

# Impact of Future Experimental Scenarios on Flavour Physics

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- Introduction
- What can we learn from the "ballistic" program
- First ideas on the impact of extreme flavour
- Conclusions and Outlook

# INTRODUCTION

- Most of the discoveries of the past 45 years anticipated by arguments or indirect evidence:
  - Ioffe&Shabalin, GIM: NP (charm) @ GeV
  - Unitarization of Fermi theory: NP at  $10^2$  GeV
  - KM: 3<sup>rd</sup> generation
  - Flavour, EW fit:  $m_t \sim 170$  GeV
  - EW fit:  $m_H = 100 \pm 30$  GeV

# INTRODUCTION II

- Now we are left with arguments only:
  - Hierarchy problem: NP close to EW scale
  - WIMP miracle: NP close to EW scale
  - gauge coupling unification: NP (SUSY) close to EW scale
- In parallel with increasing the energy probed by direct search, seek for indirect evidence!

# How much “natural” is Nature?

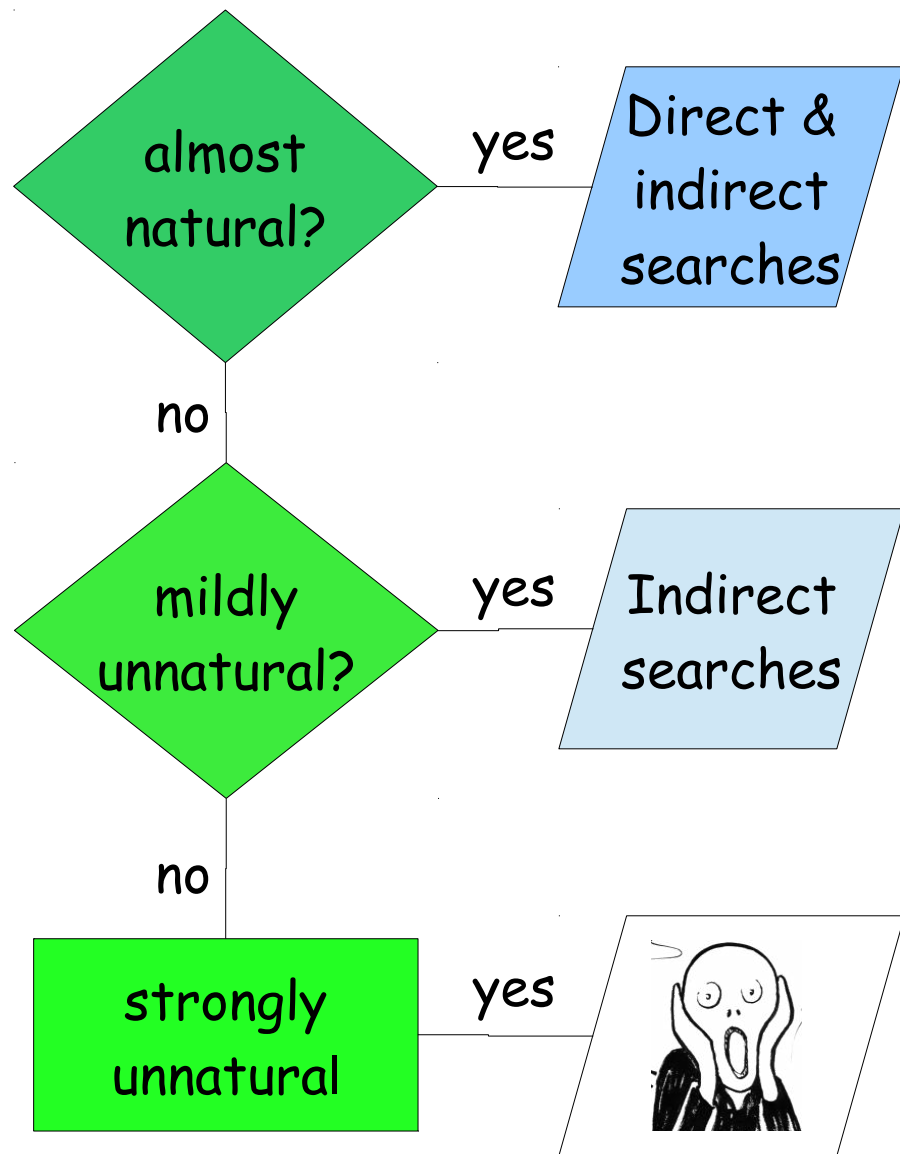


illustration by G. Villadoro

Courtesy of Marco Ciuchini

# ROLE OF FLAVOUR

- In the framework of future experimental developments, Flavour physics should:
- Guarantee that the flavour structure of any directly discovered NP can be efficiently probed, and/or
- Push the NP scale that can be indirectly probed up by (at least) one order of magnitude

