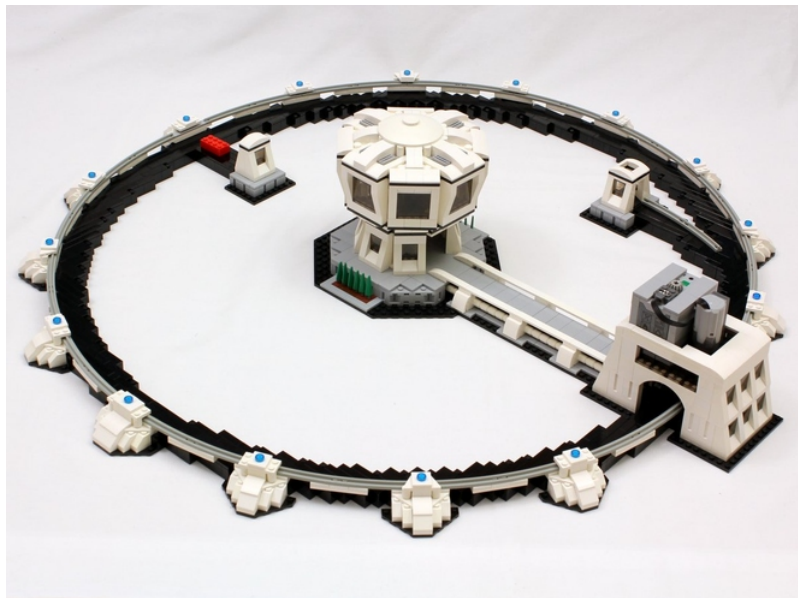


Sterile Neutrinos at Future Lepton Colliders

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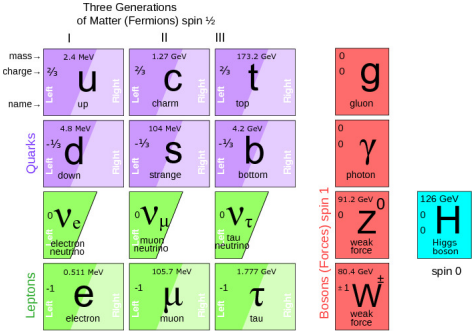
9th FCC-ee Workshop,
Pisa, February the 5th, 2015

LEGO Particle Accelerator



Motivation for Sterile Neutrinos

- ▶ Neutrino oscillations require *at least* two massive light/active SM neutrinos.
- ▶ This demands an extension of the SM.
- ▶ We consider the addition of right-handed fermion singlets – "sterile neutrinos" (N_i).
- ▶ Interesting scenario: Symmetry protected seesaw.



Courtesy Marco Drewes

Sterile Neutrinos

Incomplete author list:

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... and others.

Appologies to those who are not on the list!

How to Test Sterile Neutrinos

- ▶ Sterile Neutrino Mass (M) $>$ Electroweak scale (Λ_{EW}):
 - ▶ Indirect effect on precision observables.
 - ⇒ Presented at the 8th FCC-ee workshop in Paris.
- ▶ $M \sim \Lambda_{EW}$:
 - ▶ Indirect effect on low energy precision observables and modified effect on EWPO.
 - ▶ N decays at the Z pole.
 - ▶ N decay to leptonic final states at and beyond the WW threshold.
 - ▶ Higgs boson branching ratios.
- ▶ This talk:
 - (i) Two Sterile neutrinos with masses $\sim \Lambda_{EW}/\text{TeV}$ scale.
 - (ii) Present bounds from precision data and direct searches.
 - (iii) Sensitivities of the FCC-ee (ILC and CEPC in the Backup).

Low Scale Seesaw Scenario

with two sterile neutrinos N_i and protective symmetry

$$\mathcal{L}_N = -\frac{1}{2}\overline{N_R^I} M_{IJ}^N (N_R^J)^c - y_\alpha \overline{N_R^I} \tilde{\phi}^\dagger L^\alpha + \text{H.c.}$$

