

Hadron Reaction and Spectroscopy Studies at JPAC

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Indiana University
Jefferson Lab

Evidence of
new hadrons

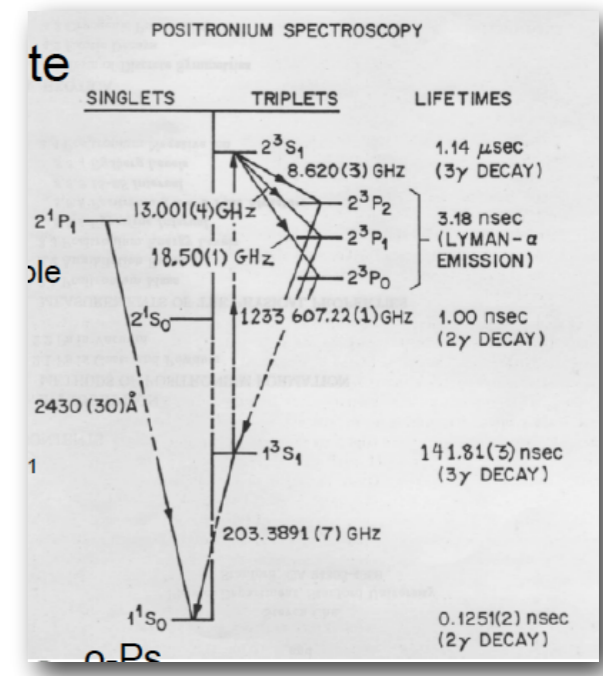
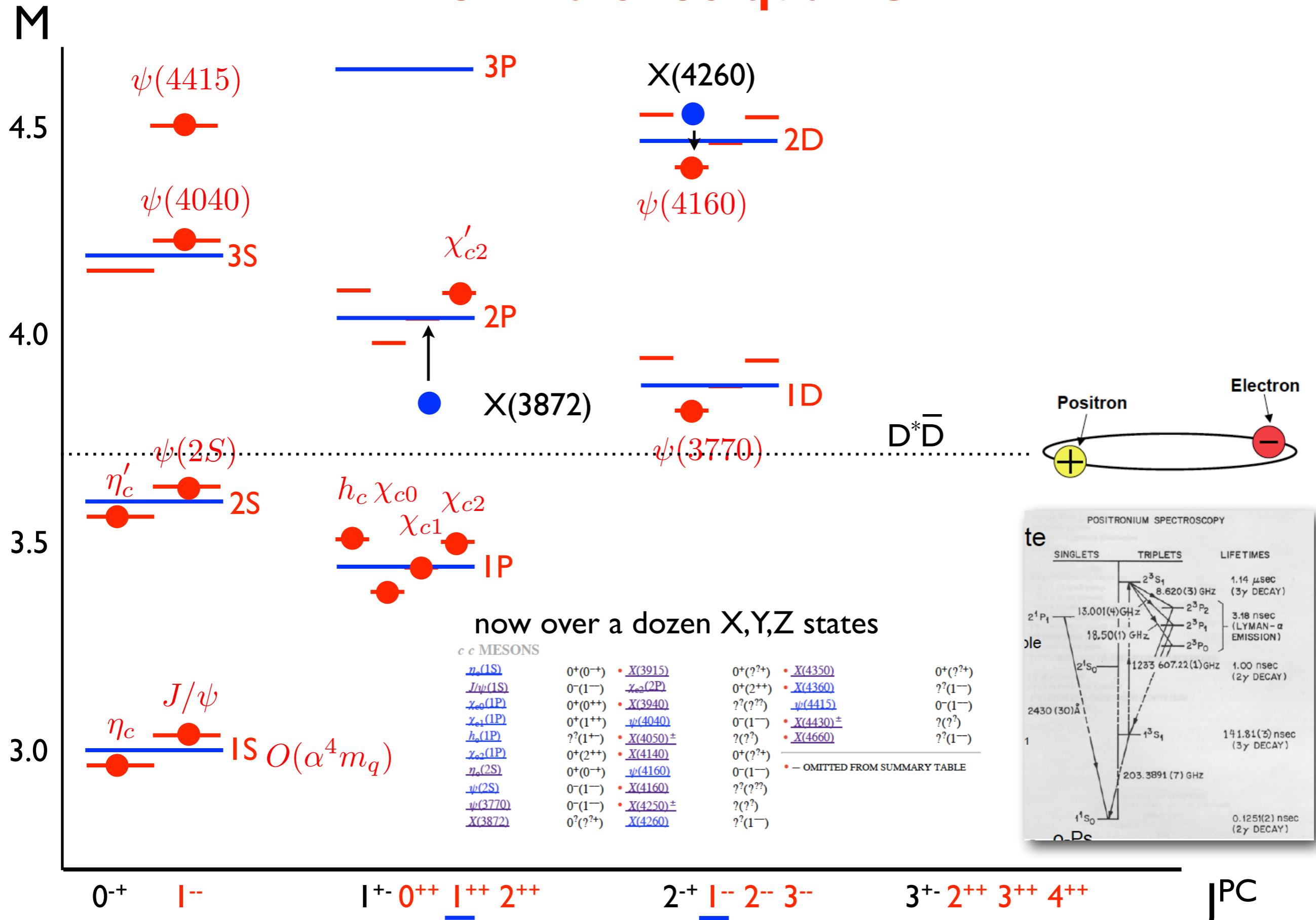
Role of reaction theory

The XYZ's and exotics

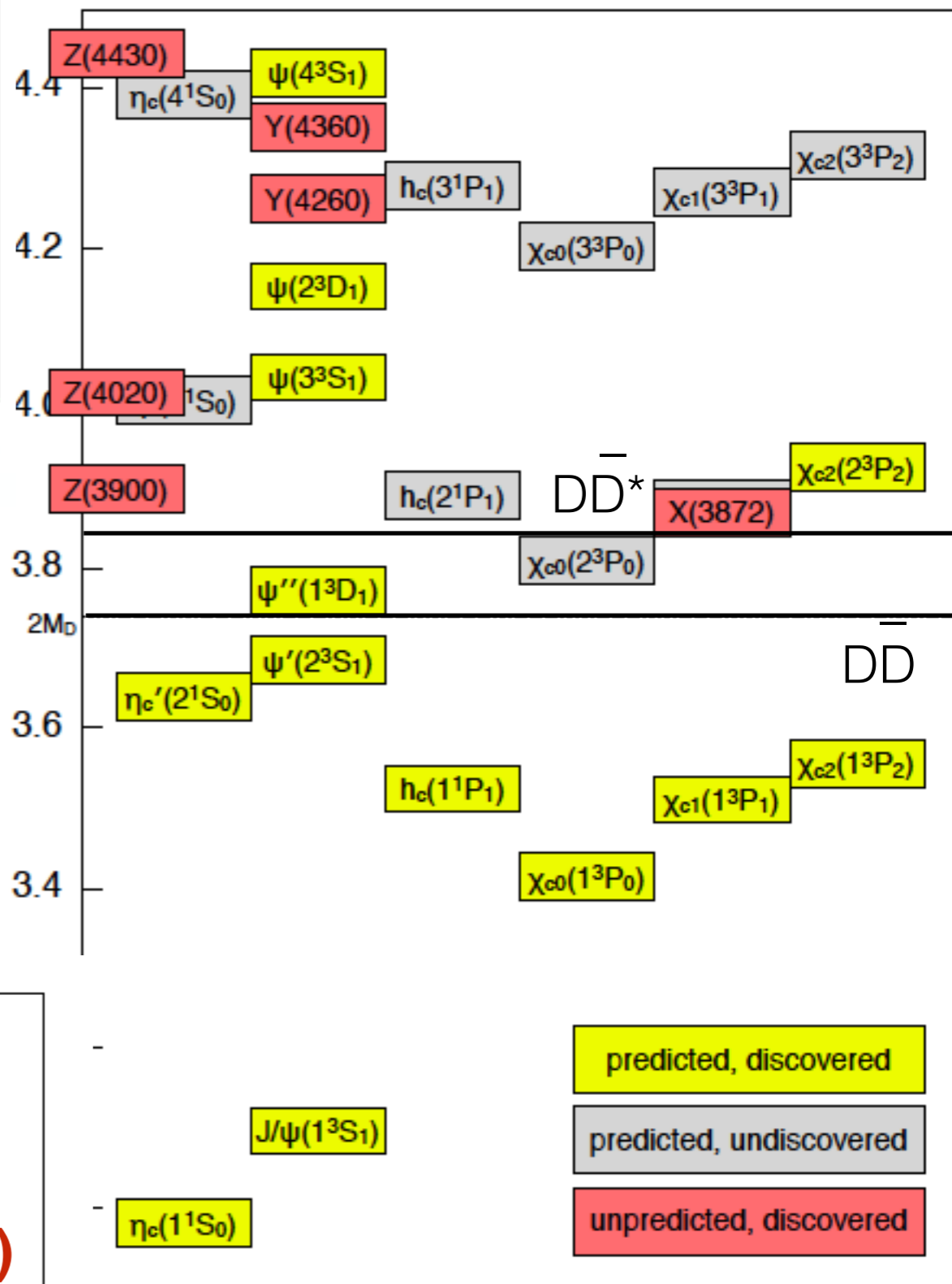
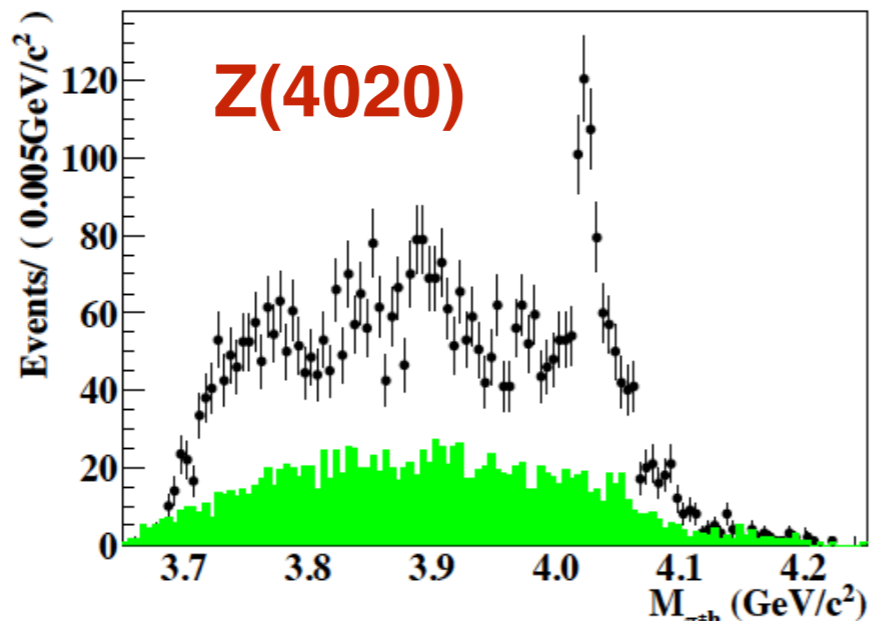
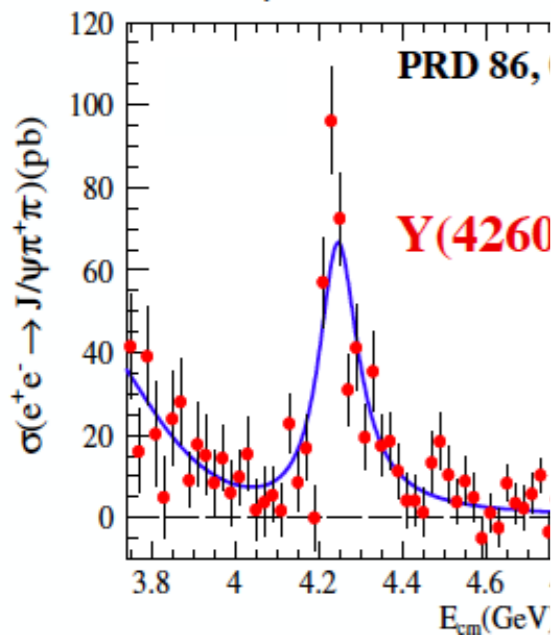
Joint Physics Analysis
Center

supported by US DOE, US NSF

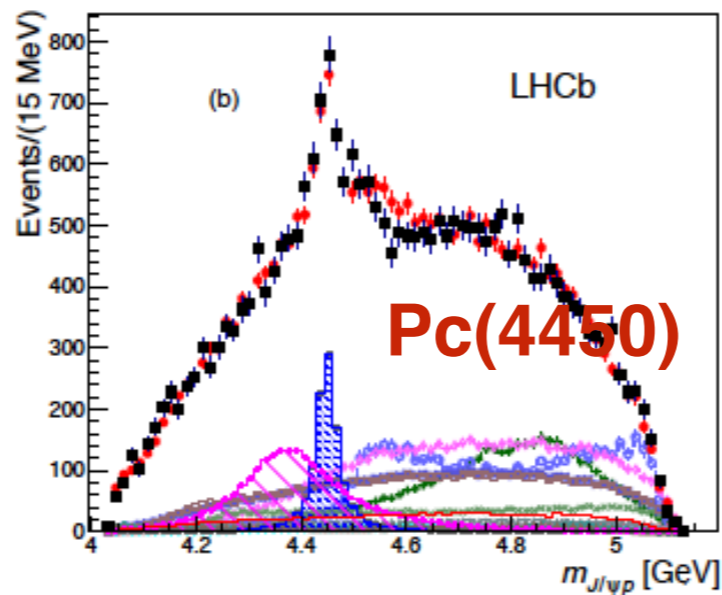
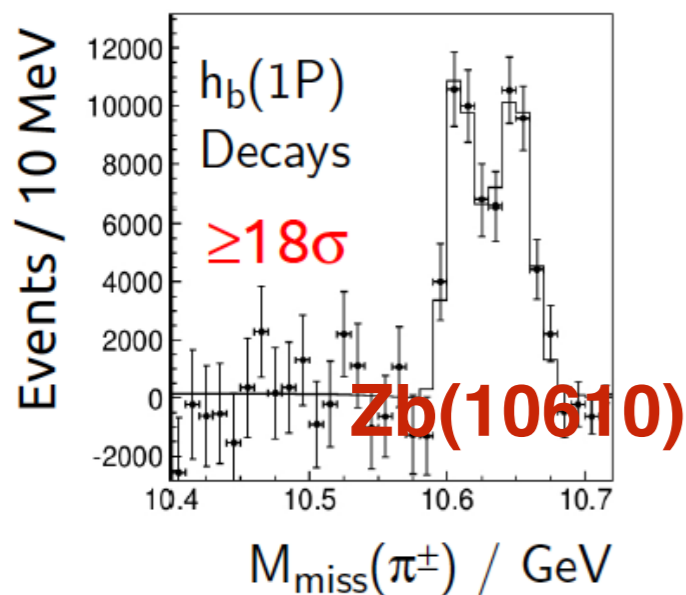
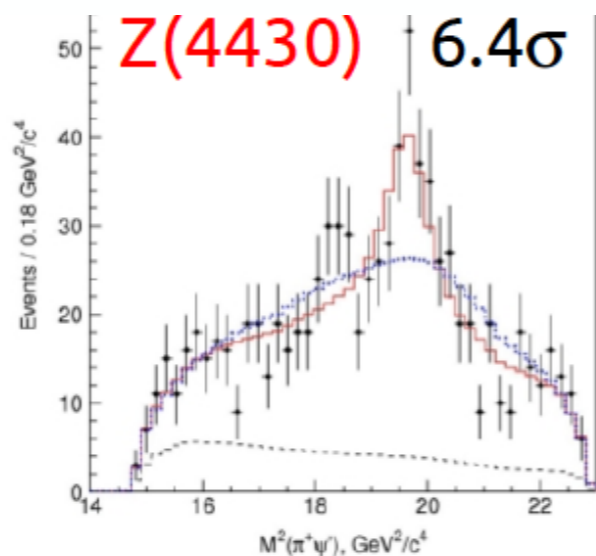
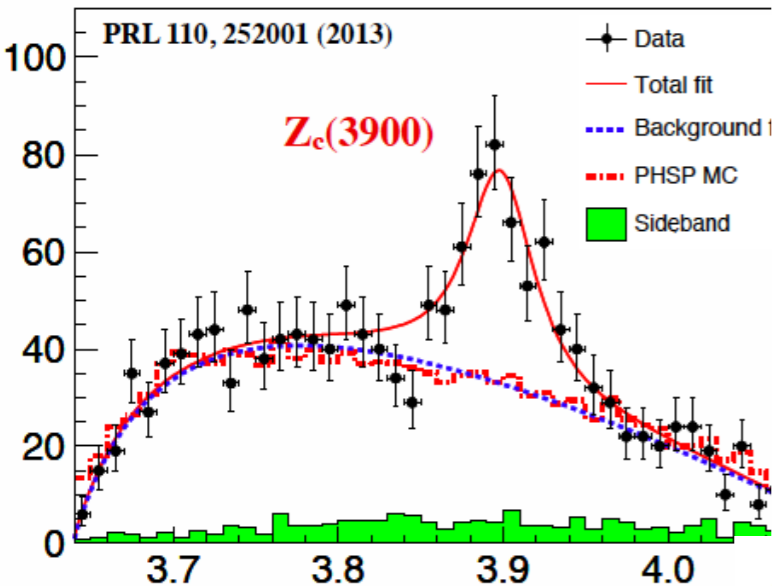
Long time ago hadrons were made from valence quarks



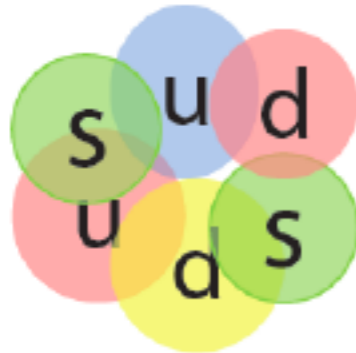
$e^+e^-(\gamma_{ISR}) \rightarrow \pi^+\pi^- J/\psi$ at BaBar



O(10) open flavor decay thresholds



before we can address the following question...



dibaryon



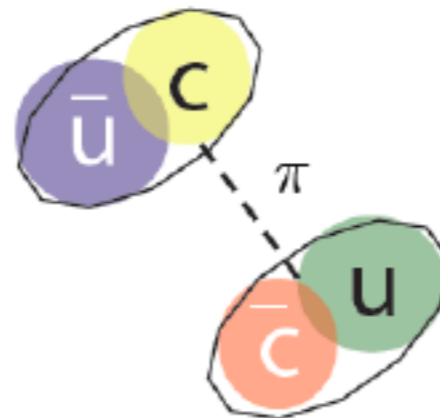
pentaquark



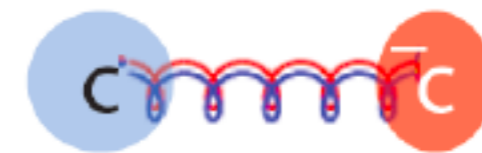
glueball



diquark + di-antiquark

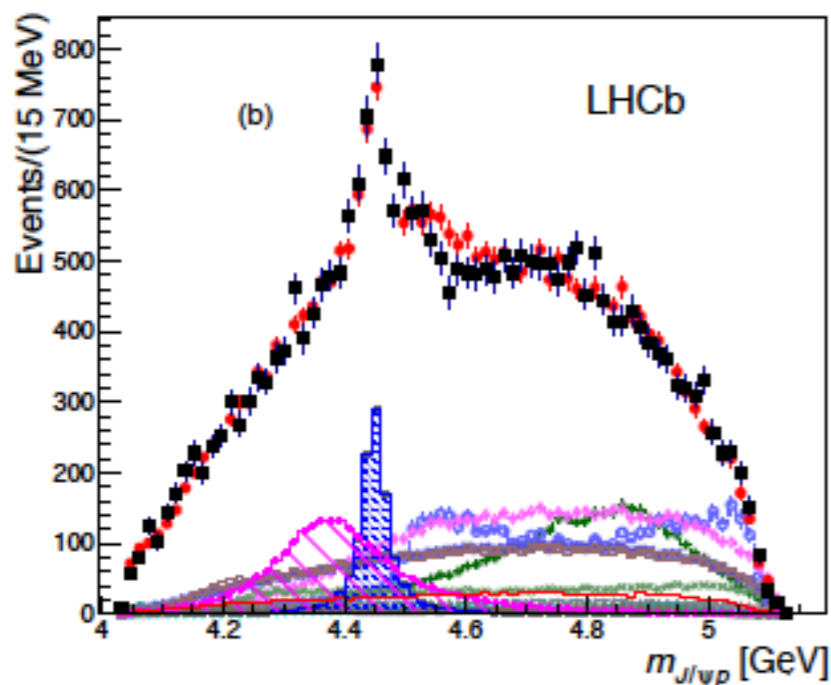
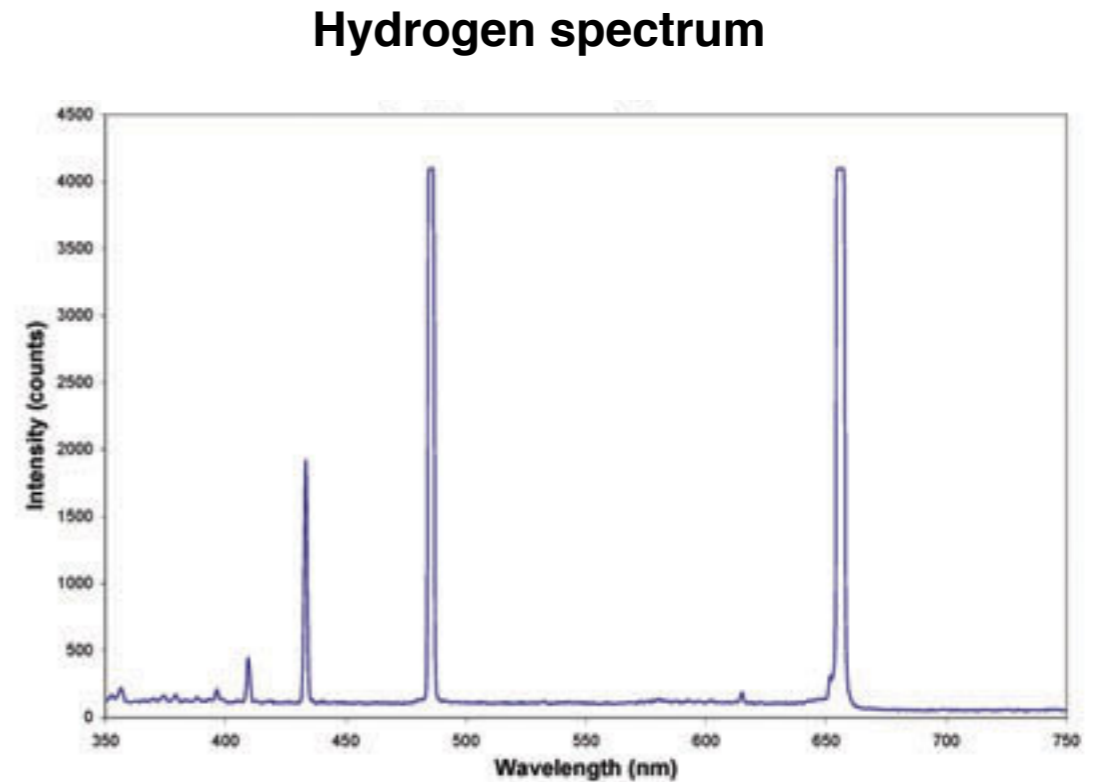
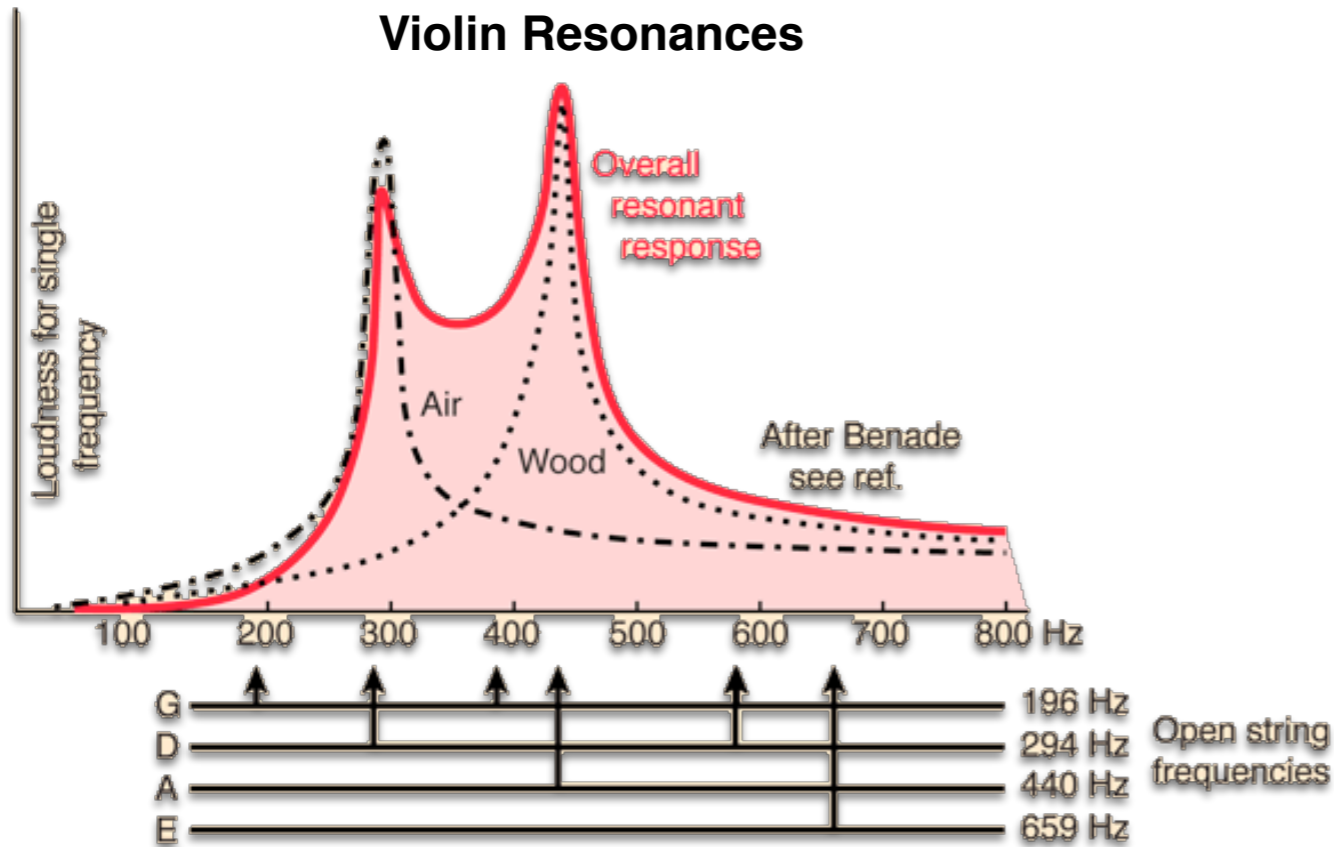


dimeson molecule

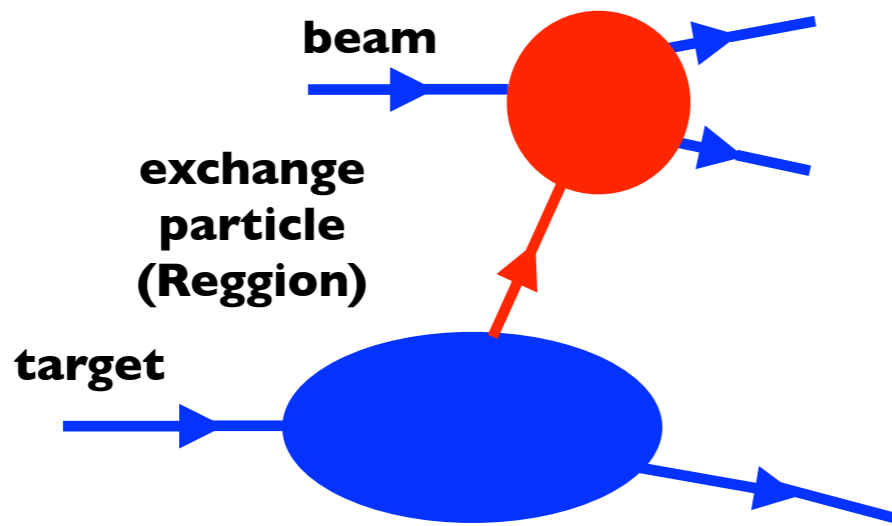


$q \bar{q} g$ hybrid

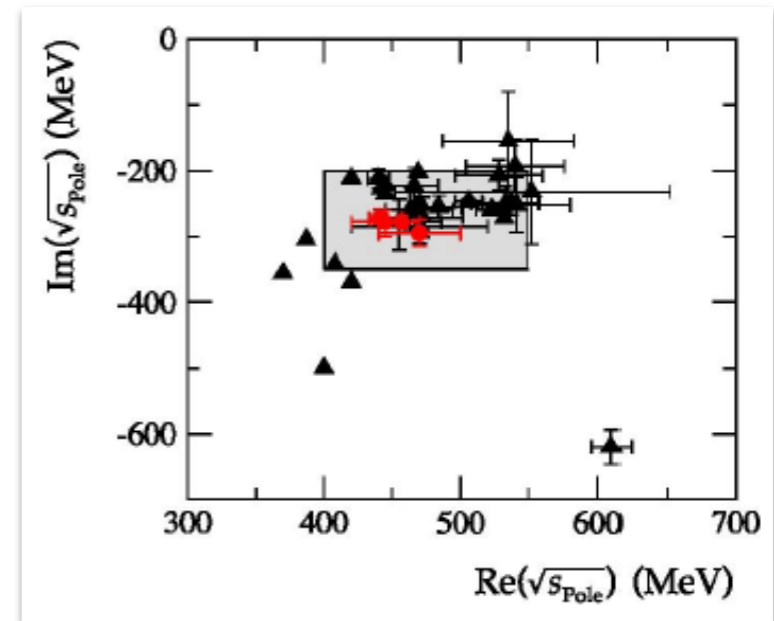
...we need to know how to interpret “peaks”



