



Discussion: Dispersive Methods, Theory vs. Experiment

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MesonNet Meeting, Frascati

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with input from J. Bijnens, M. Hoferichter, A. Kupść

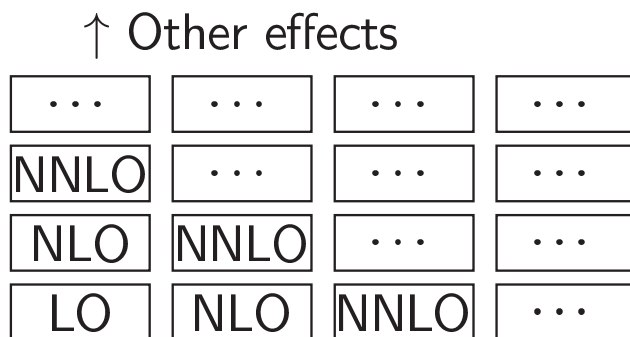
Potential topics

- $\eta \rightarrow 3\pi$: ChPT + dispersion relations
- other 3π decays (ω, ϕ, η') : effective parameterisations?
- $e^+e^- \rightarrow 3\pi$ cross sections
- theory for $\gamma^{(*)}\gamma^{(*)} \rightarrow \pi\pi$ Monte Carlo generators

ChPT + dispersion relations for $\eta \rightarrow 3\pi$

$\eta \rightarrow 3\pi$: LO, NLO, NNLO, NNNLO,...

- IN Gasser, Leutwyler, 1985 ($\sqrt{2.4} = 1.55$):
about half: $\pi\pi$ -rescattering
other half: everything else
- $\pi\pi$ -rescattering important Roiesnel, Truong, 1981
- Dispersive approach (next talk): resum all $\pi\pi$
- assume rescattering + rest separable:



→ $\pi\pi$ -rescattering

dispersive does this all the way

ChPT for
 $\eta \rightarrow 3\pi$ and
 $\eta \rightarrow \pi^0 \gamma \gamma$

Johan Bijnens

Older reviews

Model
independent

ChPT

$\eta \rightarrow 3\pi$ in
ChPT

LO
LO and NLO
NNLO

$\eta \rightarrow \pi^0 \gamma \gamma$

Conclusions

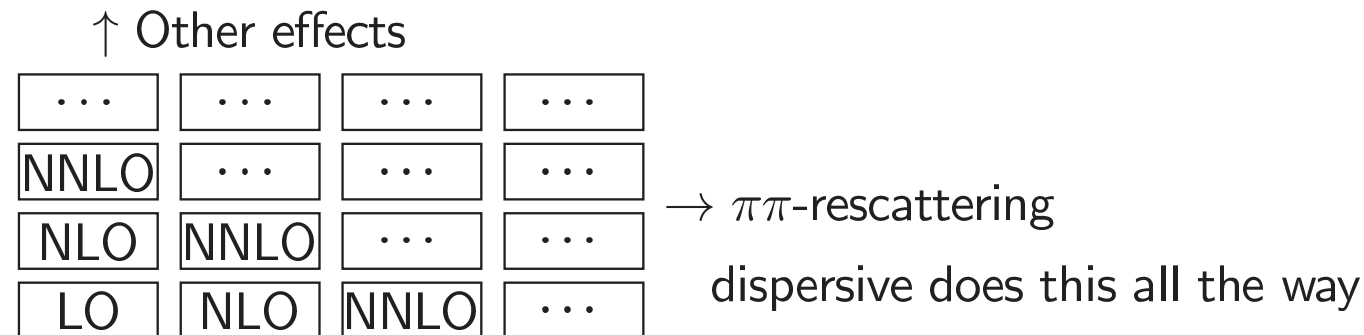


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ChPT + dispersion relations for $\eta \rightarrow 3\pi$

Why look at it this way?



