

Advanced Bunching Scheme at REGAE

Linearization of the longitudinal phase space without higher harmonic field



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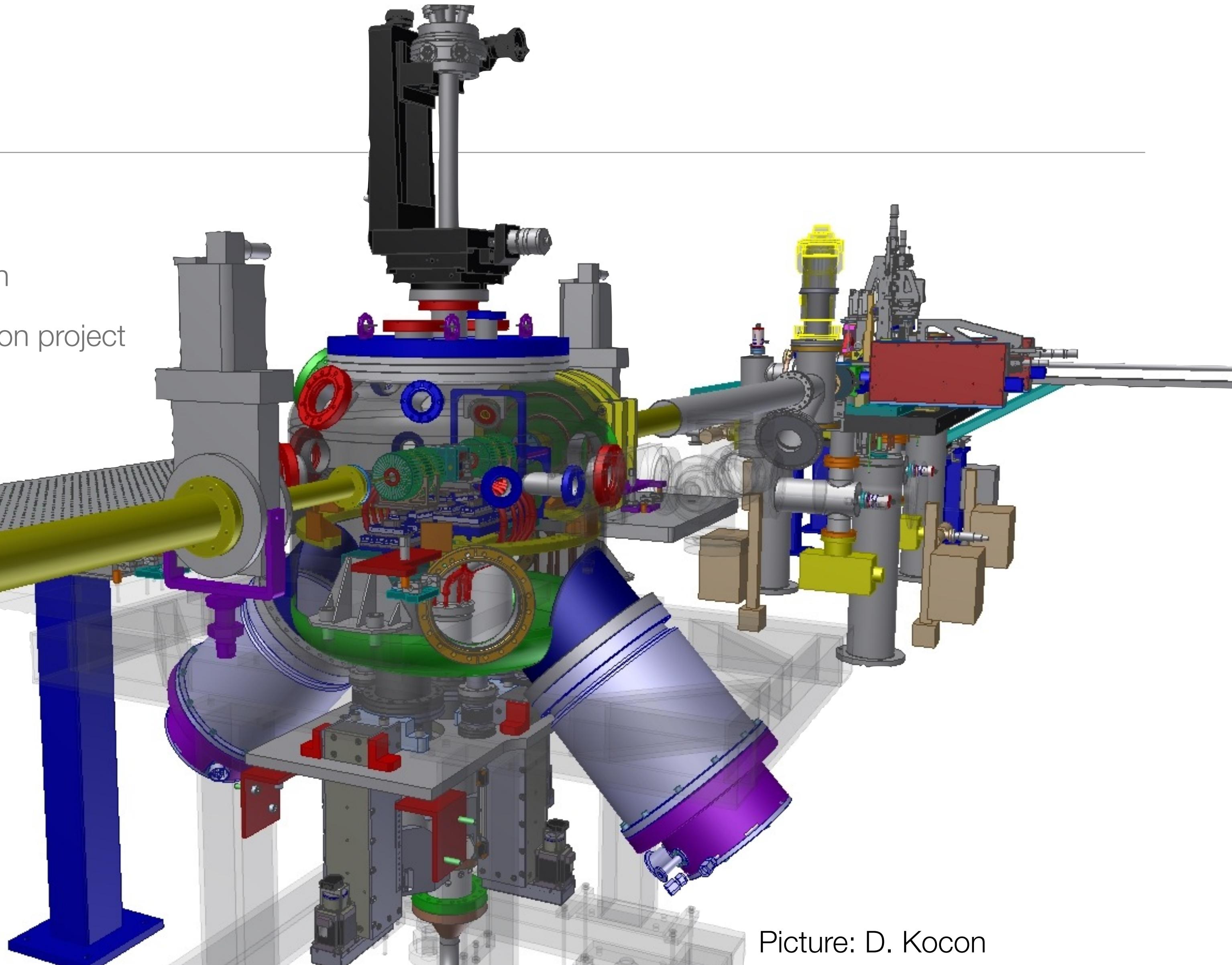
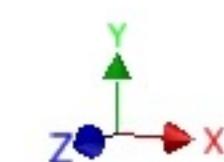
K. Floettmann, F. Gruener

[LAOLA](#). is a collaboration of



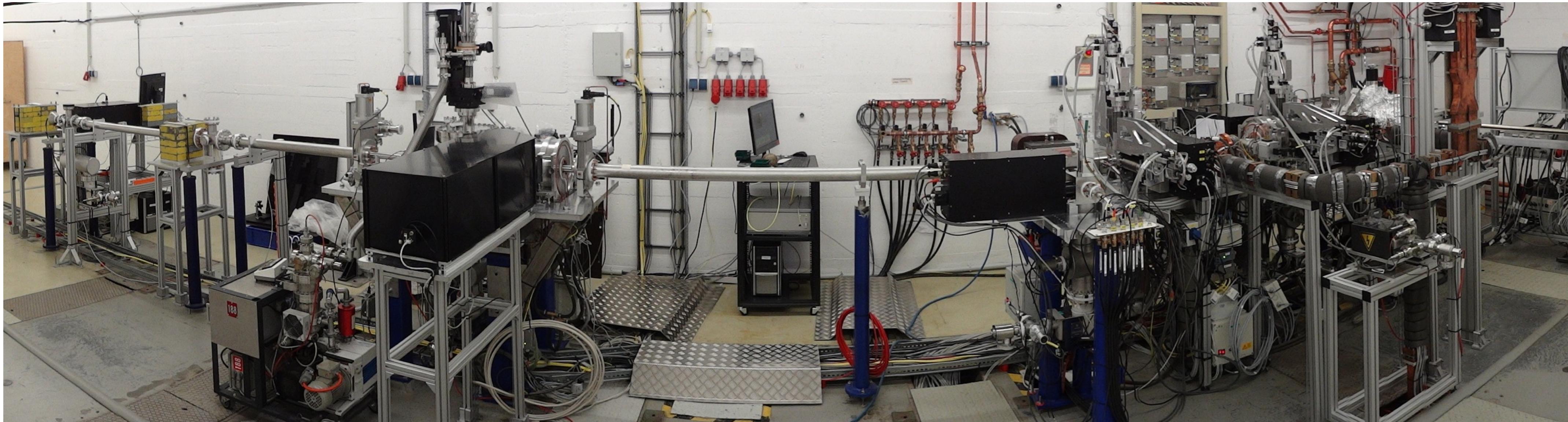
Outline

- > REGAE
 - > Time-resolved electron diffraction
 - > LAOLA@REGAE: External injection project
- > (Advanced) bunching mechanism
 - > Ballistic bunching
 - > Higher order correction
- > Results...
- > Summary & outlook



Picture: D. Kocon

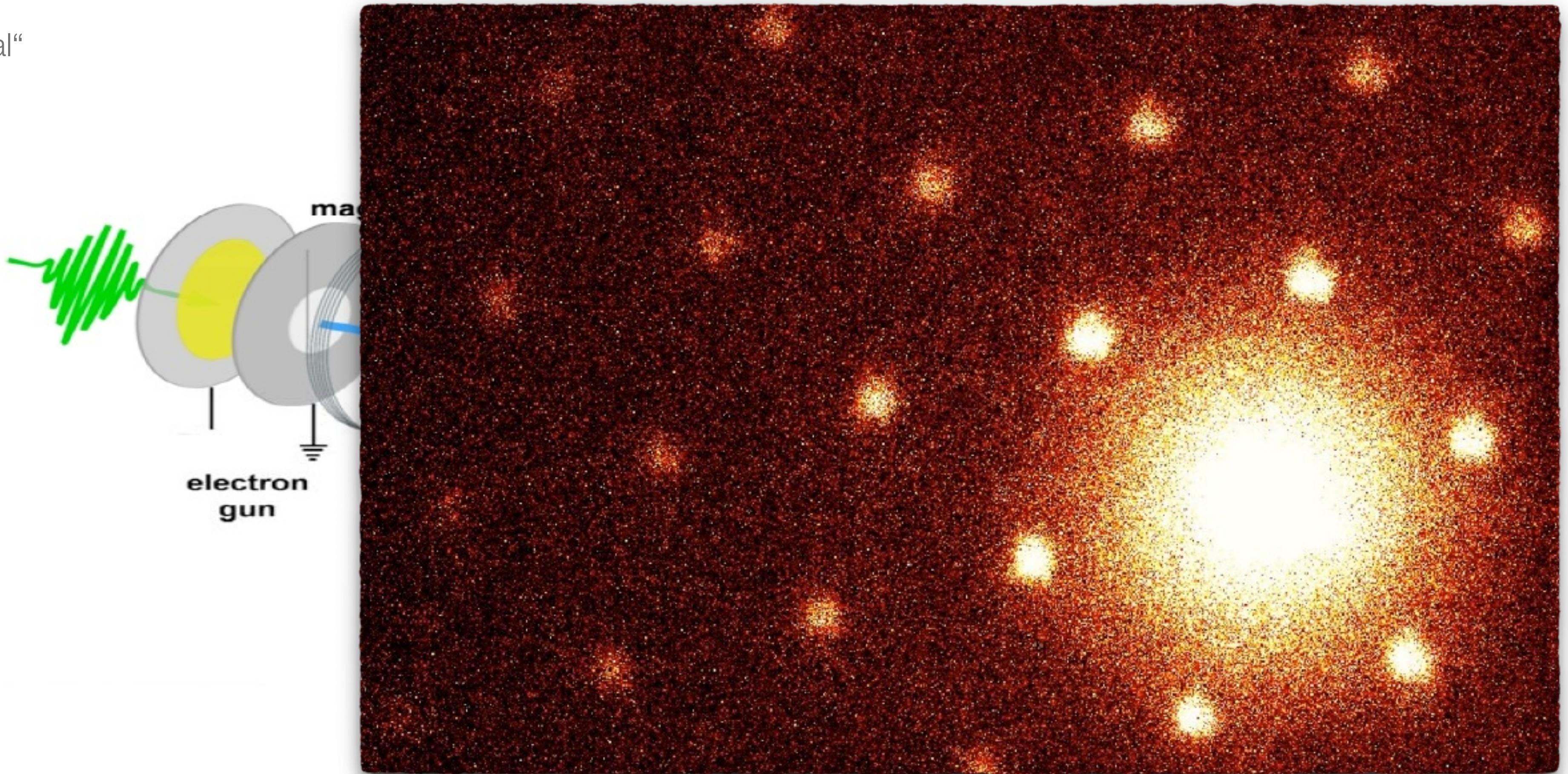
REGAE: Relativistic Electron Gun for Atomic Exploration



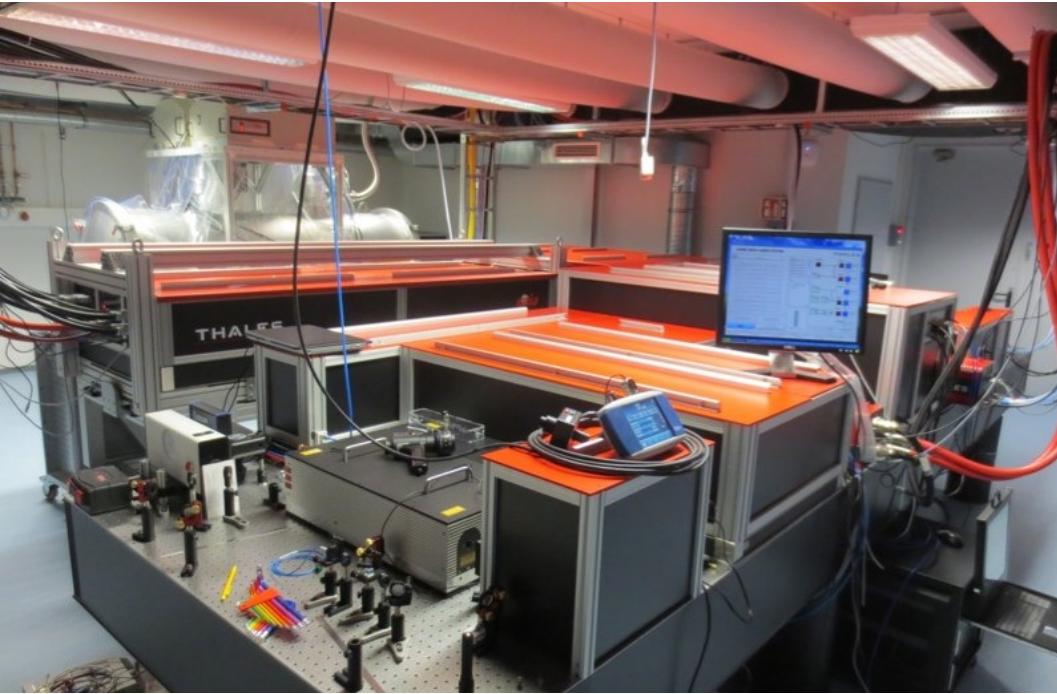
Average Energy	5.6 MeV
Energy Spread	10 keV
Bunch Charge	100 fC
Bunch Length	<10 fs (rms)
Beam Size	600 μm (rms)
Transv. Emittance	$0.03 \pi \text{ mm mrad}$

