$  BR=2.5×10<sup>-5</sup>

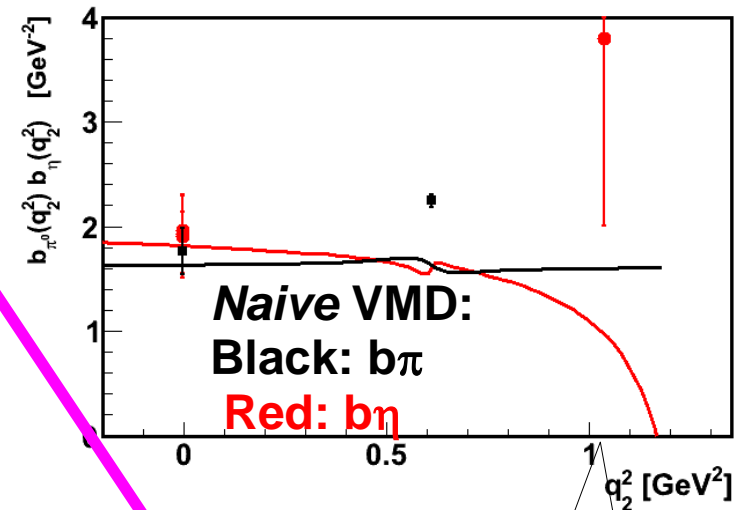
TFF≠1  $\Delta$ BR ~ 5%

# $V \rightarrow P\gamma^*$ and $e^+e^- \rightarrow PV$ processes



slopes  $b_\pi, b_\eta$

$$b_P(q_2^2) = \left. \frac{\partial \ln |F(q_1^2, q_2^2)|}{\partial q_1^2} \right|_{q_1^2=0}$$



KLOE results

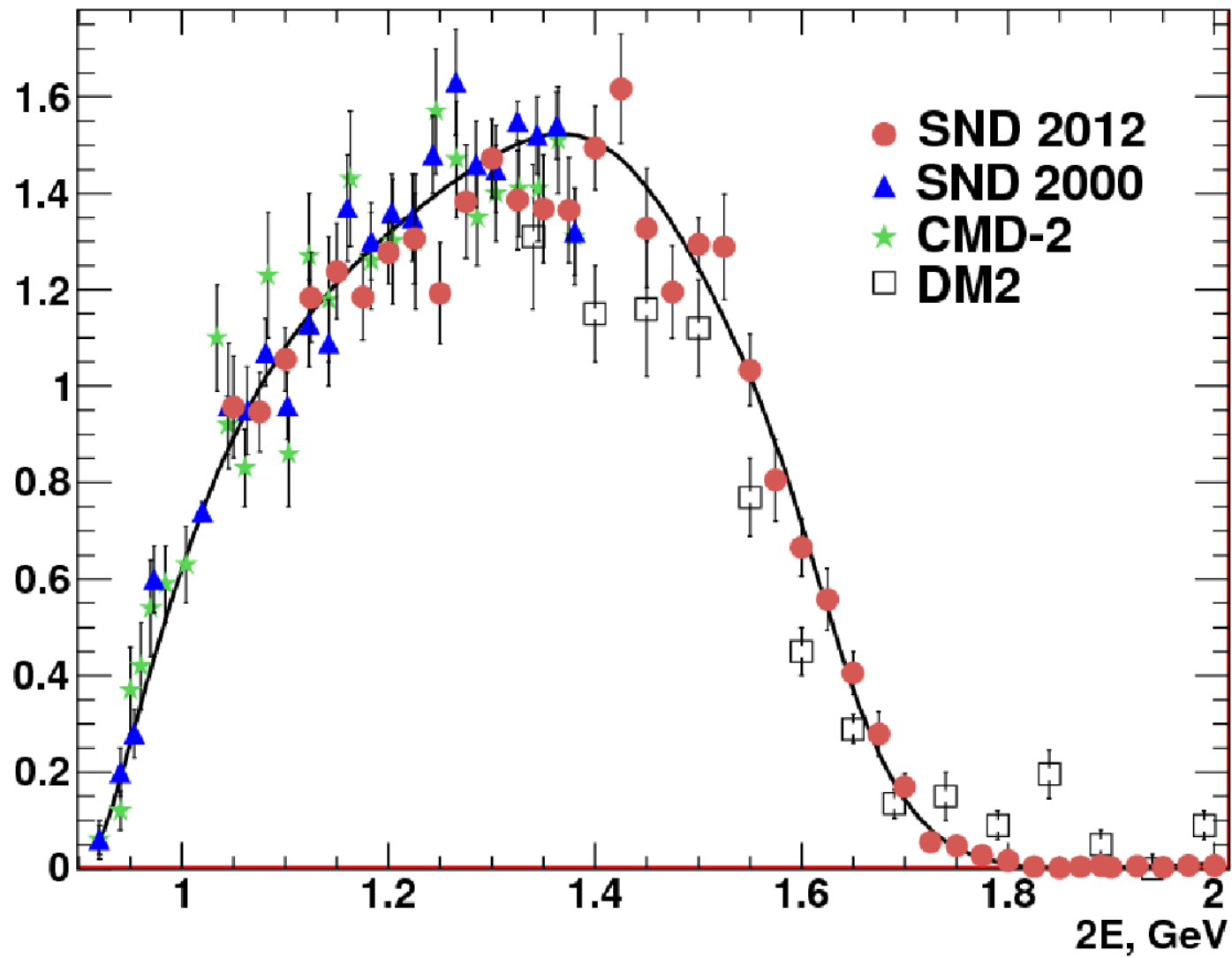
$\phi \rightarrow \eta \gamma^*$  BR  $10^{-4}$

