



# QCD e fisica di precisione a LHC

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# As of today

- As predicted in the SM, a new Yukawa force has been discovered, the first ever seen\* not mediated by a gauge vector.
- Its mediator behaves a lot like the SM scalar: H-universality of the couplings
- No significant discrepancy with respect to the SM predictions

\*fundamental, ie with elementary mediators.

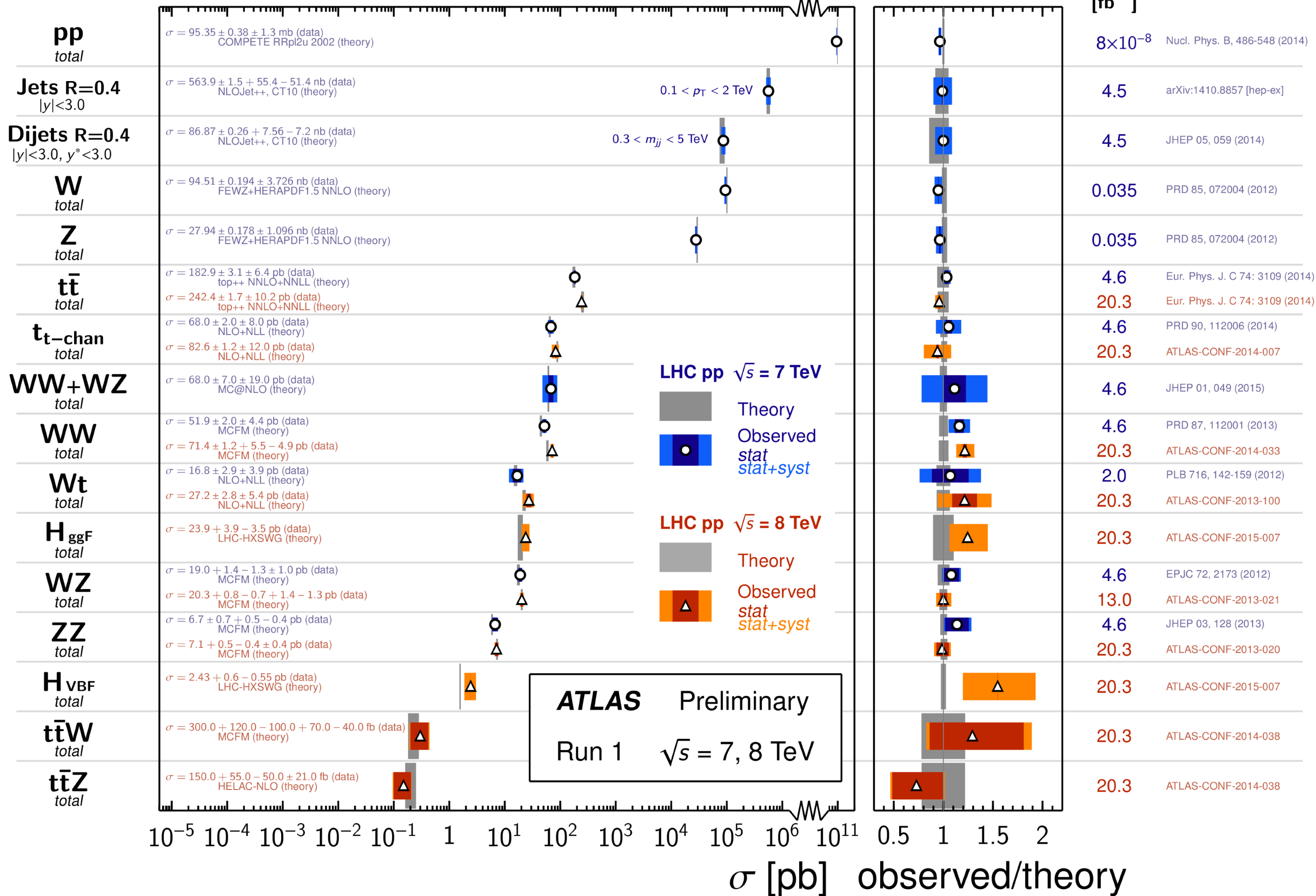


# Standard Model Total Production Cross Section Measurements

Status: March 2015

$\int \mathcal{L} dt$   
[fb<sup>-1</sup>]

Reference





# As of today

- As predicted in the SM, a new Yukawa force has been discovered, the first ever seen\* not mediated by a gauge vector.
- Its mediator behaves a lot like the SM scalar: H-universality of the couplings
- No significant discrepancy with the SM predictions
- No convincing sign of resonant new physics found so far





# ATLAS Exotics Searches\* - 95% CL Exclusion

Status: July 2015

ATLAS Preliminary

$$\int \mathcal{L} dt = (4.7 - 20.3) \text{ fb}^{-1}$$

$$\sqrt{s} = 7, 8 \text{ TeV}$$

Model	$\ell, \gamma$	Jets	$E_T^{\text{miss}}$	$\int \mathcal{L} dt [\text{fb}^{-1}]$	Limit	Reference
Extra dimensions	ADD $G_{KK} + g/q$	$\geq 1 j$	Yes	20.3	$M_D$ 5.25 TeV	$n = 2$ 1502.01518
	ADD non-resonant $\ell\ell$	-	-	20.3	$M_S$ 4.7 TeV	$n = 3 \text{ HLZ}$ 1407.2410
	ADD QBH $\rightarrow \ell q$	1 $e, \mu$ 1 j	-	20.3	$M_{\text{th}}$ 5.2 TeV	$n = 6$ 1311.2006
	ADD QBH	-	2 j	-	$M_{\text{th}}$ 5.82 TeV	$n = 6$ 1407.1376
	ADD BH high $N_{\text{trk}}$	2 $\mu$ (SS)	-	-	$M_{\text{th}}$ 4.7 TeV	$n = 6, M_D = 3 \text{ TeV, non-rot BH}$ 1308.4075
	ADD BH high $\sum p_T$	$\geq 1 e, \mu$	$\geq 2 j$	-	$M_{\text{th}}$ 5.8 TeV	$n = 6, M_D = 3 \text{ TeV, non-rot BH}$ 1405.4254
	ADD BH high multijet	-	$\geq 2 j$	-	$M_{\text{th}}$ 5.8 TeV	$n = 6, M_D = 3 \text{ TeV, non-rot BH}$ 1503.08988
	RS1 $G_{KK} \rightarrow \ell\ell$	2 $e, \mu$	-	-	$G_{KK} \text{ mass}$ 2.68 TeV	$k/\overline{M}_{Pl} = 0.1$ 1405.4123
	RS1 $G_{KK} \rightarrow \gamma\gamma$	2 $\gamma$	-	-	$G_{KK} \text{ mass}$ 2.66 TeV	$k/\overline{M}_{Pl} = 0.1$ 1504.05511
	Bulk RS $G_{KK} \rightarrow ZZ \rightarrow qq\ell\ell$	2 $e, \mu$ 2 j / 1 J	-	-	$G_{KK} \text{ mass}$ 740 GeV	$k/\overline{M}_{Pl} = 1.0$ 1409.6190
	Bulk RS $G_{KK} \rightarrow WW \rightarrow qq\ell\nu$	1 $e, \mu$ 2 j / 1 J	Yes	20.3	$W' \text{ mass}$ 760 GeV	$k/\overline{M}_{Pl} = 1.0$ 1503.04677
	Bulk RS $G_{KK} \rightarrow HH \rightarrow b\bar{b}b\bar{b}$	-	4 b	-	$G_{KK} \text{ mass}$ 500-720 GeV	$k/\overline{M}_{Pl} = 1.0$ 1506.00285
	Bulk RS $g_{KK} \rightarrow t\bar{t}$	1 $e, \mu$ $\geq 1 b, \geq 1 J/2 j$	Yes	20.3	$g_{KK} \text{ mass}$ 2.2 TeV	BR = 0.925 1505.07018
	2UED / RPP	2 $e, \mu$ (SS) $\geq 1 b, \geq 1 j$	Yes	20.3	KK mass 960 GeV	1504.04605
Gauge bosons	SSM $Z' \rightarrow \ell\ell$	2 $e, \mu$	-	20.3	$Z' \text{ mass}$ 2.9 TeV	1405.4123
	SSM $Z' \rightarrow \tau\tau$	2 $\tau$	-	19.5	$Z' \text{ mass}$ 2.02 TeV	1502.07177
	SSM $W' \rightarrow \ell\nu$	1 $e, \mu$	-	Yes 20.3	$W' \text{ mass}$ 3.24 TeV	1407.7494
	EGM $W' \rightarrow WZ \rightarrow \ell\nu\ell'\ell'$	3 $e, \mu$	-	Yes 20.3	$W' \text{ mass}$ 1.52 TeV	1406.4456
	EGM $W' \rightarrow WZ \rightarrow qq\ell\ell$	2 $e, \mu$ 2 j / 1 J	-	20.3	$W' \text{ mass}$ 1.59 TeV	1409.6190
	EGM $W' \rightarrow WZ \rightarrow qq\ell\nu$	-	2 J	-	$W' \text{ mass}$ 1.3-1.5 TeV	1506.00962
	HVT $W' \rightarrow WH \rightarrow \ell\nu b\bar{b}$	1 $e, \mu$ 2 b	Yes 20.3	$W' \text{ mass}$ 1.47 TeV	$g_V = 1$ 1503.08089	
	LRSM $W'_R \rightarrow t\bar{b}$	1 $e, \mu$ 2 b, 0-1 j	Yes 20.3	$W' \text{ mass}$ 1.92 TeV	1410.4103	
	LRSM $W'_R \rightarrow t\bar{b}$	0 $e, \mu$ $\geq 1 b, 1 J$	-	20.3	$W' \text{ mass}$ 1.76 TeV	1408.0886
	CI	CI $qqqq$	-	2 j	-	$\Lambda$ 12.0 TeV
CI $qq\ell\ell$		2 $e, \mu$	-	-	$\Lambda$ 21.6 TeV	$\eta_{LL} = -1$ 1407.2410
CI $uutt$		2 $e, \mu$ (SS) $\geq 1 b, \geq 1 j$	Yes 20.3	$\Lambda$ 4.3 TeV	$ C_{LL}  = 1$ 1504.04605	
DM	EFT D5 operator (Dirac)	0 $e, \mu$ $\geq 1 j$	Yes 20.3	$M_*$ 974 GeV	at 90% CL for $m(\chi) < 100 \text{ GeV}$ 1502.01518	
	EFT D9 operator (Dirac)	0 $e, \mu$ 1 J, $\leq 1 j$	Yes 20.3	$M_*$ 2.4 TeV	at 90% CL for $m(\chi) < 100 \text{ GeV}$ 1309.4017	
LQ	Scalar LQ 1 <sup>st</sup> gen	2 $e$ $\geq 2 j$	-	20.3	LQ mass 1.05 TeV	$\beta = 1$ Preliminary
	Scalar LQ 2 <sup>nd</sup> gen	2 $\mu$ $\geq 2 j$	-	20.3	LQ mass 1.0 TeV	$\beta = 1$ Preliminary
	Scalar LQ 3 <sup>rd</sup> gen	1 $e, \mu$ $\geq 1 b, \geq 3 j$	Yes 20.3	LQ mass 640 GeV	$\beta = 0$ Preliminary	
Heavy quarks	VLQ $TT \rightarrow Ht + X$	1 $e, \mu$ $\geq 2 b, \geq 3 j$	Yes 20.3	T mass 855 GeV	T in (T,B) doublet 1505.04306	
	VLQ $YY \rightarrow Wb + X$	1 $e, \mu$ $\geq 1 b, \geq 3 j$	Yes 20.3	Y mass 770 GeV	Y in (B,Y) doublet 1505.04306	
	VLQ $BB \rightarrow Hb + X$	1 $e, \mu$ $\geq 2 b, \geq 3 j$	Yes 20.3	B mass 735 GeV	isospin singlet 1505.04306	
	VLQ $BB \rightarrow Zb + X$	2/ $\geq 3 e, \mu$ $\geq 2/\geq 1 b$	-	20.3	B mass 755 GeV	B in (B,Y) doublet 1409.5500
	$T_{5/3} \rightarrow Wt$	1 $e, \mu$ $\geq 1 b, \geq 5 j$	Yes 20.3	$T_{5/3} \text{ mass}$ 840 GeV	1503.05425	
Excited fermions	Excited quark $q^* \rightarrow q\gamma$	1 $\gamma$ 1 j	-	20.3	$q^* \text{ mass}$ 3.5 TeV	only $u^*$ and $d^*$ , $\Lambda = m(q^*)$ 1309.3230
	Excited quark $q^* \rightarrow qg$	-	2 j	-	$q^* \text{ mass}$ 4.09 TeV	only $u^*$ and $d^*$ , $\Lambda = m(q^*)$ 1407.1376
	Excited quark $b^* \rightarrow Wt$	1 or 2 $e, \mu$ 1 b, 2 j or 1 j	Yes 4.7	$b^* \text{ mass}$ 870 GeV	left-handed coupling 1301.1583	
	Excited lepton $\ell^* \rightarrow \ell\gamma$	2 $e, \mu, 1 \gamma$	-	-	$\ell^* \text{ mass}$ 2.2 TeV	$\Lambda = 2.2 \text{ TeV}$ 1308.1364
	Excited lepton $\nu^* \rightarrow \ell W, \nu Z$	3 $e, \mu, \tau$	-	-	$\nu^* \text{ mass}$ 1.6 TeV	$\Lambda = 1.6 \text{ TeV}$ 1411.2921
Other	LSTC $a_T \rightarrow W\gamma$	1 $e, \mu, 1 \gamma$	Yes 20.3	$a_T \text{ mass}$ 960 GeV	1407.8150	
	LRSM Majorana $\nu$	2 $e, \mu$ 2 j	-	20.3	$N^0 \text{ mass}$ 2.0 TeV	1506.06020
	Higgs triplet $H^{\pm\pm} \rightarrow \ell\ell$	2 $e, \mu$ (SS)	-	-	$H^{\pm\pm} \text{ mass}$ 551 GeV	$m(W_R) = 2.4 \text{ TeV, no mixing}$ DY production, $\text{BR}(H_L^{\pm\pm} \rightarrow \ell\ell) = 1$ 1412.0237
	Higgs triplet $H^{\pm\pm} \rightarrow \ell\tau$	3 $e, \mu, \tau$	-	-	$H^{\pm\pm} \text{ mass}$ 400 GeV	DY production, $\text{BR}(H_L^{\pm\pm} \rightarrow \ell\tau) = 1$ 1411.2921
	Monotop (non-res prod)	1 $e, \mu$ 1 b	Yes 20.3	spin-1 invisible particle mass 657 GeV	$a_{\text{non-res}} = 0.2$ 1410.5404	
	Multi-charged particles	-	-	-	multi-charged particle mass 785 GeV	DY production, $ q  = 5e$ 1504.04188
	Magnetic monopoles	-	-	-	monopole mass 1.34 TeV	DY production, $ g  = 1g_D, \text{spin } 1/2$ Preliminary

$\sqrt{s} = 7 \text{ TeV}$   $\sqrt{s} = 8 \text{ TeV}$

10<sup>-1</sup> 1 10 Mass scale [TeV]

\*Only a selection of the available mass limits on new states or phenomena is shown.



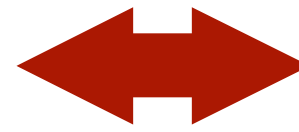
# Goals of the SM LHC programme

1. Precise determination of the fundamental parameters of the dim=4 SM lagrangian, such as masses ( $m_h$ ,  $m_W$ ,  $m_t$ ), and couplings:
  - SM measurements of fundamental parameters provide information to be fed to the whole HEP community.
  - Range of validity of the SM
2. Search and quantification of deviations from the SM (New Physics).

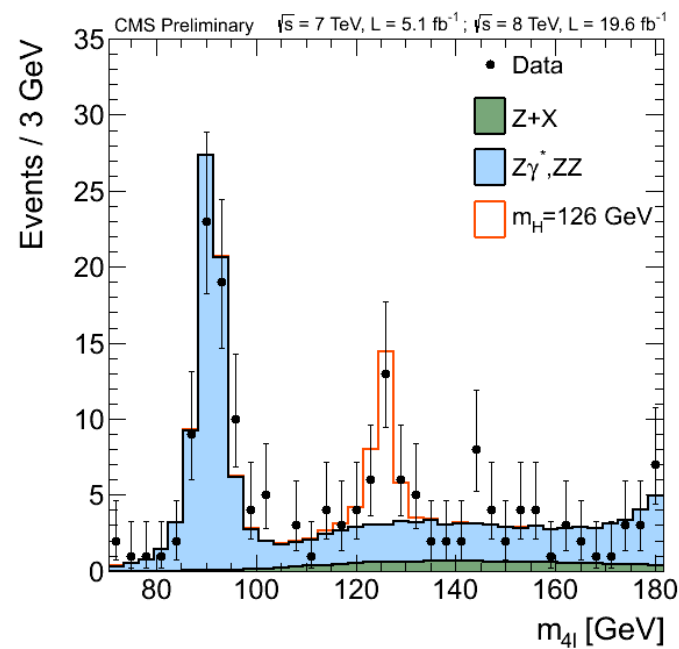
# Search for New Physics at the LHC

Two main strategies for searching new physics

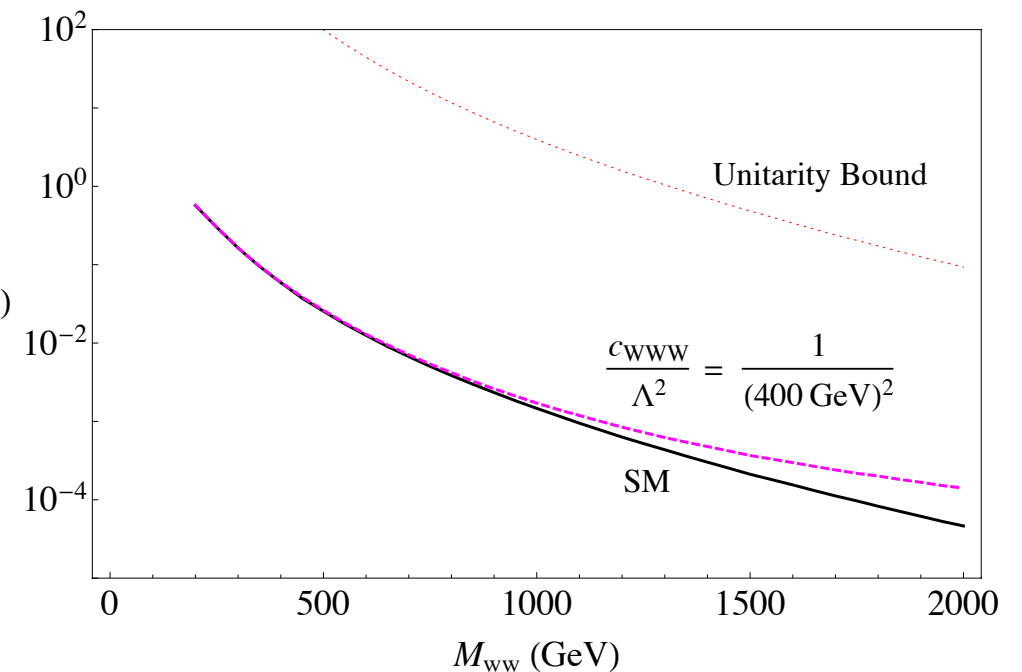
Search for new states



Search for new interactions



$$\frac{d\sigma}{dM_{ww}} \left( \frac{\text{pb}}{\text{GeV}} \right)$$



“Peak” or more complicated structures searches. Need for **descriptive MC** for discovery = Discovery is data driven. Later need precision for characterisation.

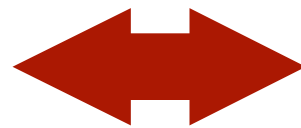
Deviations are expected to be small. Intrinsically a precision measurement. Needs for **predictive MC** and accurate predictions for SM and EFT.