REGAE: Time-resolved Electron Diffraction

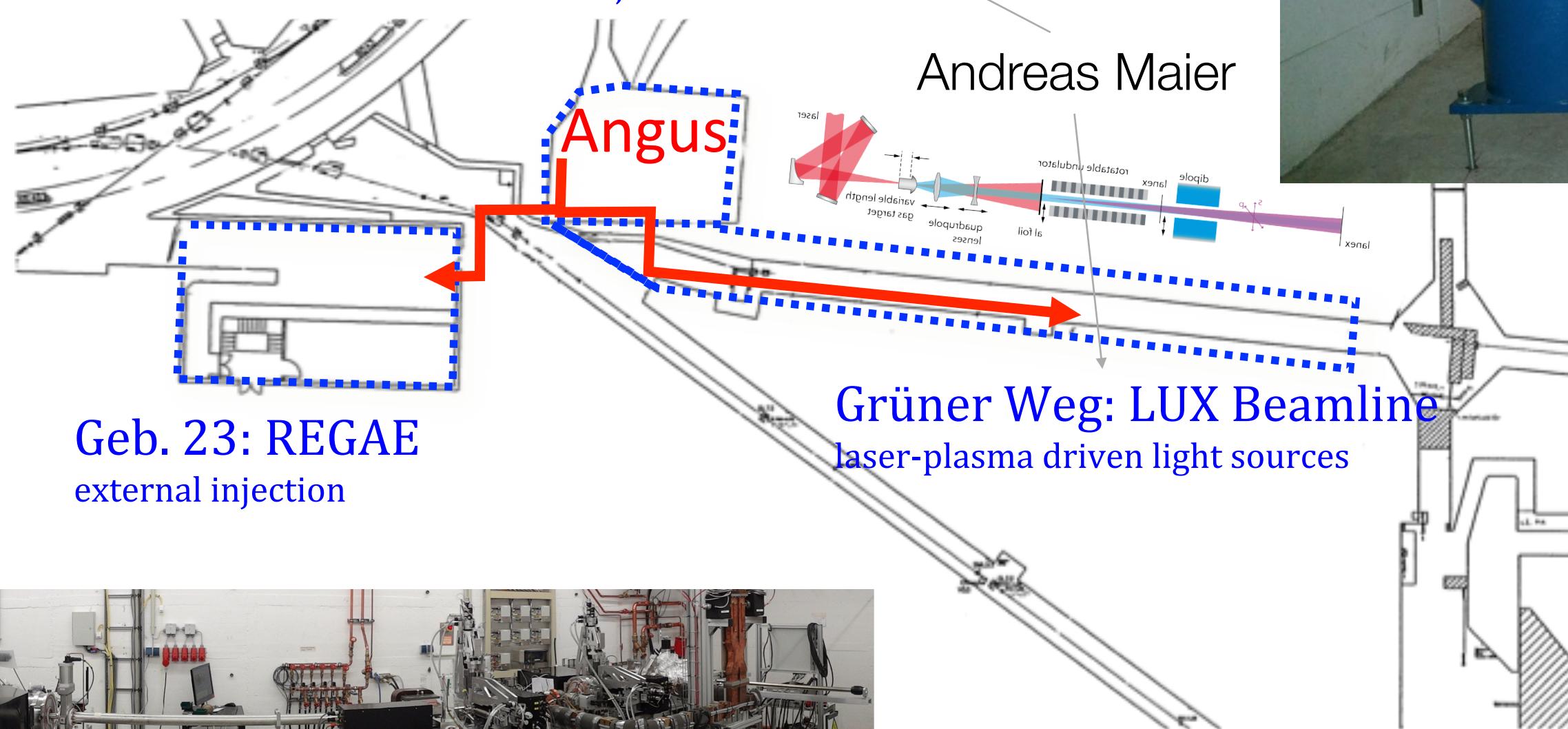
> „Design goal“



LAOLA@REGAE (& LUX Project)

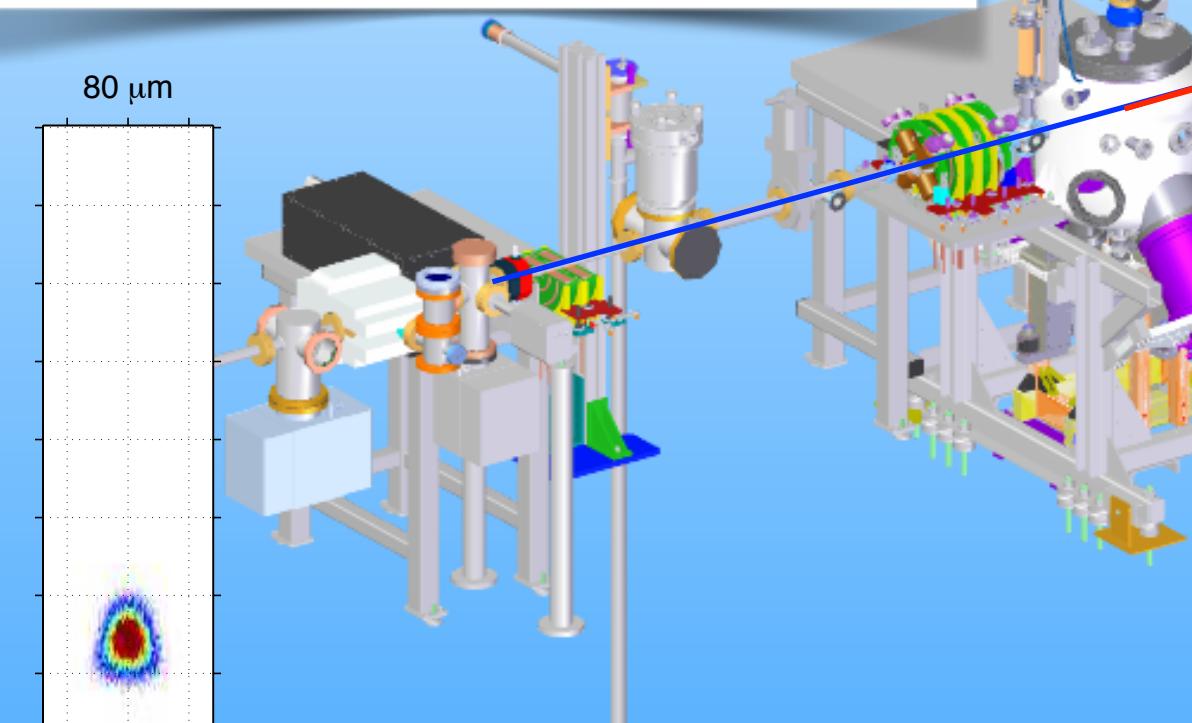
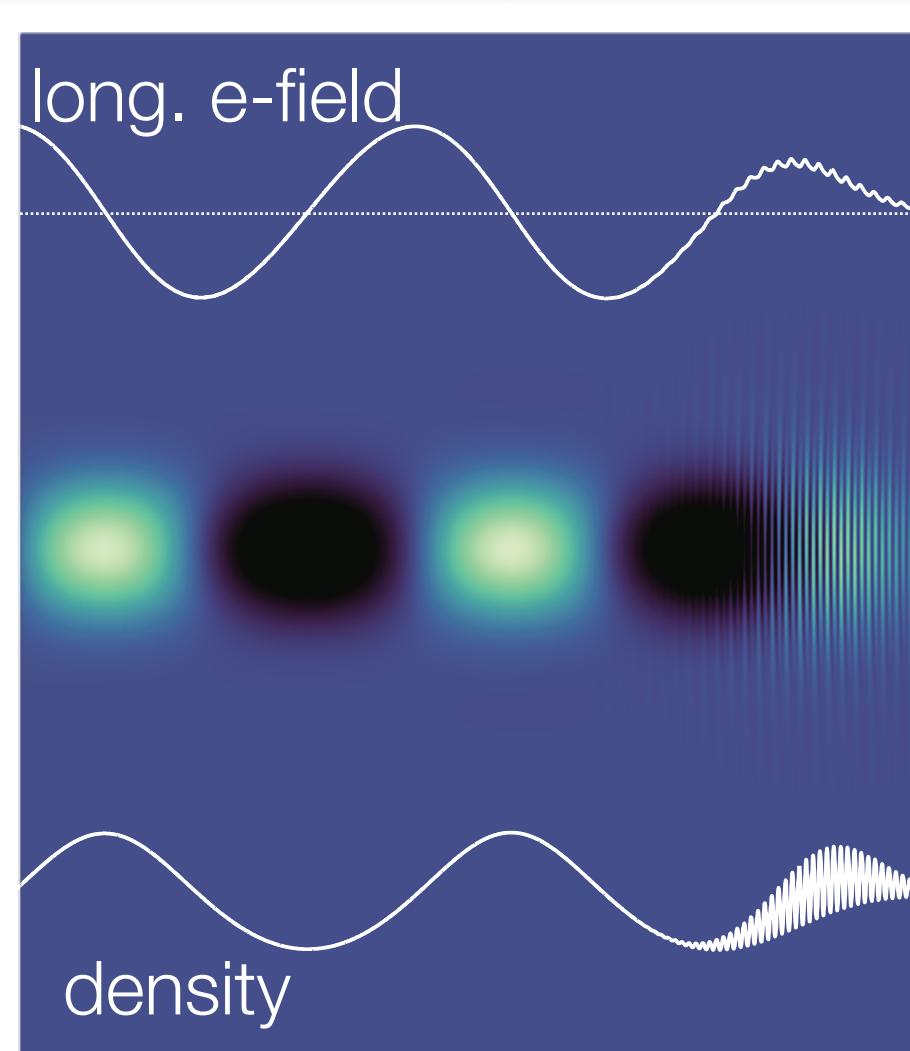
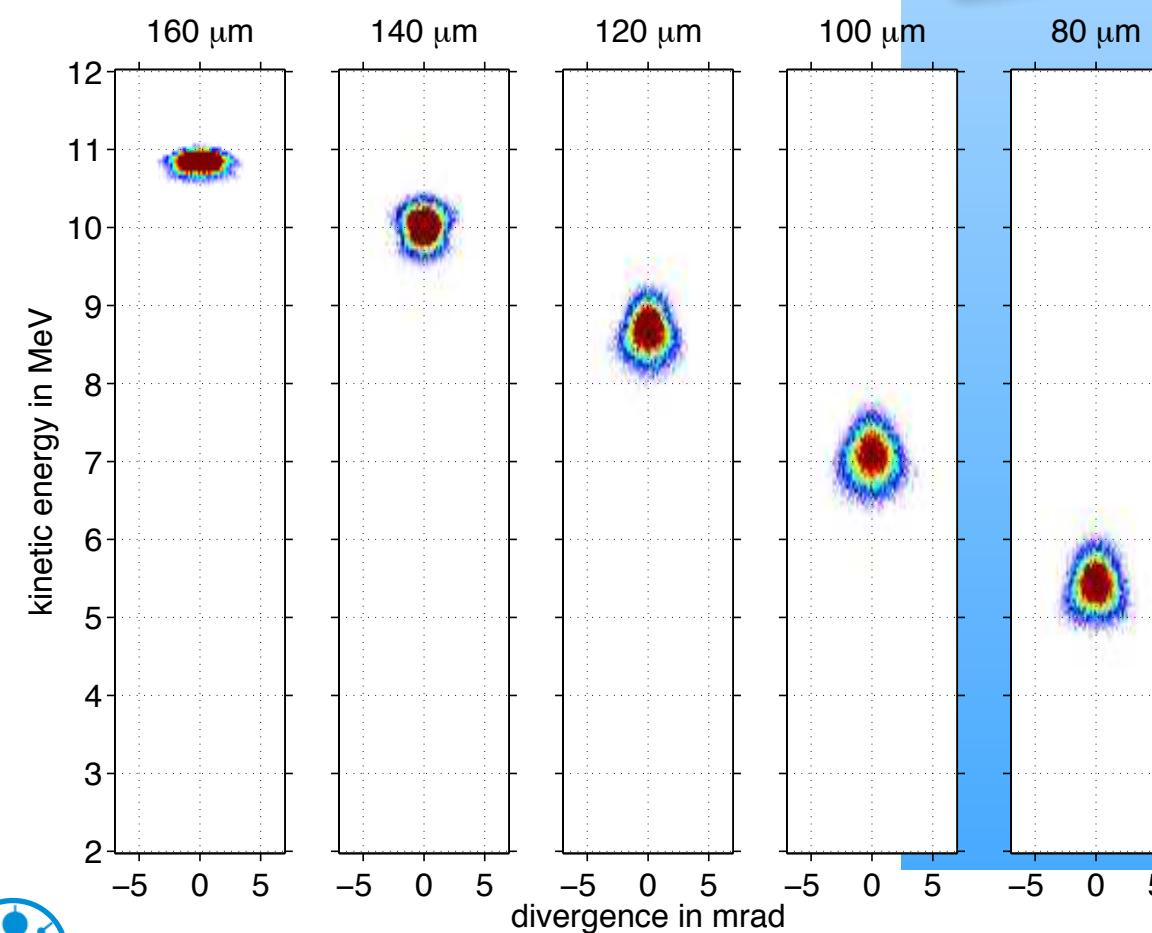


Geb. 22: New Laserlab
ANGUS, a new 200 TW laser



LAOLA@REGAE: External Injection

- > Goal: Mapping the wake
- > REGAE: Conventional electron gun
- > ANGUS: 200 TW laser
- > Laser-pump, electron-probe experiment



Merging conventional and laser wakefield accelerators

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^cDeutsches Elektronen-Synchrotron (DESY), Hamburg, Germany

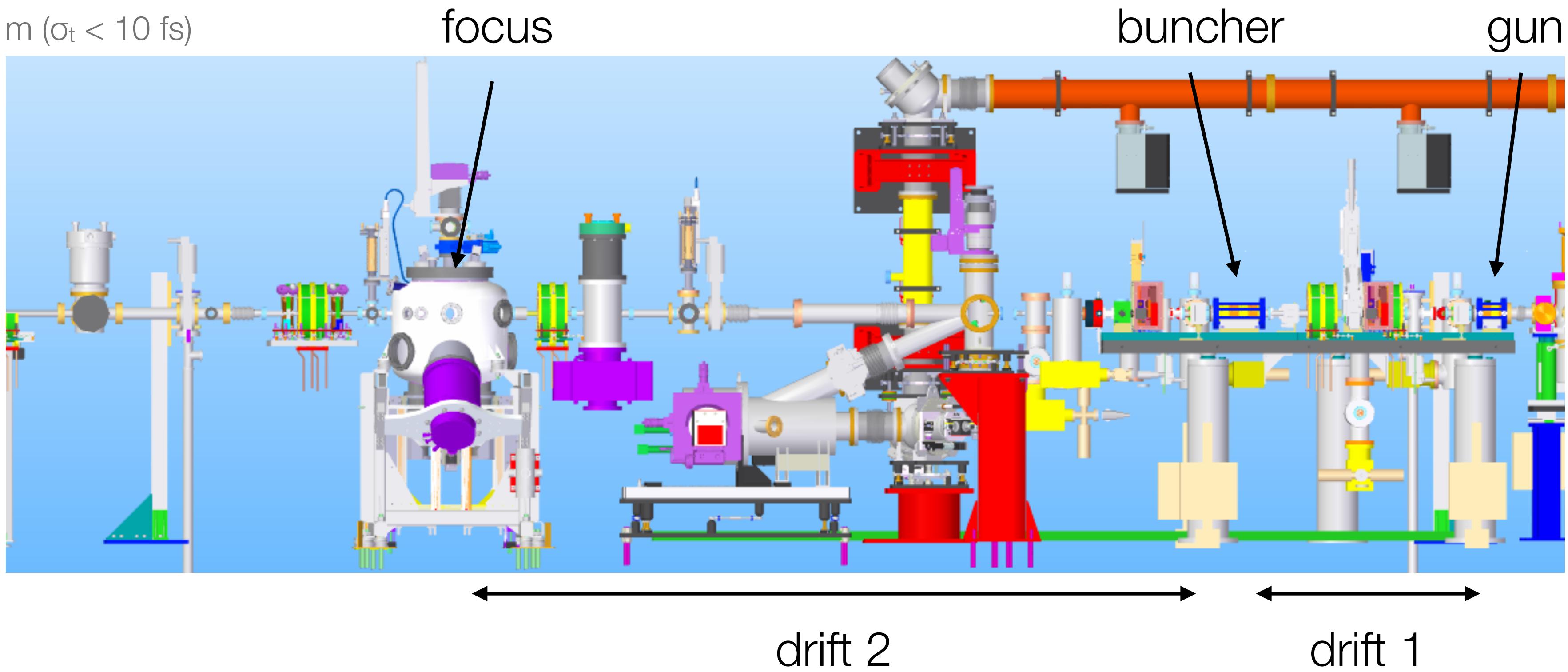
^dLudwig-Maximilians-Universität München, Munich, Germany

