

Hadron Spectroscopy

Roberto Mussa

INFN Torino

- * heavy baryons
- * heavy-light mesons
- * heavy quarkonia
- * running coupling constant?

- * 'old' exotics
- * new exotics on thresholds
- * B_c

Why hadron spectroscopy ?

- * Quark-hadron duality :
investigate the role of spin and quark masses on : hadron masses ,
hadron magnetic moments.
- * Non perturbative QCD: this is what explains most of baryon matter.
Infrared slavery is a theoretical limit, which prevents to do
predictions on an amazing set of measurable quantities. Asymptotic
freedom is nice, but being able to cope with infrared slavery is
crucial, to deeply test our understanding of the nature of matter.
- * QCD provides doors towards BSM issues : axions, instantons,
strong CP violation ... (but also glueballs , hybrids , multiquarks)
- * Last 15 years taught us that all hints of new physics in the quark
sector (and not only : See L2L in g-2) could be explained as
unexpected effects of strong interactions: badly known form factors,
final state interactions, SU(3) breaking effects ...

QED example n.1: hydrogen atom

Proton-electron bound state
Non relativistic system
velocity $\sim \beta \sim n \alpha_{\text{QED}}$

$$M_p / M_e = 938 / 0.511 = 1836$$

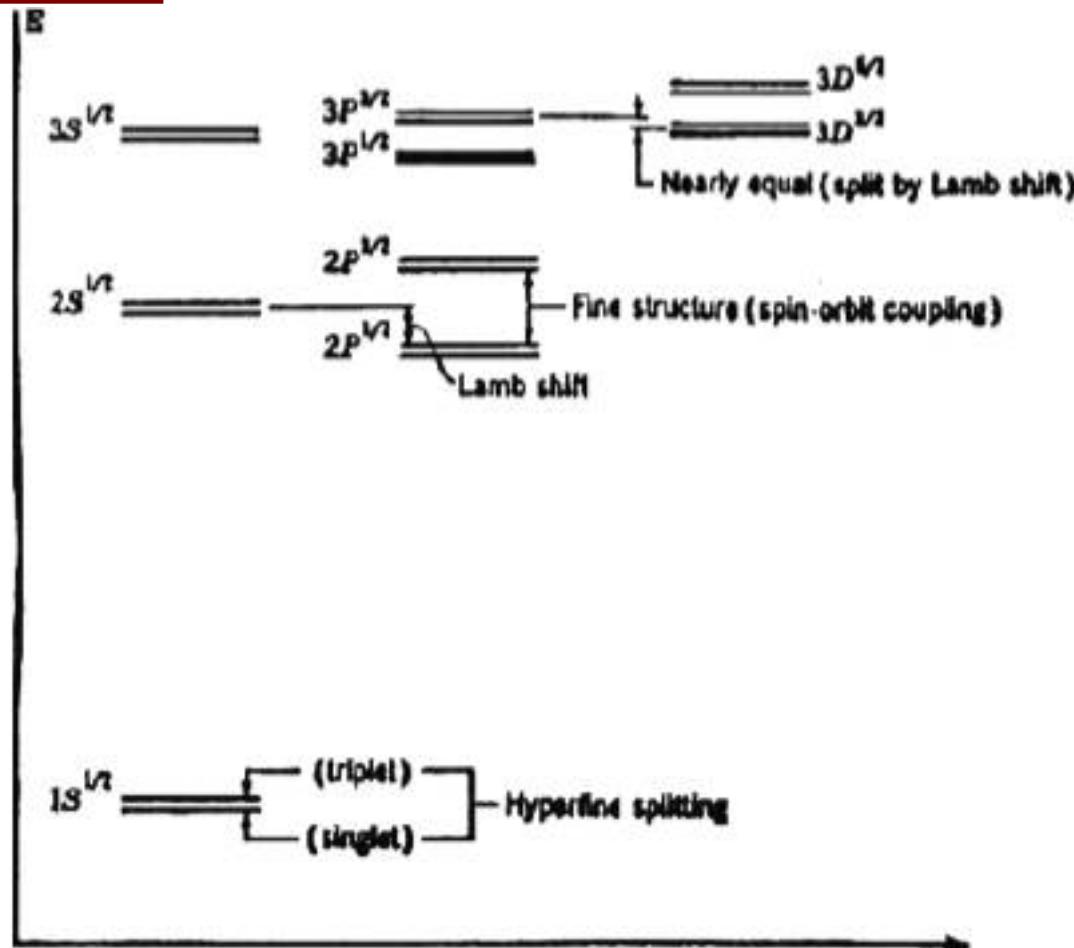
EM Transitions between energy levels
Stable ground state

2S-1S splitting $\sim 10 \text{ eV}$

Fine Splitting : $45 \mu\text{eV}(2P)$

Hyperfine Splitting : $5.9 \mu\text{eV}(1S)$
 $0.7 \mu\text{eV}(2S), 0.2 \mu\text{eV}(2P)$

2S-2P degeneration broken by
Lamb Shift : $\Delta m \sim m_e a^5_{\text{QED}} \sim 4.4 \mu\text{eV}(1S)$



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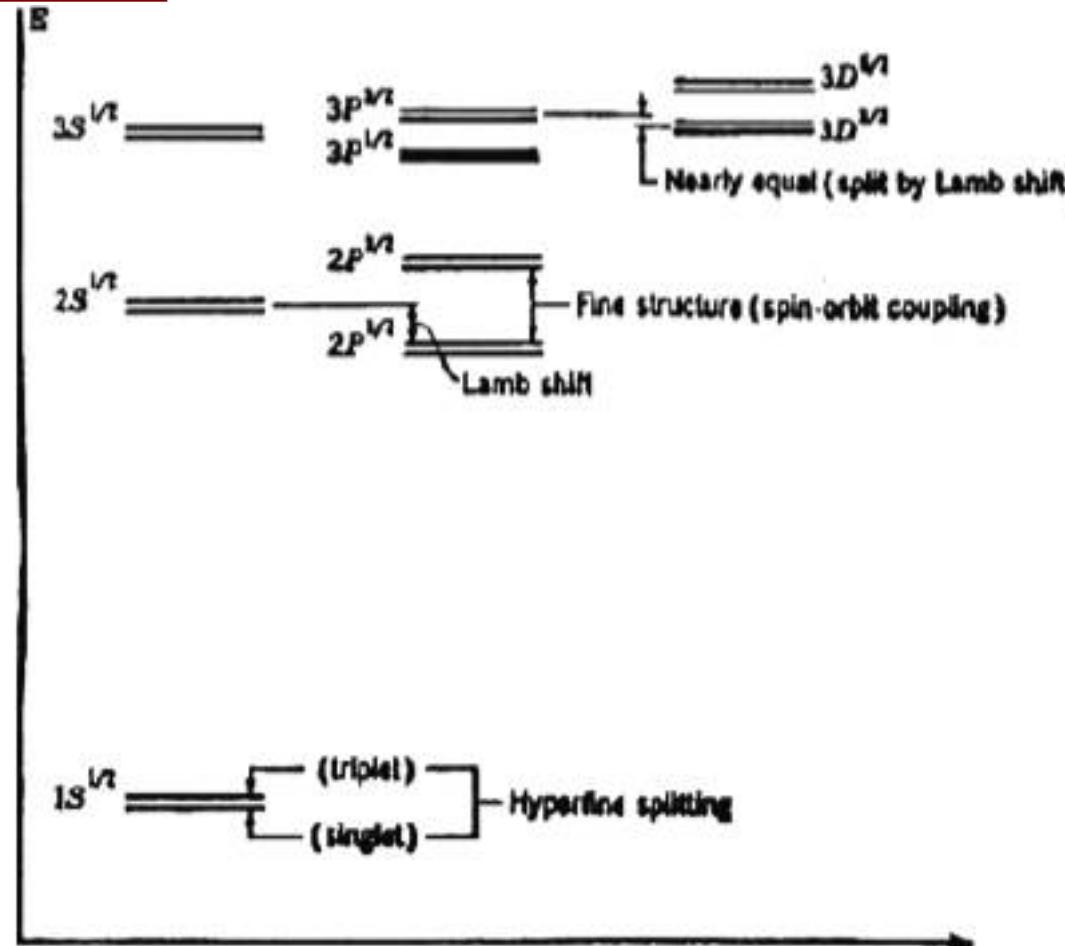
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In QCD :
heavy light
mesons+
baryons

QED example n.2: positronium

Bound state e^+e^-

Non relativistic system
velocity $\sim \beta \sim \alpha_{\text{QED}}$

J,L,S are good quantum numbers

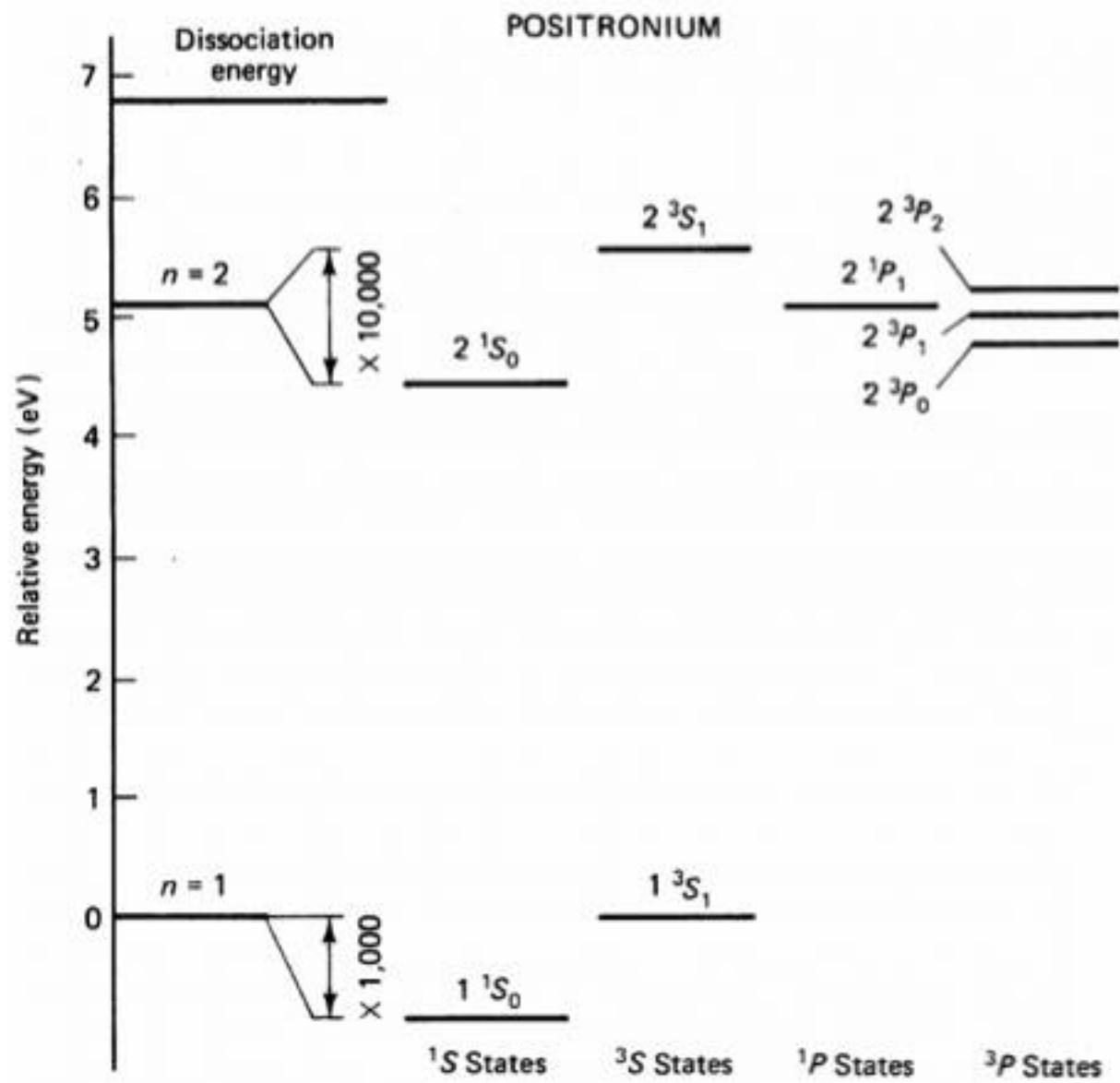
$S=0$: *parapositronium*
Decays to 2 photons
short lifetime

$S=1$: *ortopositronium*
Decays to 3 photons
long lifetime

2S-2P degeneration

Hyperfine Splitting : 1 meV (1S)
0.1 meV (2S)

Fine Splitting: 0.03 meV (2P)