# BSM goals of the SM LHC programme

Two main strategies for searching new physics

Search for new states

SUSY, EXOTICS, BSM HIGGS



Search for new interactions

SM

The matter content of SM has been experimentally verified and evidence for light states is not present. SM measurements can always be seen as searches for deviations from the dim=4 SM Lagrangian predictions.

$$\mathcal{L}_{SM}^{(6)} = \mathcal{L}_{SM}^{(4)} + \sum_i \frac{c_i}{\Lambda^2} \mathcal{O}_i + \dots$$

**BSM goal of the SM LHC program:**

**determination of the couplings of the SM lagrangian at DIM=6**



# Dim=6 SM Lagrangian

[Grazzkowski et al, 10]

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
		$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
		$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
		$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

- Based on all the symmetries of the SM
- New physics is heavier than the resonance itself :  $\Lambda > M_X$
- QCD and EW renormalizable (order by order in  $1/\Lambda$ )
- Number of extra couplings reduced by symmetries and dimensional analysis
- Extends the reach of searches for NP beyond the collider energy.
- Valid only up to the scale  $\Lambda$

$(\bar{L}L)(\bar{L}L)$	$(\bar{R}R)(\bar{R}R)$	$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$
		$Q_{ud}^{(3)}$	$(\bar{u}_p \gamma_\mu \tau^I u_r)(\bar{d}_s \gamma^\mu \tau^I d_t)$
		$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{qd}^{(3)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
		$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$	B-violating		
$Q_{ledq}$	$(\bar{l}_p^i e_r) (\bar{d}_s^j q_t^k)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{ijk} [(d_p^\alpha)^T C u_r^\beta] [(q_t^\gamma)^T C l_t^k]$
$Q_{quqd}^{(1)}$	$(\bar{q}_p^i u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$Q_{quu}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{ijk} [(q_p^\alpha)^T C q_r^\beta] [(u_t^\gamma)^T C e_t^k]$
$Q_{quqd}^{(8)}$	$(\bar{q}_p^i T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{quq}^{(1)}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{ijk} \varepsilon_{mnp} [(q_p^\alpha)^T C q_r^\beta] [(q_t^\gamma)^T C l_t^k]$
$Q_{lequ}^{(1)}$	$(\bar{l}_p^i e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{quq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma} (\tau^I \varepsilon)_{jk} (\tau^I \varepsilon)_{mn} [(q_p^\alpha)^T C q_r^\beta] [(q_t^\gamma)^T C l_t^k]$
$Q_{lequ}^{(3)}$	$(\bar{l}_p^i \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_t^\gamma)^T C e_t^k]$



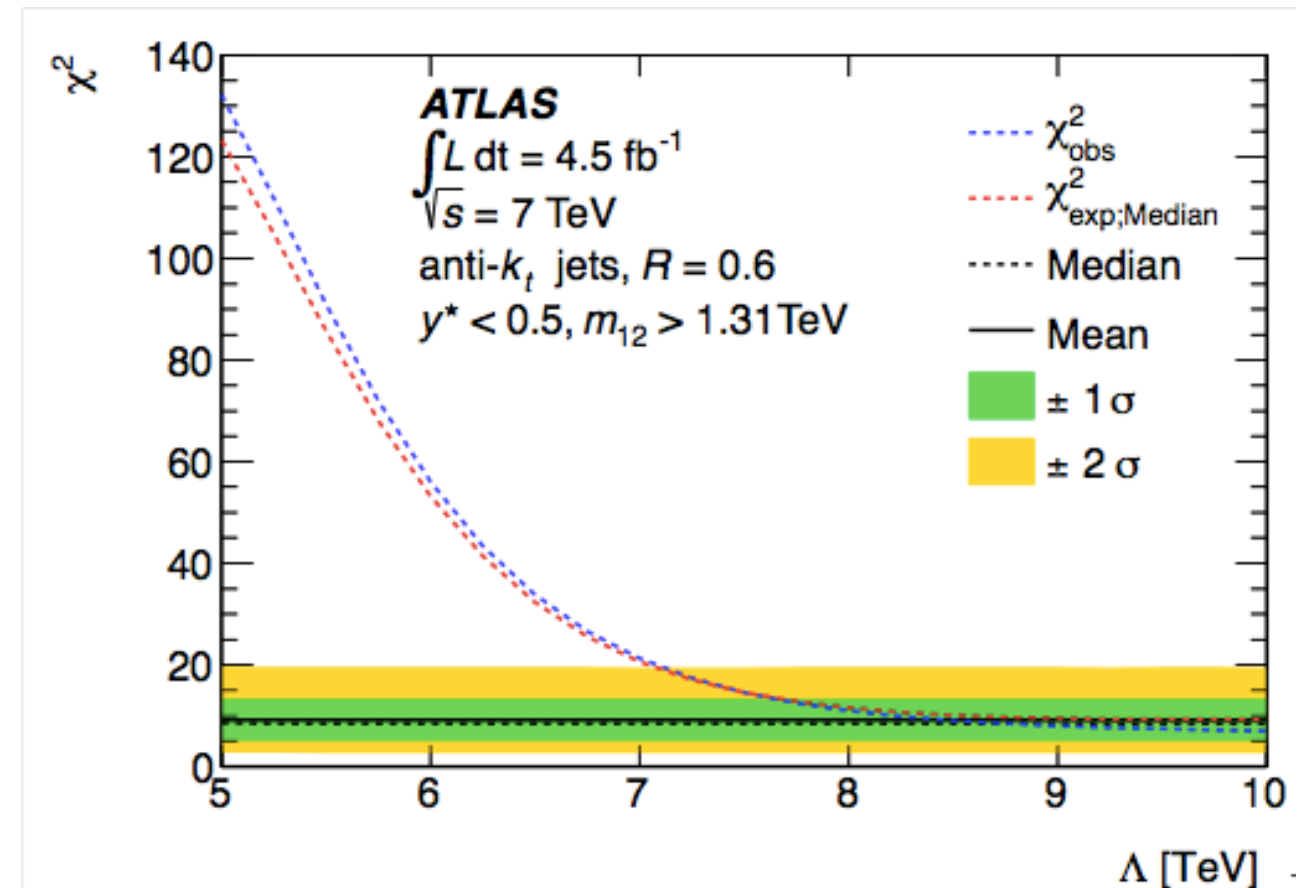
# BSM in SM dijets measurements

$$\mathcal{L}_{NP} = \frac{1}{2\Lambda^2} (c_1 O_1 + c_2 O_2)$$

$$O_1 = \delta_{ij} \delta_{kl} \left( \sum_{c=1}^3 \bar{q}_{Lci} \gamma_\mu q_{Lcj} \sum_{d=1}^3 \bar{q}_{Ldk} \gamma^\mu q_{Ldl} \right),$$

$$O_2 = T_{ij}^a T_{kl}^a \left( \sum_{c=1}^3 \bar{q}_{Lci} \gamma_\mu q_{Lcj} \sum_{d=1}^3 \bar{q}_{Ldk} \gamma^\mu q_{Ldl} \right),$$

[Gao et al, 2011]

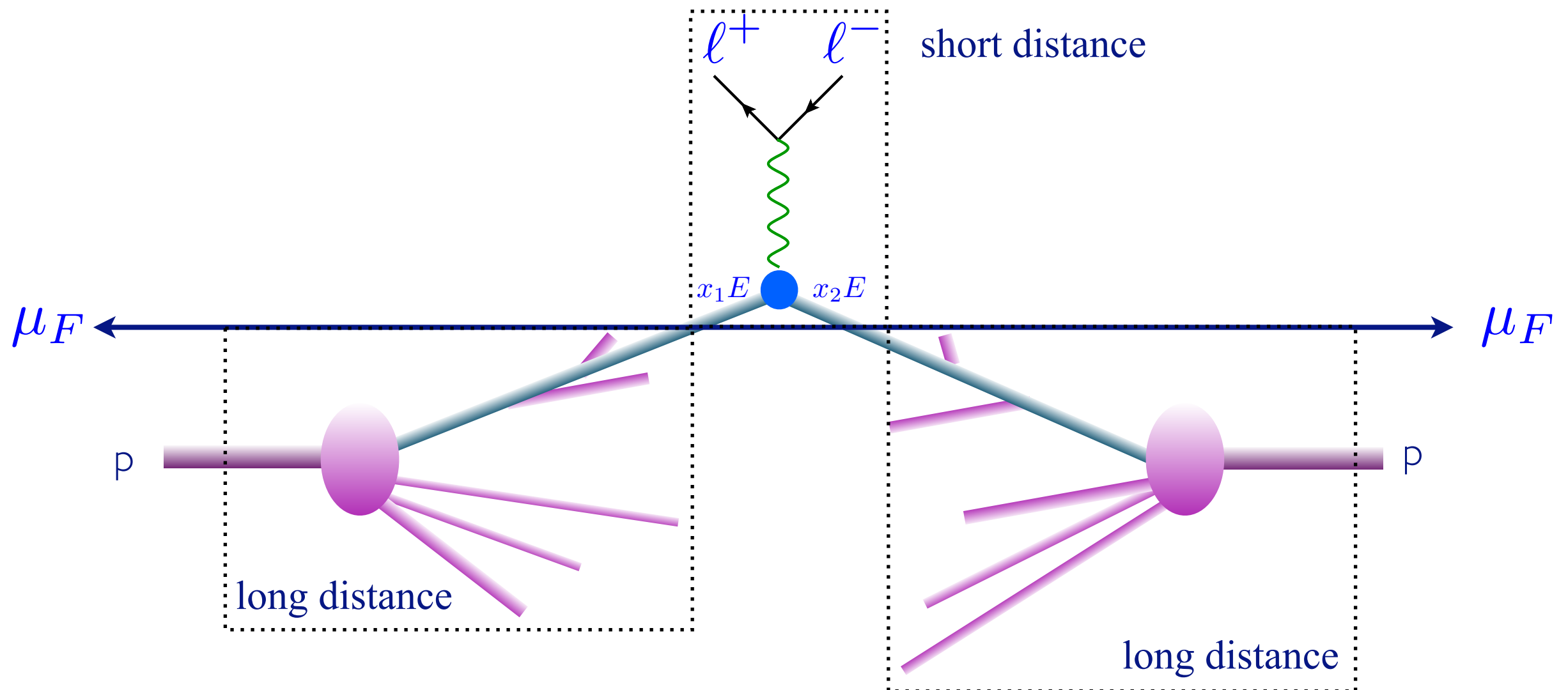


Calculation at NLO accuracy in the EFT. both operators switched on because of mixing. Comparison with SM at NLO consistent.



Many other 4F operators possible, flavour structure to be constrained, NLO+PS. Other observables with quark-gluon tagging.

# Master formula for the LHC



$$\sigma_X = \sum_{a,b} \int_0^1 dx_1 dx_2 f_a(x_1, \mu_F^2) f_b(x_2, \mu_F^2) \times \hat{\sigma}_{ab \rightarrow X}(x_1, x_2, \alpha_S(\mu_R^2), \frac{Q^2}{\mu_F^2}, \frac{Q^2}{\mu_R^2})$$

Accurate predictions for observables in hadronic collisions depend on the knowledge of both parton distribution functions and partonic x sections.

# PDFs

Non-perturbative information that is fitted from a wealth of experimental data

- The pdf is parametrised at a given low scale in terms of an analytic or NN function and momentum sum rules are imposed.
- They are evolved through the DGLAP equations:

$$Q^2 \frac{\partial f_a(x, Q^2)}{\partial Q^2} = \int_x^1 \frac{dz}{z} P_{ab}(\alpha_S(Q^2), z) f_b(x/z, Q^2)$$

$$P_{ab}(\alpha_S, z) = \frac{\alpha_S}{2\pi} P_{ab}^{(0)}(z) + \left(\frac{\alpha_S}{2\pi}\right)^2 P_{ab}^{(1)}(z) + \left(\frac{\alpha_S}{2\pi}\right)^3 P_{ab}^{(2)}(z) + \dots$$

LO (1974)

NLO (1980)

NNLO (2004)





# PDFs

Global fits: recent progress in methodology and data sets:

- NNPDF3.0 1410.8849
- MMHTCT14 1412.3989
- CT14 1506.07443

Stefano Forte®

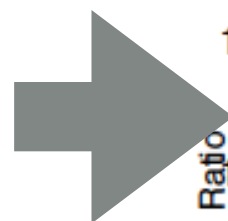
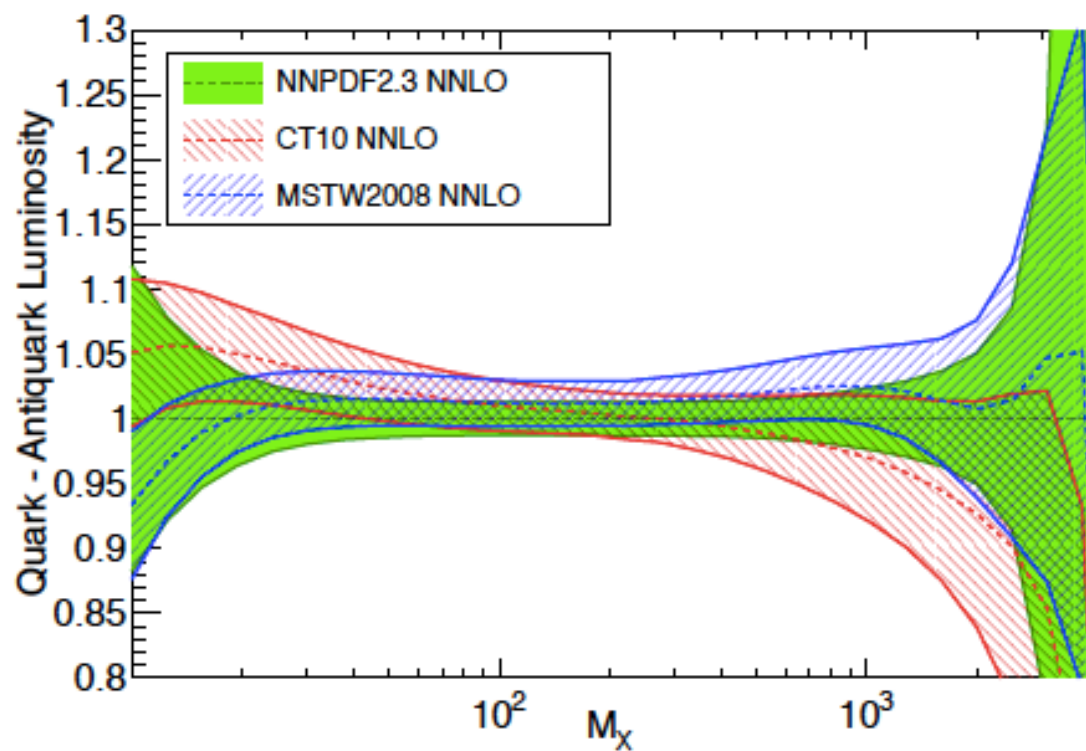
	NNPDF3.0	MMHT14	CT14
NO. OF FITTED PDFs	7	7	6
PARAMETRIZATION	NEURAL NETS	$x^a(1-x)^b \times$ CHEBYSCHEV	$x^a(1-x)^b \times$ BERNSTEIN
FREE PARAMETERS	259	37	30-35
UNCERTAINTIES	REPLICAS	HESSIAN	HESSIAN
TOLERANCE	NONE	DYNAMICAL	DYNAMICAL
CLOSURE TEST	✓	✗	✗
REWEIGHTING	REPLICAS	EIGENVECTORS	EIGENVECTORS

Other non-global sets: HeraPDF, ABM14, GJR

# QUARK-QUARK

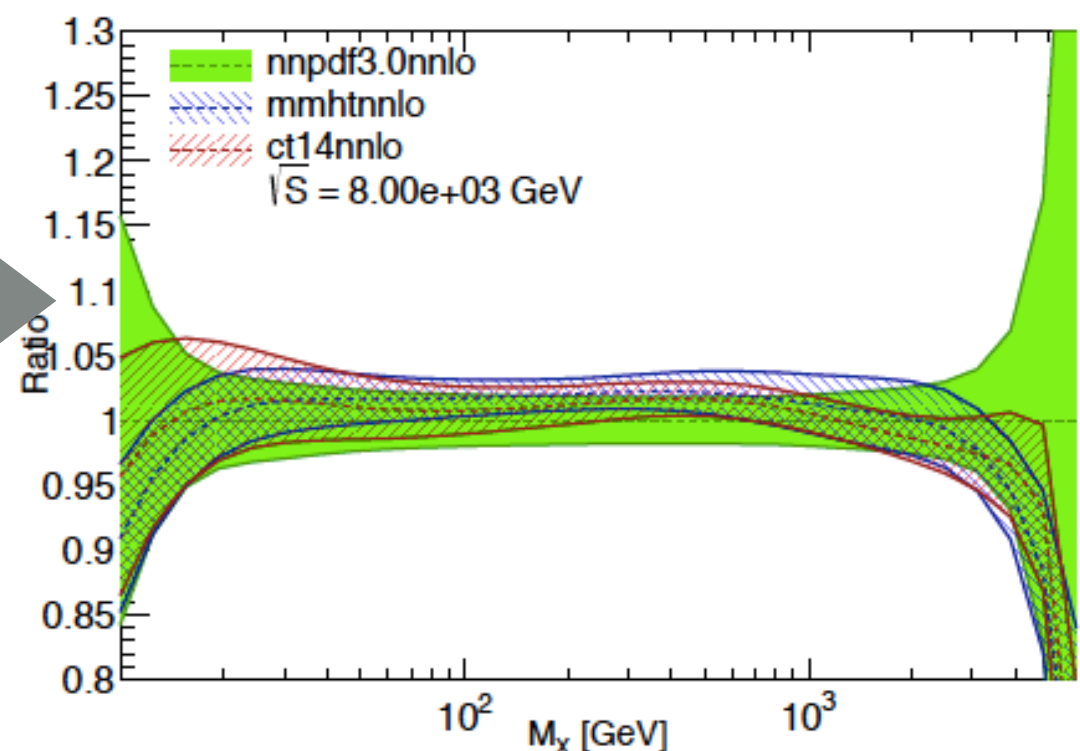
## 2012

LHC 8 TeV - Ratio to NNPDF2.3 NNLO -  $\alpha_s = 0.118$



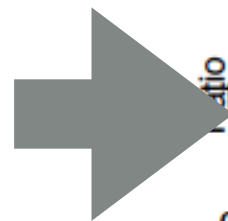
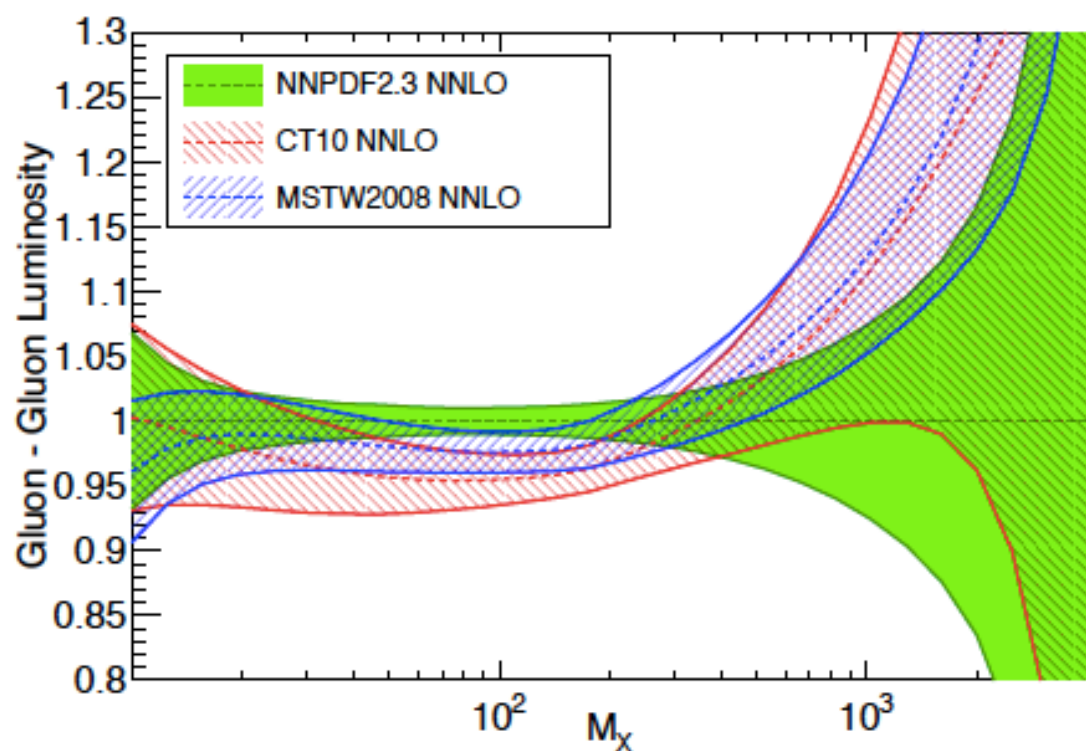
## 2015