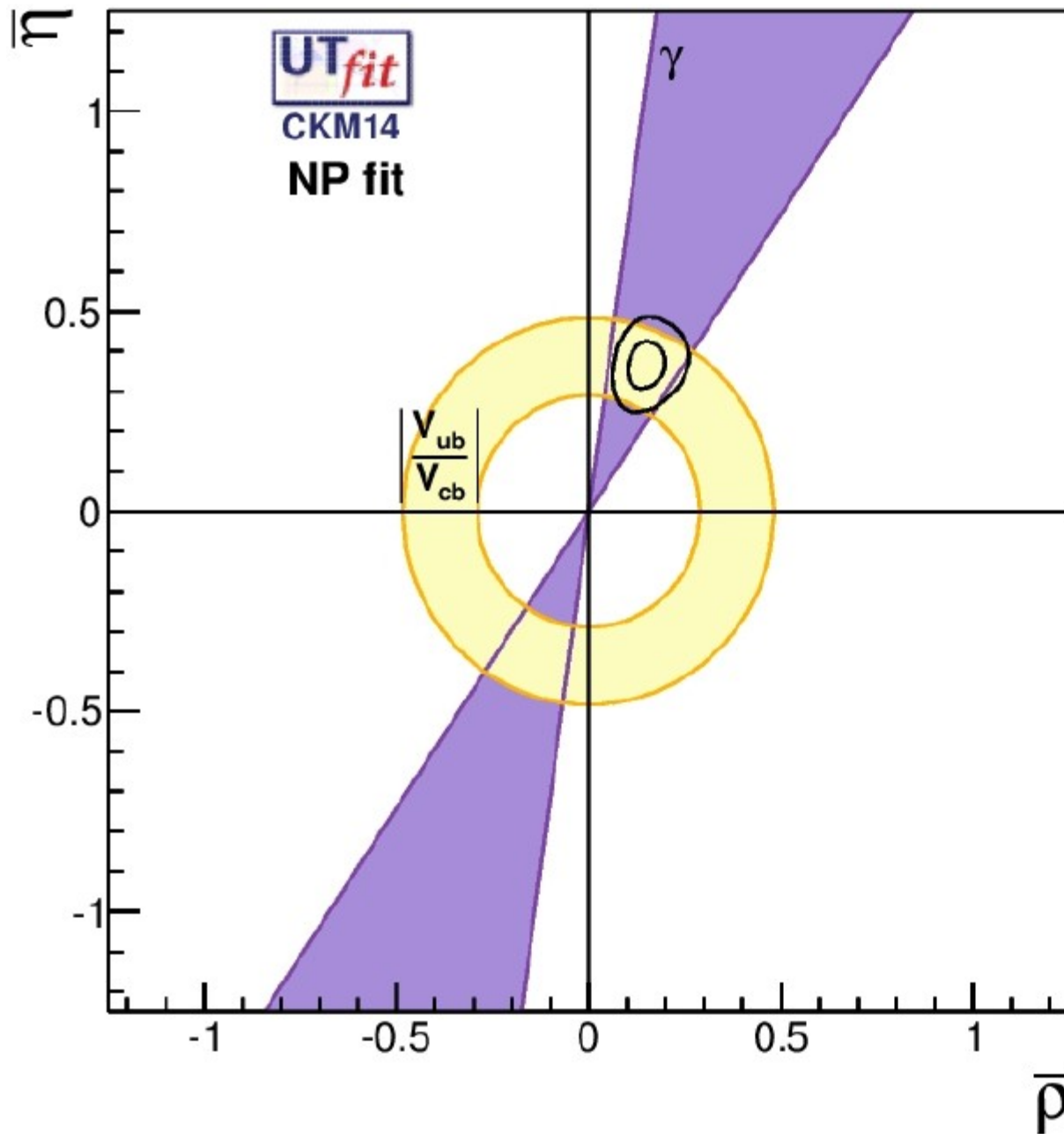
- A generic FCNC amplitude has the form

$$A_{SM} + A_{NP} = K_{SM} \frac{\alpha_W}{4\pi} \frac{F_{CKM}}{M_W^2} + K_{NP} L \frac{F_{NP}}{\Lambda^2}$$

where  $L$  is a possible loop factor,  $F_{NP}$  denotes the NP flavour coupling and  $K_{SM,NP}$   $O(1)$  #'s.

- For any directly observed NP, we know  $\Lambda$  and  $L$  and can extract  $F_{NP}$
- Assuming a value for  $L \geq \alpha_W/4\pi$  and  $F_{NP} \geq F_{SM}$ , we can extract the NP scale  $\Lambda$
- Need to improve  $A_{exp}$  &  $A_{SM}$  (where present)

# NP analysis results



$$\begin{aligned}\bar{\rho} &= 0.154 \pm 0.040 \\ \bar{\eta} &= 0.367 \pm 0.048\end{aligned}$$

**SM is**

$$\begin{aligned}\bar{\rho} &= 0.137 \pm 0.022 \\ \bar{\eta} &= 0.349 \pm 0.014\end{aligned}$$



# NP parameter results

dark: 68%

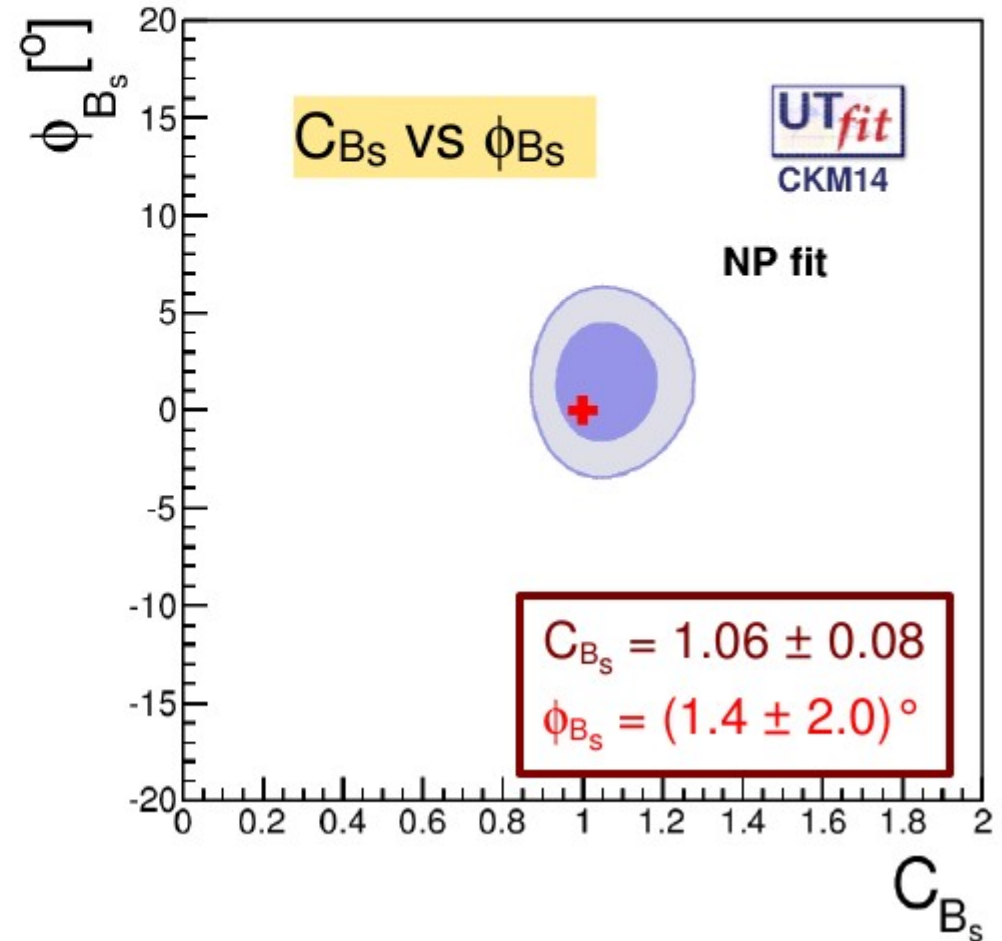
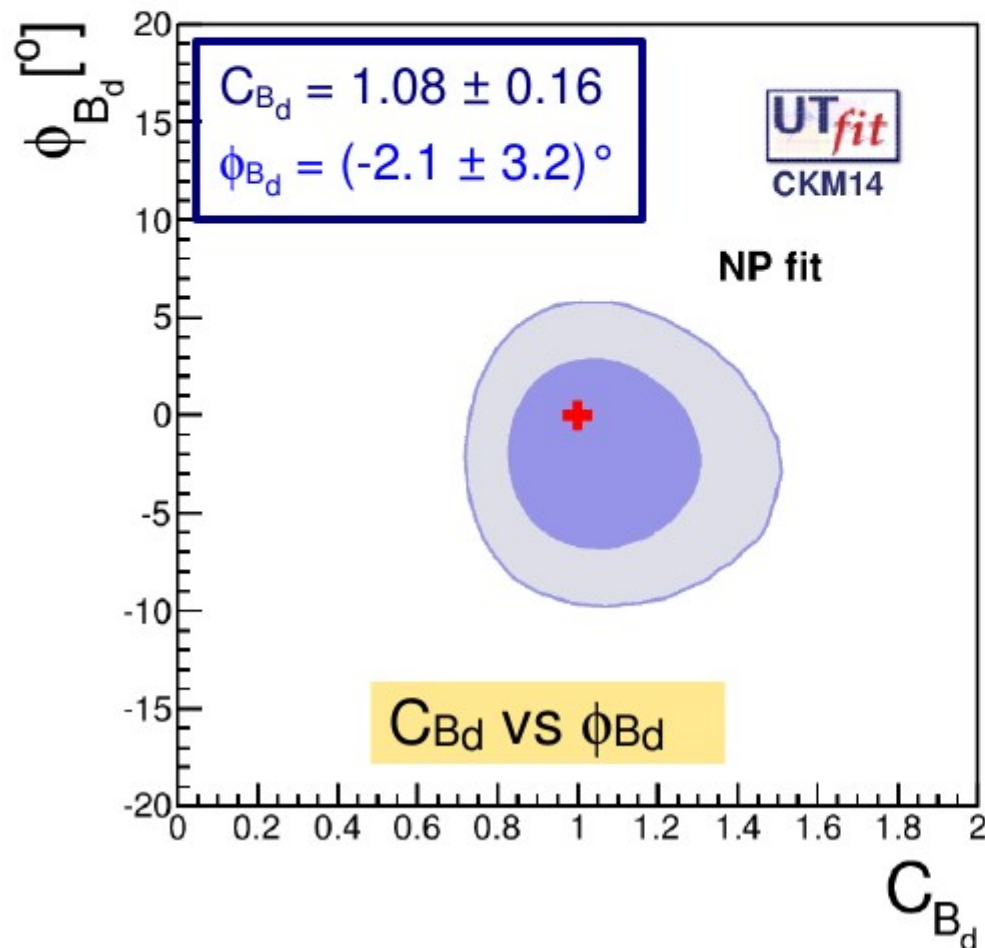
light: 95%