- $\delta_\pi = 0.3, \delta_O = 0.3$
- LO = 1
- NLO = $\delta_\pi + \delta_O = 0.6$
- NNLO = $\delta_\pi^2 + \delta_\pi\delta_O + \delta_O^2 = 0.27$
- Squared: $1 \rightarrow 2.6 \rightarrow 3.5$
- Underlying other is: $1 + 0.3 + 0.09$
- Goal: remove dispersive from ChPT, then add again via dispersion relations (but now all boxes)
- Problem: Separation is not trivial

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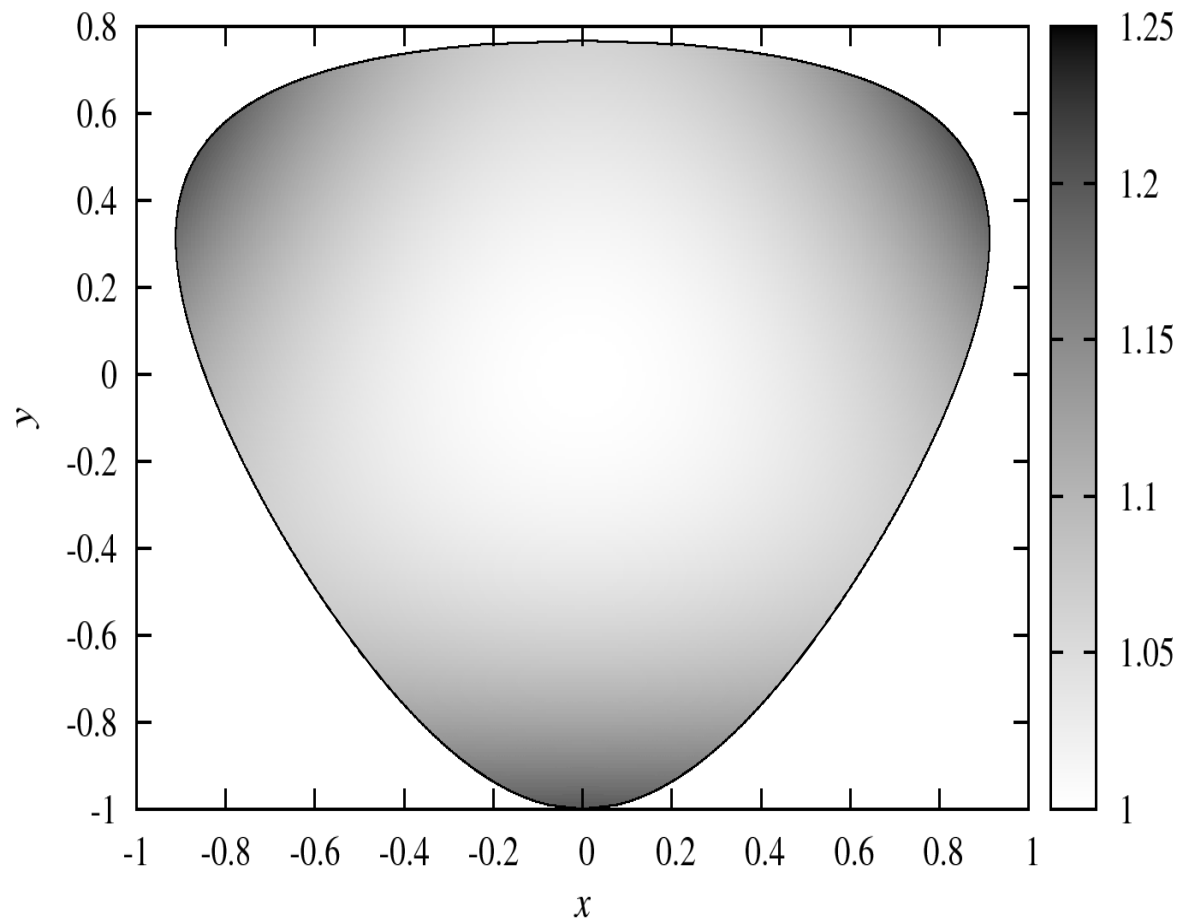
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Parameterisations for other 3π Dalitz plots

