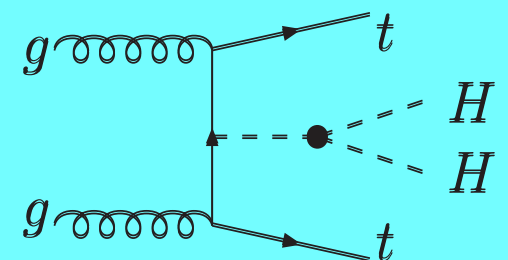
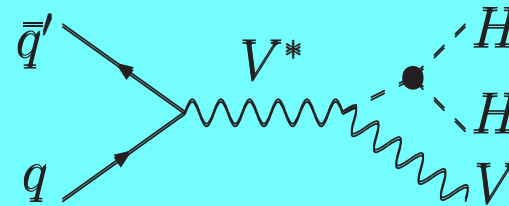
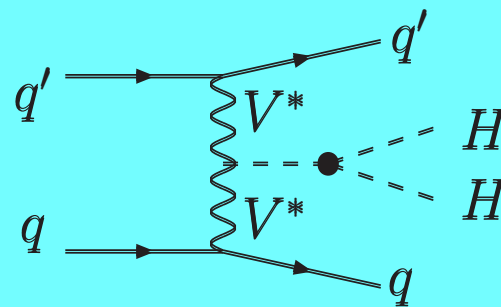
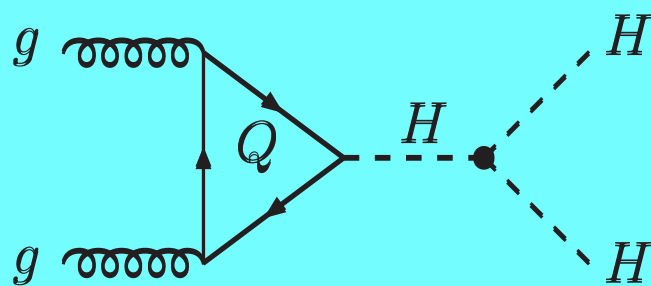


XVII Roma Tre Topical Seminar on Subnuclear Physics:

# The Higgs potential and physics at future colliders

10 December 2014, Università di Roma Tre, Italy

## Measurement of the *Higgs self-coupling* at the $\mathcal{HL-LHC}$ and future colliders



Roma, 10 December 2014

# Outline

- SM Higgs potential and Higgs self-coupling  $\lambda_{HHH}$
- $pp \rightarrow HH$  cross sections vs  $\lambda_{HHH}$
- a challenge for HH production  $\rightarrow$  TH uncertainties
- HH production BSM
- searches for HH in Run 1
- HH production at HL-LHC : present projections
- HH production at Linear Colliders : present projections
- Outlook

*updated discussion in LHC Higgs-XSections Working Groups :*

<https://indico.cern.ch/category/5847/>

*(with all relevant references...)*

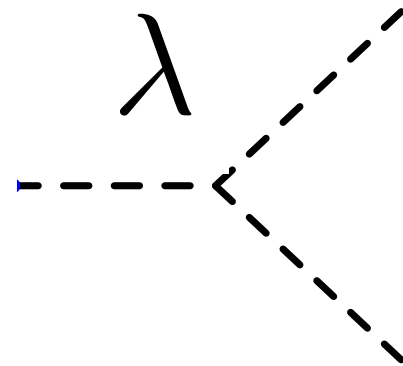
# Higgs self-couplings in the SM

$$V(H) = \frac{1}{2}M_H^2 H^2 + \lambda v H^3 + \frac{1}{4}\lambda' H^4$$

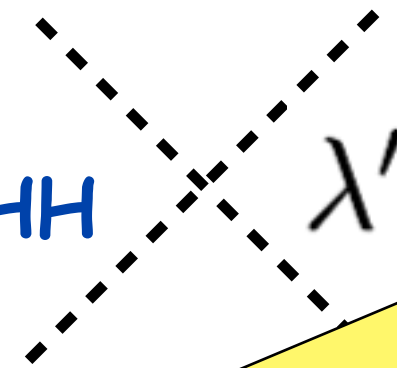
● in the SM :  $\lambda = \lambda' = M_H^2 / (2v^2) = 0.13$

***$m_H$  directly related to Higgs dynamics !***

● needs HH  
in final states



needs HHH



**out of reach !**

● BSM : Max  $\lambda$  deviations  
compatible with no  
other BSM observation:  
few % to ~20%

| Model                 | $\Delta g_{hhh} / g_{hhh}^{SM}$      |
|-----------------------|--------------------------------------|
| Mixed-in Singlet      | -18 %                                |
| Composite Higgs       | tens of %                            |
| Minimal Supersymmetry | -2 % <sup>a</sup> -15 % <sup>b</sup> |
| NMSSM                 | -25 %                                |

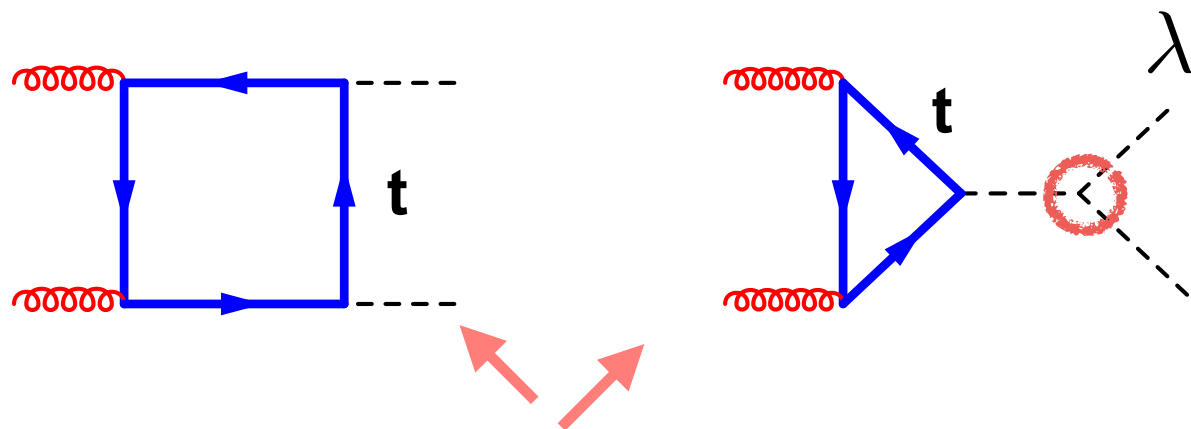
● target for both TH and EXP accuracies !

# bad news ! $\rightarrow$ tiny SM HH rates !

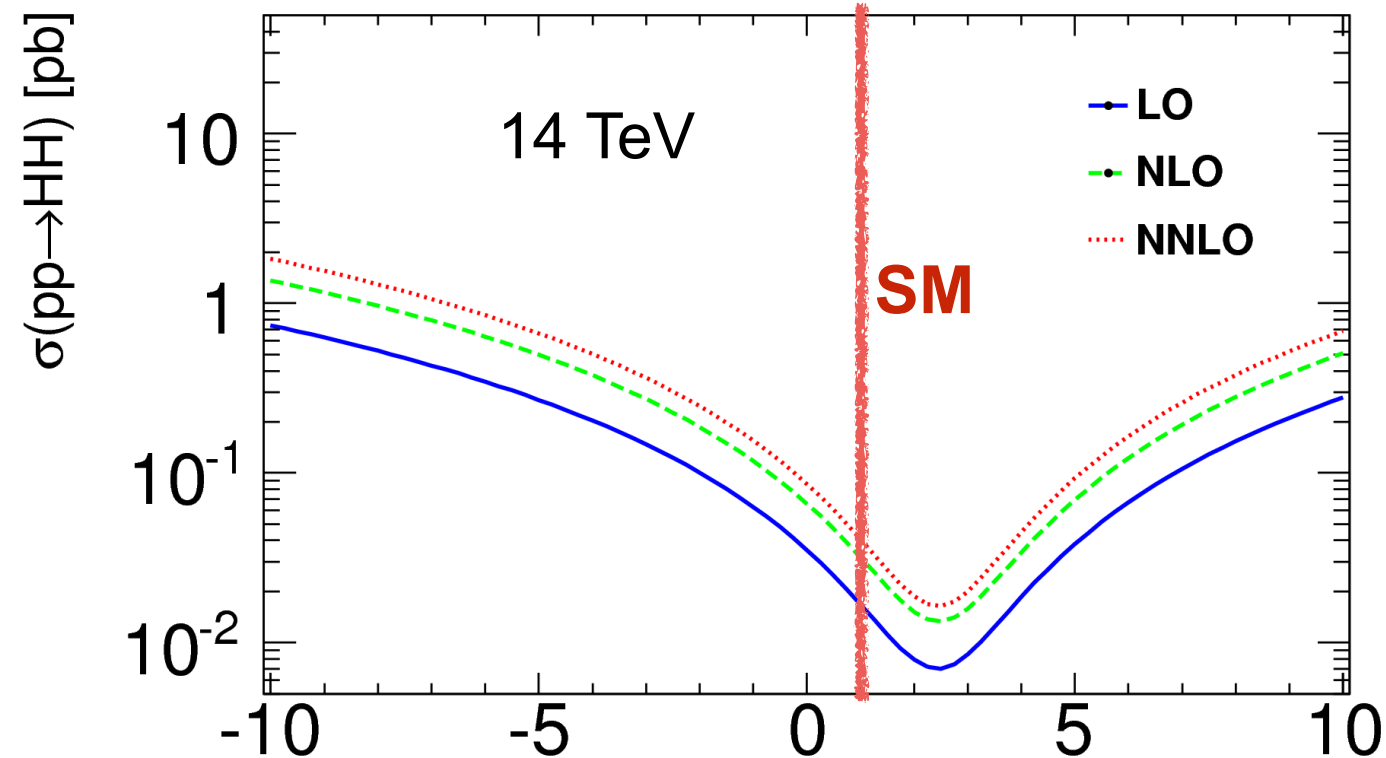
- dominant production in pp collisions :

$$\sigma(HH)_{SM} \sim 10^{-3} \sigma(H)_{SM}$$

$$gg \rightarrow HH$$



destructive interference  
ruled by  $Y_t$  and  $\lambda$



$$[\lambda^{SM} = (m_H/v)^2/2 = 0.13] \quad \lambda_{HHH} / \lambda_{HHH}^{SM}$$

- other production channels have  $\sigma < 1/10 \sigma(HH)$  :

$$qq' \rightarrow HHqq'$$

$$q\bar{q}' \rightarrow ZHH/WHH$$

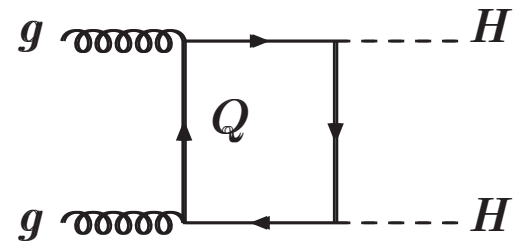
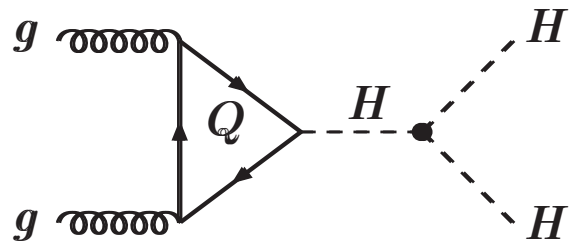
$$q\bar{q}, gg \rightarrow t\bar{t}HH$$



tiny  $\sigma$ 's !

| $\sqrt{s}$<br>(TeV) | Cross sections (fb) and theoretical uncertainties (%) |                              |                                    |                                    |  |
|---------------------|---|------------------------------|------------------------------------|------------------------------------|--|
|                     | $gg \rightarrow HH$<br>NLO                            | $qq \rightarrow qqHH$<br>NLO | $q\bar{q} \rightarrow WHH$<br>NNLO | $q\bar{q} \rightarrow ZHH$<br>NNLO | $q\bar{q}/gg \rightarrow t\bar{t}HH$<br>LO |
| 14                  | $33.89^{+37.2\%}_{-29.8\%}$                           | $2.01^{+7.6\%}_{-5.1\%}$     | $0.57^{+3.7\%}_{-3.3\%}$           | $0.42^{+7.0\%}_{-5.5\%}$           | 1.02                                       |
| 33                  | $207.29^{+33.0\%}_{-26.7\%}$                          | $12.05^{+6.1\%}_{-4.2\%}$    | $1.99^{+3.5\%}_{-3.1\%}$           | $1.68^{+7.9\%}_{-6.7\%}$           | 7.91                                       |
| 100                 | $1417.83^{+29.7\%}_{-24.7\%}$                         | $79.55^{+6.2\%}_{-4.1\%}$    | $8.00^{+4.2\%}_{-3.7\%}$           | $8.27^{+8.4\%}_{-8.0\%}$           | 77.82                                      |

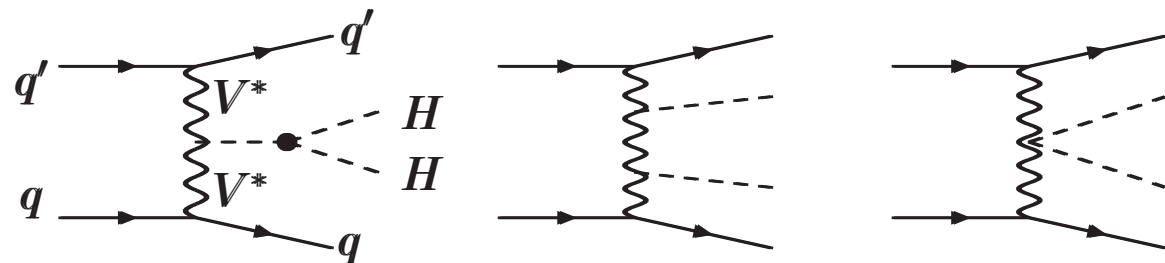
$gg$  double-Higgs fusion:  $gg \rightarrow HH$