... but state of the art analyst is based on analogy with a “very simple world”

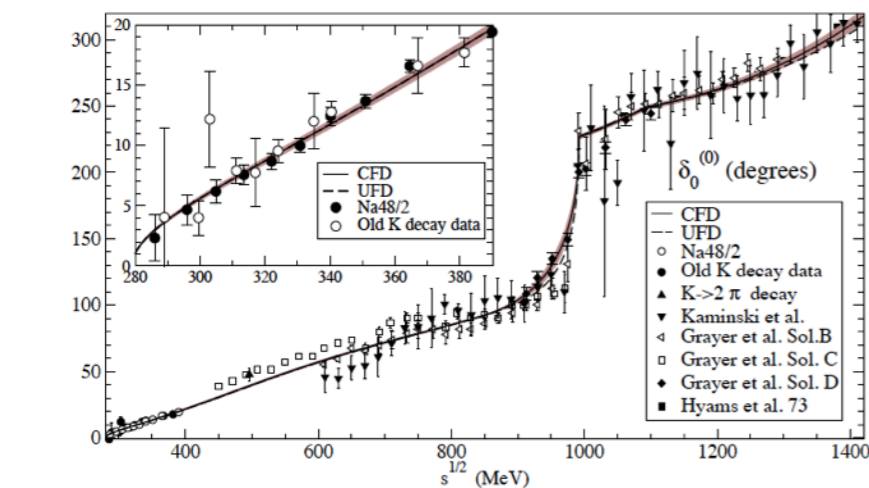
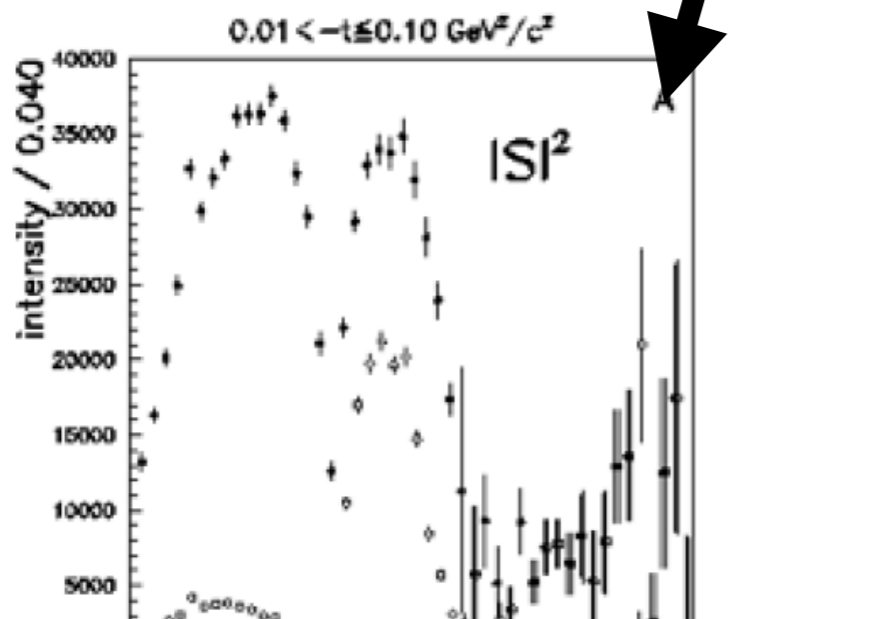


$$\sqrt{s_{\text{Pole}}} = (446 \pm 6) - i(276 \pm 5) \text{ MeV} .$$



partial wave
extraction

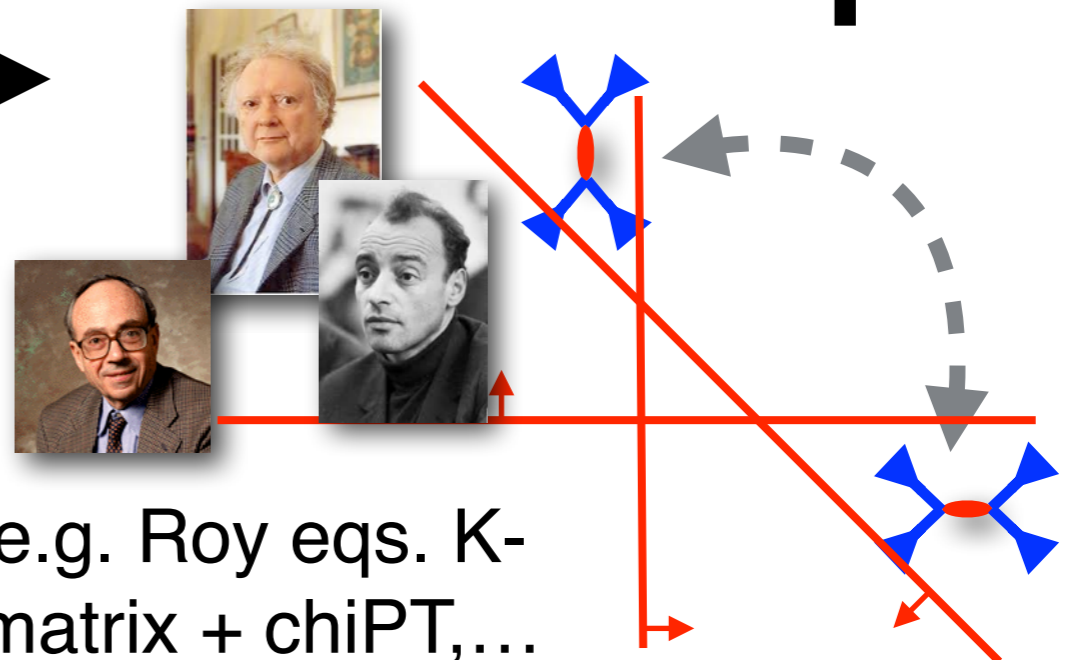
the sigma meson story



analytical
continuation



amplitude
model



e.g. Roy eqs. K-
matrix + chiPT, ...

Exploring the σ pole

Possible evidence
for non- qq nature of
light scalars

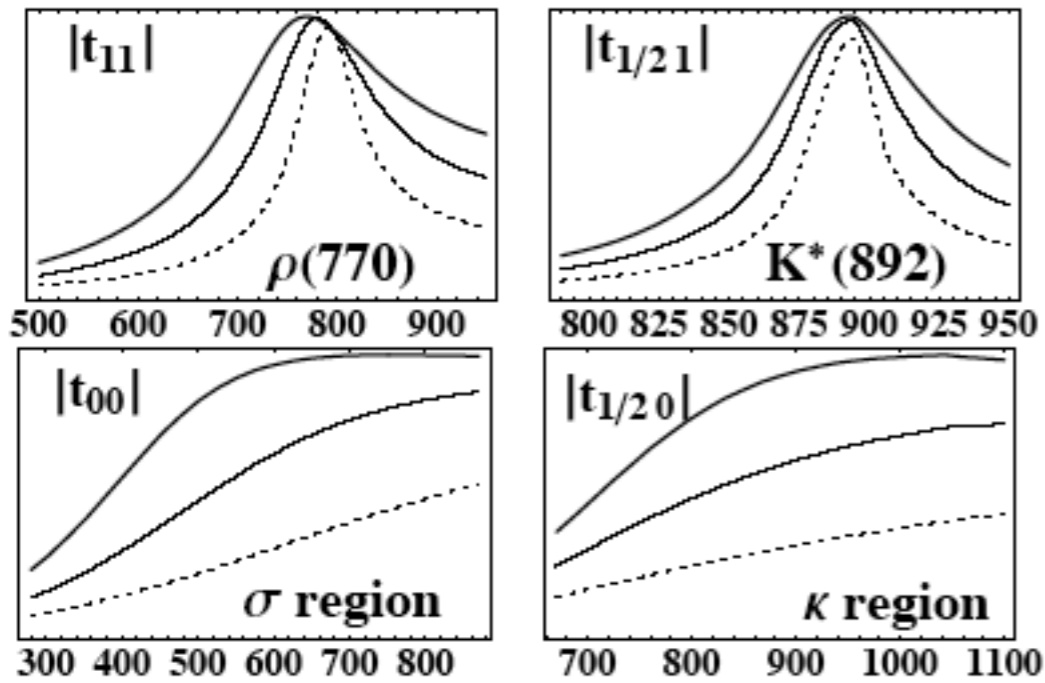
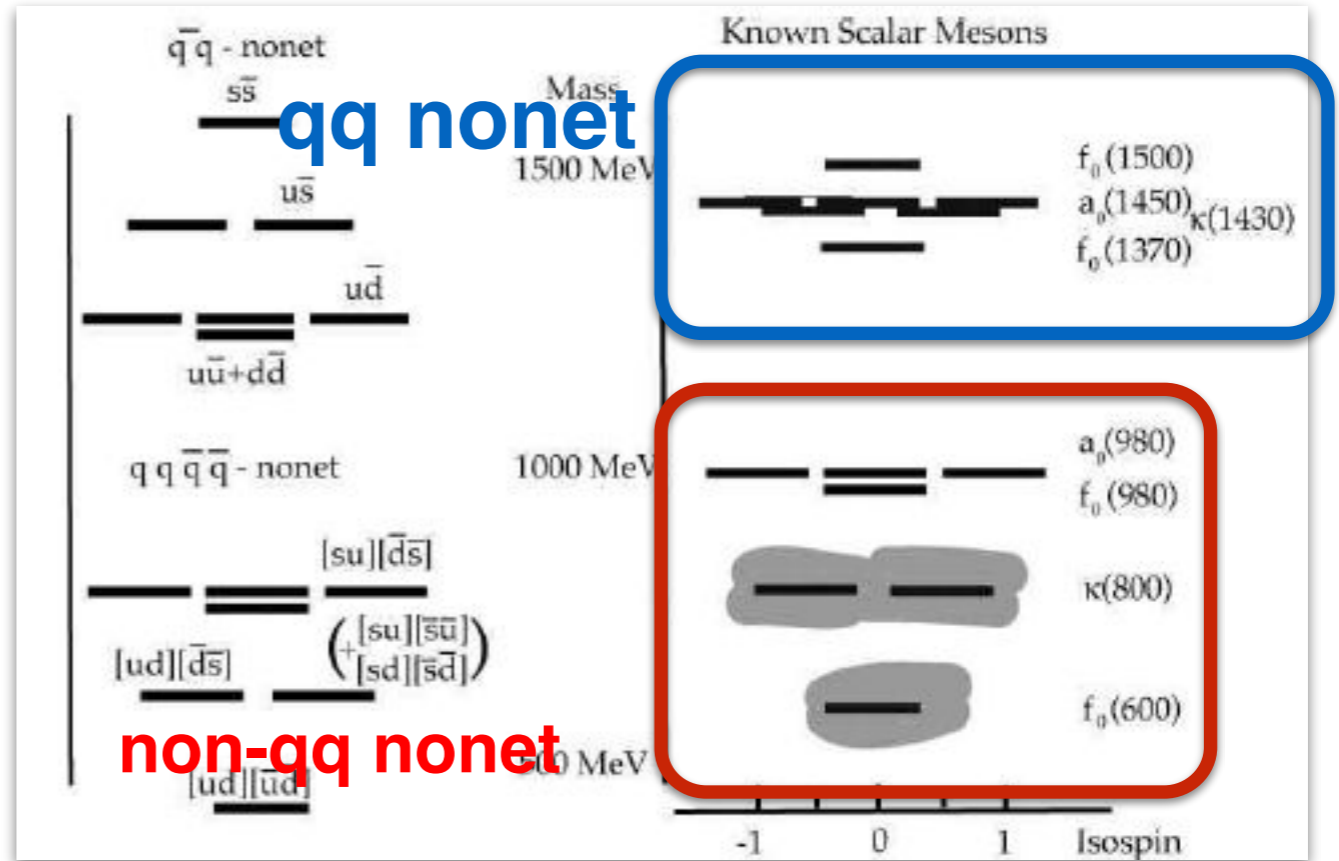
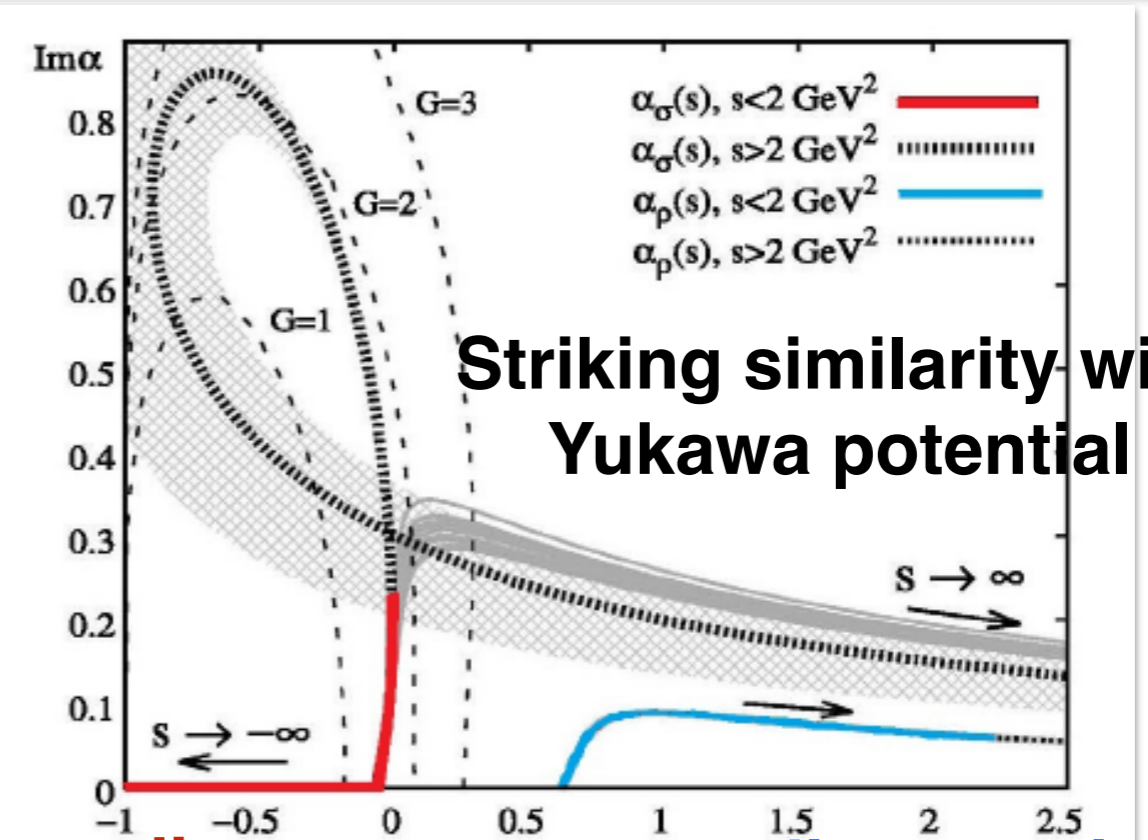


FIG. 1: Modulus of amplitudes in different meson-meson channels for $N_c = 3$ (thick line) $N_c = 5$ (thin continuous line) and $N_c = 10$ (thin dotted line), scaled at $\mu = 770$ MeV.

Pelaez



Striking similarity with
Yukawa potential

non-ordinary σ

ordinary trajectory

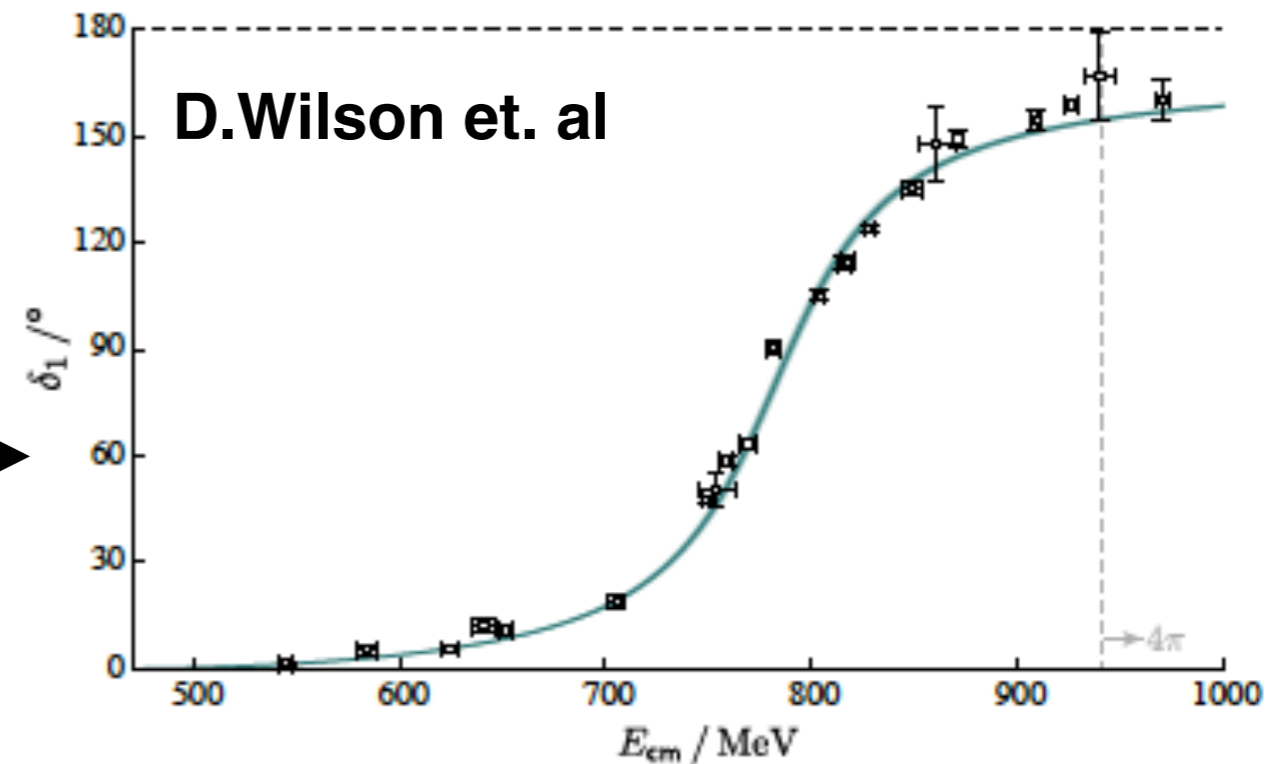
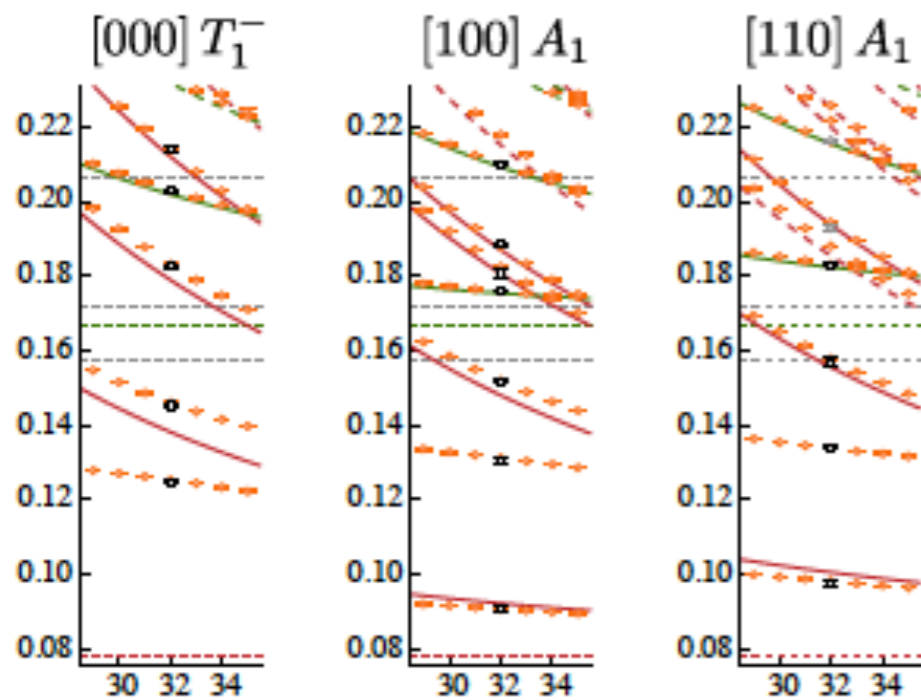
QCD on the Lattice : simulated scattering experiment

(known kinematical function)

$$Z(E_i) = T(E_i)$$

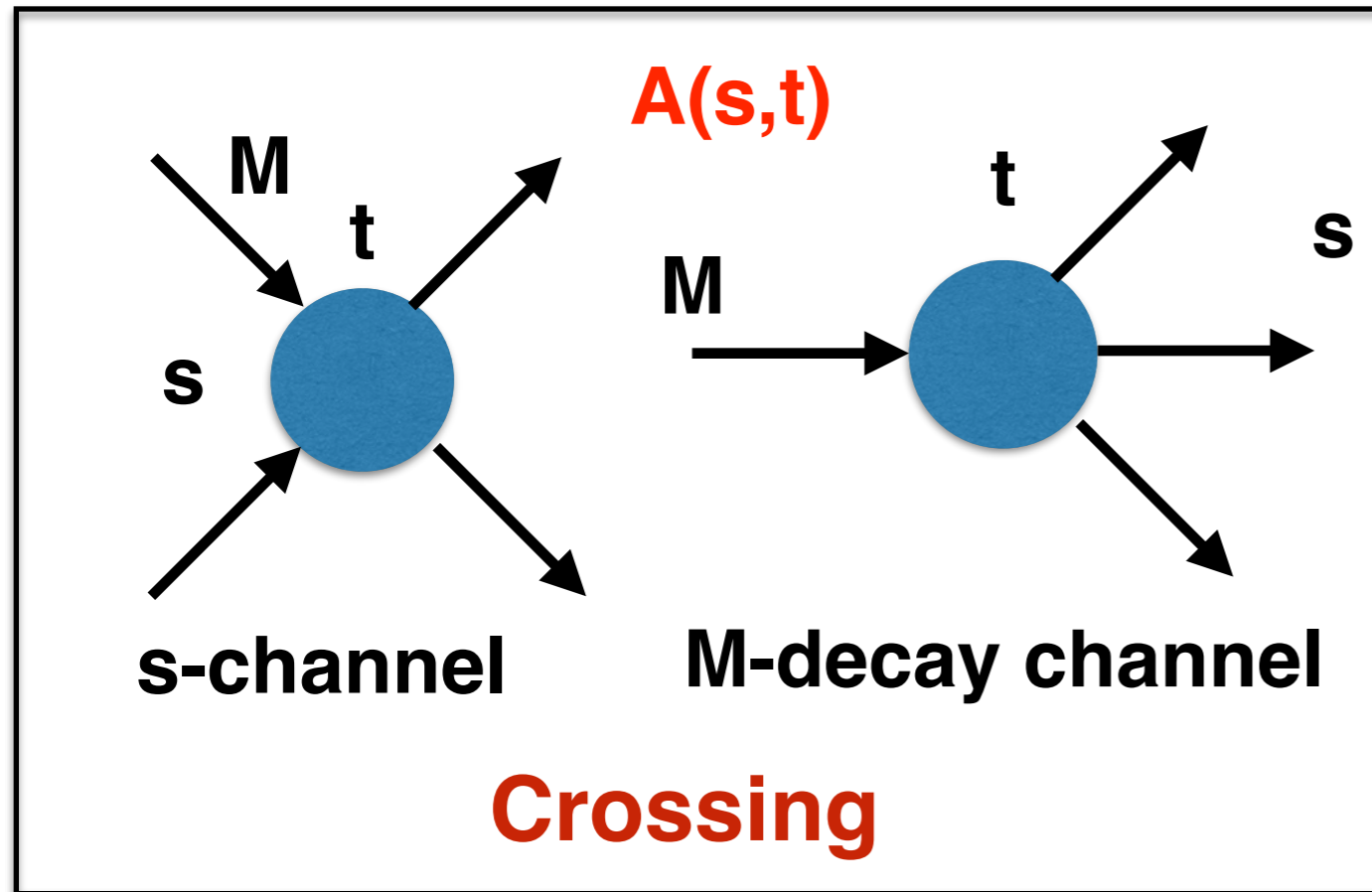
(infinite volume amplitude)

