

**NATURE AND RAMAN SIGNATURE OF THE  
HIGGS AMPLITUDE MODE IN THE  
COEXISTING SUPERCONDUCTING AND  
CHARGE-DENSITY-WAVE STATE**

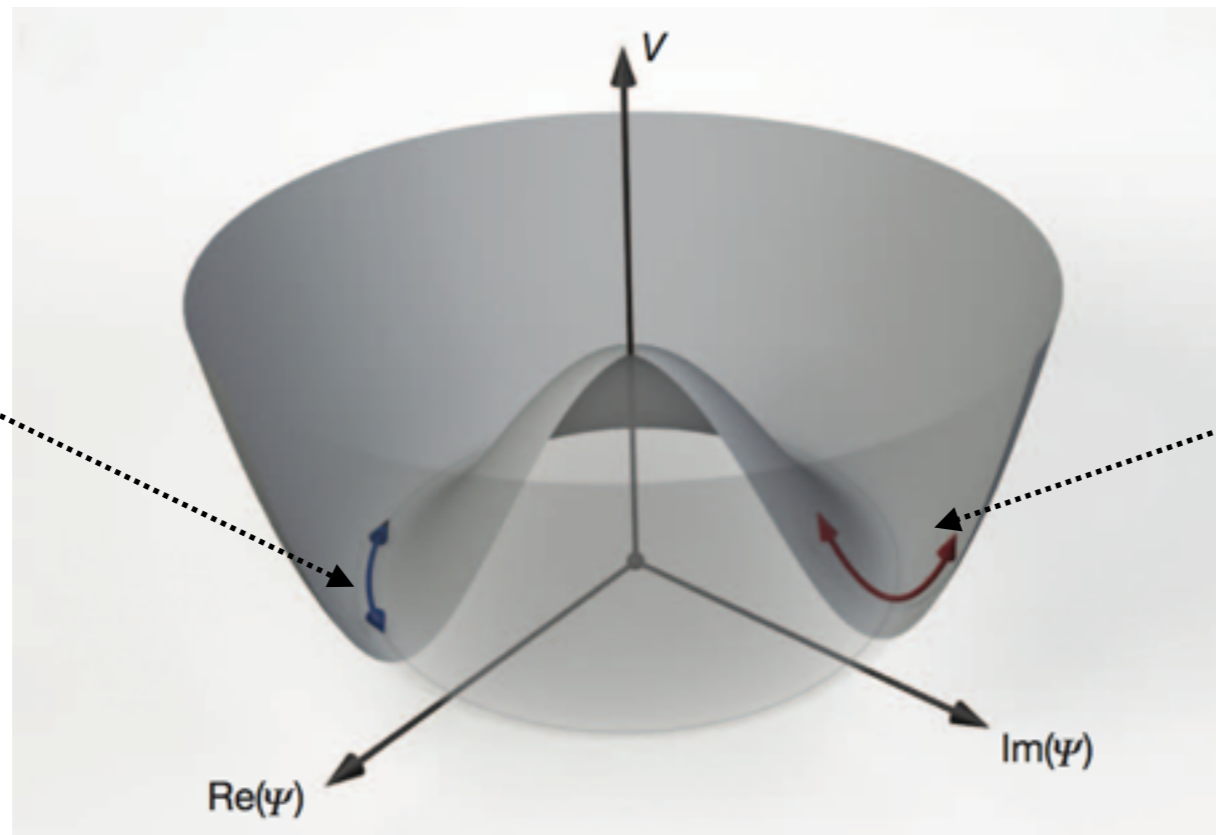
**Tommaso Cea<sup>1</sup> and Lara Benfatto<sup>1</sup>**

<sup>1</sup> ISC-CNR and Dep. of Physics, "Sapienza" University of Rome, P.le  
A. Moro 5, 00185, Rome, Italy

# HIGGS (AMPLITUDE) MODE IN SUPERCONDUCTORS AND ITS VISIBILITY

In a superconductor the breaking of the continuous  $U(1)$  symmetry comes along with the emergence of two kinds of collective modes

The phase  
(Nambu -  
Goldstone)  
modes: massless



The amplitude  
(Higgs) modes:  
massive

In a conventional BCS  
superconductor it is very  
difficult to detect the Higgs  
mode in the experiments:

- 1) Over damping by quasi-particle continuum
- 2) Weak coupling to any external probe

# DYNAMICS OF THE SC AMPLITUDE MODE

The Ginzburg-Landau model well describes the **STATIC** properties of a **BCS superconductor**

$$\mathcal{F} = a|\Psi|^2 + \frac{b}{2}|\Psi|^4 + c|\nabla\Psi|^2$$

$$\Psi = (\Delta_0 + \Delta)e^{i\theta}$$

$$a = a_0(T - T_c) \quad a_0 > 0$$

# DYNAMICS OF THE SC AMPLITUDE MODE

The Ginzburg-Landau model well describes the **STATIC** properties of a **BCS superconductor**

$$\mathcal{F} = a|\Psi|^2 + \frac{b}{2}|\Psi|^4 + c|\nabla\Psi|^2$$

$$\Psi = (\Delta_0 + \Delta)e^{i\theta}$$

$$a = a_0(T - T_c) \quad a_0 > 0 \quad T < T_c \quad \Rightarrow \quad \Delta_0 = \sqrt{-\frac{a}{b}} \neq 0$$

# DYNAMICS OF THE SC AMPLITUDE MODE

The Ginzburg-Landau model well describes the **STATIC** properties of a **BCS** superconductor

$$\mathcal{F} = a|\Psi|^2 + \frac{b}{2}|\Psi|^4 + c|\nabla\Psi|^2$$

$$\Psi = (\Delta_0 + \Delta)e^{i\theta}$$

$$a = a_0(T - T_c) \quad a_0 > 0 \quad T < T_c \quad \Rightarrow \quad \Delta_0 = \sqrt{-\frac{a}{b}} \neq 0$$

**Problem: how to introduce the DYNAMICS?**

# DYNAMICS OF THE SC AMPLITUDE MODE

First (phenomenological) way: build up the Lagrangian by adding a relativistic term to the Ginzburg-Landau picture

$$\mathcal{F} = a|\Psi|^2 + \frac{b}{2}|\Psi|^4 + c|\nabla\Psi|^2$$

# DYNAMICS OF THE SC AMPLITUDE MODE

First (phenomenological) way: build up the Lagrangian by adding a relativistic term to the Ginzburg-Landau picture

$$\mathcal{F} = a|\Psi|^2 + \frac{b}{2}|\Psi|^4 + c|\nabla\Psi|^2 + |\partial_t\Psi|^2$$

