The 3-Dimensional nucleon structure (mainly in momentum space)



Mauro Anselmino Torino University & INFN September 22, 2015

Transverse Momentum Dependent partonic distributions TMDs = exploring the 3D nucleon structure, in momentum space



Generalised Partonic Distributions GPDs = exploring the 3D nucleon structure, in coordinate space

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the nucleon is still a very mysterious object and the most abundant piece of matter in the Universe simple physical ideas...

TMDs = Transverse Momentum Dependent Parton Distribution Functions (TMD-PDF) or Transverse Momentum Dependent Fragmentation Functions (TMD-FF)

TMD-PDFs give the number density of partons, with their intrinsic motion and spin, inside a fast moving proton, with its spin.



there are 8 independent TMD-PDFs



only these survive in the collinear limit

 $f_{1T}^{\perp q}(x, k_{\perp}^{2})$

correlate k_{\perp} of quark with S_{\top} of proton (Sivers) $h_1^{\perp q}(x, k_\perp^2)$ correlate k_\perp and s_T of quark (Boer-Mulders)

$$\begin{array}{l} g_{1T}^{\perp q}(x, \boldsymbol{k}_{\perp}^2) & h_{1L}^{\perp q}(x, \boldsymbol{k}_{\perp}^2) & h_{1T}^{\perp q}(x, \boldsymbol{k}_{\perp}^2) \\ & \text{different double-spin correlations} \end{array}$$

TMD-FFs give the number density of hadrons, with their momentum, originated in the fragmentation of a fast moving parton, with its spin.



 $oldsymbol{s}_q \cdot (oldsymbol{p}_q imes oldsymbol{p}_\perp)$ "Collins effect"

there are 2 independent TMD-FFs for spinless hadrons

 $D_1^q(z, \pmb{p}_\perp^2)$ unpolarized hadrons in unpolarized quarks unintegrated fragmentation function

 $H_1^{\perp q}(z, {m p}_{\perp}^2)$ correlate ${m p}_{\perp}$ of hadron with ${m s}_{m au}$ of quark (Collins)

how to "measure" TMDs?

needs processes which relate physical observables to parton intrinsic motion via QCD factorisation



SIDISDrell-Yan processes $\ell N \to \ell h X$ $p N \to \ell^+ \ell^- X$

a similar diagram for $e^+e^- \rightarrow h_1 h_2 X$ and, possibly, for $p N \rightarrow h X$

new probes and concepts to explore the nucleon structure

TMDs - Transverse Momentum Dependent (distribution and fragmentation functions)

(polarized) SIDIS and Drell-Yan



GPDs - Generalized Partonic Distributions exclusive processes in leptonic and hadronic interactions



spatial partonic distribution in transverse space

GTMDs - Generalised Transverse Momentum Dependent (partonic distributions)

exclusive processes in leptonic and hadronic interactions





C. Lorcé, B. Pasquini, M. Vanderhaeghen, JHEP 1105 (2011) 041

phase-space parton distribution, W(k, b)





TMDs in SIDIS



(Collins, Soper, Ji, J.P. Ma, Yuan, Qiu, Vogelsang, Collins, Metz...)

$$\begin{split} \frac{\mathrm{d}\sigma}{\mathrm{d}\phi} &= F_{UU} + \cos(2\phi) \, F_{UU}^{\cos(2\phi)} + \frac{1}{Q} \, \cos\phi \, F_{UU}^{\cos\phi} + \lambda \frac{1}{Q} \, \sin\phi \, F_{LU}^{\sin\phi} \\ &+ S_L \left\{ \sin(2\phi) \, F_{UL}^{\sin(2\phi)} + \frac{1}{Q} \, \sin\phi \, F_{UL}^{\sin\phi} + \lambda \left[F_{LL} + \frac{1}{Q} \, \cos\phi \, F_{LL}^{\cos\phi} \right] \right\} \\ &+ S_T \left\{ \frac{\sin(\phi - \phi_S) \, F_{UT}^{\sin(\phi - \phi_S)} + \sin(\phi + \phi_S) \, F_{UT}^{\sin(\phi + \phi_S)} + \sin(3\phi - \phi_S) \, F_{UT}^{\sin(3\phi - \phi_S)} \\ &+ \frac{1}{Q} \left[\sin(2\phi - \phi_S) \, F_{UT}^{\sin(2\phi - \phi_S)} + \sin\phi_S \, F_{UT}^{\sin\phi_S} \right] \\ &+ \lambda \left[\cos(\phi - \phi_S) \, F_{LT}^{\cos(\phi - \phi_S)} + \frac{1}{Q} \left(\cos\phi_S \, F_{LT}^{\cos\phi_S} + \cos(2\phi - \phi_S) \, F_{LT}^{\cos(2\phi - \phi_S)} \right) \right] \right\} \end{split}$$