Quark-Quark, luminosity

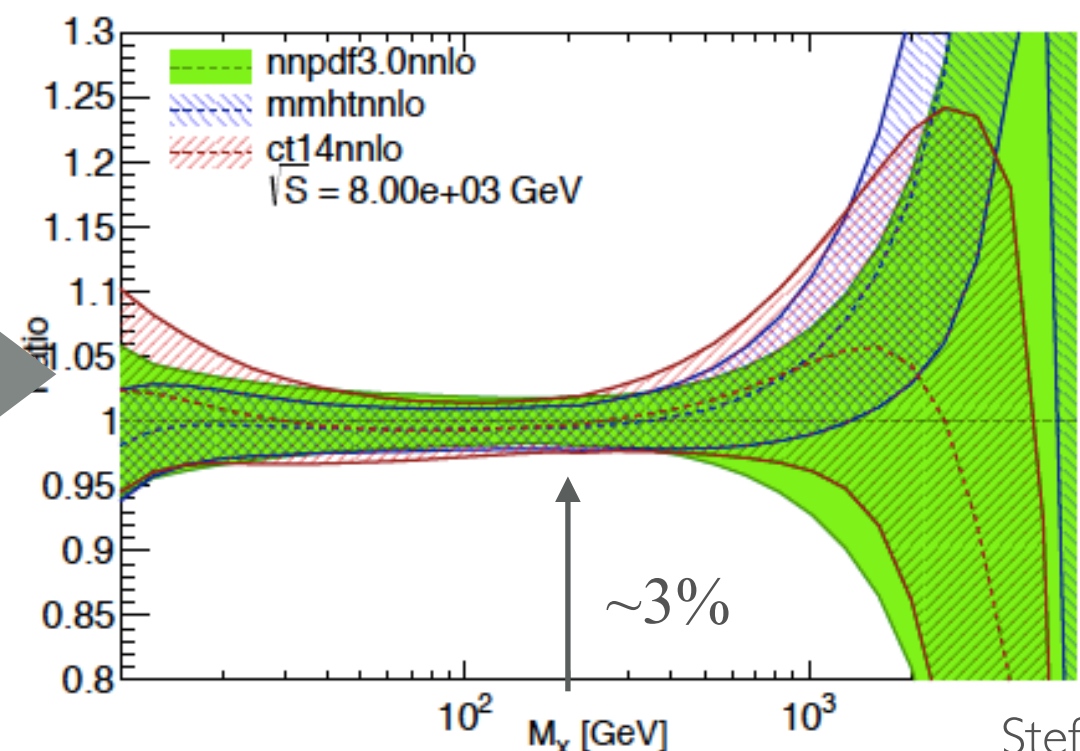


# GLUON-GLUON

LHC 8 TeV - Ratio to NNPDF2.3 NNLO -  $\alpha_s = 0.118$



Gluon-Gluon, luminosity



Stefano Forte

# Perturbative expansion

$\hat{\sigma}_{ab \rightarrow X}(\hat{S}, \mu_F, \mu_R)$  Parton-level cross section

- The parton-level cross section can be computed as a series in perturbation theory, using the coupling constant as an expansion parameter

$$\hat{\sigma} = \sigma^{\text{Born}} \left( 1 + \frac{\alpha_s}{2\pi} \sigma^{(1)} + \left( \frac{\alpha_s}{2\pi} \right)^2 \sigma^{(2)} + \left( \frac{\alpha_s}{2\pi} \right)^3 \sigma^{(3)} + \dots \right)$$

LO  
predictions

NLO  
corrections

NNLO  
corrections

NNNLO  
corrections

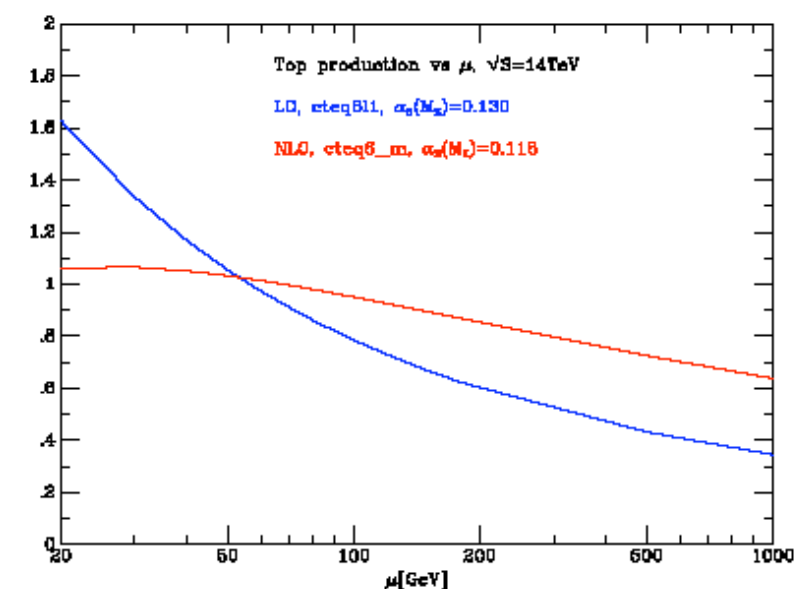
- Including higher corrections improves predictions and reduces theoretical uncertainties: improvement in accuracy and precision.

# Perturbative expansion

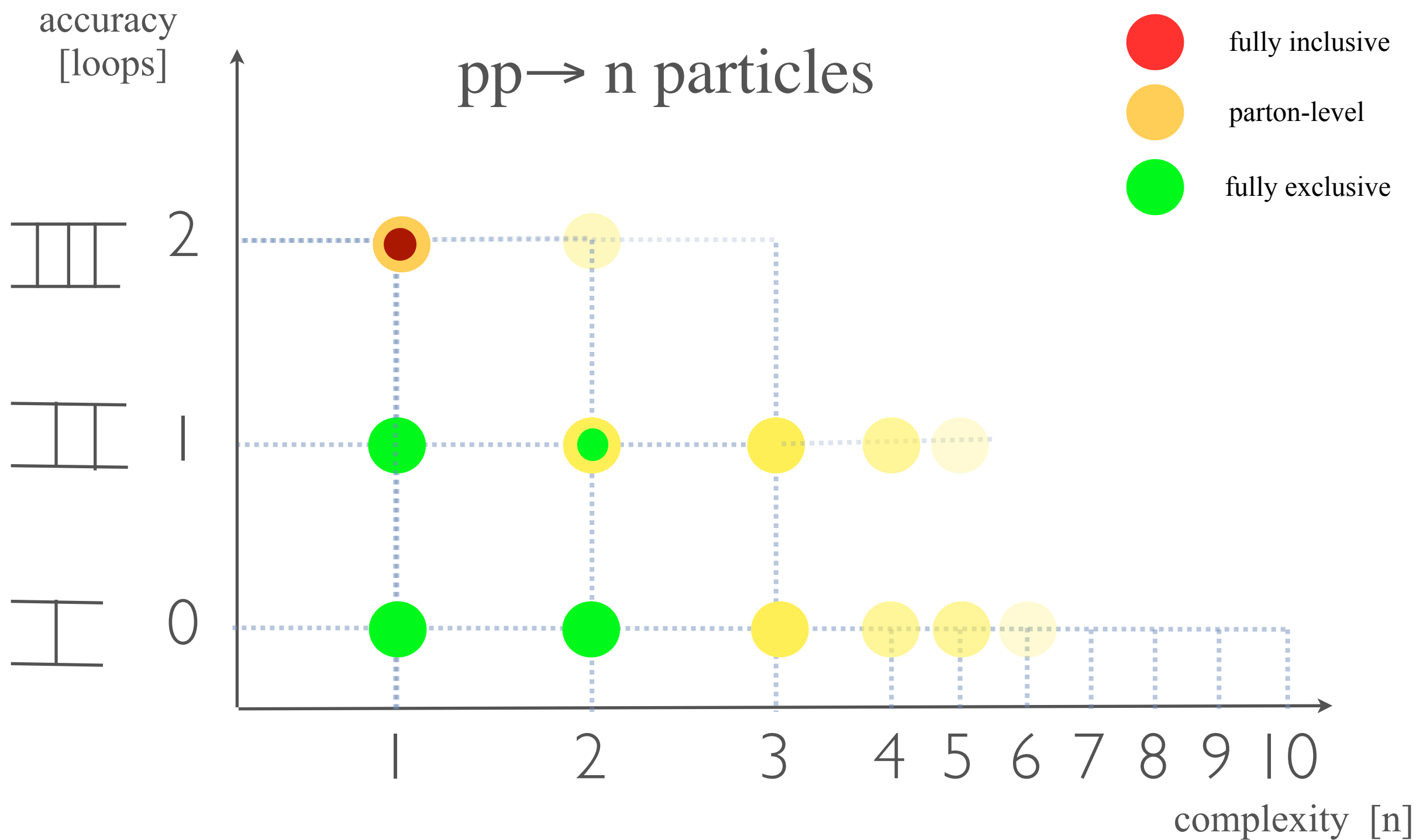
- Leading order (LO) calculations typically give only the order of magnitude of cross sections and distributions
  - the scale of  $\alpha_s$  is not defined
  - jets partons: jet structure starts to appear only beyond LO
  - Born topology might not be leading at the LHC
- To obtain reliable predictions at least NLO is needed
- NNLO allows to quantify uncertainties

Furthermore:

- Resummation of the large logarithmic terms at phase space boundaries
- NLO ElectroWeak corrections ( $\alpha_s^2 = \alpha_W$ )
- Fully exclusive predictions available in terms of event simulation that can be used in experimental analysis



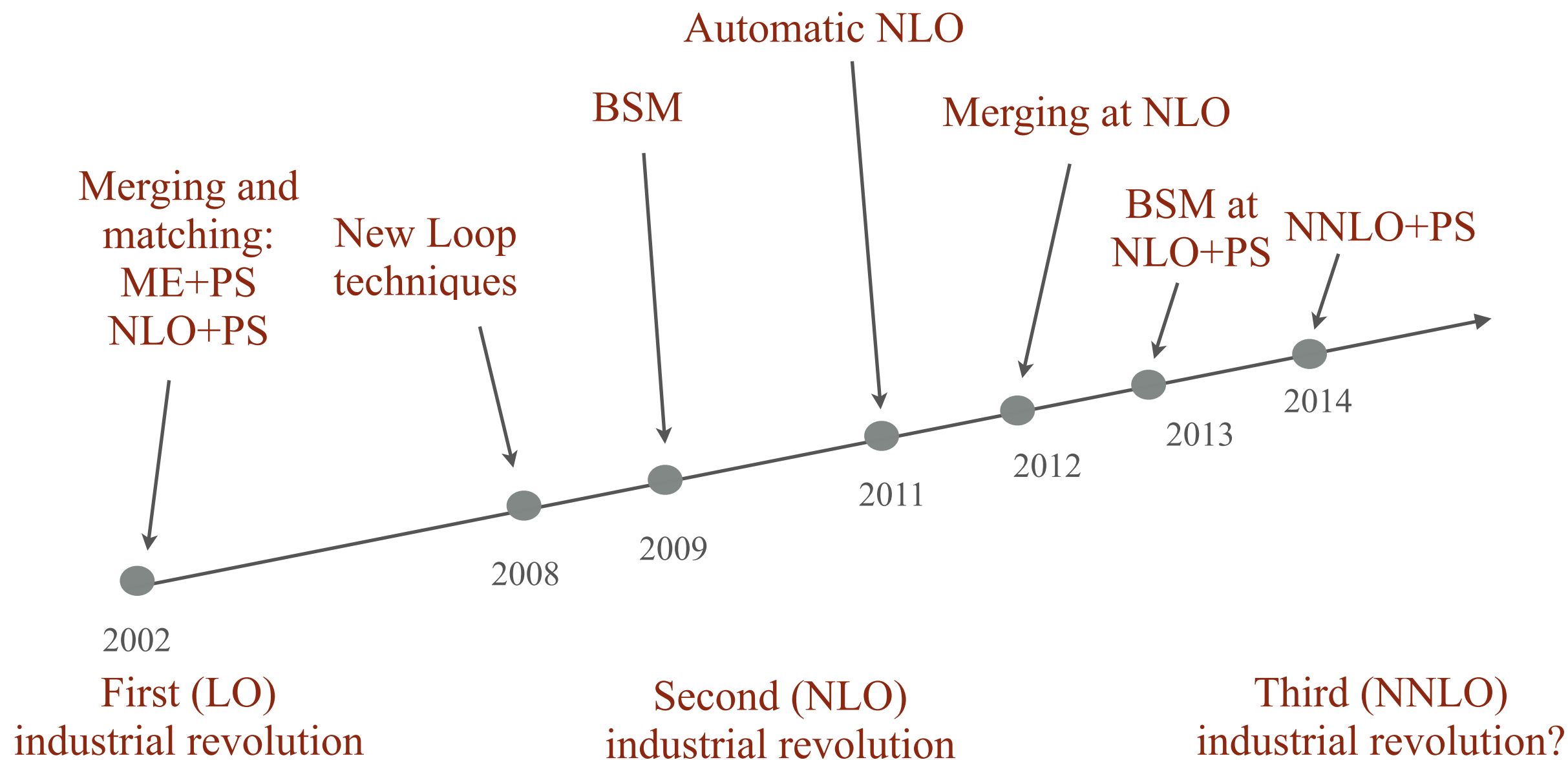
# Predictions in QCD: before the LHC





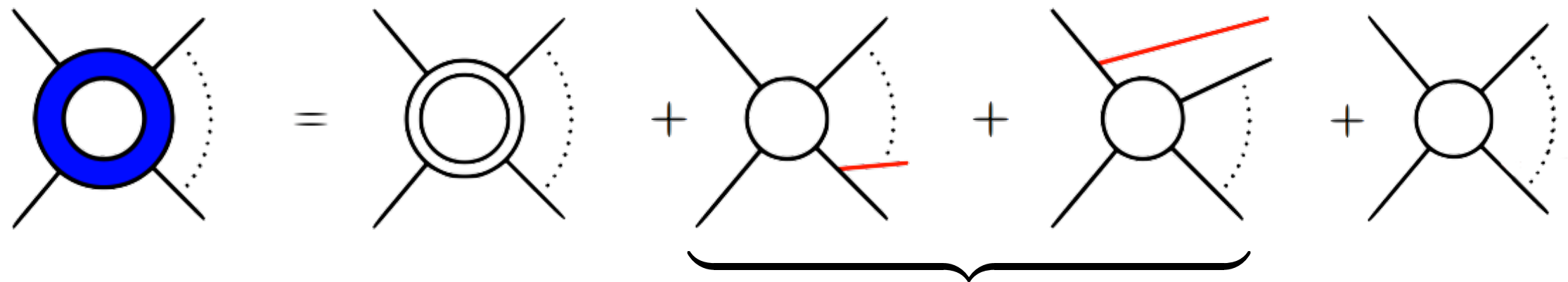


# Predictive MC (simplified) progress



# NLO Basics

NLO contributions have **three** parts



$$\sigma^{\text{NLO}} = \int_m d^{(d)} \sigma^V + \underbrace{\int_{m+1} d^{(d)} \sigma^R}_{\text{Real emission part}} + \int_m d^{(4)} \sigma^B$$

Virtual part

Real emission part

Born

- Loops have been for long the **bottleneck** of NLO computations
- Virtuals and Reals are each divergent and subtraction scheme need to be used (Dipoles, FKS, Antenna's)
- A lot of work is necessary for each computation

The cost of a new prediction at NLO used to exceed 100k€.



# New Loop techniques

For the calculation of one-loop matrix elements, several methods have been established and public tools released:

- Generalized Unitarity (ex. BlackHat, Rocket,...)

[Bern, Dixon, Dunbar, Kosower, hep-ph/9403226 + ....; Ellis, Giele, Kunszt 0708.2398, +Melnikov 0806.3467]

- Integrand Reduction (ex. CutTools, Samurai)

[Ossola, Papadopolulos, Pittau, hep-ph/0609007; del Aguila, Pittau, hep-ph/0404120; Mastrolia, Ossola, Reiter, Tramontano, 1006.0710]

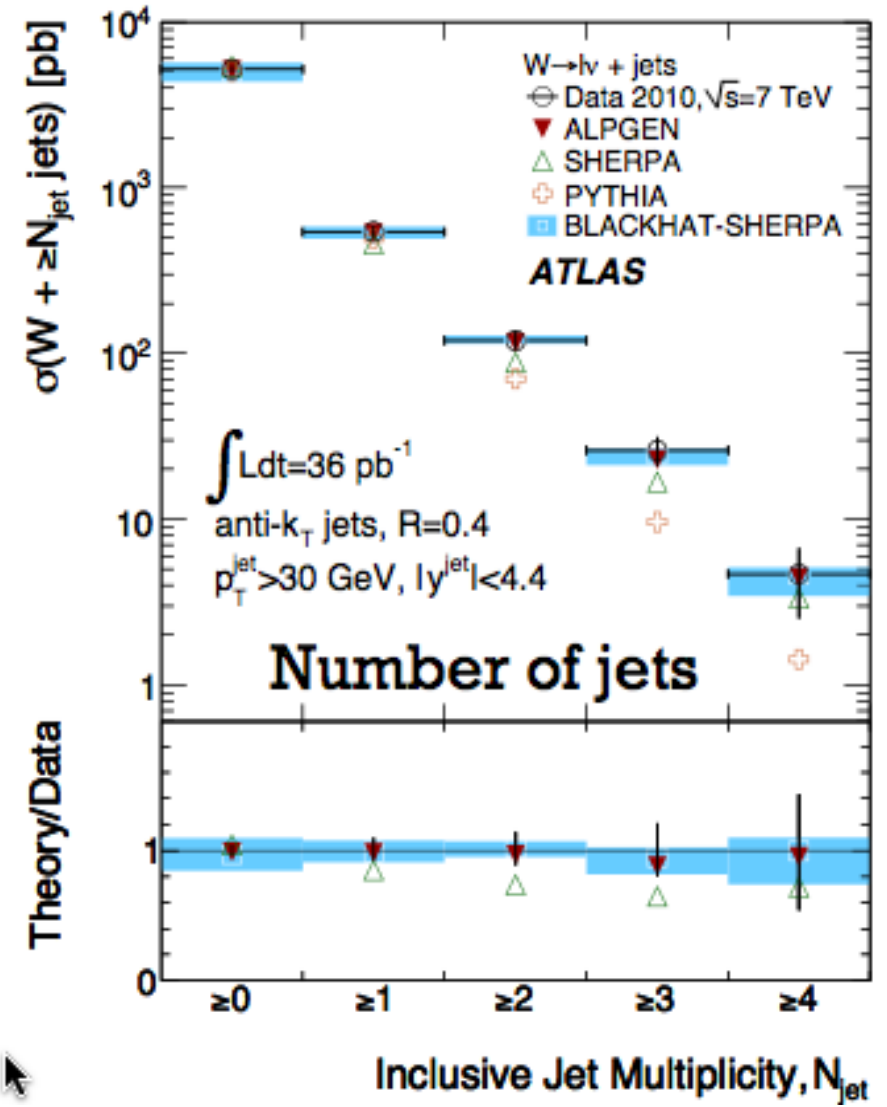
- Tensor Reduction (ex. Golem, GoSam, MadLoop)

[Passarino, Veltman, 1979; Denner, Dittmaier, hep-ph/0509141, Binoth, Guillet, Heinrich, Pilon, Reiter 0810.0092]