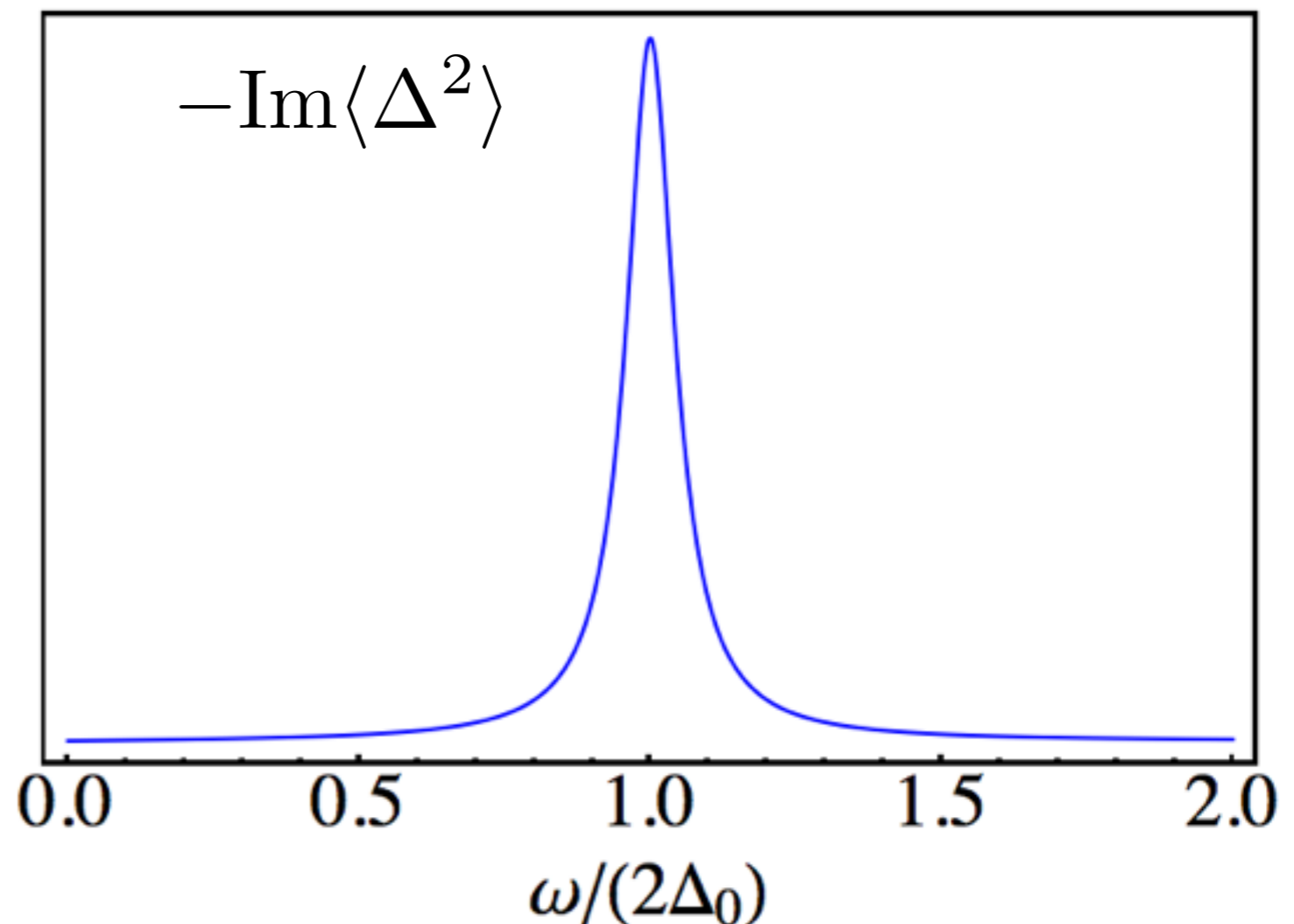
# DYNAMICS OF THE SC AMPLITUDE MODE

First (phenomenological) way: build up the Lagrangian by adding a relativistic term to the Ginzburg-Landau picture

$$\mathcal{F} = a|\Psi|^2 + \frac{b}{2}|\Psi|^4 + c|\nabla\Psi|^2 + |\partial_t\Psi|^2$$

Then a well defined power-law singularity would arise in the amplitude propagator at twice the SC gap

$$\langle\Delta^2\rangle^{-1} \propto \omega^2 - (2\Delta_0)^2$$





# DYNAMICS OF THE SC AMPLITUDE MODE

First (phenomenological) way: build up the Lagrangian by adding a relativistic term to the Ginzburg-Landau picture

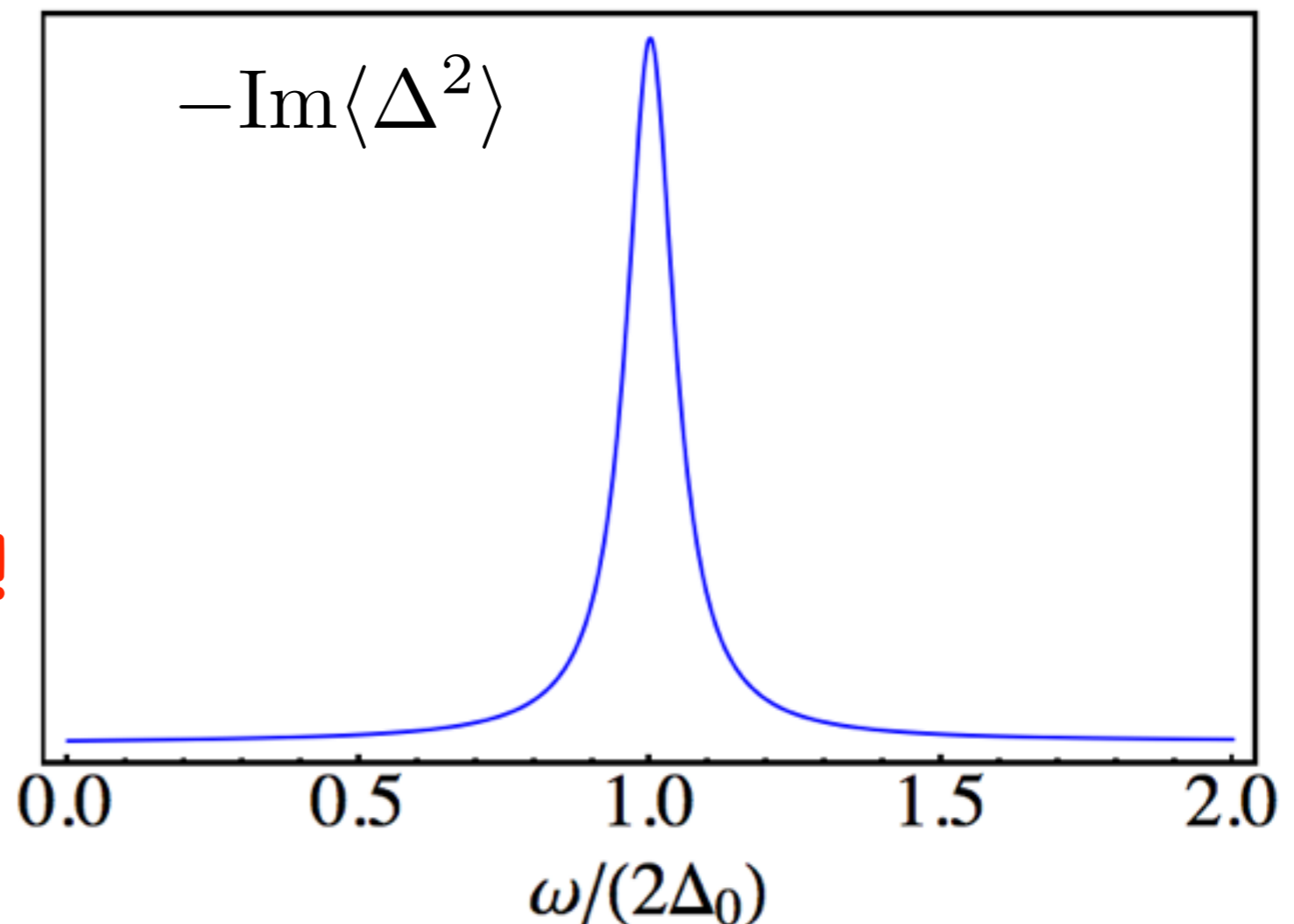
$$\mathcal{F} = a|\Psi|^2 + \frac{b}{2}|\Psi|^4 + c|\nabla\Psi|^2 + |\partial_t\Psi|^2$$

Then a well defined power-law singularity would arise in the amplitude propagator at twice the SC gap

$$\langle\Delta^2\rangle^{-1} \propto \omega^2 - (2\Delta_0)^2$$

**BUT THIS IS WRONG !!**

(See also T. Cea et al. arXiv:1503.07733,  
to appear on PRL )



# DYNAMICS OF THE SC AMPLITUDE MODE

The correct way to describe the dynamic properties of a superconductor is to use a microscopic model, taking into account the fermionic degrees of freedom

$$\mathcal{L} = \sum_{\sigma} c_{\sigma}^{\dagger} \left( i\partial_t + \frac{\nabla^2}{2m} \right) c_{\sigma} + \lambda c_{\uparrow}^{\dagger} c_{\downarrow}^{\dagger} c_{\downarrow} c_{\uparrow}$$