$b_{\pi^0}(m_\phi^2) \phi \rightarrow \pi^0 \gamma^*$  BR  $10^{-5}$

$b_\eta(m_\phi^2)$

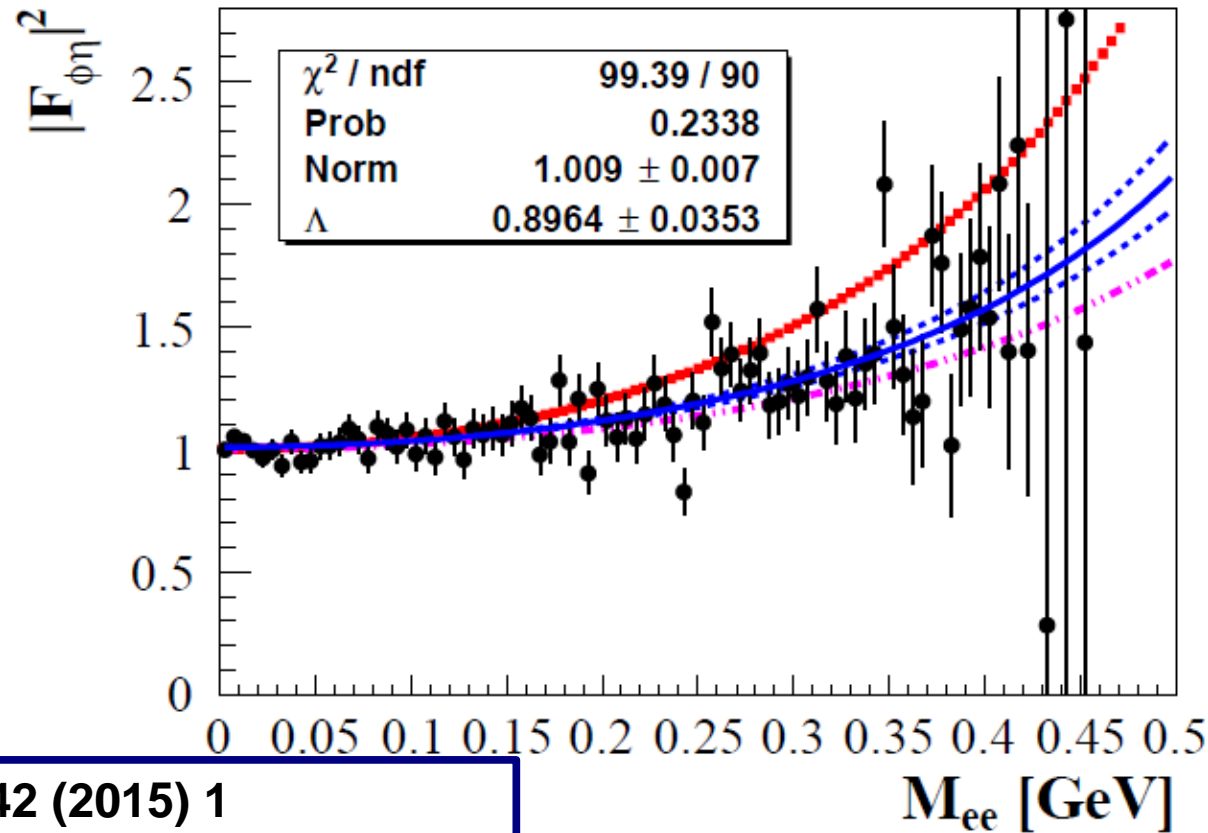
TH: Bonn, GSI, Uppsala, Kharkiv, JLab  
Relation to  $\omega/\phi \rightarrow \pi^+ \pi^- \pi^0$



$$e^+e^- \rightarrow \pi^0 \omega$$
 $\sigma_0, \text{nb}$ 

SND PRD 88 (2013) 054013

# $\phi \rightarrow e^+e^-\eta$



Form factor/BR: Phys.Lett. B742 (2015) 1

	SND/CMD-2 (2001)
$b_{\phi\eta} [\text{GeV}^{-2}]$	$3.8 \pm 1.8 / --$
BR ( $\times 10^4$ )	$1.19 \pm 0.31 /$ $1.14 \pm 0.16$