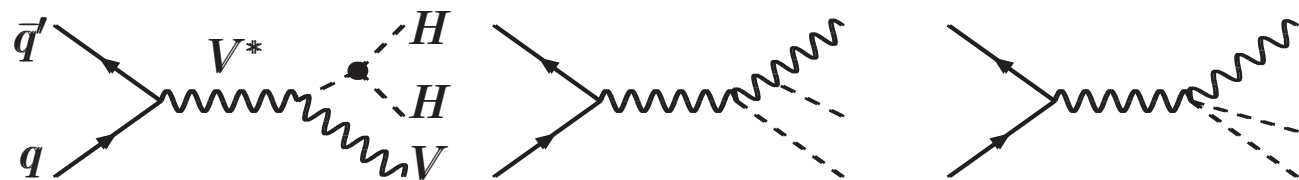
TH accuracies

$\sim qqHH$

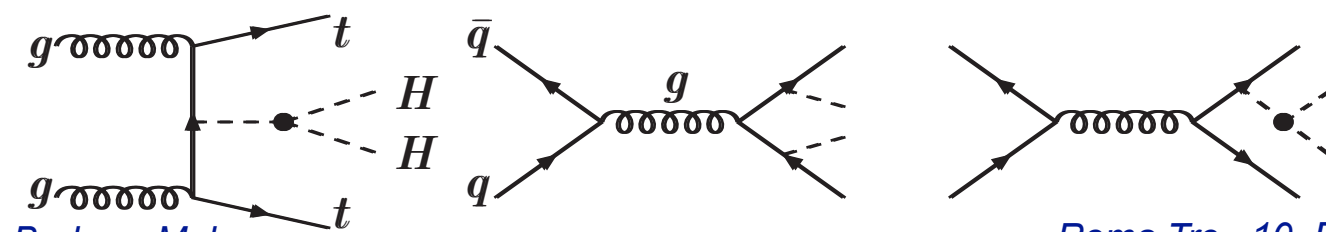
$WW/ZZ$  double-Higgs fusion:  $qq' \rightarrow HHqq'$



Double Higgs-strahlung:  $q\bar{q}' \rightarrow ZHH/WHH$

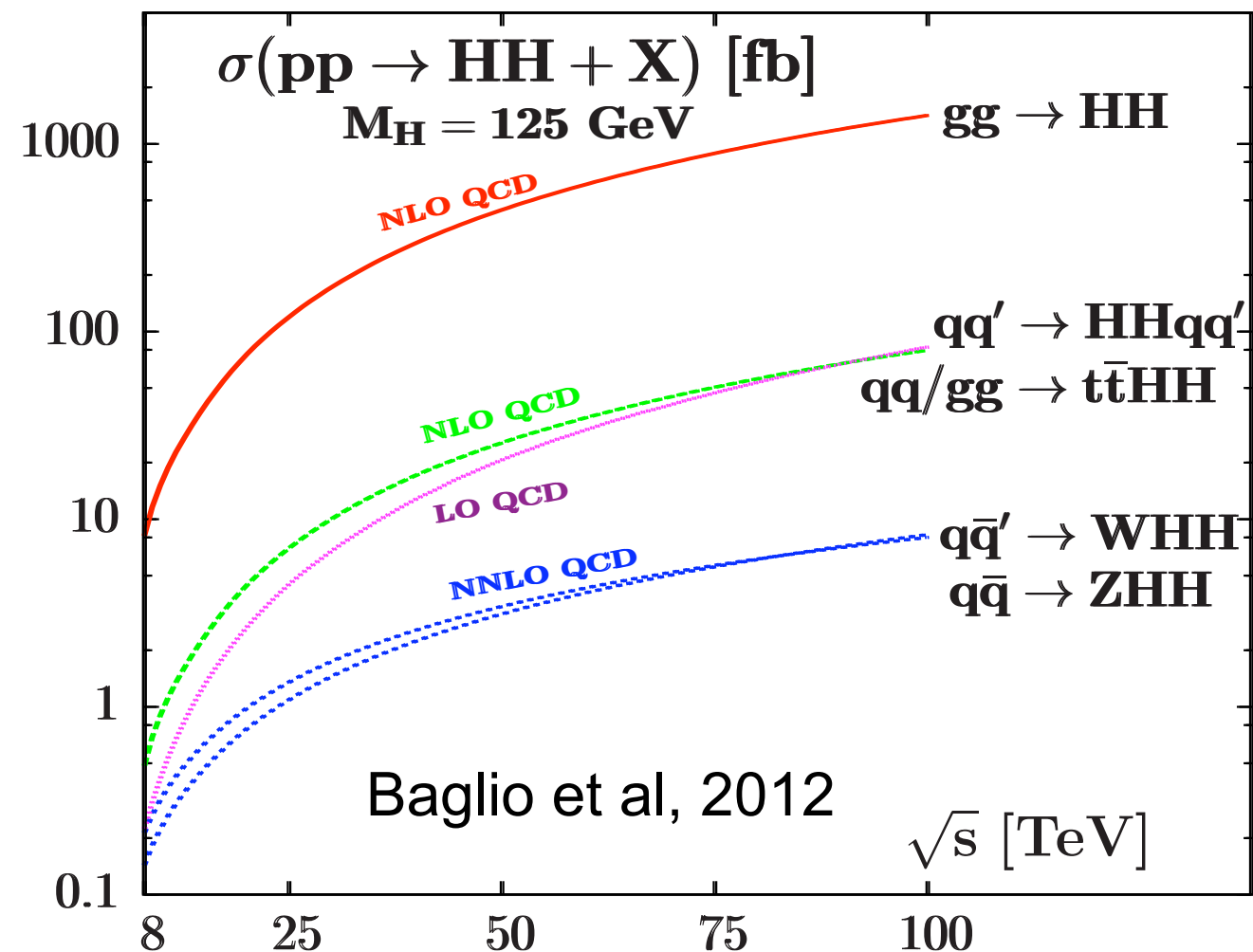


Associated production with top-quarks:  $q\bar{q}/gg \rightarrow t\bar{t}HH$

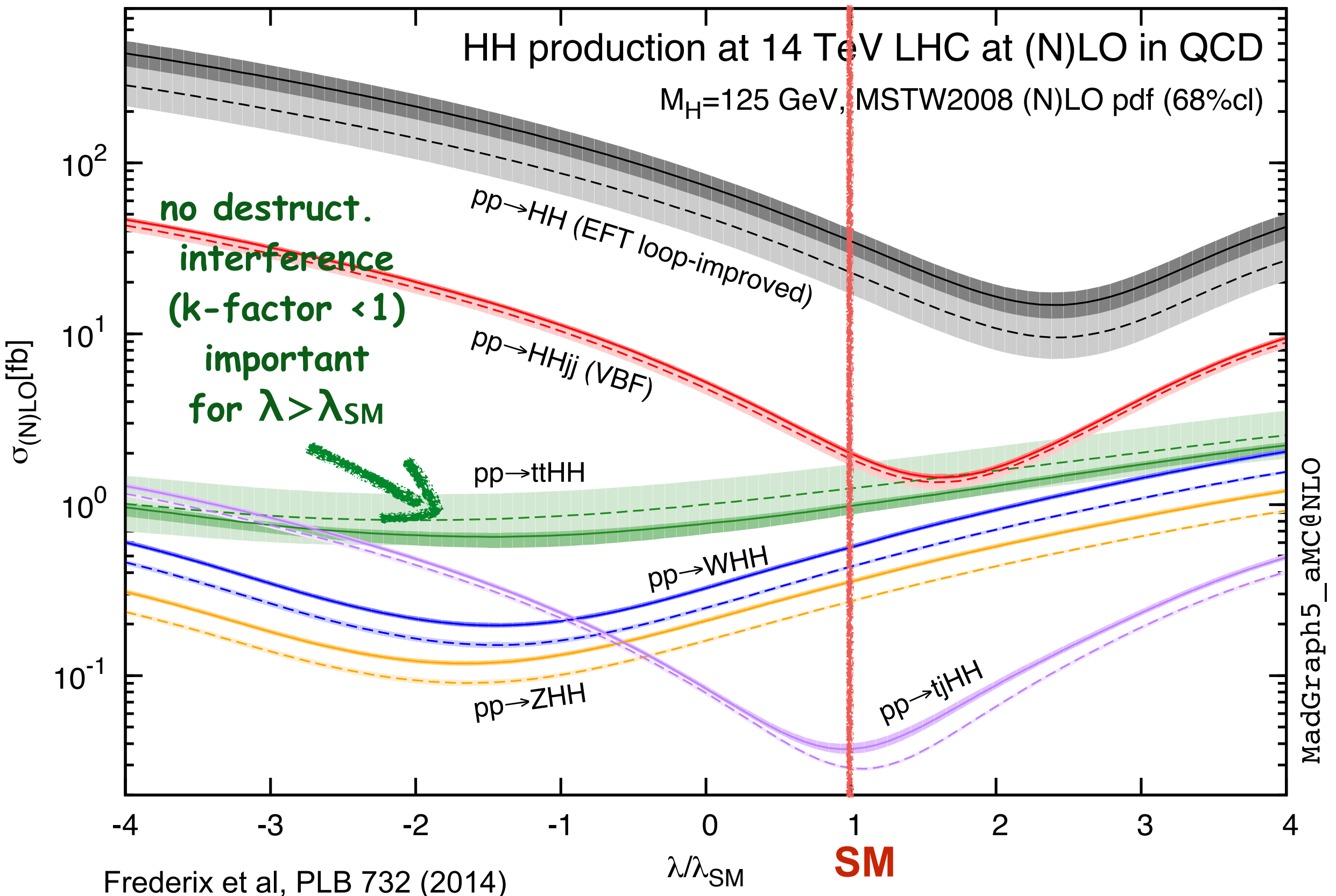


Barbara Mele

Roma Tre, 10 December 2014



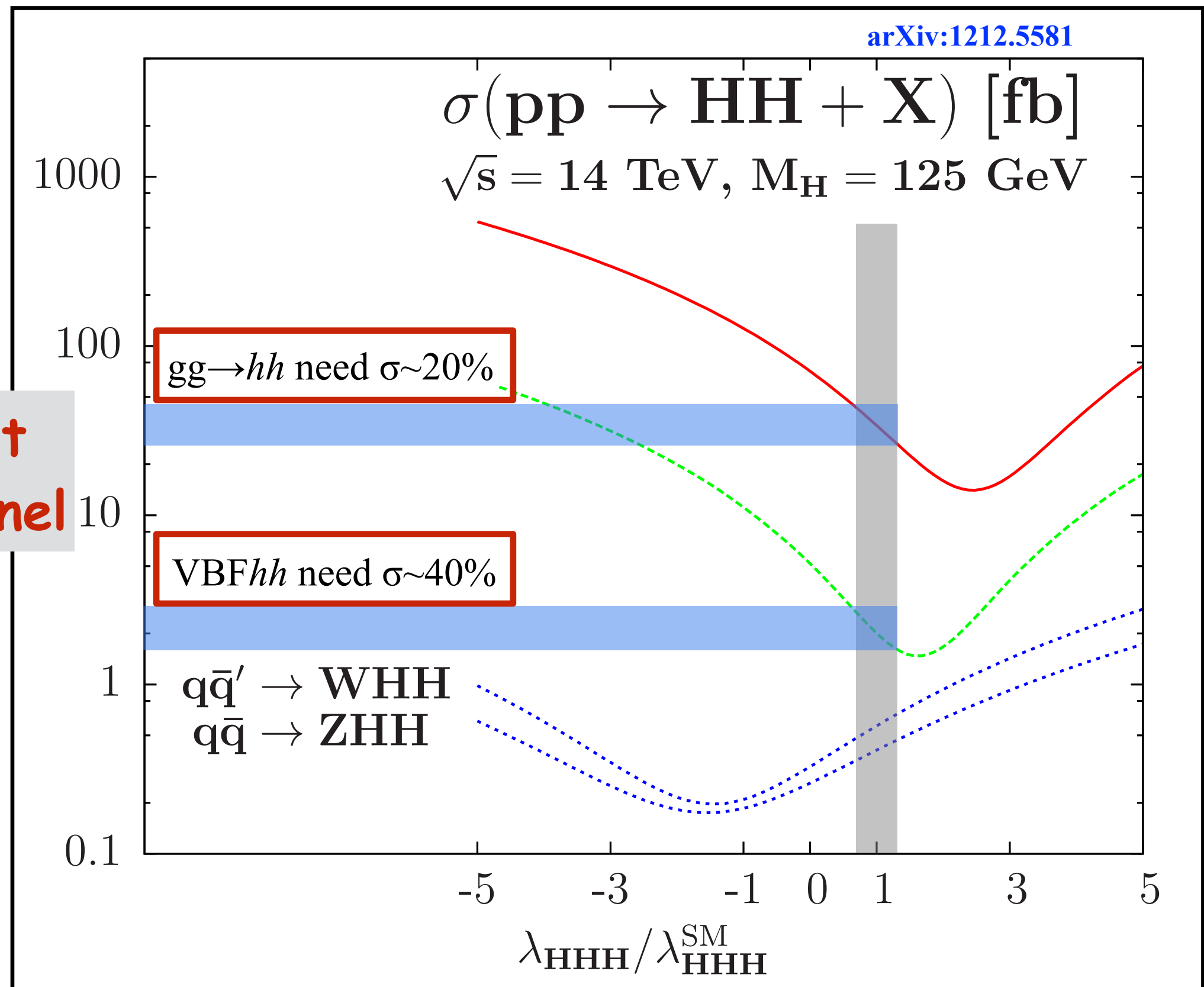
# $\sigma$ sensitivity to $\lambda H^3$ coupling at 14 TeV