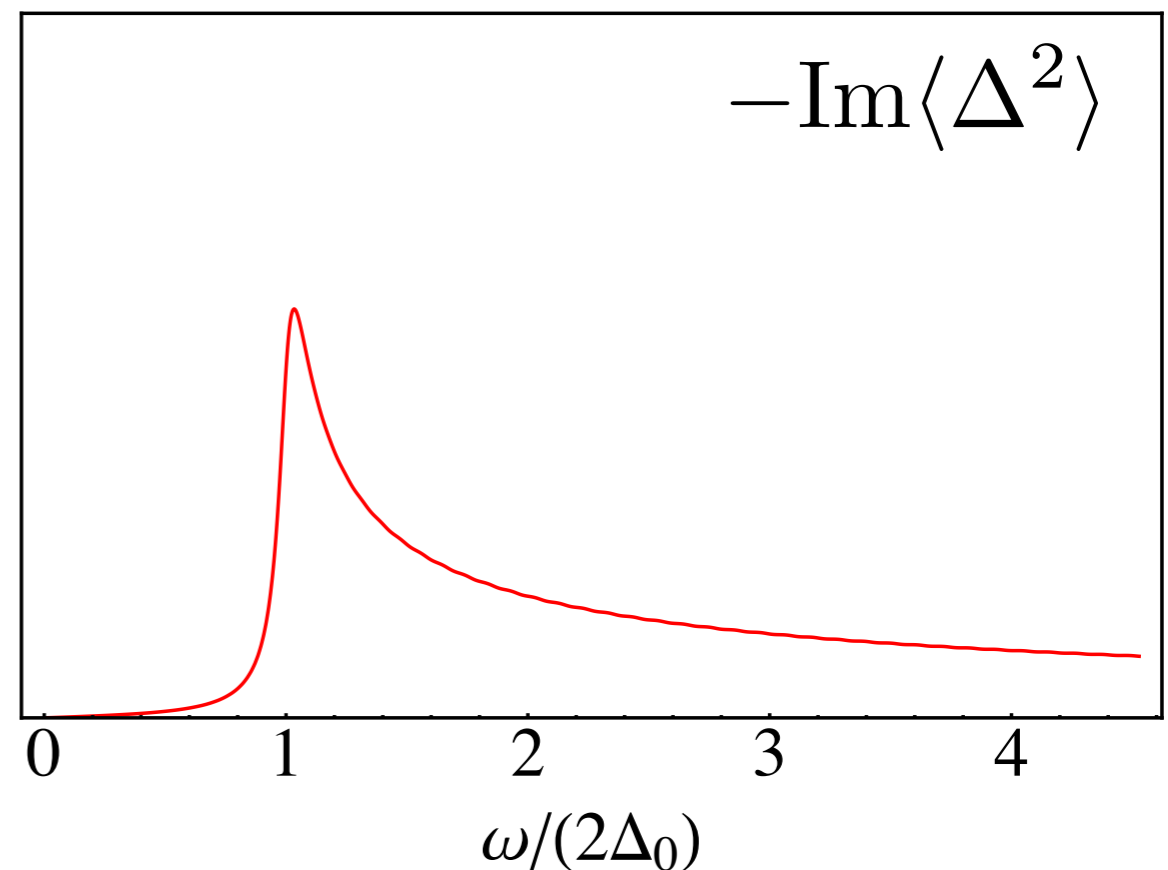
# DYNAMICS OF THE SC AMPLITUDE MODE

The correct way to describe the dynamic properties of a superconductor is to use a microscopic model, taking into account the fermionic degrees of freedom

$$\mathcal{L} = \sum_{\sigma} c_{\sigma}^{\dagger} \left( i\partial_t + \frac{\nabla^2}{2m} \right) c_{\sigma} + \lambda c_{\uparrow}^{\dagger} c_{\downarrow}^{\dagger} c_{\downarrow} c_{\uparrow}$$

A diverging quasi-particle contribution appears in the amplitude inverse propagator, giving rise to a weak square-root singularity

$$\langle \Delta^2 \rangle^{-1} \propto (\omega^2 - 4\Delta_0^2) F_{QP}(\omega) \sim \sqrt{\omega^2 - 4\Delta_0^2}$$



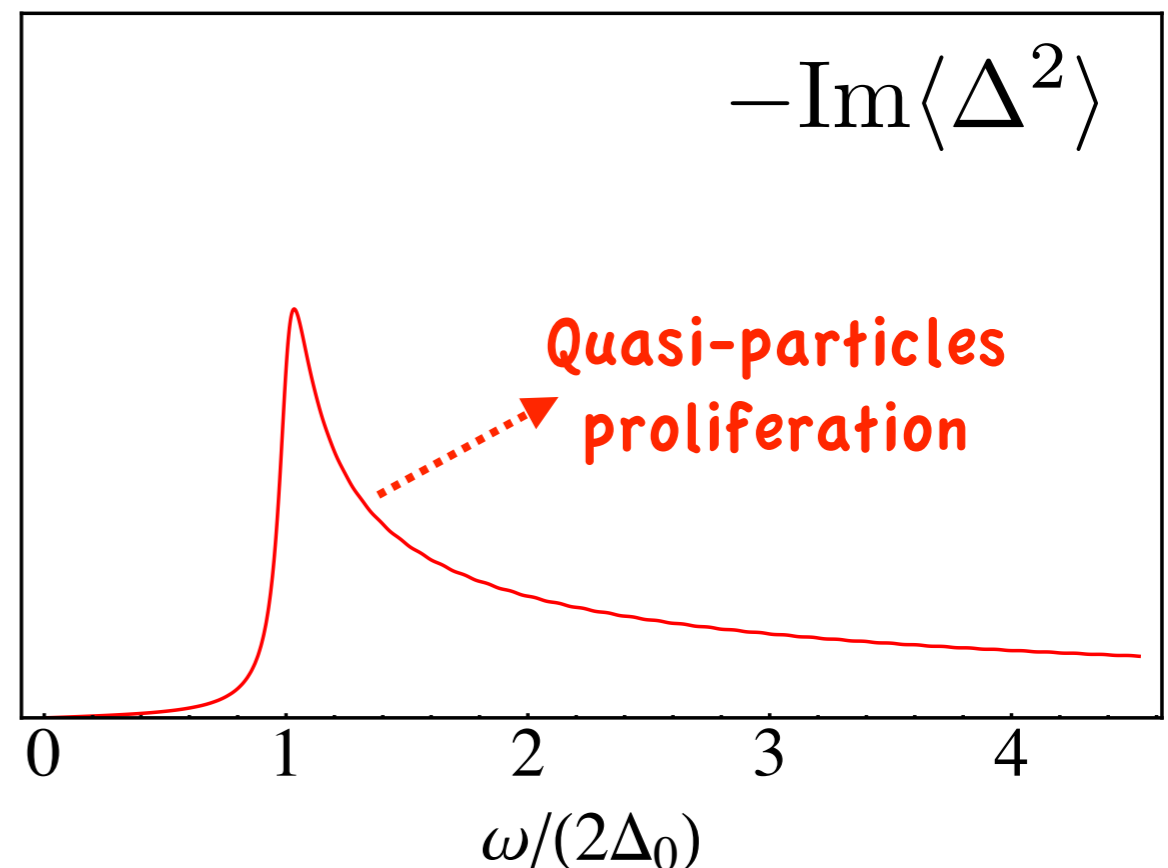
# DYNAMICS OF THE SC AMPLITUDE MODE

The correct way to describe the dynamic properties of a superconductor is to use a microscopic model, taking into account the fermionic degrees of freedom

$$\mathcal{L} = \sum_{\sigma} c_{\sigma}^{\dagger} \left( i\partial_t + \frac{\nabla^2}{2m} \right) c_{\sigma} + \lambda c_{\uparrow}^{\dagger} c_{\downarrow}^{\dagger} c_{\downarrow} c_{\uparrow}$$

A diverging quasi-particle contribution appears in the amplitude inverse propagator, giving rise to a weak square-root singularity

$$\langle \Delta^2 \rangle^{-1} \propto (\omega^2 - 4\Delta_0^2) F_{QP}(\omega) \sim \sqrt{\omega^2 - 4\Delta_0^2}$$