SM: red cross

K system

$$C_{\varepsilon_K} = 1.07 \pm 0.16$$

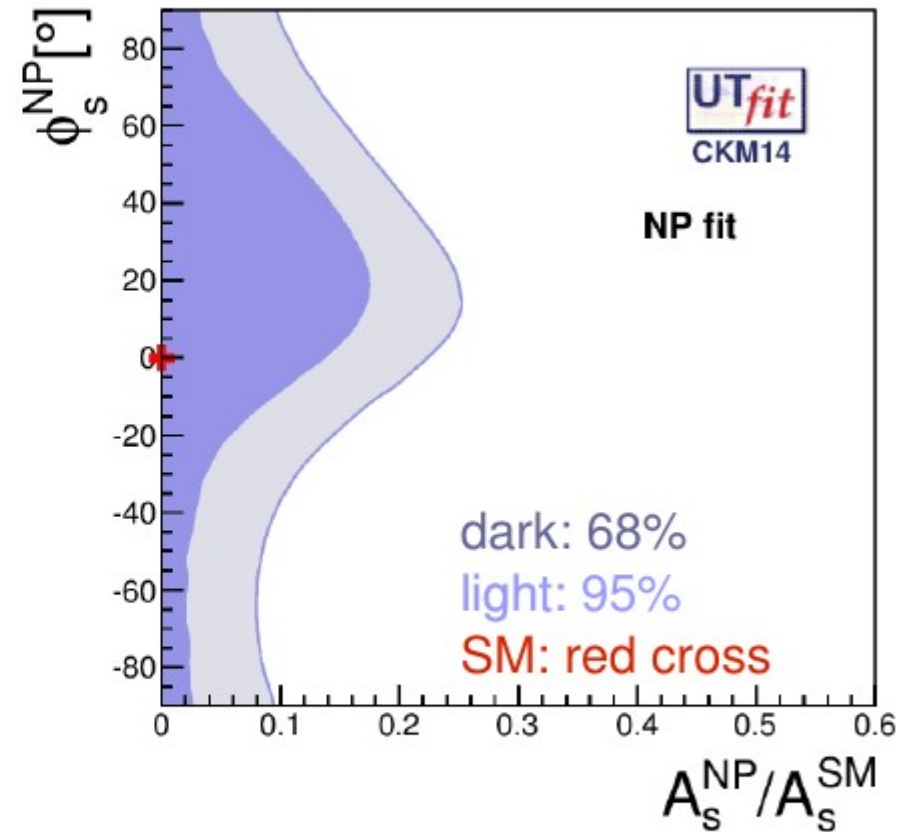
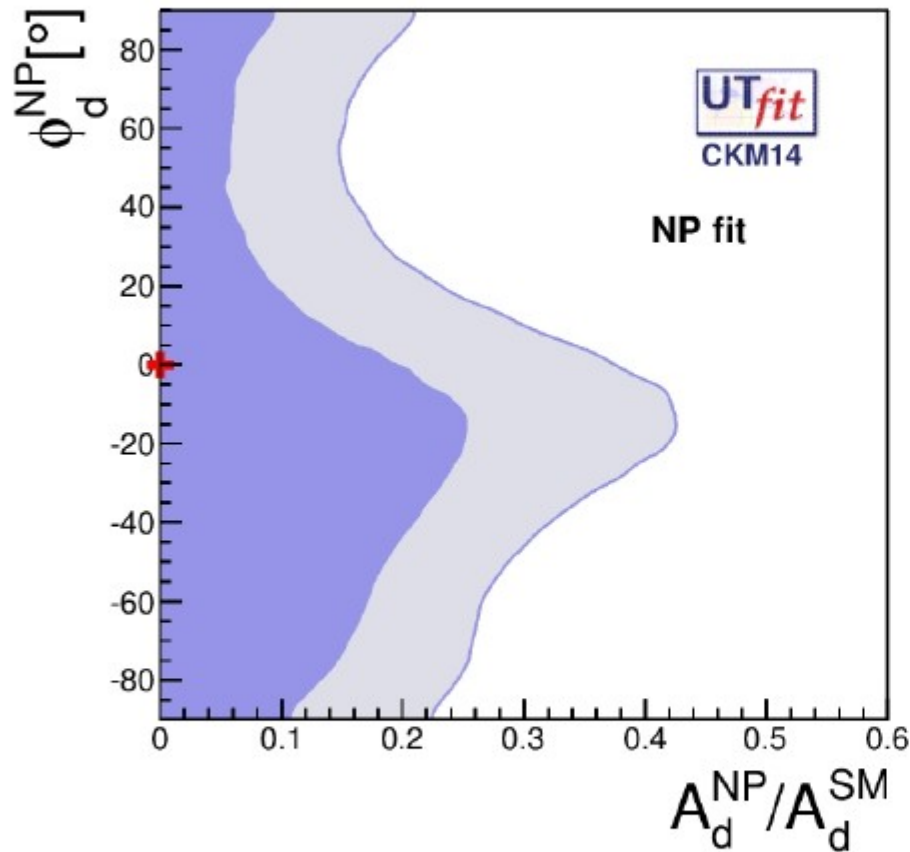
$$A_q = C_{B_q} e^{2i\varphi_{B_q}} A_q^{SM} e^{2i\varphi_q^{SM}}$$





# NP parameter results

$$A_q = \left( 1 + \frac{A_q^{NP}}{A_q^{SM}} e^{2i(\varphi_q^{NP} - \varphi_q^{SM})} \right) A_q^{SM} e^{2i\varphi_q^{SM}}$$