# Target: $\sim 20\%$ constrain on $\lambda_{HHH}$

arXiv:1212.5581

VBF HH most sensitive channel

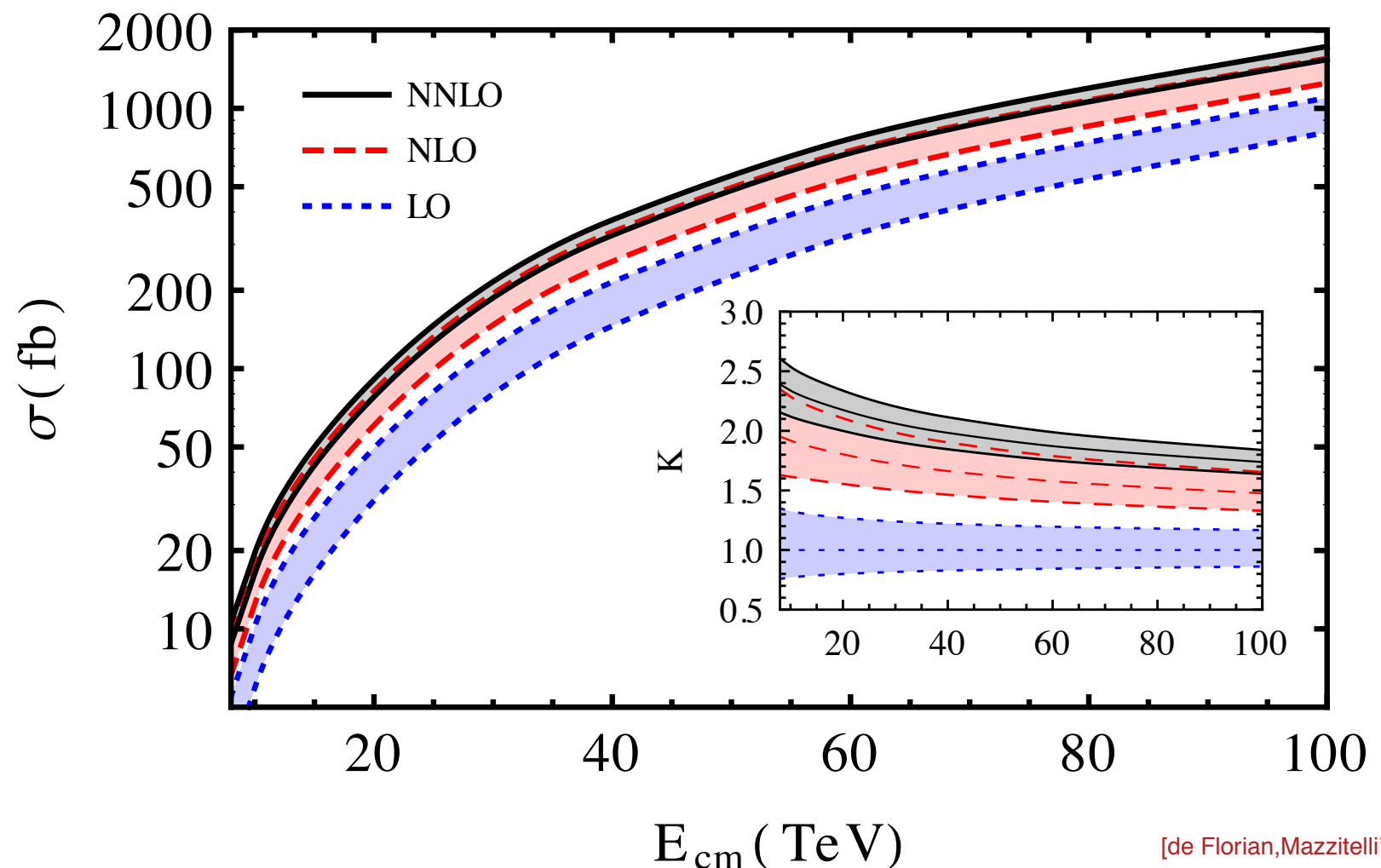
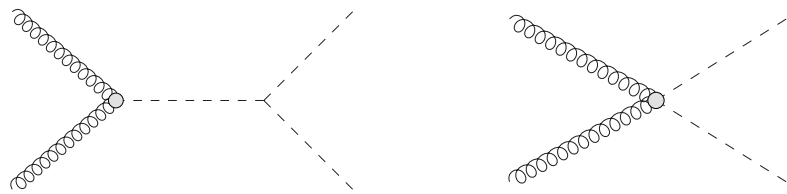


# $gg \rightarrow HH$ (TH): known results

- LO cross section  $\sim 18$  fb  $(\sqrt{S}=14$  TeV)
- NLO ( $m_t \rightarrow \infty$ )  $\sim +100\%$
- NLO including  $1/m_t$  terms  $\sim +10\%$
- NNLO ( $m_t \rightarrow \infty$ )  $\sim +20\%$
- NNLL soft-gluon resumm.  $\sim \text{NLO} + 20\%$

**Effective Lagrangian (EFT)**  
used in the large  $m_t$  limit

$$\mathcal{L}_{\text{eff}} = -\frac{1}{4}G_{\mu\nu}G^{\mu\nu} \left( C_H \frac{H}{v} - C_{HH} \frac{H^2}{v^2} \right)$$



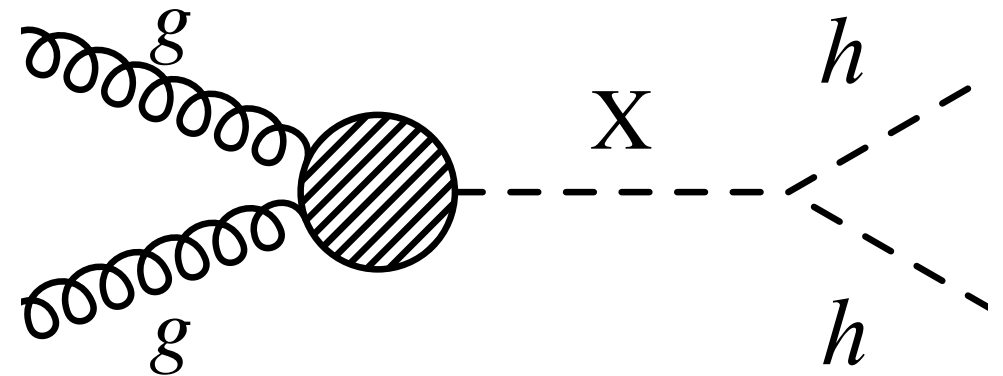
[de Florian, Mazzitelli'13]

# TH uncertainties on $gg \rightarrow HH$

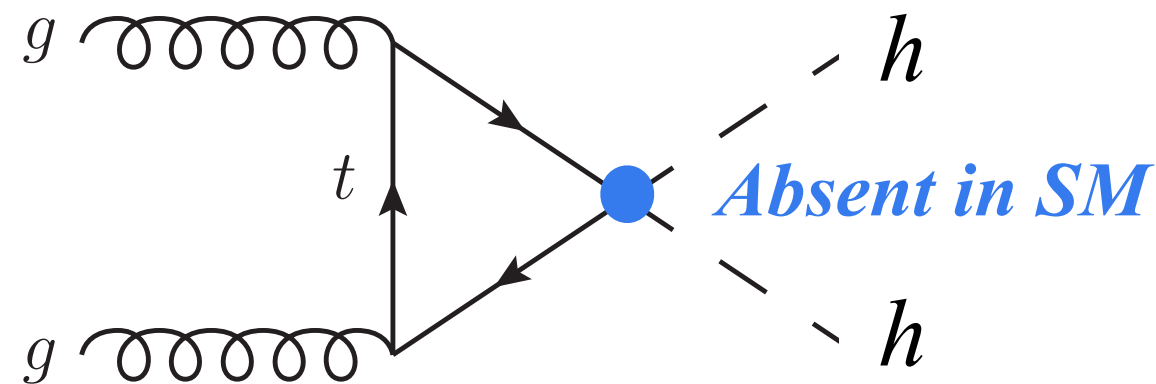
- scale uncertainty :  $\sim 20\%$  at NLO (EFT)  
 $\sim 10\%$  at NNLO (EFT)
- PDF +  $\alpha_S$  :  $\sim 10\%$
- finite  $m_{\text{top}}$  effects :  $\sim 10\%$  (?)
- $m_{\text{top}}$  uncertainties:  $\frac{\Delta\sigma}{\sigma} \simeq 0.6\% \frac{\Delta m_t}{1\text{GeV}}$
- Total  $\rightarrow \sim 30\%$  ?
- full two-loop calculation (hard) would help...

# HH production in BSM

- significant **enhancement** in many BSM frameworks
  - HH resonant production (KK-gravitons, 2HDM, (N)MSSM,...)
    - potentially large cross section (up to pb)
    - $m_X$  shape helps with bckgrs



- HH non-resonant enhancement
  - Composite Higgs/Little Higgs/...
  - can modify  $\lambda$  or/and give rise to new couplings
  - can give strong enhancement at large  $p_T(H)$

