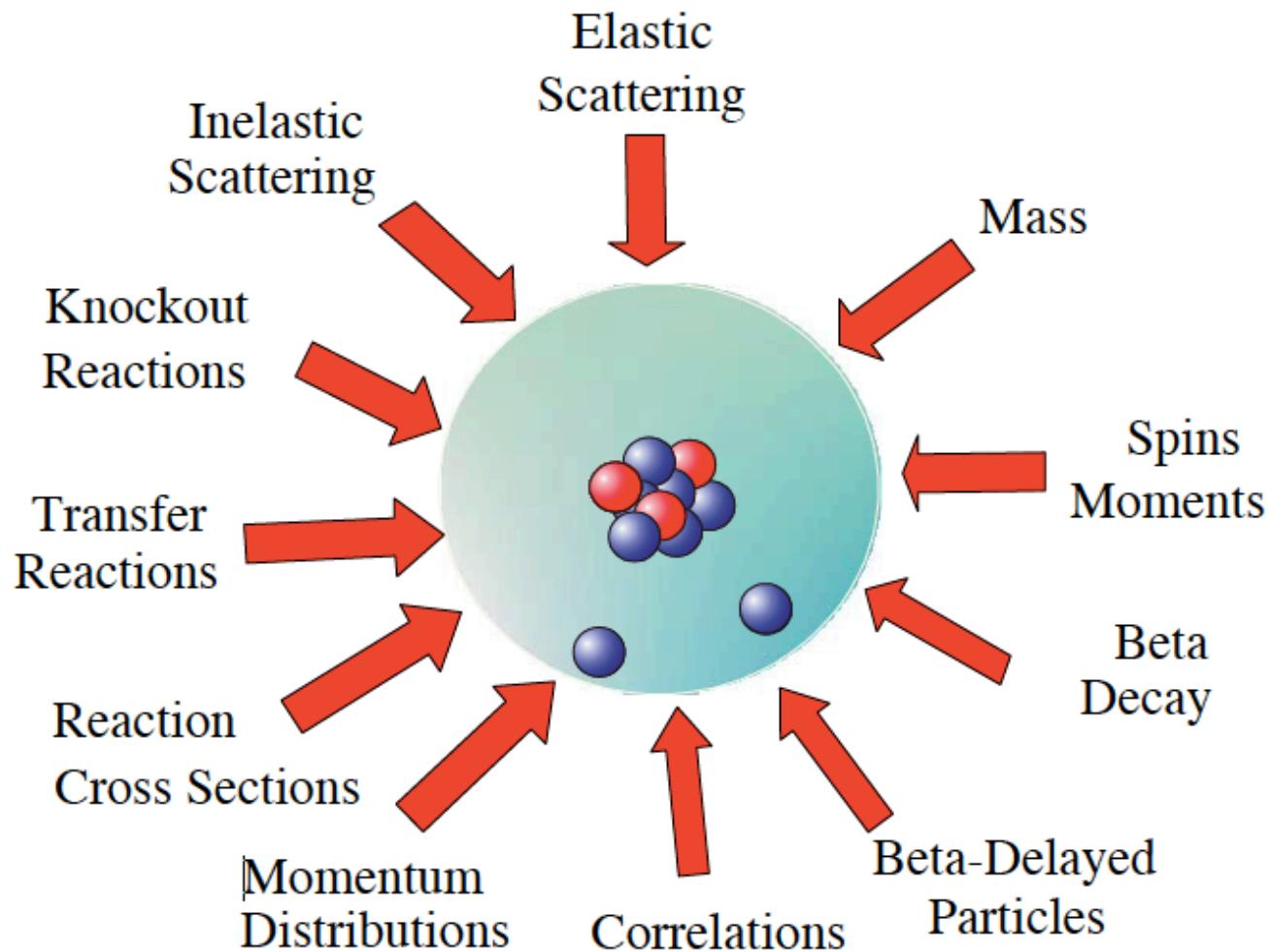


# **PROBING NUCLEAR STRUCTURE WITH DIRECT REACTIONS**

## **OBSERVABLES, METHODS AND HIGHLIGHTS WITH RARE ISOTOPES**

A. Obertelli  
*CEA Saclay, France*

**Rewriting Nuclear Physics textbooks:  
30 years of exotic nuclei studies**  
July 2015



# Nuclear reactions

***In fundamental physics, Nuclear Reactions are used for :***

- Probing **nuclear structure** (topic of this lecture)
- Production of Radioactive Ions beams
- Studying nuclear dynamics and nuclear matter equation of state

- ✓ **The quantum many-body problem can not be solved exactly**
  - ➔ true for static systems, even more true for dynamical systems
- ✓ **Strong approximations are made**
  - ➔ natural cycle (feedback) between experiment and theory

# Nuclear reactions

Impact Parameter  
(fm)

Peripheral

Surface  
 $(\approx 1.2 A^{1/3} \text{ fm})$

Central

0

Coulomb barrier

Fermi energy

1

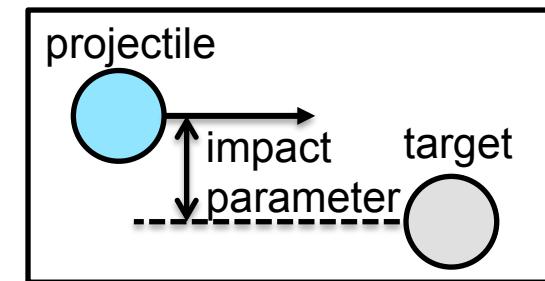
10

100

1000

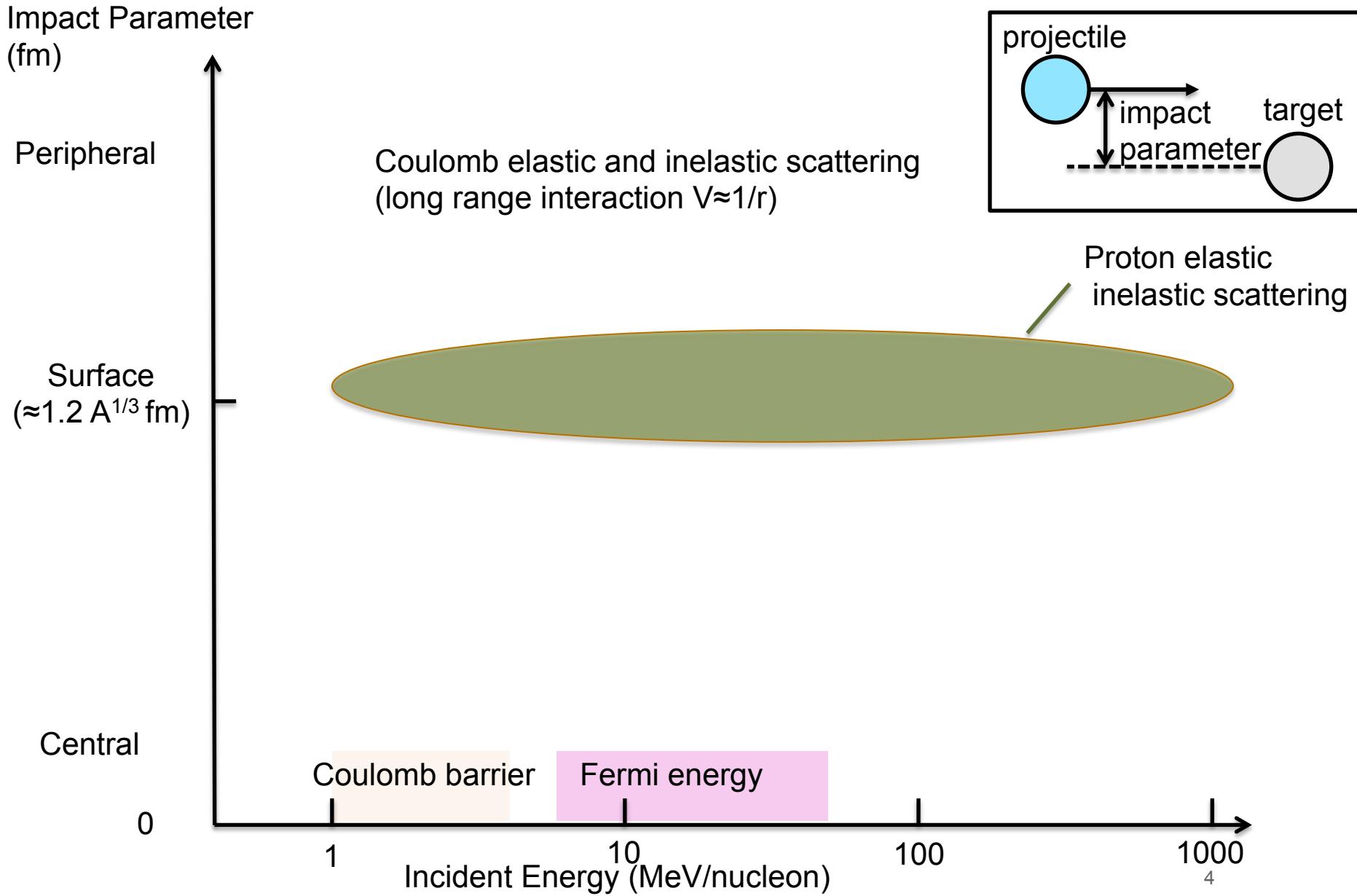
4

Incident Energy (MeV/nucleon)

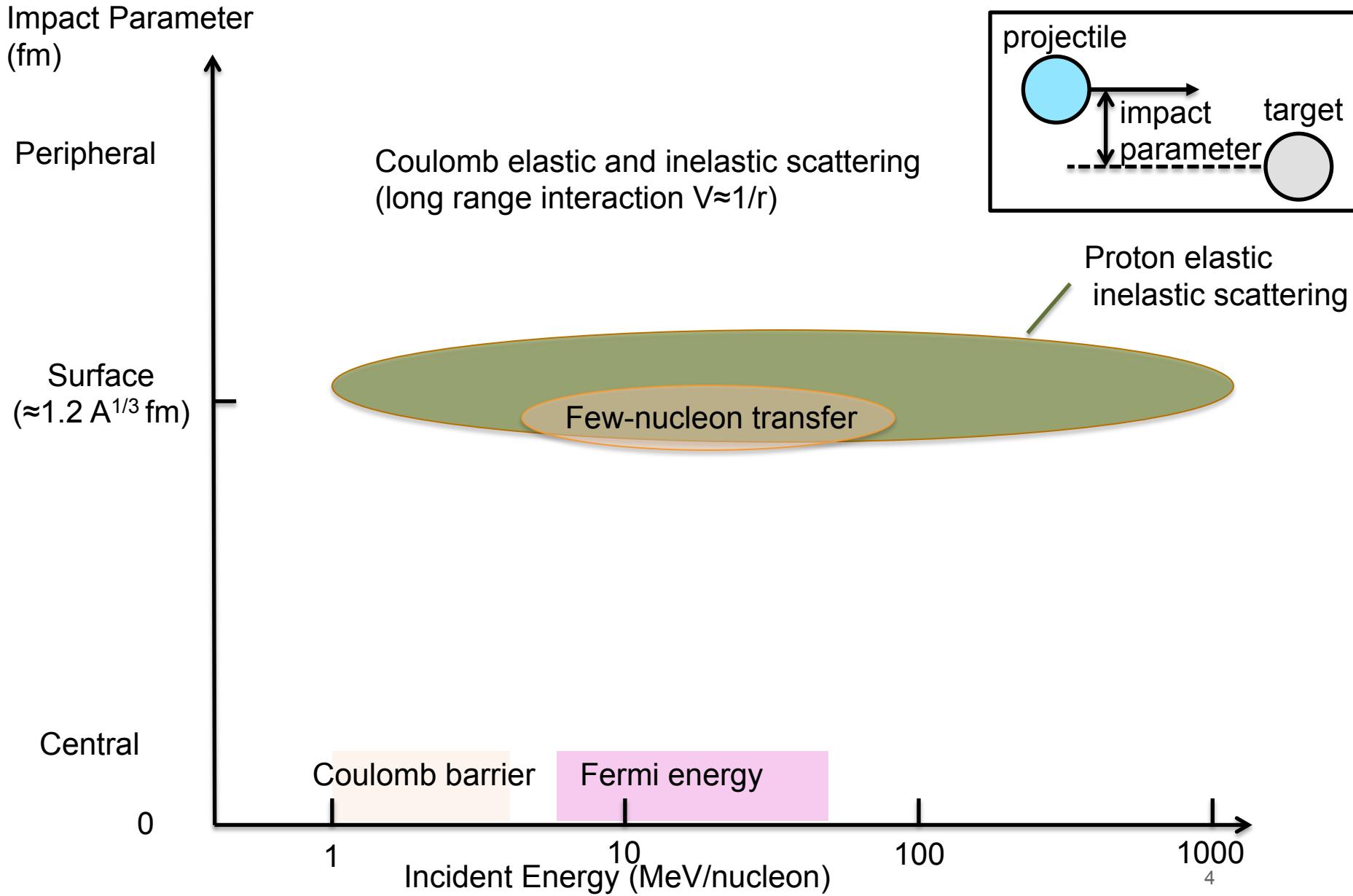


Coulomb elastic and inelastic scattering  
(long range interaction  $V \approx 1/r$ )

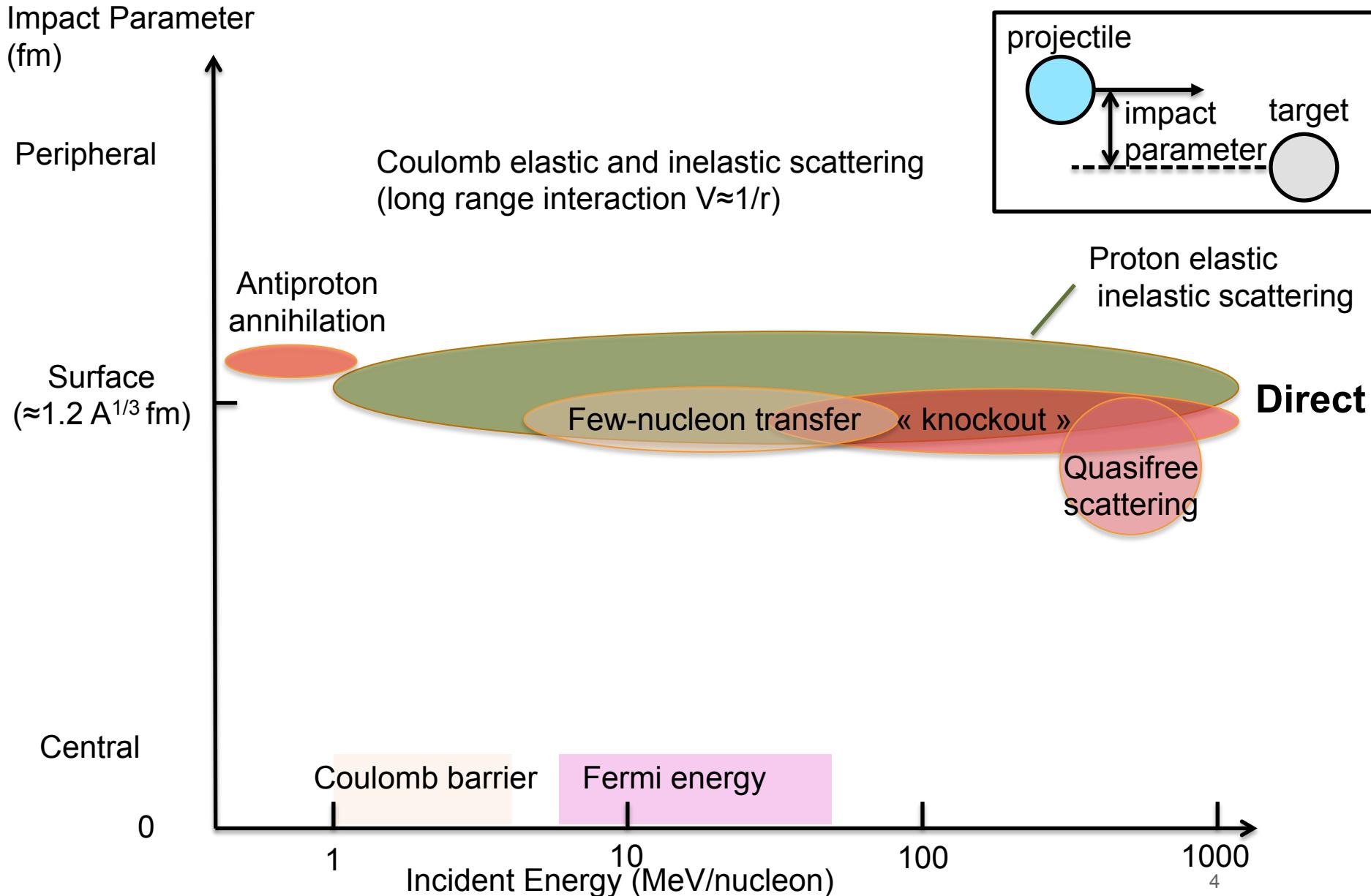
# Nuclear reactions



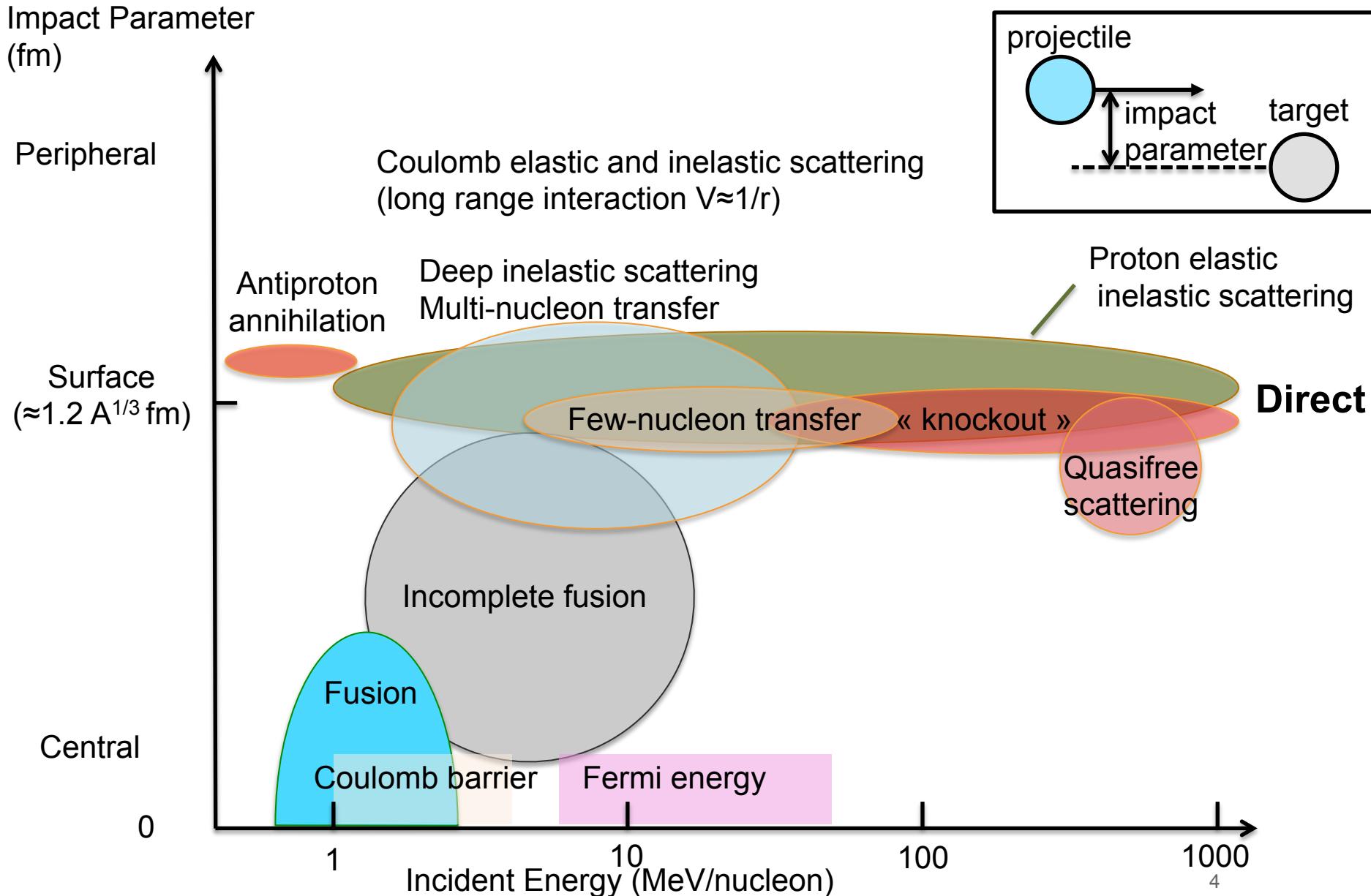
# Nuclear reactions



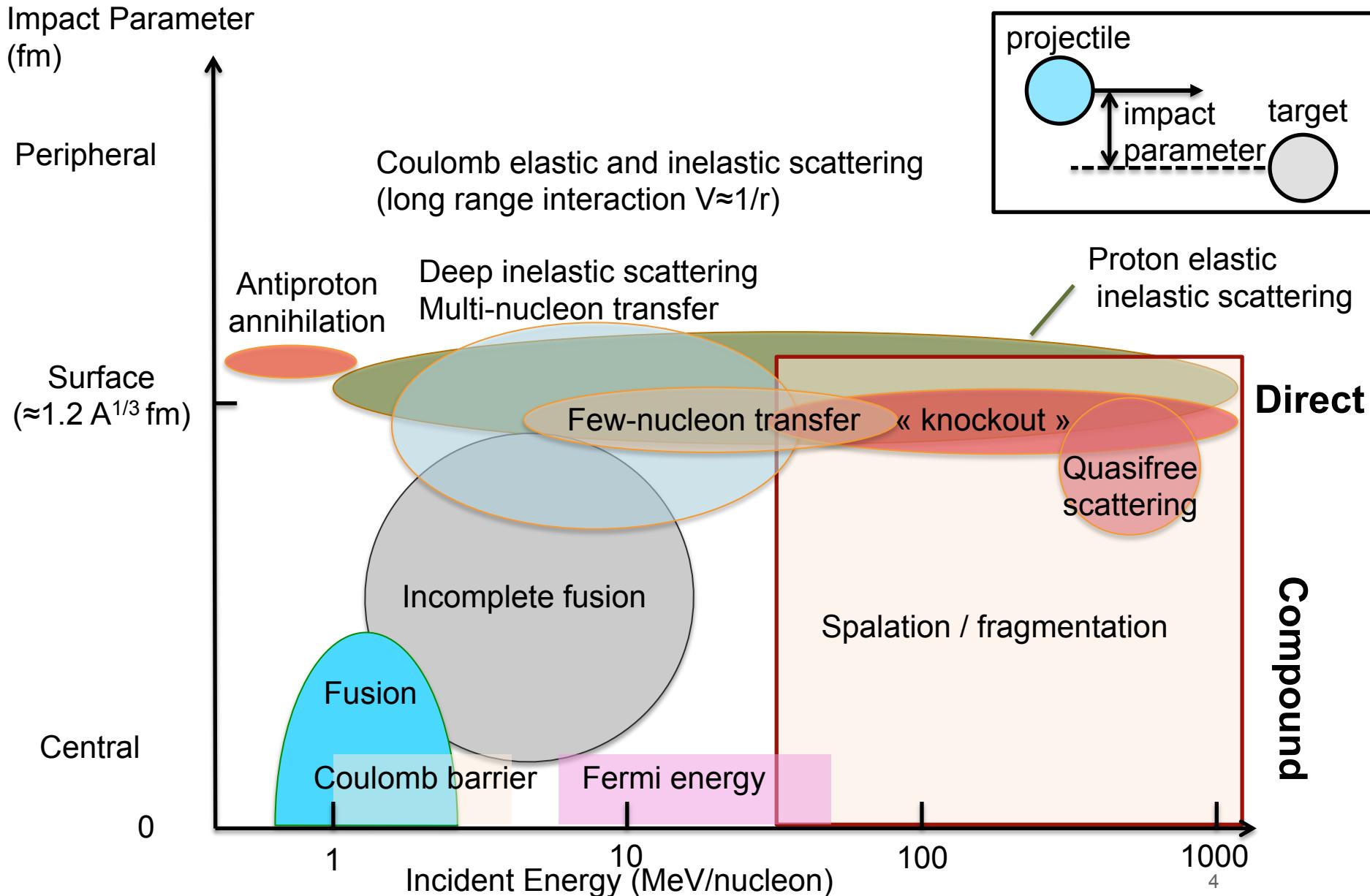
# Nuclear reactions



# Nuclear reactions

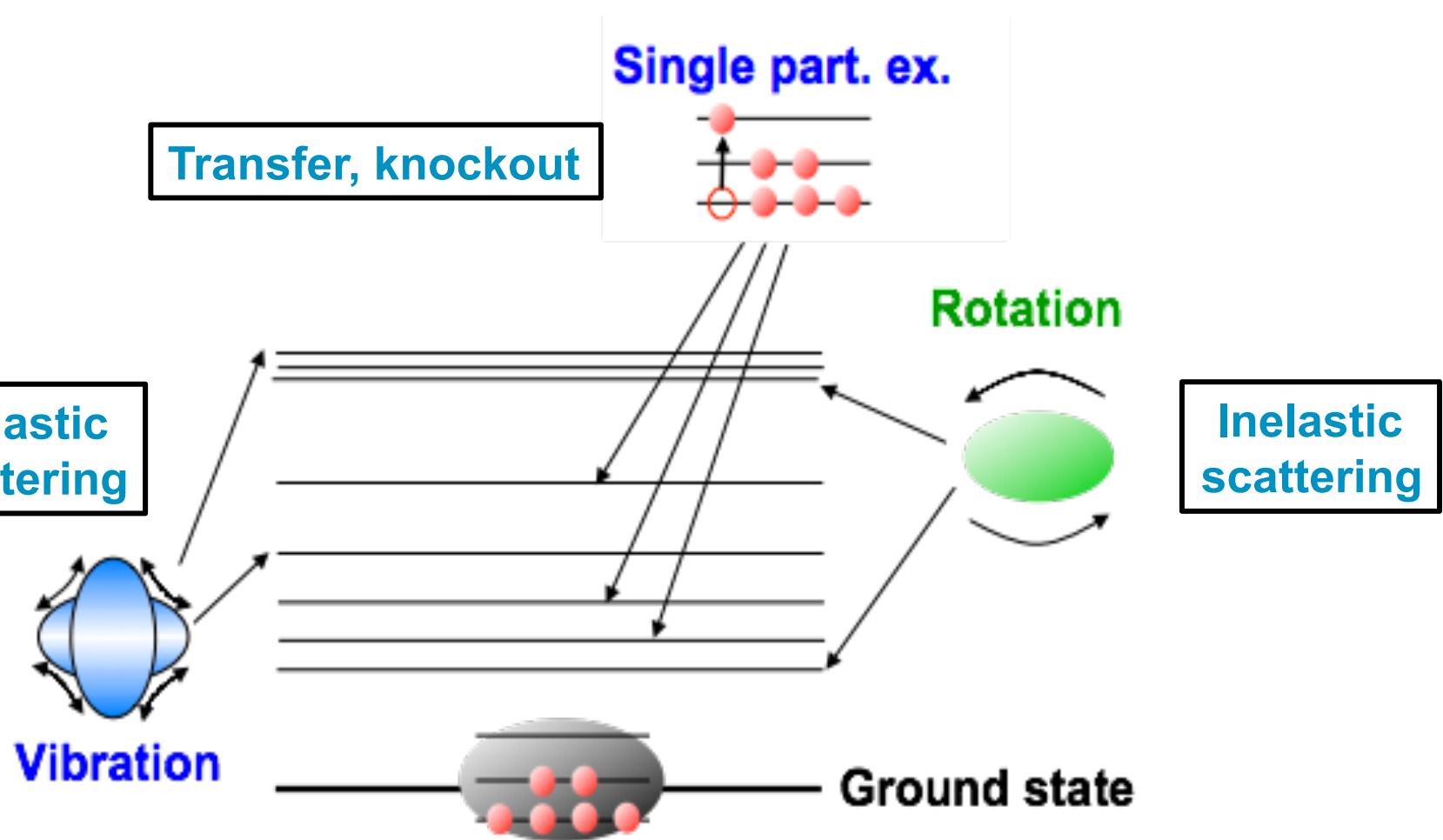


# Nuclear reactions

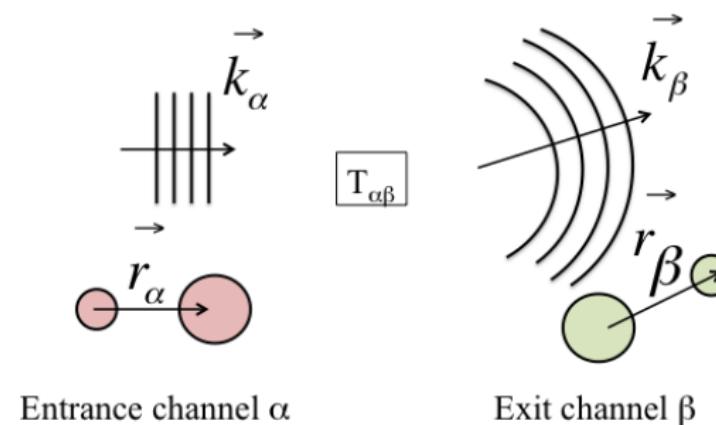


# Why do we need direct reactions?

- to go beyond ground-state properties (to **excite** nuclei)
- to measure and identify populated states (**spectroscopy**)
- to understand the nature of nuclear states (from direct reaction **cross sections**)



# Direct reaction cross sections (operator formalism)



**General form** 
$$\frac{d\sigma_{\alpha\beta}}{d\Omega} = \frac{\mu_\alpha \mu_\beta}{(2\pi\hbar^2)^2} \left(\frac{k_\beta}{k_\alpha}\right) |T_{\beta\alpha}(\vec{k}_\beta, \vec{k}_\alpha)|^2$$

where  $T_{\alpha\beta} = \langle \beta | V | \alpha \rangle$  contains all the **structure & interaction** information

## Common assumptions

- Separation of internal and relative degrees of freedom (**optical potential**)
- One-step reaction mechanism (**Born Approximation**)
- Simplification of the wave functions (clusters description / **plane or distorted waves**)