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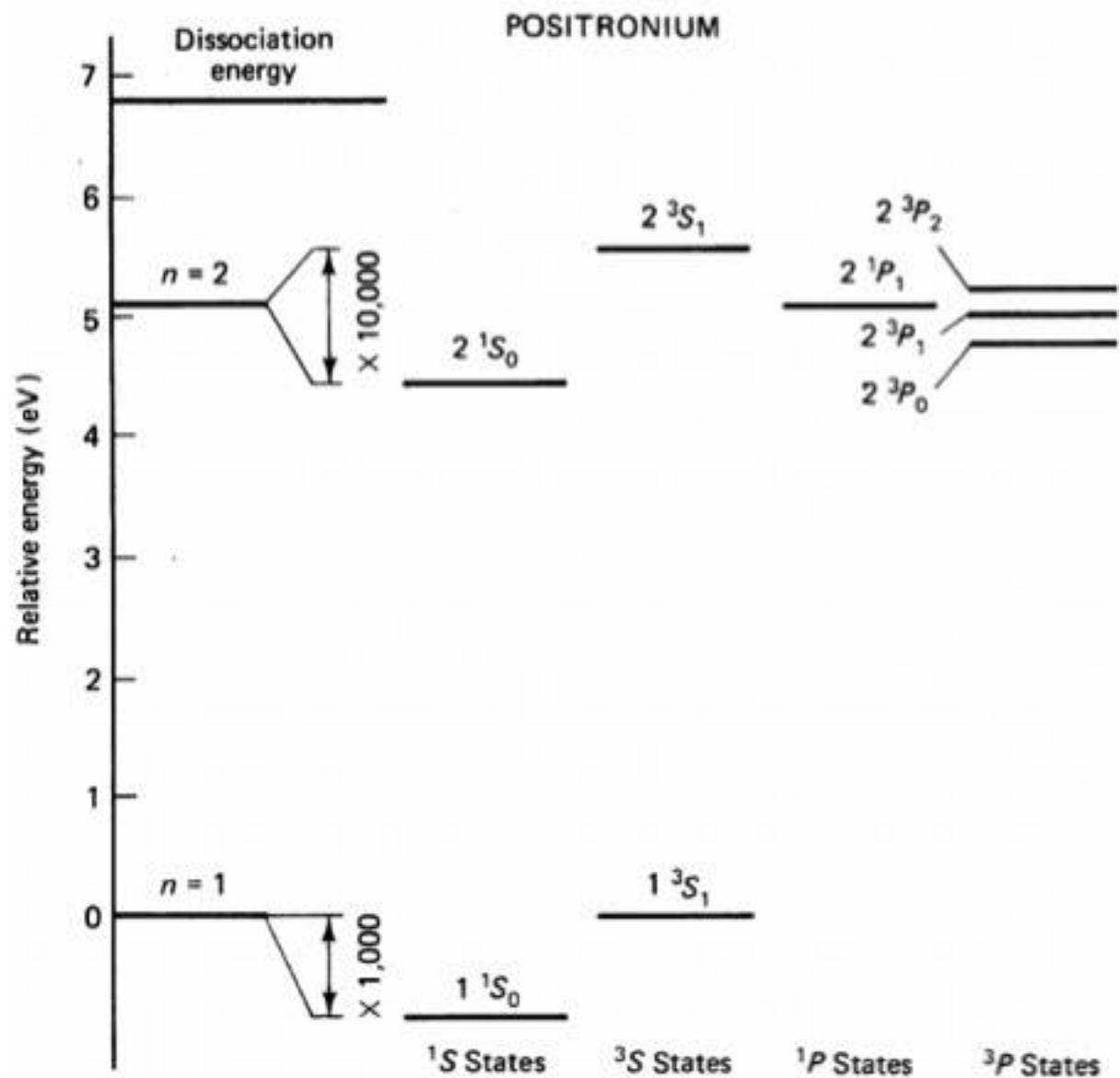
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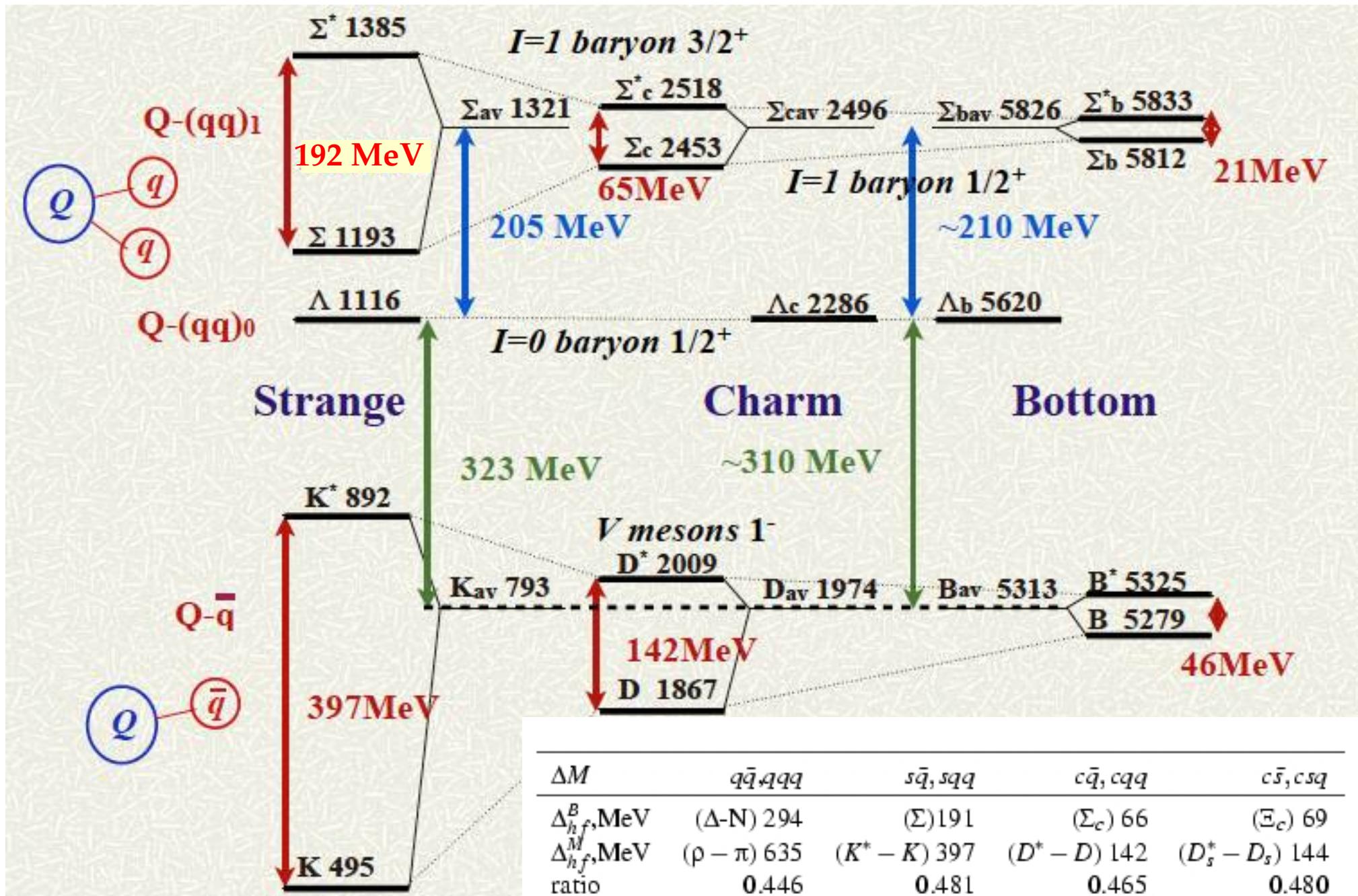
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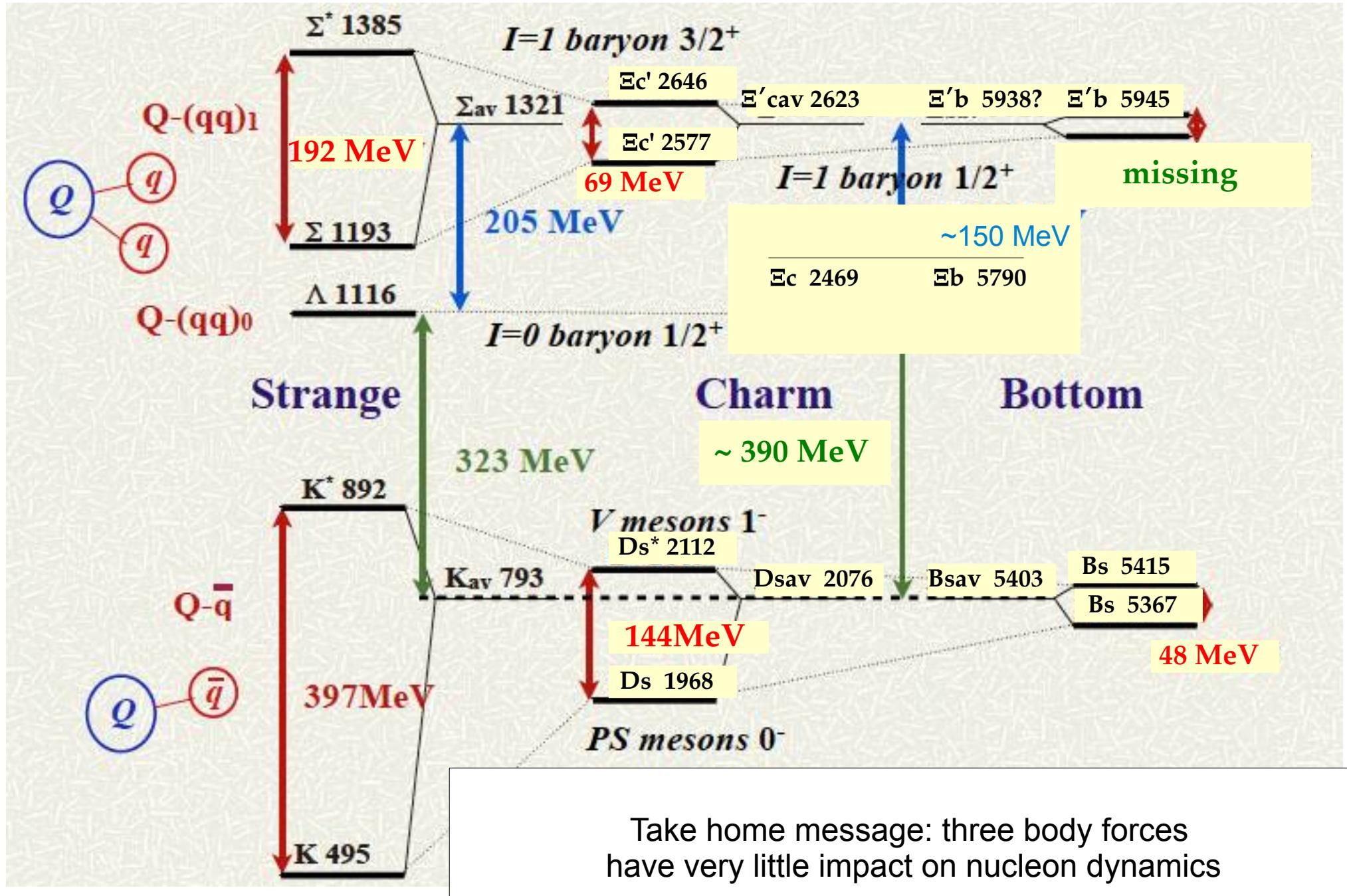


Charmed and Beauty hadron spectra

From Oka's talk
at Hadron 2013



Strange Charmed and Beauty hadron spectra



The unexpected success of constituent quark model

Using a very simple mass formula for the ground states ,
 Karliner and Lipkin (hep-ph/0307243) calculated
 constituent quark mass differences and ratios in baryons
 and mesons **with 2-3% differences: why such a precision?**

$$M = \sum_i m_i + \sum_{i>j} \frac{\vec{\sigma}_i \cdot \vec{\sigma}_j}{m_i \cdot m_j} \cdot v_{IE}^{hyp}$$

Ya.B. Zeldovich and A.D. Sakharov,
Yad. Fiz. 4(1966)395;

$$\langle m_s - m_u \rangle_{Bar} = M_{sud} - M_{uud} = M_\Lambda - M_N = 177 \text{ MeV}$$

$$\langle m_s - m_u \rangle_{Mes} = \frac{3(M_{\bar{s}\bar{d}} - M_{\bar{u}\bar{d}}) + (M_{\bar{s}\bar{d}} - M_{\bar{u}\bar{d}})}{4} = \frac{3(M_{K^*} - M_\rho) + M_K - M_\pi}{4} = 179 \text{ MeV}$$

$$\left(\frac{m_c}{m_s}\right)_{Bar} = \frac{M_{\Sigma^*} - M_\Sigma}{M_{\Sigma_c^*} - M_{\Sigma_c}} = 2.84 = \left(\frac{m_c}{m_s}\right)_{Mes} = \frac{M_{K^*} - M_K}{M_{D^*} - M_D} = 2.81$$

$$\left(\frac{m_c}{m_u}\right)_{Bar} = \frac{M_\Delta - M_p}{M_{\Sigma_c^*} - M_{\Sigma_c}} = 4.36 = \left(\frac{m_c}{m_u}\right)_{Mes} = \frac{M_\rho - M_\pi}{M_{D^*} - M_D} = 4.46$$

$$\left(\frac{\frac{1}{m_u^2} - \frac{1}{m_u m_c}}{\frac{1}{m_u^2} - \frac{1}{m_u m_s}}\right)_{Bar} = \frac{M_{\Sigma_c} - M_{\Lambda_c}}{M_\Sigma - M_\Lambda} = 2.16 \approx \left(\frac{\frac{1}{m_u^2} - \frac{1}{m_u m_c}}{\frac{1}{m_u^2} - \frac{1}{m_u m_s}}\right)_{Mes} = \frac{(M_\rho - M_\pi) - (M_{D^*} - M_D)}{(M_\rho - M_\pi) - (M_{K^*} - M_K)} = 2.10$$

Charmed baryon spectra: P waves

In blue: J=0 diquark ; L=0

In red: J=1 diquark ; L = 0

HF splitting:

[ud]c = 65 MeV

[qs]c = 69 MeV

[ss]c = 71 MeV

In green: J=0 diquark ; L=1

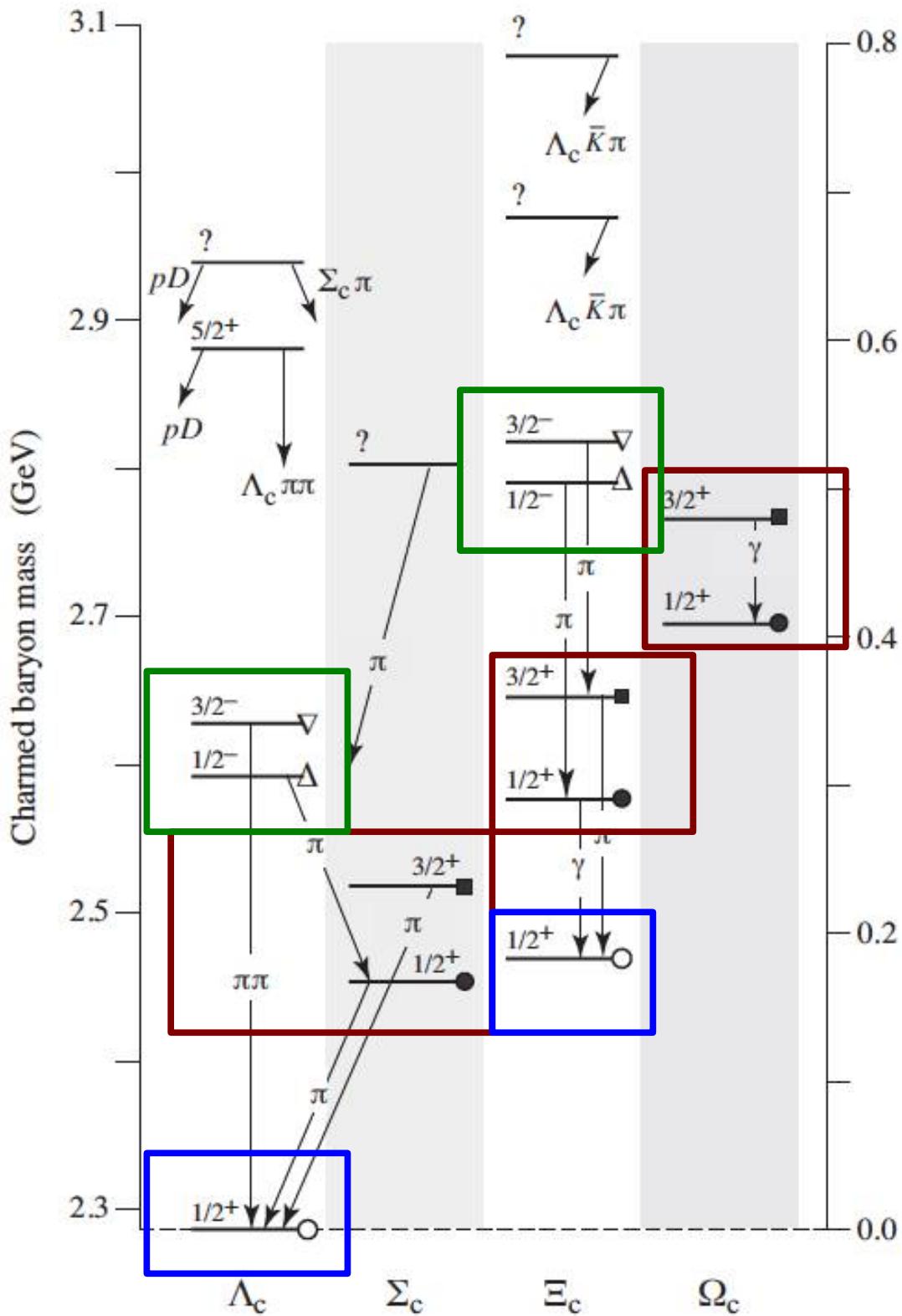
LS splitting:

$$[ud]s = 366.3 \text{ MeV}$$

$$[ud]c = 329.7 \text{ MeV}$$

$$[qs]_c = 339.8 \text{ MeV}$$

$$[ud]\bar{b} = 297.8 \text{ MeV}$$





QWG Workshops on Heavy Quarkonium:

[QWG1](#): CERN, November 8 to 10, 2002

[QWG2](#): Fermilab, September 20 to 22, 2003

[QWG3](#): Beijing, October 12 to 15, 2004

[QWG4](#): Brookhaven, June 27 to 30, 2006

[QWG5](#): DESY Hamburg, October 12 to 15, 2007

[QWG6](#): Nara Women's University, December 2 to 5, 2008

[QWG7](#): Fermilab, May 18 to 21, 2010

[QWG8](#): GSI Darmstadt, October 3 to 7, 2011

[QWG9](#): IHEP Beijing, April 22 to 26, 2013

[QWG10](#): CERN, November 10 to 14, 2014

YELLOW REPORT :
CERN-2005-005,
ArXiv: hep-ph/0412158

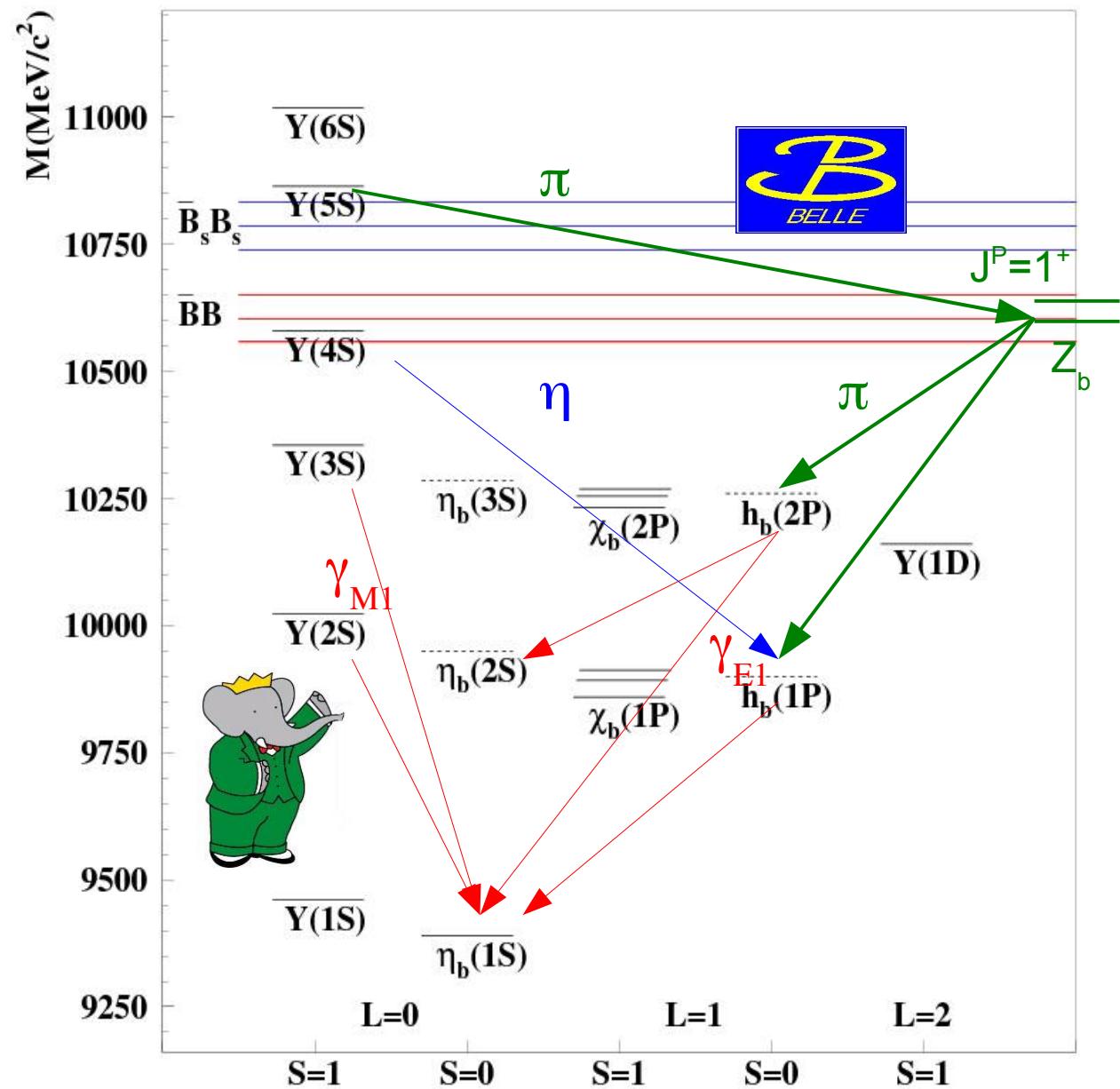
2nd QWG Report :
Eur.Phys.J. C71 (2011) 1534 ,
ArXiv:1010.5827,

The quest for parabottomonia

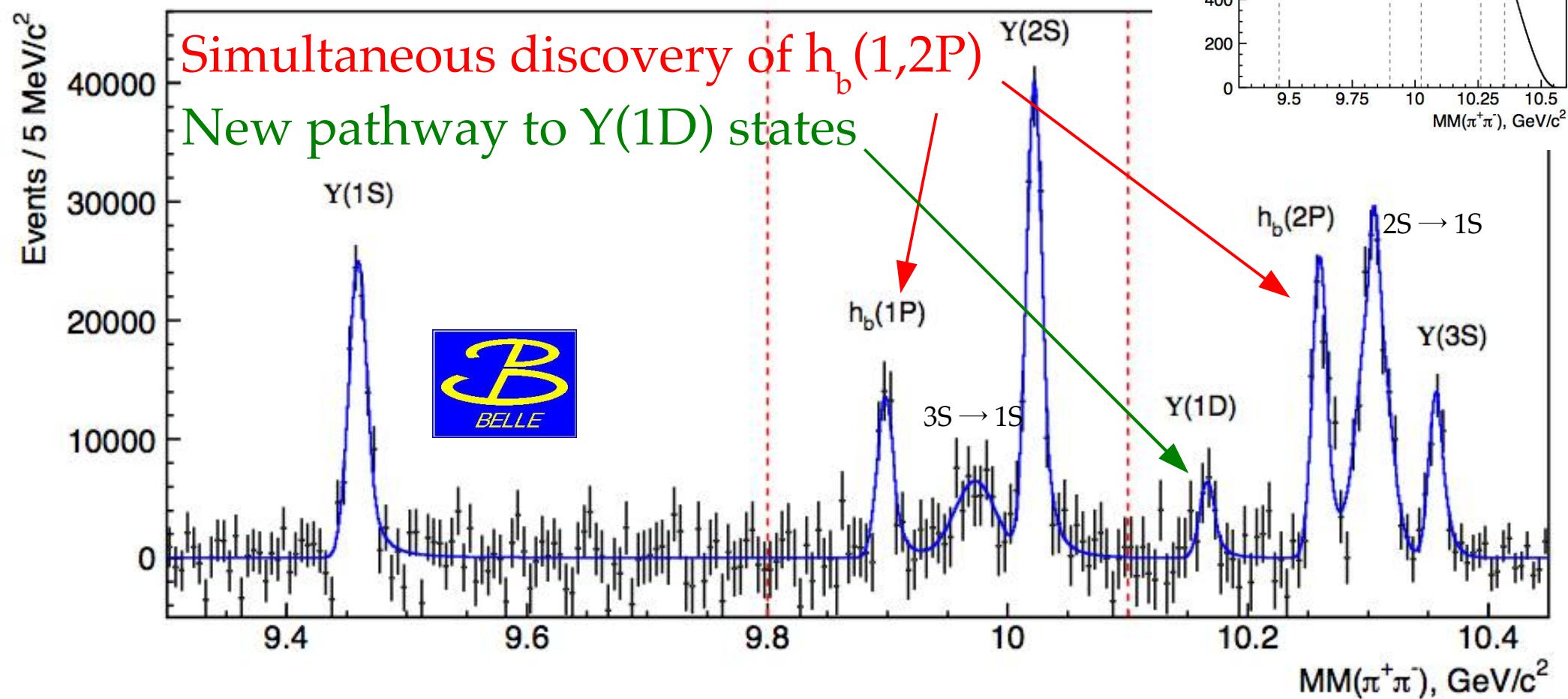
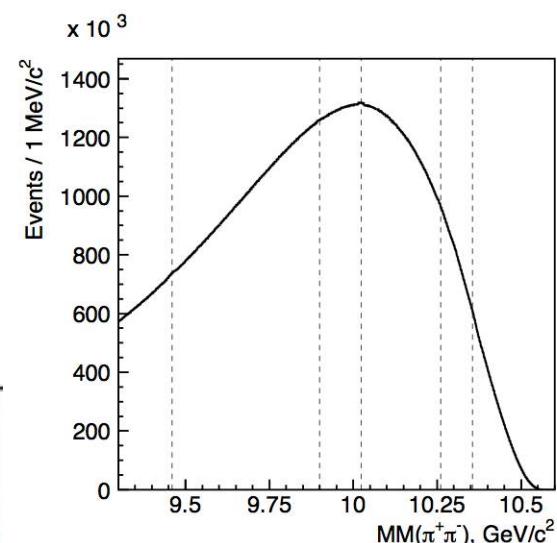
5 amazing years for
bottomonium
spectroscopy:

- Y_b / $Y(5S)$: observation
of large dipion transitions
to $Y(1,2,3S)$ from 20 MeV
above 5S peak
- 2008 Discovery of
 η_b (Babar)
- 2011-2: Discovery of the
triple cascade $Y_b \rightarrow Z_b \rightarrow$
 $h_b \rightarrow \eta_b$

Belle discovers 4
parabottomonia , and 2
4quark states in one shot!