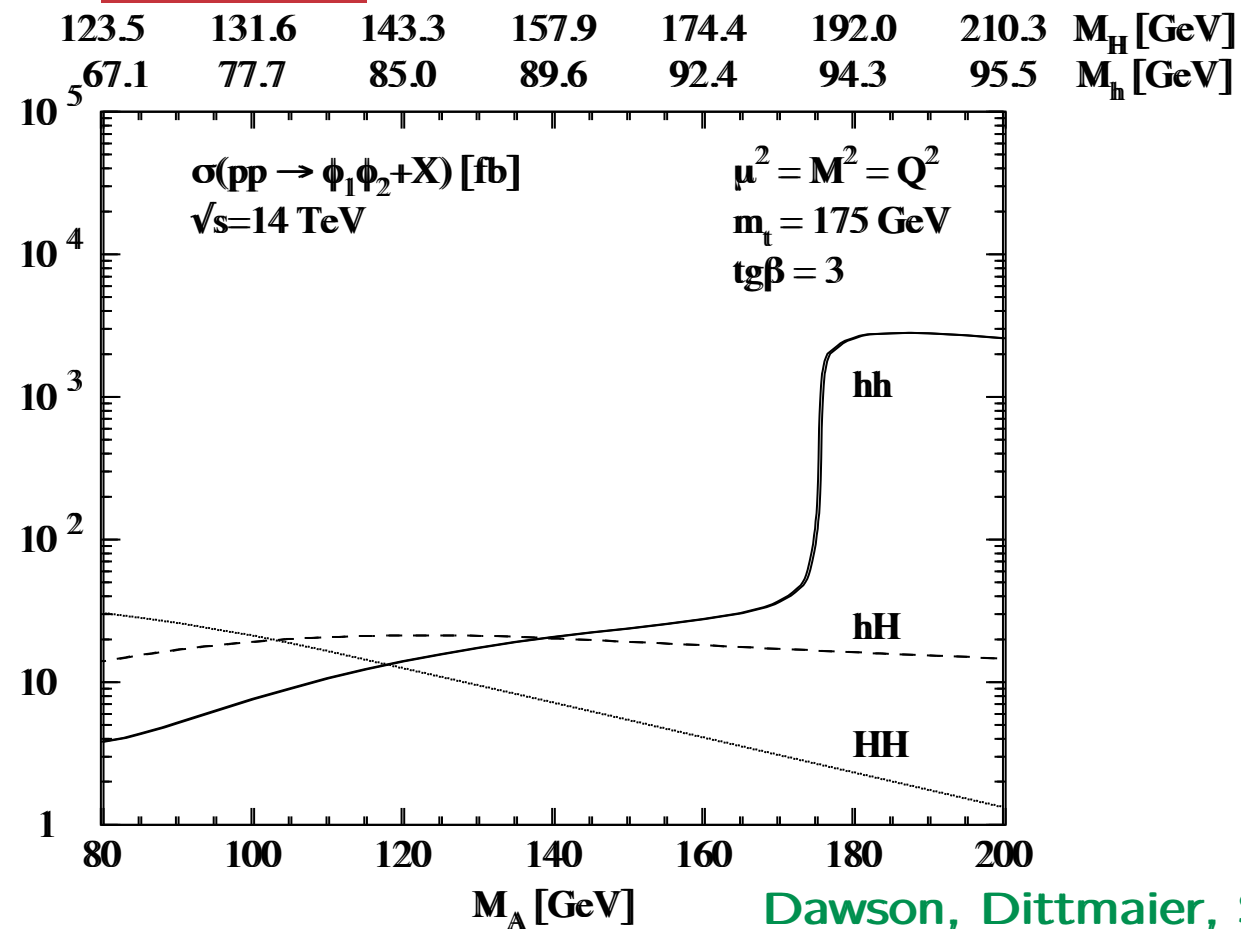


*anomalous Higgs-top  
quartic coupling*

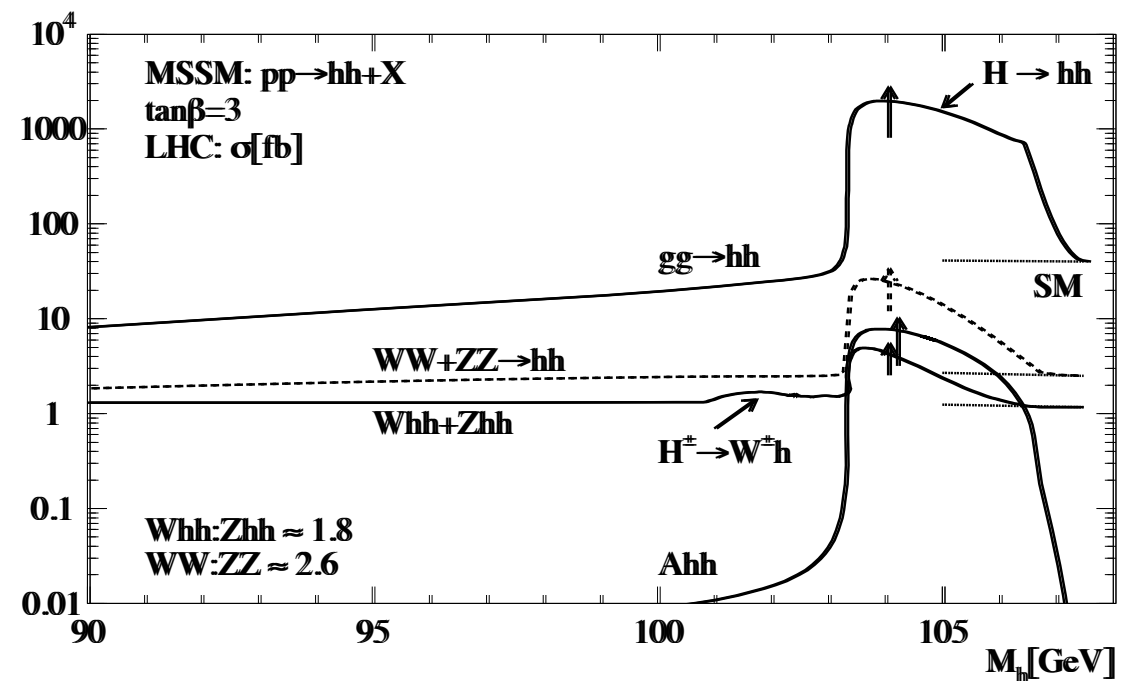
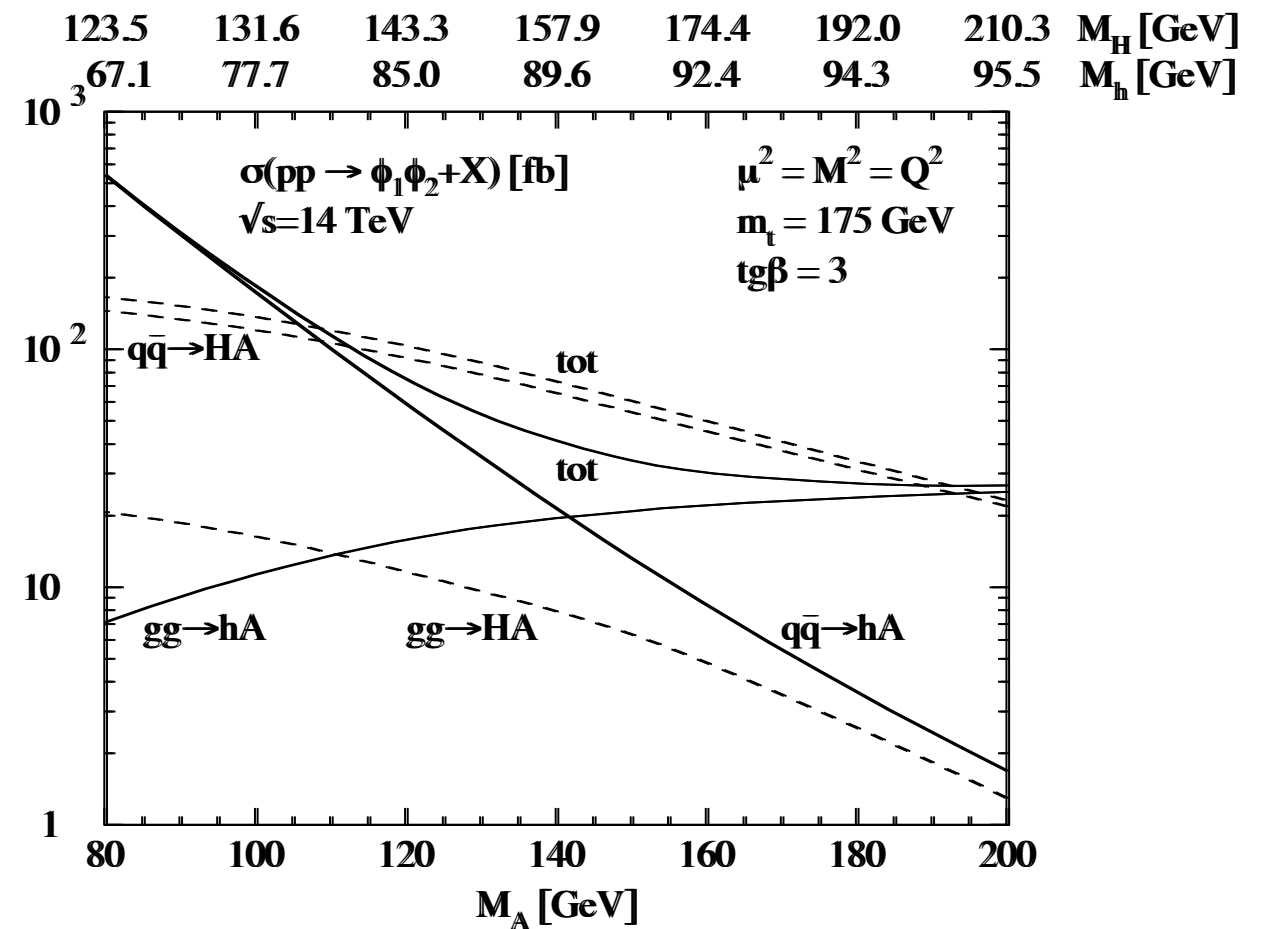
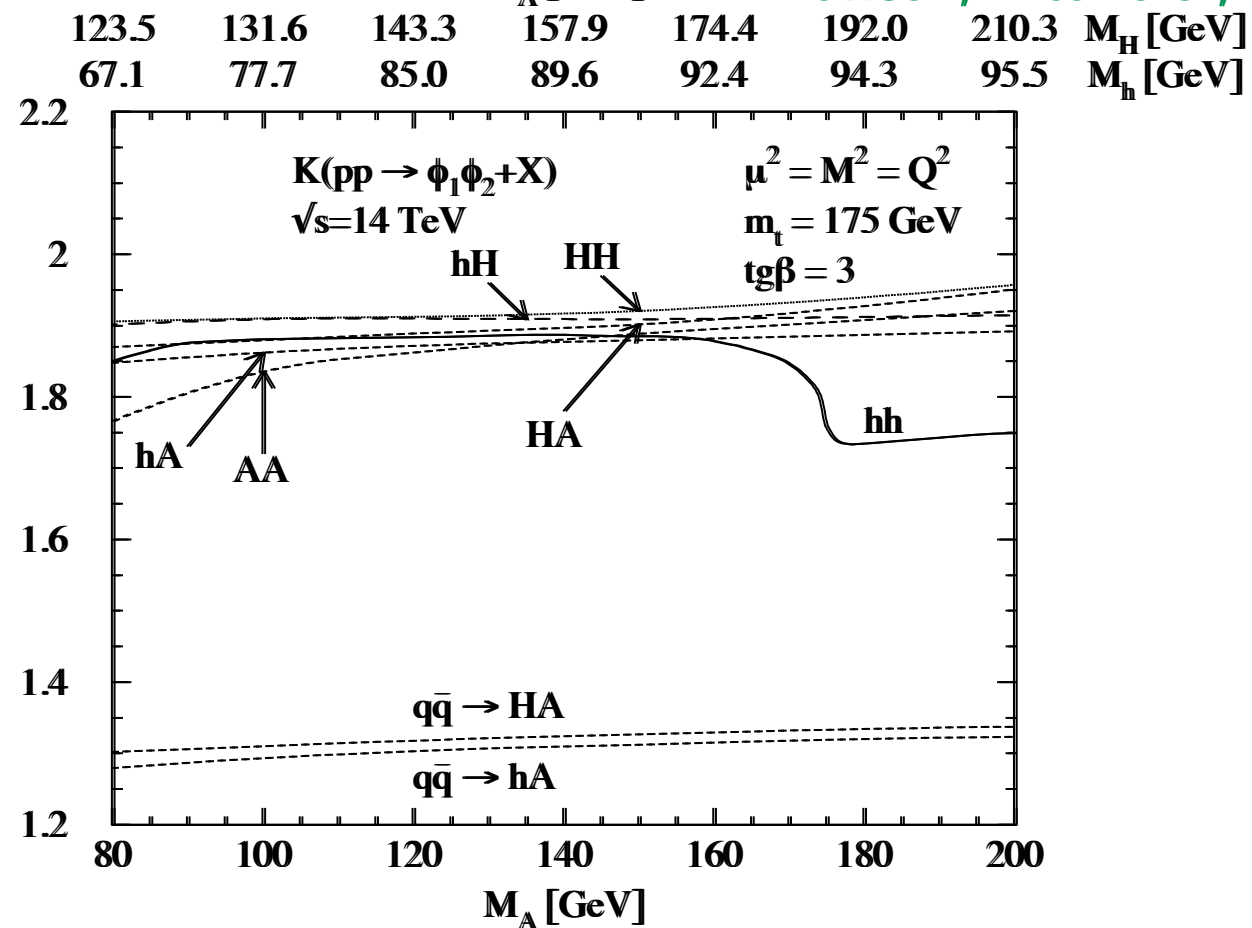
- analysis relevant also for Run 1



# MSSM $gg \rightarrow hh, hH, HH, hA, HA, AA$ and $q\bar{q} \rightarrow hA, HA$



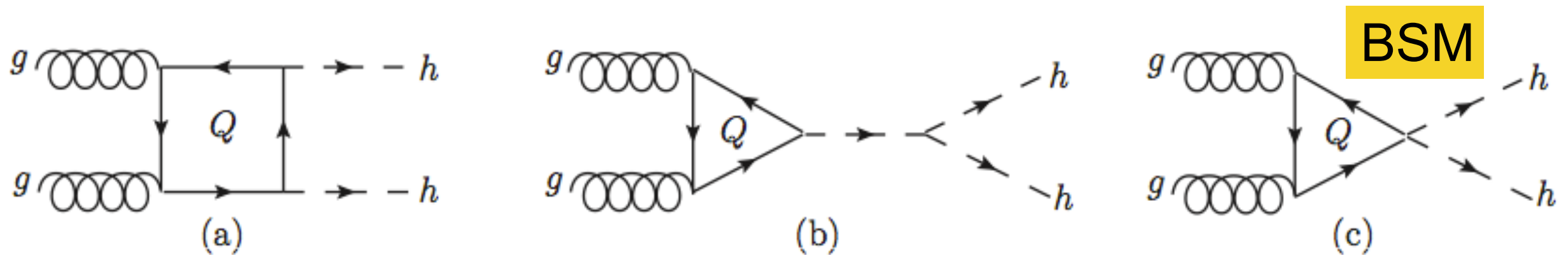
Dawson, Dittmaier, S.



Djouadi, Kilian, Mühlleitner, Zerwas

Spira HXS

# non-resonant HH enhancement



$$\frac{d\hat{\sigma}(gg \rightarrow hh)}{d\hat{t}} = \frac{G_F^2 \alpha_s^2}{512(2\pi)^3} \left[ \left| \left( c_{tri} \frac{3m_h^2}{\hat{s} - m_h^2} + c_{nl} \right) F_{\Delta} + c_{box} F_{\square} \right|^2 + |c_{box} G_{\square}|^2 \right]$$

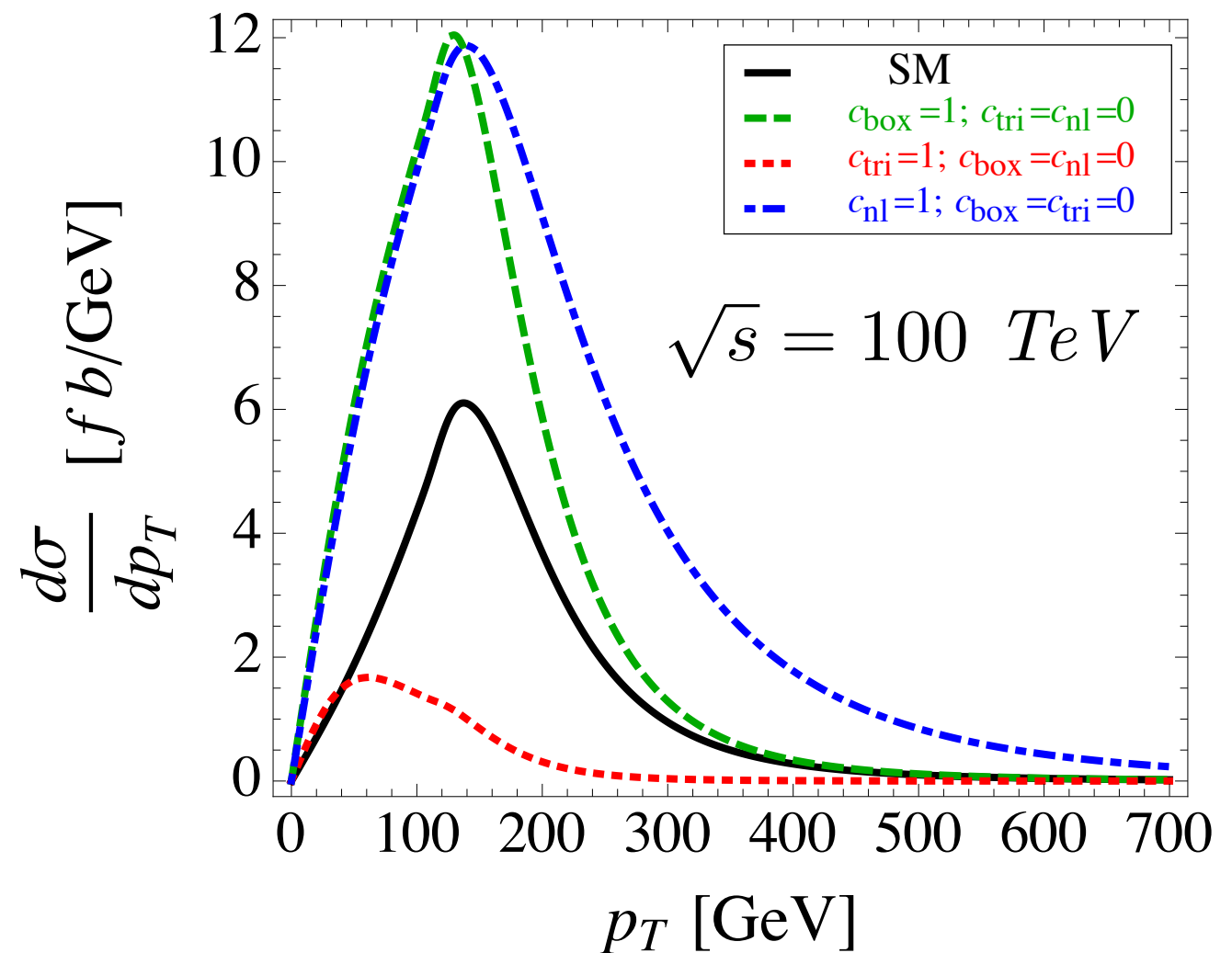
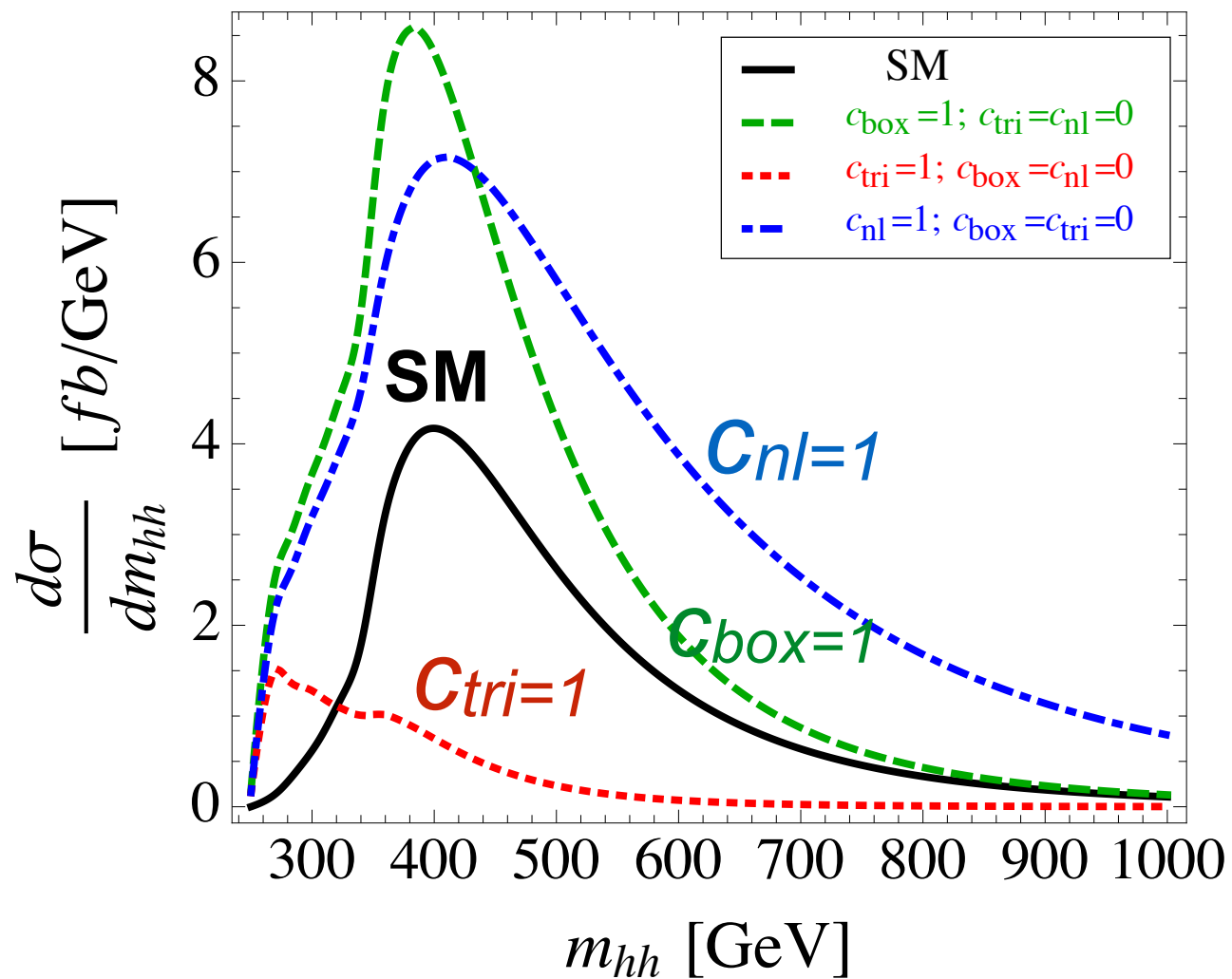
$$c_{box}^{(SM)} = 1, \quad c_{tri}^{(SM)} = 1, \quad c_{nl}^{(SM)} = 0$$