E_i = discrete energy spectrum of states in the lattice



in general “solution” of the Lusher condition requires an analytical model for T

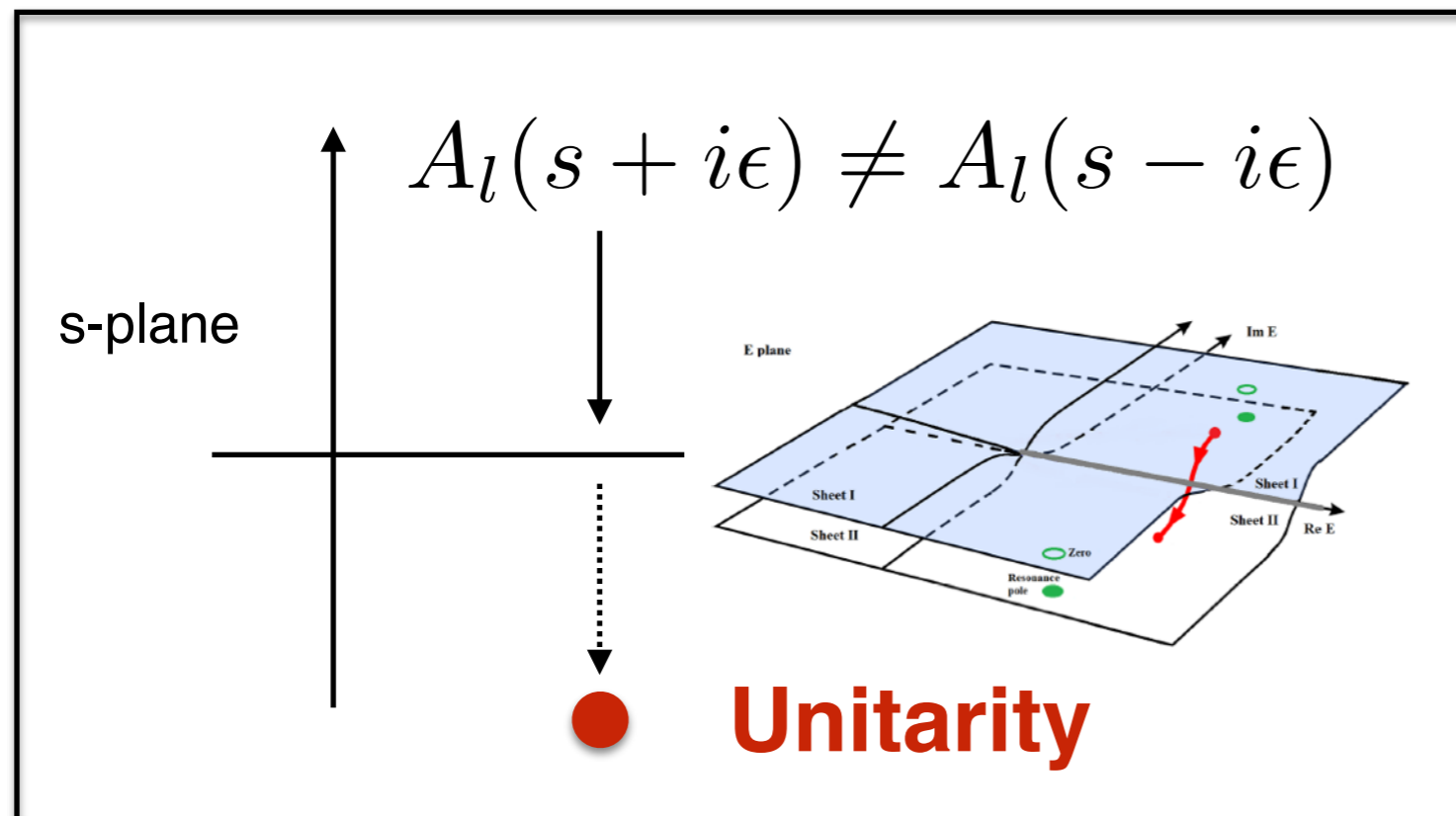
S-matrix principles: Crossing, Analyticity, Unitarity



$$A(s, t) = \sum_l A_l(s) P_l(z_s)$$

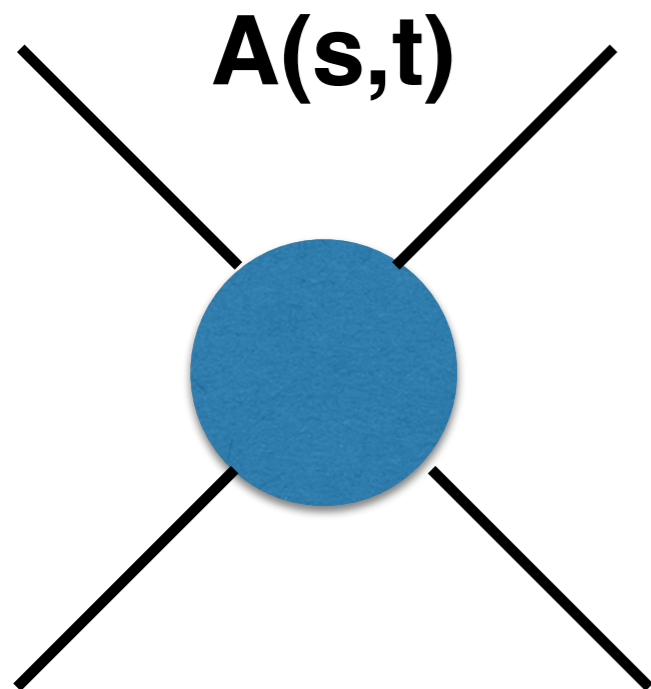
Analyticity

$$A_l(s) = \lim_{\epsilon \rightarrow 0} A_l(s + i\epsilon)$$



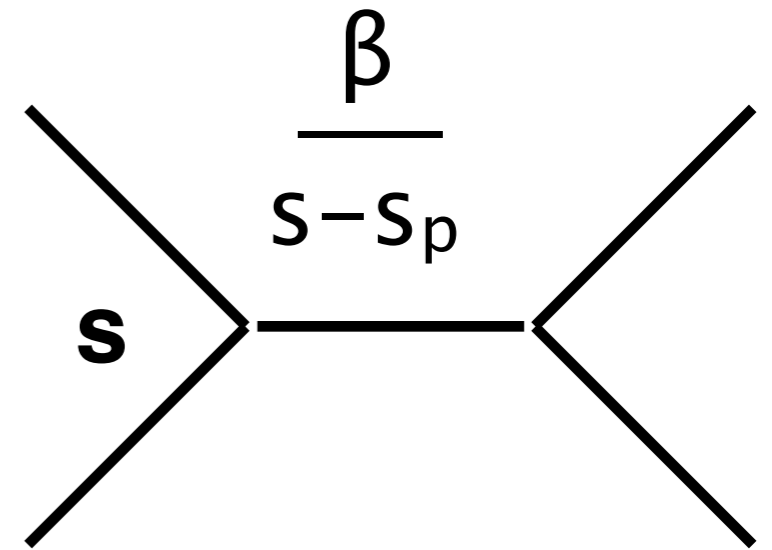
bumps/peaks on the real axis (experiment) come from singularities in the complex domain.

Origin of singularities (exchanges constrained by unitarity)

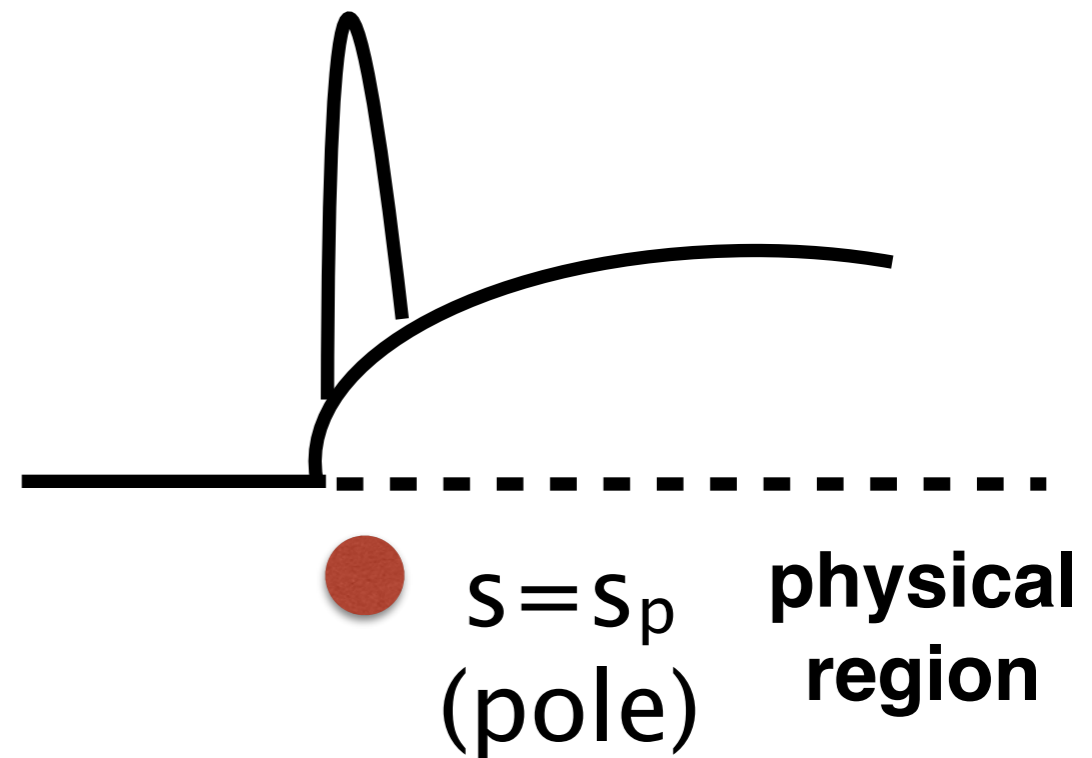


$$\Lambda_b \rightarrow \overline{K^-} p J/\psi$$

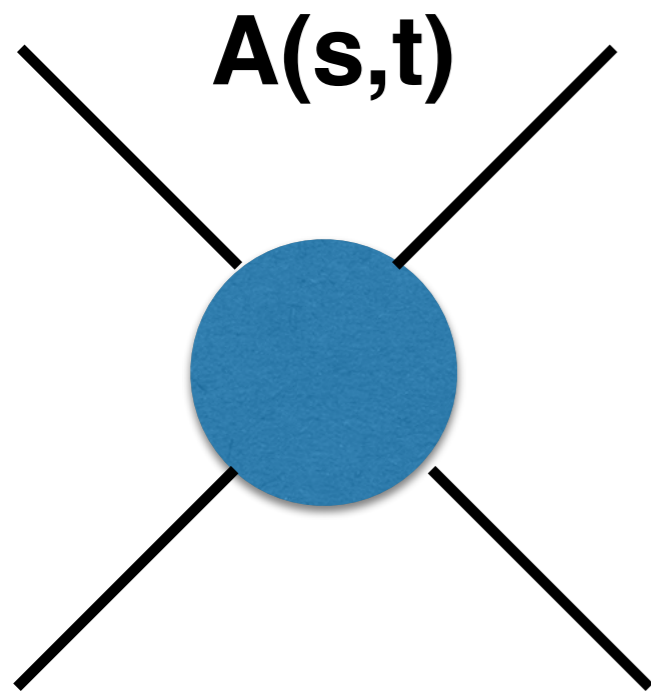
The diagram shows the reaction $\Lambda_b \rightarrow \overline{K^-} p J/\psi$. The $\overline{K^-}$ and J/ψ are underlined in red. The t channel is indicated above the $\overline{K^-}$ line, and the s channel is indicated below the p line.



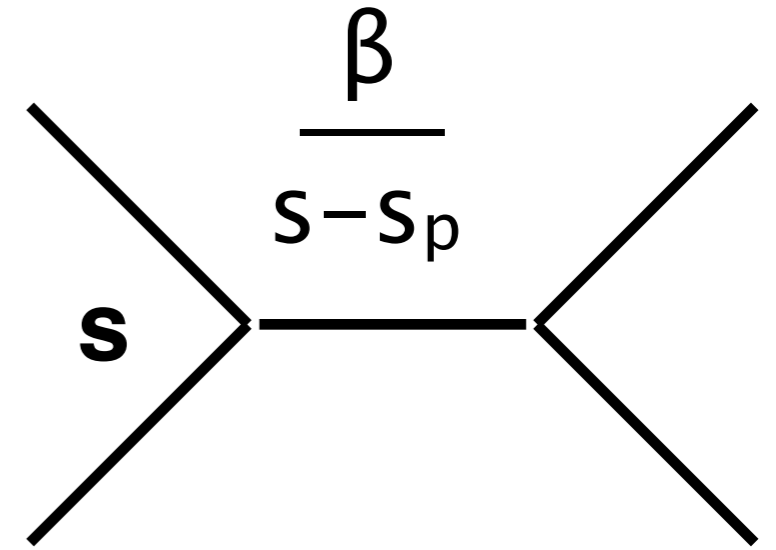
$A_I(s)$



Origin of singularities (exchanges constrained by unitarity)

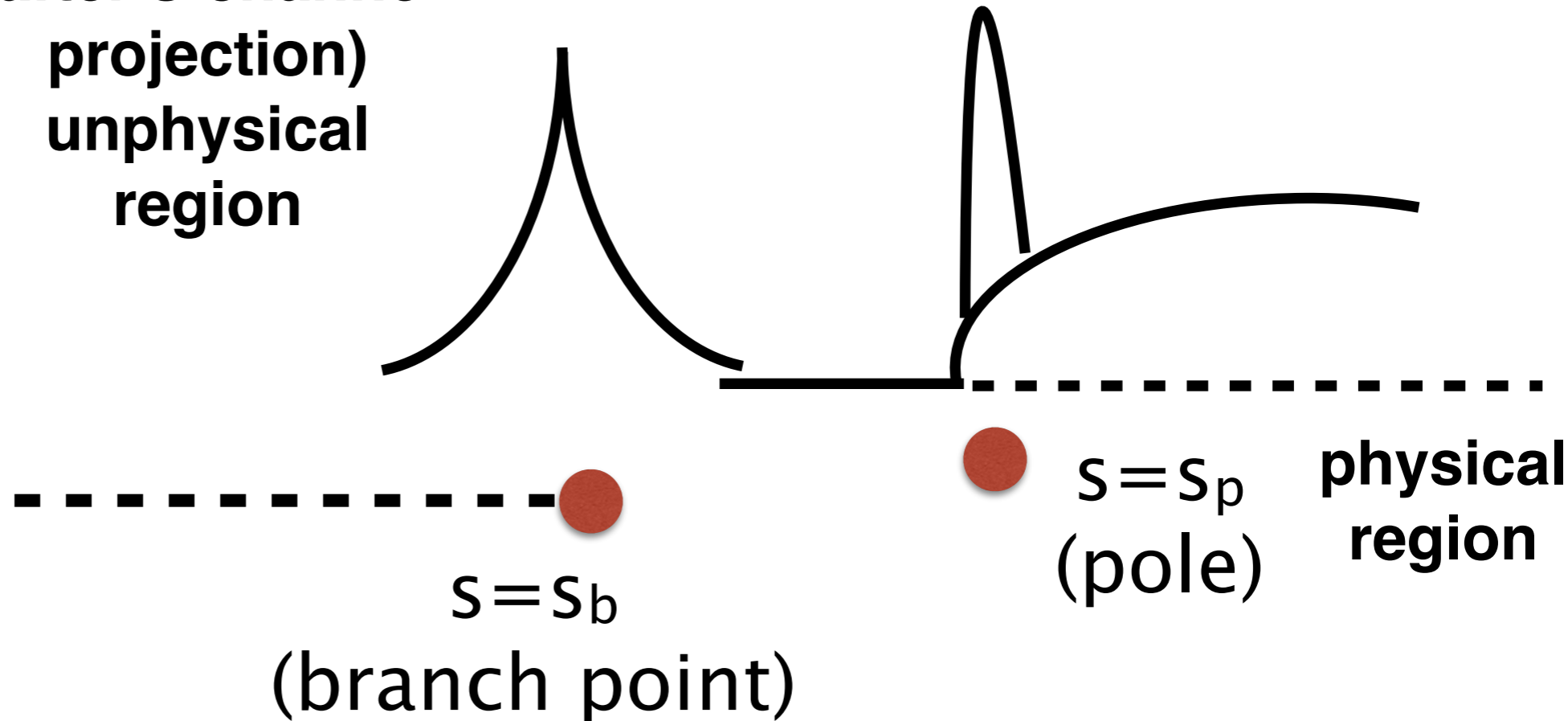
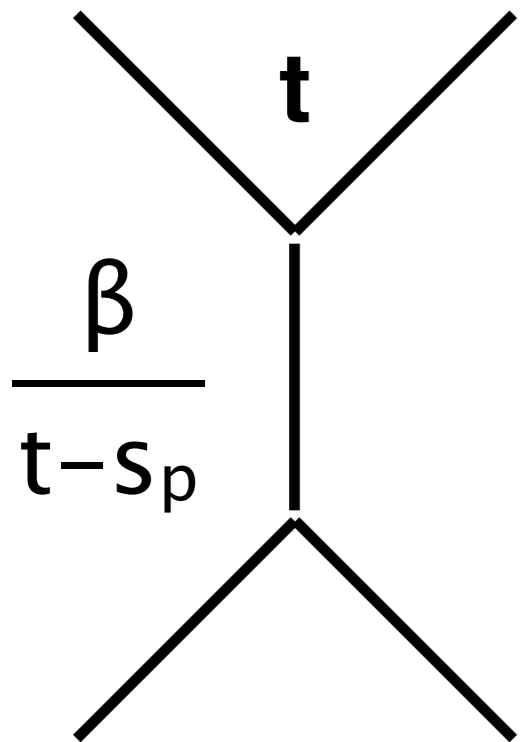


$$\Lambda_b \rightarrow \overline{K^-} p J/\psi$$

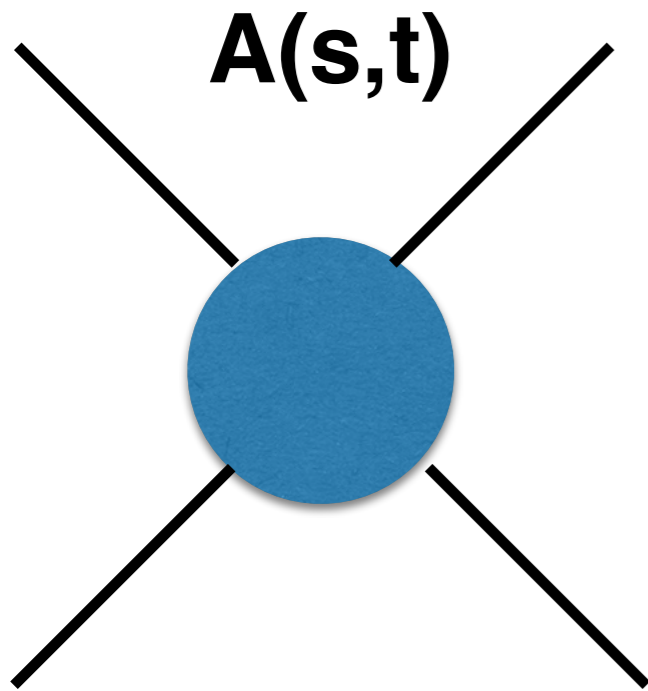


A_I(s)

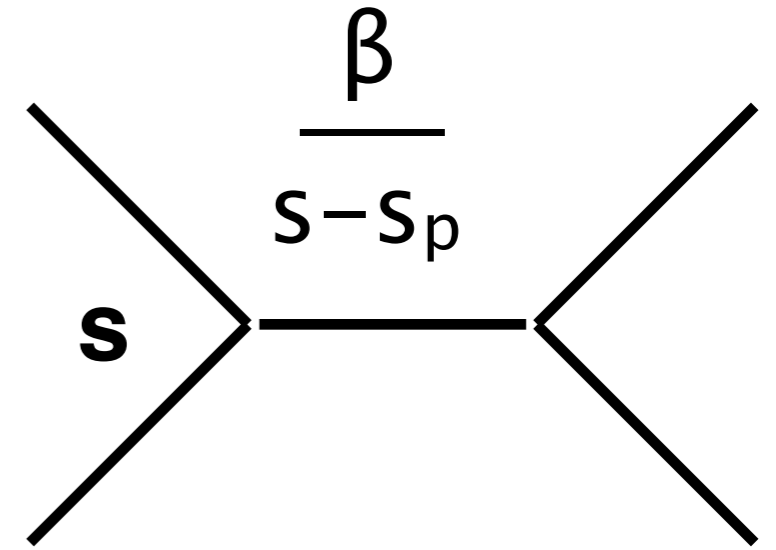
(after s-channel projection)
unphysical region



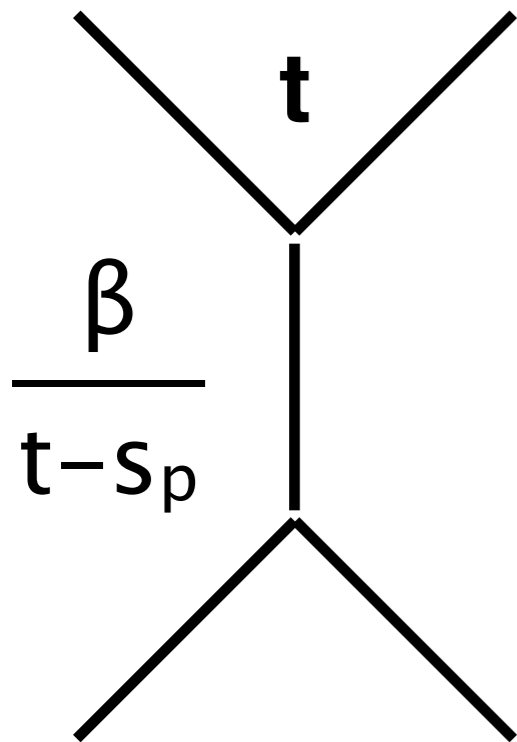
Origin of singularities (exchanges constrained by unitarity)



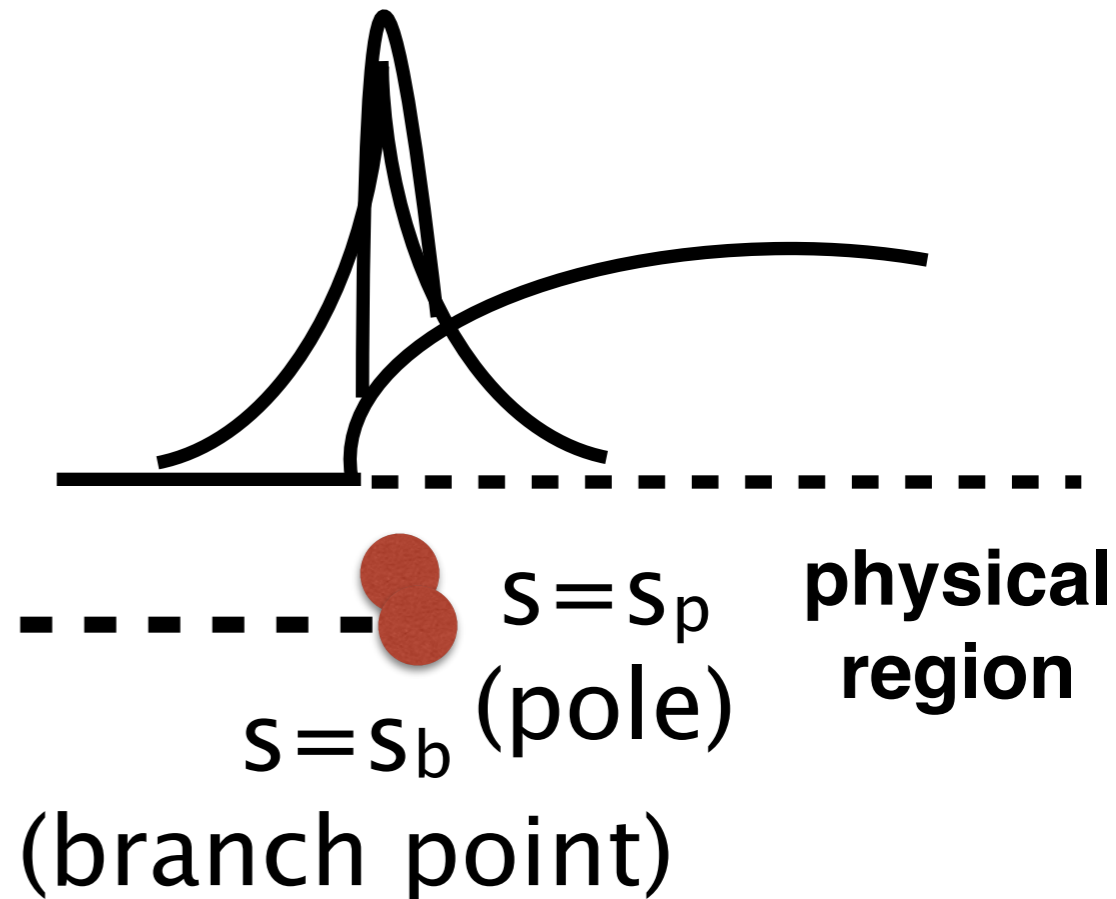
$$\Lambda_b \rightarrow \overline{K^-} p J/\psi$$



(after s-channel projection)
unphysical region



$A_I(s)$

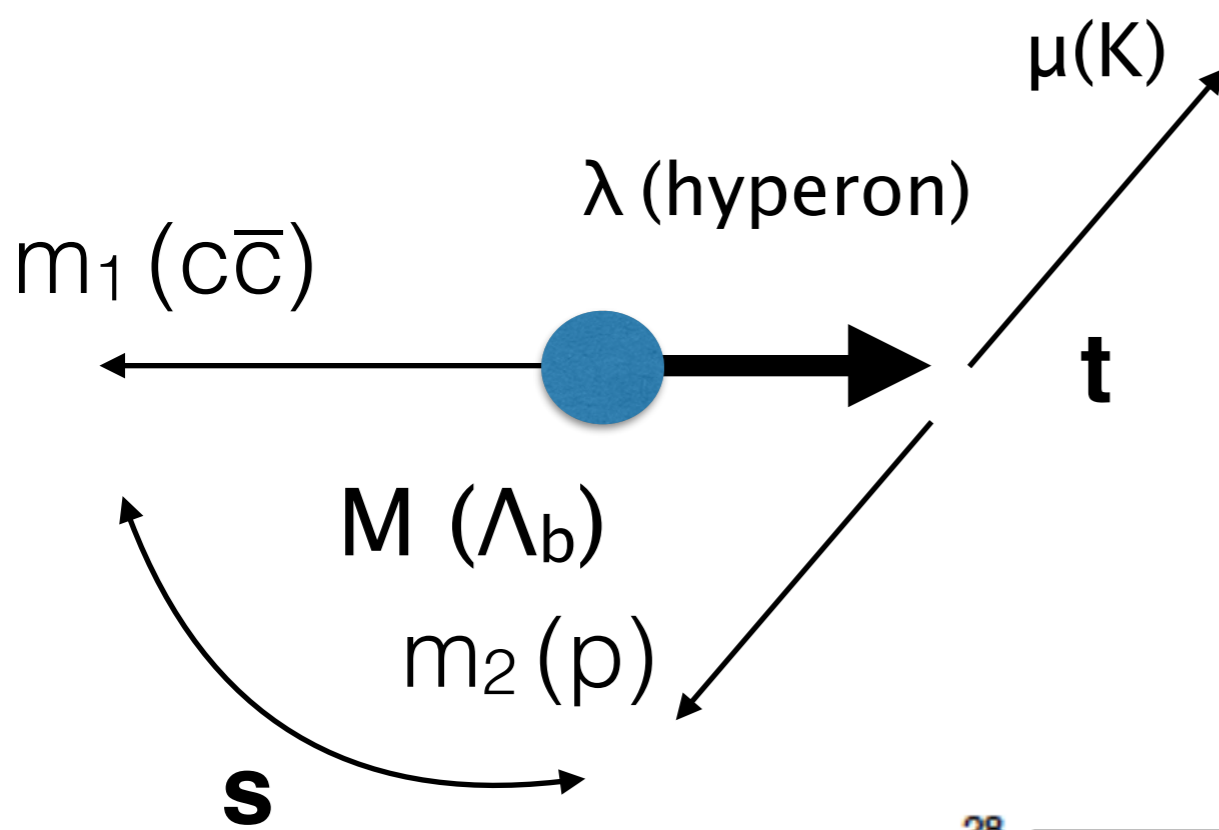


Coleman-Norton theorem

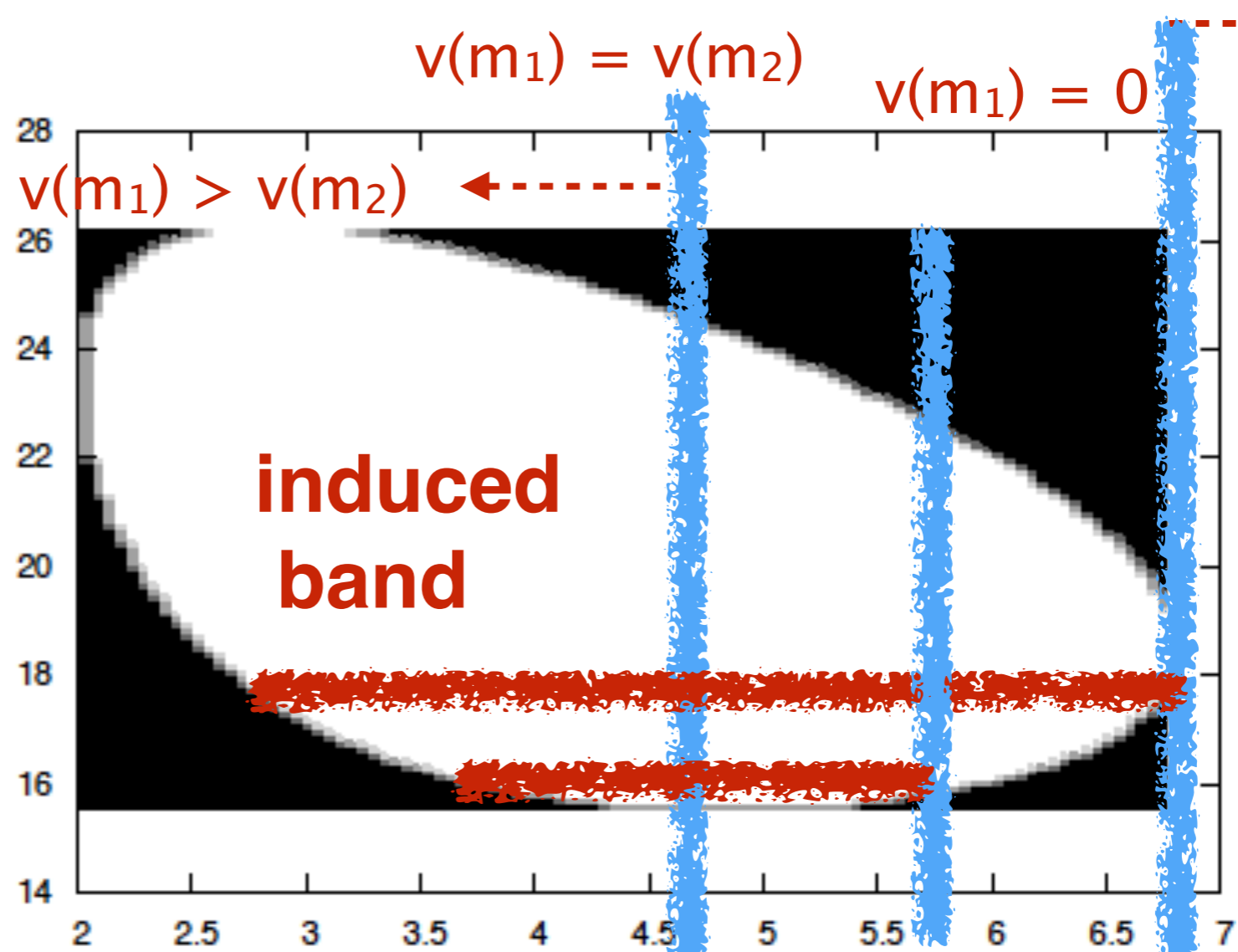
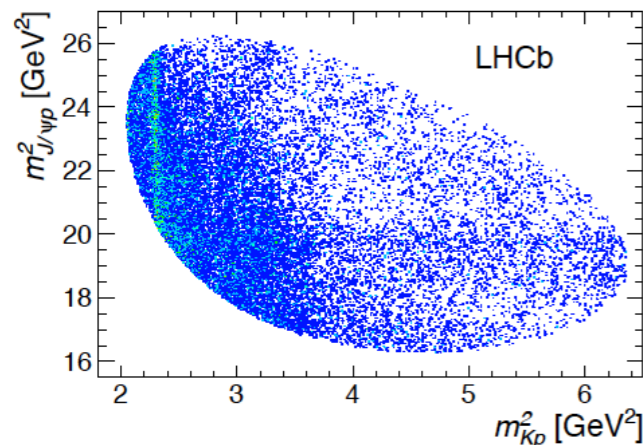
t-channel resonance can produce s-channel “band” if:

$\lambda_{\min}^2 = t$ @ Streshold
and u_{\max}

λ off-shell



all particles on-shell
 m_2 and m_1 collinear
 $v(m_2) > v(m_1)$

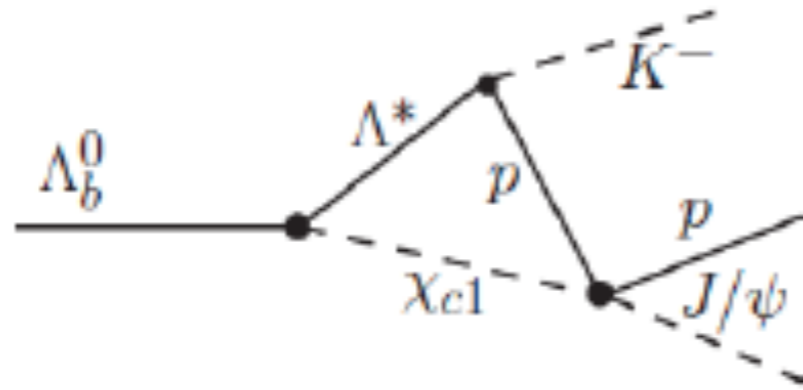


induced band

$$\lambda_{\max}^2 = (M - m_1)^2 = t_{\max}$$

s **t**

The key to the YZ phenomena are the many nearby channels



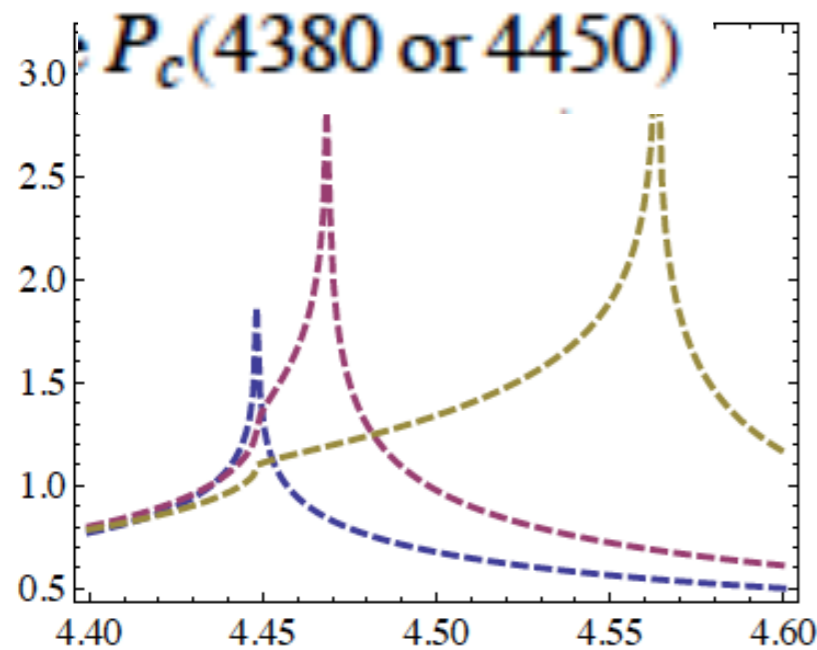
$$M_{\Lambda_b^0} = 5.6195, \mu_{K^-} = 0.4937, m_1 = m_{\chi_{c1}} = 3.510, m_2 = m_p = 0.93827$$

$$\lambda = m_{\Lambda^*} = 1.89 \text{ (they take)}$$

Coleman-Norton requires

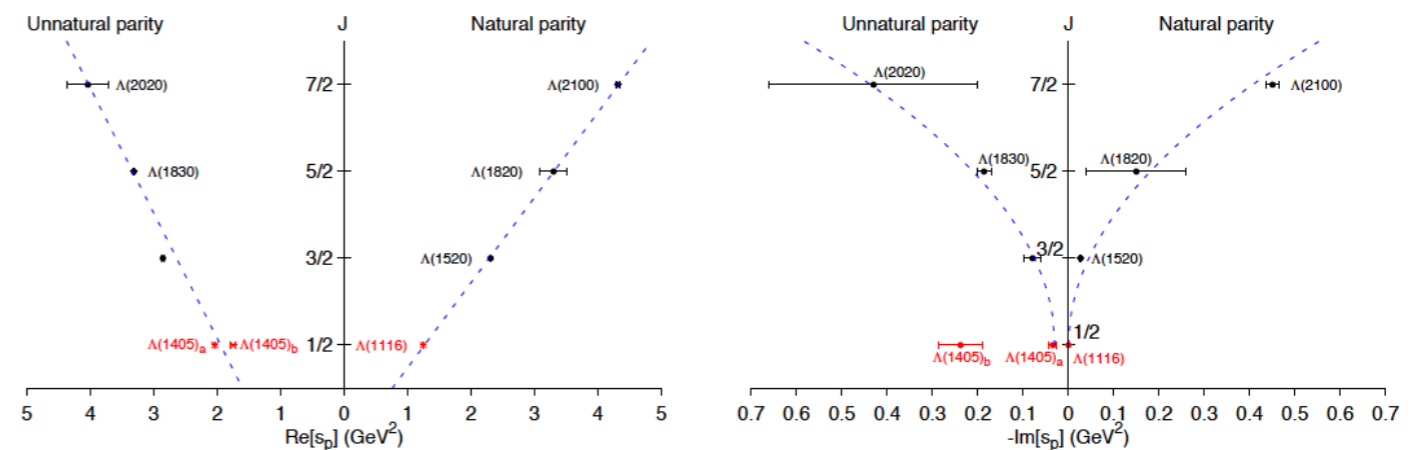
$$1.89 < \lambda < 2.11 \text{ GeV}$$

$$4.45 < \sqrt{s_{\text{peak}}} < 4.65 \text{ GeV}$$

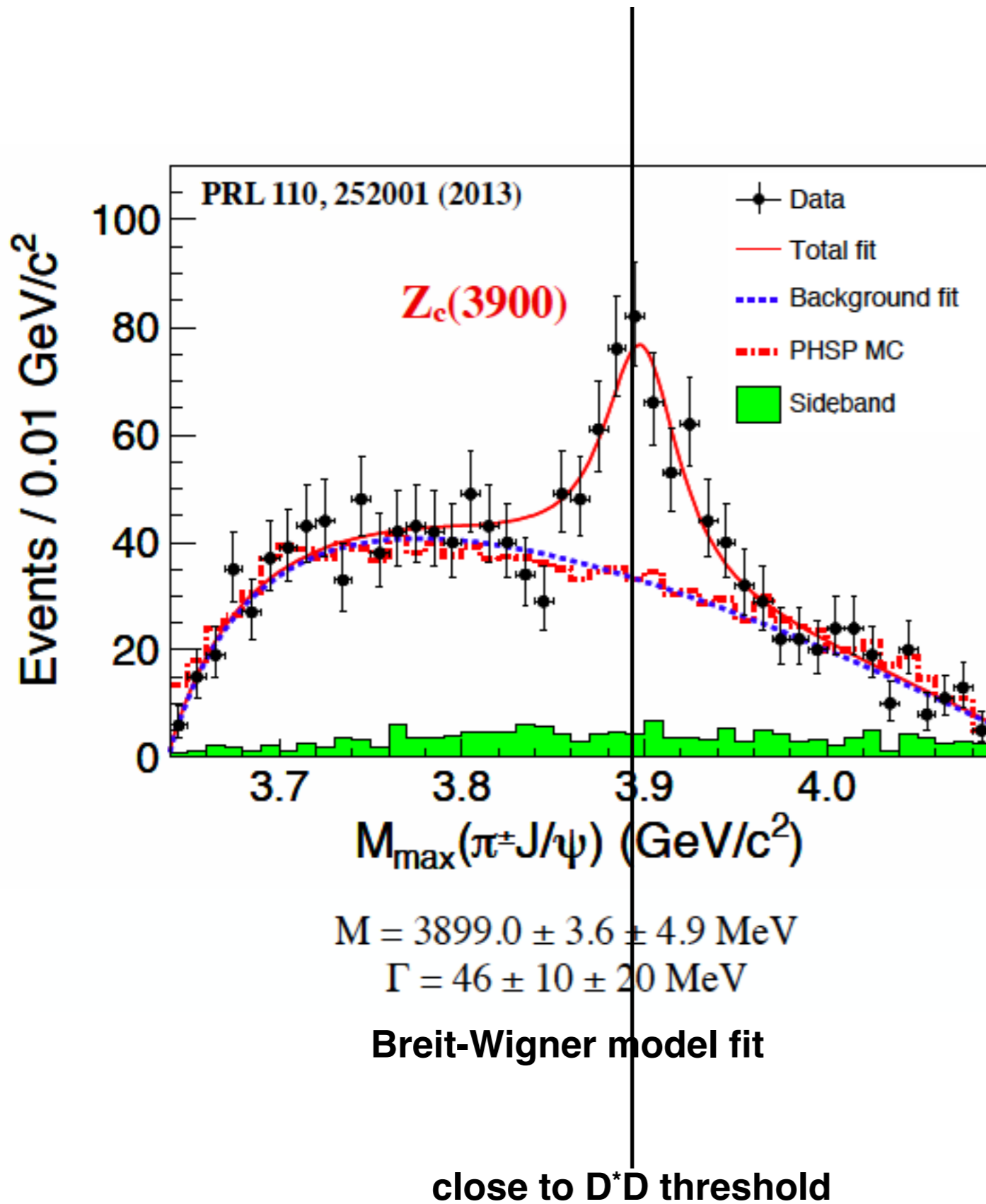


Axes : $\text{Abs}[T(s)], \sqrt{s}$

Lines : blue ($\lambda = 1.89 \text{ GeV}$), red ($\lambda = 1.99 \text{ GeV}$), yellow ($\lambda = 2.09 \text{ GeV}$)



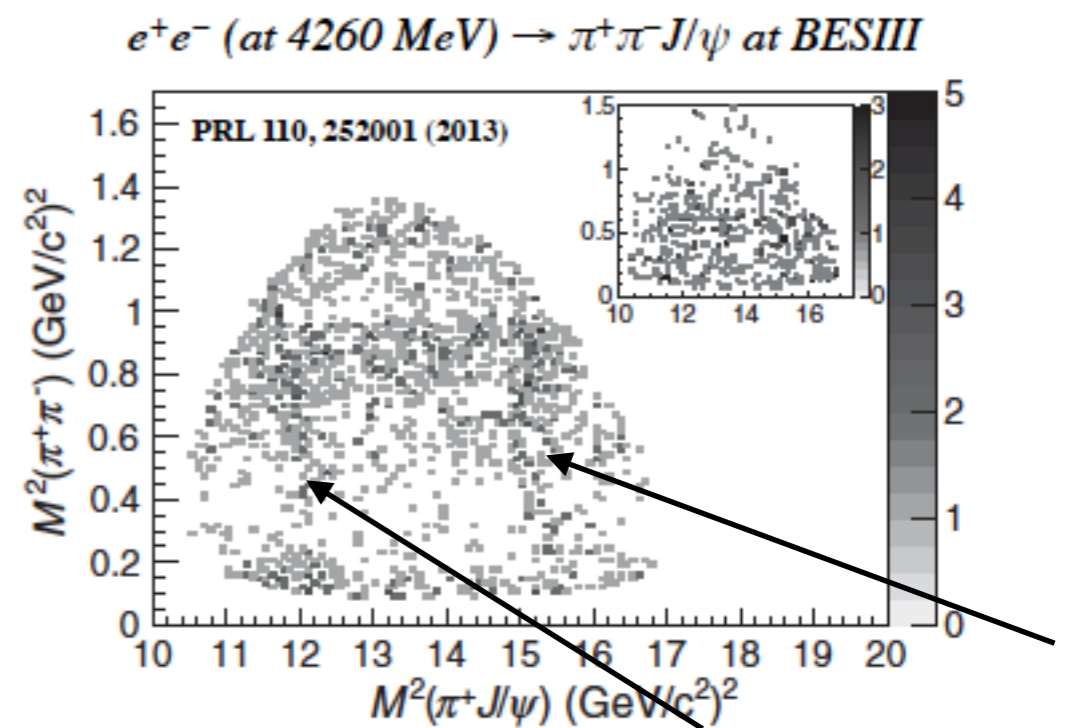
$Z_c(3900)$ Charged charmonium ?



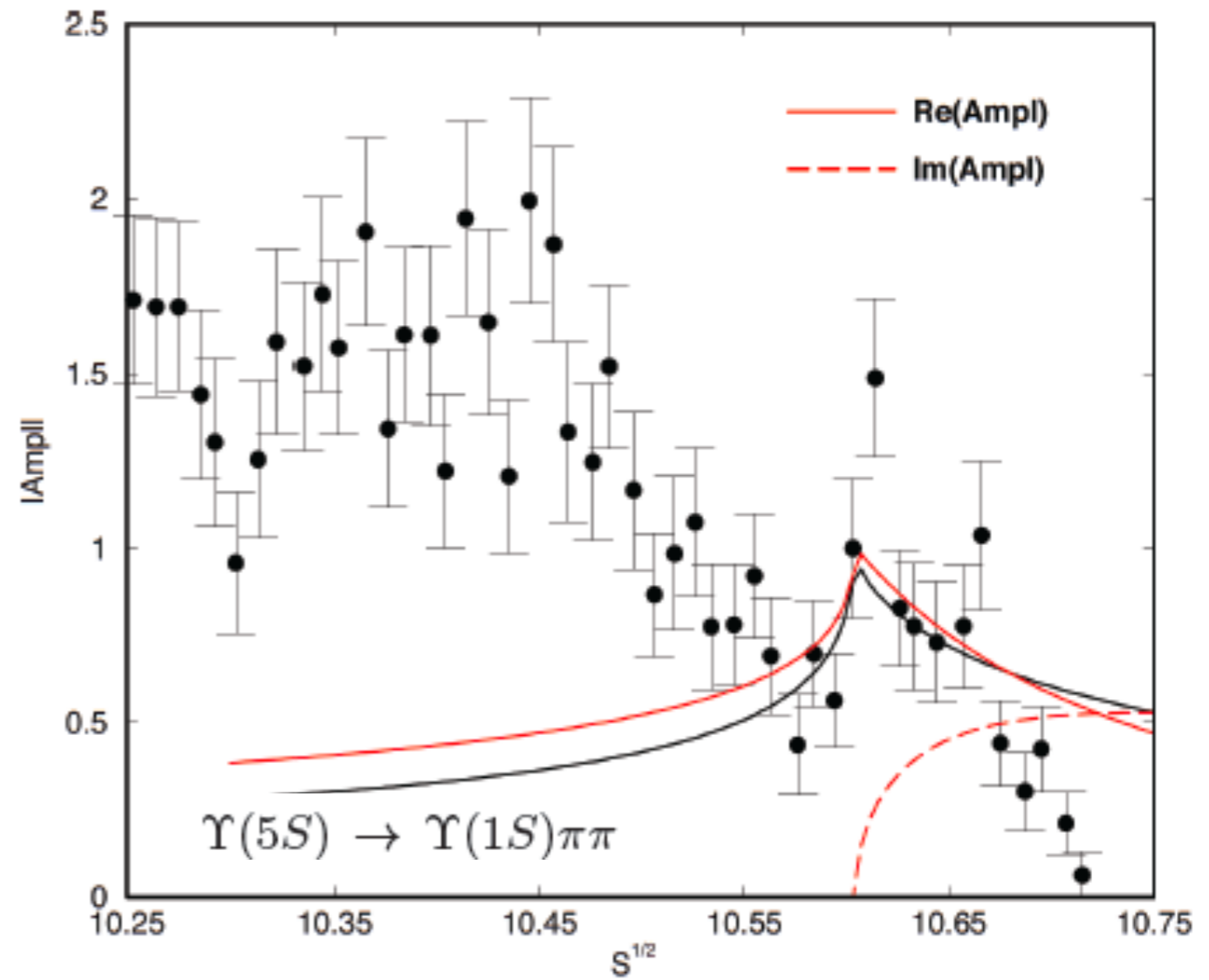
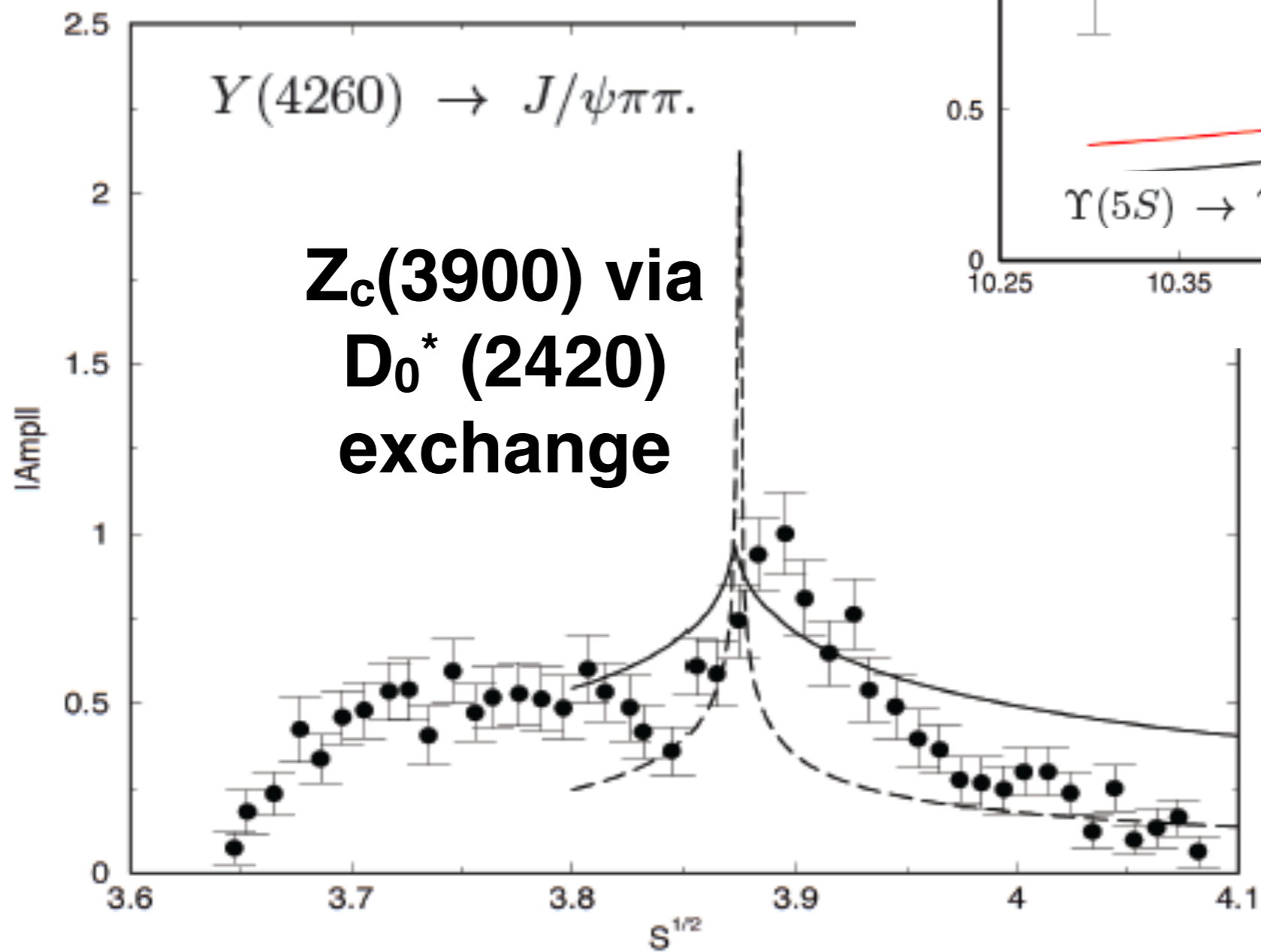
$$e^+e^- \rightarrow Y(4260)$$

$$\rightarrow \pi^+ Z_c^-(3900)$$

$$\rightarrow \pi^+ \pi^- J/\psi$$

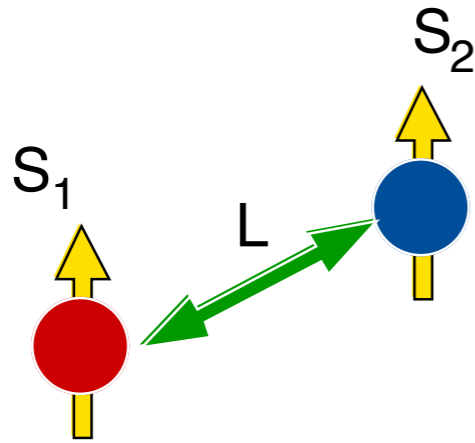


coupling to DD^*



**$Z_b(10610)$
via
 $B_J^{**}(5698)$
exchange**

Gluon excitations

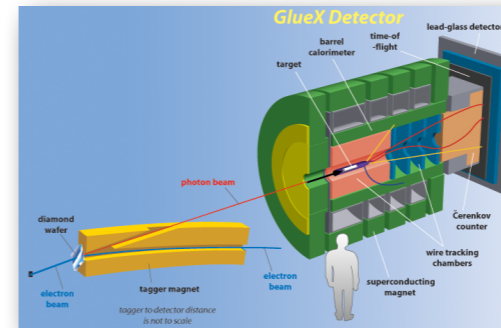
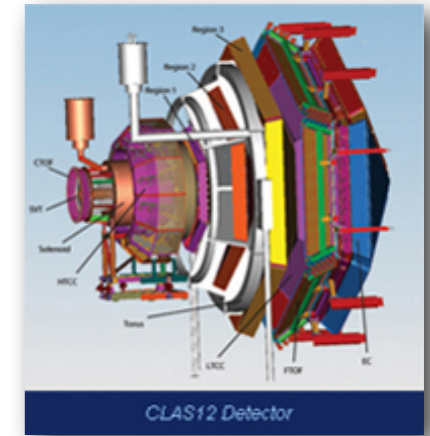


$$S = S_1 + S_2$$

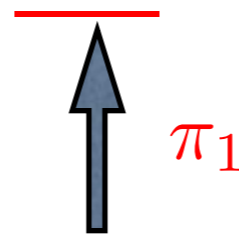
$$J = L + S$$

$$P = (-1)^{L+1}$$

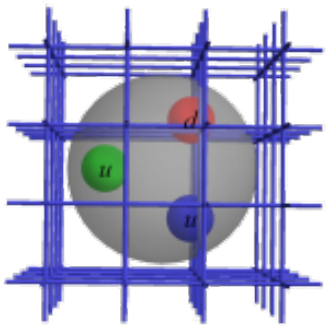
$$C = (-1)^{L+S}$$



Mesons with $J^{PC} = 0^{--}, 0^{+-}, 1^{-+}, 2^{+-}$: Exotic Quantum Numbers

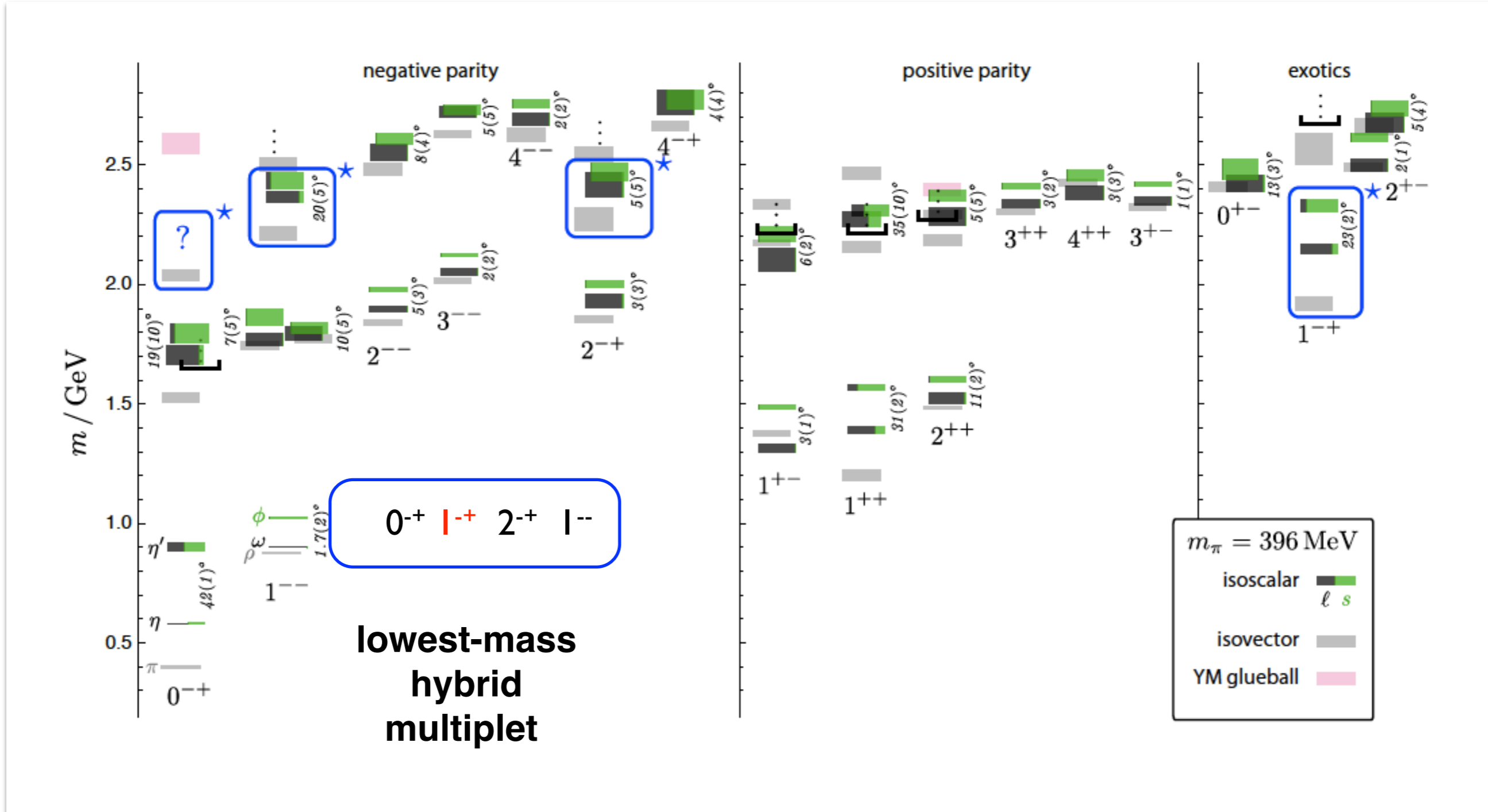


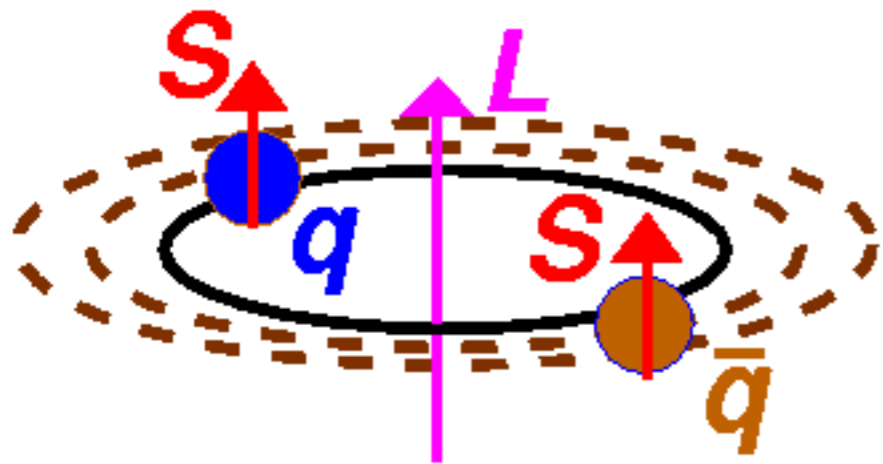
Expected to have very similar properties to ordinary $Q\bar{Q}$ mesons