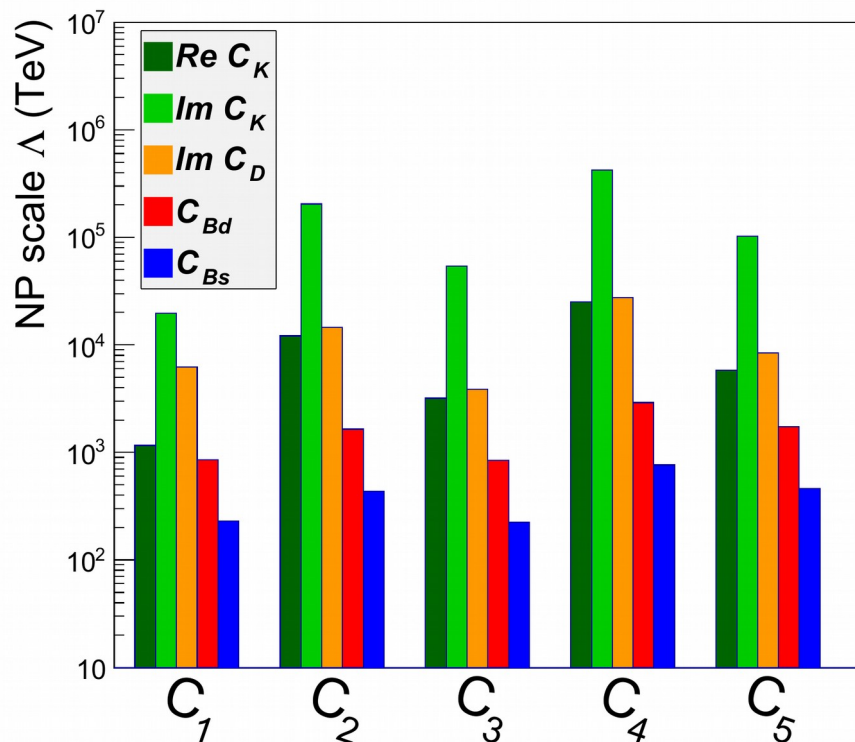
The ratio of NP/SM amplitudes is:

< 25% @68% prob. (42% @95%) in  $B_d$  mixing

< 17% @68% prob. (25% @95%) in  $B_s$  mixing

# PRESENT BOUNDS ON NP

## Bounds from $\Delta F=2$ processes



$\Delta F=2$  processes scale as  $1/\Lambda^2$

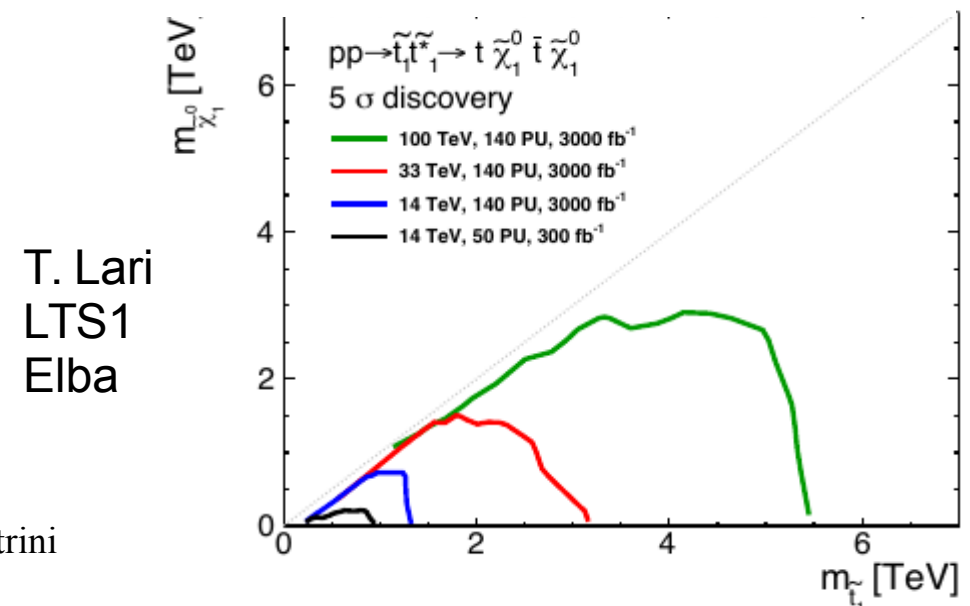
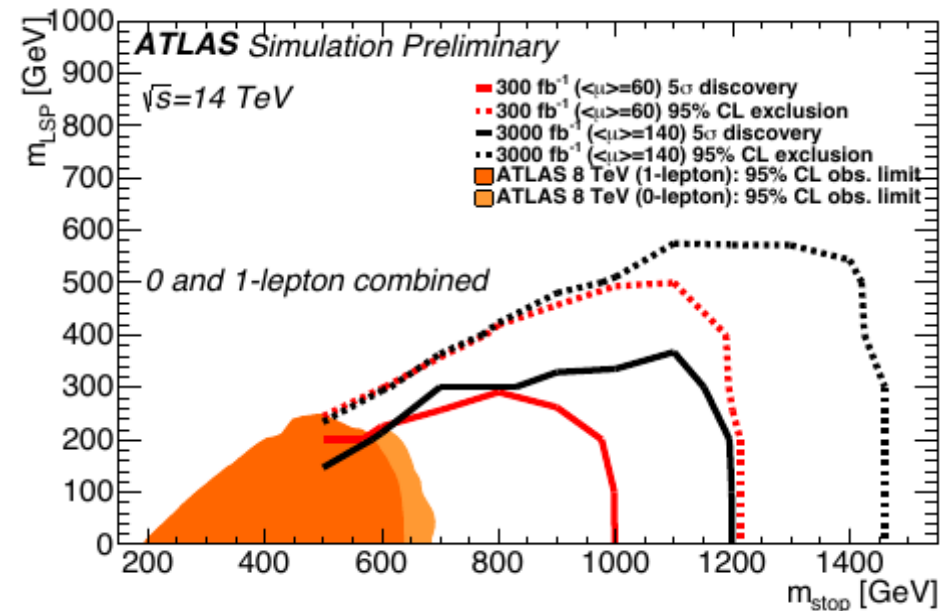
- Best bound from  $\varepsilon_K$ , dominated by CKM error
- CPV in charm mixing follows, exp error dominant
- Best CP conserving from  $\Delta m_K$ , dominated by long distance
- $B_d$  and  $B_s$  behind, error from both CKM and B-params

# INTERPRETING THE BOUNDS

- generic case (no loop, no flavour suppression, all chiral structures):  $\Lambda > 4.2 \cdot 10^5 \text{ TeV}$
- Extra-Dim case (no loop suppression, CKM suppression, all chiral structures):  $\Lambda > 96 \text{ TeV}$
- MFV case (no loop suppression, CKM suppression, only left-handed):  $\Lambda > 9 \text{ TeV}$
- weakly-interacting MFV case (EW loop & CKM suppression, left-handed):  $\Lambda > 300 \text{ GeV}$

# COMPLEMENTARITY WITH DIRECT SEARCHES

- The weakly-interacting MFV case provides a lower bound on NP contribution to flavour observables (worst-case scenario)
- This often corresponds to worst-case scenarios for direct searches as well
- Keep the two reaches in sync so that we can see flavour effects of any directly visible NP



T. Lari  
LTS1  
Elba

# BALLISTIC FUTURE

- Belle II and LHCb upgrade will improve present precision/sensitivity in B, D and  $\tau$  physics by a factor of 3-10 De Nardo, Lanfranchi
- NA62 will provide a 10% measurement of  $BR(K^+ \rightarrow \pi^+ \nu \nu)$ , KOTO should observe  $K_L \rightarrow \pi^0 \nu \nu$  Ceccucci
- MEG-II and Mu2e will improve the sensitivity on  $\mu \rightarrow e \gamma$  to  $6 \cdot 10^{-14}$  and on  $\mu \rightarrow e$  conversion to  $6-7 \cdot 10^{-17}$  Signorelli

