

# Staging acceleration to improve an energy spread in laser wakefield acceleration

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***Japan Atomic Energy Agency***

## Collaborators



R. Kodama's Group (Osaka Univ.)

T. Hosokai's Group (Osaka Univ.)



S. Yamamoto's Group (KEK)

T. Sasaki's group (Nagaoka Univ. Tech. )



## Program Manager

Y. Sano (JST)



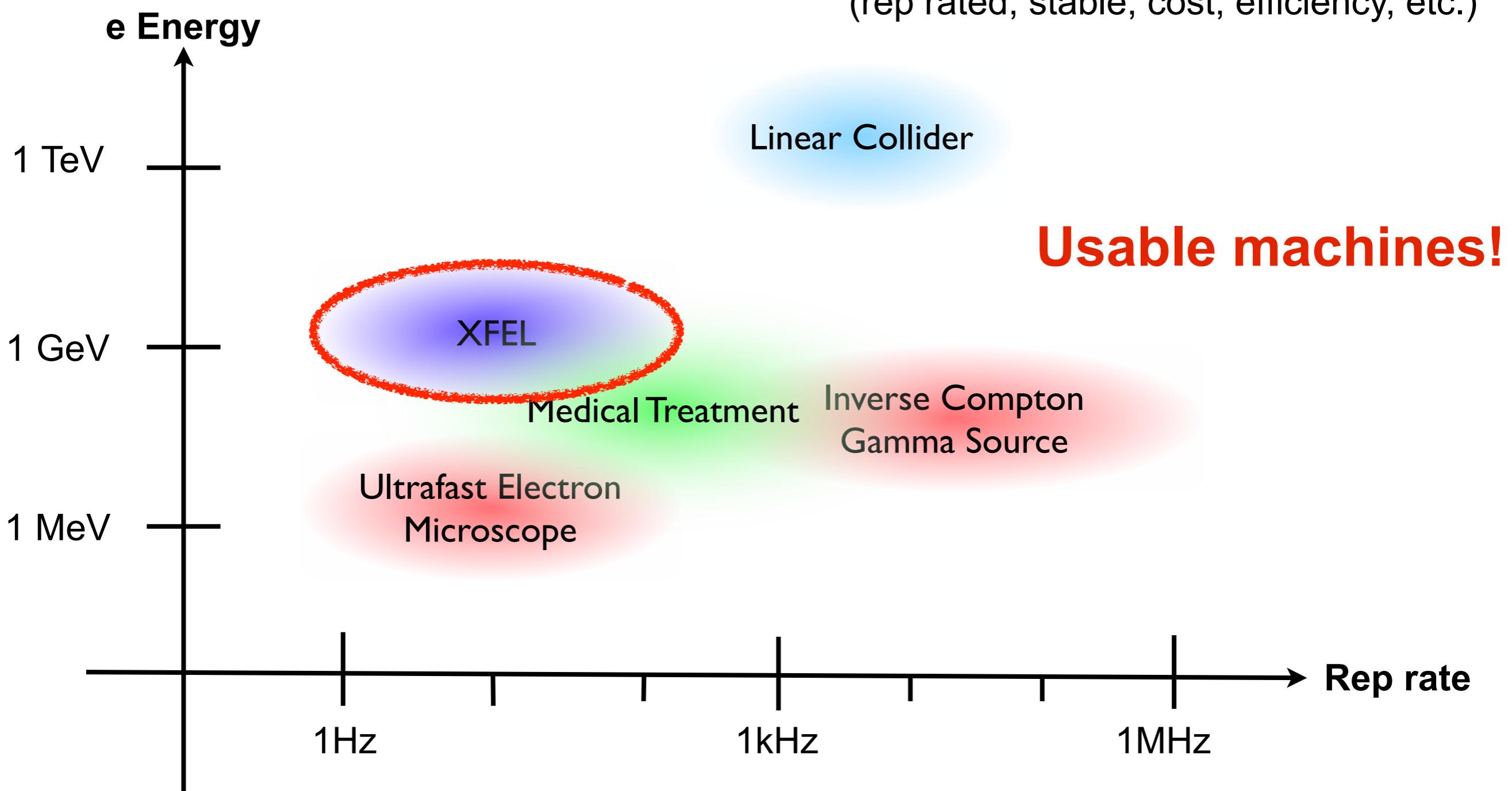
# Contents

- Introduction
- ImPACT Project
- Requirements for XFEL
- Our strategy
  - multi-stage acceleration
  - beam matching
- JAEA mission
- Summary

# Laser electron acceleration: what's next?

- many successful experiments on laser electron acceleration

Laser technology is a key for applications!  
(rep rated, stable, cost, efficiency, etc.)



# ImPACT project (FY2014-2018)

ImPACT=Impulsing Paradigm Change through disruptive Technologies Program

“Ubiquitous Power Laser for Achieving a Safe, Secure and Longevity Society” (PM: Dr. Sano)

## ■ Overview

Ubiquitous quantum beam technologies and devices will be developed through power laser ultra-miniaturization and integration with plasma and accelerator technologies, which will have applications in equipment diagnosis, security, advanced medicine and other fields, and will help to achieve a safe, secure and longevity society.

## ■ Impact on Industry and Society in the Event of Achievement

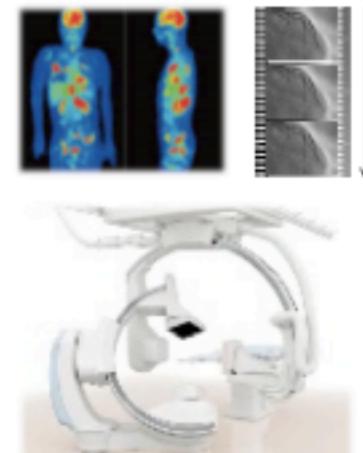
- ✓ Enabling the use of XFEL\* (a National Critical Technology), which currently exists in only two locations in the world, at each institution.
- ✓ Industrial innovation through analysis on the atomic level, ubiquitous equipment diagnosis and repair, biological imaging, quantum beam radiotherapy and so on, anytime, anywhere



XFEL (SACLAC)



Conception of tabletop XFEL



Diagnosis and life-extension of structures  
Advanced medical solutions

Disruptive technology=laser acceleration!, Hi-risk, Hi-return



# ImPACT: R&D Groups

**Project 1**  
**Laser acceleration**  
**& XFEL**  
**demonstration**

**Program Advisors**

**Program Manager**  
(PM: Dr. Sano)

**Project 2**  
**Ultra-compact**  
**power laser**

**Laser acceleration elemental technology**

Osaka Univ.  
(Prof. Hosokai)

Microundulator

KEK (Prof. Yamamoto)

Beam monitoring and control

JAEA (Dr. Kando)

Plasma device power source

Nagaoka Univ. Tech. (Prof. Sasaki)

Microchip laser

Institute for Molecular Science  
(Prof. Taira)

Waveform control laser

Hamamatsu Photonics (GD Kawashima)

**Integrated platform for laser acceleration**

Osaka Univ.  
(Prof. Kodama)

**XFEL demonstration and assessment**



Project 3

**Study of user needs and systemization assessment**

**Open bidding**

**Systemization and ultra-compact laser applications**





# Required parameters for XFEL based on 1D

Z. Huang & K. J. Kim, PRST-AB 10, 034801 (2007)

## SASE FEL

Pierce parameter

$$\rho = \left[ \frac{1}{16} \frac{I_e}{I_A} \left( \frac{K[JJ]}{\sigma_x k_u} \right)^2 \frac{1}{\gamma^3} \right]^{1/3}$$

$$N_{u,sat} \sim 1/\rho$$

$$L_s \sim \lambda_u / \rho$$

**typically  $\sim 10^{-3}\text{-}10^{-4}$**

## X-ray

X-ray wavelength

$$\lambda_x = \frac{\lambda_u}{2\gamma^2} \left( 1 + \frac{K^2}{2} \right)$$

Output power of XFEL

$$P_{out} \sim \rho P_{beam} \quad \text{e-beam power}$$

## e-beam

energy spread

$$\Delta\gamma/\gamma < \rho$$

unnormalized emittance

$$\varepsilon_{un} \leq \lambda_x/(4\pi)$$

$I_A = ec/r_e \approx 17$  [kA] Alfven current

$I_e$  Electron beam peak current

$\sigma_x$  Electron beam rms beam radius

$\gamma = E_0/mc^2$  ratio of electron beam energy to rest energy

$K = \frac{eB_0}{mck_u} = 0.934 B_0 [\text{T}] \lambda_u [\text{cm}]$  dimensionless undulator parameter  
undulator period  
maximum magnetic flux density  
(cf. a\_0)

$[JJ] = J_0 \left( K^2 / (4 + 2K^2) \right) - J_1 \left( K^2 / (4 + 2K^2) \right)$   $J_n(x)$  : nth order Bessel function of 1st kind



# XFEL parameter examples: zero-order

## Project goal

$$\underline{E_x = 1 \text{ keV}}$$

$$\lambda_x[\text{nm}] = 1.24/E_x[\text{keV}]$$

$$\lambda_x = 1.24 \text{ [nm]}$$

### Case I. SACLAC undulator

$$\lambda_u = 1.8 \text{ [cm]}, \quad K = 2.1 \quad \rightarrow \quad \gamma = 4.8 \times 10^3 \quad , \underline{E_0 = 2.5 \text{ [GeV]}}$$

possible!

### Case II. Short-period undulator (KEK, under development)

$$\underline{\lambda_u = 0.4 \text{ cm}, \quad K = 0.15 \quad (B_0 = 0.4 \text{ T})}$$

$$\gamma = 1.3 \times 10^3, \quad \underline{E_0 = 0.65 \text{ [GeV]}}$$

possible!

