

The Muon ($g-2$) and Degenerate Supersymmetry

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[To appear soon]

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Degenerate Supersymmetry: WHY?

ATLAS SUSY Searches* - 95% CL Lower Limits

Status: July 2015

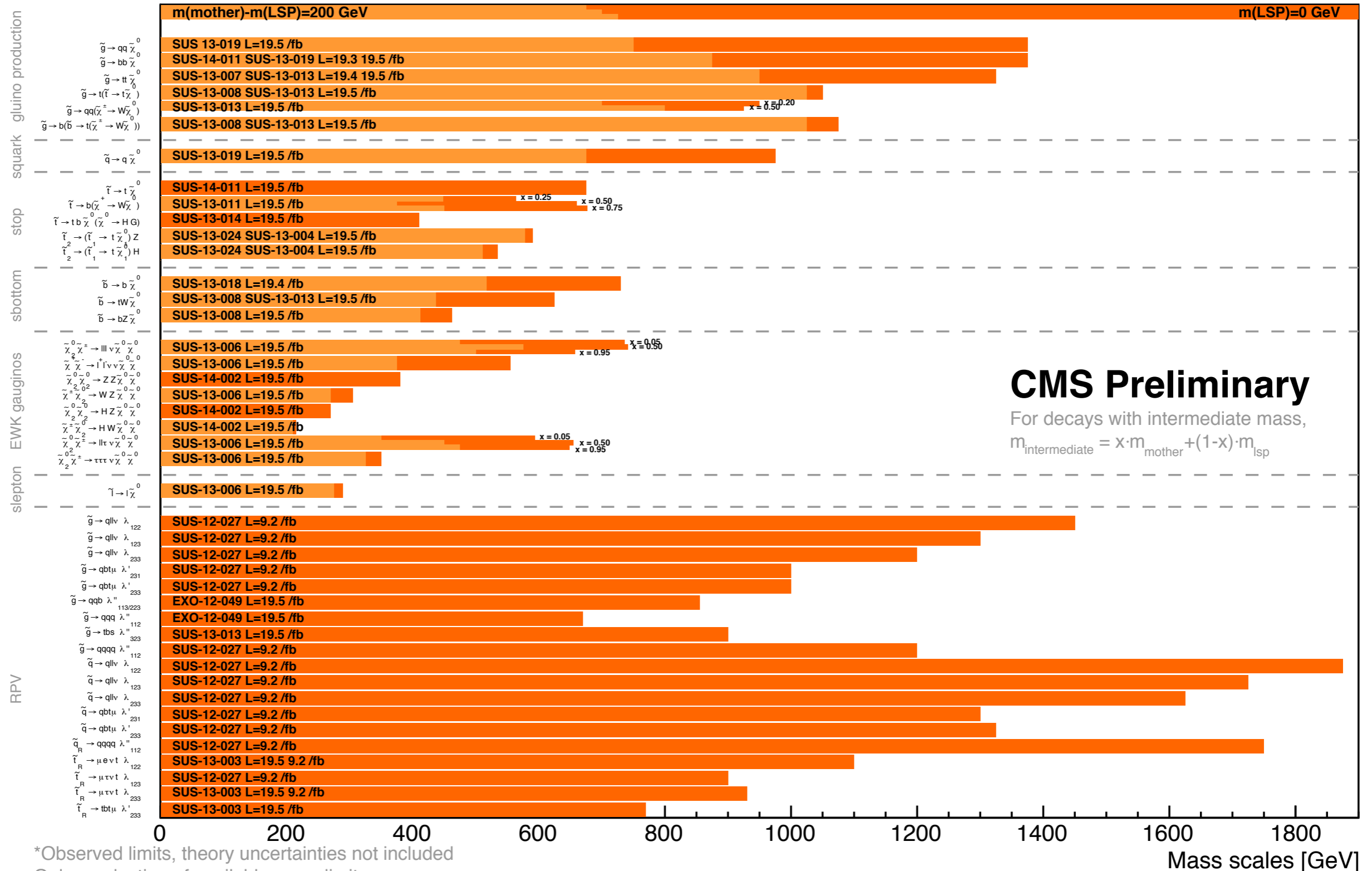
ATLAS Preliminary

$\sqrt{s} = 7, 8 \text{ TeV}$

Model	e, μ, τ, γ	Jets	E_T^{miss}	$\int \mathcal{L} dt [\text{fb}^{-1}]$	Mass limit	$\sqrt{s} = 7 \text{ TeV}$	$\sqrt{s} = 8 \text{ TeV}$	Reference	
Inclusive Searches	MSUGRA/CMSSM	0-3 e, μ /1-2 τ	2-10 jets/3 b	Yes	20.3	\tilde{q}, \tilde{g}	1.8 TeV	$m(\tilde{g})=m(\tilde{g})$	1507.05525
	$\tilde{q}\tilde{q}, \tilde{q}\tilde{q} \rightarrow q\tilde{\chi}_1^0$	0	2-6 jets	Yes	20.3	\tilde{q}	850 GeV	$m(\tilde{\chi}_1^0)=0 \text{ GeV}, m(1^{\text{st}} \text{ gen. } \tilde{q})=m(2^{\text{nd}} \text{ gen. } \tilde{q})$	1405.7875
	$\tilde{q}\tilde{q}, \tilde{q}\tilde{q} \rightarrow q\tilde{\chi}_1^0$ (compressed)	mono-jet	1-3 jets	Yes	20.3	\tilde{q}	100-440 GeV	$m(\tilde{q})-m(\tilde{\chi}_1^0)<10 \text{ GeV}$	1507.05525
	$\tilde{q}\tilde{q}, \tilde{q}\tilde{q} \rightarrow q(\ell\ell/\ell\nu/\nu\nu)\tilde{\chi}_1^0$	2 e, μ (off-Z)	2 jets	Yes	20.3	\tilde{q}	780 GeV	$m(\tilde{\chi}_1^0)=0 \text{ GeV}$	1503.03290
	$\tilde{g}\tilde{g}, \tilde{g}\tilde{g} \rightarrow q\tilde{q}\tilde{\chi}_1^0$	0	2-6 jets	Yes	20.3	\tilde{g}	1.33 TeV	$m(\tilde{\chi}_1^0)=0 \text{ GeV}$	1405.7875
	$\tilde{g}\tilde{g}, \tilde{g}\tilde{g} \rightarrow q\tilde{q}\tilde{\chi}_1^\pm \rightarrow q\tilde{q}W^\pm\tilde{\chi}_1^0$	0-1 e, μ	2-6 jets	Yes	20	\tilde{g}	1.26 TeV	$m(\tilde{\chi}_1^0)<300 \text{ GeV}, m(\tilde{\chi}^\pm)=0.5(m(\tilde{\chi}_1^0)+m(\tilde{g}))$	1507.05525
	$\tilde{g}\tilde{g}, \tilde{g}\tilde{g} \rightarrow q\tilde{q}(\ell\ell/\ell\nu/\nu\nu)\tilde{\chi}_1^0$	2 e, μ	0-3 jets	-	20	\tilde{g}	1.32 TeV	$m(\tilde{\chi}_1^0)=0 \text{ GeV}$	1501.03555
	GMSB ($\tilde{\ell}$ NLSP)	1-2 τ + 0-1 ℓ	0-2 jets	Yes	20.3	\tilde{g}	1.6 TeV	$\tan\beta > 20$	1407.0603
	GGM (bino NLSP)	2 γ	-	Yes	20.3	\tilde{g}	1.29 TeV	$c\tau(\text{NLSP})<0.1 \text{ mm}$	1507.05493
	GGM (higgsino-bino NLSP)	γ	1 b	Yes	20.3	\tilde{g}	1.3 TeV	$m(\tilde{\chi}_1^0)<900 \text{ GeV}, c\tau(\text{NLSP})<0.1 \text{ mm}, \mu<0$	1507.05493
GGM (higgsino-bino NLSP)	γ	2 jets	Yes	20.3	\tilde{g}	1.25 TeV	$m(\tilde{\chi}_1^0)<850 \text{ GeV}, c\tau(\text{NLSP})<0.1 \text{ mm}, \mu>0$	1507.05493	
GGM (higgsino NLSP)	2 e, μ (Z)	2 jets	Yes	20.3	\tilde{g}	850 GeV	$m(\text{NLSP})>430 \text{ GeV}$	1503.03290	
Gravitino LSP	0	mono-jet	Yes	20.3	$F^{1/2}$ scale	865 GeV	$m(\tilde{G})>1.8 \times 10^{-4} \text{ eV}, m(\tilde{g})=m(\tilde{q})=1.5 \text{ TeV}$	1502.01518	
3 rd gen. \tilde{g} med.	$\tilde{g}\tilde{g}, \tilde{g}\tilde{g} \rightarrow b\tilde{b}\tilde{\chi}_1^0$	0	3 b	Yes	20.1	\tilde{g}	1.25 TeV	$m(\tilde{\chi}_1^0)<400 \text{ GeV}$	1407.0600
	$\tilde{g}\tilde{g}, \tilde{g}\tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$	0	7-10 jets	Yes	20.3	\tilde{g}	1.1 TeV	$m(\tilde{\chi}_1^0) < 350 \text{ GeV}$	1308.1841
	$\tilde{g}\tilde{g}, \tilde{g}\tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^\pm$	0-1 e, μ	3 b	Yes	20.1	\tilde{g}	1.34 TeV	$m(\tilde{\chi}_1^0)<400 \text{ GeV}$	1407.0600
	$\tilde{g}\tilde{g}, \tilde{g}\tilde{g} \rightarrow b\tilde{b}\tilde{\chi}_1^\pm$	0-1 e, μ	3 b	Yes	20.1	\tilde{g}	1.3 TeV	$m(\tilde{\chi}_1^0)<300 \text{ GeV}$	1407.0600
3 rd gen. squarks direct production	$\tilde{b}_1\tilde{b}_1, \tilde{b}_1\tilde{b}_1 \rightarrow b\tilde{\chi}_1^0$	0	2 b	Yes	20.1	\tilde{b}_1	100-620 GeV	$m(\tilde{\chi}_1^0)<90 \text{ GeV}$	1308.2631
	$\tilde{b}_1\tilde{b}_1, \tilde{b}_1\tilde{b}_1 \rightarrow t\tilde{\chi}_1^\pm$	2 e, μ (SS)	0-3 b	Yes	20.3	\tilde{b}_1	275-440 GeV	$m(\tilde{\chi}_1^\pm)=2 m(\tilde{\chi}_1^0)$	1404.2500
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1\tilde{t}_1 \rightarrow b\tilde{\chi}_1^\pm$	1-2 e, μ	1-2 b	Yes	4.7/20.3	\tilde{t}_1	110-167 GeV, 230-460 GeV	$m(\tilde{\chi}_1^\pm) = 2m(\tilde{\chi}_1^0), m(\tilde{\chi}_1^0)=55 \text{ GeV}$	1209.2102, 1407.0583
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1\tilde{t}_1 \rightarrow Wb\tilde{\chi}_1^0$ or $t\tilde{\chi}_1^0$	0-2 e, μ	0-2 jets/1-2 b	Yes	20.3	\tilde{t}_1	90-191 GeV, 210-700 GeV	$m(\tilde{\chi}_1^0)=1 \text{ GeV}$	1506.08616
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1\tilde{t}_1 \rightarrow c\tilde{\chi}_1^0$	0	mono-jet/c-tag	Yes	20.3	\tilde{t}_1	90-240 GeV	$m(\tilde{t}_1)-m(\tilde{\chi}_1^0)<85 \text{ GeV}$	1407.0608
	$\tilde{t}_1\tilde{t}_1$ (natural GMSB)	2 e, μ (Z)	1 b	Yes	20.3	\tilde{t}_1	150-580 GeV	$m(\tilde{\chi}_1^0)>150 \text{ GeV}$	1403.5222
	$\tilde{t}_2\tilde{t}_2, \tilde{t}_2\tilde{t}_2 \rightarrow \tilde{t}_1 + Z$	3 e, μ (Z)	1 b	Yes	20.3	\tilde{t}_2	290-600 GeV	$m(\tilde{\chi}_1^0)<200 \text{ GeV}$	1403.5222
EW direct	$\tilde{\ell}_{L,R}\tilde{\ell}_{L,R}, \tilde{\ell}\tilde{\ell} \rightarrow \ell\tilde{\chi}_1^0$	2 e, μ	0	Yes	20.3	$\tilde{\ell}$	90-325 GeV	$m(\tilde{\chi}_1^0)=0 \text{ GeV}$	1403.5294
	$\tilde{\chi}_1^\pm\tilde{\chi}_1^\pm, \tilde{\chi}_1^\pm\tilde{\chi}_1^\pm \rightarrow \tilde{\ell}\nu(\tilde{\ell}\bar{\nu})$	2 e, μ	0	Yes	20.3	$\tilde{\chi}_1^\pm$	140-465 GeV	$m(\tilde{\chi}_1^0)=0 \text{ GeV}, m(\tilde{\ell}, \tilde{\nu})=0.5(m(\tilde{\chi}_1^\pm)+m(\tilde{\chi}_1^0))$	1403.5294
	$\tilde{\chi}_1^\pm\tilde{\chi}_1^\pm, \tilde{\chi}_1^\pm\tilde{\chi}_1^\pm \rightarrow \tilde{\tau}\nu(\tilde{\tau}\bar{\nu})$	2 τ	-	Yes	20.3	$\tilde{\chi}_1^\pm$	100-350 GeV	$m(\tilde{\chi}_1^0)=0 \text{ GeV}, m(\tilde{\tau}, \tilde{\nu})=0.5(m(\tilde{\chi}_1^\pm)+m(\tilde{\chi}_1^0))$	1407.0350
	$\tilde{\chi}_1^\pm\tilde{\chi}_2^0 \rightarrow \tilde{\ell}\nu\tilde{\ell}_L(\tilde{\nu}\nu), \tilde{\ell}\tilde{\nu}\tilde{\ell}_L(\tilde{\nu}\nu)$	3 e, μ	0	Yes	20.3	$\tilde{\chi}_1^\pm, \tilde{\chi}_2^0$	700 GeV	$m(\tilde{\chi}_1^\pm)=m(\tilde{\chi}_2^0), m(\tilde{\chi}_1^0)=0, m(\tilde{\ell}, \tilde{\nu})=0.5(m(\tilde{\chi}_1^\pm)+m(\tilde{\chi}_1^0))$	1402.7029
	$\tilde{\chi}_1^\pm\tilde{\chi}_2^0 \rightarrow W\tilde{\chi}_1^0 Z\tilde{\chi}_1^0$	2-3 e, μ	0-2 jets	Yes	20.3	$\tilde{\chi}_1^\pm, \tilde{\chi}_2^0$	420 GeV	$m(\tilde{\chi}_1^\pm)=m(\tilde{\chi}_2^0), m(\tilde{\chi}_1^0)=0, \text{ sleptons decoupled}$	1403.5294, 1402.7029
	$\tilde{\chi}_1^\pm\tilde{\chi}_2^0 \rightarrow W\tilde{\chi}_1^0 h\tilde{\chi}_1^0, h \rightarrow b\tilde{b}/WW/\tau\tau/\gamma\gamma$	e, μ, γ	0-2 b	Yes	20.3	$\tilde{\chi}_1^\pm, \tilde{\chi}_2^0$	250 GeV	$m(\tilde{\chi}_1^\pm)=m(\tilde{\chi}_2^0), m(\tilde{\chi}_1^0)=0, \text{ sleptons decoupled}$	1501.07110
	$\tilde{\chi}_2^0\tilde{\chi}_3^0, \tilde{\chi}_2^0\tilde{\chi}_3^0 \rightarrow \tilde{\ell}_R\ell$	4 e, μ	0	Yes	20.3	$\tilde{\chi}_2^0, \tilde{\chi}_3^0$	620 GeV	$m(\tilde{\chi}_2^0)=m(\tilde{\chi}_3^0), m(\tilde{\chi}_1^0)=0, m(\tilde{\ell}, \tilde{\nu})=0.5(m(\tilde{\chi}_2^0)+m(\tilde{\chi}_1^0))$	1405.5086
	GGM (wino NLSP) weak prod.	1 $e, \mu + \gamma$	-	Yes	20.3	\tilde{W}	124-361 GeV	$c\tau < 1 \text{ mm}$	1507.05493
Long-lived particles	Direct $\tilde{\chi}_1^\pm\tilde{\chi}_1^\pm$ prod., long-lived $\tilde{\chi}_1^\pm$	Disapp. trk	1 jet	Yes	20.3	$\tilde{\chi}_1^\pm$	270 GeV	$m(\tilde{\chi}_1^\pm)-m(\tilde{\chi}_1^0)\sim 160 \text{ MeV}, \tau(\tilde{\chi}_1^\pm)=0.2 \text{ ns}$	1310.3675
	Direct $\tilde{\chi}_1^\pm\tilde{\chi}_1^\pm$ prod., long-lived $\tilde{\chi}_1^\pm$	dE/dx trk	-	Yes	18.4	$\tilde{\chi}_1^\pm$	482 GeV	$m(\tilde{\chi}_1^\pm)-m(\tilde{\chi}_1^0)\sim 160 \text{ MeV}, \tau(\tilde{\chi}_1^\pm)<15 \text{ ns}$	1506.05332
	Stable, stopped \tilde{g} R-hadron	0	1-5 jets	Yes	27.9	\tilde{g}	832 GeV	$m(\tilde{\chi}_1^0)=100 \text{ GeV}, 10 \mu\text{s}<\tau(\tilde{g})<1000 \text{ s}$	1310.6584
	Stable \tilde{g} R-hadron	trk	-	-	19.1	\tilde{g}	1.27 TeV	-	1411.6795
	GMSB, stable $\tilde{\tau}, \tilde{\chi}_1^0 \rightarrow \tilde{\tau}(\tilde{e}, \tilde{\mu})+\tau(e, \mu)$	1-2 μ	-	-	19.1	$\tilde{\chi}_1^0$	537 GeV	$10 < \tan\beta < 50$	1411.6795
	GMSB, $\tilde{\chi}_1^0 \rightarrow \gamma\tilde{G}$, long-lived $\tilde{\chi}_1^0$	2 γ	-	Yes	20.3	$\tilde{\chi}_1^0$	435 GeV	$2 < \tau(\tilde{\chi}_1^0) < 3 \text{ ns}, \text{ SPS8 model}$	1409.5542
	$\tilde{g}\tilde{g}, \tilde{\chi}_1^0 \rightarrow ee\nu/\mu\nu/\mu\mu\nu$	displ. $ee/\mu\mu/\mu\mu\nu$	-	-	20.3	$\tilde{\chi}_1^0$	1.0 TeV	$7 < c\tau(\tilde{\chi}_1^0) < 740 \text{ mm}, m(\tilde{g})=1.3 \text{ TeV}$	1504.05162
	GGM $\tilde{g}\tilde{g}, \tilde{\chi}_1^0 \rightarrow Z\tilde{G}$	displ. vtx + jets	-	-	20.3	$\tilde{\chi}_1^0$	1.0 TeV	$6 < c\tau(\tilde{\chi}_1^0) < 480 \text{ mm}, m(\tilde{g})=1.1 \text{ TeV}$	1504.05162
LFV	$pp \rightarrow \tilde{\nu}_\tau + X, \tilde{\nu}_\tau \rightarrow e\mu/\tau\mu$	$e\mu, e\tau, \mu\tau$	-	-	20.3	$\tilde{\nu}_\tau$	1.7 TeV	$\lambda'_{311}=0.11, \lambda_{132/133/233}=0.07$	1503.04430
	Bilinear RPV CMSSM	2 e, μ (SS)	0-3 b	Yes	20.3	\tilde{q}, \tilde{g}	1.35 TeV	$m(\tilde{q})=m(\tilde{g}), c\tau_{\text{LSP}}<1 \text{ mm}$	1404.2500
	$\tilde{\chi}_1^\pm\tilde{\chi}_1^\pm, \tilde{\chi}_1^\pm\tilde{\chi}_1^\pm \rightarrow W\tilde{\chi}_1^0, \tilde{\chi}_1^0 \rightarrow ee\tilde{\nu}_\mu, e\mu\tilde{\nu}_e$	4 e, μ	-	Yes	20.3	$\tilde{\chi}_1^\pm$	750 GeV	$m(\tilde{\chi}_1^0)>0.2 \times m(\tilde{\chi}_1^\pm), \lambda_{121} \neq 0$	1405.5086