Inclusive search : $e^+e^- \rightarrow \Upsilon(5S) \rightarrow \pi^+\pi^- + \dots$



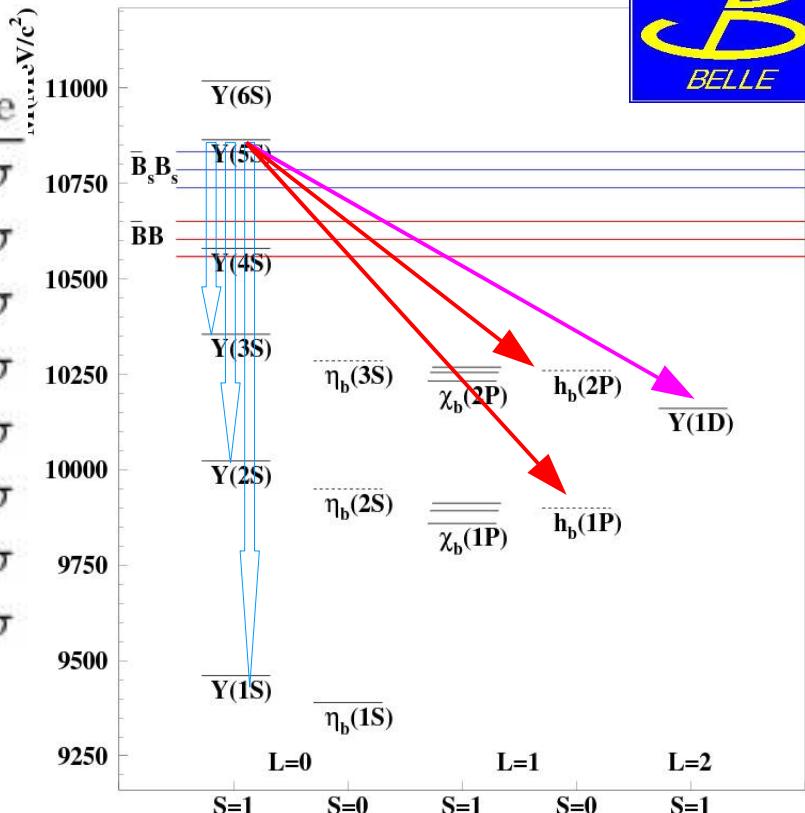
$h_b(1,2P)$ from $\Upsilon(5S)$

PRL108,032001



	Yield, 10^3	Mass, MeV/c^2	Significance
$\Upsilon(1S)$	$105.2 \pm 5.8 \pm 3.0$	$9459.4 \pm 0.5 \pm 1.0$	$\leftrightarrow 18.2\sigma$
$h_b(1P)$	$50.4 \pm 7.8^{+4.5}_{-9.1}$	$9898.3 \pm 1.1^{+1.0}_{-1.1}$	$\leftrightarrow 6.2\sigma$
$3S \rightarrow 1S$	56 ± 19	9973.01	2.9σ
$\Upsilon(2S)$	$143.5 \pm 8.7 \pm 6.8$	$10022.3 \pm 0.4 \pm 1.0$	$\leftrightarrow 16.6\sigma$
$\Upsilon(1D)$	22.0 ± 7.8	10166.2 ± 2.6	$\leftrightarrow 2.4\sigma$
$h_b(2P)$	$84.4 \pm 6.8^{+23.}_{-10.}$	$10259.8 \pm 0.6^{+1.4}_{-1.0}$	$\leftrightarrow 12.4\sigma$
$2S \rightarrow 1S$	$151.7 \pm 9.7^{+9.0}_{-20.}$	$10304.6 \pm 0.6 \pm 1.0$	15.7σ
$\Upsilon(3S)$	$45.6 \pm 5.2 \pm 5.1$	$10356.7 \pm 0.9 \pm 1.1$	$\leftrightarrow 8.5\sigma$

Significance after correcting $h_b(1P)$ 5.5σ
for systematics effects: $h_b(2P)$ 11.2σ



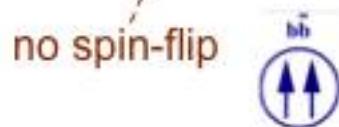
Masses very close to the state COG of χ states, as $\Delta M_{HF}(1P) = 1.6 \pm 1.5 \text{ MeV}/c^2$ $\Delta M_{HF}(2P) = 0.5^{+1.6}_{-1.2} \text{ MeV}/c^2$ expected from theory.



Ratio of spin flip vs noflip dipion transitions totally unexpected from theory....

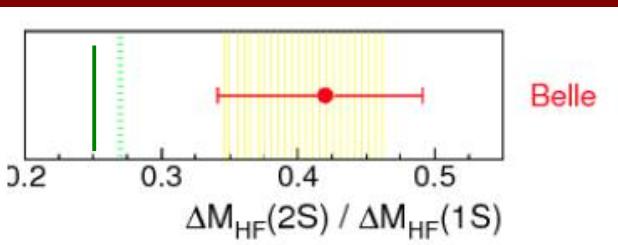


$$\frac{\Gamma[\Upsilon(5S) \rightarrow h_b(nP) \pi^+ \pi^-]}{\Gamma[\Upsilon(5S) \rightarrow \Upsilon(2S) \pi^+ \pi^-]} = \begin{cases} 0.46 \pm 0.08^{+0.07}_{-0.12} & \text{for } h_b(1P) \\ 0.77 \pm 0.08^{+0.22}_{-0.17} & \text{for } h_b(2P) \end{cases}$$



Parabottomonia vs theory

$\eta_b(2S)$ vs $\eta_b(1S)$

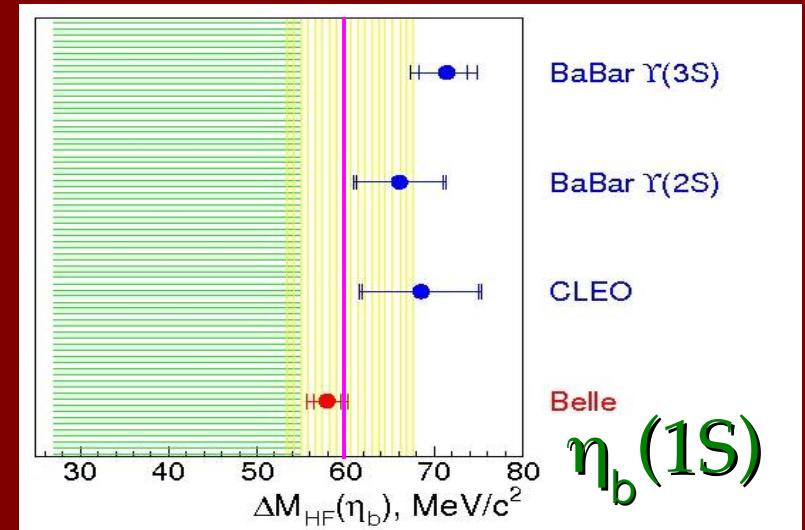


PNRQCD@NLL
PRL92,242001(2004)

Lattice QCD
PRD82,114502(2010)

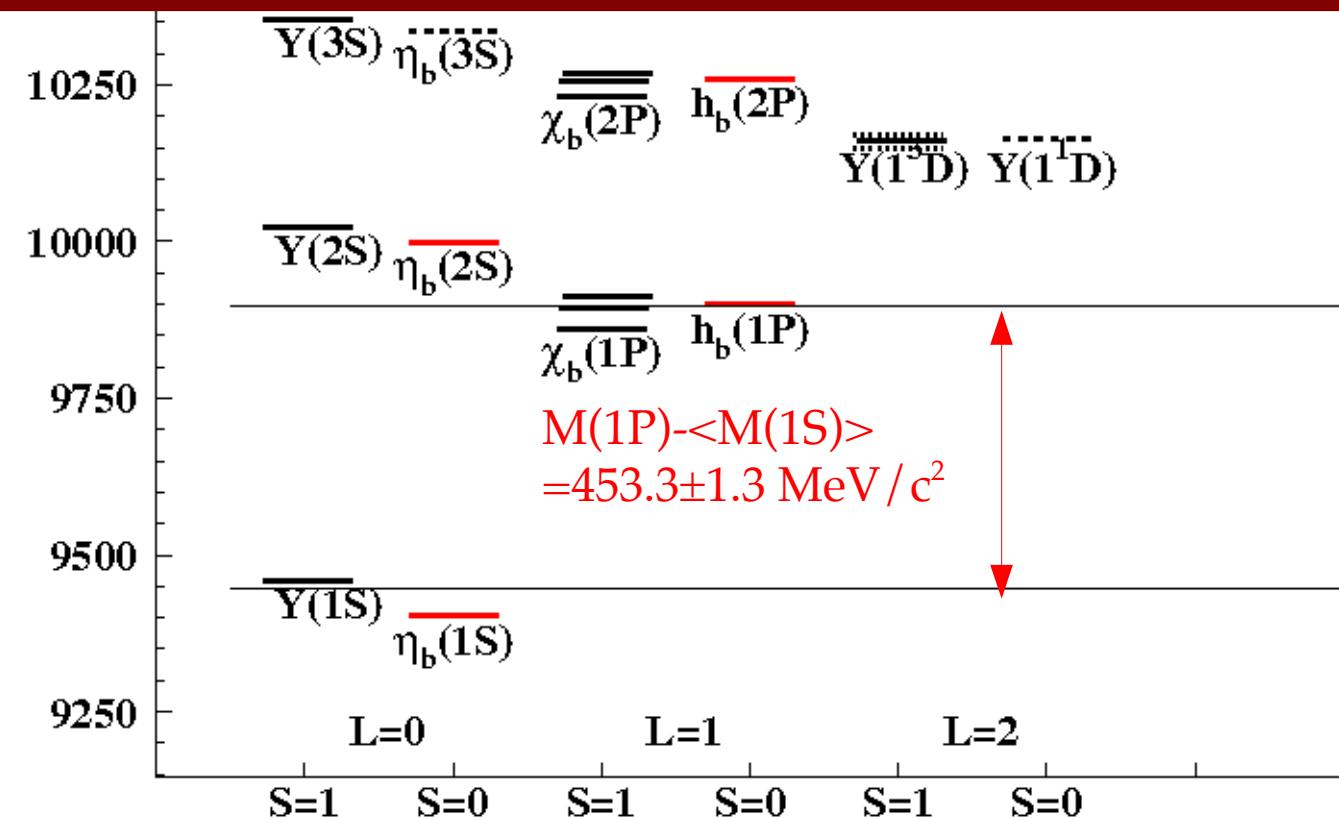
Godfrey-Isgur,
PRD32,189 (1985)

10 MeV discrepancy
w/ earlier Babar
and CLEO results



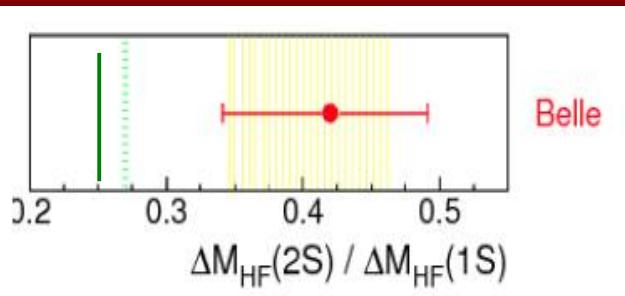
Some tension with the
most accurate NRQCD
prediction , but very close
to lattice QCD (Meinel)
predictions.

Spin averaged 1P-1S
splitting seems not
to depend on scale



Parabottomonia vs theory

$\eta_b(2S)$ vs $\eta_b(1S)$

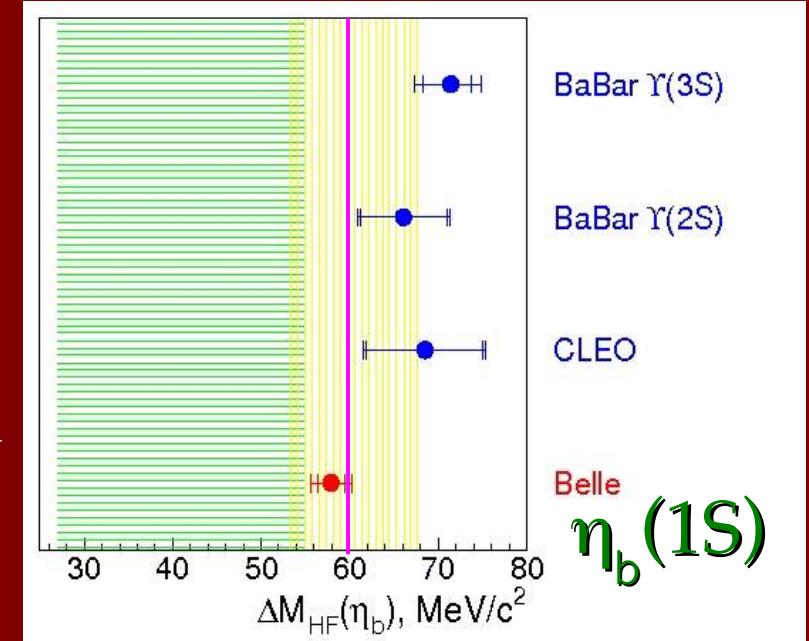


PNRQCD@NLL
PRL92,242001(2004)

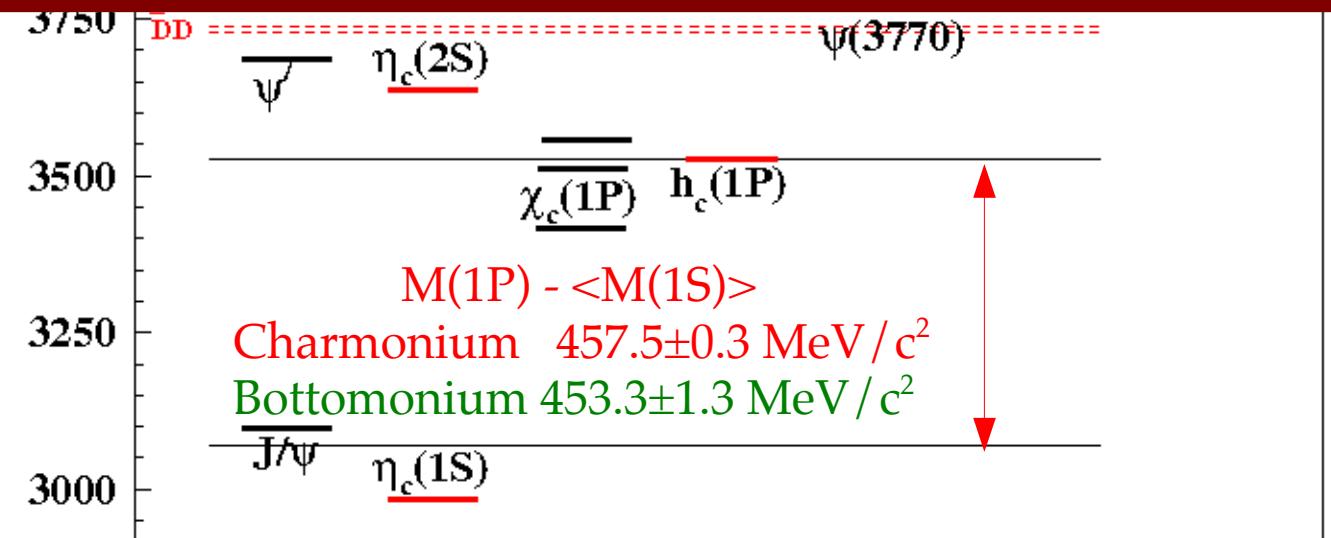
Lattice QCD
PRD82,114502(2010)

Godfrey-Isgur,
PRD32,189 (1985)

10 MeV discrepancy
w/ earlier Babar
and CLEO results:
Skewed lineshape as
in charmonium?



Spin averaged 1P-1S
splitting seems not to
depend on scale:
only 1% difference with
charmonium: similarly,
the tensor-vector
splitting remains
constant also in D,Ds.