Energy spread should be smaller than the following values.

$$\rho = \begin{cases} 2.5 \times 10^{-3} & (\text{case I}) \\ 5.9 \times 10^{-4} & (\text{case II}) \end{cases}$$

challenge

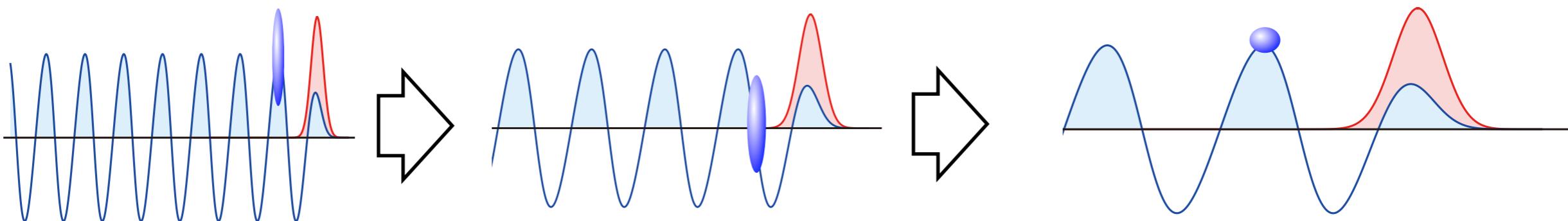
The emittance should satisfy  $\varepsilon_{un} \leq \lambda_x/(4\pi) = 9.87 \times 10^{-5} \text{ mm mrad}$

$$\varepsilon_n \approx \gamma \varepsilon_{un} < \begin{cases} 0.48 \text{ mm mrad} & (\text{case I}) \\ 0.13 \text{ mm mrad} & (\text{case II}) \end{cases}$$

possible!

our strategy  
to get monochromatic electrons

- We use separate-function accelerating stages.
- In the latter part, the longer pulse duration is employed.

**Injector**

3-10 TW  
**<30 fs**  
 $a_0 > 1$

**Phase rotator**

3-10 TW  
**~60 fs**  
 $a_0 \leq 1$

**Booster**

>100 TW  
**~100 fs**  
 $a_0 \leq 1$

- Preliminary implementation at Osaka Univ. (T. Hosokai's lab.)
- Booster acceleration test with **J-KAREN-P** laser.

Finally, all the system will be implemented at the **integrated platform**  
**“LAPLACIAN” (RIKEN, Harima).**

Nakanii's talk (yesterday)  
Hosokai's talk (tomorrow)

# Theoretical consideration supports proper staging

S. V. Bulanov, in preparation

## Unlimited acceleration

In inhomogeneous plasma target the wake wave phase velocity depends on the laser power and plasma density as

$$\gamma_w = \sqrt{a} \left( \frac{\omega}{\omega_{pe}} \right) = \left( \frac{\mathcal{P}}{\bar{\mathcal{P}}} \right)^{1/6} \left( \frac{n_0}{n_{cr}} \right)^{1/3}$$

and for electron energy we have

$$\frac{d\gamma}{dx} = \frac{eE}{m_e c^2} = \sqrt{a} \left( \frac{\omega_{pe}}{c} \right) = \frac{2\pi}{\lambda} \left( \frac{\mathcal{P}}{\bar{\mathcal{P}}} \right)^{1/6} \left( \frac{n_0}{n_{cr}} \right)^{1/3}$$

This yields the equation for the density profile

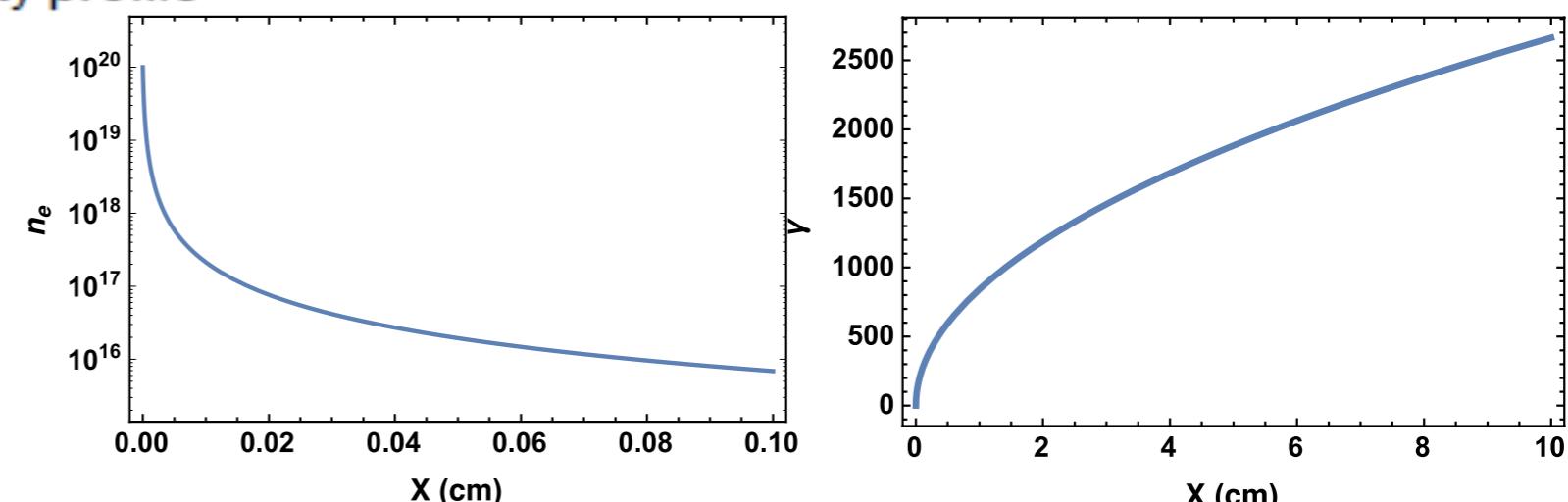
$$\frac{d}{dx} \left( \frac{\omega}{\omega_{pe}} \right)^{2/3} = \frac{2\pi}{\lambda} \left( \frac{\omega_{pe}}{\omega} \right)^{1/3}$$

Its solution

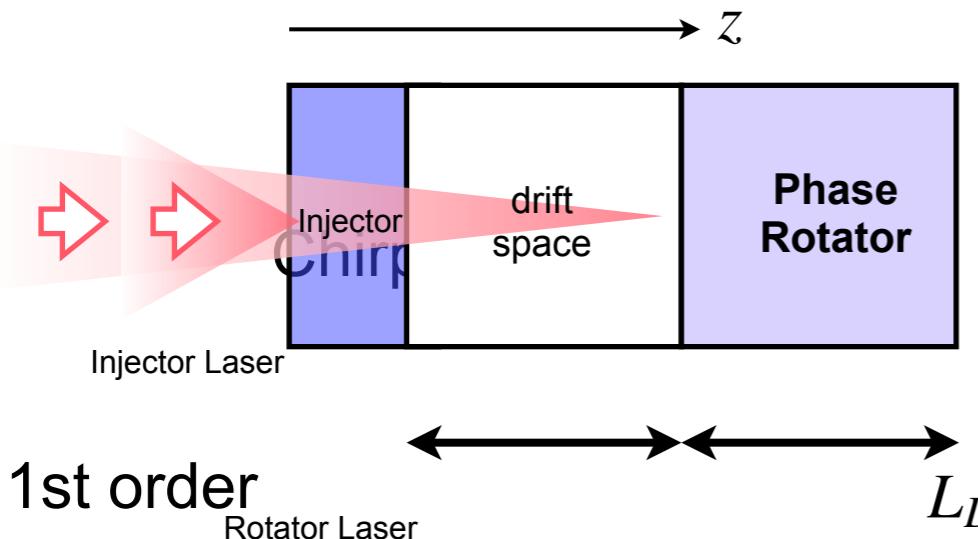
$$n(x) = n_{cr} \left( \frac{\pi x}{\lambda} + \left( \frac{\omega}{\omega_{pe}(0)} \right)^{4/3} \right)^{-3/2}$$

The electron energy asymptotically grows as

$$\gamma(x) = \left( \frac{\mathcal{P}}{\bar{\mathcal{P}}} \right)^{1/6} \left( \frac{\pi x}{\lambda} \right)^{1/2}$$