Degenerate Supersymmetry: WHY?

Summary of CMS SUSY Results* in SMS framework



Degenerate Supersymmetry: WHY?

Compact / Compressed / Degenerate SUSY

[LeCompte, Martin (2011,2012)]

Low visible and missing energy in the sparticle decays

Signal can remain hidden from the collider searches

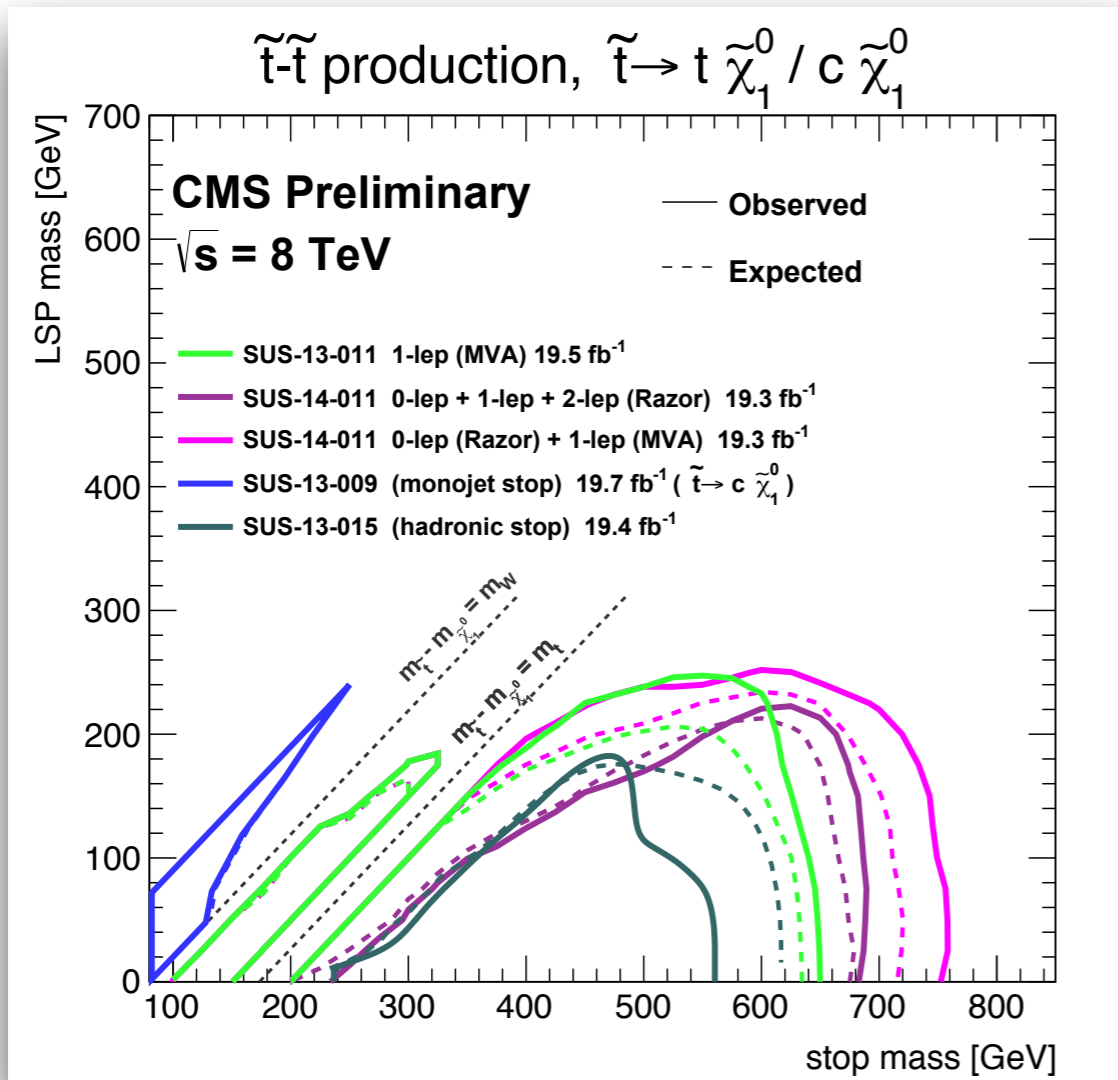
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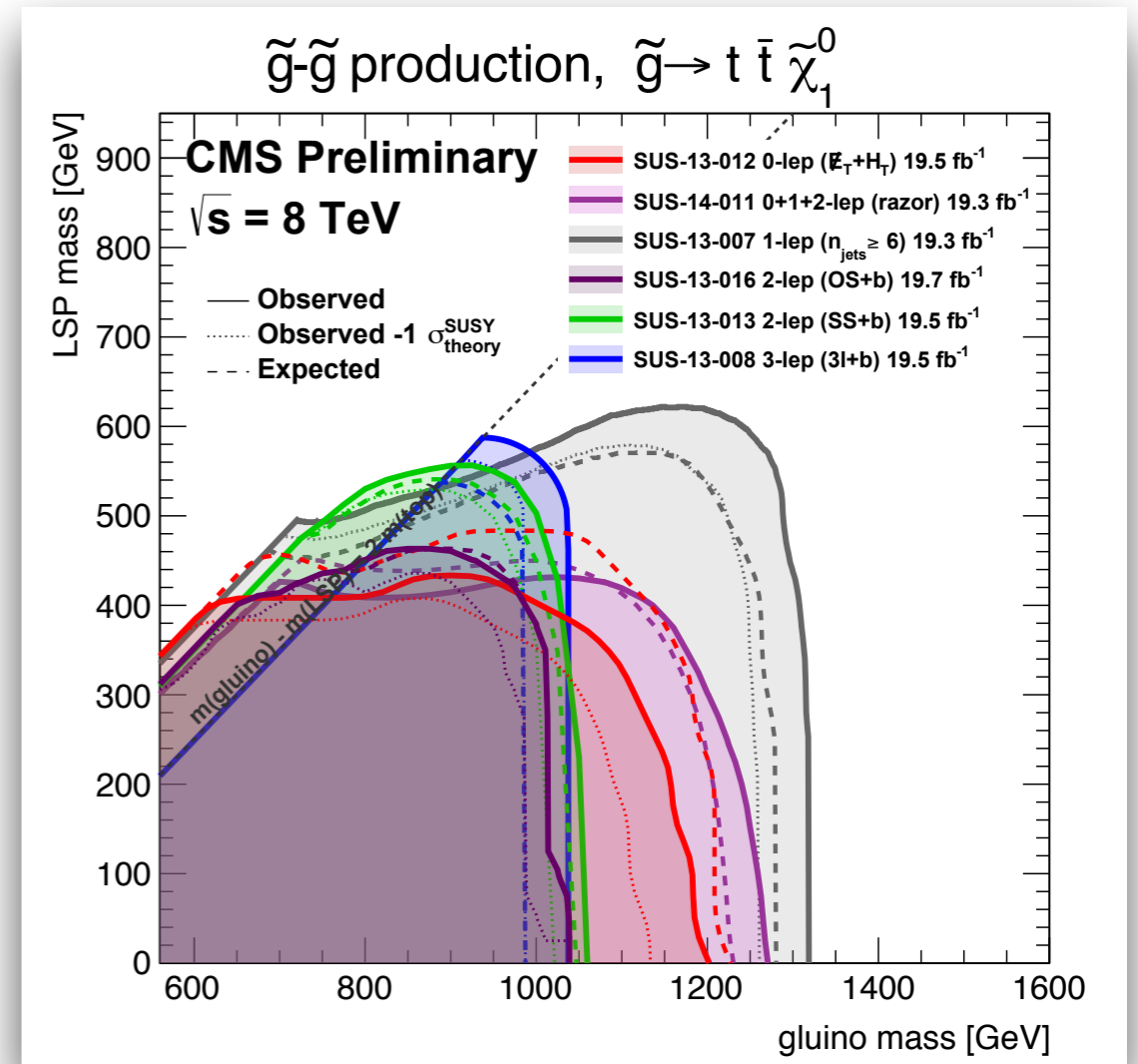
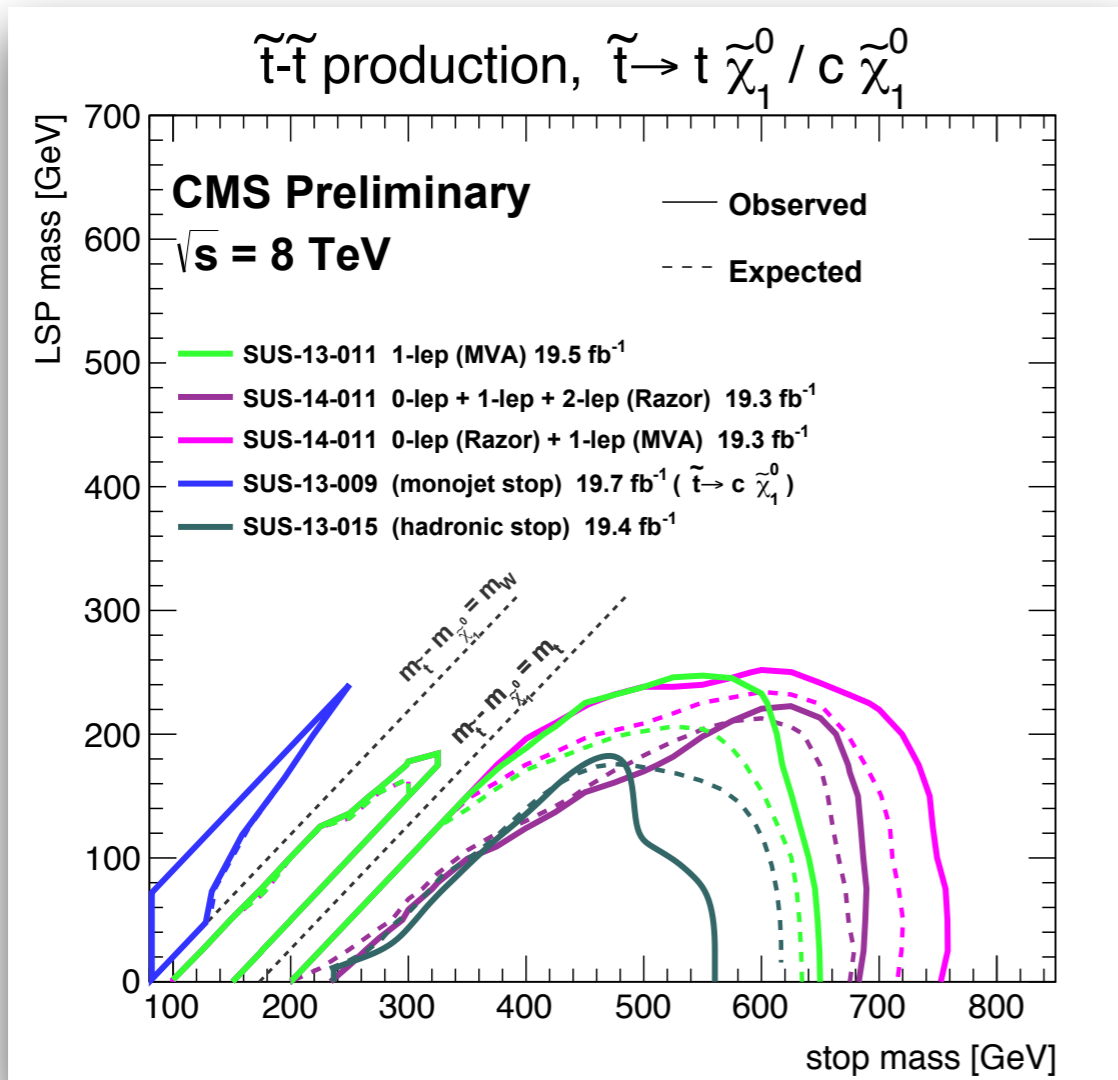
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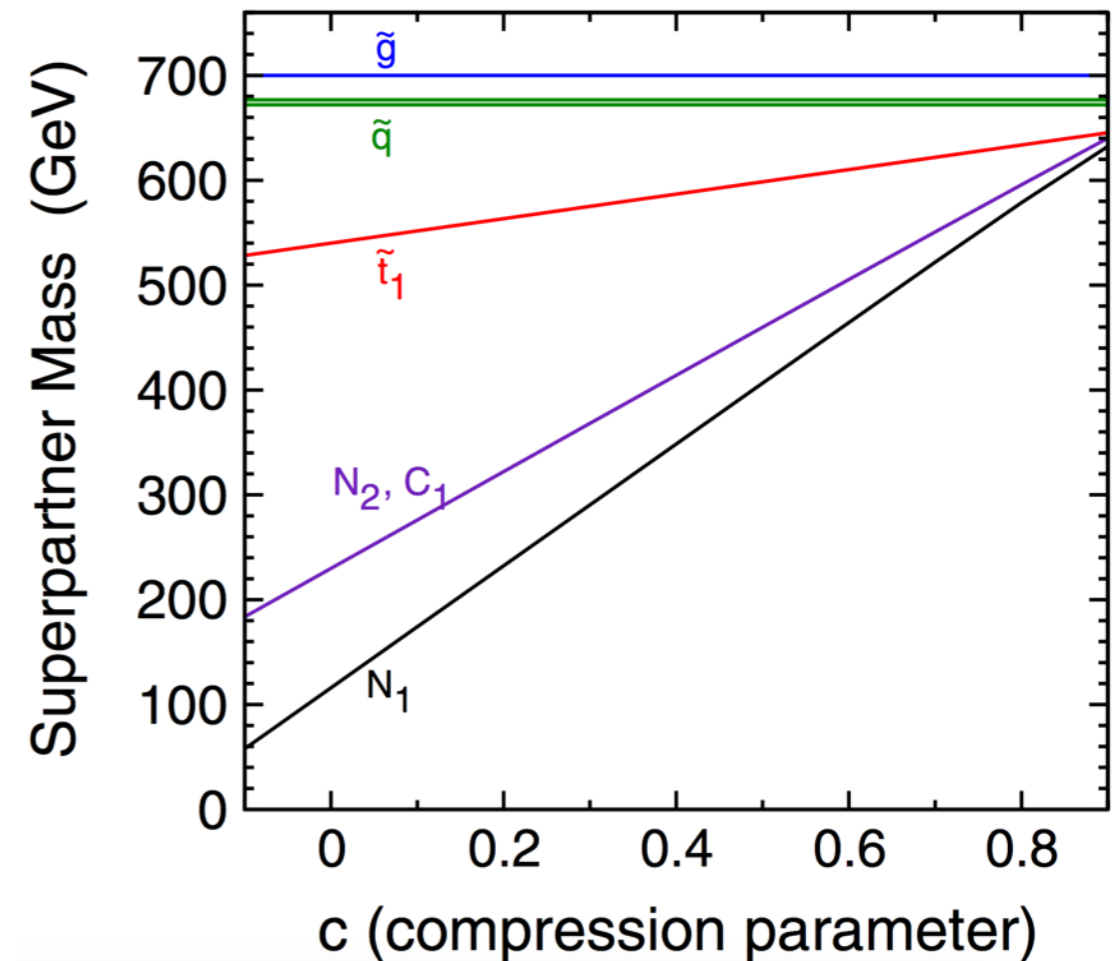


Degenerate Supersymmetry: WHY?