& contribution at EAAC2013

REGAE

> Relevant parameters:

- > Electron gun: $E_G \leq 120 \text{ MV/m}$, $z_G = 0 \text{ m}$
- > Buncher: $E_B = 10..40 \text{ MV/m}$, $z_B = 1.3 \text{ m}$
- > Focus: $z_F = 5.5 \text{ m}$ ($\sigma_t < 10 \text{ fs}$)
- > Drift 1: ~1 m
- > Drift 2: ~4 m

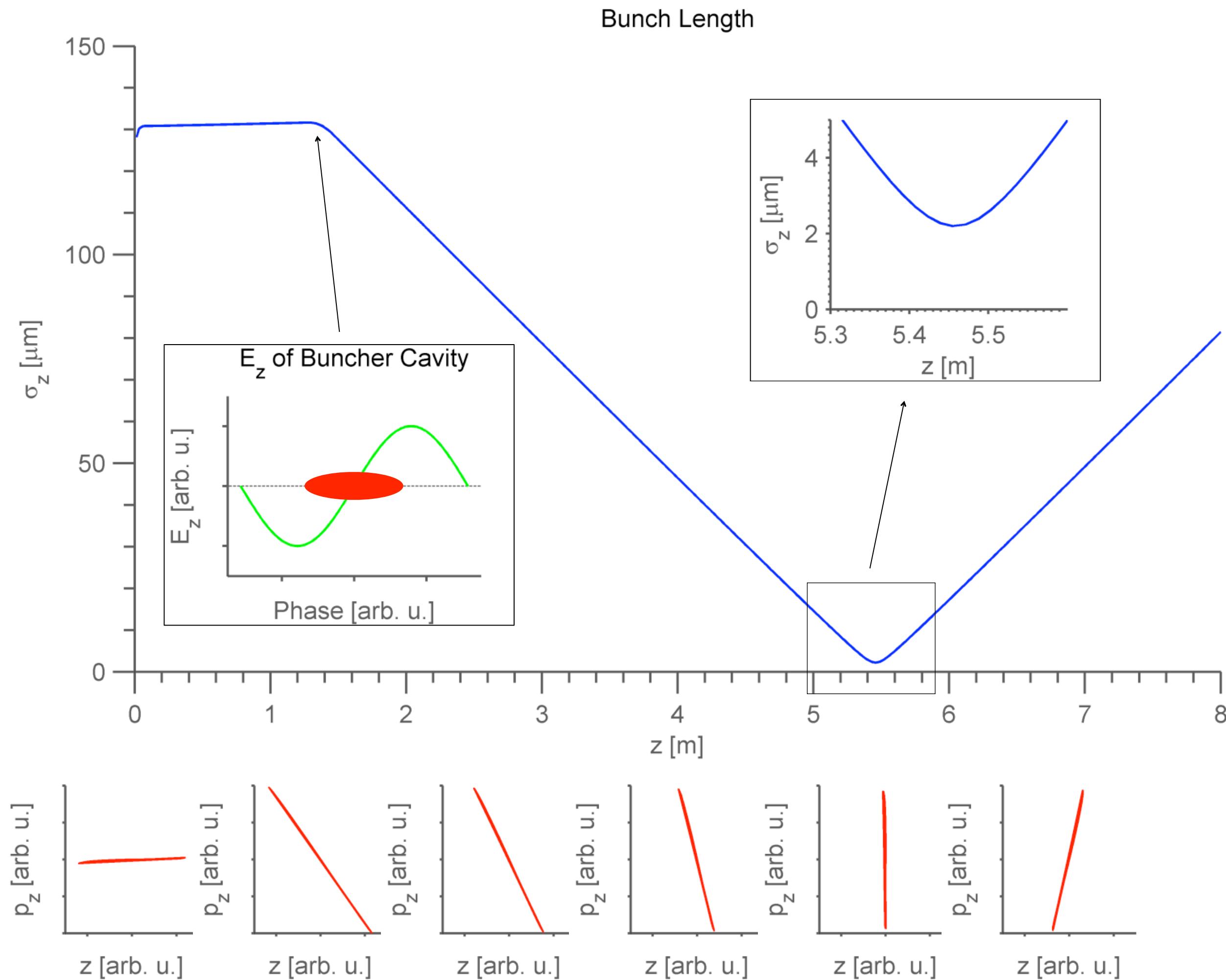


Ballistic Bunching: REGAE

- > Zero-crossing of buncher cavity
- > Linear correlated energy spread
- > +Drift: Longitudinal focusing
- > Result: Bunch length <10 fs

- > But...
- > Low energy (~5 MeV)
- > Low charge (~100 fC)

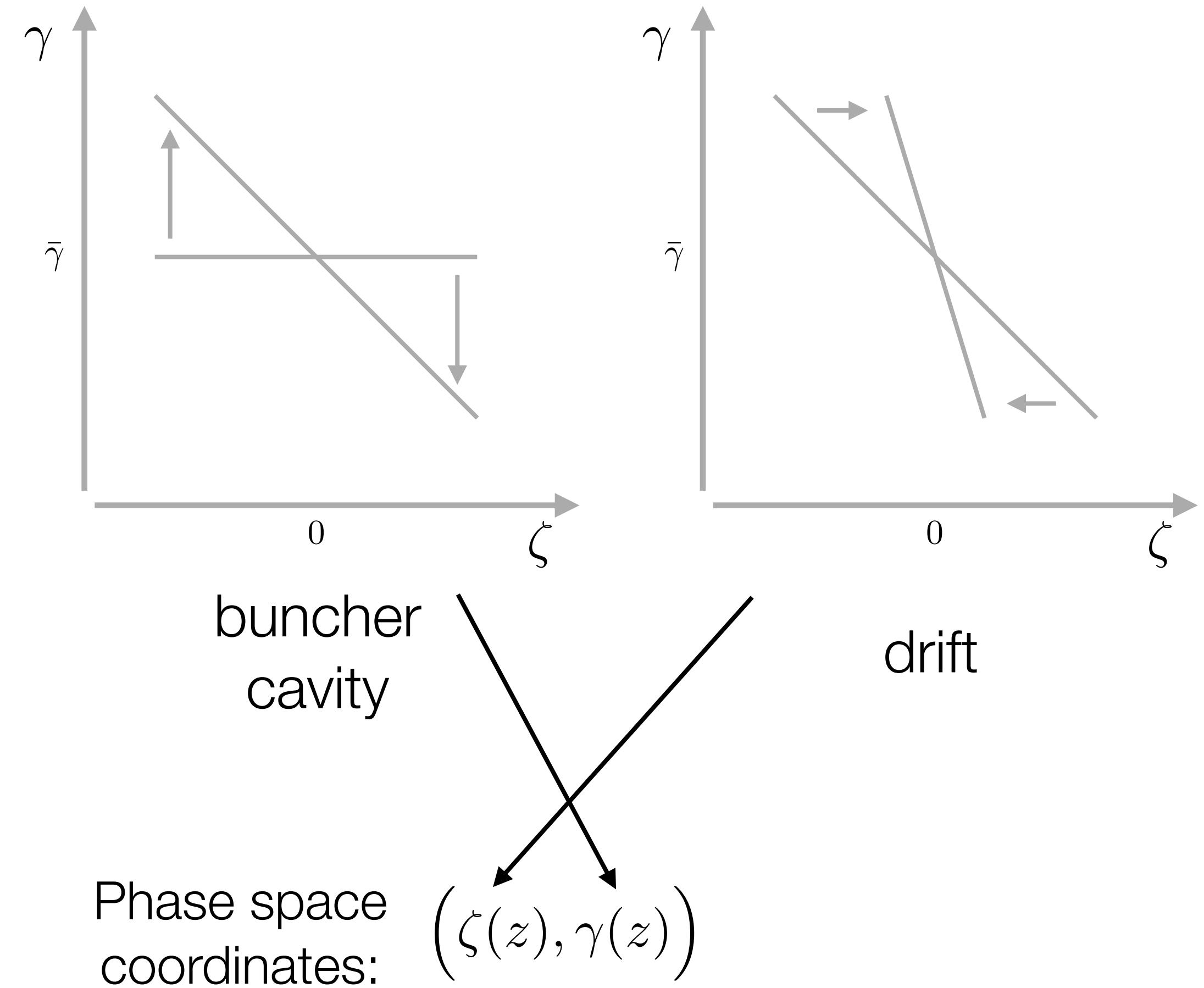
- > Limit(s) of bunch length?
- > Space charge repulsion
- > Phase space curvature



Ballistic Bunching: Phase Space Curvature

- > Basic concept:
 - > Linear correlated **velocity** spread
 - > Free drift leads to longitudinal focus
- > Note: Drift changes ζ , cavity changes γ
- > But... zero crossing of cavity:
 - > Linear correlated **energy** spread

$$\beta = \sqrt{1 - \frac{1}{\gamma^2}}$$

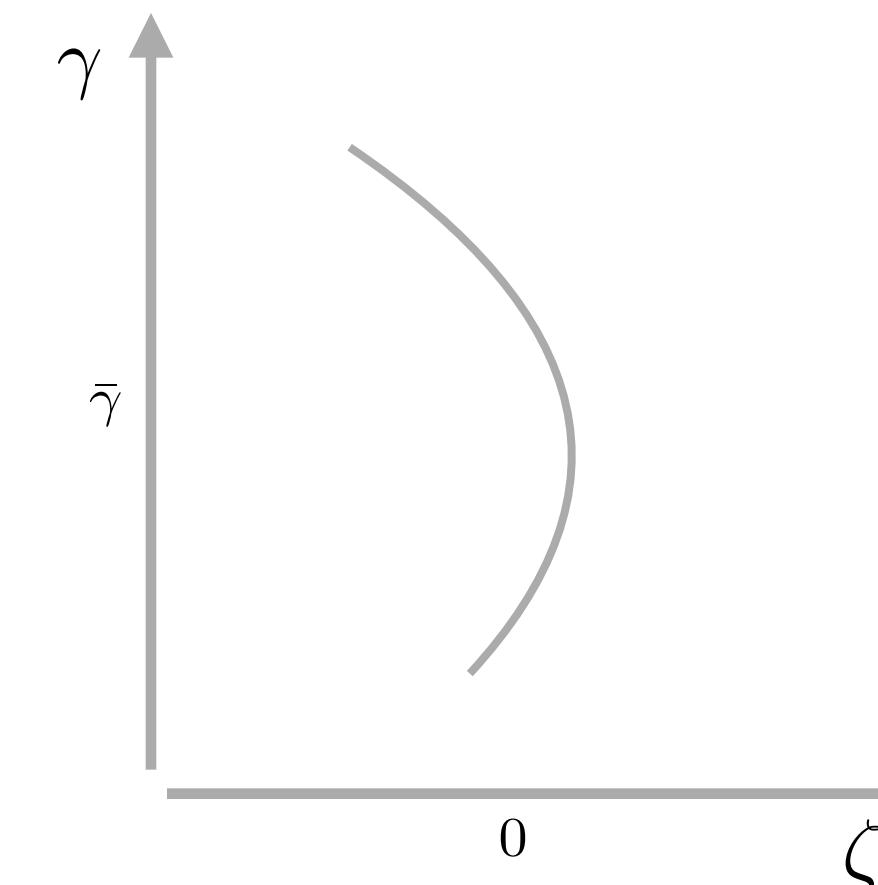
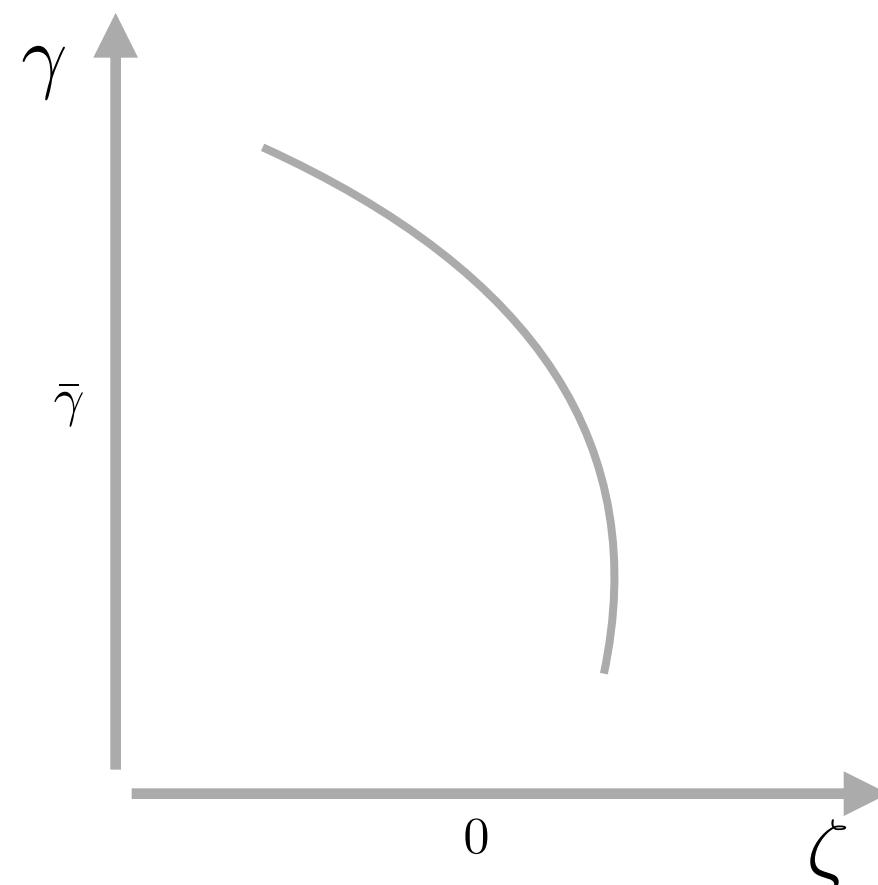
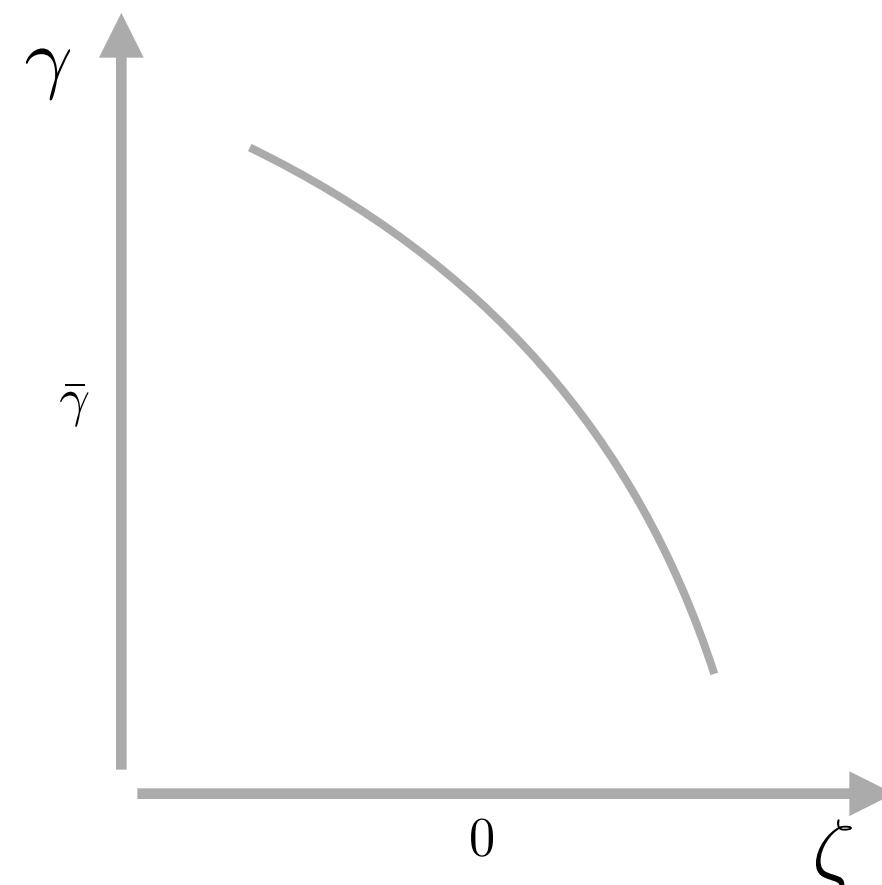