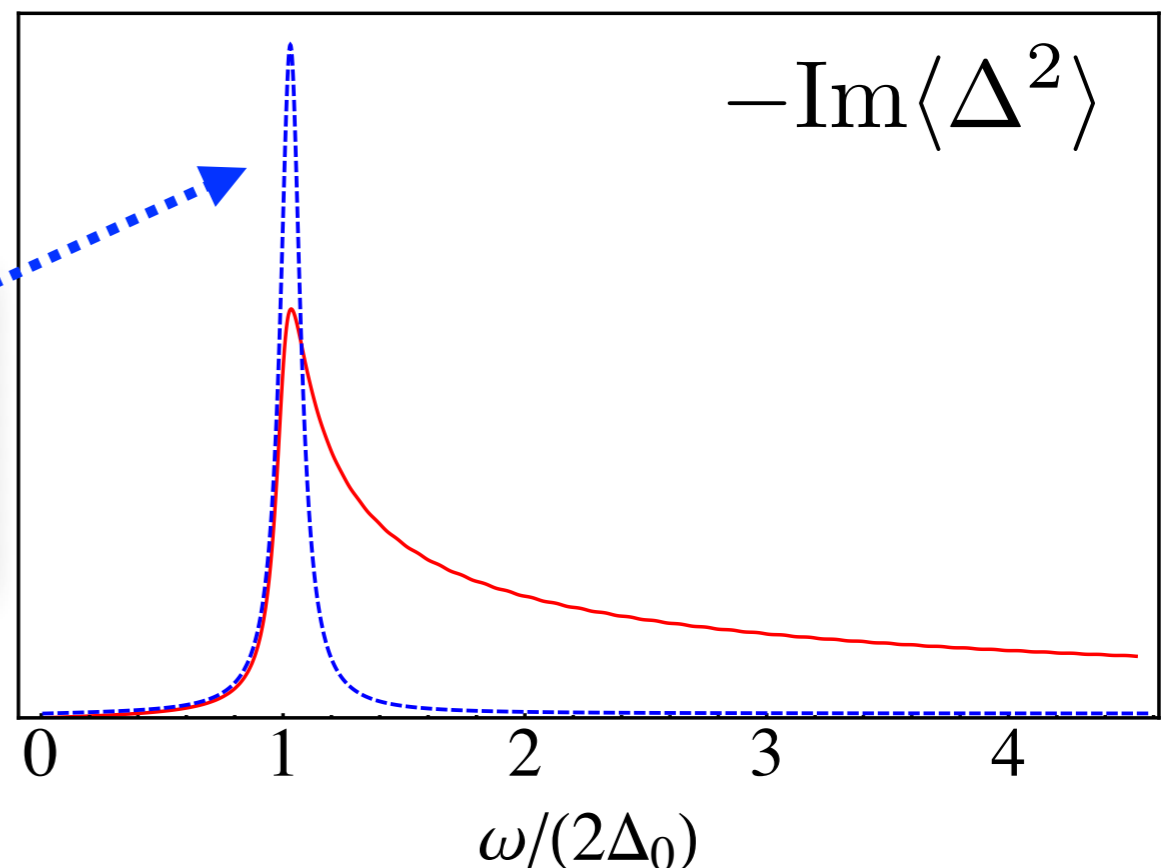
# DYNAMICS OF THE SC AMPLITUDE MODE

The correct way to describe the dynamic properties of a superconductor is to use a microscopic model, taking into account the fermionic degrees of freedom

$$\mathcal{L} = \sum_{\sigma} c_{\sigma}^{\dagger} \left( i\partial_t + \frac{\nabla^2}{2m} \right) c_{\sigma} + \lambda c_{\uparrow}^{\dagger} c_{\downarrow}^{\dagger} c_{\downarrow} c_{\uparrow}$$

A diverging quasi-particle contribution appears in the amplitude inverse propagator, giving rise to a weak square-root singularity

Very different picture as compared to the "relativistic" one



# DYNAMICS OF THE SC AMPLITUDE MODE

Despite all this, we show that, when **SUPERCONDUCTIVITY coexists with a preformed CHARGE-DENSITY-WAVE order** the dynamics of the SC amplitude fluctuations displays a relativistic behavior

# DYNAMICS OF THE SC AMPLITUDE MODE

Despite all this, we show that, when **SUPERCONDUCTIVITY coexists with a preformed CHARGE-DENSITY-WAVE order** the dynamics of the SC amplitude fluctuations displays a relativistic behavior

$$\langle \Delta^2 \rangle^{-1} \propto (\omega^2 - 4\Delta_0^2) F_{QP}(\omega)$$

The QP continuum starts at the energy  $E_{\text{gap}}$  where  $F_{QP}$  diverges

# DYNAMICS OF THE SC AMPLITUDE MODE

Despite all this, we show that, when **SUPERCONDUCTIVITY coexists with a preformed CHARGE-DENSITY-WAVE order** the dynamics of the SC amplitude fluctuations displays a relativistic behavior

$$\langle \Delta^2 \rangle^{-1} \propto (\omega^2 - 4\Delta_0^2) F_{QP}(\omega)$$

The QP continuum starts at the energy  $E_{\text{gap}}$  where  $F_{QP}$  diverges

Conventional SC:  $F_{QP}(\omega) = \sum_{\mathbf{k}} \frac{E_{\mathbf{k}}^{-1}}{(\omega + i\delta)^2 - 4(\Delta_0^2 + \xi_{\mathbf{k}}^2)}$

$E_{\text{gap}} = 2\Delta_0$  coincides with the Higgs energy



# DYNAMICS OF THE SC AMPLITUDE MODE

Despite all this, we show that, when **SUPERCONDUCTIVITY coexists with a preformed CHARGE-DENSITY-WAVE order** the dynamics of the SC amplitude fluctuations displays a relativistic behavior

$$\langle \Delta^2 \rangle^{-1} \propto (\omega^2 - 4\Delta_0^2) F_{QP}(\omega)$$

The QP continuum starts at the energy  $E_{\text{gap}}$  where  $F_{QP}$  diverges

Conventional SC: 
$$F_{QP}(\omega) = \sum_{\mathbf{k}} \frac{E_{\mathbf{k}}^{-1}}{(\omega + i\delta)^2 - 4(\Delta_0^2 + \xi_{\mathbf{k}}^2)}$$

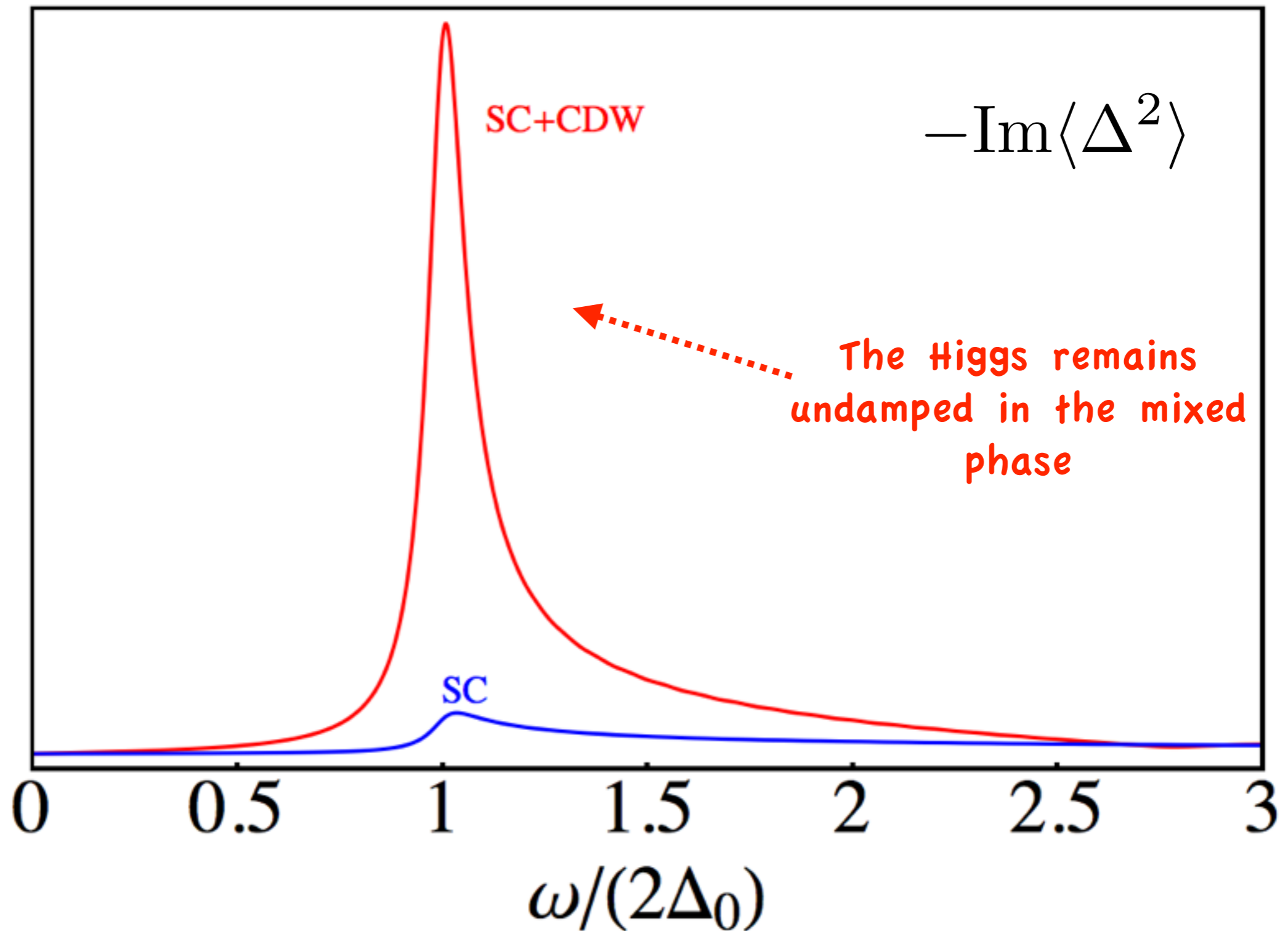
$E_{\text{gap}} = 2\Delta_0$  coincides with the Higgs energy