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$$M_1 = \left(\frac{1+5c}{6}\right)M_{\tilde{g}}, \quad M_2 = \left(\frac{1+2c}{3}\right)M_{\tilde{g}}.$$



Degenerate Supersymmetry: WHY?

Compact / Compressed / Degenerate SUSY

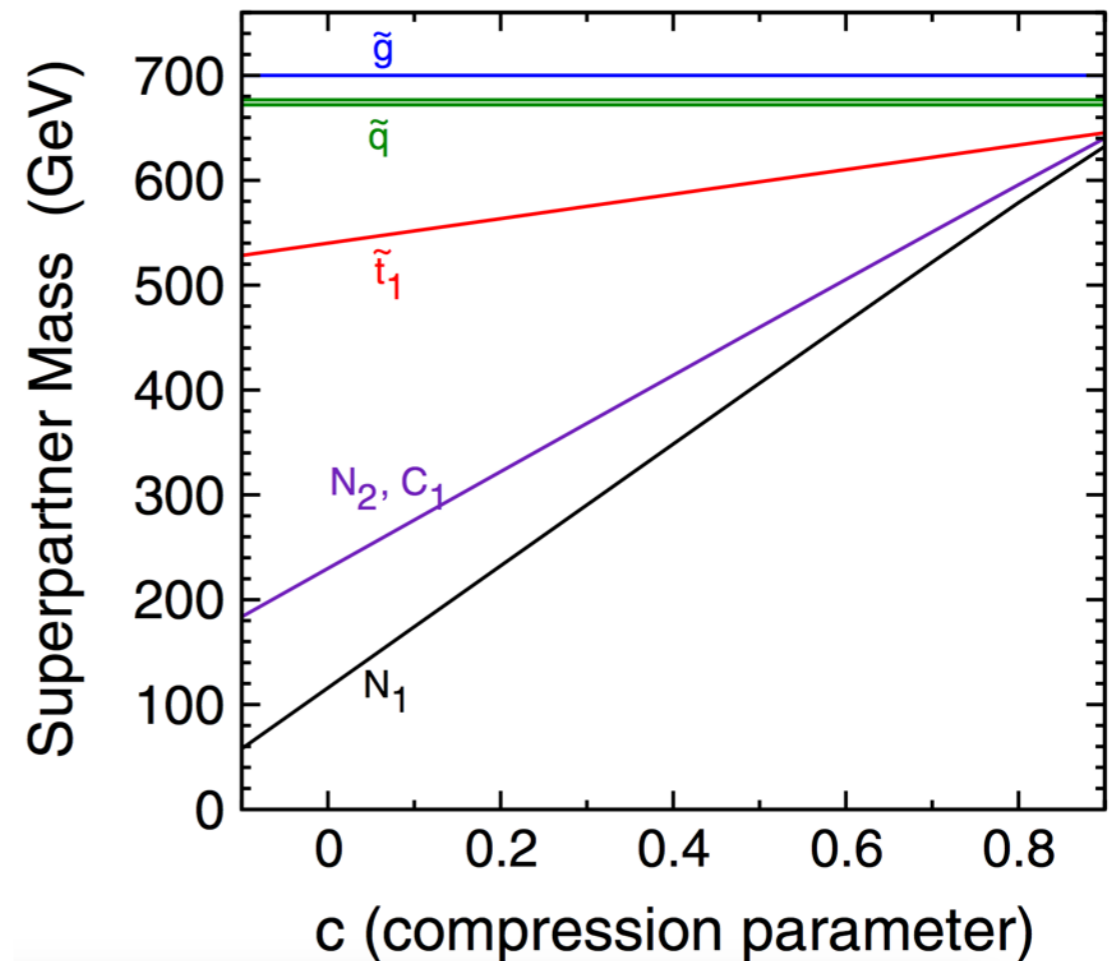
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$c=0$ mSUGRA like spectrum

Light Neutralinos, Charginos
High Visible/Missing Energy

Easy to rule it out !



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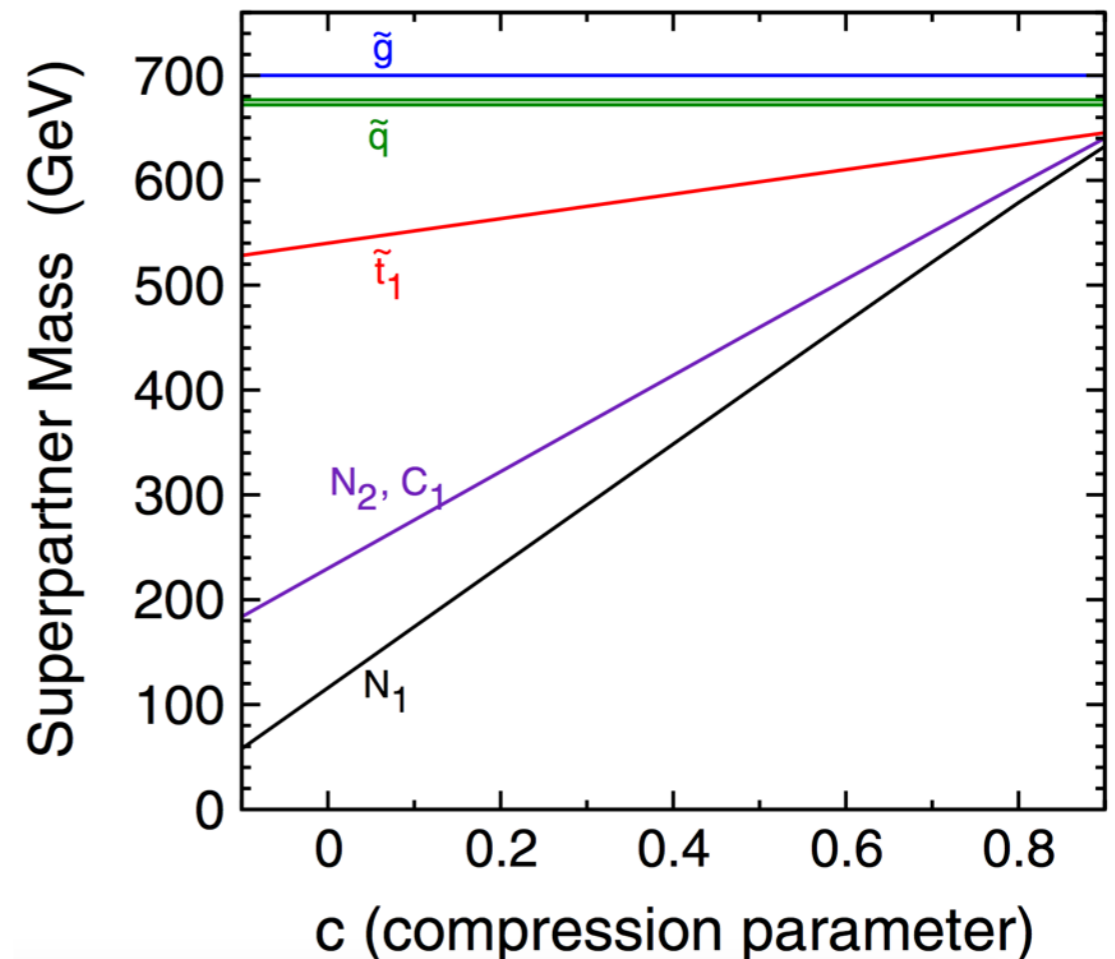
Easy to rule it out !

$c=1$ Compressed SUSY spectrum

Heavy Neutralinos, Charginos
Low Visible/Missing Energy

Hard to rule it out

Can we constrain it using (g-2) and/or flavour observables?



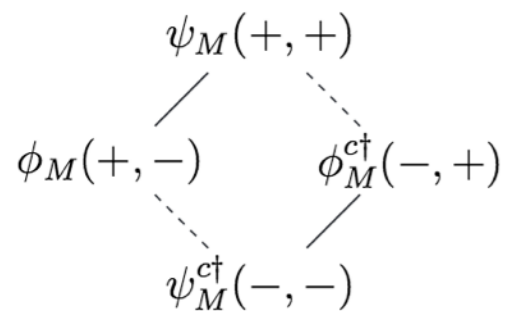
Degenerate Supersymmetry: HOW?

Degenerate SUSY spectrum can arise in some models

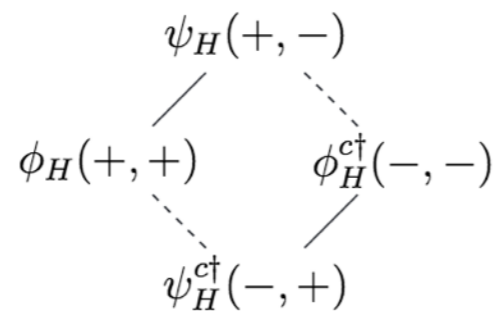
e.g. Scherk-Schwarz compactification in 5D

[Pomarol, Quiros (1998); Barbieri, Hall, Nomura (2001,02); Murayama et al (2012)]

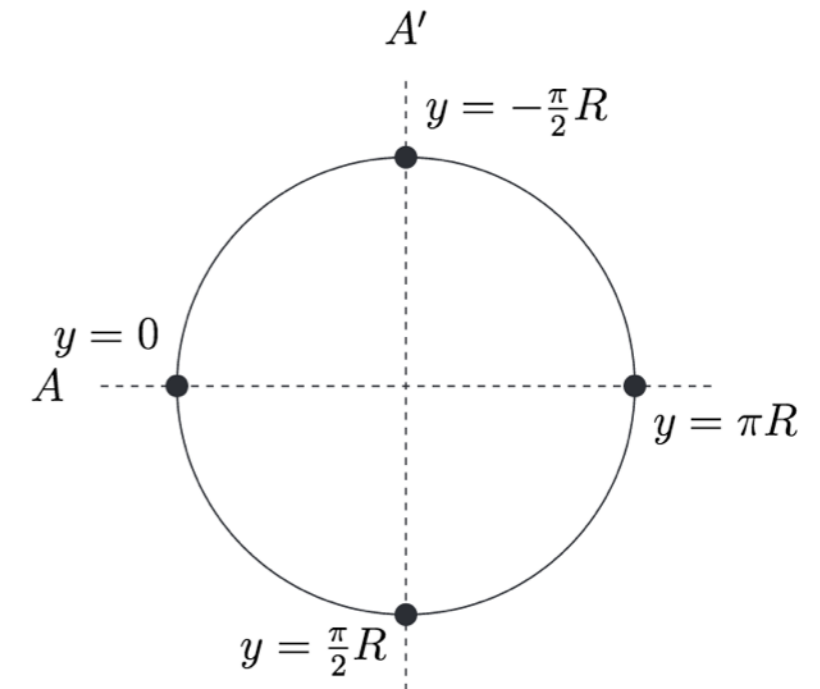
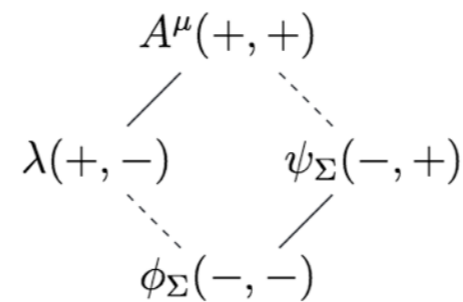
Matter



Higgs



Gauge



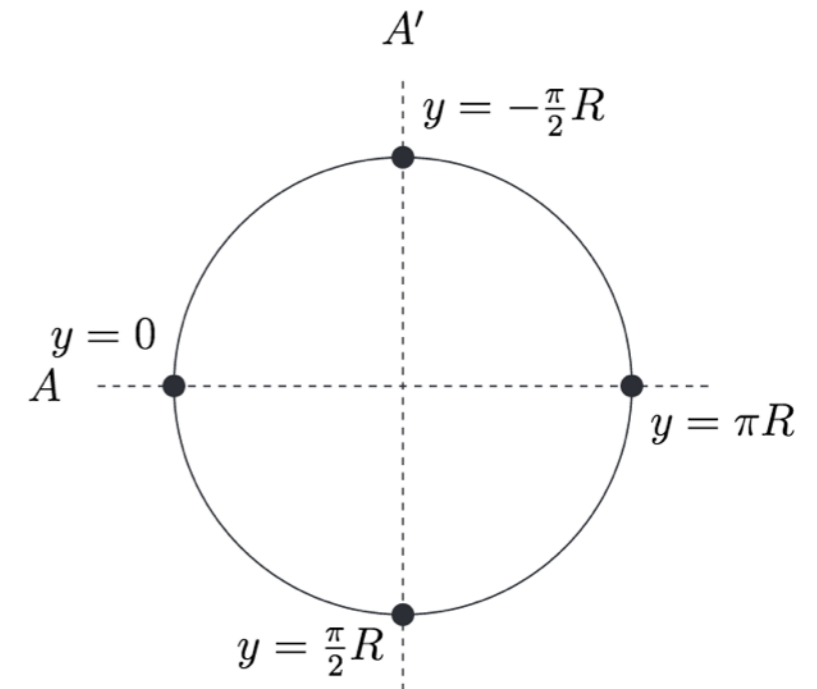
$S^1/(Z_2 \times Z'_2)$ orbifold in the fifth dimension.

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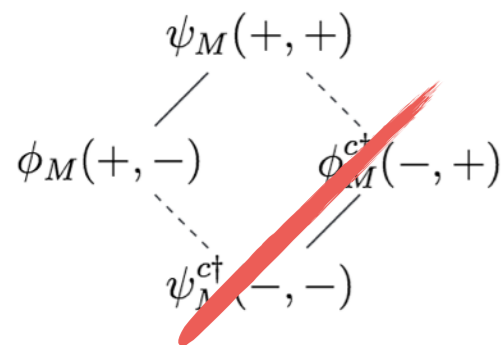
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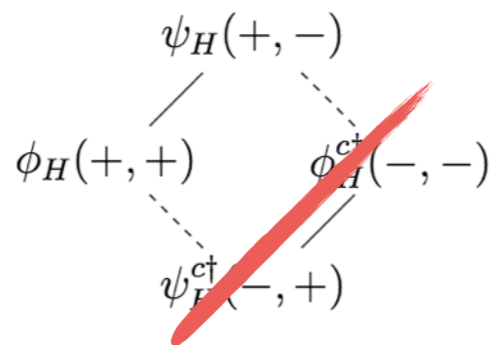