# Design of phase-space rotator



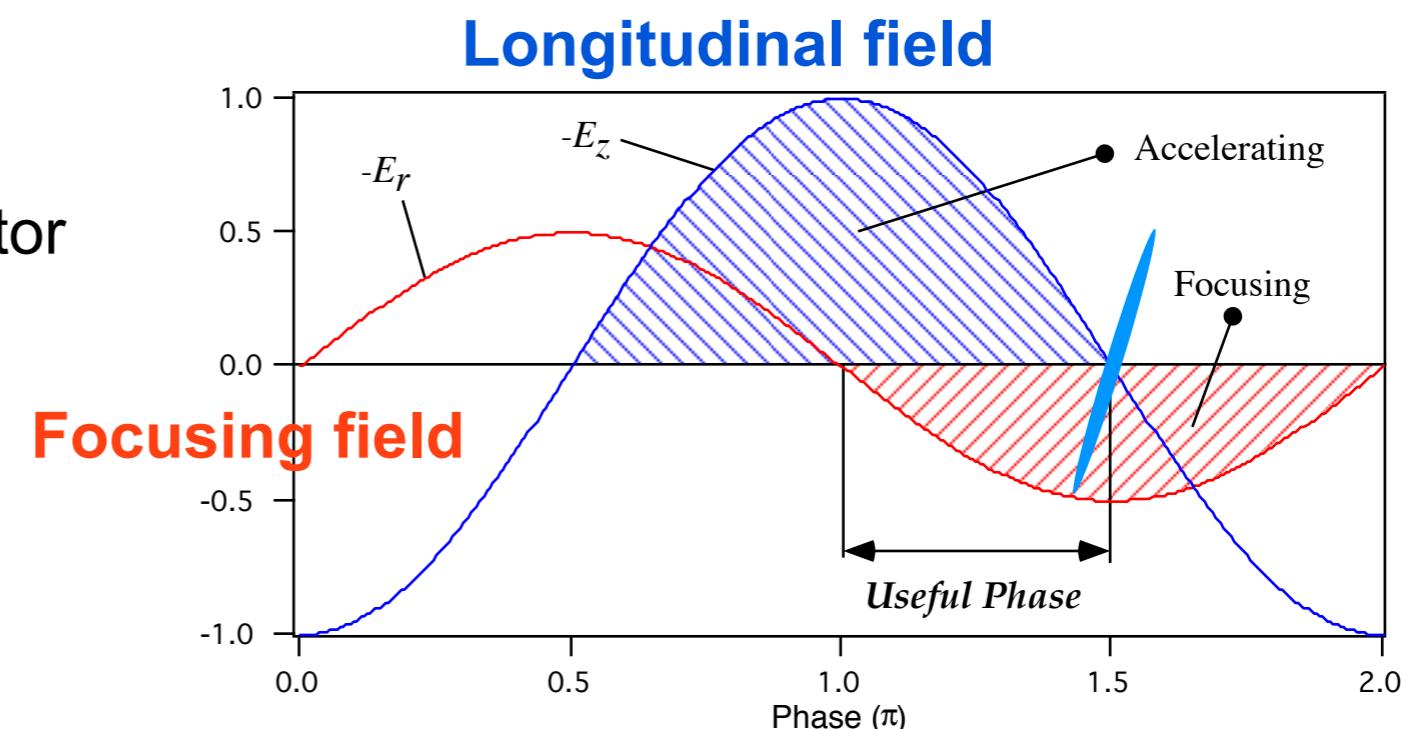
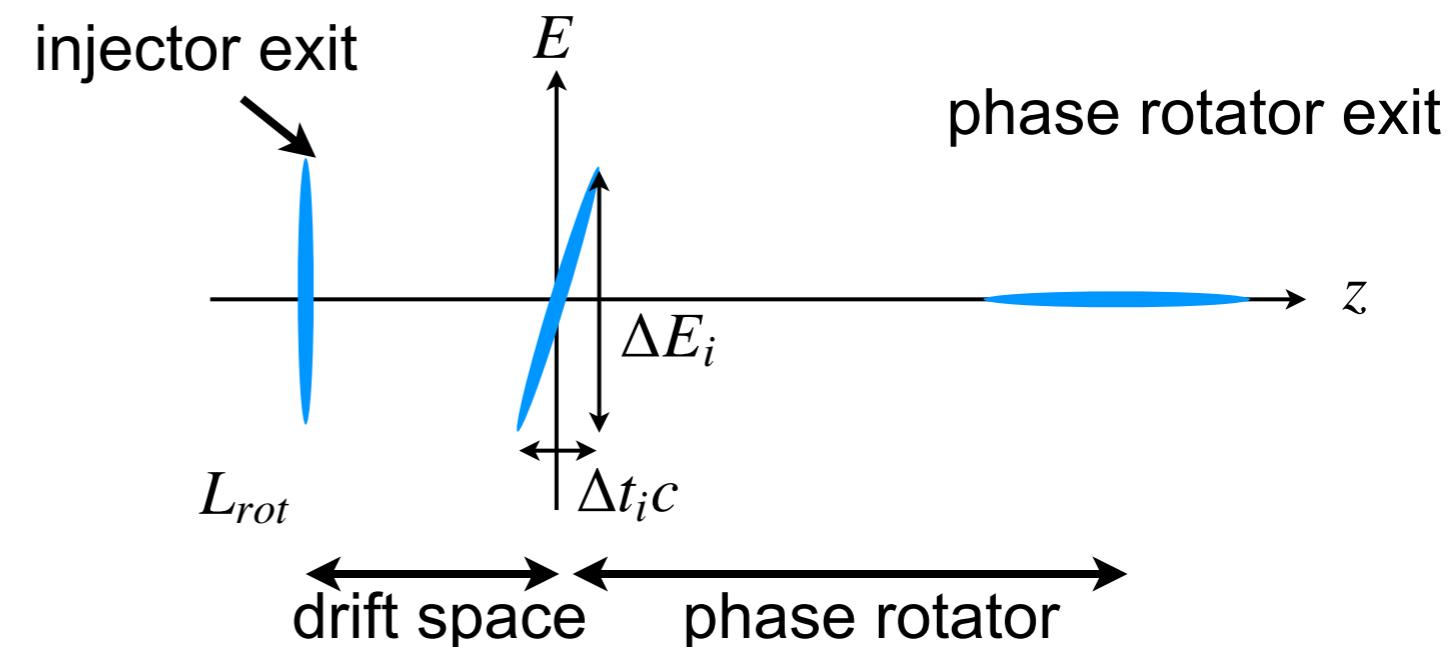
$$\frac{E_{acc}L_{rot}}{\lambda_p} = \frac{\Delta E_i/2}{\Delta t_i c}$$

Input electron beam:  $\Delta E_i, \Delta t_i$

Parameters of Phase-space rotator

$E_{acc}, L_{rot}, \lambda_{p,r}$

These 3 parameters are determined so as to cancel the chirp of electron beam.

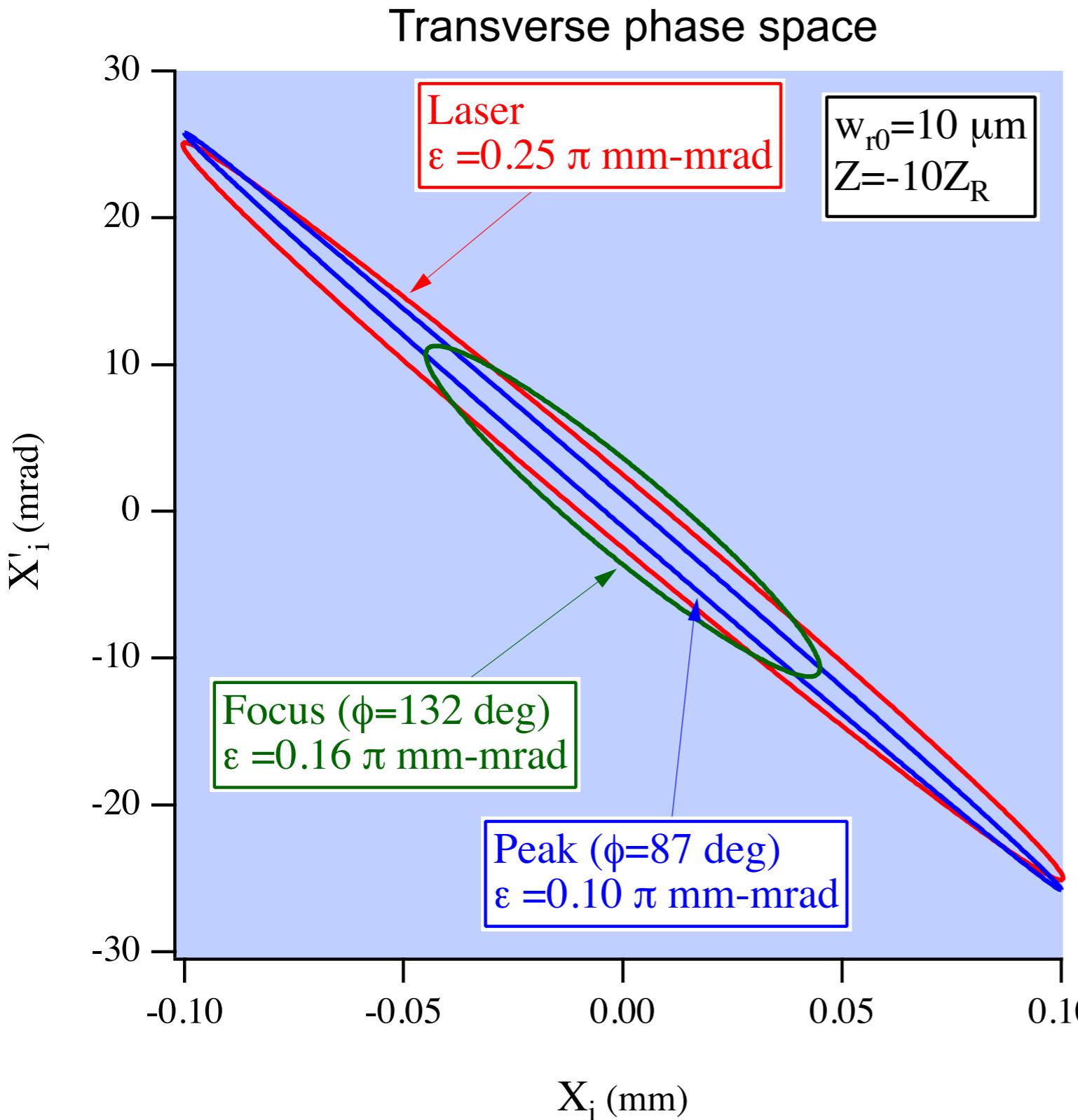




# Example parameters for phase rotator

				Case I	Case II
Injector	e-energy	$E_i$	MeV	30	10
	dispersion	$\Delta E_i/E_i$	MeV	3	1
Drift space	length	$L_D$	m	0.3	0.01
	chirp rate		MeV/ $\mu\text{m}$	$1.7 \times 10^{-1}$	$1.9 \times 10^{-1}$
Phase rotator	e-pulse duration	$\Delta t_i$	fs	30	8.8
		$\Delta t_i c$	$\mu\text{m}$	8.8	2.6
Phase rotator	phase		deg.	0	0
	laser amplitude	$a_{0,r}$	-	0.7	0.5
	laser pulse duration	$\tau_r$	fs	100	50
	laser power	$P_r$	TW	106	14
	spot radius	$w_{0,r}$	$\mu\text{m}$	80	40
	pl. wavelength	$\lambda_{p,r}$	$\mu\text{m}$	80	40
	length	$L_{rot}$	$\mu\text{m}$	1560	810
	pl. density	$n_{e,r}$	$\text{cm}^{-3}$	$1.7 \times 10^{17}$	$6.9 \times 10^{17}$