LEPTON SCATTERING PLANE

TMDs in Drell-Yan processes COMPASS, RHIC, Fermilab, NICA, AFTER...



factorization holds, two scales, M^2 , and $q_T \leftrightarrow M$

$$\mathrm{d}\sigma^{D-Y} = \sum_{a} f_q(x_1, \boldsymbol{k}_{\perp 1}; Q^2) \otimes f_{\bar{q}}(x_2, \boldsymbol{k}_{\perp 2}; Q^2) \,\mathrm{d}\hat{\sigma}^{q\bar{q} \rightarrow \ell^+ \ell^-}$$

direct product of TMDs, no fragmentation process

Case of one polarized nucleon only





Collins-Soper frame

naive collinear parton model: $\lambda = 1$ $\mu = \nu = 0$



another similar asymmetry can be measured, A₀

Experimental results: clear evidence for Sivers and Collins effects from SIDIS data (HERMES, COMPASS, JLab)



independent evidence for Collins effect from e⁺e⁻ data at Belle, BaBar and BES-III

$$A_{12}(z_1, z_2) \sim \Delta^N D_{h_1/q^{\uparrow}}(z_1) \otimes \Delta^N D_{h_2/\bar{q}^{\uparrow}}(z_2)$$



I. Garzia, arXiv:1201.4678

a similar asymmetry just measured by BES-III (arXiv 1507:06824)



Collins effect clearly observed both in SIDIS and e+e- processes, by several Collaborations

J 0.05

 $\bm{A}_{\rm UL}$

TMD extraction from data - first phase (simple parameterisation, no TMD evolution, limited number of parameters, ...)

unpolarised TMDs - fit of SIDIS multiplicities (M.A, Boglione, Gonzalez, Melis, Prokudin, JHEP 1404 (2014) 005)



strong support for a gaussian distribution

$$\frac{d^2 n^h(x_{\scriptscriptstyle B}, Q^2, z_h, P_T)}{dz_h dP_T^2} = \frac{1}{2P_T} M_n^h(x_{\scriptscriptstyle B}, Q^2, z_h, P_T) = \frac{\pi \sum_q e_q^2 f_{q/p}(x_{\scriptscriptstyle B}) D_{h/q}(z_h)}{\sum_q e_q^2 f_{q/p}(x_{\scriptscriptstyle B})} \frac{e^{-P_T^2/\langle P_T^2 \rangle}}{\pi \langle P_T^2 \rangle}$$

$$\langle P_T^2 \rangle = \langle p_\perp^2 \rangle + z_h^2 \langle k_\perp^2 \rangle$$

$$f_{q/p}(x, k_\perp) = f_{q/p}(x) \frac{e^{-k_\perp^2/\langle k_\perp^2 \rangle}}{\pi \langle k_\perp^2 \rangle}$$

$$D_{h/q}(z, p_\perp) = D_{h/q}(z) \frac{e^{-p_\perp^2/\langle p_\perp^2 \rangle}}{\pi \langle p_\perp^2 \rangle}$$

$$\langle k_\perp^2 \rangle = 0.57 \qquad \langle p_\perp^2 \rangle = 0.12$$

a similar analysis performed by Signori, Bacchetta, Radici, Schnell, JHEP 1311 (2013) 194; it also assumes gaussian behaviour

TMD extraction: transversity and Collins functions - first phase M. A., M. Boglione, U. D'Alesio, S. Melis, F. Murgia, A. Prokudin, PRD 87 (2013) 094019



SIDIS and e+e- data, simple parameterization, no TMD evolution, agreement with extraction using di-hadron FF

(recent papers by Bacchetta, Courtoy, Guagnelli, Radici, JHEP 1505 (2015) 123; Kang, Prokudin, Sun, Yuan, Phys. Rev. D91 (2015) 071501; arXiv:1505.05589)

extraction of u and d Sivers functions - first phase M.A, M. Boglione, U. D'Alesio, S. Melis, F. Murgia, A. Prokudin (in agreement with several other groups)

 $x \Delta^N f_q^{(1)}(x,Q)$



Q² evolution only taken into account in the collinear part (usual PDF)

Sivers effects induces distortions in the parton distribution (quarks polarised along y-direction)



courtesy of A. Bacchetta

b_{\perp} distribution at different values of x (nucleon tomography)