SC+CDW state: 
$$F_{QP}(\omega) = \sum_{\mathbf{k}} \frac{E_{\mathbf{k}}^{-1}}{(\omega + i\delta)^2 - 4(\Delta_0^2 + D_0^2 + \xi_{\mathbf{k}}^2)}$$

$E_{\text{gap}} = 2(\Delta_0^2 + D_0^2)^{1/2}$ , so the Higgs remains undamped

$D_0$  is the CDW gap

# DYNAMICS OF THE SC AMPLITUDE MODE



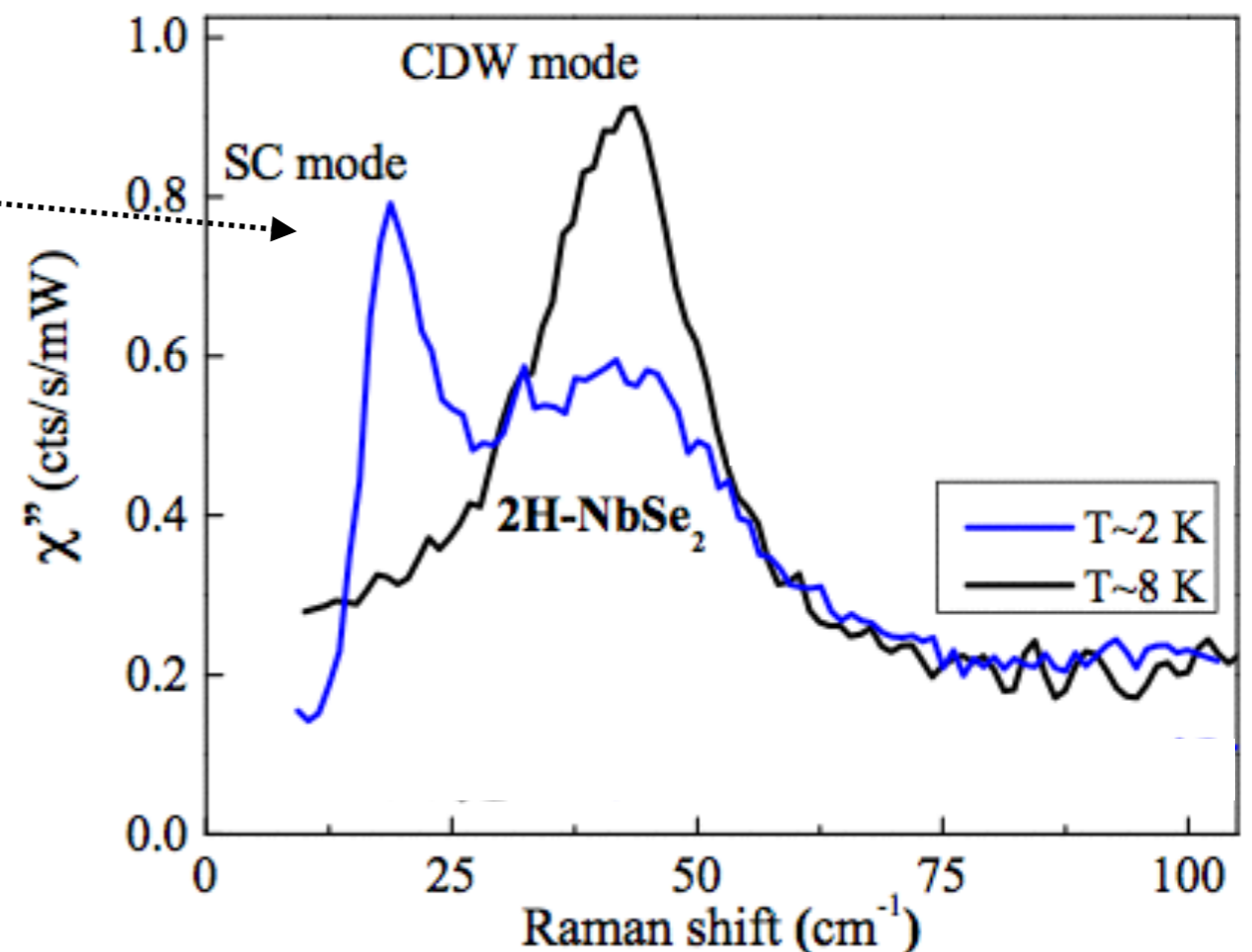
T. Cea and L. Benfatto PRRB 90, 224515 (2014)

# THE PECULIAR CASE OF NbSe<sub>2</sub>

NbSe<sub>2</sub> presents the coexistence of SC with CDW:  
 $T_c=7K$  and  $T_{CDW}=33K$

The Higgs mode becomes visible via Raman spectroscopy

At  $T < T_c$  a strong peak in the Raman response appears at the typical scale of the Higgs mass  $\omega_{\text{Higgs}} = 2\Delta_0$