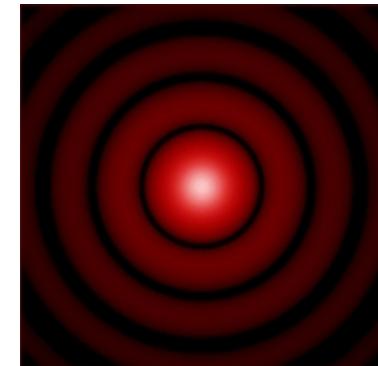
# Outline

- **Elastic and inelastic scattering**
- **Nucleon transfer**
  - sensitivity to the shell model / spectroscopic factors
  - the Distorted-Wave Born Approximation (DWBA)
  - achievements with exotic nuclei
  - correlations from two nucleon transfer
- **Knockout reactions**
  - S-matrix theory and eikonal approximation
  - Nuclear structure from knockout & in-beam  $\gamma$  spectroscopy
  - Absolute SF: transfer versus knockout
  - Quasifree scattering
- **Future developments and probes**

# Diffractive pattern / electron elastic scattering

Light diffraction off an aperture:

- Far source
  - Far detection
- } Fraunhofer diffraction

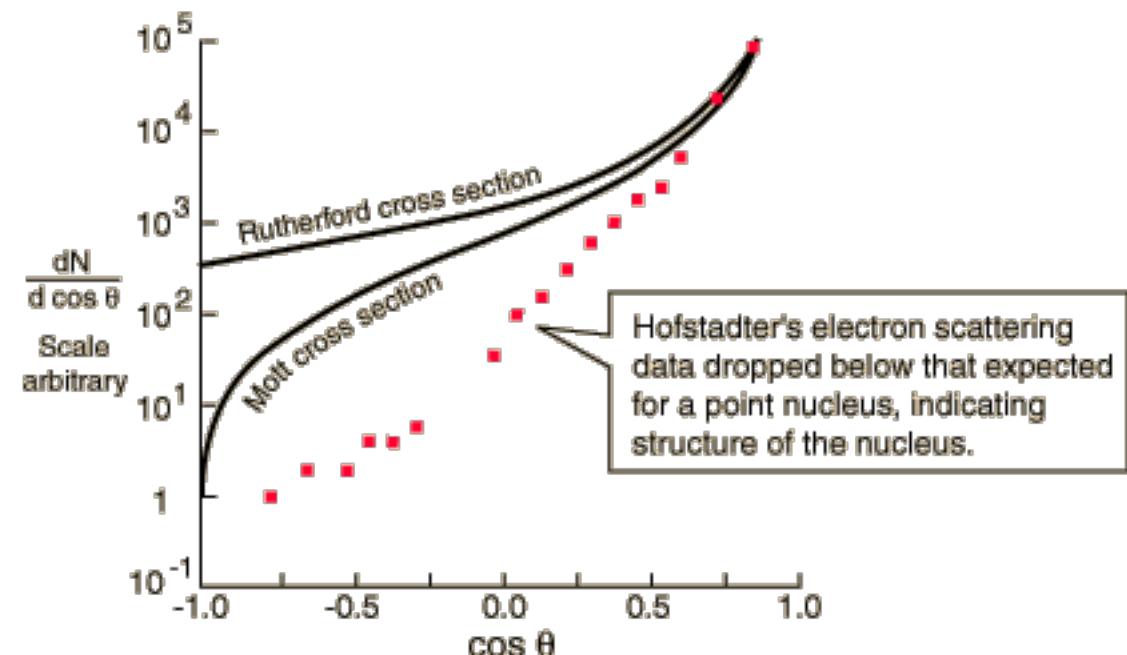


Pattern oscillations (Airy) :  $\Delta\theta = \lambda / (2R)$

→ Depends on the **size of the aperture**

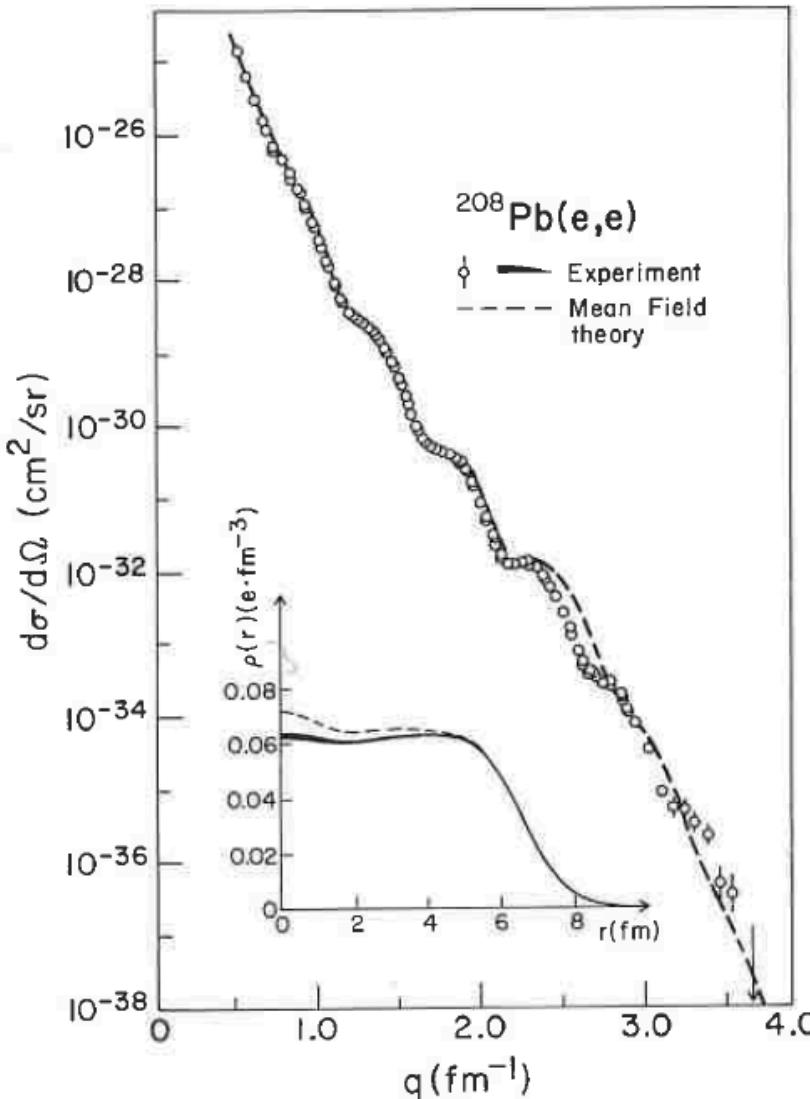
Electron scattering off a nucleus:

$$\lambda = \frac{\hbar}{p}$$



# Mott cross section and charge form factor

B. Frois and C.N. Papanicolas,  
Ann. Rev. Nucl. Part. Sci. 37, 133 (1987)



- **Elastic scattering cross section:**  
(assuming ONE exchanged direct photon)

$$\frac{d^2\sigma}{dEd\Omega} = \sigma_{Mott} |F(q)|^2$$

$q$ : transferred momentum

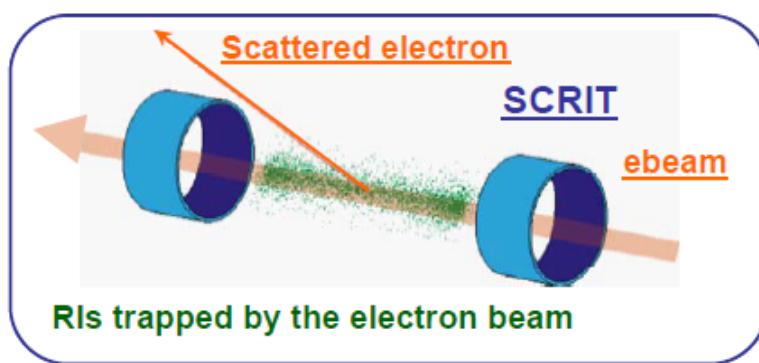
$$q^2 = 4EE' \sin^2\left(\frac{\theta}{2}\right)$$

- **Form factor:**

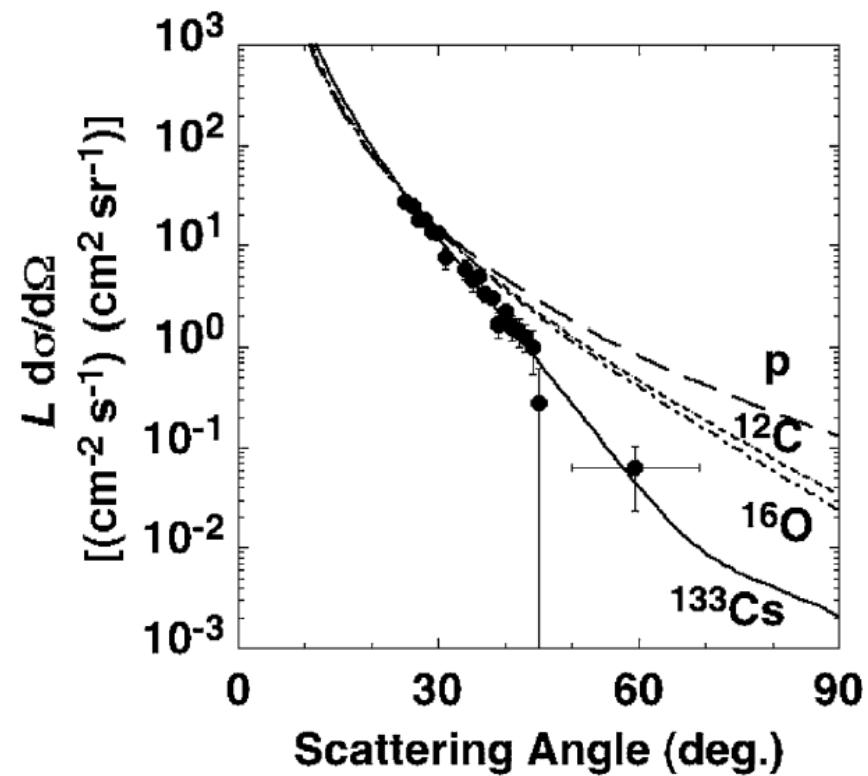
$$\begin{aligned} F(q) &= \langle \phi_{k_f} | V | \phi_{k_i} \rangle \\ &= \int e^{\frac{i\vec{q} \cdot \vec{r}}{\hbar}} \rho(\vec{r}') d^3 \vec{r}' \end{aligned}$$

# Electron scattering from unstable nuclei

e-RI scattering, SCRIT ring at RIKEN



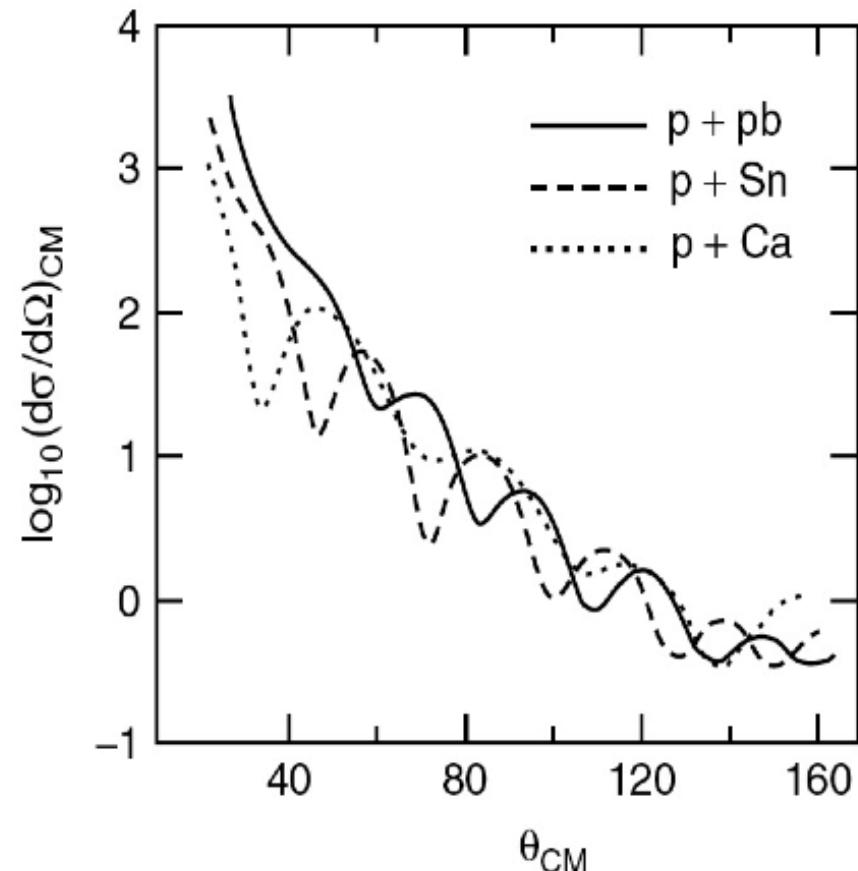
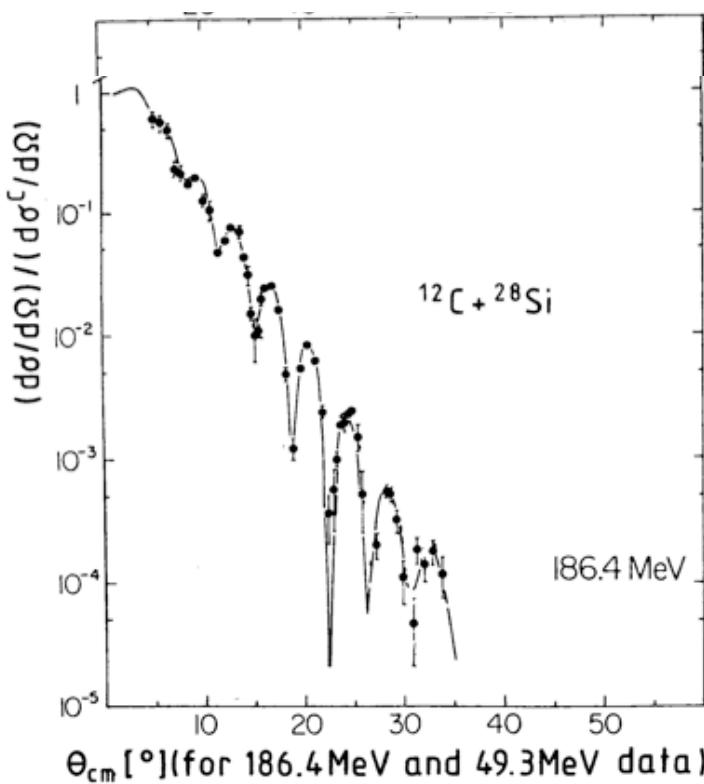
Luminosity up to  $10^{27} \text{ cm}^{-2} \text{ s}^{-1}$



T. Suda *et al.*, Phys. Rev. Lett. **102** (2009).

# Heavy-ion & proton elastic scattering

- Nuclear absorption
  - Fraunhofer-type interferences
- $$\Delta\theta = 1/(Rp)$$



C. Bertulani, Wiley Encyclopedia of Physics

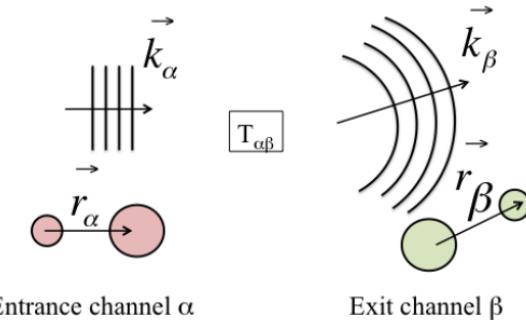
# Solving the Schrodinger equation for elastic scattering

$$(H - E)\psi = 0$$

$$V_\alpha = V_\alpha(\vec{r}_\alpha) \quad \text{optical potential approximation}$$

$$H = h_\alpha + T_\alpha + V_\alpha \quad \text{with } h_\alpha \text{ is the intrinsic hamitonian}$$

$$\psi = \Phi_A \chi \quad \text{intrinsic wave } \mathbf{X} \text{ relative motion}$$



**Homogenous equation** (no interaction potential)

$$(h_\alpha + T_\alpha - E)\phi_\alpha = 0 \Rightarrow \phi_\alpha = e^{i\vec{k}_\alpha \cdot \vec{r}_\alpha} \Phi_\alpha$$

**Inhomogenous equation:**  $(T_\alpha - E)\chi = -V_\alpha \chi$

$$\Rightarrow \chi = \phi_\alpha - \frac{V_\alpha}{T_\alpha - E} \chi \quad \text{distorted wave}$$

$$T_{\alpha\beta} = \langle \phi_\beta | V_\alpha | \chi_\alpha \rangle \quad \text{transition matrix element (prior form)}$$

Remark if one assumes  $\psi_\alpha = \phi_\alpha$  (**First Born approximation**)

$$T_{\alpha\beta} = \langle \phi_\beta | V | \phi_\alpha \rangle = \int e^{i(\vec{k}_\alpha - \vec{k}_\beta) \cdot \vec{r}} V(\vec{r}) d^3 r \quad \text{for elastic scattering}$$

# Optical potentials

## 1) Empirical Optical Potentials (Parameterized on data)

$$V(R) = V_0(R) + i W(R) + \dots \text{ (surface, spin-orbite, Coulomb)}$$

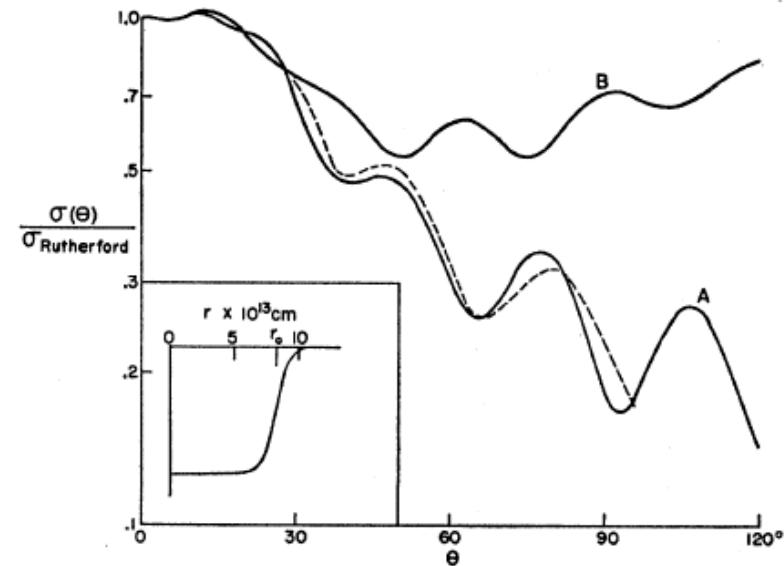


FIG. 1. Elastic scattering of 22-Mev protons by Pt relative to Rutherford scattering. The dashed curve is the experimental result of Cohen and Neidigh (see reference 3), the normalization of which is somewhat uncertain. Curve A is calculated for a diffuse surface model with  $V=38$  Mev,  $W=9$  Mev,  $r_0=8.24 \times 10^{-13}$  cm, and  $a=0.49 \times 10^{-13}$  cm. The shape of the well is shown in the small drawing at the lower left. Curve B is calculated for a square well of comparable size and depth.

# Optical potentials

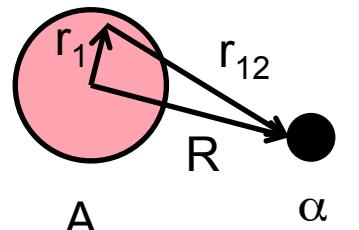
## 1) Empirical Optical Potentials (Parameterized on data)

$$V(R) = V_0(R) + i W(R) + \dots \text{ (surface, spin-orbite, Coulomb)}$$

## 2) Microscopic Optical Potential

*Simple folding*

$$V(\vec{R}) = \int \rho_A v(\vec{r}_{12})$$



*Double folding*

$$V(\vec{R}) = \int \int \rho_\alpha \rho_A v(\vec{r}_{12})$$

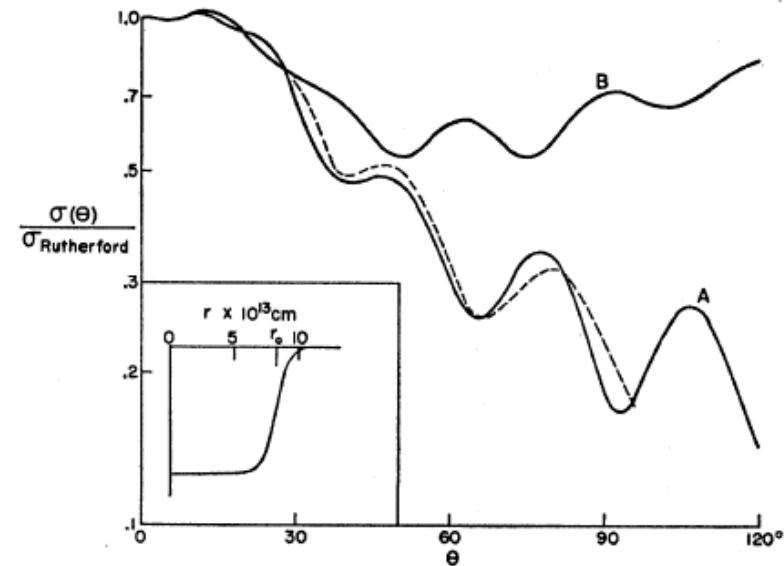
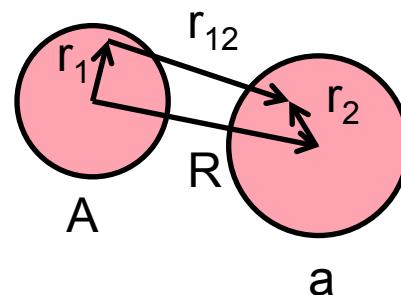
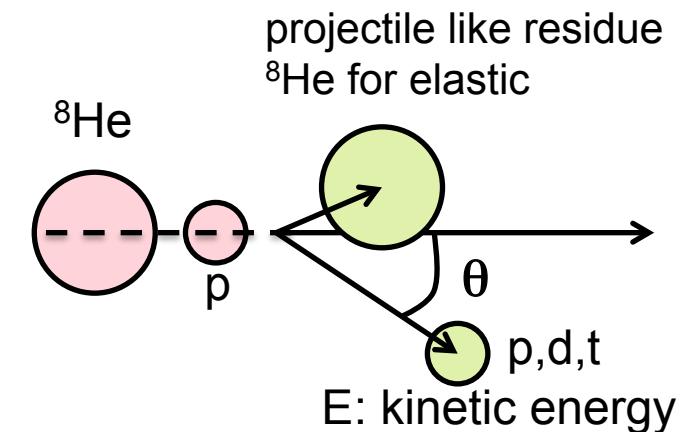
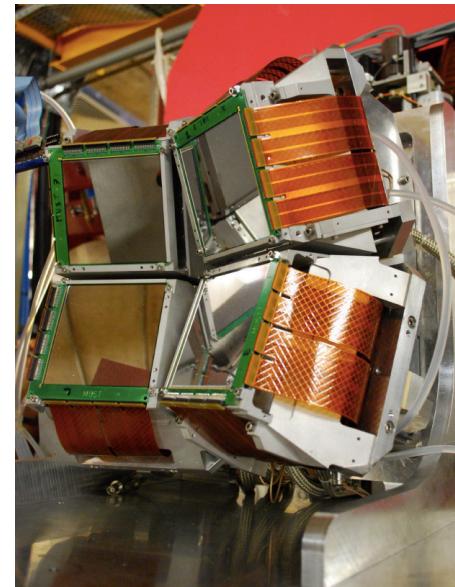
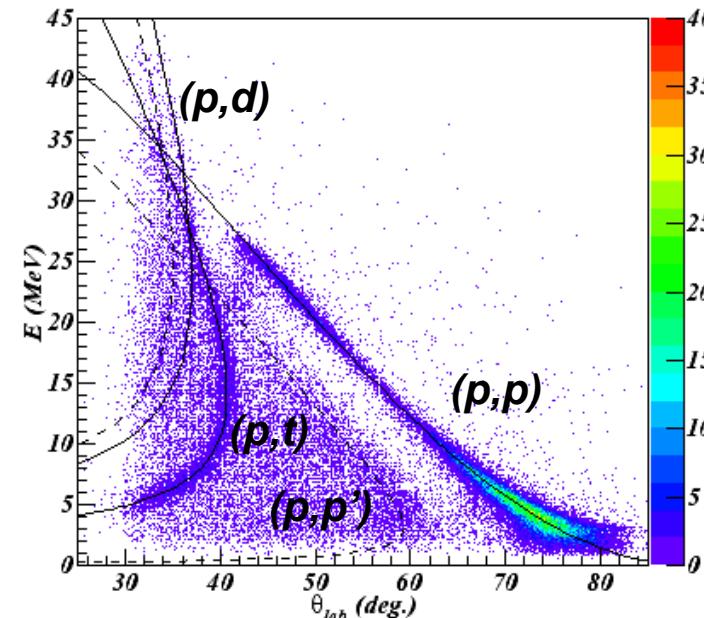


FIG. 1. Elastic scattering of 22-Mev protons by Pt relative to Rutherford scattering. The dashed curve is the experimental result of Cohen and Neidigh (see reference 3), the normalization of which is somewhat uncertain. Curve A is calculated for a diffuse surface model with  $V = 38$  Mev,  $W = 9$  Mev,  $r_0 = 8.24 \times 10^{-13}$  cm, and  $a = 0.49 \times 10^{-13}$  cm. The shape of the well is shown in the small drawing at the lower left. Curve B is calculated for a square well of comparable size and depth.

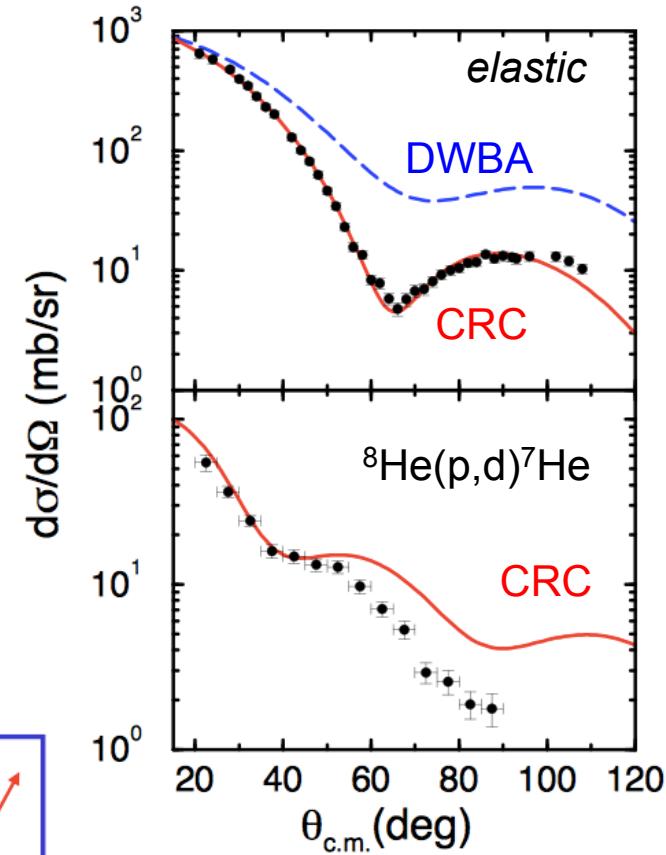
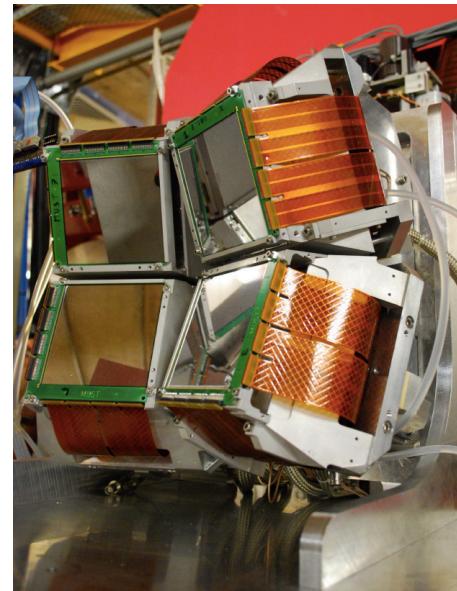
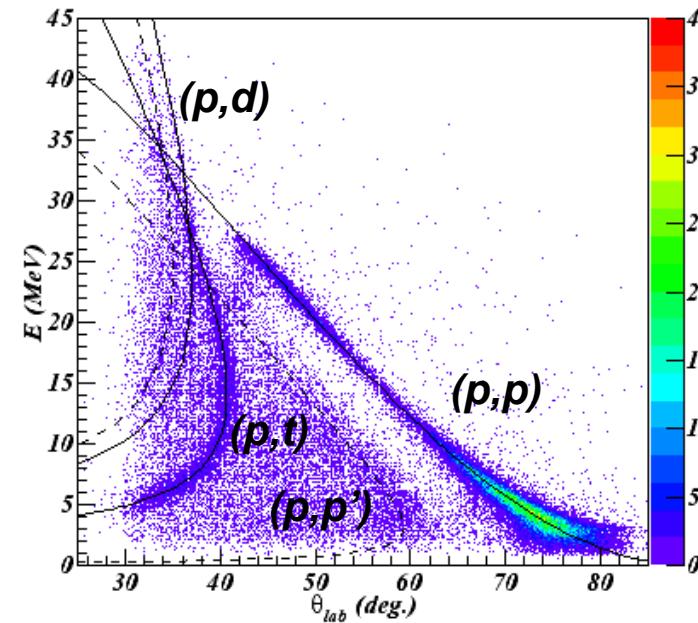
# Example of proton elastic scattering from ${}^8\text{He}$

${}^8\text{He} + \text{p}$  at 16 MeV/nucleon, with MUST2 @ GANIL



# Example of proton elastic scattering from ${}^8\text{He}$

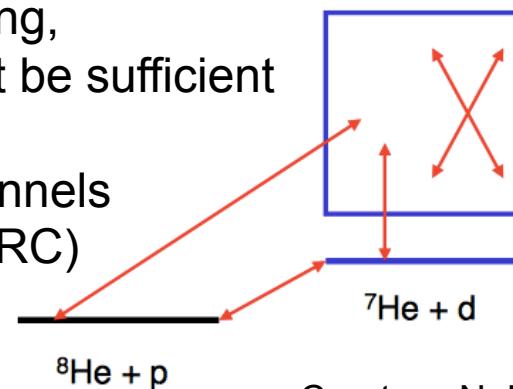
${}^8\text{He} + \text{p}$  at 16 MeV/nucleon, with MUST2 @ GANIL



## Nota Bene:

When reaction channels are strong,  
treating the elastic alone may not be sufficient

- Explicit treatment of other channels
- Coupled reaction channels (CRC)