 $x_{B} = 0.25$





 $q(x, \boldsymbol{b}_T)$



femtophotography or tomography of the nucleon

TMDs at LHC - linearly polarised gluons in unpolarized protons



 $K_{\perp} = (K_{H\perp} - K_{j\perp})/2$ $q_T = K_{H\perp} + K_{j\perp}$ Boer, Pisano, Phys. Rev. D91 (2015) 7, 074024 Z-boson transverse momentum q_T spectrum in pp collisions at the LHC



The small q_T region cannot be explained by usual collinear PDF factorization: needs TMD-PDFs Phys. Rev. D85 (2012) 032002

other measured evidence of the Sivers and Collins effects



TMDs and QCD - TMD evolution study of the QCD evolution of TMDs and TMD factorisation in rapid development Collins-Soper-Sterman resummation - NP B250 (1985) 199 Idilbi, Ji, Ma, Yuan - PL B597, 299 (2004); PR D70 (2004) 074021 Ji, Ma, Yuan - PL B597 (2004) 299; PR. D71 (2005) 034005 Collins, "Foundations of perturbative QCD", Cambridge University Press (2011) Aybat, Rogers, PR D83 (2011) 114042 Aybat, Collins, Qiu, Rogers, PR D85 (2012) 034043 Echevarria, Idilbi, Schafer, Scimemi, arXiv:1208.1281 Echevarria, Idilbi, Scimemi, JHEP 1207 (2012) 002 Aybat, Prokudin, Rogers, PRL 108 (2012) 242003 Anselmino, Boglione, Melis, PR D86 (2012) 014028 Aidala, Field, Gamberg, Rogers, PR D89 (2014) 094002 Echevarria, Idilbi, Kang, Vitev, PR D89 (2014) 074013 Bacchetta, Prokudin, NP B875 (2013) 536 Godbole, Misra, Mukherjee, Raswoot, PR D88 (2013) 014029 Boer, Lorcé, Pisano, Zhou, arXiv:1504.04332 (2015) Boglione, Gonzalez, Melis, Prokudin, JHEP 1502 (2015) 095 Kang, Prokudin, Sun, Yuan, arXiv:1505.05589 + many more authors...

different TMD evolution schemes and different implementation within the same scheme

dedicated workshops, QCD Evolution 2011, 2012, 2013, 2014, 2015

see, "Transverse momentum dependent (TMD) parton distribution functions: status and prospects", arXiv: 1507.05267 (from "Resummation, Evolution, Factorization", Antwerp 2014)

dedicated tools:

TMDlib and TMDplotter: library and plotting tools for transverse-momentum-dependent parton distributions Hautmann, Jung, Kramer, Mulders, Nocera, Rogers, Signori

TMD phenomenology - phase 2 how does gluon emission affect the transverse motion? a few selected results

TMD evolution of up quark Sivers function



Aybat, Collins, Qiu, Rogers, Phys. Rev. D85 (2012) 034043

TMD evolution of up quark Sivers function



Aybat, Collins, Qiu, Rogers, Phys.Rev. D85 (2012) 034043

TMD evolution of Sivers function studied also by Echevarria, Idilbi, Kang, Vitev, Phys. Rev. D89 (2014) 074013 Extraction of transversity and Collins functions with TMD evolution (Kang, Prokudin, Sun, Yuan, arXiv:1505.05589)





comparison with phase 1 extraction, $Q^2 = 2.4 \text{ GeV}^2$

(Kang, Prokudin, Sun, Yuan, arXiv:1505.05589)



predictions for BES-III e⁺e⁻ Collins asymmetry A₀ in excellent agreement with data, Q² = 13 GeV² (some difficulties without TMD evolution)

(Kang, Prokudin, Sun, Yuan, arXiv:1505.05589)



so far

Sivers and Collins effects are well established, many transverse spin asymmetries resulting from them. Sivers function and orbital angular momentum? GPDs and orbital angular momentum?

Evidence for gaussian k_{\perp} and p_{\perp} dependence of unpolarised TMD-PDFs and TMD-FFs

Gluon TMDs deserve special attention; they might play a role at LHC

Much progress in studies of TMD factorisation and TMD evolution; phenomenological implementation in progress

Combined data from SIDIS, Drell-Yan, e+e-, with theoretical modelling, should lead to a true 3D imaging of the proton

waiting for JLab 12, new COMPASS results, future facilities....

some hadron physics in the world





Electron Ion Collider plans in the world....



Electron Ion Collider: The Next QCD Frontier

Understanding the glue that binds us all

future facilities and experiments: D-Y@COMPASS JLAB 12 GeV EIC BESIII AFTER NICA-SPD

1D



exploring the 3D structure of the nucleon

courtesy of A. Bacchetta

1D