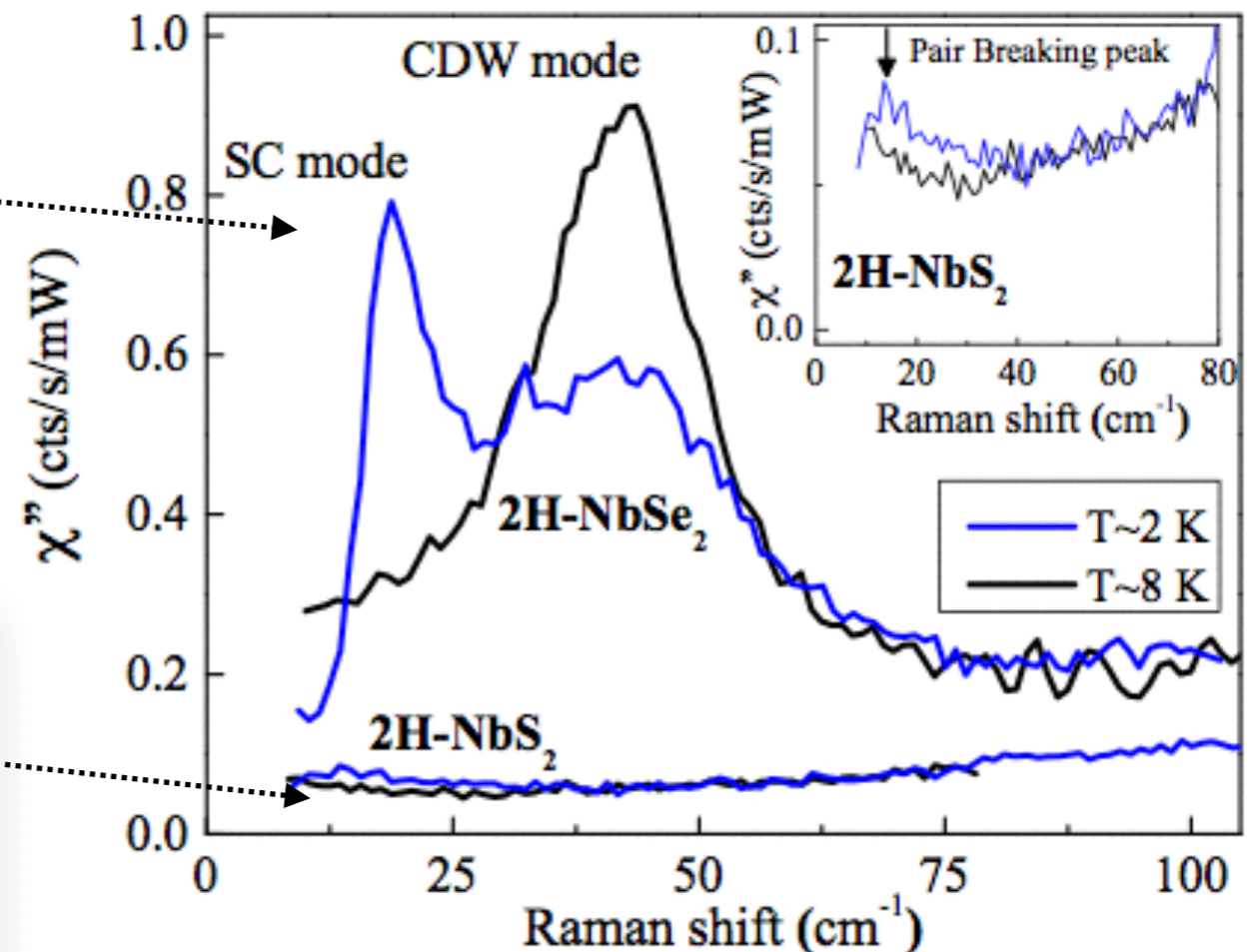
# THE PECULIAR CASE OF NbSe<sub>2</sub>

NbSe<sub>2</sub> presents the coexistence of SC with CDW:  
 $T_c=7K$  and  $T_{CDW}=33K$

The Higgs mode becomes visible via Raman spectroscopy

At  $T < T_c$  a strong peak in the Raman response appears at the typical scale of the Higgs mass  $\omega_{\text{Higgs}} = 2\Delta_0$

The direct comparison with the isostructural superconductor NbS<sub>2</sub> displays only a weak pair breaking signal



# THE ROLE OF THE CDW PHONON

CDW order  lattice instability

CDW induced by the coupling of a phonon to the  
electronic density

$$H_{CDW} \rightarrow H_{ph} + H_{e-ph}$$

$$H_{ph} = \omega_0 a_{\mathbf{Q}}^\dagger a_{\mathbf{Q}}$$

$$H_{e-ph} = \frac{g}{\sqrt{N}} \left( a_{\mathbf{Q}} + a_{-\mathbf{Q}}^\dagger \right) \sum_{\mathbf{k}\sigma} \gamma_{\mathbf{k}} c_{\mathbf{k}+\mathbf{Q}\sigma}^\dagger c_{\mathbf{k}\sigma}$$

The phonon acts as an additive collective mode which couples to  
both the Higgs mode and the Raman probe

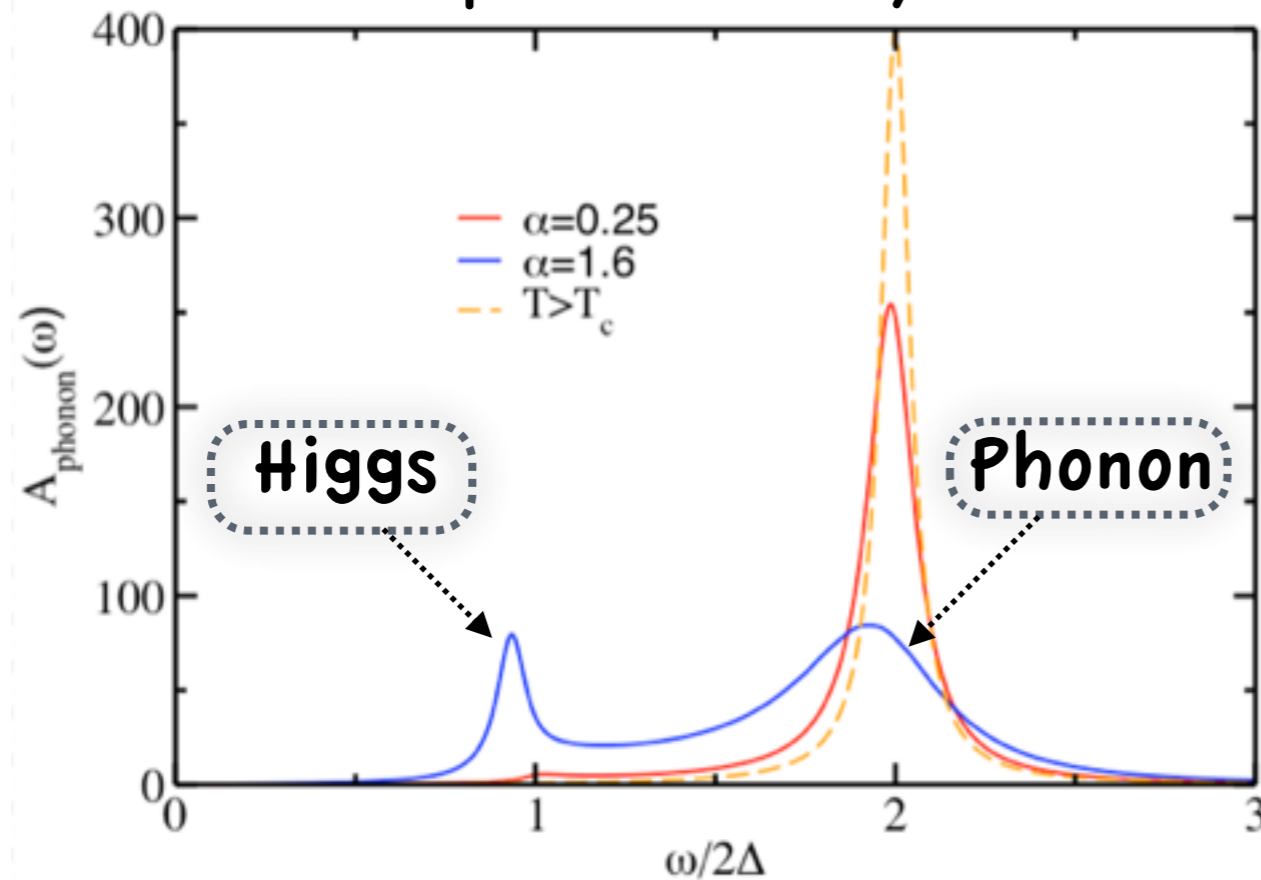
# PREVIOUS THEORETICAL INTERPRETATION

Finite coupling of the Higgs to the CDW phonon

P. B. Littlewood and C. M. Varma PRB (1982)

D. A. Browne and K. Levine PRB (1983)

Effective phonon density of states



The Higgs mode moves below the quasi-particle threshold  $2\Delta_0$  but remains weak if the Higgs were over damped