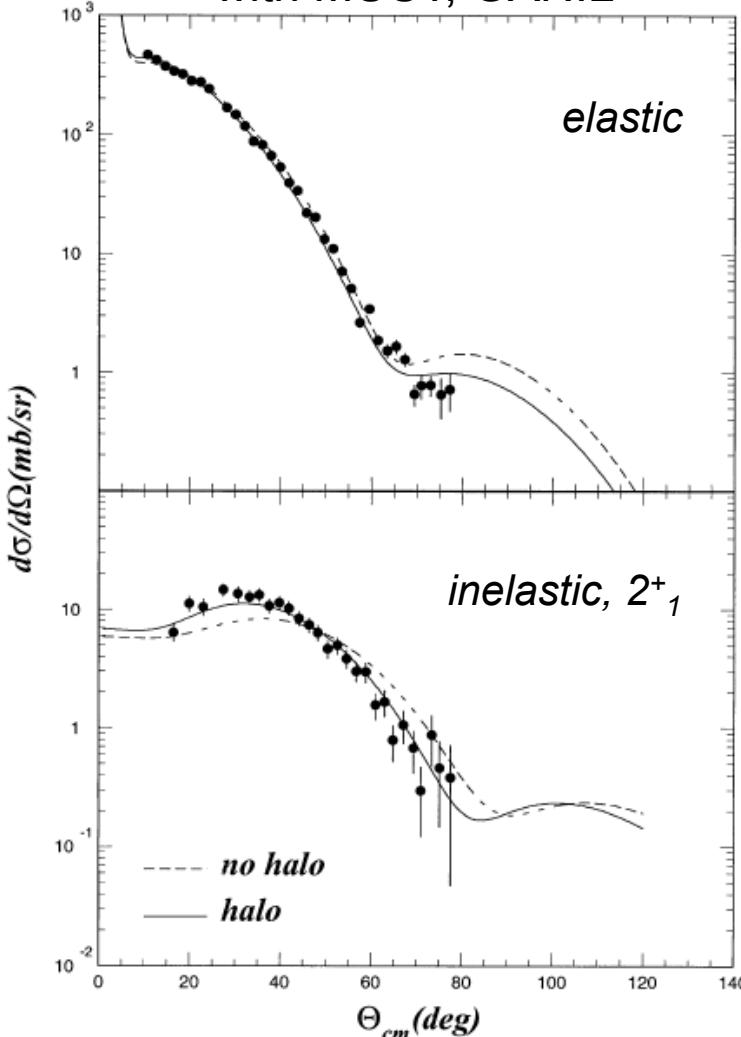


N. Keeley et al., PLB 619 (2005).

Courtesy N. Keeley (Warsaw) and V. Lapoux (CEA)

# Proton inelastic scattering

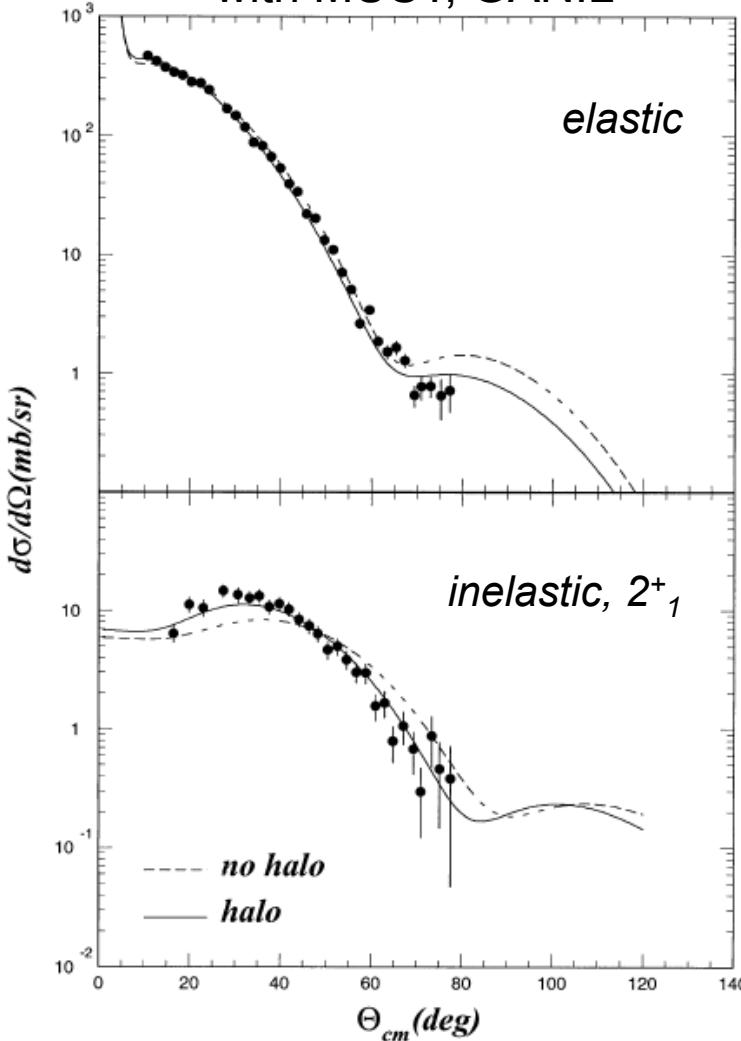
${}^6\text{He}(p,p')$  at 40.9 MeV/nucleon,  
with MUST, GANIL



A. Lagoyannis et al., PLB 518 (2001).

# Proton inelastic scattering

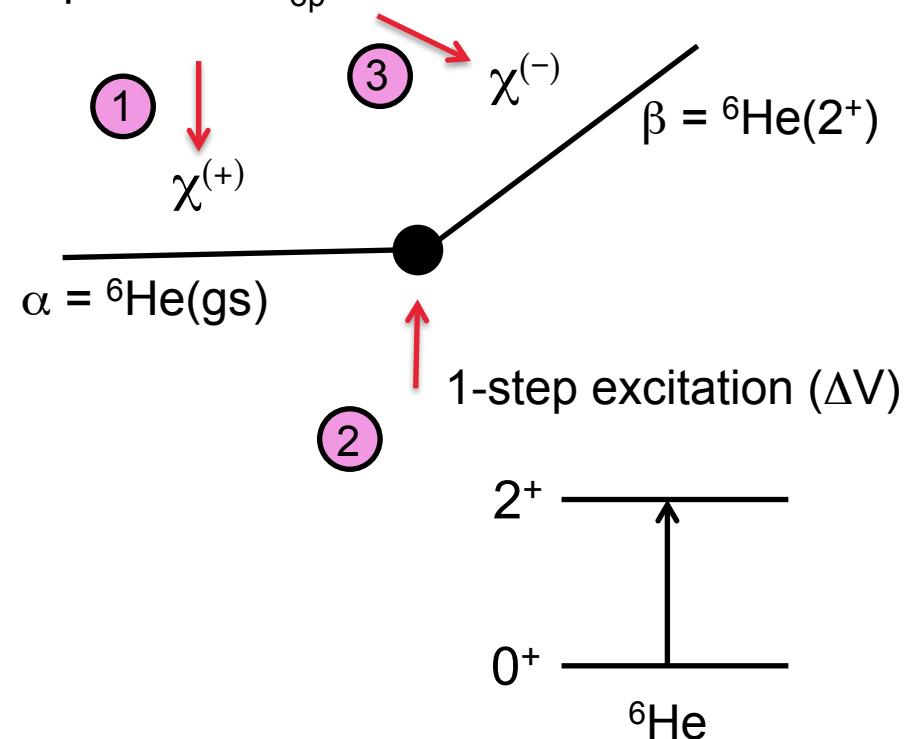
${}^6\text{He}(p,p')$  at 40.9 MeV/nucleon,  
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A. Lagoyannis et al., PLB 518 (2001).

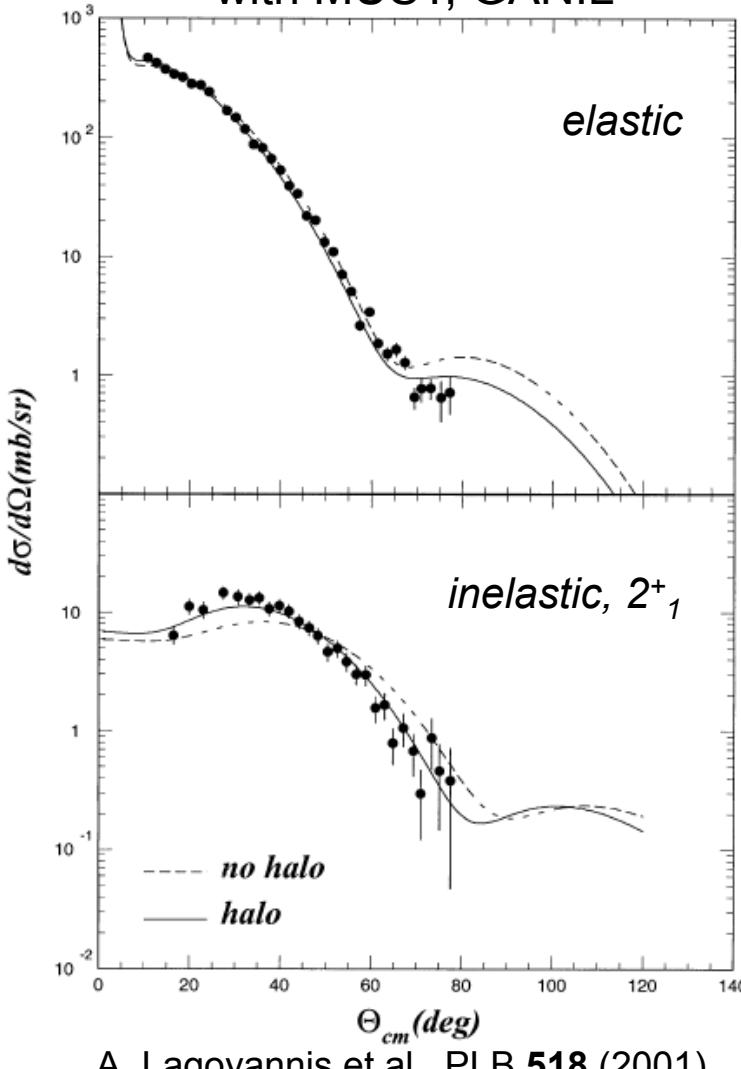
## The Distorted Wave Born approximation

Distorsion of the incoming & outgoing waves  
Optical potential  $V_{op}$



# Proton inelastic scattering

${}^6\text{He}(p,p')$  at 40.9 MeV/nucleon,  
with MUST, GANIL



A. Lagoyannis et al., PLB 518 (2001).

**Two potential equation**

$$(H - E)\psi = 0$$

$$H = h_\alpha + T_\alpha + V_{OP} + \Delta V$$

**Distorted wave  $\chi$ :**

$$(h_\alpha + T_\alpha + V_{OP} - E)\chi_\alpha^{(+)} = 0$$

**Transition matrix element (DWBA approximation)**

$$\begin{aligned} T_{\alpha\beta} &= \langle \chi_\beta^{(-)} \Phi_\beta | \Delta V | \chi_\alpha^{(+)} \Phi_\alpha \rangle \\ &= \int \int \chi_\beta^{(-)}(\vec{k}_\beta, \vec{r}_\beta) \langle \Phi_\beta | \Delta V | \Phi_\alpha \rangle \chi_\alpha^{(+)}(\vec{k}_\alpha, \vec{r}_\alpha) d^3 r_\alpha d^3 r_\beta \end{aligned}$$

**Nota Bene:**  $\Delta V$  depends on the structure model

**1) Microscopic description of  $\langle \Phi_\beta | \Delta V | \Phi_\alpha \rangle$**

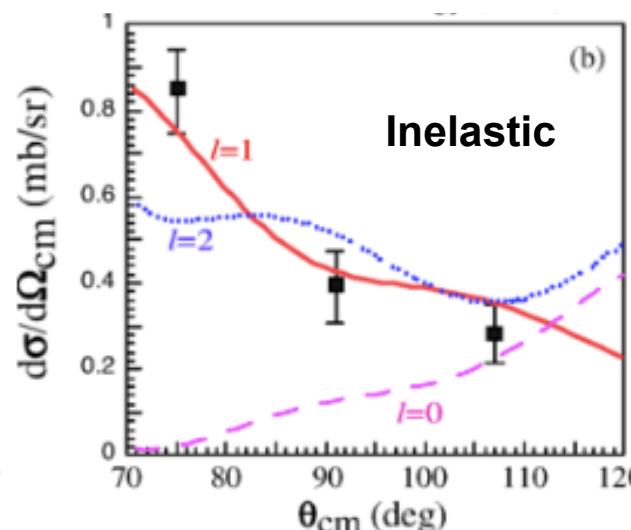
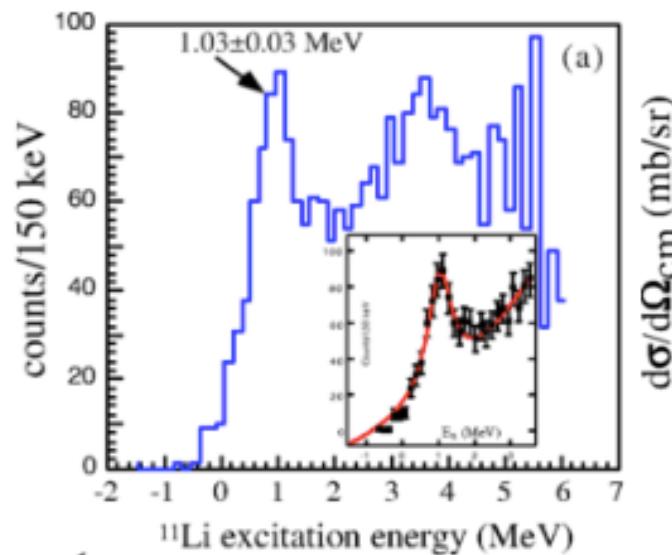
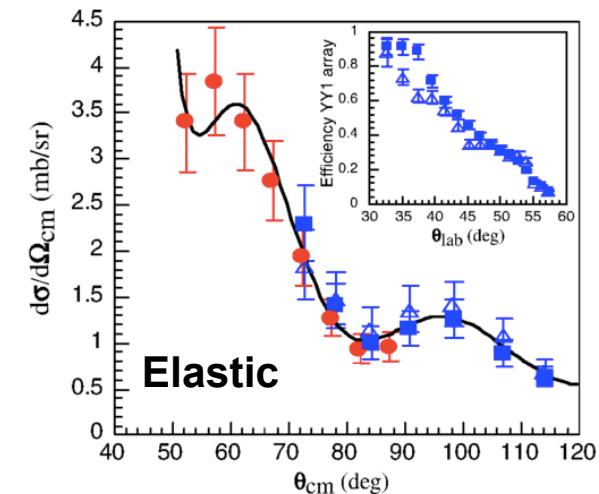
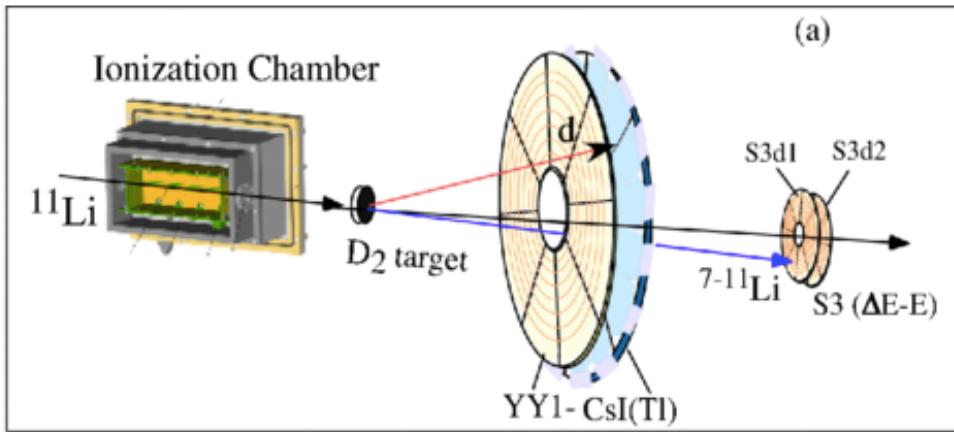
**2) Collective model (ex. rotational)**

Amplitude of  $\Delta V$  governed by a parameter

$\delta_{LM}$  = deformation length

# Inelastic scattering from $^{11}\text{Li}$ : soft dipole resonance

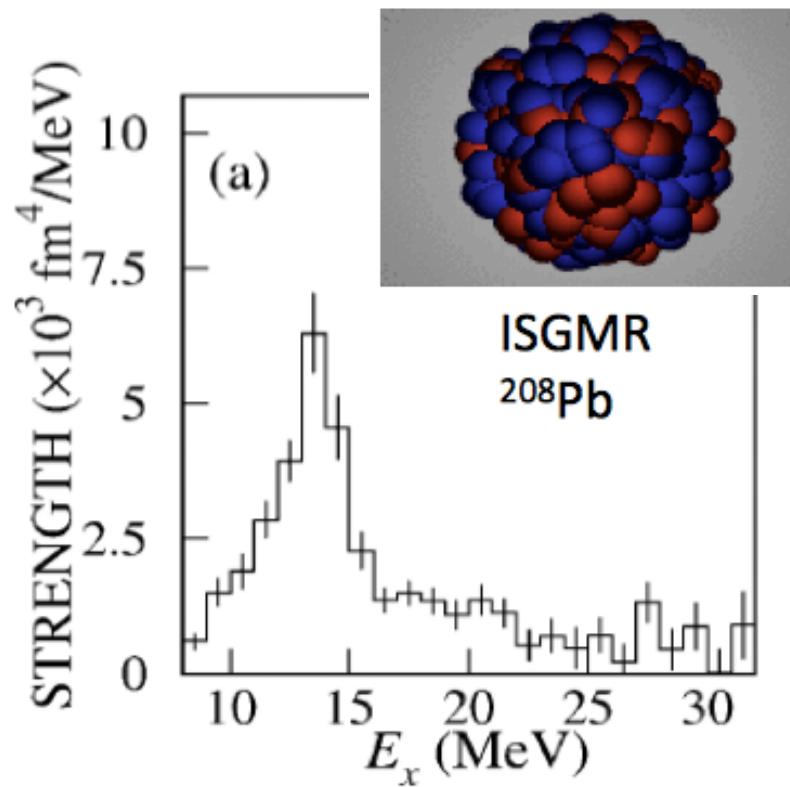
R. Kanungo et al., PRL 114 (2015)



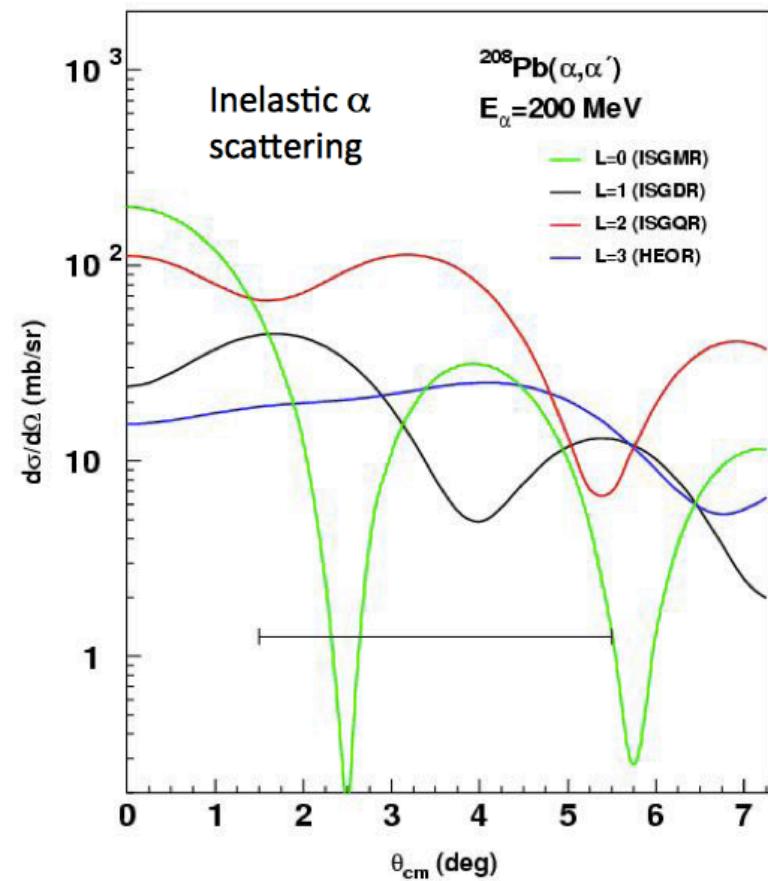
- $^{11}\text{Li}$  at 5.5 MeV/u
- 3000 pps
- $\text{D}_2$  solide target (100 $\mu\text{m}$ )
- TRIUMF
- DWBA analysis
- collective ( $\delta$ ) model
- L = 1 assignement
- Dipole resonnance

# Giant Monopole Resonance (GMR)

Isoscalar Giant Monopole Resonance: **compression mode** of the nucleus  
**Measure around  $0^\circ_{\text{cm}}$**  is needed to maximize and extract the Monopole ( $L=0$  transfer)



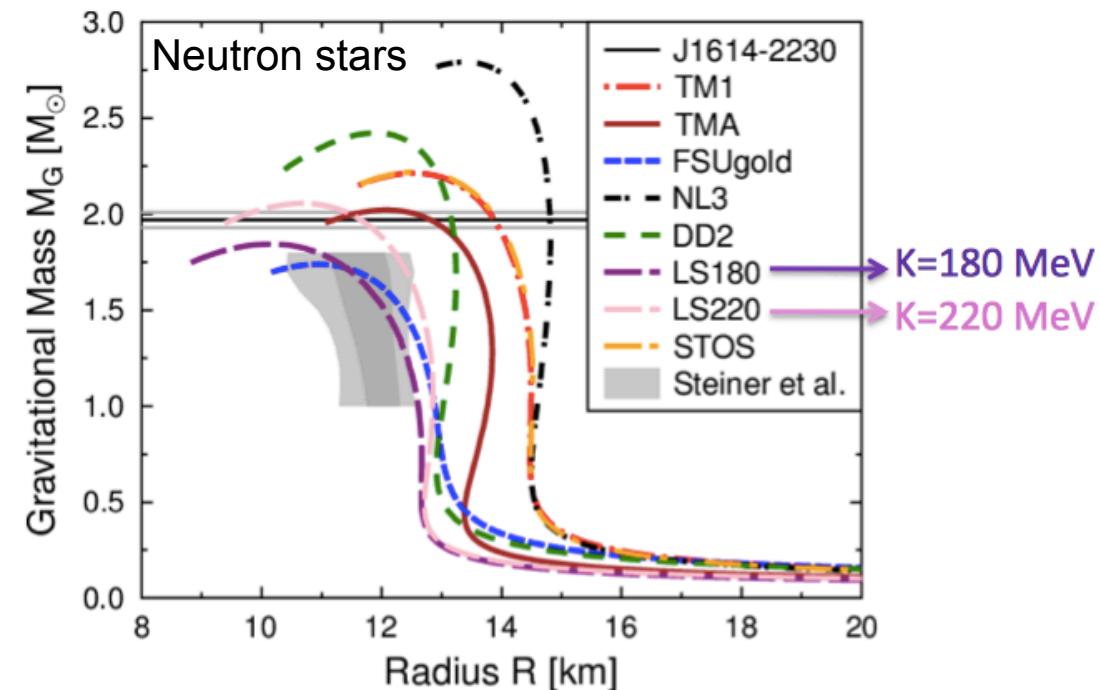
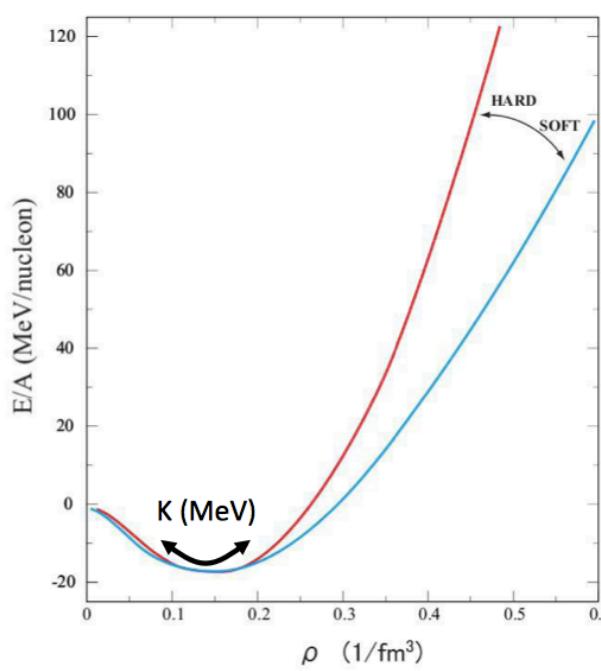
M. Uchida *et al.*, Phys. Lett. B **557** (2003)



# Nuclear incompressibility and Giant Resonances

## Nuclear incompressibility

Energy needed to change the density of nuclear matter around equilibrium



Incompressibility from a nucleus to the infinite matter:

$$K_A = K_\infty + K_{surf} A^{-1/3} + K_\tau \delta^2 + K_{Coul} \frac{Z^2}{A^{4/3}}$$

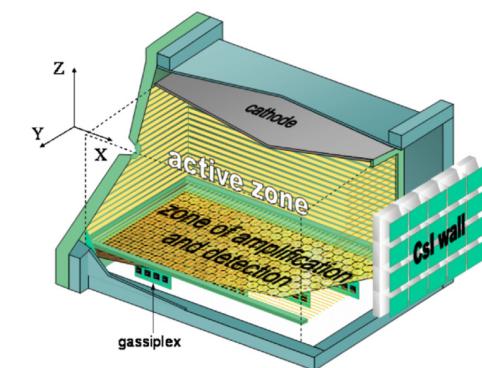
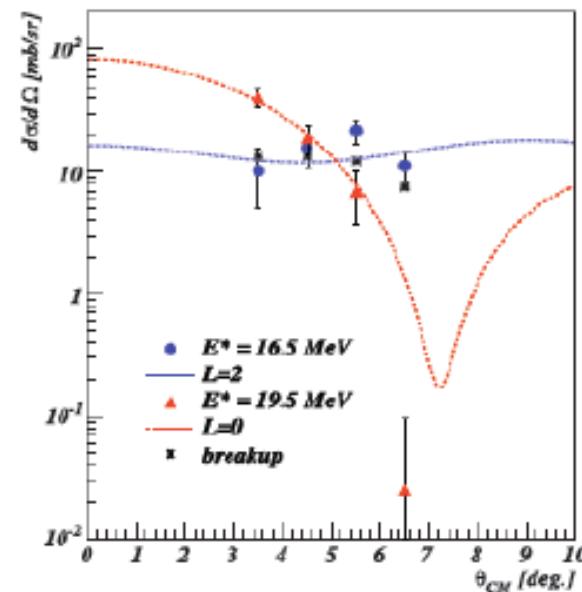
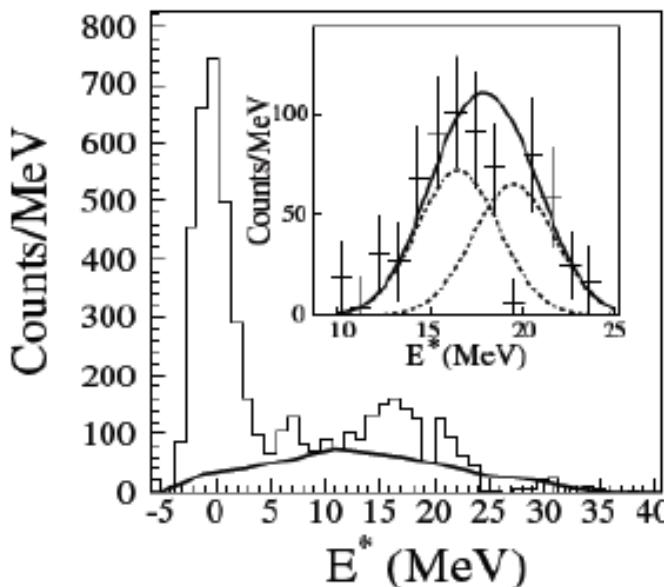
↑  
From GMR energy

asymmetry term  $\delta = (N-Z)/A \Rightarrow$  exotic nuclei only!

# GMR in unstable nuclei

Low-energy recoil (specific detection), incident energies from 50 to 100 MeV/nucleon

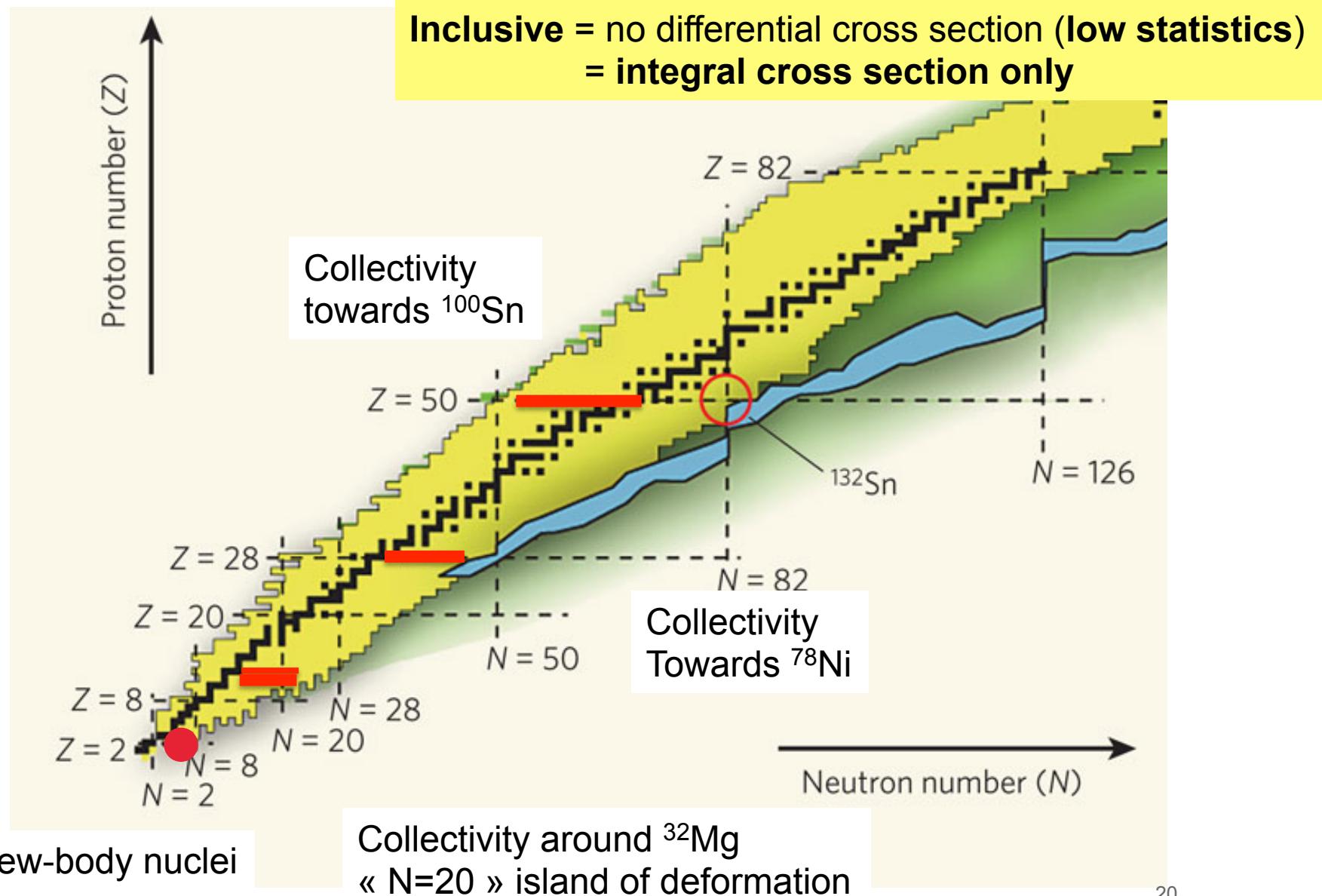
$^{56}\text{Ni}(\alpha, \alpha')$  at 50 A MeV, GANIL with MAYA : first GMR from unstable nucleus



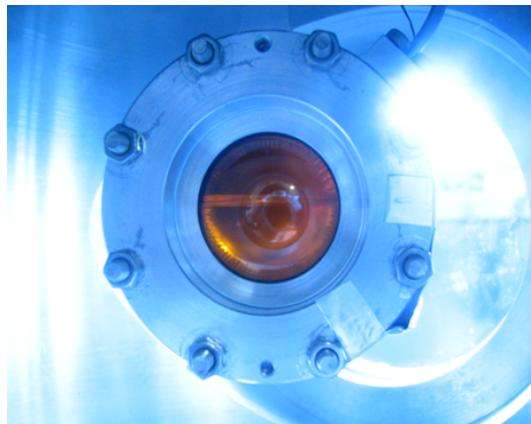
C. Monrozeau *et al.*, Phys. Rev. Lett. **100** (2008).