# Flavour Golden Modes

Experiment: No Result

Moderately precise

Precise

Very precise

Theory: Moderately clean

Clean, needs Lattice

Clean

©A. Stocchi

Observable/mode	Current ~ 1 ab <sup>-1</sup>	LHCb (2017) 5 fb <sup>-1</sup>	Belle II (2022) 50 ab <sup>-1</sup>	LHCb upgrade 50 fb <sup>-1</sup>	Theory
$\tau$ Decays					
$\tau \rightarrow \mu \gamma$					
$\tau \rightarrow e \gamma$					
$B_{u,d}$ Decays					
$B \rightarrow \tau \nu, \mu \nu$					
$B \rightarrow K^{(*)+} \nu \bar{\nu}$					
S in $B \rightarrow K_s^0 \pi^0 \gamma$					
S (other penguin modes)					
$A_{CP} (B \rightarrow X_s \gamma)$					
$BR(B \rightarrow X_s \gamma)$					
$BR(B \rightarrow X_s ll)$					
$BR(B \rightarrow K^{(*)} ll)$					
$B_s$ Decays					
$B_s \rightarrow \mu \mu$					
$\beta_S$ from $B_s \rightarrow J/\psi \phi$					
$B_s \rightarrow \gamma \gamma$					
$a_{sl}$					
$D$ Decays					
Mixing parameters					
CP Violation					

based on arXiv:1109.5028

very precise with improved detector  
statistically limited  
right handed currents  
Belle II measures many more modes  
systematic error is main challenge  
control systematic error with data  
Belle II measures e mode well, LHCb does  $\mu$

Comparison of present and future flavour experiments on "golden modes" (an incomplete list)

Observable/mode	Current ~ 1 fb <sup>-1</sup>	LHCb (2017) 5 fb <sup>-1</sup>	SuperB (2022) 75 ab <sup>-1</sup>	LHCb upgrade 50 fb <sup>-1</sup>	Theory
Luminosity					
$\alpha$					
$\beta$ from $b \rightarrow c \bar{c} s$					
$B_d \rightarrow J/\psi \pi^0$					
$B_s \rightarrow J/\psi K_s^0$					
$\gamma$					
$ V_{ub} $ inclusive					
$ V_{ub} $ exclusive					
$ V_{cb} $ inclusive					
$ V_{cb} $ exclusive					

LHCb can only use  $p\bar{p}$   
 $\beta$  theory error  $B_d$   
 $\beta$  theory error  $B_s$   
need an  $e^+e^-$  environment to do a precision measurement using semi-leptonic B decays.



# Precision flavour physics & theory uncertainties

no theory improvements needed	$\beta(J/\psi K), \gamma(DK), \alpha(\pi\pi)^*,$ lepton FV and UV, CPV in $B \rightarrow X_{s+d}\gamma$ , $\tau$ decays zero of FB asymmetry $B \rightarrow X_s l^+ l^-$	NP insensitive or null tests of the SM or SM already known with the required accuracy
improved lattice QCD	meson mixing, $B \rightarrow D(*) l \nu$ , $B \rightarrow \pi(\rho) l \nu$ $B \rightarrow K^* \gamma$ , $B \rightarrow \rho \gamma$ , $B \rightarrow l \nu$ , $B_s \rightarrow \mu \mu$	target error: ~1-2% Feasible
improved OPE+HQE	$B \rightarrow X_{u,c} l \nu$ , $(B \rightarrow X_s \gamma)$	target error: ~1-2% Possibly feasible with large samples. Detailed studies required
improved QCDF/SCET or flavour symmetries	S from TD $A_{CP}$ in $b \rightarrow s$ transitions	target error: ~2-3% large and hard to improve uncertainties on small corrections. FS+data can bound the th. error

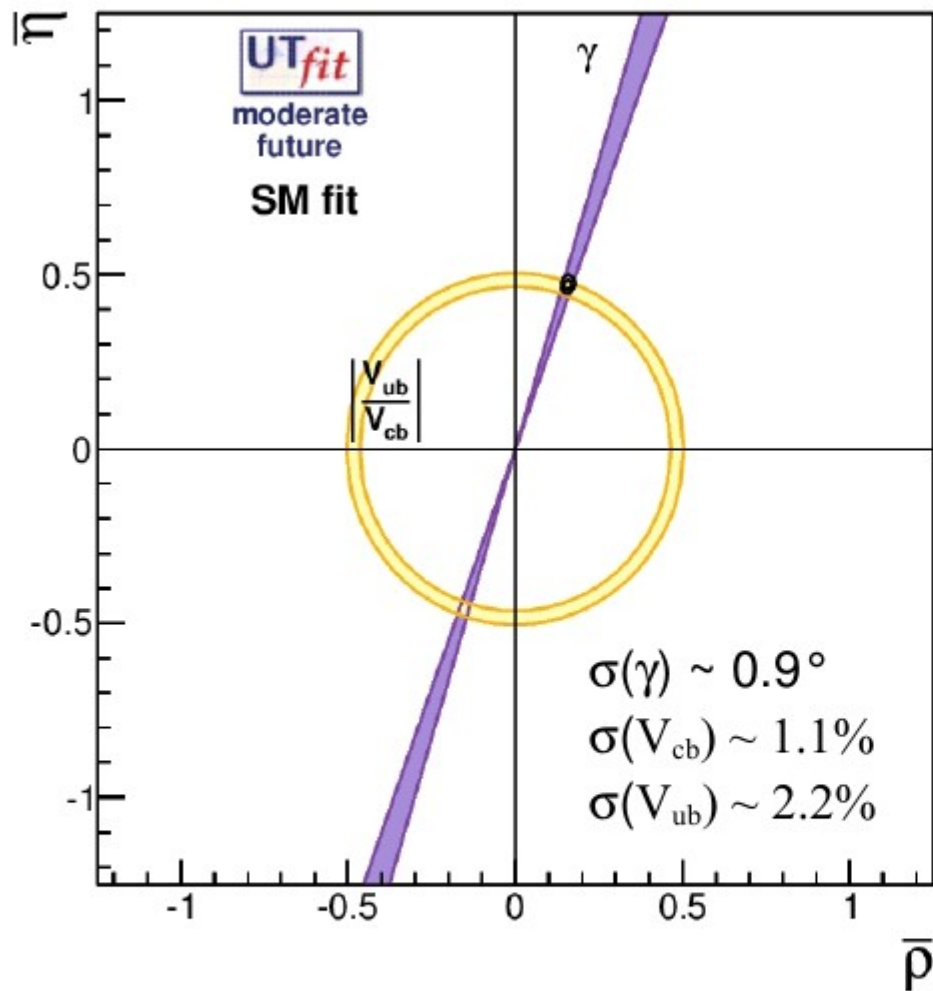


# Therefore, my tentative (INACCURATE!) estimates are:

Hadronic parameter	L.Lellouch ICHEP 2002 [hep-ph/0211359]	FLAG 2013 [1310.8555]	2025 [What Next]
$f_+^{K\pi}(0)$	- First Lattice result in 2004 [0.9%]	[0.4%]	[0.1%]
$\hat{B}_K$	[17%]	[1.3%]	[0.1-0.5%]
$f_{B_s}$	[13%]	[2%]	[0.5%]
$f_{B_s}/f_B$	[6%]	[1.8%]	[0.5%]
$\hat{B}_{B_s}$	[9%]	[5%]	[0.5-1%]
$B_{B_s}/B_B$	[3%]	[10%]	[0.5-1%]
$F_{D^*}(1)$	[3%]	[1.8%]	[0.5%]
$B \rightarrow \pi$	[20%]	[10%]	[>1%]