# Beam matching to the wake is important



Example:  $dE/E = 10\%$

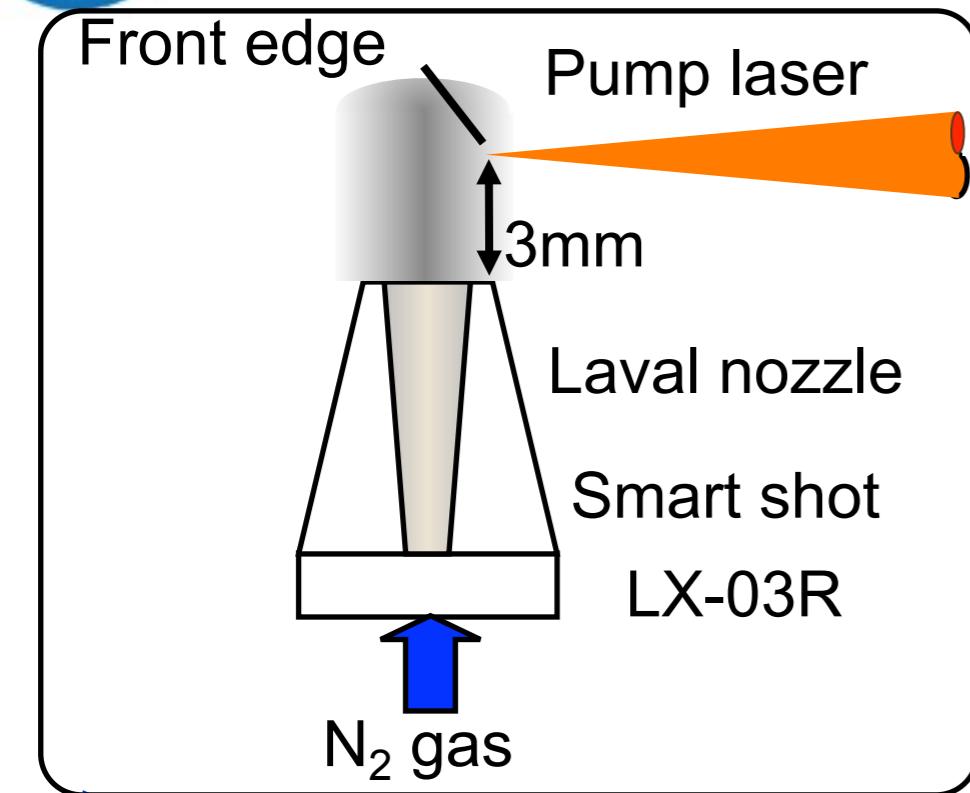
laser vacuum waist	10 $\mu\text{m}$
electron vacuum focus (peak)	4.6 $\mu\text{m}$
(focus)	14 $\mu\text{m}$

## Message:

- transverse matching is important!
- matching depends on phase!

# Injector results at JAEA

# Injector: example



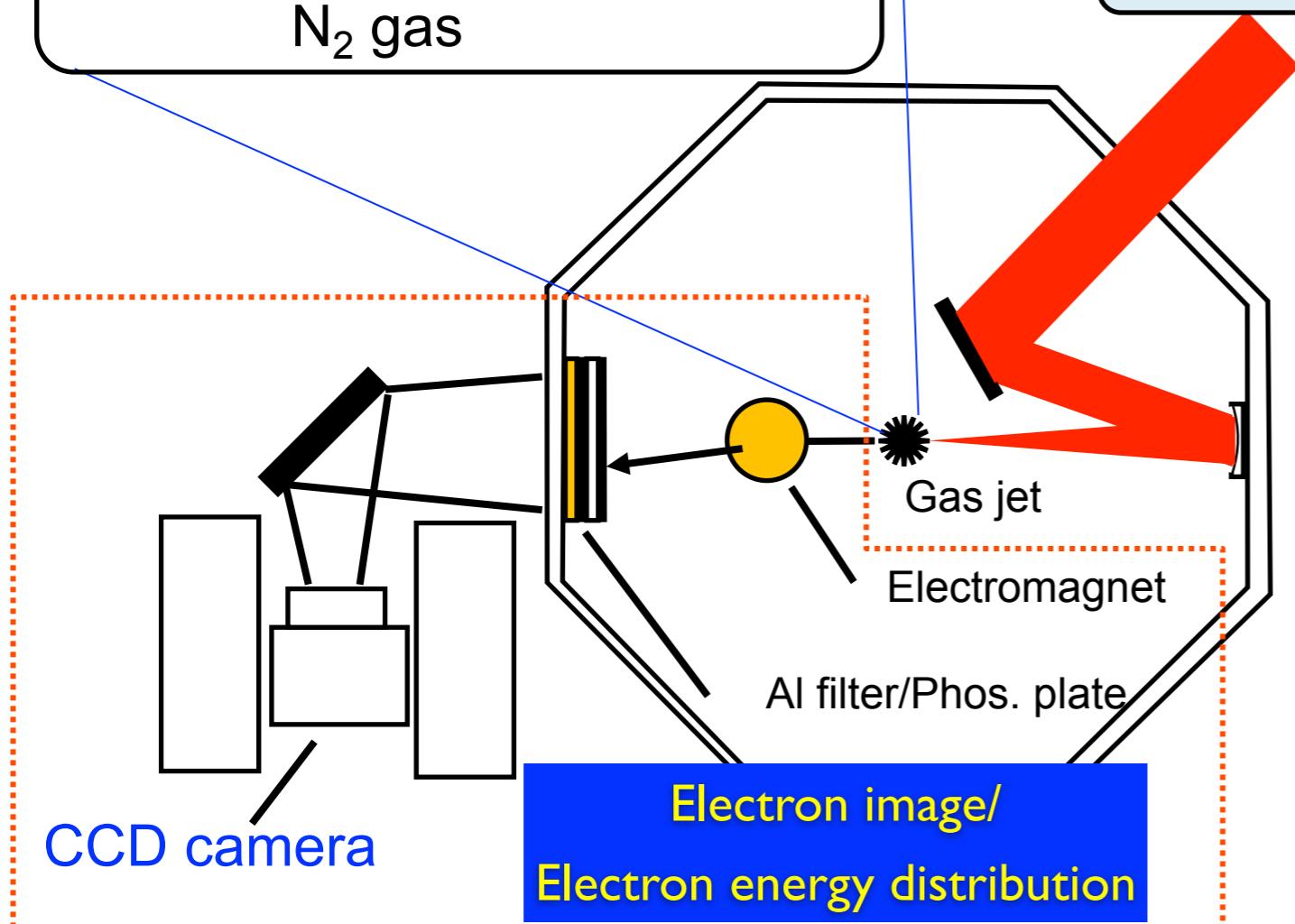
## Laser condition

$$\lambda = 800\text{nm}$$

$$E = 160 \pm 4.8\text{mJ}, \tau = 40\text{fs} (\text{i.e. } P = 4\text{TW})$$

$$\text{Laser intensity: } 9 \times 10^{17} \text{ W/cm}^2 (a_0 = 0.6)$$

$$\begin{aligned} \text{ASE pedestal: } & 2 \times 10^{-6} (-500\text{ps} < t < -1\text{ps}) \\ & 2 \times 10^{-8} (< -500\text{ps}) \end{aligned}$$



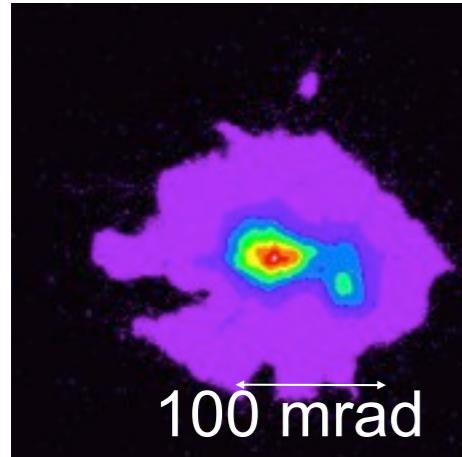
## Target condition

$$\begin{aligned} \text{Density scale: } & \sim 3500 \text{ um} \\ \text{Neutral Gas density: } & 0.3 \times 10^{18} \text{ cm}^{-3} (N_2) \end{aligned}$$



