

$$\cot \frac{2q}{2q-1} \left(\frac{\pi}{N} \right) + 1 = \left[\frac{\tilde{u}_r(N)}{u_c(N)} \right]^{\frac{2q}{3(2q-1)}}$$