Recently  $^{68}\text{Ni}(\alpha, \alpha')$ , GANIL, M. Vandebruck *et al.*, Phys. Rev. Lett. **113** (2014).  
 Near future,  $^{132}\text{Sn}(\alpha, \alpha')$ , RIKEN, S. Ota (CNS) *et al.*

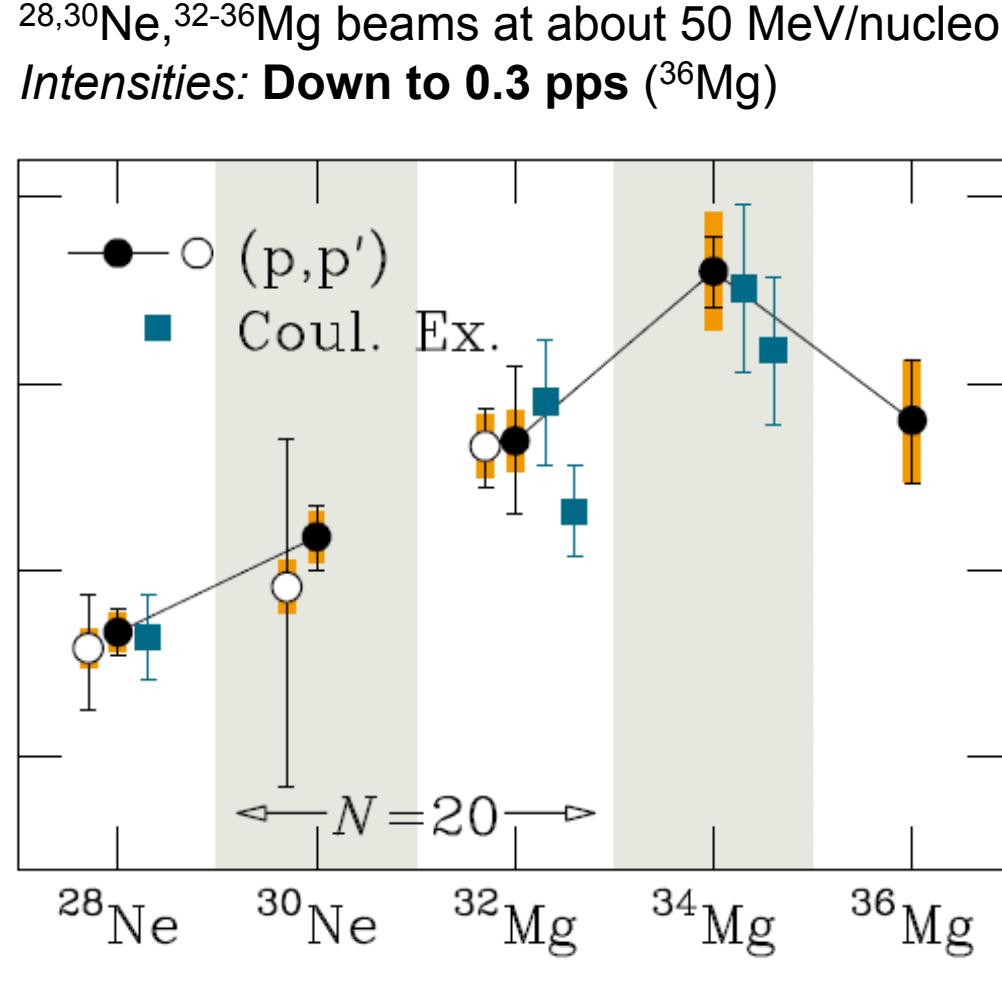
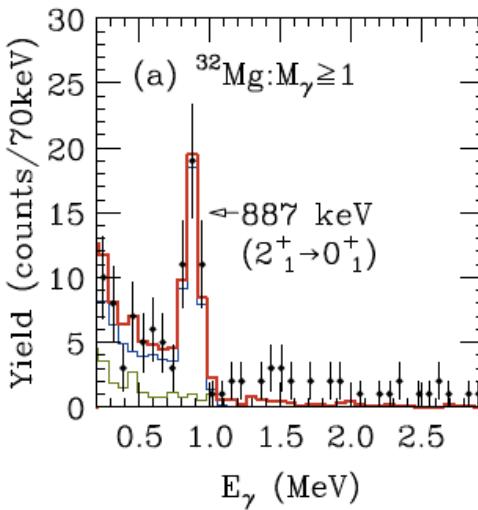
# Collectivity in unstable nuclei from inclusive ( $p,p'$ )



# Onset of deformation in the region of $^{32}\text{Mg}$ ( $N=20$ )



**RIKEN experiment:**  
liquid  $\text{H}_2$  target  
+ DALI2 NaI scintillator array

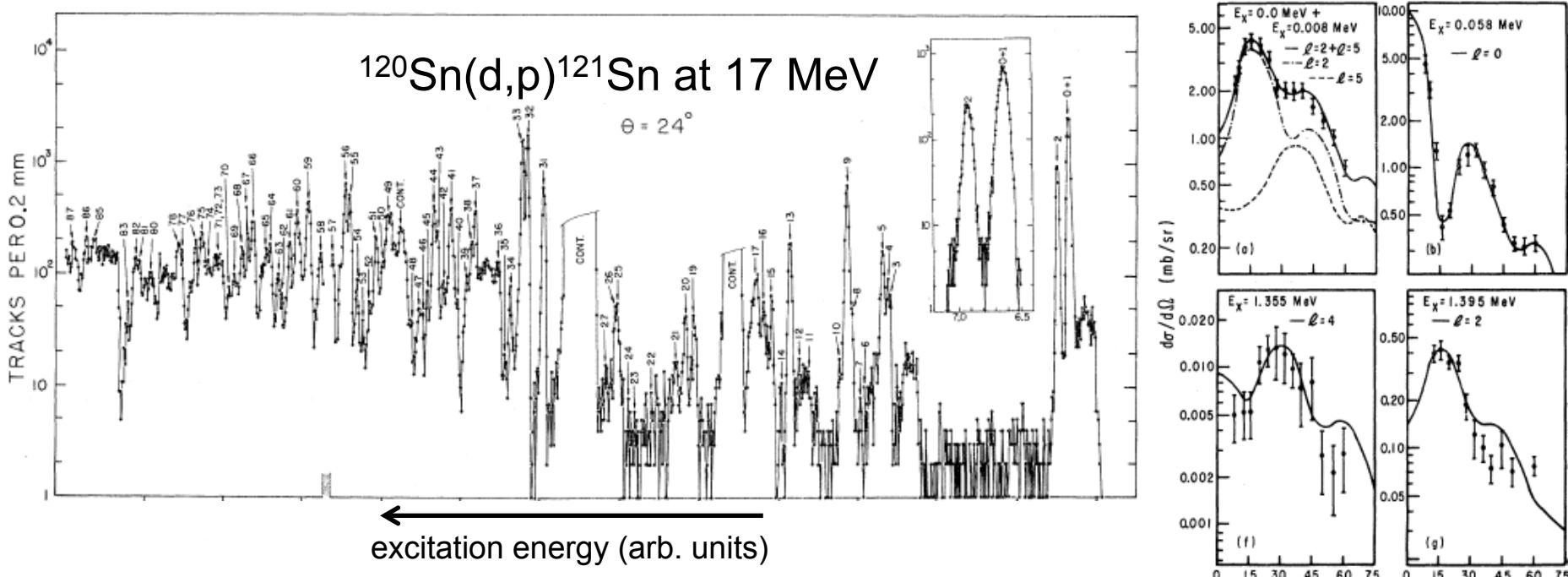


Inclusive cross section: low beam intensity... and high uncertainties <sub>21</sub>

# Outline

- **Elastic and inelastic scattering**
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  - achievements with exotic nuclei
  - correlations from two nucleon transfer
- **Knockout reactions**
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  - Absolute SF: transfer versus knockout
  - Quasifree scattering
- **Future developments and probes**

# Transfer reactions : selectivity / direct



M.J.Bechara and O.Dietzsch, Phys. Rev. C **12** (1975).

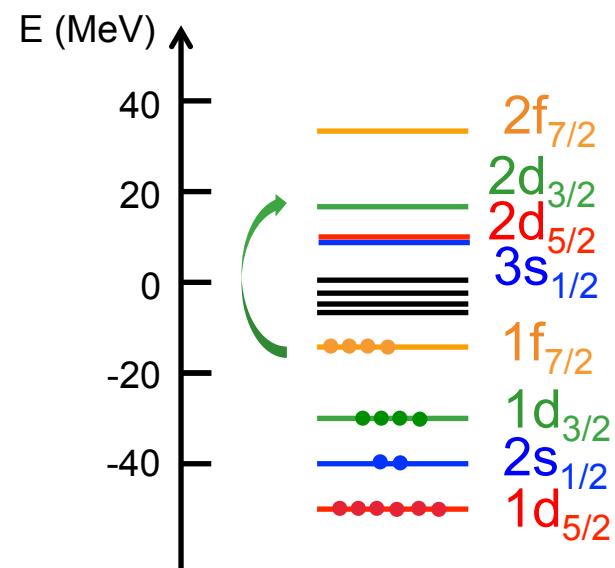
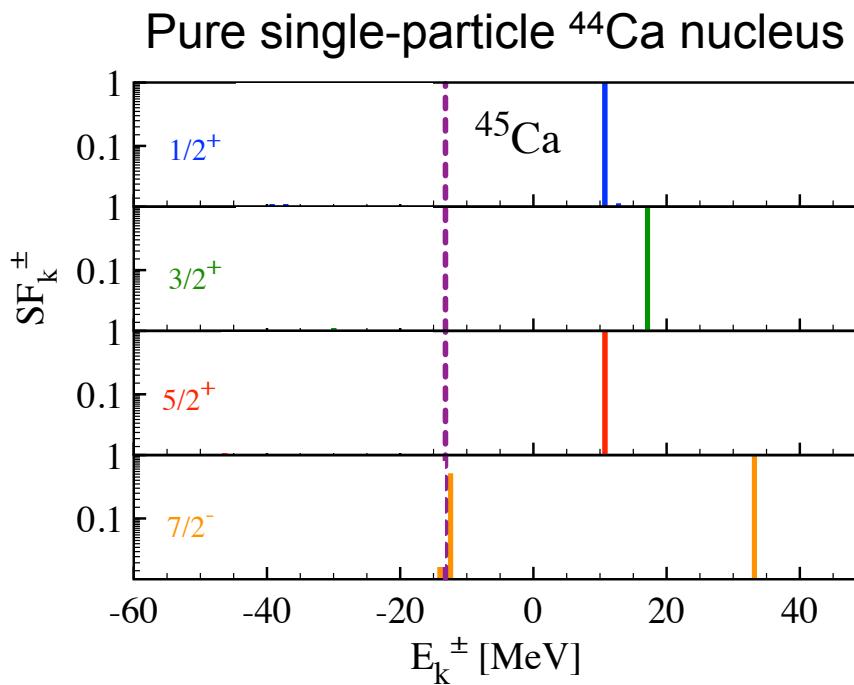
- Direct: **surface process**
- Transfer: **momentum matching** (Fermi velocities, 5 to 50 MeV/nucleon)
- **Conservation** of: spin, parity, angular momentum

# Intuitive view of Spectroscopic Factors (SFs)

**Spectroscopic factor:** the square overlap of a final state with a single particle state

$$S_k^{nlj\pm} = \left| \left\langle \psi_k^{A+1} \left| a_{nlj}^{\pm} \right| \psi_0^A \right\rangle \right|^2$$

Pickup, ex:  $^{44}\text{Ca}(\text{d},\text{p})^{45}\text{Ca}$



# Intuitive view of Spectroscopic Factors (SFs)

**Spectroscopic factor:** the square overlap of a final state with a single particle state

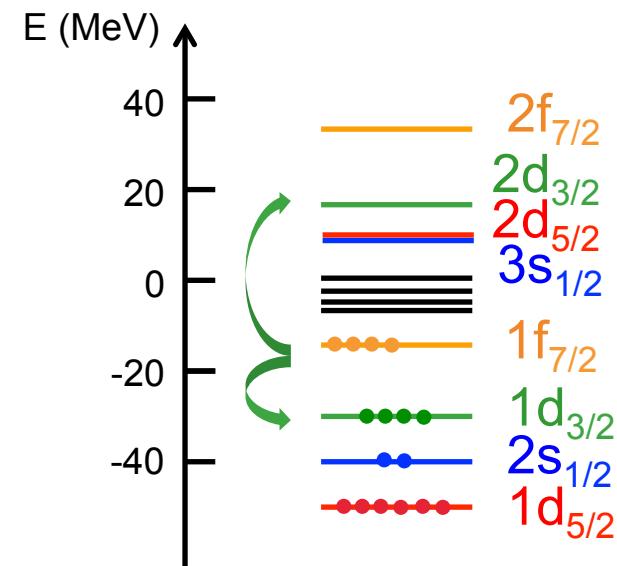
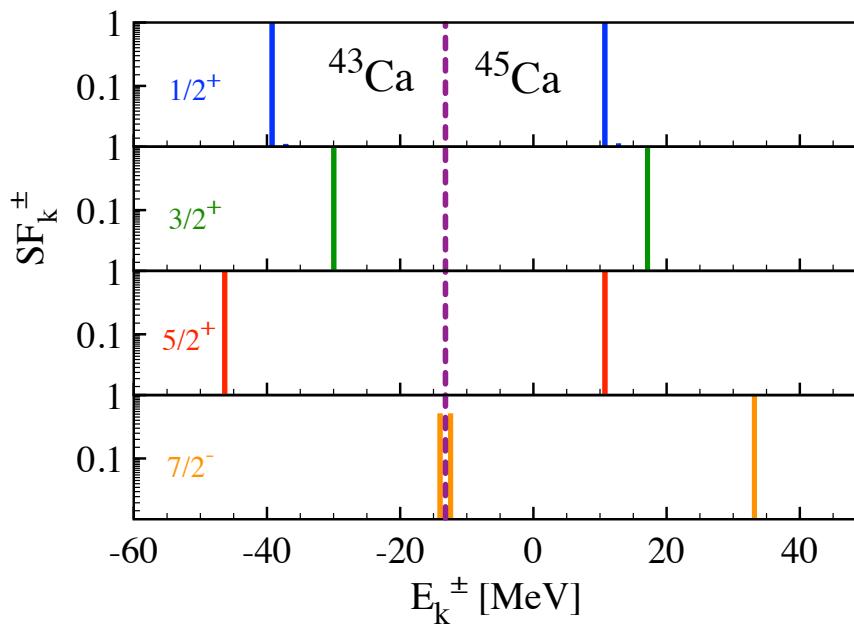
$$S_k^{nlj\pm} = \left| \left\langle \psi_k^{A+1} \left| a_{nlj}^{\pm} \right| \psi_0^A \right\rangle \right|^2$$

Pickup, ex:  $^{44}\text{Ca}(\text{d},\text{p})^{45}\text{Ca}$

$$S_k^{nlj\mp} = \left| \left\langle \psi_k^{A-1} \left| a_{nlj} \right| \psi_0^A \right\rangle \right|^2$$

Stripping, ex:  $^{44}\text{Ca}(\text{p},\text{d})^{43}\text{Ca}$

Pure single-particle  $^{44}\text{Ca}$  nucleus



# Intuitive view of Spectroscopic Factors (SFs)

**Spectroscopic factor:** the square overlap of a final state with a single particle state

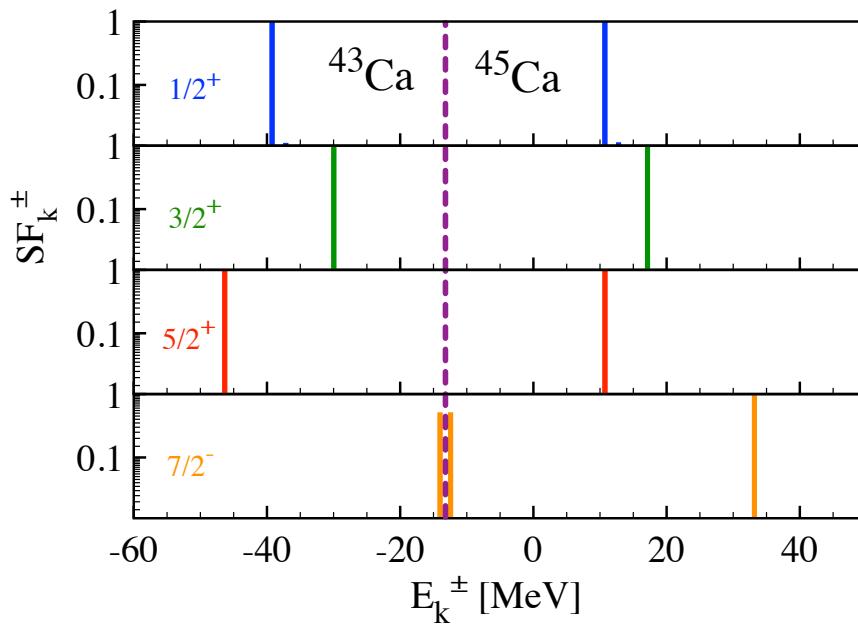
$$S_k^{nlj+} = \left| \left\langle \psi_k^{A+1} \left| a_{nlj}^+ \right| \psi_0^A \right\rangle \right|^2$$

Pickup, ex:  $^{44}\text{Ca}(\text{d},\text{p})^{45}\text{Ca}$

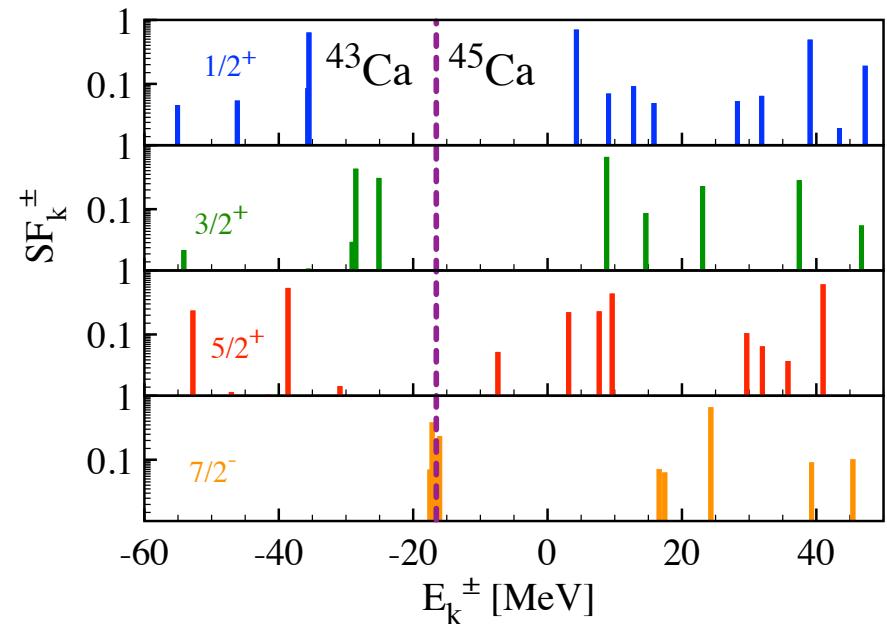
$$S_k^{nlj-} = \left| \left\langle \psi_k^{A-1} \left| a_{nlj}^- \right| \psi_0^A \right\rangle \right|^2$$

Stripping, ex:  $^{44}\text{Ca}(\text{p},\text{d})^{43}\text{Ca}$

Pure single-particle  $^{44}\text{Ca}$  nucleus



Real (correlated)  $^{44}\text{Ca}$  nucleus



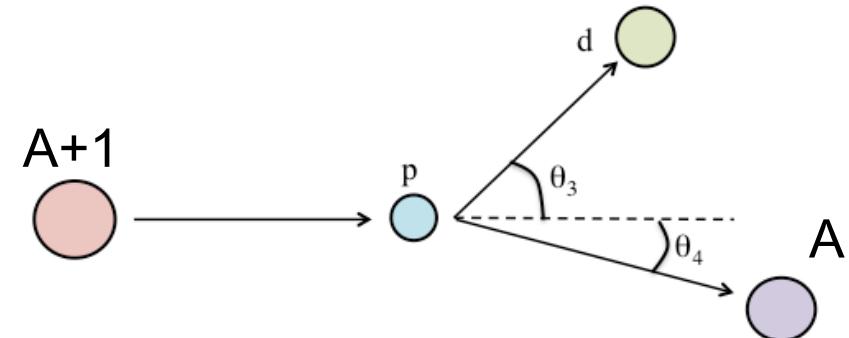
In reality:  $0 < \text{SF} < 1$

# Transfer reaction in the Born Approximation

**Plane wave approx.:  $p + (A+1) \rightarrow d + A$**

$$|\psi_\alpha\rangle = e^{i\vec{k}_p \cdot \vec{r}_p} \Phi_{A+1,\alpha}$$

$$|\psi_\beta\rangle = e^{i\vec{k}_d \cdot \vec{r}_d} \Phi_{A,\beta} \Phi_d(\vec{r}_n - \vec{r}_p)$$



**Transition matrix element**

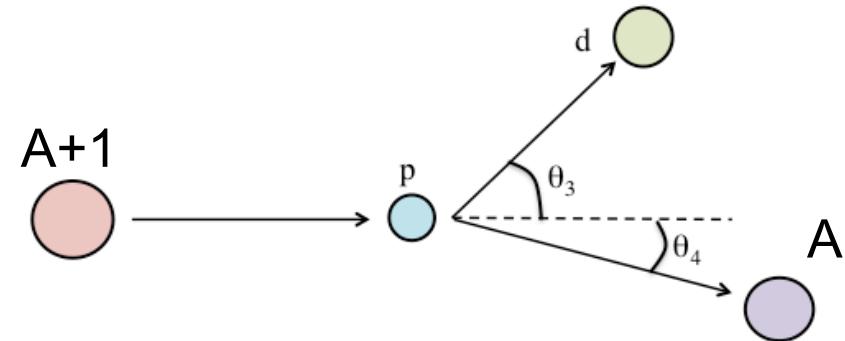
$$T \propto \langle \psi_\beta | V | \psi_\alpha \rangle = \int e^{-i\vec{k}_d \cdot \vec{r}_d} \Phi_d^*(\vec{r}) \Phi_A^*(\vec{r}) V(\vec{r}) e^{i\vec{k}_p \cdot \vec{r}_p} \Phi_{A+1} d^3 r_{A+1} d^3 r_p$$

# Transfer reaction in the Born Approximation

**Plane wave approx.: p+(A+1) → d + A**

$$|\psi_\alpha\rangle = e^{i\vec{k}_p \cdot \vec{r}_p} \Phi_{A+1,\alpha}$$

$$|\psi_\beta\rangle = e^{i\vec{k}_d \cdot \vec{r}_d} \Phi_{A,\beta} \Phi_d(\vec{r}_n - \vec{r}_p)$$



**Transition matrix element**

$$T \propto \langle \psi_\beta | V | \psi_\alpha \rangle = \int e^{-i\vec{k}_d \cdot \vec{r}_d} \Phi_d^*(\vec{r}) \Phi_A^*(\vec{r}) V(\vec{r}) e^{i\vec{k}_p \cdot \vec{r}_p} \Phi_{A+1} d^3 r_{A+1} d^3 r_p$$

In the case of a **pure single-particle neutron state**  $\Phi_{A+1,\alpha} = \Phi_{A,\beta} \phi_{n\ell j}(\vec{r}_n)$

$$T = \int e^{-i\vec{k}_d \cdot \vec{r}_d} \Phi_d^*(\vec{r}) \Phi_A^*(\vec{r}) V_{np}(\vec{r}) e^{i\vec{k}_p \cdot \vec{r}_p} \phi_{n\ell j} \Phi_A d^3 r_A d^3 r_n d^3 r_p$$

Fourier transform of  
The picked-up neutron

which leads to

$$T = \int e^{-i\vec{K} \cdot \vec{r}} \Phi_d^*(\vec{r}) V_{np}(\vec{r}) d^3 r \left( \int_R^\infty e^{-i\vec{q} \cdot \vec{r}_n} \phi_{n\ell j}(\vec{r}_n) d^3 r_n \right)$$

$$\vec{q} = \vec{k}_d - \vec{k}_p \quad \text{momentum carried by the picked-up neutron}$$

$$K = k_p - k_n / 2$$

# Transfer reactions: DWBA

$$\begin{aligned}
 T_{\alpha\beta} &= \left\langle \chi_{\beta}^{(-)} \Phi_{\beta} \left| V \right| \chi_{\alpha}^{(+)} \Phi_{\alpha} \right\rangle \quad \text{with} \quad \left| \Phi_{A+1,\beta} \right\rangle = \sum_{nlj} \sqrt{S_{\beta}^{nlj+}} \left| \phi_{nlj} \Phi_A \right\rangle \\
 &= \sum_{nlj} \sqrt{S_{\beta}^{nlj+}} \int \chi_d^{(-)*}(\vec{k}_d, \vec{r}_d) \Phi_d^*(\vec{r}) \left\langle \Phi_A^* \phi_{nlj}^* \left| V_{np}(\vec{r}) \right| \Phi_{A+1,\beta} \right\rangle \chi_p^{(+)}(\vec{k}_p, \vec{r}_p) d^3 r_p d^3 r_d
 \end{aligned}$$

nuclear structure      deuteron wf & reaction process

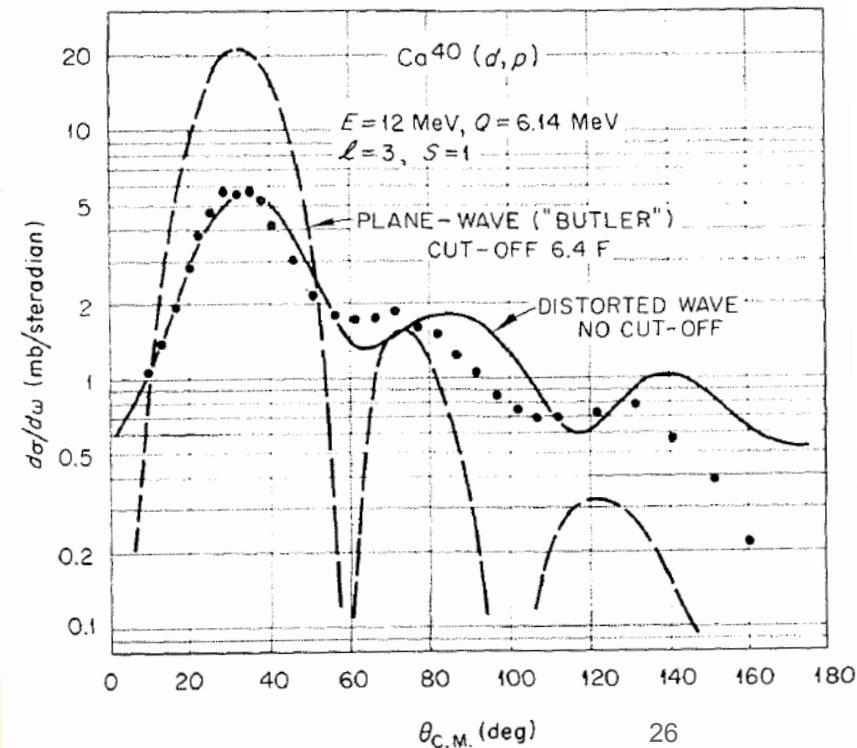
**Nota Bene:** in the DWBA, reaction mechanism and structure are separated

## Transfer cross section in DWBA

$$\frac{d\sigma_{\alpha\beta}}{d\Omega} = \sum_{nlj} S_{nlj} \frac{d\sigma_{\alpha\beta}}{d\Omega} \Big|_{nlj}$$

## Analysis of experiments

- 1) Measure  $d\sigma/d\Omega$
- 2) Calculate  $d\sigma/d\Omega$  single particle
- 3) Extract  $S_{nlj}$  by comparison
- 4) Compare to  $S_{nlj}$  from theoretical model



# Why spectroscopic factors are so important?

Single particle energies  $e_{nlj}$  can be accessed from:

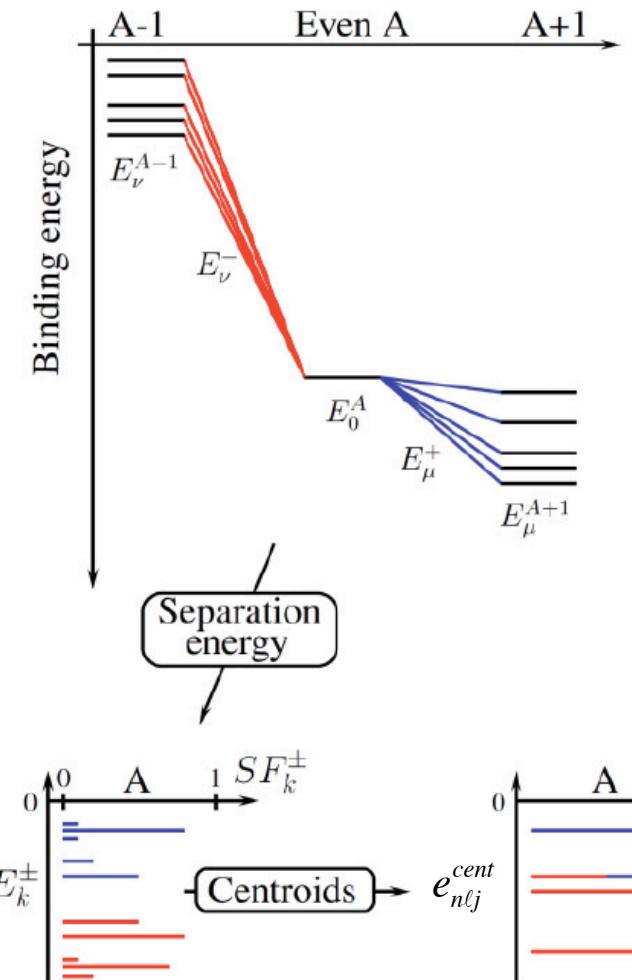
- **physical state energies  $E_k$**  (observables)  
from pickup AND stripping
- **spectroscopic factors  $S_k^{nlj}$**  (not observables)

**Baranger equation:**

$$e_{nlj} = \frac{\sum_k S_k^{nlj+} (E_k - E_0) + S_k^{nlj-} (E_0 - E_k)}{\sum_k S_k^{nlj+} + S_k^{nlj-}}$$

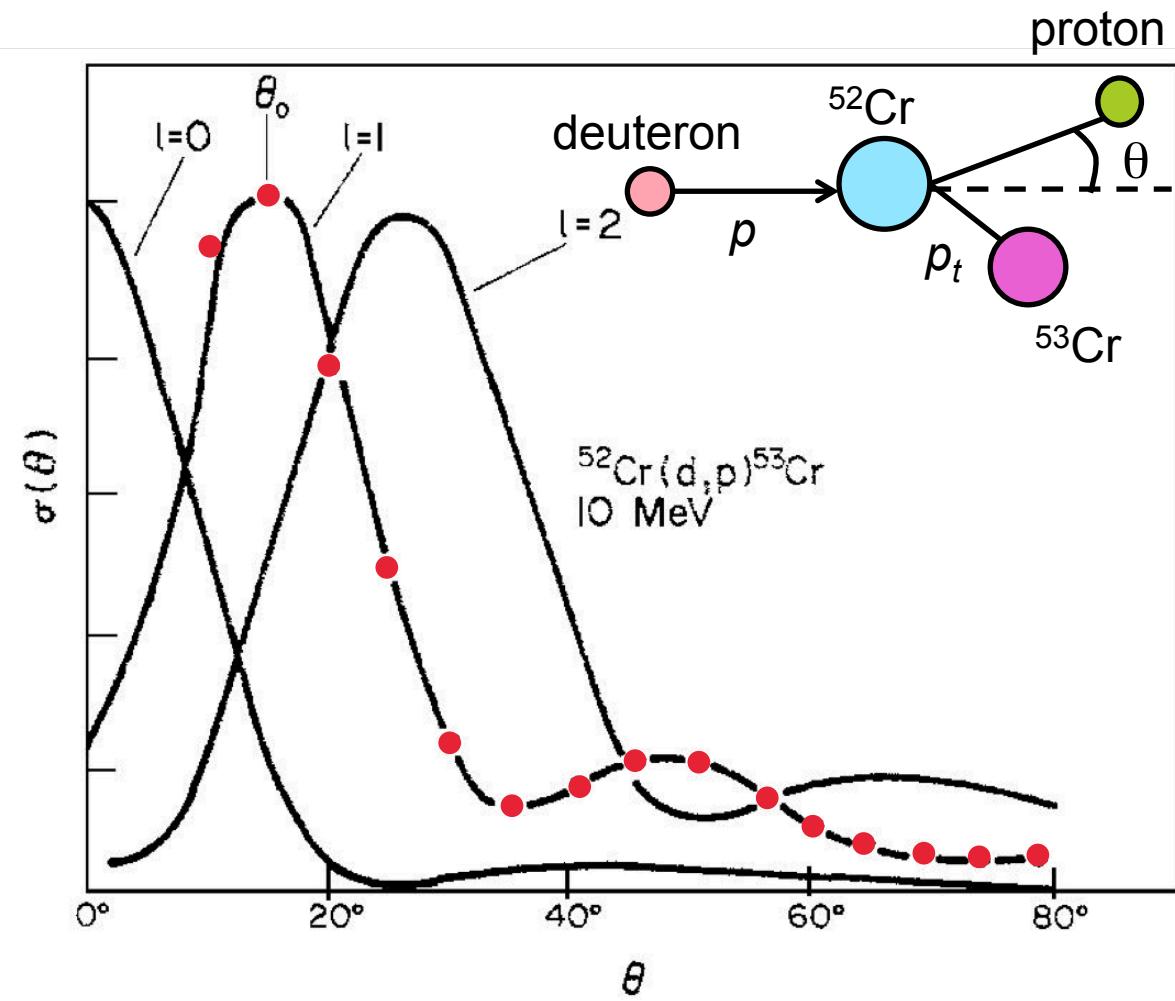
**In principle**, in a given theoretical framework,  
**SFs** can be obtained from **cross sections**.

**In reality, uncertainties are today too large**  
to extract single-particle energies directly from the  
Baranger equation.



T. Duguet and G. Hagen, PRC **85** (2012)

# Transfer reactions: angular distributions



L.D. Knutson and W. Haeberli, Prog. Part. Nucl. Phys. **3** (1980).

- Classical derivation:

$$\hat{L}^2 |\phi_{nlj}\rangle = (\ell + 1)\ell \hbar^2 |\phi_{nlj}\rangle$$

$$p_t \approx p \times \sin(\theta)$$

$$L = R \times p_t \Rightarrow Rp \sin(\theta) = \sqrt{(\ell + 1)\ell} \hbar$$

$$\Rightarrow \theta_0 = \sin^{-1}\left(\frac{\sqrt{(\ell + 1)\ell} \hbar}{Rp}\right)$$

- Numerical application:

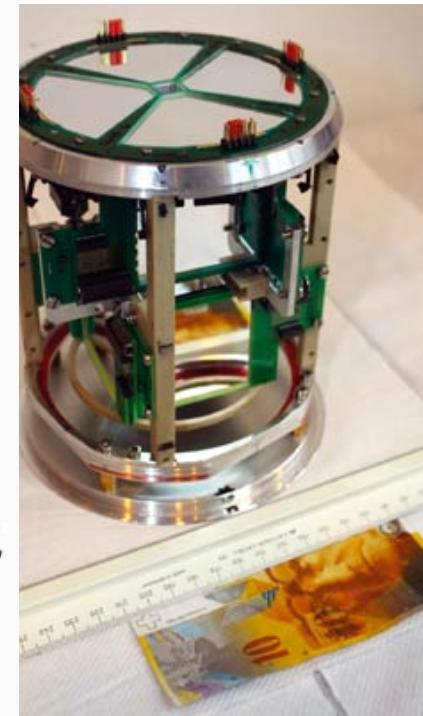
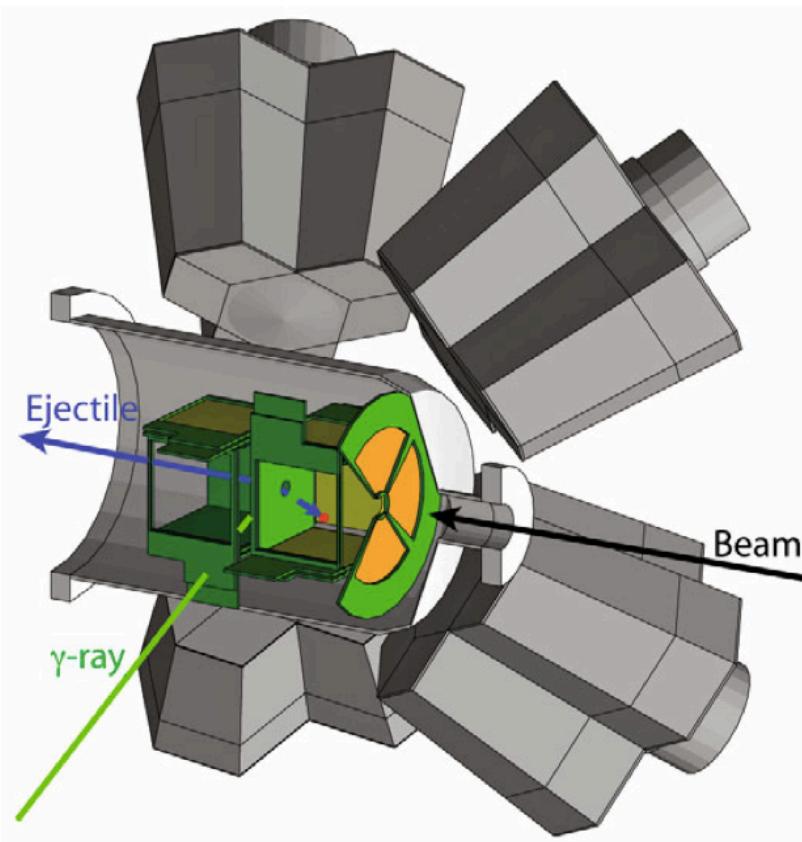
$$\ell = 0 \Rightarrow \theta_0 = 0^\circ$$

$$\ell = 1 \Rightarrow \theta_0 = 19^\circ$$

$$\ell = 2 \Rightarrow \theta_0 = 34^\circ$$

# Example of setup for low-energy reaction studies

**T-REX+MINIBALL** setup at **ISOLDE, CERN**: particle- $\gamma$  detection for direct reactions  
ISOLDE: energies up to 5.5 MeV/nucleon (from 2015), up to 8 MeV/nucleon from 2018

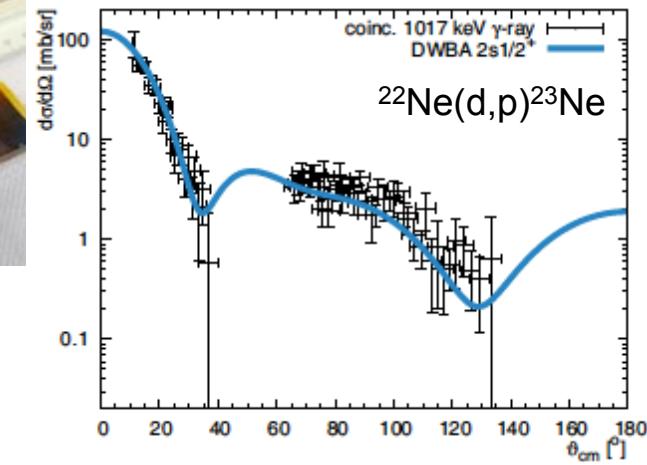


## Particle resolution

- 150 keV FWHM  
For a  $100 \text{ }\mu\text{g.cm}^{-2}$  target
- 600 keV FWHM  
For a  $1 \text{ mg.cm}^{-2}$  target

## Photopeak gamma efficiency

5% at 1.3 MeV



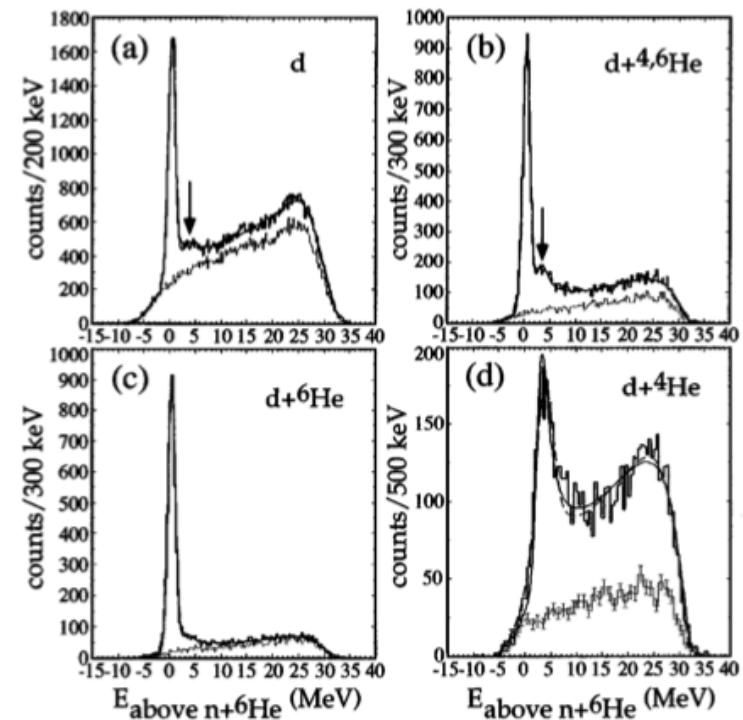
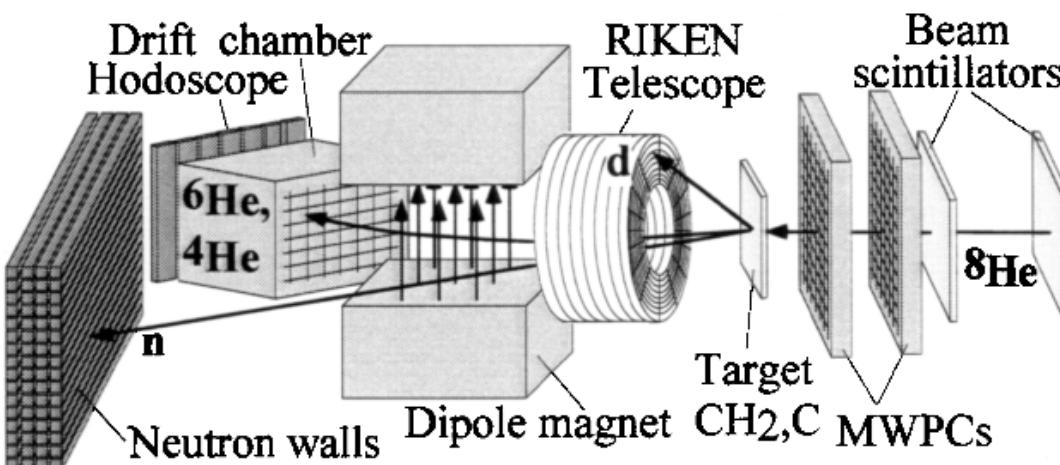
Other « similar » setups worldwide:

SHARC+Tigress at TRIUMF, TIARA+MUST2+EXOGAM at GANIL

... other ongoing developments (TRACE - GASPARD for SPES/GANIL in Europe)

# Few-body systems and nuclear resonances

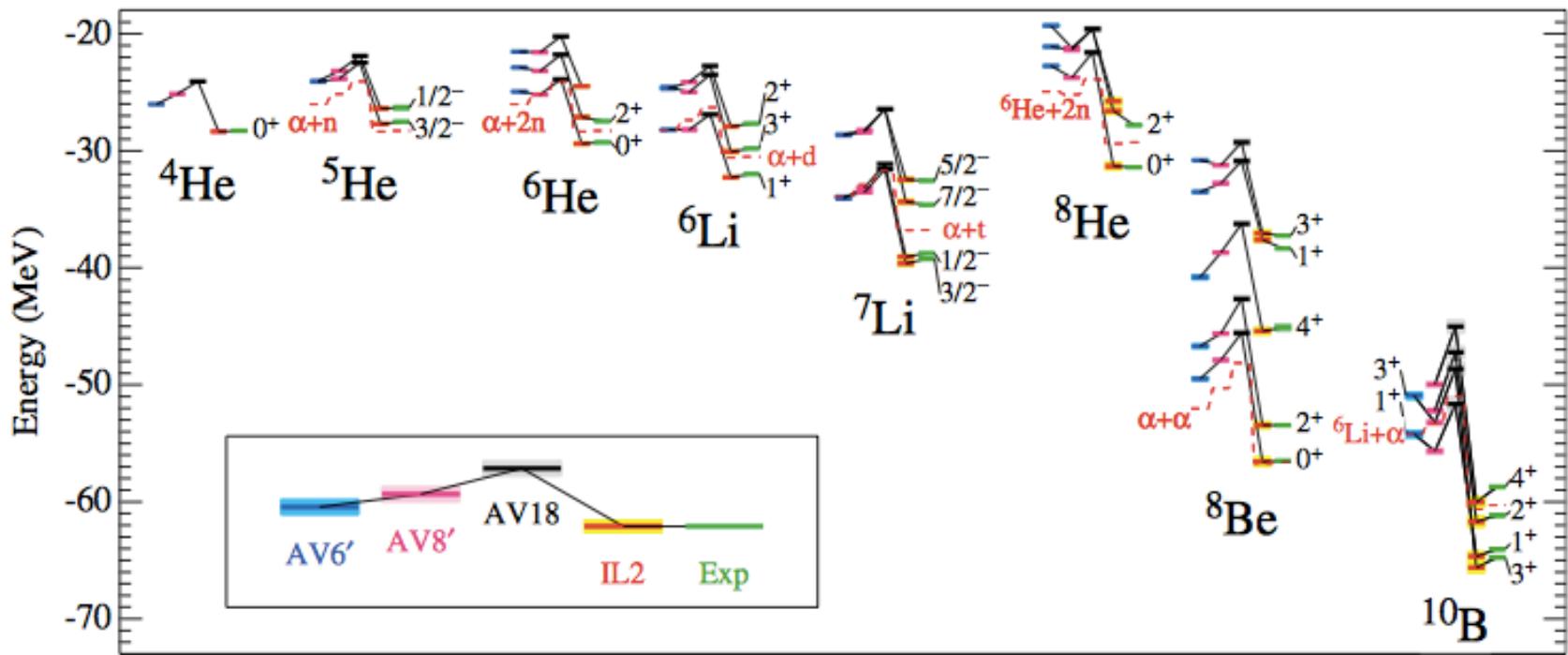
- spectroscopy of **few-body systems** (bound and **unbound states**) is key to understand nuclear structure
- transfer reactions are unique **to populate selectively and identify states**
- a huge work in many laboratories (Dubna, RIKEN, GANIL, TRIUMF,...)



$^8\text{He}(\text{p},\text{d})^7\text{He}$  at 50 MeV/nucleon, RIPS, RIKEN  
A.A. Korshenninikov *et al.*, PRL **82** (1999)

# Few-body systems and nuclear resonances

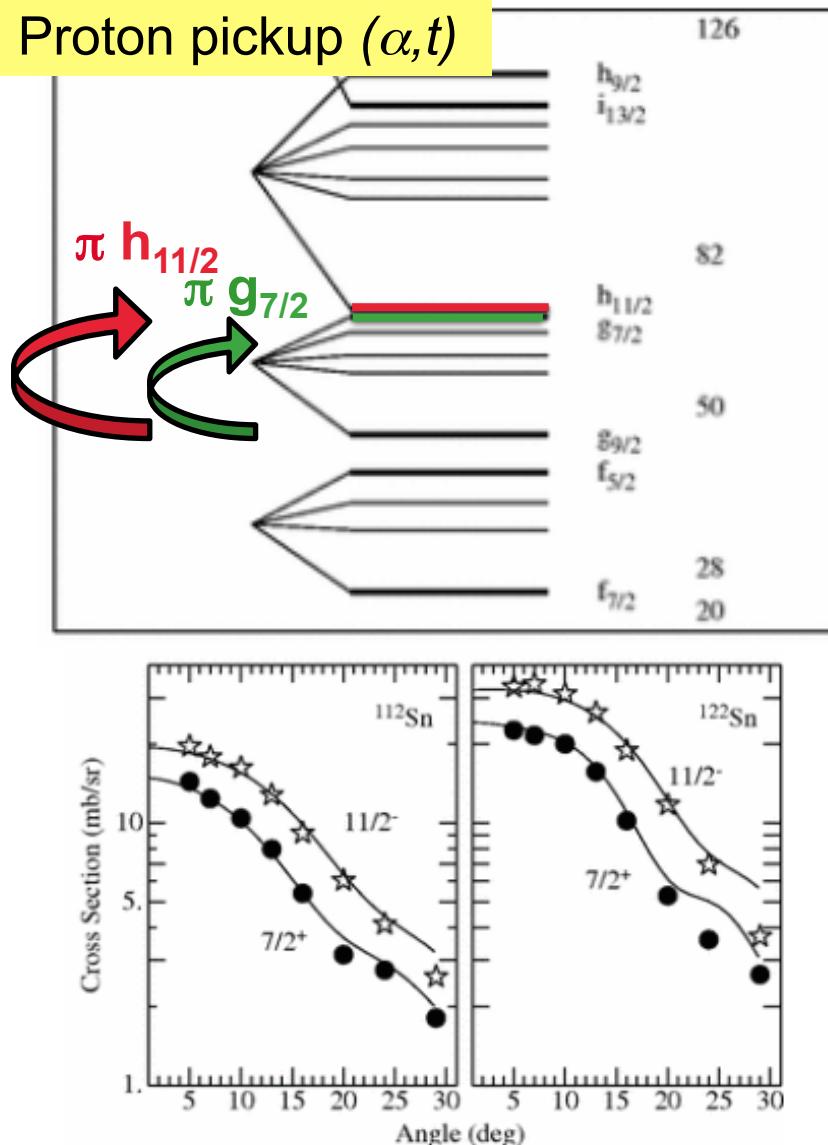
R.B. Wiringa *et al.*, PRL **89** (2002)



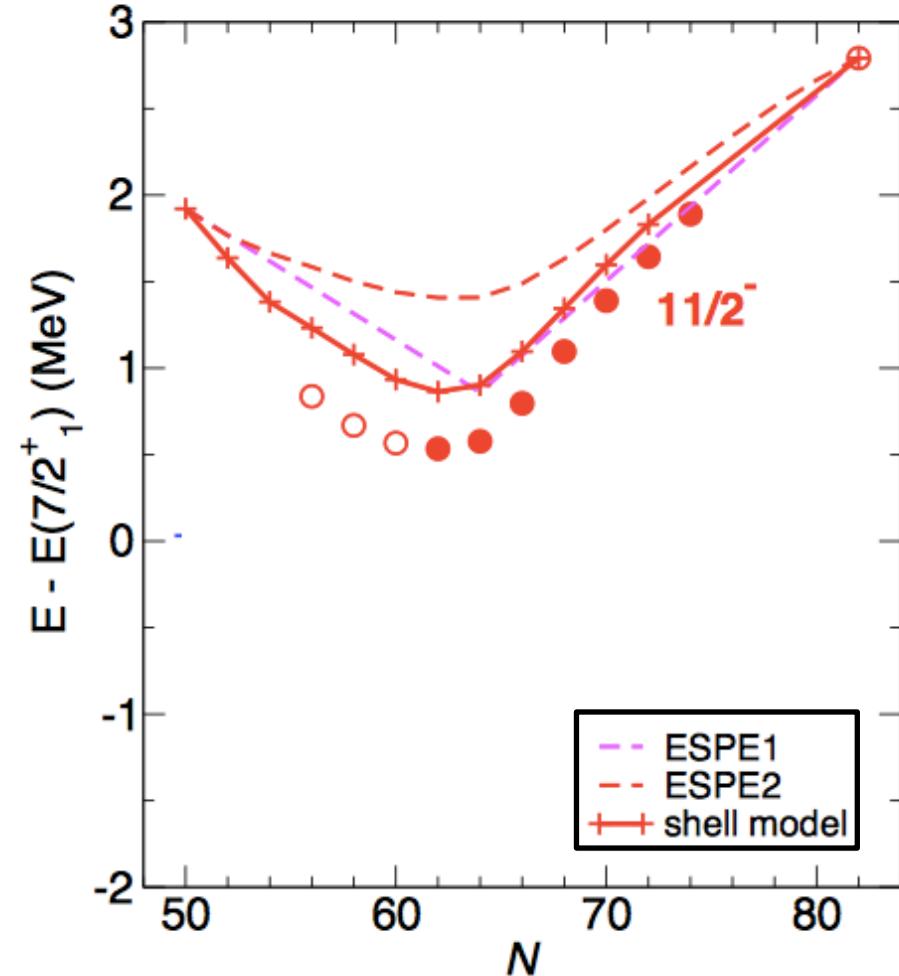
- Few-body resonances are still searched experimentally
- Transfer to the continuum active domain
  - Ex. MAGNEX collaboration in Catania, MUST2 collaboration

# Shell evolution: spin-orbit reduction

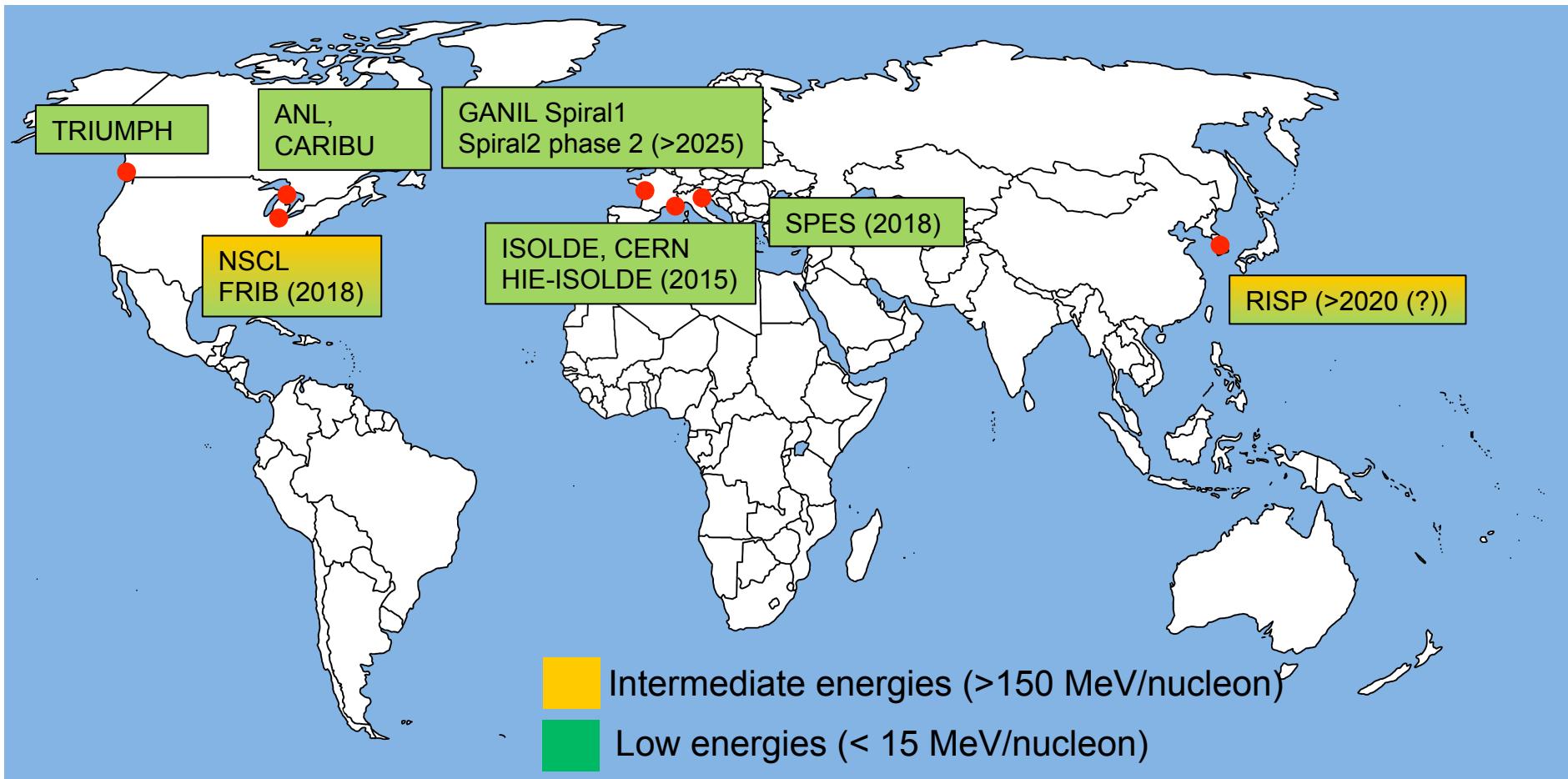
Proton pickup ( $\alpha, t$ )



Shell model calculations



# New ISOL / re-accelerated beam facilities worldwide

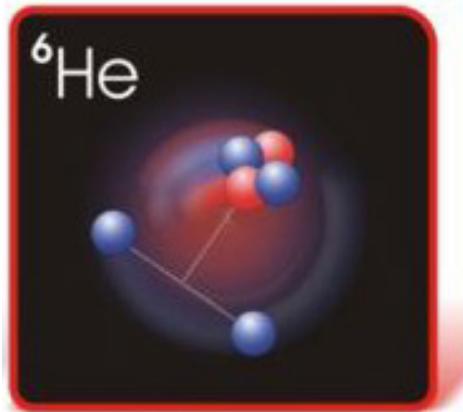
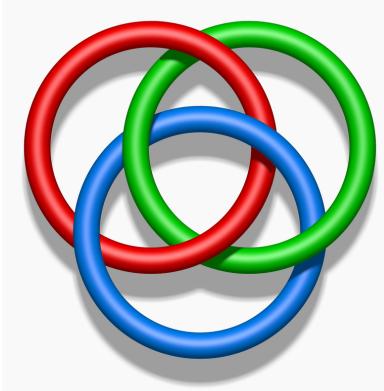


...and many associated new detector developments

See lecture by R. Raabe

# Beyond single particles : few body correlations

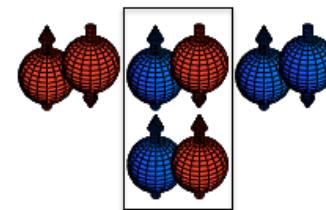
## T=1 pairing, dineutron



→ two-neutron transfer

## T=0 pairing

triplet

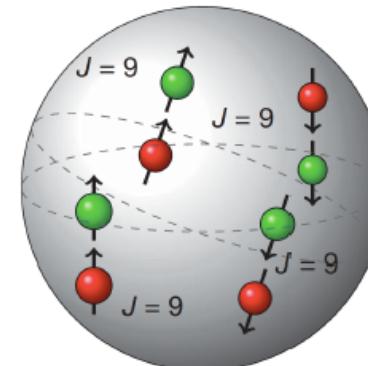


singlet

$T_z:$

nn	np	pp
+1	0	-1

Does this T=0 phase exist ?

