













Space Charge induced emittance oscillations in a laminar beam



















Bunch length in the moving frame S'

More interesting is the bunch dynamics as seen by a moving reference frame S', that we assume it has a relative velocity V with respect to S such that at the end of the process the accelerated bunch will be at rest in the moving frame S'. It is actually a deceleration process as seen by S'

Inverse Lorentz transformations:

$$\begin{cases} ct' = \gamma \left(ct - \frac{V}{c} z \right) \\ z' = \gamma \left(z - Vt \right) \end{cases}$$

,

leading for the tail particle to: and for the head particle to:

$$\begin{cases} t \\ z \end{cases}$$

V

$$\begin{cases} t'_{o,t} = t_o = 0 \\ z'_{o,t} = z_{o,t} = 0 \end{cases}$$

$$\begin{aligned} t'_{o,h} &= -\frac{1}{c} \gamma'_o L_o < t_o \\ z'_{o,h} &= \gamma'_o L_o > z_{o,h} \end{aligned}$$

The key point is that as seen from S' the decelerating force is not applied *simultaneously* along the bunch but with a *delay* given by:

$$\Delta t'_{o} = t'_{o,h} - t'_{o,t} = -\frac{V}{c} \gamma'_{o} L_{o} < 0$$