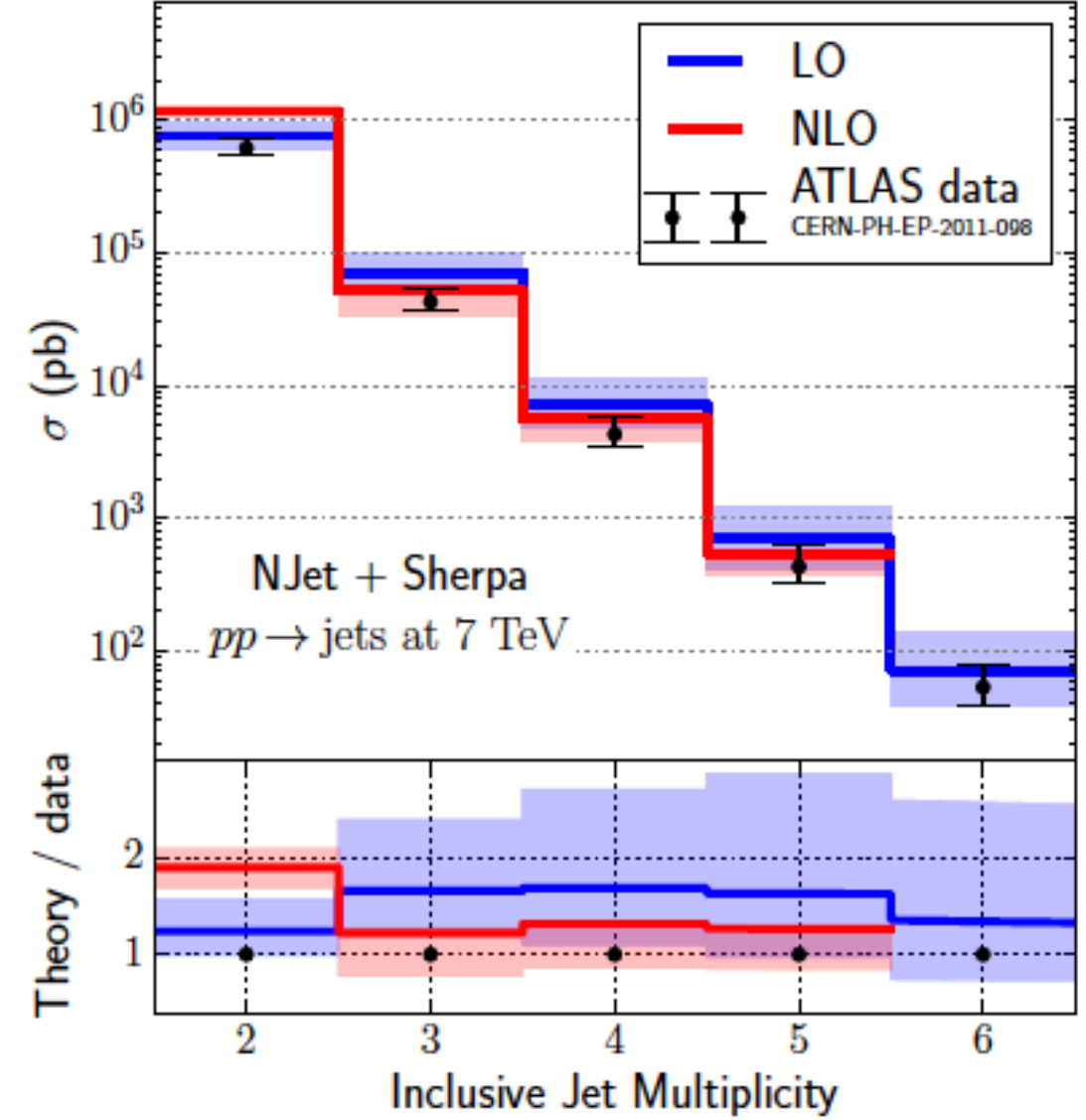
# The NLO Guinness World Records

$p p \rightarrow W + 5 \text{ jets}$



[Bern et al., 1304.1253]

$p p \rightarrow 5 \text{ jets}$



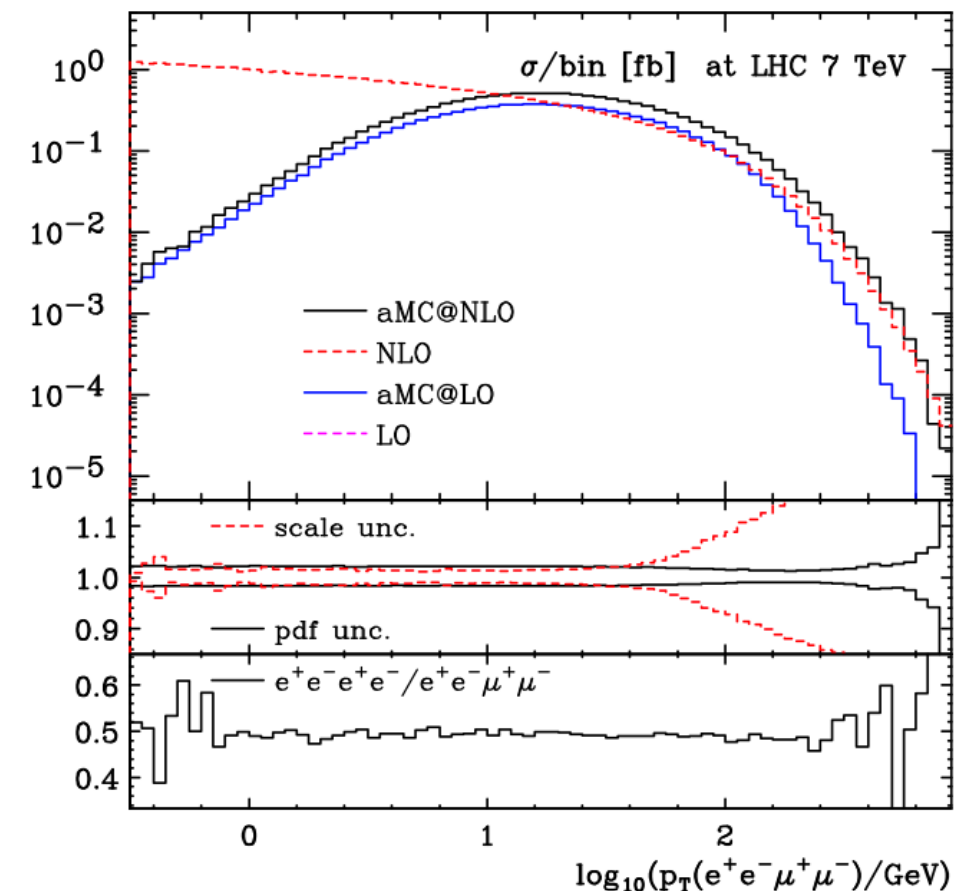
[Badger et al. 1309.6585]

# NLO+PS matching

Parton Shower Monte Carlo provide a simulation of all the stages of the hadronic collision: merge QCD matrix element + shower in the soft collinear approximation +hadronization model

The **MC@NLO** and **POWHEG** methods allow to combine NLO calculations with existing shower/hadronisation programs such as PYTHIA8, HERWIG++, SHERPA....

POWHEG and MC@NLO implementations have same formal accuracy but differ in the amount of radiation that is exponentiated.



The MC@NLO method has been extended to deal with samples of different jet multiplicity (merging) keeping NLO accuracy (FxFx in MG5aMC, ME@NLOPS in SHERPA)

The POWHEG method has been extended via the MINLO technique to obtain inclusive samples without merging scales.

# Automation of NLO+PS

- **MadGraph5\_aMC@NLO** Alwall, Frederix, Frixione, FM, Mattelaer, Shao, Stelzer, Torrielli, Zaro et al, 0908.4272, 1103.062, 1104.5613, 1110.4738, 1110.5502, 1304.7927, 1305.7088, 1306.6464, 1311.1829, 1401.7340, 1405.0301, 1407.5089, 1409.5301, 1504.00611, 1507.05640, 1507.02549, 1508.05327...

Fully automatic framework, where all the elements of a NLO+PS computation in the SM and (BSM) are automatically generated.

- **POWHEG-BOX** and applications: Alioli, Nason, Oleari, Re et al, 1002.2581, 1009.2450, 1009.5594, 1012.3380, 1102.4846, 1105.4488, 1107.5051, 1108.0909, 1310.4491, 1306.2442, 1311.1365, 1402.4001:

Framework which allows to promote a standard NLO calculation into a MC at NLO generator. Very popular choice. More than ~30 processes implemented. Similar in spirit to MCFM.

- **SHERPA** Hoeche et al, 1008.5399, 1009.1127, 1111.1220, 1402.6293, 1403.7516

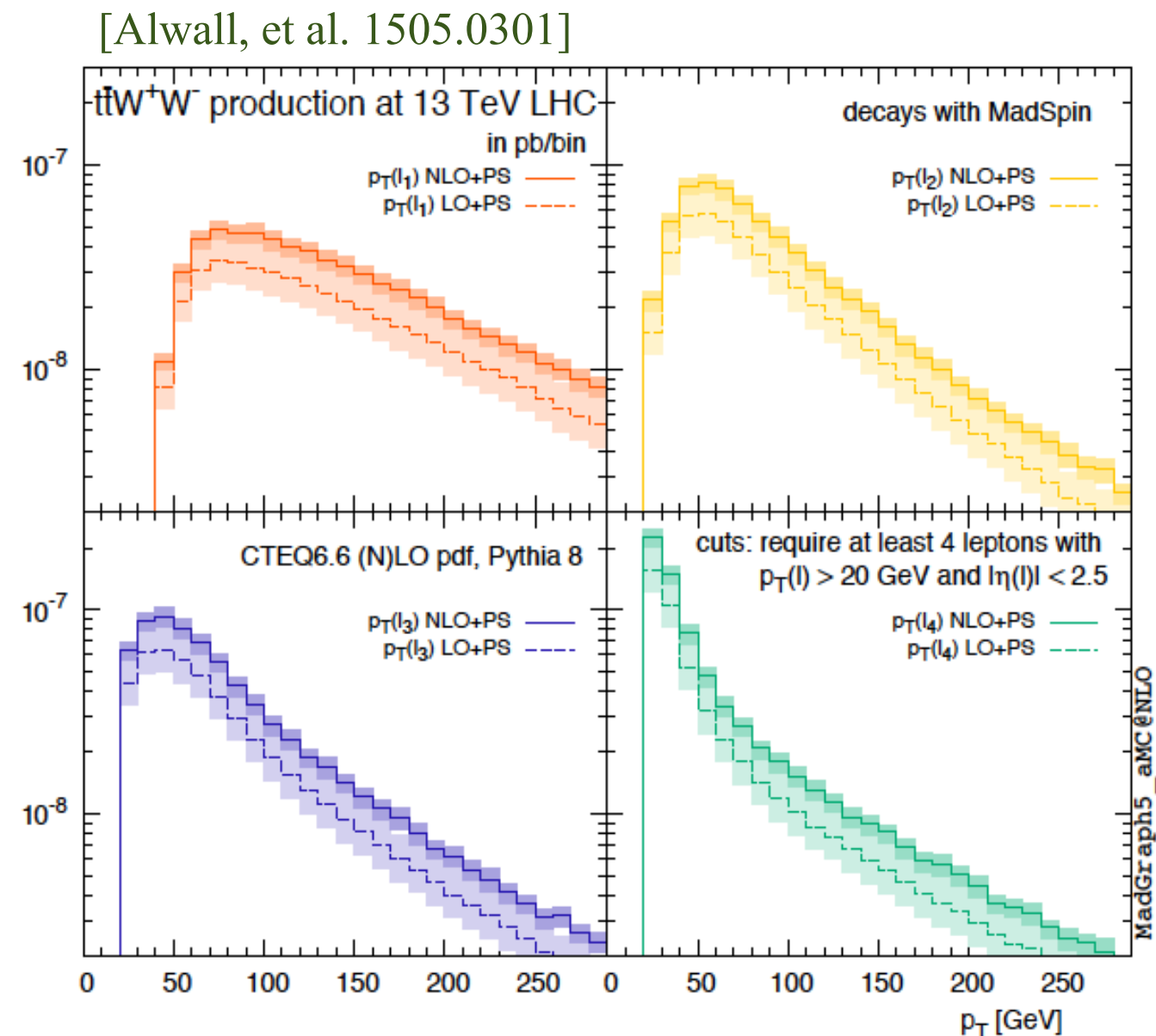
Flexible framework having both MC@NLO and POWHEG methods based on CS dipoles, needs virtuals. Fully automatic except for virtuals which are taken from BlackHAT, OpenLoops, GoSam..

# NLO+PS Automation

For example, the level of automation in MadGraph5\_aMC@NLO is as follows:

```
./bin/mg5_aMC  
> generate p p > t t~ W+ W- [QCD]  
> output ttww  
> launch
```

Uncertainties from scale variation and pdfs are automatically computed (at no extra cost) and associated to each of the unweighted events (=any distribution will have the corresponding uncertainty band). Short-distance events ready to be “dressed” by PS and hadronisation.



Virtually unlimited set of LHC processes available at NLO

# NLO+PS Automation

The same level of automation is being achieved for BSM:

[Degrande, Fuks, Hirschi, Proudome, Shao, 1412.5589, 1509.XXXX]

```

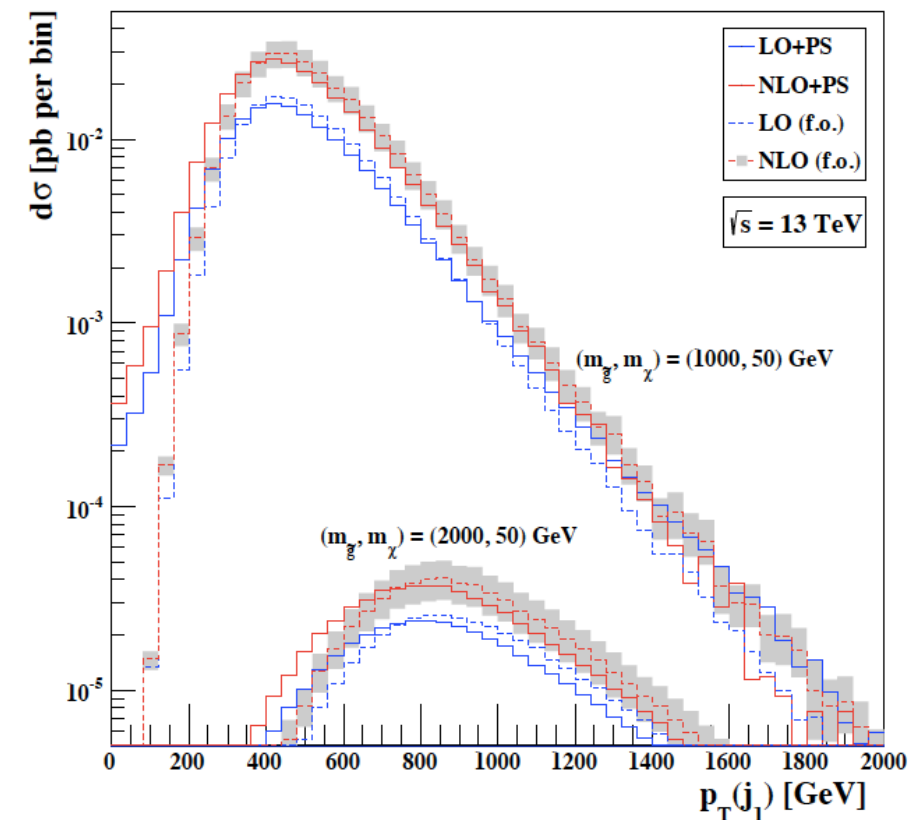
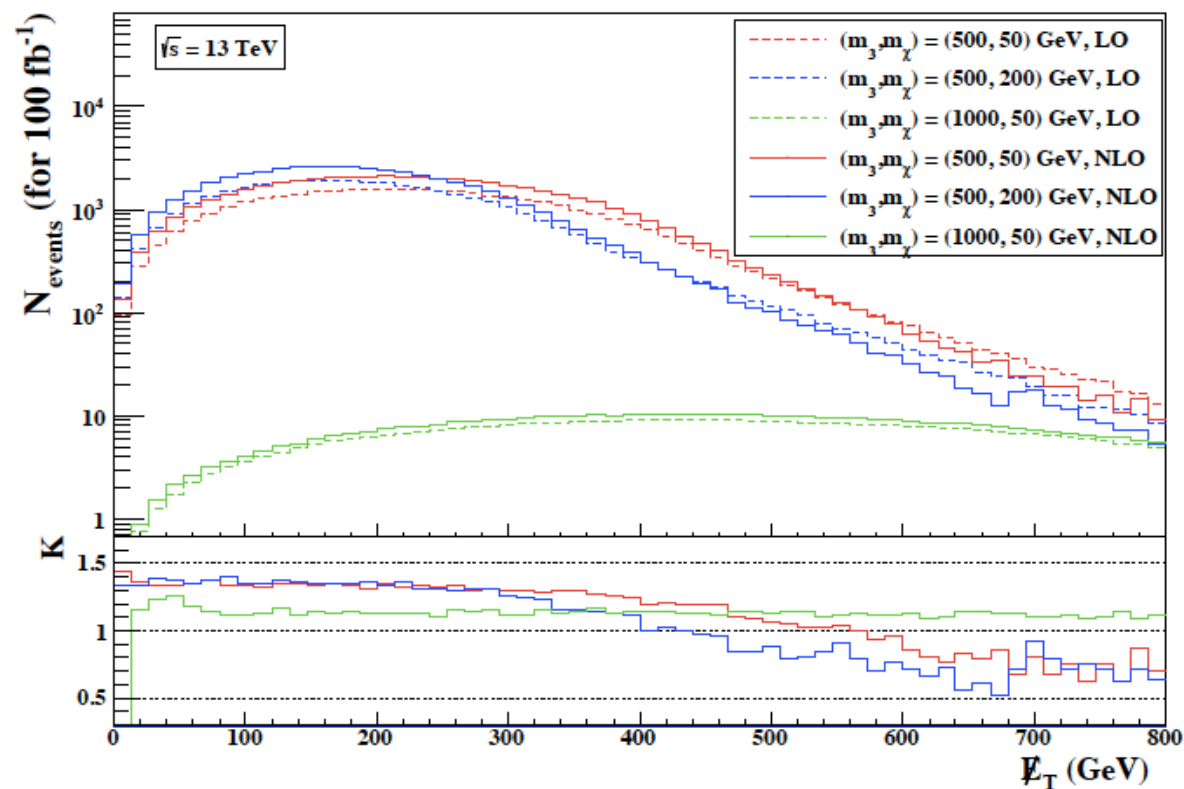
./bin/mg5_aMC
> import model SUSYQCD
> generate p p > t1 t1~ [QCD]
> output StopPair
> launch

```

```

./bin/mg5_aMC
> import model SUSYQCD
> generate p p > g1 g1 [QCD]
> output GluinoPair
> launch

```



# NLO+PS Automation

The same level of automation is being achieved for EFT's:

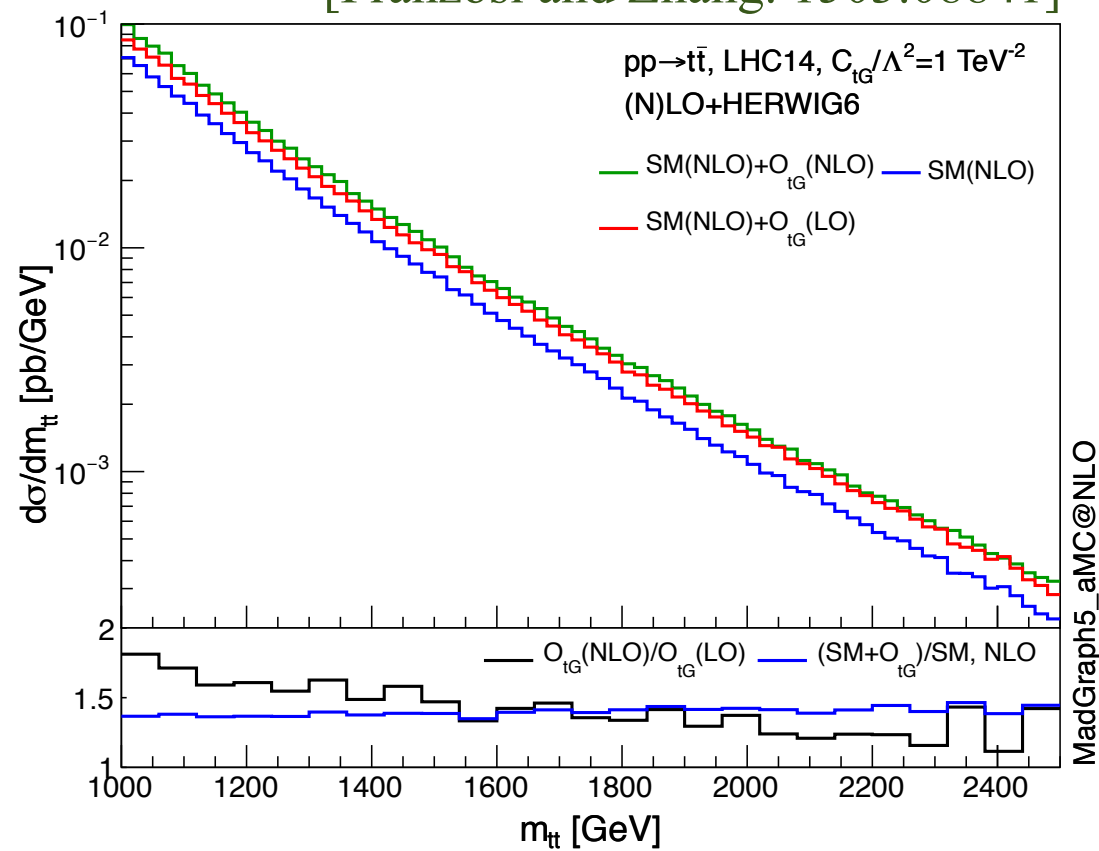
```

./bin/mg5_aMC
> import model TopEFT
> generate p p > t t~ , NP=1 [QCD]
> output Chromott
> launch
  