interferences between graphs → degeneracies in  $\sigma$ 's

$$\sigma(gg \rightarrow hh) = \sigma^{SM}(gg \rightarrow hh) [1.849 c_{box}^2 + 0.201 c_{tri}^2 + 2.684 c_{nl}^2 - 1.050 c_{box} c_{tri} - 3.974 c_{box} c_{nl} + 1.215 c_{tri} c_{nl}].$$

Chen, Low, arXiv:1405.7040

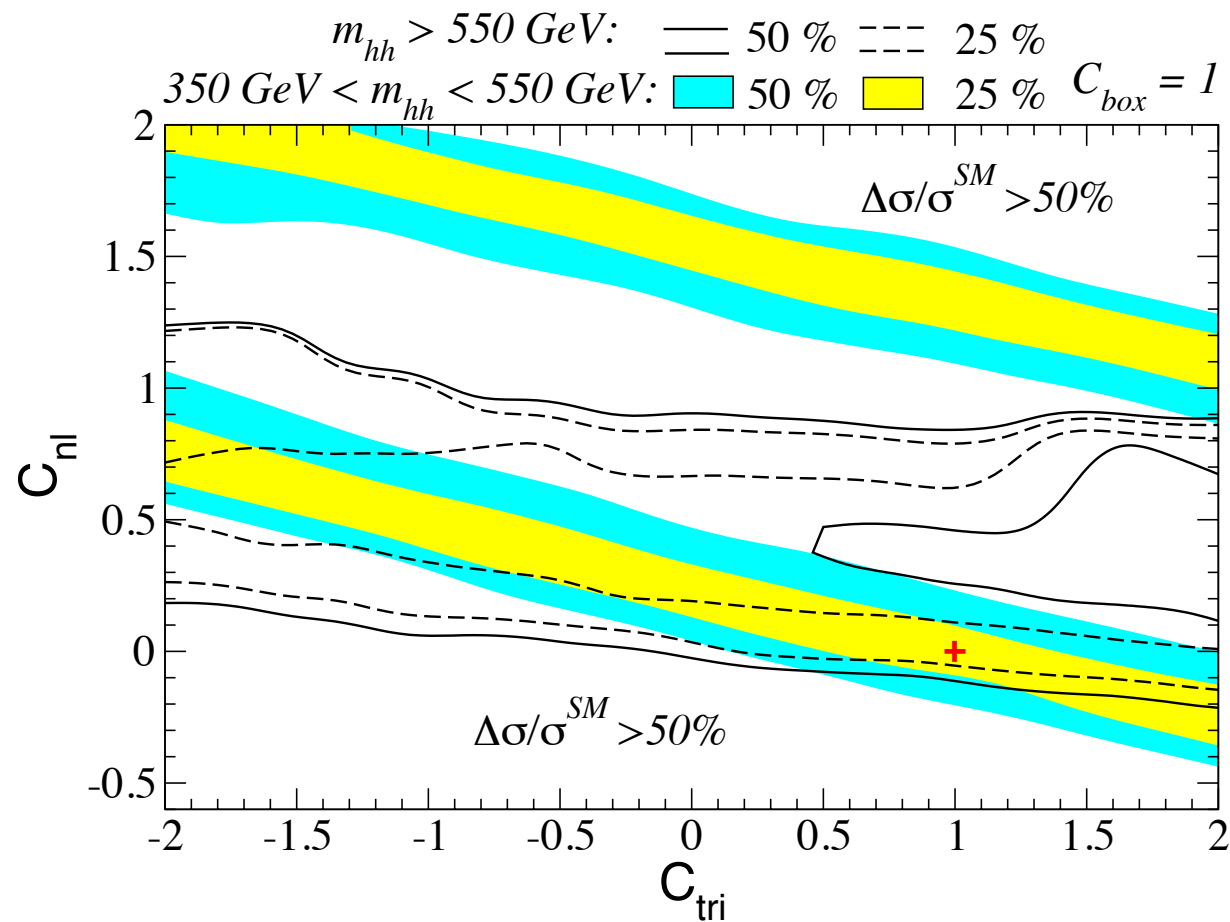
# kinematic. distributions can help



**Warning** : a small  $C_{nl}$  could mimic effects from BSM  $C_{tri}$

Chen, Low, arXiv:1405.7040

# moderate sensitivity to $C_{\text{tri}}$ ( $\lambda$ )

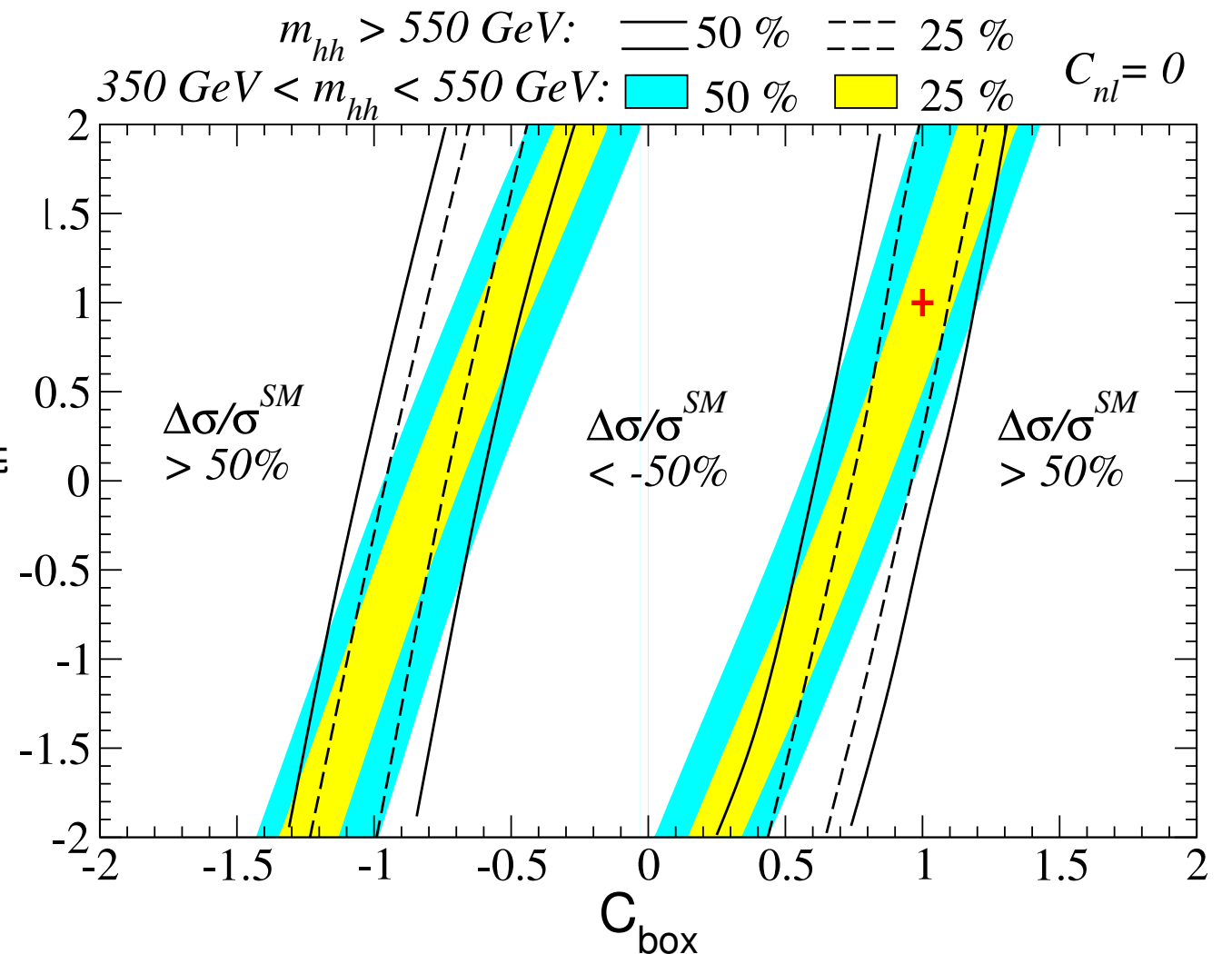


kinem information from two different  $m_{hh}$  bins allows for a significant improvement in constraining  $C_{\text{tri}}$  wrt using the  $\sigma$  measurement alone.

Chen, Low, arXiv:1405.7040

$$\sqrt{s} = 100 \text{ TeV}$$

sensitivity on self-coupling still the least !



# (SM) HH rates at HL-LHC (ev/3000fb<sup>-1</sup>)

| Decay Channel                 | Branching Ratio | Total Yield (3000 fb <sup>-1</sup> ) |
|-------------------------------|-----------------|--------------------------------------|
| $b\bar{b} + b\bar{b}$         | 33%             | 40,000                               |
| $b\bar{b} + W^+W^-$           | 25%             | 31,000                               |
| $b\bar{b} + \tau^+\tau^-$     | 7.3%            | 8,900                                |
| $ZZ + b\bar{b}$               | 3.1%            | 3,800                                |
| $W^+W^- + \tau^+\tau^-$       | 2.7%            | 3,300                                |
| $ZZ + W^+W^-$                 | 1.1%            | 1,300                                |
| $\gamma\gamma + b\bar{b}$     | 0.26%           | 320                                  |
| $\gamma\gamma + \gamma\gamma$ | 0.0010%         | 1.2                                  |

selection of HH final states has to account for:

(40.8 fb NNLO HH)

- final states experimentally clear and robust
- final states with large enough production rate

HH → bbWW [large rates but  $S(\sim 10^3)/B(\text{tt pairs}) \sim 10^{-4}$ ]

HH → bbγγ [clean but small rates], (also HH → bb[ττ, bb, ZZ, μμ])

many studies ... results not yet robust !