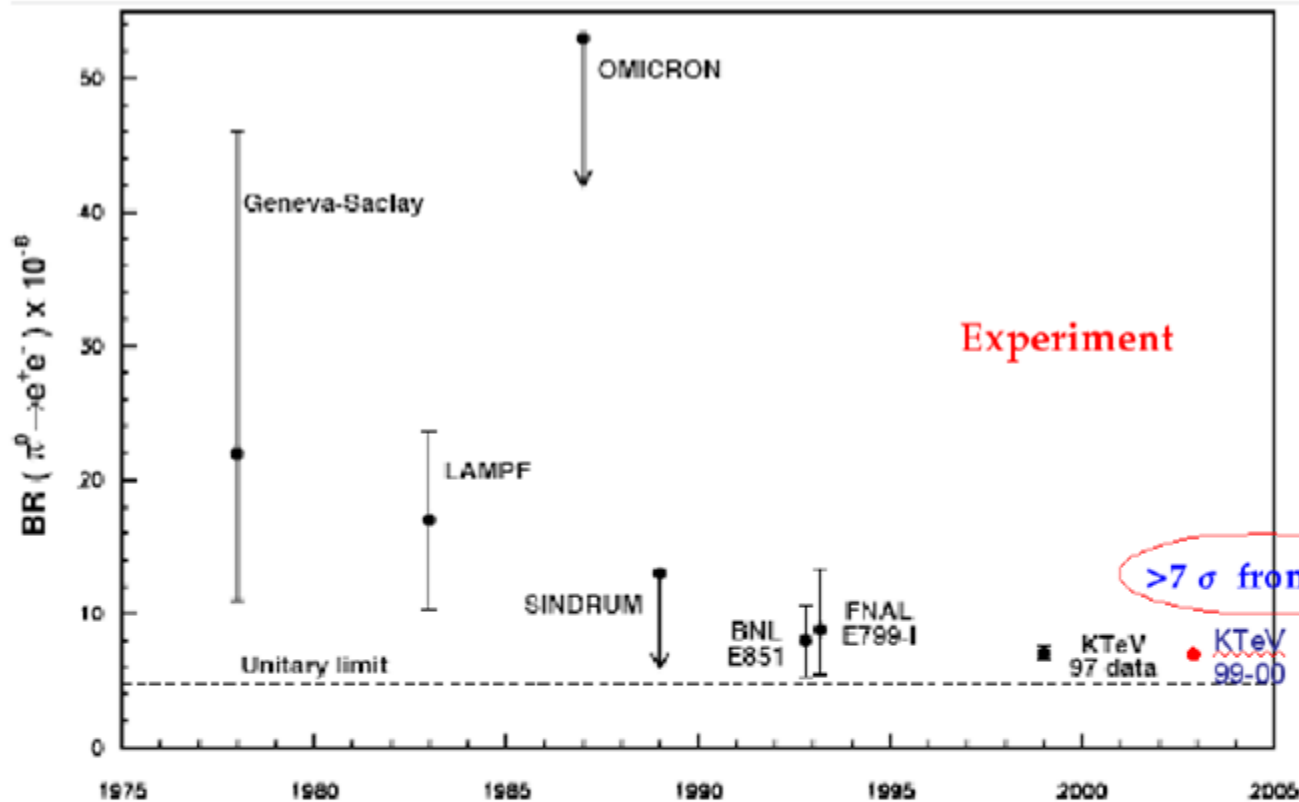
**KLOE 2015**

$$1.17 \pm 0.10^{+0.07}_{-0.11}$$

$$(1.075 \pm 0.007 \pm 0.038)$$

$$F_{\eta}(q^2, m_{\phi}^2) \propto \frac{1}{1 - b_{\eta}(m_{\phi}^2)q^2}$$

# History of $\pi^0 \rightarrow e^+e^-$ measurements



$$BR \approx \alpha^2 \left( \frac{m_e}{m_\pi} \right)^2 \approx O(10^{-8})$$

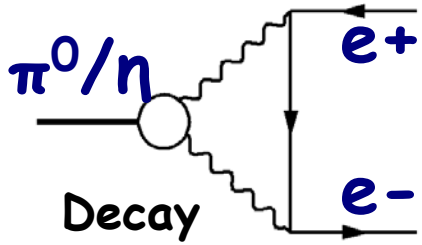
- Unitary bound (model independent)  $BR \geq 4.75 \cdot 10^{-8}$
- Experiment: KTeV (794 events from  $K_L \rightarrow 3\pi^0$ ):  

$$BR(\pi^0 \rightarrow e^+e^-) = (6.44 \pm 0.25_{stat} \pm 0.22_{syst}) \times 10^{-8}$$

$$BR_{\text{no-rad}}(\pi^0 \rightarrow e^+e^-) = (7.48 \pm 0.29_{stat} \pm 0.25_{syst}) \times 10^{-8}$$

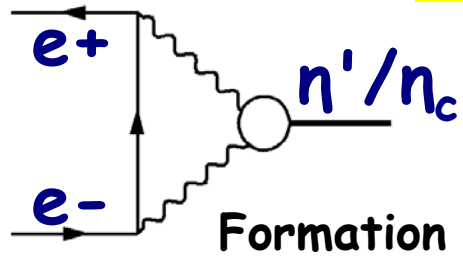
PRD75:012004(07)

# $P \rightarrow e^+e^-$



HADES  
WASA  
Cball, NA60

	UB	SM	$3\sigma$ diff	EXP
$\mathcal{B}(\pi^0 \rightarrow e^+e^-) \times 10^8$	$\geq 4.69$	$6.23 \pm 0.12$		$7.49 \pm 0.38$ KTeV2007
$\mathcal{B}(\eta \rightarrow e^+e^-) \times 10^9$	$\geq 1.78$	$5.2 \pm 0.3$		$\leq 5.6 \cdot 10^3$ HADES2012
$\mathcal{B}(\eta' \rightarrow e^+e^-) \times 10^{10}$	$\geq 0.36$	$1.9 \pm 0.3$		$\leq 2.1 \cdot 10^3$ ND1988
$\mathcal{B}(\eta_c \rightarrow e^+e^-) \times 10^{14}$	$\geq 4.2$	<b>Dorokhov, PLB667,145</b>		