$M(2^+)-M(1^-)$, in MeV/c^2

452 ± 2

449 ± 4

461 ± 2

458.3 ± 0.1

452.3 ± 0.6

Holy Grail: $\eta_b(1S) \rightarrow \gamma\gamma$

Search for $\eta_b(1S) \rightarrow \gamma\gamma$

via exclusive channel: $\pi^+\pi^-\gamma(\gamma\gamma)$!!

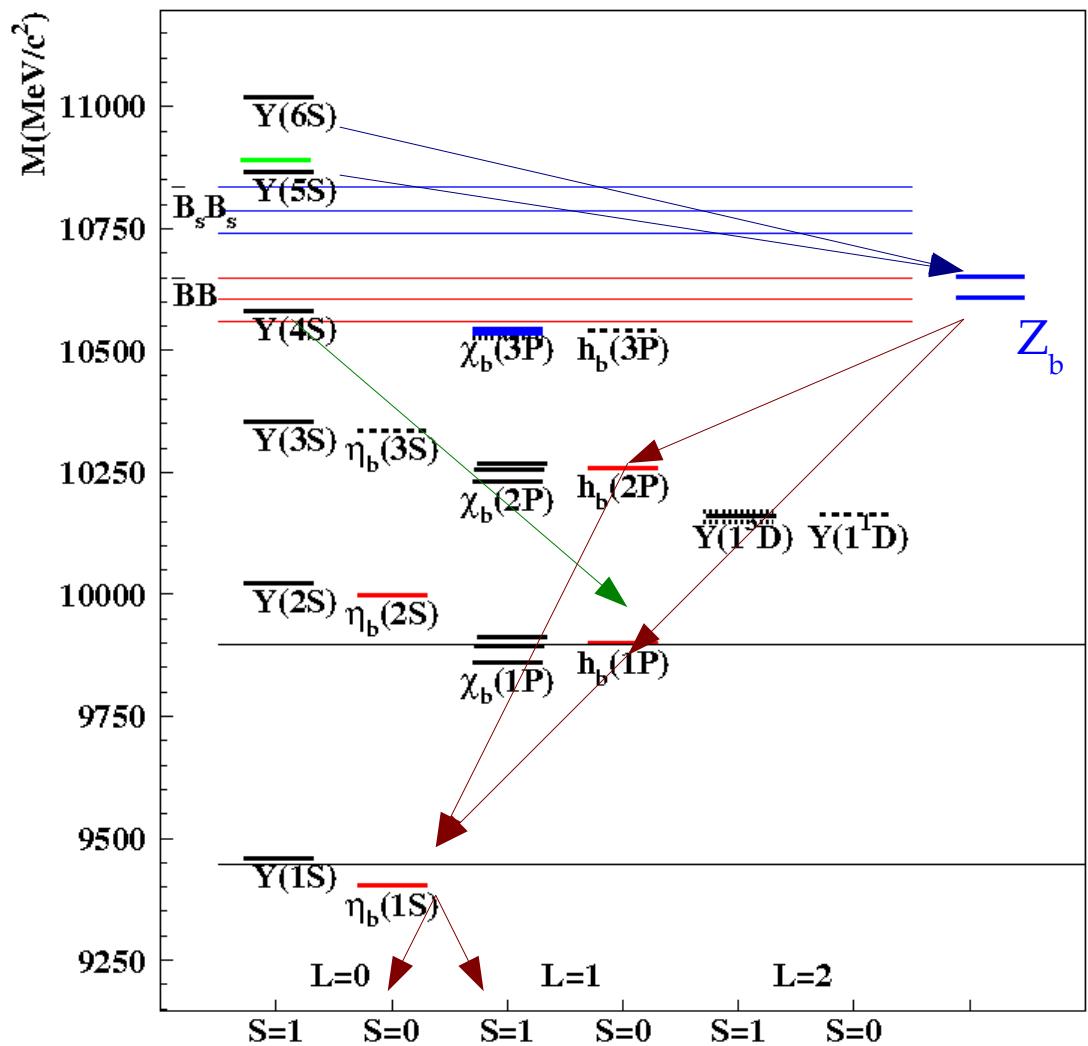
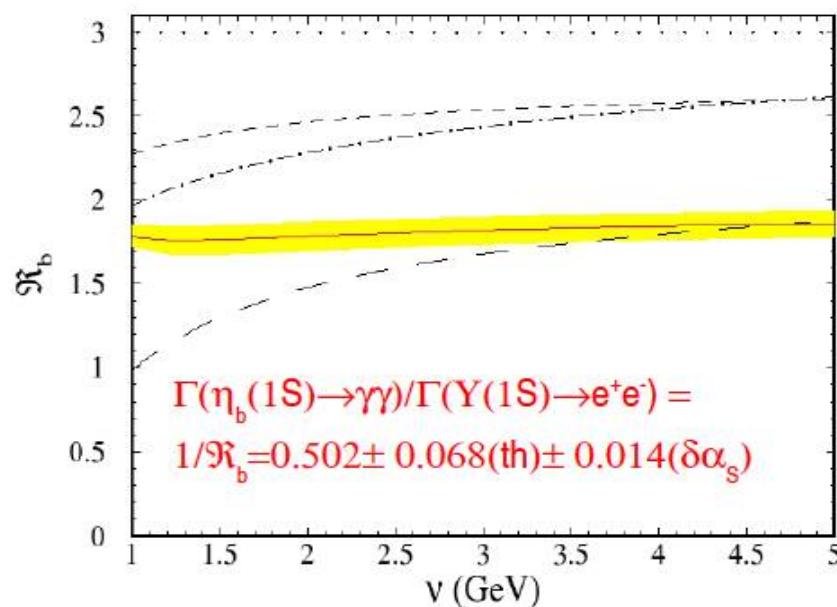
NRQCD NNLL prediction:

Penin et al., NP B699(2004), 183

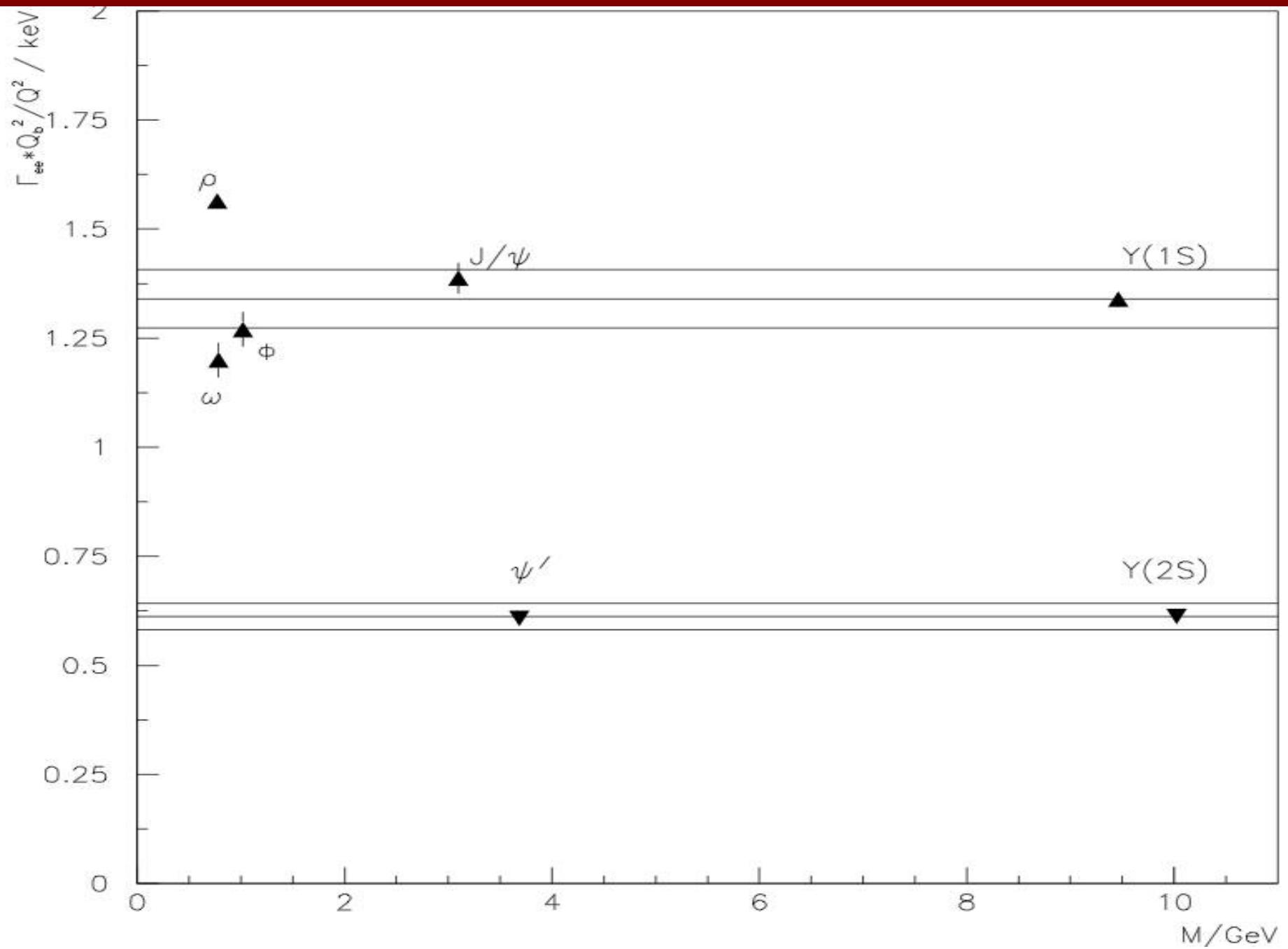
$$\Gamma(\eta_b(1S) \rightarrow \gamma\gamma) = 0.66 \pm 0.09 \text{ keV}$$

With $\Gamma(\eta_b) = 10 \text{ MeV}$,

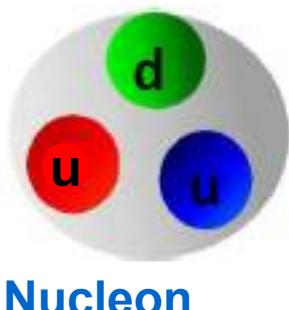
$$\text{BR}(\eta_b(1S) \rightarrow \gamma\gamma) = 0.66 * 10^{-4}$$



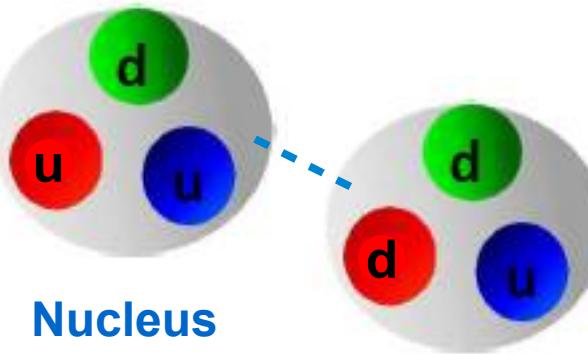
Why the van Royen-Weisskopf formula works so well?



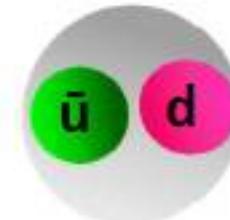
Bound states in QCD



Nucleon



Nucleus



Meson

.... what else?



Pentaquark

$S = +1$
Baryon



H di-Baryon

Tightly bound
6 quark state

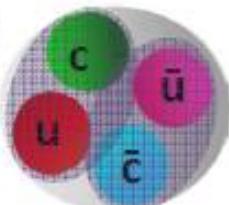


Glueball

Color-singlet multi-
gluon bound state

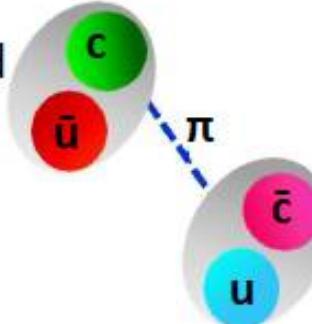
Tetraquark

Tightly bound
diquark &
anti-diquark

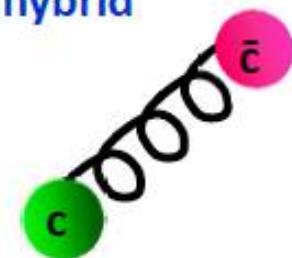


Molecule

loosely bound
meson-
antimeson
"molecule"



$q\bar{q}$ -gluon hybrid
mesons

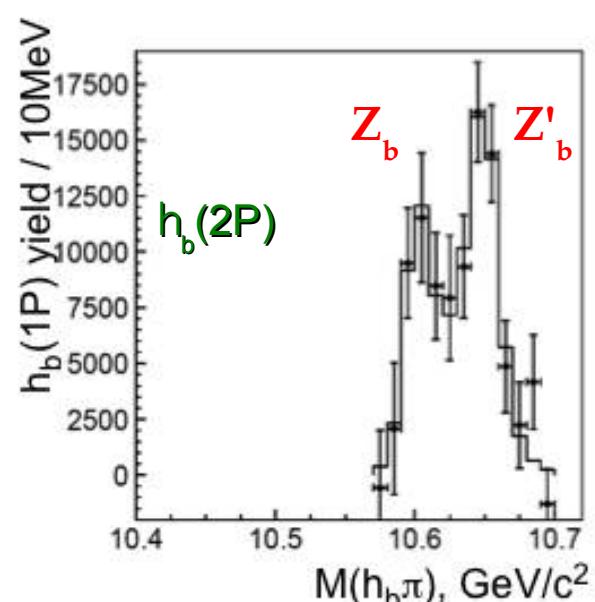
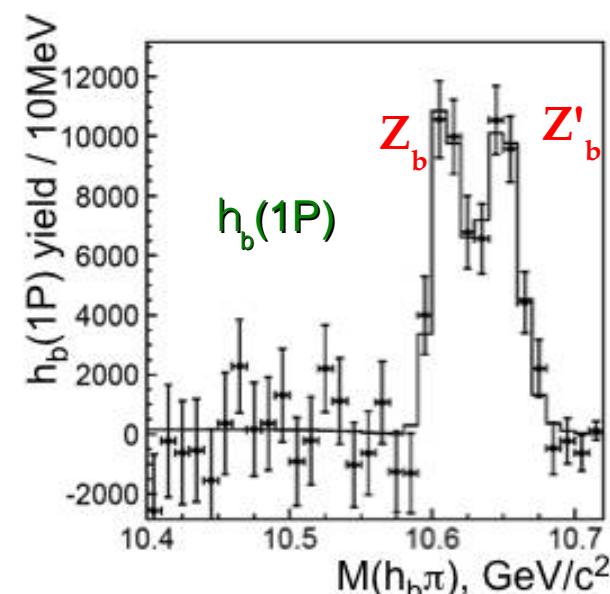