# Experimental results of e-beam generation

e-beam spatial profile



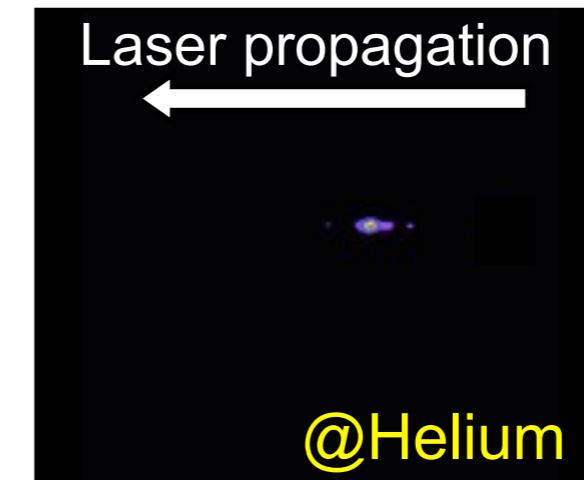
Helium



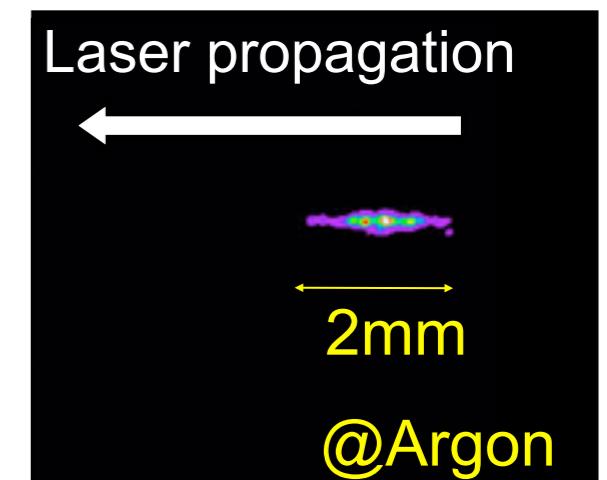
Argon

M Mori et al., PRST-AB

Thomson scattering image



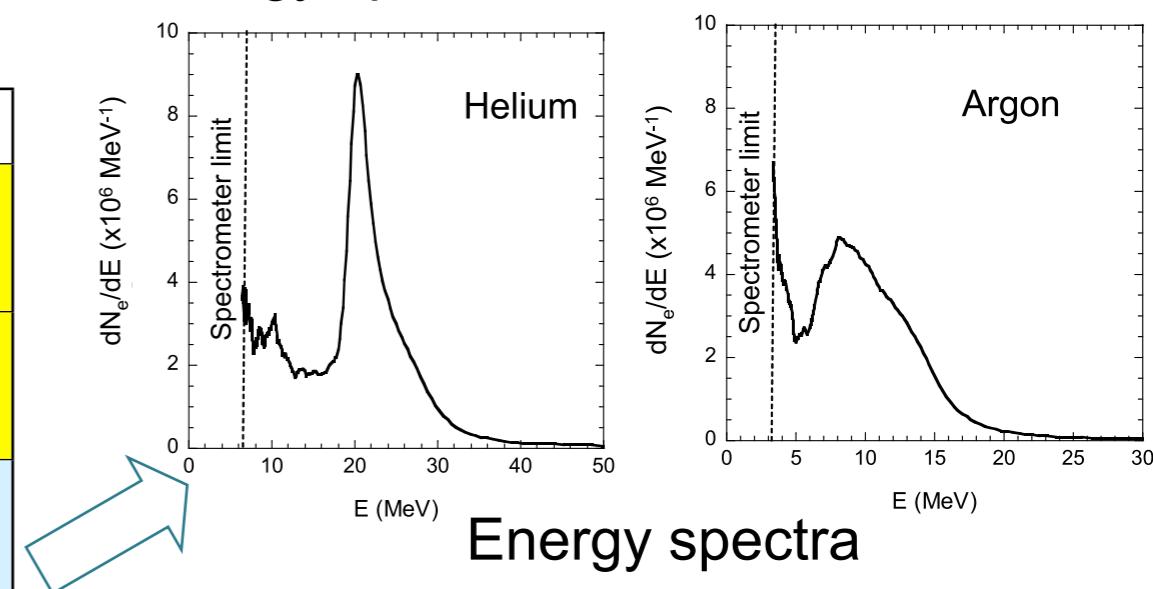
@Helium



@Argon

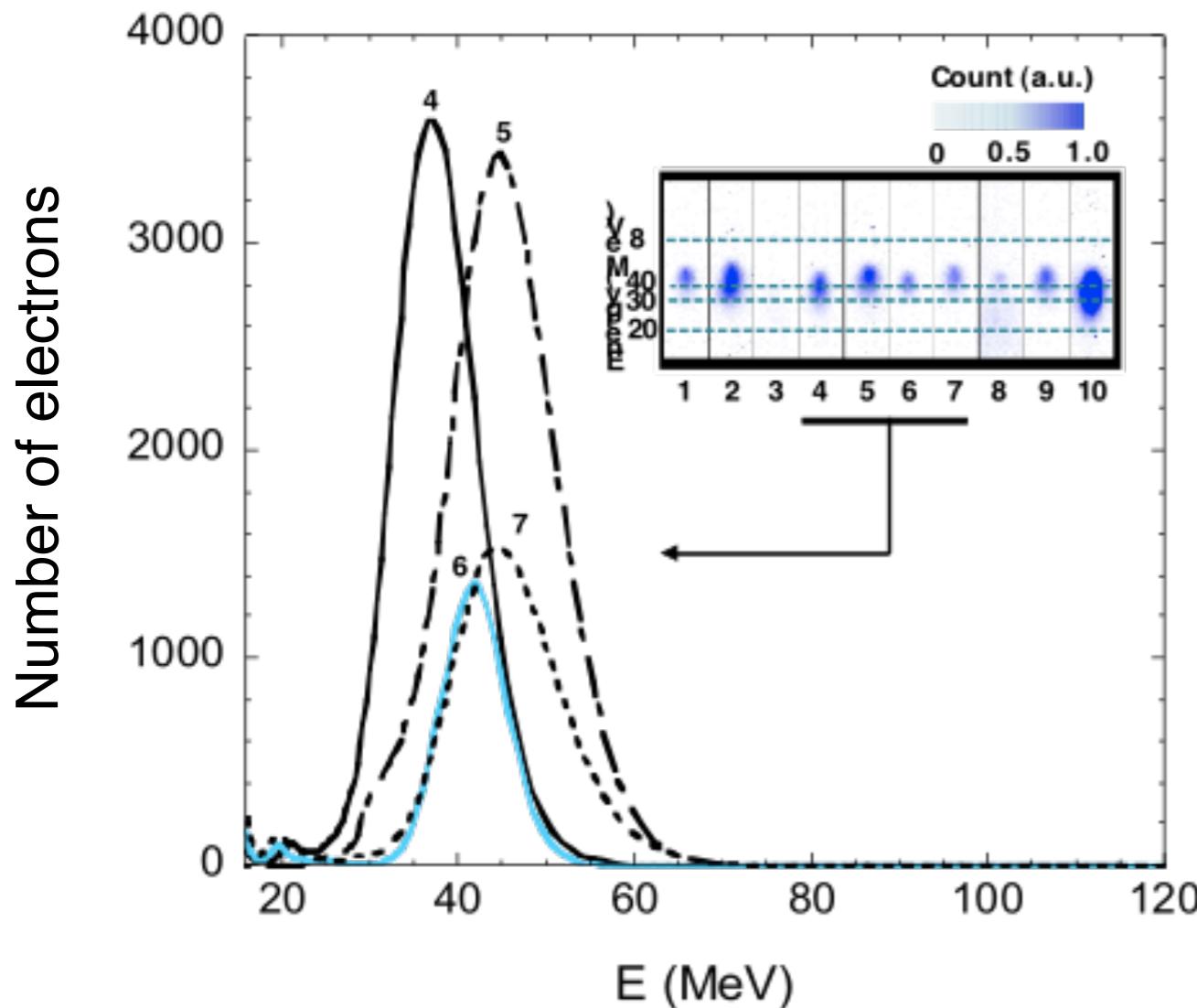
Argon : better pointing but broader energy spread

Target	Helium	Argon
Pointing stability (mrad) (rms)	9.8	2.4
Beam divergence (mrad) (avg±s.d.)	$29.8 \pm 8.8$	$10.4 \pm 2.0$
Peak Energy (MeV) (avg±s.d.)	$24.8 \pm 3.6$	$8.5 \pm 0.8$
Yield (pC/shot)	$19.8 \pm 10.6$	$9.2 \pm 3.3$
QME reproducibility (%)	38	84

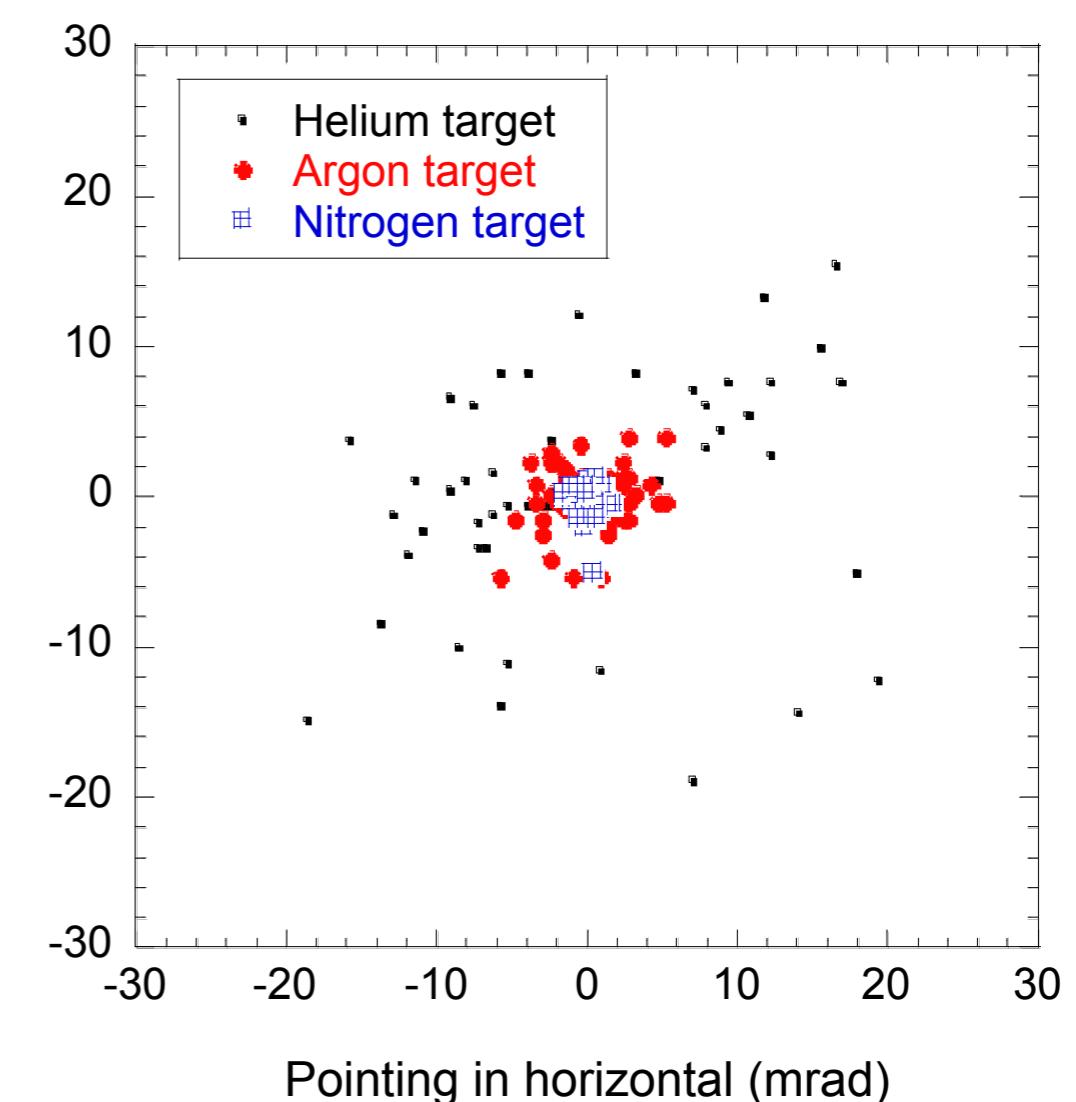


# N<sub>2</sub> gas is suitable in our case

Mori et al, IPAC2010



Number of electrons  
Pointing in vertical (mrad)



Pointing stability (1.7mrad)