- ▶ The leptonic mixing matrix to leading order in the active-sterile mixing parameters:

$$\mathcal{U} = \begin{pmatrix} \mathcal{N}_{1e} & \mathcal{N}_{1\mu} & \mathcal{N}_{1\tau} & -\frac{i}{\sqrt{2}}\theta_e & \frac{1}{\sqrt{2}}\theta_e \\ \mathcal{N}_{2e} & \mathcal{N}_{2\mu} & \mathcal{N}_{2\tau} & -\frac{i}{\sqrt{2}}\theta_\mu & \frac{1}{\sqrt{2}}\theta_\mu \\ \mathcal{N}_{3e} & \mathcal{N}_{3\mu} & \mathcal{N}_{3\tau} & -\frac{i}{\sqrt{2}}\theta_\tau & \frac{1}{\sqrt{2}}\theta_\tau \\ 0 & 0 & 0 & \frac{i}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ -\theta_e^* & -\theta_\mu^* & -\theta_\tau^* & -\frac{i}{\sqrt{2}}\left(1 - \frac{\theta^2}{2}\right) & \frac{1}{\sqrt{2}}\left(1 - \frac{\theta^2}{2}\right) \end{pmatrix}.$$

- ▶ Active-sterile neutrino mixing parameters:

$$\theta_\alpha = \frac{y_\alpha}{\sqrt{2}} \frac{v_{\text{EW}}}{M}, \quad \alpha = e, \mu, \tau$$

Interactions between Heavy Neutrinos and the SM

- ▶ **Charged current (CC):**

$$j_{\mu}^{\pm} = \frac{g}{2} \theta_{\alpha} \bar{\ell}_{\alpha} \gamma_{\mu} (-iN_1 + N_2)$$

- ▶ **Neutral current (NC):**

$$j_{\mu}^0 = \frac{g}{2 c_W} \left[\theta^2 \bar{N}_2 \gamma_{\mu} N_2 + (\bar{\nu}_i \gamma_{\mu} \xi_{\alpha 1} N_1 + \bar{\nu}_i \gamma_{\mu} \xi_{\alpha 2} N_2 + \text{H.c.}) \right]$$

- ▶ Higgs boson **Yukawa** interaction:

$$\mathcal{L}_{\text{Yukawa}} = \sum_{i=1}^3 \xi_{\alpha 2} \frac{\sqrt{2} M}{v_{\text{EW}}} \nu_i \phi^0 (\bar{N}_1 + \bar{N}_2)$$

- ▶ With the mixing parameters:

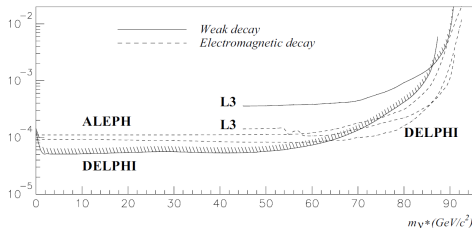
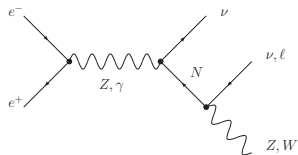
$$\xi_{\alpha 1} = \sum_{\beta=e,\mu,\tau} (-i) \mathcal{N}_{\alpha\beta}^* \frac{\theta_{\beta}}{\sqrt{2}}, \quad \text{and} \quad \xi_{\alpha 2} = \sum_{\beta=e,\mu,\tau} \mathcal{N}_{i\beta}^* \frac{\theta_{\beta}}{\sqrt{2}}$$

Decays involving Heavy Neutrinos

$$\begin{aligned}\Gamma_{W \rightarrow N \ell} &= \frac{|\theta_\alpha|^2}{2} \frac{G_F m_W^3}{6\sqrt{2}\pi} \Pi_{(1+1)}^W & \Gamma_{N \rightarrow W \ell} &= \frac{|\theta_\alpha|^2}{2} \frac{G_F M^3}{4\sqrt{2}\pi} \Pi_{(1+1)}^W \\ \Gamma_{Z \rightarrow \nu N} &= |\xi_{ij}|^2 \frac{G_F m_Z^3}{6\sqrt{2}\pi} \Pi_{(1+1)}^Z & \Gamma_{N \rightarrow Z \nu} &= |\xi_{ij}|^2 \frac{G_F M^3}{4\sqrt{2}\pi} \Pi_{(1+1)}^Z \\ \Gamma_{Z \rightarrow N N} &= |\xi_{55}|^2 \frac{G_F m_Z^3}{6\sqrt{2}\pi} \Pi_{(2)}^Z & \Gamma_{N \rightarrow h \nu} &= |\xi_{ij}|^2 \frac{M}{16\pi} \left(1 - \frac{m_h^2}{M^2}\right)^2 \\ \Gamma_{h \rightarrow \nu N} &= \frac{m_h \theta^2 M^2}{8\pi v_{EW}^2} \left(1 - \frac{M^2}{m_h^2}\right)^2\end{aligned}$$

Π^W, Π^Z : Phase space factors.