Formation

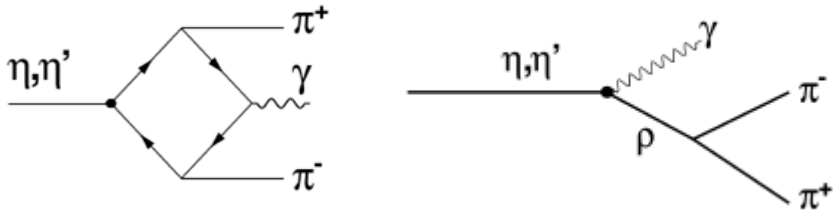
ND  $L=0.5 \text{ pb}^{-1}$   
 $B < 1.2 \cdot 10^{-7}$

VEPP2000  
BESIII

$$\mathcal{B}_{\eta' \rightarrow e^+e^-}$$

CMD3 PLB740, 273 (2015)  
SND PRD91 092010 (2015)  
 $2.9 \text{ pb}^{-1}/\text{exp}$   
Combined  $B < 5.6 \cdot 10^{-9}$  90% CL

# $\eta \rightarrow \pi^+\pi^-\gamma$

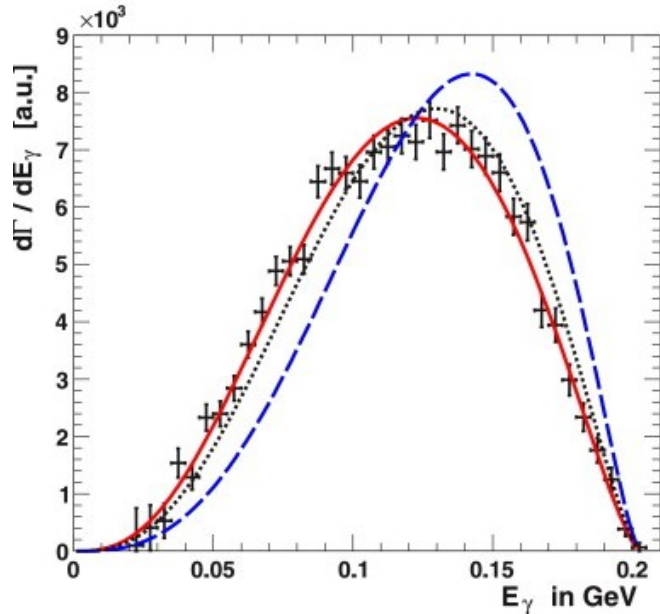


$$\frac{d\Gamma_{\eta(\eta')}}{ds_{\pi\pi}} \propto \left| C + \frac{1}{s_{\pi\pi} - m_\rho^2 - im_\rho\Gamma_\rho} \right|^2$$

