

$$u_c(N) = -\frac{2}{N} \sum_{k=1}^{N-1} \frac{N-k}{k^3}$$