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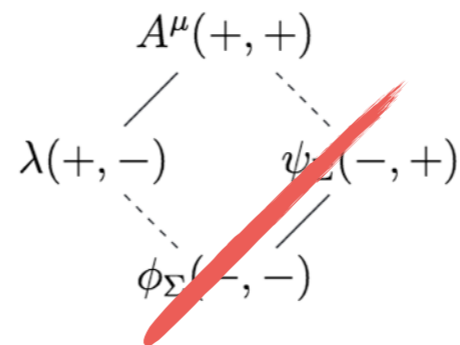
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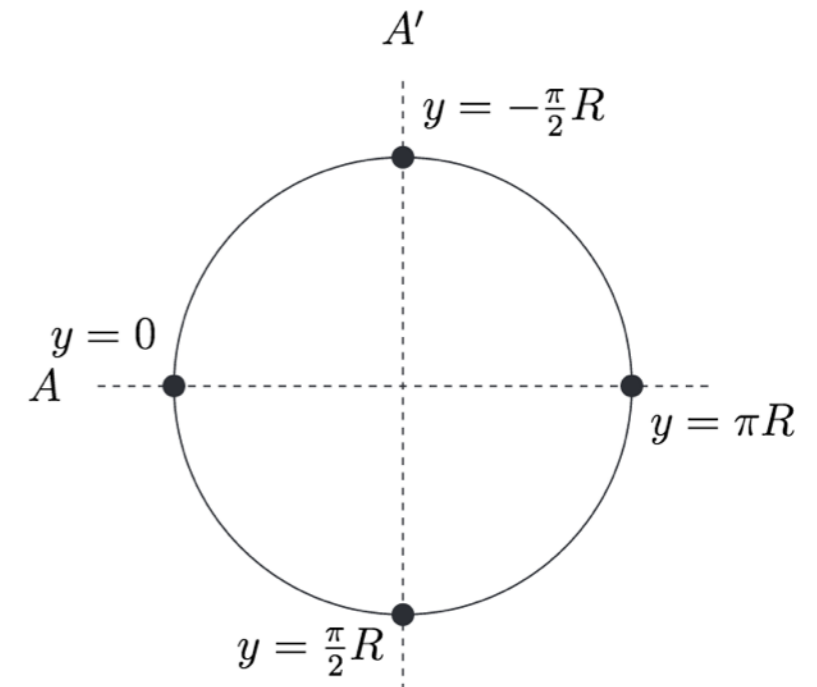
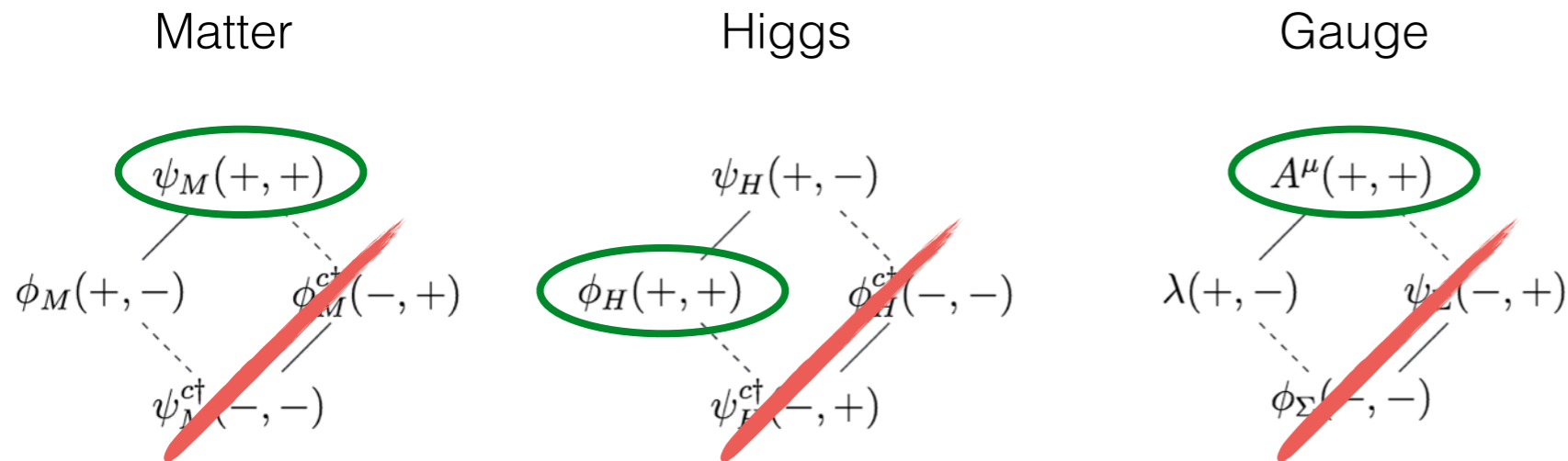
N=2 SUSY fields

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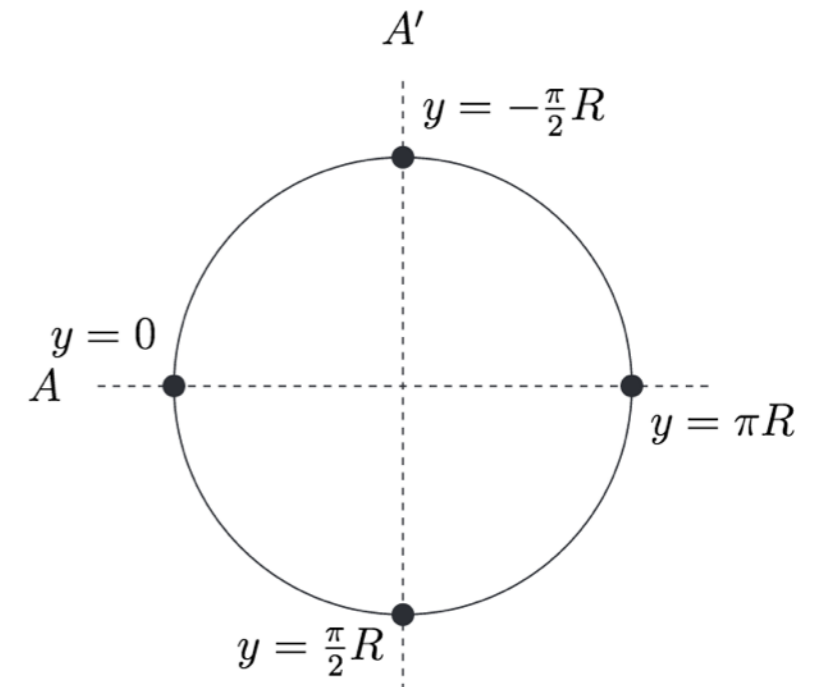
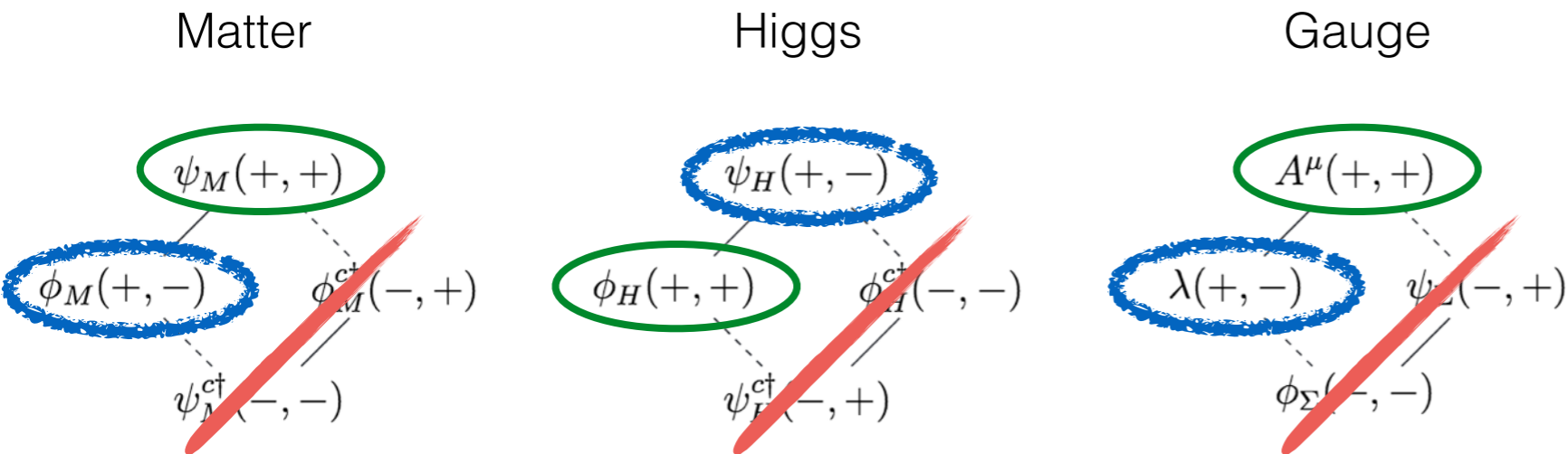
SM fields

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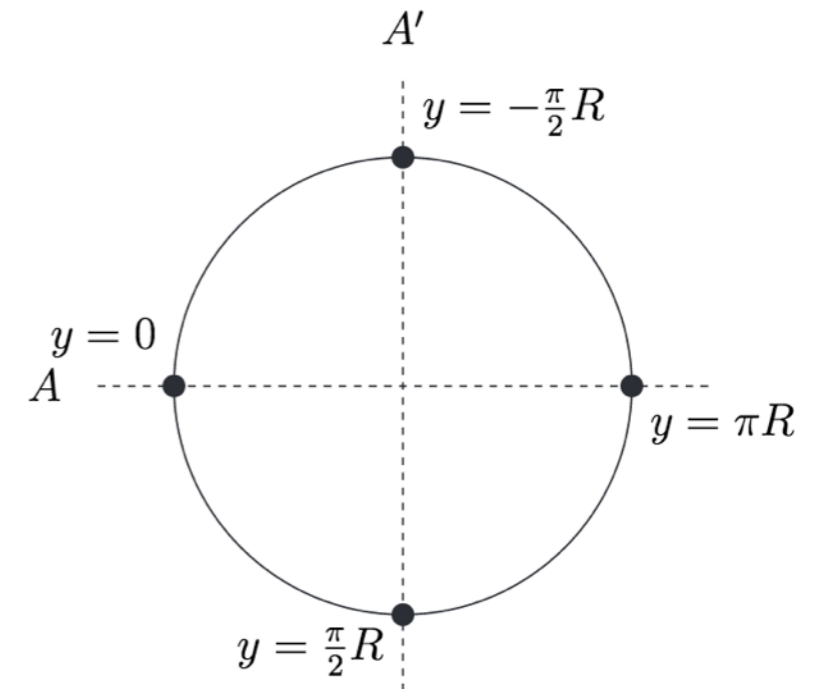
N=1 fields; MSSM super partners

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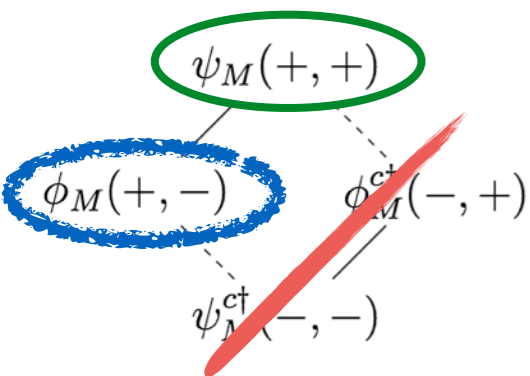
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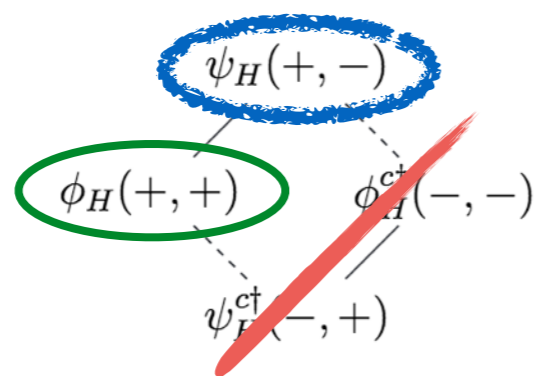


$S^1/(Z_2 \times Z'_2)$ orbifold in the fifth dimension.

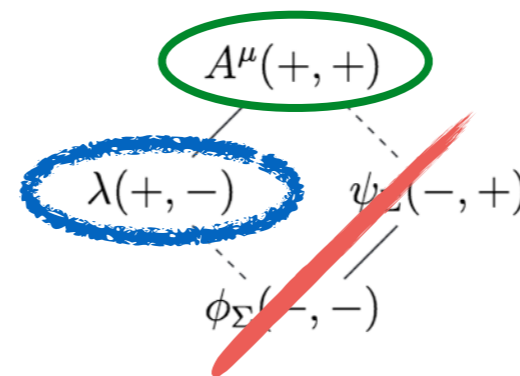
Matter



Higgs



Gauge



N=2 SUSY fields

SM fields

N=1 fields; MSSM super partners

$$A = -3\frac{\alpha}{R}, \quad \mu = \frac{\gamma}{R}, \quad \mu B = -2\frac{\alpha\gamma}{R^2}$$

$$M_1 = M_2 = M_3 = \frac{\alpha}{R}, \quad m_{H_u}^2 = m_{H_d}^2 = m_{\tilde{Q}}^2 = m_{\tilde{U}}^2 = m_{\tilde{D}}^2 = m_{\tilde{L}}^2 = m_{\tilde{E}}^2 = \left(\frac{\alpha}{R}\right)^2$$

Degenerate Supersymmetry: Indirect constraints

Weak scale Degenerate MSSM (DMSSM)

(Partially) Phenomenological approach :

$$M_1 \approx M_2 \approx M_3 \equiv M_D, \quad m_{\tilde{Q}}^2 \approx m_{\tilde{U}}^2 \approx m_{\tilde{D}}^2 \approx m_{\tilde{L}}^2 \approx m_{\tilde{E}}^2 \equiv M_D^2$$

$$|\mu|^2 = k_\mu M_D^2, \quad \text{and} \quad m_A^2 = k_A M_D^2;$$

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Neutralinos : $\chi_{1,2}^0 \approx M_D$ $\chi_{3,4}^0 \approx |\mu|$

Degenerate Supersymmetry: Indirect constraints

Weak scale Degenerate MSSM (DMSSM)

(Partially) Phenomenological approach :

$$M_1 \approx M_2 \approx M_3 \equiv M_D, \quad m_{\tilde{Q}}^2 \approx m_{\tilde{U}}^2 \approx m_{\tilde{D}}^2 \approx m_{\tilde{L}}^2 \approx m_{\tilde{E}}^2 \equiv M_D^2$$

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Sfermions : $m_{\tilde{f}}^2 = \begin{pmatrix} M_D^2 + m_f^2 + \Delta_{\tilde{f}_L} & m_f X_f \\ m_f X_f & M_D^2 + m_f^2 + \Delta_{\tilde{f}_R} \end{pmatrix}$

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$m_{\tilde{f}_2}^2 - m_{\tilde{f}_1}^2 \approx |2m_f X_f|$
maximally mixed stops !

Degenerate Supersymmetry: Indirect constraints

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$$M_{\text{SUSY}} \equiv \sqrt{m_{\tilde{t}_1} m_{\tilde{t}_2}} = M_D \left(1 - \frac{m_t^2 X_t^2}{M_D^4} + 2 \frac{m_t^2}{M_D^2} + \frac{m_t^4}{M_D^4} \right)^{1/4}$$

Degenerate Supersymmetry: Indirect constraints

DMSSM as a solution of muon $(g-2)$??

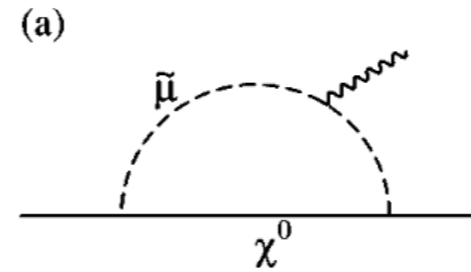
[Moroi (1995)]

[...talk by D. Stockinger]

Degenerate Supersymmetry: Indirect constraints

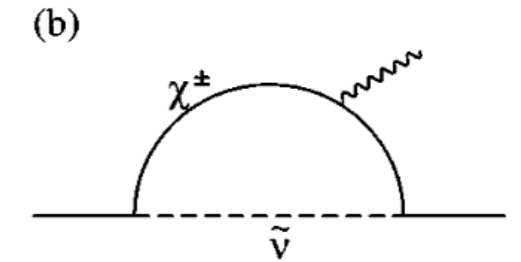
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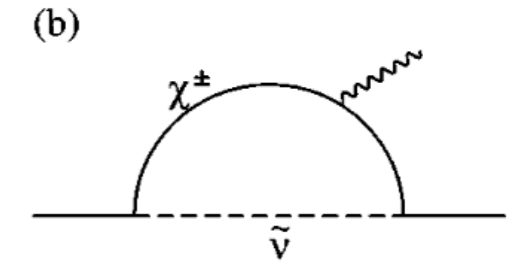
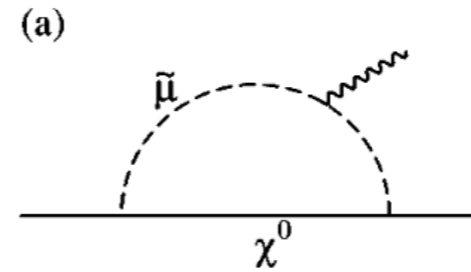
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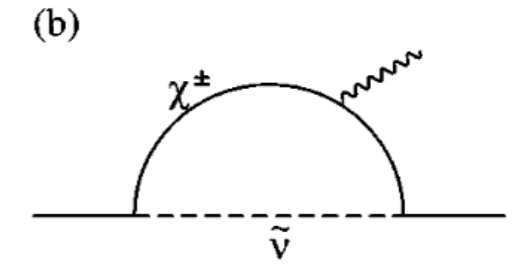
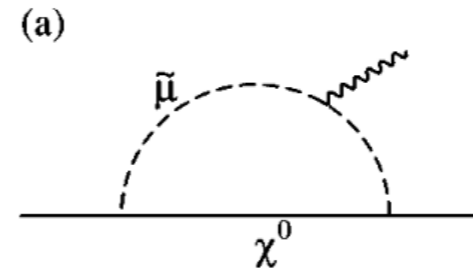
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In the degenerate limit,

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where $x_r \equiv \mu/M_D$

Degenerate Supersymmetry: Indirect constraints

DMSSM as a solution of muon (g-2) ??