$$\frac{d\Gamma}{ds} = |A(1 + \alpha s + \dots)F_V(s)|^2 K_P(s)$$

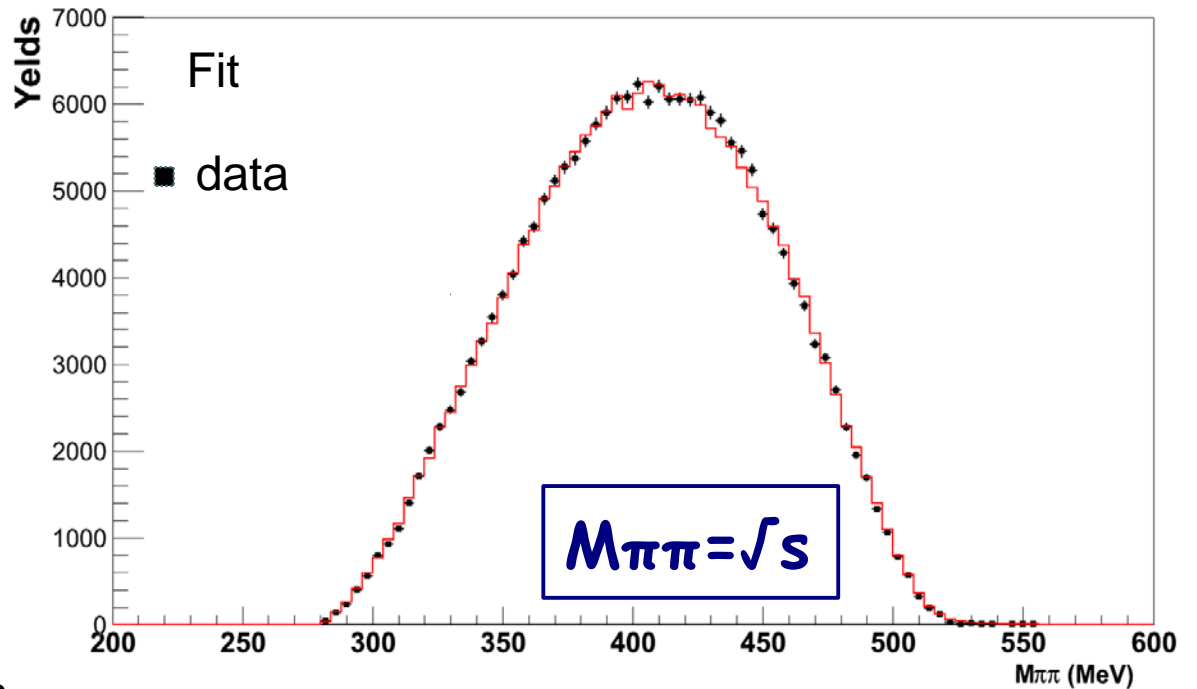
PLB707 (2012) 184

$e^+e^- \rightarrow \pi^+\pi^-$



$$\alpha = 1.89 \pm 0.25_{\text{stat}} \pm 0.59_{\text{syst}} \text{ GeV}^{-2}$$

[WASA PLB707 (2012) 243]



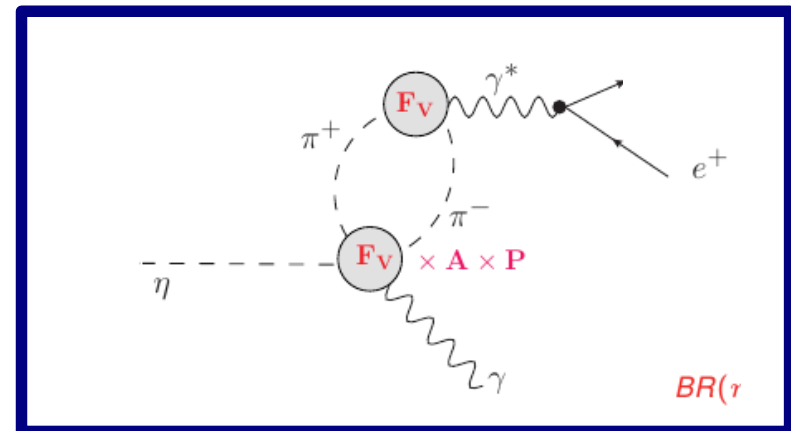
$$\alpha = 1.31 \pm 0.08_{\text{stat}} \pm 0.40_{\text{syst}} \text{ GeV}^{-2}$$

[KLOE PLB718 (2013) 910]

# From $\eta \rightarrow \pi^+\pi^-\gamma$ to $\eta \rightarrow e^+e^-\gamma$

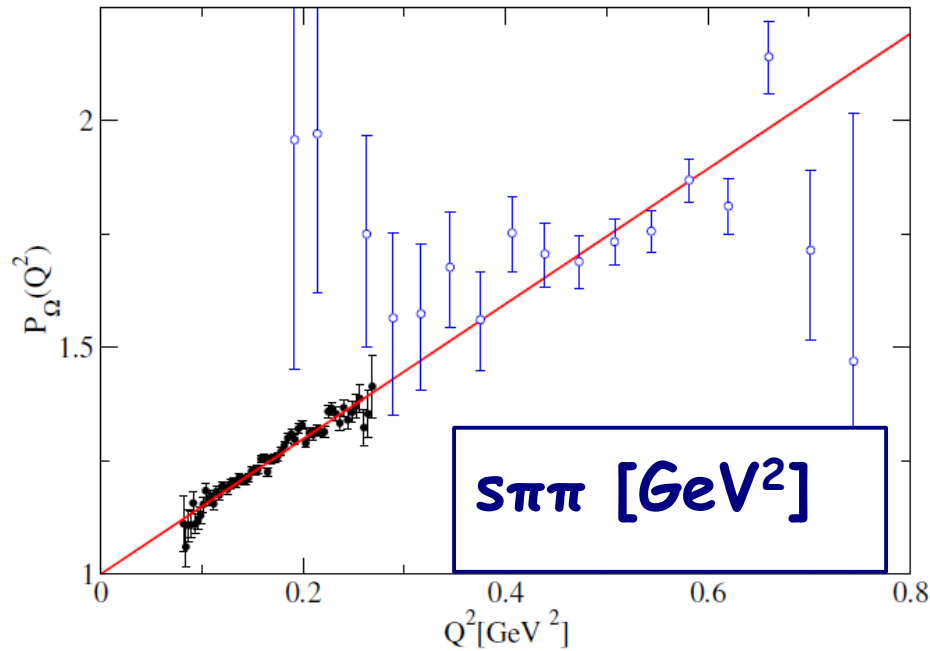
$$P(s_{\pi\pi}) = A_0(1 + \alpha s_{\pi\pi})$$

- $\alpha$  reaction specific
- $\alpha[\eta] = \alpha[\eta']$  understood  
1-loop ChPT + large  $N_c$