Charged Bottomonia : Z_b 's

The two charged bottomonium states are observed in single pion recoil in 5 processes:

- inclusive $Y(5S)$ decays to $h_b(1,2P)$

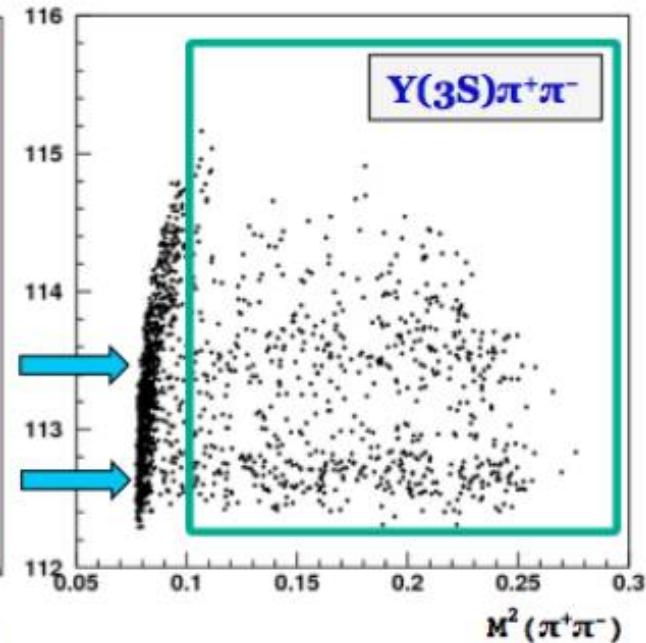
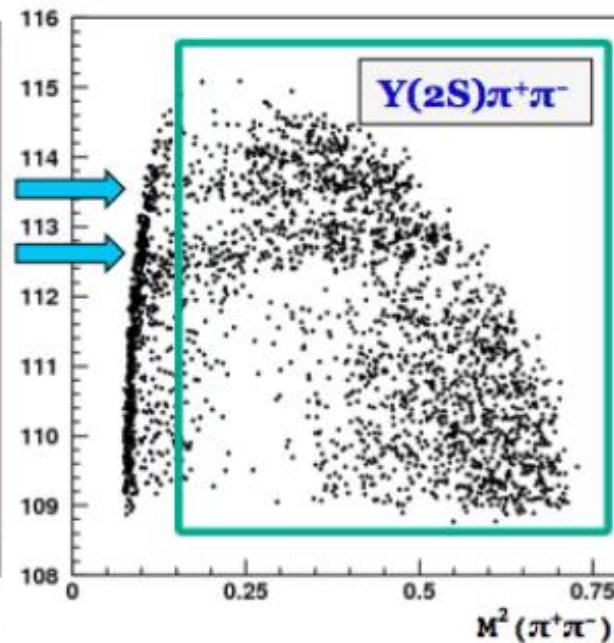
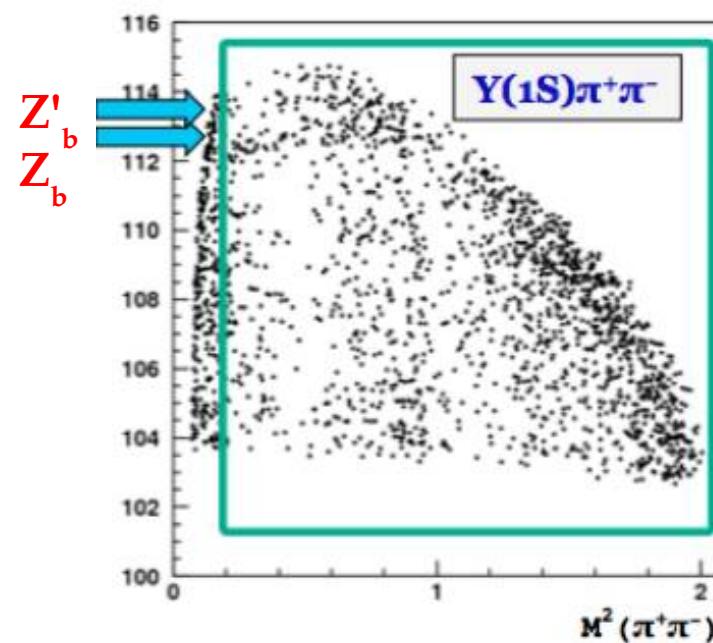
- Dalitz plot of exclusive $Y(5S)$ dipion transitions to $Y(1,2,3S)$



9.43 GeV < MM($\pi^+\pi^-$) < 9.48 GeV

10.05 GeV < MM($\pi^+\pi^-$) < 10.10 GeV

10.33 GeV < MM($\pi^+\pi^-$) < 10.38 GeV



Z_b parameters

PRL108,122001(2011)

Belle discovered two charged bottomonium-like resonances:

$Z(10610)$

$M = 10607.2 \pm 2.0$ MeV

$\Gamma = 18.4 \pm 2.4$ MeV

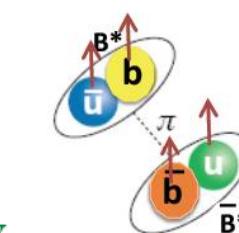
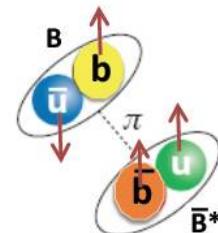
$M_B + M_{B^*} = 10604.5 \pm 0.6$ MeV

$Z(10650)$

$M = 10652.2 \pm 1.5$ MeV

$\Gamma = 11.5 \pm 2.2$ MeV

$M_{B^*} + M_{B^{**}} = 10650.2 \pm 1.0$ MeV

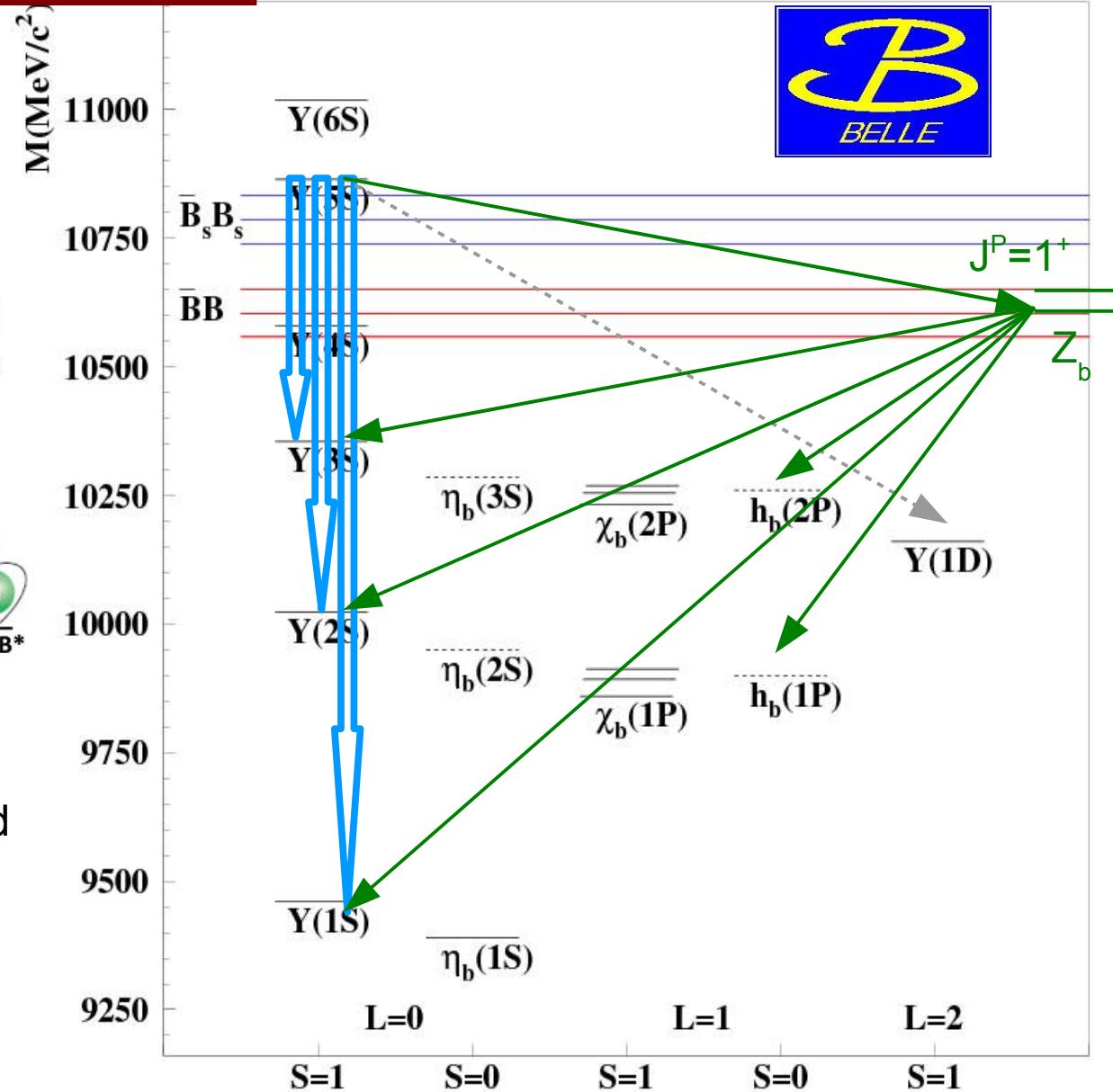


Analysis of angular distributions suggests $J^P=1^+$ for both these states. Observation of Z_b decays to BB^* and B^*B^* is consistent with molecular nature of the charged bottomonia. (Voloshin, Bondar, et al)

ArXiv:1207.4345:

Evidence of neutral partner of lower Z_b in $Y\pi^0$ with 4.9 sigma significance

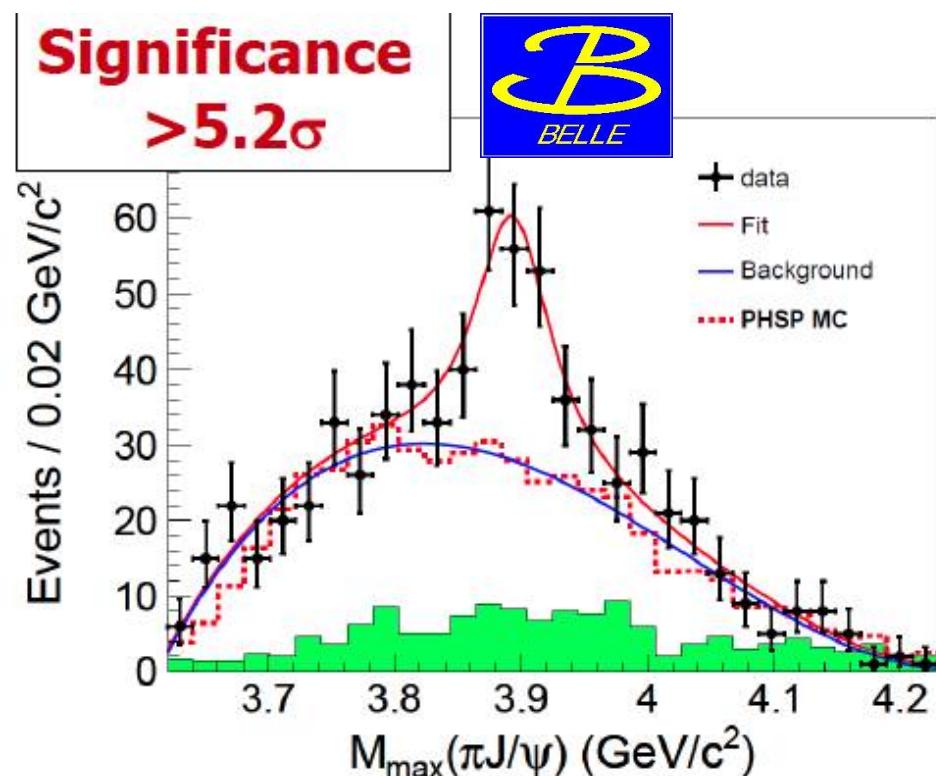
52nd Bormio Meeting, 29/1/2014



R.Mussa, Hadron Physics at Belle II

Zc(3900): tetraquarks or meson molecules?