J. Dudek et al.

same pattern in $\bar{s}s, \bar{c}c$
 hybrid interpretation of the $Y(4260)$





$$P_{q\bar{q}} = (-1)^{L+1}$$

$$C_{q\bar{q}} = (-1)^{L+S}$$

$$J_g^{PC} = 1^{+-}$$



$$P \times C = +1$$

$$J^{PC} = 1^{--}$$

J^{PC} glue

$J^{PC} Q\bar{Q}$

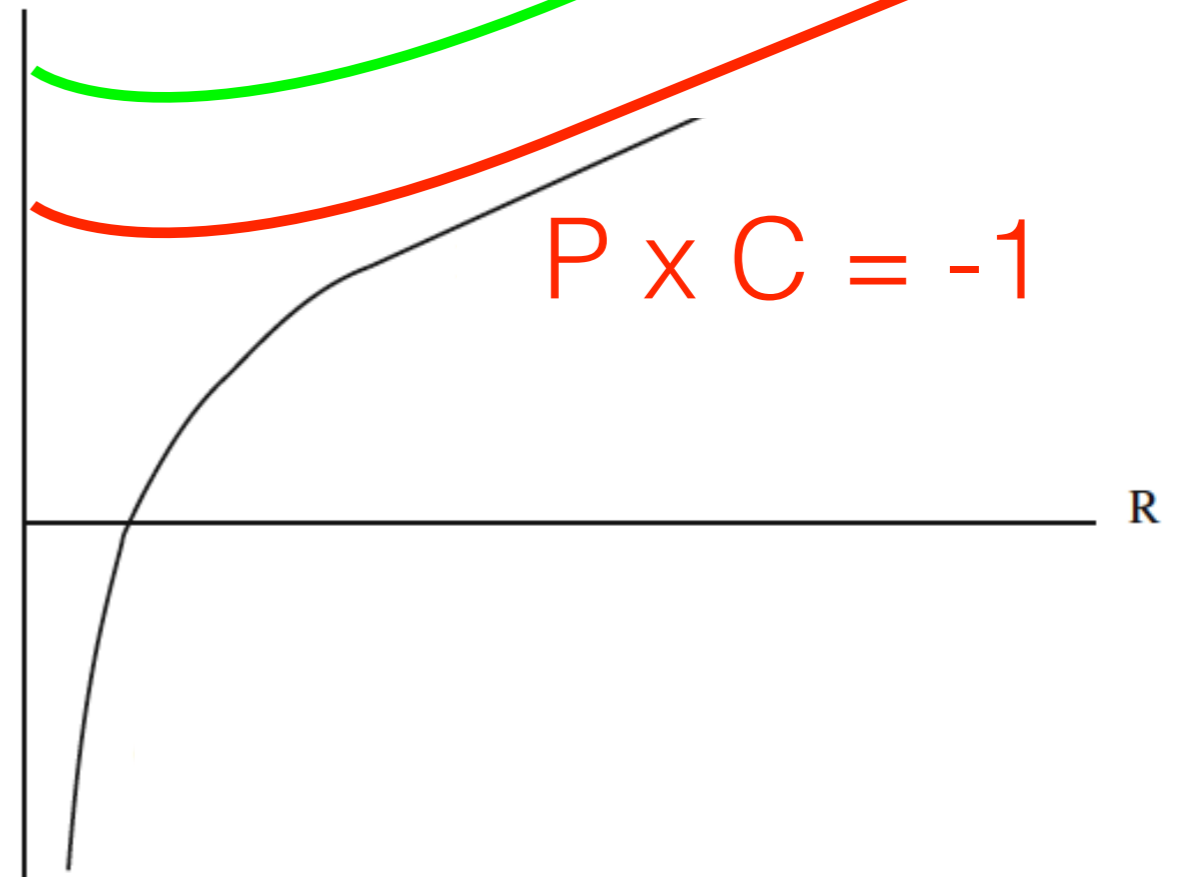
$$1^{+-} \times 0_{S_{Q\bar{Q}}}^{-+} = \boxed{1^{--}}$$

$$1^{+-} \times 1_{S_{Q\bar{Q}}=1}^{--} = \boxed{0^{-+}, 1^{-+}, 2^{-+}}$$

Energy of the gluon field

$$J^{PC} = 1^{+-}$$

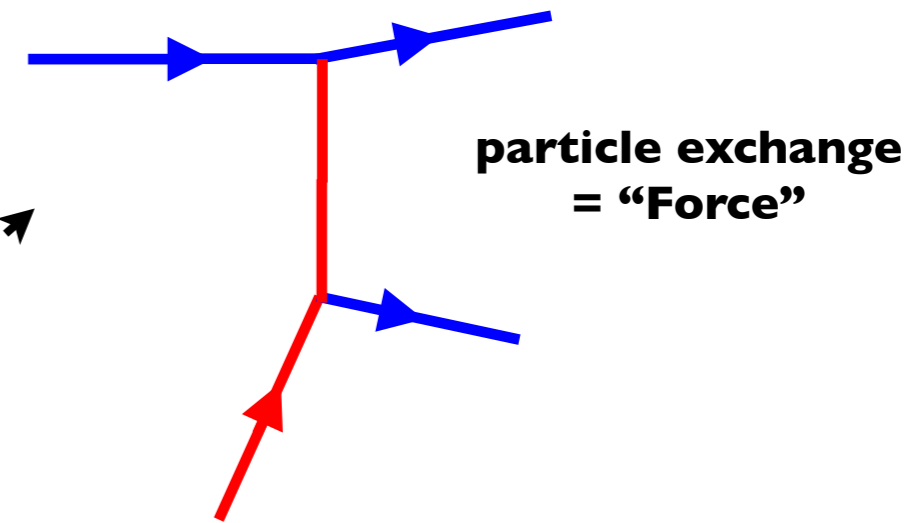
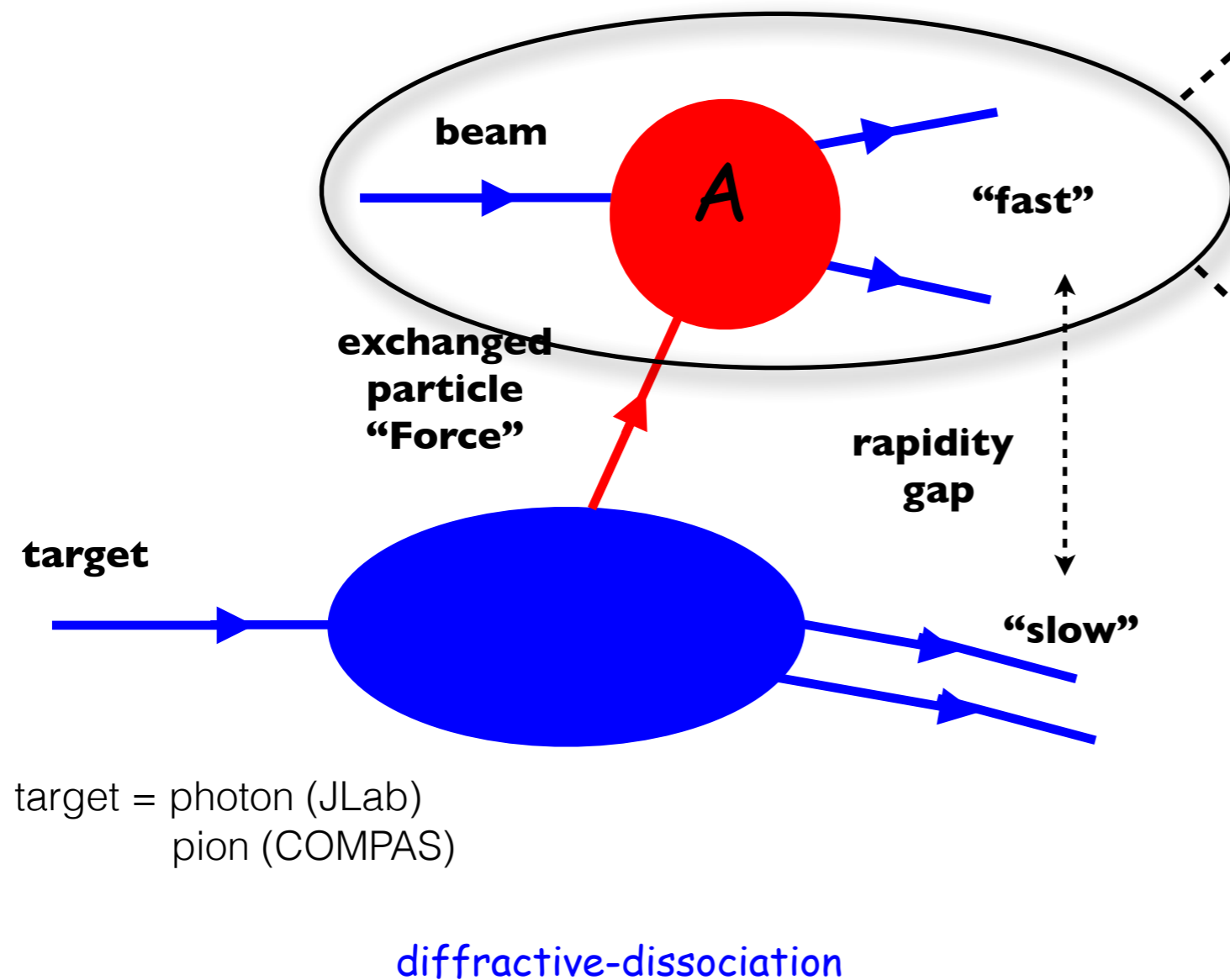
$$P \times C = -1$$



Prediction of Coulomb gauge QCD

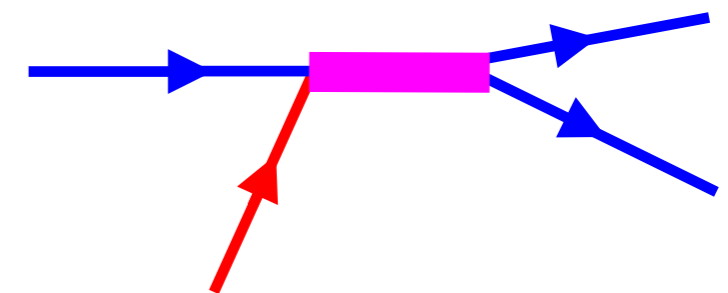
Hunting for Resonances in fixed target experiments

COMPASS, JLAB 12 GeV



Particle ↔ Force duality

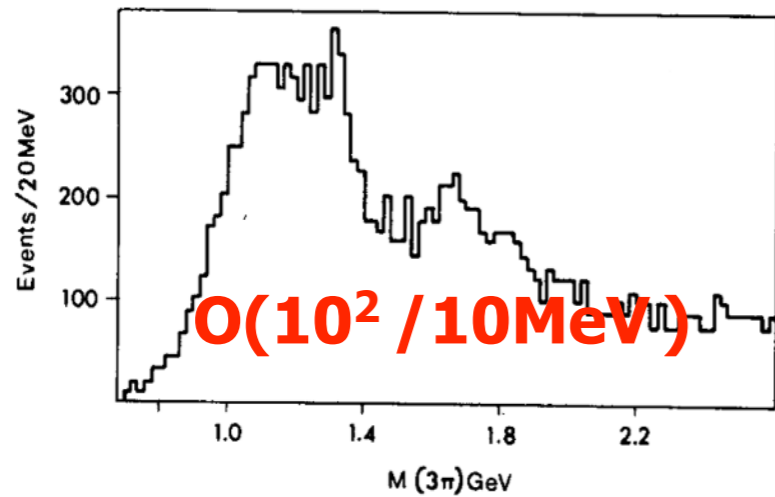
Resonance, "R" production



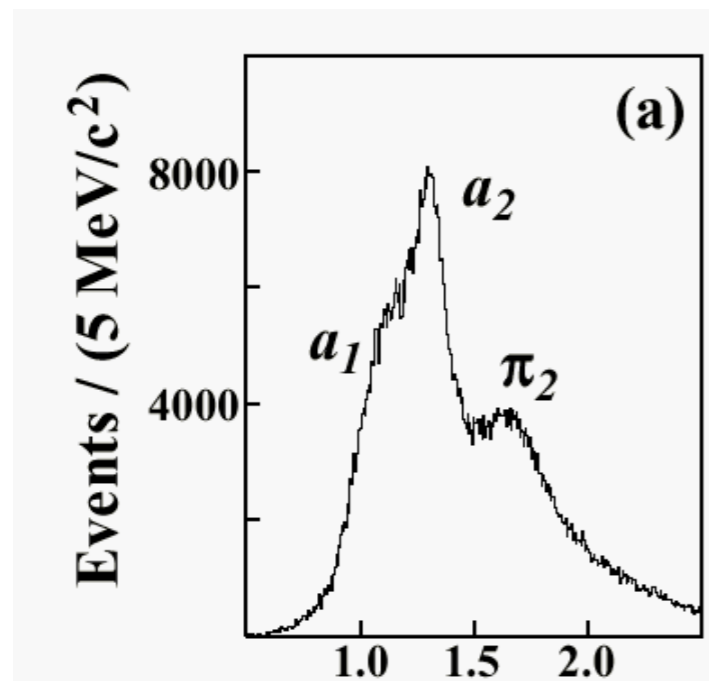
Evolution in statistics

$$\pi^- p \rightarrow \pi^- \pi^+ \pi^- p$$

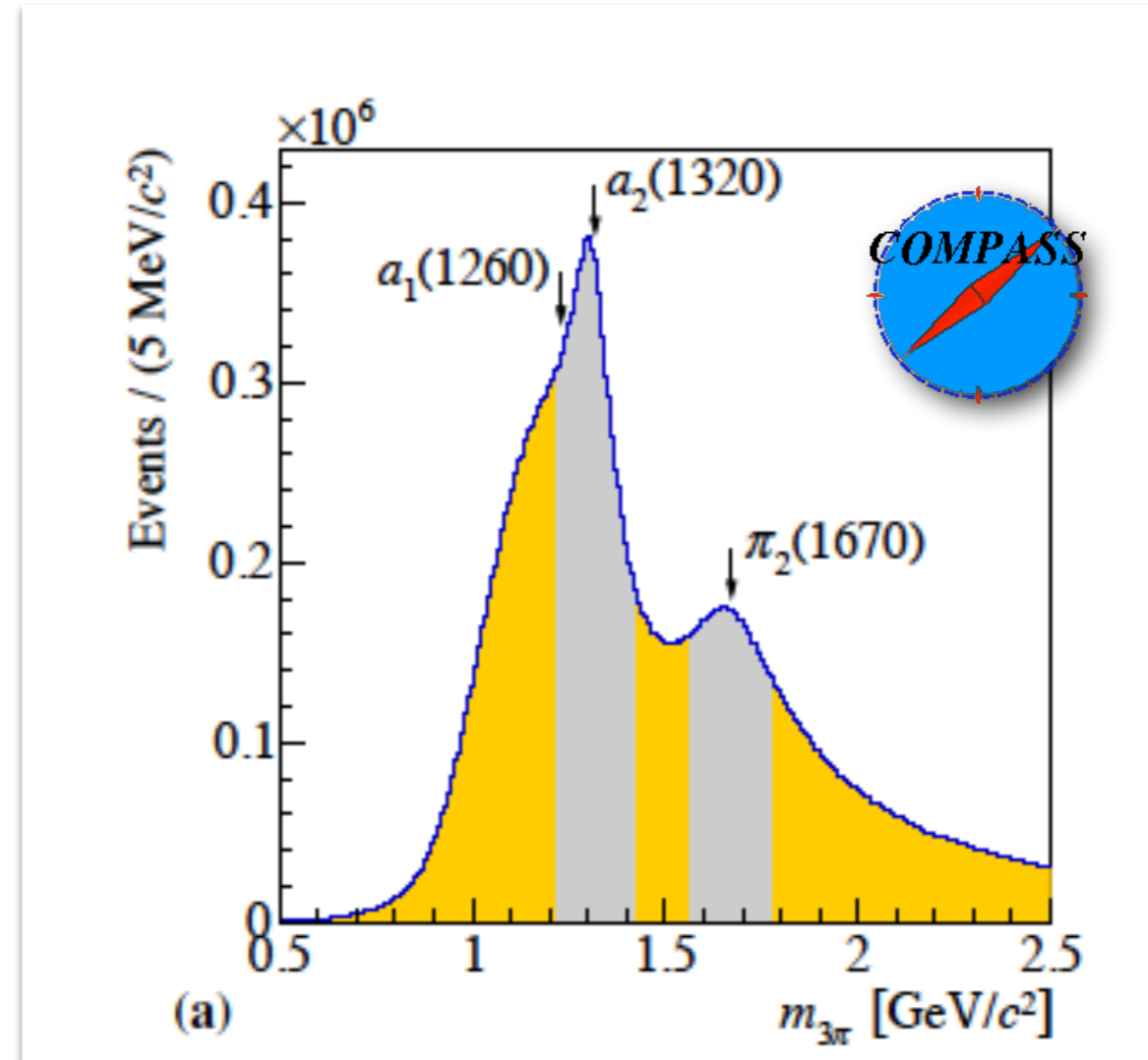
CERN ca. 1970



BNL (E852) ca 1995

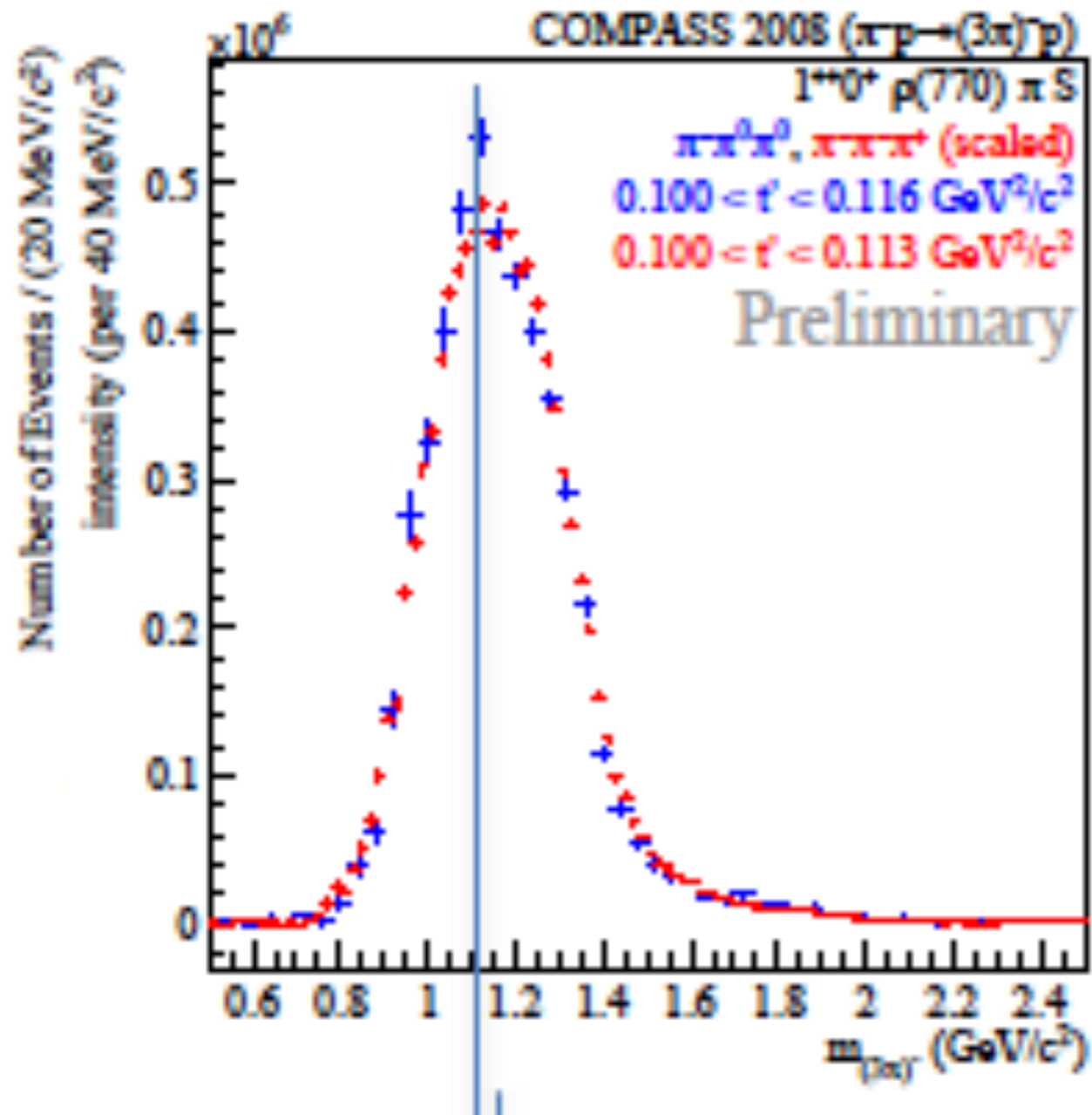


E852 (Full sample) $\sim 10^5/10\text{MeV}$



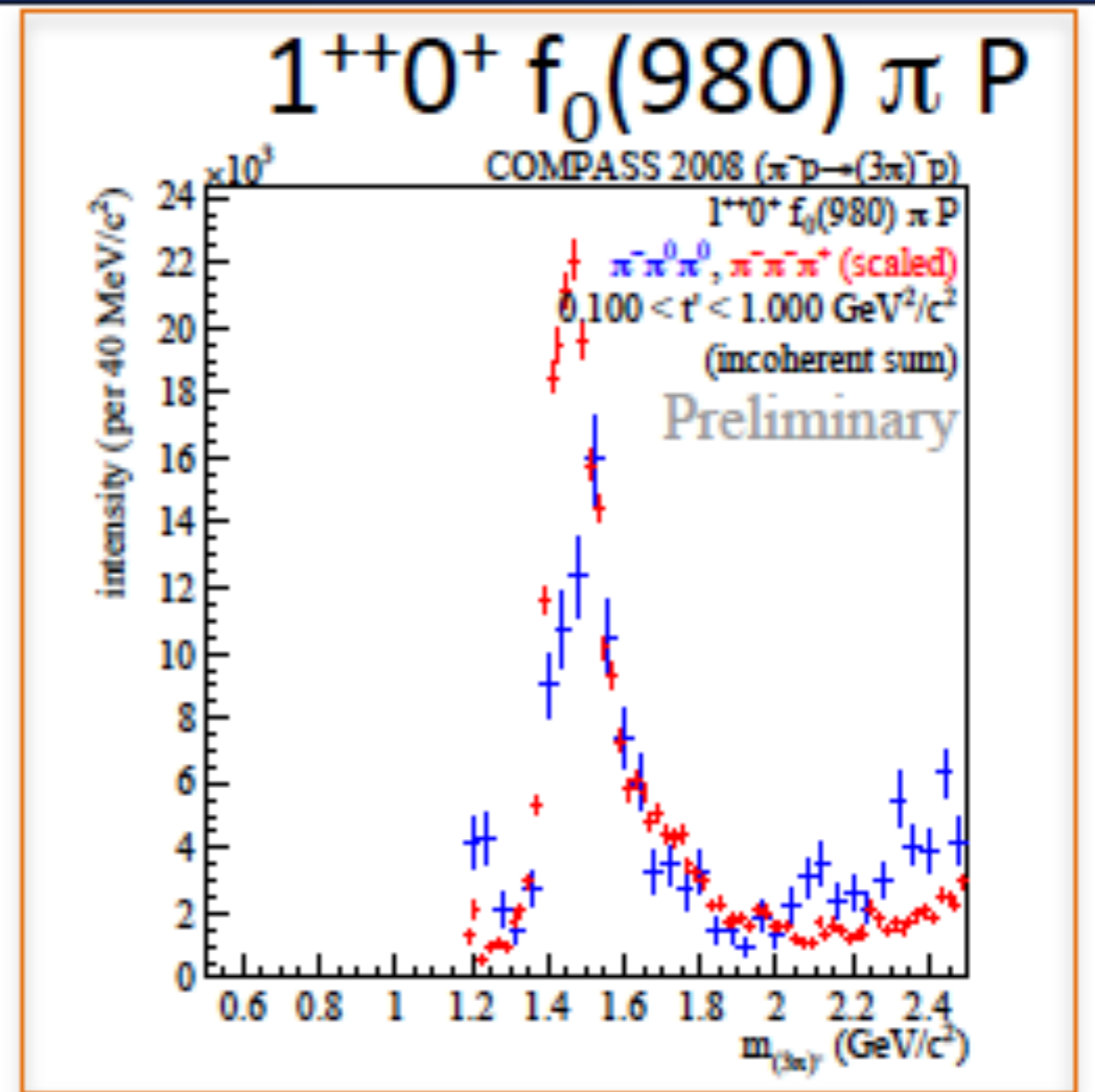
$O(10^6 / 10\text{MeV})$

COMPASS's a_1 meson(s) $J^{PC} = 1^{++}$ ($L=1, S=1$)