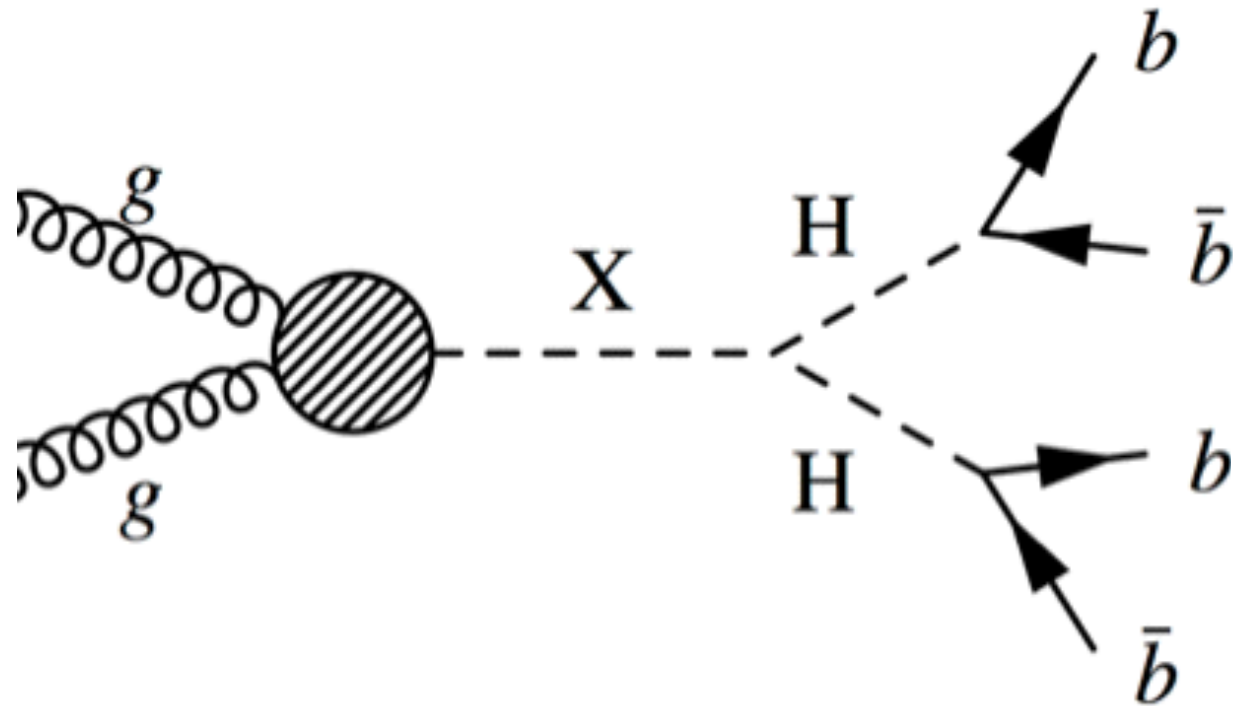
| Decay                  | Issues   | Expectation<br>3000 ifb   | References  |
|------------------------|--|---|---|
| $b\bar{b}\gamma\gamma$ | <ul style="list-style-type: none"> <li>• Signal small</li> <li>• BKG large &amp; difficult to asses</li> <li>• Simple reconst.</li> </ul>                              | $S/B \simeq 1/3$<br>$S/\sqrt{B} \simeq 2.5$   | [Baur, Plehn, Rainwater]<br>[Yao 1308.6302]<br>[Baglio et al. JHEP 1304]                      |
| $b\bar{b}\tau^+\tau^-$ | <ul style="list-style-type: none"> <li>• tau rec tough</li> <li>• largest bkg tt</li> <li>• Boost+MT2 might help</li> </ul>  | <b>differ a lot</b><br>$S/B \simeq 1/5$<br>$S/\sqrt{B} \simeq 5$                        | [Dolan, Englert, MS]<br>[Barr, Dolan, Englert, MS]<br>[Baglio et al. JHEP 1304]               |
| $b\bar{b}W^+W^-$       | <ul style="list-style-type: none"> <li>• looks like tt</li> <li>• Need semilep. W to rec. two H</li> <li>• Boost + BDT proposed</li> </ul>                             | <b>differ a lot</b><br><b>best case:</b><br>$S/B \simeq 1.5$<br>$S/\sqrt{B} \simeq 8.2$ | [Dolan, Englert, MS]<br>[Baglio et al. JHEP 1304]<br>[Papaefstathiou, Yang, Zurita 1209.1489] |
| $b\bar{b}b\bar{b}$     | <ul style="list-style-type: none"> <li>• Trigger issue (high pT kill signal)</li> <li>• 4b background large difficult with MC</li> <li>• Subjets might help</li> </ul> | $S/B \simeq 0.02$<br>$S/\sqrt{B} \leq 2.0$  | [Dolan, Englert, MS]<br>[Ferreira de Lima, Papaefstathiou, MS]<br>[Wardrope et al, 1410.2794] |
| others                 | <ul style="list-style-type: none"> <li>• Many taus/W not clear if 2 Higgs</li> <li>• Zs, photons no rate</li> </ul>  |   |   |



# resonant HH : Run 1 results (8 TeV)

narrow resonances from  
WED radion/graviton, 2HDM

competitive with  
VV searches

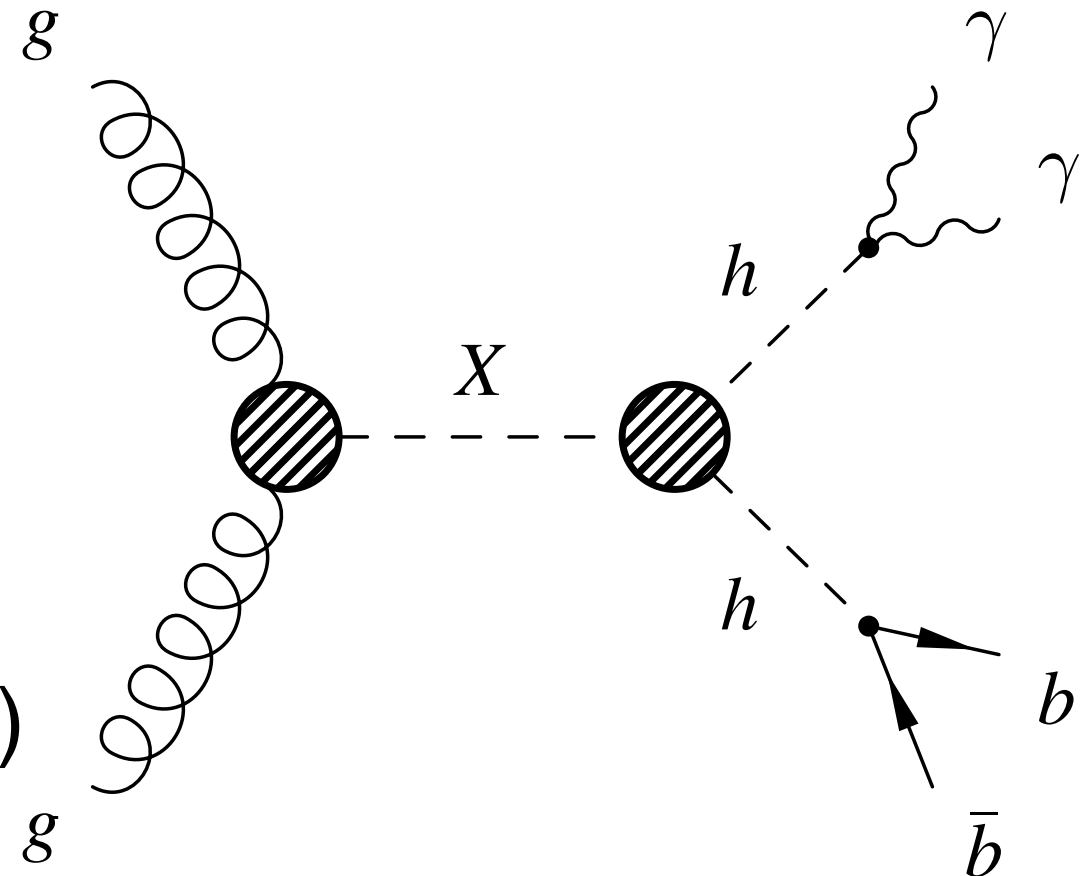


ATLAS-CONF-2014-005 (bbbb)

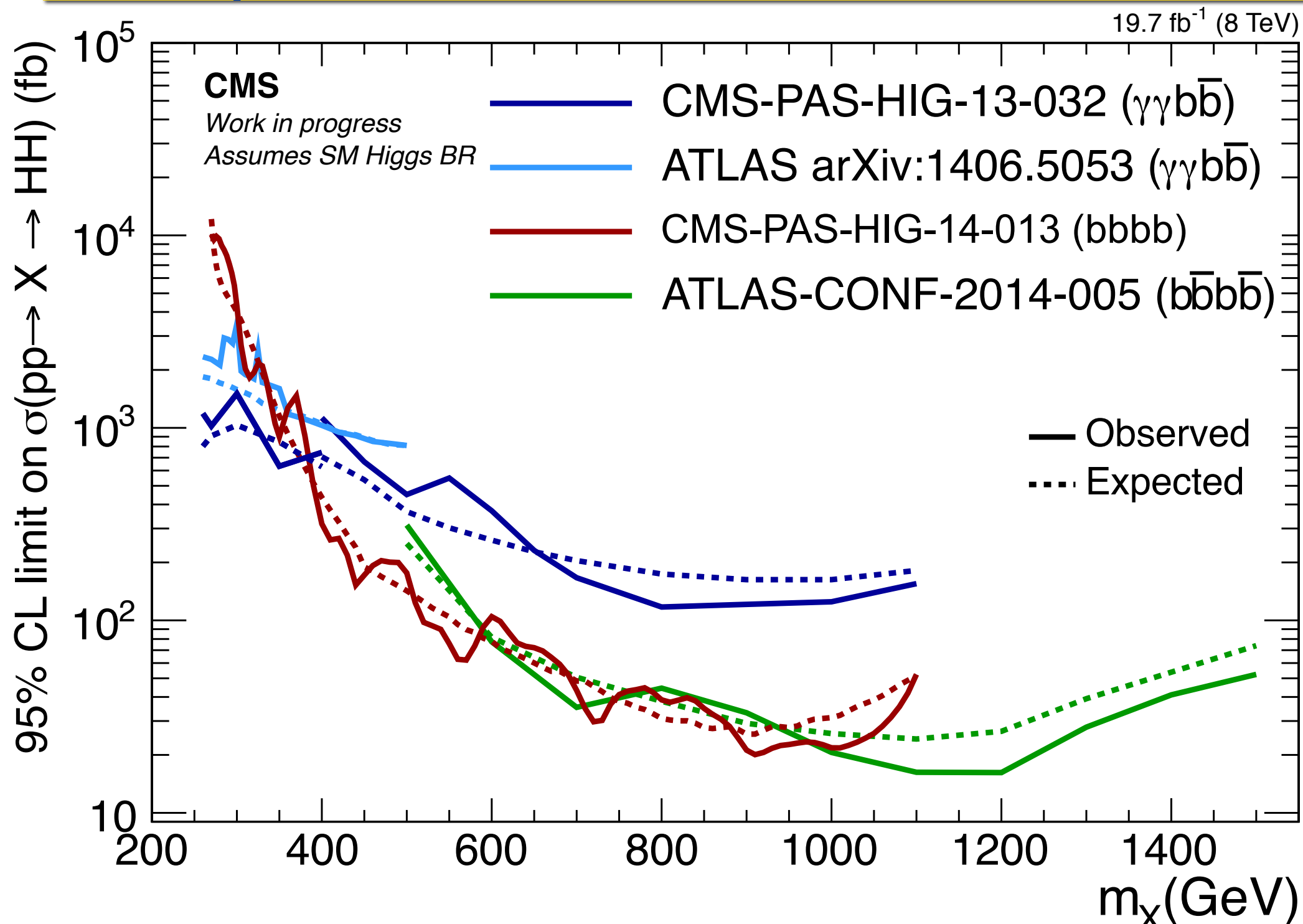
CMS-PAS-HIG-14-013 (bbbb)

CMS-PAS-HIG-13-032 ( $\gamma\gamma bb$ )

ATLAS arXiv:1406.5053 ( $\gamma\gamma bb$ )



# Comparison of sensitivities (ATLAS+CMS)



bbbb and  $\gamma\gamma b\bar{b}$   
complementary

Run 1 (8 TeV)

best limits on cross section for  $X \rightarrow HH$  in  $m_X$  range  
380-600 GeV (921-93 fb) 700-970 GeV (136-23 fb)

$HH \rightarrow bb\gamma\gamma$

(Snowmass studies)