Ballistic Bunching: Phase Space Curvature

> Consequence?

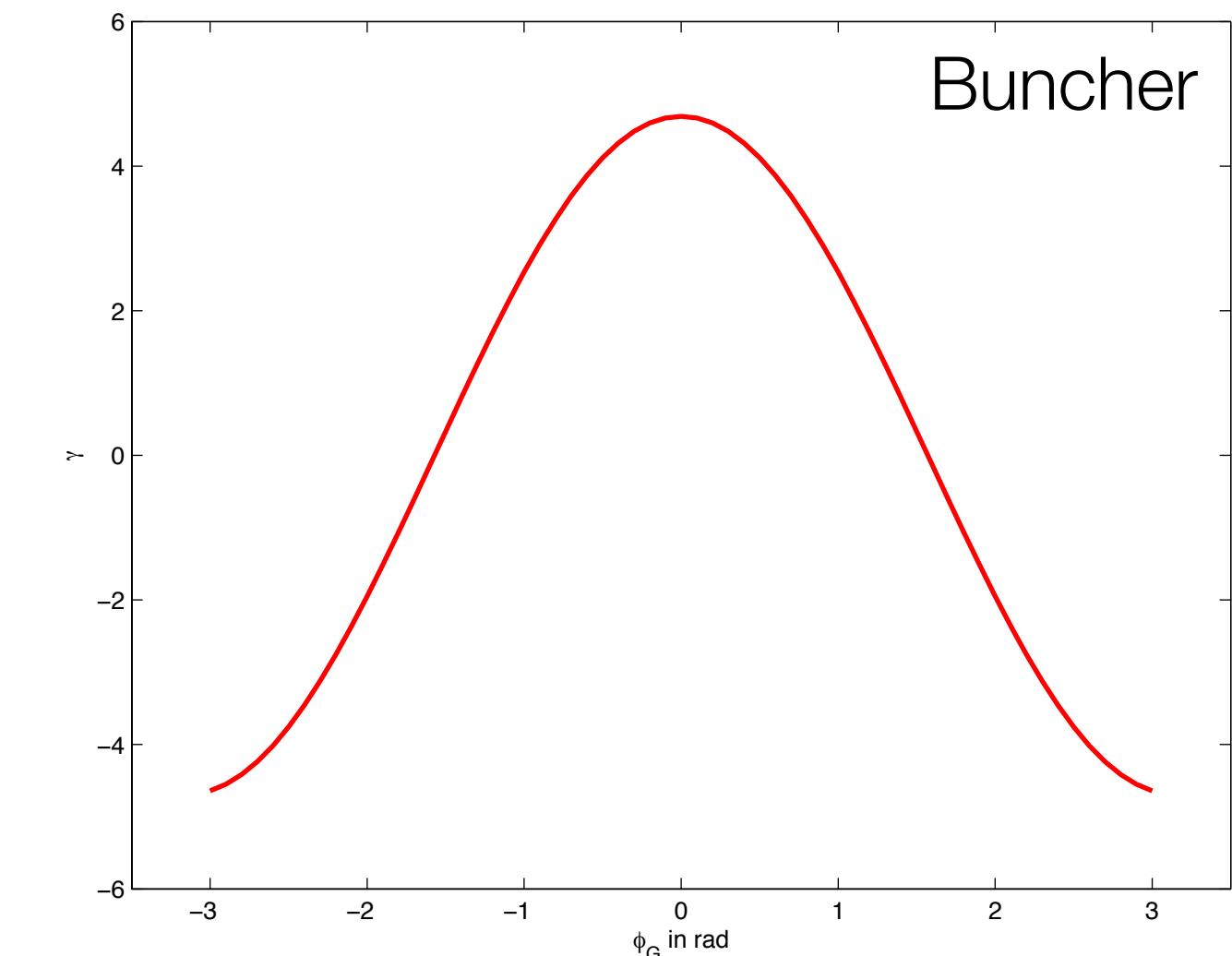
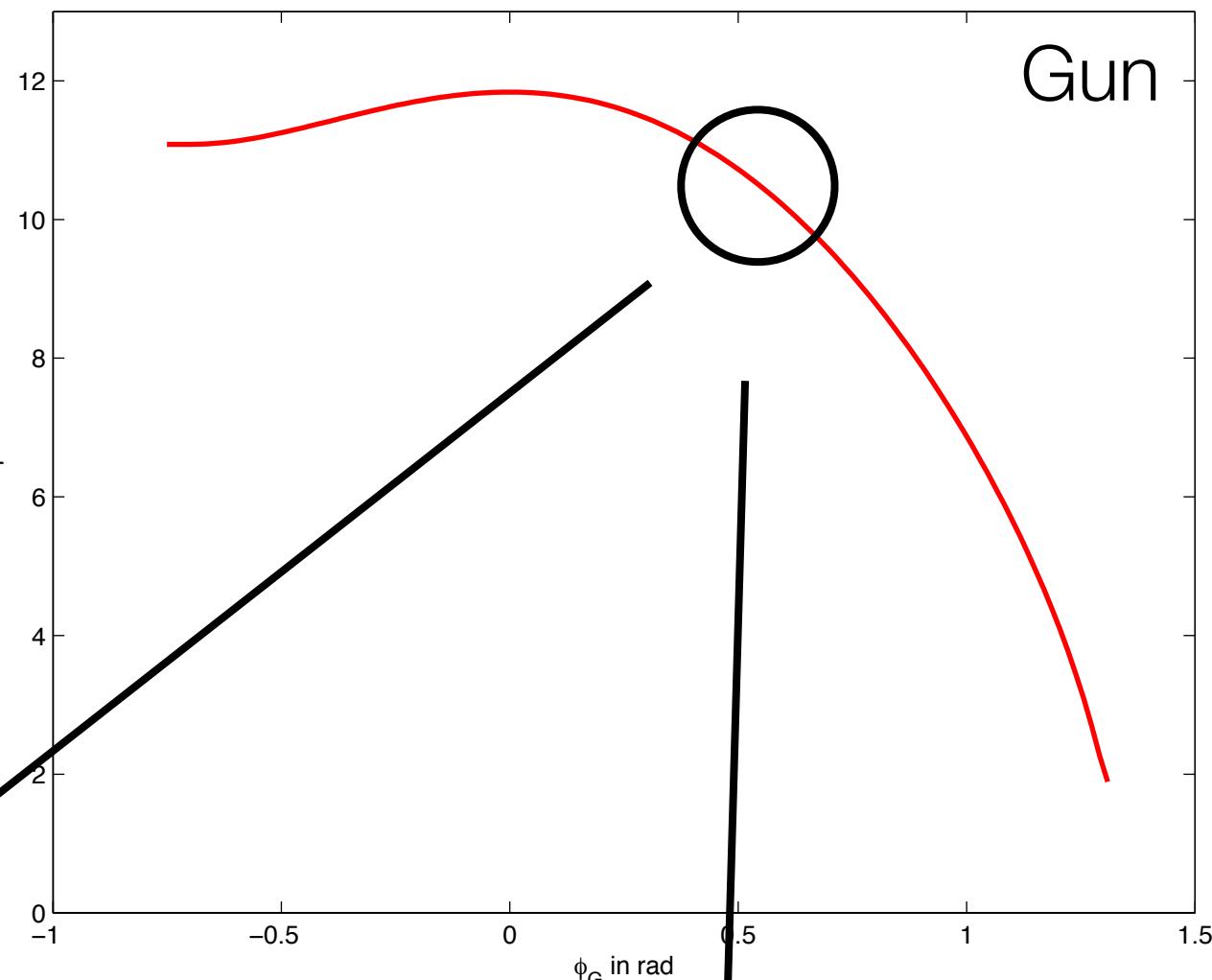
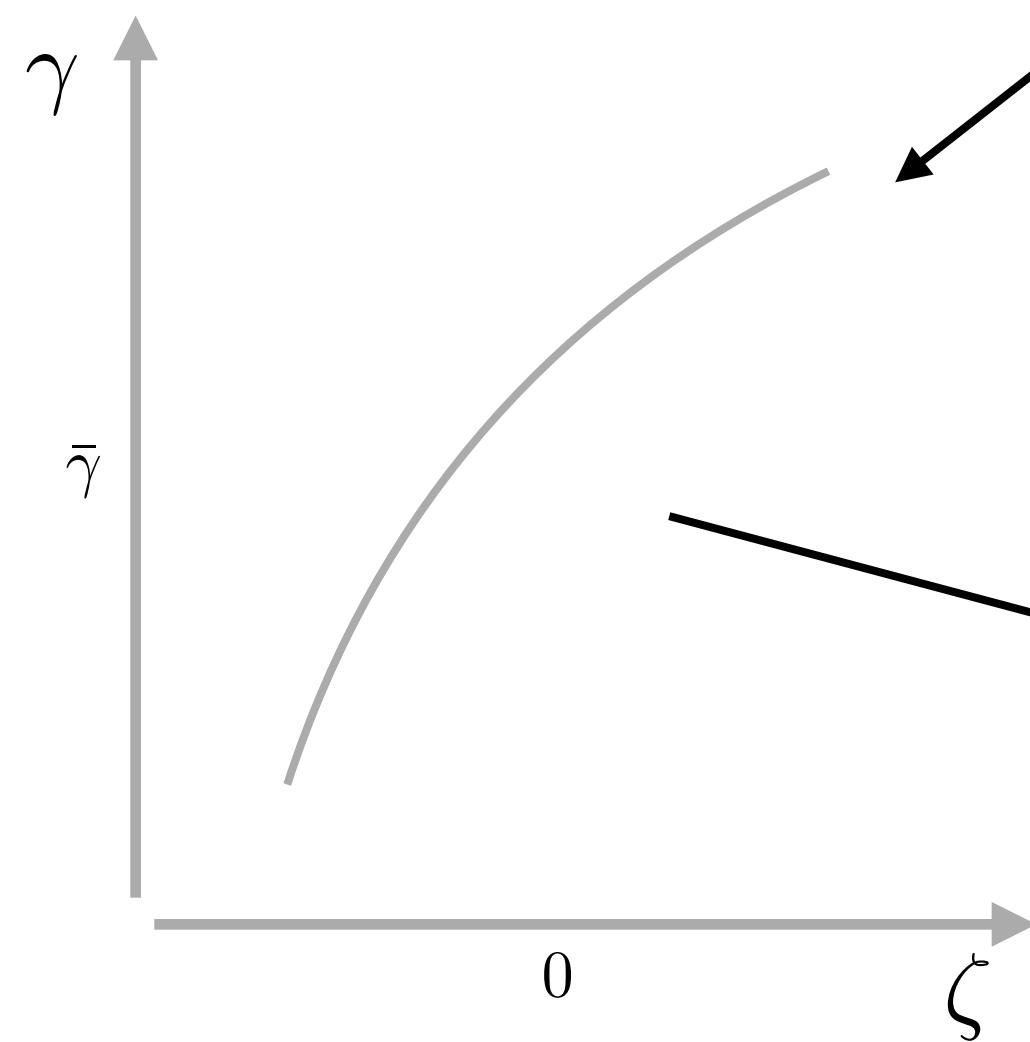
> Curvature due to drift!