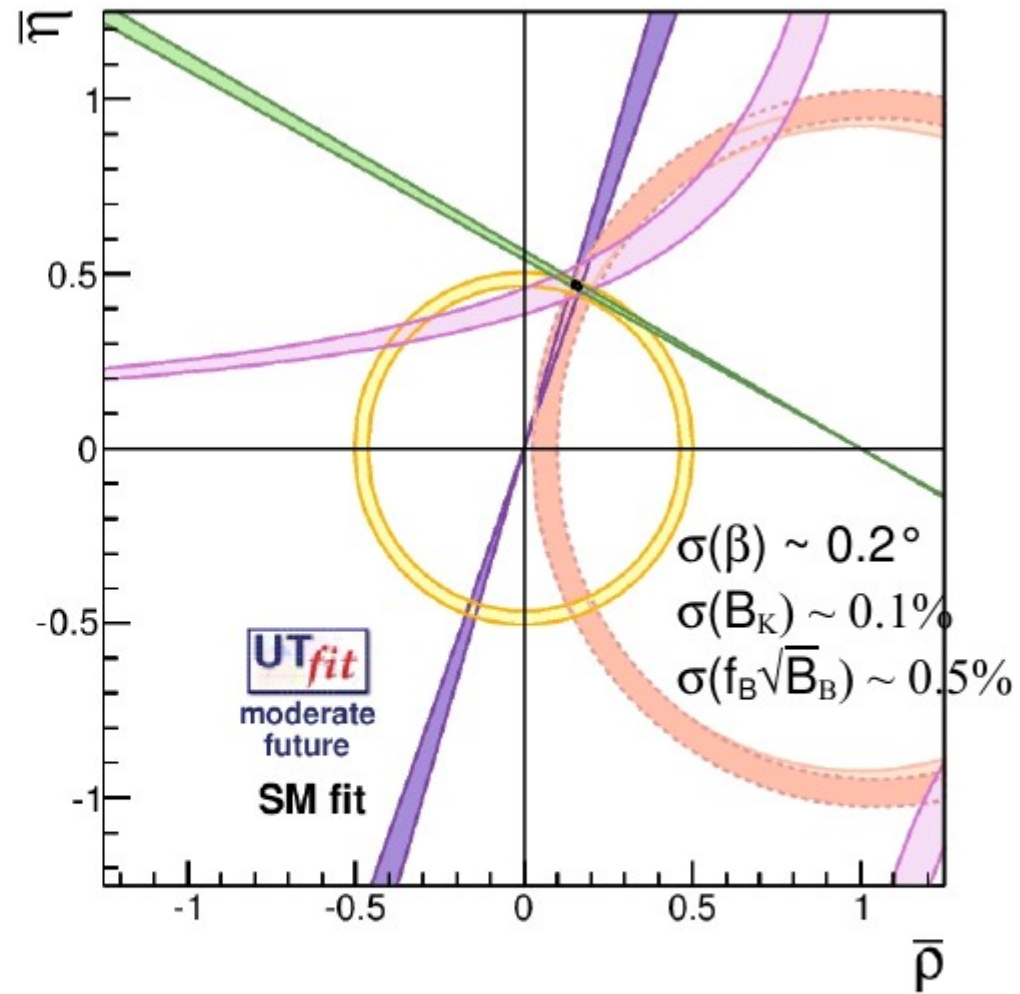
C. Tarantino  
LTS1  
Elba 2014

More unpredictable but more surprising progresses can occur for the observables that today are very difficult (or infeasible):  $K \rightarrow \pi \nu \bar{\nu}$ ,  $K \rightarrow \pi l^+ l^-$ ,  $K \rightarrow \pi \pi$ ,  $\Delta m_K$



errors from tree-only fit on  $\rho$  and  $\eta$ :

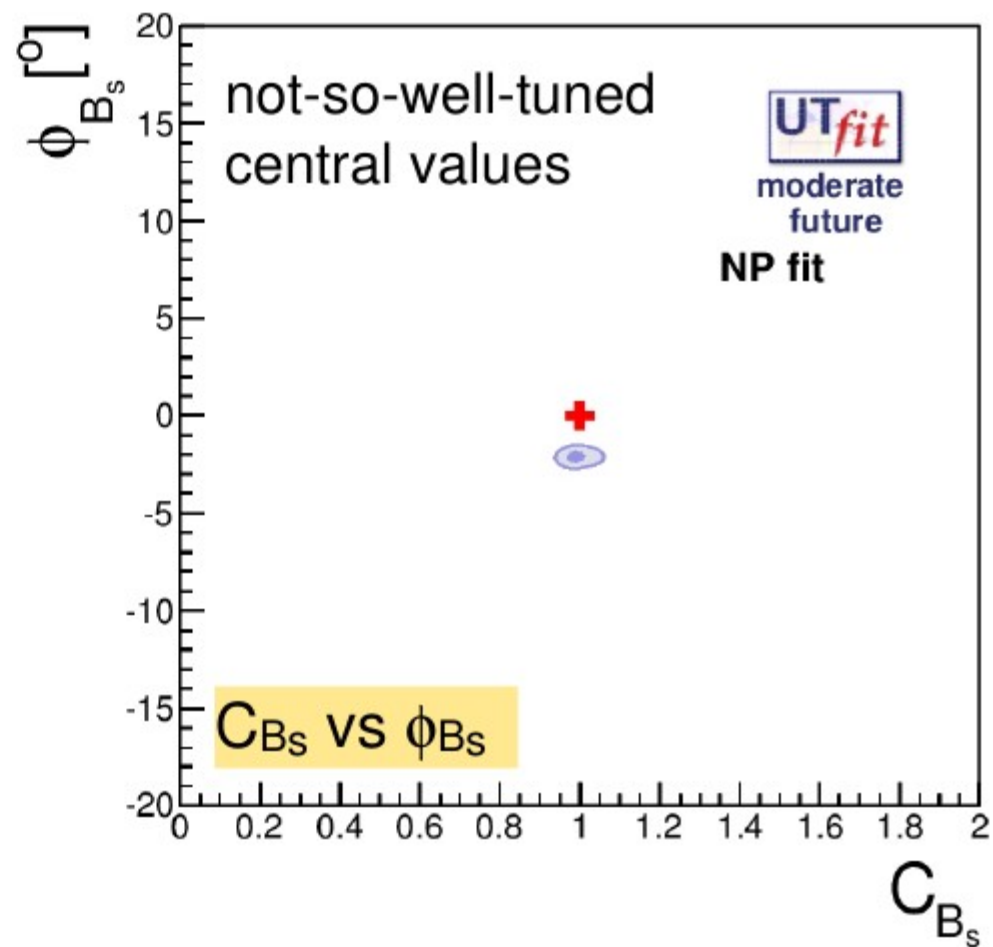
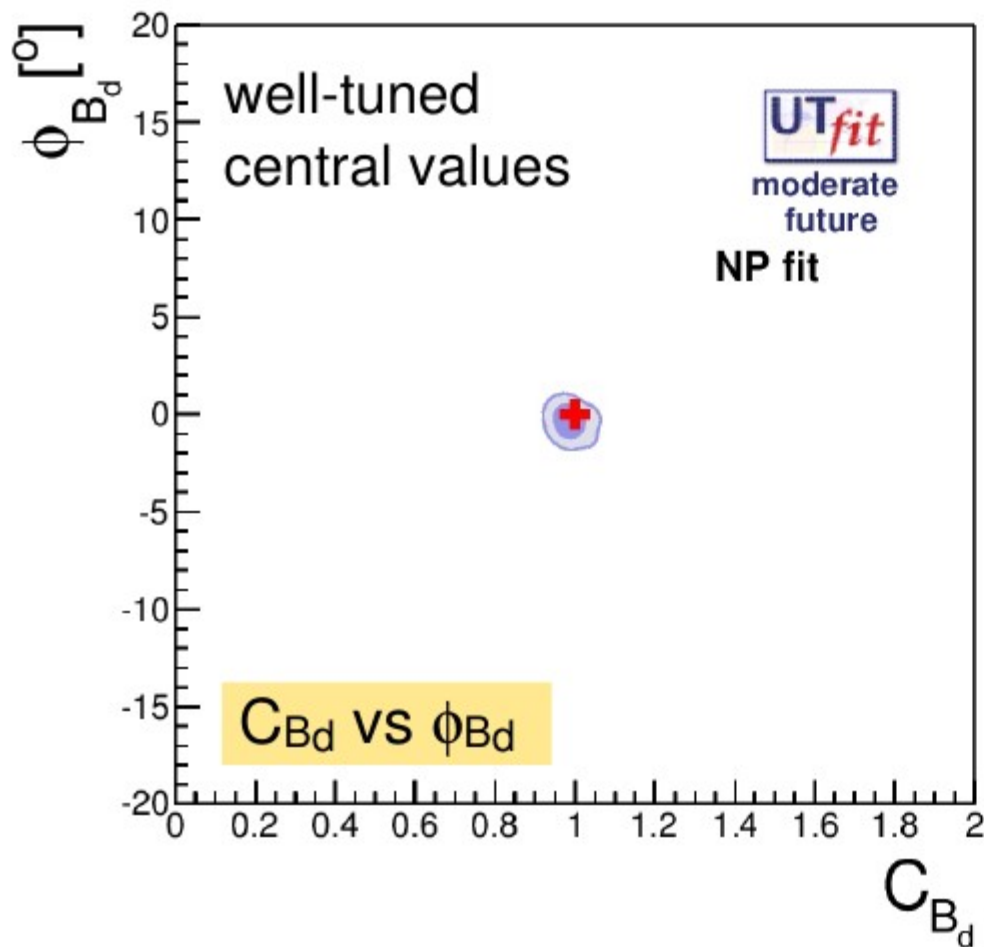
$\sigma(\rho) = 0.008$  [currently 0.051]  
 $\sigma(\eta) = 0.010$  [currently 0.050]