**KLOE:  $A + \alpha \Rightarrow b\eta = 2.05^{+0.22}_{-0.10} \text{ GeV}^{-2}$**

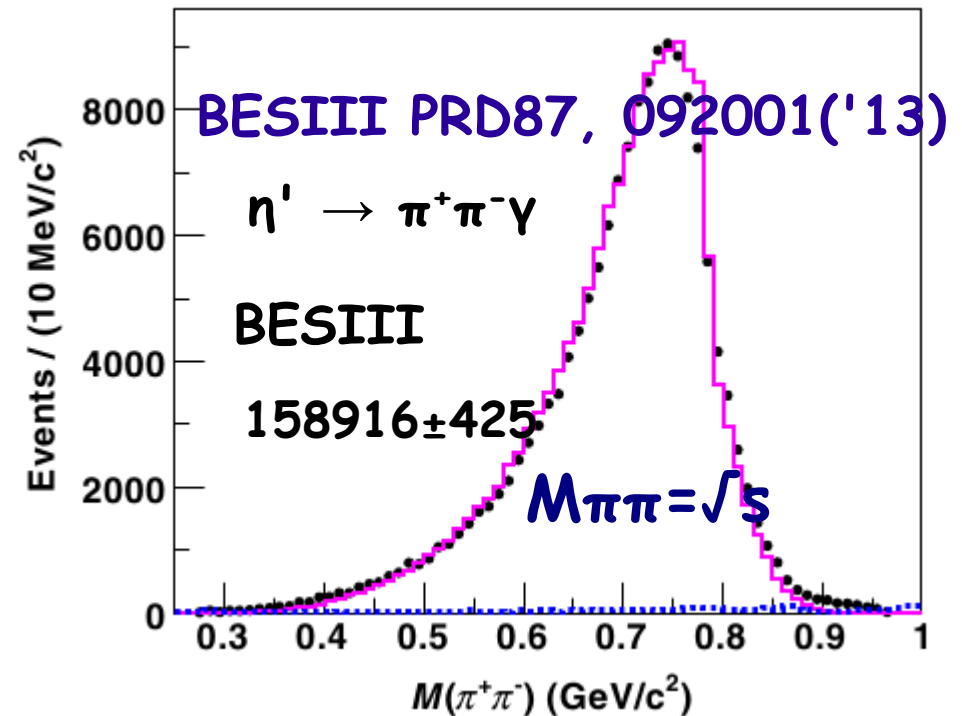
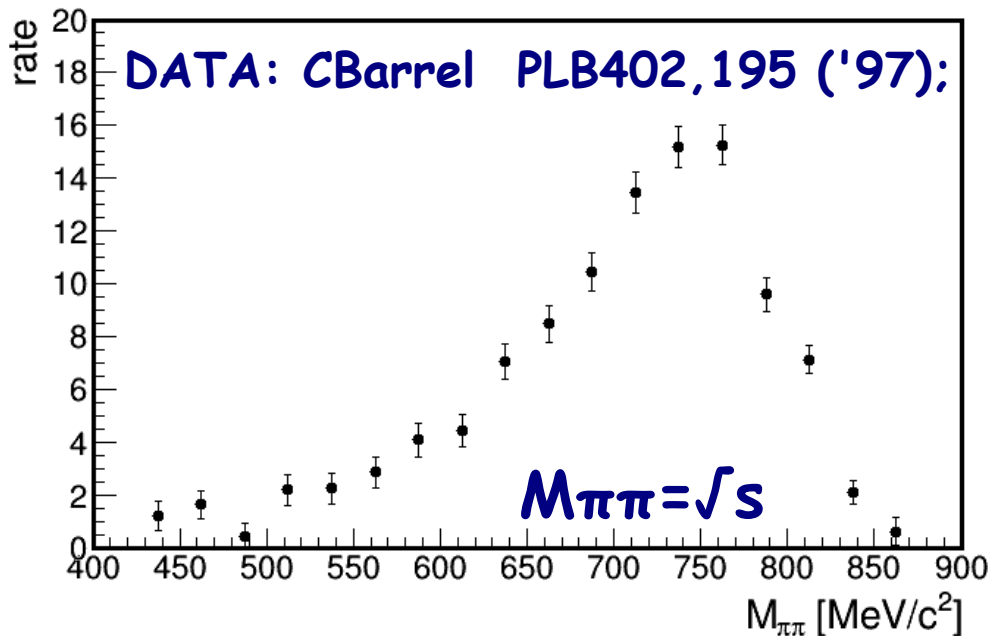
# $\eta' \rightarrow \pi^+\pi^-\gamma$



$$P(s_{\pi\pi}) = A_0(1 + \alpha s_{\pi\pi})$$

→  $\alpha$  reaction specific

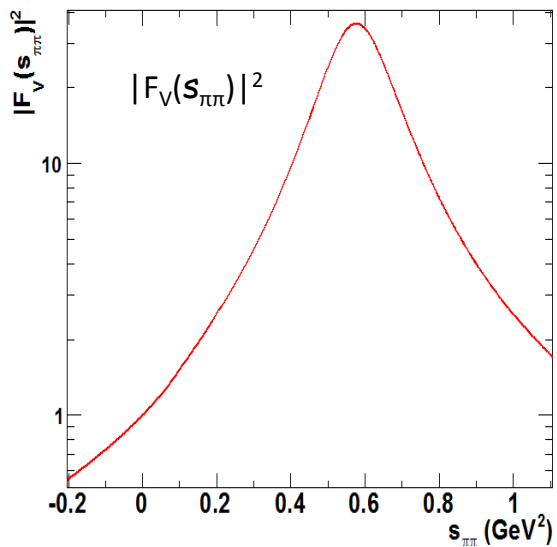
→  $\alpha[\eta] = \alpha[\eta']$  understood  
1-loop ChPT + large  $N_c$