$$\begin{aligned} \Delta\beta \cdot c &\quad \frac{1}{\beta c} \cdot (z - z_0) \\ \Delta\zeta(z) &= \Delta v \cdot (t(z) - t(z_0)) = \frac{1}{\beta} \Delta\beta(\gamma) \cdot (z - z_0) \\ &= \frac{1}{\bar{\beta}} \left[\frac{d\beta}{d\gamma} \Big|_{\bar{\gamma}} \cdot \delta\gamma + \frac{1}{2} \frac{d^2\beta}{d\gamma^2} \Big|_{\bar{\gamma}} \cdot (\delta\gamma)^2 + \frac{1}{6} \frac{d^3\beta}{d\gamma^3} \Big|_{\bar{\gamma}} \cdot (\delta\gamma)^3 + \dots \right]_{z_0} \cdot (z - z_0) \\ &= \left[\underbrace{\frac{1}{\bar{\gamma}^3 \bar{\beta}^2} \cdot \delta\gamma}_{\eta_1(\bar{\gamma})} + \underbrace{\frac{2 - 3\bar{\gamma}^2}{2\bar{\gamma}^6 \bar{\beta}^4} \cdot (\delta\gamma)^2}_{\eta_2(\bar{\gamma})} + \underbrace{\frac{2 - 5\bar{\gamma}^2 + 4\bar{\gamma}^4}{2\bar{\gamma}^9 \bar{\beta}^6} \cdot (\delta\gamma)^3}_{\eta_3(\bar{\gamma})} + \dots \right]_{z_0} \cdot (z - z_0) \end{aligned}$$



Ballistic Bunching: Phase Space Curvature

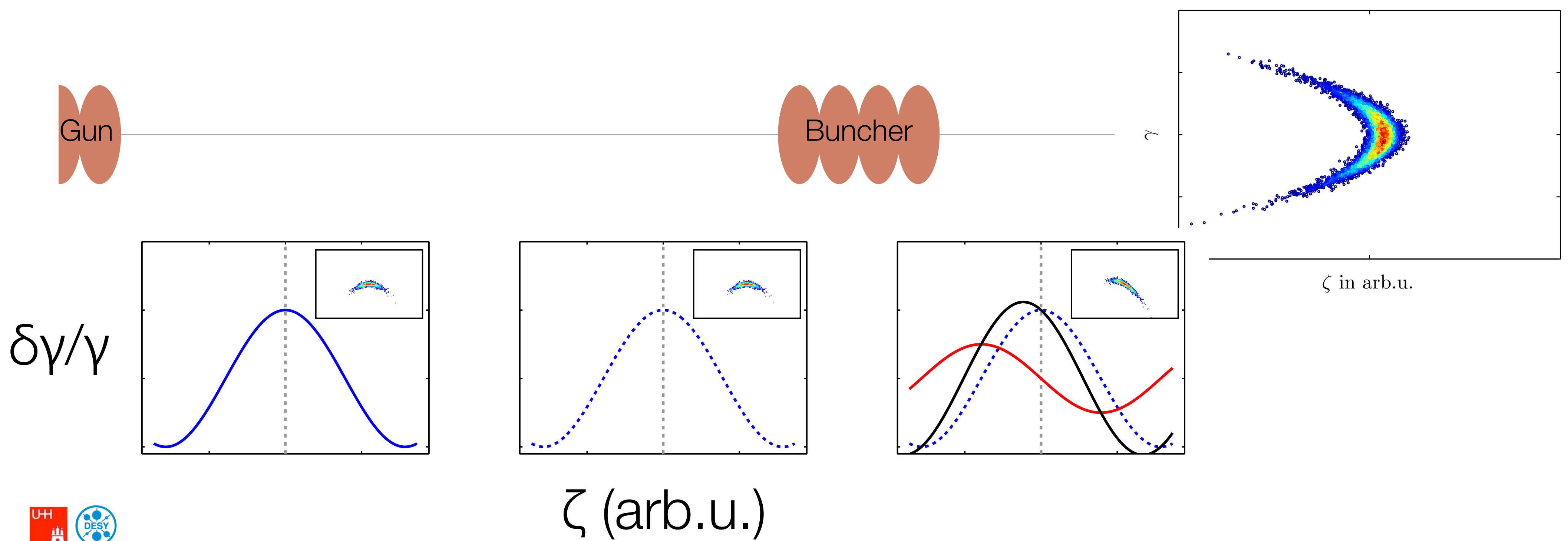
- > But: Linear correlated **energy** spread?
- > Only to first order
- > General description... curved
 - > Polynomial/Taylor expansion



$$\gamma(\zeta_0) = \underbrace{A_0}_{\bar{\gamma}} + \underbrace{A_1 \zeta_0 + A_2 \zeta_0^2 + A_3 \zeta_0^3}_{\delta\gamma(\zeta_0)}$$

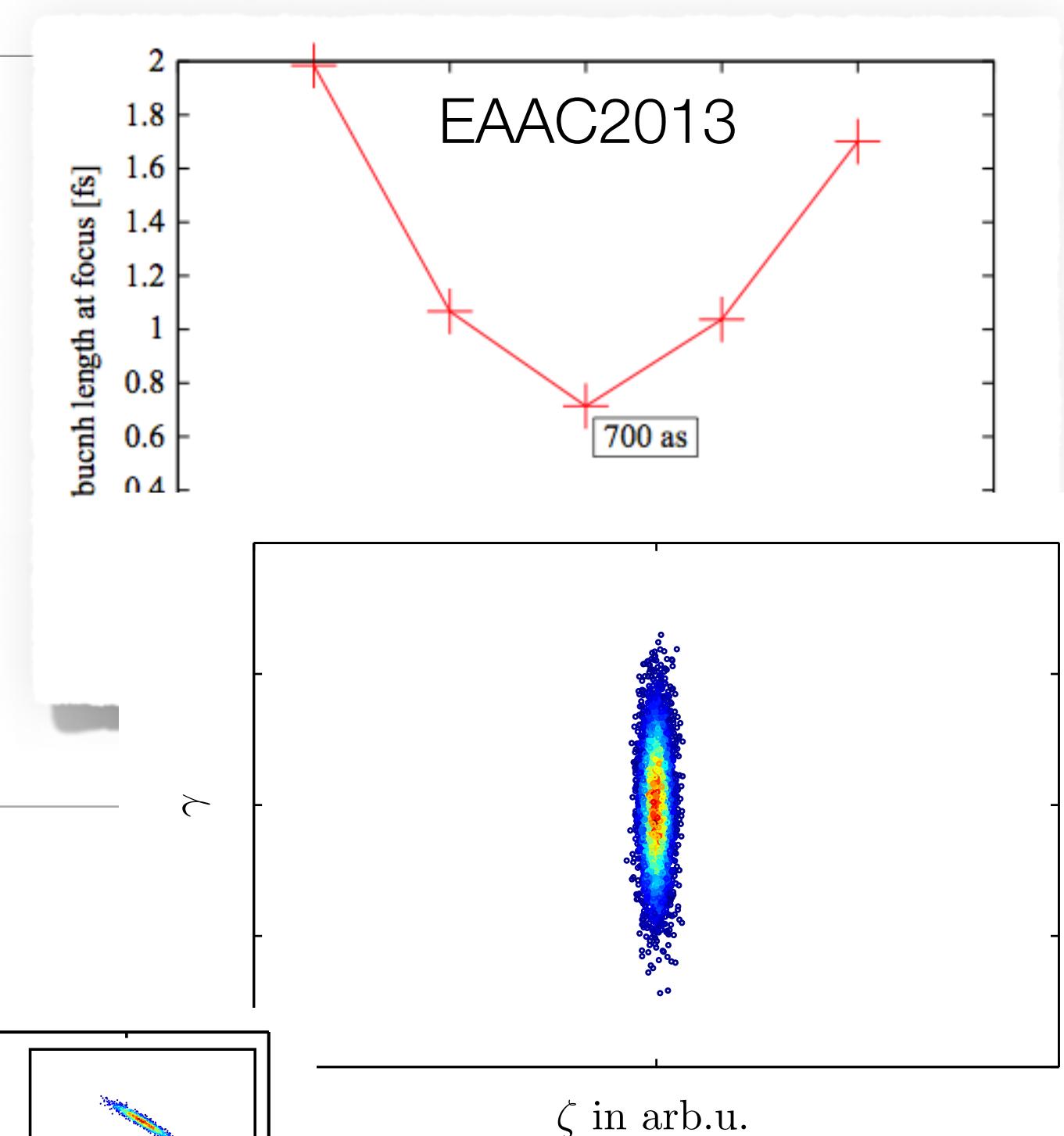
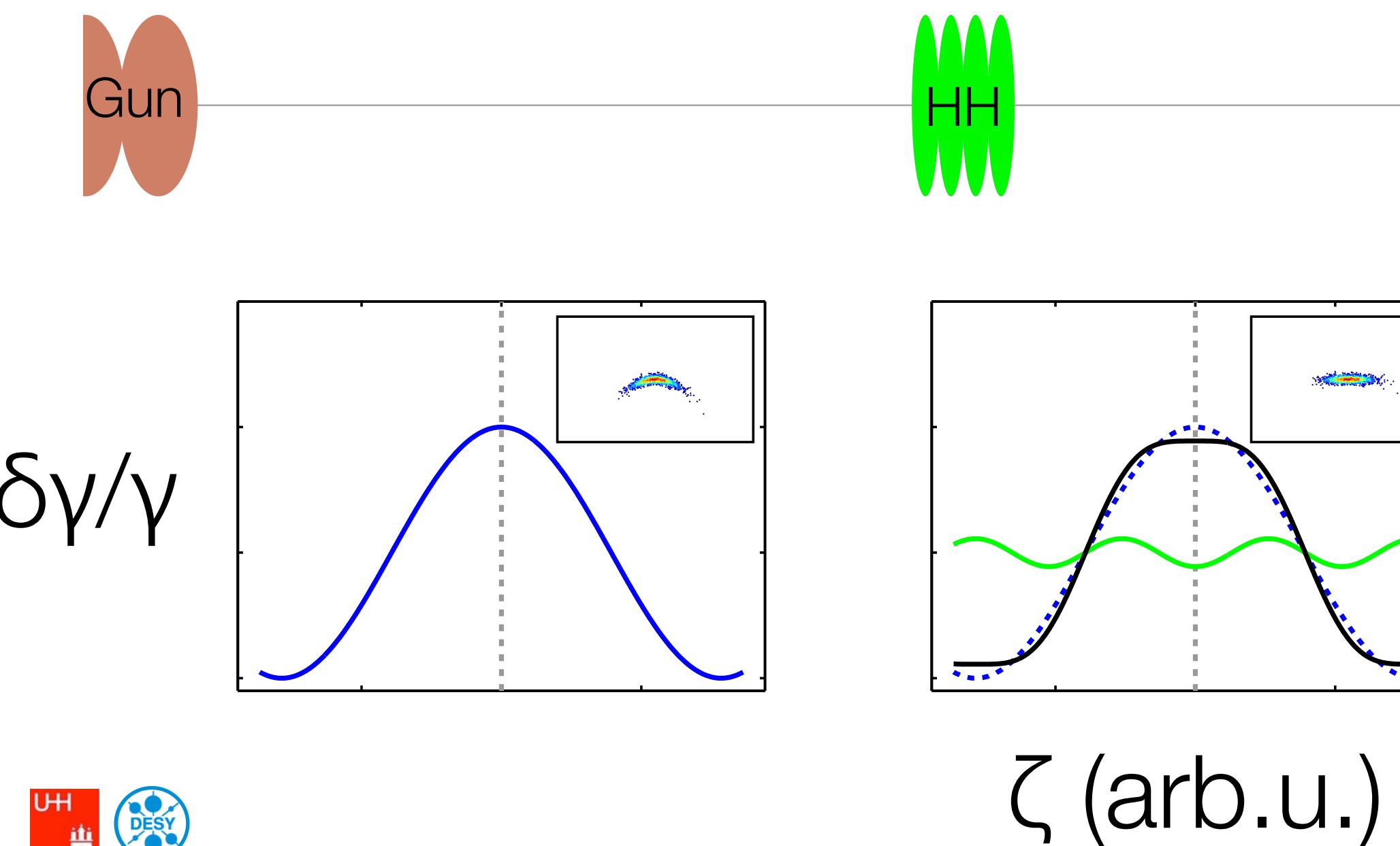
Phase Space Linearization

- > Simplified problem:
 - > Curvature only from cavities
 - > No non-linear evolution in drift



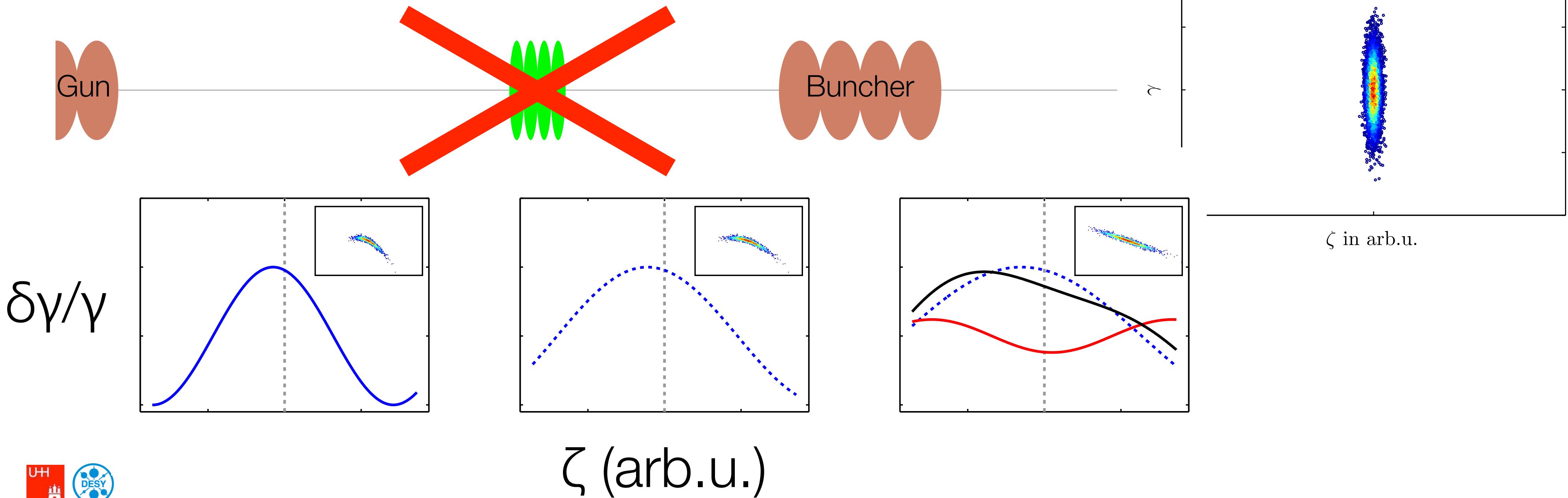
Phase Space Linearization

- > Solution 1: 3rd harmonic cavity
- > (Fourier series: Plateau by summation of uneven frequencies)
- > Works: 700 as (K. Floettmann, Nucl. Instr. Meth. Phys. Res. A, Vol. 740, 2014)
- > No space & money: X-band structure...