JAEA mission

# Wakefield measurement

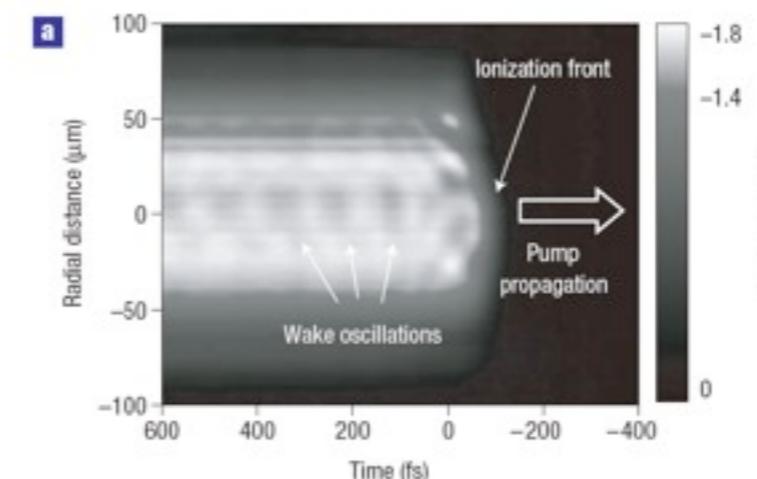
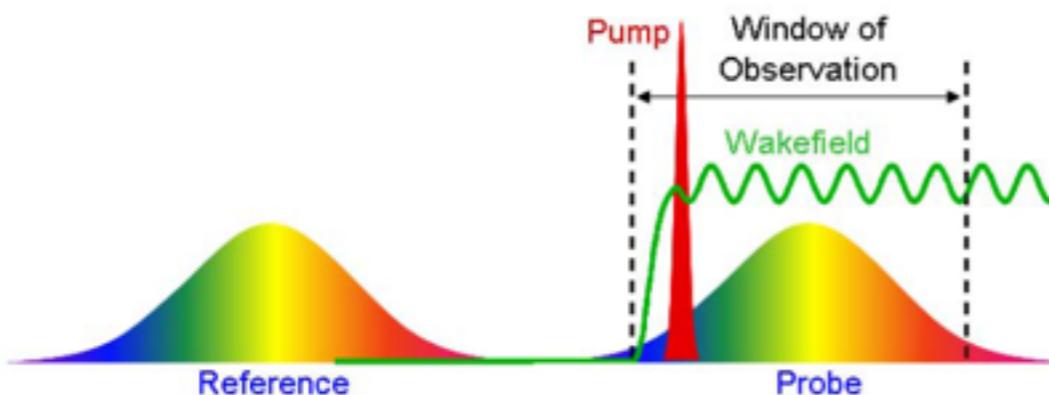
**Plasma wave (wakefield) is one of the important parameters.**

Electron energy, focusing

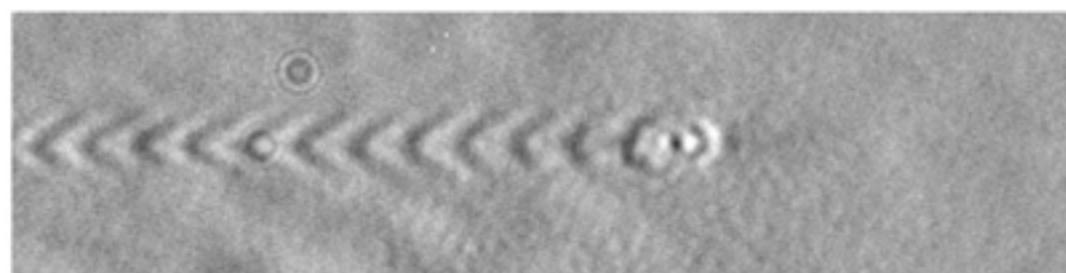
Also important in phase rotation

## 1. Single-shot based measurement: Frequency-Domain Holography

N. Matlis, M. Downer, Nature Phys. 2, 749 (2006)



## 2. Sub-10 fs probe -shadowgraphy



A. Buck et al., Nature Phys, 7, 543 (2011)

M. B. Schwab et al., APL, 103, 191118 (2013)

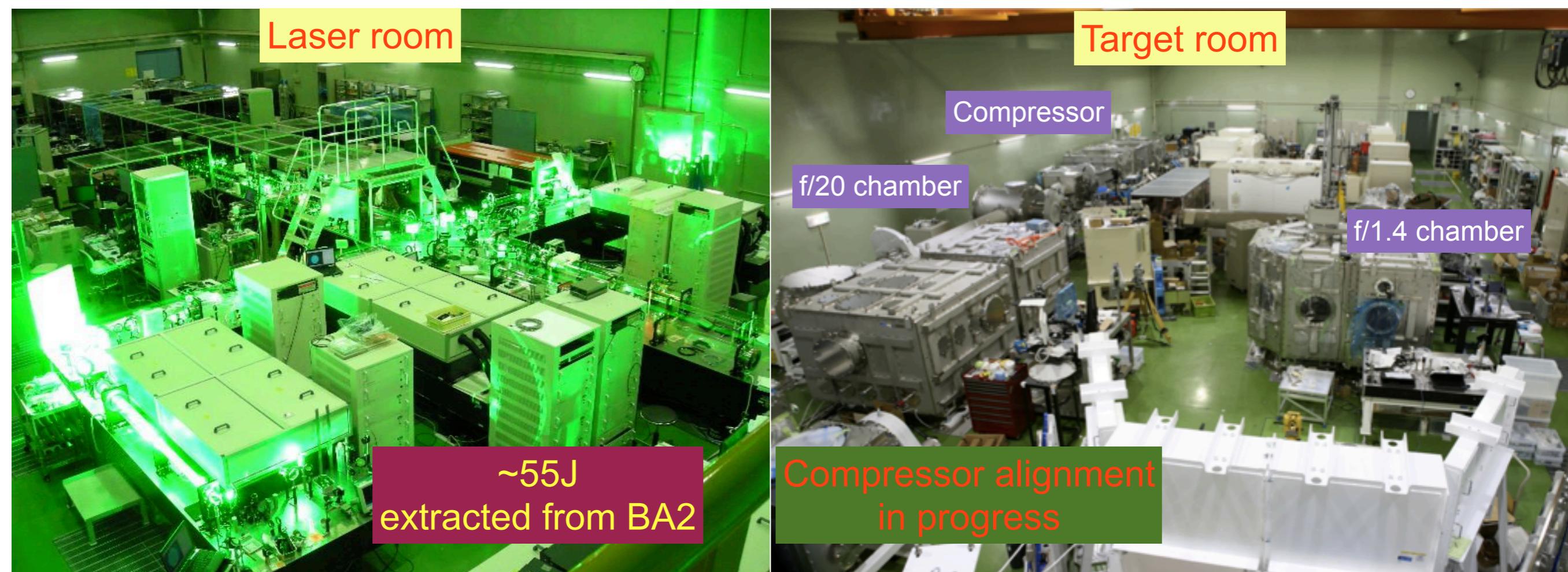
A. Sävert et al., PRL 115, 055002 (2015)

# Booster acceleration test

At KPSI-JAEA, we are upgrading our J-KAREN laser to PW level on target. 30 fs, ~30 J (1 PW on target), 0.1Hz. “**J-KAREN-P**”

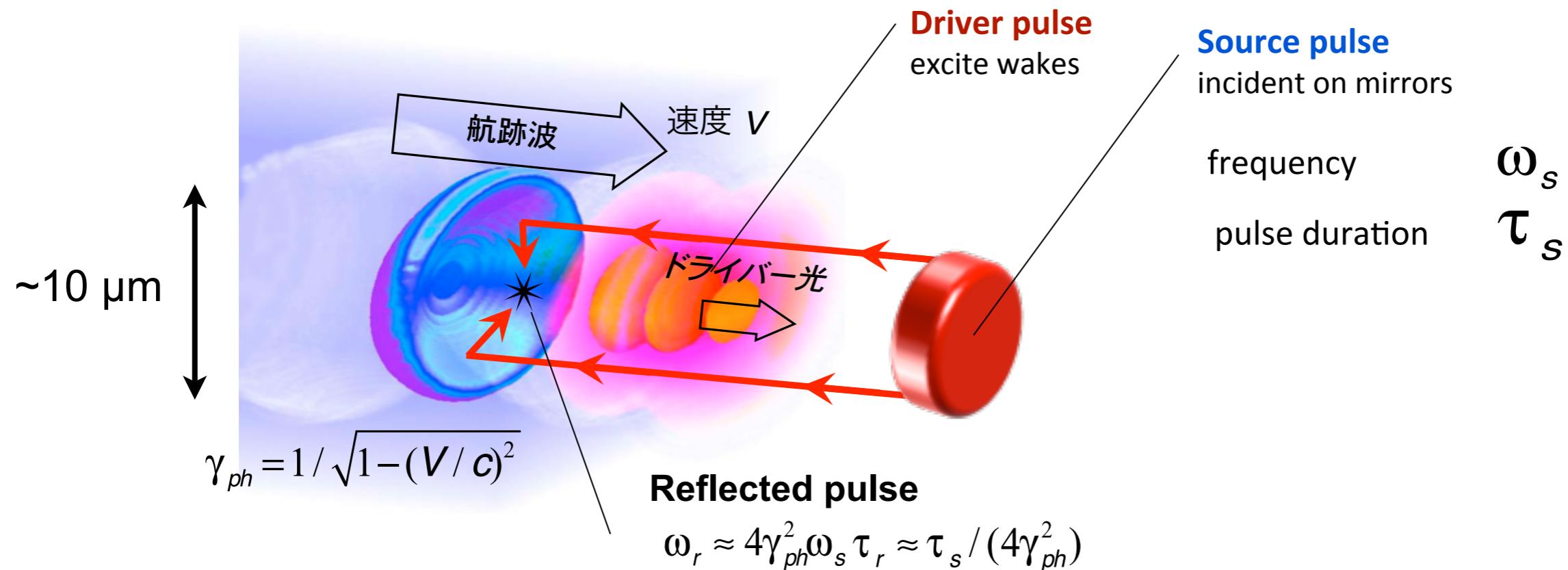
**Challenges:**

- Chirp pulse effect
- Stable acceleration
- long propagation (~10cm) in waveguide