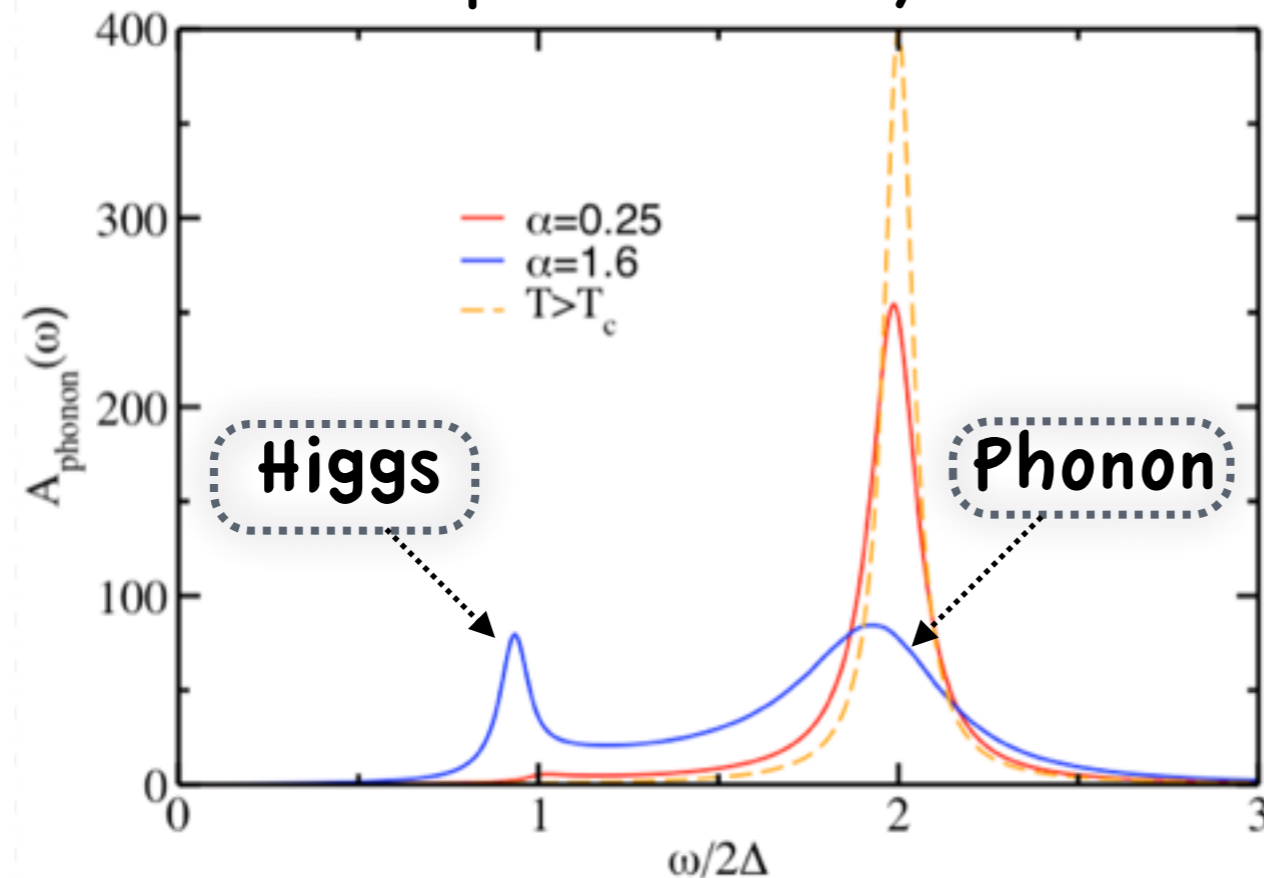
# PREVIOUS THEORETICAL INTERPRETATION

Finite coupling of the Higgs to the CDW phonon

P. B. Littlewood and C. M. Varma PRB (1982)

D. A. Browne and K. Levine PRB (1983)

Effective phonon density of states

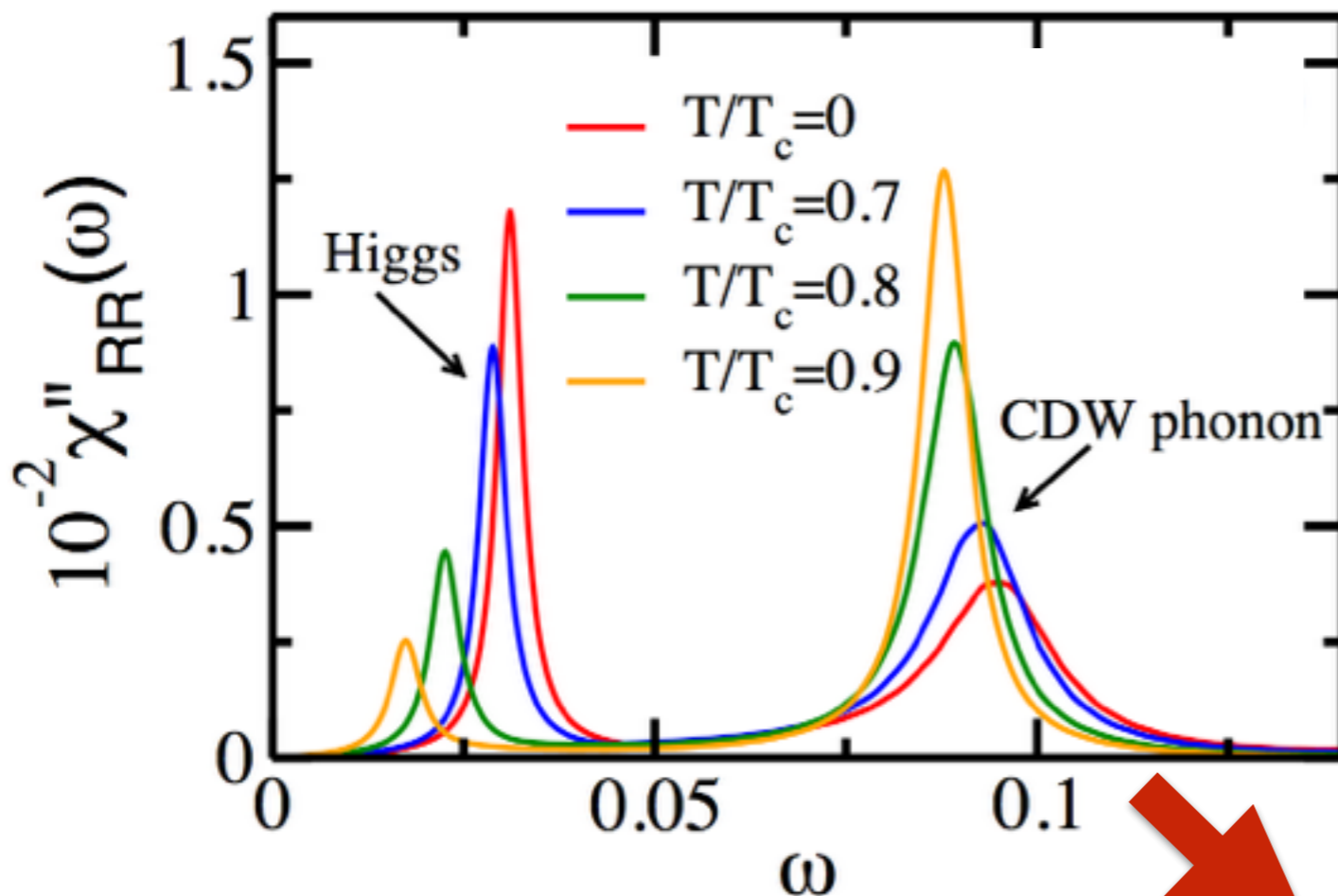


The Higgs mode moves below the quasi-particle threshold  $2\Delta_0$  but remains weak if the Higgs were over damped