- $\omega \rightarrow 3\pi$ Dalitz plot smooth \rightarrow polynomial parameterisation

$$|\mathcal{F}_{\text{pol}}(z, \phi)|^2 = |\mathcal{N}|^2 \left\{ 1 + 2\alpha z + 2\beta z^{3/2} \sin 3\phi + 2\gamma z^2 + 2\delta z^{5/2} \sin 3\phi + \mathcal{O}(z^3) \right\}$$

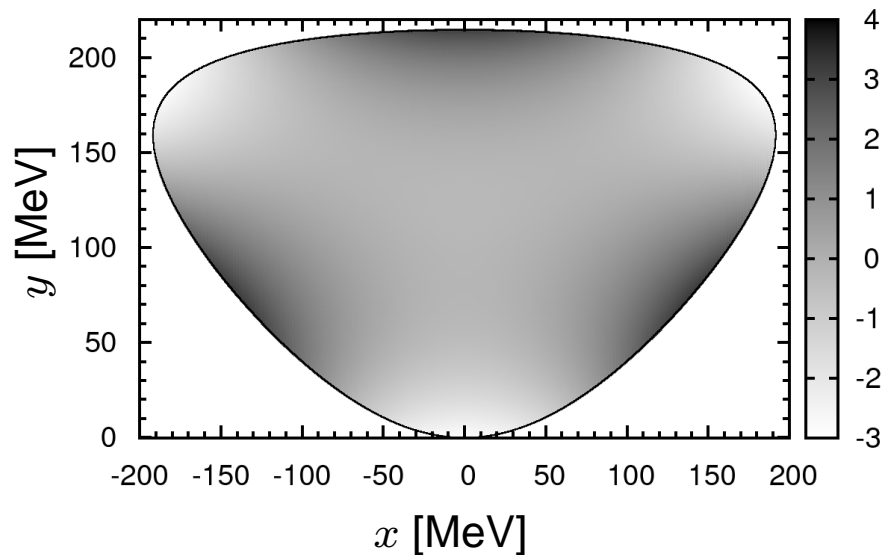


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$$\left(|\mathcal{F}_{\text{pol}}(z, \phi)|^2 / |\mathcal{F}(z, \phi)|^2 - 1 \right) [\%]$$



$\alpha \times 10^3$	$\beta \times 10^3$	$\gamma \times 10^3$	$\delta \times 10^3$
84 ... 96	—	—	—
74 ... 84	24 ... 28	—	—
73 ... 81	24 ... 28	3 ... 6	—
74 ... 83	21 ... 24	0 ... 2	7 ... 8