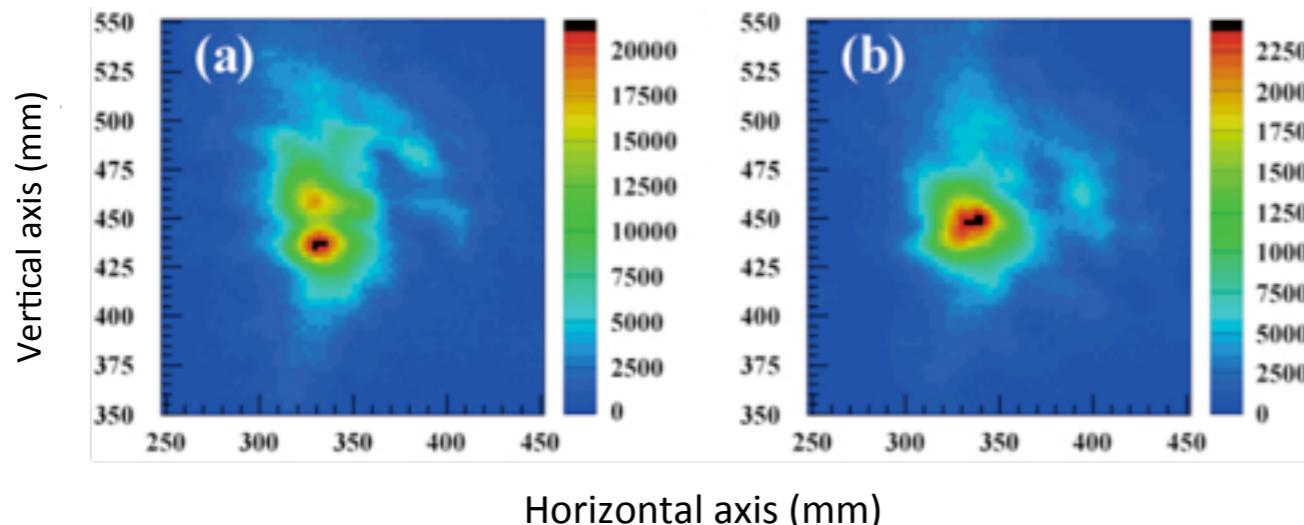
# Pulse alignment method

- In multi-staging acceleration, alignment method is necessary for two (or three) pulses properly.
- At JAEA, in the study of ***relativistic flying mirrors***, which uses **nonlinear wake** as a moving mirror, we have developed several techniques.



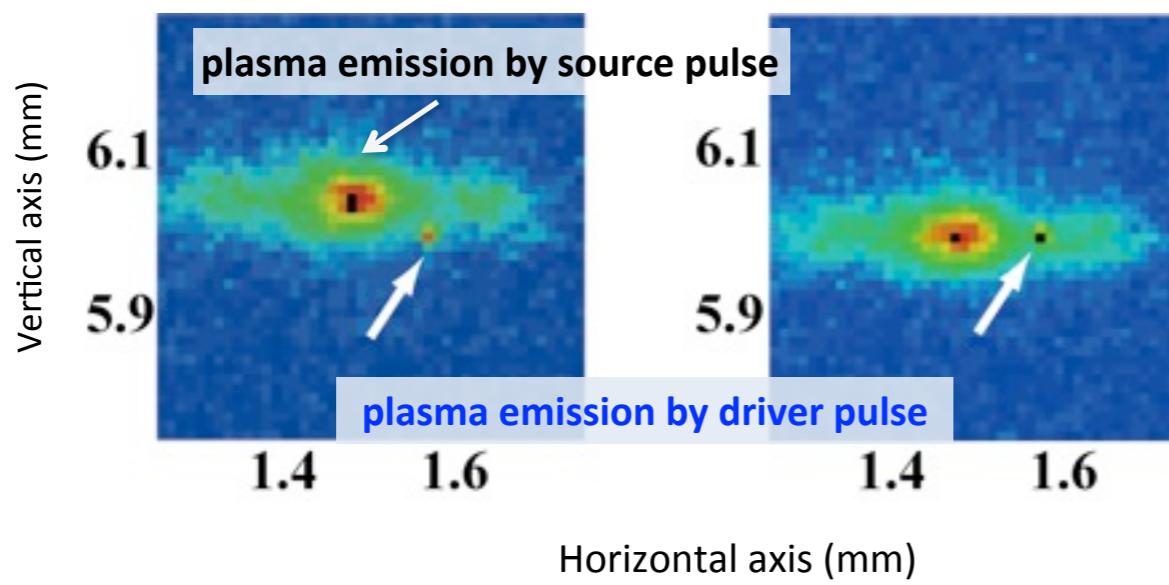
# Several alignment method

## ex1) Far-field (Two laser pulses), online



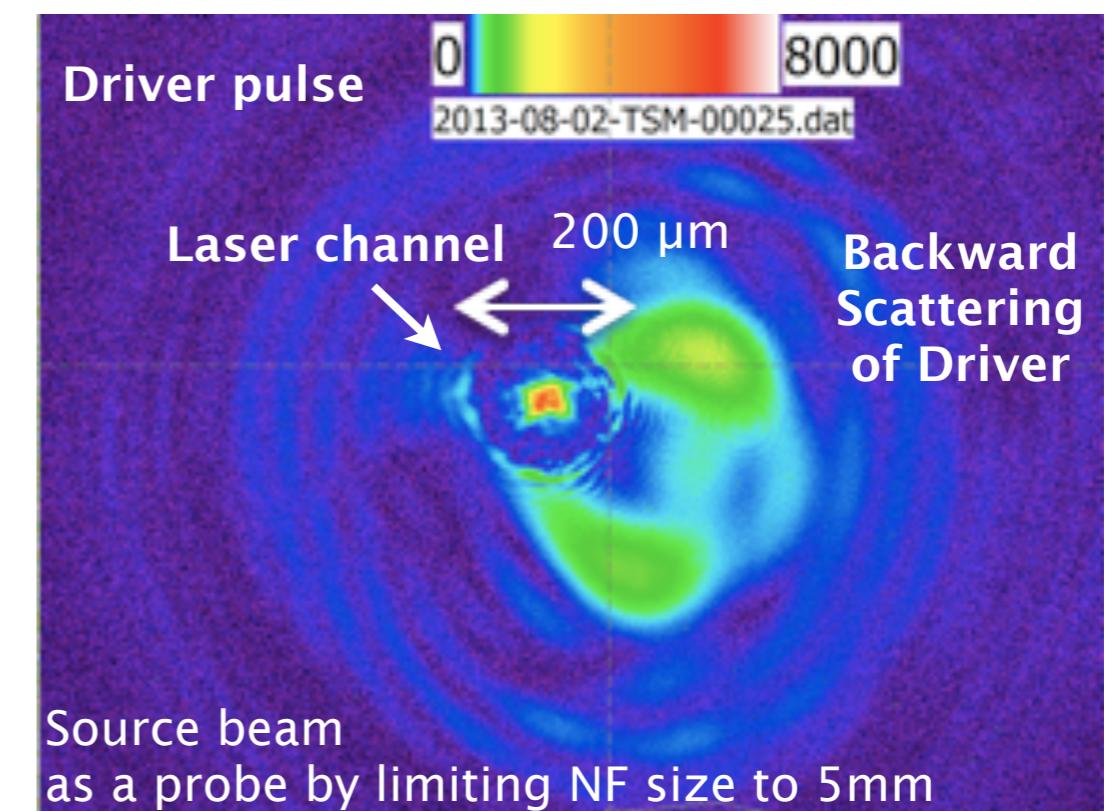
- Spatial resolution  $\sim 15\mu\text{m}$

## ex2) XUV imaging



- spatial resolution  $\sim 6\mu\text{m}$

## ex3) Longitudinal shadowgram (main channel reflection)



M. Kando et al., in preparation

- Spatial resolution  $\sim 2\mu\text{m}$

We have developed suitable alignment methods when two laser pulses are used.

# Importance of laser stabilization

- **Electric fields are determined by laser**
  - Intensity
  - Profiles (both radial and longitudinal)

**Density**

$$\frac{\delta n}{n} = \frac{k_p a_0^2}{2} \left[ 1 + \frac{4}{k_p^2 \sigma_r^2} \left( 1 - \frac{r^2}{\sigma_r^2} \right) \right] \exp\left(-\frac{r^2}{\sigma_r^2}\right) \sin(k_p \zeta)$$

**Axial electric field**

$$eE_z(r, \zeta) = \frac{\sqrt{\pi} mc^2 k_p^2 \sigma_z a_0^2}{2} \exp\left(-\frac{r^2}{\sigma_r^2} - \frac{k_p^2 \sigma_z^2}{4}\right) \cos(k_p \zeta)$$