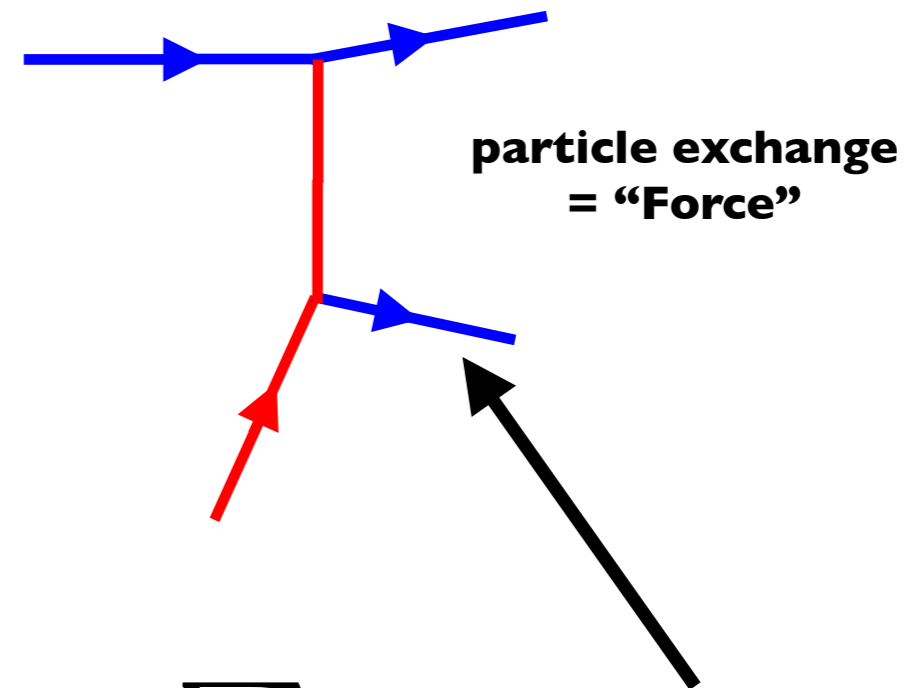
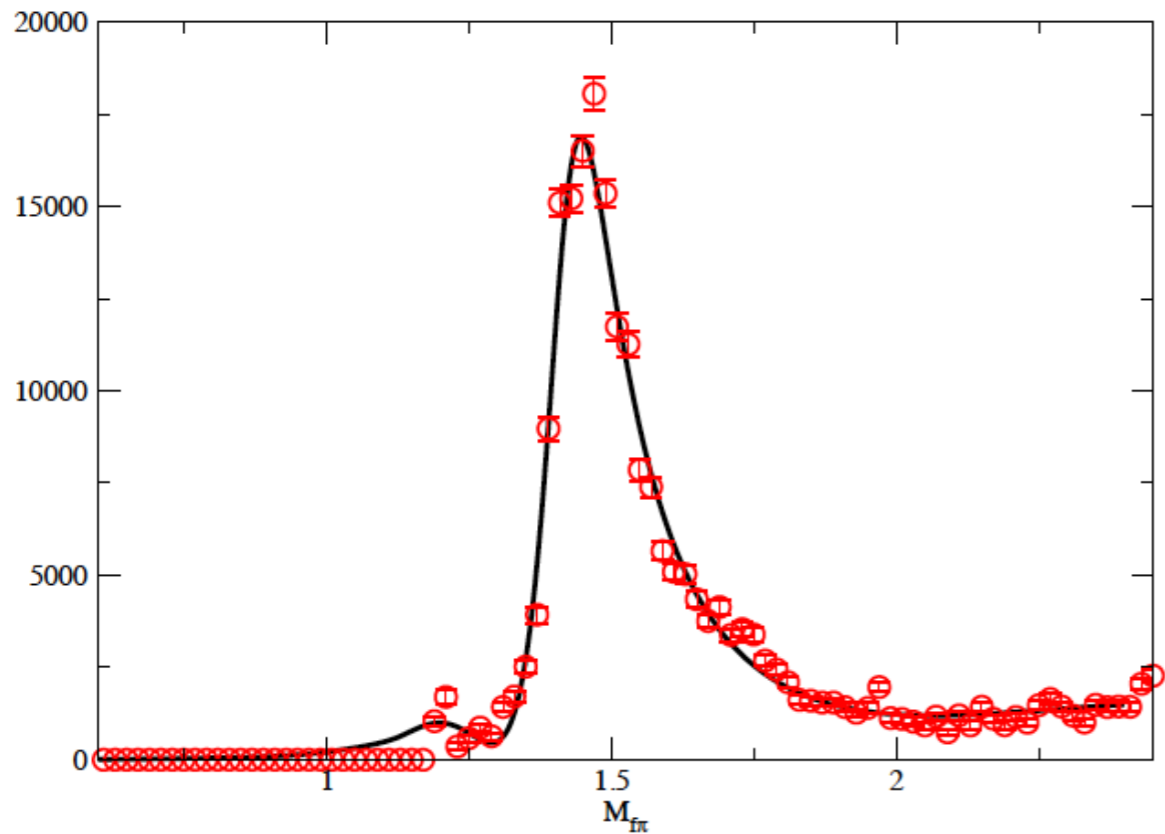
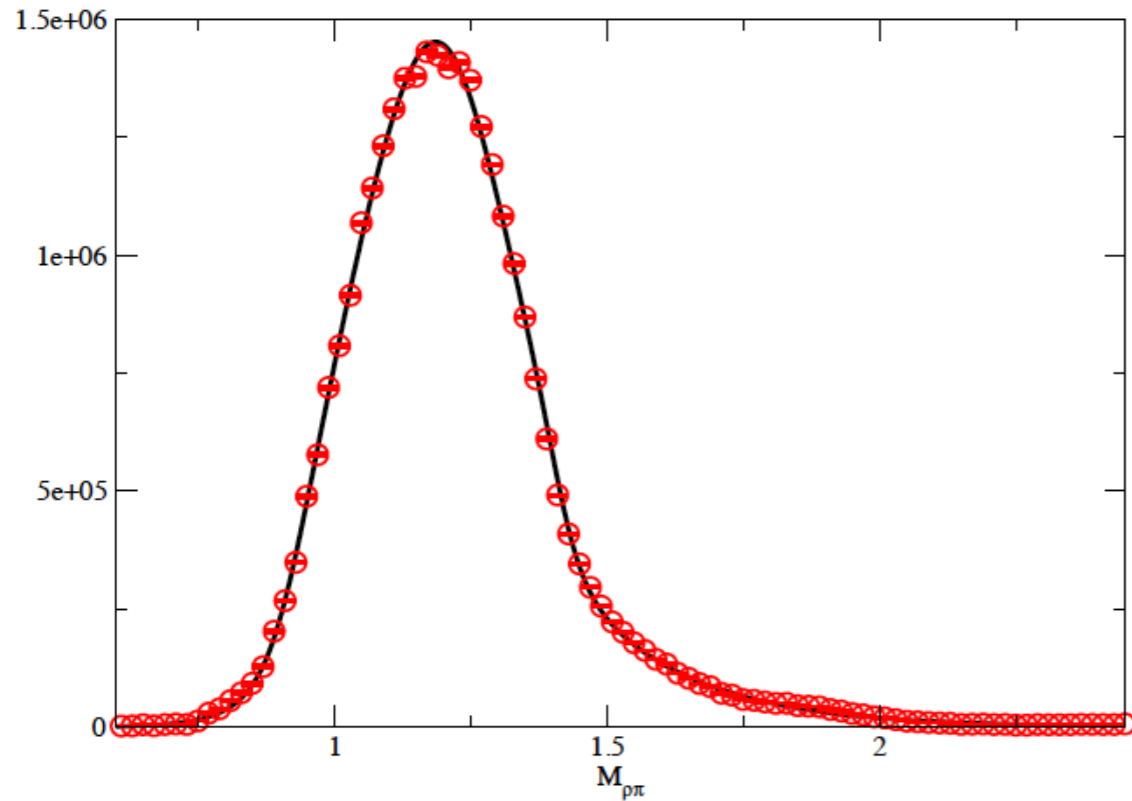
“Old” a_1 in $\rho\pi$ S-wave

New a_1 in $f_0 \pi$ P-wave



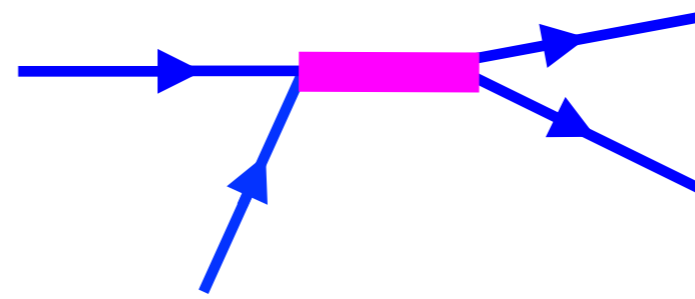
Two Breit-Wigner resonances (COMPASS)

$$\Delta A_i(s) = \sum_{j=f_0\pi, \rho\pi} T_{ij}^*(s) \rho_j(s) A_j(s)$$



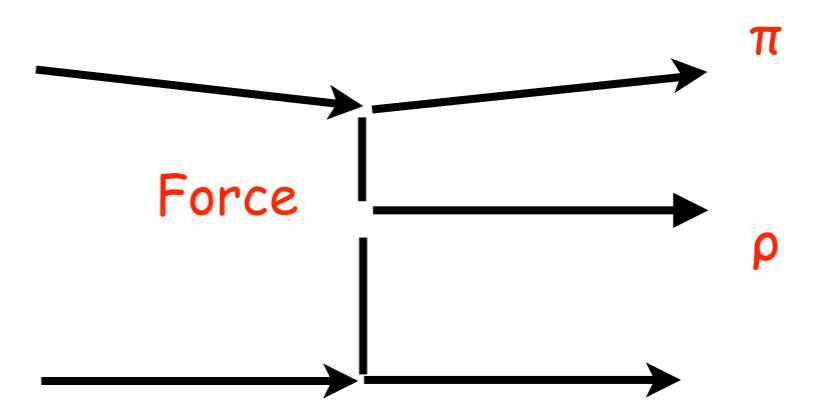
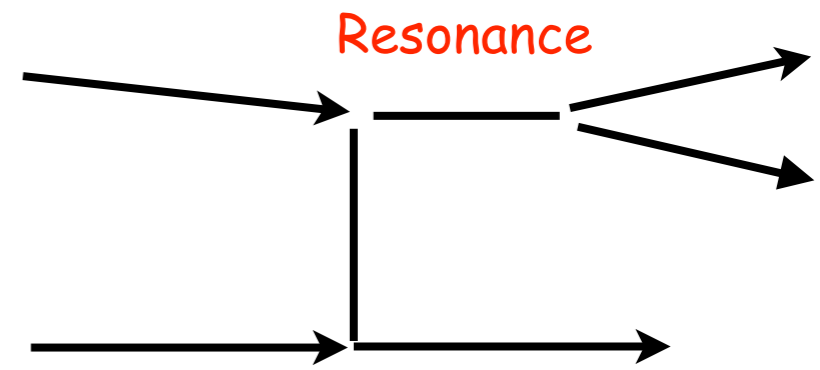
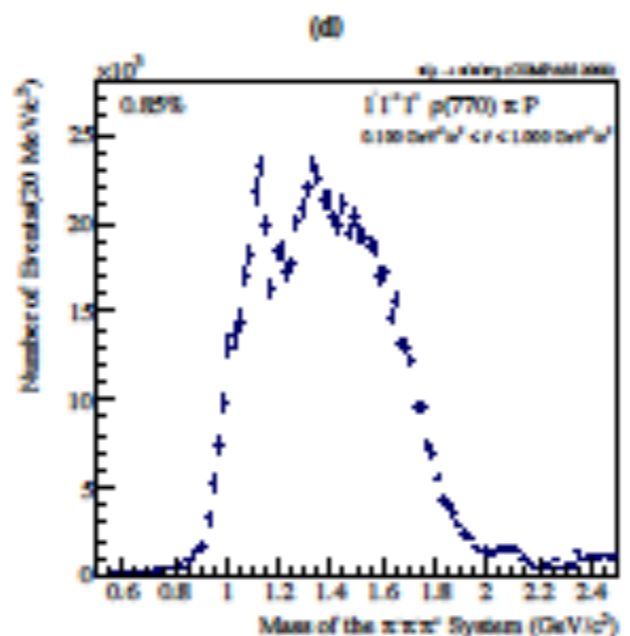
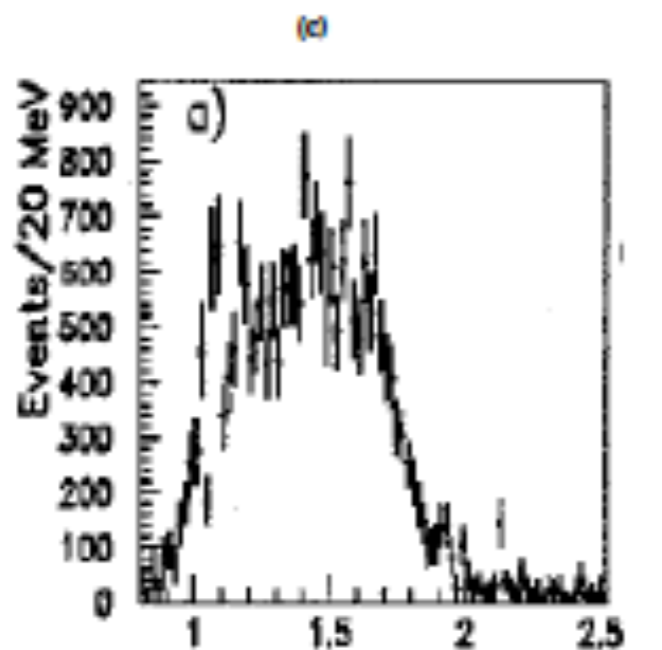
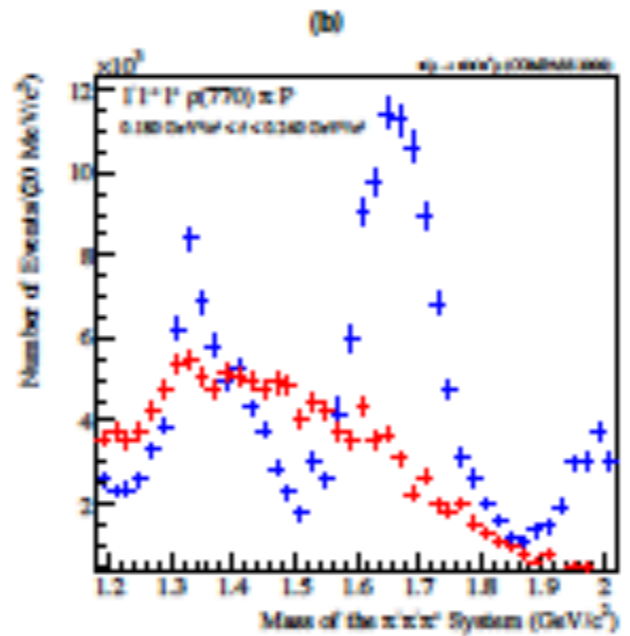
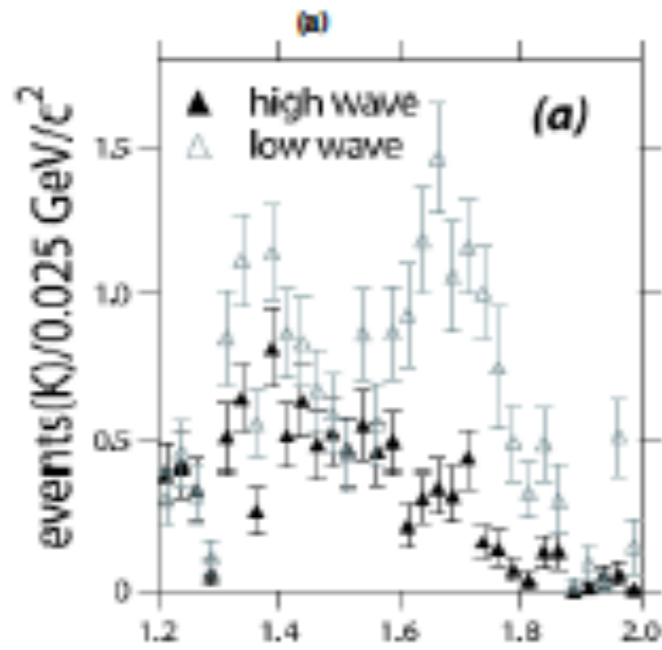
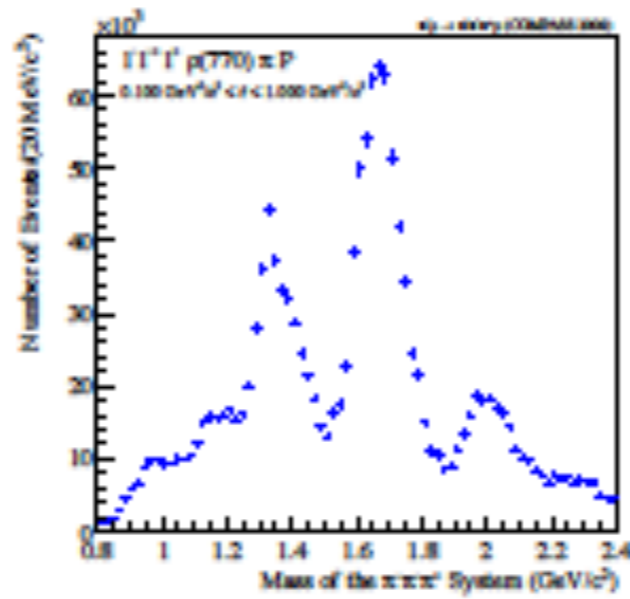
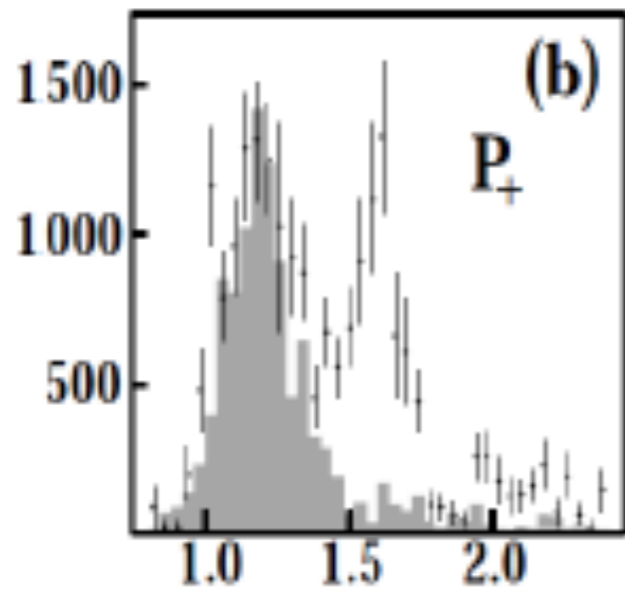
$$A_i(s) = \sum_{j=f_0\pi, \rho\pi} T_{ij}(s) P_j(s)$$

Resonance, "R" production

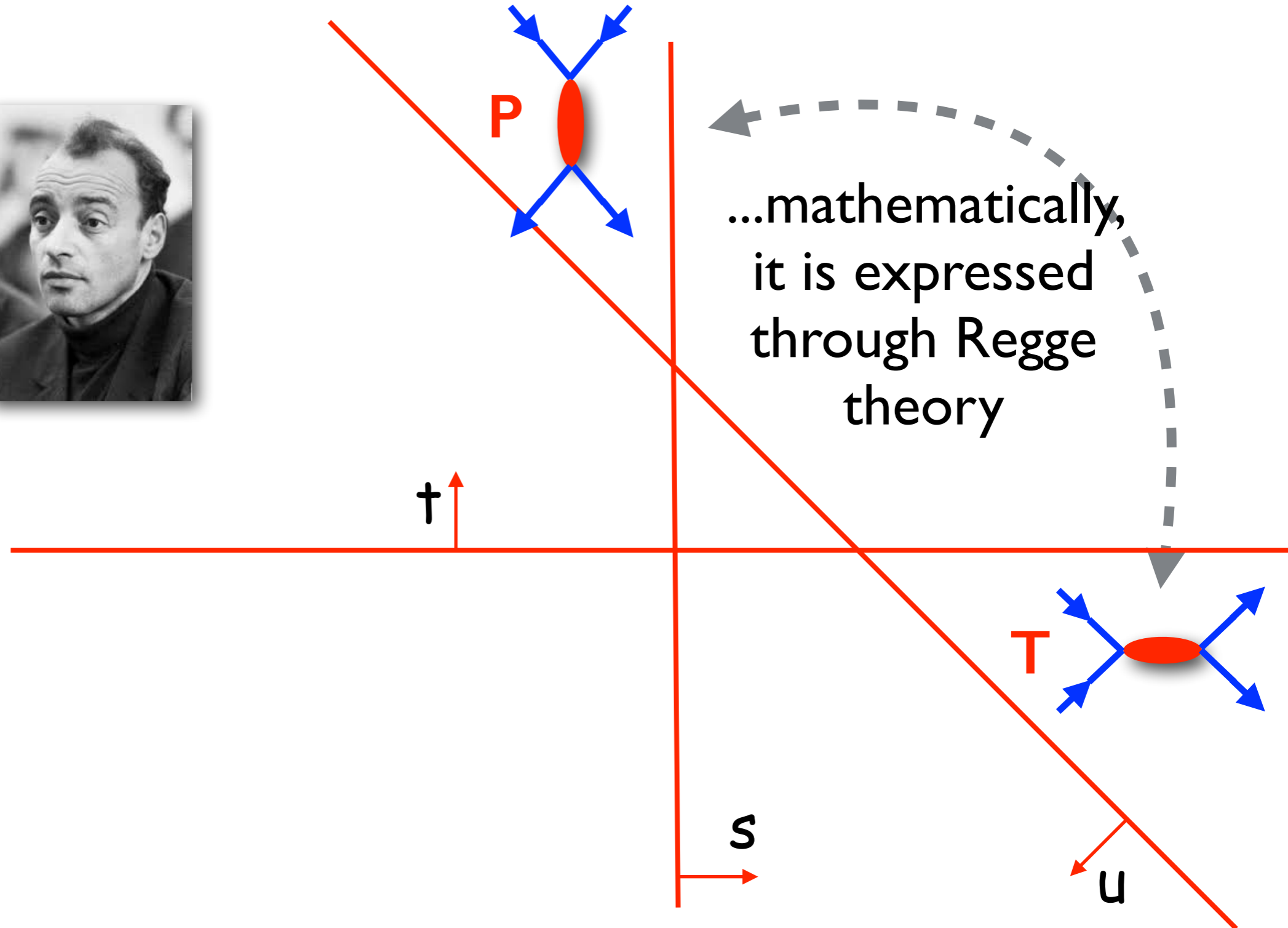


One resonance underlies both peaks

3pion spectrum in diffractive dissociation on hydrogen
COMPASS vs E852/BNL and VES