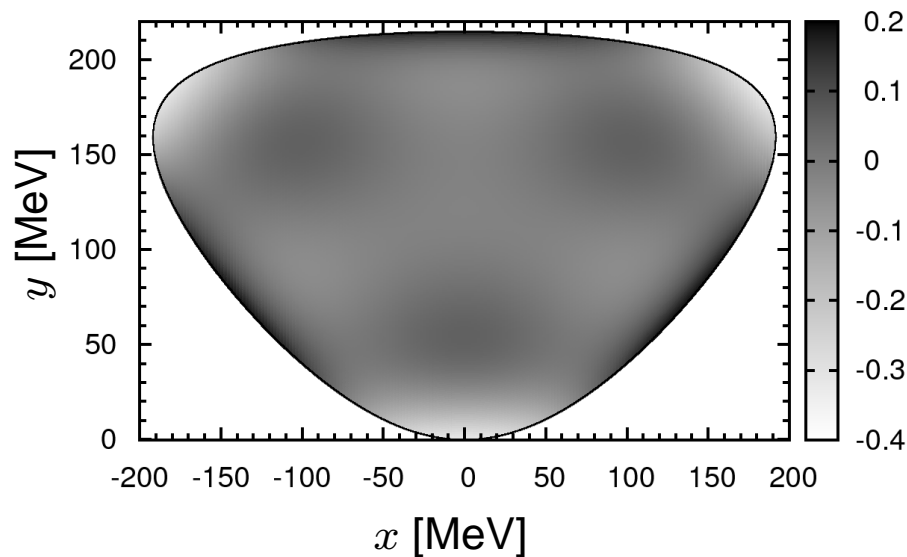
Niecknig, BK, Schneider 2012

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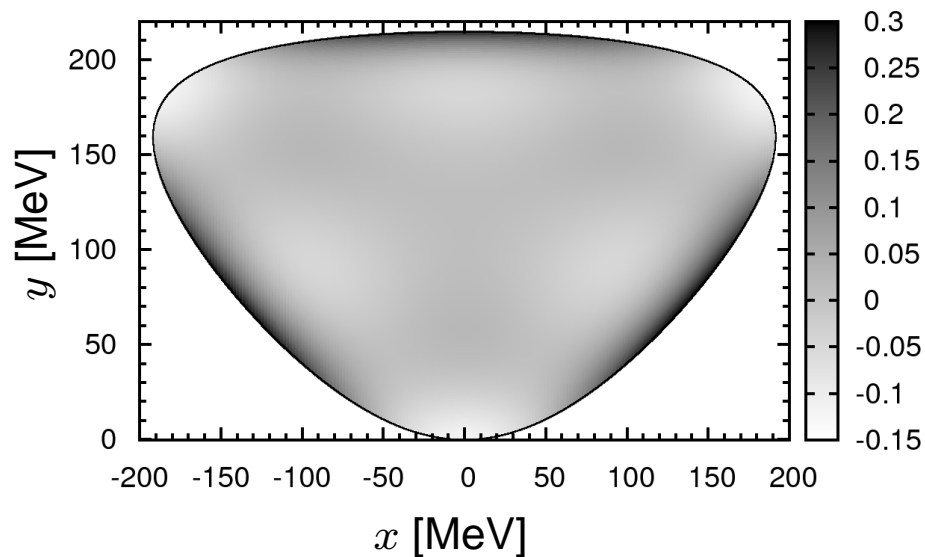
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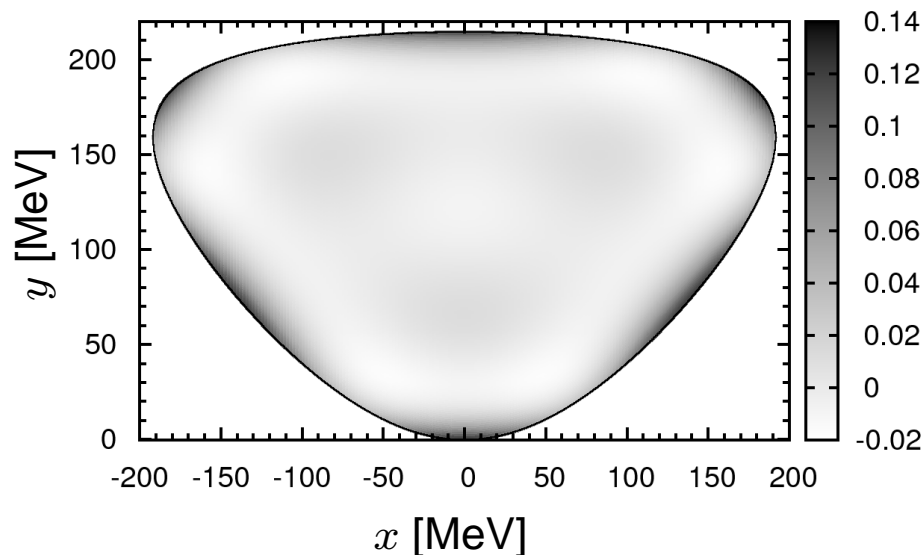