Sterile Neutrino searches @ the Z pole I



DELPHI collaboration, Abreu et al. (1997)

- ▶ Search for $Z \rightarrow \nu N$ in Z-pole data at LEP.
- ▶ Null results \Rightarrow Upper limit on active-sterile neutrino mixing.

Sterile Neutrino searches @ the Z pole II

- ▶ Exclusion contour at 95% confidence level:

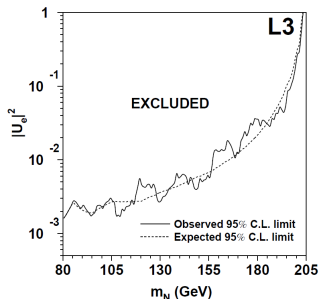
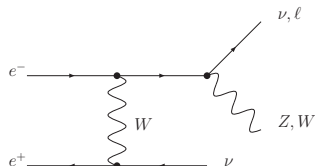
$$\theta^2 = \sum_{\alpha=e,\mu,\tau} |\theta_\alpha|^2 \leq \frac{1.1 \times 10^{-5}}{\Pi_{(1+1)}^Z}$$

- ▶ Search for displaced vertices at the FCC-ee (TLEP) by [Blondel, Graverini, Serra, Shaposhnikov \(2014\)](#).
- ▶ In general: the sensitivity scales with the luminosity.

⇒ Limit on Yukawa couplings:

$$\theta_\alpha = \frac{y_\alpha}{\sqrt{2}} \frac{v_{EW}}{M}, \quad \Rightarrow \sum_{\alpha=e,\mu,\tau} |y_\alpha|^2 \leq \frac{M}{v_{EW}} \frac{1.5 \times 10^{-5}}{\Pi_{(1+1)}^Z}$$

Searches in 4ℓ Final States for $\sqrt{s} \geq 2 m_W$



L3 collaboration, Achard et al. (2001)

- ▶ N decay also contributes to 4ℓ final states.
- ▶ We use the experimental uncertainty from the Aleph measurement of the WW production cross section.

$$\frac{n_{WW}^{Aleph}}{n_{WW}^{SM}} = 0.995 \pm 0.011_{stat} \pm 0.007_{syst}$$

OPAL collaboration, Abbiendi et al. (2007)

Present Indirect Constraints from Precision Data

The following sets of precision observables are used:

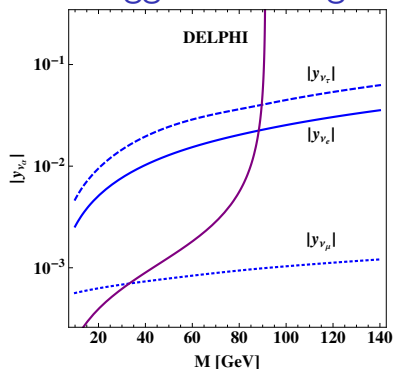
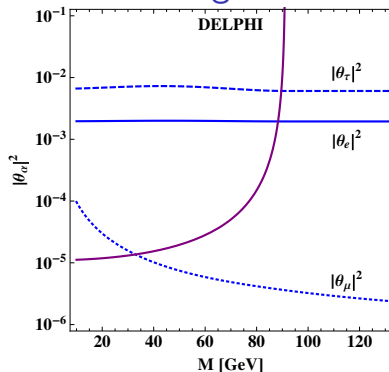
- ▶ Electroweak Precision Observables (mainly LEP).
- ▶ Non-universality observables at low Energy (decays of μ, τ, π, K).
- ▶ Rare charged lepton flavour violating decays.
- ▶ CKM unitarity tests.
- ▶ Low energy measurements of the weak mixing angle.

Note that the EWPO predictions change wrt. MUV:

$$R_{inv} = [R_{inv}]_{SM} \left(1 - \frac{2}{3} \sum_{\alpha} |\theta_{\alpha}|^2 \left(1 - c_R \Pi_{(1+1)}^Z\right) - 0.09(|\theta_e|^2 + |\theta_{\mu}|^2)\right)$$

$c_R \neq -1$ for sterile neutrinos decaying within the detector.