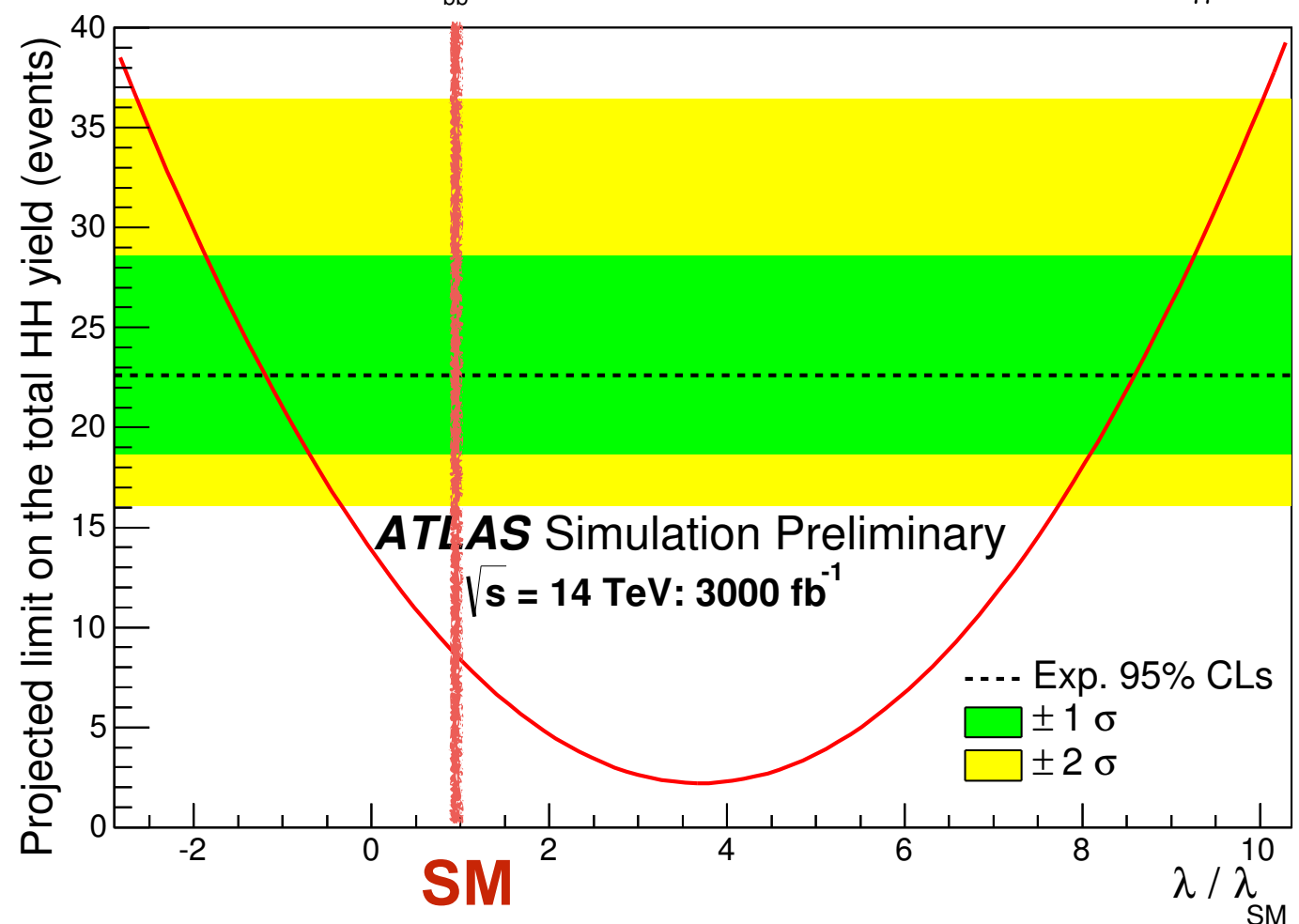
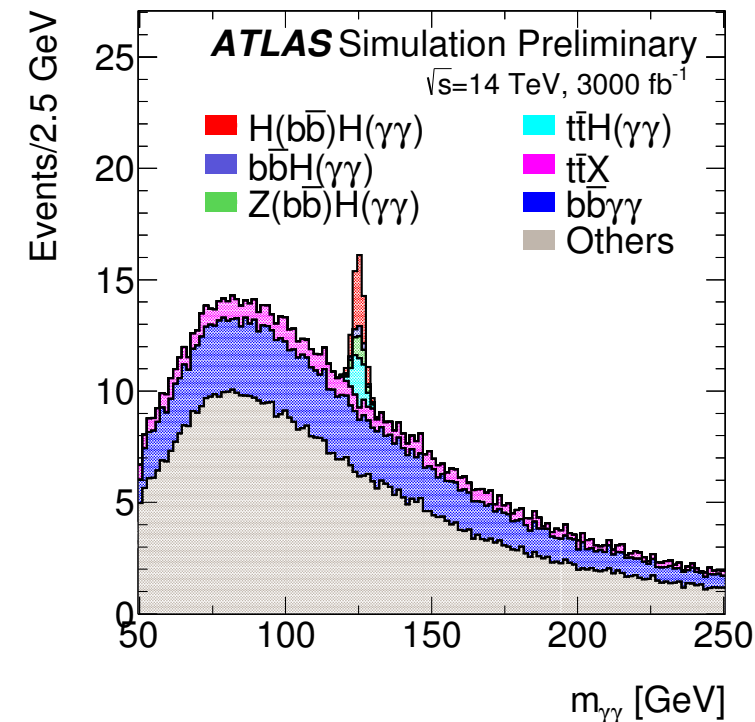
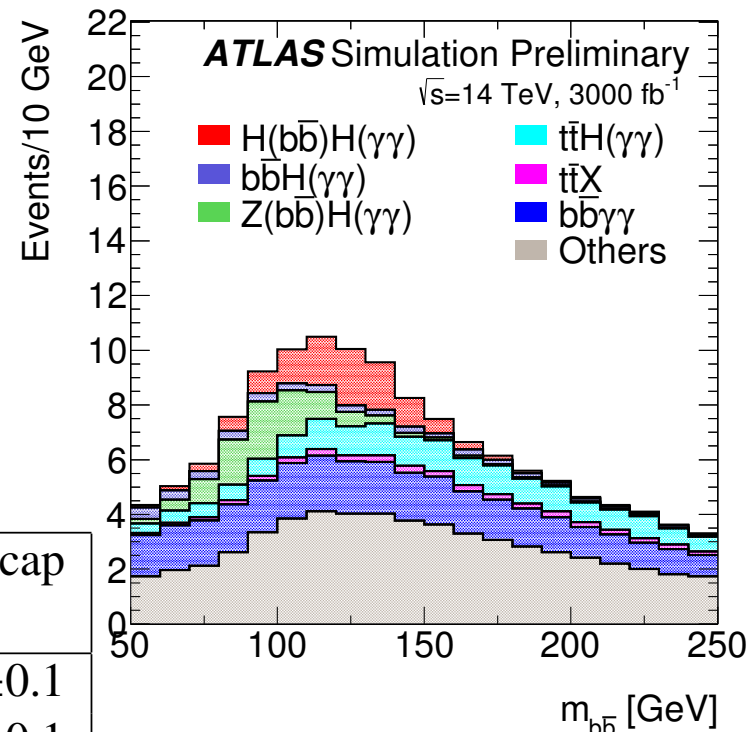
|   | HL-LHC | HE-LHC | VLHC |
|---|--------|--------|------|
| $\sqrt{s}$ (TeV)  | 14     | 33     | 100  |
| $\int \mathcal{L} dt$ (fb <sup>-1</sup> )                                   | 3000   | 3000   | 3000 |
| $\sigma \cdot \text{BR}(pp \rightarrow HH \rightarrow bb\gamma\gamma)$ (fb) | 0.089  | 0.545  | 3.73 |
| $S/\sqrt{B}$  | 2.3    | 6.2    | 15.0 |
| $\lambda$ (stat)  | 50%    | 20%    | 8%   |

# ATLAS at HL-LHC : $HH \rightarrow b\bar{b}\gamma\gamma$

ATL-PHYS-PUB-2014-019

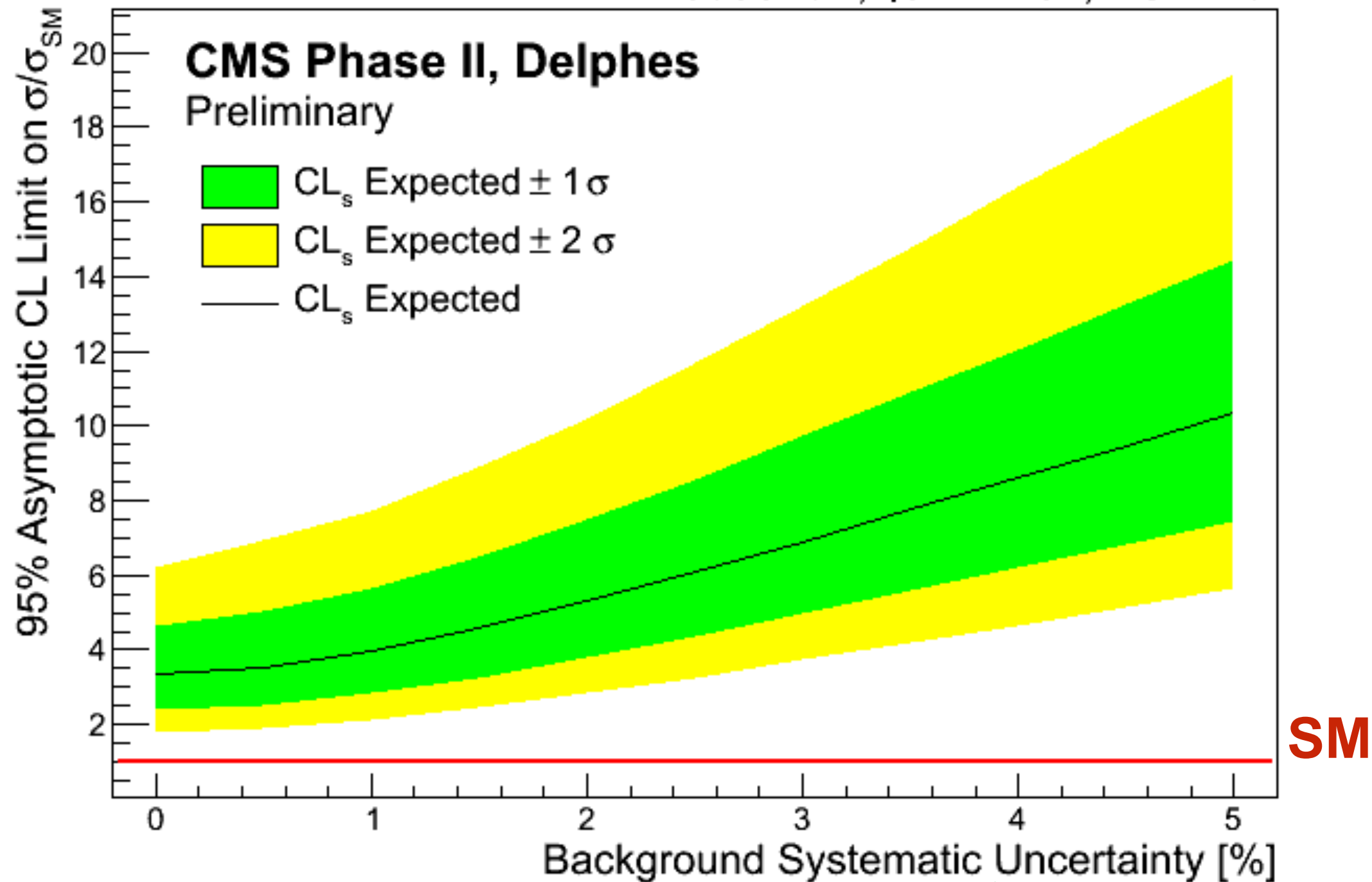
combining “barrel” and  
“endcap” categories  
significance reaches  $\sim 1.3\sigma$

| Expected yields (3000 fb <sup>-1</sup> )<br>Samples     | Total          | Barrel         | End-cap        |
|---|----------------|----------------|----------------|
| $H(b\bar{b})H(\gamma\gamma)(\lambda/\lambda_{SM} = 1)$  | $8.4 \pm 0.1$  | $6.7 \pm 0.1$  | $1.8 \pm 0.1$  |
| $H(b\bar{b})H(\gamma\gamma)(\lambda/\lambda_{SM} = 0)$  | $13.7 \pm 0.2$ | $10.7 \pm 0.2$ | $3.1 \pm 0.1$  |
| $H(b\bar{b})H(\gamma\gamma)(\lambda/\lambda_{SM} = 2)$  | $4.6 \pm 0.1$  | $3.7 \pm 0.1$  | $0.9 \pm 0.1$  |
| $H(b\bar{b})H(\gamma\gamma)(\lambda/\lambda_{SM} = 10)$ | $36.2 \pm 0.8$ | $27.9 \pm 0.7$ | $8.2 \pm 0.4$  |
| $b\bar{b}\gamma\gamma$                                  | $9.7 \pm 1.5$  | $5.2 \pm 1.1$  | $4.5 \pm 1.0$  |
| $c\bar{c}\gamma\gamma$                                  | $7.0 \pm 1.2$  | $4.1 \pm 0.9$  | $2.9 \pm 0.8$  |
| $b\bar{b}\gamma j$                                      | $8.4 \pm 0.4$  | $4.3 \pm 0.2$  | $4.1 \pm 0.2$  |
| $b\bar{b}jj$  | $1.3 \pm 0.2$  | $0.9 \pm 0.1$  | $0.4 \pm 0.1$  |
| $jj\gamma\gamma$  | $7.4 \pm 1.8$  | $5.2 \pm 1.5$  | $2.2 \pm 1.0$  |
| $t\bar{t}(\geq 1 \text{ lepton})$                       | $0.2 \pm 0.1$  | $0.1 \pm 0.1$  | $0.1 \pm 0.1$  |
| $t\bar{t}\gamma$  | $3.2 \pm 2.2$  | $1.6 \pm 1.6$  | $1.6 \pm 1.6$  |
| $t\bar{t}H(\gamma\gamma)$                               | $6.1 \pm 0.5$  | $4.9 \pm 0.4$  | $1.2 \pm 0.2$  |
| $Z(b\bar{b})H(\gamma\gamma)$                            | $2.7 \pm 0.1$  | $1.9 \pm 0.1$  | $0.8 \pm 0.1$  |
| $b\bar{b}H(\gamma\gamma)$                               | $1.2 \pm 0.1$  | $1.0 \pm 0.1$  | $0.3 \pm 0.1$  |
| Total Background  | $47.1 \pm 3.5$ | $29.1 \pm 2.7$ | $18.0 \pm 2.3$ |
| $S / \sqrt{B}(\lambda/\lambda_{SM} = 1)$                | 1.2            | 1.2            | 0.4            |



# CMS at HL-LHC : $HH \rightarrow bbWW$

3000 fb<sup>-1</sup>,  $\sqrt{s}=14$  TeV, PU=140



*Data driven technique should constrain this to percent level*

in conclusion...