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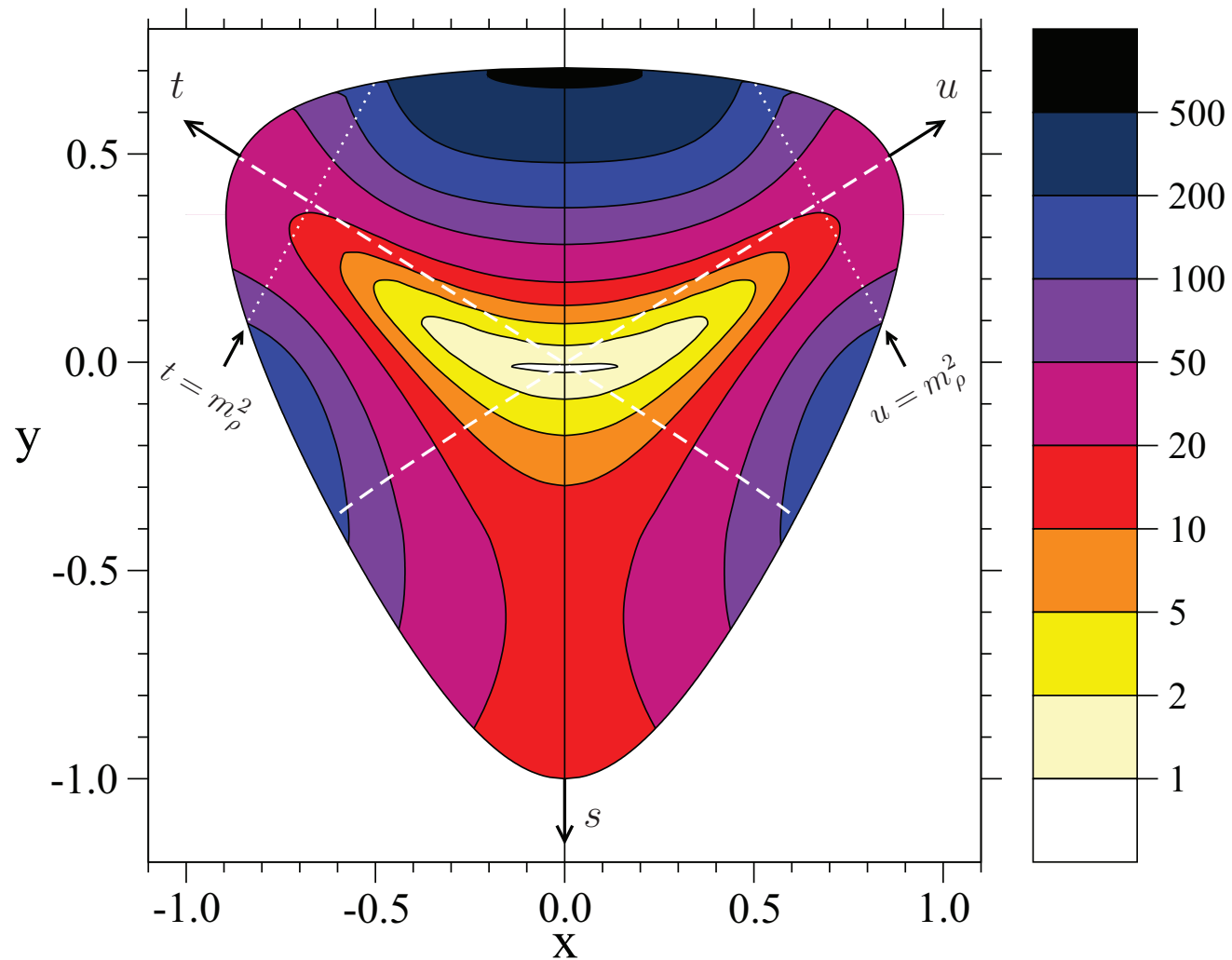
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\rightarrow Dalitz plot parameters not efficient/not precise enough