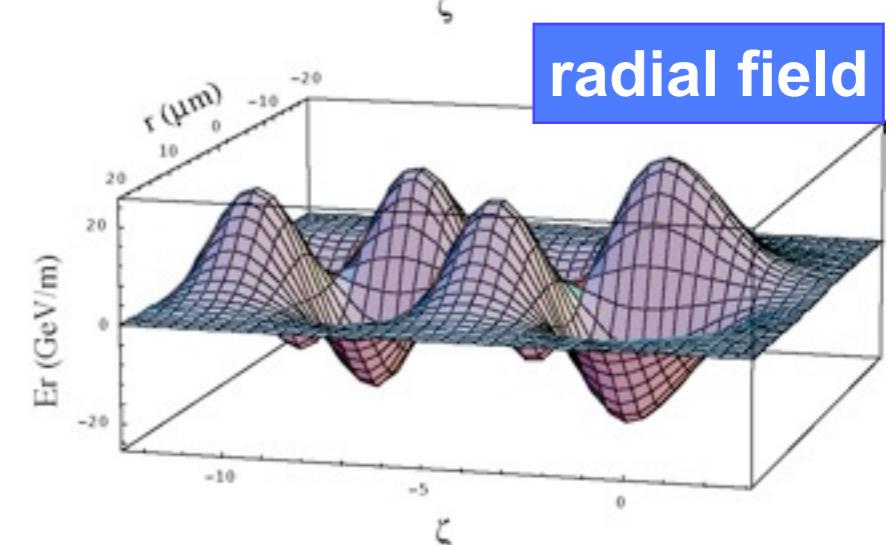
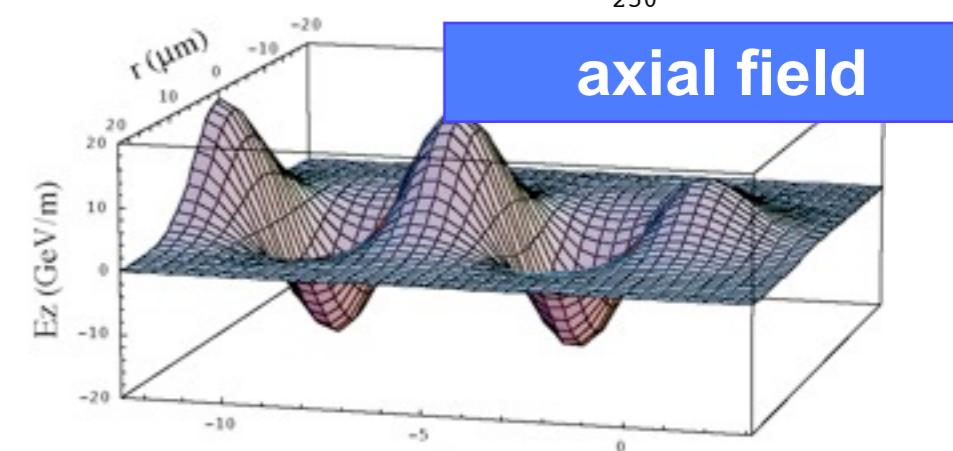
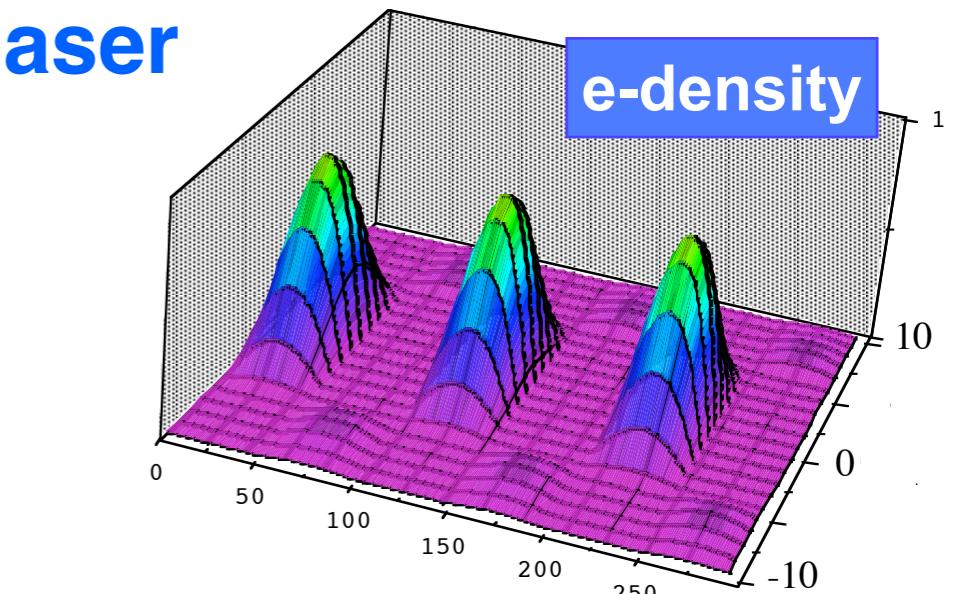
**Radial electric field**

$$eE_r(r, \zeta) = \frac{\sqrt{\pi} mc^2 k_p \sigma_z a_0^2 r}{\sigma_r^2} \exp\left(-\frac{r^2}{\sigma_r^2} - \frac{k_p^2 \sigma_z^2}{4}\right) \sin(k_p \zeta)$$

**Normalized laser amplitude**

$$a_0 = 8.5 \times 10^{-10} \lambda_0 [\mu m] \sqrt{I [W/cm^2]}$$

**In the linear regime ( $a_0 \ll 1$ ) the amplitudes are proportional to  $a_0^2$  (=intensity)**



# Stability of laser (example: J-KAREN)

Power amp mode: 2012.9.27

<b>Spot radius</b> ( $1/e^2$ , $\mu\text{m}$ )	x: $18.0 \pm 1.5$	8.4%
	y: $20.7 \pm 2.6$	12.6%
<b>Energy</b> (J)	$0.648 \pm 0.011$	1.8%
<b>Pulse duration</b> (FWHM, fs)	$38.5 \pm 6.4$	16.6%
<b>Pointing</b> (rms, $\mu\text{rad}$ )	x: 4.6 y: 5.9	12% 14%

## Intensity

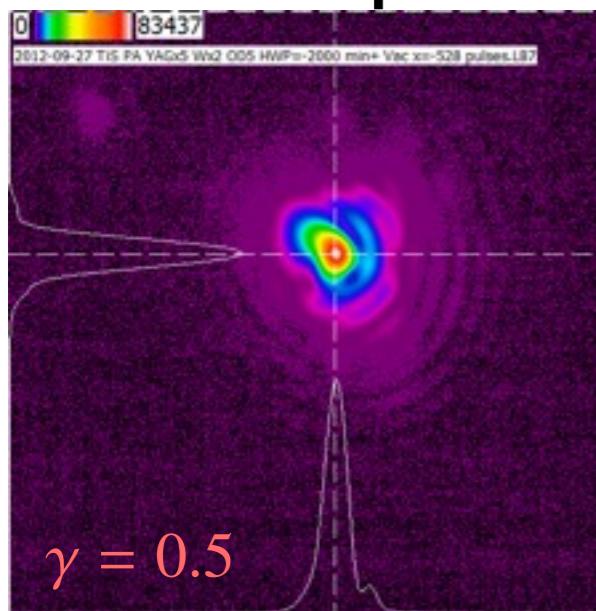
$$I = (4.3 \pm 0.7) \times 10^{18} \text{ W/cm}^2 (17\%)$$

$$a_0 = 1.44 \pm 0.12 (8.6\%)$$

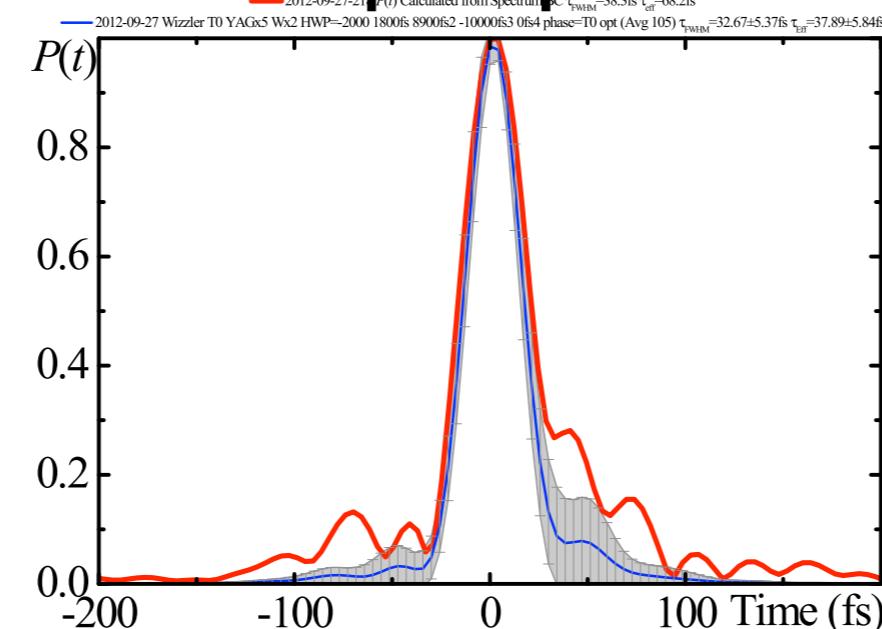
In the project,

- improve the intensity stability
- improve pointing stability

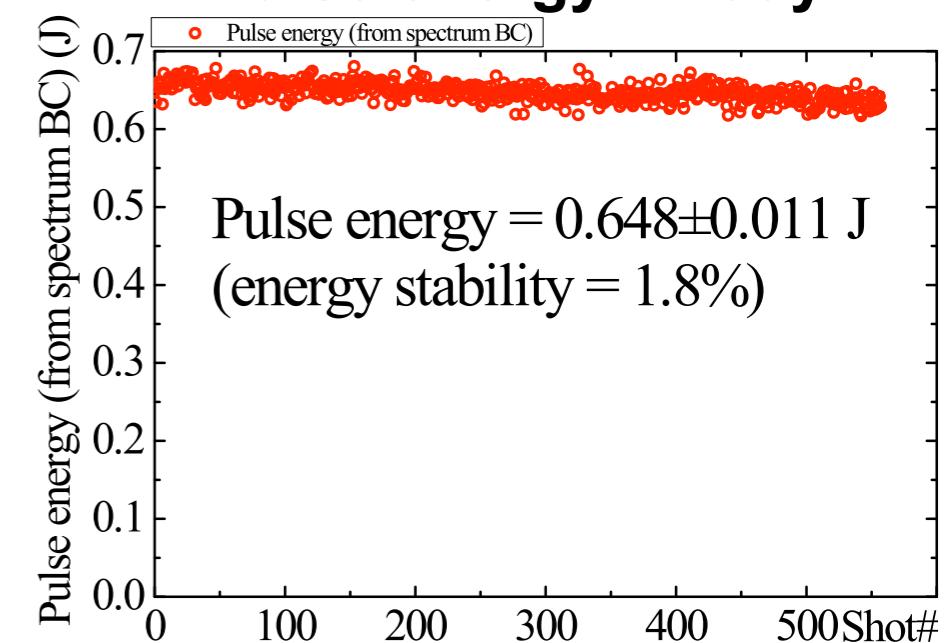
## Focal spot



## Temporal profile



## Pulse energy in day

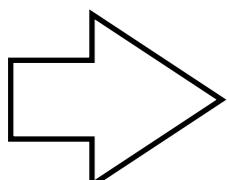




# Causes of instability

- air fluctuation
- vibration from the ground
- temperature drift
- nonlinear effects in laser amp.
- angular chirp
- strehl ratio
- etc.

In this project,



- We will improve laser stability.
  - Test bench, implementation to J-KAREN-P
  - The know-how will be used in the Platform laser.





# Summary

- The ImPACT program for “laser acceleration based XFEL” has been started.
- Minimum goal : 1 GeV, 1% spread, Q=1pC, t=1fs (kA), 1 μm
- We presented our strategy to get high quality beams with rough estimate. Detailed calculation with PIC is in progress.
- At JAEA, we will measure wakefield, alignment method, booster acceleration, laser control and stabilization.

**Call for post-docs!** (2 persons, deadline: 30 Oct. 2015)  
<http://www.jaea.go.jp/english/news/recruitment/re15090901.html>