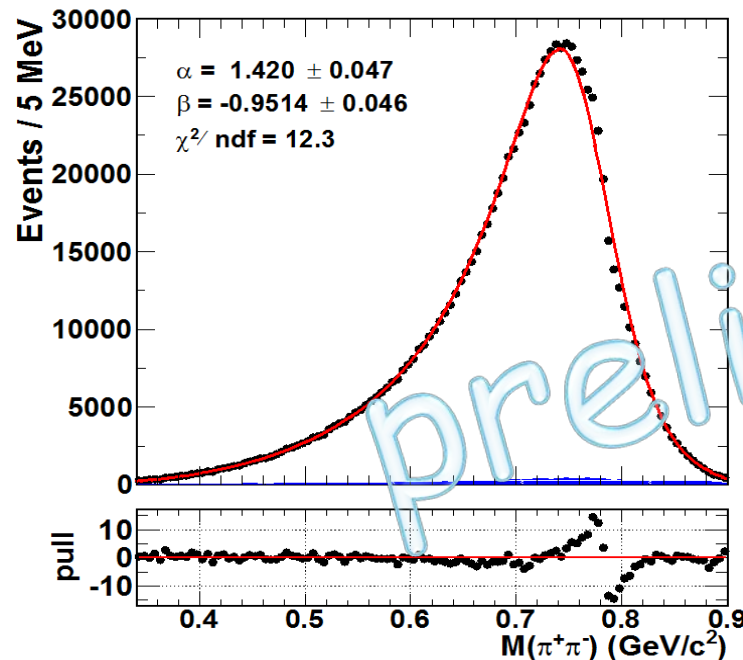
KLOE PL B718, 910 ('13)

# BESIII: Model-independent fit

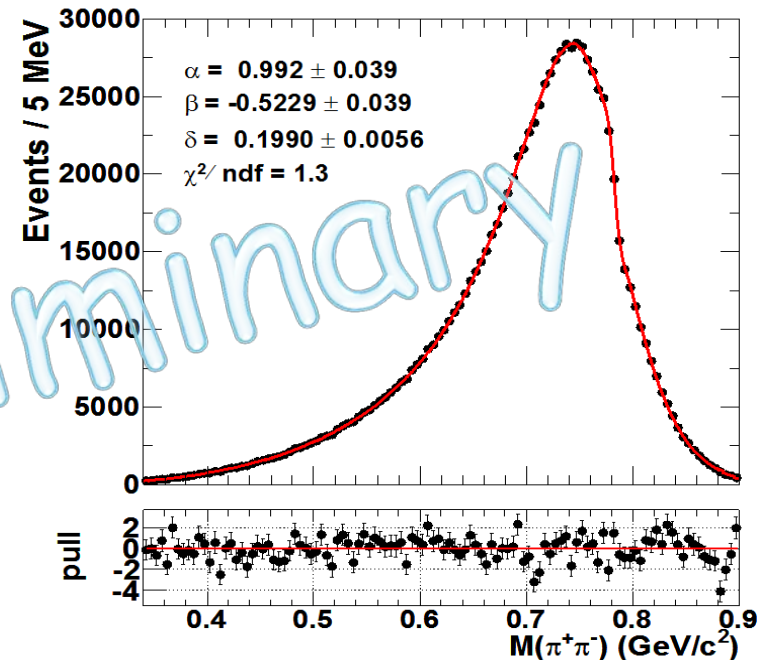
$$\frac{d\Gamma}{ds_{\pi\pi}} = |AP(s_{\pi\pi})F_V(s_{\pi\pi})|^2 \Gamma_0(s_{\pi\pi})$$



$$P(s_{\pi\pi}) = 1 + \alpha s_{\pi\pi} + \beta s_{\pi\pi}^2$$



$$P(s_{\pi\pi}) = 1 + \alpha s_{\pi\pi} + \beta s_{\pi\pi}^2 + \delta BW_\omega$$