Phase Space Linearization

- > Solution 2: Stretcher mode
 - > Gun settings: (far) off-crest
 - > Beam expansion between gun and buncher
 - > pseudo HH with **same** RF system as gun



Stretcher Mode: Method

- > Analytic description of bunch dynamics in gun, drift(s) & buncher in phase space
 - > Third order polynomial in ζ —> three coefficient-equations X_i
 - > Four free parameters (cavity fields & phases)
- > Optimization with Astra (and Matlab):
 - > Seed parameters from analytical method
 - > Longitudinal rms emittance: measure for nonlinearities
 - > Match minimum of emittance and bunch length
 - > Two parameters —> buncher phase/amplitude
- > Note: Publication with referees (PRSTAB)

$$\zeta_z = \zeta_B + \Delta\zeta(z) = X_1\zeta_B + X_2\zeta_B^2 + X_3\zeta_B^3$$

$$X_1 := 1 + (z - z_B) \cdot [H_1 S_1]$$

$$X_2 := (z - z_B) \cdot [H_1 S_2 + H_2 S_1^2]$$

$$X_3 := (z - z_B) \cdot [H_1 S_3 + 2H_2 S_1 S_2 + H_3 S_1^3]$$

S_i=a_i+B_i: Sum of γ-Coefficients
H_i=n_i(a₀+B₀)



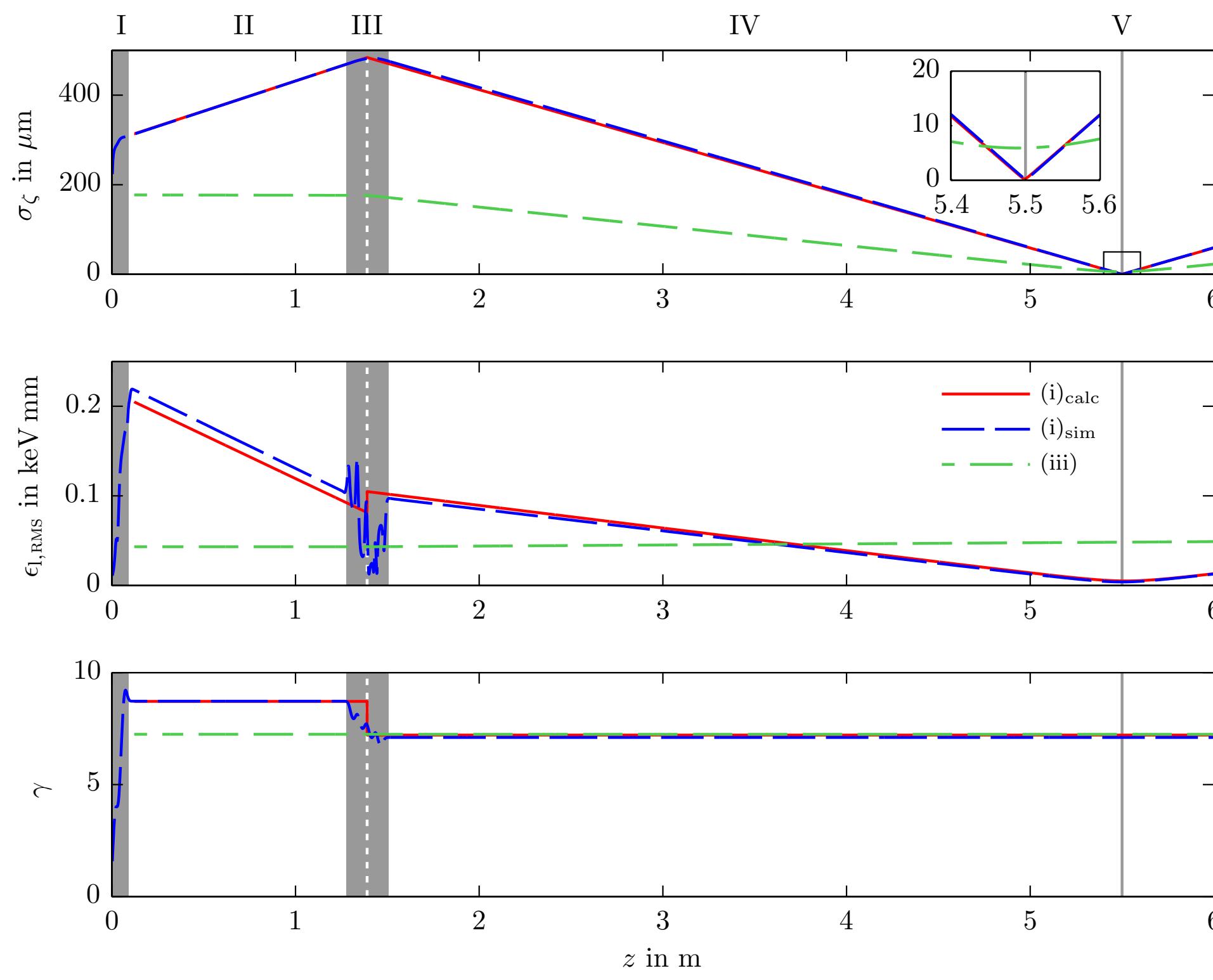
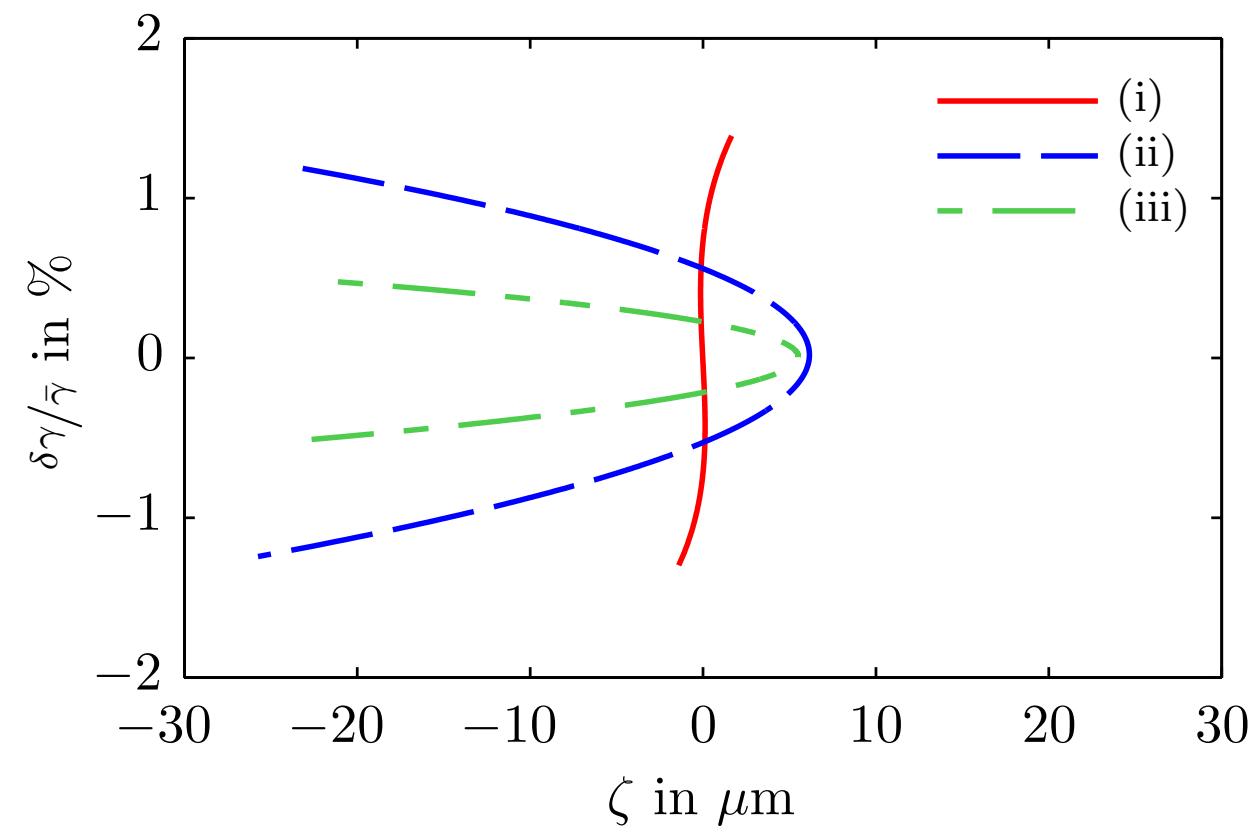
Applications: Second Order

> Comparison of theory and simulation: case (i)

> Calc & sim: $E_G = 100.0 \text{ MV/m}$, $\phi_G = 34.1 \text{ deg}$
 Calc: $E_B = 21.2 \text{ MV/m}$, $\phi_B = -109.3 \text{ deg}$
 Sim: $E_B = 21.7 \text{ MV/m}$, $\phi_B = -112.0 \text{ deg}$

> Standard bunching scheme: case (iii)

> Calc: $E_G = 70.0 \text{ MV/m}$, $\phi_G = 0.0 \text{ deg}$
 Calc: $E_B = 6.6 \text{ MV/m}$, $\phi_B = -90.0 \text{ deg}$