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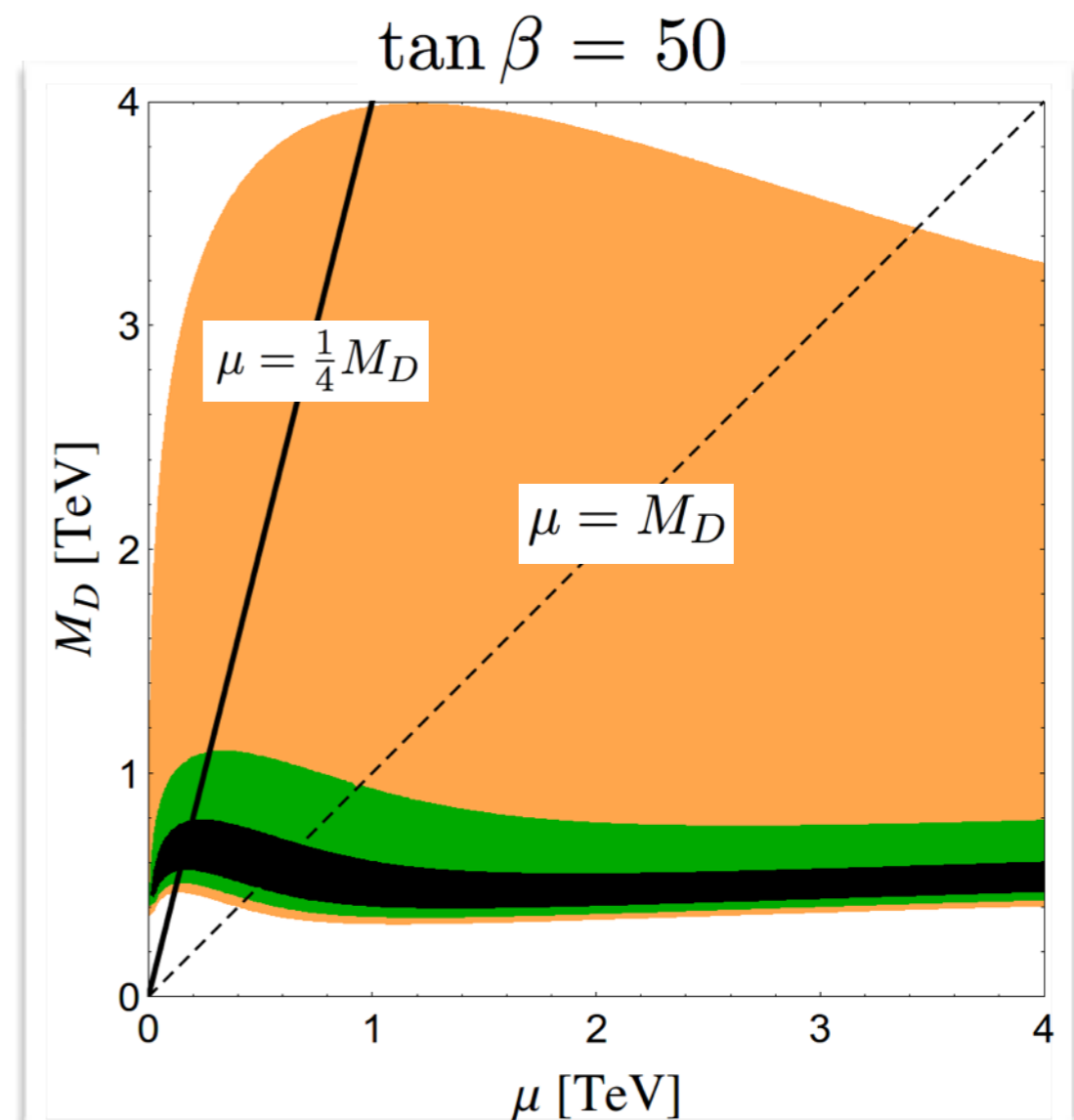
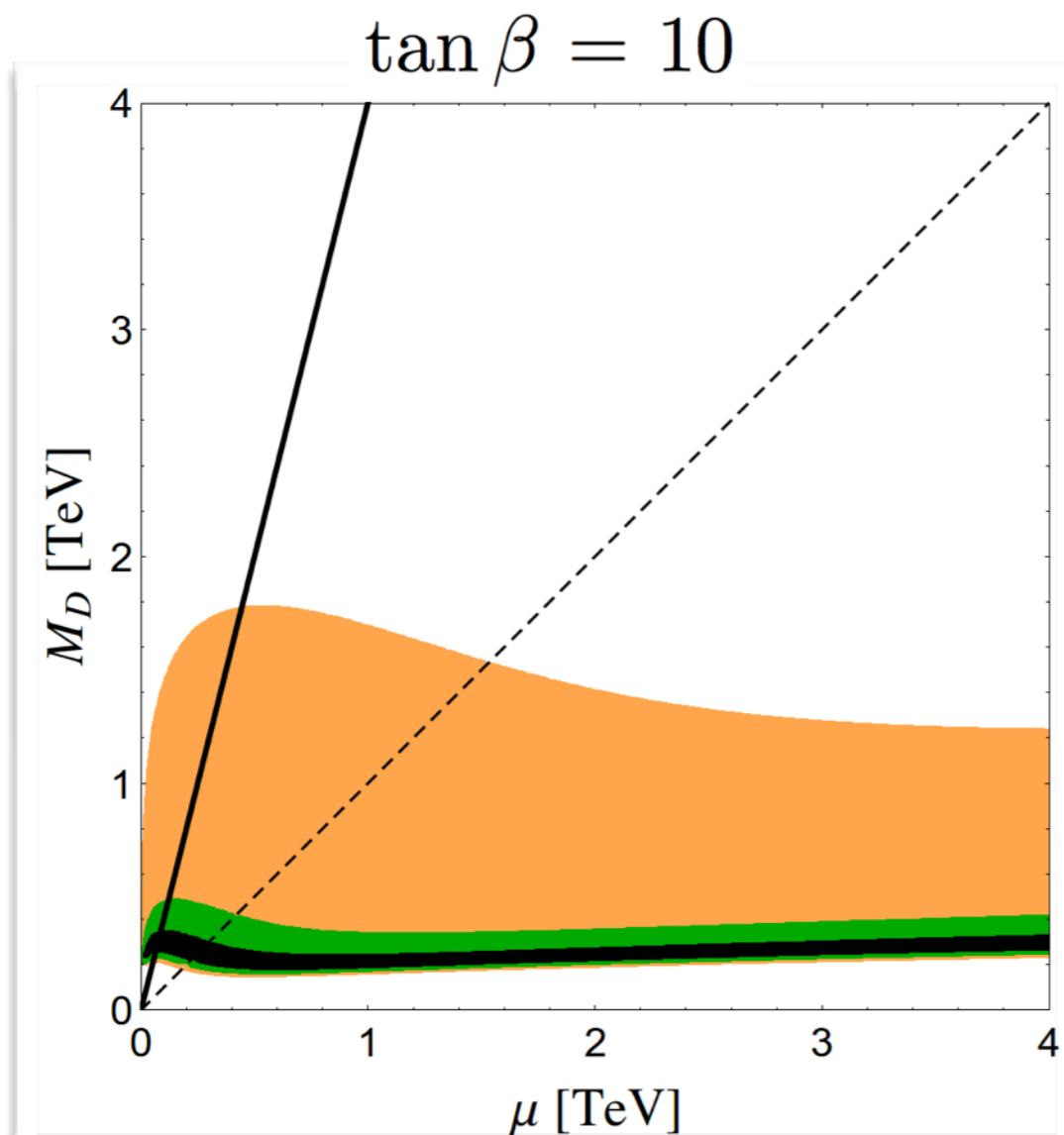
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Degenerate Supersymmetry: Indirect constraints

DMSSM as a solution of muon $(g-2)$ and ...?

Degenerate Supersymmetry: Indirect constraints

DMSSM as a solution of muon (g-2) and ...?

Higgs mass:

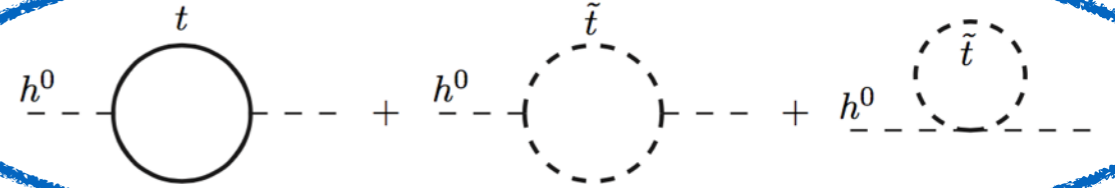
$$m_h^2 = m_Z^2 \cos^2 2\beta + \delta m_h^2$$

Degenerate Supersymmetry: Indirect constraints

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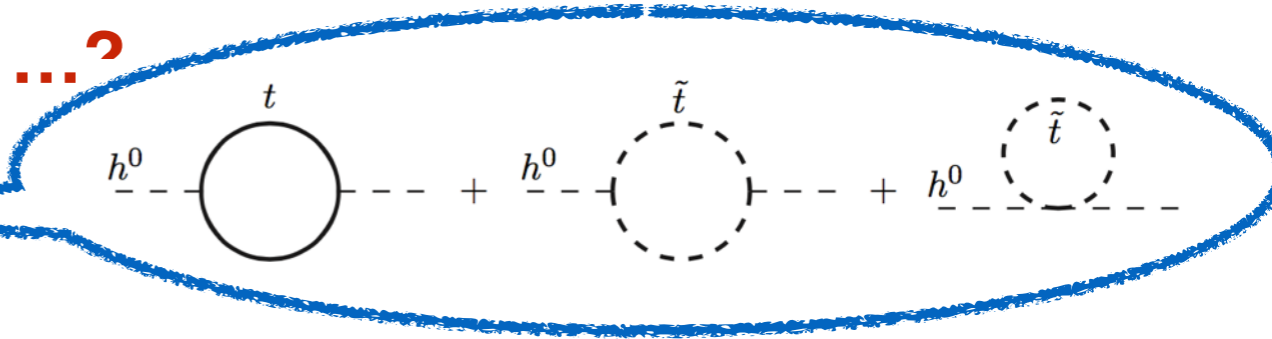
$$\delta m_h^2 = \frac{3}{4\pi^2} \frac{m_t^4}{v^2} \left(\log \left(\frac{M_{\text{SUSY}}^2}{m_t^2} \right) + \frac{X_t^2}{M_{\text{SUSY}}^2} - \frac{X_t^4}{12M_{\text{SUSY}}^4} \right) + \dots$$

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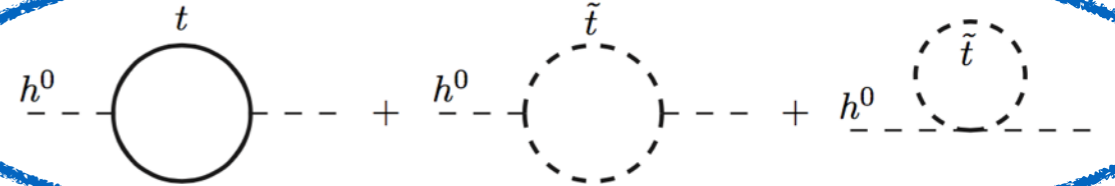
$X_t = A_t - \mu \cot \beta$
 prefers **large** trilinear term!

Degenerate Supersymmetry: Indirect constraints

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B decays:

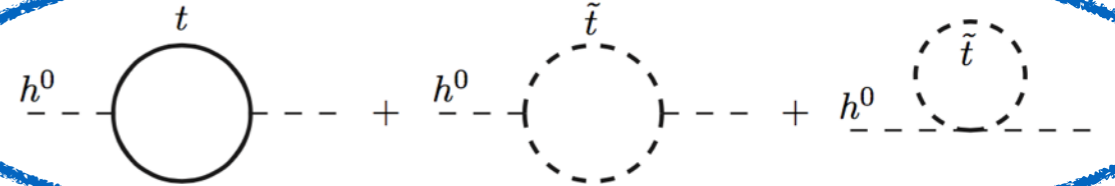
$$R_{bsg} \equiv \frac{\text{BR}(B \rightarrow X_s \gamma)}{\text{BR}(B \rightarrow X_s \gamma)_{\text{SM}}} = 1 - 2.45 C_7^{NP} - 0.59 C_8^{NP}$$

Degenerate Supersymmetry: Indirect constraints

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$$C_7^{\tilde{H}} = -\frac{t_\beta}{1 + \epsilon_b t_\beta} \frac{5}{72} \frac{A_t m_t^2}{M_D^3}$$

$$C_7^{\tilde{g}} = \frac{g_3^2}{g_2^2} \frac{\epsilon_b^{\tilde{H}} t_\beta^2}{(1 + \epsilon_b t_\beta)(1 + \epsilon_0 t_\beta)} \frac{2}{27} \frac{m_W^2}{M_D^2}$$

$$C_7^{\tilde{W}} = \frac{\epsilon_b^{\tilde{H}} t_\beta^2}{(1 + \epsilon_b t_\beta)(1 + \epsilon_0 t_\beta)} \frac{7}{24} \frac{m_W^2}{M_D^2}$$

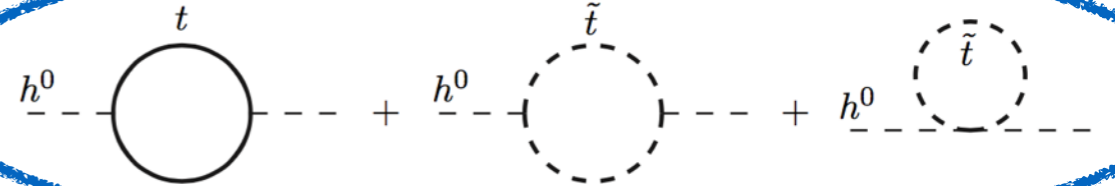
prefers **small** trilinear term!

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$$R_{B_s \mu\mu} \equiv \frac{\text{BR}(B_s \rightarrow \mu^+ \mu^-)}{\text{BR}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}}} \simeq |\mathcal{A}|^2 + |1 - \mathcal{A}|^2$$