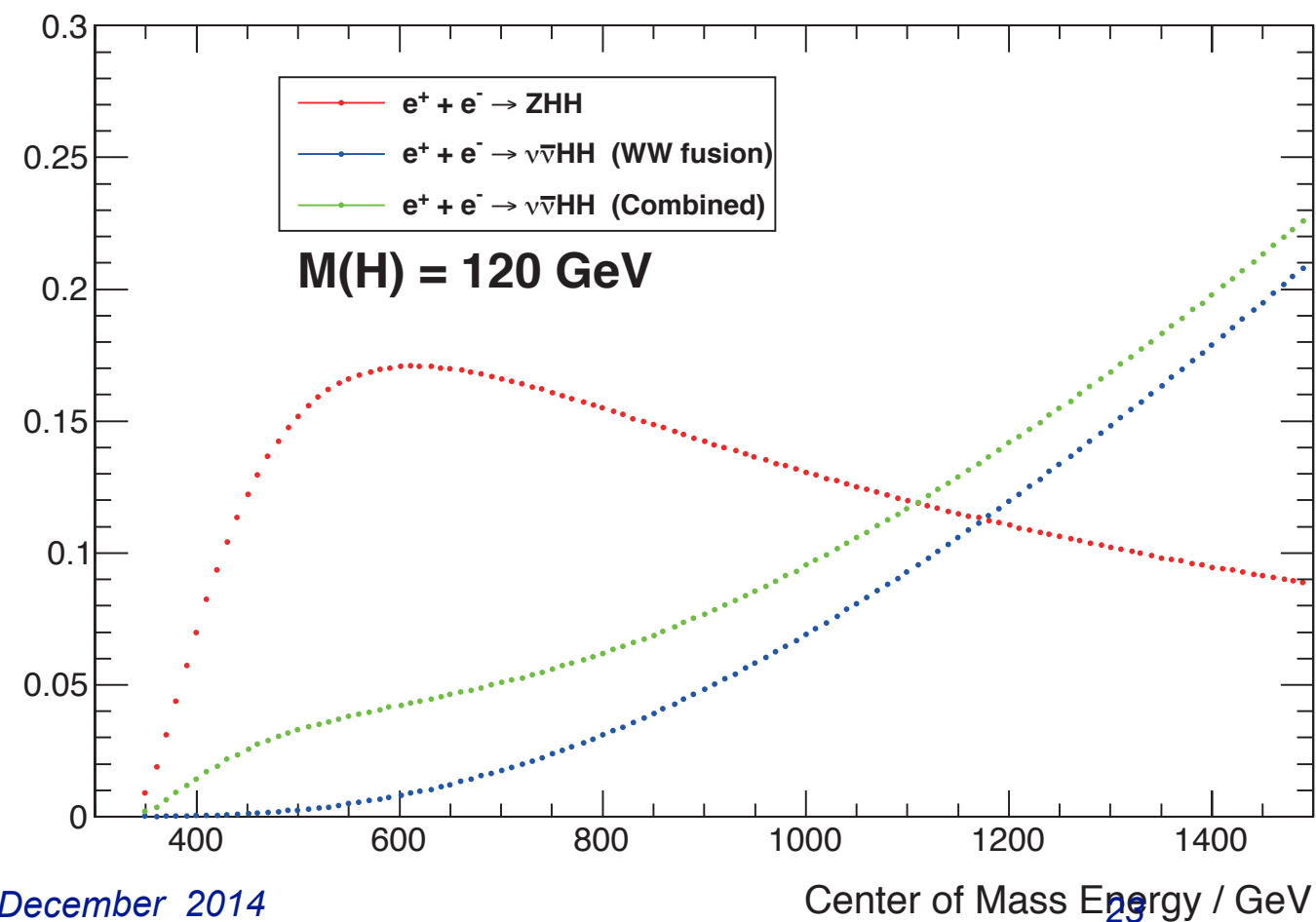
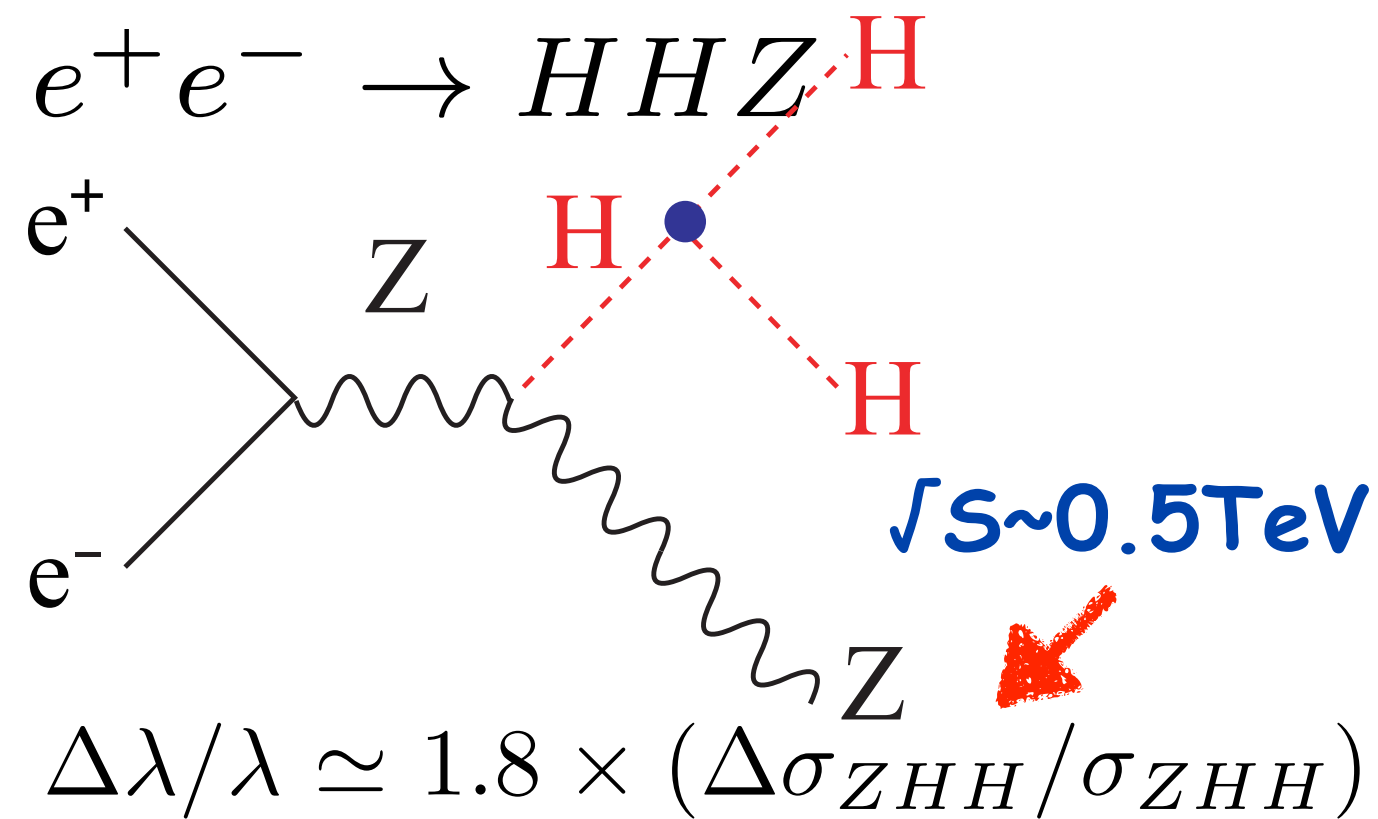
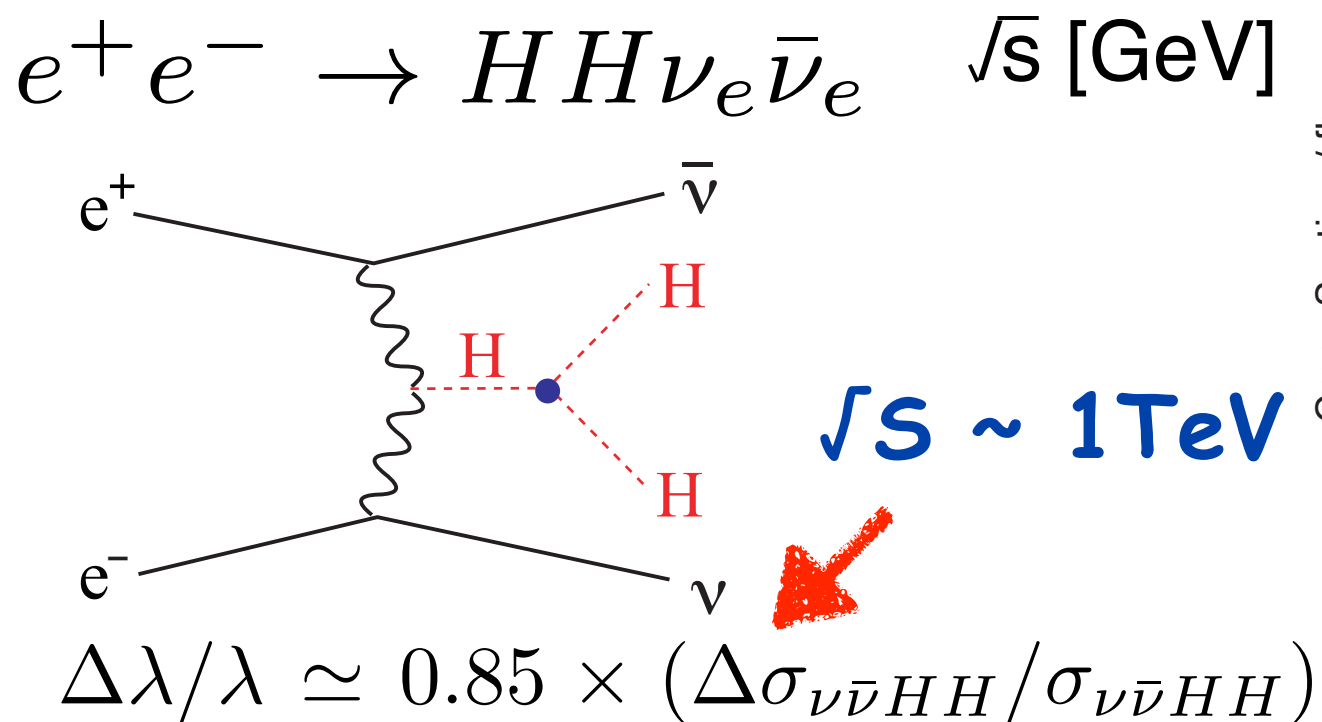
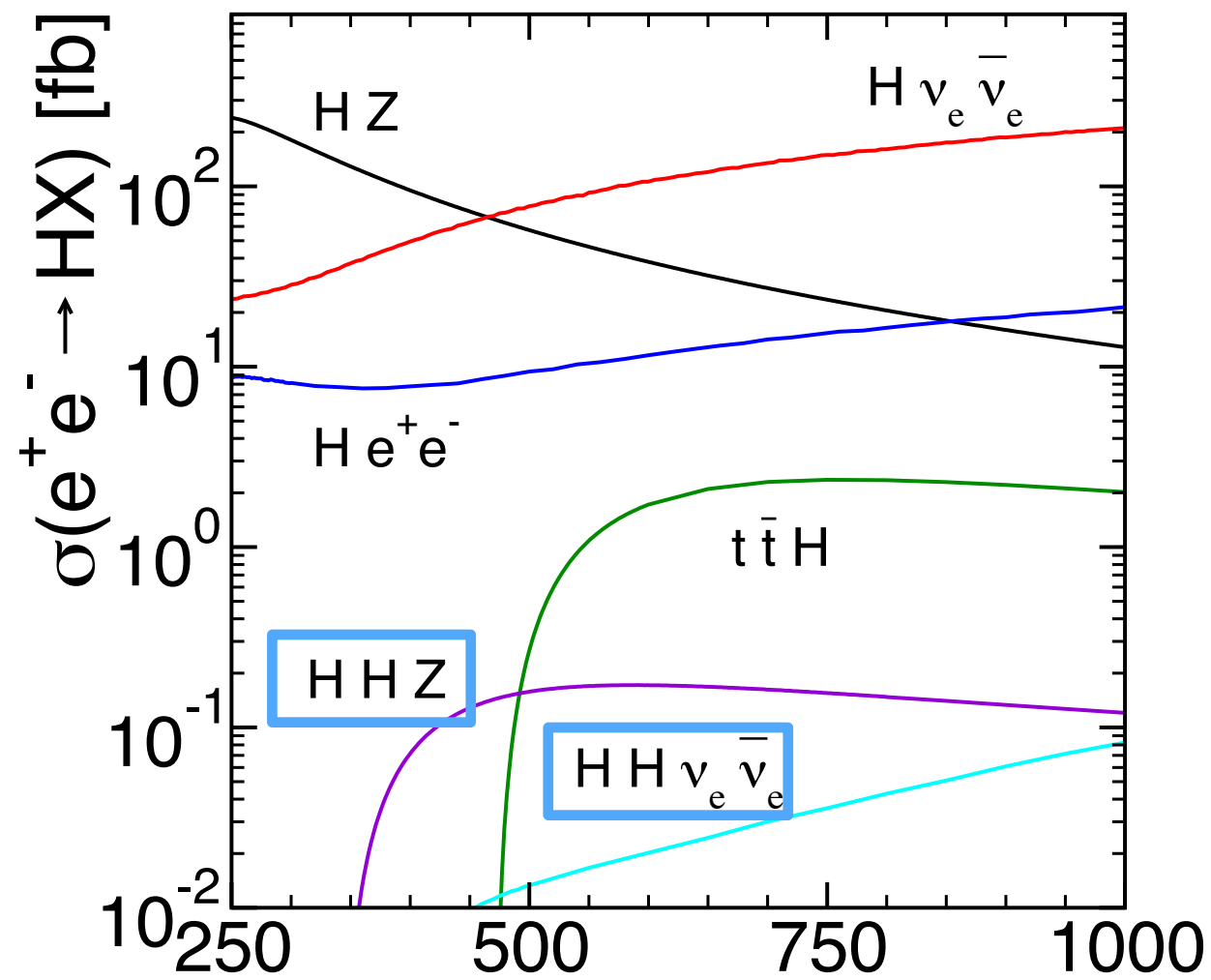
a lot of work still needed to assess  
the actual **HL-LHC** sensitivity  
to  **$\lambda H^3$**  coupling !

will likely benefit a lot from  
new exp strategies developed in Run 2  
and knowledge of actual HL detector upgrades

( $3\sigma$  significance (SM) / 3ab-1 doable ?)



# HH production in $e^+e^-$ collisions



# $e^+e^-$ colliders

## ILC TDR + Snowmass projections

|                                     | ILC500      | ILC500-up        | ILC1000         | ILC1000-up            | CLIC1400         | CLIC3000         |
|-------------------------------------|-------------|------------------|-----------------|-----------------------|------------------|------------------|
| $\sqrt{s}$ (GeV)                    | 500         | 500              | 500/1000        | 500/1000              | 1400             | 3000             |
| $\int \mathcal{L} dt$ (fb $^{-1}$ ) | 500         | 1600 $^\ddagger$ | 500+1000        | 1600+2500 $^\ddagger$ | 1500             | +2000            |
| $P(e^-, e^+)$                       | (-0.8, 0.3) | (-0.8, 0.3)      | (-0.8, 0.3/0.2) | (-0.8, 0.3/0.2)       | (0, 0)/(-0.8, 0) | (0, 0)/(-0.8, 0) |
| $\sigma(ZHH)$                       | 42.7%       |                  | 42.7%           | 23.7%                 | —                | —                |
| $\sigma(\nu\bar{\nu}HH)$            | —           | —                | 26.3%           | 16.7%                 |                  |                  |
| $\lambda$                           | 83%         | 46%              | 21%             | 13%                   | 28/21%           | 16/10%           |

based on  $bbbb$  and  $WWbb$  simulation at ILC  
and  $bbbb$  at CLIC  
(to be improved - ongoing simulations)

needs full luminosity program !

# Outlook

- Higgs self-coupling measurement crucial to characterize Higgs
- tiny rates for HH prod. → very hard EXP (and TH) problem !
- “training” in Run 1 for searches of BSM-resonance signatures
- HL-LHC lumi needed to approach SM signal sensitivity  
(HH excellent benchmark for trigger/detector HL-LHC studies !)
- sensitivity to individual channels low → need combination of many
- simulations in different HH decay channels ongoing in ATLAS and CMS to assess the actual potential of HL-LHC
- e+e- excellent potential, needs large cm energies ( $\geq 500$  GeV) and high luminosities
- mandatory to extend studies to FCC-hh ...