errors from 5-constraint fit on  $\rho$  and  $\eta$ :

$\sigma(\rho) = 0.005$  [currently 0.034]  
 $\sigma(\eta) = 0.004$  [currently 0.015]

M. Bona @ CKM2014



errors on general NP parameters:

$$\sigma(C_{B_d}) = 0.03 \text{ [currently } 0.16]$$

$$\sigma(\phi_{B_d}) = 0.7 \text{ [currently } 3.2]$$

$$\sigma(C_{B_s}) = 0.03 \text{ [currently } 0.08]$$

$$\sigma(\phi_{B_s}) = 0.6 \text{ [currently } 2.0]$$

M. Bona @ CKM2014

# CHARM CPV EXTRAPOLATED

- SM contribution to  $\phi_{M12}$  negligible, while one could envisage  $\phi_{\Gamma12} O(1^\circ)$  due to LD penguins  
Zupan
- Present fit:
  - $\phi_{M12} = [-4, 12]^\circ$  @ 95% prob., no reach on  $\phi_{\Gamma12}$
  - $\Lambda > 3.5 \cdot 10^4 \text{ TeV}$
- LHCb upgrade / Belle II:
  - $\delta\phi_{M12} = \pm 1^\circ$  and  $\delta\phi_{\Gamma12} = \pm 2^\circ$  @ 95% prob.
  - $\Lambda > 10^5 \text{ TeV}$

# EXTREME FLAVOUR

- A very interesting possibility has been put forward: collect 100x the LHCb upgrade luminosity
- A detailed study of the impact of such possibility should be carried out to assess its full physics potential.
- I'll just briefly flash a few items to make you interested

# ASSESSING THE IMPACT OF EXTREME FLAVOUR

- Determine expected exp and th uncertainties on the widest spectrum of observables
- Extrapolate accuracy in CKM determination in the presence of NP
- Assess the NP reach in all sectors and various scenarios

# EXTREME UTA INPUT

Parameter	Error	comments
$\alpha_s(M_Z)$	$2 \cdot 10^{-4}$	
$m_t$	250 MeV	theory limited
$m_b$	10 MeV	$\times 3$ better
$V_{us}$	$1 \cdot 10^{-4}$	$\times 10$ better
$V_{cb}$	1%	Belle II
$V_{ub}$	1%	extreme baryons + $B_s$
$\epsilon_K$	0.4%	includes a 5% error on long distance + dim. 8
$B_K^i$		$\times 10$ better
$F_{B_s}$	1 MeV	
$F_{B_s}/F_{B_d}$	0.5%	
$B_{B_s}$	6%	
$B_{B_s}/B_{B_d}$	0.5%	
$\Delta M_d$	0.06%	
$\Delta M_s$	0.01%	
$\sin 2\beta$	0.06%	th. error from $B_d \rightarrow J/\psi \pi^0$
$\gamma$	$0.09^\circ$	
$\phi_{B_s}$	$0.0004^\circ$	th. error to be investigated



# EXTREME UTA (PRELIMINARY)

Parameter	SM fit error		NP fit error	
	now	extreme	now	extreme
$\bar{\rho}$	16%	0.4%	26%	1.5%
$\bar{\eta}$	4%	0.1%	13%	1.4%
$\text{Im}\lambda_t$	2.8%	0.8%	13%	1.4%
$\text{Re}\lambda_t$	2.9%	0.8%	7.4%	2.1%
$ V_{td}/V_{ts} $	2.3%	0.09%	5%	0.15%
$C_{\epsilon_K}$	—	—	0.16	0.034
$C_{B_d}$	—	—	0.16	0.029
$\phi_{B_d}$	—	—	$3.2^\circ$	$0.41^\circ$
$C_{B_s}$	—	—	0.08	0.028
$\phi_{B_s}$	—	—	$2.0^\circ$	$0.023^\circ$

# EXTREME BEYOND UTA

- D mixing, scaling LHCb upgrade estimates for  $K_S\pi\pi$  and  $\gamma_{CP}$ ,  $A_\Gamma$ :
  - $\delta\phi_{M12} = \pm 0.1^\circ$  and  $\delta\phi_{\Gamma12} = \pm 0.2^\circ$  @ 95% prob.
  - $\Lambda > 3 \cdot 10^5 \text{ TeV}$ , close to the bound from  $\varepsilon_K$
- $\text{BR}(B_d \rightarrow \mu^+\mu^-)/\text{BR}(B_s \rightarrow \mu^+\mu^-)$  @ ~4%, with much smaller theoretical uncertainty: very powerful probe of MFV
- ...