```

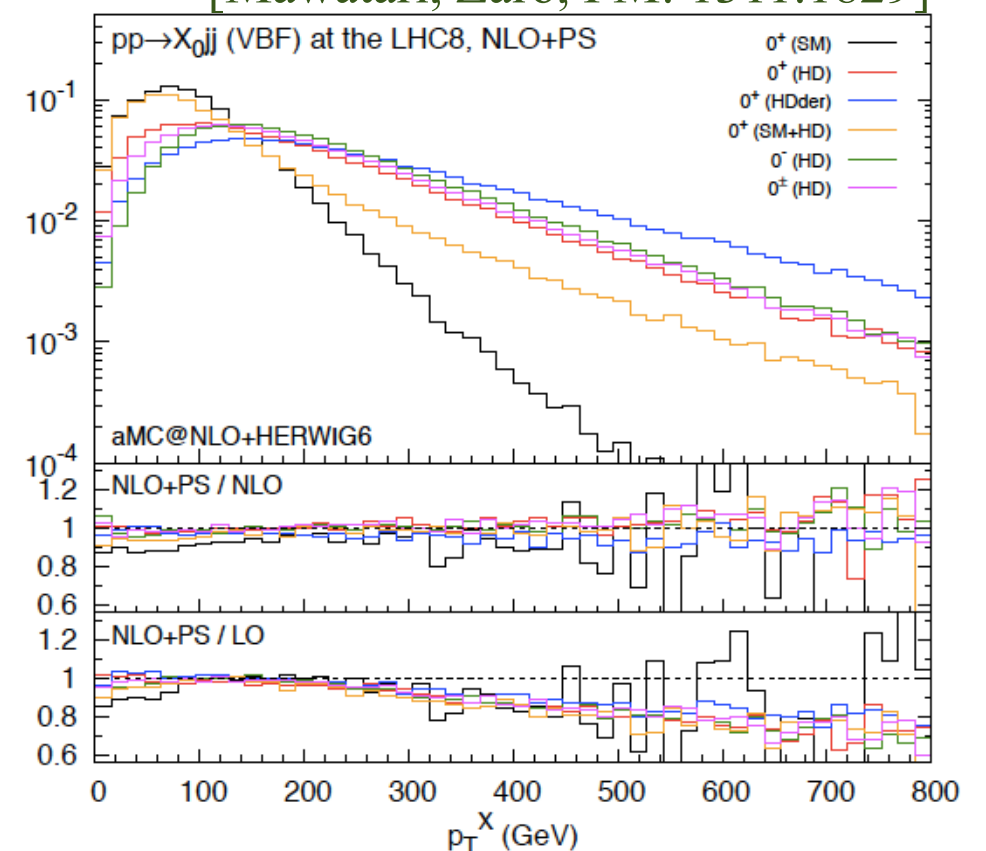
```

./bin/mg5_aMC
> import model HC
> generate p p > X0 j j [QCD]
> output VBFdim6
> launch
  
```

[Franzosi and Zhang. 1503.08841]



[Mawatari, Zaro, FM: 1311.1829]





# The NNLO era

NNLO calculations important at least for the following cases:

1) Benchmark processes measured with high precision	$e^+e^- \rightarrow 3 \text{ jets}$	✓
	$pp \rightarrow W, Z$	✓
	$pp \rightarrow 2 \text{ jets}$	partial
	$pp \rightarrow t \bar{t}$	✓
2) Processes with large NLO corrections (eg, new channels)	$pp \rightarrow H \text{ (EFT)}$	✓
	$pp \rightarrow H + \text{jet (EFT)}$	✓
	$pp \rightarrow HH \text{ (EFT)}$	✓
3) Important/Irreducible backgrounds for Higgs or NP searches	$pp \rightarrow t \bar{t}$	✓
	$pp \rightarrow VV' (W, \gamma, Z)$	✓
	$pp \rightarrow W/Z j$	✓

In addition it is essential to provide codes that are able to deal with final state selections (at the parton level) so that fiducial cross sections and distributions can be directly compared with data.

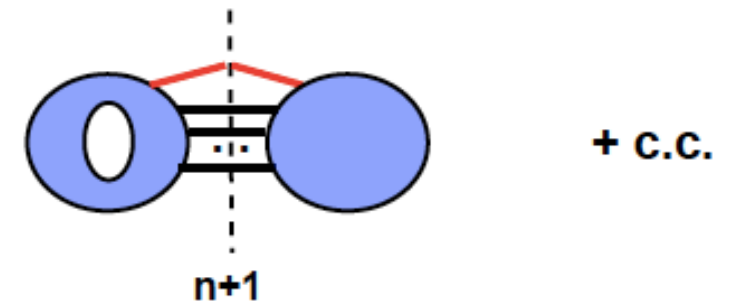
MGrazzini®

# Ingredients of NNLO calculations

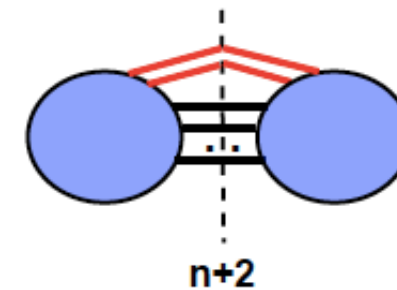
Double virtual contribution with  $n$  resolved partons



Real-virtual contribution with 1 unresolved parton



Double-real contribution with 2 unresolved partons



Each of the three contributions is divergent, yet the sum is finite (KLN theorem).  
How to deal with IR singularities ?



# NNLO methods

There are two main approaches available in the literature:

## 1. Organise the calculation from scratch so as to cancel all the singularities

- sector decomposition
- antenna subtraction
- “colourful” subtraction
- joint use of subtraction and sector decomposition

T. Binoth, G.Heinrich (2000,2004)  
C.Anastasiou, K.Melnikov, F.Petriello (2004)  
A. & T. Gehrmann, N. Glover (2005)  
G, Somogyi, Z. Trocsanyi, V. Del Duca (2005, 2007)  
M.Czakon (2010,2011)\$  
R.Boughezal, K.Melnikov, F.Petriello (2011)

## 2. Start from an inclusive NNLO calculation and combine it with an NLO calculation for $n+1$ parton process

- $q_T$  subtraction
- “N-jettiness” method
- “Born projection” method for VBF

S.Catani, M.Grazzini (2007)  
R.Boughezal, C.Focke,X.Liu, F.Petriello (2015)  
F.Tackmann et al. (2015)  
M.Cacciari, F.Dreyer, A.Karlberg, G.Salam,G.Zanderighi (2015)

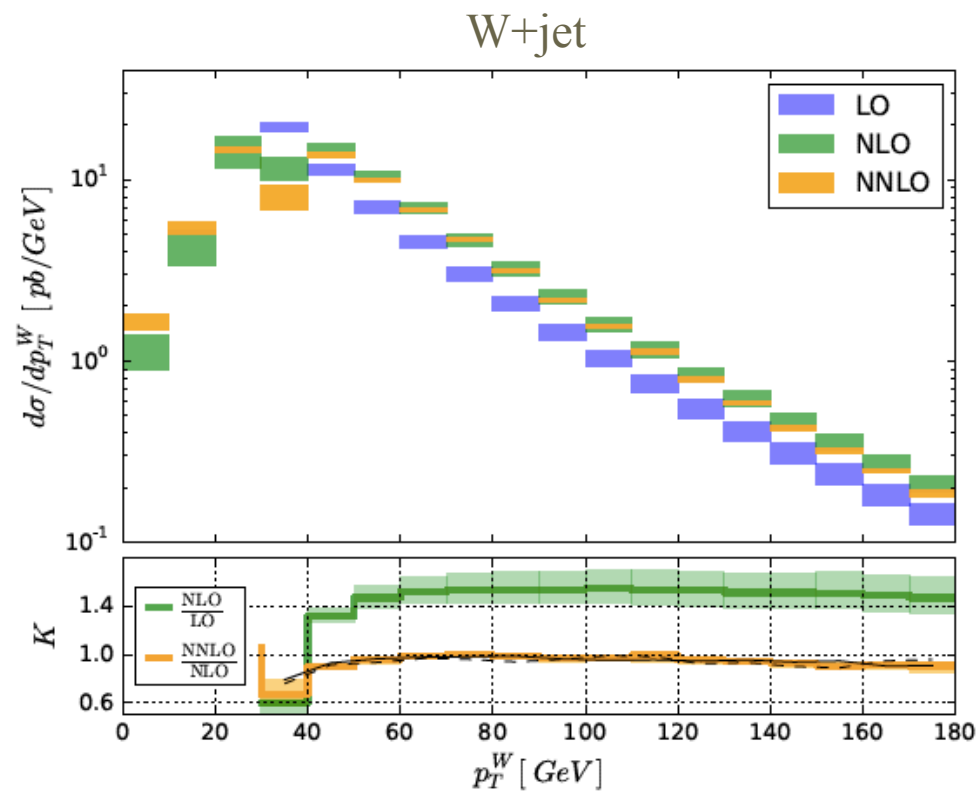
...and then of course the (sometimes extremely hard) two-loop amplitudes !

C.Anastasiou, F.Caola, M.Czakon, T.Gehrmann, N.Glover, M.Jaquier, A. Koukoutsakis  
C.Oleari, K.Melnikov, L.Tancredi, M.E. Tejeda-Yeomans, A. von Manteuffel and many others

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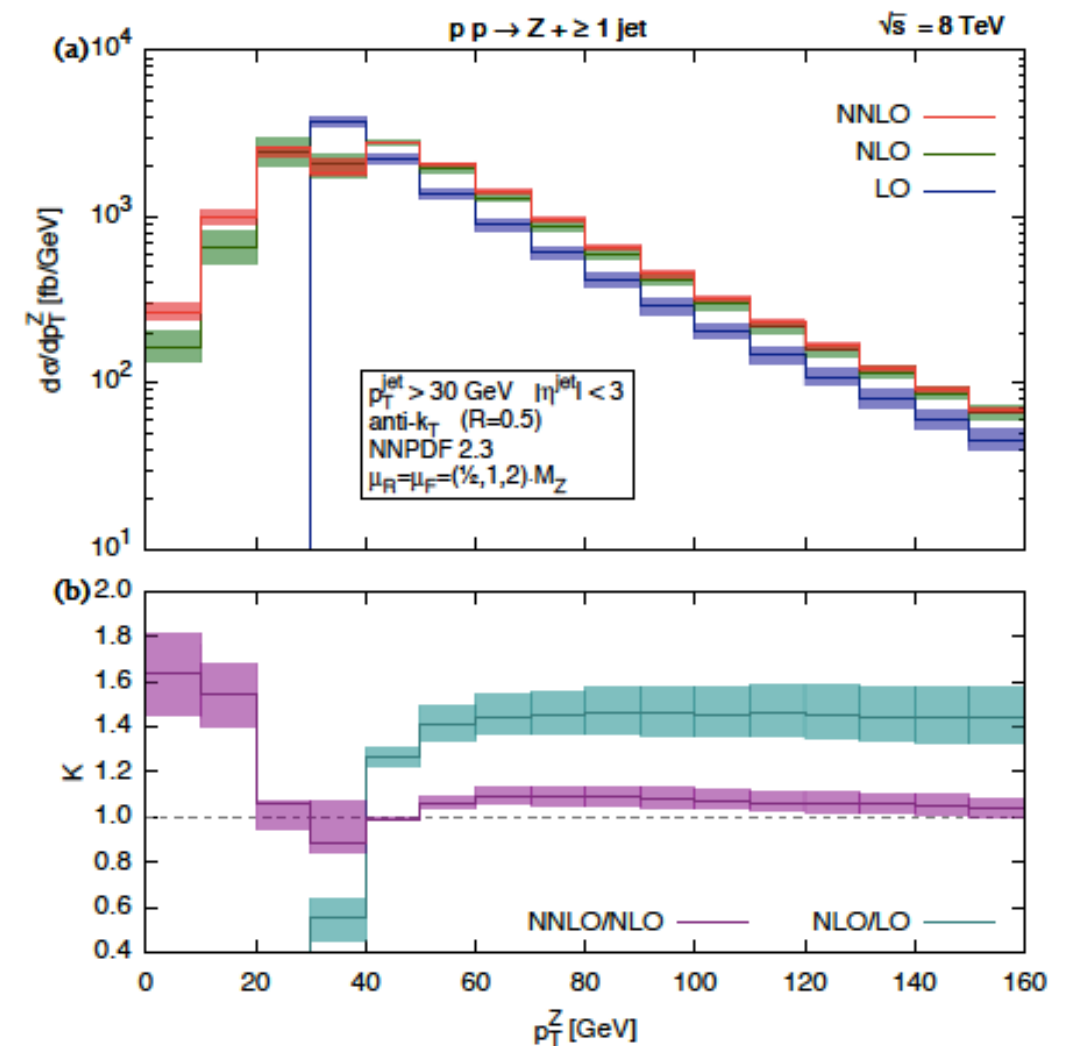
# V+jet at NNLO

[R.Boughezal, C.Focke, X.Liu, F.Petriello (2015)]



Small NNLO effect and significant reduction of scale uncertainties. First application of new “N-jettiness” method: relatively flat NNLO correction.

[A and T. Gehrmann, N. Glover, T.Morgan, A.Huss (2015)]

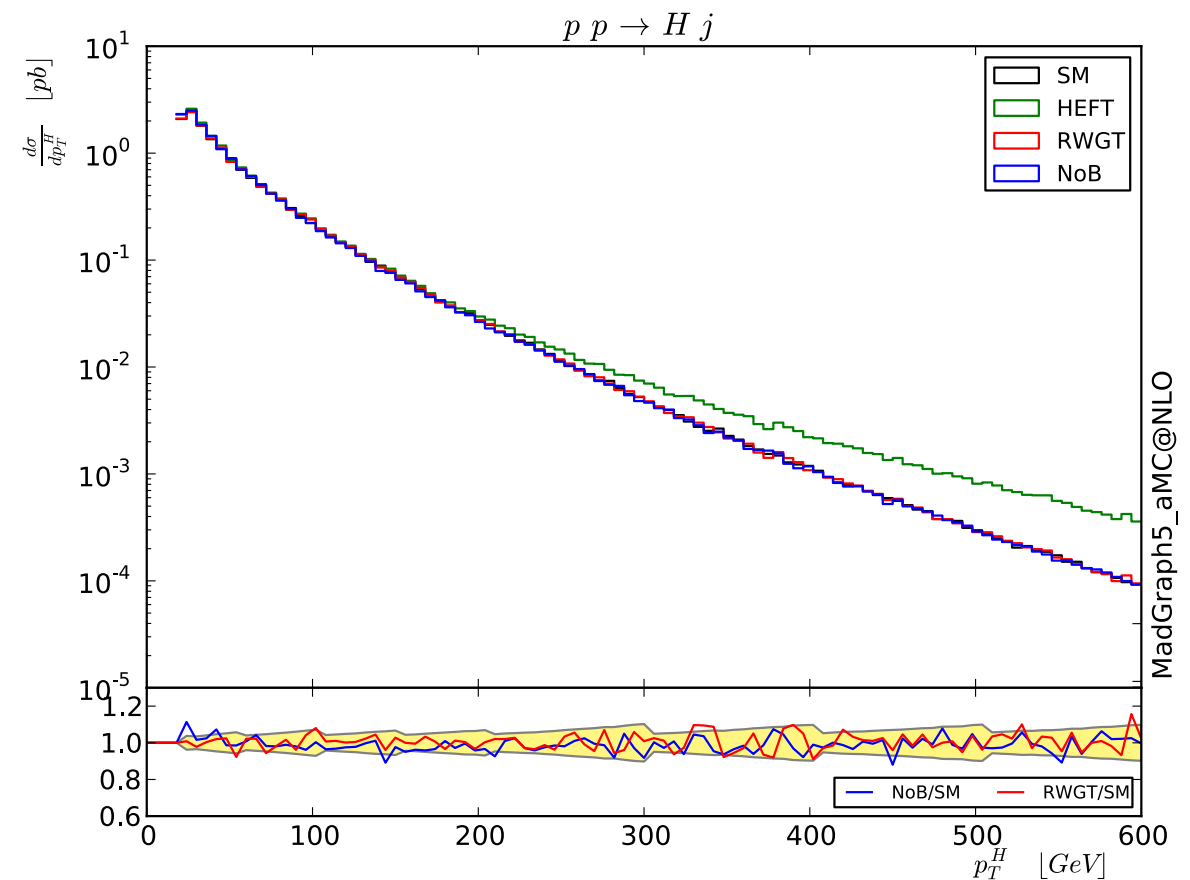
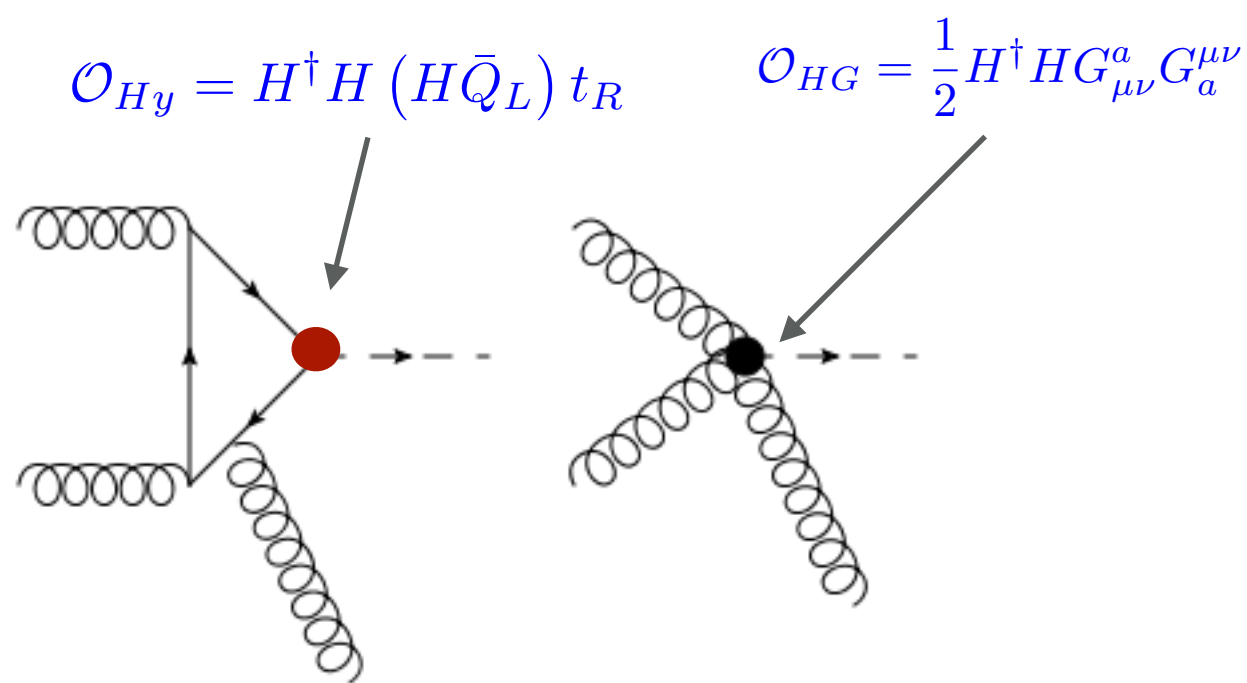


Similar effects for Z+jet: antenna subtraction (large  $N_c$  approximation for the dominant channels)

# H+jet

From a global fit the coupling of the higgs to the top is poorly determined: the loop could still be dominated by np.