Now  $1.9 \times 10^6 \eta \rightarrow \pi^+\pi^-\gamma$

Crystal Barrel:  $\alpha = (1.80 \pm 0.49 \pm 0.04)\text{GeV}^{-2}$

$\beta = (0.04 \pm 0.36 \pm 0.03)\text{GeV}^{-4}$

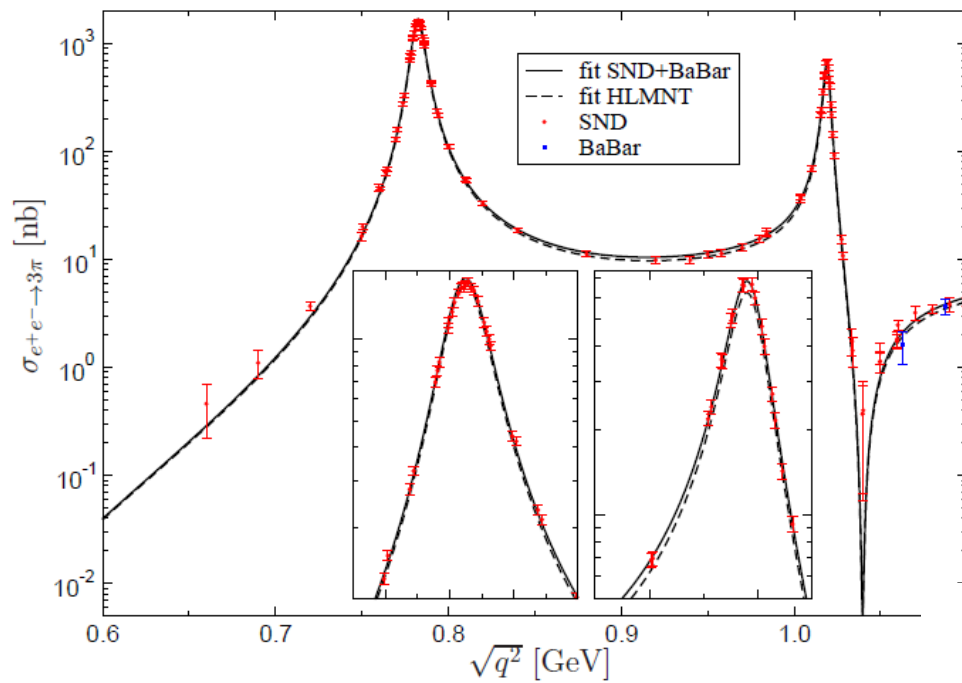
GAMS-2000:  $\alpha = (2.7 \pm 1.0)\text{GeV}^{-2}$

$\omega$  contribution is necessary

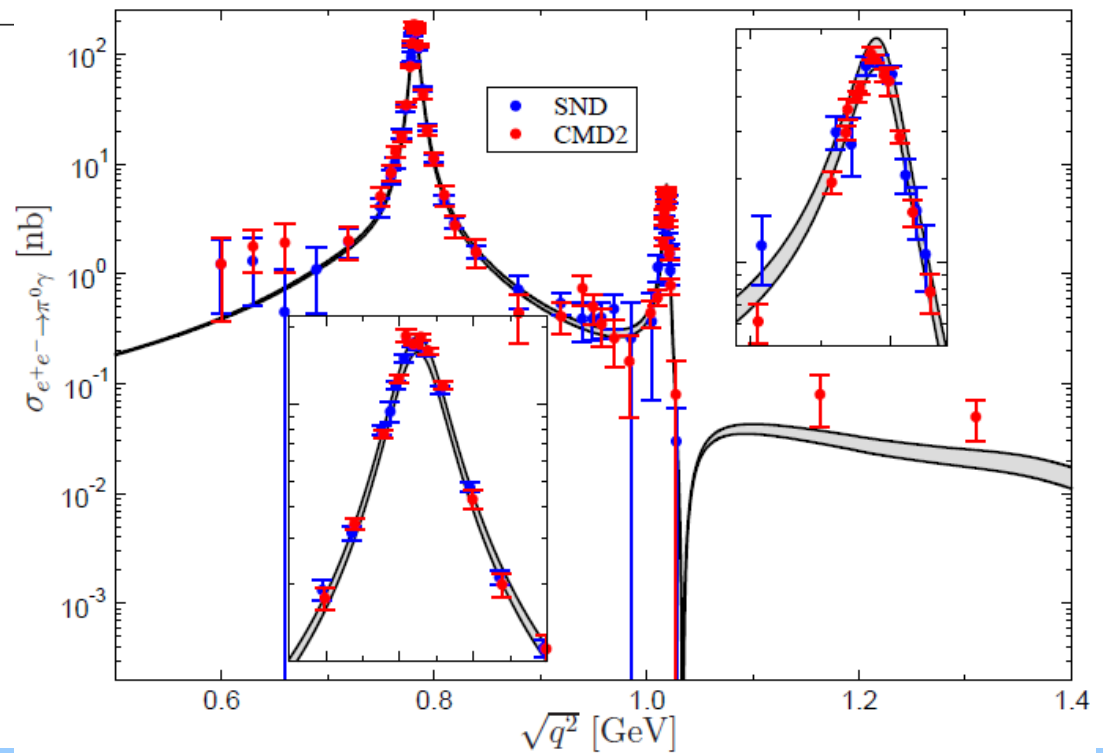
Linear polynomial is insufficient...



# From $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ to $\pi^0$ TFF



$\pi\pi$  phase shifts +  $e^+e^- \rightarrow 3\pi$  data  
Eur.Phys.J. C74 (2014) 3180



Similar strategy for  $\eta$   
From  $e^+e^- \rightarrow \pi^+\pi^-\eta$  to  $\eta$  TFF

arXiv:1509.02194

# Summary and outlook

- TFF Neutral meson structure
- Relation to muon  $(g-2)$  HLbL
- Relation to HVP:  $e^+e^- \rightarrow$  hadrons
- Dark photon searches
- $P \rightarrow e^+e^-$
- Tests of SM in  $\pi^0$ ,  $\eta$ ,  $\eta'$  decays
- Data samples:

KLOE, MAMI, NA62, WASA, HADES, JLAB,  
BESIII... ( $10^{10}\pi^0$ ,  $10^9\eta$ ,  $10^7\eta'$ ,  $10^{10}\varphi$ )