Bounds on Mixing Parameters and Higgs Branching Ratios

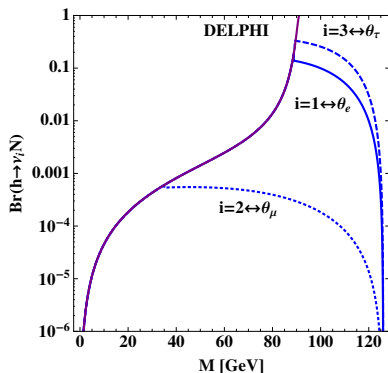


Antusch, Fischer (2015) *to appear*

- ▶ Reminder: Delphi constraints 95% confidence level.
- ▶ Large branchings of Higgs to sterile neutrinos are possible.
- ▶ Investigated also by [Dev, Franceschini, Mohapatra \(2012\)](#) and [Cely, Ibarra, Molinaro, Petcov \(2013\)](#).

Higgs Boson Branching Ratio into Neutrinos

- ▶ From “indirect” tests and Delphi.
 - ▶ $\mathcal{O}(1)$ branching ratio possible.
- ⇒ Possible effect on Higgs decay rates into Standard Model particles.



Constraints from Higgs Branching Ratios

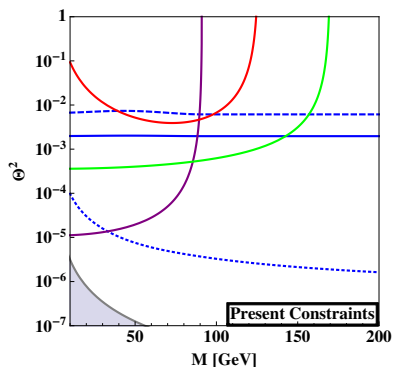
- ▶ Focus on the currently best measured branching ratios $h \rightarrow ZZ, WW, \gamma\gamma$.
- ▶ Include N decays as misidentified vector boson events.
- ▶ Branching ratios become modified by heavy neutrinos:

$$Br_{h \rightarrow XX} = r Br_{h \rightarrow XX, \text{SM}} + c_X Br_{h \rightarrow \nu N}$$

$$r = \frac{\Gamma_{h, \text{SM}}}{\Gamma_{h, \text{SM}} + \Gamma_{h \rightarrow \nu N}}, \quad c_X = \begin{cases} \frac{1}{2}, & X = Z, W \\ 0, & X = \gamma, f \end{cases}$$

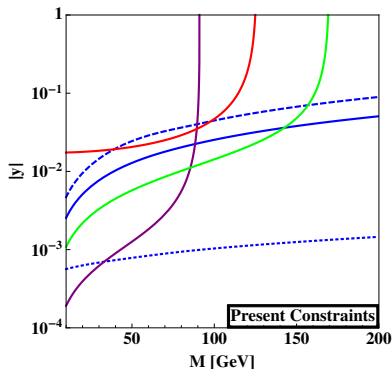
- ▶ CMS+Atlas: $Br_{h \rightarrow \gamma\gamma} = 1.15(27)$

Combination of Present Bounds



Direct searches

- Delphi (N decays) @ 2σ : $|y| = \sqrt{\sum_{\alpha} |y_{\alpha}|^2}$, $\Theta^2 = \sum_{\alpha} |\theta_{\alpha}|^2$
- LHC (Higgs decays*) @ 1σ : $|y| = \sqrt{\sum_{\alpha} |y_{\alpha}|^2}$, $\Theta^2 = \sum_{\alpha} |\theta_{\alpha}|^2$
- Opal ($e^+e^- \rightarrow 4$ leptons) @ 1σ : $|y| = |y_e|$, $\Theta^2 = |\theta_e|^2$



Other (global fit)

- $|y| = |y_e|$, $\Theta^2 = |\theta_e|^2$
- $|y| = |y_{\mu}|$, $\Theta^2 = |\theta_{\mu}|^2$
- $|y| = |y_{\tau}|$, $\Theta^2 = |\theta_{\tau}|^2$

Antusch, Fischer (2015) to appear

* Currently dominated by $h \rightarrow \gamma\gamma$.

Improvements in Precision at Future Lepton Colliders - I

- ▶ Systematical uncertainty for the EWPO from 1308.6176.
- ▶ Summary table for all the future colliders in the backup.