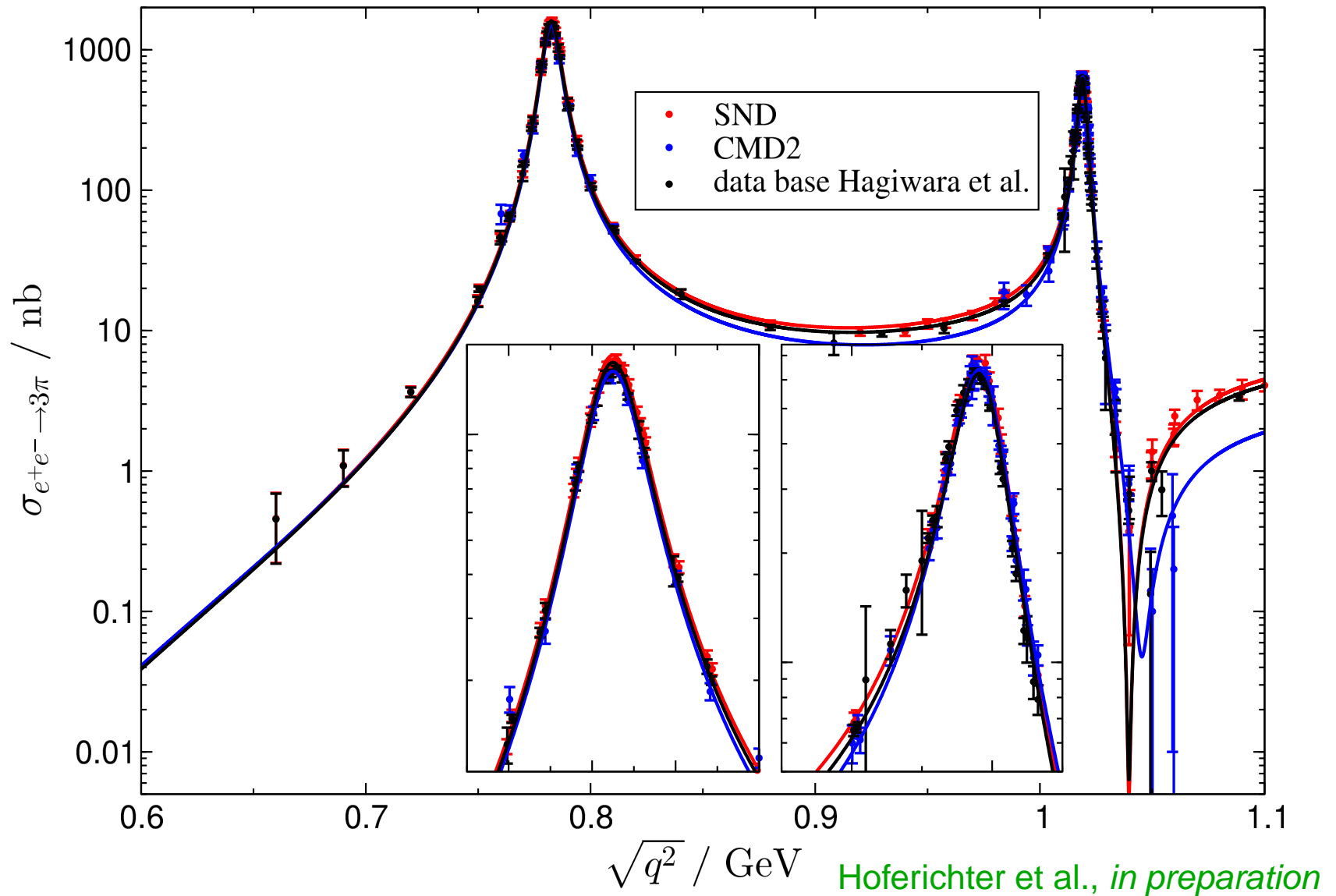
Parameterisations for other 3π Dalitz plots