Forces (P) and Resonances (T) are not independent

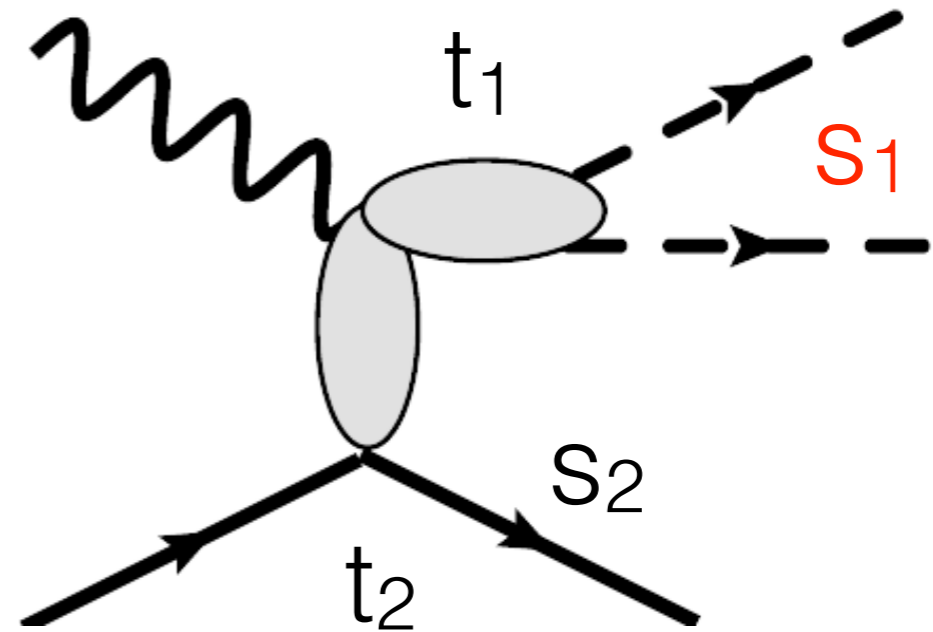
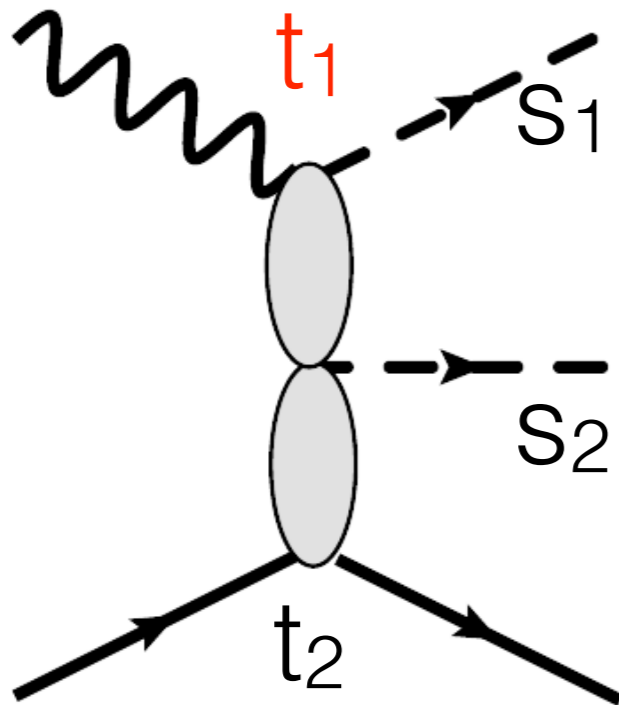
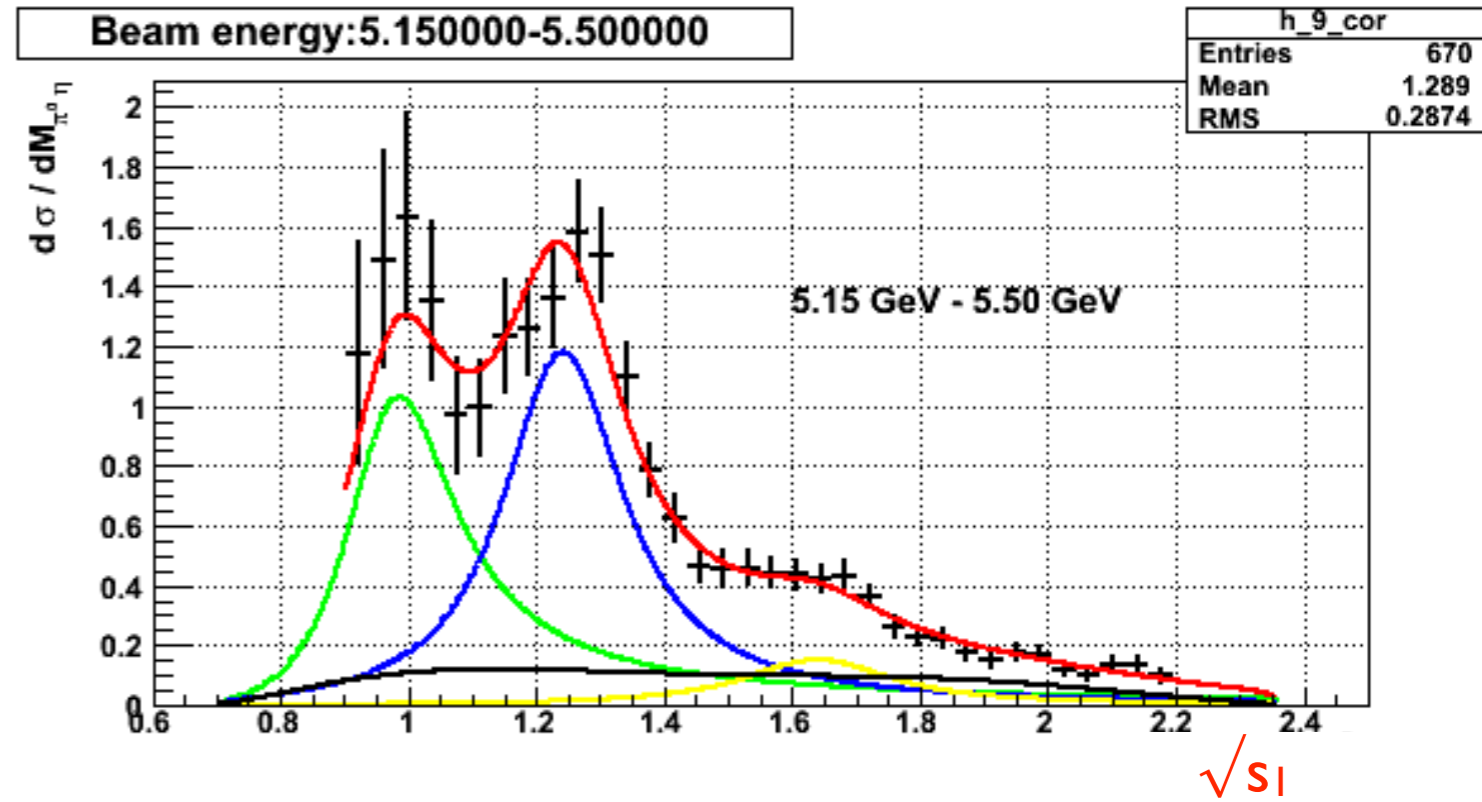
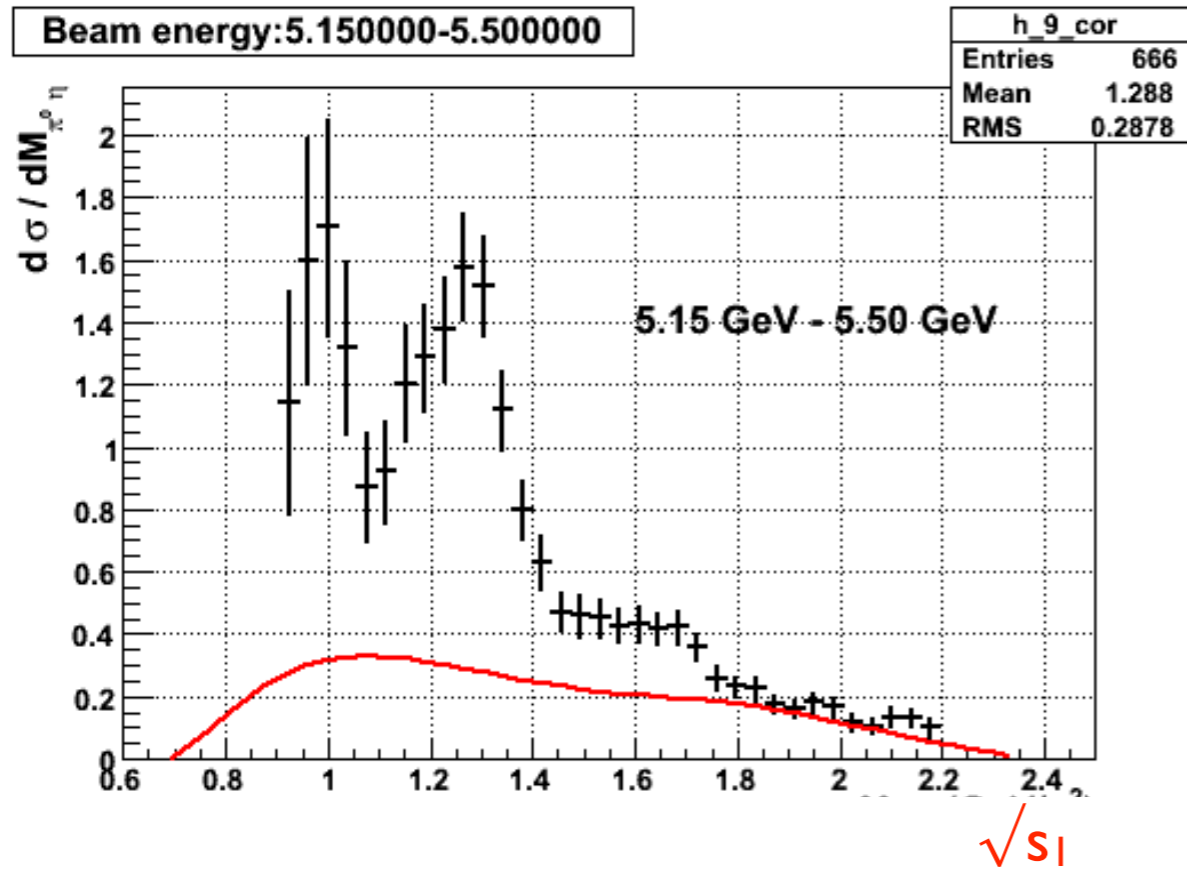


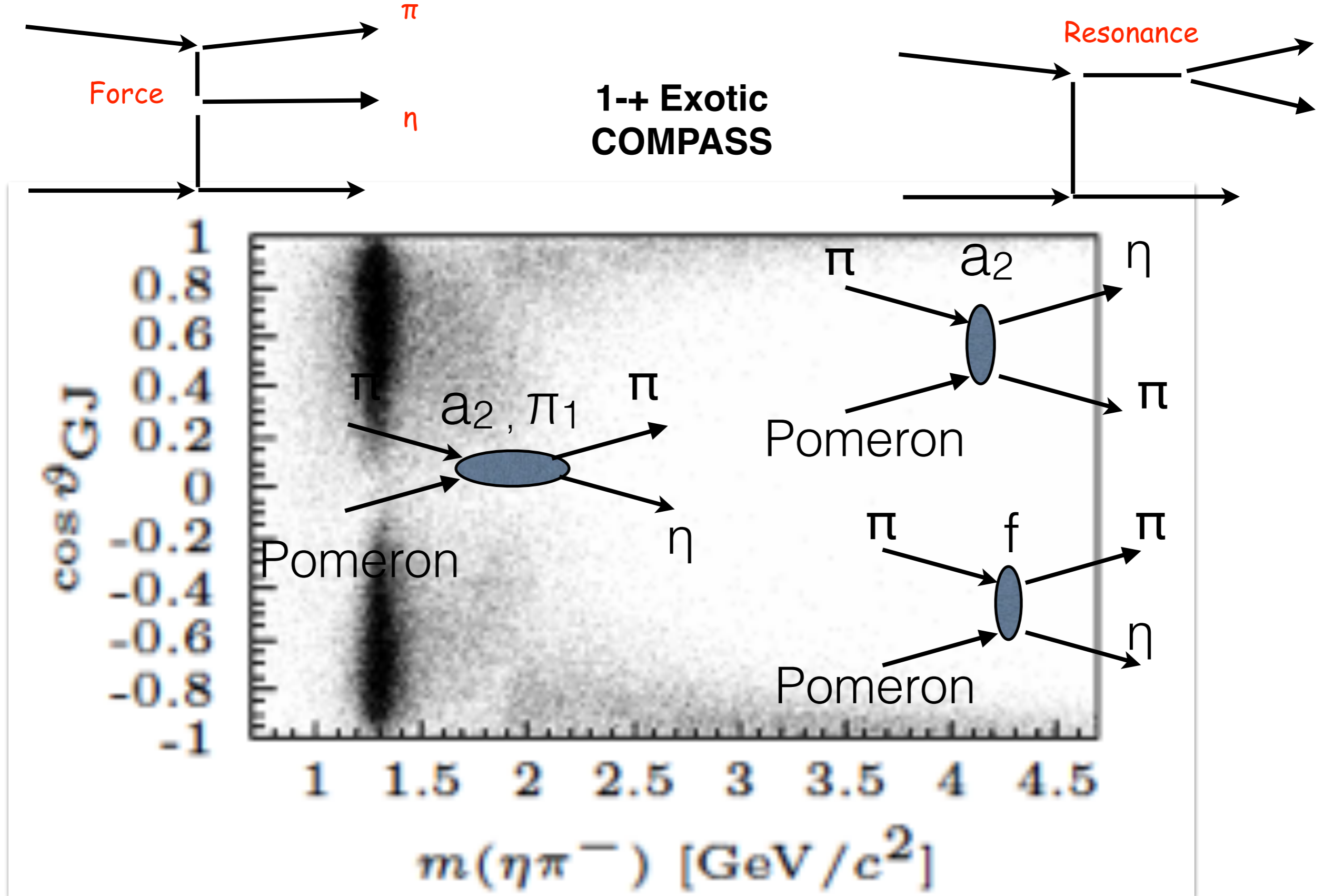
...mathematically,
it is expressed
through Regge
theory

Unitarity enforces Force-Resonance duality = Regge theory

$\Upsilon\rho \rightarrow \eta\pi^0\rho$ (g12)

A.Celentano, PhD, HASPEC/JPAC





duality \rightarrow the production channel is dominated by spin-even partial waves. What is the exotic (P-wave) dual to ?

JPAC: helping to repair the gap



**Develop
theoretical, phenomenological/
computational tools for hadron
experiments**

**Experiment-theory
collaboration**

GLOBAL EFFORT

**Create a vibrant
community**

JPAC : Specific Analyses

Light meson decays and light quark resonance

$$\omega/\phi \rightarrow 3\pi, \pi\gamma \text{ (Khuri-Treiman)}$$

$$\omega \rightarrow 3\pi \text{ (Veneziano, B4)}$$

$$\eta \rightarrow 3\pi, \eta \rightarrow \eta' \pi \pi \text{ (Khuri-Treiman)}$$

$$J/\psi \rightarrow \gamma \pi^0 \pi^0$$

Photoproduction: (production models, FESR and duality)

$$\gamma p \rightarrow \pi^0 p$$

$$\gamma p \rightarrow p K^+ K^-$$

Launched in the Fall of 2014
~20 papers published

Exotica and XYZ's:

$$\pi^- p \rightarrow \pi^- \eta p \text{ \& } \pi^- p \rightarrow \pi^- \eta' p \text{ (FESR)}$$

$$B^0 \rightarrow \psi' \pi^- K^+ u, \psi(4260) \rightarrow J/\psi \pi^+ \pi^-$$

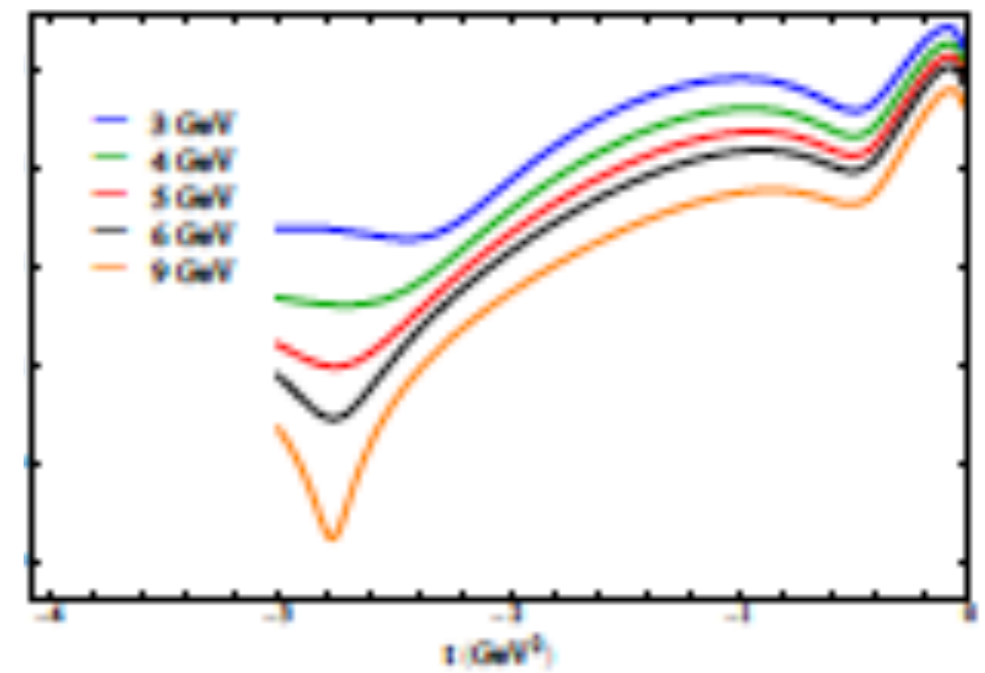
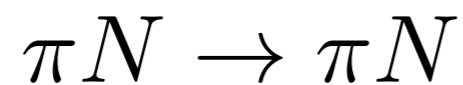
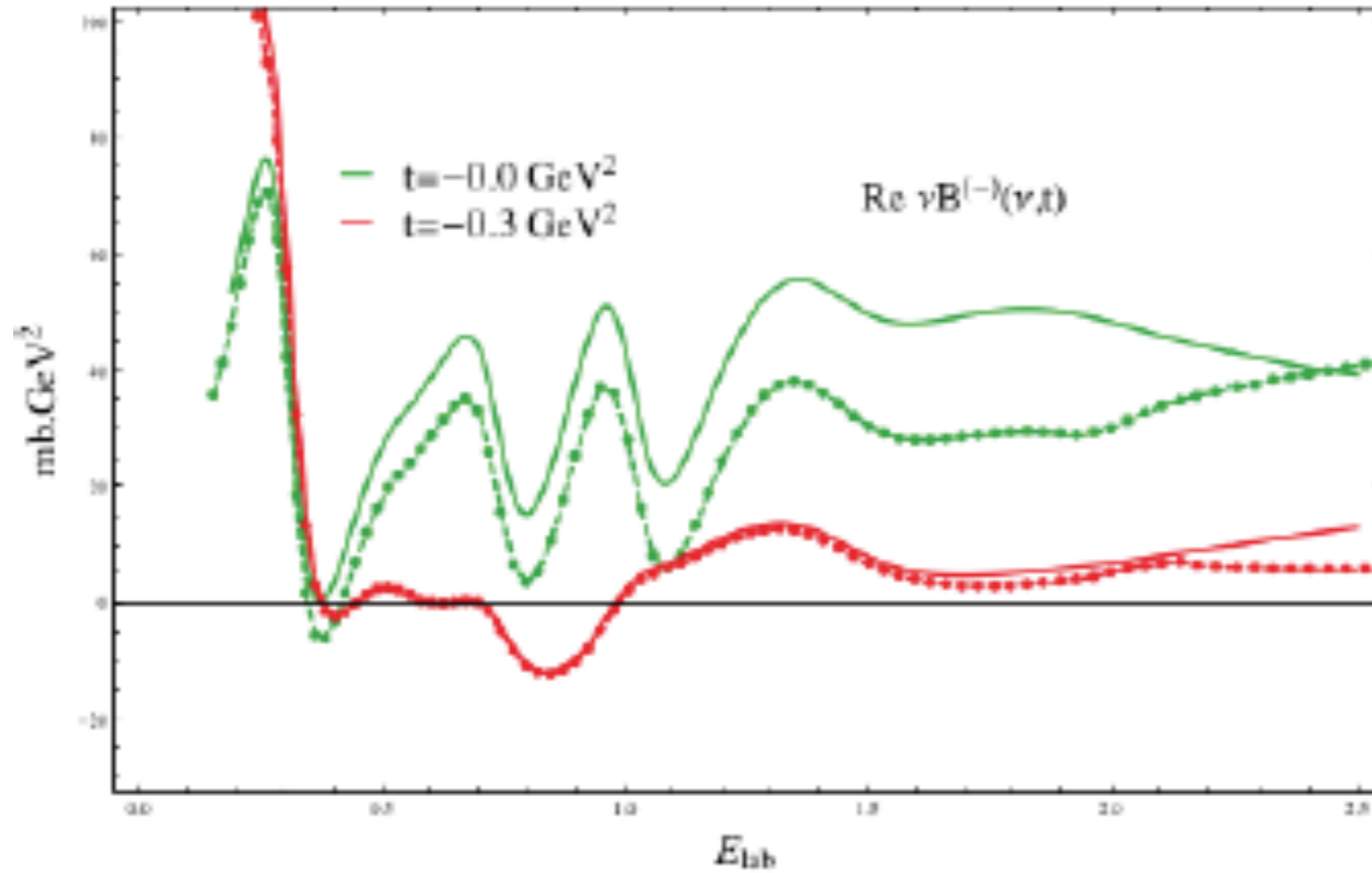
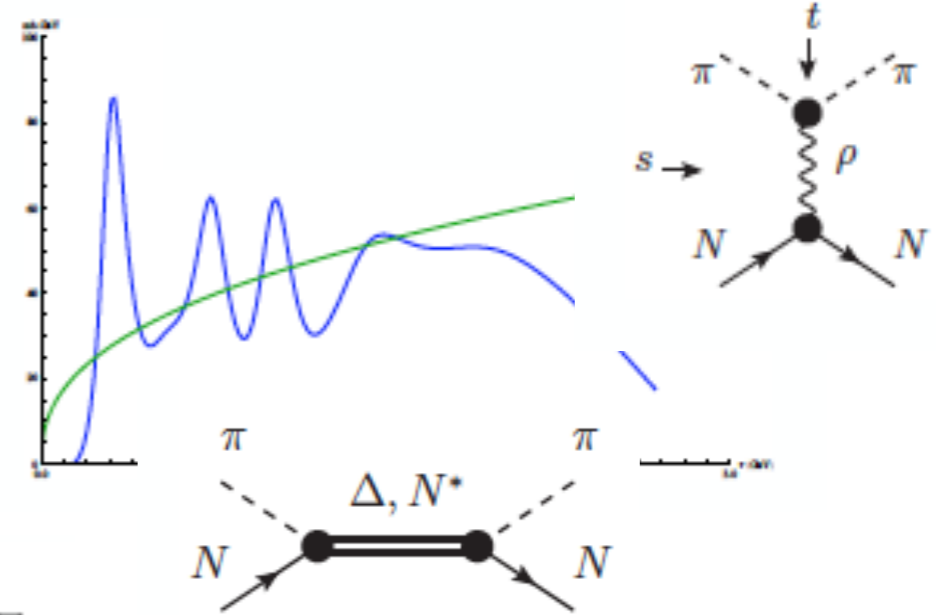
$$J/\psi \rightarrow 3\pi \text{ (Veneziano, B4)}$$

Resonance-Regge physics in meson-baryon scattering

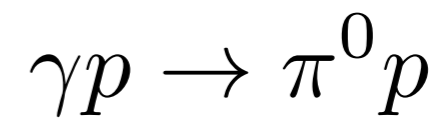
$$\int_{\nu_0}^{\Lambda} \text{Im } A^{(-)}(\nu', t) \nu'^{2k} d\nu' = \beta(t) \frac{\Lambda^{\alpha_{\rho}(t)+2k+1}}{\alpha_{\rho}(t) + 2k + 1}$$

Resonance

Regge



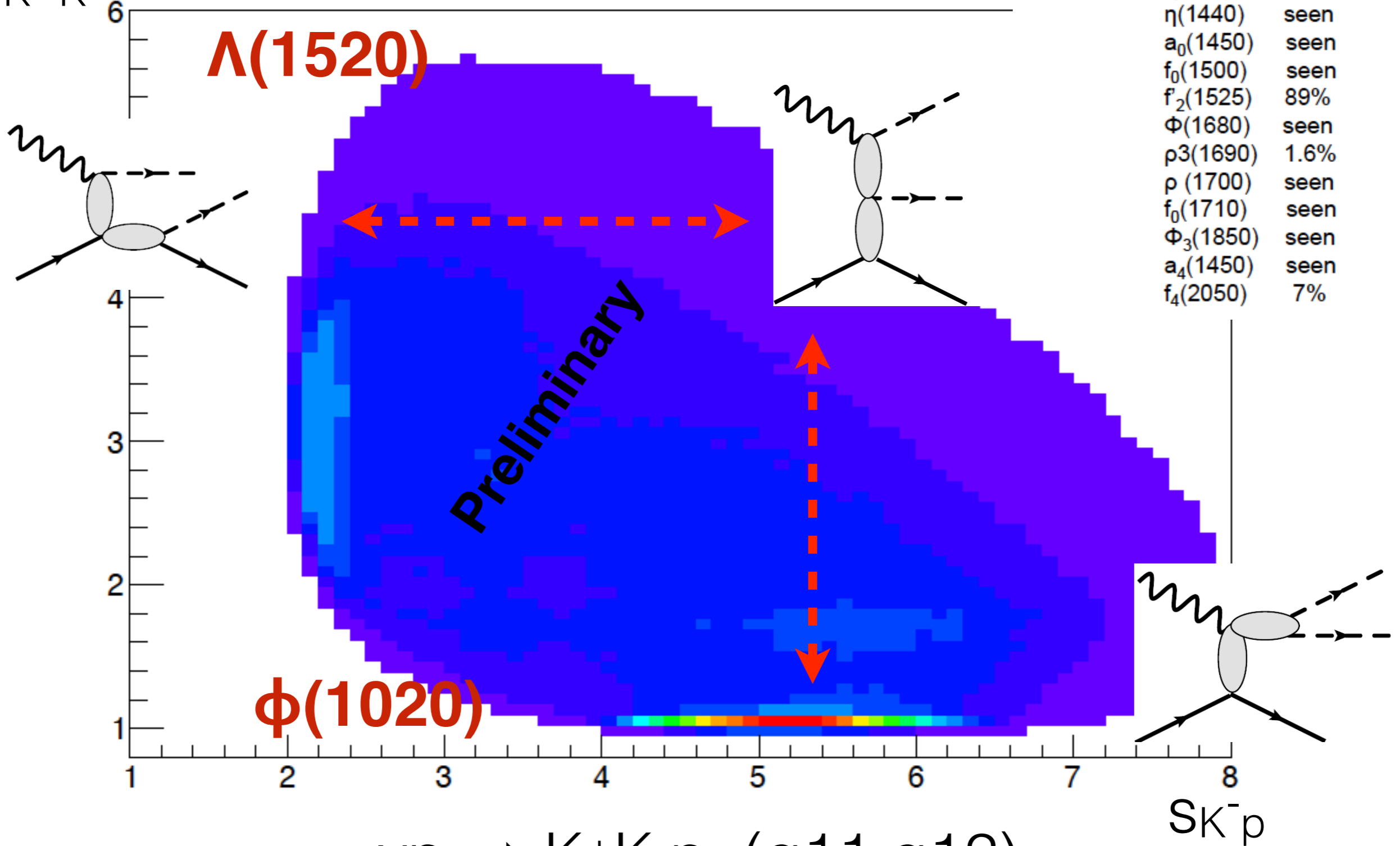
section at CLAS and GlueX energies.



Duality @ JLab

B_5 amplitude description

$S_{K^+K^-}$



$\Lambda(1520)$

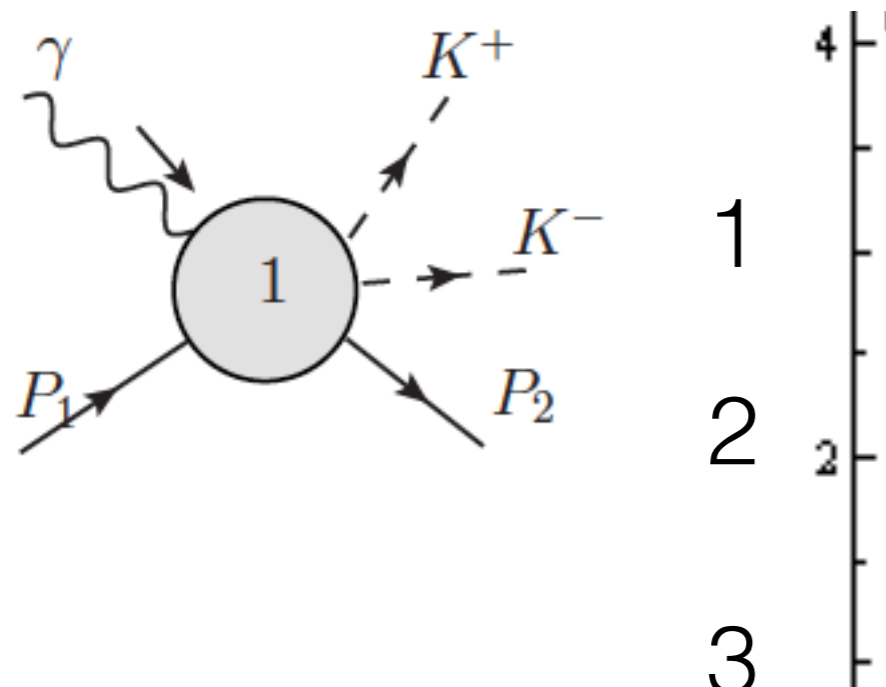
$\phi(1020)$

Preliminary

$\Phi(1020)$	49%
$f_2(1270)$	46%
$f_1(1285)$	9%
$a_2(1320)$	49%
$f_0(1370)$	seen
$f_1(1420)$	dominant
$\eta(1440)$	seen
$a_0(1450)$	seen
$f_0(1500)$	seen
$f_2(1525)$	89%
$\Phi(1680)$	seen
$\rho_3(1690)$	1.6%
$\rho(1700)$	seen
$f_0(1710)$	seen
$\Phi_3(1850)$	seen
$a_4(1450)$	seen
$f_4(2050)$	7%