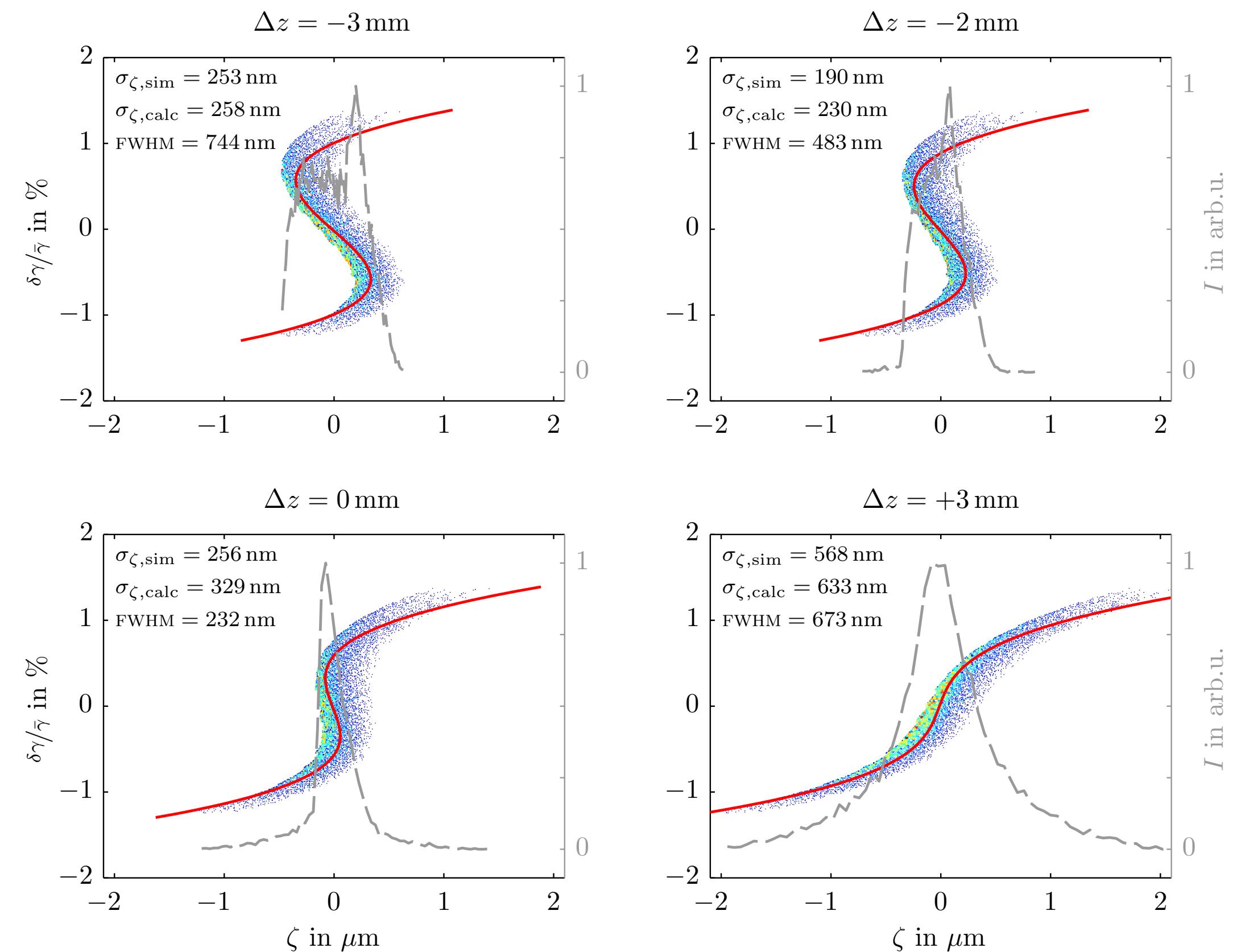
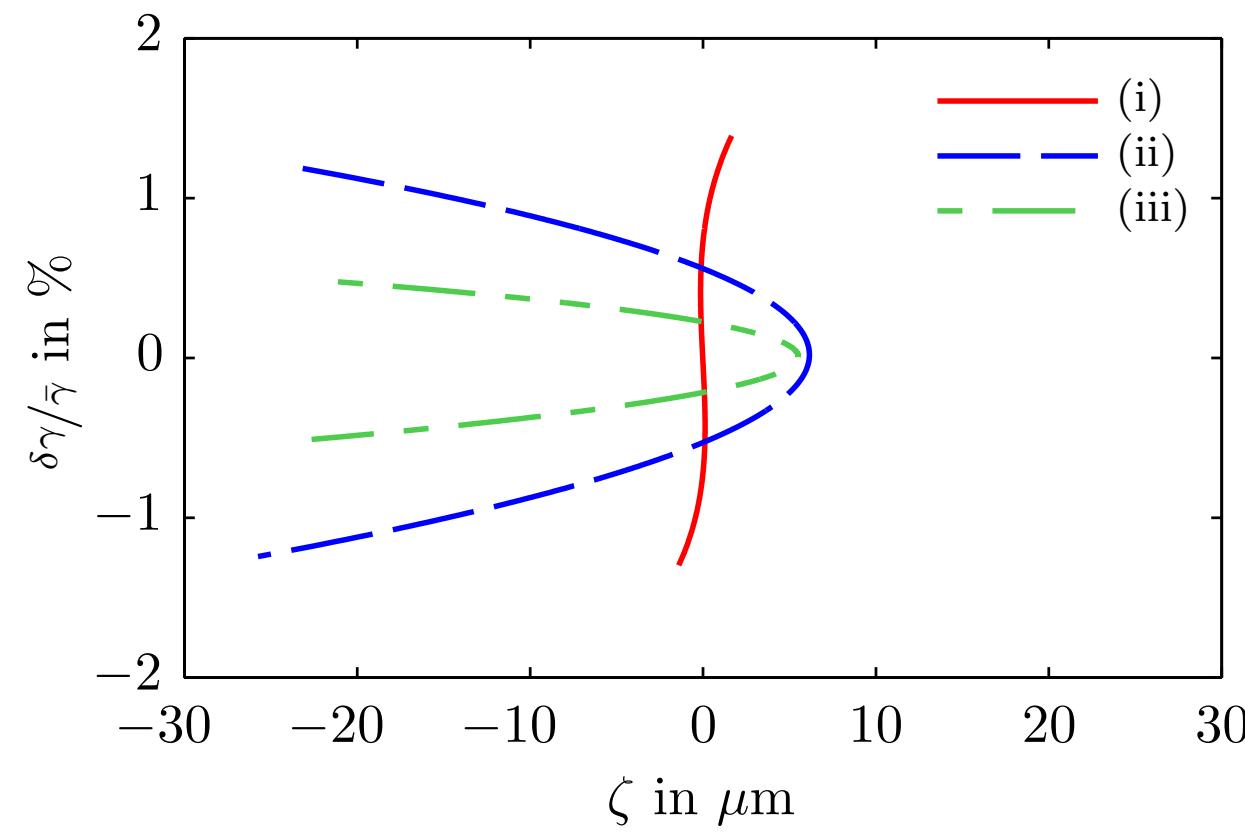
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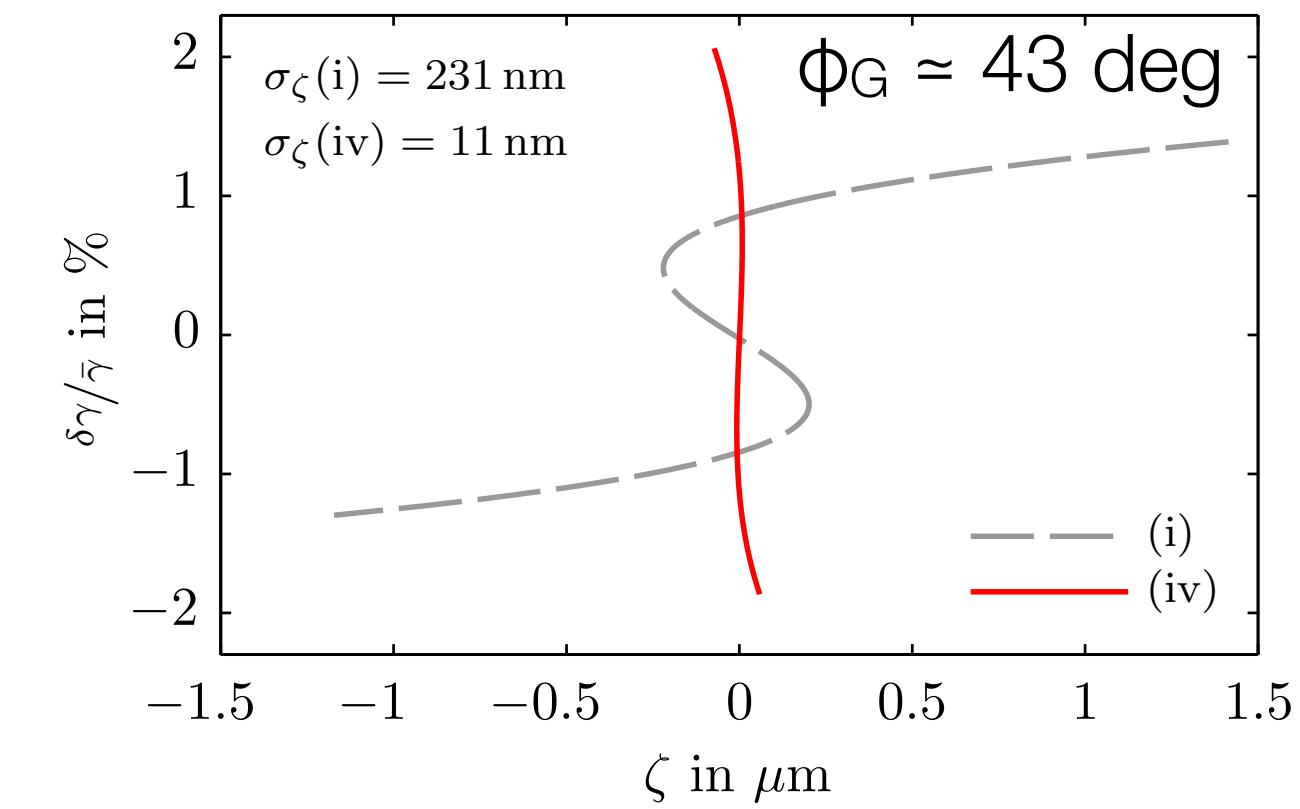
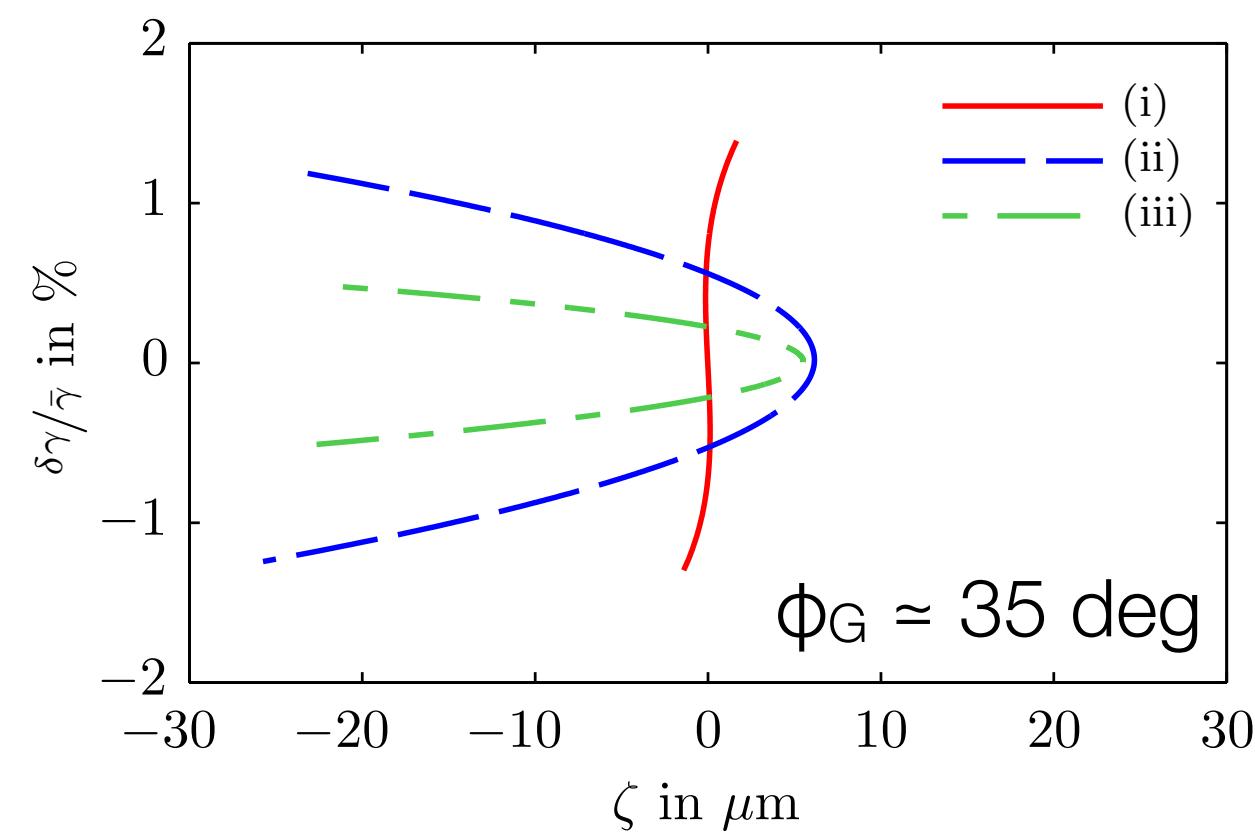
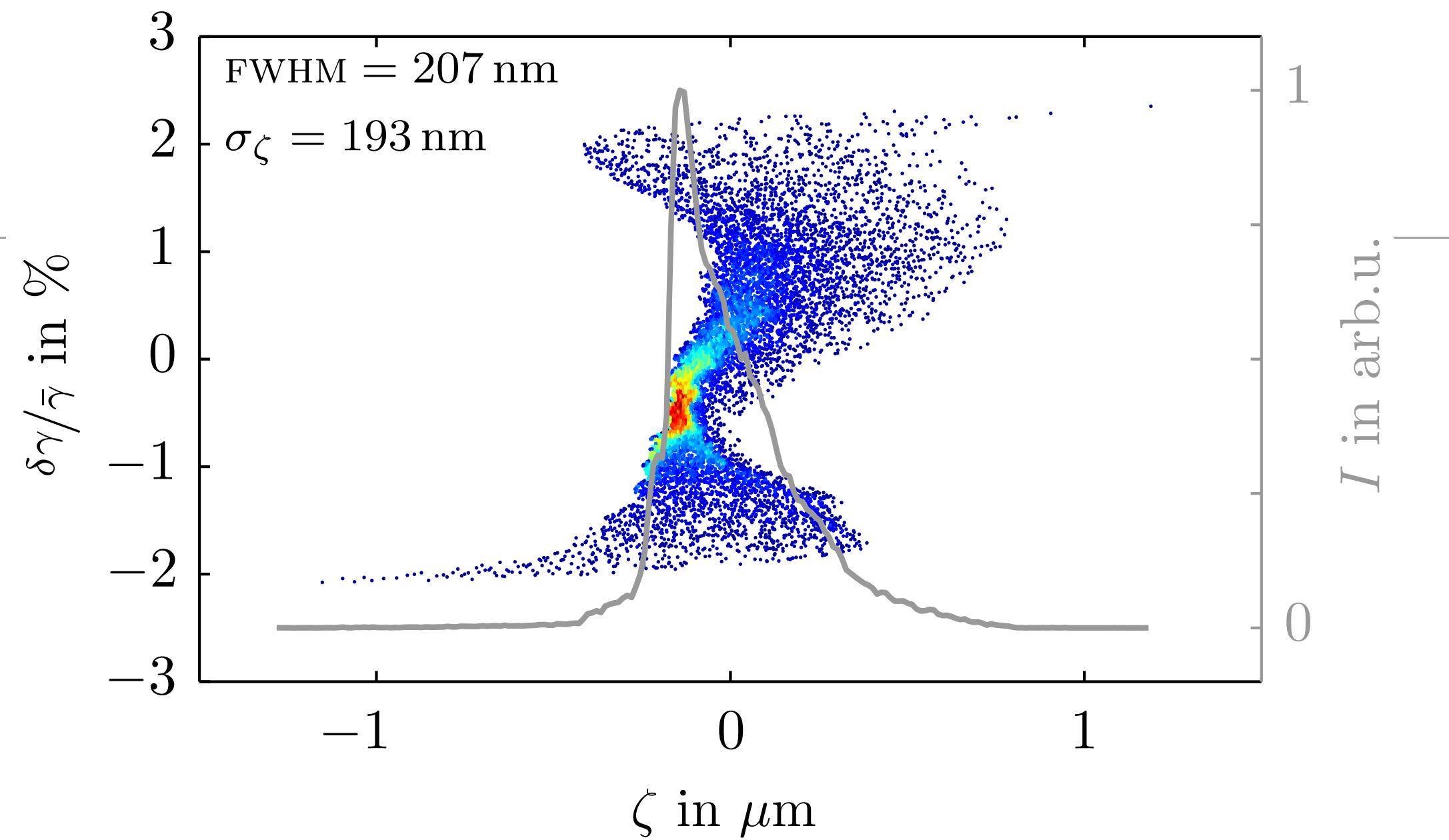
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Applications: Third Order

- > Use of gun phase ϕ_G
- > Gun: $E_G = 120.0 \text{ MV/m}$, $\phi_G = 44.3 \text{ deg}$
Buncher: $E_B = 29.3 \text{ MV/m}$, $\phi_B = -97.5 \text{ deg}$
- > $Q = 50 \text{ fC}$
- > $E_{\text{kin}} = 3.7 \text{ MeV}$
- > $\sigma_\zeta = 175 \text{ nm} \triangleq 580 \text{ as}$



Applications...

> How about...