Improvements in Precision at Future Lepton Colliders - II

- ▶ Higgs measurements (per year of data taking for one detector):

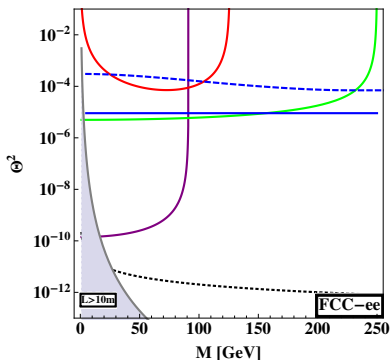
Branching ratio	ILC [%]	CEPC [%]	FCC-ee [%]
$\delta Br_{h \rightarrow WW}$	6.4	1.3	0.9
$\delta Br_{h \rightarrow ZZ}$	19	5.1	3.1
$\delta Br_{h \rightarrow \gamma\gamma}$	35	8	3.0
Reference	1310.6708	1411.5606	1308.6176

- ▶ Analysis uses 10 years of data taking with two detectors.
- ▶ Expected W boson yield:

	Opal	ILC	CEPC	FCC-ee
# W 's prod.	10^4	10^7	10^8	2×10^8
$\delta_{\text{stat.}}$	0.011	3×10^{-4}	10^{-4}	7×10^{-4}
$\delta_{\text{syst.}}$	0.007	n.a.	n.a.	n.a.

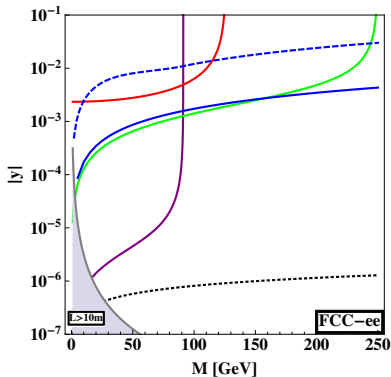
- ▶ At the moment it seems $\delta_{\text{syst.}} \sim \delta_{\text{theo.}} \sim 10^{-3}$ is realistic. (Not considered in the following.)

Prospects of Sensitivity at the FCC-ee



Direct searches

- Z pole search @ 2σ : $|y| = \sqrt{\sum_{\alpha} |y_{\alpha}|^2}$, $\Theta^2 = \sum_{\alpha} |\theta_{\alpha}|^2$
- Higgs \rightarrow WW @ 1σ : $|y| = \sqrt{\sum_{\alpha} |y_{\alpha}|^2}$, $\Theta^2 = \sum_{\alpha} |\theta_{\alpha}|^2$
- $e^+e^- \rightarrow 4$ leptons* @ 1σ : $|y| = |y_e|$, $\Theta^2 = |\theta_e|^2$



Other

- Precision constraints: $|y| = \sqrt{|y_e|^2 + |y_{\mu}|^2}$, $\Theta^2 = |\theta_e|^2 + |\theta_e|^2$
- - - Precision constraints: $|y| = |y_{\tau}|$, $\Theta^2 = |\theta_{\tau}|^2$
- Unprotected type-I seesaw

Antusch, Fischer (2015) to appear

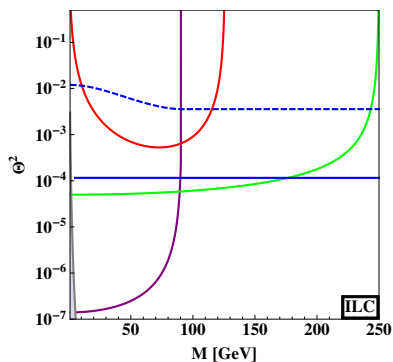
* Preliminary estimate using statistical uncertainty only.

Summary and Conclusions

- ▶ Sterile neutrinos are well motivated extensions of the SM.
- ▶ Symmetry protected scenarios allow for electroweak scale sterile neutrino masses and $\mathcal{O}(1)$ active-sterile mixings.
- ▶ LHC starts to constrain Higgs branching ratios to sterile neutrinos.
- ▶ Searches in Z , W , h decay data @ FCC-ee are very sensitive probes of sterile neutrino extensions of the SM.
- ▶ There is **a lot** to do.
- ▶ Feedback is very welcome.

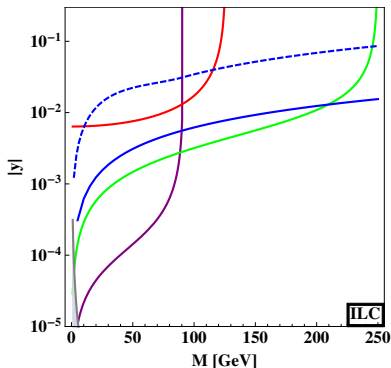
Thank you for your attention.