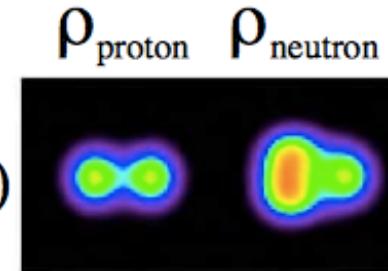


→ deuteron transfer

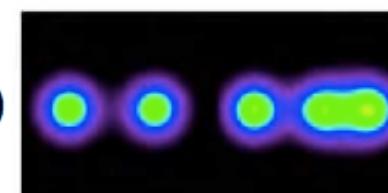
## $\alpha$ cluster states

$T=1,$

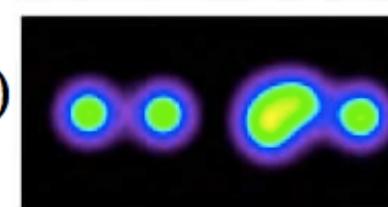
$T=0, {}^{10}\text{Be}(0_1^+)$



${}^{10}\text{Be}(0_2^+)$



${}^{10}\text{Be}(1_1^-)$



→  $\alpha$  cluster transfer

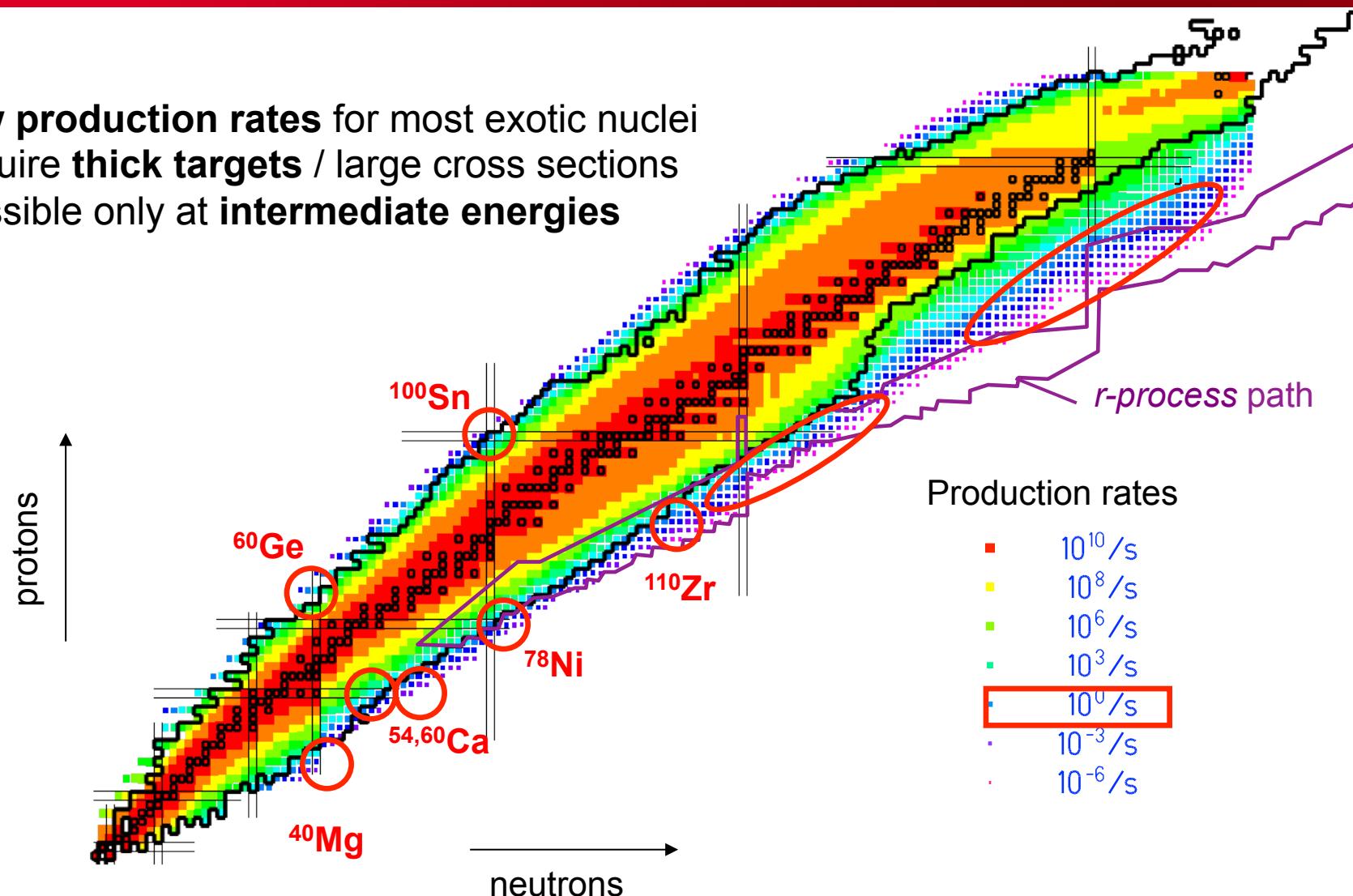
... small cross sections and complex analysis compared to one-nucleon transfer

# Outline

- **Elastic and inelastic scattering**
- **Nucleon transfer**
  - sensitivity to the shell model / spectroscopic factors
  - the Distorted-Wave Born Approximation (DWBA)
  - achievements with exotic nuclei
  - correlations from two nucleon transfer
- **Knockout reactions**
  - S-matrix theory and eikonal approximation
  - Nuclear structure from knockout & in-beam  $\gamma$  spectroscopy
  - Absolute SF: transfer versus knockout
  - Quasifree scattering
- **Future developments and probes**

# Shell evolution: far away from stability

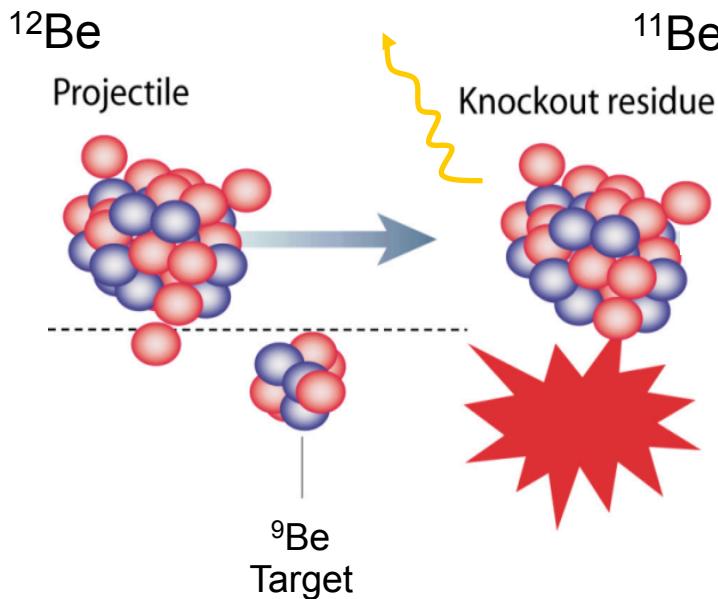
- low production rates for most exotic nuclei
- require thick targets / large cross sections
- possible only at intermediate energies



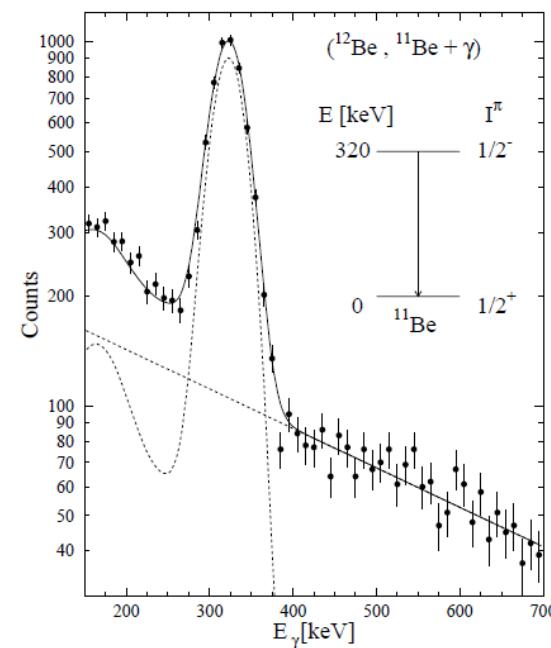
# Inclusive knockout reactions

**Inclusive** = detection of the projectile-like residue  
 [what happens to the removed nucleon or target is unknown]

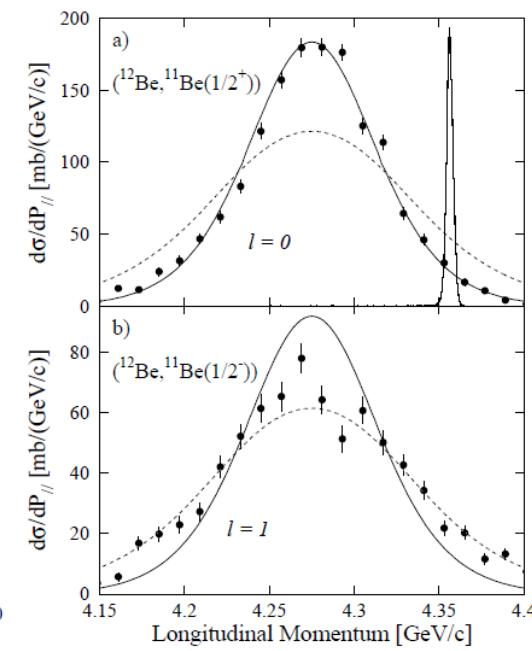
**In-beam gamma spectroscopy** to tag final states (« *exclusive* » cross sections)



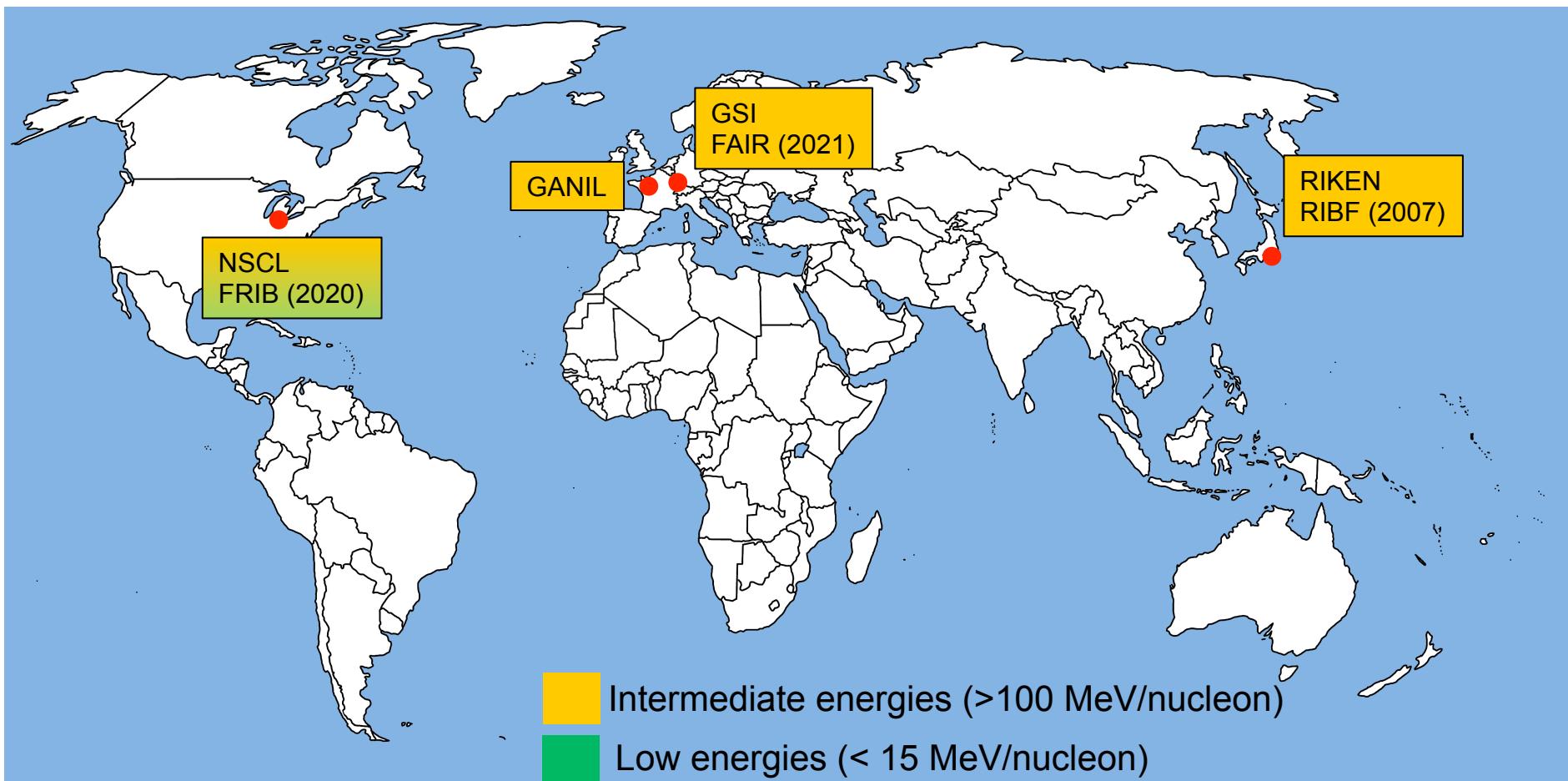
2000 pps  
 80 MeV/nucleon, NSCL



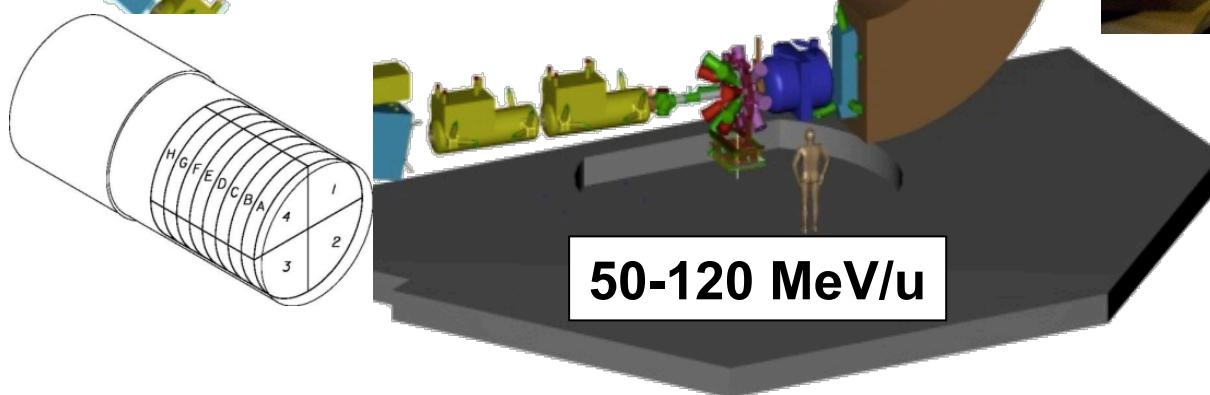
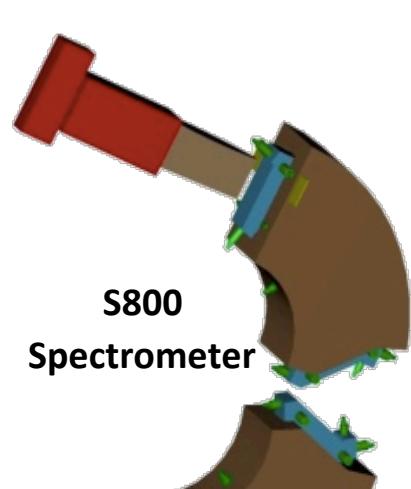
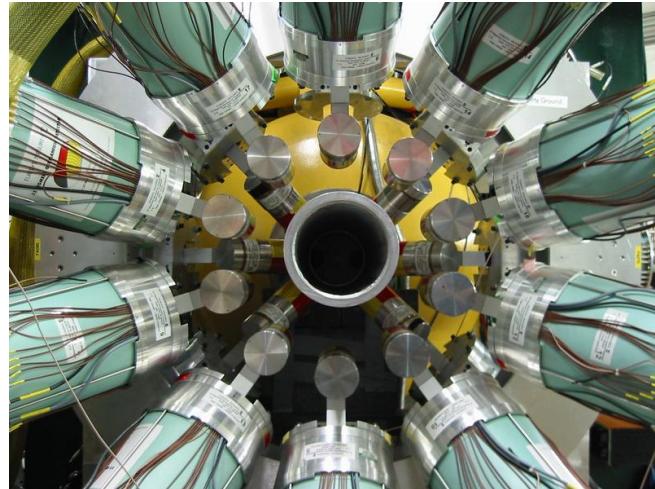
A. Navin *et al.*, PRL 85 (2000)



# Leading fragmentation RIB facilities in the world



# Example of setup: SeGA/GRETINA + S800 @ NSCL



**GRETINA=** US Ge array  
new generation / tracking  
(like AGATA in Europe)

**SeGa**=18 HPGe detectors

- Resolution=2-4% @ 1 MeV  $\beta=0.4$
- $\epsilon=2.5\%$  @ 1 MeV and  $\beta=0.4$

**GRETINA=Greta/4@MSU (2013-2014):**

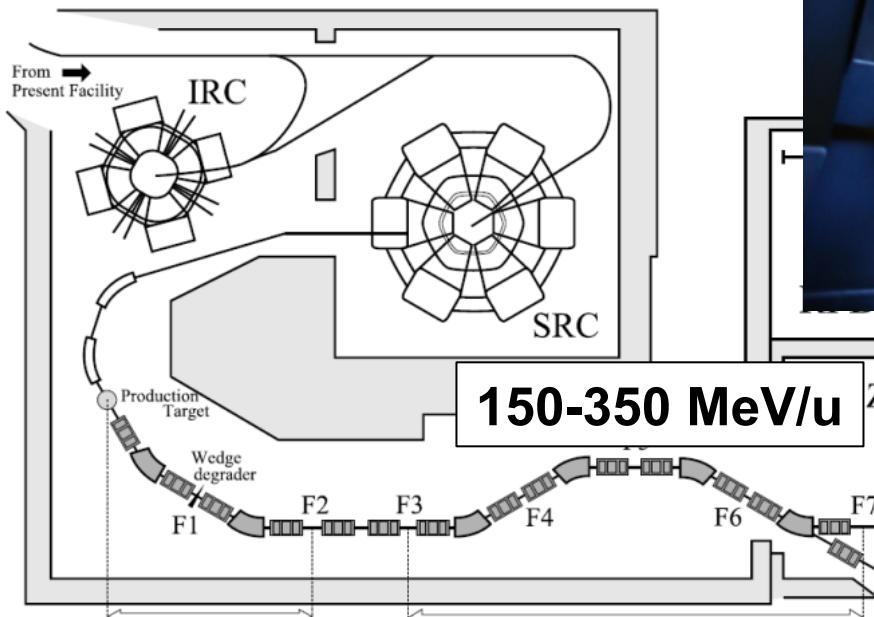
7 quadruplets x 4 HPGe crystals

- Resolution 1% FWHM @ 1 MeV and  $\beta=0.4$
- $\epsilon=9\%$  @ 1 MeV and  $\beta=0.4$

# Another experimental setup: DALI2 @ RIBF

DALI2=186 NaI(Tl) crystals

- Resolution=10% @ 1 MeV  $\beta=0.6$
- $\varepsilon=20\%$  @ 1 MeV and  $\beta=0.6$

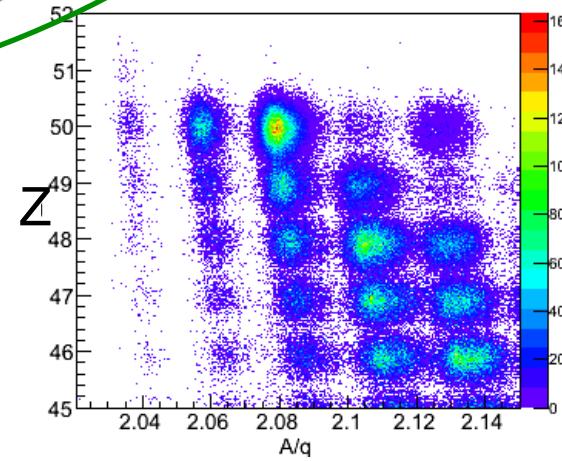


T. Takeuchi *et al.*, Nucl. Instr. Meth. A **763** (2014)



**ZeroDegree Spectrometer**

- Momentum acceptance:  $\pm 3\%$
- High resolution:  $P/DP \approx 6000$



# Eikonal approximation, S matrix and knockout

$$\psi(\vec{r}) = s(\vec{r}) e^{i\vec{k} \cdot \vec{r}}$$

$$\text{and } S(\vec{r}) = e^{-i\frac{\mu}{\hbar^2 k} \int_{-\infty}^z U(\sqrt{b^2 + z'^2}) dz'}$$

**Eikonal approximation: straight line**

with  $b = r_\perp$

## Single-particle cross section

$$\sigma_{sp}(n\ell j) = \sigma_{sp}^{strip}(n\ell j)$$

## Stripping cross section (the target is excited)

$$\sigma^{strip} = 2\pi \int_0^\infty b db \int d^3r \left| \phi_{n\ell j}(\vec{r}) \right|^2 \left| S_{core}(\vec{b}_c) \right|^2 (1 - \left| S_{nucl}(\vec{b}_n) \right|^2)$$

↑                      ↑  
Core « survives » × Nucleon « adsorbed »

# Eikonal approximation, S matrix and knockout

$$\psi(\vec{r}) = s(\vec{r}) e^{i\vec{k} \cdot \vec{r}}$$

and  $S(\vec{r}) = e^{-\frac{i\mu}{\hbar^2 k} \int_{-\infty}^z U(\sqrt{b^2 + z'^2}) dz'}$

**Eikonal approximation: straight line**

## Single-particle cross section

$$\sigma_{sp}(n\ell j) = \sigma_{sp}^{strip}(n\ell j) + \sigma_{sp}^{diff}(n\ell j)$$

## Stripping cross section (the target is excited)

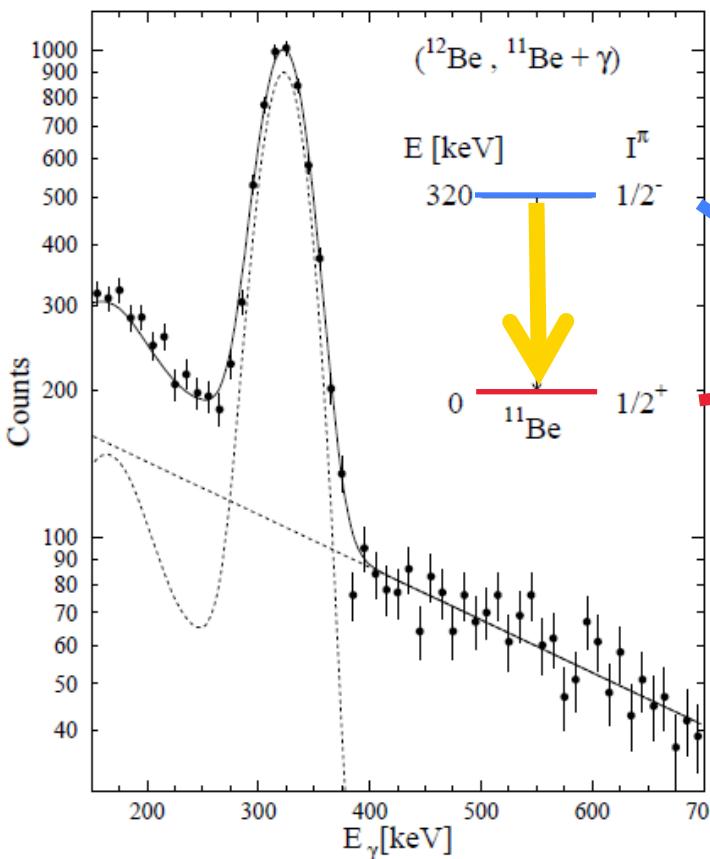
$$\sigma^{strip} = 2\pi \int_0^\infty b db \int d^3 r \left| \phi_{n\ell j}(\vec{r}) \right|^2 \left| S_{core}(\vec{b}_c) \right|^2 (1 - \left| S_{nucl}(\vec{b}_n) \right|^2)$$

↑                      ↑  
Core « survives » × Nucleon « adsorbed »

## Diffractive cross section (the target remains in its ground state)

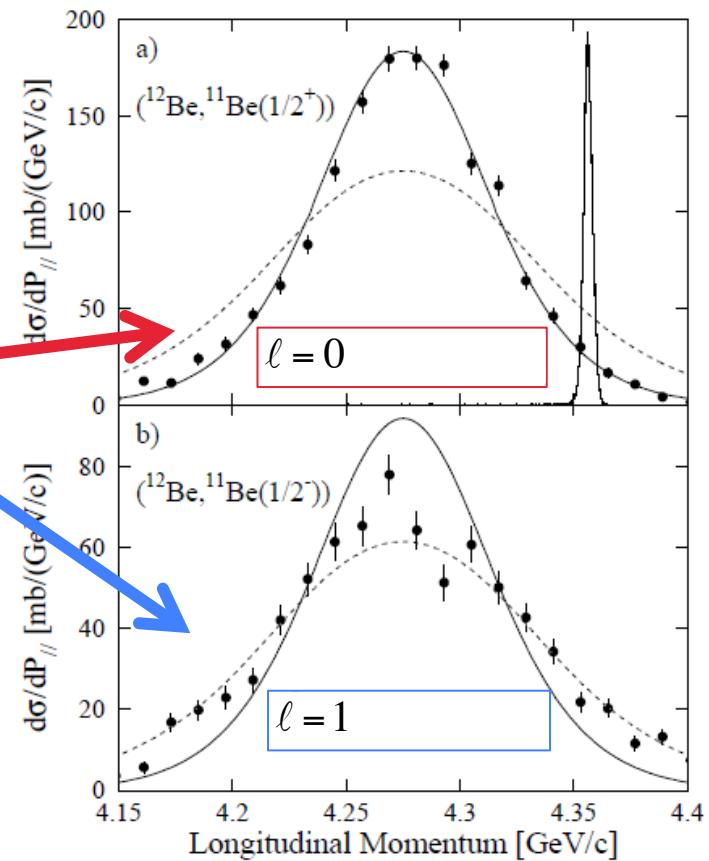
$$\sigma_{diff} = 2\pi \int b db \left\langle \phi_0 \left| S_{core} S_{nucl} \right|^2 \phi_0 \right\rangle - \left| \left\langle \phi_0 \left| S_{core} S_{nucl} \right| \phi_0 \right\rangle \right|^2$$