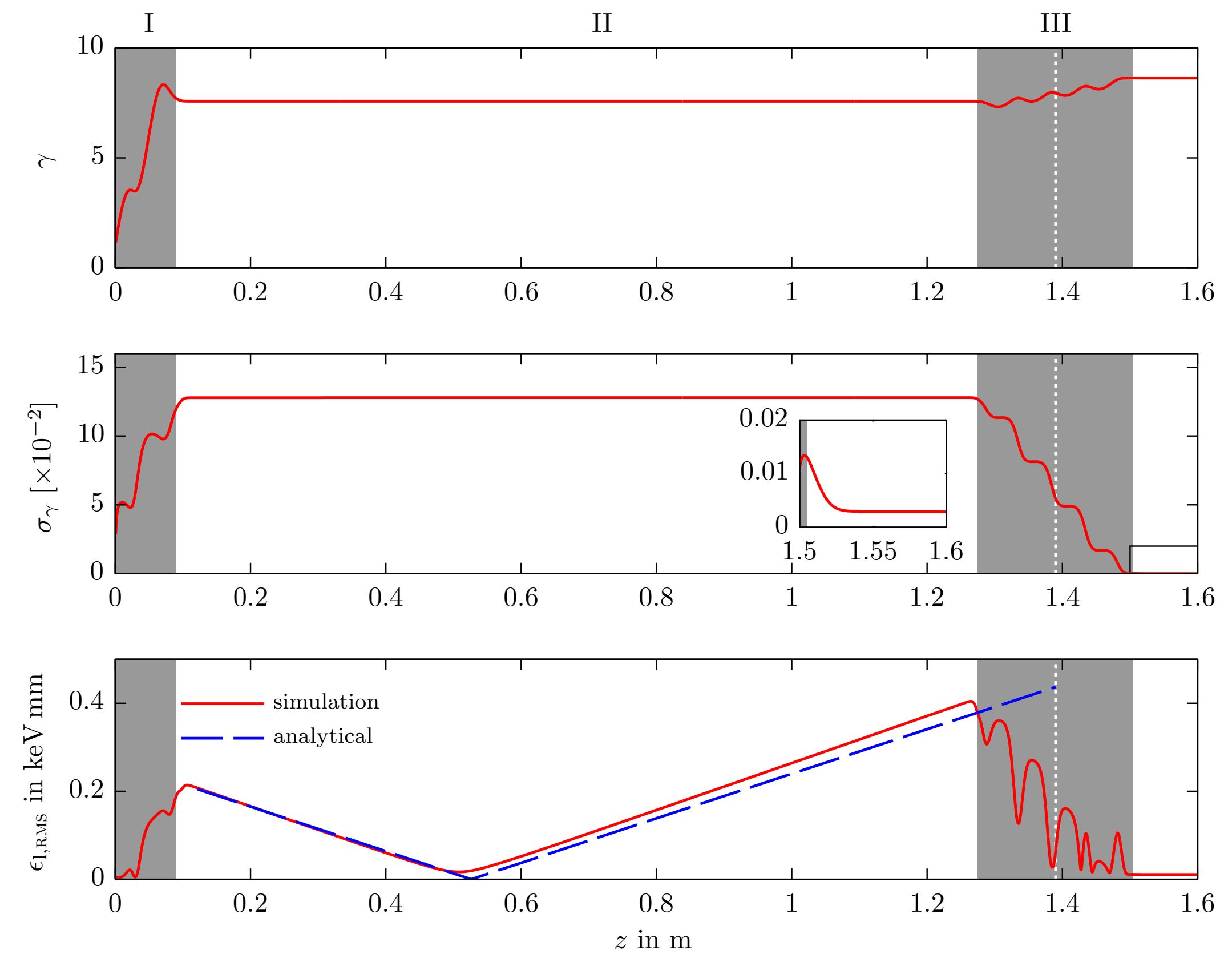
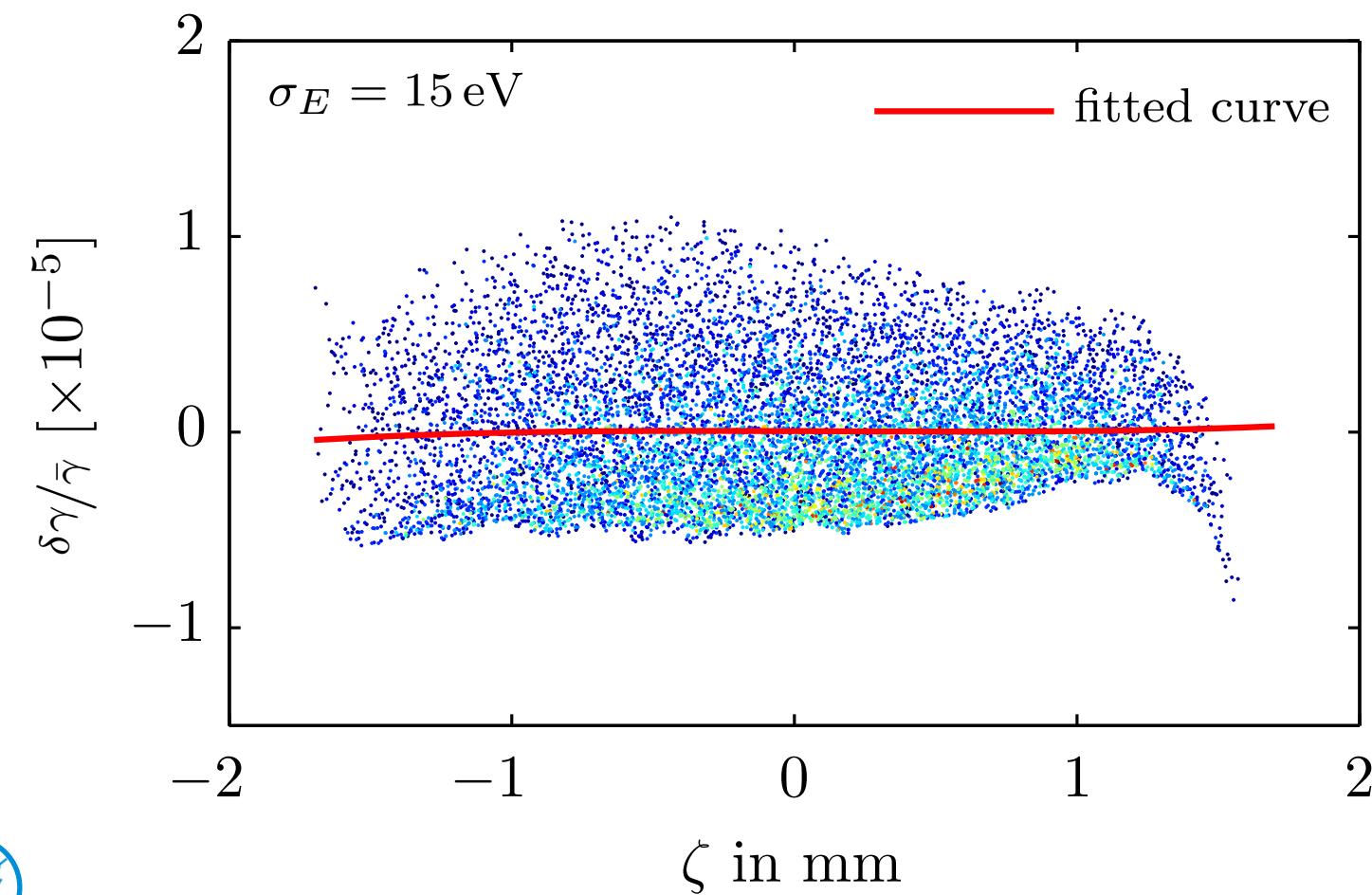
> Gun: $E_G = 100.0 \text{ MV/m}$, $\phi_G = 45.7 \text{ deg}$
Buncher: $E_B = 14.1 \text{ MV/m}$, $\phi_B = -69.9 \text{ deg}$

> $Q = 50 \text{ fC}$

> $E_{\text{kin}} = 3.9 \text{ MeV}$, $\sigma_{E_{\text{kin}}} = 15 \text{ eV}$

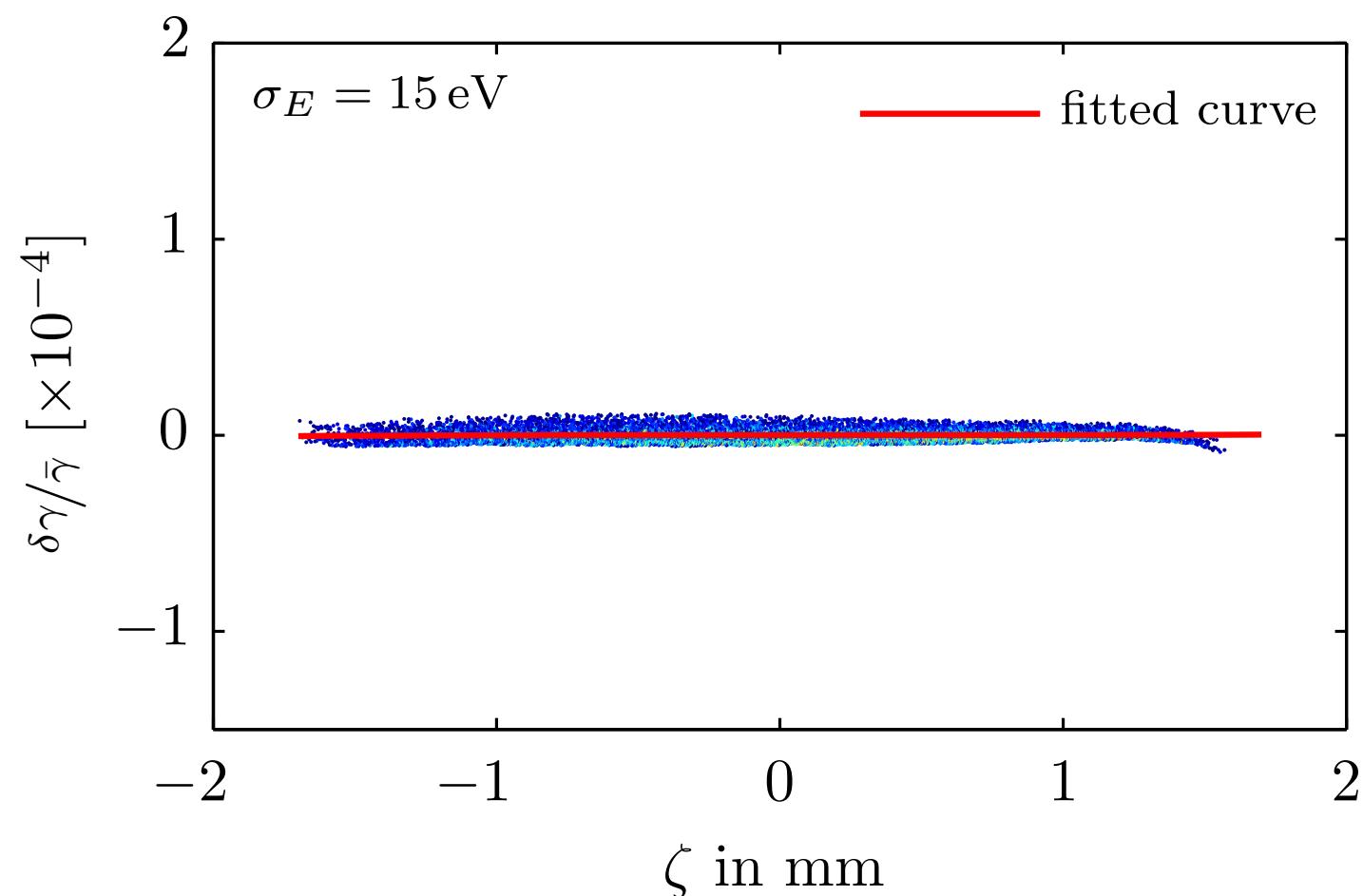
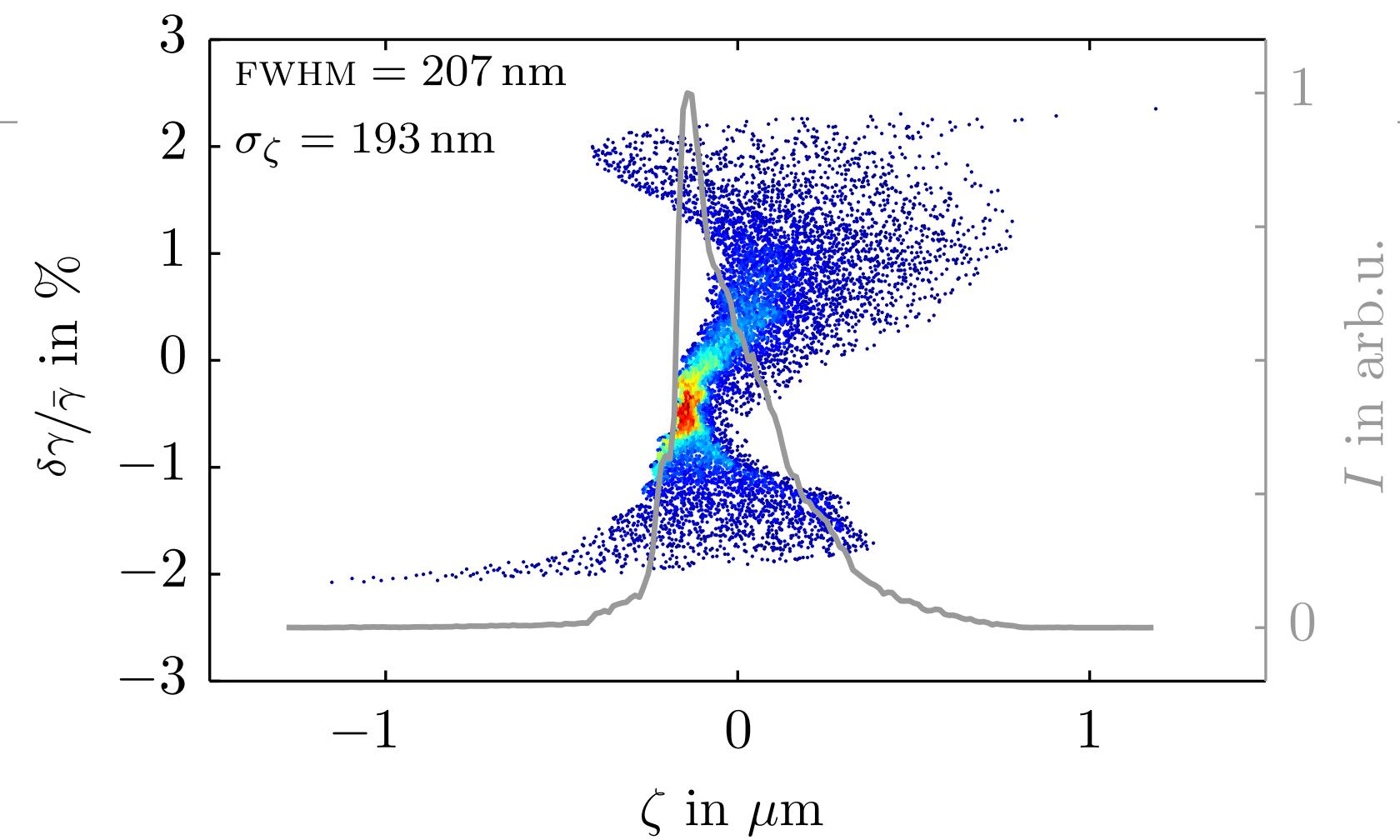
> Relative energyspread: $4 \cdot 10^{-6}$

> Accelerating phase



Summary & Outlook

- > Summary
 - > Basic concept of ballistic bunching
 - > Correction of curvature w/o 3rd harmonic structure
 - > Stretcher mode
 - > Sub-fs bunches at REGAE
 - > Energy spread compensation
- > Outlook
 - > Concept applicable... now
 - > But, how to measure?
 - > Concept could be adapted to other machines



Thanks

funding contributed by



Partnership of
Universität Hamburg and DESY



LBNL
WARP code



JÜLICH FORSCHUNGSZENTRUM JUROPA
supercomputer



M Division