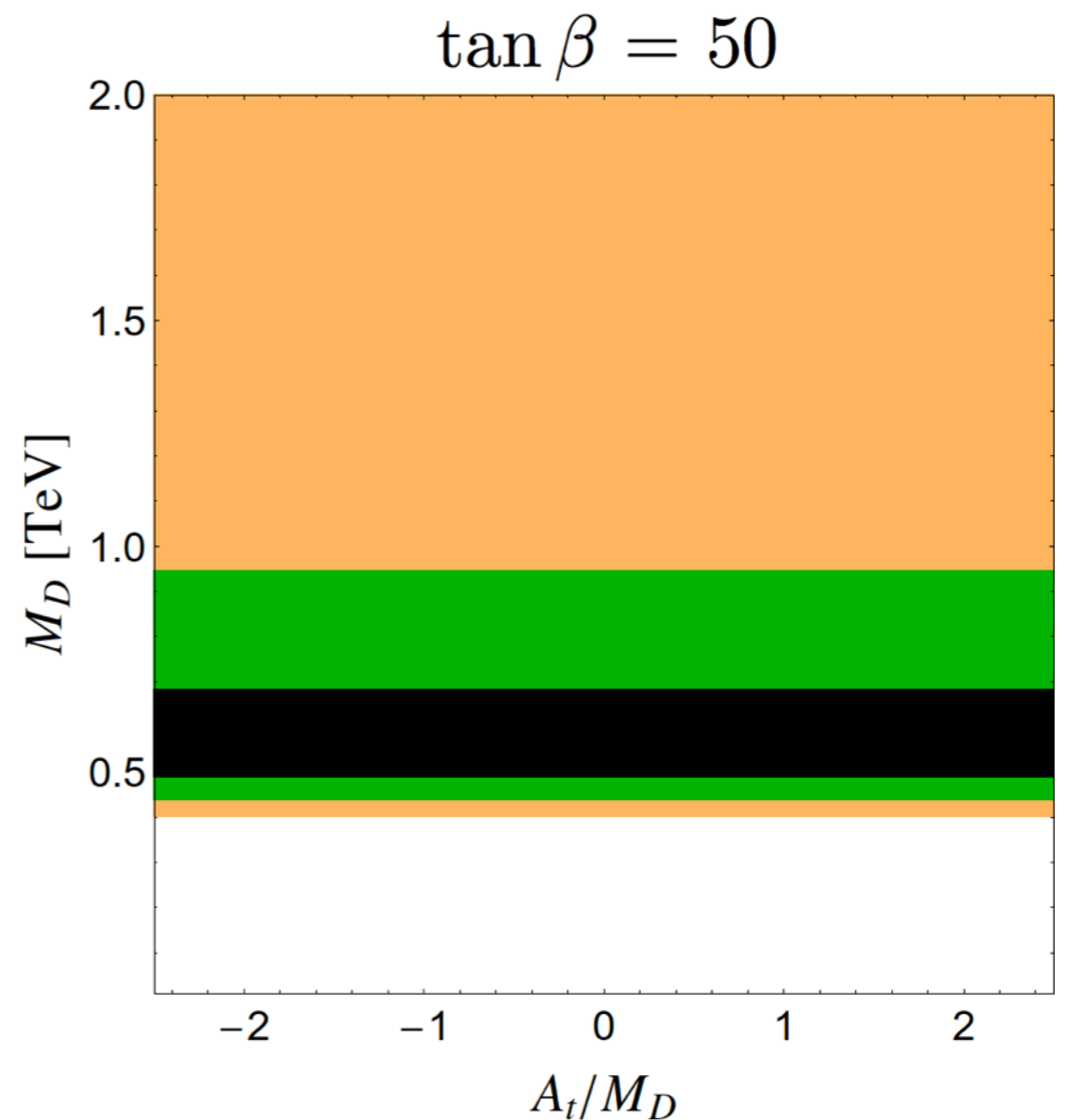
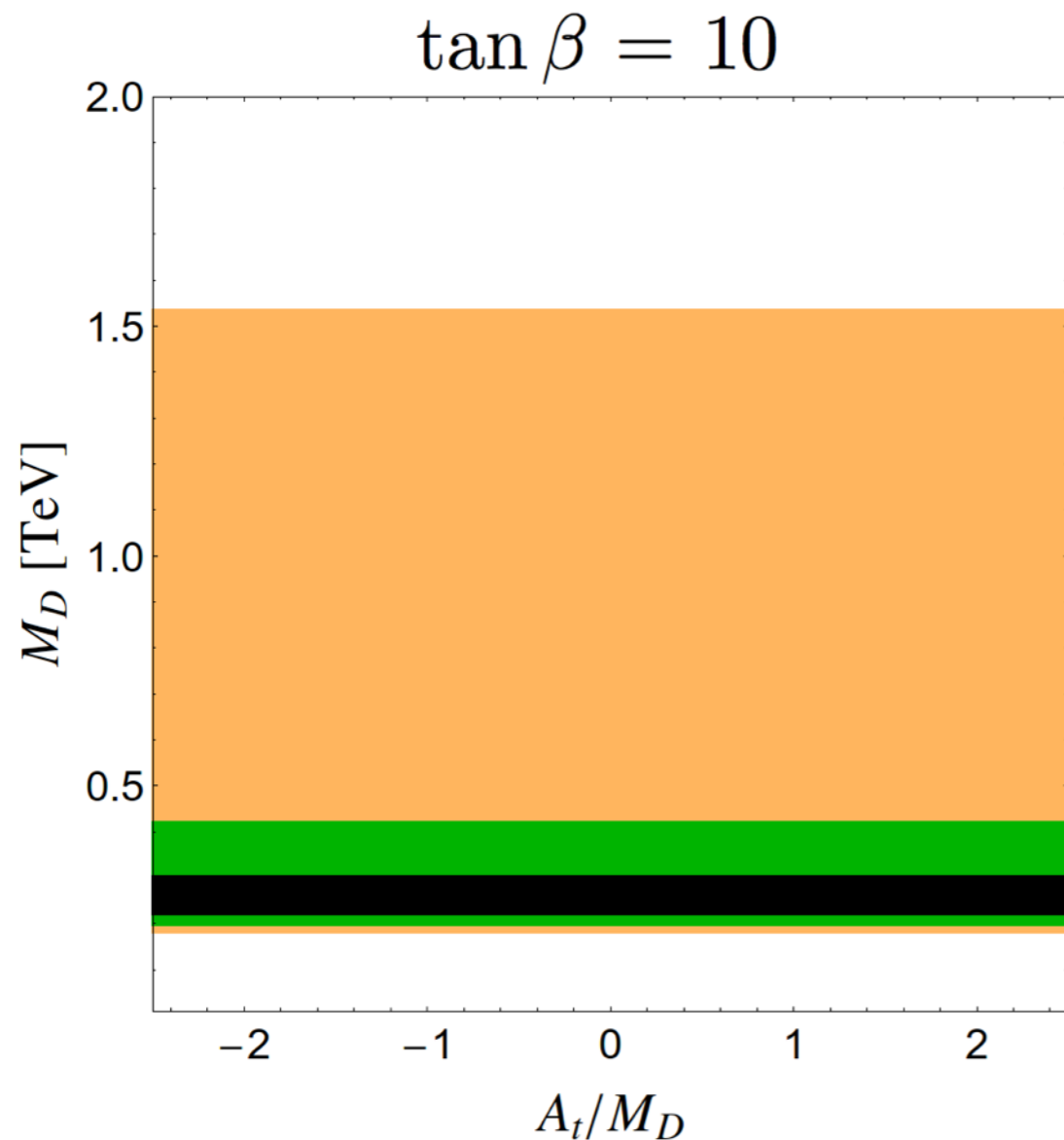
$$\mathcal{A} = \frac{4\pi}{\alpha_2} \frac{m_{B_s}^2}{4M_A^2} \frac{\epsilon_{FC} \tan^3 \beta}{(1 + \epsilon_b \tan \beta)(1 + \epsilon_0 \tan \beta)(1 + \epsilon_l \tan \beta)} \frac{1}{2C_A}$$

prefers **large** pseudoscalar mass!

Degenerate Supersymmetry: Indirect constraints

DMSSM as a solution of muon (g-2) and ...?

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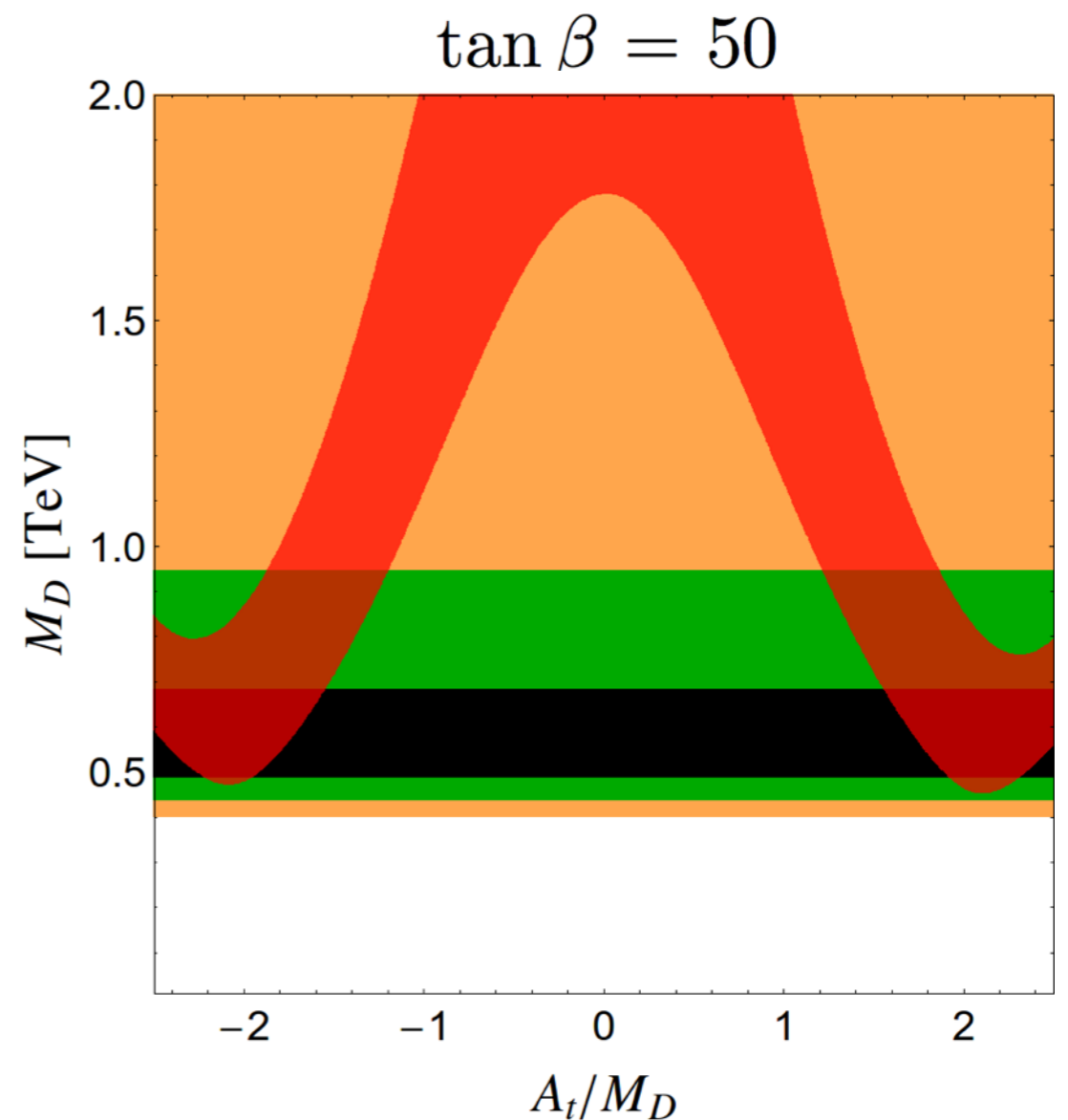
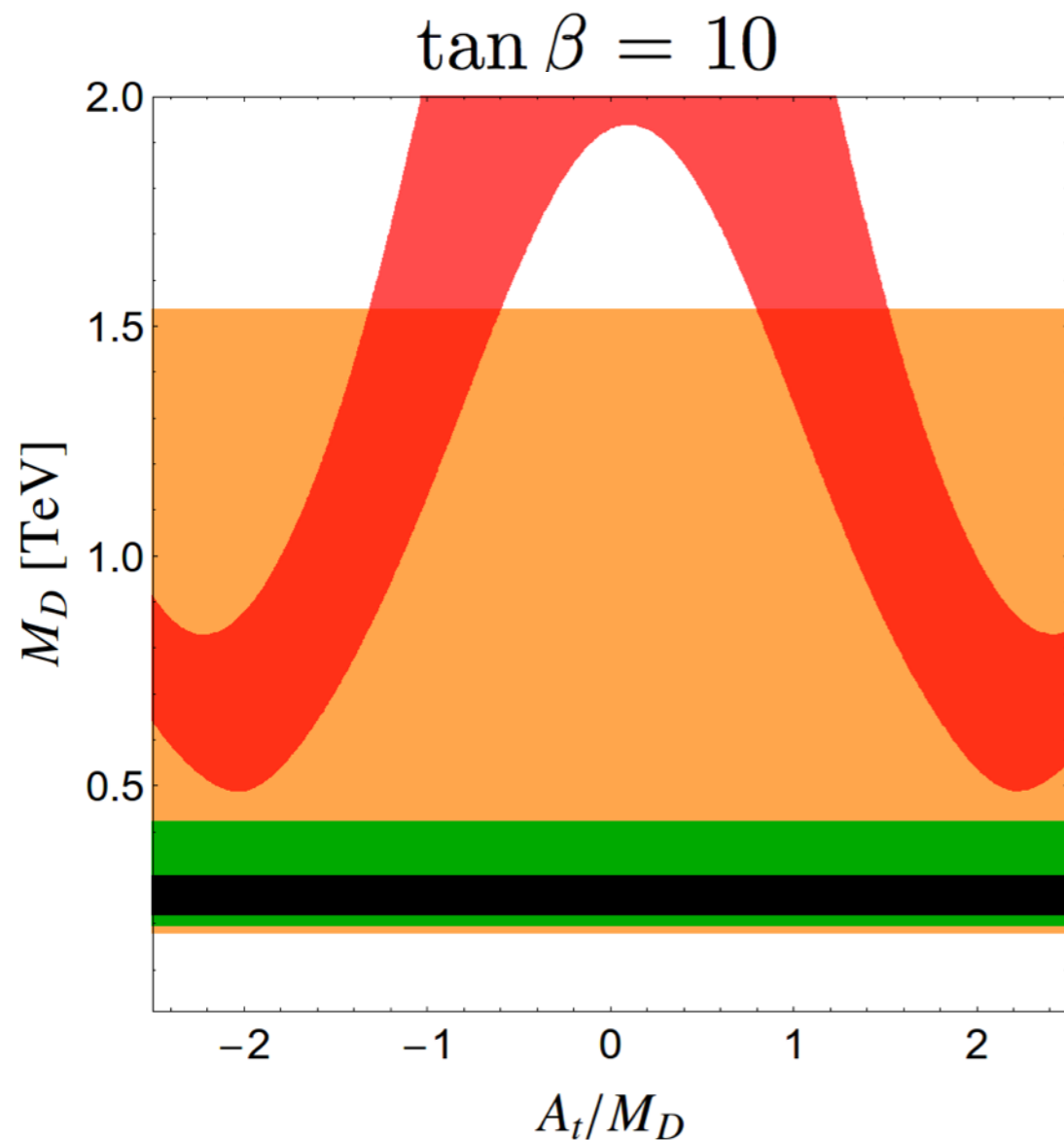


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$$m_{h^0} \in [122.4, 127.8] \text{ GeV}$$