- $\eta' \rightarrow \pi^+ \pi^- \pi^0$ Dalitz plot



Nißler, PhD thesis 2007

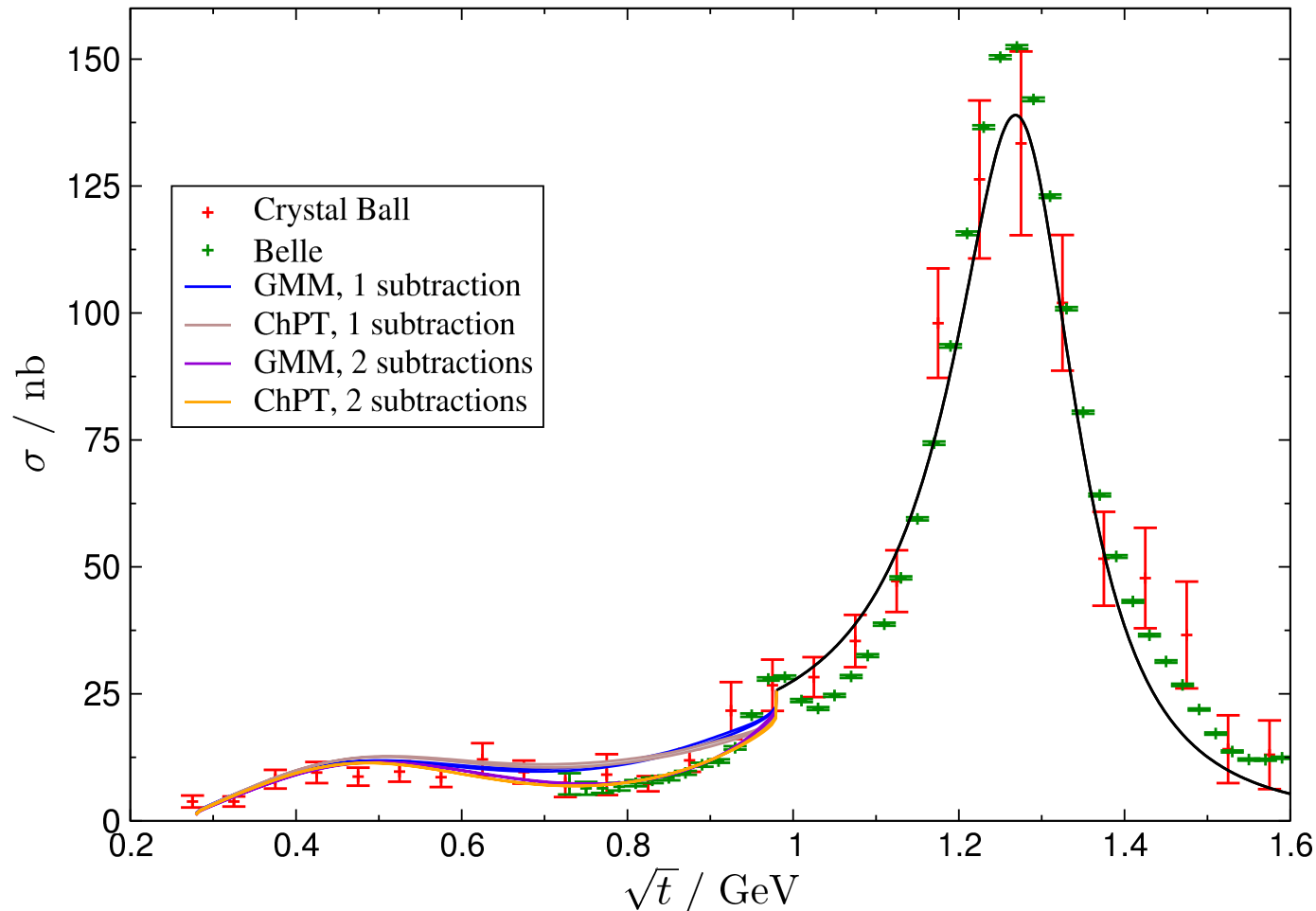
Inconsistent $e^+e^- \rightarrow 3\pi$ data sets



→ $\chi^2 / \#\text{dof}$ [SND / CMD-2 / Hagiwara et al.] = 1.0 / 2.4 / 6.3

Monte Carlo for $\gamma^{(*)}\gamma^{(*)} \rightarrow \pi\pi$

- pion–pion S-waves: $f_0(500)$; D-waves: $f_2(1270)$



Hoferichter, Phillips, Schat 2011

→ good parameterisations made available for MC generators?