# Breakdown of the N=8 shell closure

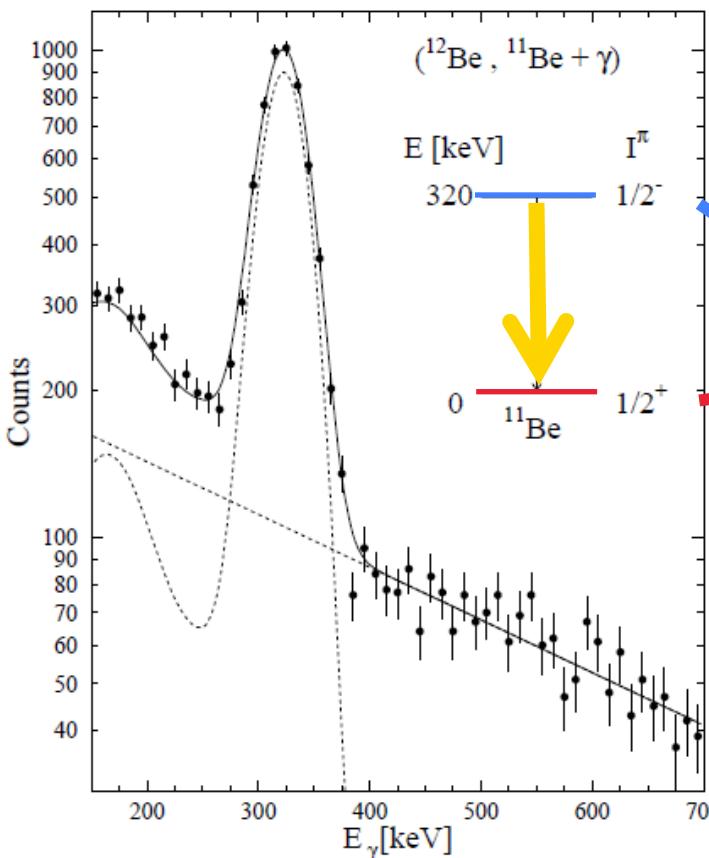


$$\sigma_{1/2^+} = 32(5) \text{ mb}$$

$$\sigma_{1/2^-} = 17(3) \text{ mb}$$

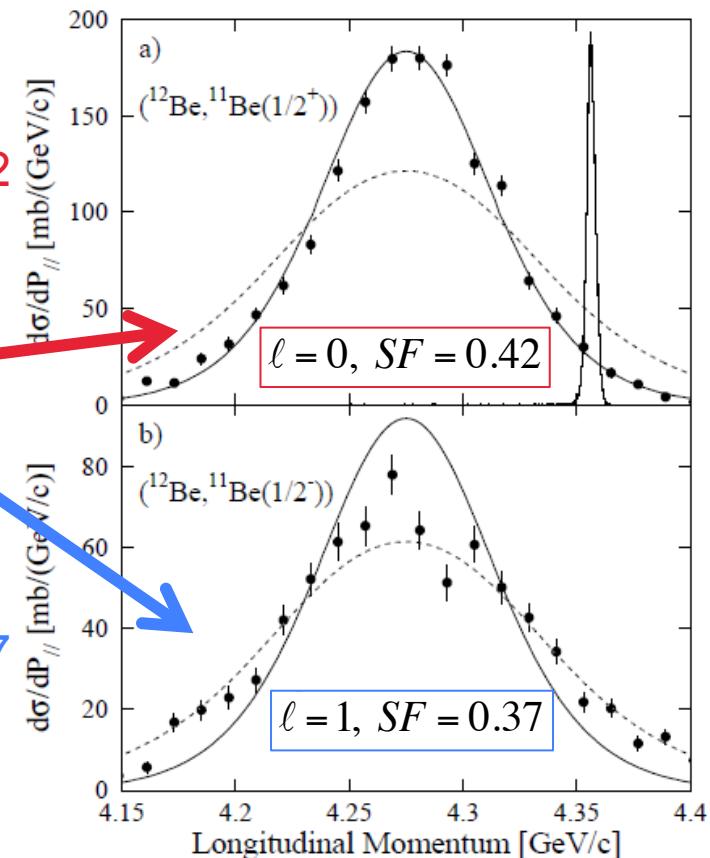


# Breakdown of the N=8 shell closure

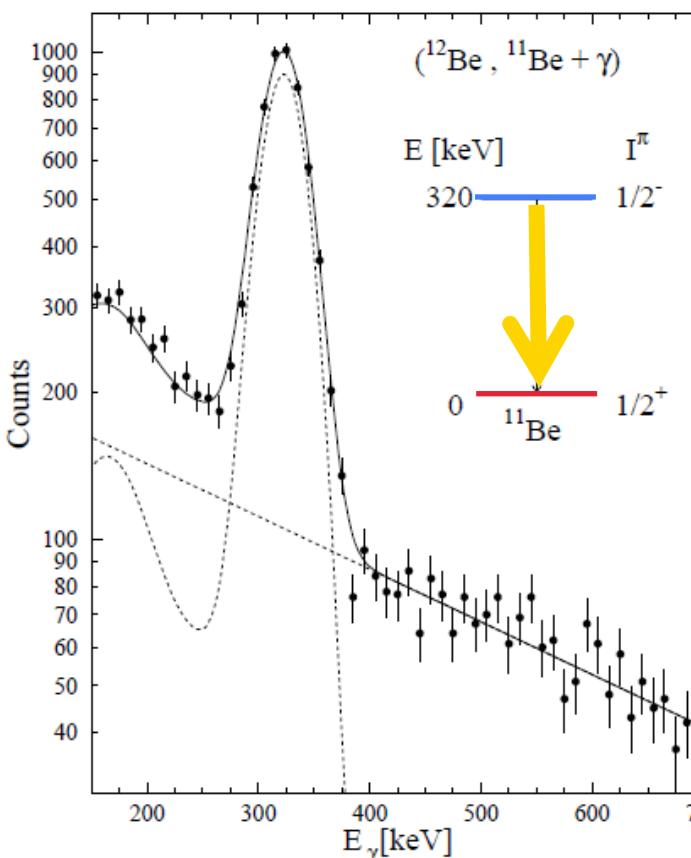
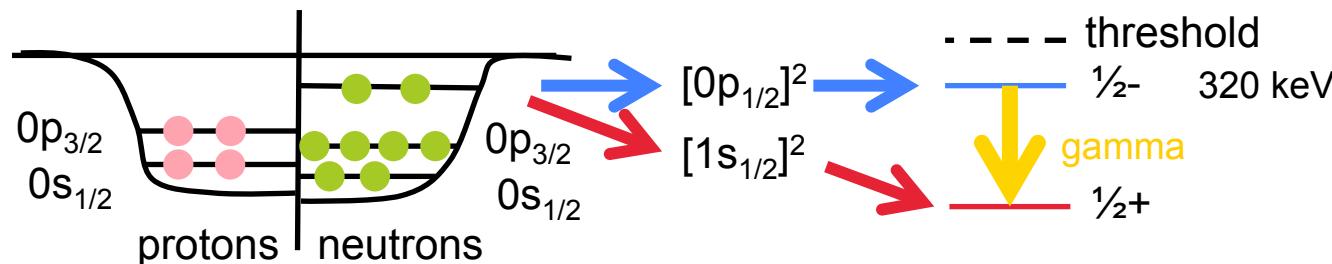


$$\begin{aligned} \sigma_{1/2+} &= 32(5) \text{ mb} \\ \sigma_{\text{eik}}(l=0) &= 76 \text{ mb} \\ \rightarrow SF &= 32/76 = 0.42 \end{aligned}$$

$$\begin{aligned} \sigma_{1/2-} &= 17(3) \text{ mb} \\ \sigma_{\text{eik}}(l=1) &= 47 \text{ mb} \\ \rightarrow SF &= 17/47 = 0.37 \end{aligned}$$

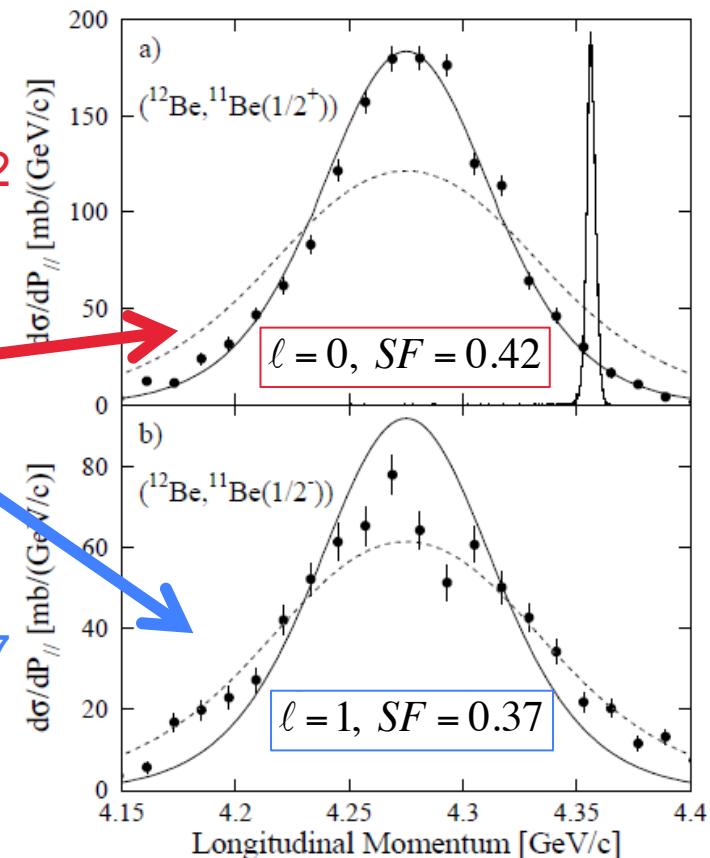


# Breakdown of the N=8 shell closure



$$\begin{aligned} \sigma_{1/2^+} &= 32(5) \text{ mb} \\ \sigma_{\text{eik}}(l=0) &= 76 \text{ mb} \\ \rightarrow SF &= 32/75 = 0.42 \end{aligned}$$

$$\begin{aligned} \sigma_{1/2^-} &= 17(3) \text{ mb} \\ \sigma_{\text{eik}}(l=1) &= 47 \text{ mb} \\ \rightarrow SF &= 17/47 = 0.37 \end{aligned}$$

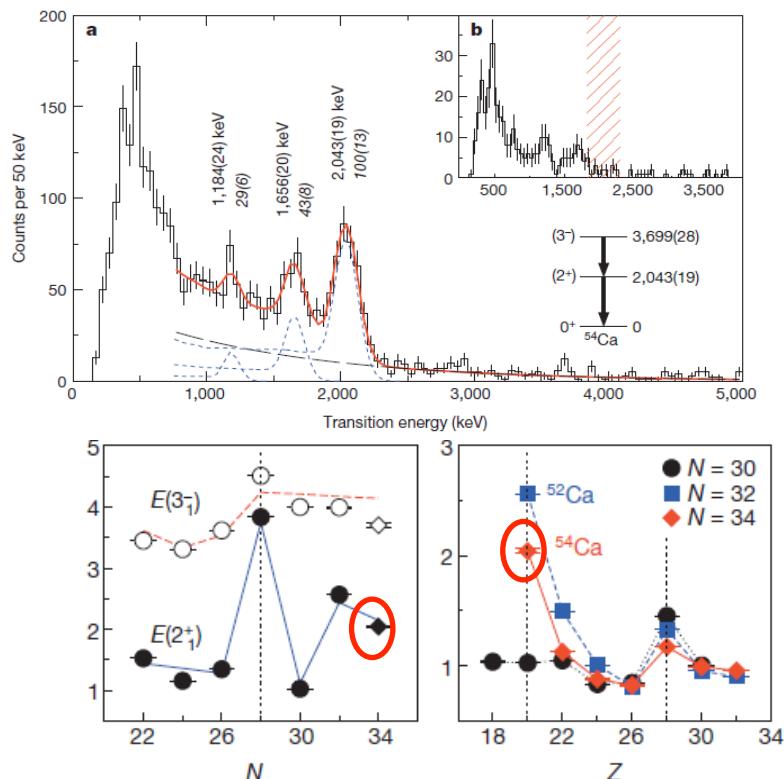


# The N=34 new magic number

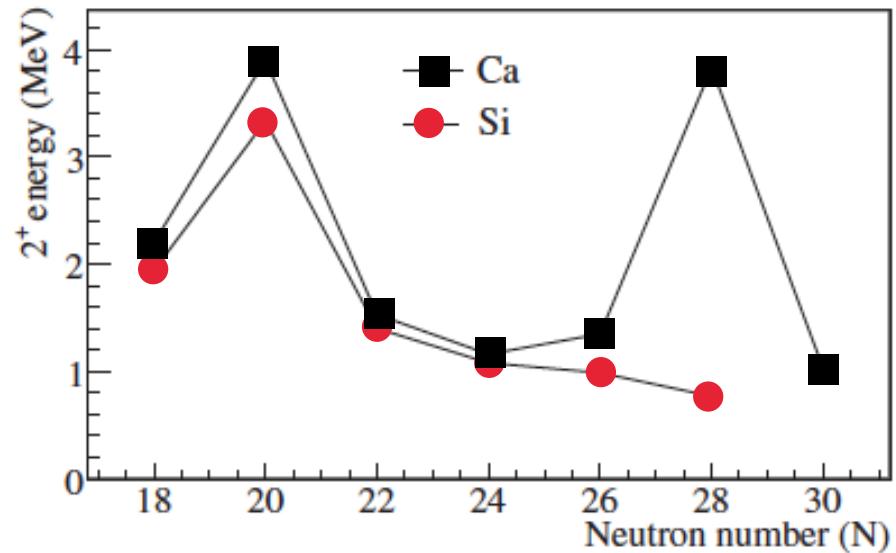
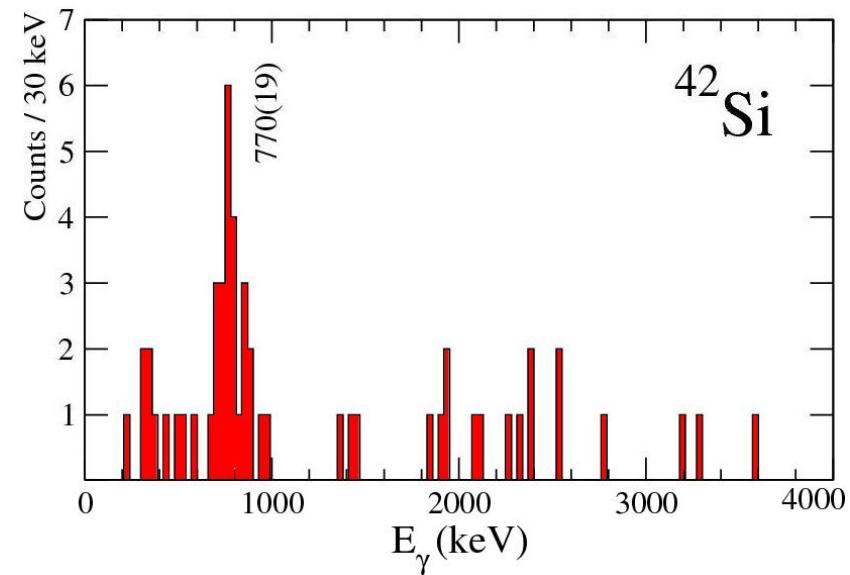
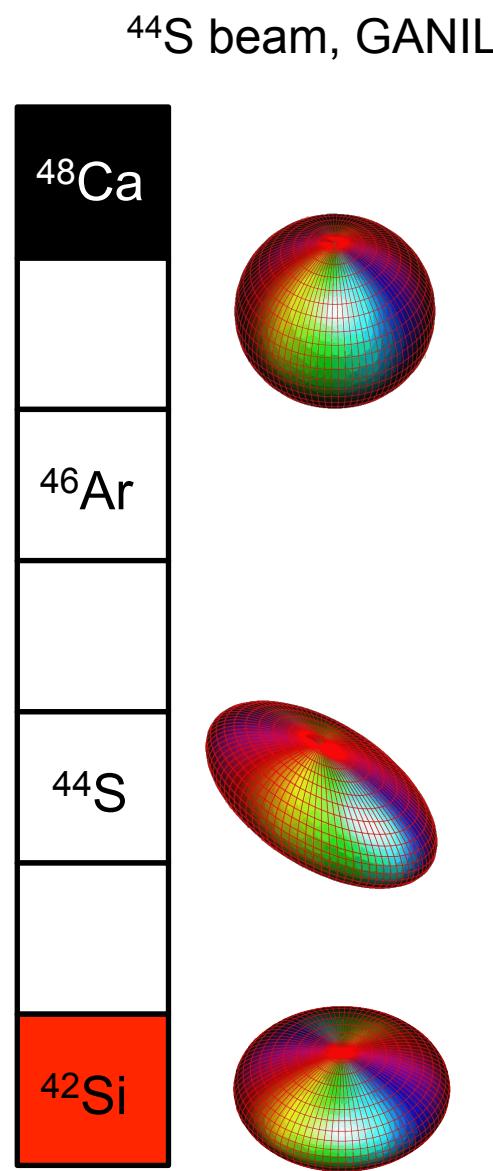
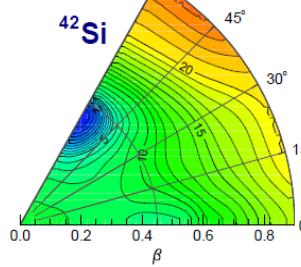
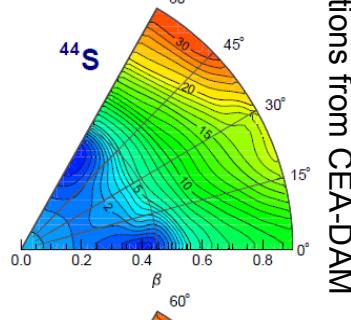
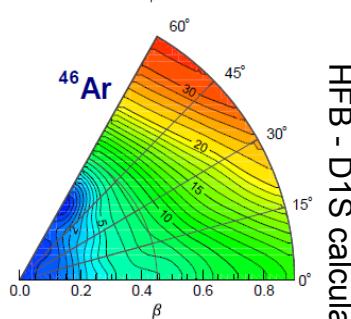
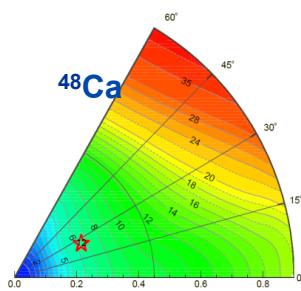
D. Steffenbeck *et al.*, Nature 502 (2013)

$^{70}\text{Zn}$  primary beam (100 pnA max)  
 $^{56}\text{Ti}$  120 pps/pnA,  $^{55}\text{Sc}$  12 pps/pnA

$^{54}\text{Ca}$  produced by one, two proton knockout:  
 $^{56}\text{Ti}, 55\text{Sc} + \text{Be} \rightarrow ^{54}\text{Ca} + X$



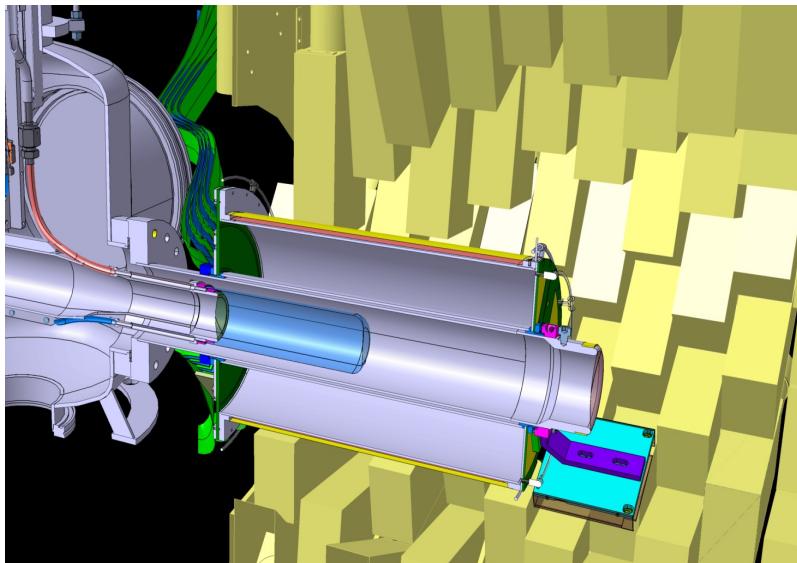
# Collapse of the N=28 shell closure in $^{42}\text{Si}$



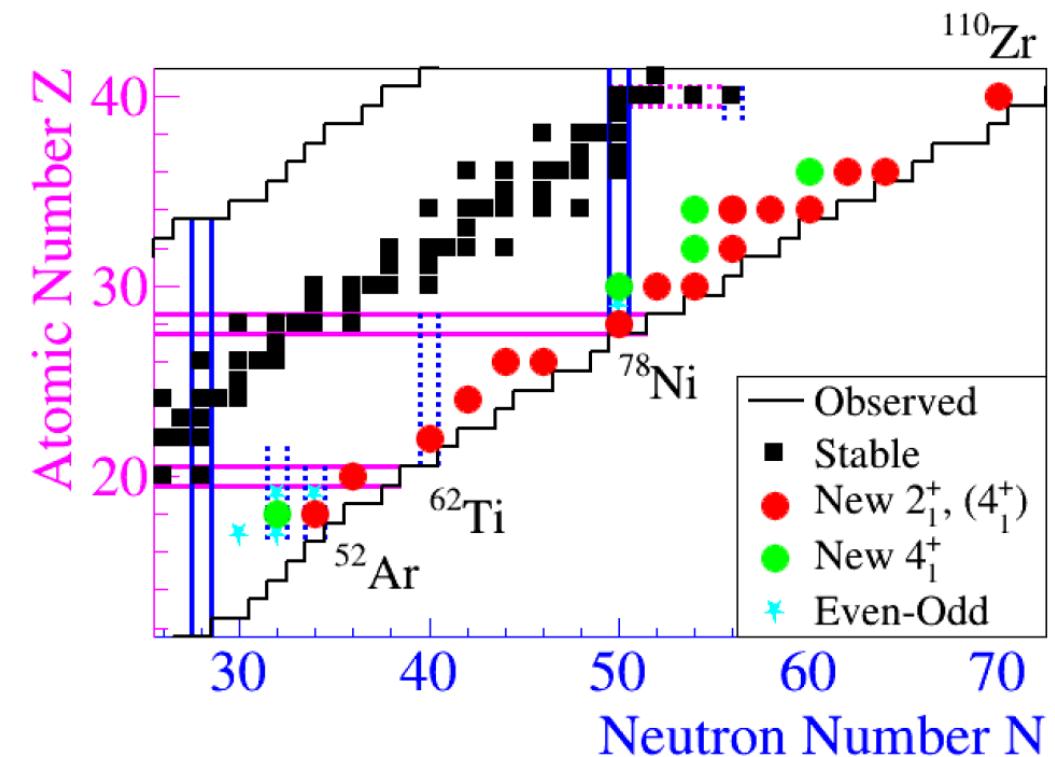
# The SEASTAR program at the RIBF

Seastar: Shell Evolution and Search for Two-plus energies At the RIBF

Setup composed of DALI2 scintillator array + MINOS (thick H<sub>2</sub> target and Vertex tracker)  
First experiments in **2014** and **2015**

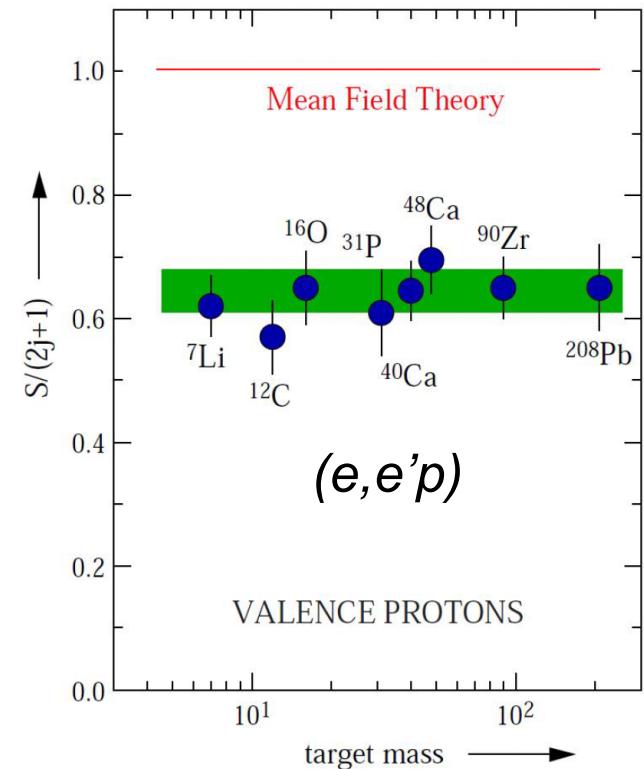
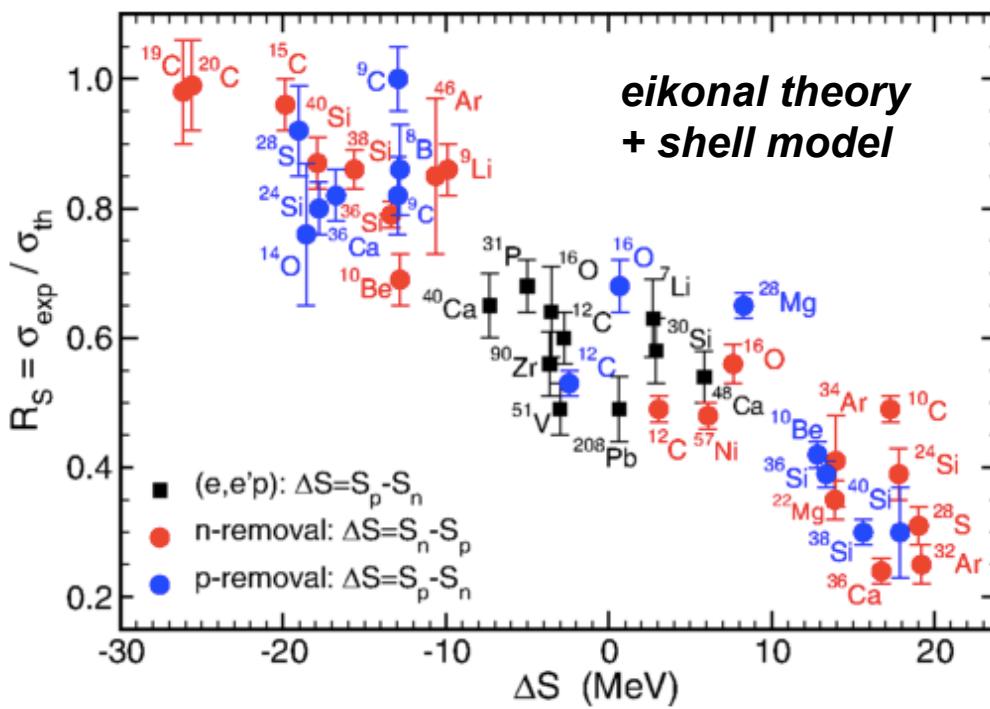


MINOS: AO *et al.*, EPJA **50** (2014)



# Stripping cross sections: eikonal versus data

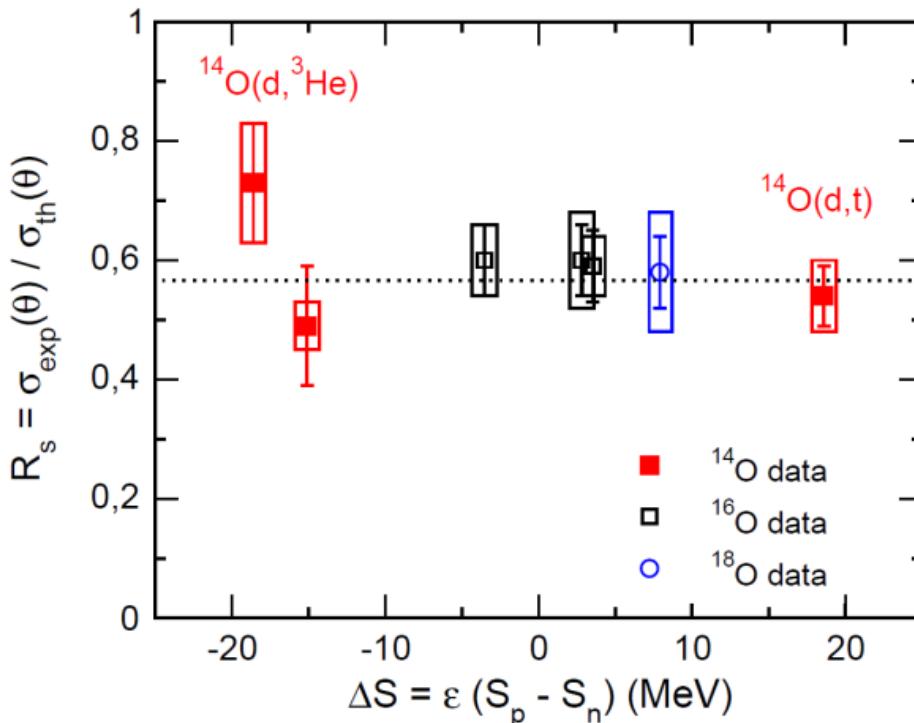
A. Gade *et al.*, Phys. Rev. C **77** (2008)  
J.A. Tostevin and A. Gade, Phys. Rev. C **90** (2014)



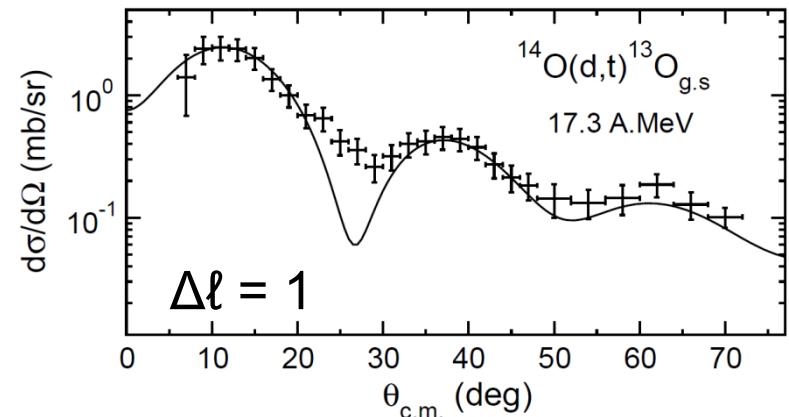
**Intermediate-energy knockout**  
**Disagreement** between theory and experiment

# Comparing heavy-ion induced knockout and transfer

$^{14}\text{O}(\text{d},\text{t})$ ,  $(\text{d},{}^3\text{He})$  and elastic scattering, 19 MeV/nucleon, SPIRAL (GANIL)  $\Delta S \sim 19$  MeV



F. Flavigny *et al.*, Phys. Rev. Lett. **110** (2013).

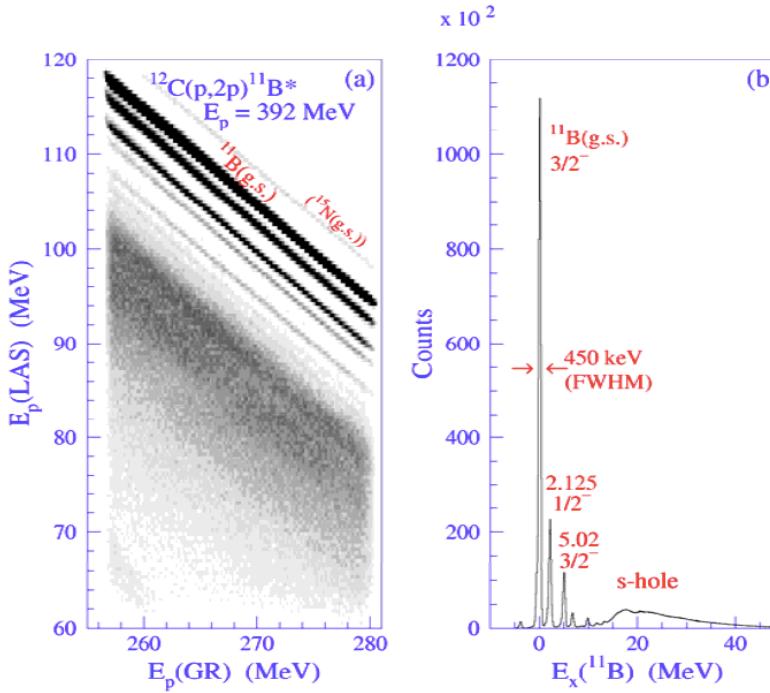


Coupled channel analysis

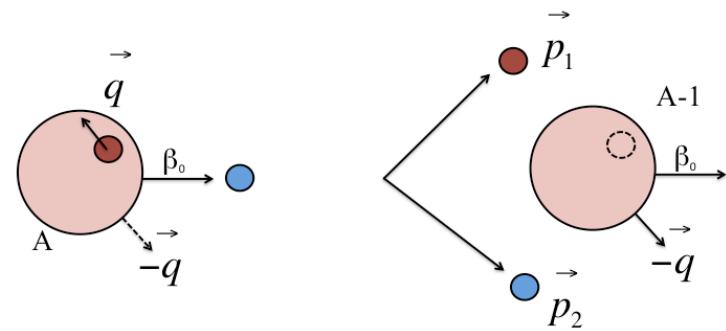
## Conclusions

- weak  $\Delta S$  dependence
- Disagreement between intermediate-energy nucleon removal and transfer analysis
- *Ab initio* calculations in agreement with transfer

# Proton-induced quasifree scattering



Direct kinematics  $^{12}\text{C}(p,2p)^{12}\text{C}$ , RCNP (Japan)