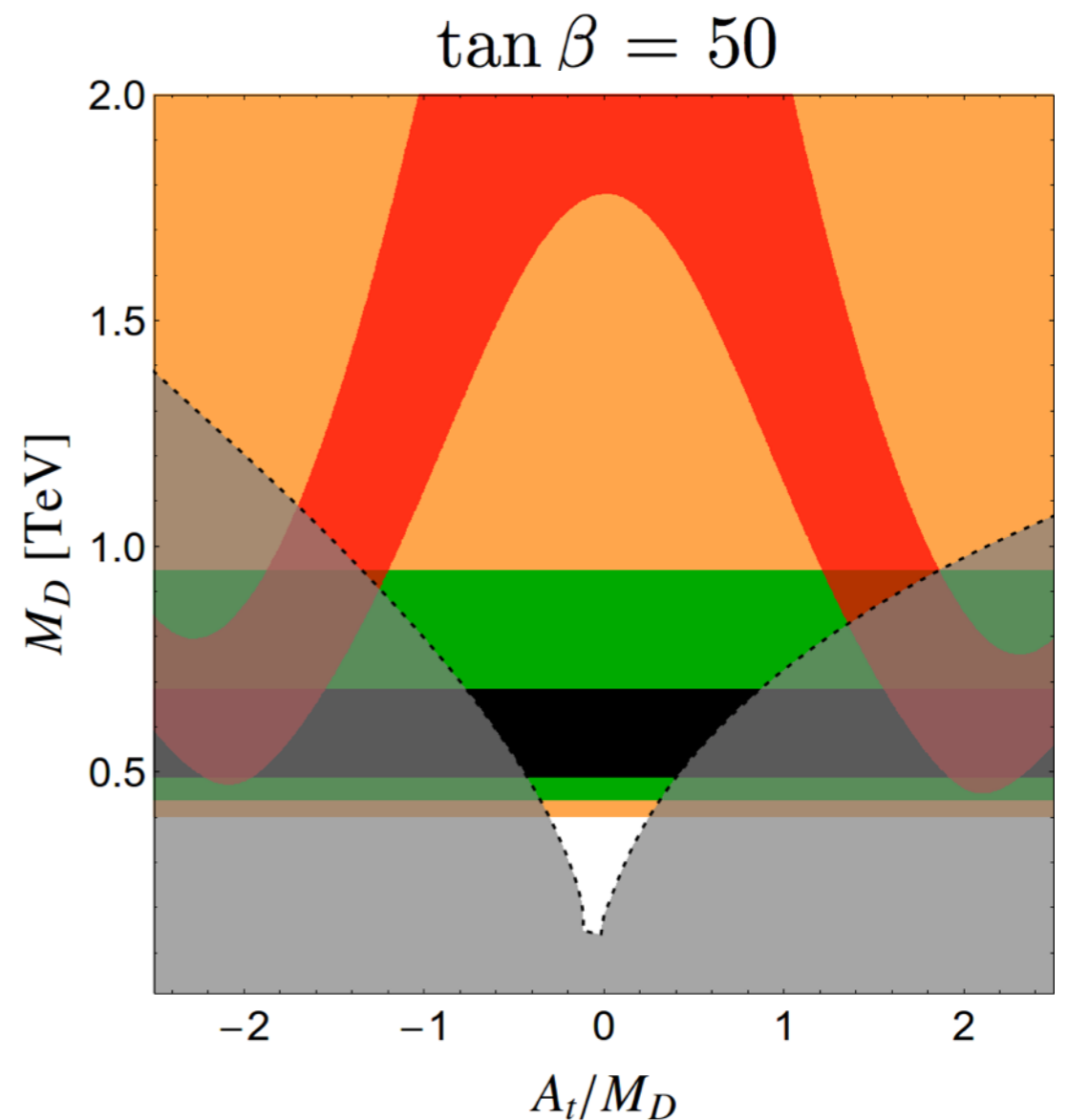
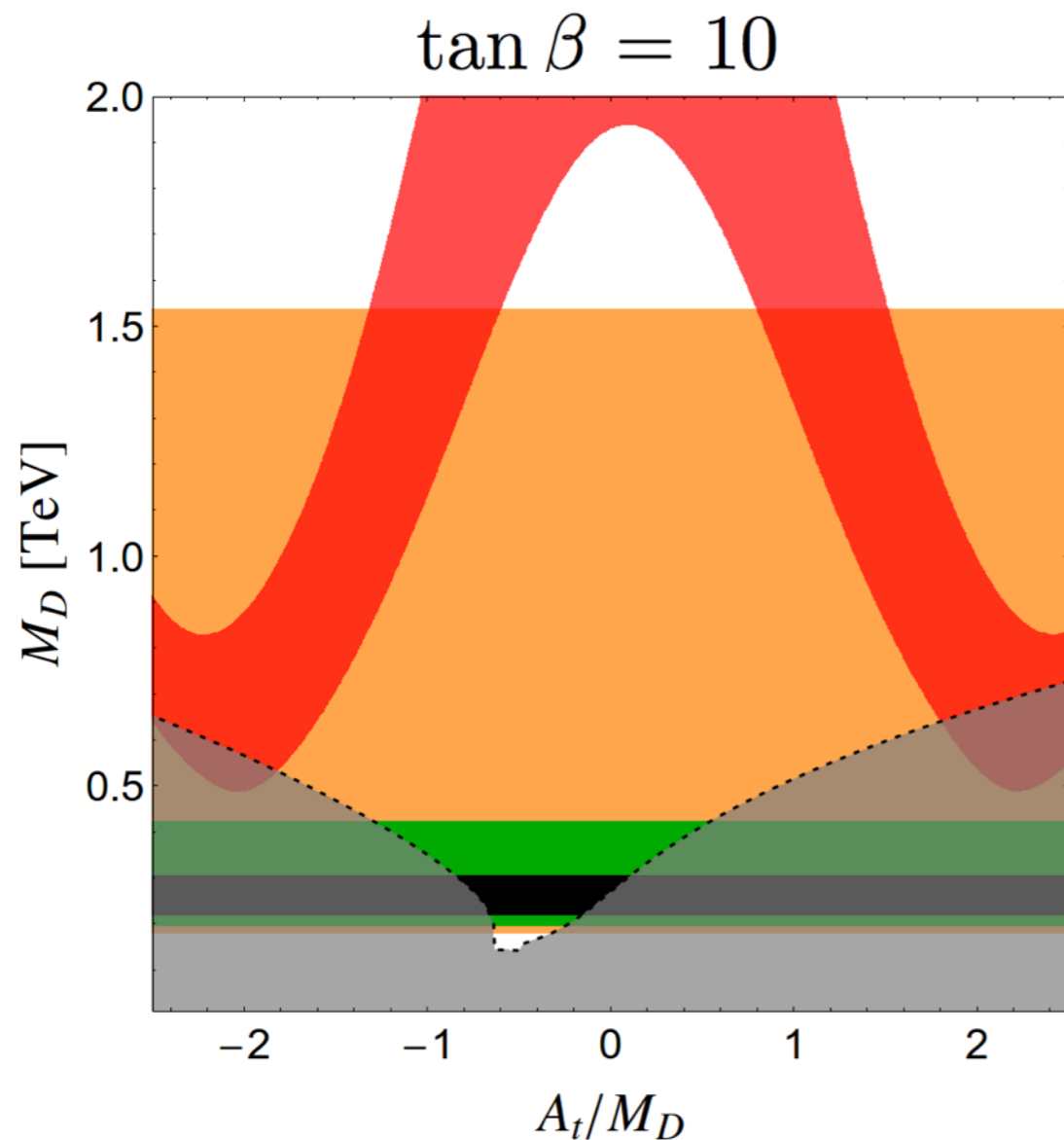
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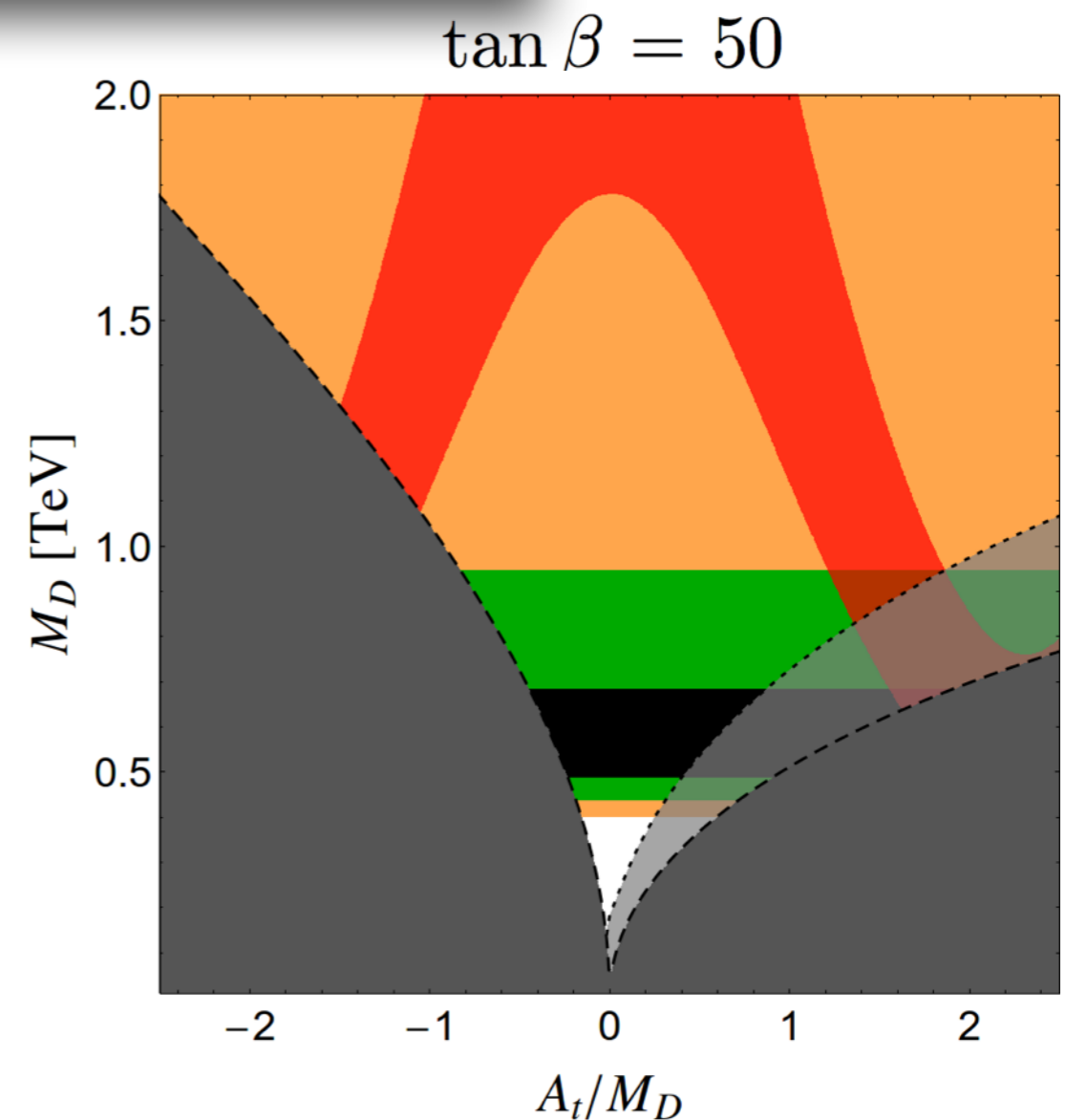
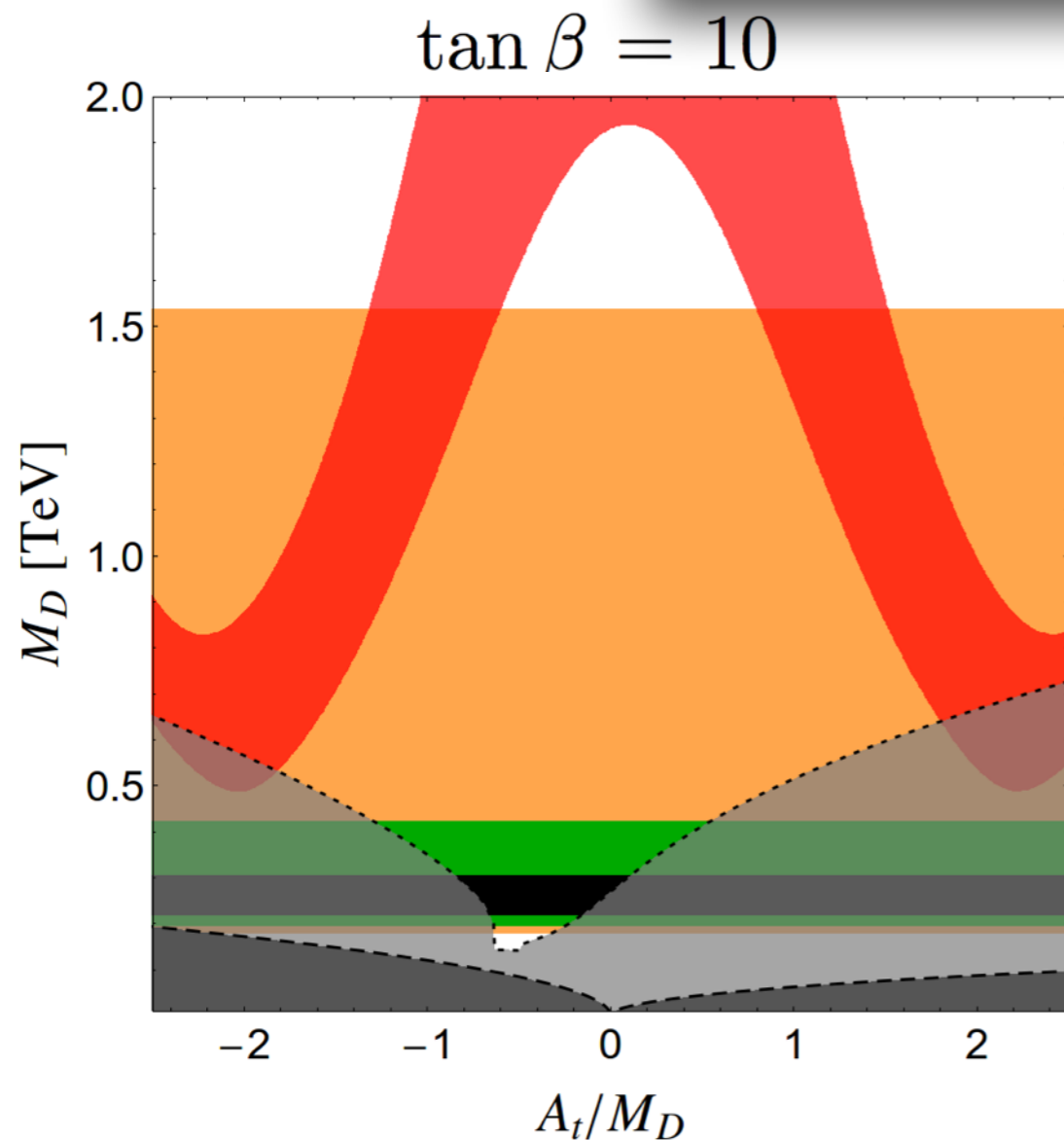
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Degenerate Supersymmetry: Indirect constraints

DMSSM as a solution of muon (g-2): Full numerical analysis

Numerical analysis considering 10% deviations from the exact degeneracy

$$\begin{aligned}m_{\tilde{f}_i} &\in M_D (1 + \delta_{m_{\tilde{f}}}), \\M_1 = M_2 = M_3 &\in M_D (1 + \delta_M), \\ \mu &\in M_D (1 + \delta_\mu).\end{aligned}$$

Degenerate Supersymmetry: Indirect constraints

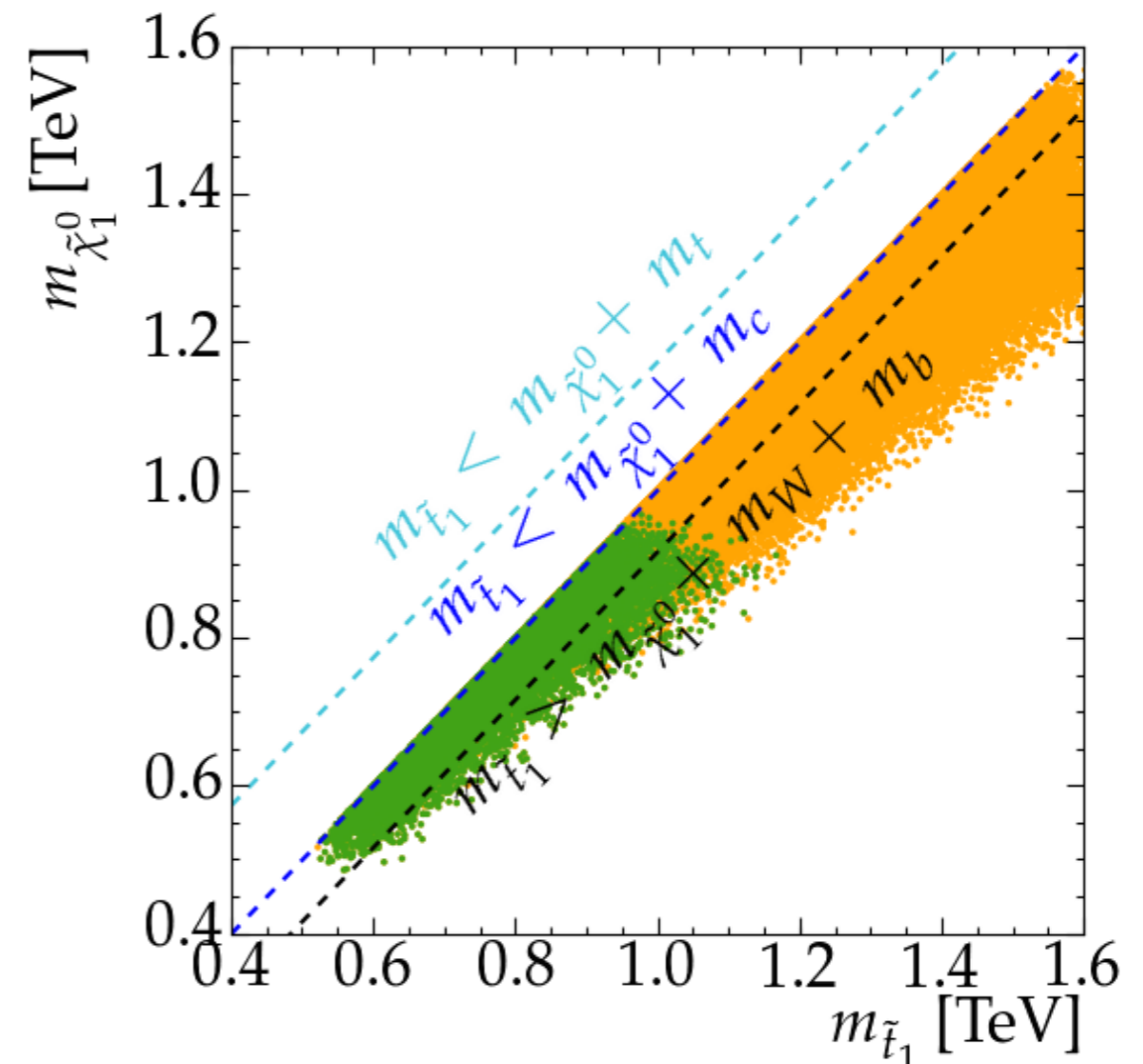
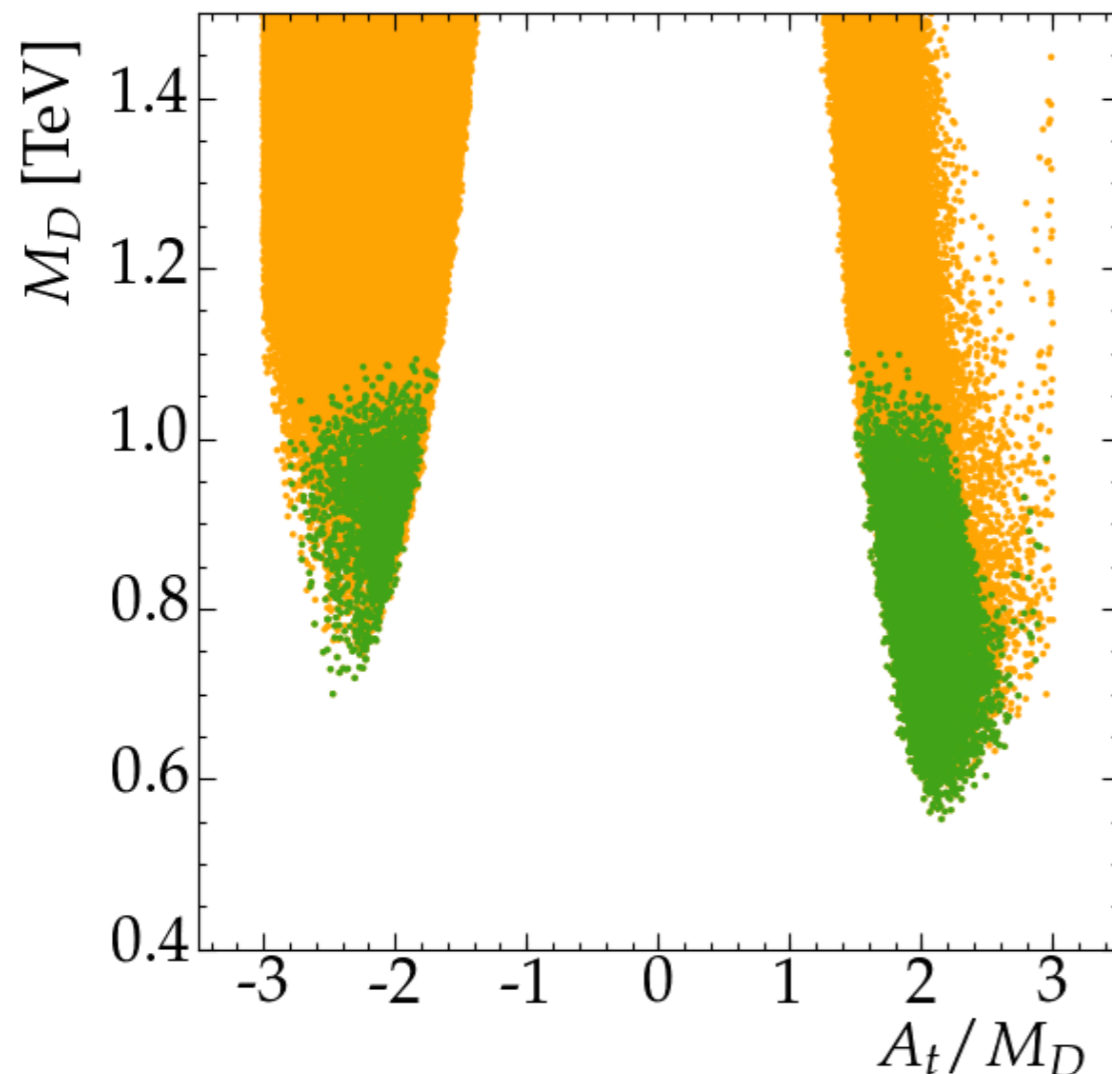
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Degenerate Supersymmetry: Dark Matter