[Grojean et al., 2013][Banfi et al. 2014] [Buschmann, et al. 2014]



EFT at NLO predictions available, yet SM NLO predictions are needed to control accuracy and precision. NLO prediction for H+1jet with top loops not yet available.

# H+jet at NNLO (in the EFT)

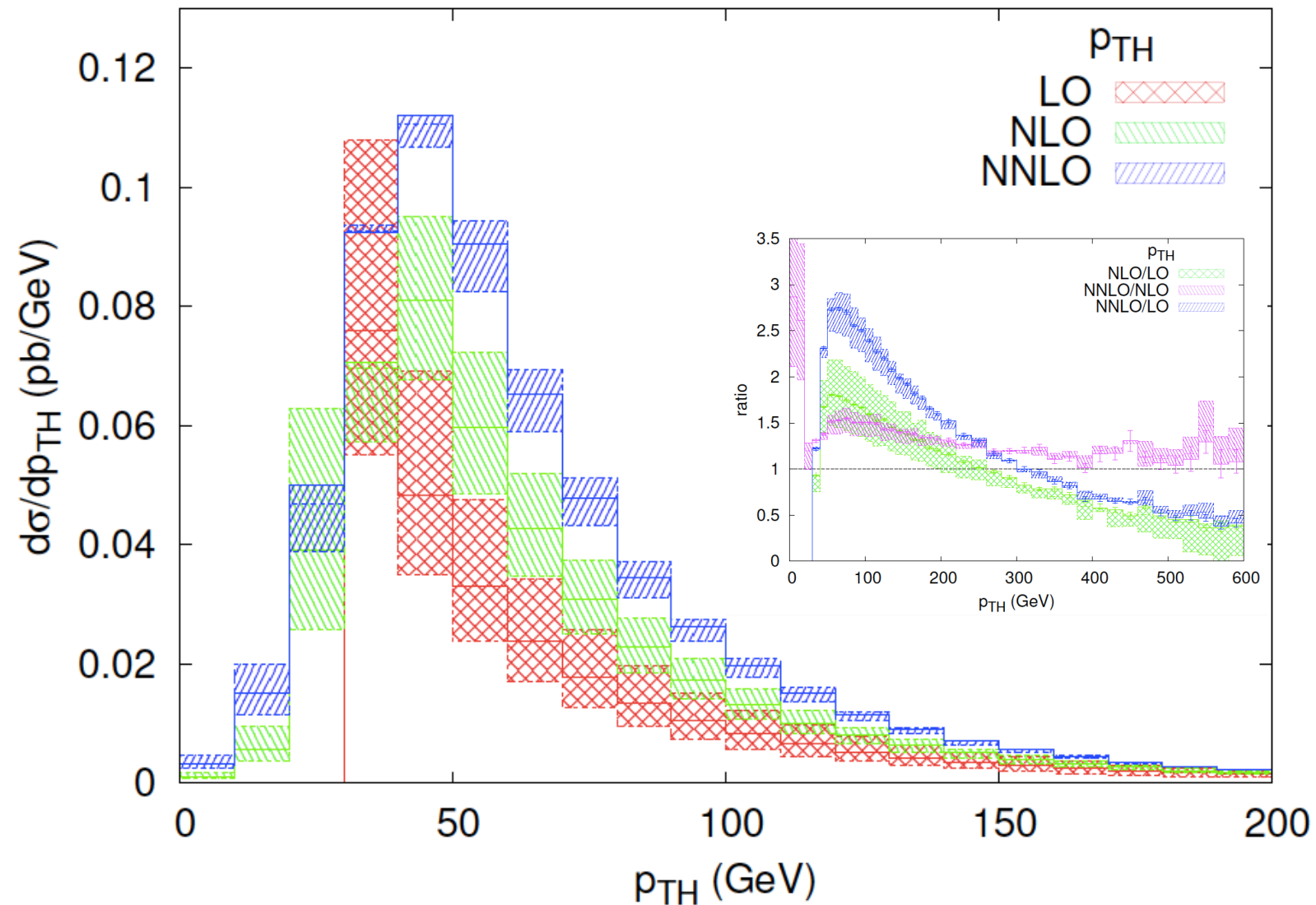
NNLO calculation carried out with three independent methods (antenna subtraction, subtraction+sector, N-jettiness)

X. Chen, T. Gehrmann, N. Glover, M. Jaquier (2014)

R. Boughezal, F. Caola, K. Melnikov, F. Petriello, M. Schulze (2015)

R. Boughezal, C. Focke, W. Giele, X. Liu, F. Petriello (2015)

Quantitative effect smaller than previously anticipated from gg only: at the 20% level ( $\mu = m_H$ )



# VBF at NNLO

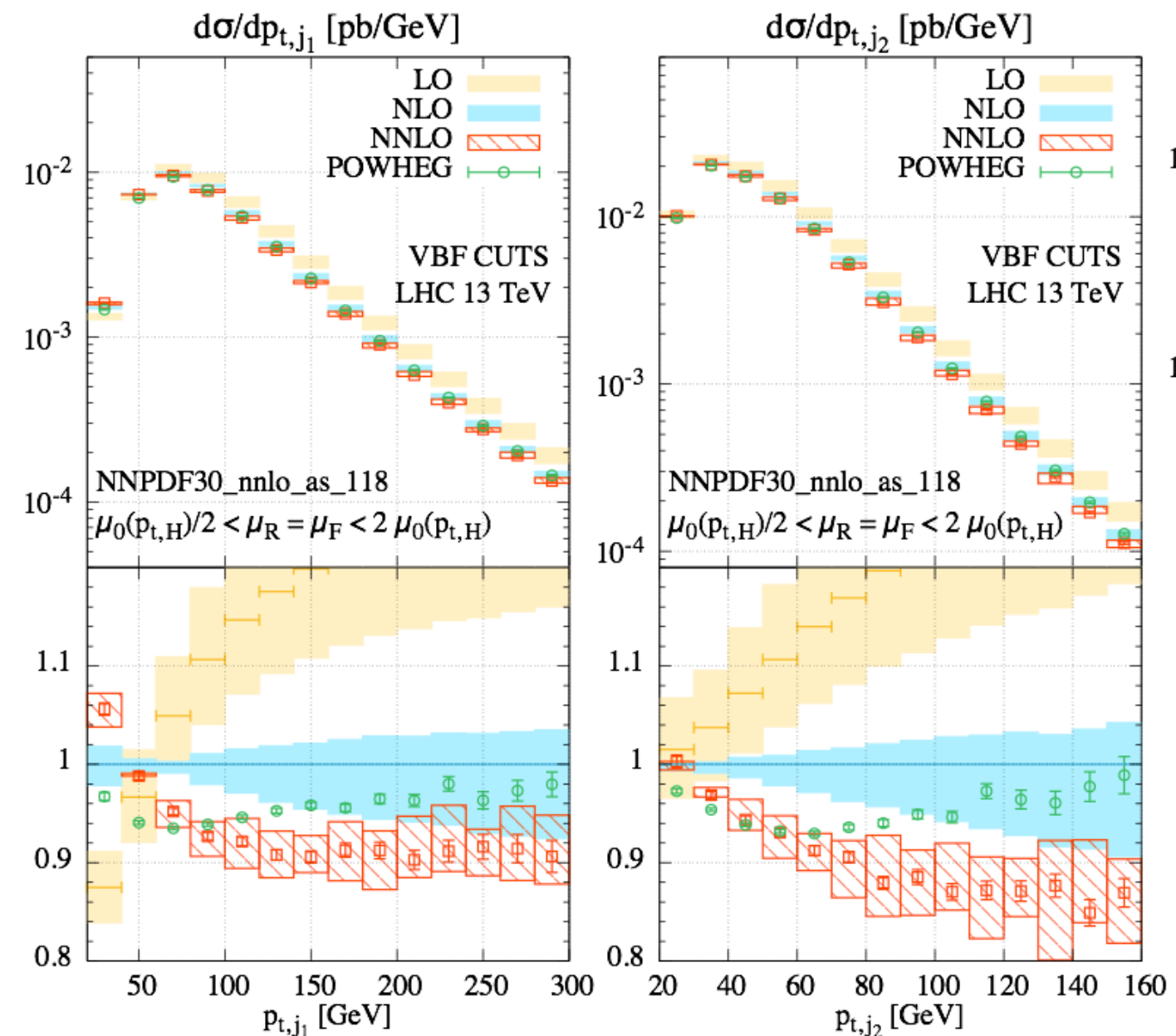
Vector boson fusion (VBF) is an important production channel for the Higgs boson: distinctive signature with little hadronic activity in the central rapidity region.

Fully inclusive NNLO corrections known since quite some time [P.Bolzoni, F.M,S.Moch,M.Zaro (2010)] in the structure function approach:  $O(1\%)$  effect.

Fully exclusive NNLO computation recently completed (still neglecting color exchanges between quark lines) [M.Cacciari, F.Dreyer, A.Karlberg, G.Salam,G.Zanderighi (2015)]

NNLO corrections make  $p_T$  spectra softer  
larger impact when VBF cuts are applied

	$\sigma^{(\text{no cuts})}$ [pb]	$\sigma^{(\text{VBF cuts})}$ [pb]
LO	$4.032^{+0.057}_{-0.069}$	$0.957^{+0.066}_{-0.059}$
NLO	$3.929^{+0.024}_{-0.023}$	$0.876^{+0.008}_{-0.018}$
NNLO	$3.888^{+0.016}_{-0.012}$	$0.826^{+0.013}_{-0.014}$





# $t\bar{t}$ cross section at NNLO

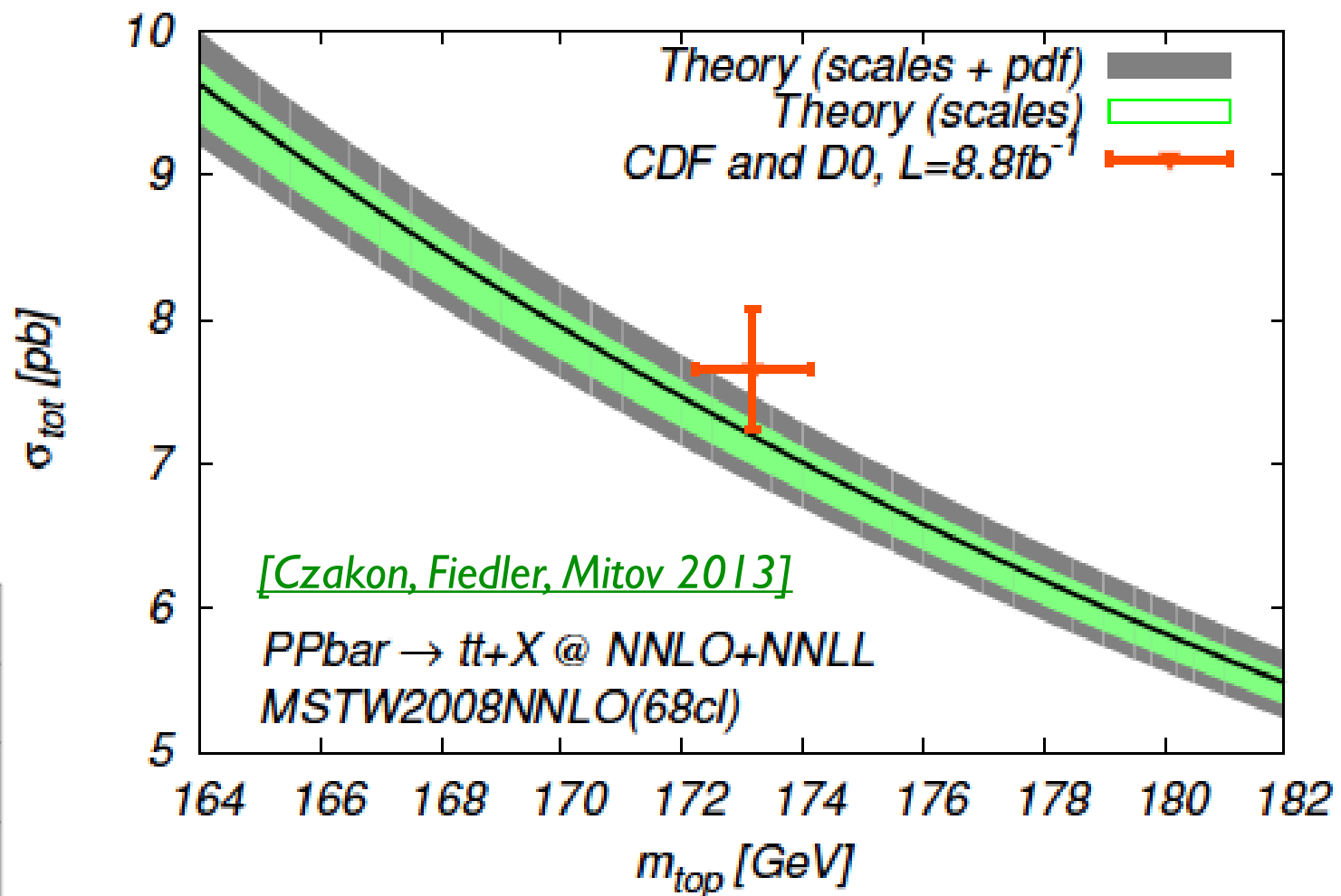
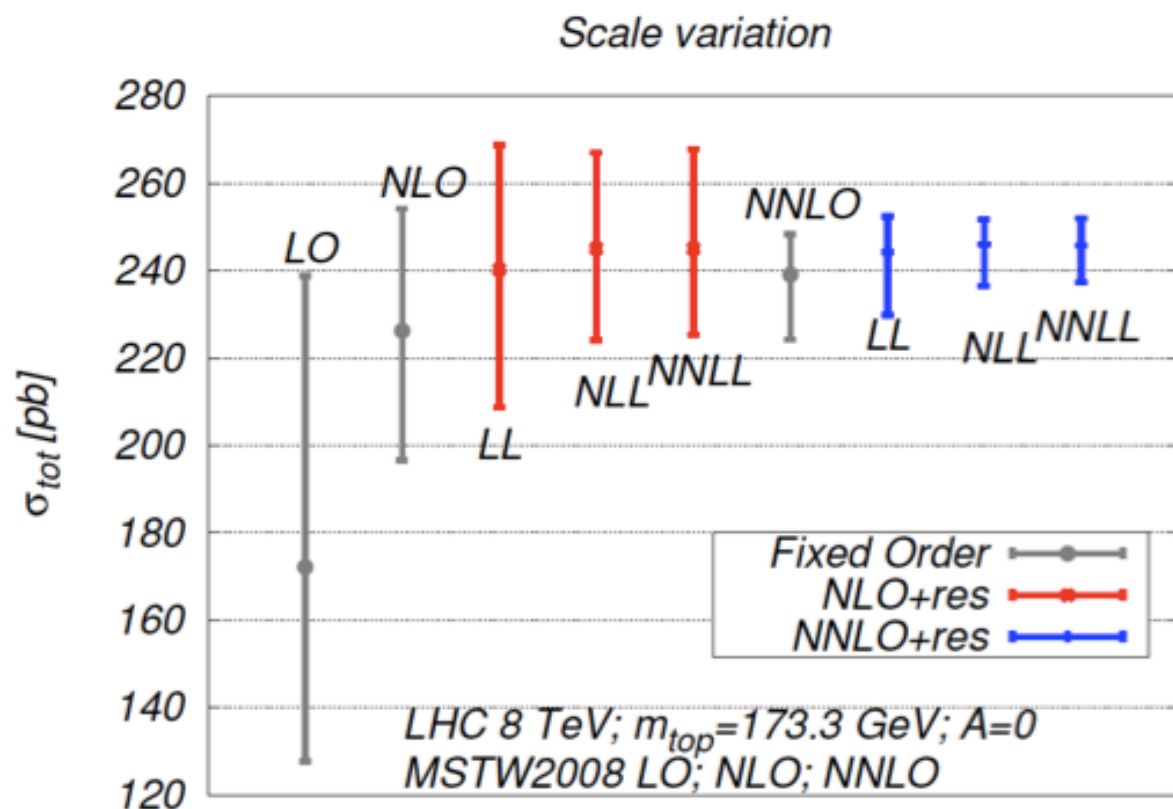
Monumental MILESTONE in perturbative QCD:

[[Bärnreuther, Czakon, Mitov 2012](#)]

[[Czakon, Mitov 2012](#)]

[[Czakon, Mitov 2012](#)]

[[Czakon, Fiedler, Mitov 2013](#)]



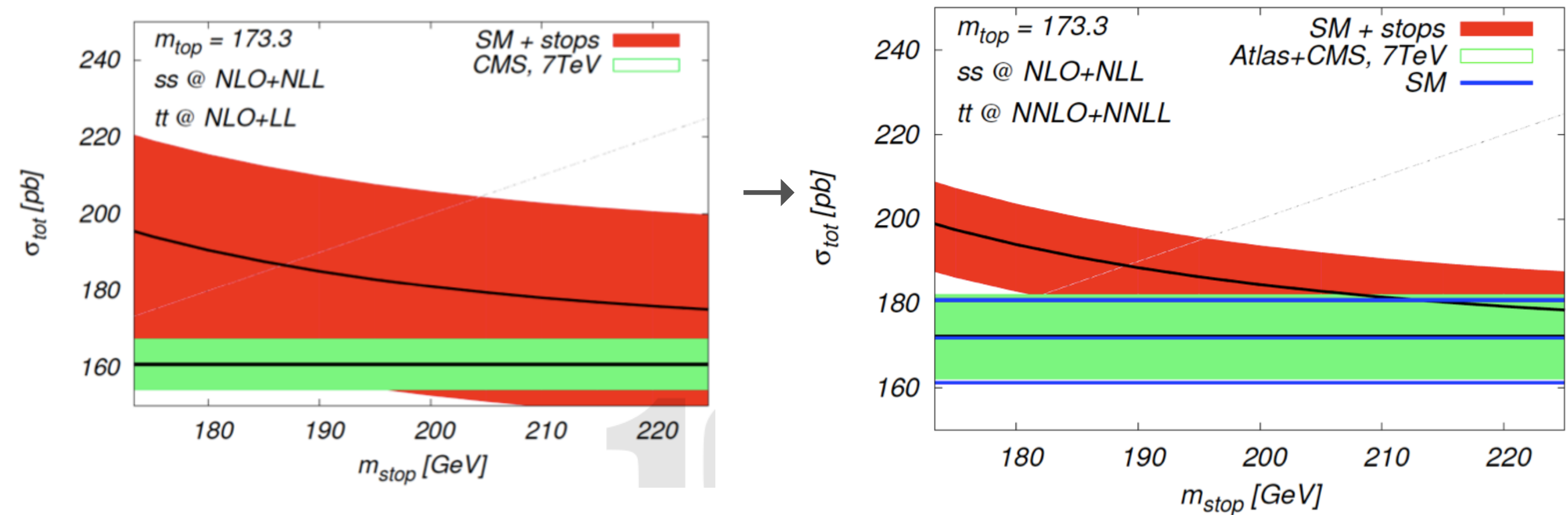
- Two loop hard matching coefficient extracted and included
- Very weak dependence on unknown parameters (sub 1%): gg NNLO,  $A$ , etc.
- $\sim 50\%$  scales reduction compared to the NLO+NNLL analysis

# $t\bar{t}$ cross section at NNLO

Having a NNLO prediction opens the door to new possibilities.