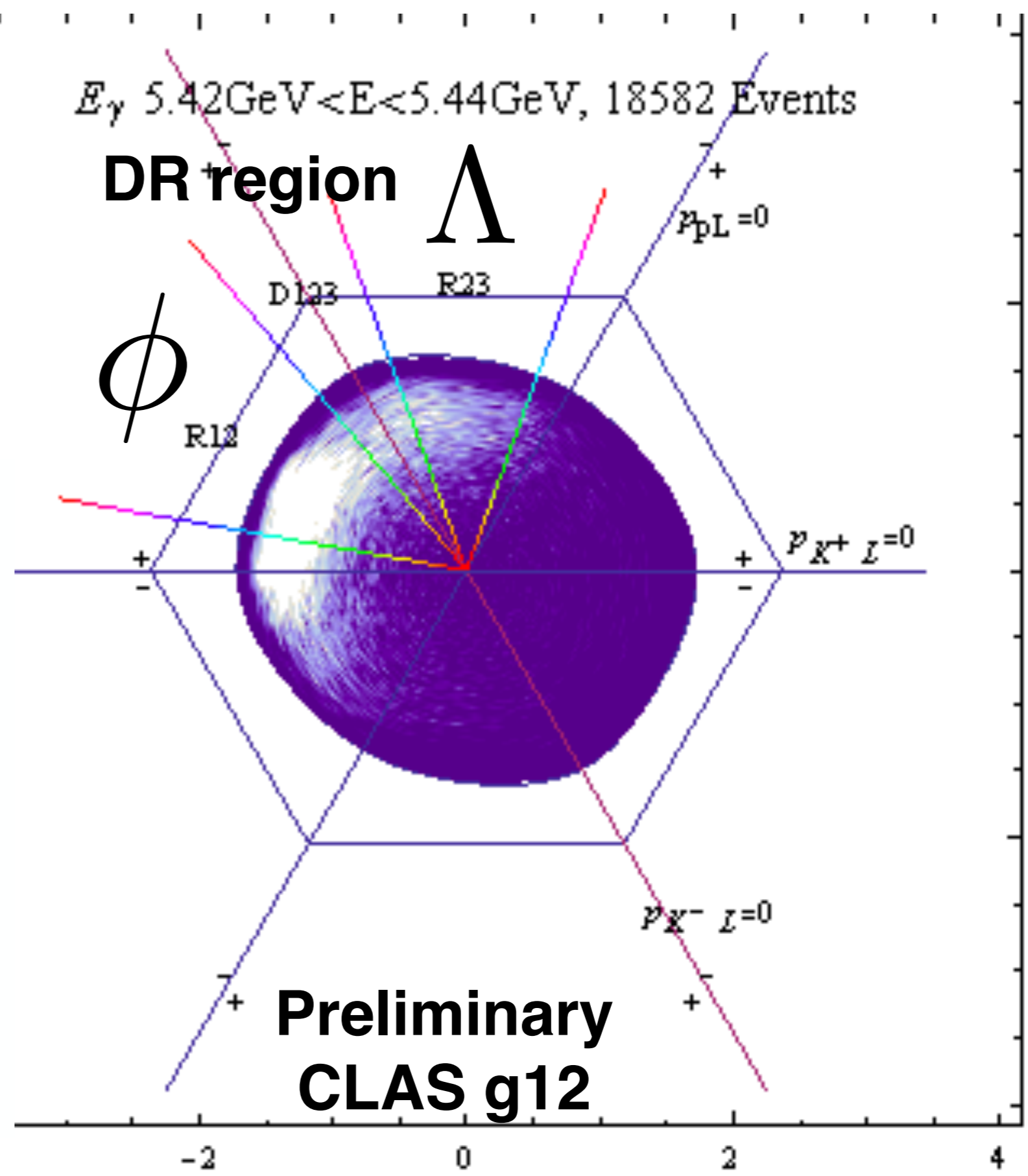
$\gamma p \rightarrow K^+ K^- p \quad (g_{11}, g_{12})$

van Hove longitudinal plot

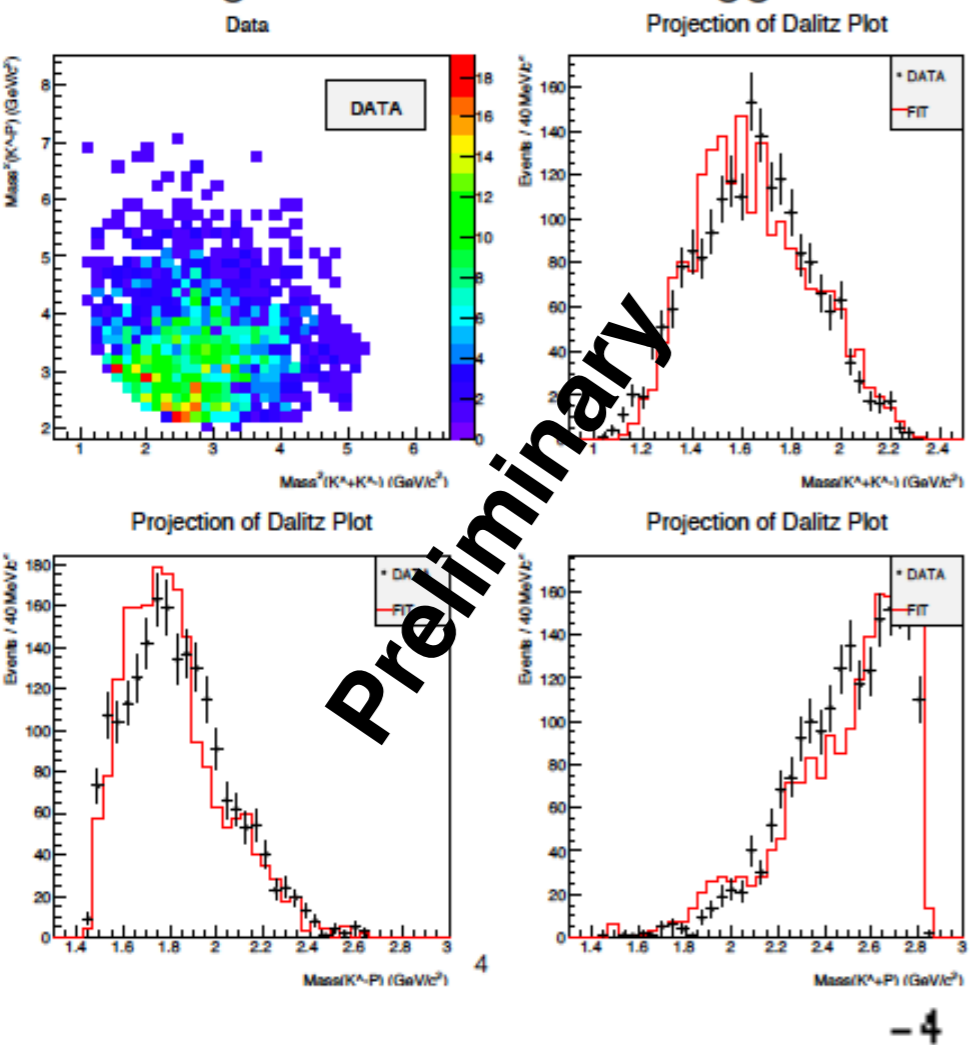


E_γ 5.42 GeV < E < 5.44 GeV, 18582 Events

DR region Λ



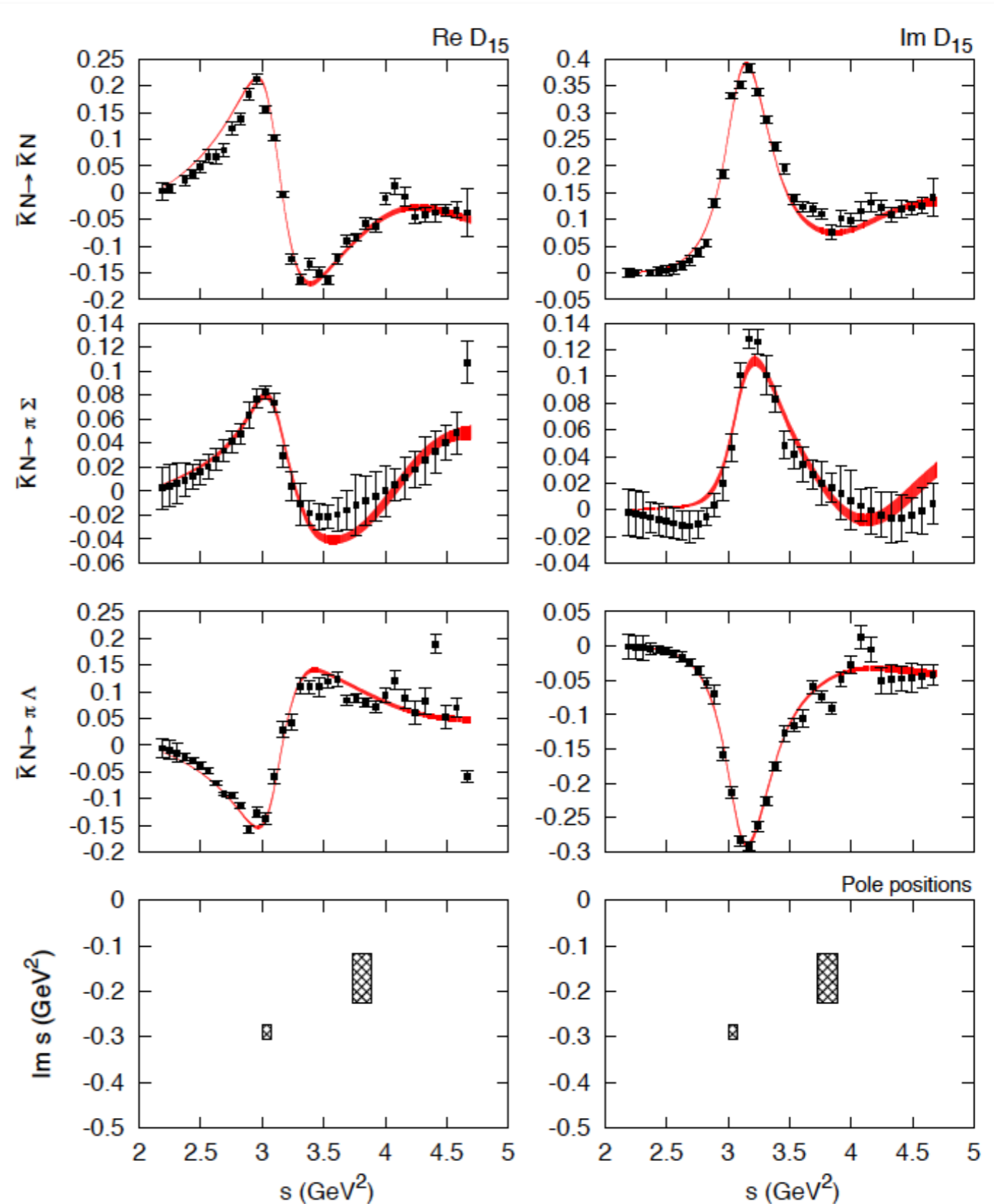
Fitting Result for double Regge limit



**Preliminary
CLAS g12**

$$(\bar{K}N), (\pi\Sigma), (\pi\Lambda) \rightarrow (\bar{K}N), (\pi\Sigma), (\pi\Lambda)$$

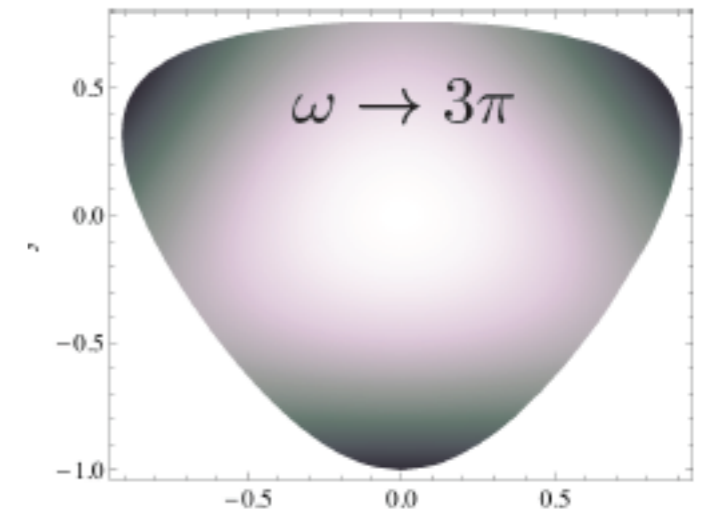
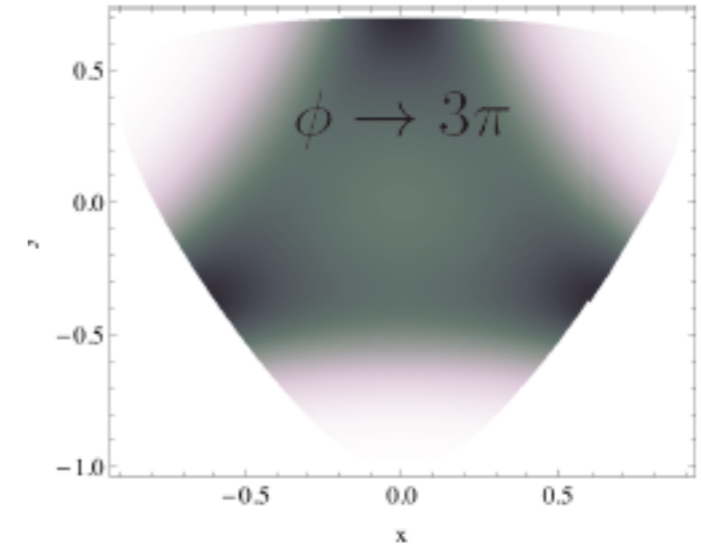
Hyperon production
what is $\Lambda(1405)$?



Light meson decays

$$\eta \rightarrow 3\pi \quad \omega \rightarrow 3\pi \quad \phi \rightarrow 3\pi$$

- **Constrained phase space,**
- **Effective (chiral) dynamics,**
- **Small number of partial waves,**
- **Amendable to dispersive methods**

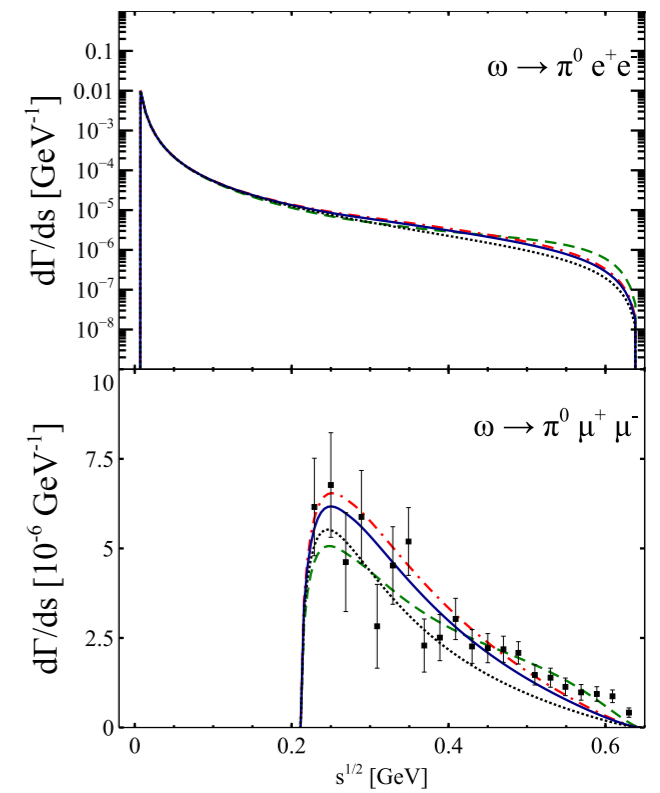
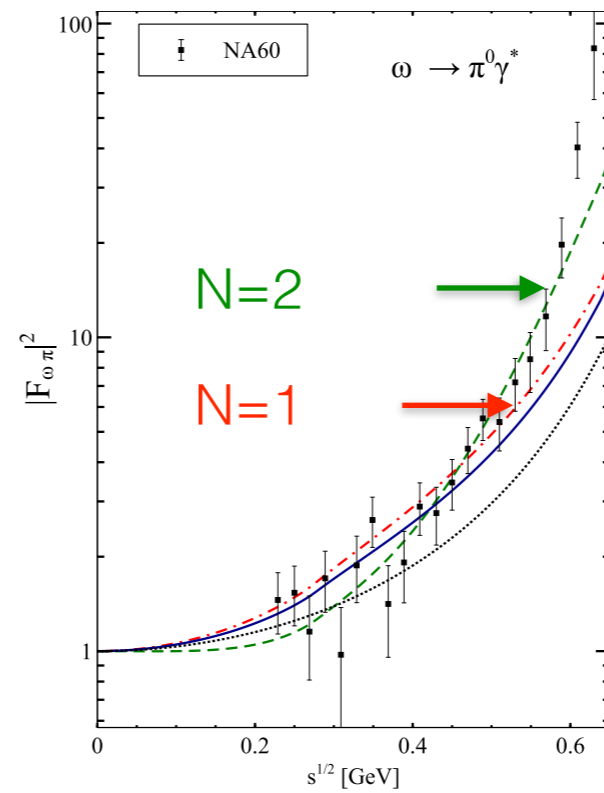
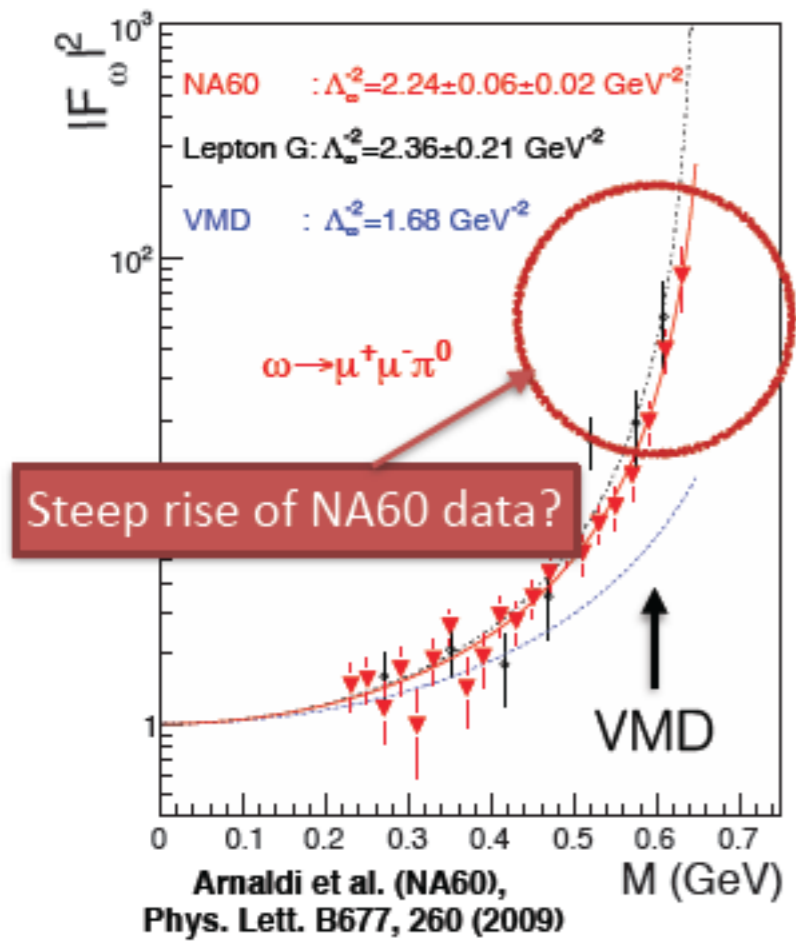


$$\eta \rightarrow 3\pi$$

$$A(s, t, u) = -\frac{1}{Q^2} \frac{M_K^2}{M_\pi^2} \frac{M_K^2 - M_\pi^2}{3\sqrt{3}F_\pi^2} M(s, t, u)$$

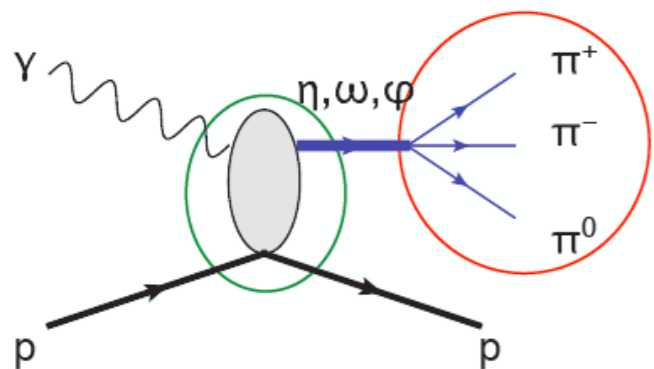
$$\left(Q^2 \equiv \frac{m_s^2 - \hat{m}^2}{m_d^2 - m_u^2} \right)$$

$$\omega \rightarrow \pi^0 \gamma^*$$

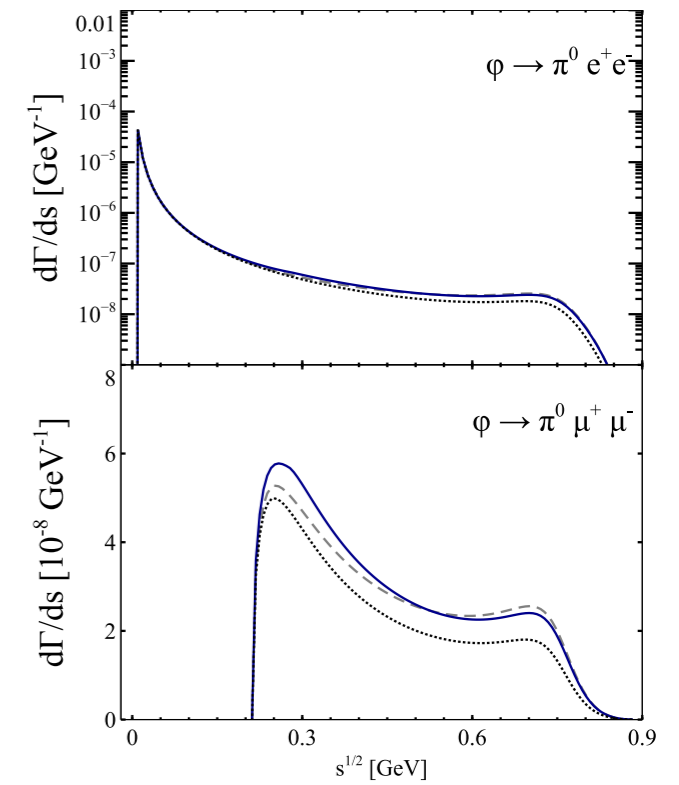
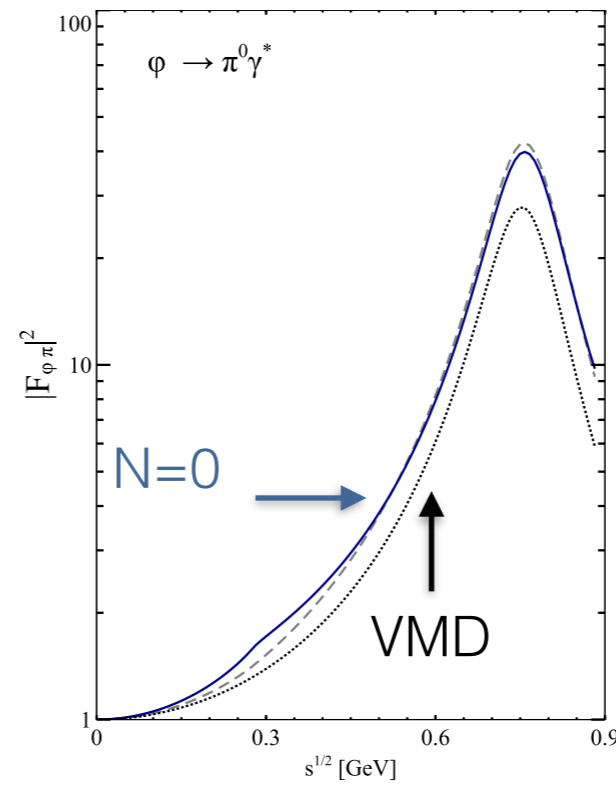


I. Danilkin, JPAC

$$f_{V\pi}(s) = \int_{s_\pi}^{s_i} \frac{ds'}{\pi} \frac{\text{Disc } f_{V\pi}(s')}{s' - s} + \sum_{i=0}^N C_i \omega(s)^i$$



upcoming
CLAS g12



JPAC memebrebrs

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Vincent Mathieu

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<https://wiki.jlab.org/jpac/>

$\gamma p \rightarrow \pi^0 p$

- Formalism
- Model
- Resources
- Run

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$\gamma p \rightarrow \pi^0 p$

We present the model published in [Mat15a].

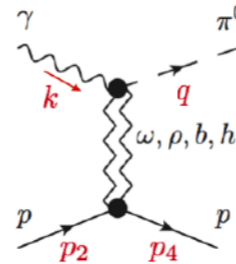
The differential cross section for $\gamma p \rightarrow \pi^0 p$ is computed with Regge amplitudes in the domain $E_\gamma \geq 4$ GeV and $0.01 \leq |t| \leq 3$ (in GeV²).

The formulas can be extrapolated outside these intervals.

We use the CGLN invariant amplitudes A_i defined in [Chew57a].

See the section Formalism for the definition of the variables.

The fitting procedure is detailed in [Mat15a]. We report here only the main feature of the model.



Formalism

The differential cross section is a function of 2 variables. The first is the beam energy in the laboratory frame E_γ (in GeV) or the total energy squared s (in GeV²). The second is the cosine of the scattering angle in the rest frame $\cos \theta$ or the momentum transferred squared t (in GeV²).

The momenta of the particles are k (photon), q (pion), p_2 (target) and p_4 (recoil). The pion mass is μ and the proton mass is M . The Mandelstam variables, $s = (k + p_2)^2$, $t = (k - q)^2$, $u = (k - p_4)^2$ are related through $s + t + u = 2M^2 + \mu^2$.

The differential cross section is expressed in term of the parity conserving helicity invariant amplitudes in the t -channel F_i

$$\frac{d\sigma}{dt} = \frac{389.4}{64\pi} \frac{k_t^2}{4M^2 E_\gamma^2} \left[2 \sin^2 \theta_t (|F_1|^2 + 4p_t^2 |F_2|^2) + (1 - \cos \theta_t)^2 |F_3 + 2\sqrt{t} p_t F_4|^2 + (1 + \cos \theta_t)^2 |F_3 - 2\sqrt{t} p_t F_4|^2 \right]$$

The differential cross section is expressed in $\mu\text{b}/\text{GeV}^2$. We used $(\hbar c)^2 = 0.3894 \text{ mb}\cdot\text{GeV}^2$.

The t -channel is the rest frame of the process $\gamma\pi^0 \rightarrow p\bar{p}$.

In the t -channel, the momenta of the nucleon p_t and the pion k_t and the cosine of the scattering angle are

$$k_t = \frac{1}{2} \sqrt{t - 4M^2}, \quad q_t = \frac{t - \mu^2}{2\sqrt{t}}, \quad \cos \theta_t = \frac{s - u}{4p_t k_t}. \quad (\text{A.1})$$

The invariant amplitudes F_i are related through the CGLN A_i amplitudes [Chew57a] by

$$F_1 = -A_1 + 2MA_4, \quad \eta = +, \quad CP = + \quad (\text{A.2})$$

$$F_2 = A_1 + tA_2, \quad \eta = -, \quad CP = - \quad (\text{A.3})$$

$$F_3 = 2MA_1 - tA_4, \quad \eta = +, \quad CP = + \quad (\text{A.4})$$

$$F_4 = A_3, \quad \eta = -, \quad CP = + \quad (\text{A.5})$$

The F_i amplitudes have good quantum numbers of the t -channel, the naturality $\eta = P(-1)^J$ and the product CP .

Run the code

Choose the beam energy in the lab frame E_γ , the other variable (t or $\cos \theta$) and its minimal, maximal, and increment values. If you choose t (\cos) only the min, max and step values of t ($\cos \theta$) are read.

E_γ in GeV

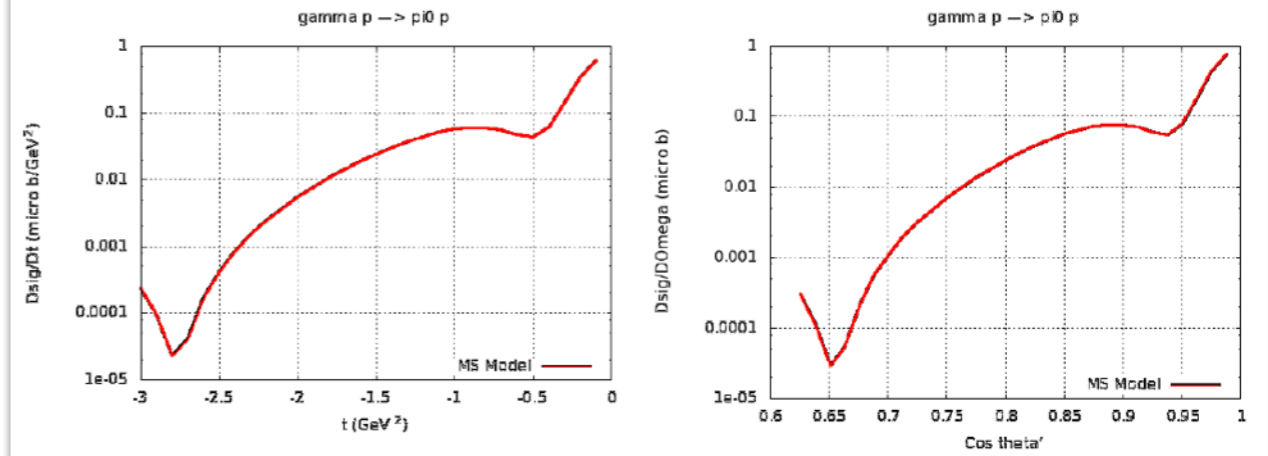
t \cos

t in GeV² (min max step)

$\cos \theta$ (min max step)

Download the output file, the plot with $Ox=t$, the plot with $Ox=\cos$.

In the file, the columns are: t (GeV²), \cos , $D\text{sig}/D\text{t}$ (micro barn/GeV²), $D\text{sig}/D\text{Omega}$ (micro barn)



special thanks to Vincent Mathieu



<http://cgl.soic.indiana.edu/jpac>



supported by NSF "Physics at the Information Frontier: Extensible Computational Services for Discovery of New Particles"