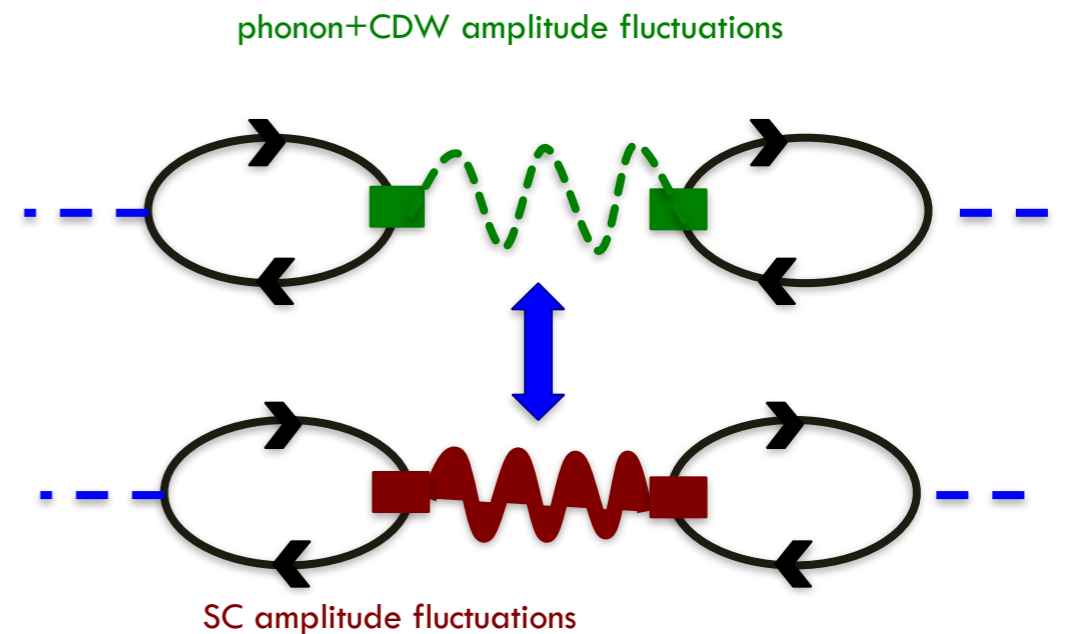
This is not enough to explain the experiments: the true nature of the Higgs and the computation of the full Raman response are needed

# THE RAMAN RESPONSE

We compute the RPA Raman response function by including the contributions of both the (undamped) Higgs and the CDW phonon



T. Cea and L. Benfatto PRB 90, 224515 (2014)

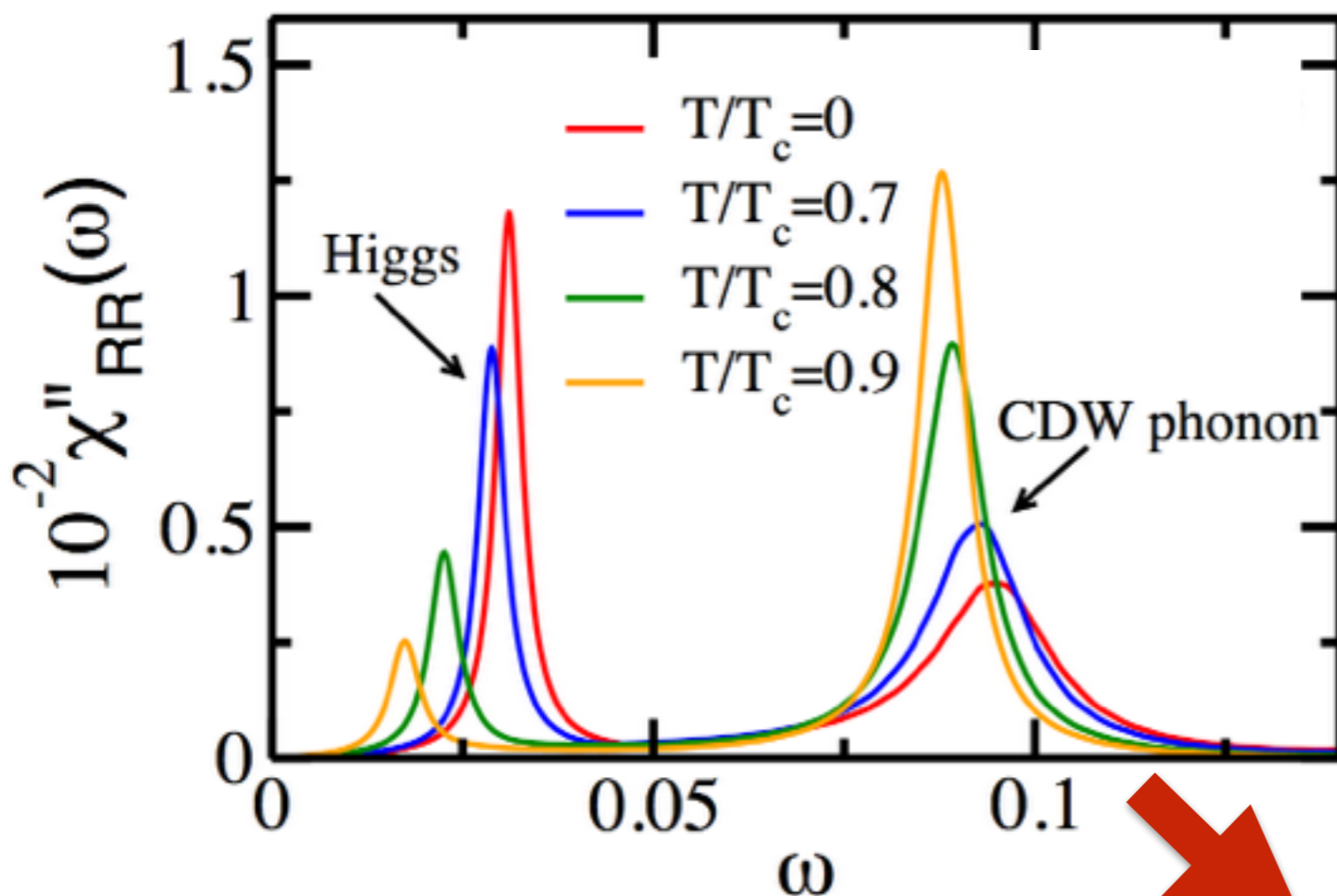


Two peaks appears below  $T_c$

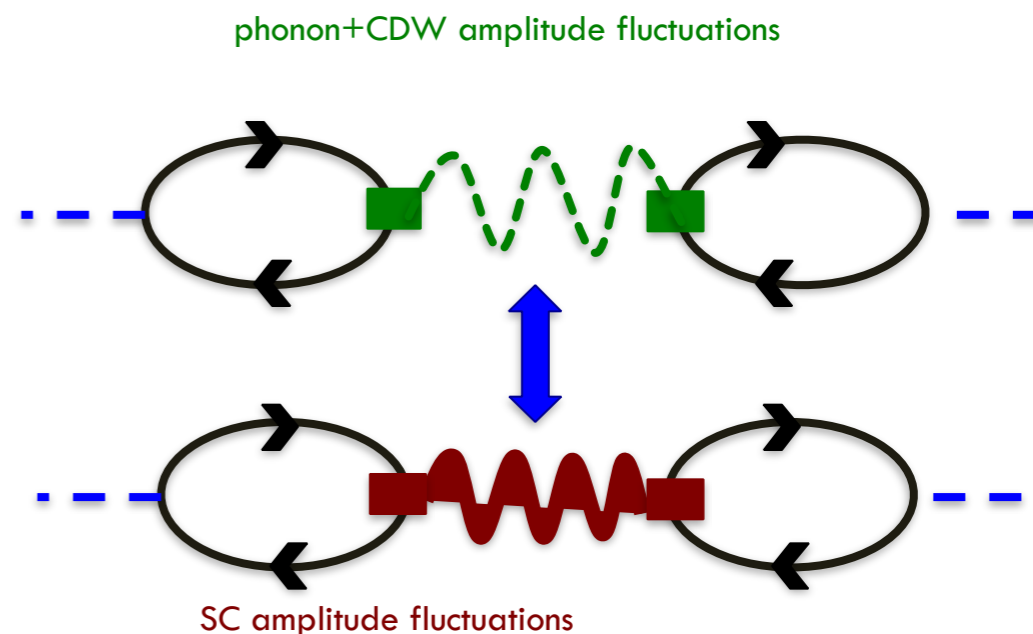


# THE RAMAN RESPONSE

We compute the RPA Raman response function by including the contributions of both the (undamped) Higgs and the CDW phonon



T. Cea and L. Benfatto PRB 90, 224515 (2014)



The Higgs mode seems to acquire spectral weight from the CDW phonon by entering in the SC phase

## CONCLUSIONS AND PERSPECTIVES

- New nature of the amplitude fluctuations in the SC+CDW state (power-law singularity)
- The Higgs manifests itself as a sharp resonance in the Raman response
- What about the dynamics of the Higgs?



Pump-probe tests...

Matsunaga et al. PRL (2013), Science (2014)