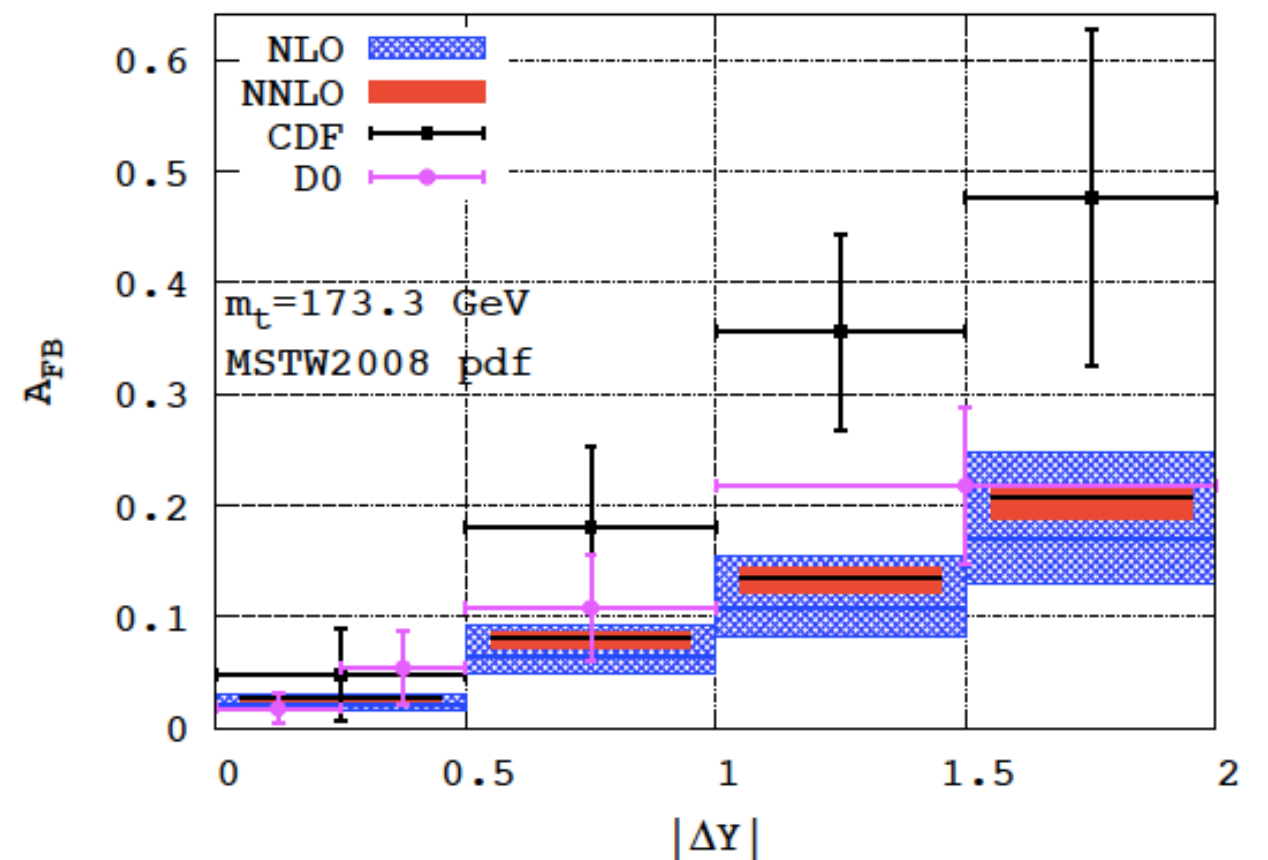
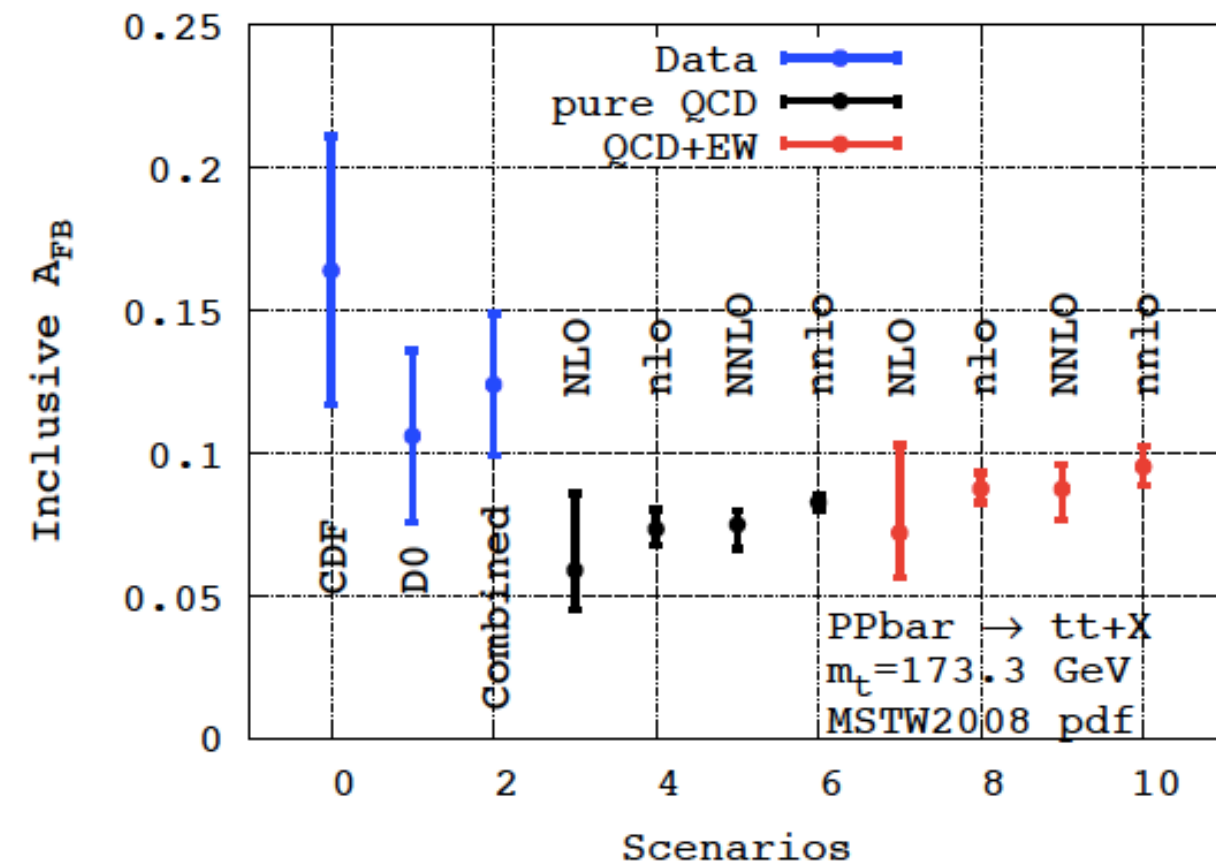
Consider the light stop window in a compressed spectrum, that mimicks the normal  $t\bar{t}b\bar{a}$  production:

[\[Czakon, Mitov, Papucci, Ruderman, Weiler, 2014\]](#)



# $t\bar{t}$ forward-backward asymmetry

[Czakon, Fiedler, Mitov, 2014]



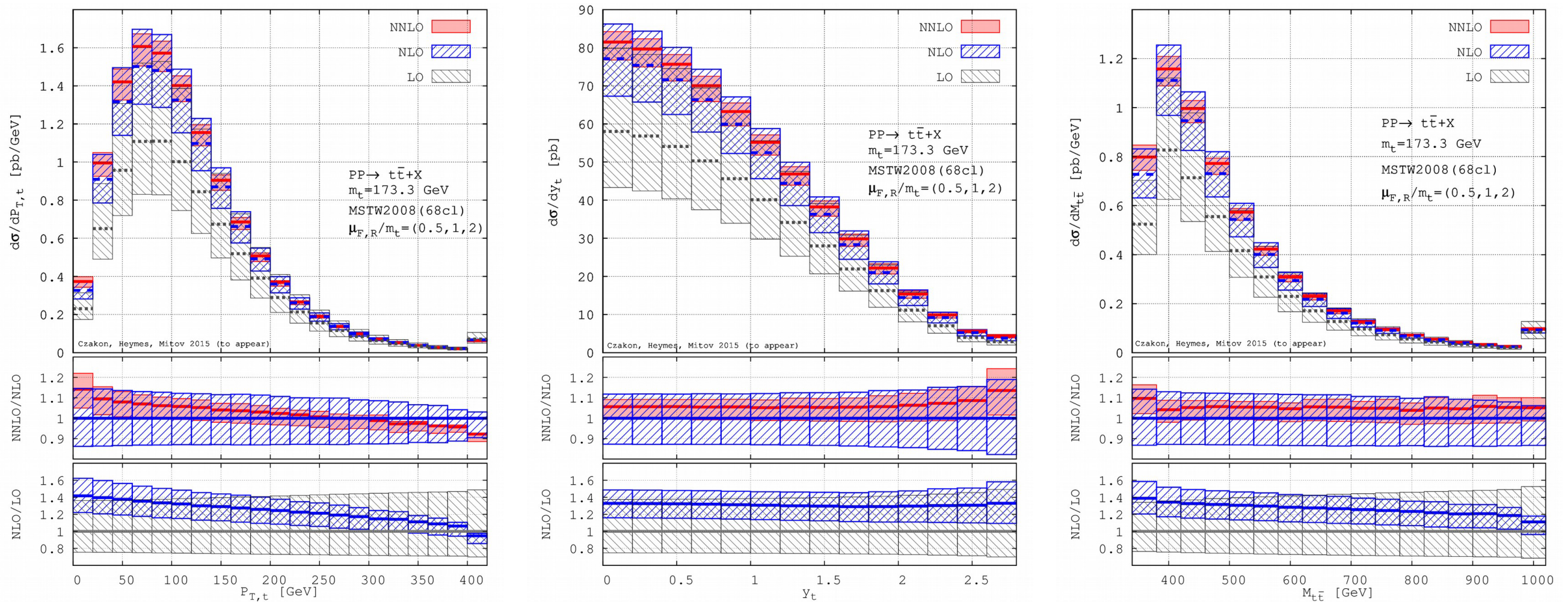
The asymmetry at NLO accuracy (from the NNLO total cross section calculation) is sizeably larger and much more precise than the LO result.



# $t\bar{t}$ at NNLO : differential distributions

The first differential distributions at NNLO for the  $p_T$  (top),  $y$ (top),  $m(t\bar{t})$ :

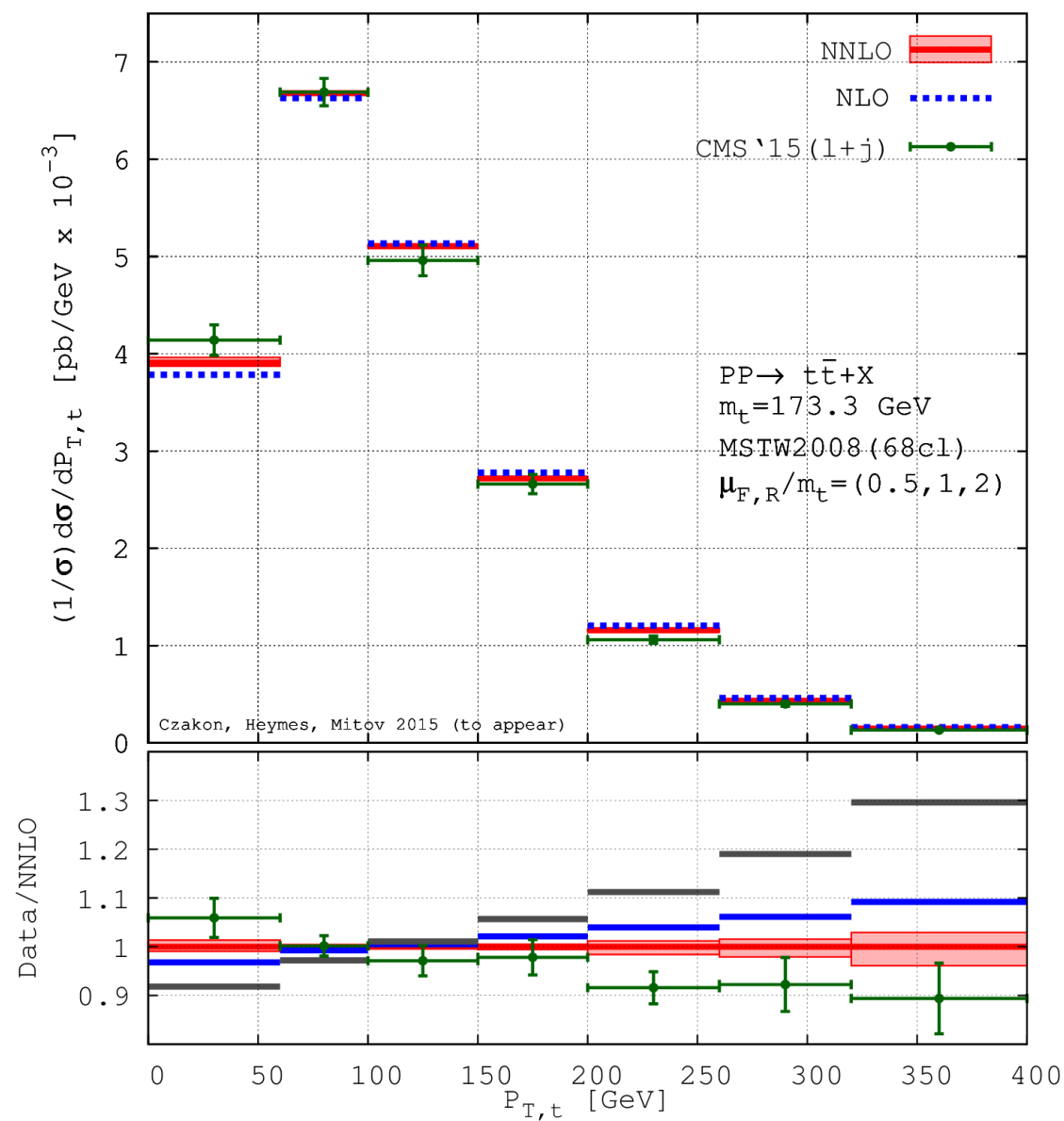
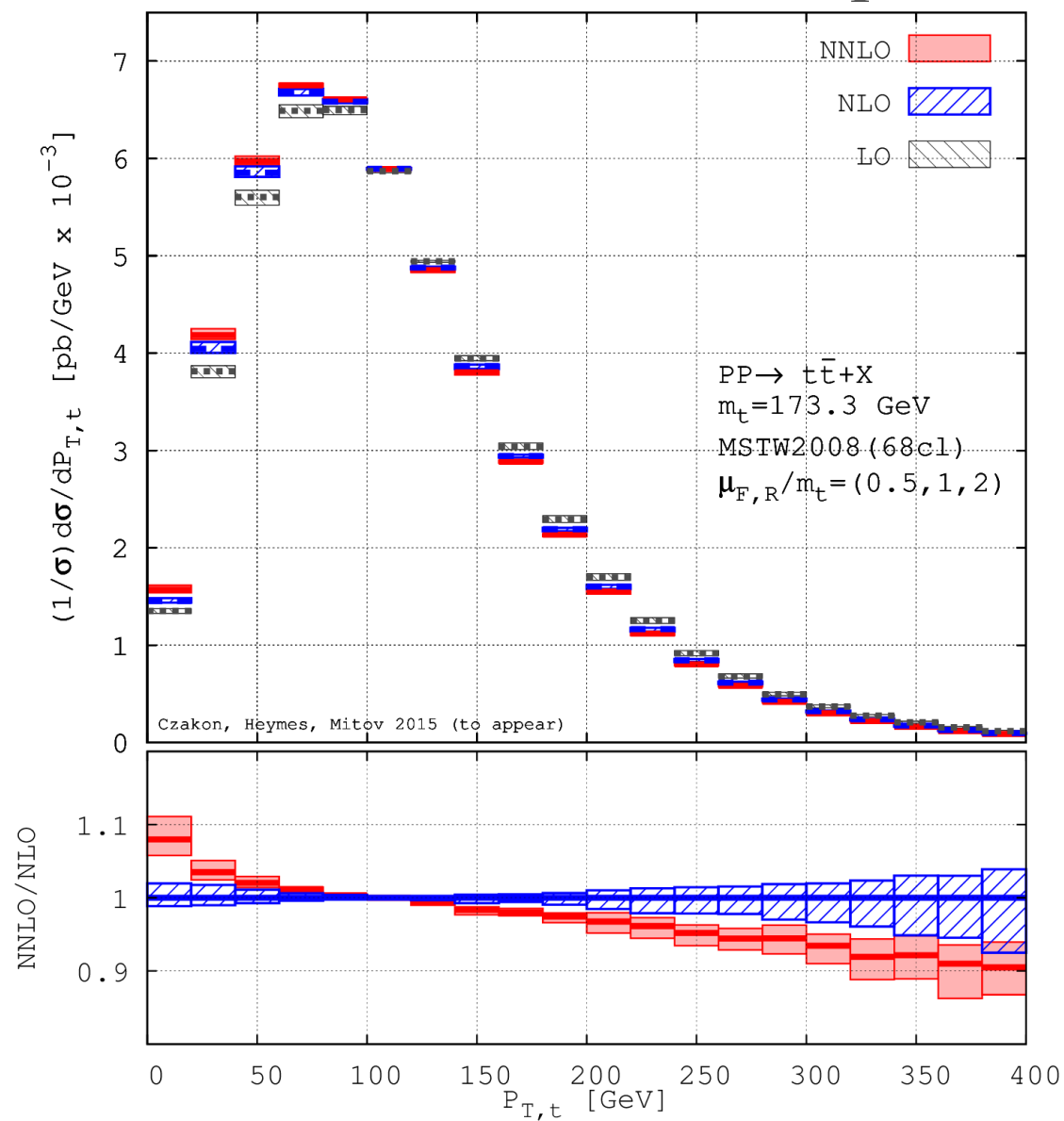
[Czakon, Fiedler, Heymes, Mitov.; in preparation]



Good perturbative convergence. Improved precision.

# $t\bar{t}$ at NNLO : differential distributions

For the first time the issue of “a softer than NLO”  $p_T$  (top) has been seen in data can be studied. NNLO predictions seem to go in the direction of data.