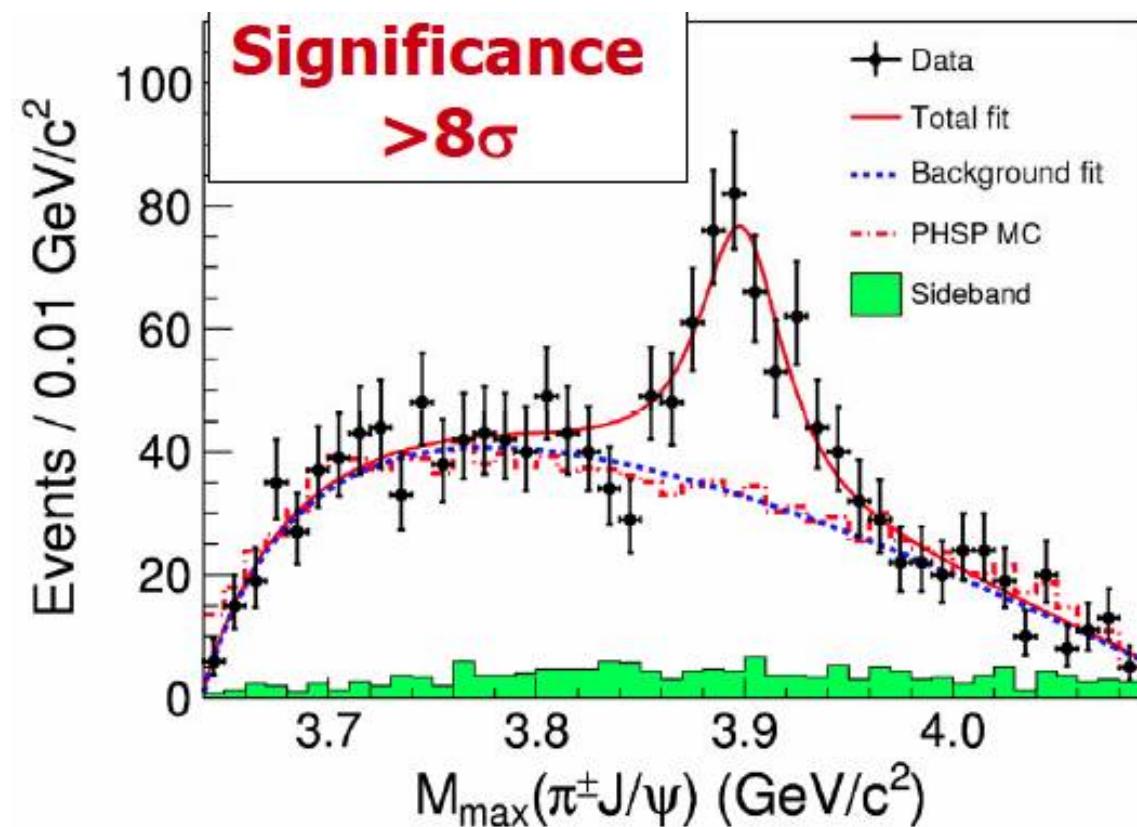
BES-III



Belle: 927 fb^{-1} of ISR data at $\Upsilon(nS)$ energy

Phys.Rev.Lett. 110 (2013) 252002

- Mass = $(3894.5 \pm 6.6 \pm 4.5) \text{ MeV}$
- Width = $(63 \pm 24 \pm 26) \text{ MeV}$
- Fraction = $(29.0 \pm 8.9)\%$ (stat. error only)

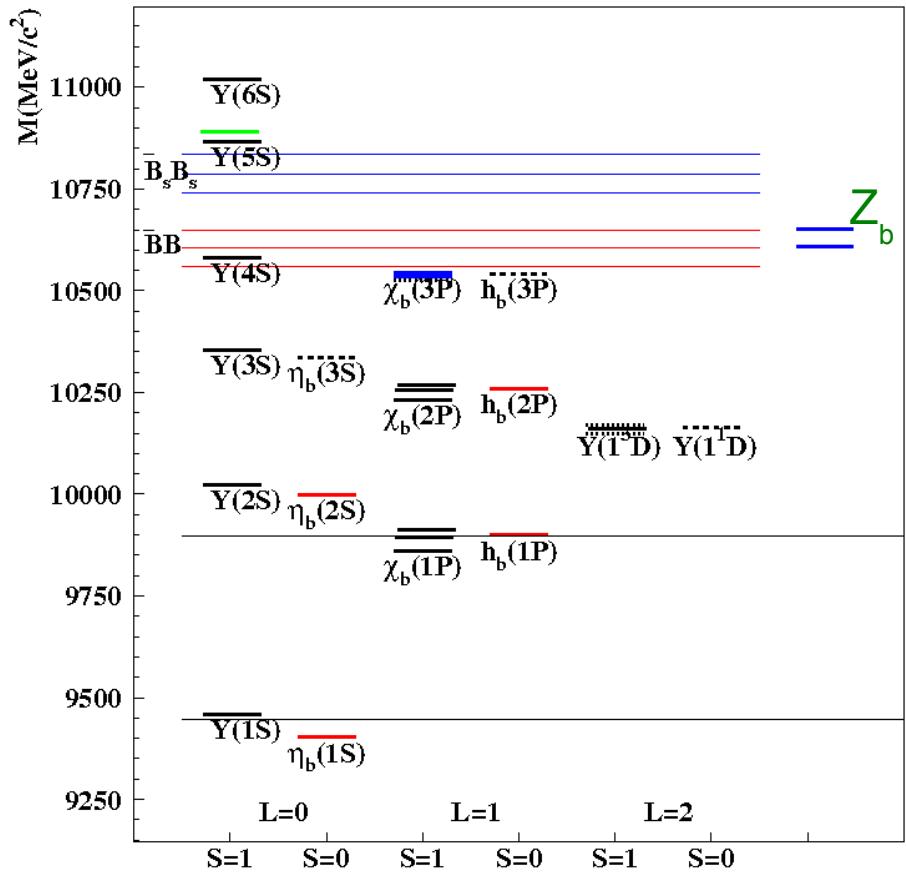
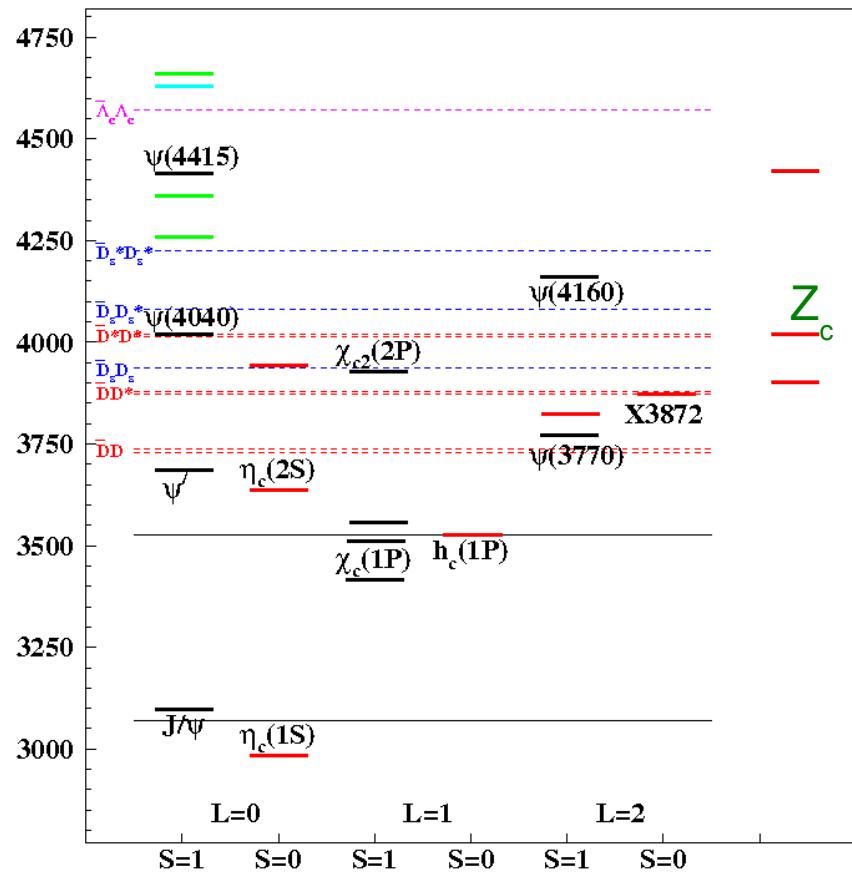


BES-III: 525 pb^{-1} @ $\Upsilon(4260)$ peak energy

Phys.Rev.Lett. 110 (2013) 252001

- Mass = $(3899.0 \pm 3.6 \pm 4.9) \text{ MeV}$
- Width = $(46 \pm 10 \pm 20) \text{ MeV}$
- Fraction = $(21.5 \pm 3.3 \pm 7.5)\%$

Charged heavy quarkonia

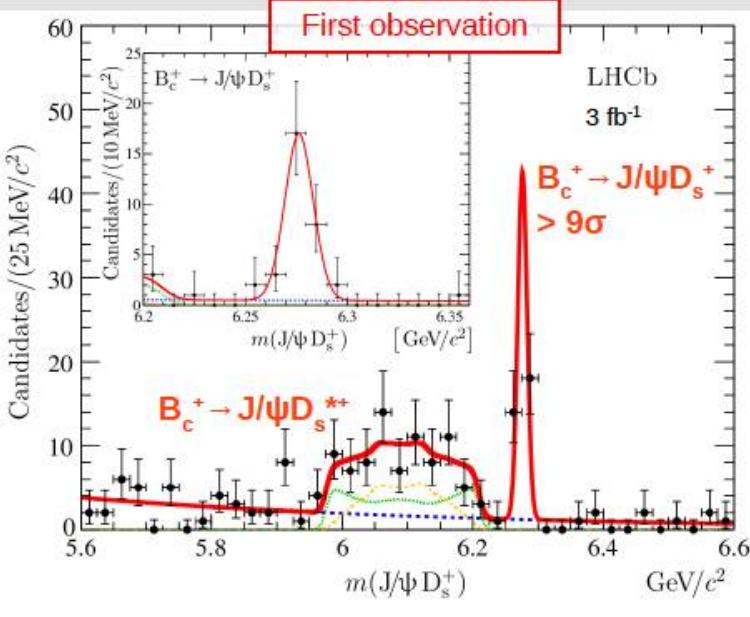


In the last years , 2 (+3 in B decays) Zc states and 2 Zb states were observed: their nature is still uncertain : tetraquark or molecules? Further studies are needed to build a model of these states.

Future: Bc spectroscopy

Most precise mass measurement

- by studying $B_c^+ \rightarrow J/\psi D_s^{(*)+}$ decays

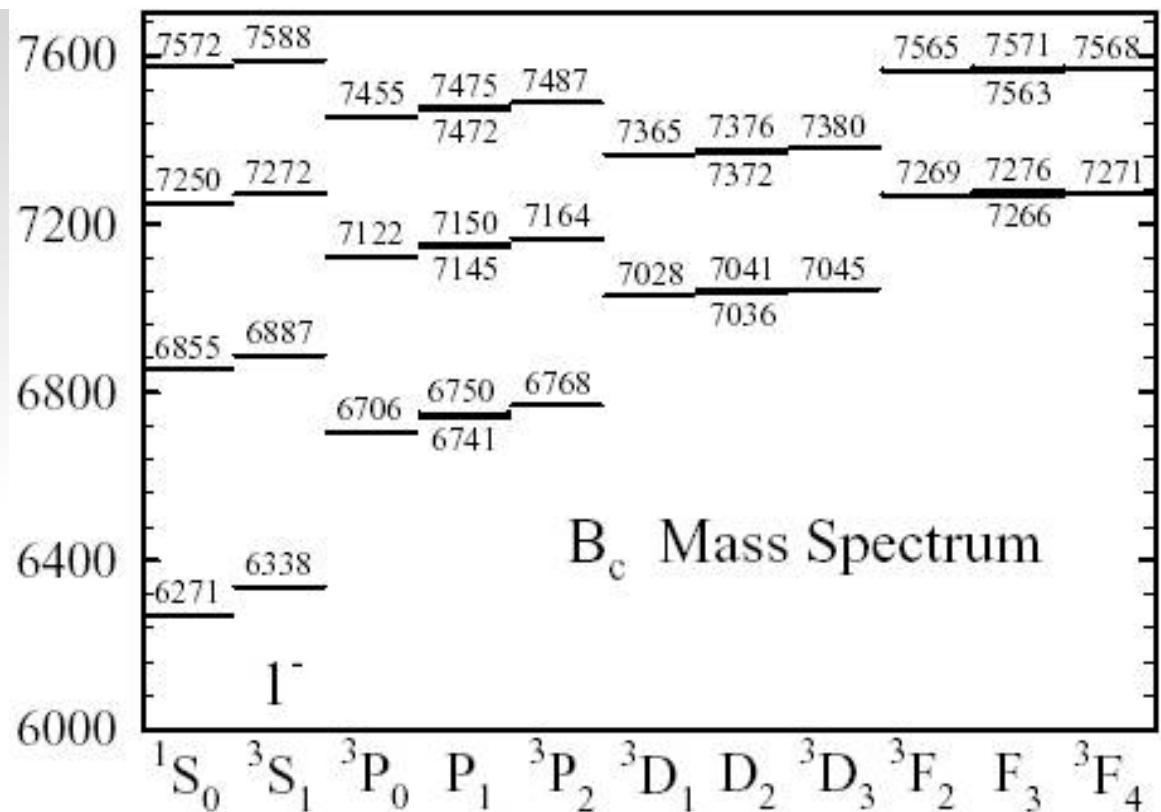


$$m_{B_c} = 6276.28 \pm 1.44 \text{ (stat)} \pm 0.36 \text{ (syst)} \text{ MeV}/c^2$$

LHCb, 3 fb⁻¹, PRD 87 (2013) 112012

- In agreement with world average:
 $m(B_c^+) = 6274.5 \pm 1.8 \text{ MeV}/c^2$

Polyakov Ivan, Moriond QCD, 24 March 2014



Photon and dipion transitions
to study the Bc spectrum : a
great opportunity for **LHCb!**

A pretty consistent pattern is emerging in the spectra of heavy baryons, heavy-light mesons, heavy onia, which shows little dependence on the mass scale, and on the running properties of QCD coupling constant. Besides the large developments of QCD based EFTs (NRQCD,HQET, chiral EFT,SCET, and lattice QCD) the success of constituent quark model is hard to be explained from first principles. Are we overlooking some hidden symmetry?

Spin anomalies in hadron transition amplitudes has led to nice surprises in the recent years of heavy quarkonium spectroscopy, and may need to further interesting developments.

While future spectroscopy studies will focus on B_c , P waves, and multiquark systems, more information can come from the studies of hadronic and radiative transitions of known states.