# CONCLUSIONS

- In a global strategy for NP searches, improving the accuracy on FCNC and CPV processes has a key role to ensure that:
  - we are able to determine the flavour structure of any NP directly seen, and hopefully understand its origin; roughly 3x in  $M_{NP} \Leftrightarrow 10x$  in exp & th  $\Leftrightarrow 100x$  in L
  - we increase the sensitivity of indirect searches (flavour has the lead in this field) and maybe detect an indirect NP signal


# CONCLUSIONS II

- Impact of “ballistic” flavour program studied in detail, expected improvements will keep indirect searches in sync with direct ones
- First steps to assess the impact of an extreme flavour experiment in progress:
  - extrapolation of lattice errors (done)
  - prelim. estimate of exp. reach (in progress)
  - projection of UTA (in progress)
  - projection of NP sensitivities in all sectors

# BACKUP SLIDES

I follow Vittorio Lubicz's  
Appendix in the SuperB CDR (2007 -> 2015)  
(and Stephen Sharp's talk at *Lattice QCD: Present and Future* (Orsay, 2004))

Values of the simulation parameters ( $N_{\text{conf}}$ ,  $a$ ,  $m_l$ ,  $L$ )  
to achieve a certain accuracy (1%, 0.5%, 0.1%)



Computational cost of the corresponding simulation



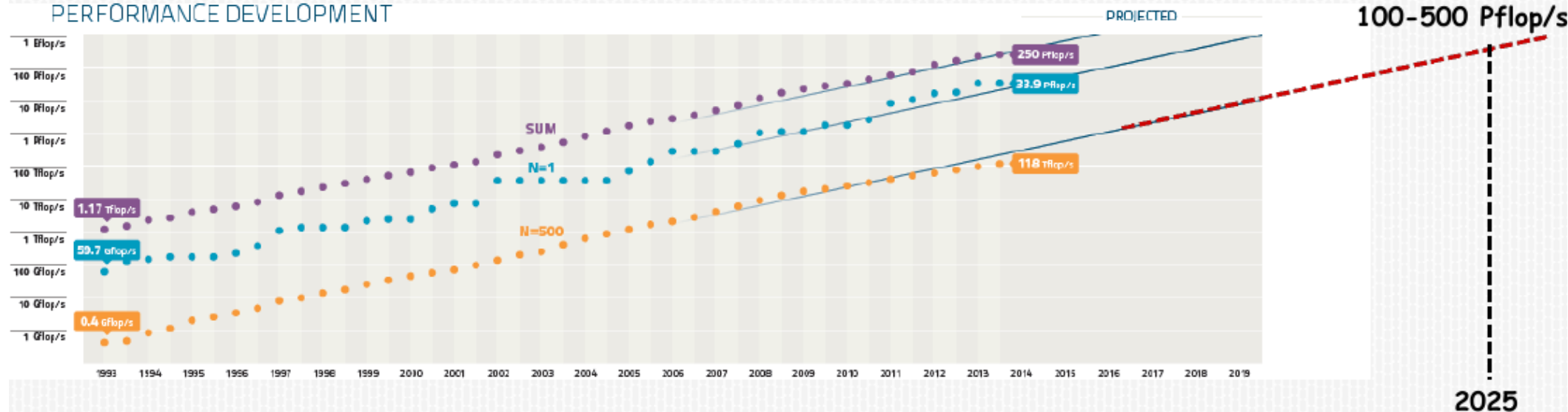
Comparison to the expected future computational power

# History (and prediction) of the computational power from Moore's Law (1965):

*The number of transistors on integrated circuits doubles approximately every two years  
(thanks to miniaturization)*

➔ **Performance improvement of  $O(10^3)$  every 10 years**

PERFORMANCE DEVELOPMENT



**Lattice collaborations typically have at hand per year  
a computational power similar to the 500<sup>th</sup> most powerful computer  
(0.1-0.5 Pflops-years in 2014 → 100-500 Pflops-years in 2025)**



# Computational cost of a Lattice Simulation as a function of the parameter values (e.g. Wilson-like fermions, $N_f=2$ )

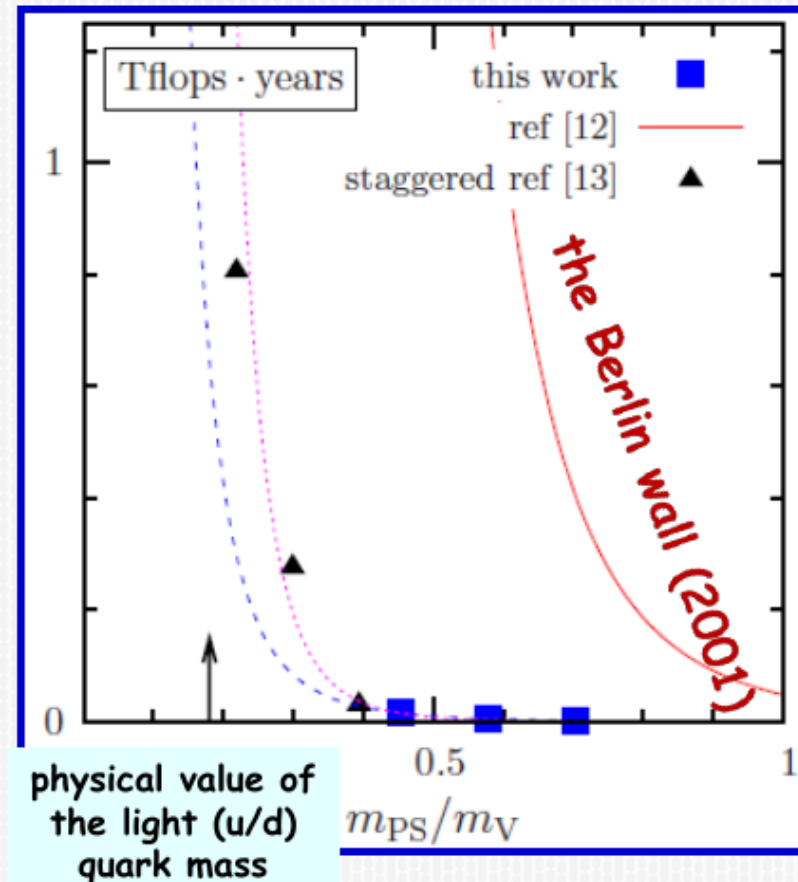
Del Debbio, Giusti, Luscher, Petronzio, Tantalò, hep-lat/0610059

$$\text{TFlops} - \text{years} \simeq 0.03 \left( \frac{N_{\text{conf}}}{100} \right) \left( \frac{L_s}{3 \text{ fm}} \right)^5 \left( \frac{L_t}{2L_s} \right) \left( \frac{0.2}{\hat{m}/m_s} \right) \left( \frac{0.1 \text{ fm}}{a} \right)^6$$

0.03 → 0.1 [ $N_f=2+1$ ]  
→ 0.05 [ $O(a)$ -improved]  
→ 0.3-1.0 [Ginsparg-Wilson]

x3 of overhead (less expensive simulations to perform continuum extrapolation...)

(We will see if a more detailed study of recent simulations provides a more optimistic estimate)



C. Tarantino @ LTS1 Elba 2014

The wall fall ( $1/m_l^3 \rightarrow 1/m_l$ ) is an important example of how unpredictable (theoretical and algorithmic) developments can have a significant impact

# EXP INPUT FOR CHARM MIXING

- LHCb upgrade:
  - $\delta x = 1.5 \cdot 10^{-4}$ ,  $\delta y = 10^{-4}$ ,  $\delta |q/p| = 10^{-2}$ ,  $\delta \phi = 3^\circ$  (from  $K_s \pi \pi$ );  $\delta y_{CP} = \delta A_\Gamma = 4 \cdot 10^{-5}$  (from  $K^+ K^-$ )
- extreme (LHCb upgrade lumi  $\times 100$ ):
  - $\delta x = 1.5 \cdot 10^{-5}$ ,  $\delta y = 10^{-5}$ ,  $\delta |q/p| = 10^{-3}$ ,  $\delta \phi = .3^\circ$  (from  $K_s \pi \pi$ );  $\delta y_{CP} = \delta A_\Gamma = 4 \cdot 10^{-6}$  (from  $K^+ K^-$ )