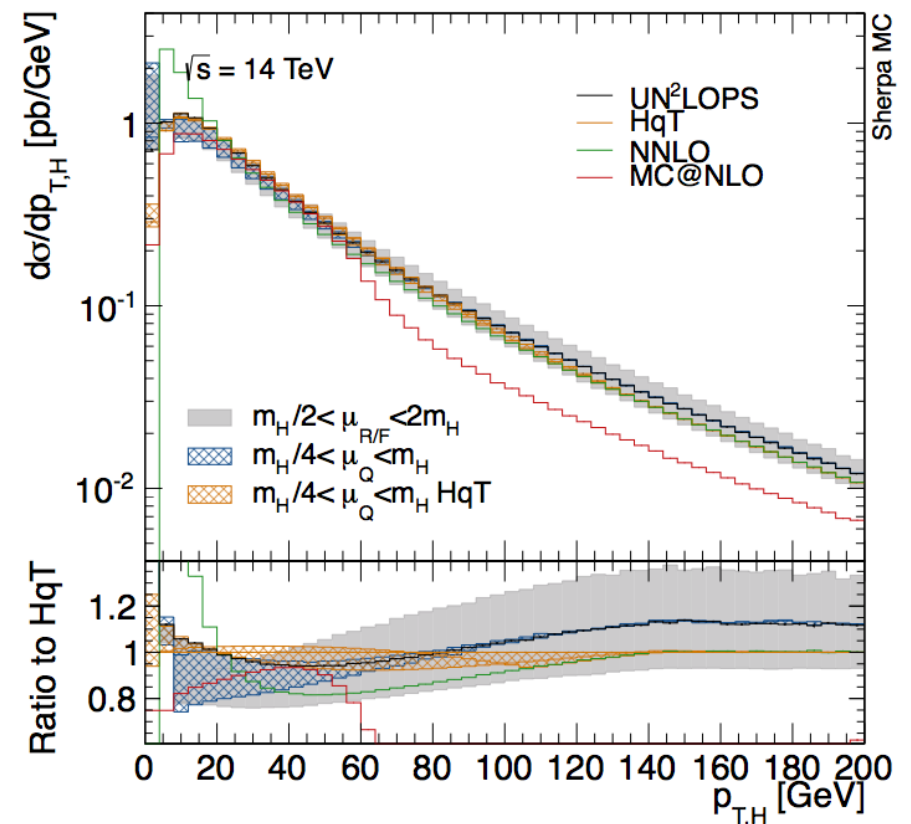
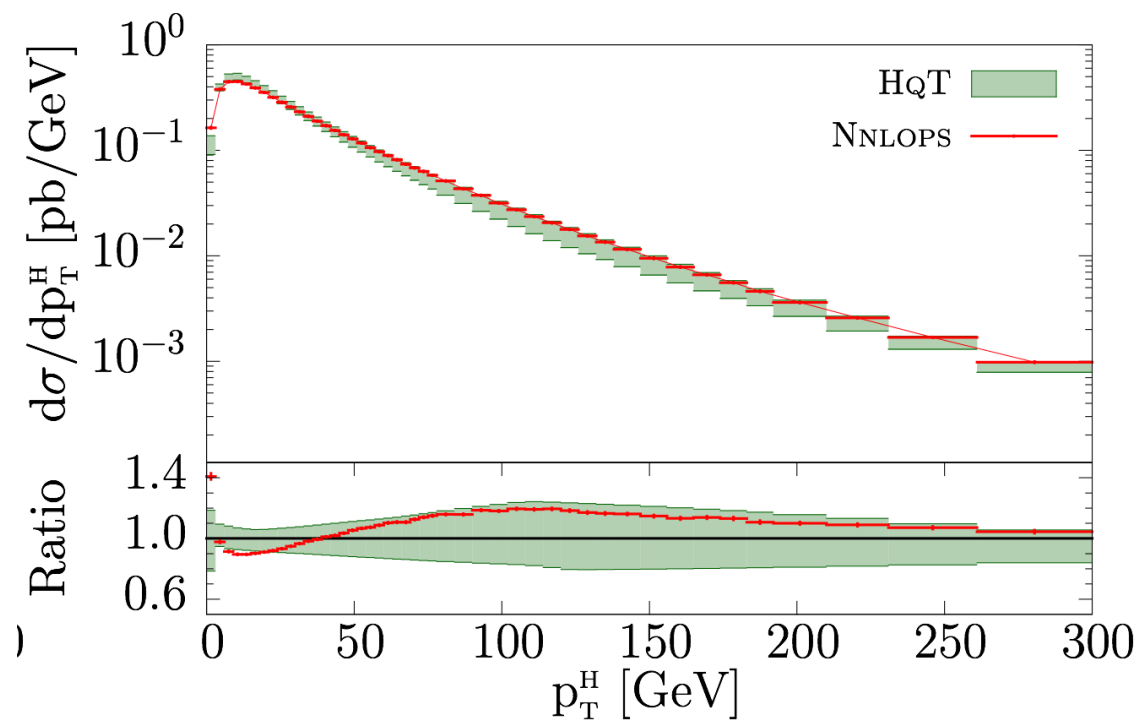
[Czakon, Fiedler, Heymes, Mitov.; in preparation]

# NNLO + PS

NLO matching well established, while NNLO matching still in its infancy

1) **NNLOPS**: use MINLO to obtain a NLO generator for both H and H+jet(s)  
 [K.Hamilton, P.Nason, G.Zanderighi (2014,2015)]

2) **UN2LOPS**: use S-MC@NLO + UNLOPS +  $q_T$  slicing  
 [N.Lavesson, L.Lonnblad (2008), S.Hoeche, Y.Li, S.Prestel (2014)]



Enforce correct NNLO normalisation by reweighing the inclusive rapidity distribution to the NNLO calculation

NNLO virtual corrections confined in the low  $p_T$  region while in the POWHEG-MINLO approach they are spread over the whole  $p_T$  region



# The frontier: N3LO

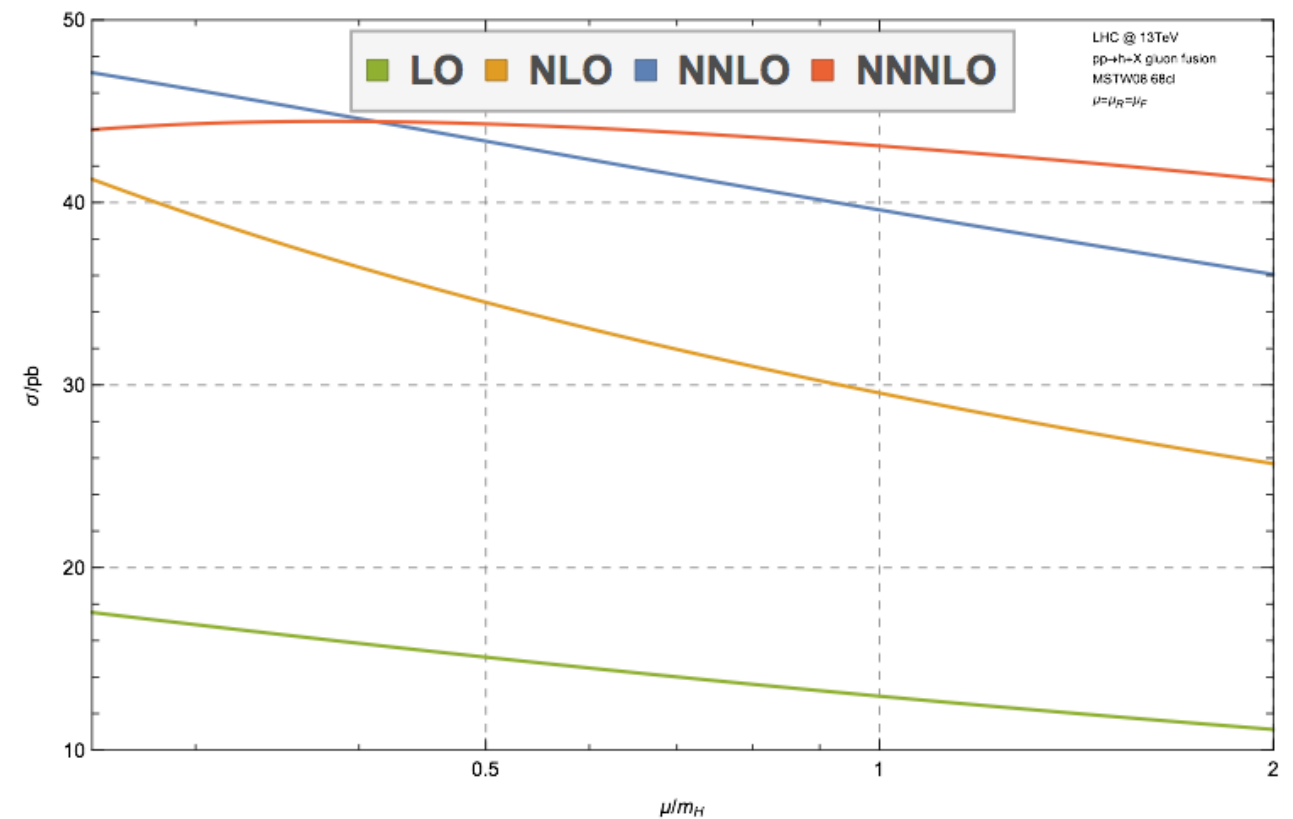
[C.Anastasiou, C.Duhr, F.Dulat, F.Herzog, B.Mistlberger (2015)]

Full calculation for the  $gg \rightarrow H$  completed through the evaluation of 30 terms in the soft-expansion: first ever complete calculation at N3LO in hadronic collisions.

Significant reduction of uncertainties from missing higher orders and PDF+ $\alpha_s$

Scale dep. stabilizes around  $\mu=m_H/2$

N3LO effect +2.2% at  $\mu=m_H/2$

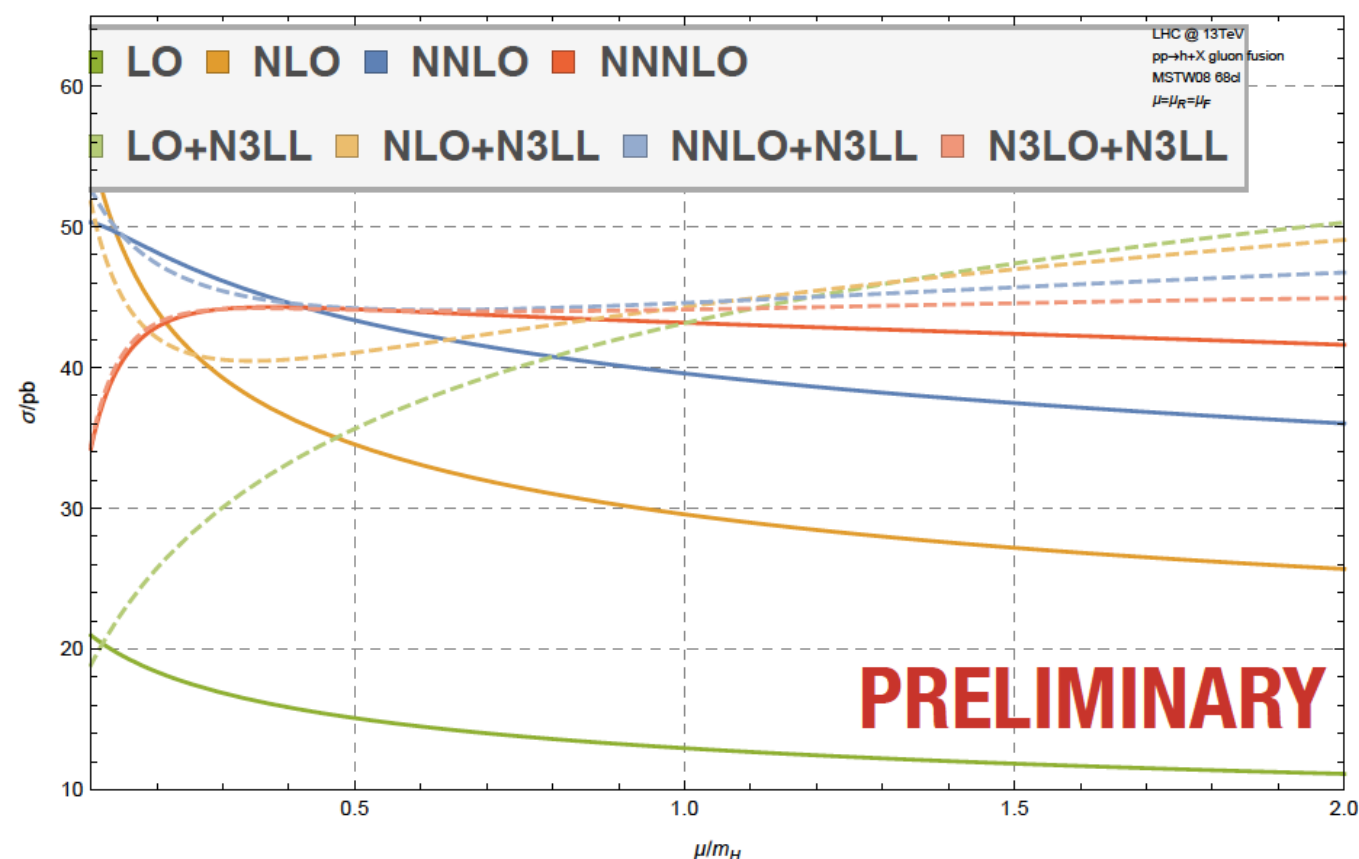


Corresponding new results for the Higgs cross section including mass effects at NLO and the other known corrections at 13 TeV expected soon.

# The frontier: N3LO

The best predictions for Higgs production include threshold resummation effects.

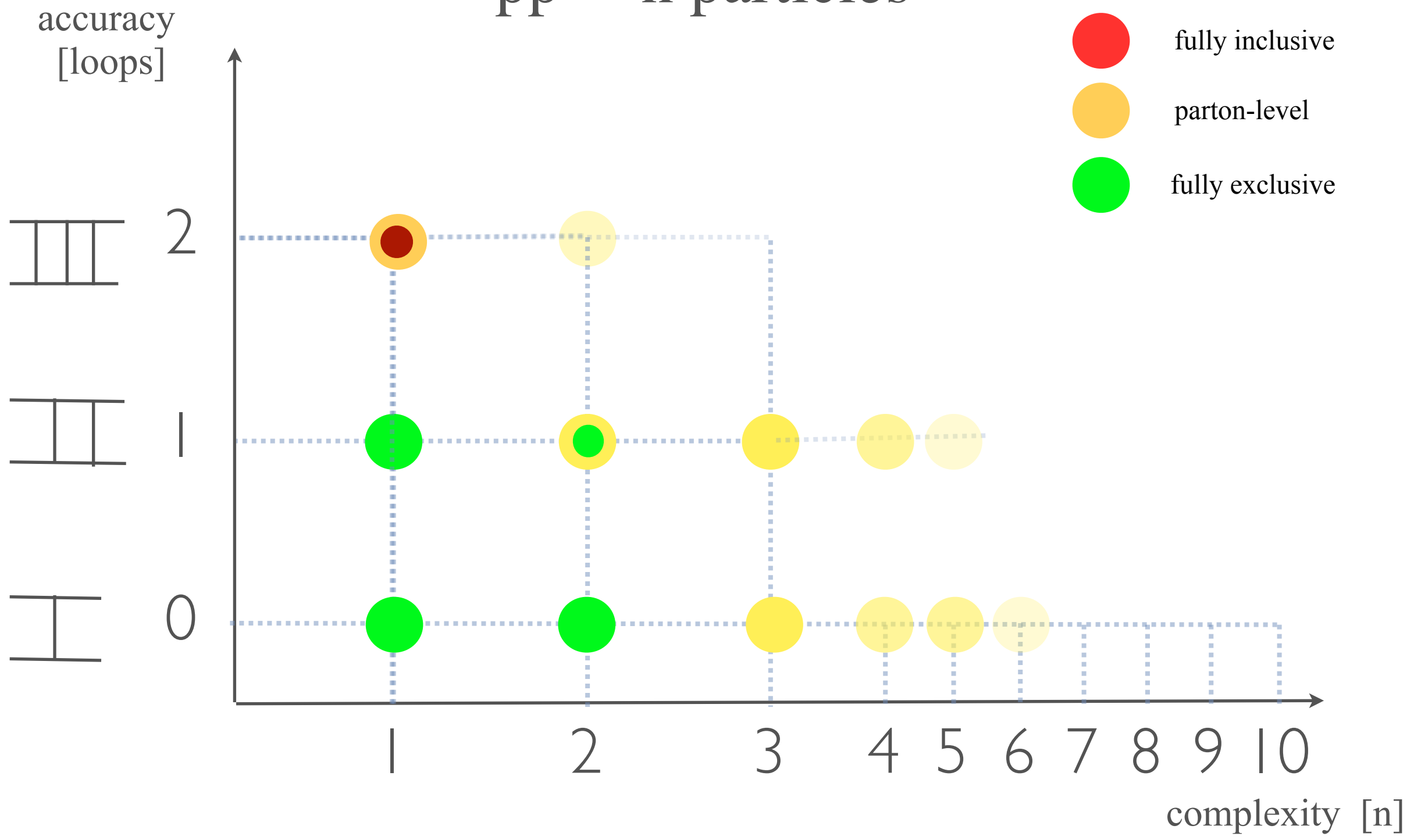
Results of systematically including the resummation of the threshold logs points towards a stabilisation of the scale dependence.



Such a flat behaviour puts into question the reliability of very method that we use to evaluate the effects of unknown higher-order contributions through scale variation.

# Predictions in QCD: before the LHC

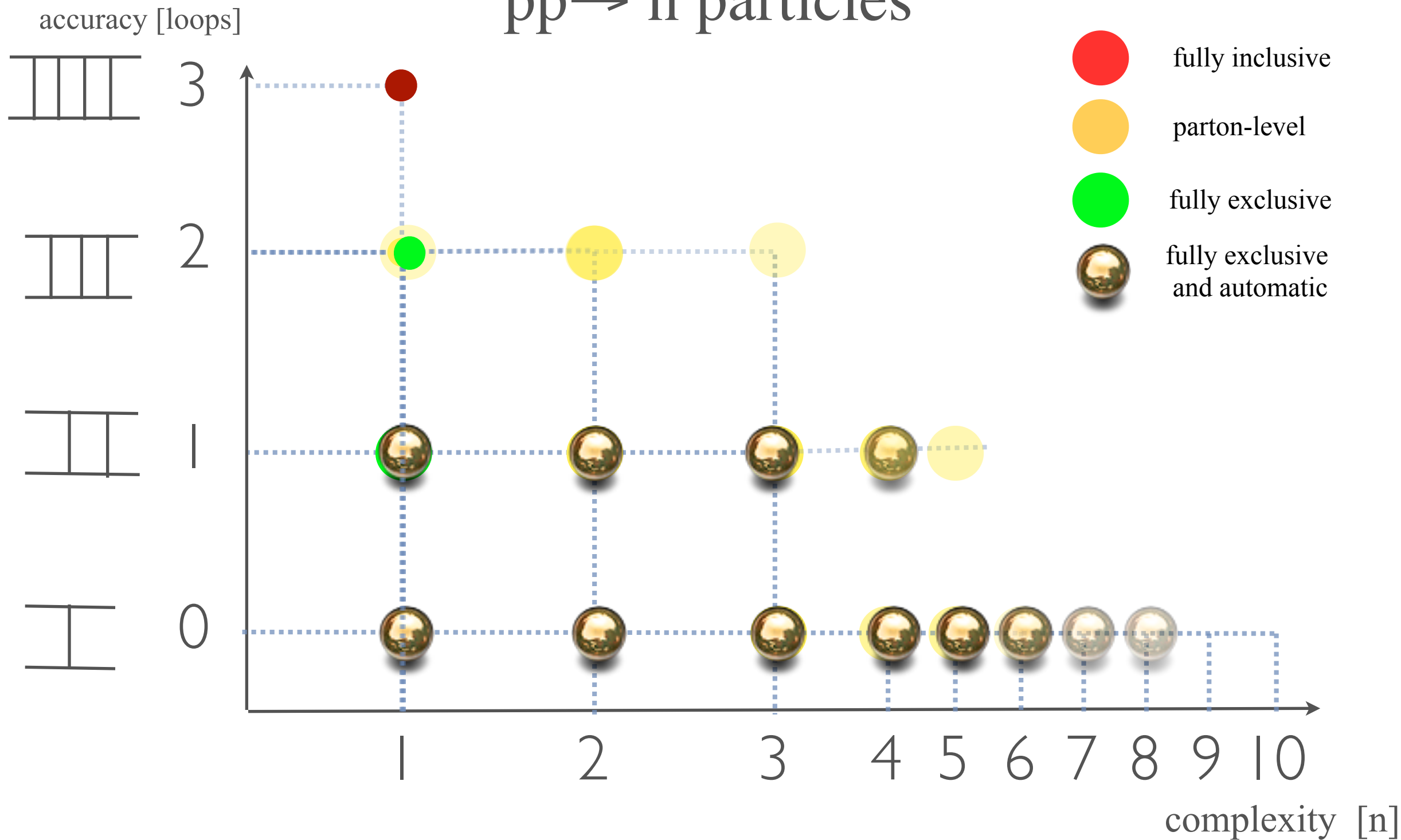
$pp \rightarrow n$  particles





# Predictions in QCD for the LHC: status 2015

$pp \rightarrow n$  particles



# Summary

- The LHC physics program demands predictions at an unprecedented level of accuracy and precision.
- Rapid and impressive progress in techniques in the last few years has lead to:
  - Full automation of the computation of NLO QCD corrections and their matching/merging with parton shower program: experimental grade predictions are now available for SM and BSM (resonant and in EFTs). Automatic NLO EW is being achieved now.
  - The new era of differential predictions at NNLO in QCD for a every-day increasing set of important SM processes  $2 \rightarrow 2$ , such as H+jet, V+jet, VV, t tbar production. In addition first exploration of NNLO+PS for  $2 \rightarrow 1$  process has started.
  - Moving the frontier to N3LO.
- Main outcomes:
  - Progress in understanding of QCD and pp collisions at high  $Q^2$
  - TH Ready for Run II LHC



# Credits

A special thank to the italian TH QCD/MC at LHC community, currently working in Italy or **abroad**, great collaborators and precision passionates (rnd order):

Francesco Tramontano, **Michelangelo Mangano**, **Andrea Banfi**, Paolo Nason, **Marco Bonvini**, Giovanni Ridolfi, Stefano Frixione, **Giulia Zanderighi**, Stefano Catani, Carlo Oleari, **Giovanni Ossola**, Pierpaolo Mastrolia, Giancarlo Ferrera, **Emanuale Re**, Paolo Torrielli, **Roberto Pittau**, Stefano Forte, Alessandro Vicini, **Simone Alioli**, **Alberto Guffanti**, **Fabrizio Caola**, Gennaro Corcella, **Massimiliano Grazzini**, Fulvio Piccinini, **Matteo Cacciari**, **Maria Ubiali**, **Vittorio del Duca**, **Simone Marzani**, Stefano Forte, **Laura Reina**, **Marco Zaro**, **Davide Pagani**, ...

**Thanks to** Massimiliano Grazzini for his great talk at EPS 2015, that was extensively used in this seminar.