## Distorted Wave Impulse Approximation

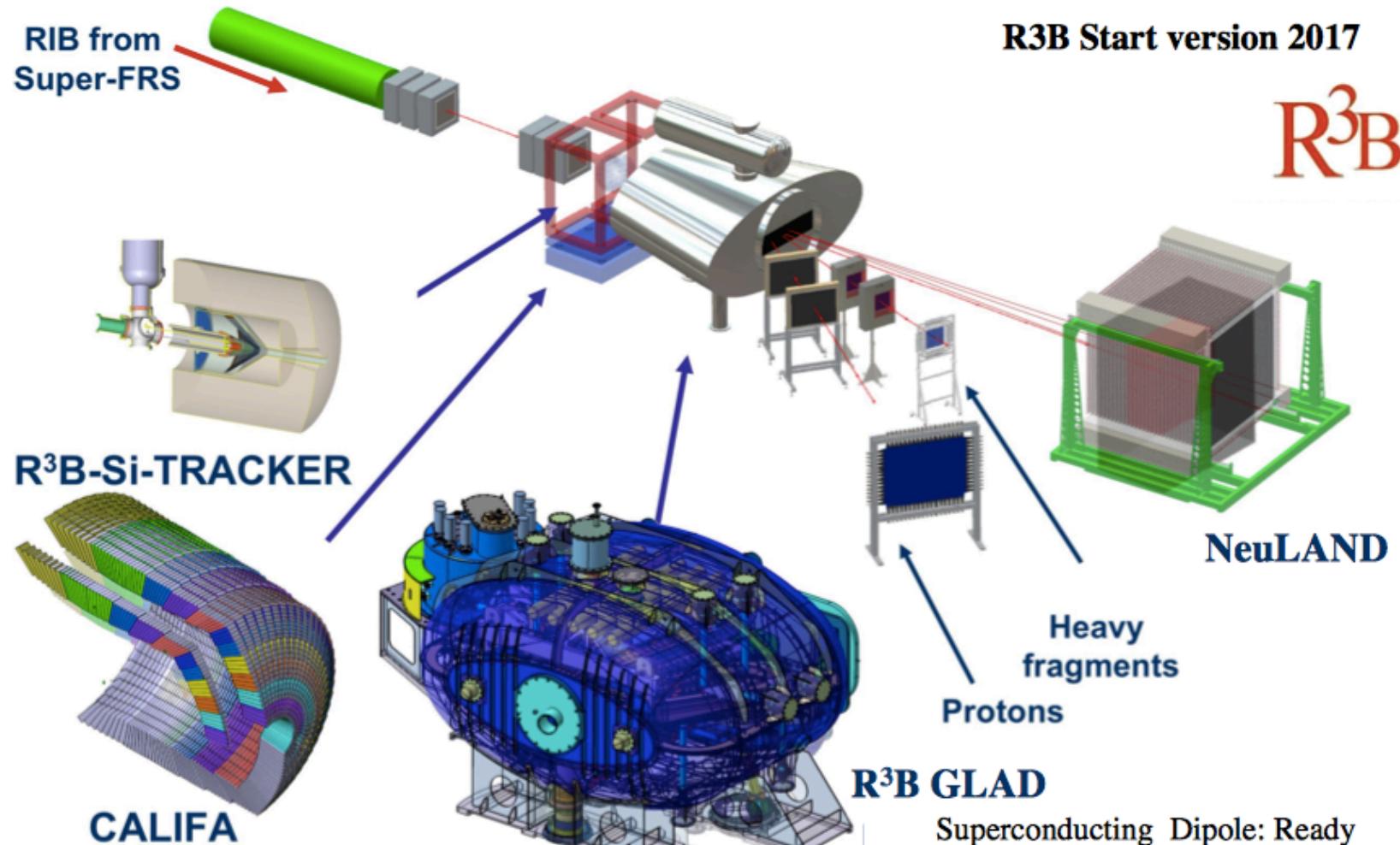
$$T_{p,pN} = \sqrt{S_{n\ell j}} \left\langle \chi_{k'_p}^{(-)} \chi_{k_N}^{(-)} \right| \tau_{pN} \left| \chi_{k_p}^{(+)} \phi_{n\ell j} \right\rangle$$

Recent work:

T. Aumann, C. Bertulani, J. Ryckebusch, PRC **88** (2013)

- **(e,e'p) best spectroscopic tool** proton stripping (electromagnetic interaction)
- large momentum transfer: minimize final state interactions
- **(e,e'p)** = not sensitive to neutron, not possible with short-lived nuclei
  
- **(p,2p) exclusive quasifree scattering** expected to be a clean high energy probe  
In inverse kinematics: best energies from 300/nucleon to 1 GeV/nucleon

# The R3B project at GSI/FAIR



Slide taken from T. Aumann, 2014

Superconducting Dipole: Ready  
for installation in Q4/2014  
Construction by CEA Saclay

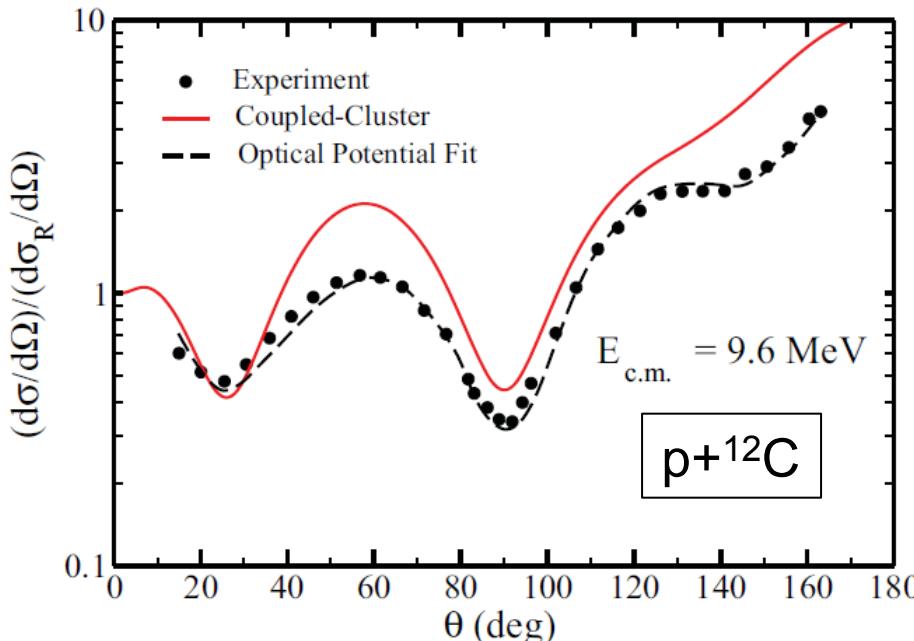
Similar setup / program at **RIBF** with the **SAMURAI** spectrometer and collaboration

# Outline

- **Elastic and inelastic scattering**
- **Nucleon transfer**
  - sensitivity to the shell model / spectroscopic factors
  - the Distorted-Wave Born Approximation (DWBA)
  - achievements with exotic nuclei
  - correlations from two nucleon transfer
- **Knockout reactions**
  - S-matrix theory and eikonal approximation
  - Nuclear structure from knockout & in-beam  $\gamma$  spectroscopy
  - Absolute SF: transfer versus knockout
  - Quasifree scattering
- **Future developments and probes**

# *Ab initio* description of reactions

*Long term objective: a fully consistent treatment of reaction and structure  
i.e. same initial Hamiltonian, parameter free and theoretical uncertainties*



G. Hagen and N. Michel, PRC **86** (2012)

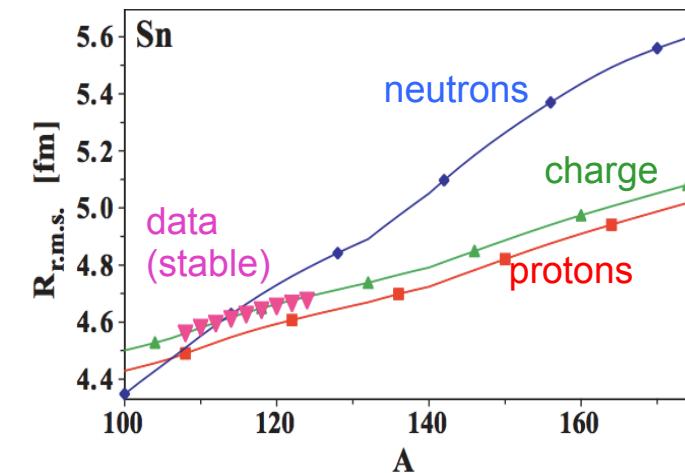
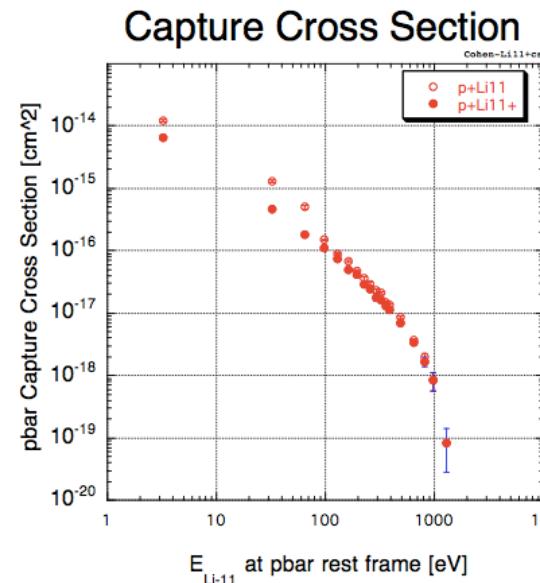
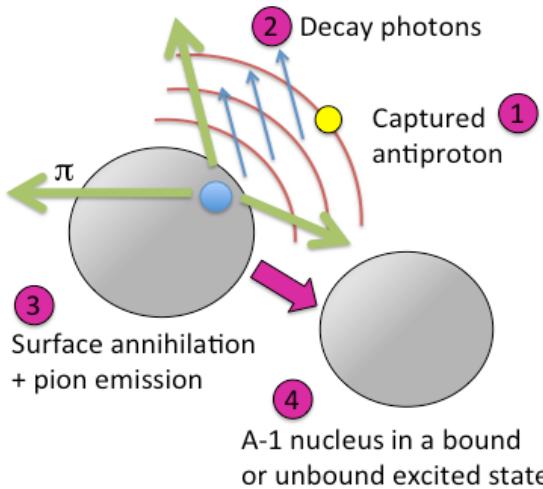
*Ingredients:*  
Coupled Cluster theory

*Two- and three body interactions  
from chiral theory*

Also :first ab initio description of low energy fusion reactions (No Core SM)  
P. Navratil and S. Quaglioni, PRL **108** (2012)

# Antiprotons annihilation from RI: neutron skins

- **antiproton annihilation** with neutrons and protons
- very high cross section at low energy (**up to Giga-barns!!!**)
- very clean probe (pure stripping) with no Coulomb barrier effect



M. Wada and Y. Yamazaki, Nucl. Instr. Meth. B **214** (2004)

**Direct measurement of surface neutron vs proton densities!**

**How to collide antiprotons and exotic nuclei?**

- 1) Bringing antiprotons to RI facilities → portable trap
- 2) Low energy collider → FLAIR@FAIR (>2030)

# ELISe at FAIR: electron – Radioactive Ion collider

## Electron – RIB collider

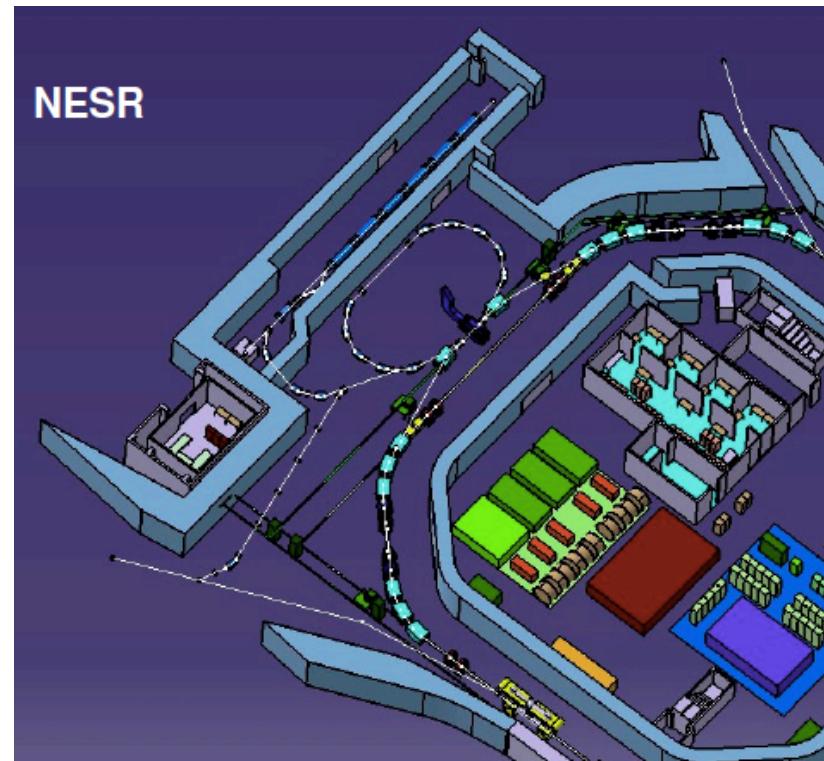
- 125-500 MeV electrons
- 200-700 MeV/u RIBs

Part of the FAIR facility (expected >2030)

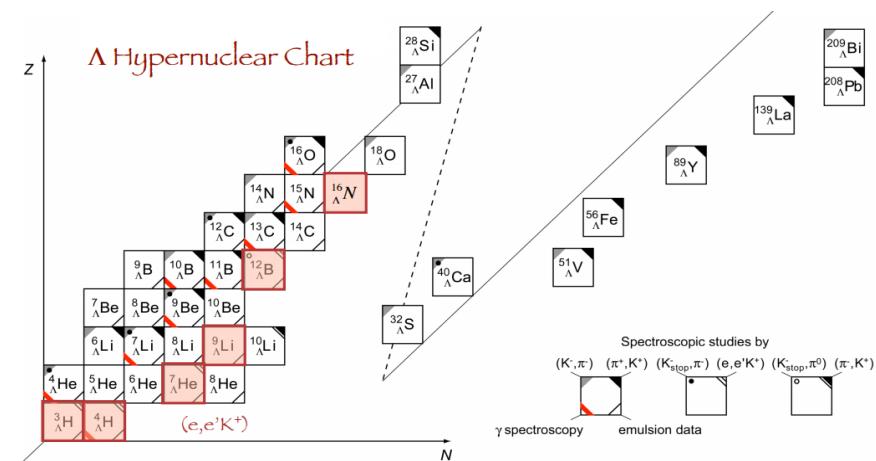
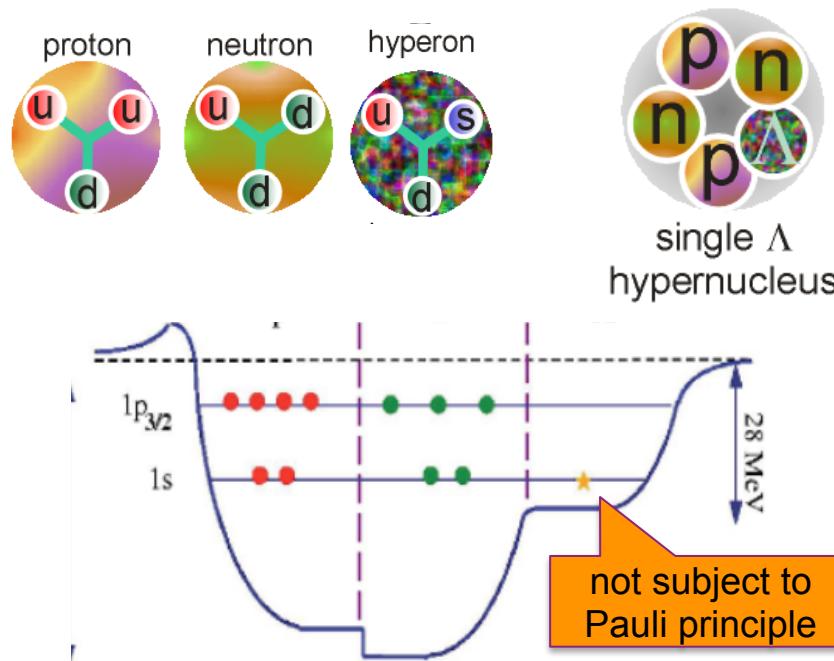
## Pure electromagnetic studies with RIBs

(luminosity  $<10^{28} \text{ cm}^2\text{s}^{-1}$  / Lorentz focusing)  
High resolution spectrometer

- charge distributions
- access to nuclear interior
- high-precision spectroscopic factors



# Neutron rich hypernuclei



**Unique probe of  $\Lambda N$  interaction**

**Today:** direct kinematics from **stable nuclei**

Hypernuclei experiments at COSY (Germany), Berkeley (USA), DAPHNE (Italy), J-PARC (Japan), JLAB (USA), GSI (Germany)....

**Tomorrow:** **Neutron-rich hypernuclei**

Existing program at GSI/FAIR (HyPHI, T. Saito, GSI)

New opportunity of production from direct reaction:  ${}^A_X + p \rightarrow {}^A_\Lambda X$

# Summary

- Elastic, inelastic, transfer, knockout and quasi-free scattering
- Unique probes for **quantum nuclear effects in Exotic Nuclei**:
  - ✓ Nuclear size and density distributions (elastic/inelastic scattering)
  - ✓ Nuclear collectivity (neutron vs protons, compression modes (GMR), ...)
  - ✓ Shell evolution with isospin
  - ✓ Short range correlations
  - ✓ Pairing correlations ( $T=1$ ,  $T=0$ )
  - ✓ Shape / configuration coexistence
- Importance of **hydrogen**-induced and exclusive reactions  
(simplest and cleanest hadronic probe among all)
- Large prospects and **detection developments** in view of new/recent RIB machines  
Ex. RIBF (Japan), FAIR, HIE-ISOLDE, SPES, SPIRAL2 (Europe) and FRIB (US)
- **Many new prospects**:  
ex. Fully consistent theory, p-bar annihilation, electron-RI collider, neutron-rich hypernuclei,...

# So more to say about direct reactions...

- Charge exchange reactions
- proton-neutron pairing and cluster states from transfer reactions
- two-nucleon correlations via knockout
- cluster components from alpha quasifree scattering
- Quantum decoherence from elastic scattering and coupling to the continuum
- Proton versus neutron collectivity from inelastic scattering
- Short range correlations by high energy transfer (momentum matching)
- Many experimental recent highlights with exotic nuclei
- Progresses of theory beyond DWBA (coupled channels)
- ...

# References to go further

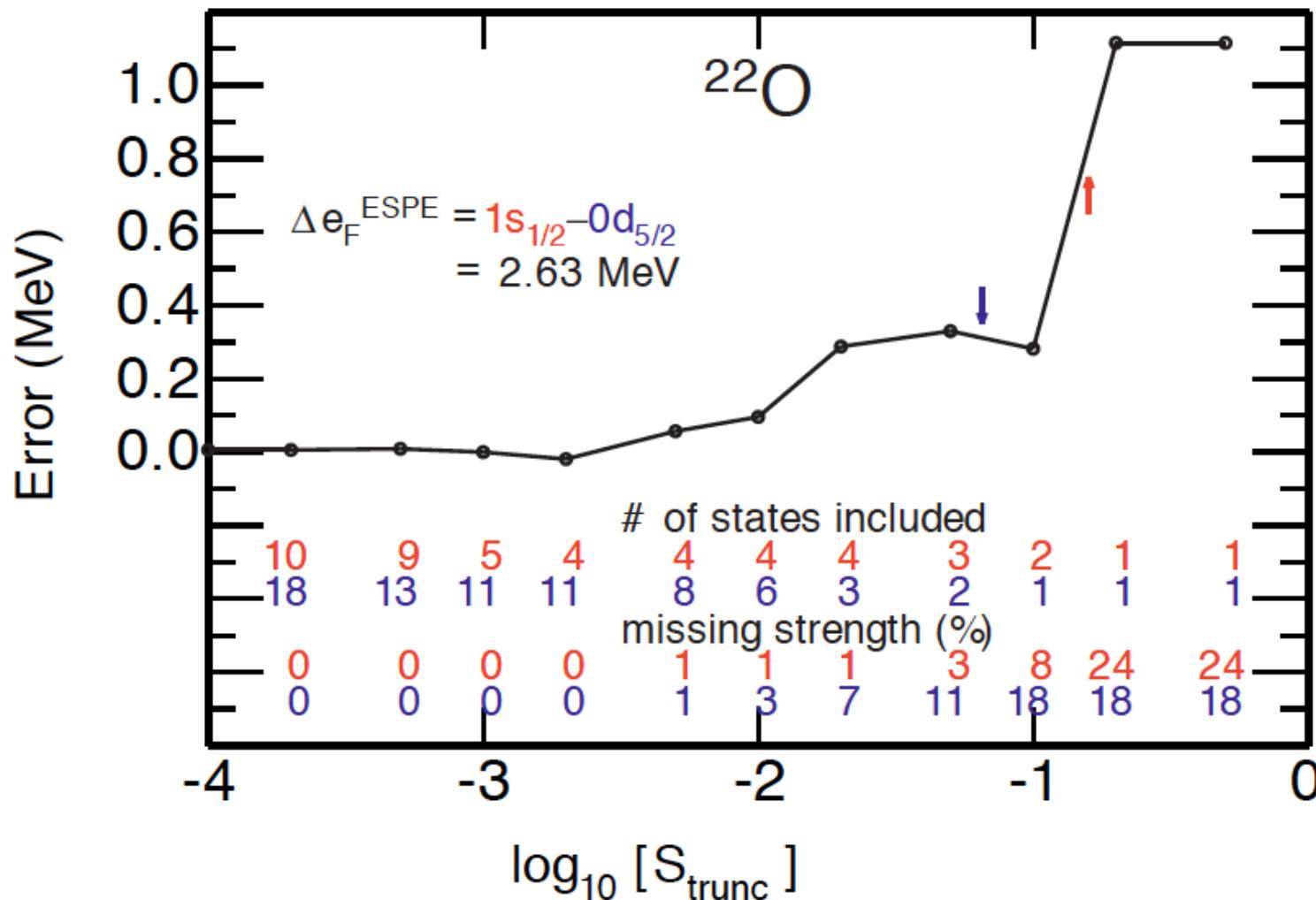
- **NR**, D. F. Jackson, Methuen edition (1970)
- **Introduction to NR**, G.R. Satchler, Mc Millan press (1980)
- **Direct NR**, N. K. Glendenning, World Scientific (1983)
- **Introduction to NR**, C. A. Bertulani and P. Danielewicz, IoP (2004)
- **NR for Astrophysics**, I. J. Thompson and F. M. Nunes, Cambridge (2009)

NR = Nuclear Reactions

Few backup slides

# Importance of most “all” states to extract shell gaps

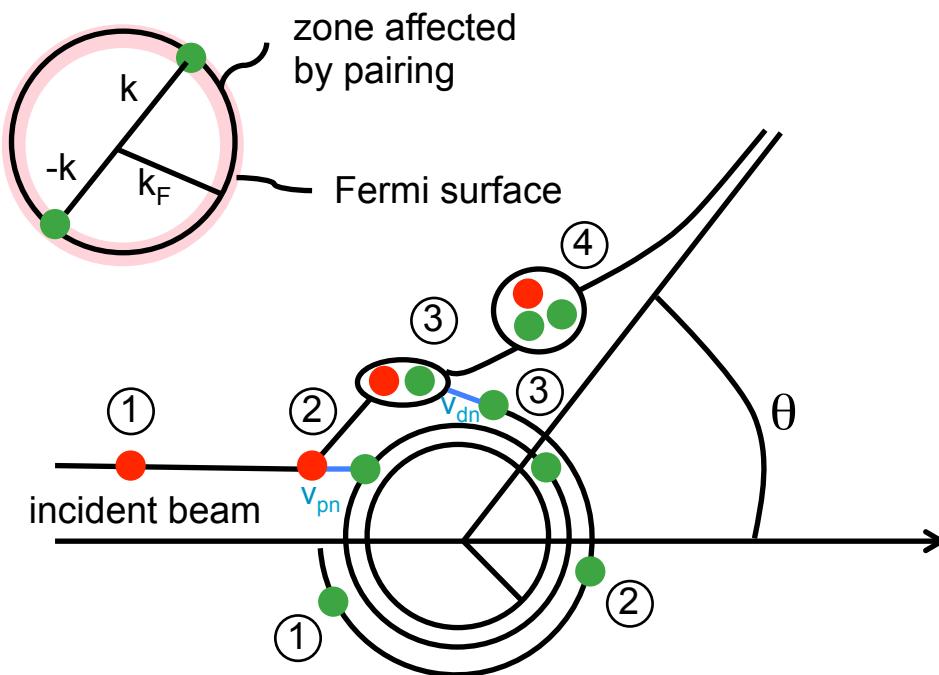
$^{22}\text{O}(\text{d},\text{p})^{23}\text{O}$  : a theoretical study by A. Signoracci, T. Duguet



# Two-nucleon transfer: a probe for pairing correlations

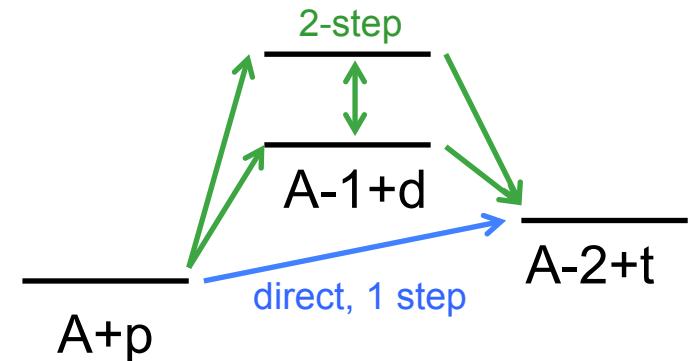
Ex. (p,t), (t,p), ( $^{12}\text{C}$ ,  $^{14}\text{C}$ ), ...

two-nucleon transfer probes  
**spatial, momentum, spin correlations**

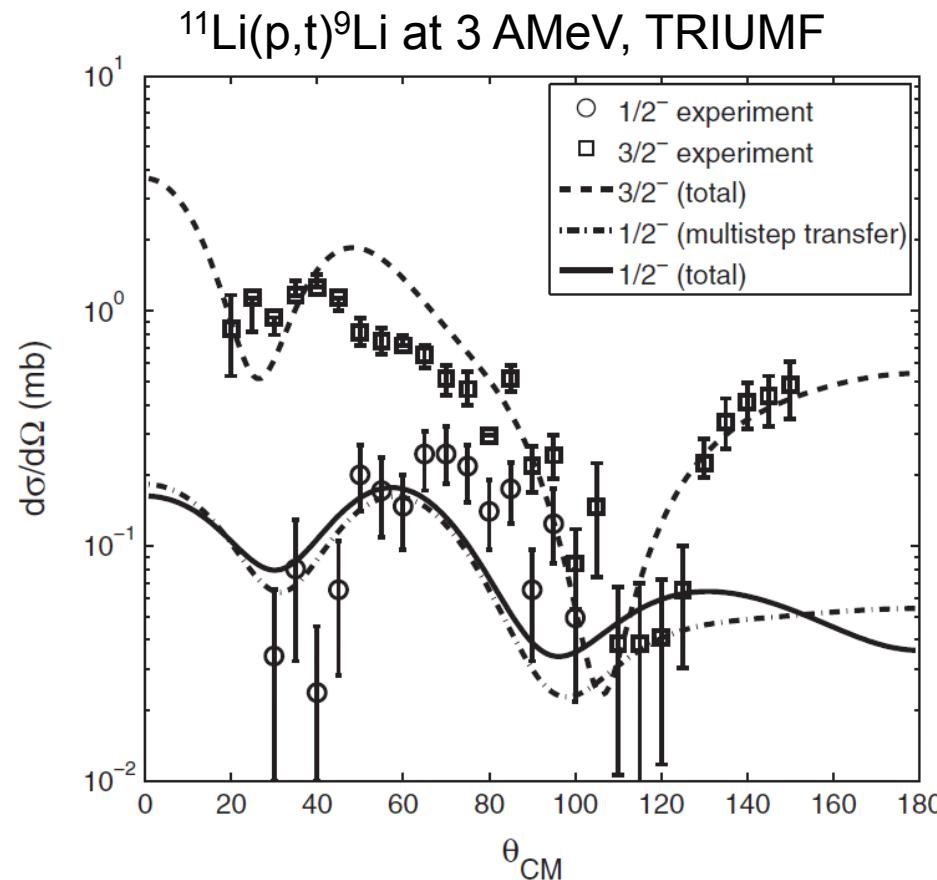


- depends on **correlations functions**  

$$\langle \Phi_{A-2,\beta} | a_{nlj} a_{n'\ell'j'} | \Phi_{A,\alpha} \rangle$$
- transferred angular momentum** obtained from angular distribution
- More complex mechanism:  
**> 1-step and 2-step components**
- low cross section** (typically 0.1-1 mb)



# Two-nucleon transfer: a probe for pairing correlations



I. Tanihata *et al.*, Phys. Rev. Lett. **100** (2008).  
G. Potel *et al.*, Phys. Rev. Lett. **105** (2010).

Energies from few to 50 MeV/nucleon / low cross sections (100  $\mu\text{b}$ )

# ( $p, 2p$ ) quasifree scattering

## Kinematics

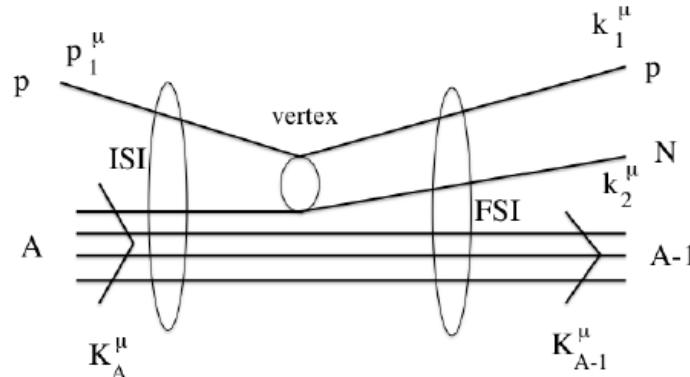
$$\vec{q}_\perp = +\vec{p}_{1\perp} + \vec{p}_{2\perp}$$

$$\vec{q}_{\parallel} = \frac{(\vec{p}_{1\parallel} + \vec{p}_{2\parallel}) - \gamma(M_A - M_{A-1})}{\gamma}$$

$$E_s = T_0 - \gamma(T_1 + T_2) - 2(\gamma - 1)m_p + \beta\gamma(\vec{p}_{1\parallel} + \vec{p}_{2\parallel}) - \frac{q^2}{2M_{A-1}}$$

## Distorted Wave Impulse Approximation

$$T_{p,pN} = \sqrt{S_{nlj}} \left\langle \chi_{k'_p}^{(-)} \chi_{k_N}^{(-)} \left| \tau_{pN} \right| \chi_{k_p}^{(+)} \phi_{nlj} \right\rangle$$



Recent work: T. Aumann, C. Bertulani, J. Ryckebusch, PRC **88** (2013)