Backup I - ILC Summary Plot



Direct searches

- Z pole search @ 2σ : $|y| = \sqrt{\sum_{\alpha} |y_{\alpha}|^2}$, $\Theta^2 = \sum_{\alpha} |\theta_{\alpha}|^2$
- Higgs \rightarrow WW @ 1σ : $|y| = \sqrt{\sum_{\alpha} |y_{\alpha}|^2}$, $\Theta^2 = \sum_{\alpha} |\theta_{\alpha}|^2$
- $e^+e^- \rightarrow 4$ leptons* @ 1σ : $|y| = |y_e|$, $\Theta^2 = |\theta_e|^2$



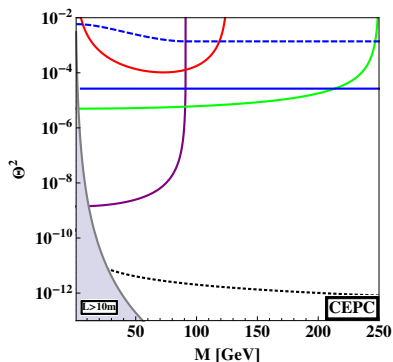
Other

- Precision constraints: $|y| = \sqrt{|y_e|^2 + |y_{\mu}|^2}$, $\Theta^2 = |\theta_e|^2 + |\theta_{\mu}|^2$
- Precision constraints: $|y| = |y_{\tau}|$, $\Theta^2 = |\theta_{\tau}|^2$
- Unprotected type-I seesaw

Antusch, Fischer (2015) to appear

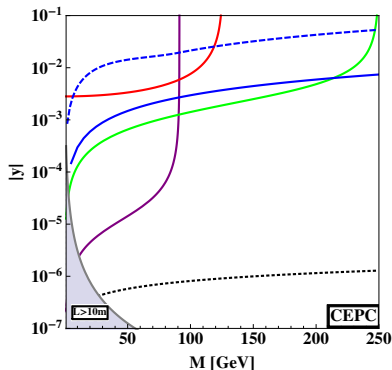
* Preliminary estimate using statistical uncertainty only.

Backup II - CEPC Summary Plot



Direct searches

- Z pole search @ 2σ : $|y| = \sqrt{\sum_{\alpha} |y_{\alpha}|^2}$, $\Theta^2 = \sum_{\alpha} |\theta_{\alpha}|^2$
- Higgs \rightarrow WW @ 1σ : $|y| = \sqrt{\sum_{\alpha} |y_{\alpha}|^2}$, $\Theta^2 = \sum_{\alpha} |\theta_{\alpha}|^2$
- $e^+e^- \rightarrow 4$ leptons* @ 1σ : $|y| = |y_e|$, $\Theta^2 = |\theta_e|^2$



Other

- Precision constraints: $|y| = \sqrt{|y_e|^2 + |y_{\mu}|^2}$, $\Theta^2 = |\theta_e|^2 + |\theta_{\mu}|^2$
- - - Precision constraints: $|y| = |y_{\tau}|$, $\Theta^2 = |\theta_{\tau}|^2$
- Unprotected type-I seesaw

Antusch, Fischer (2015) to appear

* Preliminary estimate using statistical uncertainty only.

Backup III - Electroweak Precision Observables

Observable	ILC	FCC-ee	CEPC	CEPC*
R_ℓ	0.004	0.001	0.01	0.003*
R_{inv}	0.01	0.002	0.012	0.006*
R_b	0.0002	0.00002	0.00017	0.00007*
M_W [MeV]	2.5	0.5	0.5	0.5
$s_{eff}^{2,\ell}$	1.3×10^{-5}	1×10^{-6}	2.3×10^{-5}	3.3×10^{-6} *
σ_h^0 [nb]	0.025	0.0025	n.a.	0.008*
Γ_ℓ [MeV]	0.042	0.0042	n.a.	0.014*
Reference	1310.6708	1308.6176	Ruan (2014) [†]	scaled*

† Private communication.

* Assumption: CEPC produces 10^{11} Z bosons, compared to the 10^{12} Z bosons @FCC-ee.

⇒ Uncertainties scaled: $\delta_{\text{CEPC}} = \delta_{\text{FCC-ee}} \times \sqrt{10}$.