The η transitions

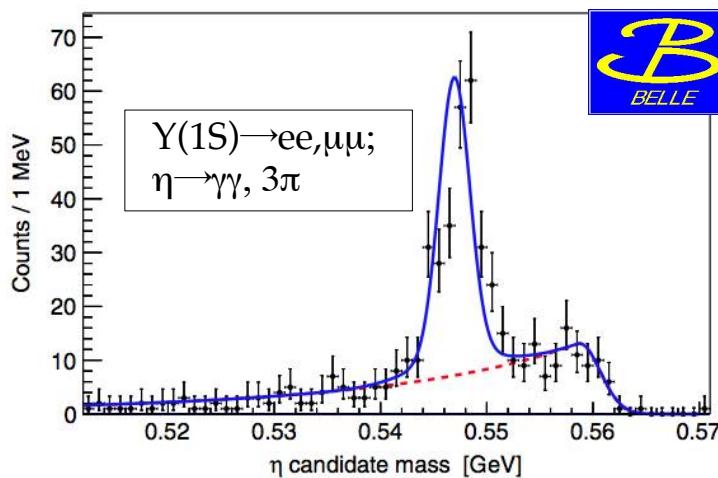
Testing QCD multipole expansion

In low mass region:

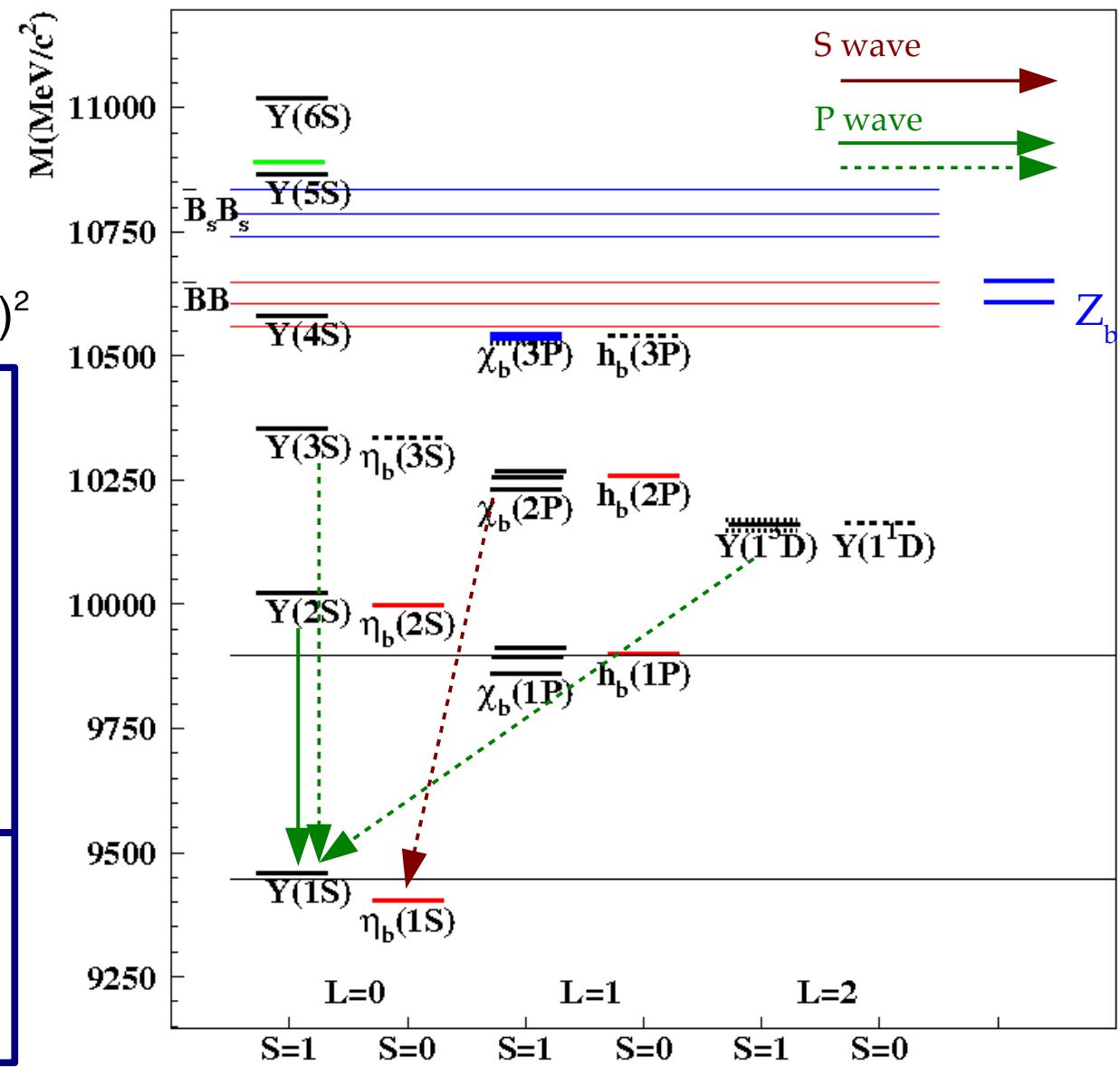
$$Y' \rightarrow \eta Y : M2^*E1 + M1^*M1$$

$$Y' \rightarrow \pi\pi Y : E1^*E1$$

$$(Y' \rightarrow \eta Y) / (Y' \rightarrow \pi\pi Y) \sim (\Lambda_{\text{QCD}} / m_b)^2$$



$B(Y(2S) \rightarrow \eta Y(1S))$	theory(*): $\sim 4 \times 10^{-4}$
CLEO PRL101,192001	$(2.10 \pm 0.70 \pm 0.40) \times 10^{-4}$
BaBar PRD84,42003(2011)	$(2.39 \pm 0.31 \pm 0.14) \times 10^{-4}$
Belle PRD87,011104(R)(2013)	$(3.41 \pm 0.28 \pm 0.35) \times 10^{-4}$



(*) Most theory papers are in the range $7-16 \times 10^{-4}$. Voloshin, Prog.Part.Nucl.Phys.61,455(2008), predicts 4.3×10^{-4}

- The process $Y(1D) \rightarrow \eta Y(1S)$ should be enhanced with respect to $Y(1D) \rightarrow \pi\pi Y(1S)$ because of Triangle anomaly in QCD Voloshin: PLB 562, 68(2003) **Work in progress at Belle**

The η transitions

QCDME does not apply on higher states: coupled channel effects proposed, need more crosschecks.

Babar [PRD78,112002 \(2008\)](#)

$B(\Upsilon(4S) \rightarrow \eta \Upsilon(1S))$

$$= (1.96 \pm 0.06 \pm 0.09) \times 10^{-4}$$

$$= 2.5 \times B(\Upsilon(4S) \rightarrow \pi\pi \Upsilon(1S))$$

Belle

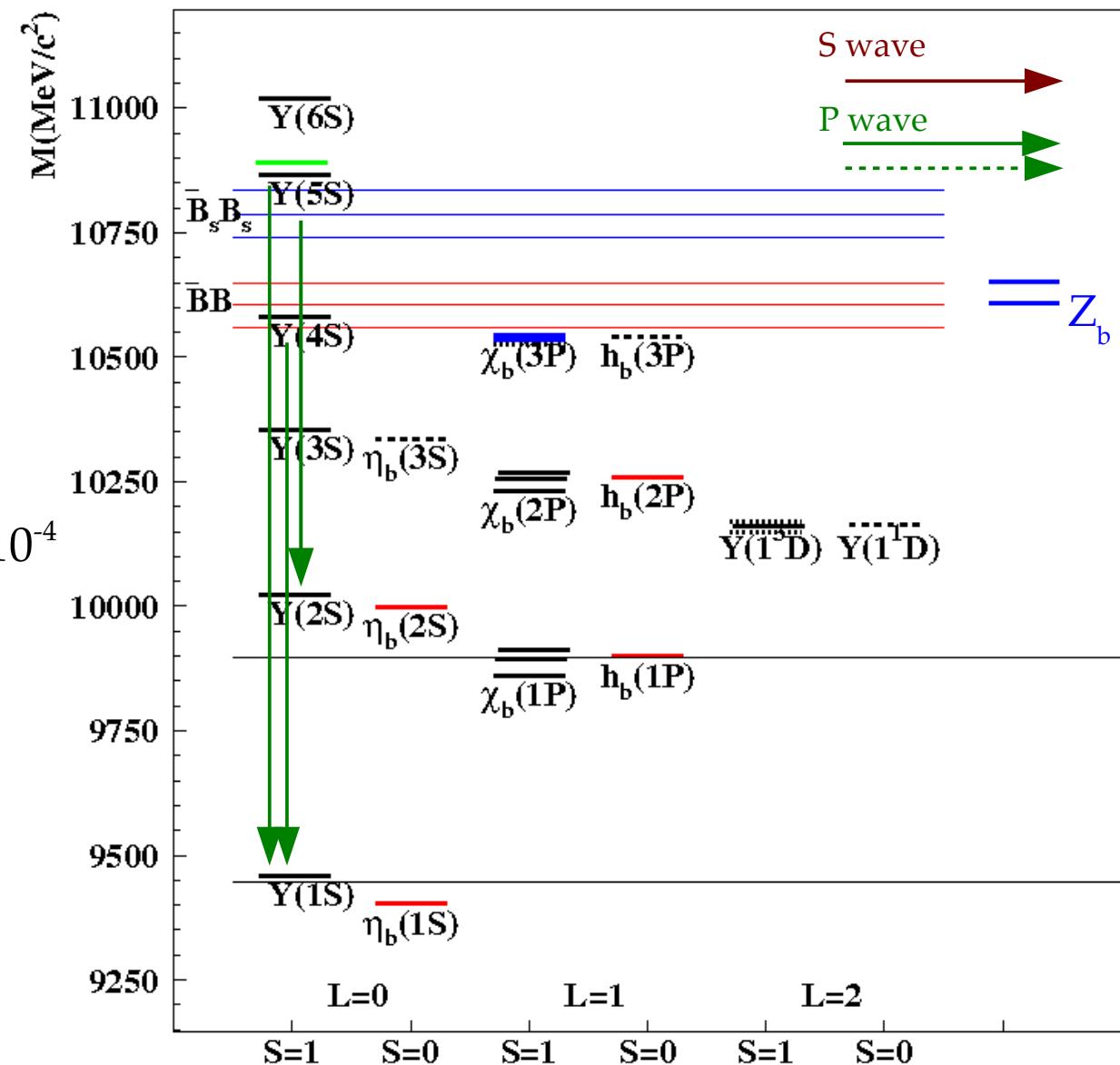
$B(\Upsilon(5S) \rightarrow \eta \Upsilon(1S)) = (7.3 \pm 1.6 \pm 0.8) \times 10^{-4}$

$$= 0.25 \times B(\Upsilon(5S) \rightarrow \pi\pi \Upsilon(1S))$$

$B(\Upsilon(5S) \rightarrow \eta \Upsilon(2S)) = (38 \pm 4 \pm 5) \times 10^{-4}$

$$= B(\Upsilon(5S) \rightarrow \pi\pi \Upsilon(2S))$$

All measured η transitions are P-wave.



The η transitions

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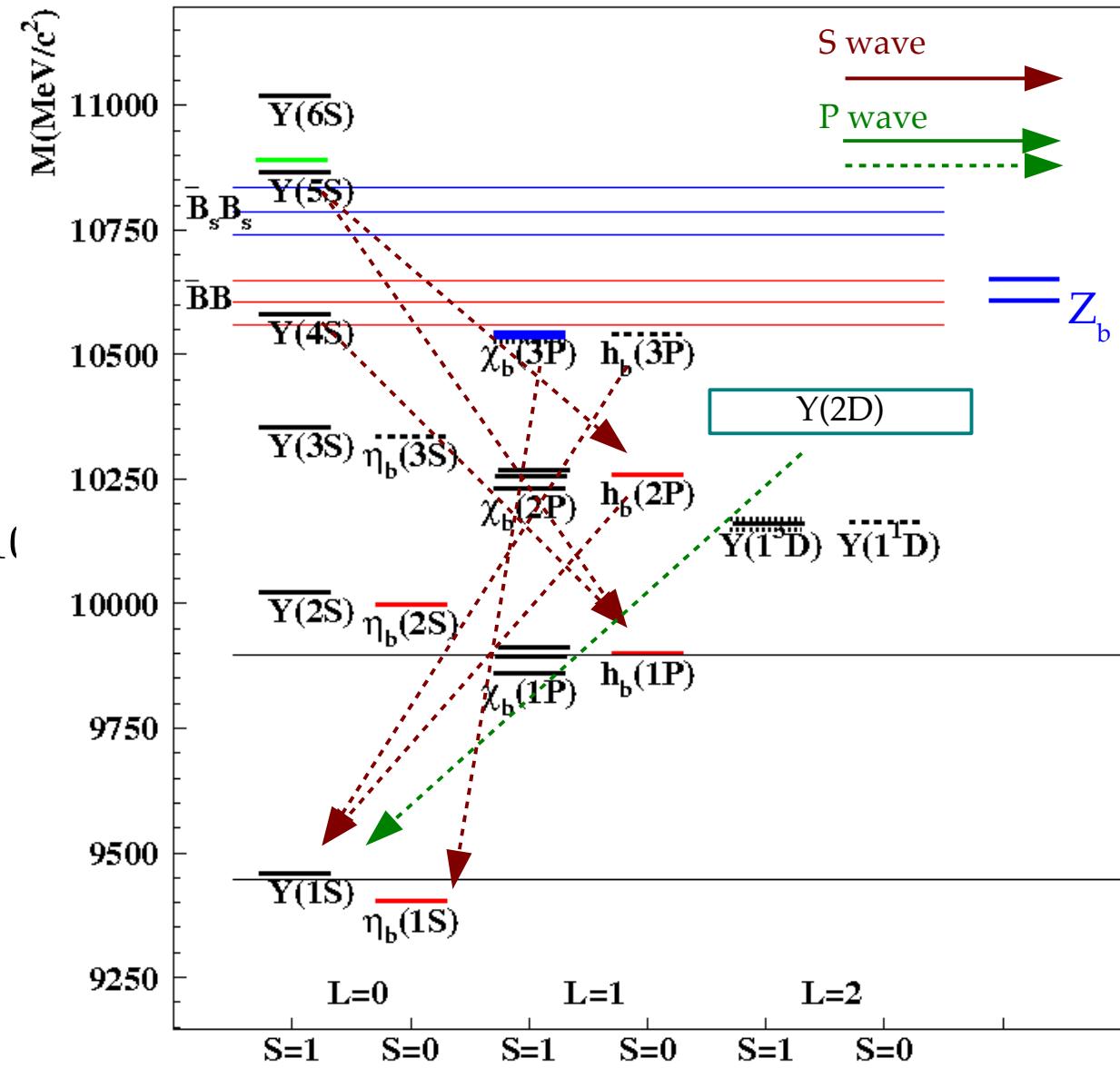
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All measured η transitions are P-wave.

Belle is now searching for all missing S-wave transitions





$h_b(1P)$ decay
from $\Upsilon(5S)$