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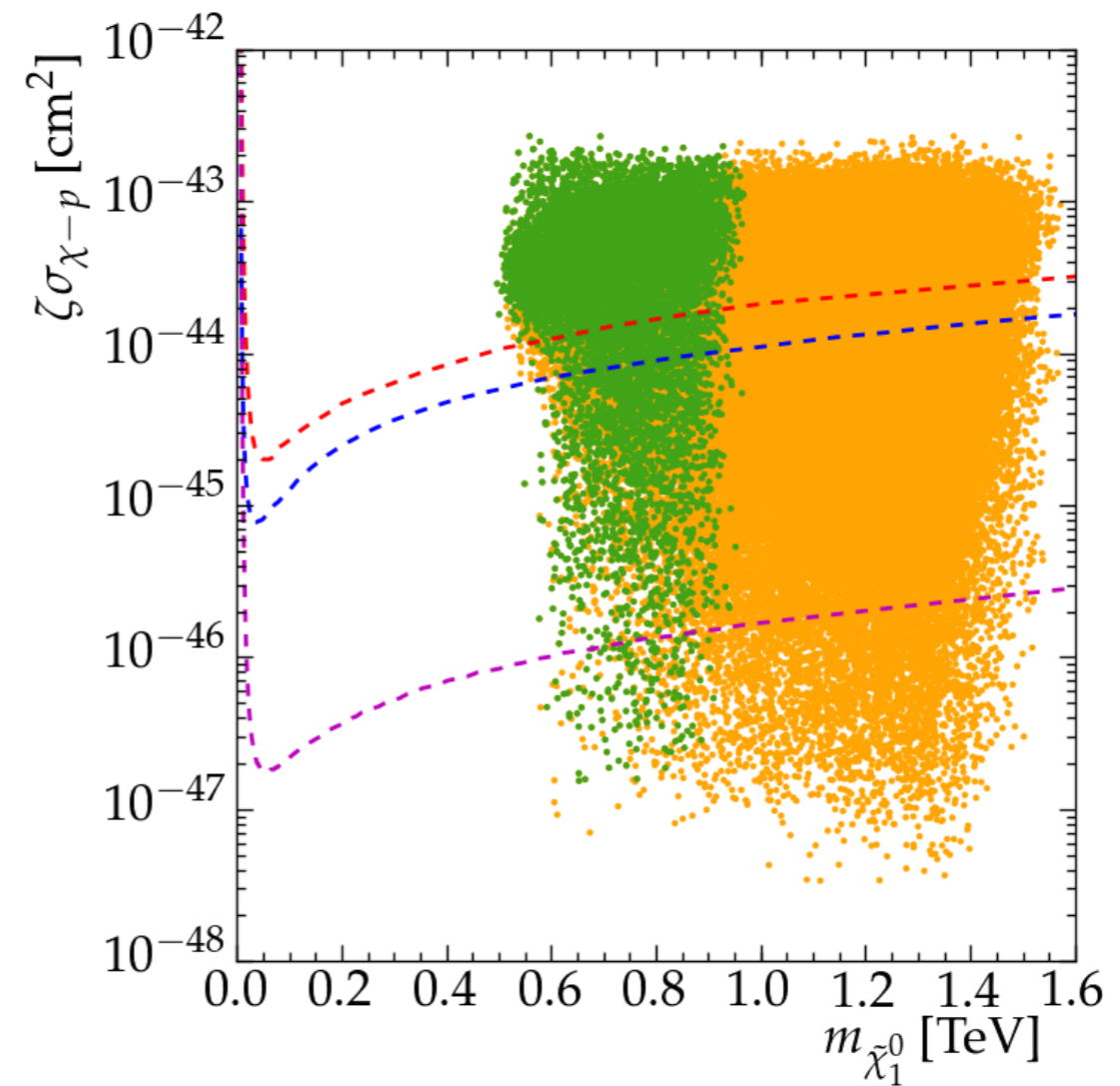
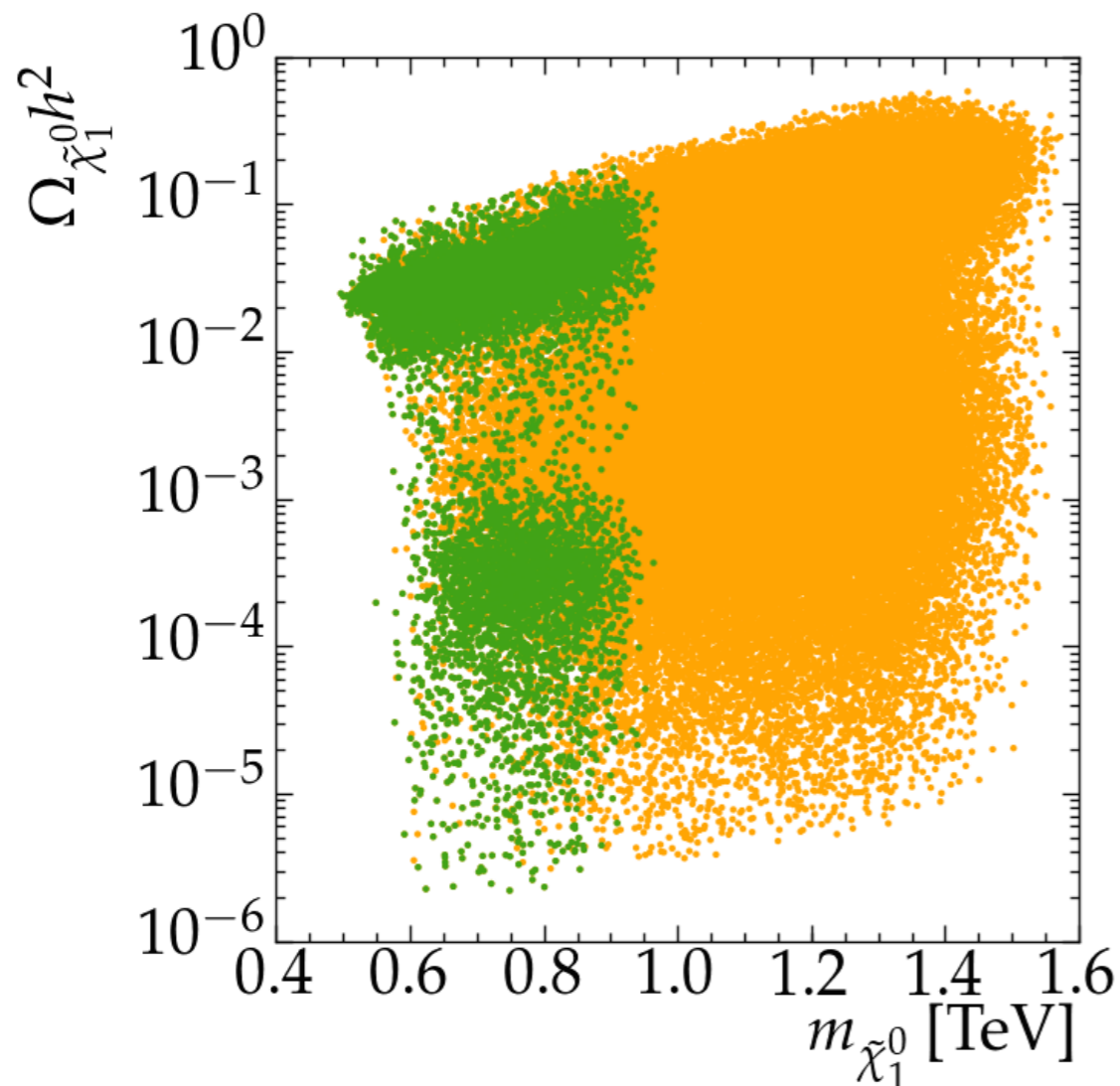
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Numerical analysis considering 10% deviations from the exact degeneracy

$$m_{\tilde{f}_i} \in M_D (1 + \delta_{m_{\tilde{f}}}),$$

$$M_1 = M_2 = M_3 \in M_D (1 + \delta_M),$$

$$\mu \in M_D (1 + \delta_\mu).$$



Conclusions

Degenerate MSSM can account for the measured value of muon $(g-2)$ at or less than 2σ , if the degenerate scale is M_D is in the range of 300–500 GeV (500 – 1100 GeV) for small (large) $\tan \beta$.

The observed Higgs mass requires large negative A_t for such a light M_D leading to sizeable flavour violations in B decays, particularly in $B_S \rightarrow X_S \gamma$ channel.

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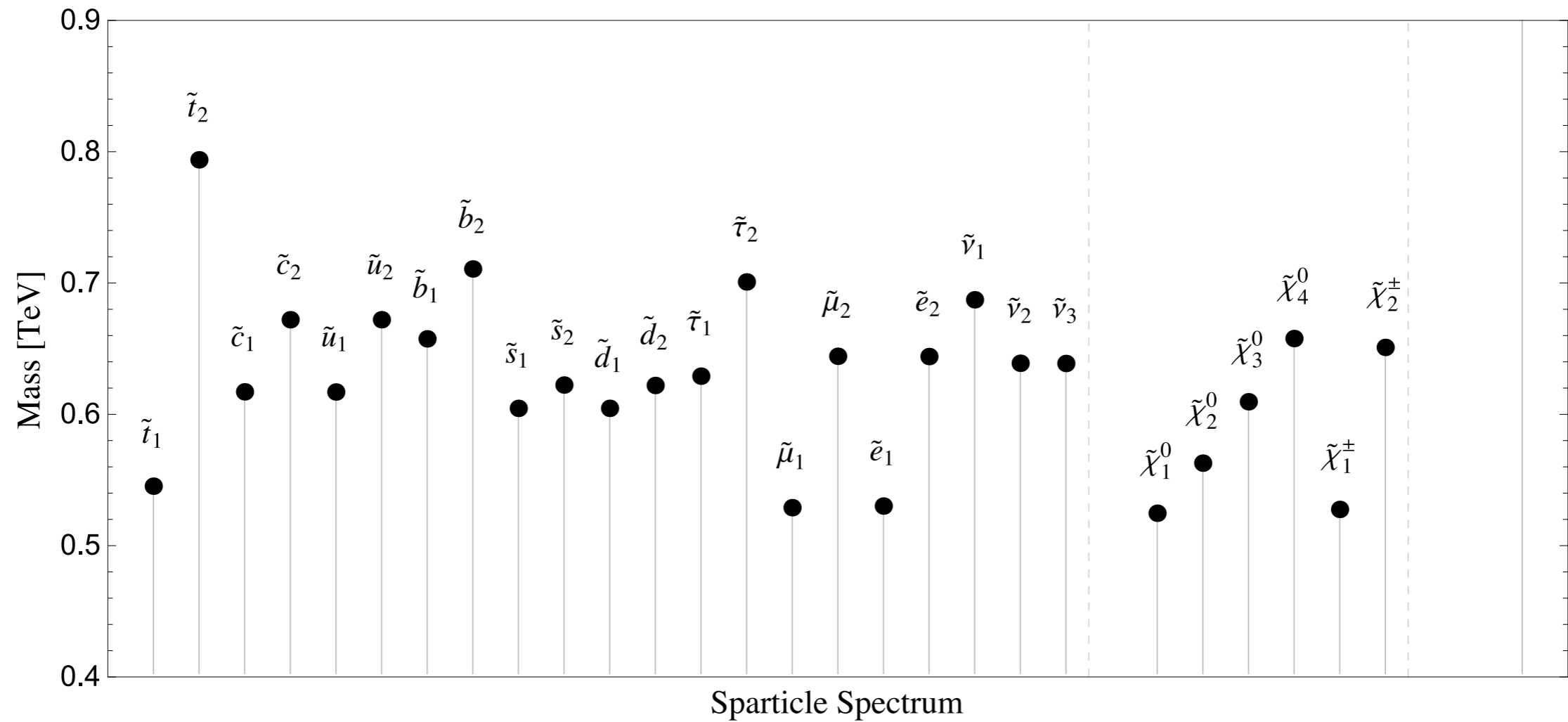
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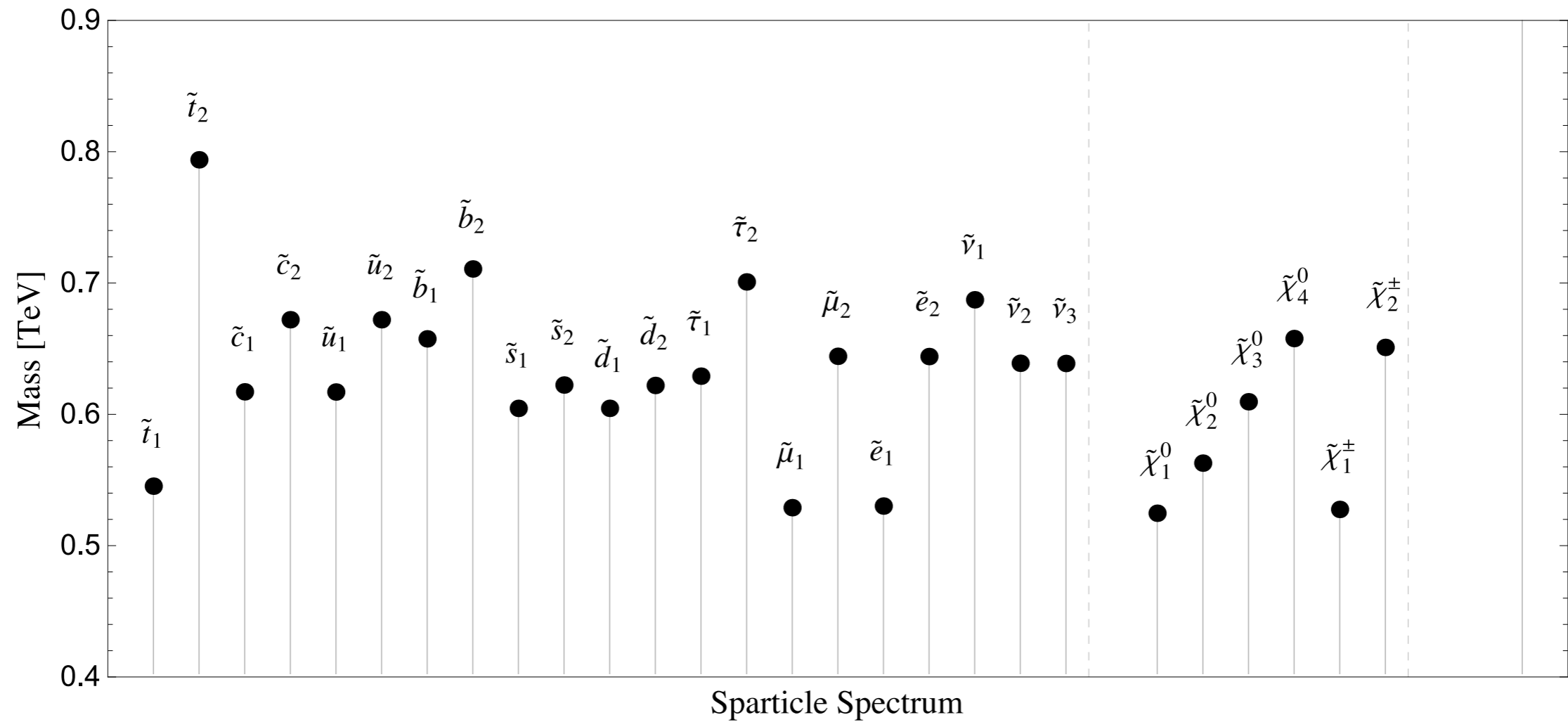
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The neutralino cannot make all of the dark matter and multi-component scenario is essentially required.

Conclusions



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Thanks